

# The role of correlations in disentangling between heavy-flavor energy-loss Models

*Winter Summer Workshop on Nuclear Dynamics*

*La Guadeloupe (Fr)*

**P.B. Gossiaux**

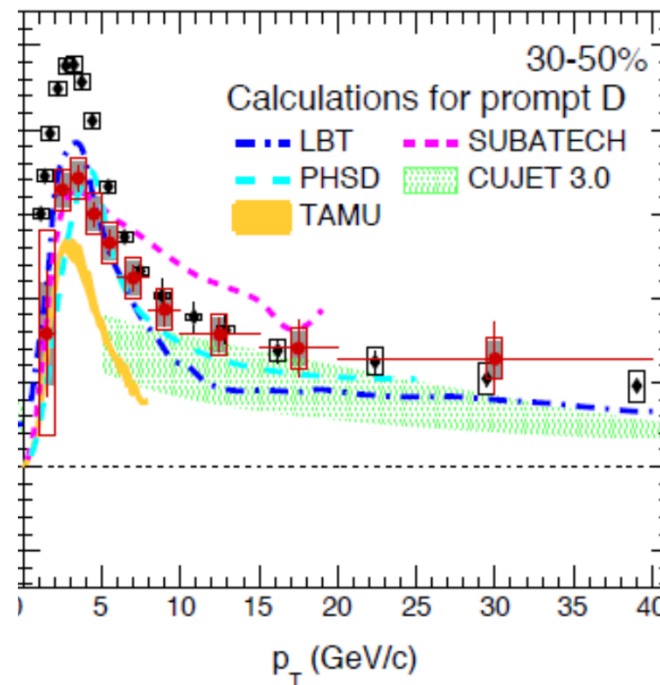
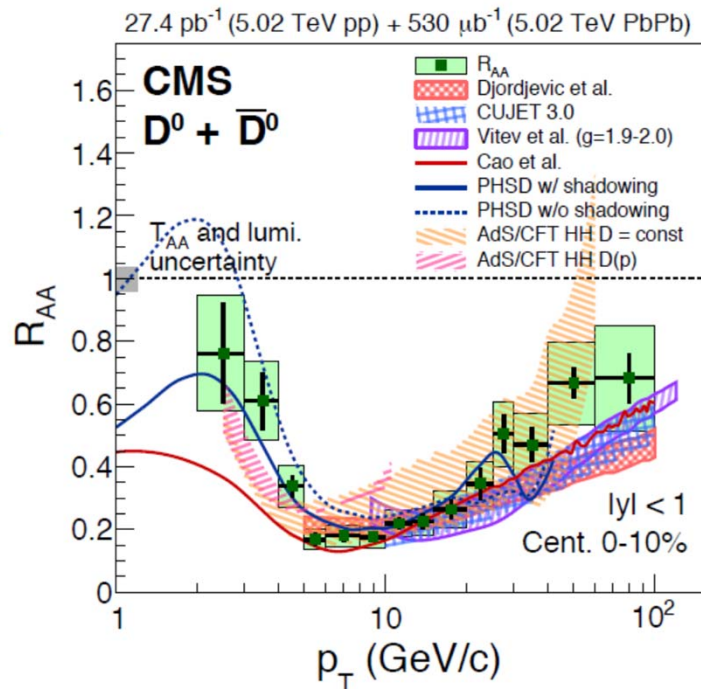
SUBATECH, UMR 6457

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In collaboration with J. Aichelin, B. Guiot, A. Mischke, M. Nahrgang, T. Pierog, L. Vermuunt, K. Werner

# (Short) Motivation

- Nowadays, a large variety of models (most of them presented as “effective approaches”) are confronted with the data for the  $R_{AA}$  &  $v_2$  single particle observables

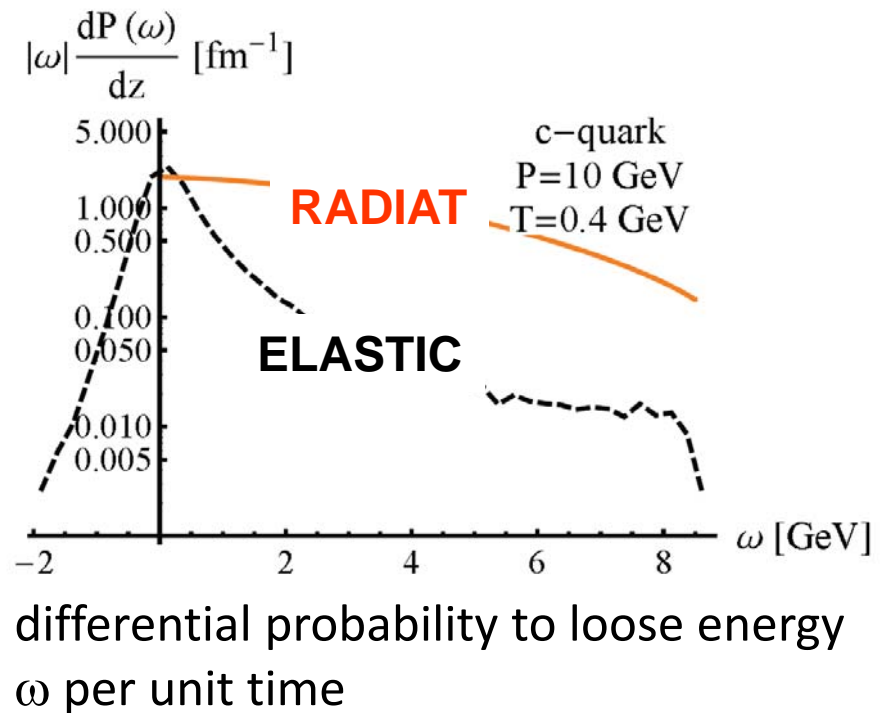
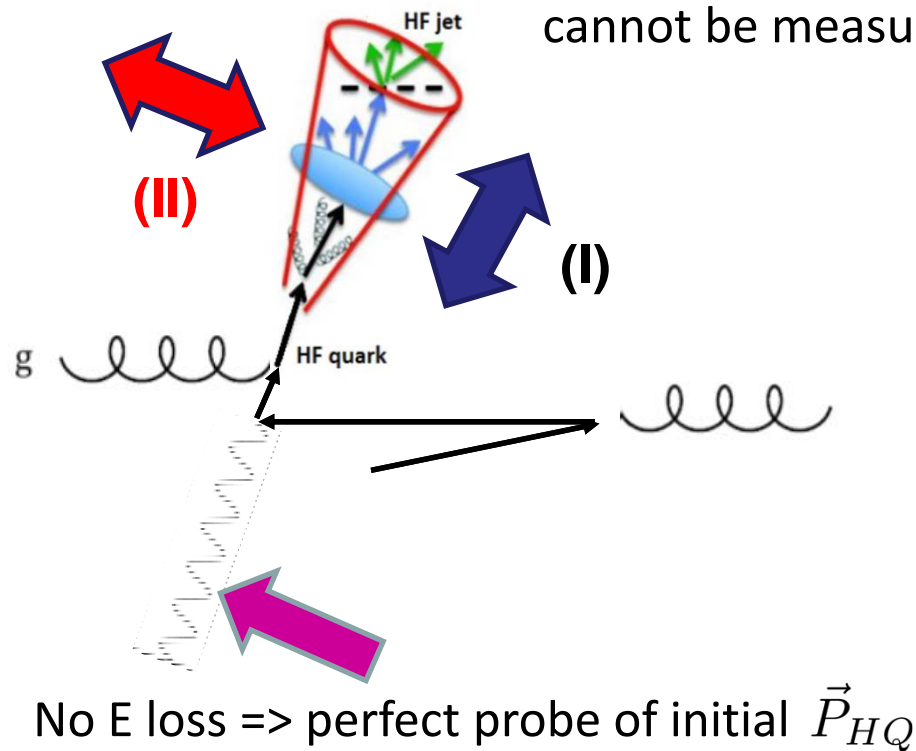


- For the purpose of making the contact with the fundamental theory, it is desirable to “constrain / pre-sort / rule out” some of the approaches
- Very often, correlations are advocated to be useful in this respect (**warning: main viewpoint adopted in this presentation**)

# How does it help ? Best HF Correlation ever ?

➤  $\gamma$  – D/B/c jet /b jet:

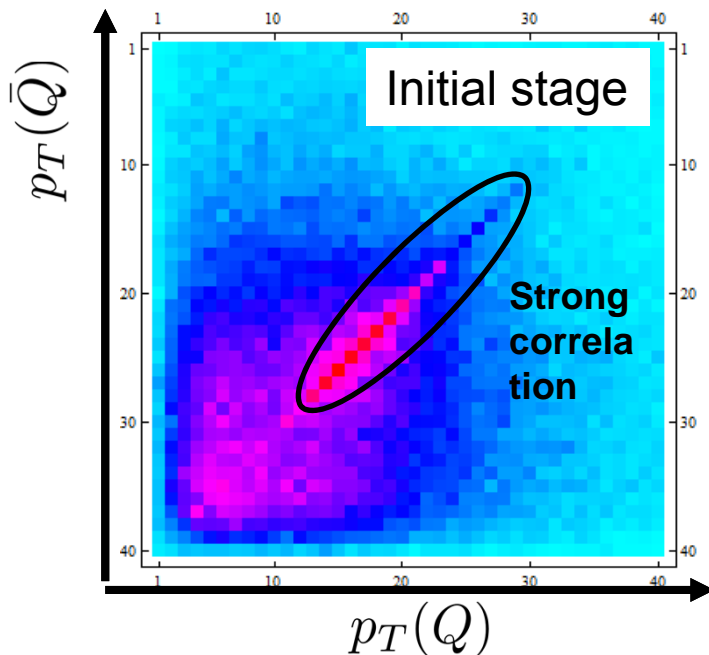
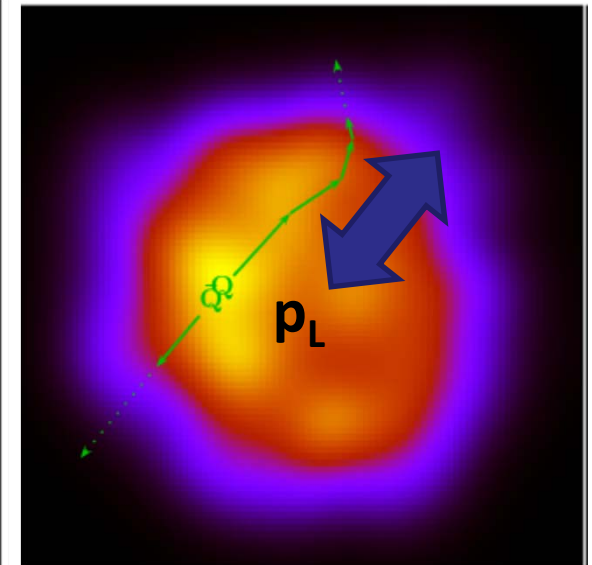
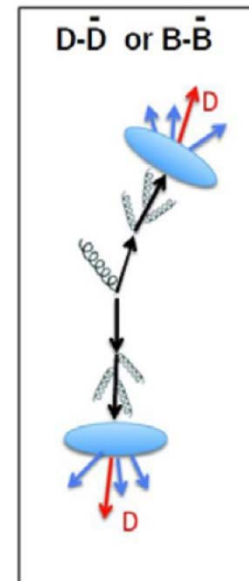
In QGP: **Longitudinal and transverse (qhat) fluctuations** of the HQ, which crucially depend on the Eloss mechanism and cannot be measured in usual observables like  $R_{AA}$  or  $v_2$



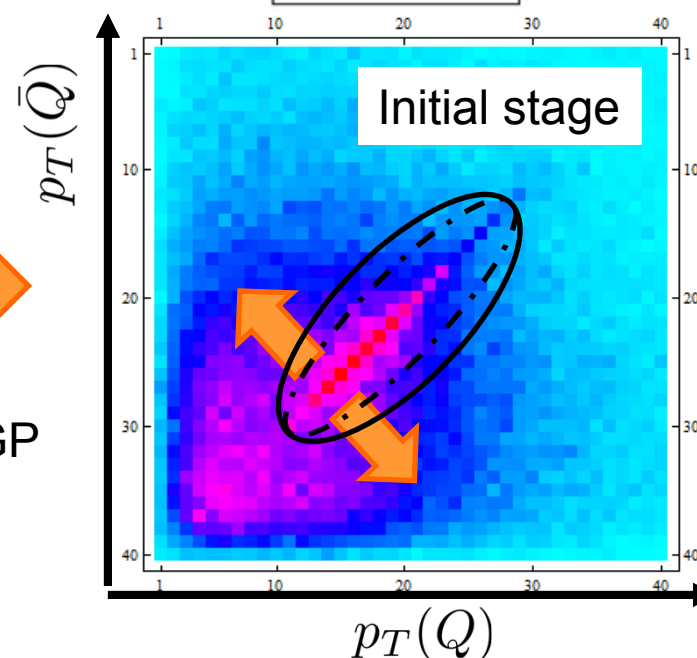
➤ Of course: NLO effect in the production mechanisms makes it not so trivial (not to speak about exp. Issues... RUN3 ? RUN4 ?)

# Next best thing: HF-HF correlations

- Back to back D/Dbar or B/Bbar: As compared to  $\gamma$ -D/B: “triggering” itself is affected but symmetry between both particles could limitate the various effects:
- Large number of c-cbar from various NN collisions => large uncorrelated background
- Competing effects due to energy loss: ...



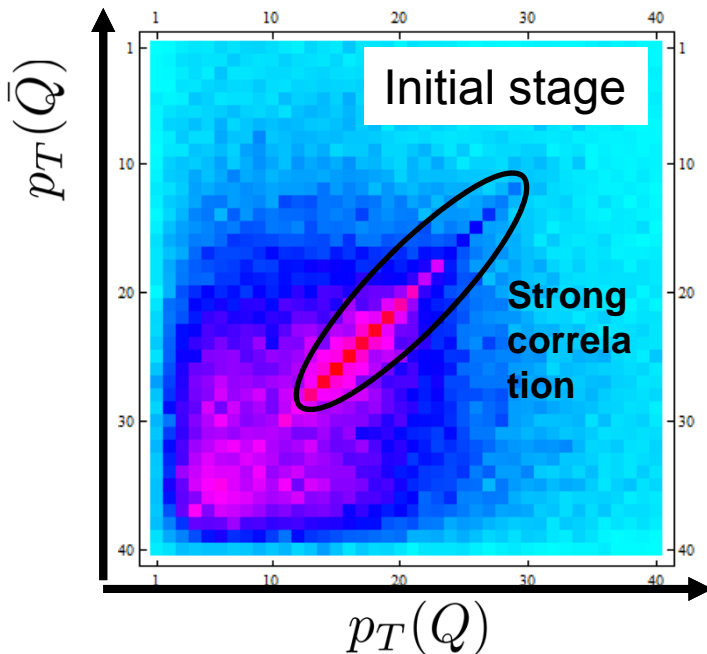
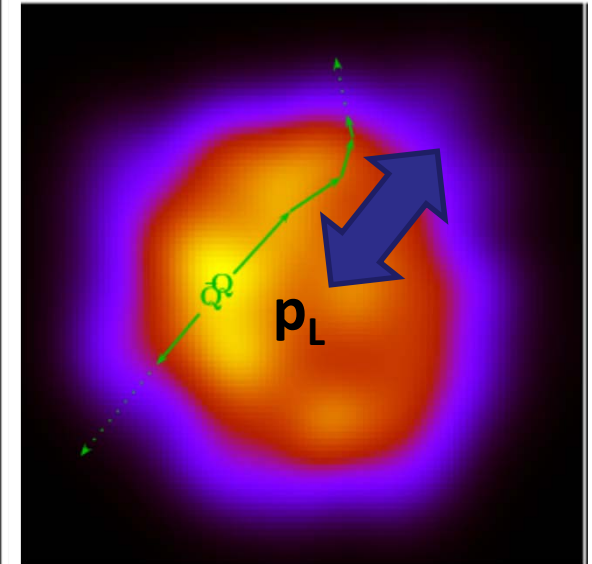
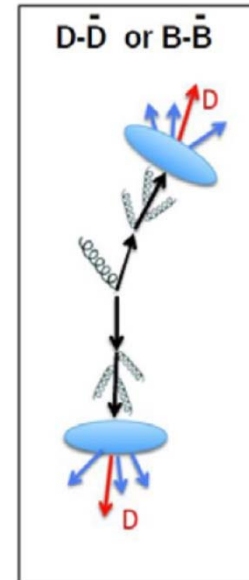
Evolution  
in hot QGP  
medium



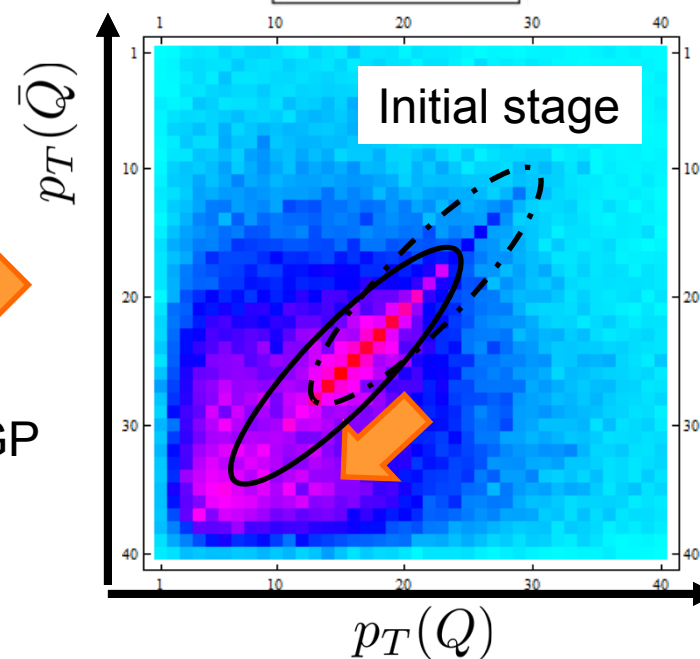
- decorrelation due to various path lengths + fluctuations: **reduction**

# Next best thing: HF-HF correlations

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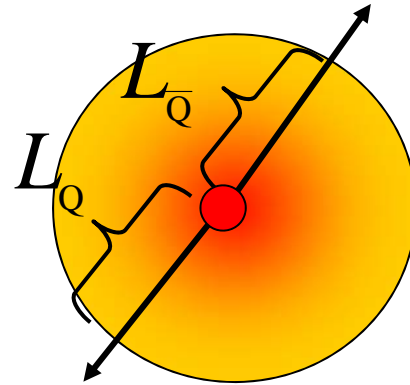
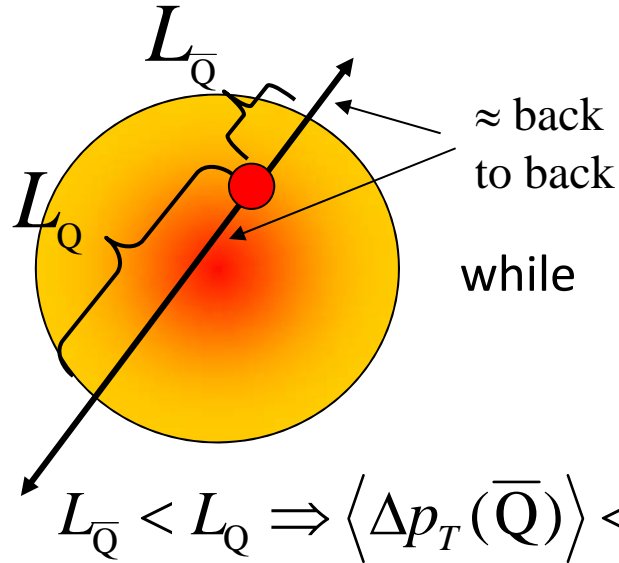
➔ Evolution in hot QGP medium



- feeding from higher  $p_T$  (stronger) correlations: **increase**

# Once upon a time: momentum imbalance for hot core

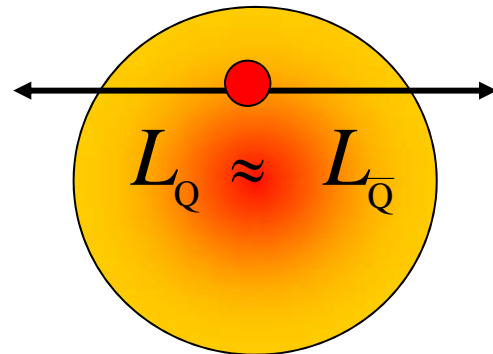
- Challenge: tagging on the “central” Q, i.e. getting closer to the ideal “penetrating probe” concept:



$$L_{\bar{Q}} \approx L_Q \Rightarrow \langle \Delta p_T(\bar{Q}) \rangle \approx \langle \Delta p_T(Q) \rangle$$

- Reversing the argument: selecting  $\langle \Delta p_T(\bar{Q}) \rangle \approx \langle \Delta p_T(Q) \rangle$  might bias the data in favor of “central” pairs

Possible caveat:

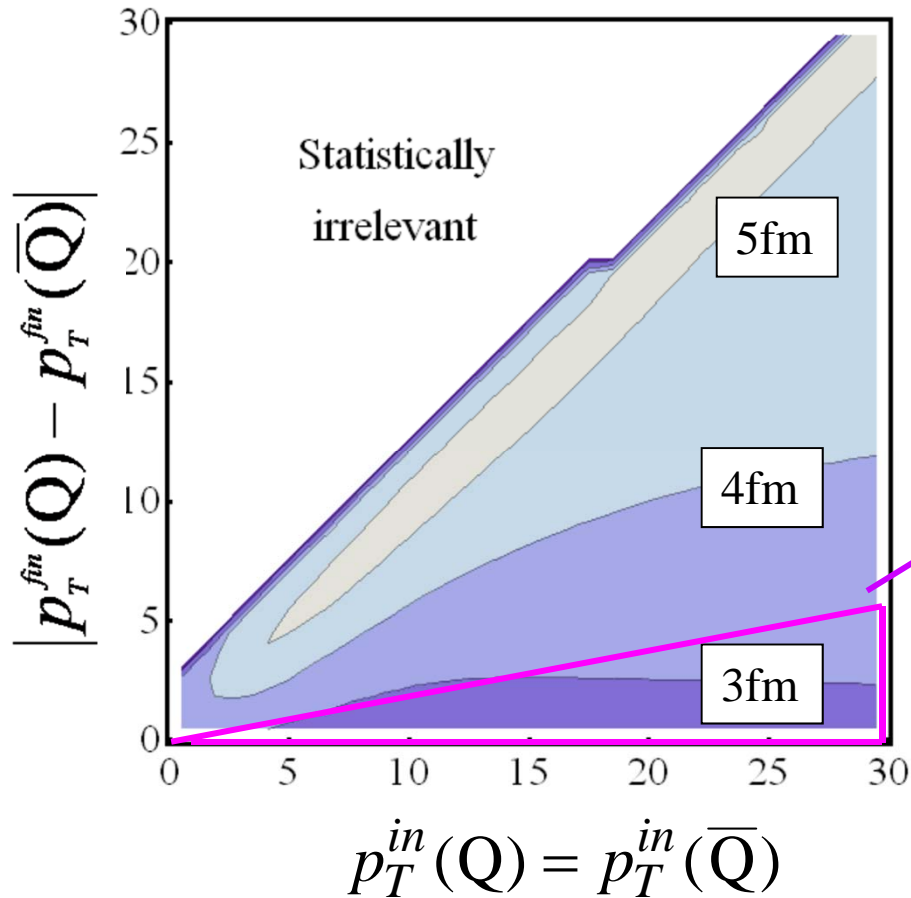


$\Rightarrow$  Need for a detailed study

Gossiaux et al, PHYSICAL REVIEW C 79, 044906 (2009)

# Once upon a time: momentum imbalance for hot core

Average transv.-dist. to center as a function of  $\Delta p_T^{\text{fin}}$  for various  $p_T^{\text{in}}$



Indeed some (favorable) bias for init  $p_T^{\text{in}} > 5\text{GeV}/c$  and “small”  $\Delta p_T^{\text{fin}}$

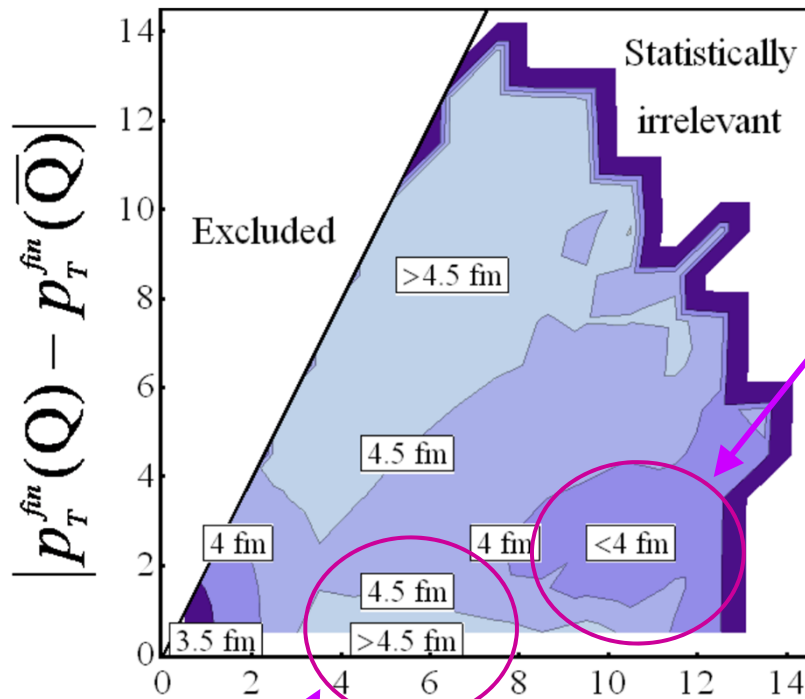
Hope to probe hotter regions of the QGP

However: No access to  $p_T^{\text{in}}$  !!!

