

# Theory of Lepton Number and Lepton Flavour Violation

Frank Deppisch

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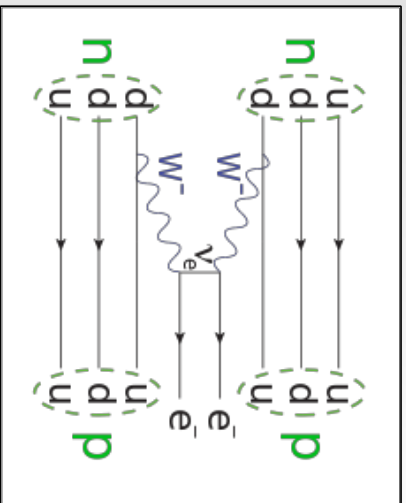
University College London

SHIP Colloquium | CERN | 9 November 2017

# Lepton Flavour versus Lepton Number Violation

Neutrinoless

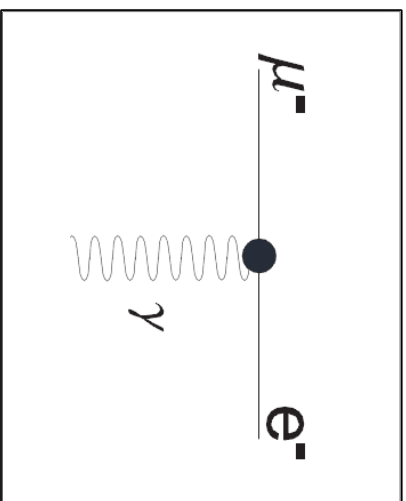
double beta decay



$$\Delta L_e = 2, \Delta L_\mu = 0, \Delta L = 2$$

Lepton Number Violation

$$\mu^- \rightarrow e^- \gamma$$

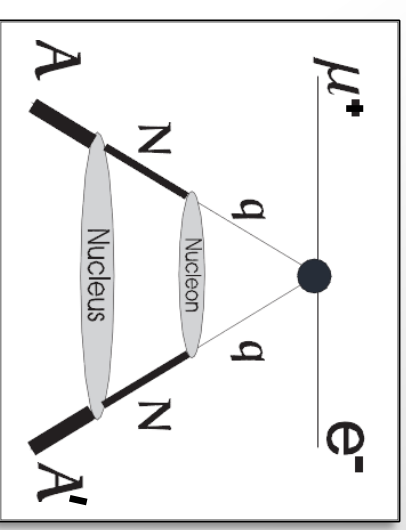


$$\Delta L_e = 1, \Delta L_\mu = -1, \Delta L = 0$$

Lepton Flavour Violation

$$\mu^+ \rightarrow e^-$$

conversion in nuclei



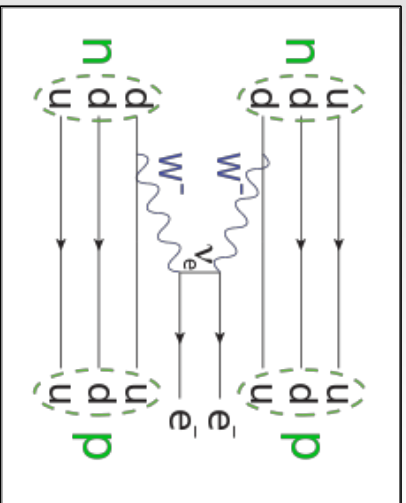
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Lepton Flavour Violation + Lepton Number Violation

# Lepton Flavour versus Lepton Number Violation

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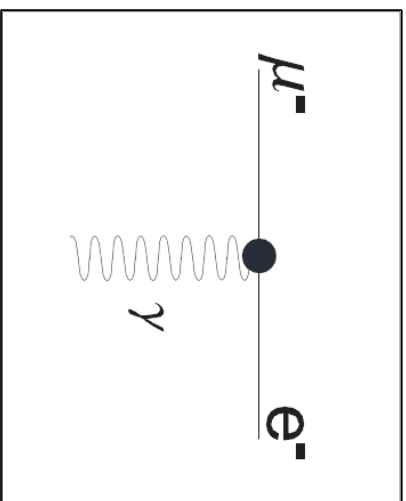
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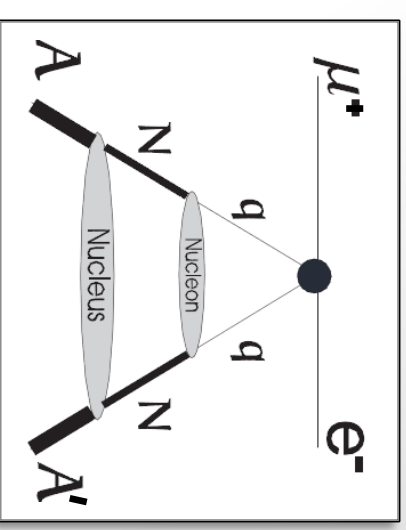


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Lepton Flavour Violation

$$\mu^+ \rightarrow e^-$$

conversion in nuclei



$$\Delta L_e = 1, \Delta L_\mu = 1, \Delta L = 2$$

Lepton Flavour Violation + Lepton Number Violation

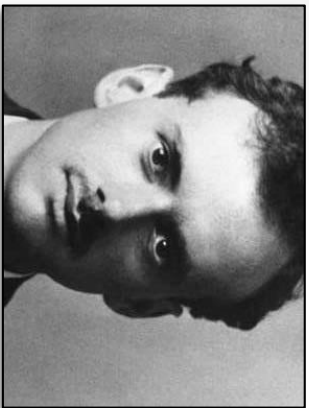


Neutrino Oscillations

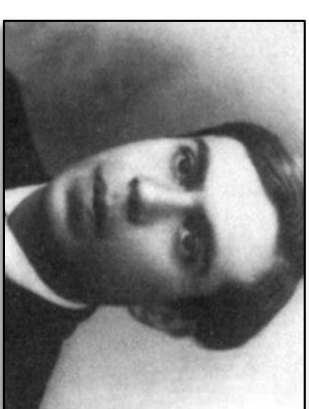
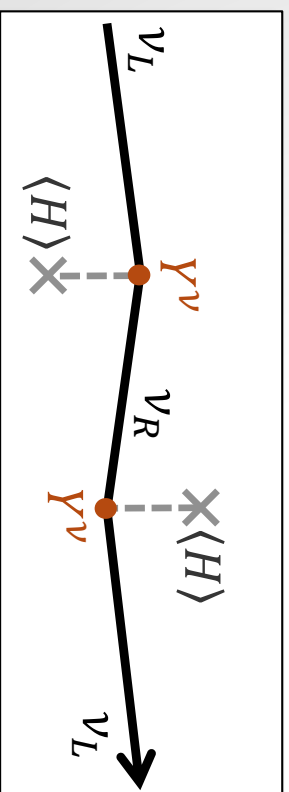
[nobelprize.org](http://nobelprize.org)

# Dirac vs Majorana

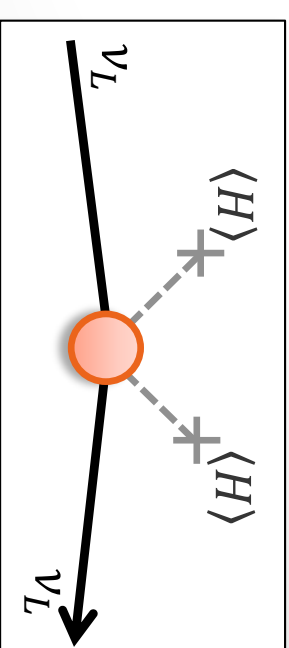
- ▶ Origin of neutrino masses beyond the Standard Model
- ▶ Two possibilities to define neutrino mass



Dirac mass analogous to other fermions but with  $m_\nu / \Lambda_{EW} \approx 10^{-12}$  couplings to Higgs



Majorana mass, using only a left-handed neutrino  
→ Lepton Number Violation



# Neutrino Oscillations

- ▶ Neutrino interaction eigenstates different from mass eigenstates

- Neutrino flavour can change through propagation

$$\nu_i = U_{\alpha i} \nu_\alpha, \quad \nu_i(t) = e^{-i(Et - p \cdot x)} \nu_i(0)$$

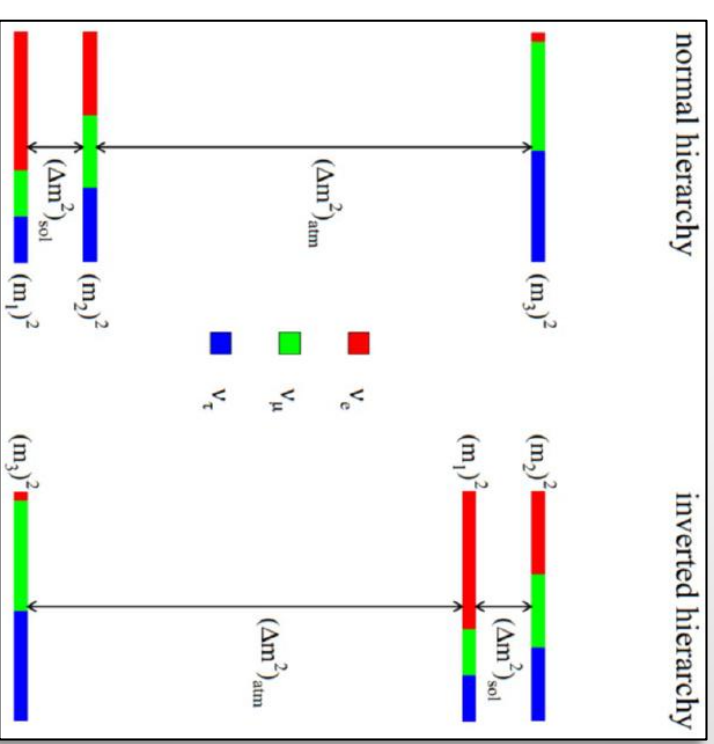
$$\Rightarrow P_{\alpha \rightarrow \beta} = \sin^2 2\theta \sin^2 \left( 1.27 \frac{\Delta m^2 L / \text{km}}{\text{eV}^2 E / \text{GeV}} \right)$$

