

Adversarial Games for Particle Physics

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Accelerating the Search for Dark Matter with Machine Learning
January 18, 2018



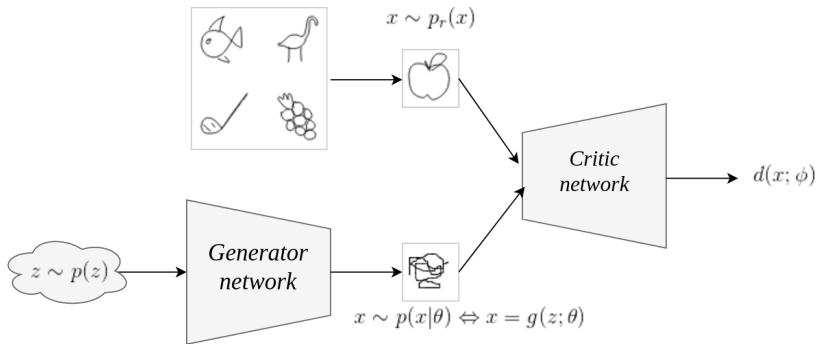
A STEVEN SPIELBERG FILM

catch me

if you can



Generative adversarial networks

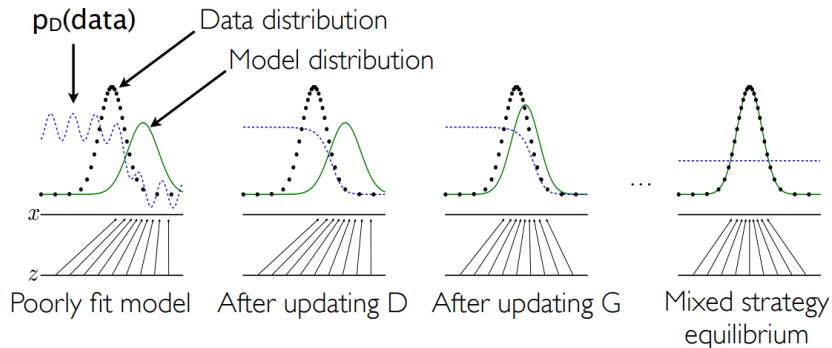


$$\mathcal{L}_d(\phi) = \mathbb{E}_{\mathbf{x} \sim p(\mathbf{x}|\theta)} [d(\mathbf{x}; \phi)] - \mathbb{E}_{\mathbf{x} \sim p_r(\mathbf{x})} [d(\mathbf{x}; \phi)] + \lambda \Omega(\phi)$$

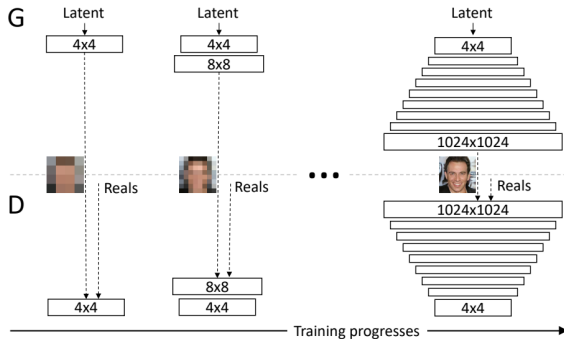
$$\mathcal{L}_g(\theta) = -\mathbb{E}_{\mathbf{x} \sim p(\mathbf{x}|\theta)} [d(\mathbf{x}; \phi)]$$

(Wasserstein GAN + Gradient Penalty)

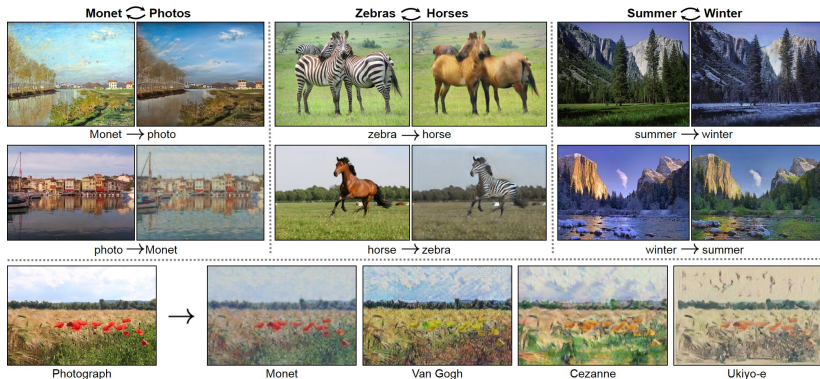
Learning process



State-of-the-art



Style transfer



From **simulated** data to **realistic** data?