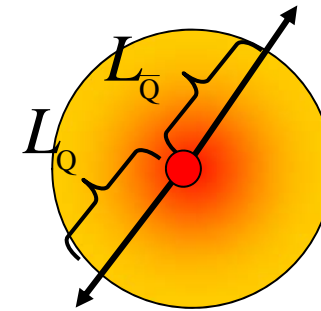
# Once upon a time: momentum imbalance for hot core

**Best ansatz:**  $p_T^{in}(Q) \rightarrow \bar{p}_T^{fin} := \frac{p_T^{fin}(Q) + p_T^{fin}(\bar{Q})}{2}$

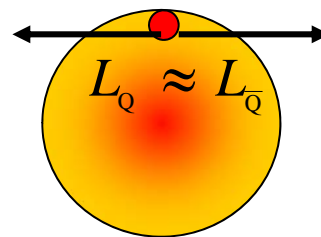
Average transv.-dist. to center as a function of  $\Delta p_T^{fin}$  for various  $\bar{p}_T^{fin}$



Central production:



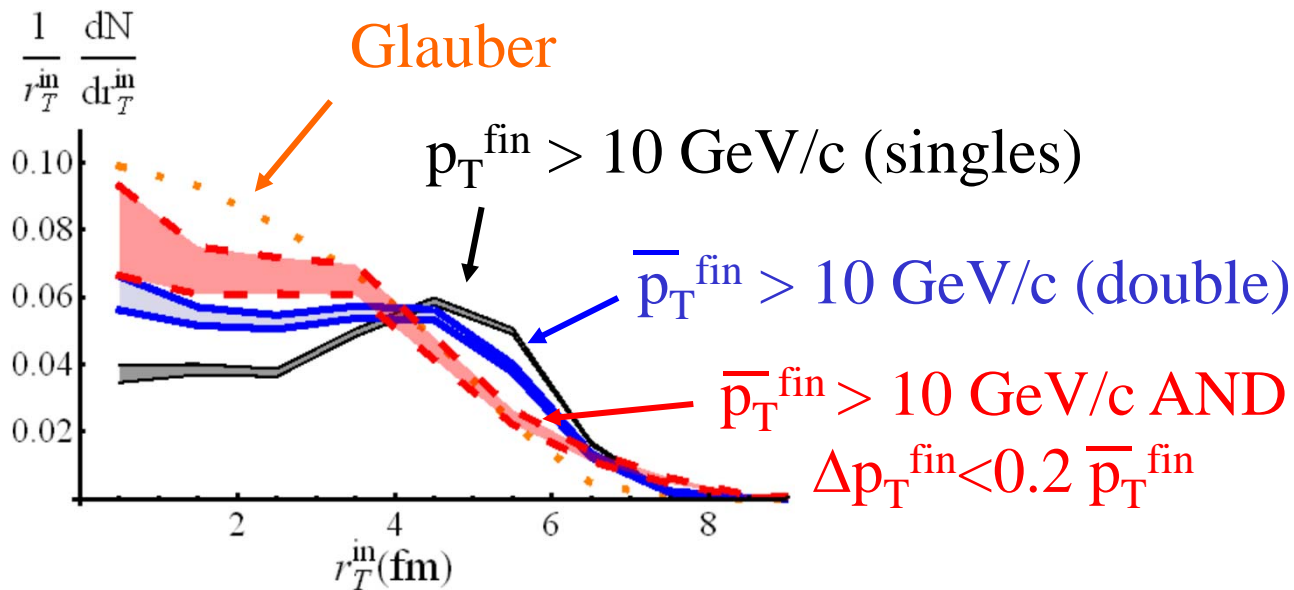
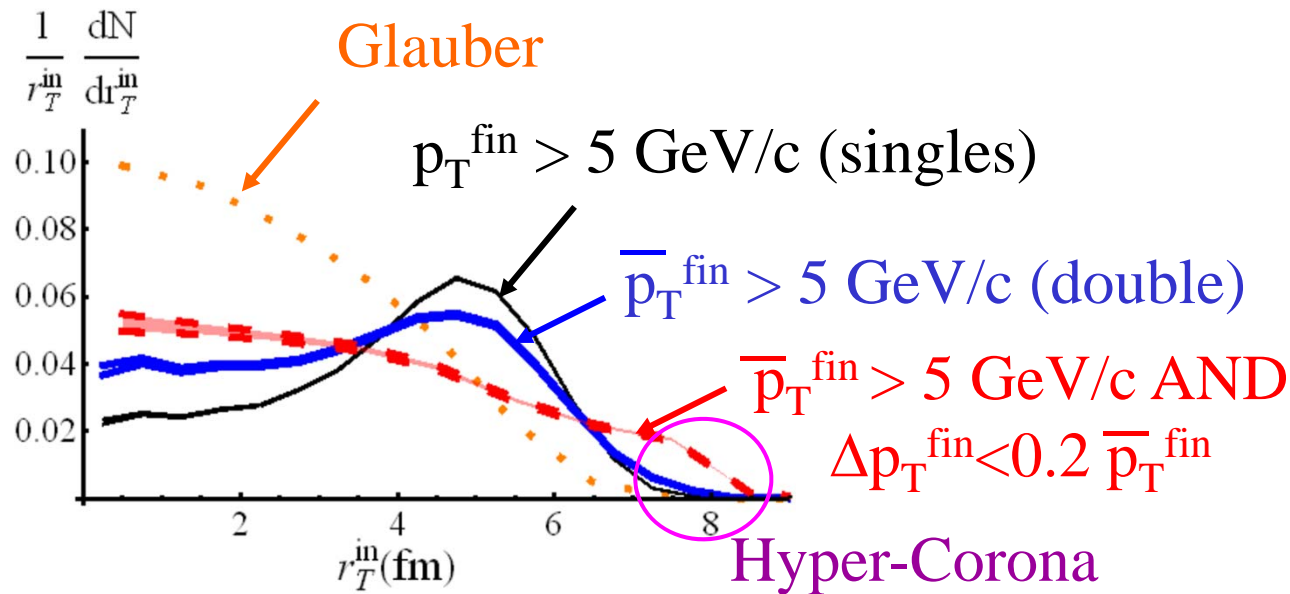
Tangential production



Conclusion: Favorable bias for  $\text{av. } p_T^{fin} > 8 \text{ GeV}/c$  and “small”  $\Delta p_T^{fin}$

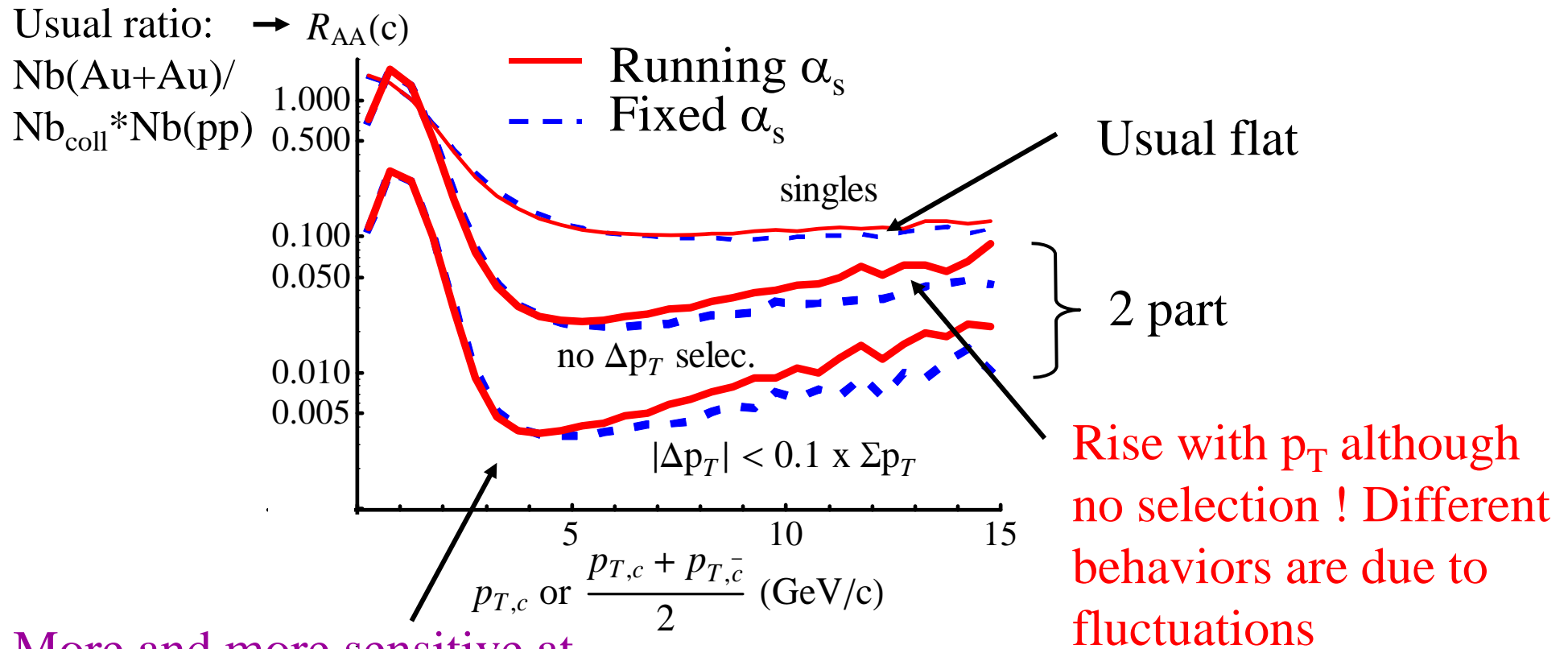


# momentum imbalance for hot core: back to $r_T$ distributions



- Final cuts lead to various distributions of initial position
- One nearly recovers the Glauber profile for most severe cut

# momentum imbalance: increase $R_{AA}$ sensitivity

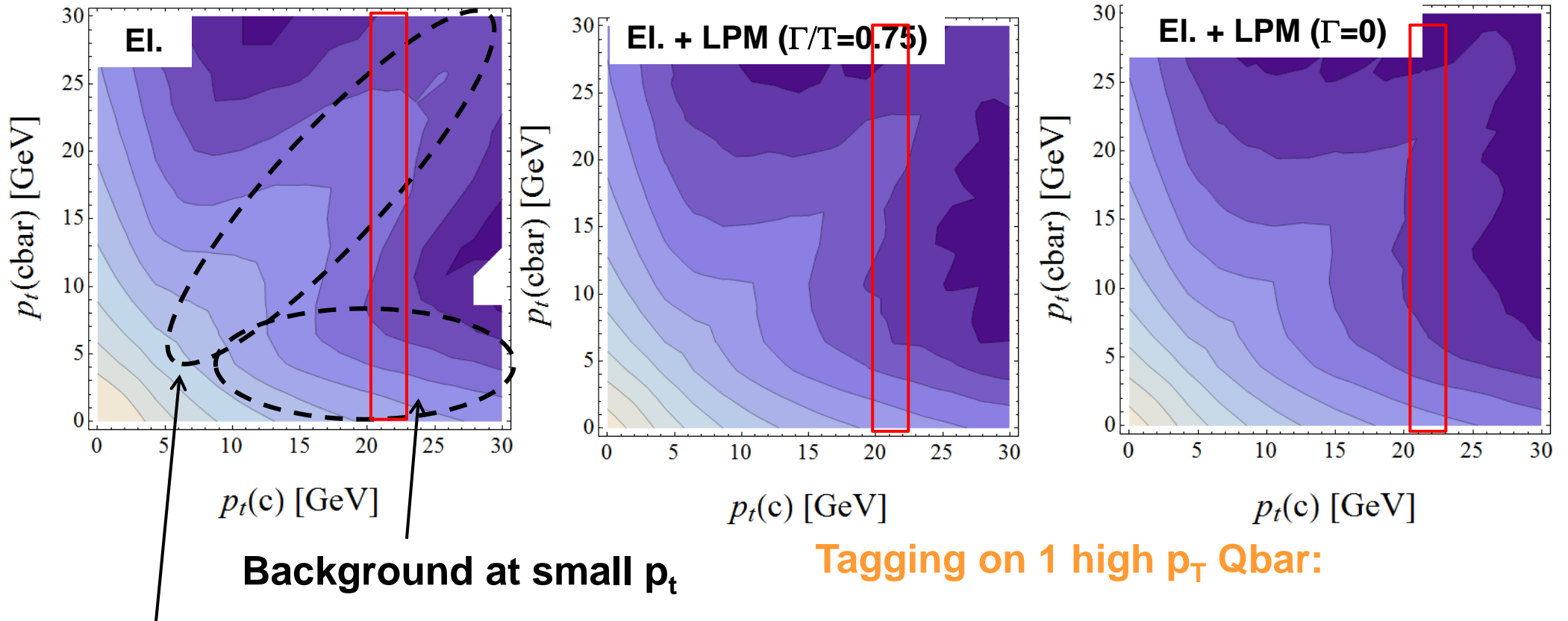


More and more sensitive at large  $p_T$  for HQ from center

Close to experimental prediction but not yet (Hadronization, NLO at the time of production, background subtraction,...)

# Consequences on the observables: $p_t(c)$ - $p_t(\bar{c})$ correlations

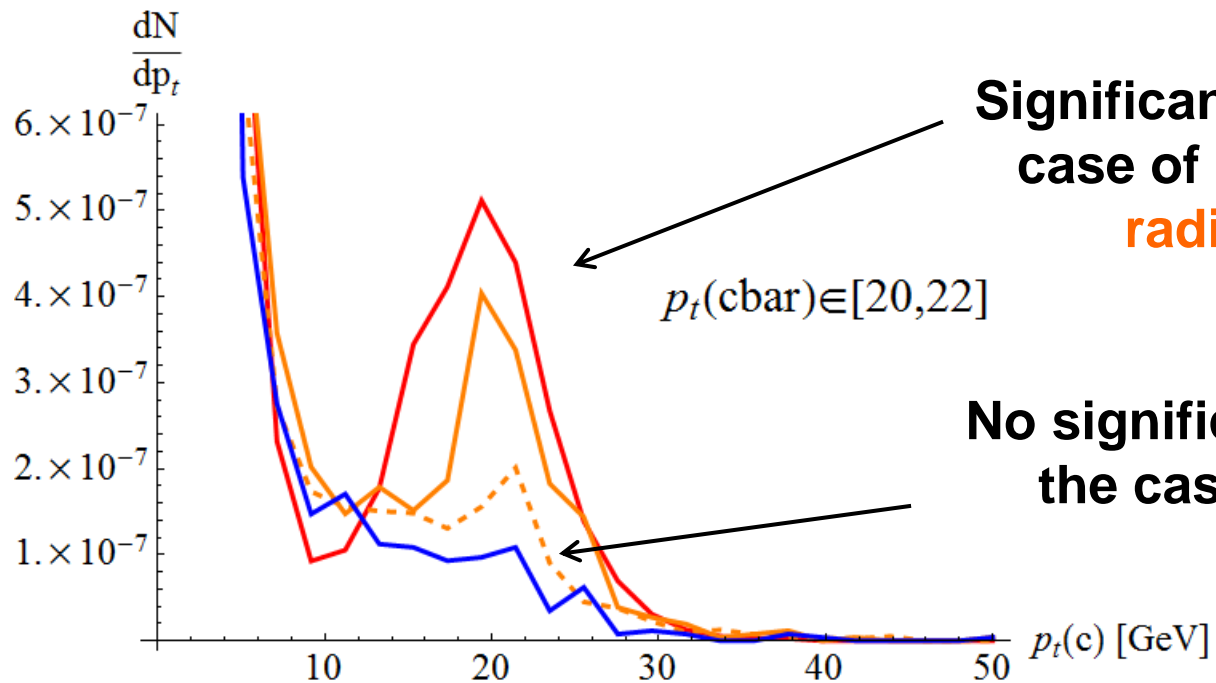
Pb-Pb @ 2.76 TeV; 40-60%. Toy study: back to back c-cbar (no NLO corrections)



Residual correlation after evolution through QGP  
(similar path length for most of HQ produced in the core of the reaction)

# Consequences on the observables: $p_T$ - $p_{Tbar}$ correlations

Pb-Pb @ 2.76 TeV; 40-60%. Toy study (proof of principle): back to back c-cbar



Significant residual correlation for the case of **Elastic energy loss** or **LPM radiative + gluon damping**

In the B2B region:  
No significant residual correlation for the case of **radiative GB** or **LPM radiative**

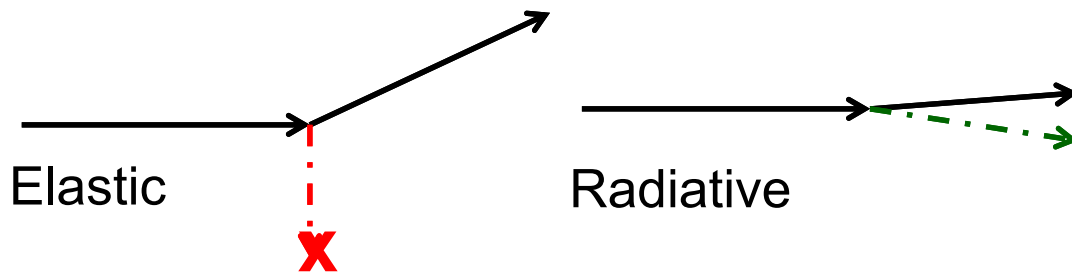
Background at small  $p_t$

WWND 2014  
Galveston

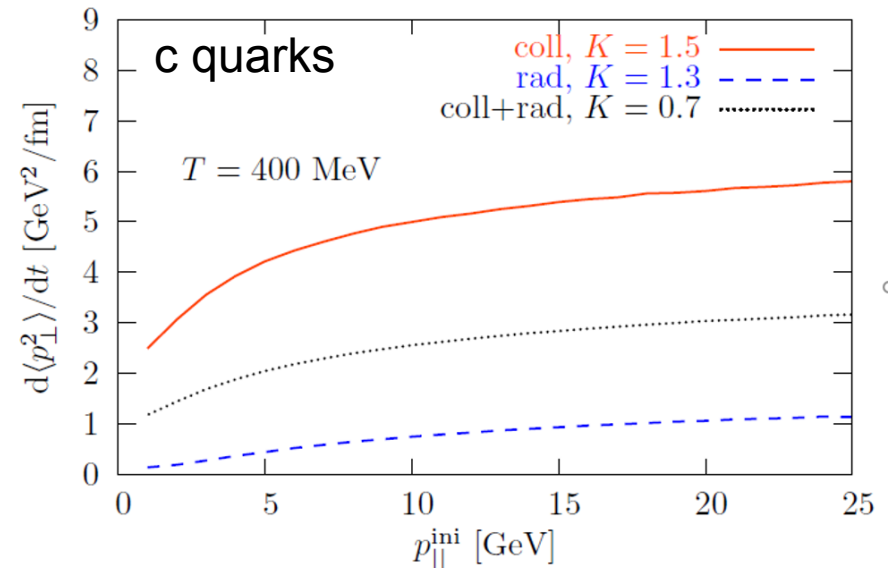
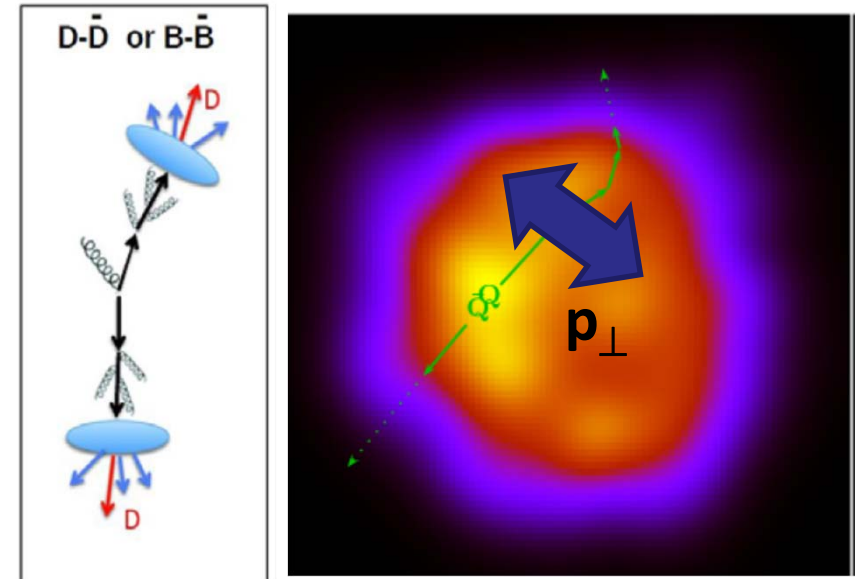
How does DGLAP evolution blur momentum imbalance ?

# Next best thing: HF-HF correlations

- Back to back D/Dbar or B/Bbar: As compared to  $\gamma$ -D/B: “trigger” itself is affected but symmetry between both particles limitates the various effects.
- Elastic Eloss vs radiative Eloss: **The purely collisional scatterings lead to a larger average  $\langle p_{\perp}^2 \rangle$  than the radiative “corrections”** (need for large scattering to be efficient)... although both types can give correct agreement with the data at intermediate  $p_T$ .