- ▶ Era of neutrino precision physics

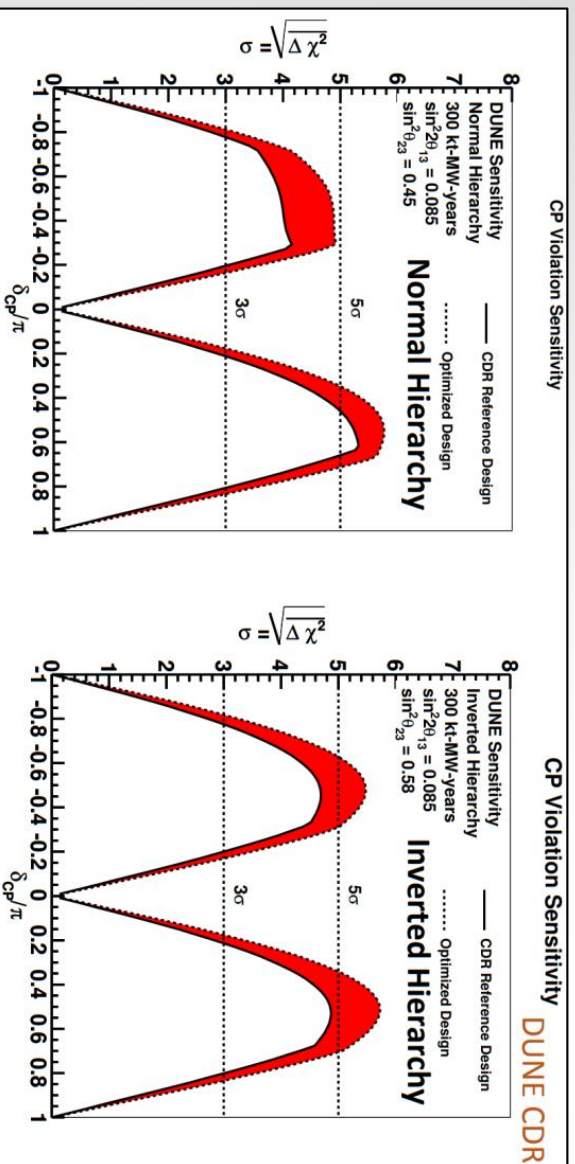
- Current errors  $\sim 1-10\%$

- ▶ Experimental unknowns and anomalies

- CP Violation? Sign of  $\Delta m_{23}$ ? Octant of  $\theta_{23}$ ? Sterile Neutrinos?

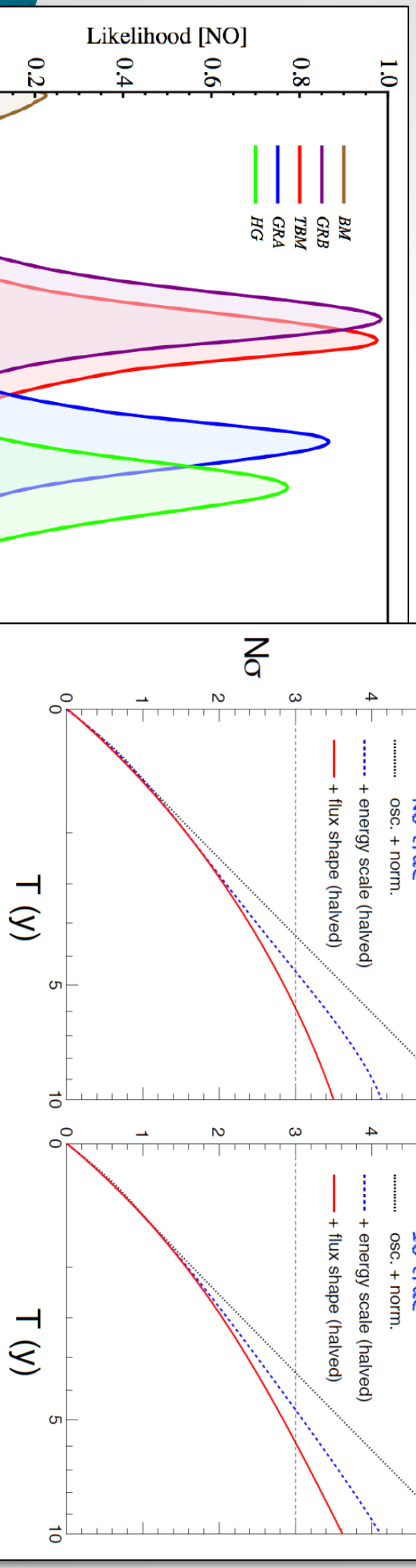


# Neutrino Oscillations



Dune sensitivity to CP violating phase

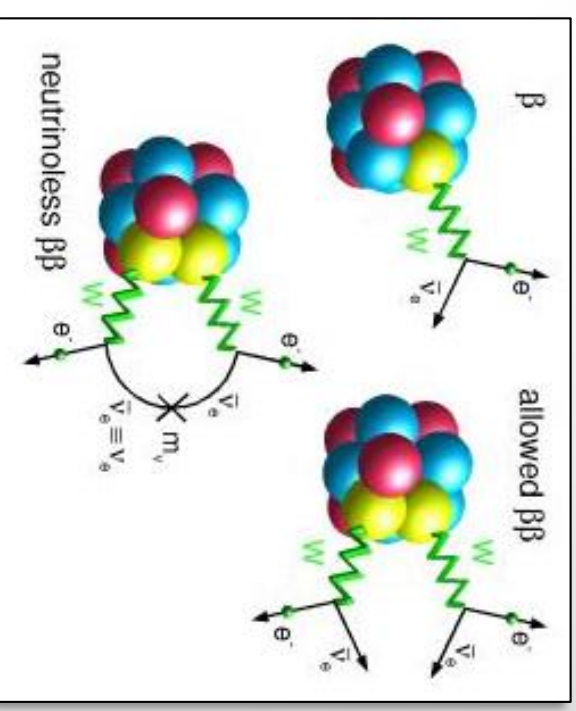
JUNO sensitivity to mass ordering (Marrone et al. '15)



Impact on flavour models (Girardi '14)

# Beta decays

- ▶ Single beta decay  
 $(A, Z) \rightarrow (A, Z + 1) + e^- + \bar{\nu}_e$
- ▶ Allowed double beta ( $2\nu\beta\beta$ ) decay  
 $(A, Z) \rightarrow (A, Z + 2) + 2e^- + 2\bar{\nu}_e$
- ▶ Neutrinoless double beta ( $0\nu\beta\beta$ ) decay  
 $(A, Z) \rightarrow (A, Z + 2) + 2e^-$ 
  - Violation of lepton number
  - Mediated by Majorana neutrinos
  - Variants
    - $0\nu\beta^+\beta^+$ :  $(A, Z) \rightarrow (A, Z - 2) + 2e^+$
    - $0\nu\beta^+\text{EC}$ :  $(A, Z) + e^- \rightarrow (A, Z - 2) + e^+$
    - $0\nu\text{ECEC}$ :  $(A, Z) + 2e^- \rightarrow (A, Z - 2)^*$
- ▶ Majoron-assisted  $0\nu\beta\beta$  decay  
 $(A, Z) \rightarrow (A, Z + 2) + 2e^- + n\chi$

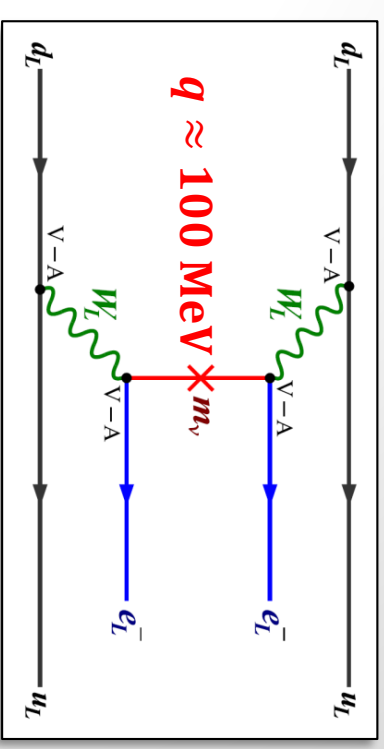


# 0νββ

## ▶ Half-life

$$T_{1/2}^{-1} = |m_{\beta\beta}|^2 G^{0\nu} |M^{0\nu}|^2$$

## ▶ Particle Physics



$$\mathcal{A}_{\mu\nu}^{lep} = \frac{1}{4} \sum_{i=1}^3 U_{ei}^2 \gamma_\mu (1 + \gamma_5) \frac{\not{q} + m_{\nu i}}{q^2 - m_{\nu i}^2} \gamma_\nu (1 - \gamma_5) \approx \frac{\gamma_\mu (1 + \gamma_5) \gamma_\nu}{4q^2} \sum_{i=1}^3 U_{ei}^2 m_{\nu i} \rightarrow m_{\beta\beta}$$

## ▶ Atomic Physics

- Leptonic phase space  $G^{0\nu}$

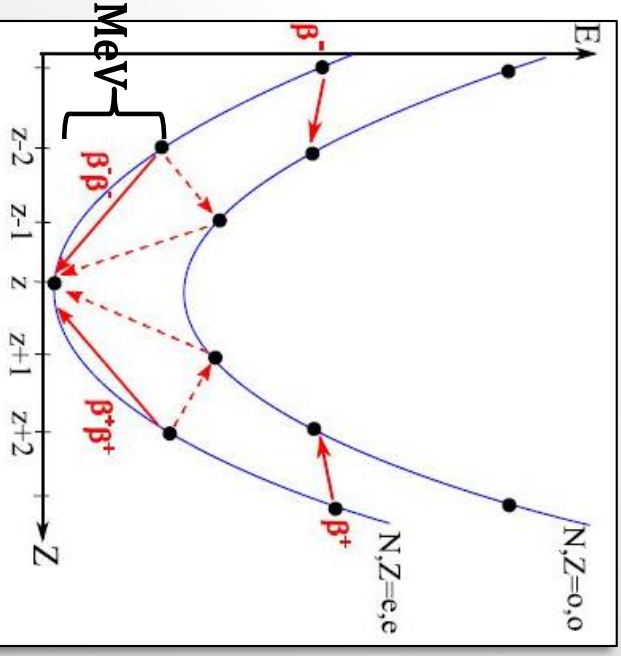
## ▶ Nuclear Physics

- Nuclear transition matrix element  $M^{0\nu}$

$$T_{1/2}^{-1} \propto \frac{|m_{\beta\beta}|^2}{q^4} G_F^4 Q^5$$

$$\frac{10^{25} \text{ yr}}{T_{1/2}} \approx \left( \frac{|m_{\beta\beta}|}{\text{eV}} \right)^2$$