Super-resolution

bicubic
(21.59dB/0.6423)



SRResNet
(23.53dB/0.7832)



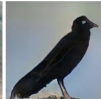
SRGAN
(21.15dB/0.6868)



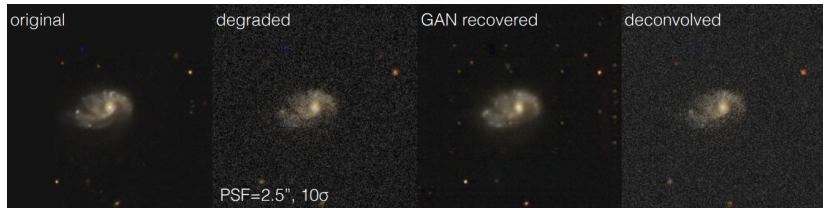
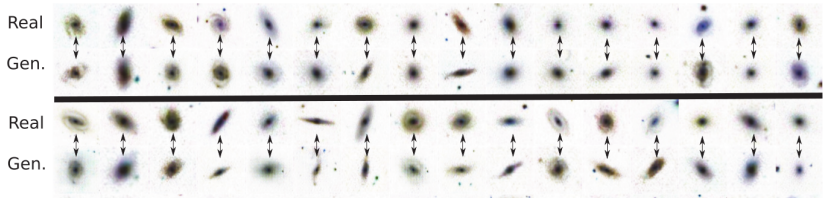
original



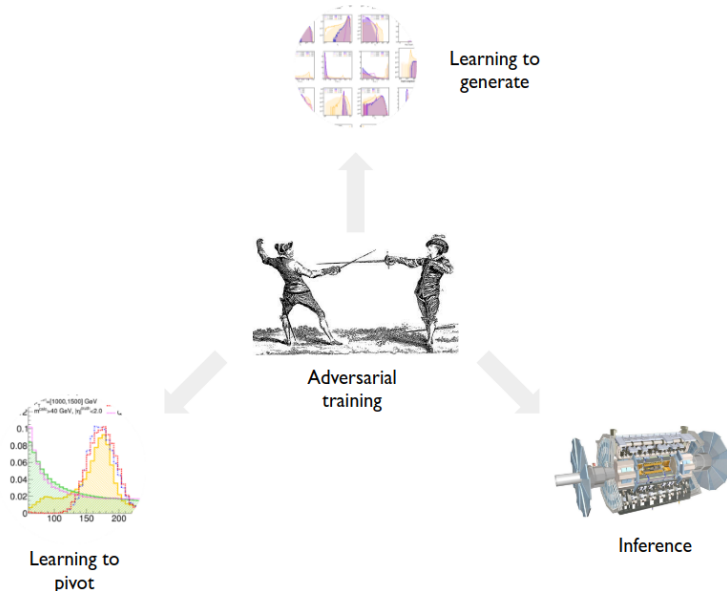
Text-to-image synthesis

Text description	This bird is red and brown in color, with a stubby beak	The bird is short and stubby with yellow on its body	A bird with a medium orange bill white body gray wings and webbed feet	This small black bird has a short, slightly curved bill and long legs	A small bird with varying shades of brown with white under the eyes	A small yellow bird with a black crown and a short black pointed beak	This small bird has a white breast, light grey head, and black wings and tail
64x64 GAN-INT-CLS							
128x128 GAWWN							
256x256 StackGAN							