- Expected consequences for azimuthal correlations (probe of  $B_T$ : good: **complimentary** to usual RAA and  $v_2$ )

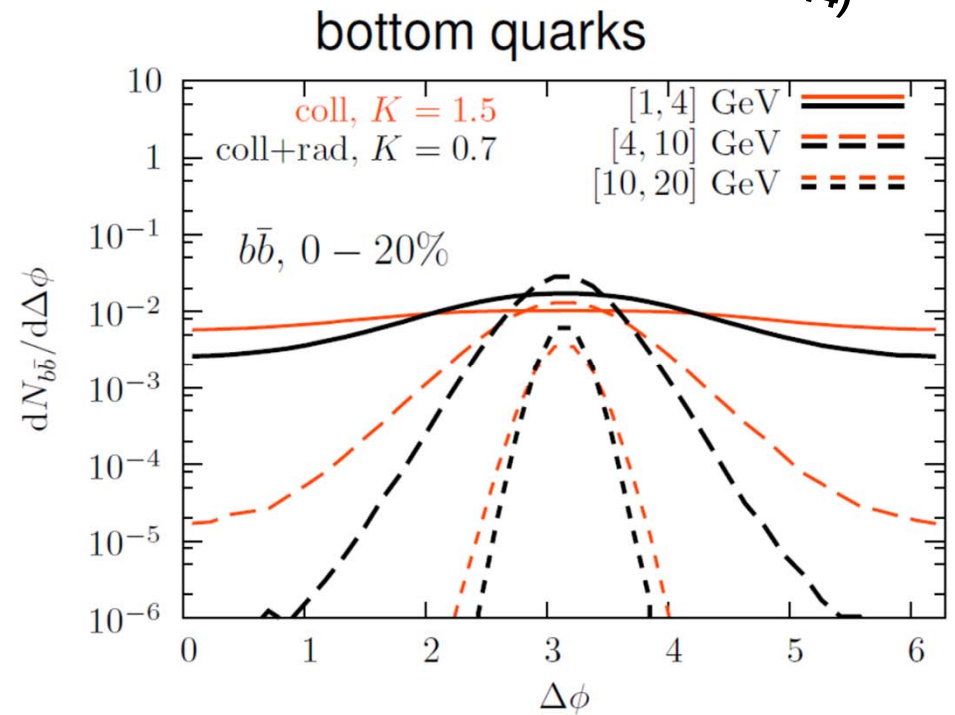
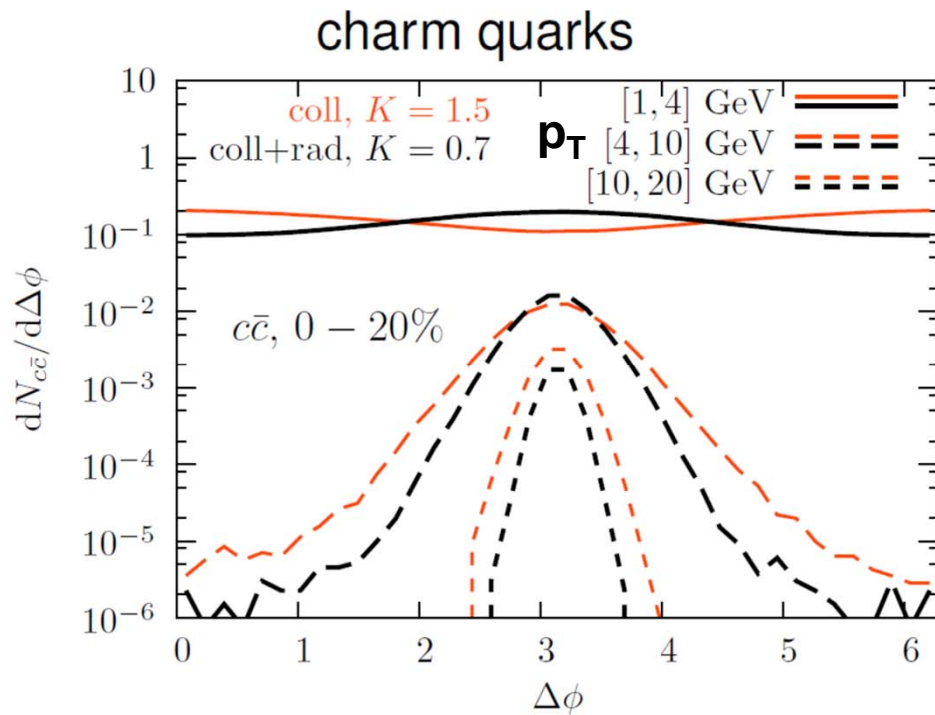


Tuned to reproduce the  $R_{AA}$

# Next best thing: azimuthal correlations

Nahrgang et al.  
Phys. Rev. C 90,  
024907 (2014)

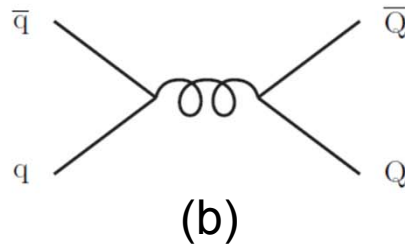
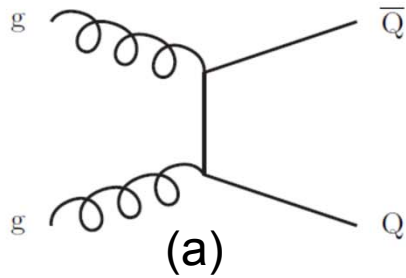
- Assumption of back 2 back emission of initial QQbar (naïve LO...)



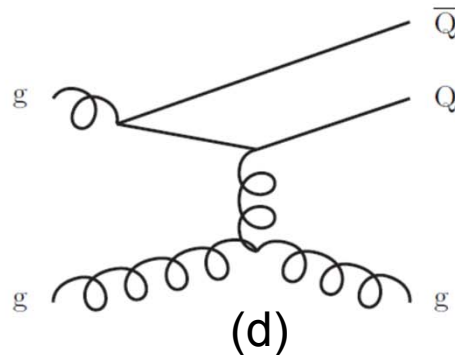
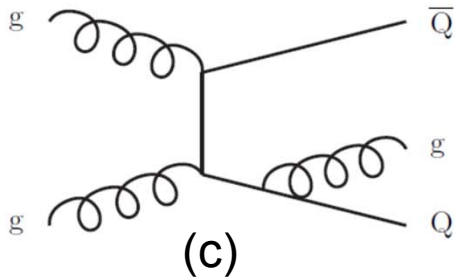
- Indeed, rather large differences found for both b and c, and all kind of  $p_T$  cuts (... but good to see there is an effect though,...)
- For the smallest  $p_T$  bin and elastic energy loss, we even find an inversion of the correlation (“hot partonic wind” push;  $v_0$  bulk  $\Rightarrow v_1$  correl; underlying event)

# Next best thing: azimuthal correlations

➤ ...but higher orders can have a significant impact:



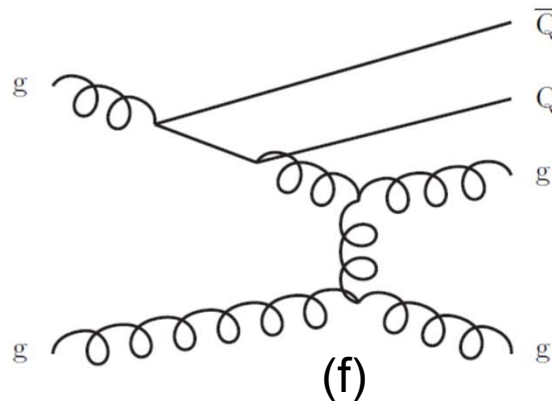
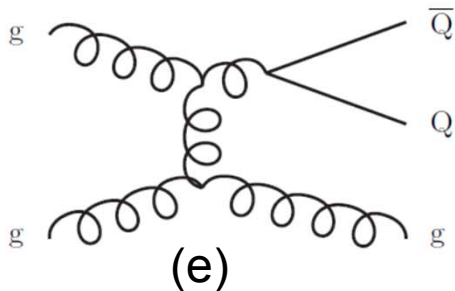
➤ LO; (a): back to back peak



➤ NLO;

(c): “blurring” of B2B peak

(d): “flavor excitation”: no strong azimuthal correlation expected

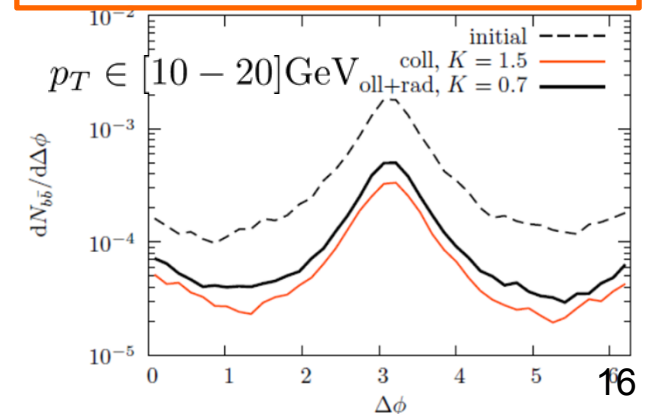
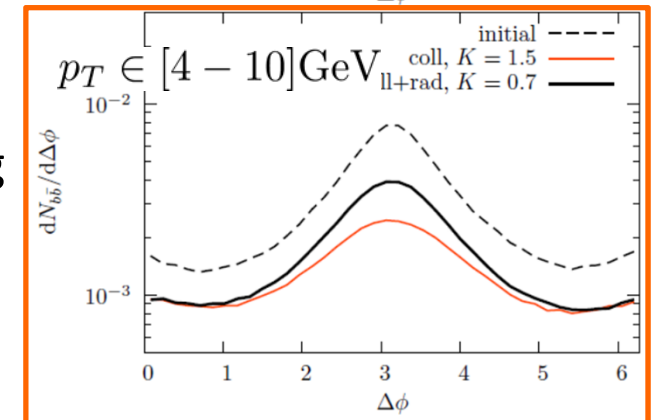
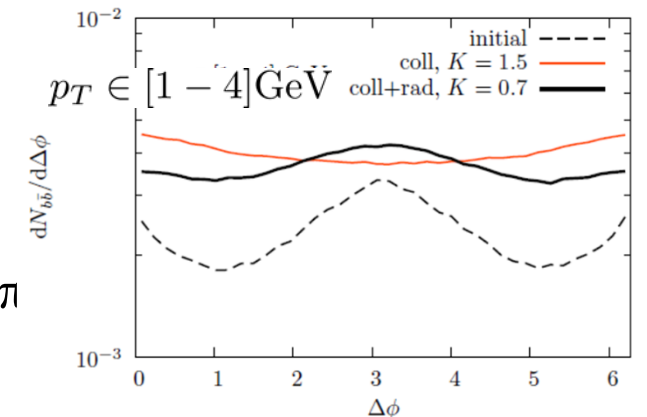


(e): gluon splitting: strong peak around  $\Delta\phi=0$

(f): higher order FE; both Q and Qbar in the “remnant” region

# Next best thing: azimuthal correlations

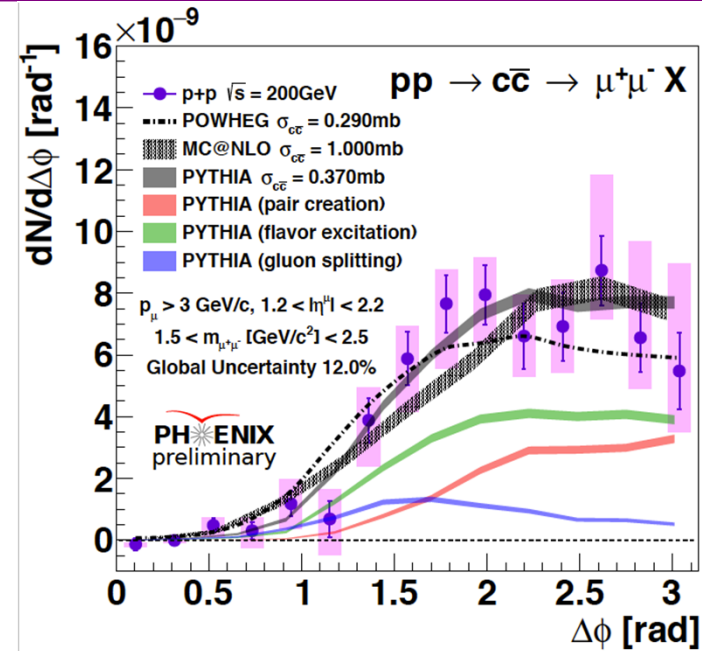
- NLO effect simulated with MC@NLO + HERWIG (parton shower)
- Gluon splitting processes lead to an initial enhancement of the correlations around  $\Delta\phi=0$ ; Strong broadening of the  $\Delta\phi=\pi$  peak (“vacuum” radiation is dominant)
- For intermediate  $p_T$  : increase of the variances due to Eloss from 0.43 (initial NLO) to 0.51 (+20%) for the purely elastic mechanisms and to 0.47 (+10%) for the interaction including **radiative** corrections.
- Correlations at large  $p_T$  seem to be dominated by the initial correlations. **Nothing will be learned on the Eloss mechanisms in this region**
- Different NLO+parton shower approaches agree on bottom quark production, differences remain for charm quark production
- Study by other groups (Duke, CCNU-LBL,PHSD,...)



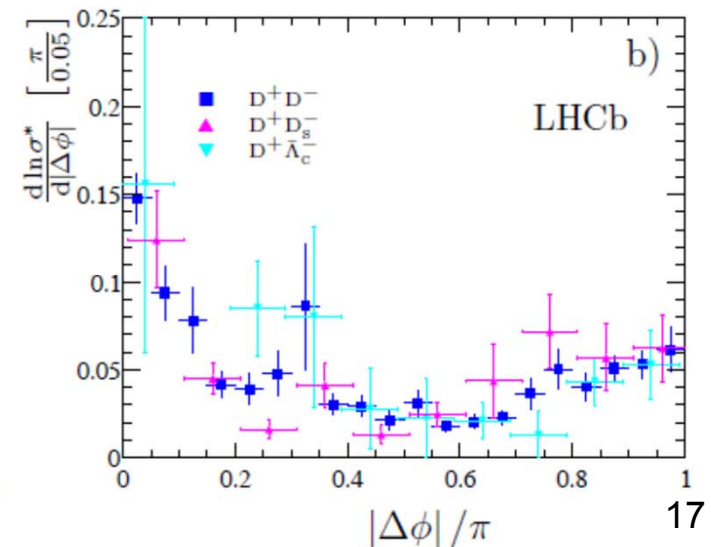
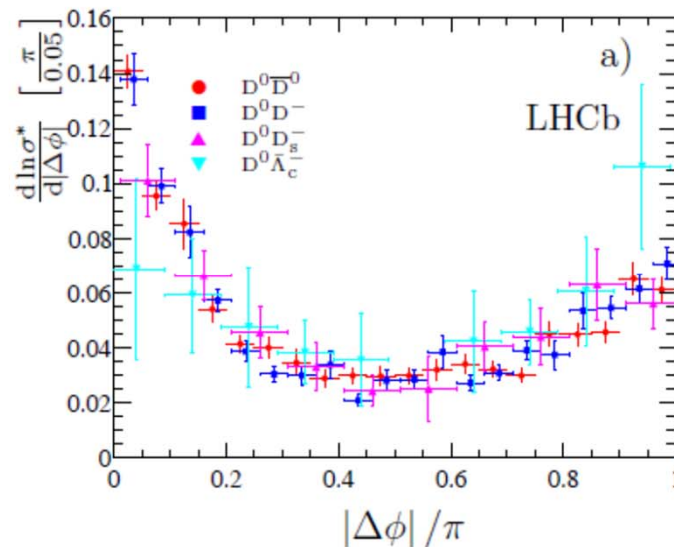


# Azimuthal correlations from experimental viewpoint

- Measured in pp both at RHIC and LHC (rising gluon splitting peak)
- Not even sure one could resolve a 10% difference in the width for the pp !!!
- A+A: expected after upgrades ?



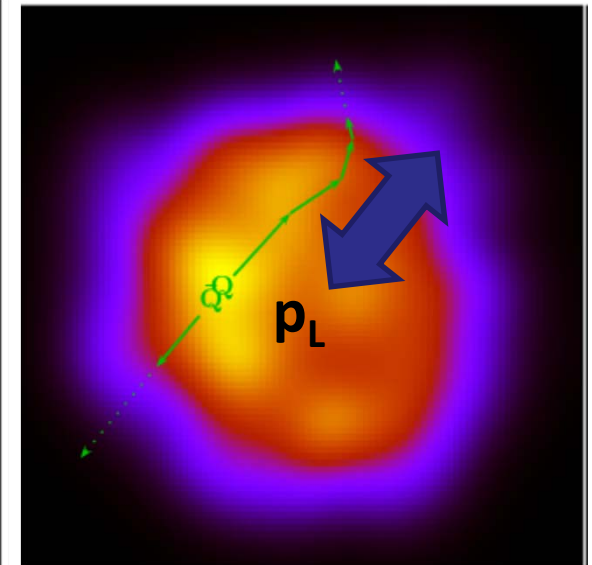
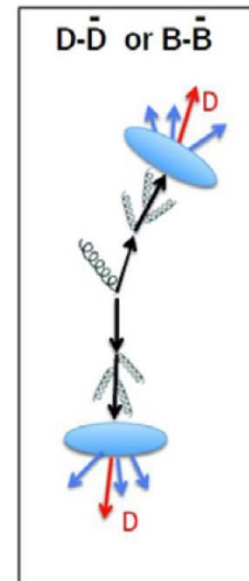
PHENIX



LHCb

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- Large number of  $c$ - $\bar{c}$  from various NN collisions => large uncorrelated background
- Competing effects due to energy loss
- Of course: **NLO effect in the production mechanisms makes it not so trivial** (not to speak about exp. Issues... RUN 3 ? RUN 4 ?)



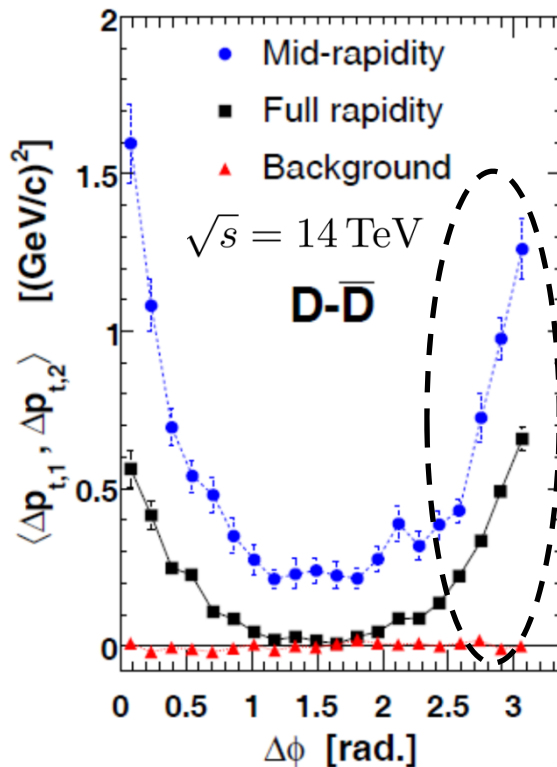
# Not so naïve approach: Momentum imbalance in pp

➤ ... including “realistic” initial stage in pp (PYTHIA 6)

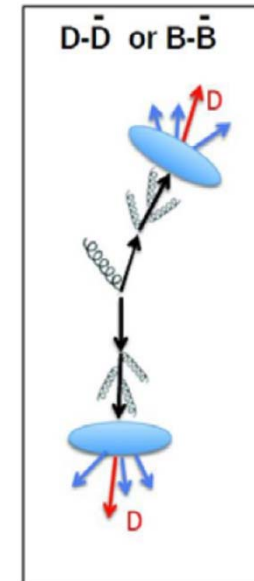
➤ Average auto-correlation:

$$\langle \Delta p_{t,1}, \Delta p_{t,2} \rangle^{(D\bar{D})} = \frac{1}{\sum_{k=1}^{n_{ev}} N_k^D N_k^{\bar{D}}} \cdot \sum_{k=1}^{n_{ev}} \sum_{i=1}^{N_k^D} \sum_{j=1}^{N_k^{\bar{D}}} (p_{ti} - \bar{p}_t^{(D)}) (p_{tj} - \bar{p}_t^{(\bar{D})})$$

G. Tsileidakis et al., Nucl. Phys. A 858 (2011) 86.



In the back-to back region, NLO corrections (FSR) still preserve some degree of correlation



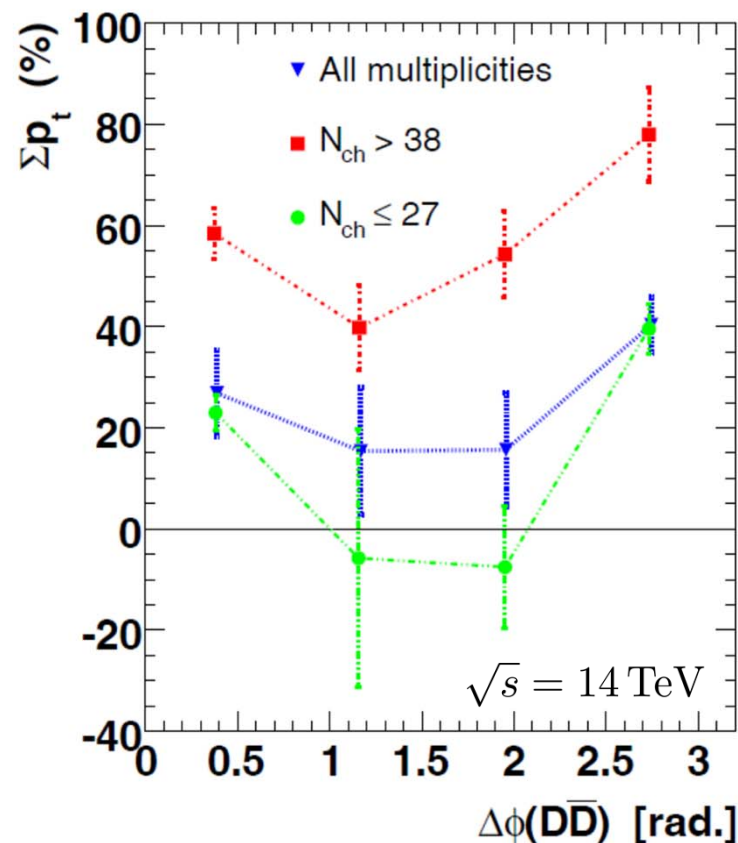
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➤ Average *relative* auto-correlation:

$$\Sigma_{pt} = \text{sgn}(\langle \Delta p_{t,1}, \Delta p_{t,2} \rangle) \frac{\sqrt{|\langle \Delta p_{t,1}, \Delta p_{t,2} \rangle|}}{\bar{p}_t}$$

G. Tsiledakis et al., Nucl. Phys. A 858 (2011) 86.



- Encouraging signs of significant finite (transverse) momentum correlation in pp, i.e. in the initial stage of A-A collisions
- Going beyond average ?
- Lessons from CMS: Pythia has problems to reproduce Q-Qbar azimuthal correlations

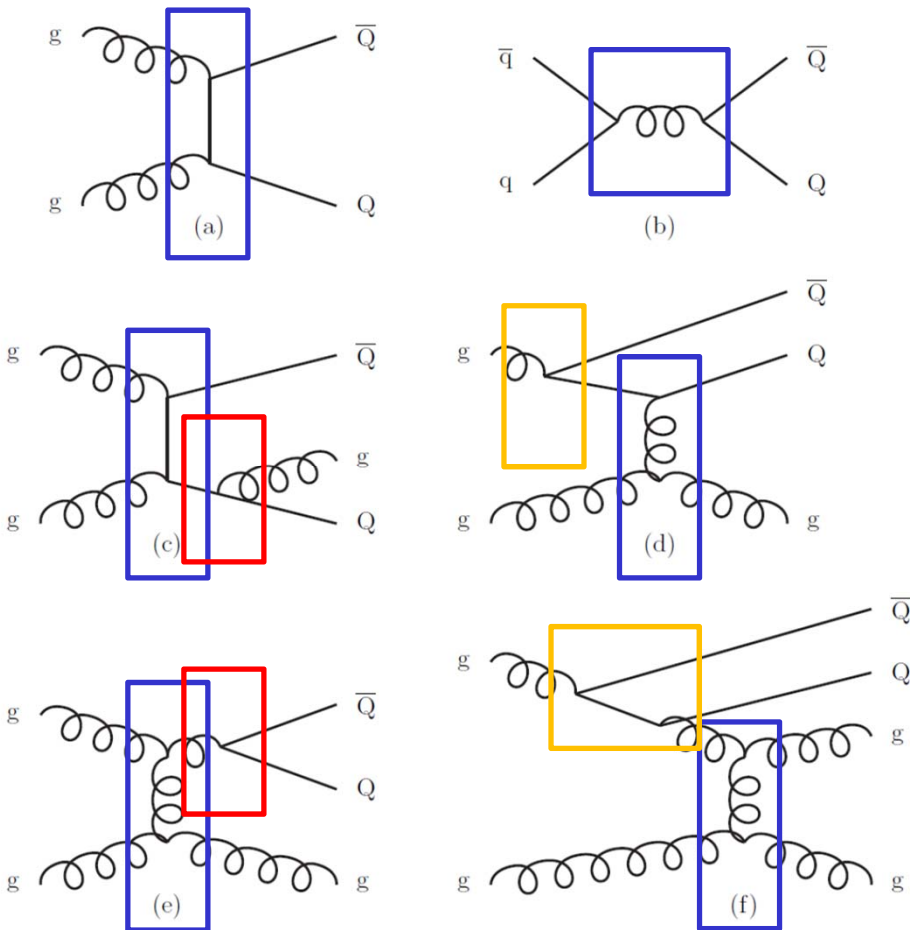
CMS-PASHIN-16-005.