$$Q \approx 2-4 \text{ MeV}$$





# 0νββ

- ▶ Half-life

$$T_{1/2}^{-1} = |m_{\beta\beta}|^2$$

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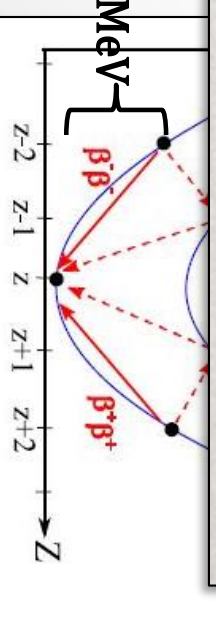
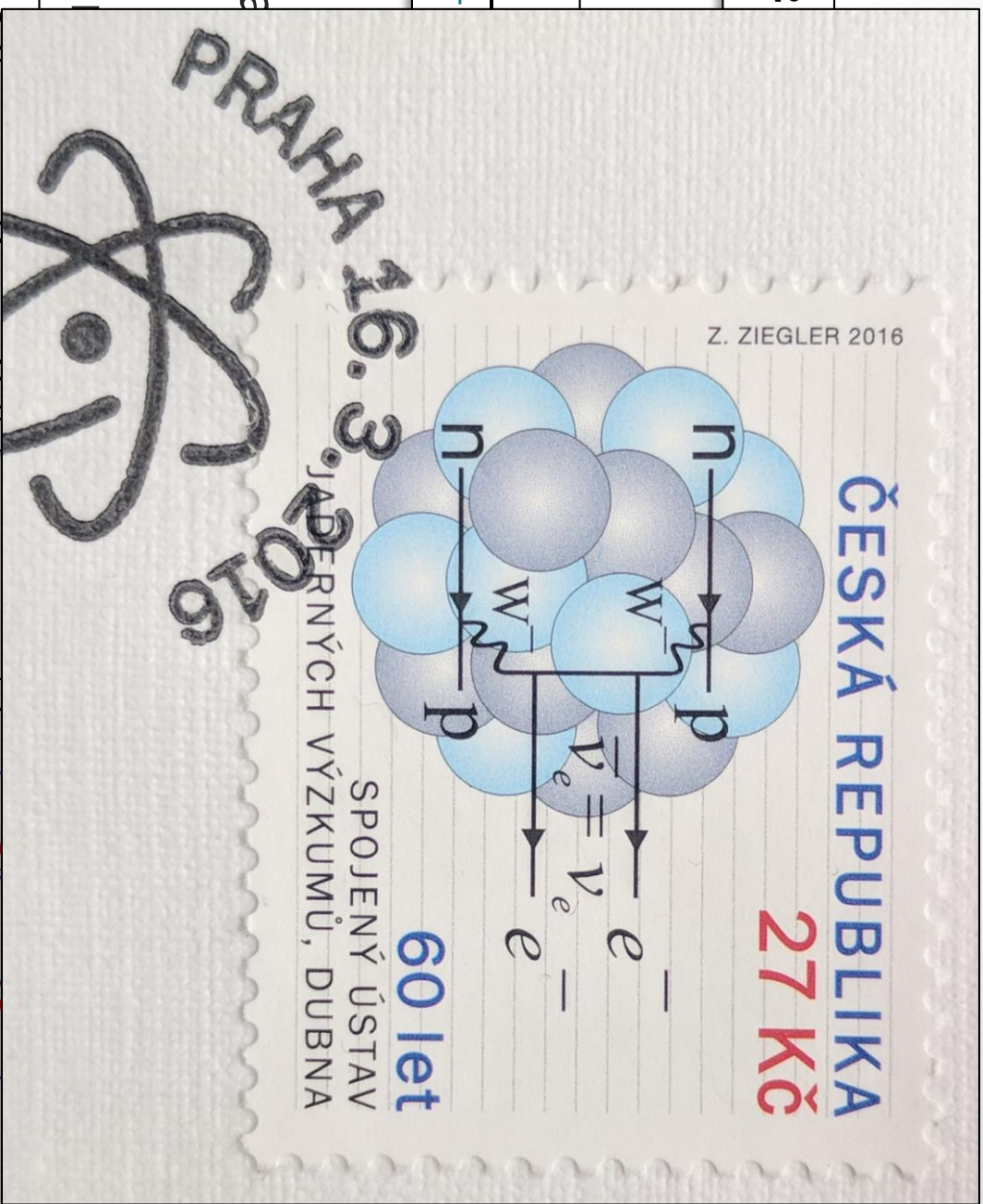
$$\mathcal{A}_{\mu\nu}^{lep} = \frac{1}{4} \sum_{l=1}^3 U_{ei}^2 \gamma_{\mu} (1 + \gamma_5) \frac{\not{q} + \not{p}_l}{q^2 - m_l^2}$$

- ▶ Atomic Physics
  - Leptonic phase space
- ▶ Nuclear Physics
  - Nuclear transition

$$T_{1/2}^{-1} \propto \frac{|m_{\beta\beta}|^2}{q^4} G_F^4 Q^5$$

$$\frac{10^{25} \text{ yr}}{T_{1/2}} \approx \left( \frac{|m_{\beta\beta}|}{\text{eV}} \right)^2$$

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# $0\nu\beta\beta$ - Light Neutrinos

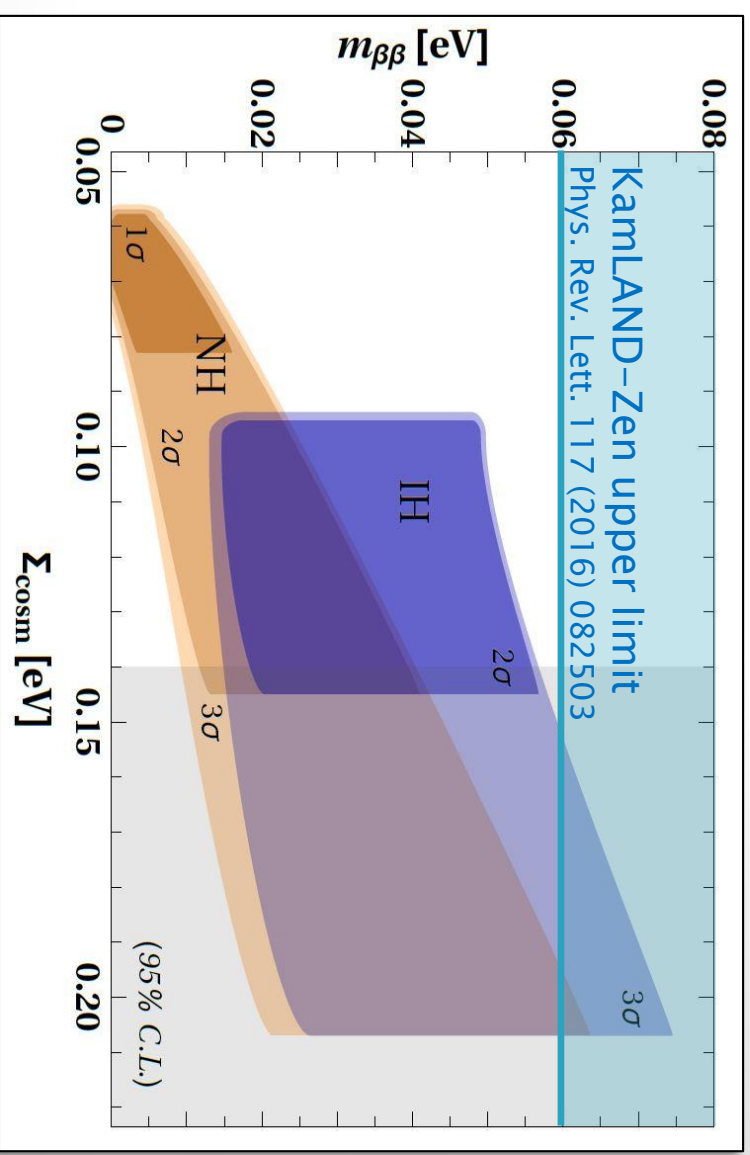
- ▶ Effective  $0\nu\beta\beta$  Mass

$$m_{\beta\beta} = c_{12}^2 c_{13}^2 m_{\nu_1} + s_{12}^2 c_{13}^2 m_{\nu_2} e^{i\phi_{12}} + s_{13}^2 m_{\nu_3} e^{i\phi_{13}}$$

- ▶ Degenerate Regime

$$|m_{\beta\beta}| = m_\nu \sqrt{1 - \sin^2(2\theta_{12})} \sin^2\left(\frac{\phi_{12}}{2}\right)$$

- ▶ Uncertainty from unknown Majorana phases
- ▶ Accidental cancellation for NH possible



# $0\nu\beta\beta$ - Light Neutrinos

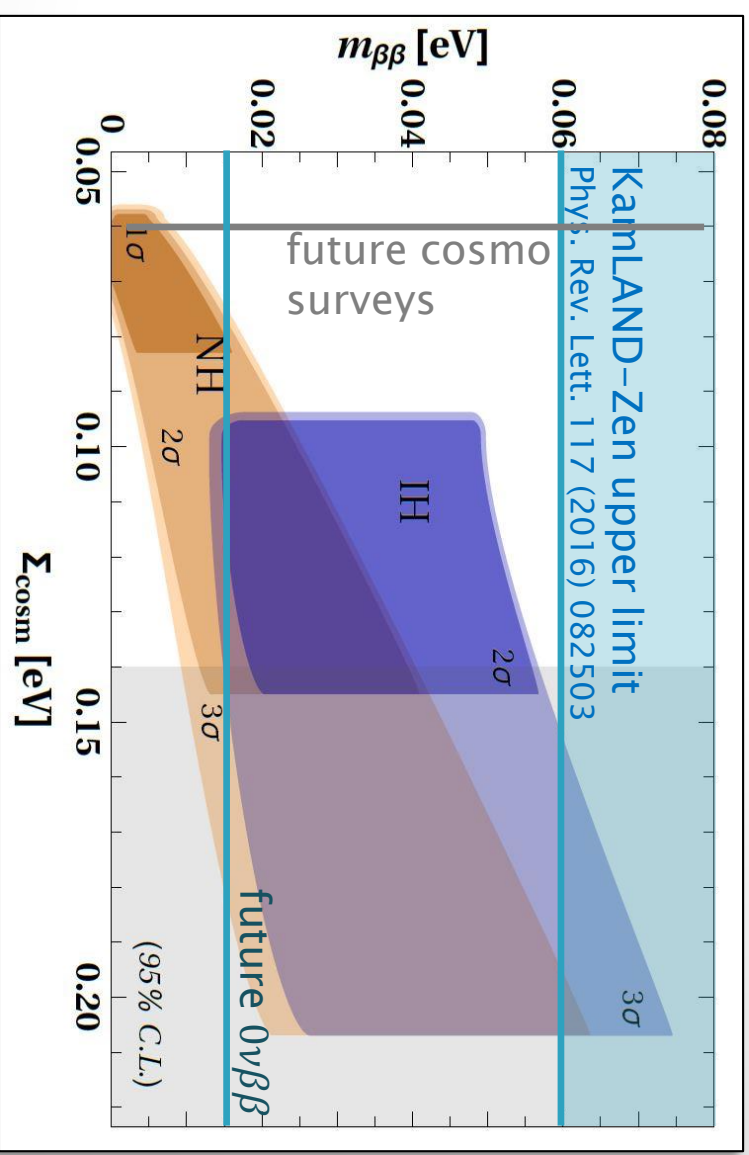
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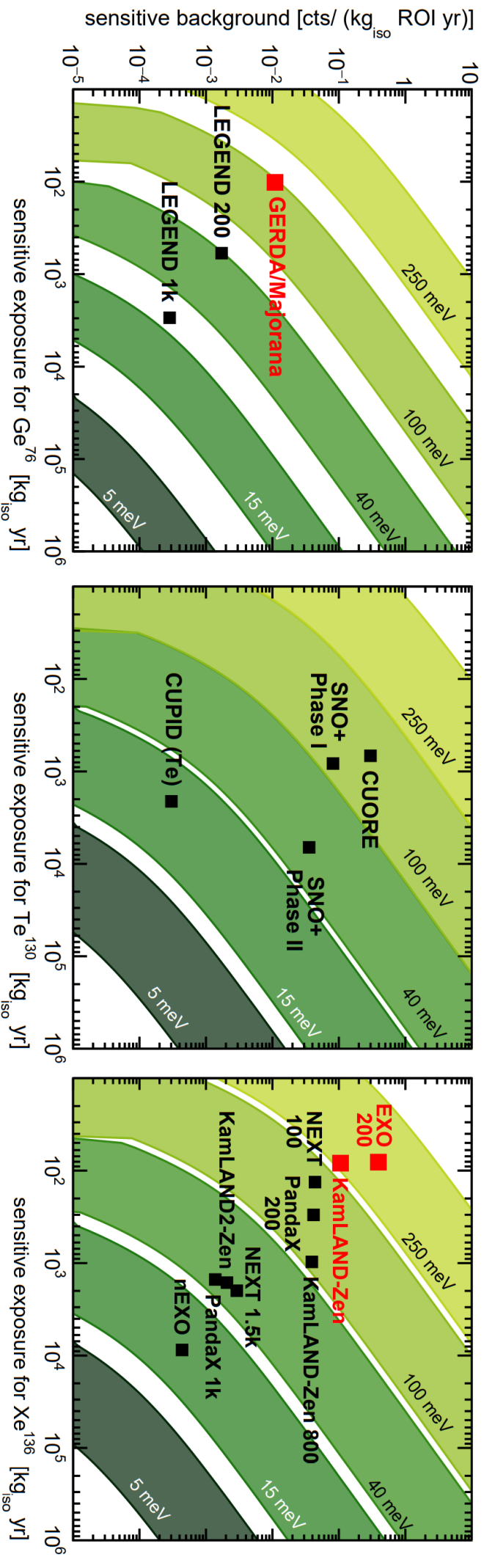
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Dell'Oro, Marcocci, Viel, Vissani,  
Adv. High Energy Phys. (2016) 2162659