GANs for galaxies



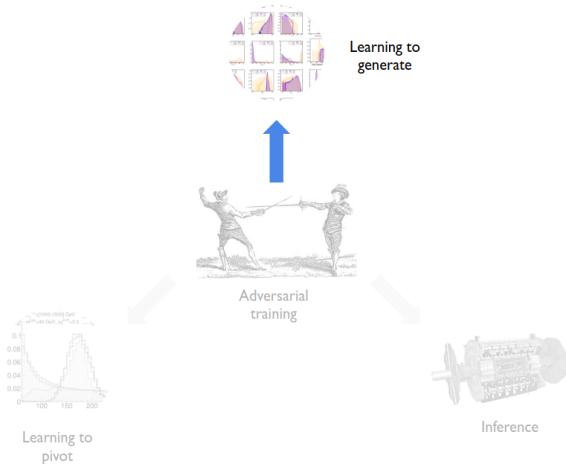
Adversarial games for particle physics

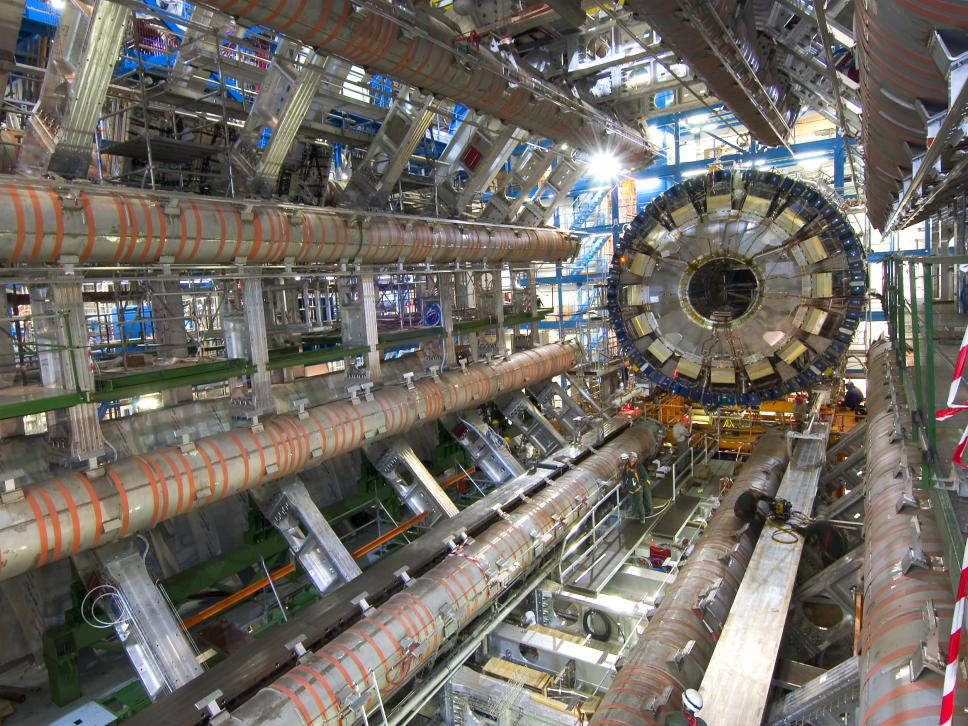


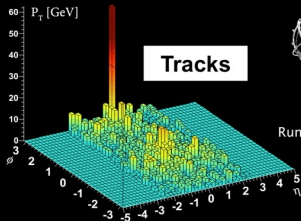
Joint work with



I. Fast simulation



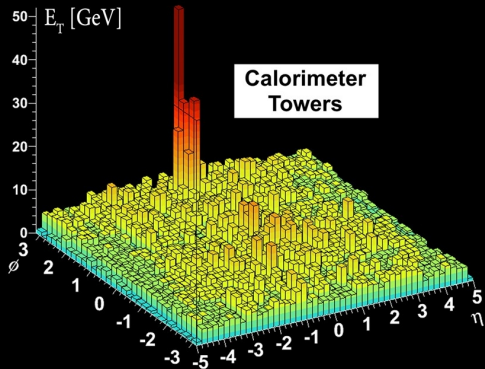
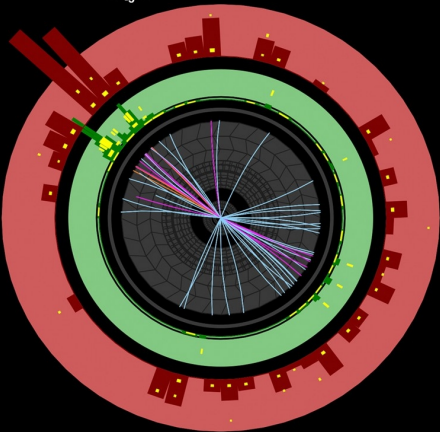
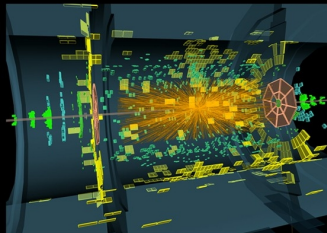




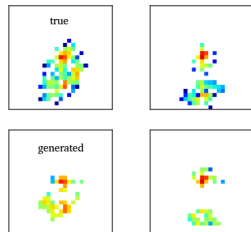
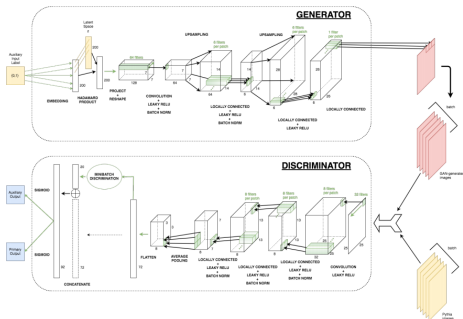
ATLAS EXPERIMENT