# Momentum imbalance: not so naïve approach

- Goal of the study: investigate whether  $p_T$ - $p'_T$  correlations survive NLO effects

L. Vermunt et al.  
arXiv:1710.09639

- Method for “systematics”: use 2 event generators: PYTHIA (6.4) & EPOS3

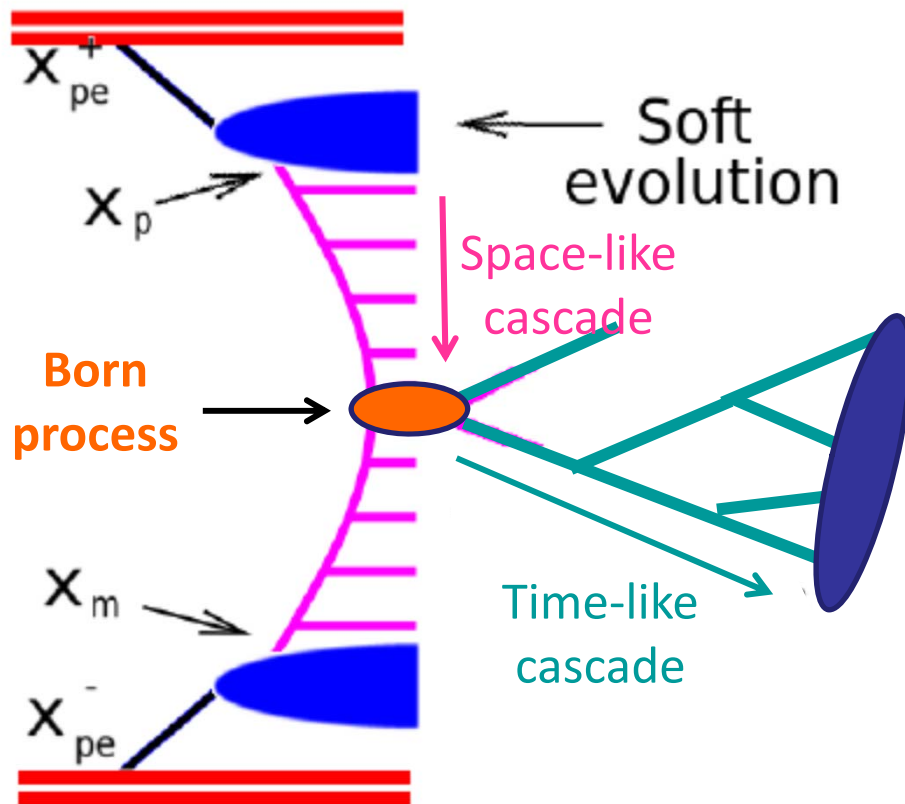


- In pythia, those topologies are generated by coupling LO processes (implying 0,1 or 2 HQ) and ISR + FSR ... This will be referred to as « LO + NLO ccbar » (strictly speaking, no NLO !)

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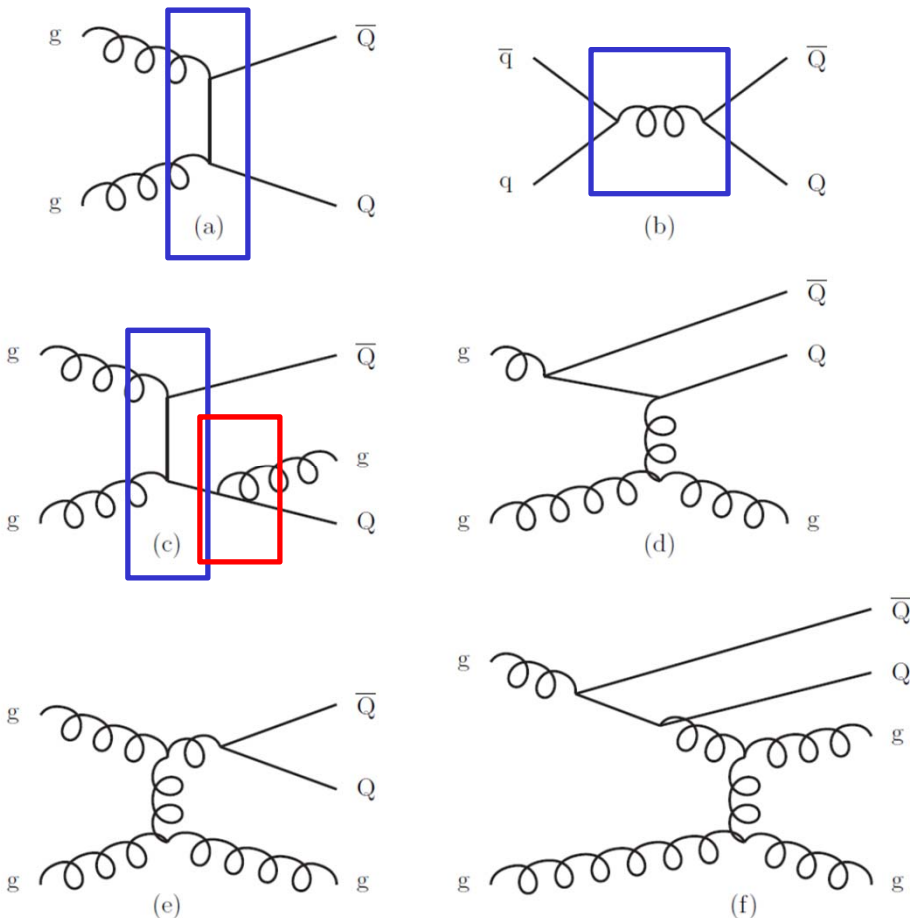
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- Same « strategy » in EPOS3, with « semi-hard pomeron » approach (with some soft evolution included), with various LO Born processes.

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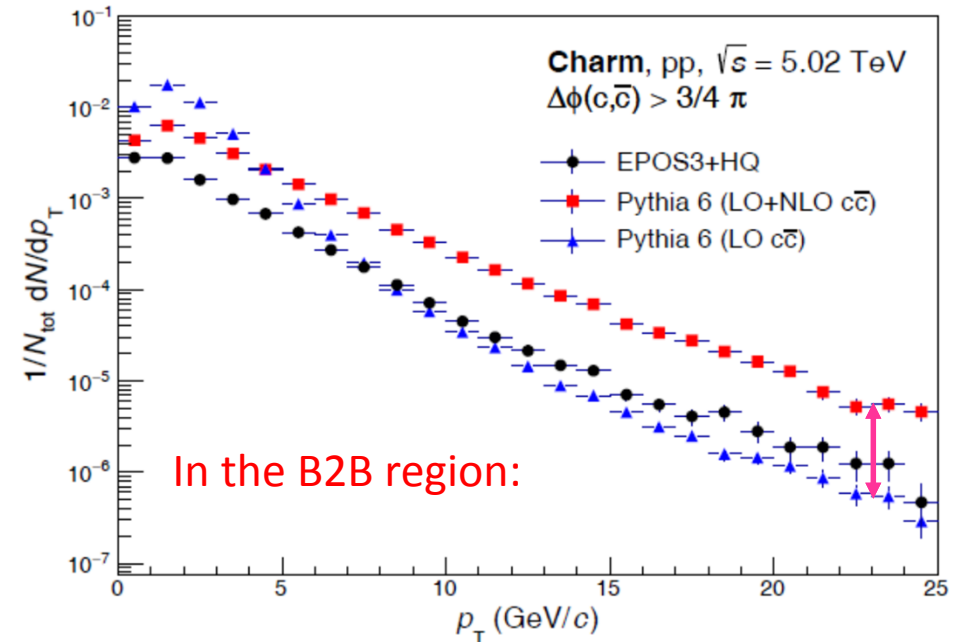
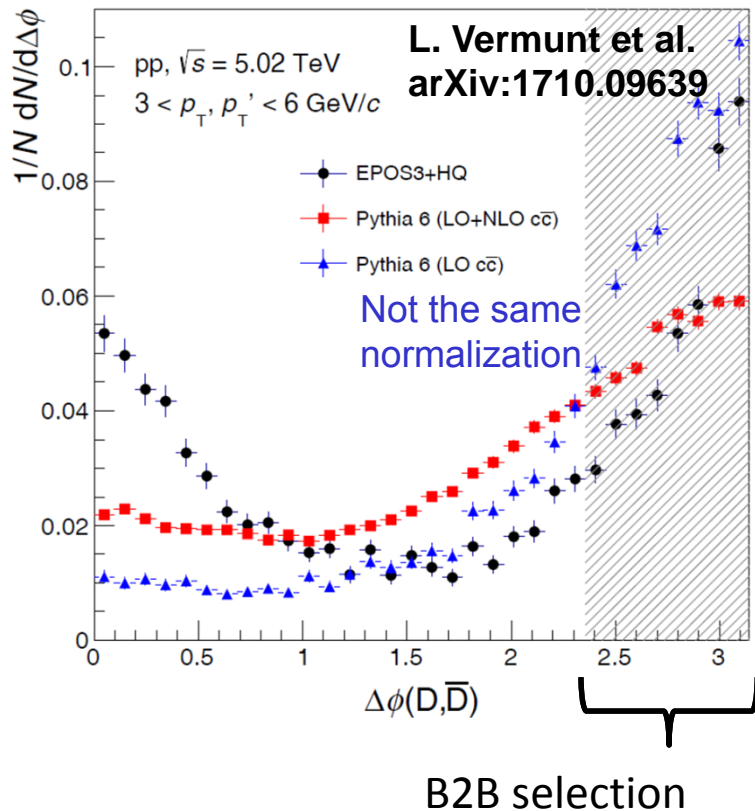
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- In pythia, those topologies are generated by coupling LO processes (implying 0,1 or 2 HQ) and ISR + FSR ... This will be referred to as « LO + NLO ccbar » (strictly speaking, no NLO !)
- Same « strategy » in EPOS3, with « semi-hard pomeron » approach (with some soft evolution included), with various LO Born processes.
- In pythia, possibility to restrict to LO ccbar production processes with massive elements (MSEL=1 -> MSEL=4 flag), still switching on the ... ISR + FSR ... This will be referred to as « LO ccbar »

# Momentum imbalance: not so naïve approach

- Including NLO effects in the charm production (N.B. :beauty would be better for our purpose, but very low statistics)



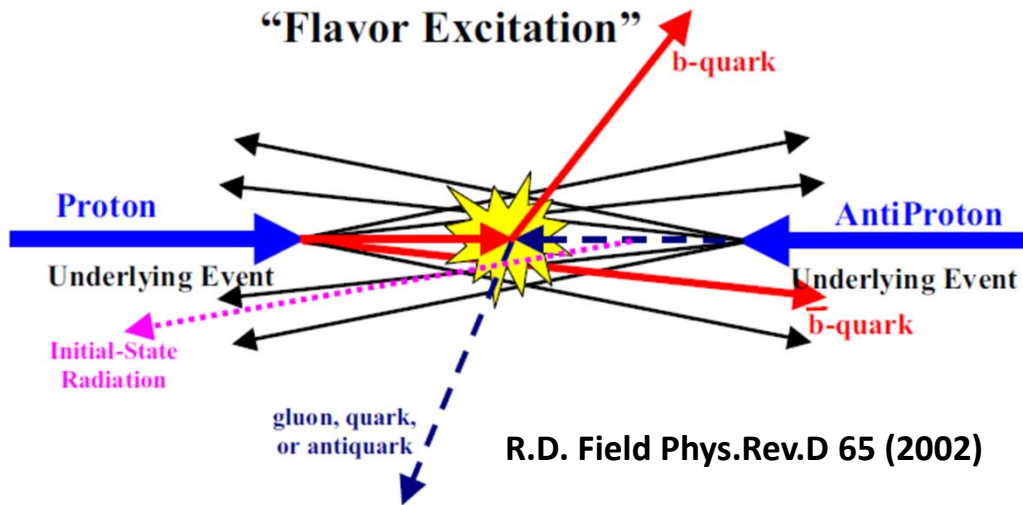
- Good agreement in the normalization for EPOS3 vs PYTHIA « LO » (MSEL=4)
- Large excess PYHTIA « NLO »; shown to be due to **flavor excitation like process**

N.B.: Pythia MSEL=4: at least 1 ccbar pair un each event => Normalized according to high- $p_T$  LO charm creation in Pythia MSEL=1

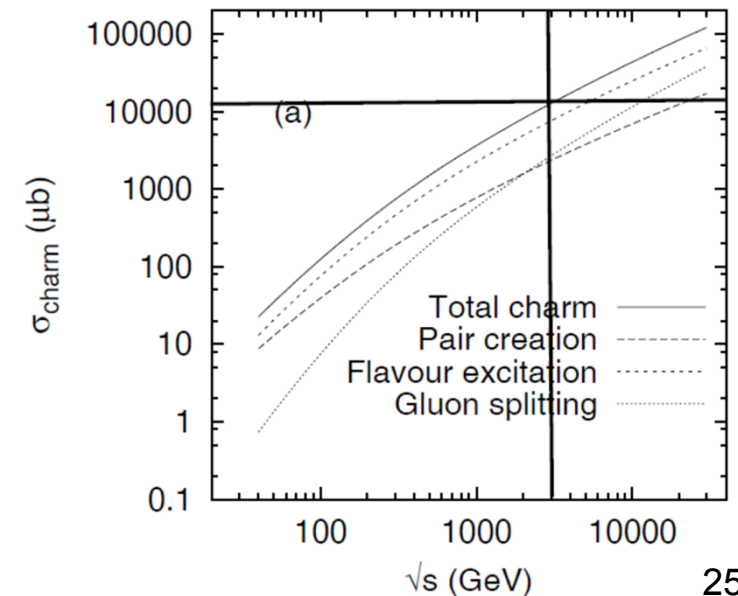
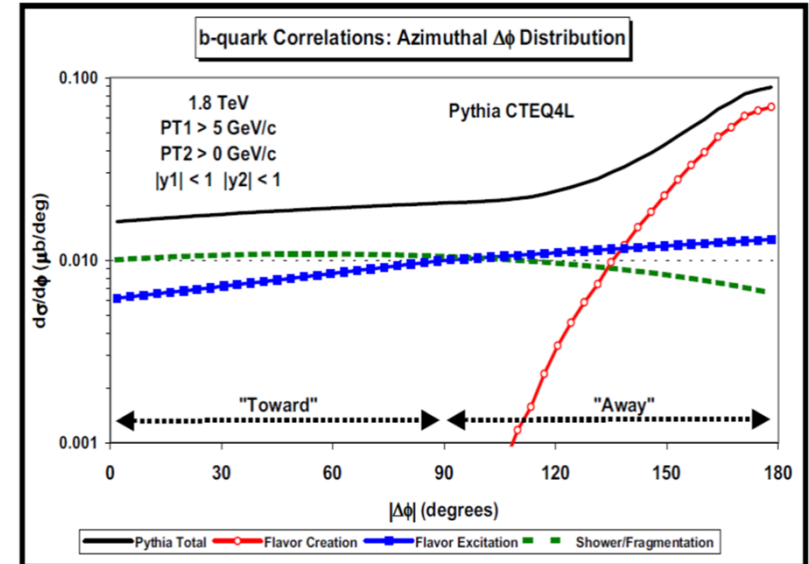


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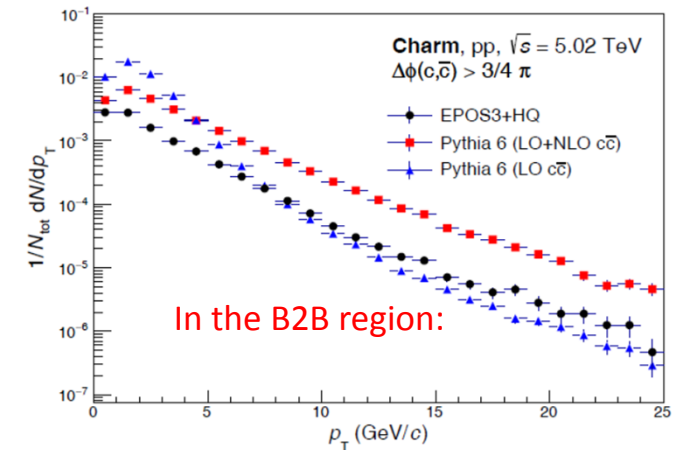
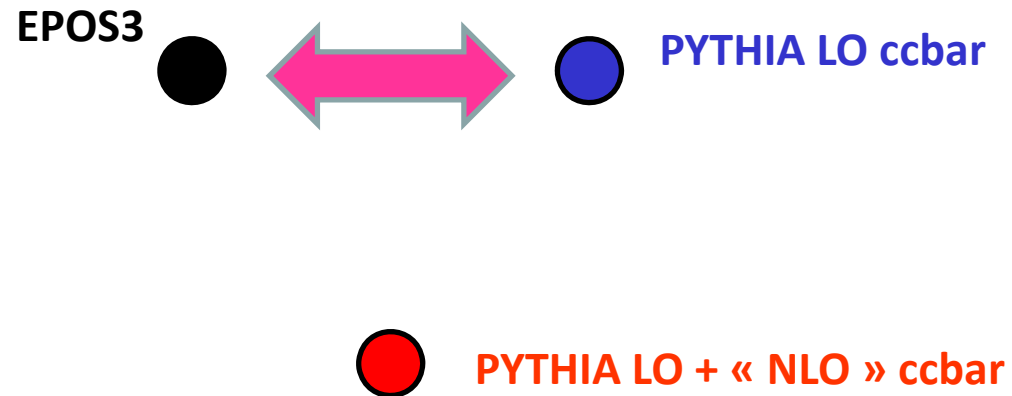
- Including NLO effects in the charm production:



- Flavor excitation: very sensitive to the  $c\bar{c}$  in the proton sea, i.e. to the gluon evolution  $\rightarrow$  large  $Q^2$
- $\sigma_{\text{charm}}$  (Pythia 6,) exceeds measured ALICE value by a factor 3-5. Mostly due to large FEX contribution.
- Similar conclusion of sur-abundant FEX found by CMS (CMS-PAS-HIN-16-005) for beauty quarks

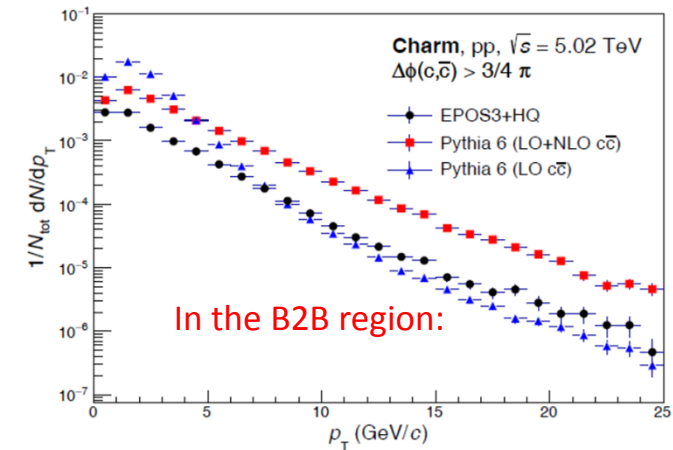
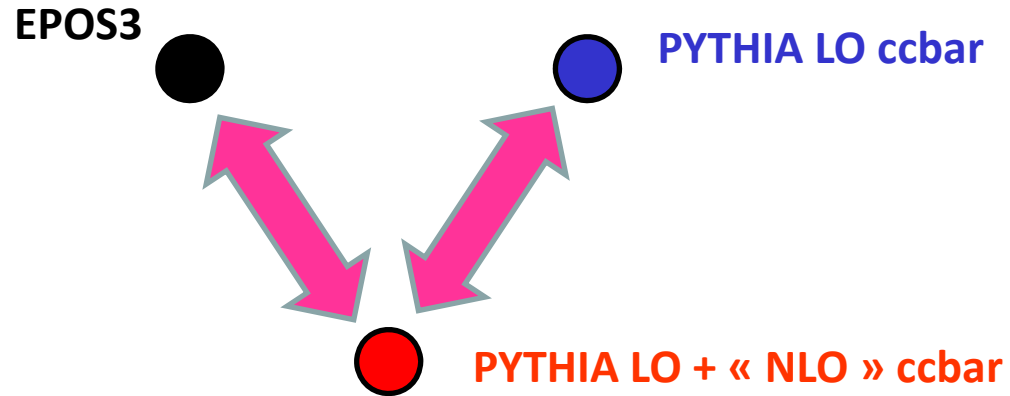


# Momentum imbalance: not so naïve approach



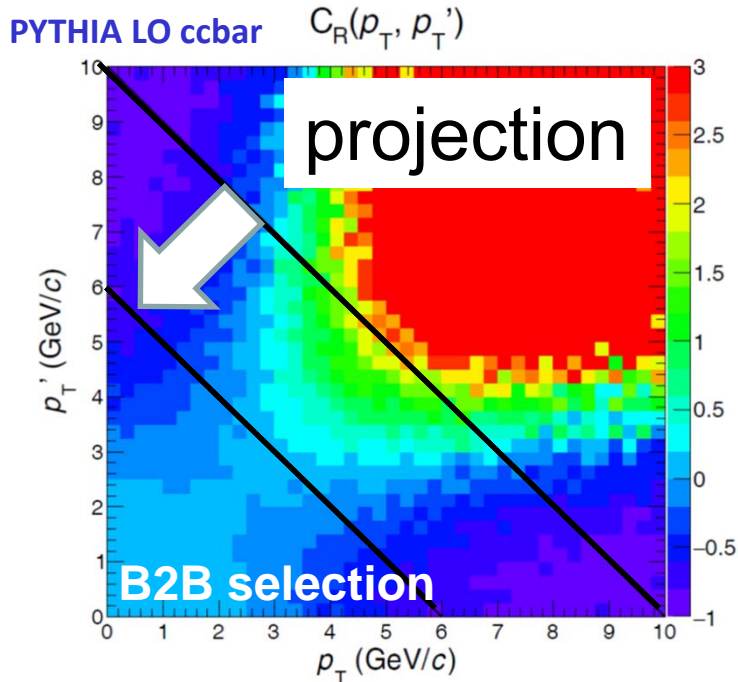
- Same process in the B2B => use the  $p_T$  correlations to investigate FSR

# Momentum imbalance: not so naïve approach



- Same process in the B2B => use the  $p_T$  correlations to investigate FSR
- Use  $p_T$  correlations to resolve FEX contribution in the B2B region

# Momentum imbalance: not so naïve approach



- Different  $p_T$  imbalance for 3 production models in pp
- 2 of them show that NLO effects does not completely destroy the perfect correlation found in LO production
- Similar results for DDbar

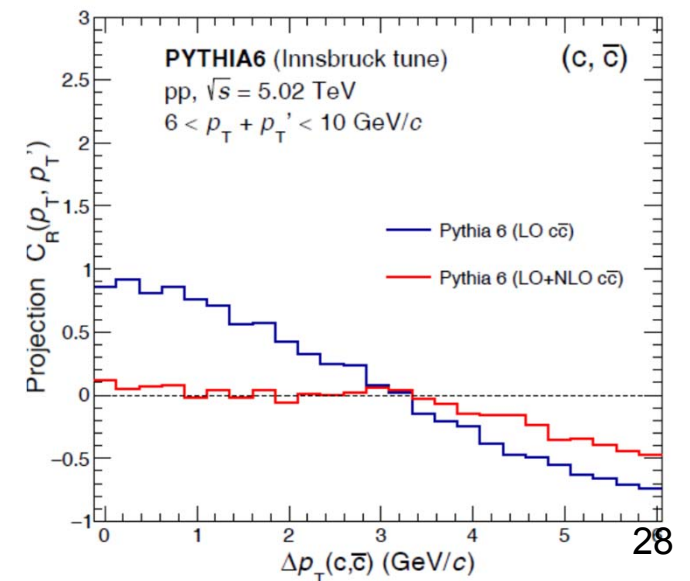
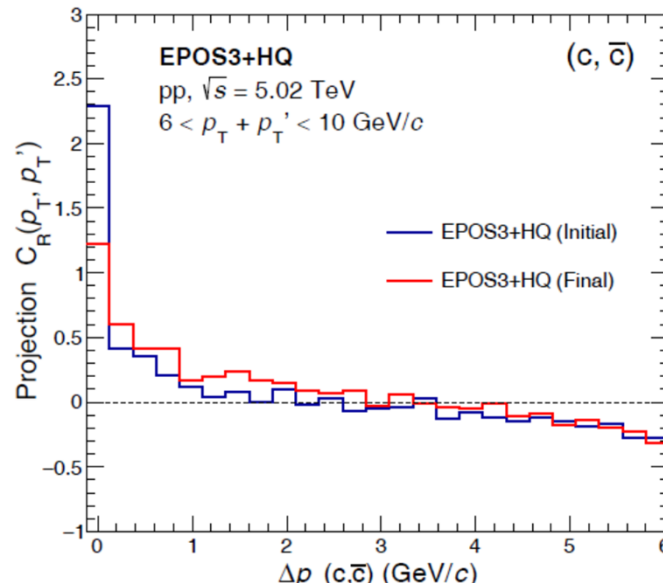
Absolute correlation:

$$C(p_T, p'_T) := \frac{1}{N} \frac{d^2 N(p_T, p'_T)}{dp_T dp'_T} - \frac{1}{N} \frac{dN(p_T)}{dp_T} \times \frac{1}{N} \frac{dN(p'_T)}{dp'_T}$$