# $0\nu\beta\beta$ - Light Neutrinos

## Experimental Sensitivity



Agostini, Benato, Detwiler  
arXiv: 1705.02996

# Nuclear Matrix Elements



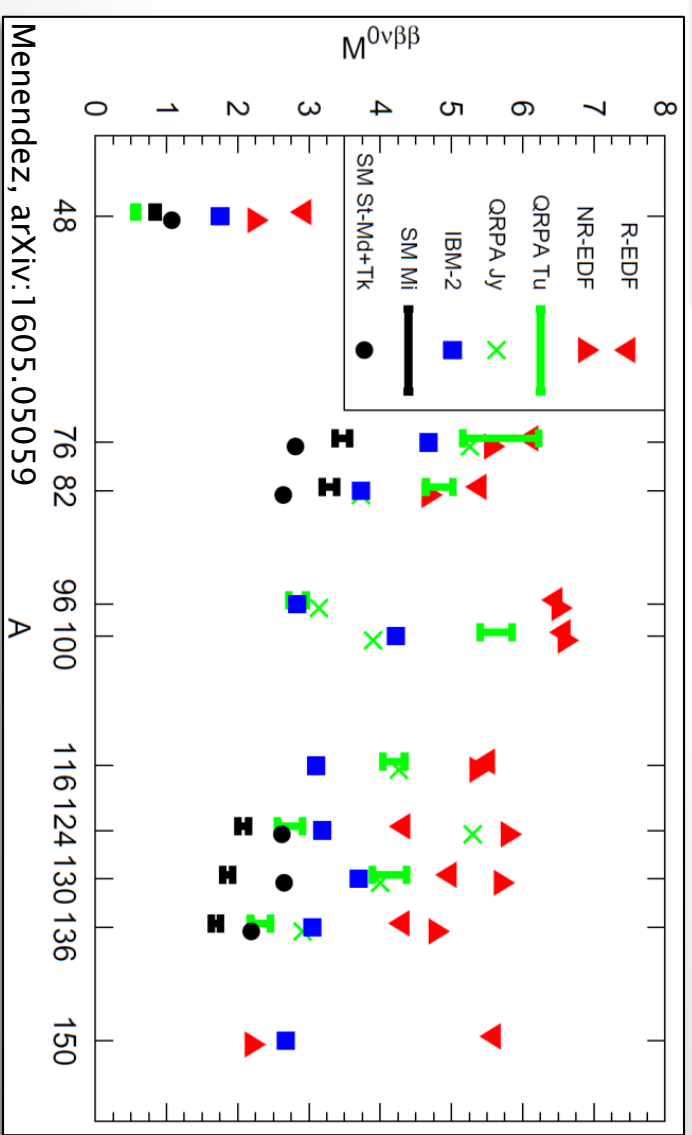
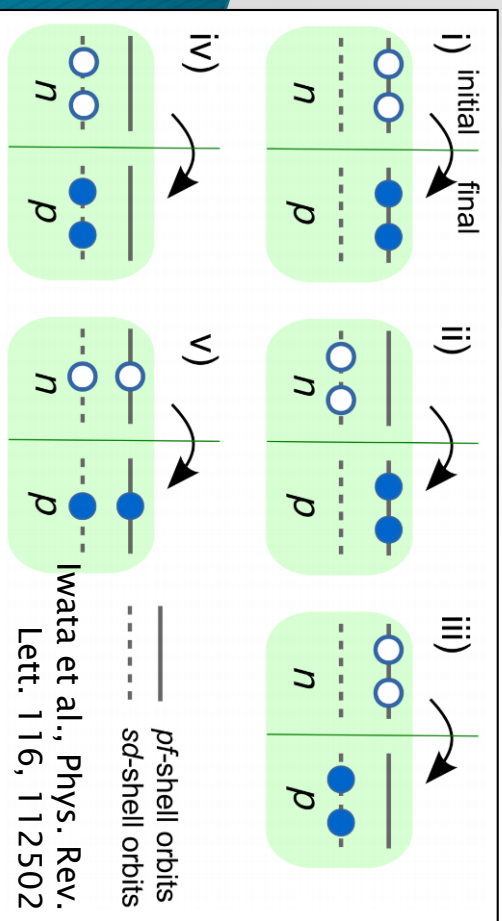
- ▶ Hadronic current

$$J^\mu(q) = g_V \gamma^\mu - g_A \gamma^\mu \gamma^5 + \frac{ig_M}{2m_N} \sigma^{\mu\nu} q_\nu - g_P \gamma^5 q_\mu$$

- ▶ Nuclear Matrix Element  $M^{0\nu}$

$$M^{0\nu} = g_A^2 \left( M_{GT} - \frac{g_V^2}{g_A^2} M_F + M_T \right)$$

- Many-body problem
- Factor 2 - 3 uncertainty between nuclear models



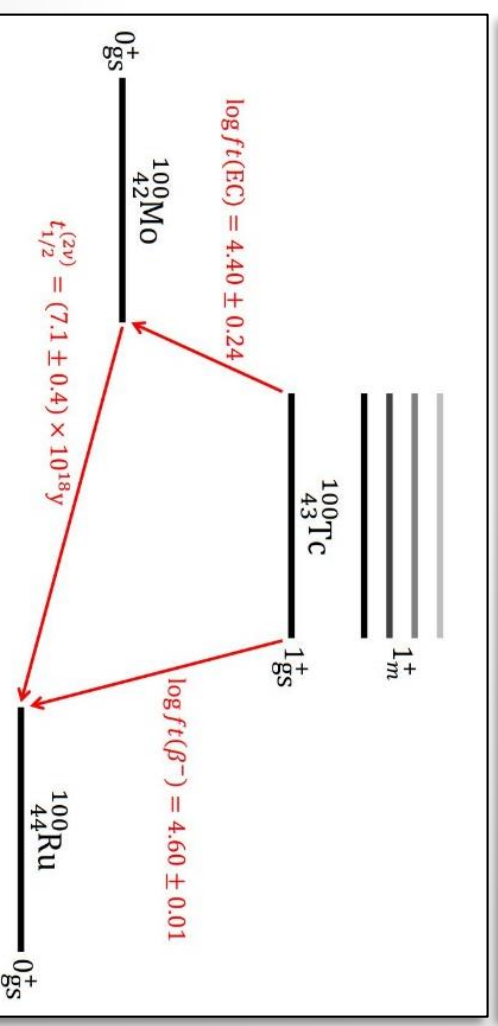
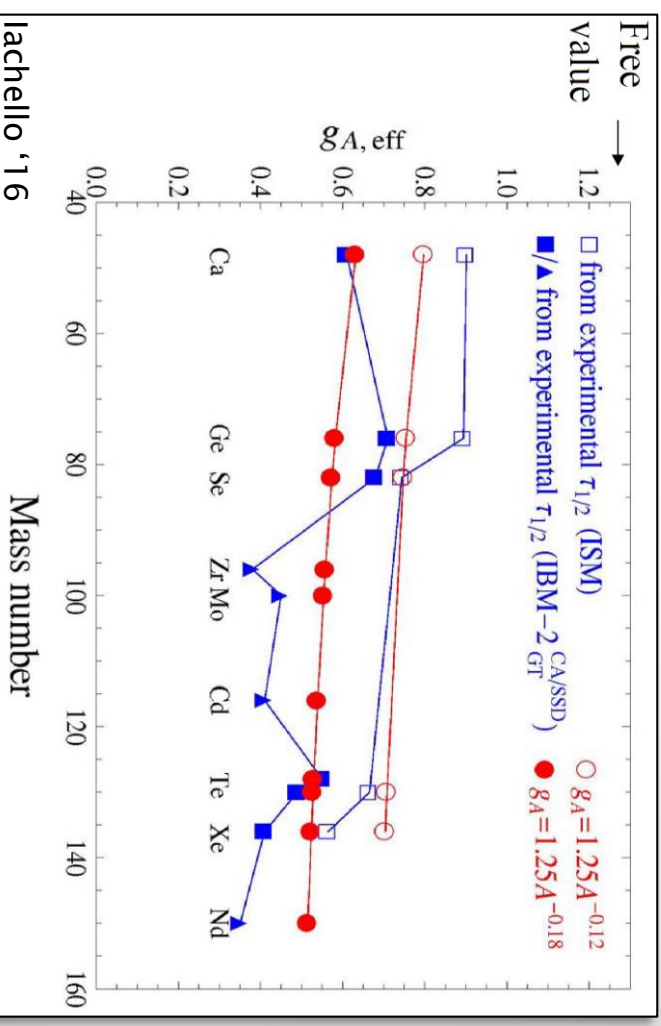
# Quenching of $g_A$ ?