Run Number: 169045, Event Number: 1914004

Date: 2010-11-12 04:11:44 CET

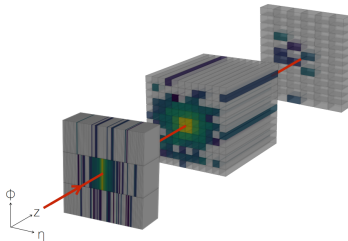


Fast simulation

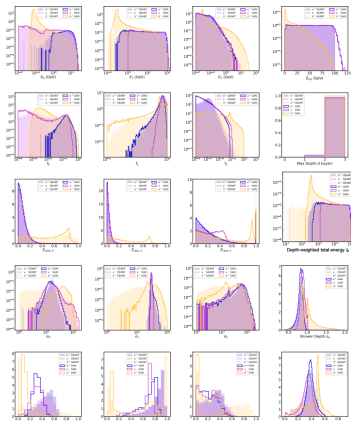


Challenges:

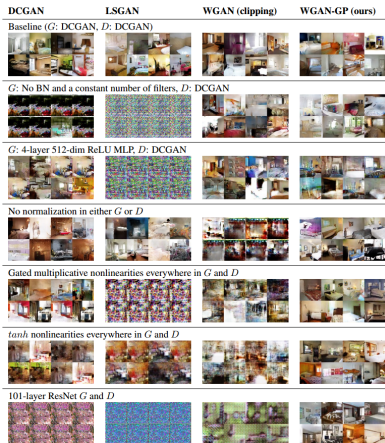
- How to ensure physical properties?
- Non-uniform geometry
- Mostly sparse
- How to scale to full resolution?



Evaluation



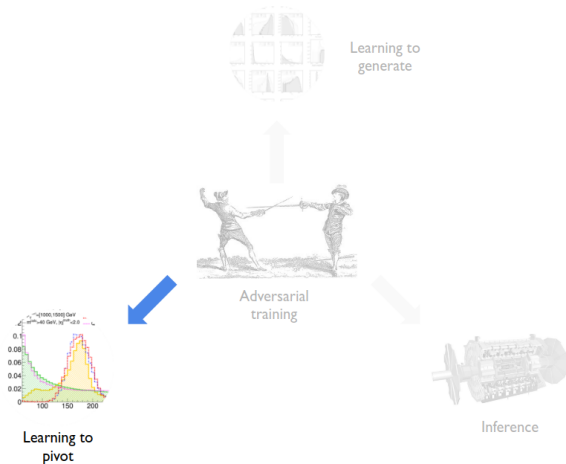
Physics: Evaluate well-known physical variates



ML: Look at generated images

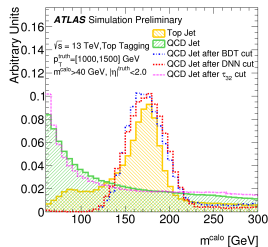
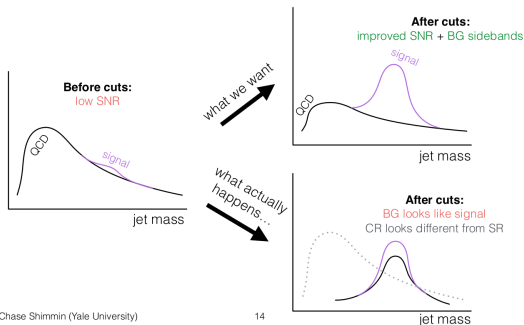
How to be sure the generator is physically correct?

II. Learning to Pivot



Independence from physics variates

- Analysis often rely on the model being **independent from some physics variates** (e.g., mass).
- Correlation leads to systematic uncertainties, that cannot easily be characterized and controlled.



Independence from known unknowns

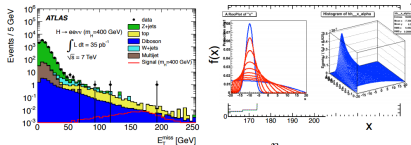
- The generation process is often **not uniquely specified** or known exactly, hence systematic uncertainties.
- Parametrization through **nuisance parameters**.
- Ideally, we would like a classifier that is robust to nuisance parameters.