- Vanishes if  $d^2N$  factorizes ( $d^2N(p, p') = dN(p) \times dN(p')$ )
- Satisfies  $\int C(p_T, p'_T) dp_T dp'_T = 0$

Relative correlation:  $C_R(p_T, p'_T) := \frac{C(p_T, p'_T)}{\frac{1}{N} \frac{dN(p_T)}{dp_T} \times \frac{1}{N} \frac{dN(p'_T)}{dp'_T}}$

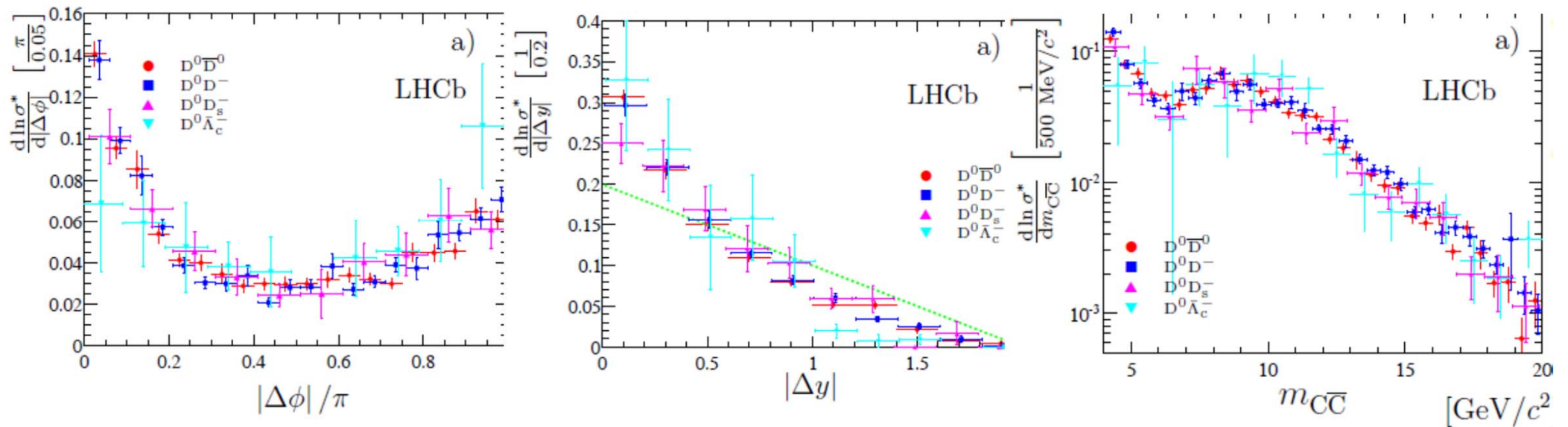
- Reveals correlation at finite  $p_T$



# From the experimental viewpoint

- No momentum imbalance so far in pp @ LHC (to my knowledge)...
- But valuable data from LHCb on DD:

LHCb, J. High Energy Phys. 06, 141 (2012)



- Under present investigation

# Momentum imbalance in A-A

➤ Some recent works:

➤ J. Uphoff et al. (BAMPS): Phys. Rev. C 89 (2014), 064906

**All including realistic  
c-cbar « initial »  
production**

# Momentum imbalance in A-A

J. Uphoff et al. (BAMPS): Phys. Rev. C 89 (2014), 064906:

- **Collisional Energy loss model** calibrated on  $v_2(D)$  meson; lead to acceptable results for  $R_{AA}$  as well.

➤ Chosen observable:

$$A_D = \frac{p_{T;1}^D - p_{T;2}^D}{p_{T;1}^D + p_{T;2}^D}$$

Leading D/Dbar      Sub- Leading D/Dbar

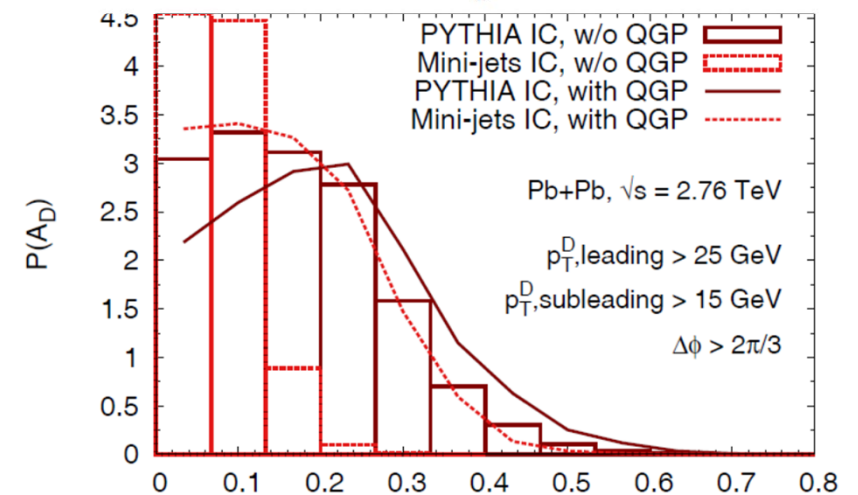
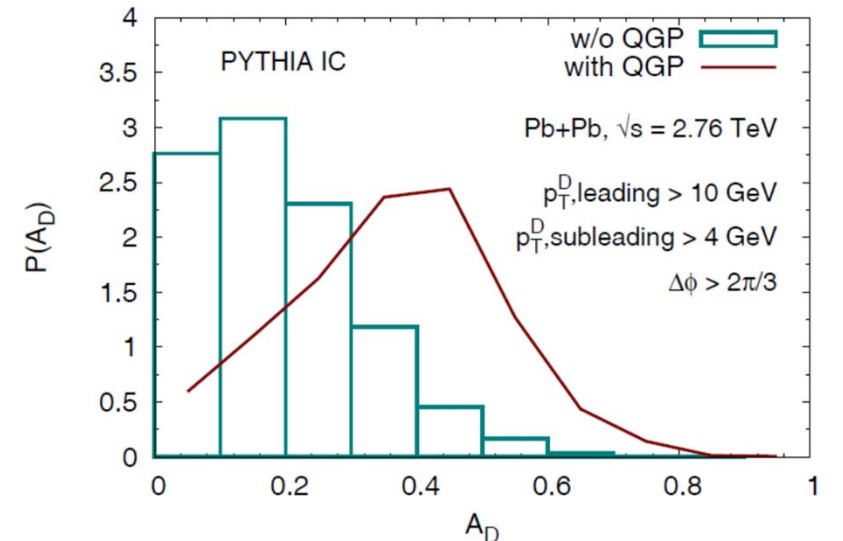
- Back to back selection

- Two selections for most central Pb-Pb collisions:

- “Intermediate”:  $p_{T;1}^D > 10 \text{ GeV}$  and  $p_{T;2}^D > 4 \text{ GeV}$
- “High”:  $p_{T;1}^D > 25 \text{ GeV}$  and  $p_{T;2}^D > 15 \text{ GeV}$

# Momentum imbalance in A-A (BAMPS)

- Intermediate  $p_T$  selection:
  - Strong momentum imbalance resulting from c-quark interaction with QGP
  - Large fraction of c-cbar pairs stemming from disconnected NN interactions
  
- High  $p_T$  selection (focusing on PYTHIA IC):
  - Large fraction of c-cbar pairs stemming from single NN interactions Strong
  - **Moderate** momentum imbalance resulting from c-quark interaction with QGP (MI dominated by IC, as for azimuthal correlations)



“ Furthermore, it would be intriguing to include also radiative processes for charm quarks and investigate their effects on  $A_D$  »

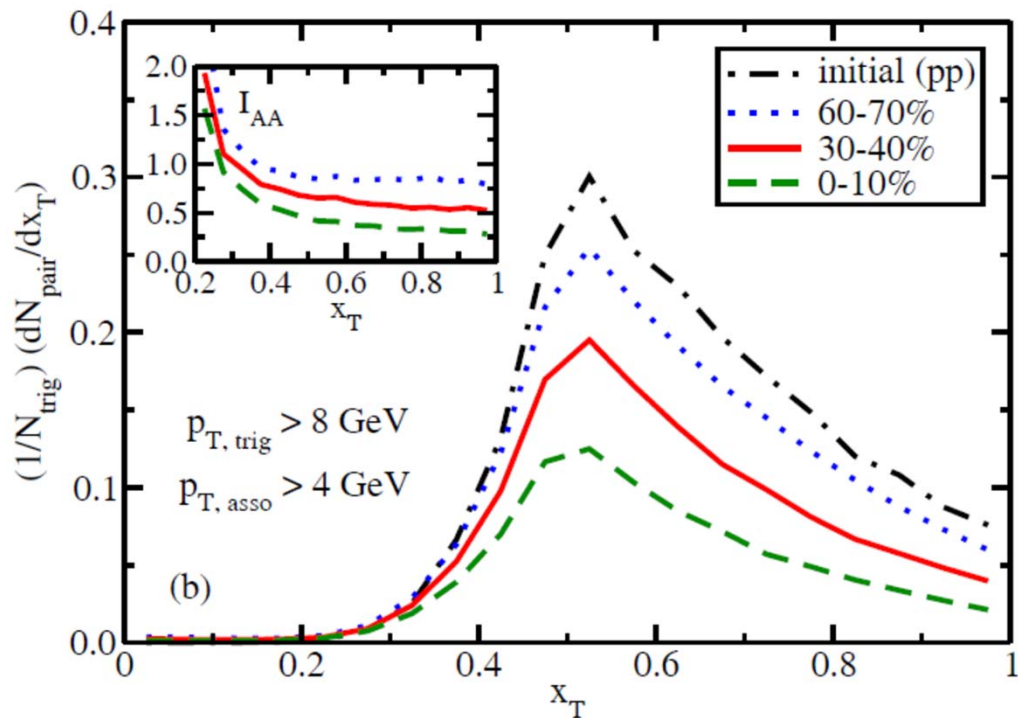


# Momentum imbalance in A-A

➤ Some recent works:

➤ S. Cao et al.: Phys. Rev. C 92 (2015), 054909 (focused on RHIC energies)

All including realistic c-cbar  
« initial » production



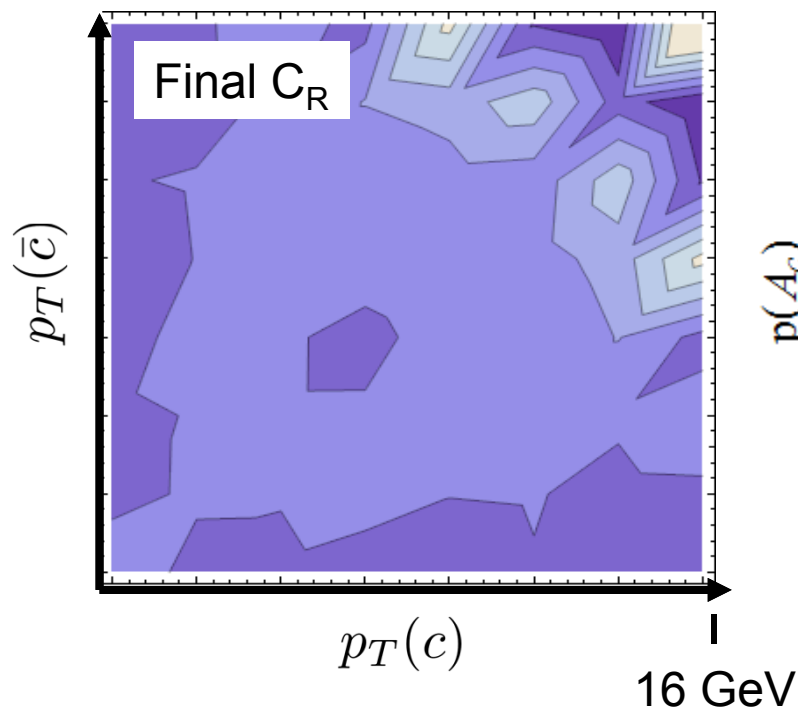
- Observable:  $x_T := \frac{p_T^{D(\bar{D}),\text{sublead}}}{p_T^{\bar{D}(D),\text{lead}}}$
- Moderate increase of momentum imbalance from pp → peripheral Au-Au → central Au-Au collisions
- “...momentum imbalances ... value does not strongly depend on the detailed energy loss mechanism as long as the transport coefficient is properly adjusted to describe the D meson RAA. »

➤ T. Song et al. (PHSD): Phys. Rev. C 96 (2017), 014905 (azimuthal correlations)

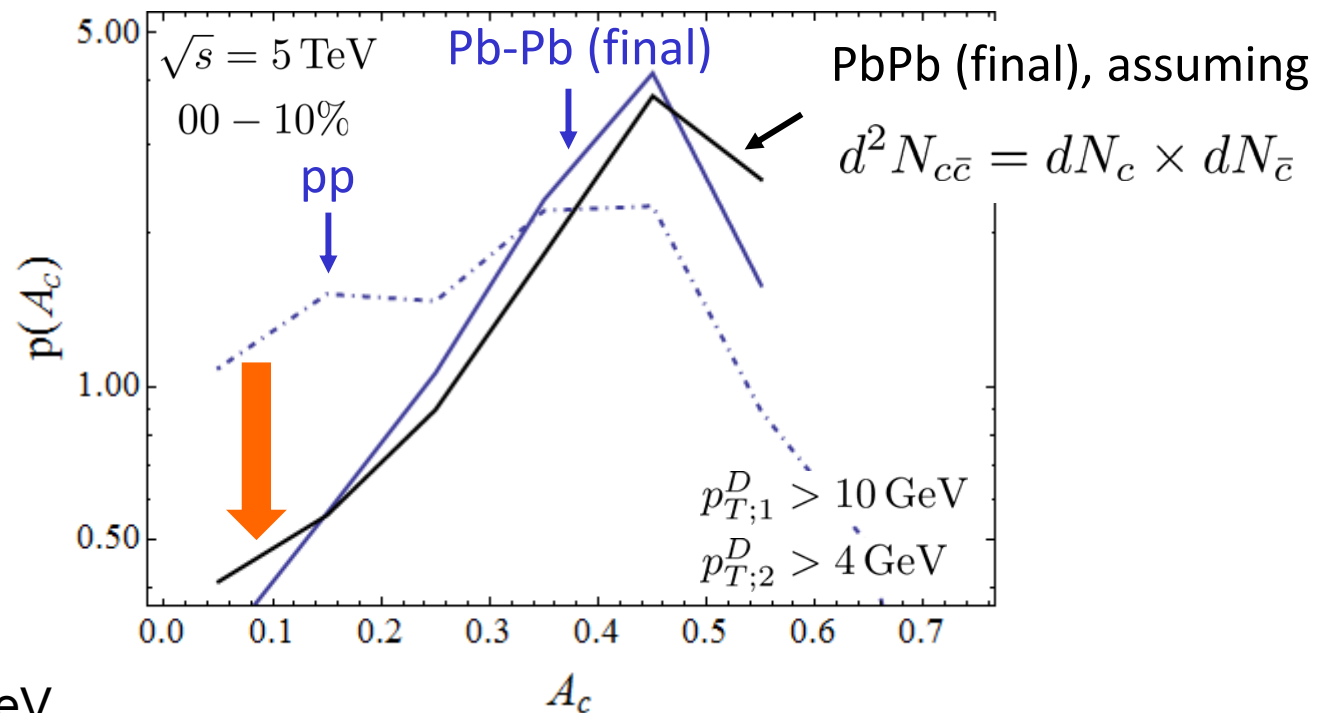
# Momentum imbalance in central Pb-Pb (EPOSHQ)



- All HQ produced according to EPOSHQ (V3210)
- Final c-cbar:



## Collisional Energy loss (K=1.5)



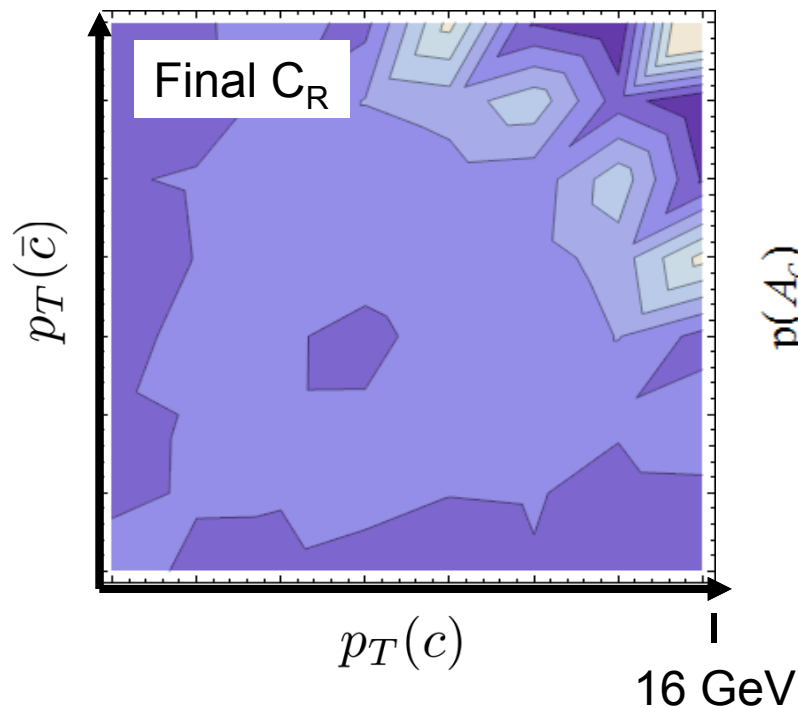
- Very few remaining correlations in the final stage of the collision

- $\approx 100\%$  memory loss of initial correlations

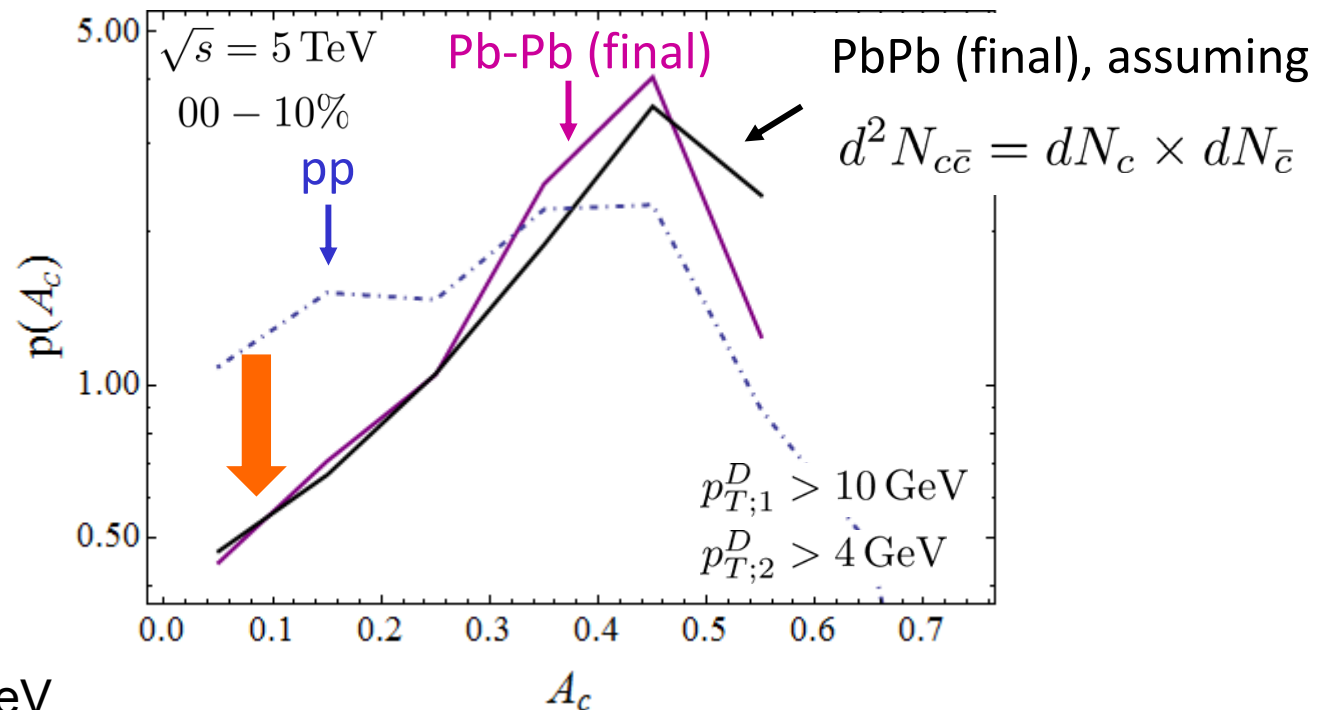
# Momentum imbalance in central Pb-Pb (EPOSHQ)



- All HQ produced according to EPOSHQ (V3210)
- Final c-cbar:



## Col + Rad Energy loss (K=0.8)

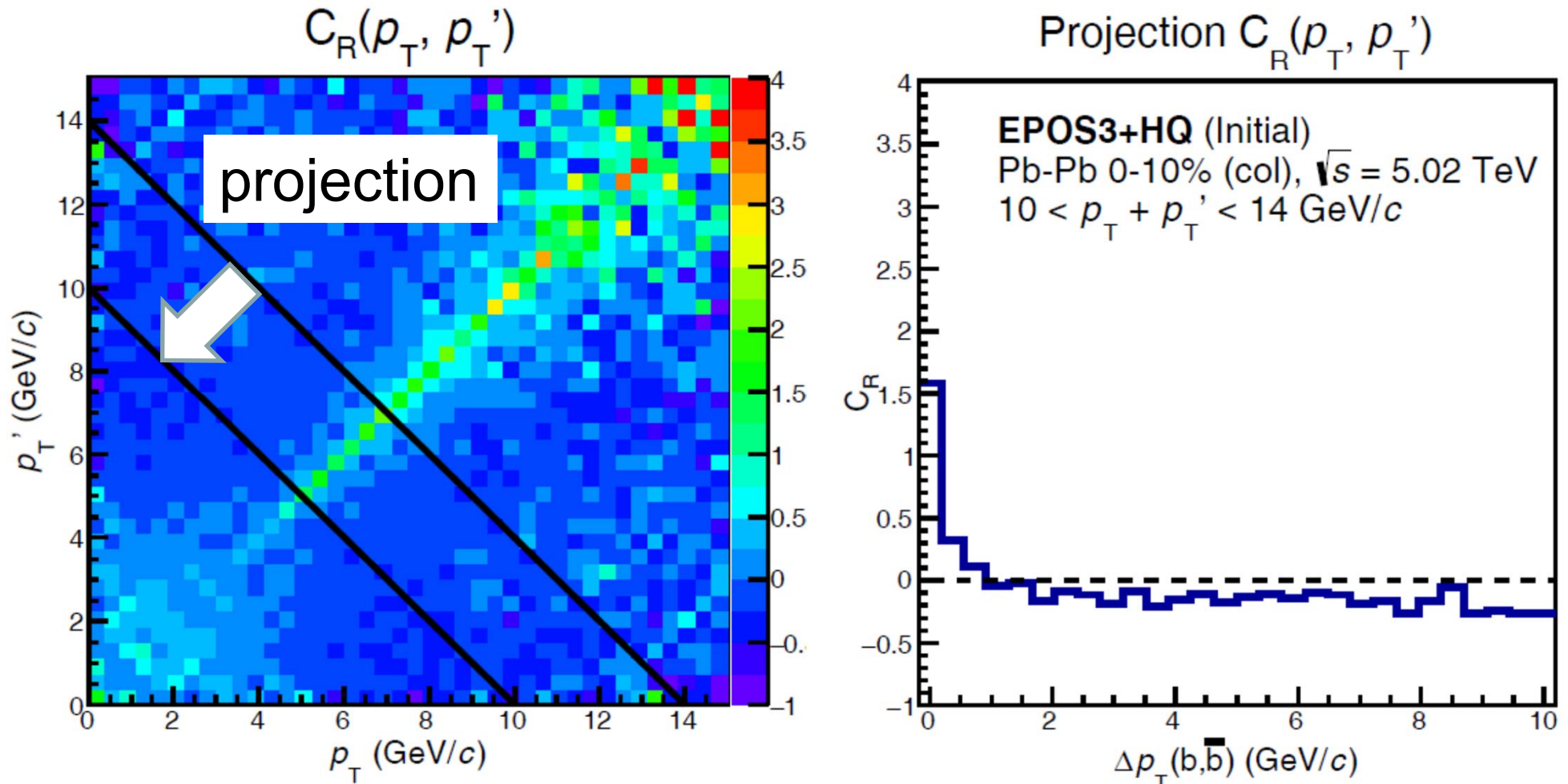


- Very few remaining correlations in the final stage of the collision
- $\approx 100\%$  memory loss of initial correlations, irrespective of E loss mechanism => no good discrimination (also for beauty)
- Problem with  $A_D$ : no clear decorrelation limit