## ▶ Nuclear matrix element

$$M^{0\nu} = g_A^2 \left( M_{GT} - \frac{g_V^2}{g_A^2} M_F + M_T \right)$$

## ▶ Axial-vector coupling $g_A$

- Free nucleon:  $g_A \approx 1.27$
- Comparison of single  $\beta$  and  $2\nu\beta\beta$  decay with theory:  $g_A \approx 0.6-0.8$
- If applicable to  $0\nu\beta\beta$ , reduction of sensitivity
- Genuine effect or short-coming of models?



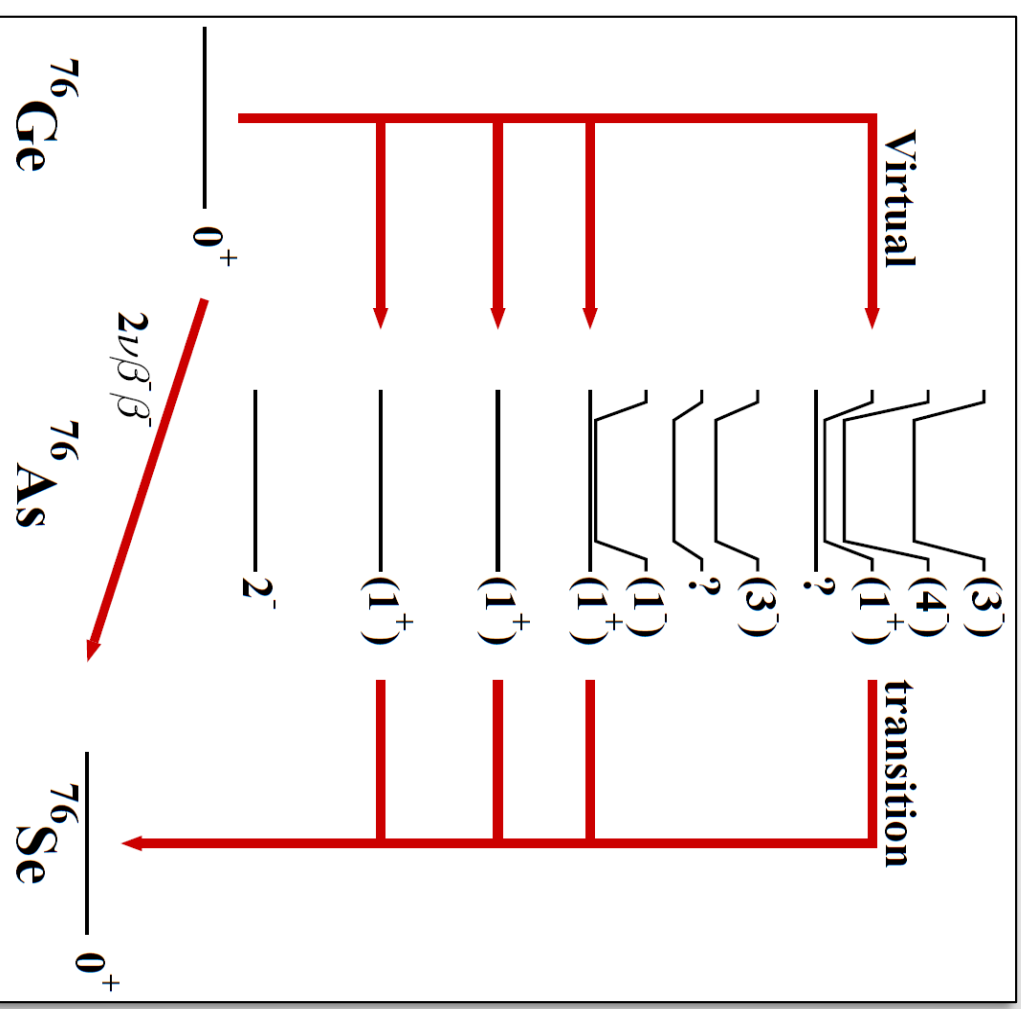
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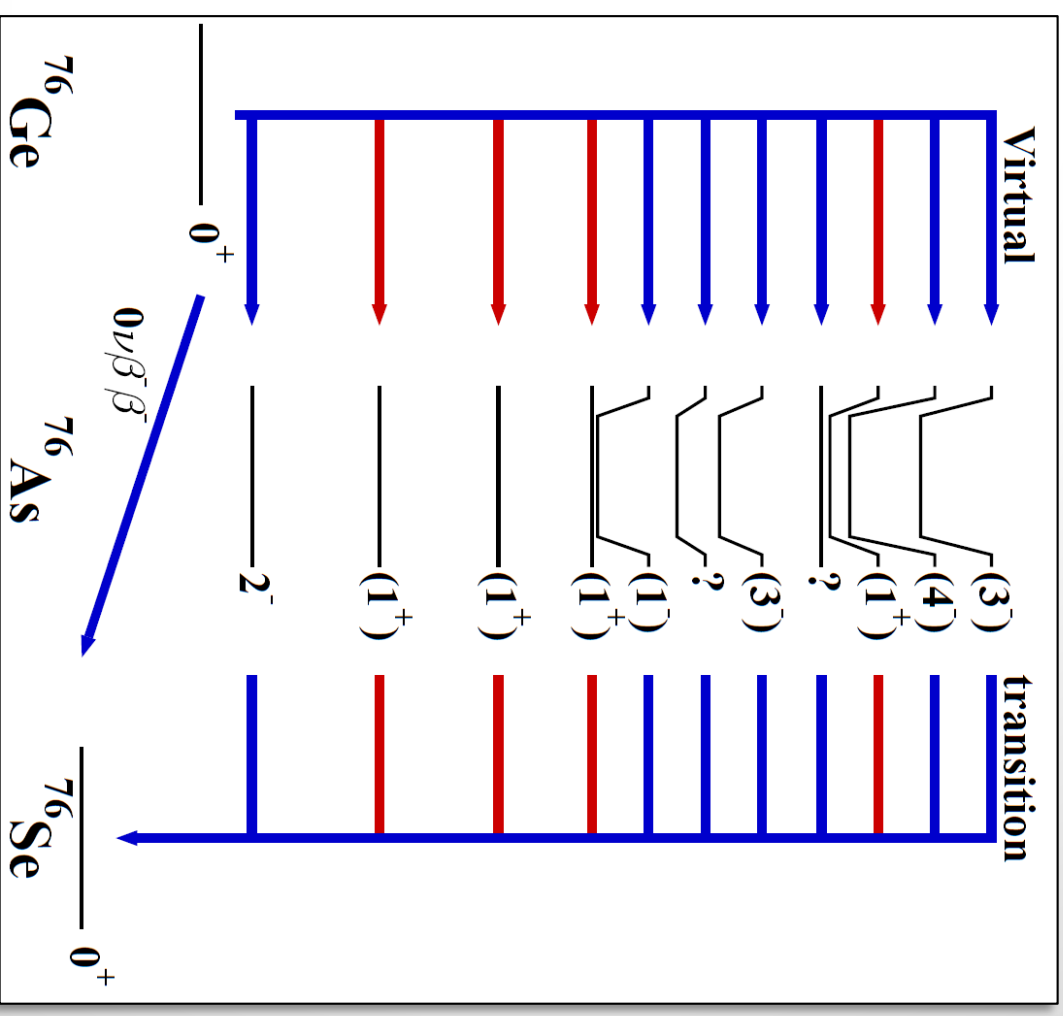
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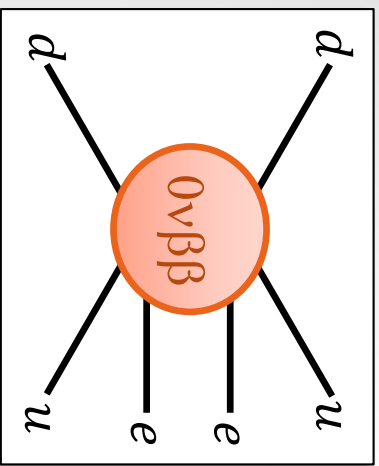
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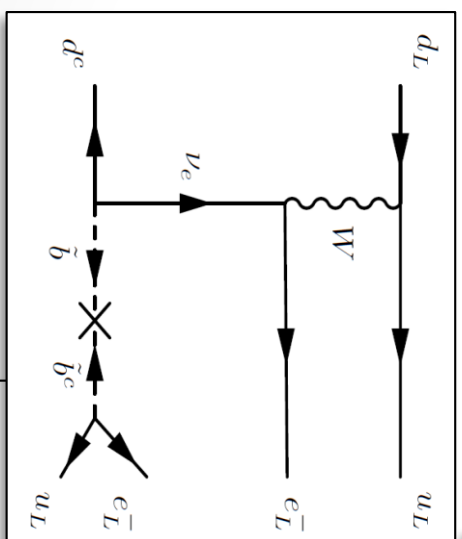
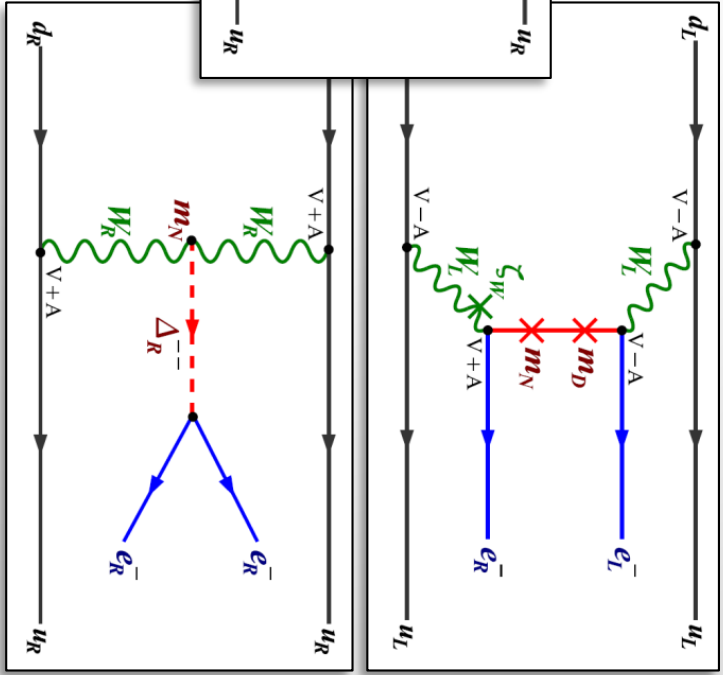
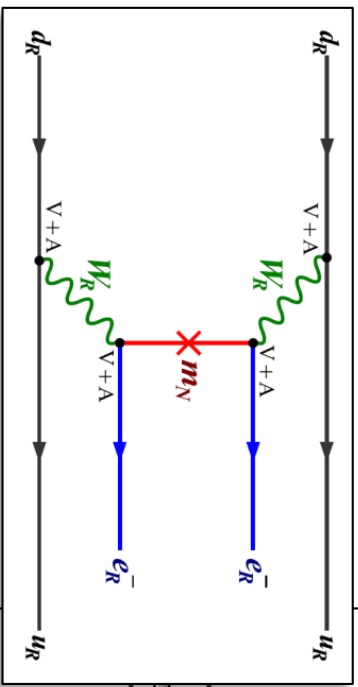