Incorporating Systematic Effects



Tabulate effect of individual variations of sources of systematic uncertainty

- typically one at a time evaluated at nominal and $\pm 1 \sigma$
- use some form of interpolation to parametrize p^{th} variation in terms of **nuisance parameter** α_p



$$f(\mathcal{D}|\alpha) = \text{Pois}(n|\nu(\alpha)) \prod_{e=1}^n f(x_e|\alpha)$$

Problem statement

- Assume a family of data generation processes $p(X, Y, Z)$ where
 - X are the data (taking values $x \in \mathcal{X}$),
 - Y are the target labels (taking values $y \in \mathcal{Y}$),
 - Z is an auxiliary random variable (taking values $z \in \mathcal{Z}$).
 - Z corresponds to physics variates or nuisance parameters.
- Supervised learning: learn a function $f(\cdot; \theta_f) : \mathcal{X} \mapsto \mathcal{Y}$.
- We want inference based on $f(X; \theta_f)$ to be **robust** to the value $z \in \mathcal{Z}$.
 - E.g., we want a classifier that does not change with systematic variations, even though the data might.

Pivot

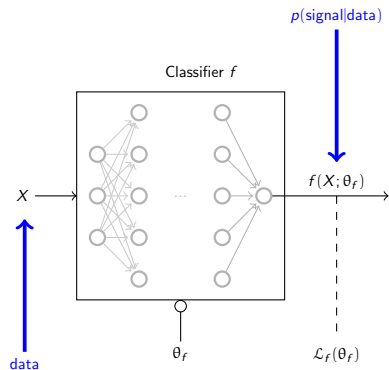
- We define robustness as requiring the distribution of $f(X; \theta_f)$ conditional on Z to be **invariant** with Z . That is, such that

$$p(f(X; \theta_f) = s|z) = p(f(X; \theta_f) = s|z')$$

for all $z, z' \in \mathcal{Z}$ and all values $s \in \mathcal{S}$ of $f(X; \theta_f)$.

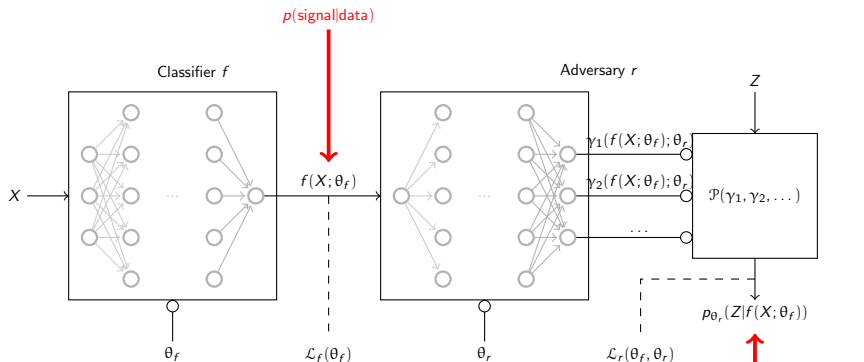
- If f satisfies this criterion, then f is known as a **pivotal quantity**.
- Same as requiring $f(X; \theta_f)$ and Z to be **independent random variables**.

Adversarial game



Consider a classifier f built as usual, minimizing the cross-entropy $\mathcal{L}_f(\theta_f) = \mathbb{E}_{x \sim X} \mathbb{E}_{y \sim Y|x} [-\log p_{\theta_f}(y|x)]$.

Adversarial game

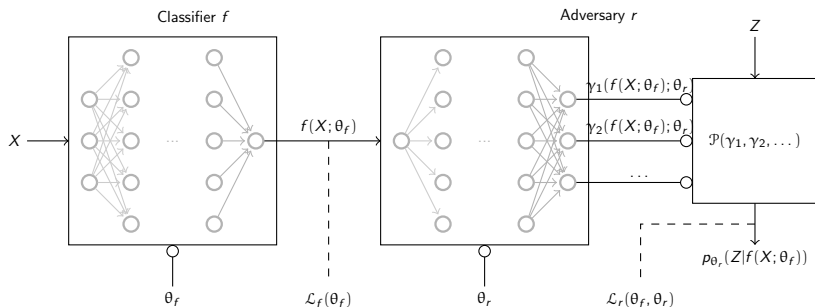


Pit f against an **adversary network** r producing as output the posterior $p_{\theta_r}(z|f(X; \theta_f) = s)$.