# Momentum imbalance: $b$ -bar in Pb-Pb



- “Initial” stage (before evolution with the medium)



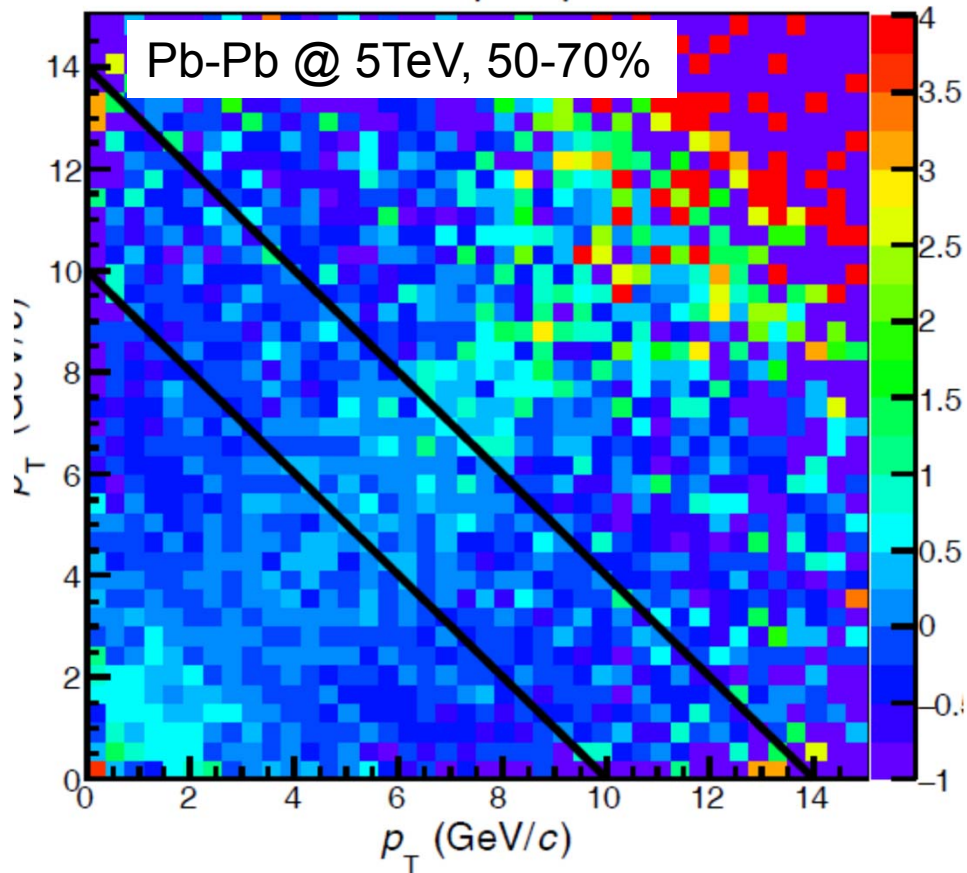
- Very good correlation for intermediate  $p_T$
- Much less uncorrelated background than for  $c$ -bar.

# Momentum imbalance: b-bar in Pb-Pb



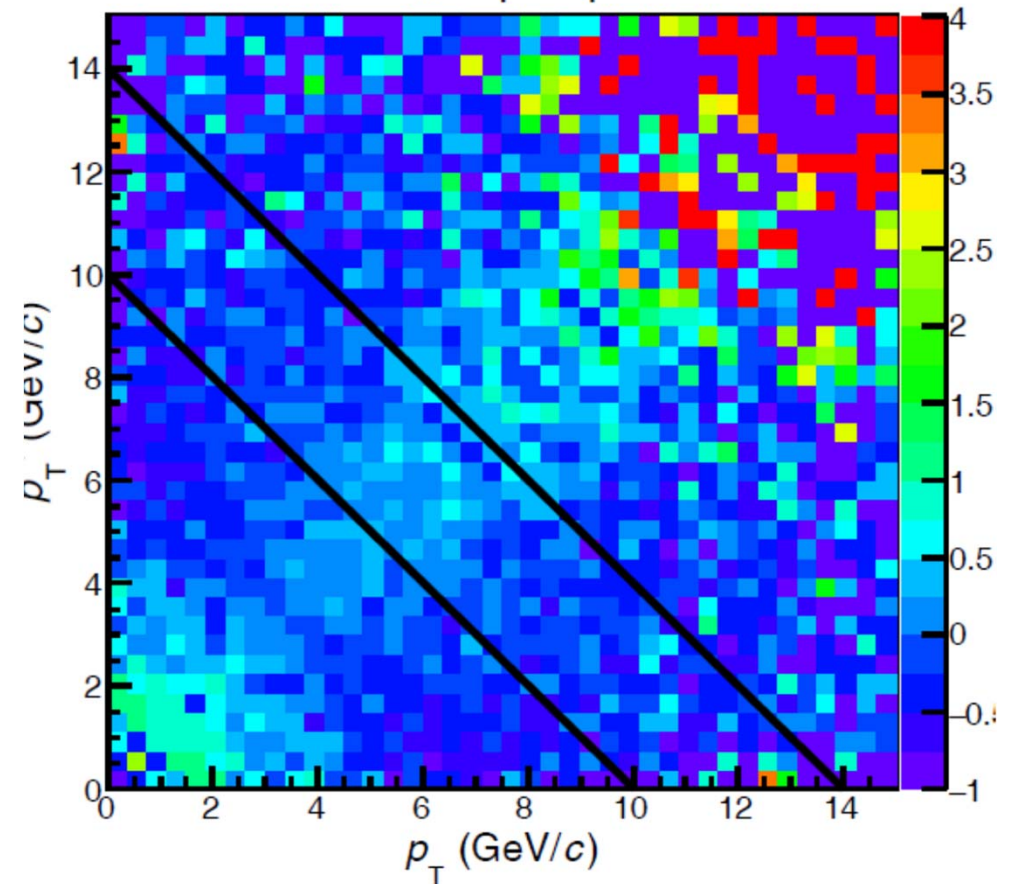
Elastic Energy loss

$$C_R(p_T, p_T')$$

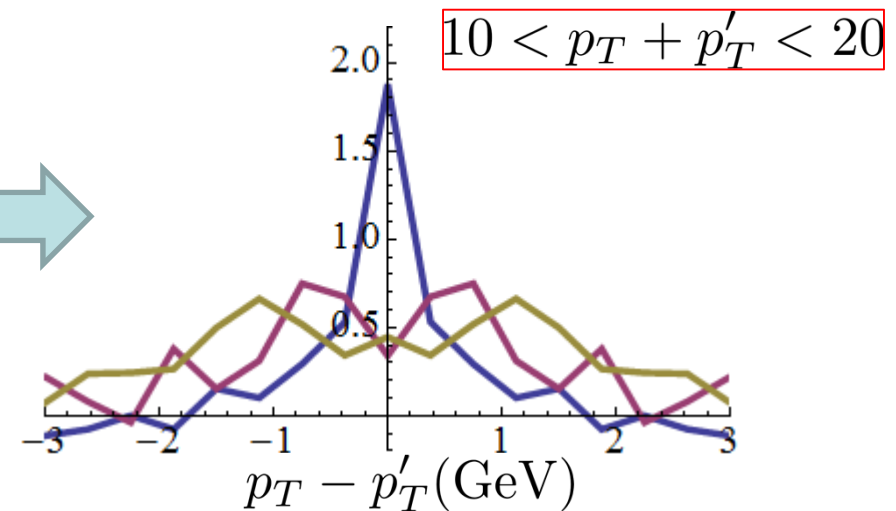
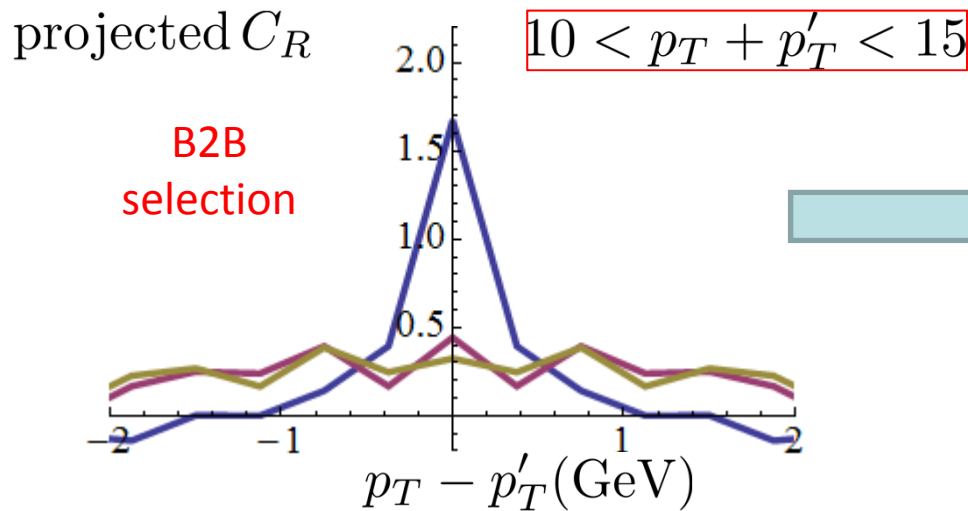
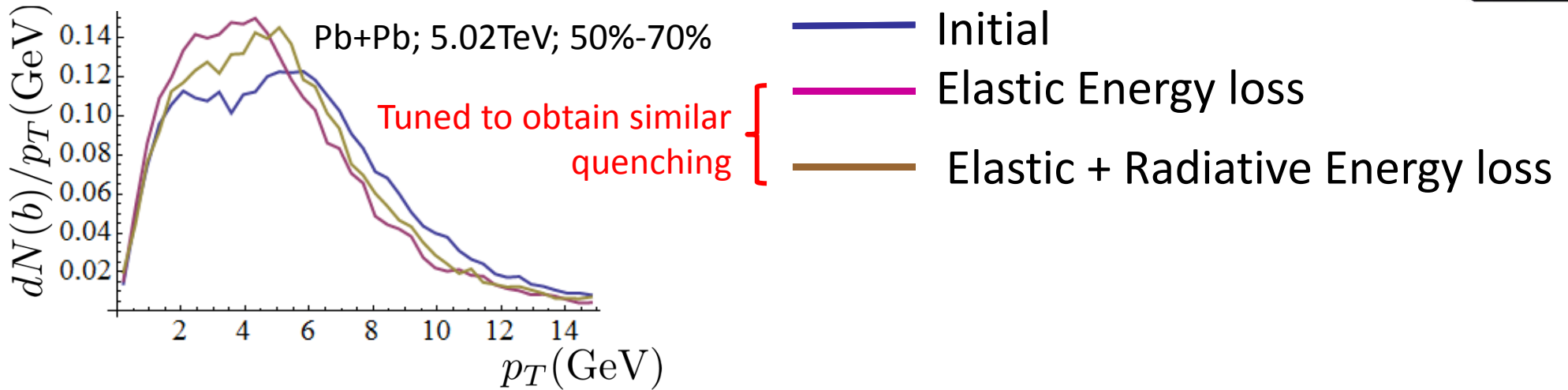


Elastic + Radiative Energy loss

$$C_R(p_T, p_T')$$

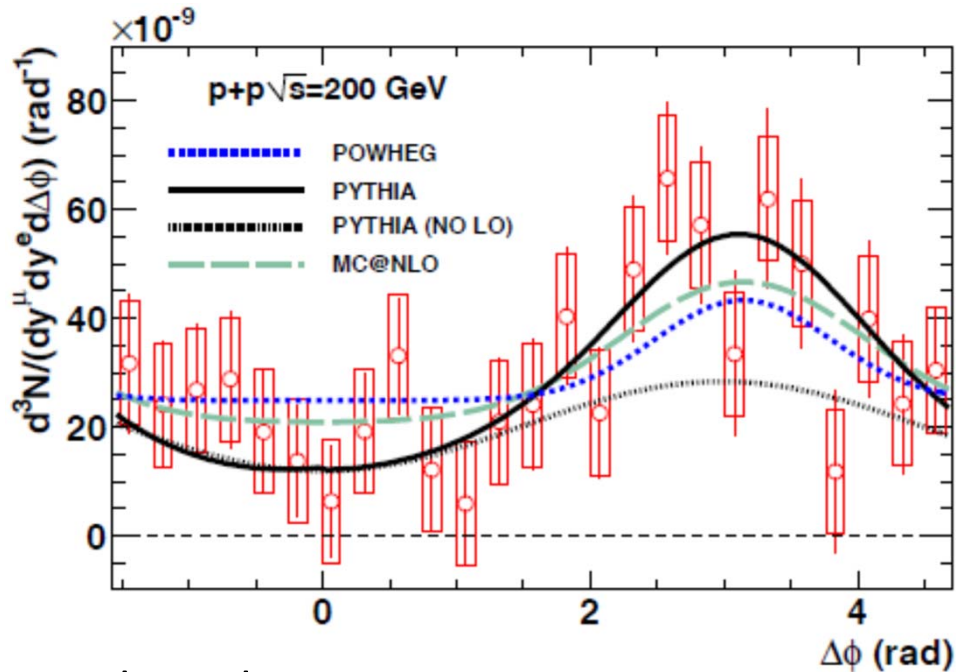


# Momentum imbalance: b-bar in Pb-Pb



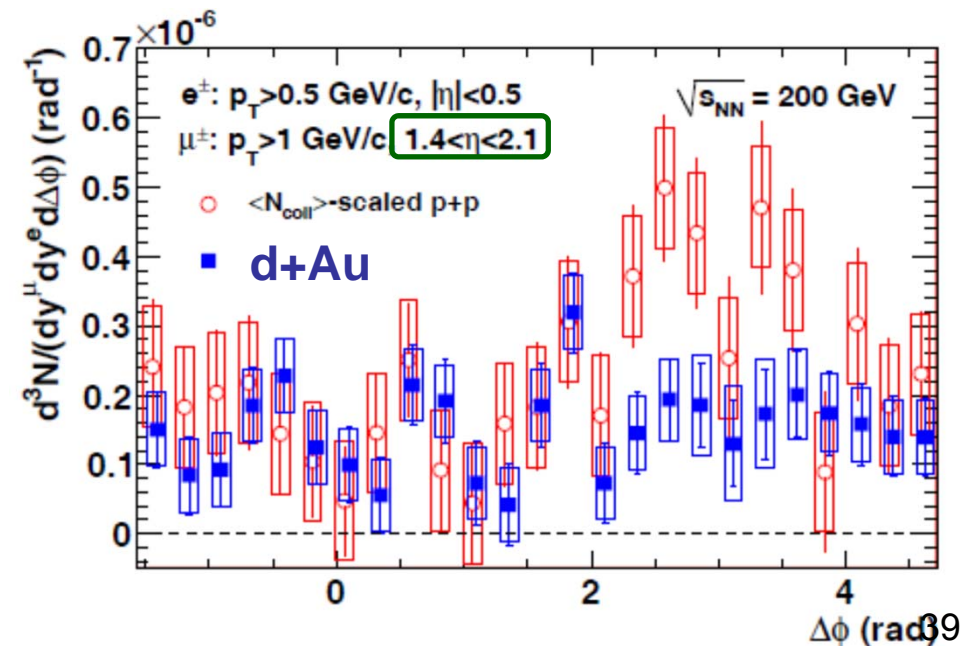
- QGP partly washes away the correlation peak... Possible window to estimate the relative weights of elastic and radiative energy loss for bottom quarks

# Next best thing: HF-HF $\rightarrow$ e- $\mu$ correlations



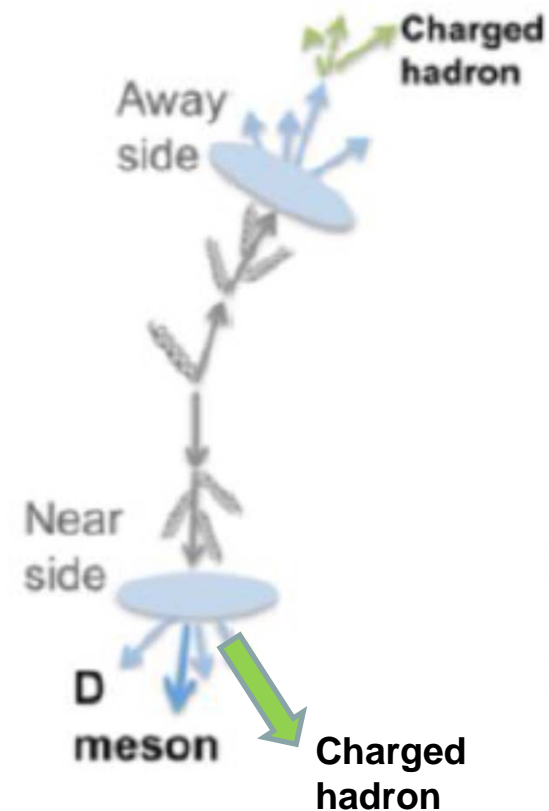
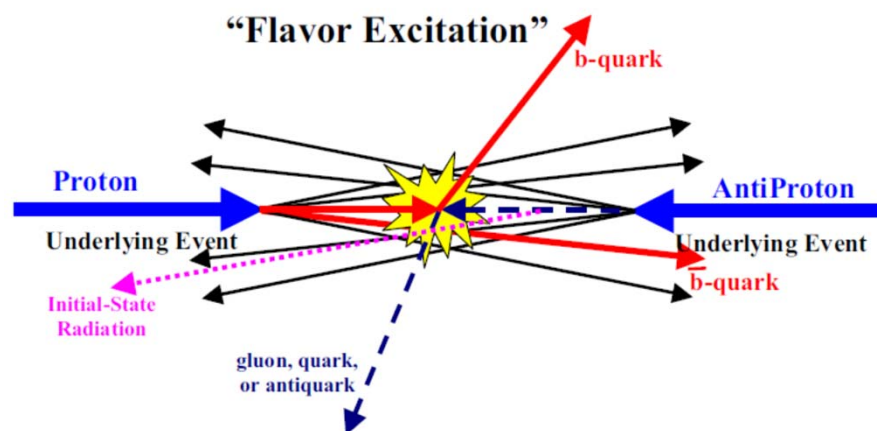
PHENIX: Phys. Rev. C. 89, 034915 (2014)

- Puzzle in the picture:
- “Such a suppression could arise due to nuclear PDF shadowing, saturation of the gluon wavefunction in the Au nucleus, or initial/final state energy loss and multiple scattering. »
- Did not seem to have received enough attention from the community



## Some words on D/B-h / e-h / ... correlations

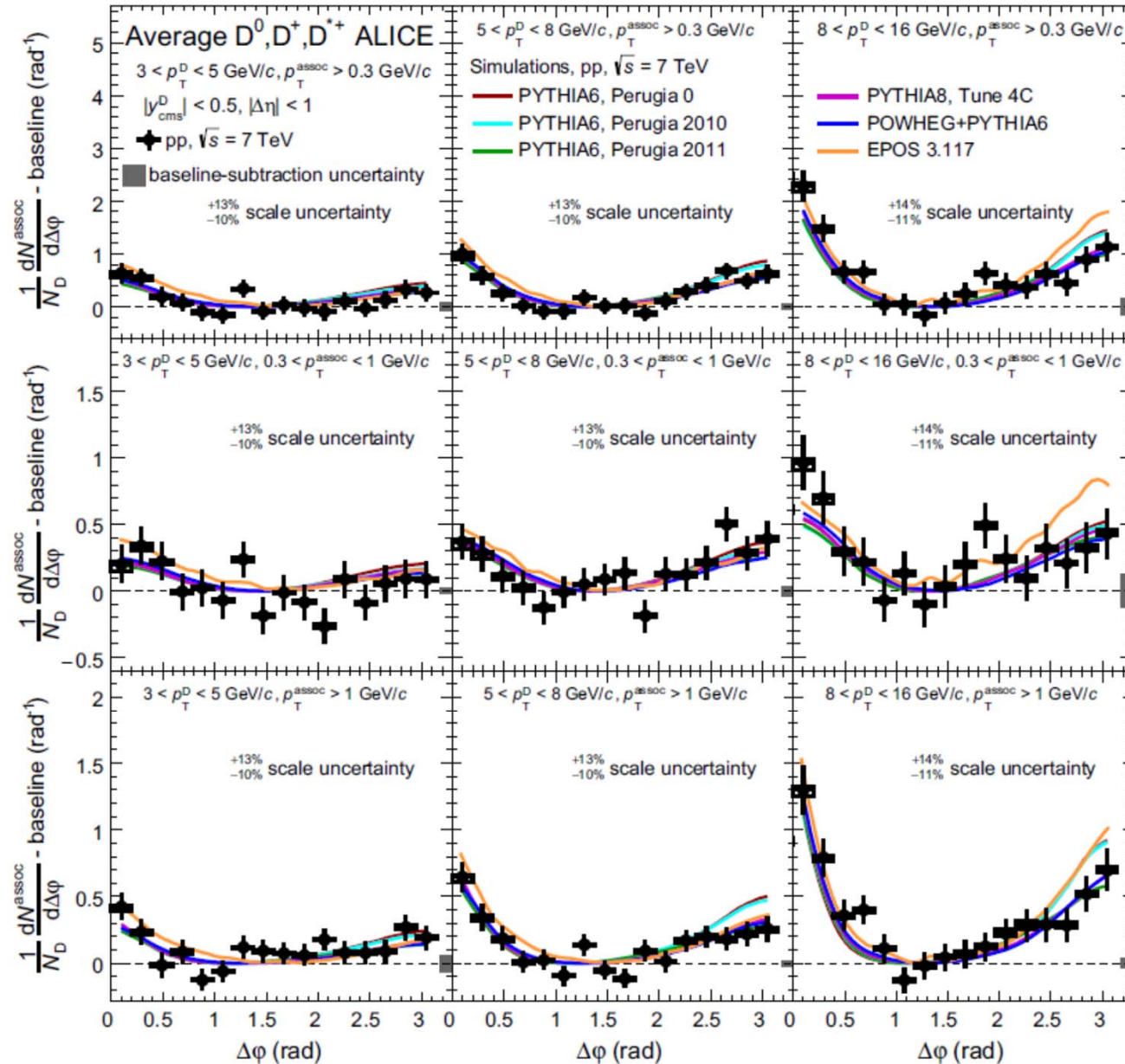
- + : less demanding in terms of statistics (already some experimental results at RHIC and at LHC after run 2 @ LHC)
- + : the near side can provide us new information about the “in medium” fragmentation.
- - : Access to QQbar angular correlations is more indirect and “washed out“
- - : More influenced by the “underlying event” than HF-HF correlations : maybe, HF also feel the influence of the bulk
- - : New processes implied in the away side region:



More involved from a theory / modelling view point; requires multi-component models



# Some words on D-h ... in pp



ALICE, Eur. Phys. J. C (2017) 77:245

- Qualitative agreement between data and models, within the (large) uncertainties
- EPOS3 predicts larger and wider peaks than the PYTHIA/POWHEG for  $\Delta\phi$  correlations

Calibration  $\approx$  ok

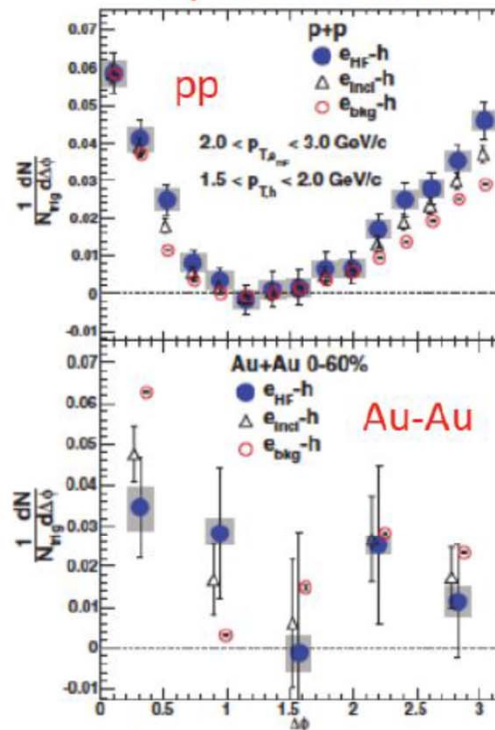
# Some words on e-h / ... in AA (at RHIC)

## Heavy-flavour electron – charged particle correlations at RHIC, PHENIX

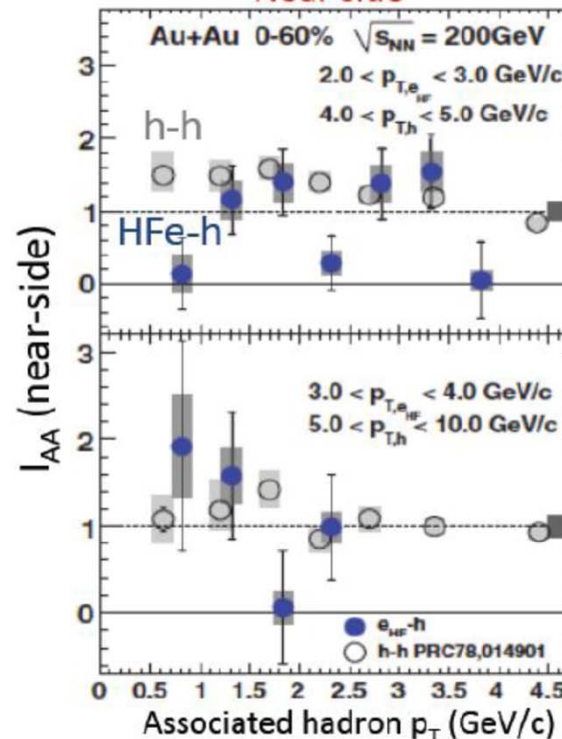
PHENIX Coll.: PRC 83, 044912 (2011)

$I_{AA}$  = ratio of associated yield (Au-Au)/pp

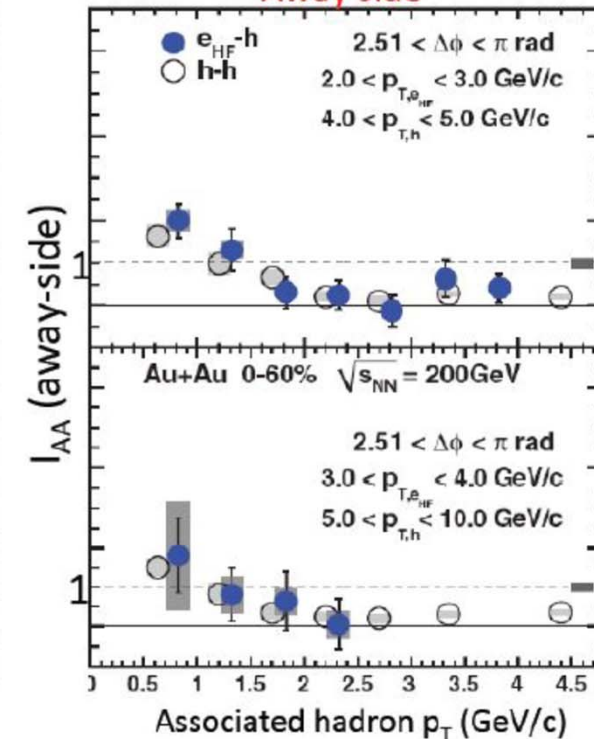
$\Delta\phi$  distributions



Near side



Away side



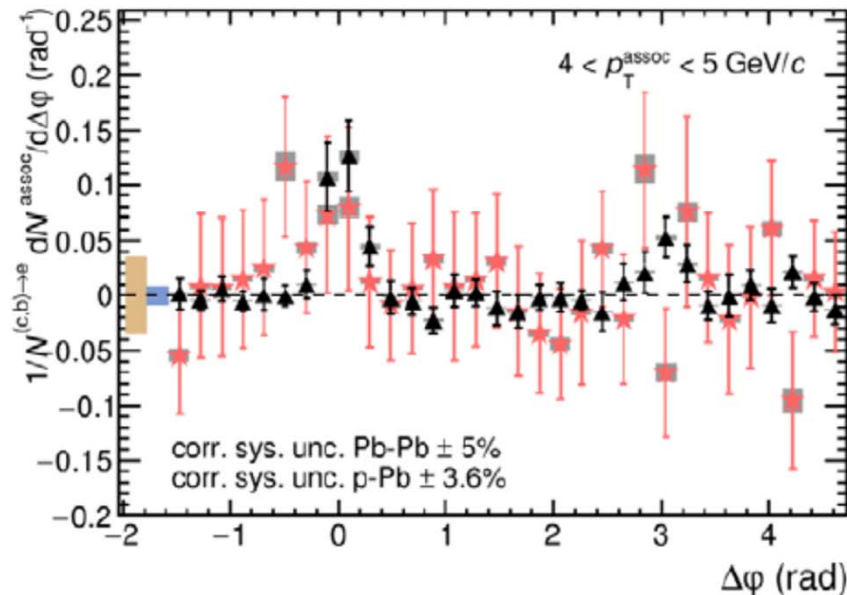
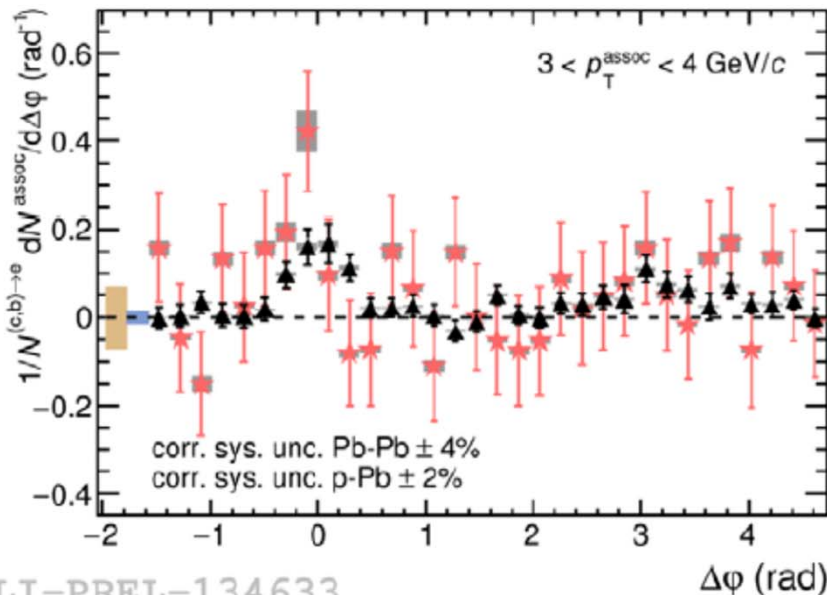
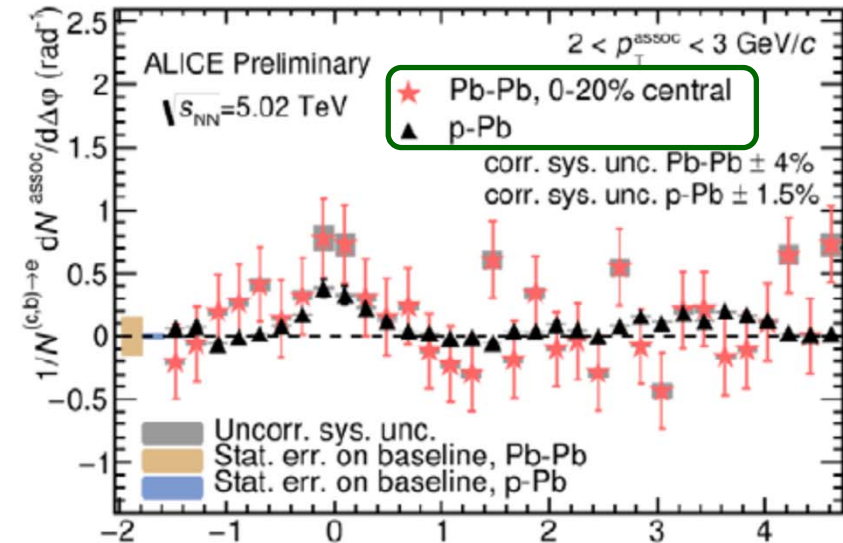
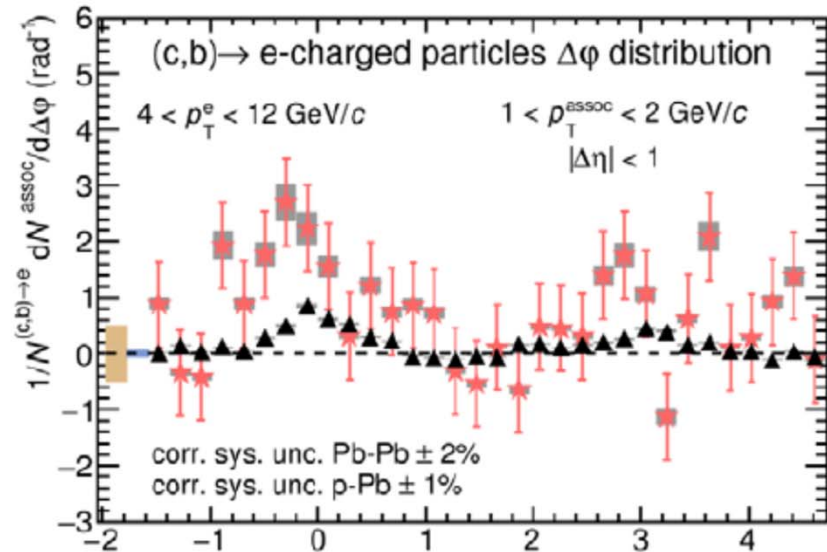
Large uncertainties in Au-Au measurement prevent firm conclusions

Suggest a decreasing  $I_{AA}$  trend with hadron  $p_T$  in the away side

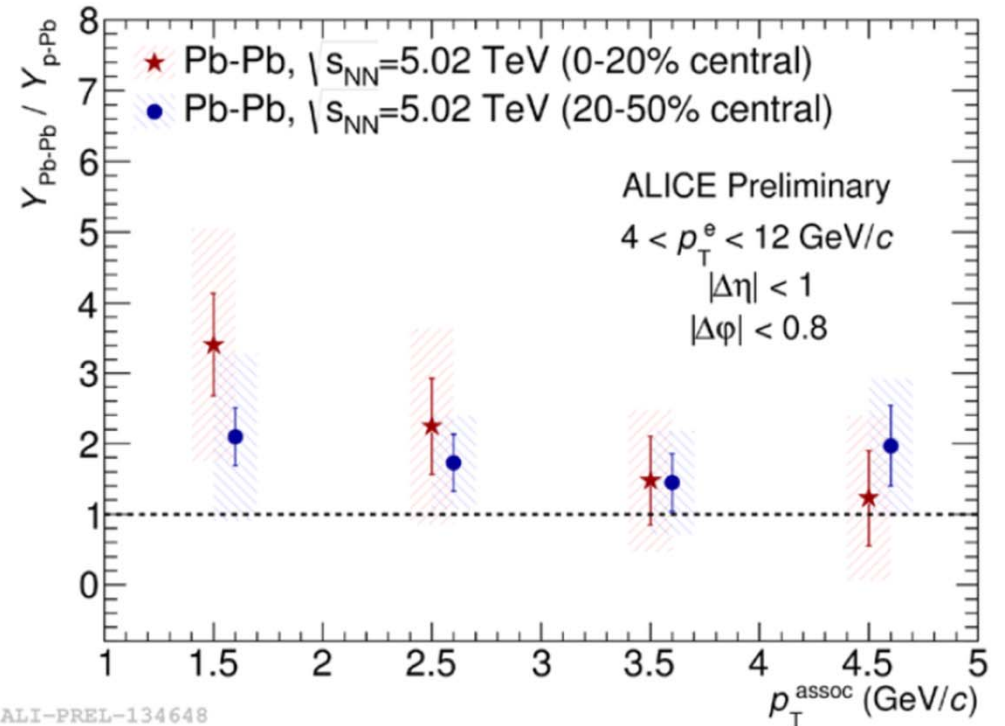
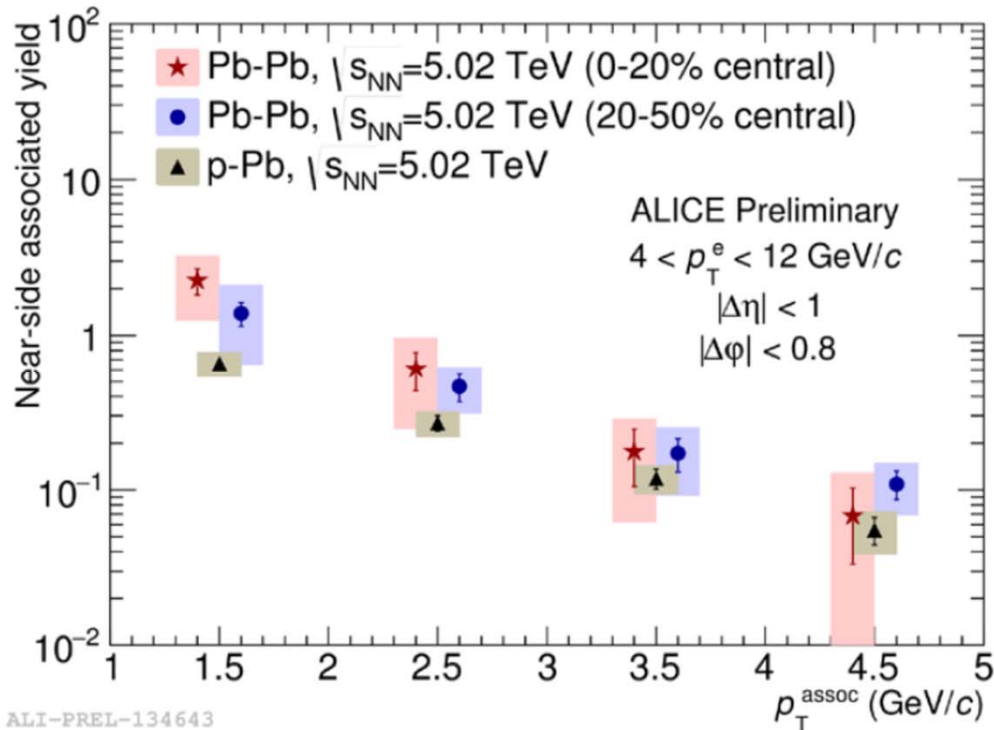
Similar results than hadron-hadron correlations (a coincidence?)

→ Higher precision  
with new data

# Some words on e-h / ... in AA (at LHC)



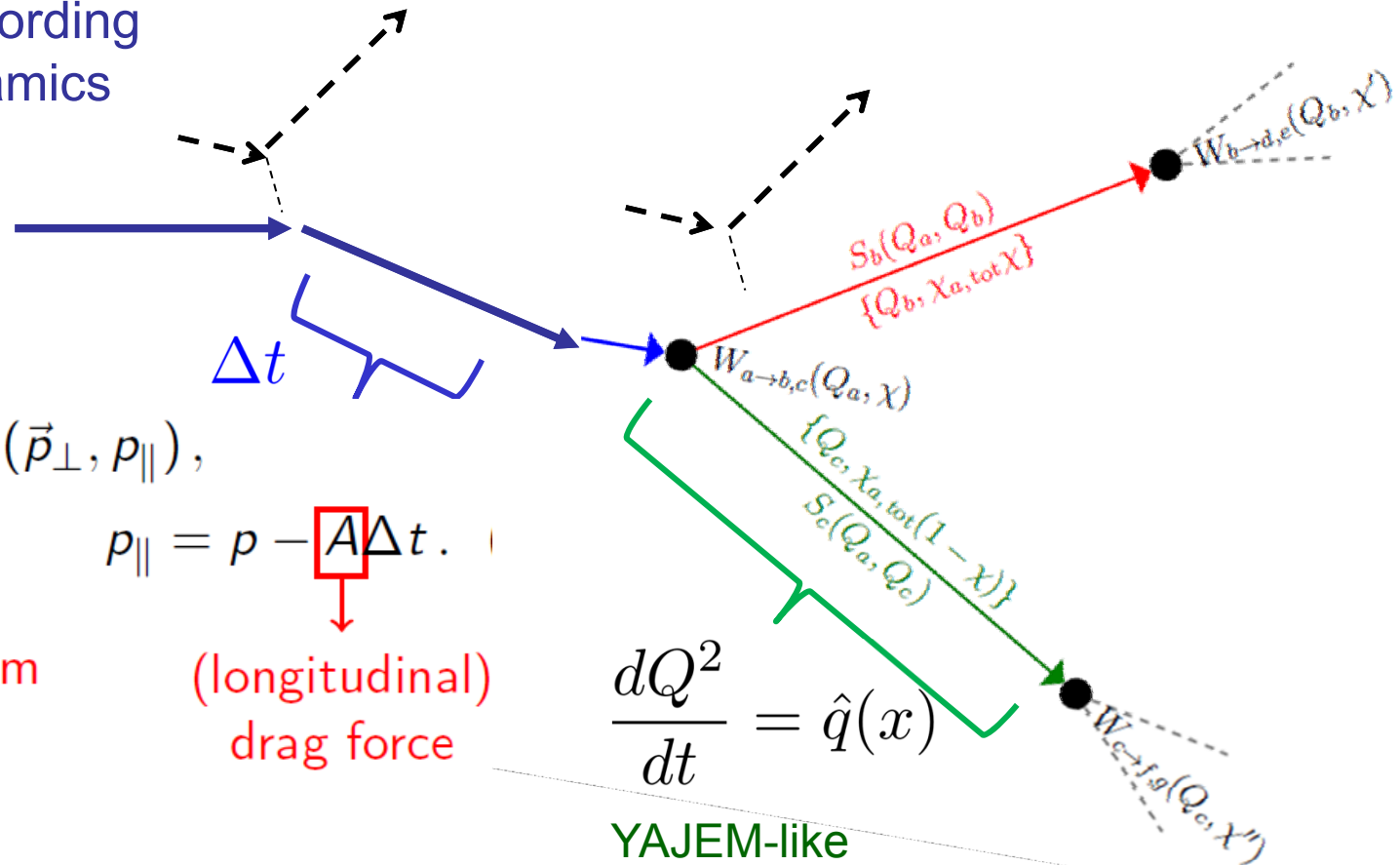
# Some words on e-h / ... in AA (at LHC)



- ALICE concludes: “Going lower with  $p_T^{\text{assoc}}$ , hints of a hierarchy in NS yields: Pb-Pb 0-20% shows an enhancement w.r.t. p-Pb, despite very large total uncertainties” : **priority 1**
- No conclusion for the away side peak after run 2. **priority >1**

# Modified DGLAP (Elastic + induced radiation)

Rescattering according to Langevin dynamics



$$\vec{p} = (\vec{0}, p) \mapsto \vec{p}' = (\vec{p}_\perp, p_\parallel),$$

$$p_\perp = \sqrt{\hat{q} \Delta t},$$

$$p_\parallel = p - A \Delta t.$$

transverse momentum transfer

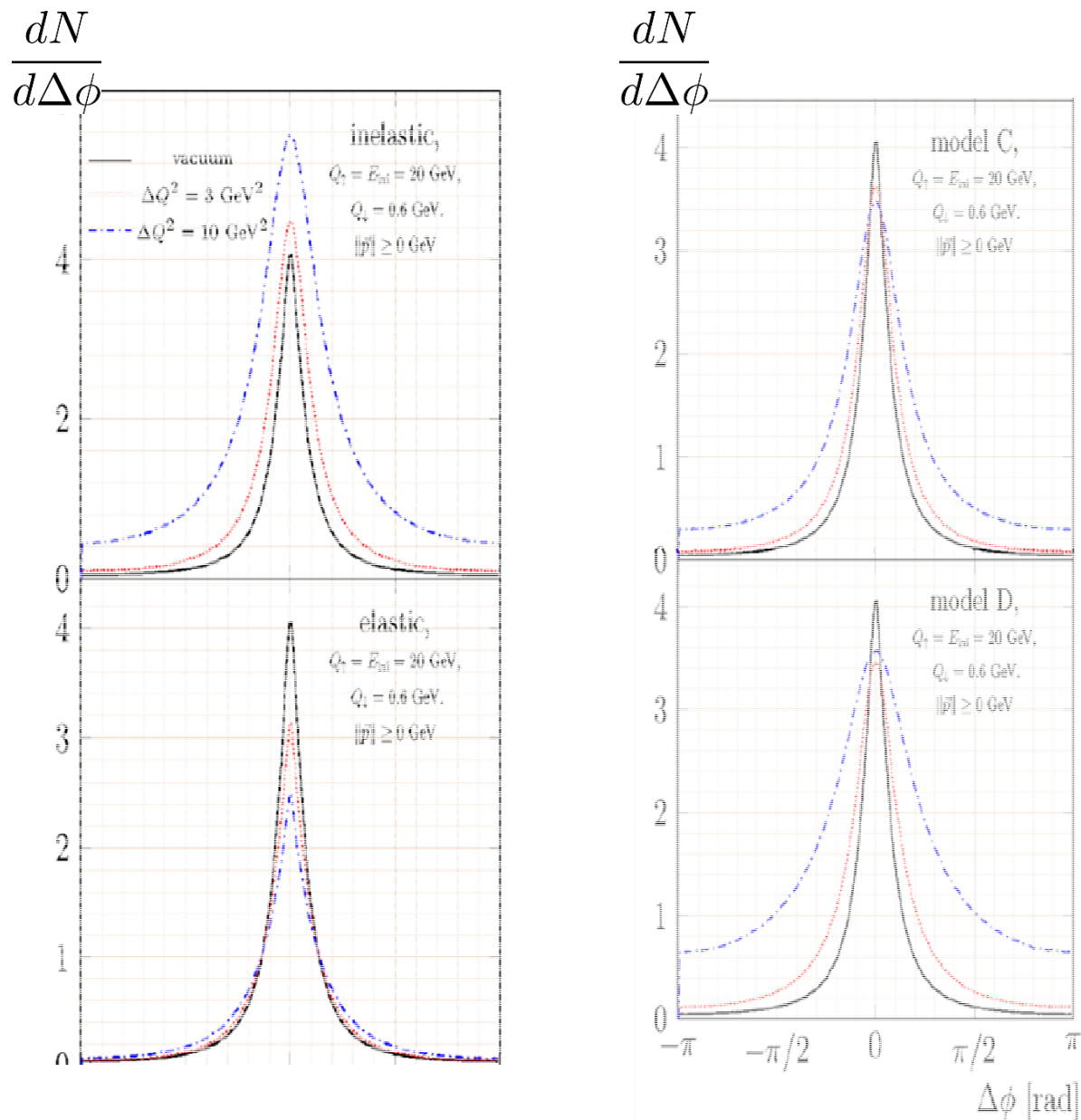
(longitudinal) drag force

$$A = \frac{\hat{q}}{\kappa T}$$

[H. Berrehrah et al. PRC 90, 064906 (2014)]

increase of the virtuality => extra induced radiation.