# New Physics and $0\nu\beta\beta$

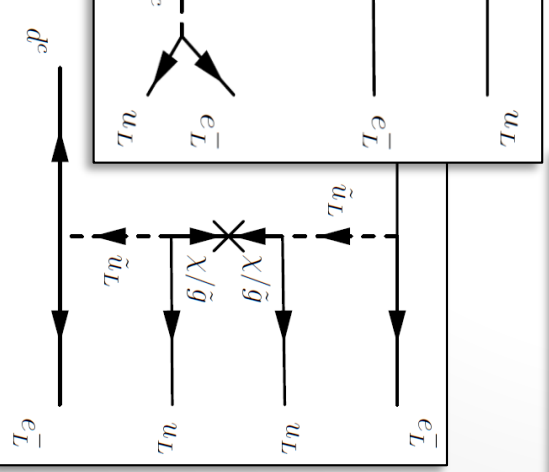
- ▶ Plethora of New Physics scenarios



$$T_{1/2}^{-1} = \epsilon_{NP}^2 G_{NP}^{0\nu} |M_{NP}^{0\nu}|^2$$



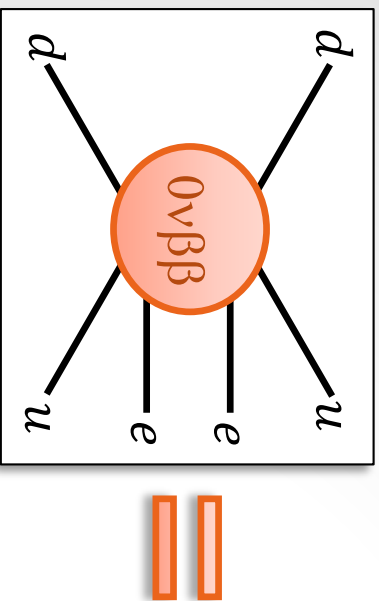
R-Parity Violating SUSY



- Extra Dimensions
- Majorons
- Leptoquarks
- ...

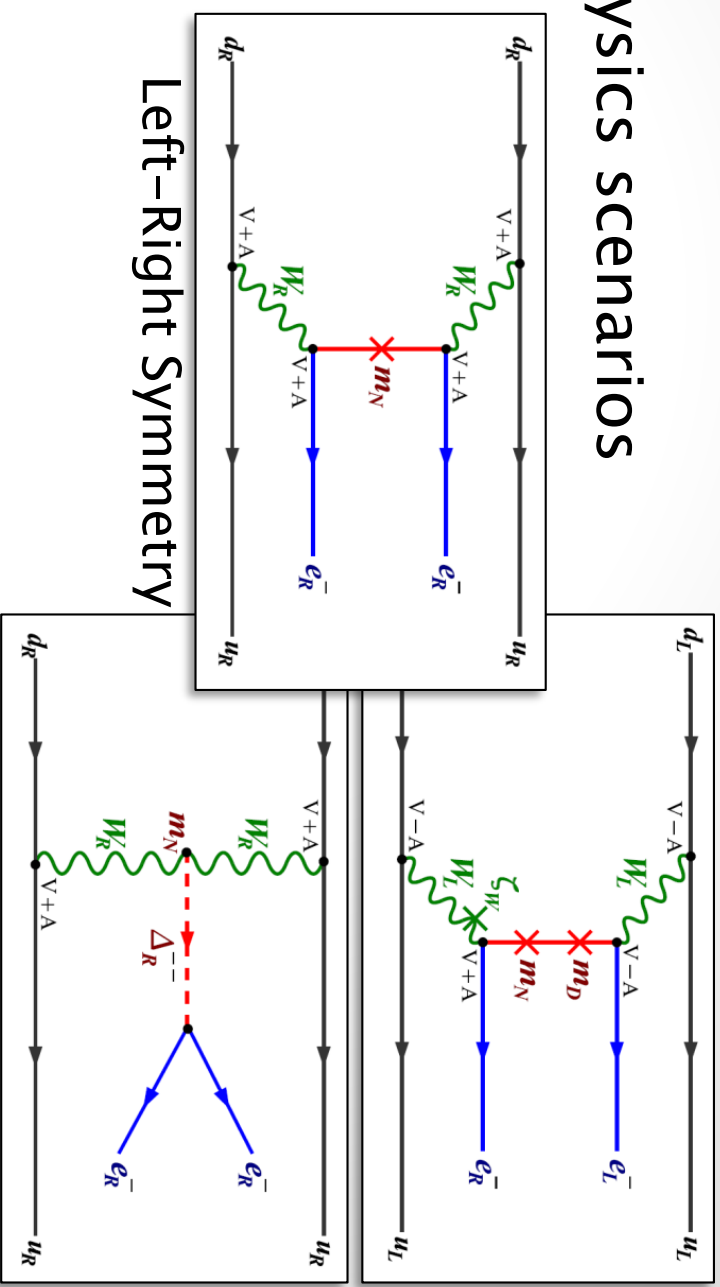
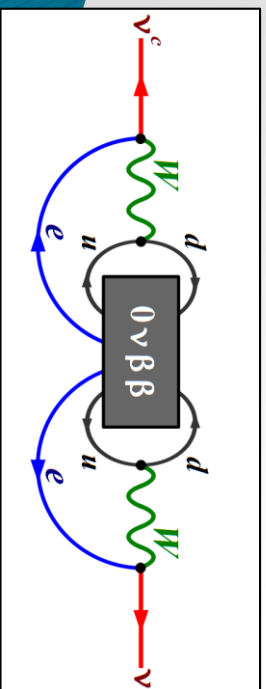
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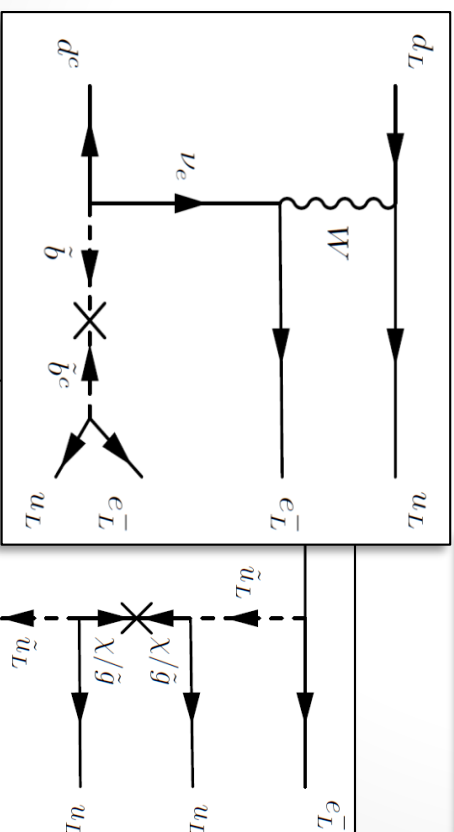


$$T_{1/2}^{-1} = \epsilon_{NP}^2 G_{NP}^{0\nu} |M_{NP}^{0\nu}|^2$$

- ▶ Neutrinos still Majorana

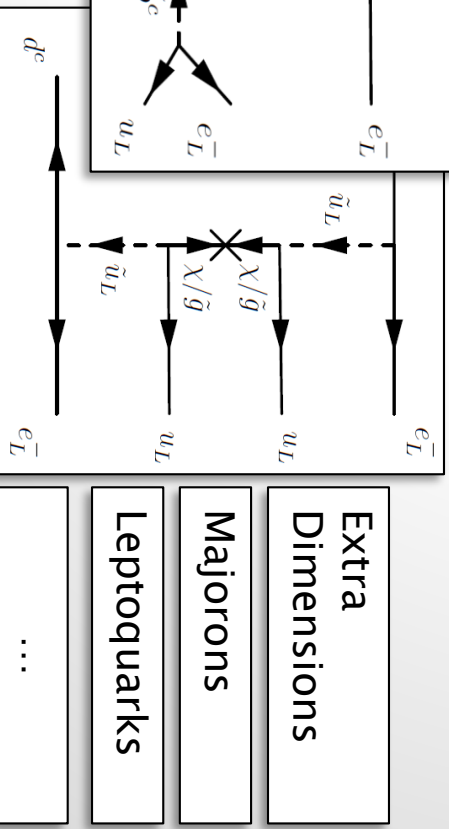


Left-Right Symmetry



R-Parity

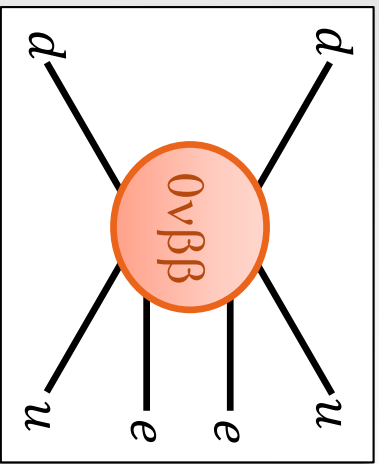
Violating SUSY



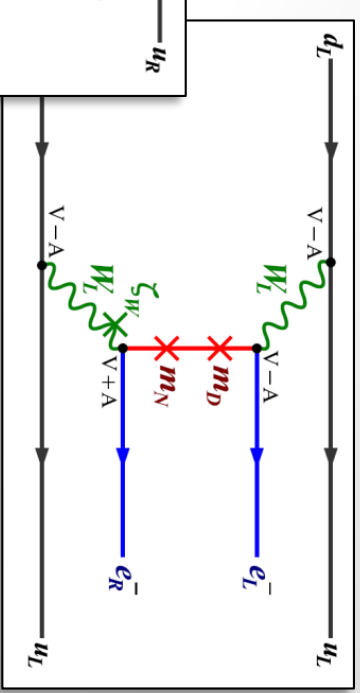
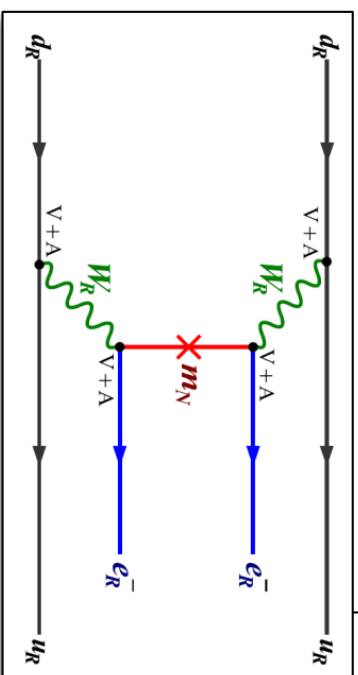
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- ...