Set r to minimize the cross entropy

$$\mathcal{L}_r(\theta_f, \theta_r) = \mathbb{E}_{s \sim f(X; \theta_f)} \mathbb{E}_{z \sim Z|s} [-\log p_{\theta_r}(z|s)].$$

Adversarial game



Goal is to solve: $\hat{\theta}_f, \hat{\theta}_r = \arg \min_{\theta_f} \max_{\theta_r} \mathcal{L}_f(\theta_f) - \mathcal{L}_r(\theta_f, \theta_r)$

Intuitively, r penalizes f for outputs that can be used to infer Z .

In practice

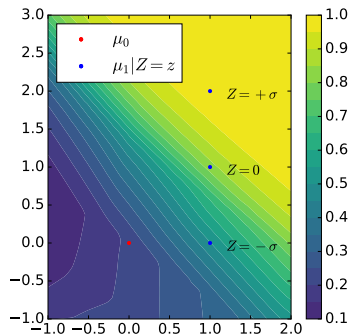
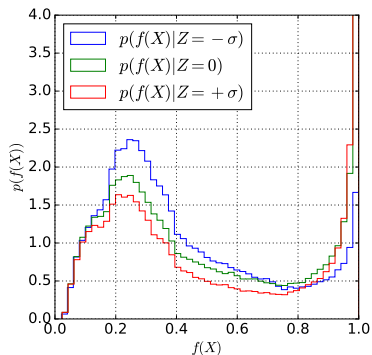
- The assumption of existence of a classifier that is both optimal and pivotal may not hold.
- However, the minimax objective can be rewritten as

$$E_{\lambda}(\theta_f, \theta_r) = \mathcal{L}_f(\theta_f) - \lambda \mathcal{L}_r(\theta_f, \theta_r)$$

where λ controls the trade-off between the performance of f and its independence w.r.t. Z .

- Setting λ to a large value enforces f to be pivotal.
 - Setting λ close to 0 constraints f to be optimal.
- Tuning λ is guided by a higher-level objective (e.g., statistical significance).

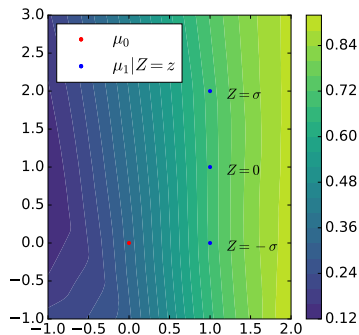
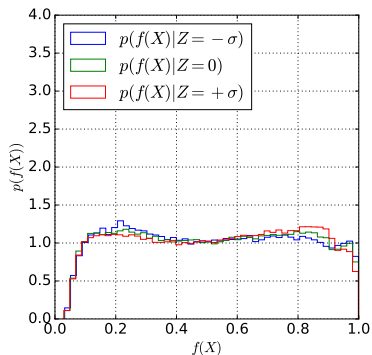
Toy example (without adversarial training)



(Left) The conditional probability distributions of $f(X; \theta_f)|Z = z$ changes with z .

(Right) The decision surface strongly depends on X_2 .

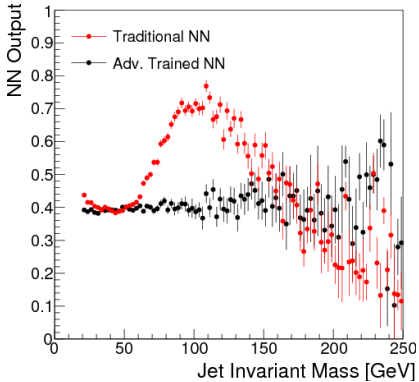
Toy example (with adversarial training)



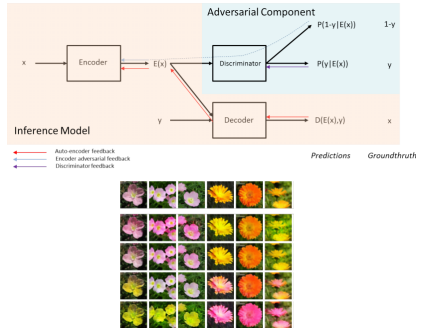
(Left) The conditional probability distributions of $f(X; \theta_f)|Z = z$ are now (almost) invariant with z !

(Right) The decision surface is now independent of X_2 .