# Near side study with a generic jet – medium model



M. Rohrmoser's PhD thesis (2017)

Preliminary results in J.Phys. Conf. Ser. 779 (2017), 012032

...To be implemented in EPOSHQ with bulk back-reaction

# Conclusions

- HF Correlations are for sure interesting per se and offers a bright future... but:
- One should not expect huge effects ! Up to now, the best effects I am aware of in realistic calculations are of the order of 10 %
- They often imply a much deeper understanding of the production mechanisms (one additional ingredient in the game !)
- Brand new study on momentum imbalance : avoid central (and even semi-central) collisions in order to discriminate between Eloss mechanisms.
- Too early to conclude; as a theorist, one has to get ready to deal with the improved precision data in the HF-HF or  $\gamma$ -HF sector
- HF – hadrons correlations requires fully fledged models and simulators
- By then, the most efficient “constrain” can be obtained by performing systematic multi-domain comparison of the traditional single particle observables...

# Pentaquark state discovered at “La Guadeloupe”





Back up

# Our basic ingredients for HQ energy loss

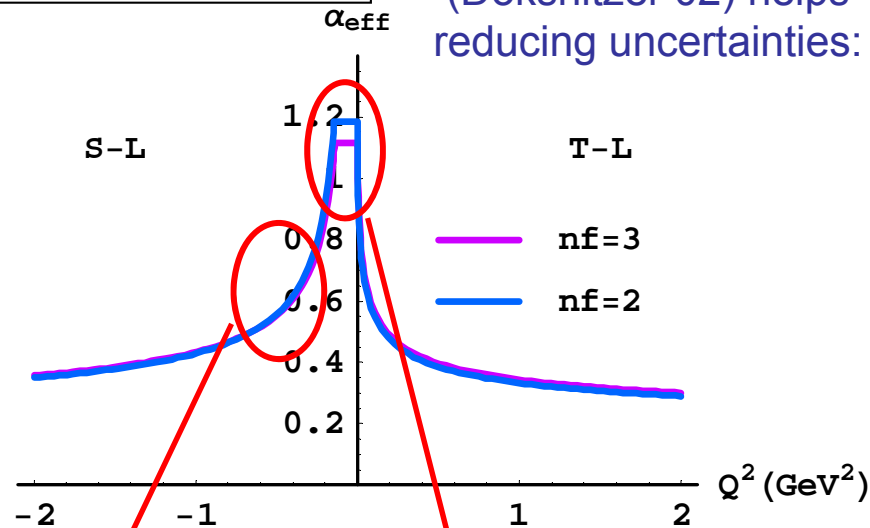
## Elastic

Motivation: Even a fast parton with the largest momentum  $P$  will undergo collisions with moderate  $q$  exchange and large  $\alpha_s(Q^2)$ . The running aspect of the coupling constant is often “forgotten/neglected” in some approaches

Effective  $\alpha_s(Q^2)$  (Dokshitzer 95, Brodsky 02)

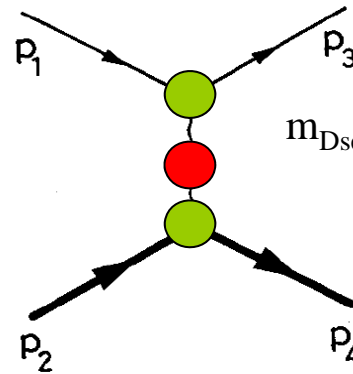
$$\frac{1}{Q_u} \int_{|Q^2| \leq Q_u^2} dQ \alpha_s(Q^2) \approx 0.5$$

“Universality constrain” (Dokshitzer 02) helps reducing uncertainties:



IR safe.  $Q^2$  close to 0 does not contribute to Eloss

Large values for intermediate momentum-transfer => larger cross section

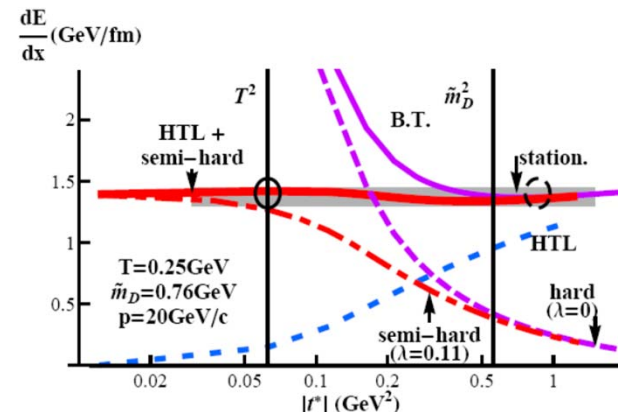


$$m_{\text{Dself}}^2(T) = (1+n_f/6) 4\pi\alpha_{\text{eff}}(m_{\text{Dself}}^2) T^2$$

$$\text{prop} \propto \frac{1}{q^2 - \kappa m_{\text{Dself}}^2(T)}$$

+ u and s channels

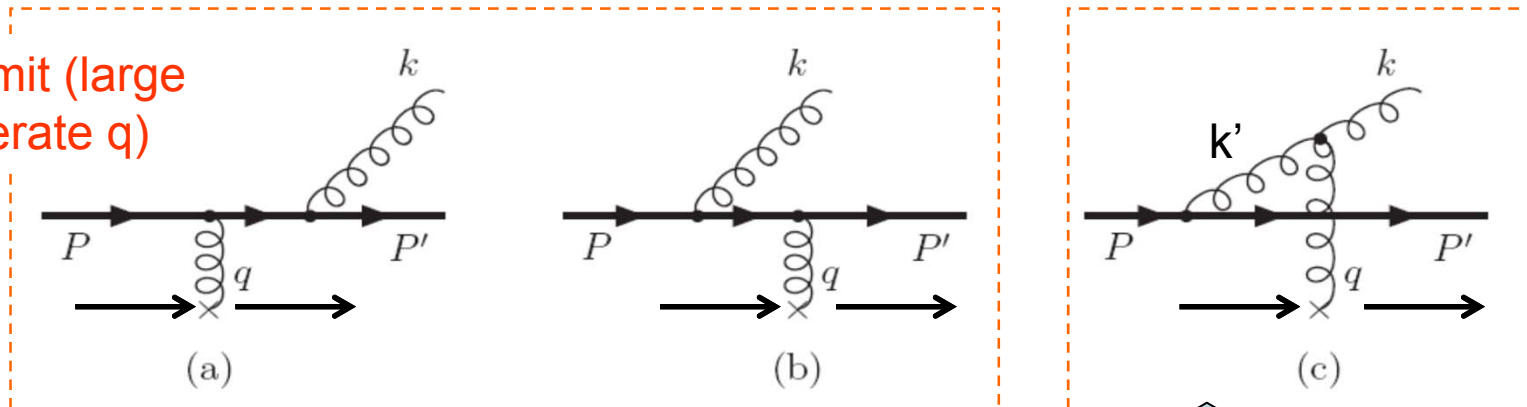
One gluon exchange effective propagator, designed in order to guarantee maximal insensitivity of  $dE/dx$  in Braaten-Thomas scheme



# Induced Energy Loss

Generalized Gunion-Bertsch (NO COHERENCE) for finite HQ mass, dynamical light partons

Eikonal limit (large E, moderate q)



$$\omega \frac{d^3 \sigma_{\text{rad}}^{x \ll 1}}{d\omega d^2 k_{\perp} dq_{\perp}^2} = \frac{N_c \alpha_s}{\pi^2} (1-x) \times \frac{J_{\text{QCD}}^2}{\omega^2} \times \frac{d\sigma_{\text{el}}^{Qq}}{dq_{\perp}^2}$$

Dominates as small x as one “just” has to scatter off the virtual gluon k’

with

$$\frac{J_{\text{QCD}}^2}{\omega^2} = \left( \frac{\vec{k}_{\perp}}{k_{\perp}^2 + x^2 M^2 + (1-x)m_g^2} - \frac{\vec{k}_{\perp} - \vec{q}_{\perp}}{(\vec{k}_{\perp} - \vec{q}_{\perp})^2 + x^2 M^2 + (1-x)m_g^2} \right)^2$$

Gluon thermal mass  $\sim 2T$  (phenomenological; not in BDMPS)

Quark mass

Both cures the collinear divergences and influence the radiation spectra (dead cone effect)

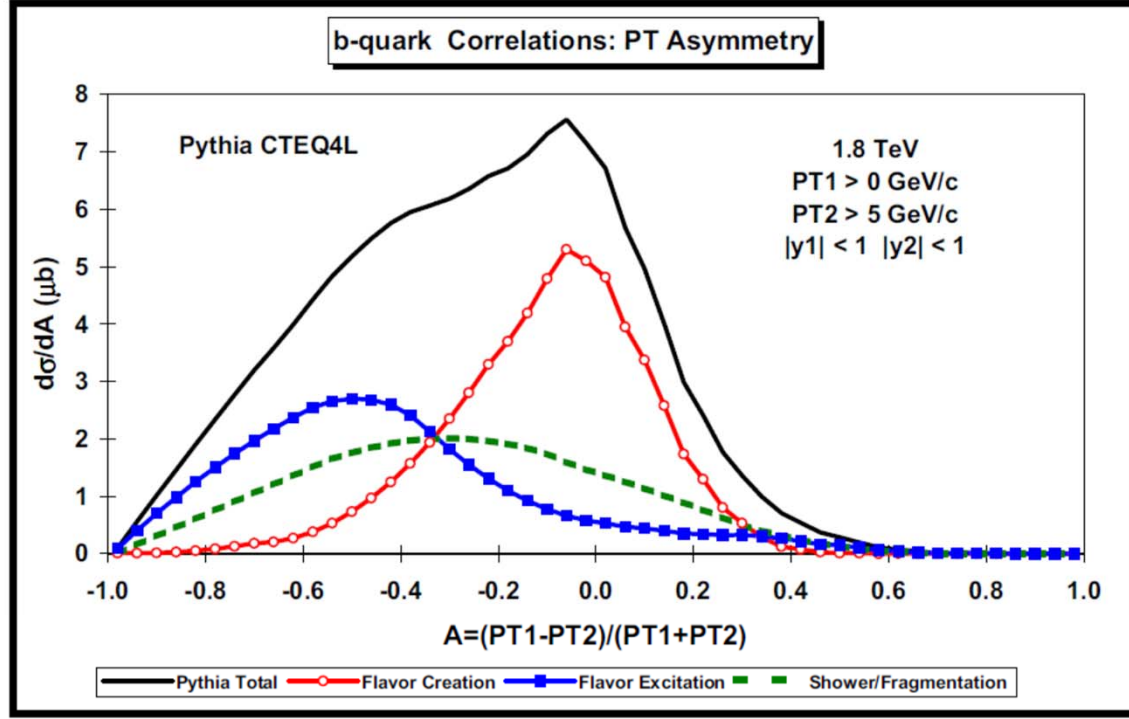


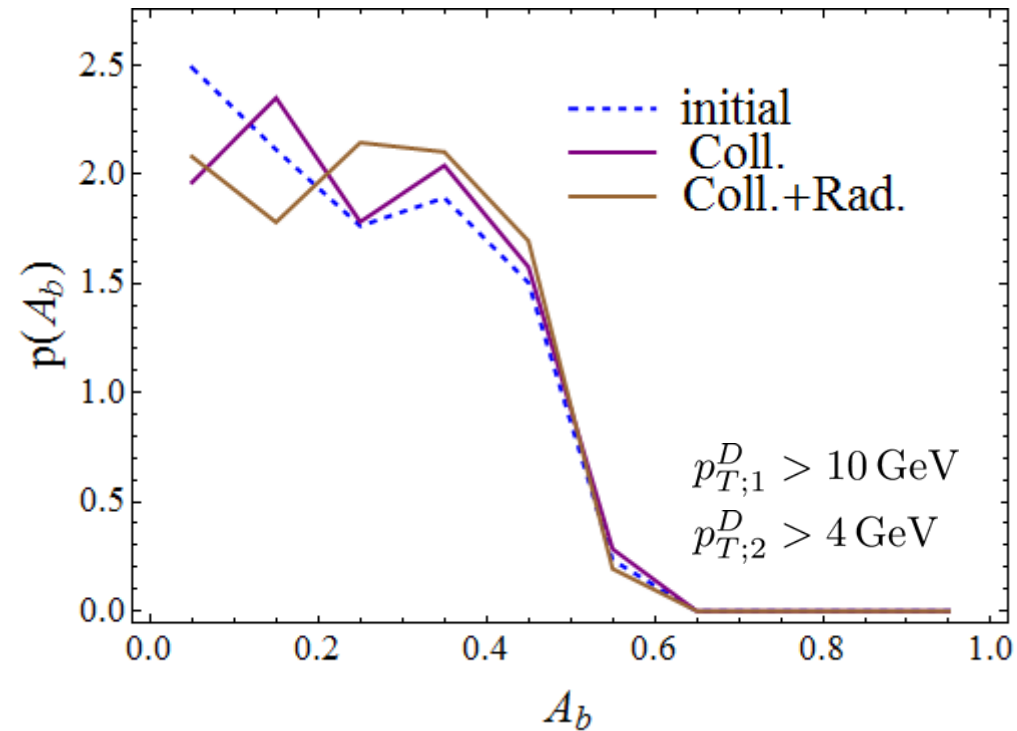
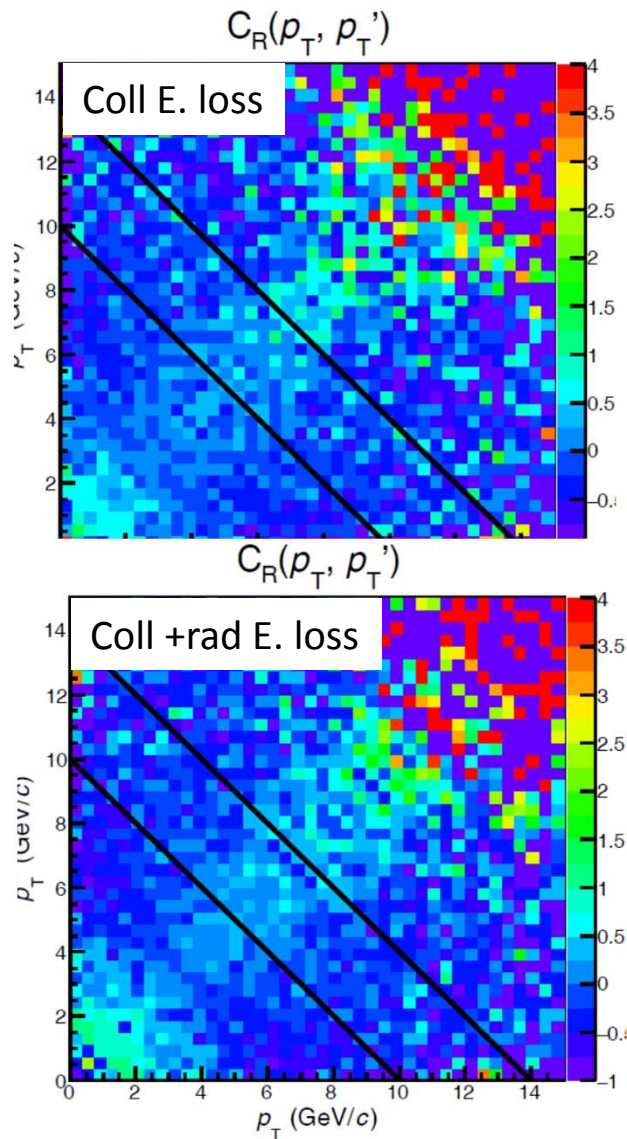
FIG. 18: Prediction of PYTHIA 6.158 (CTEQ4L,  $p_T(\text{hard}) > 0$ ) for the  $p_T$  asymmetry,  $A = (p_{T1} - p_{T2})/(p_{T1} + p_{T2})$ , for events with a  $b$ -quark with  $p_{T1} > 0$  and  $|y_1| < 1.0$  and a  $\bar{b}$ -quark with  $p_{T2} > 5$  GeV/c and  $|y_2| < 1.0$  in proton-antiproton collisions at 1.8 TeV. The curves correspond to  $d\sigma/dA$  ( $\mu\text{b}$ ) for flavor creation (FIG. 1), flavor excitation (FIG. 3), shower/fragmentation (FIG. 4), and the resulting total.

$$\frac{d\sigma}{dA} = \int_{\Sigma} \frac{d\Sigma}{2} \frac{d\sigma}{dp_T dp'_T} \left( p_T = \frac{\Sigma}{2}(1 + A), p'_T = \frac{\Sigma}{2}(1 - A) \right)$$

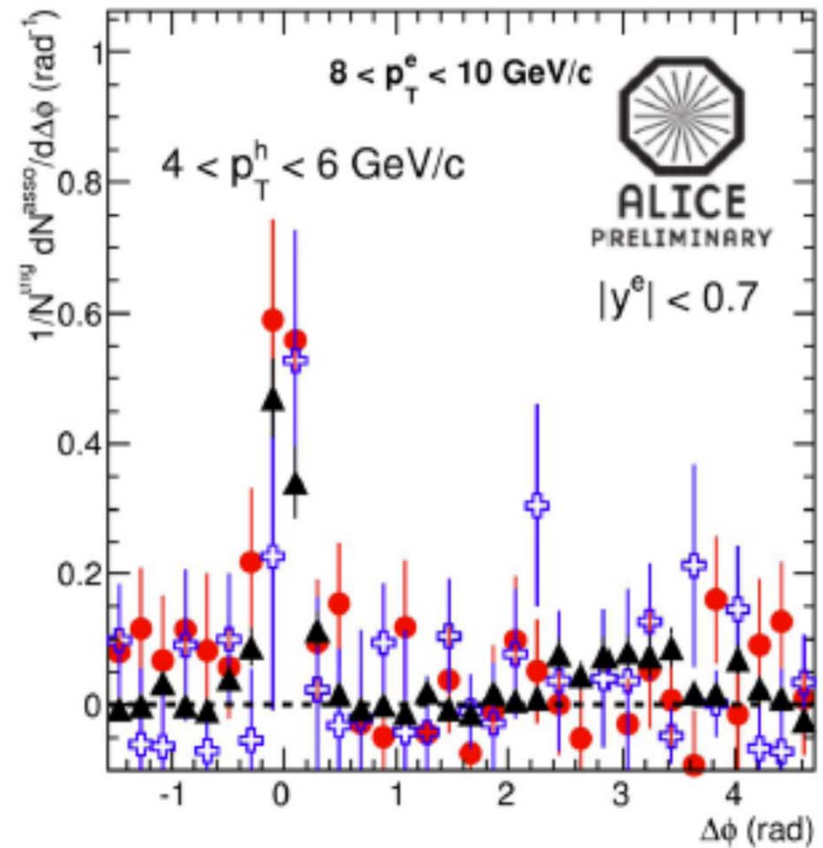
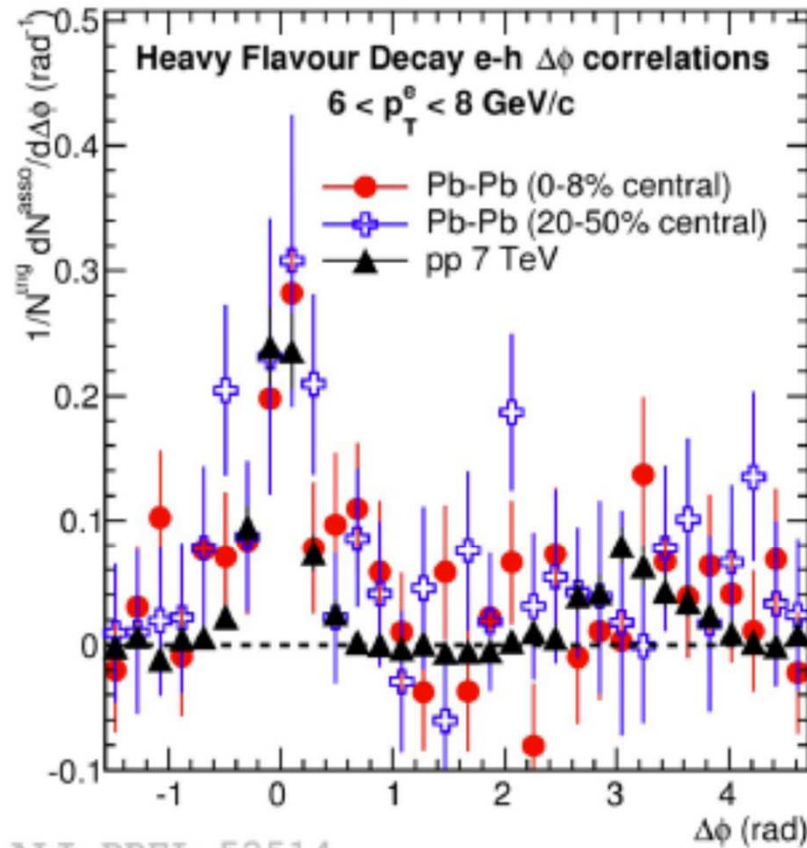
# Momentum imbalance: b-bar in Pb-Pb



Pb-Pb @ 5TeV, 50-70%



# ALICE: e-h correlations in Pb-Pb



## Modified DGLAP (“full”; model D)

« Full » : we combine ingredients from model A and model B:

Both induced radiation, rescattering of partons in the jet and energy loss -> medium

model	Q	$\vec{p}_{\parallel}$	$\vec{p}_{\perp}$	E	
A (radiative/YaJEM-like)	↑	=	=	↑	
B (collisional)	=	↓	↑	↓↑	Most questionable
C (hybrid/no transverse force)	↑	↓	=	↓↑	
D (hybrid/transverse force)	↑	↓	↑	↓↑	Most « realistic »

**Motivation: Looking at various observables for these models may help us to better understand the role of induced energy loss**

**Medium evolution: For the time, we use a toy-model parametrization of the transport coefficient:**

**D & C vs A: role of the Energy transfer -> medium & medium response**

# Further model ingredients

1. Medium evolution: For the time, we use a toy-model parametrization of the transport coefficient:

$$\hat{q}(t) = \frac{a}{(t + b)^c} \quad \text{With } b=1.5 \text{ fm/c, } c=2.2$$

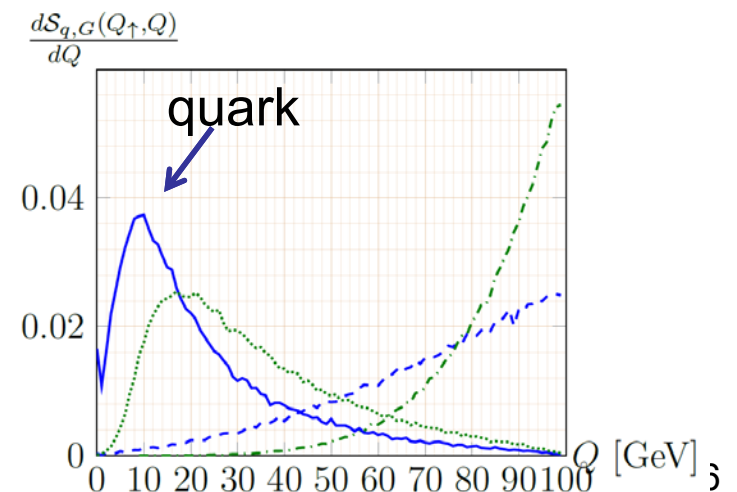
(jet emanating from the center of the medium)

[Th. Renk:  
Phys.Rev.C 78,  
034908 (2008)]

with  $\int_{t_0}^{t_f} \hat{q}(t) dt = \Delta Q^2$  Parameter fixing the jet-medium coupling

2. Evolutions are initiated starting from a HQ with energy  $E_{\text{ini}}$  and a virtuality ranging from  $Q_{\uparrow} = E_{\text{ini}}$  down to  $Q_0 \approx 1 \text{ GeV}$

3. For the following results: no further evolution in the QGP once partons are on-shell





# Double differential angular correlations