# New Physics and $0\nu\beta\beta$

- ▶ Examples in Left-Right Symmetry



=



$$T_{1/2}^{-1} = \epsilon_{NP}^2 G_{NP}^{0\nu} |M_{NP}^{0\nu}|^2$$

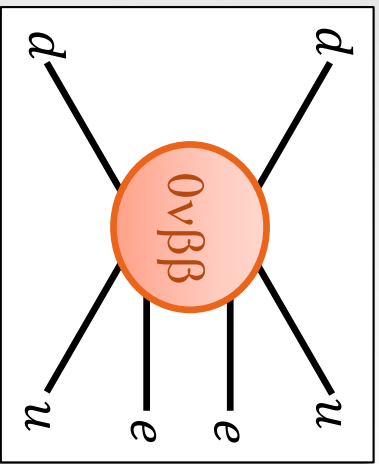
- ▶  $0\nu\beta\beta$  probes the TeV scale

$$\epsilon_{3}^{RRZ} = \sum_{i=1}^3 V_{ei}^2 \frac{m_p}{m_N} \frac{m_W^4}{m_{W_R}^4} \approx \frac{10^{-8}}{(\Lambda/1 \text{ TeV})^5}$$

$$\epsilon_{V-A}^{V+A} = \sum_{i=1}^3 U_{ei} W_{ei} \tan \zeta_W \approx \frac{10^{-9}}{(\Lambda/10 \text{ TeV})^3}$$

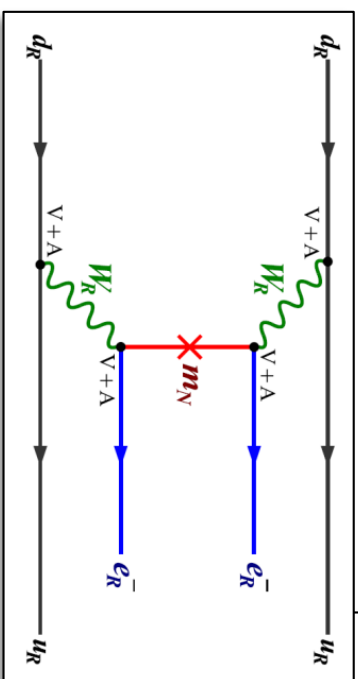
# New Physics and $0\nu\beta\beta$

## Examples in Left-Right Symmetry



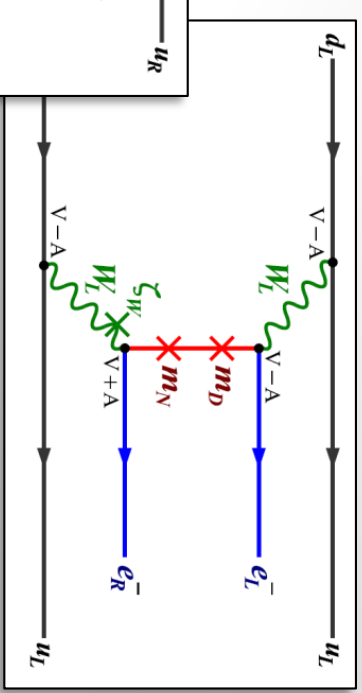
$$T_{1/2}^{-1} = \epsilon_{NP}^2 G_{NP}^{0\nu} |M_{NP}^{0\nu}|^2$$

## $0\nu\beta\beta$ probes the TeV scale



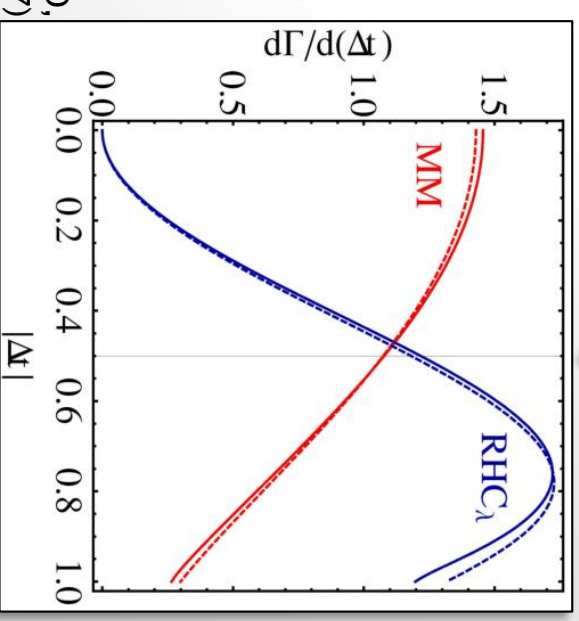
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Modified angular and energy distribution of emitted electrons (Doi et al. '83; Ali et al. '06)



$$\epsilon_{V-A}^{V+A} = U_{ei} W_{ei} \tan \zeta_W$$

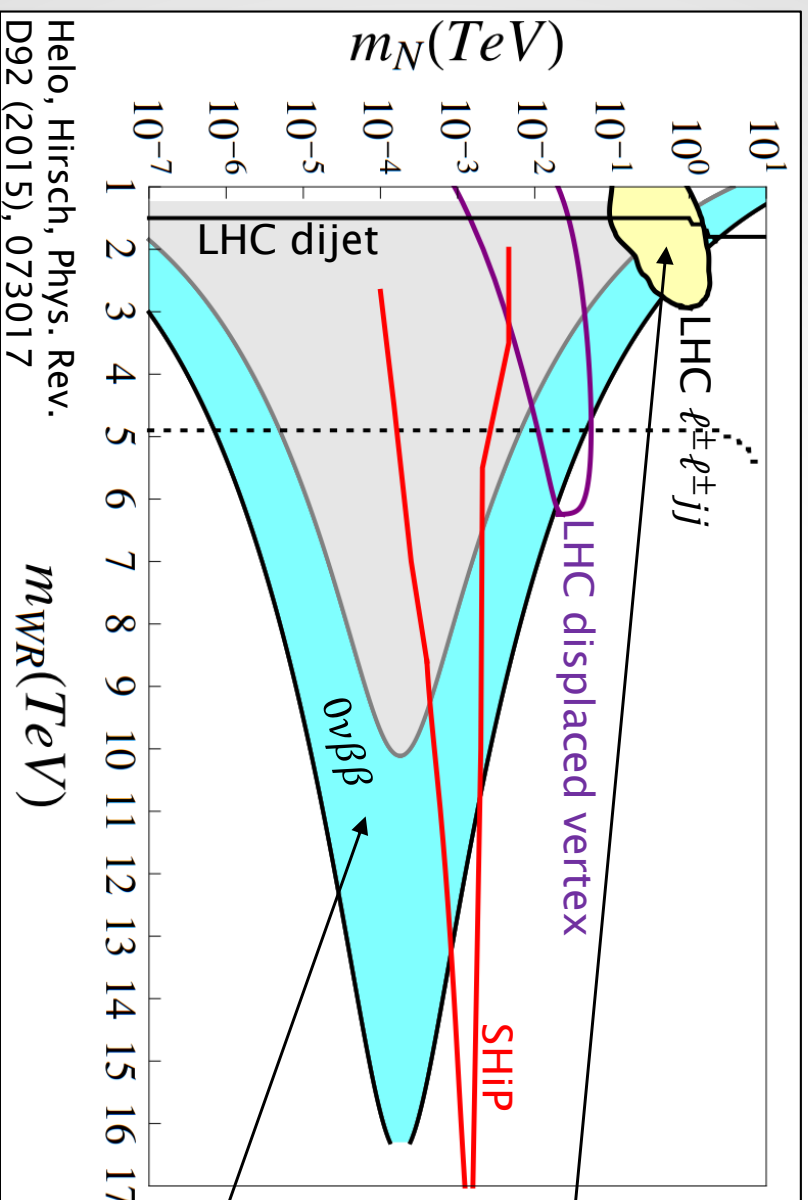
$$\approx \frac{10^{-9}}{(\Lambda/1 \text{ TeV})^3}$$



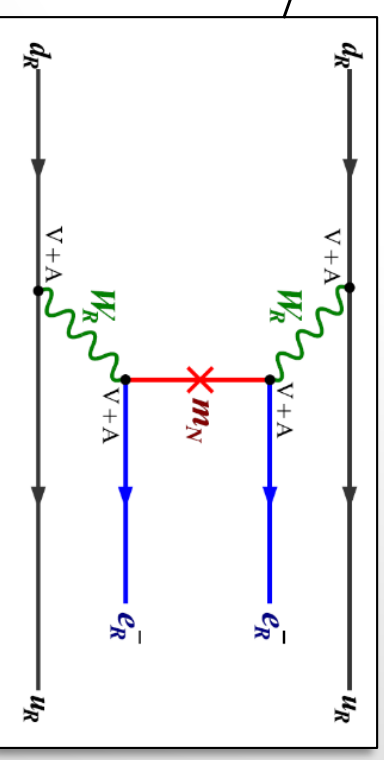
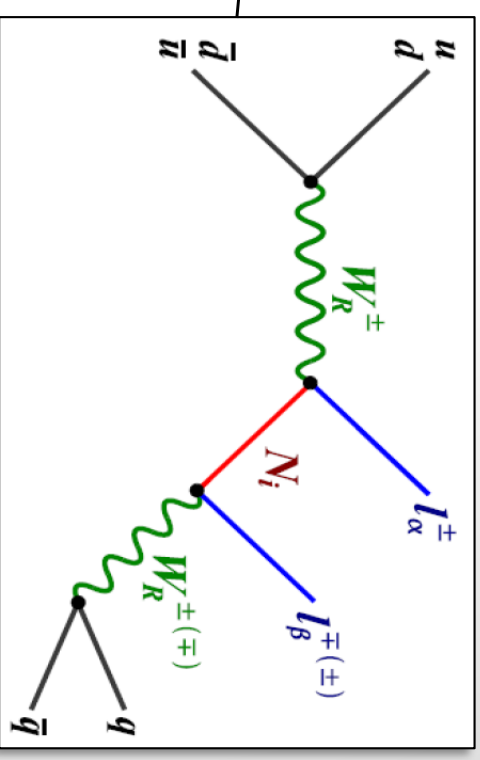
FFD, SuperNEMO, Eur.Phys.J. C70 (2010) 9277)

# $0\nu\beta\beta$ vs LHC

- ▶ Example of Left-Right Symmetry  
(Mohapatra, Senjanovic '75)