Applications

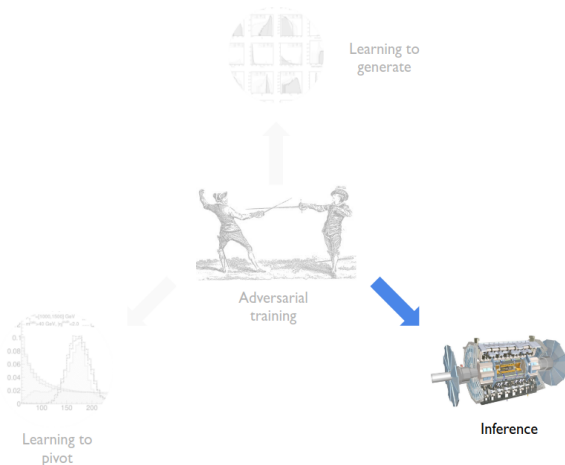


Decorrelated Jet Substructure Tagging using Adversarial Neural Networks

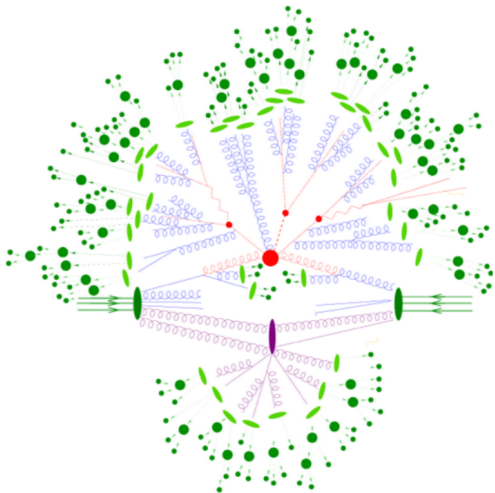


Fader networks

III. Adversarial Variational Optimization



Microscopic picture

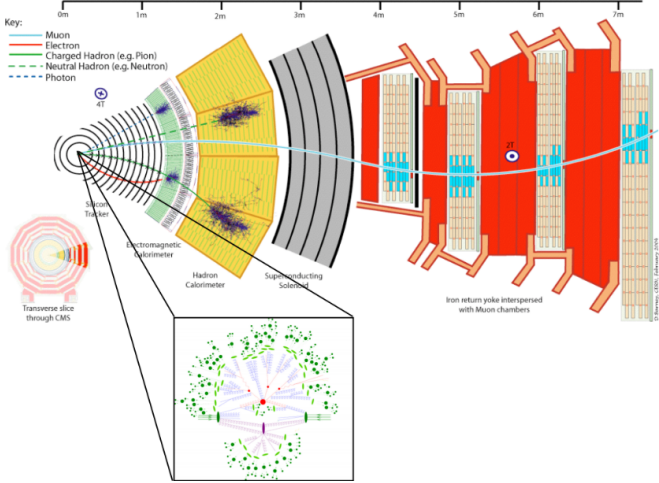


Pencil and paper
calculable from first
principles.

Controlled approximation
of first principles.

Phenomenological model.

Macroscopic picture



Simulate interactions of outgoing particles with the detector.

Likelihood-free assumptions

Operationally,

$$\mathbf{x} \sim p(\mathbf{x}|\boldsymbol{\theta}) \Leftrightarrow \mathbf{z} \sim p(\mathbf{z}|\boldsymbol{\theta}), \mathbf{x} = g(\mathbf{z}; \boldsymbol{\theta})$$

where

- \mathbf{z} provides a source of randomness;
- g is a non-differentiable deterministic function (e.g. a computer program).

Accordingly, the density $p(\mathbf{x}|\boldsymbol{\theta})$ can be written as

$$p(\mathbf{x}|\boldsymbol{\theta}) = \int_{\{\mathbf{z}:g(\mathbf{z};\boldsymbol{\theta})=\mathbf{x}\}} p(\mathbf{z}|\boldsymbol{\theta}) d\mathbf{z}$$

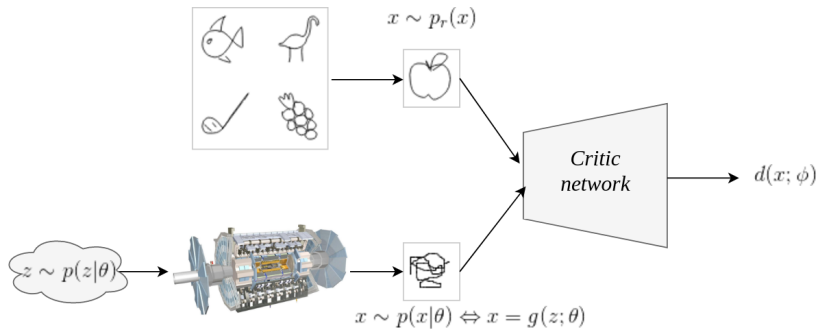
Evaluating the integral is often **intractable**.

Inference

Given observations $\mathbf{x} \sim p_r(\mathbf{x})$, we seek:

$$\boldsymbol{\theta}^* = \arg \min_{\boldsymbol{\theta}} \rho(p_r(\mathbf{x}), p(\mathbf{x}|\boldsymbol{\theta}))$$

Adversarial game

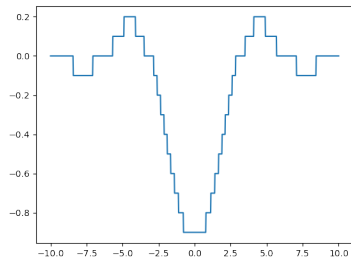


Replace g with an actual scientific simulator!

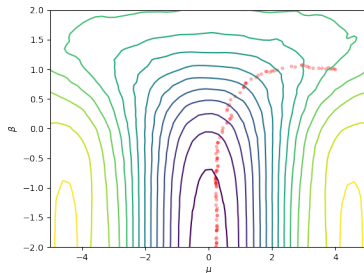
Variational Optimization

$$\min_{\theta} f(\theta) \leq \mathbb{E}_{\theta \sim q(\theta|\psi)} [f(\theta)] = U(\psi)$$

$$\nabla_{\psi} U(\psi) = \mathbb{E}_{\theta \sim q(\theta|\psi)} [f(\theta) \nabla_{\psi} \log q(\theta|\psi)]$$



Piecewise constant $-\frac{\sin(x)}{x}$



$q(\theta|\psi = (\mu, \beta)) = \mathcal{N}(\mu, e^{\beta})$

(Similar to REINFORCE gradient estimates)

Adversarial Variational Optimization

- Replace the generative network with a non-differentiable forward simulator $g(\mathbf{z}; \boldsymbol{\theta})$.
- With VO, optimize upper bounds of the adversarial objectives:

$$U_d = \mathbb{E}_{\boldsymbol{\theta} \sim q(\boldsymbol{\theta}|\boldsymbol{\psi})}[\mathcal{L}_d] \quad (1)$$

$$U_g = \mathbb{E}_{\boldsymbol{\theta} \sim q(\boldsymbol{\theta}|\boldsymbol{\psi})}[\mathcal{L}_g] \quad (2)$$

respectively over ϕ and ψ .

Operationally,

$$\mathbf{x} \sim q(\mathbf{x}|\psi) \Leftrightarrow \boldsymbol{\theta} \sim q(\boldsymbol{\theta}|\psi), \mathbf{z} \sim p(\mathbf{z}|\boldsymbol{\theta}), \mathbf{x} = g(\mathbf{z}; \boldsymbol{\theta})$$

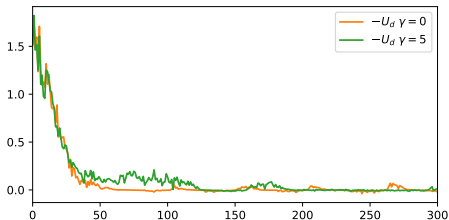
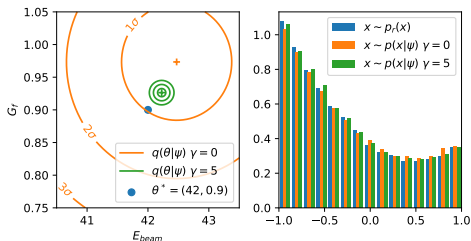
Therefore, $q(\mathbf{x}|\psi)$ is the marginal $\int p(\mathbf{x}|\boldsymbol{\theta})q(\boldsymbol{\theta}|\psi)d\boldsymbol{\theta}$.

- If $p(\mathbf{x}|\boldsymbol{\theta})$ is misspecified, $q(\mathbf{x}|\psi)$ will attempt to smear the simulator to approach $p_r(\mathbf{x})$.
- If not, $q(\mathbf{x}|\psi)$ will concentrate its mass around the true data-generating parameters.
 - Entropic regularization can further be used to enforce that.

Preliminary results

Simplified simulator for electron–positron collisions resulting in muon–antimuon pairs.

- Parameters: E_{beam} , G_f .
- Observations:
 $\mathbf{x} = \cos(A) \in [-1, 1]$,
where A is the polar angle of the outgoing muon wrt incoming electron.



Ongoing work

- Benchmark against alternative methods (e.g., ABC).
- Scale to a full scientific simulator.
- Control variance of the gradient estimates.

Summary



- Adversarial training = indirectly specifying complicated loss functions.
 - For generation
 - For enforcing constraints
- Directly useful in domain sciences, such as particle physics.