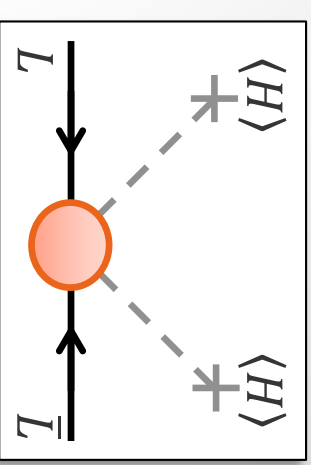
Helo, Hirsch, Phys. Rev. D92 (2015), 073017



# Neutrino Mass Models

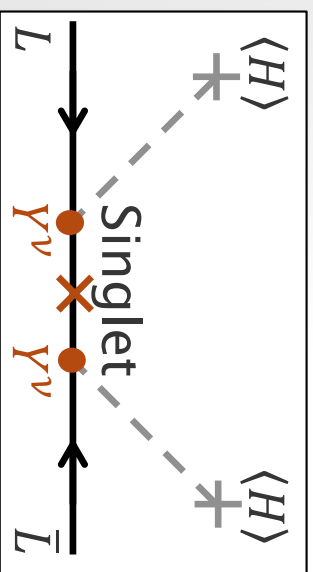
- Effective operator for Majorana neutrino mass
  - Only dimension-5 operator beyond SM

$$\mathcal{L} \supset \frac{1}{2} \frac{h_{ij}}{\Lambda_{LNV}} (\bar{L}_i^c \cdot H) (H^T \cdot L_j) \xrightarrow{\langle H \rangle} \frac{1}{2} (m_\nu)_{ij} \bar{\nu}_i^c \nu_j$$

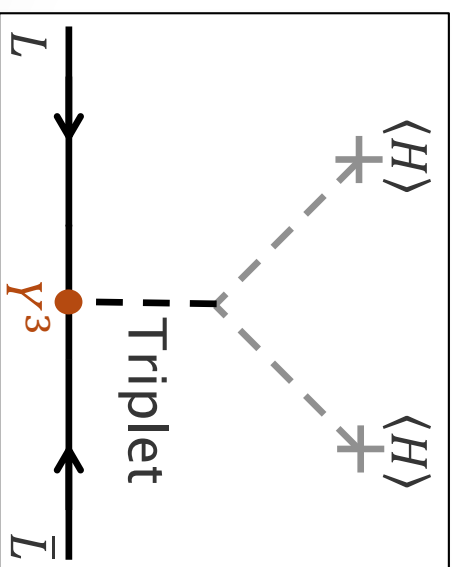


## Seesaw Mechanism

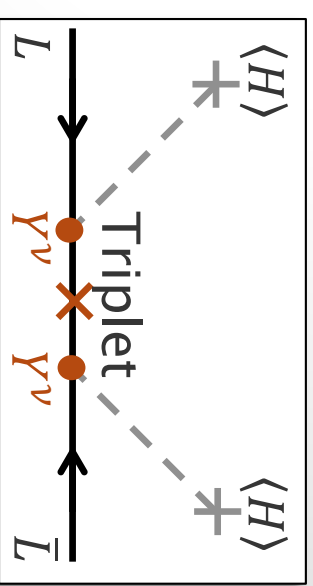
### Seesaw I



### Seesaw II



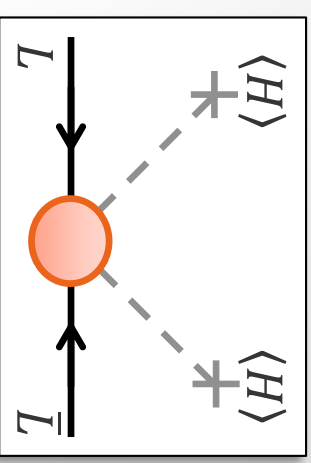
### Seesaw III



# Neutrino Mass Models

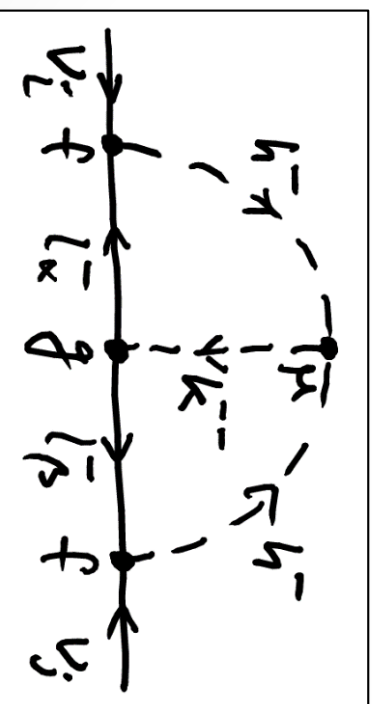
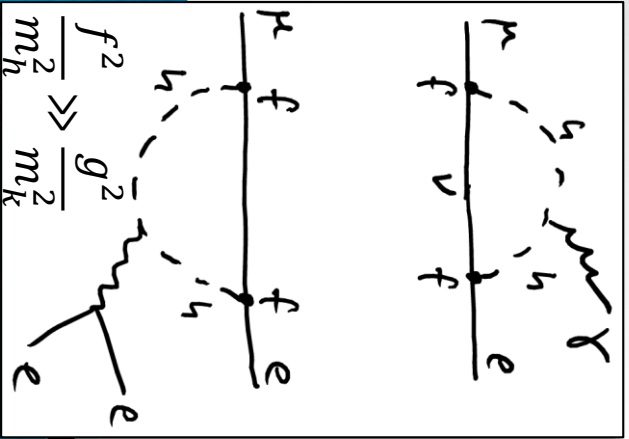
- ▶ Effective operator for Majorana neutrino mass
  - Only dimension-5 operator beyond SM

$$\mathcal{L} \supset \frac{1}{2} \frac{h_{ij}}{\Lambda_{LNV}} (\bar{L}_i^c \cdot H) (H^T \cdot L_j) \xrightarrow{\langle H \rangle} \frac{1}{2} (m_\nu)_{ij} \bar{\nu}_i^c \nu_j$$

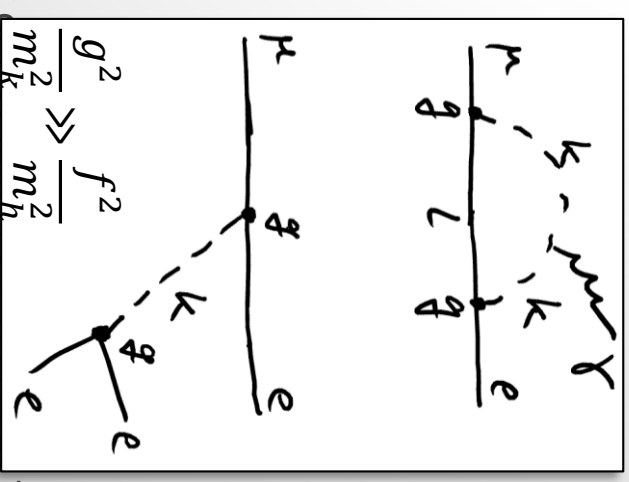


## ▶ Radiative Generation via Loops

- Alternative to Seesaw, e.g. Babu-Zee model (Zee '85, Babu '88)



Neutrino masses suppressed at 2-loop



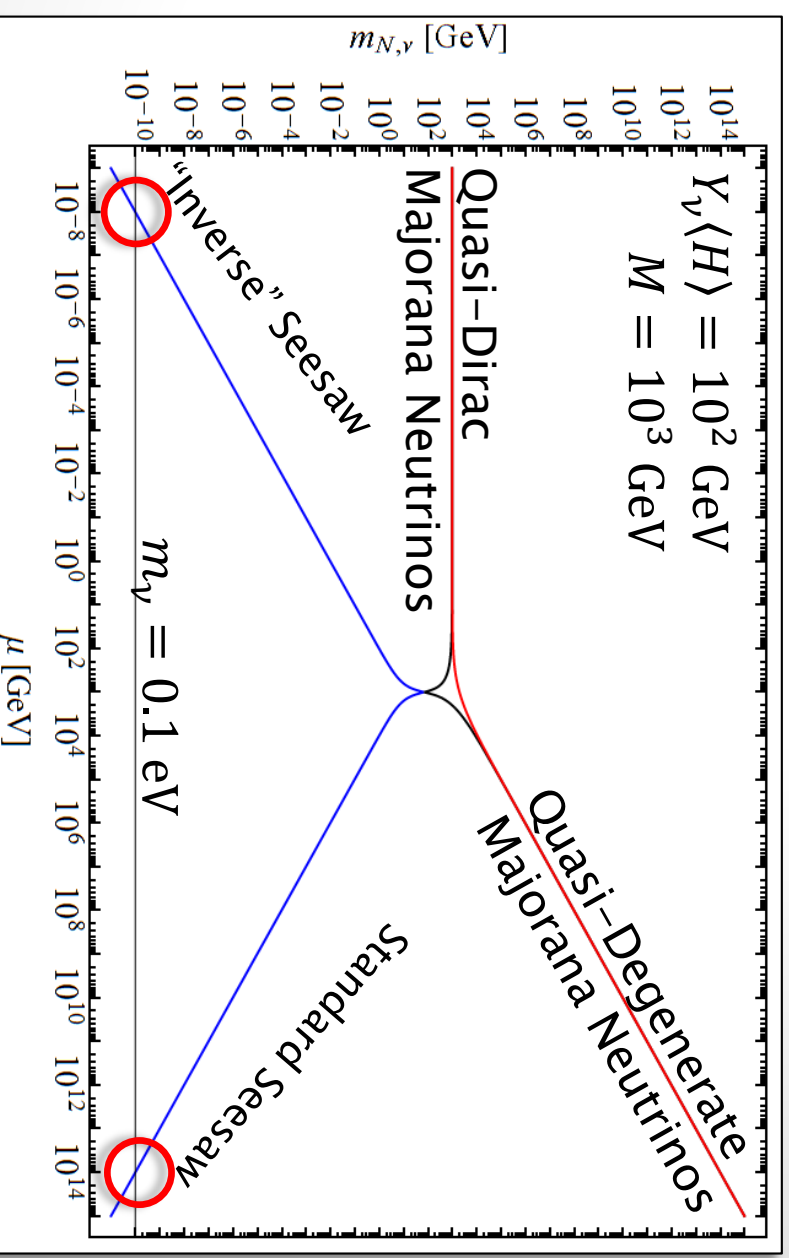
# Heavy Sterile Neutrinos

- ▶ Correct light neutrino masses for TeV scale heavy neutrinos
  - Seesaw Mechanism with TeV scale heavy neutrinos
  - Standard Seesaw with small Yukawa couplings
  - CLFV remains small
- “Bent” Seesaw mechanisms

- Decouple  $\Delta_{LNV}$  from heavy neutrino mass
- Example

$$\mathcal{M} = \begin{pmatrix} 0 & Y_\nu \langle H \rangle & 0 \\ Y_\nu \langle H \rangle & \mu & M \\ 0 & M & \mu \end{pmatrix}$$

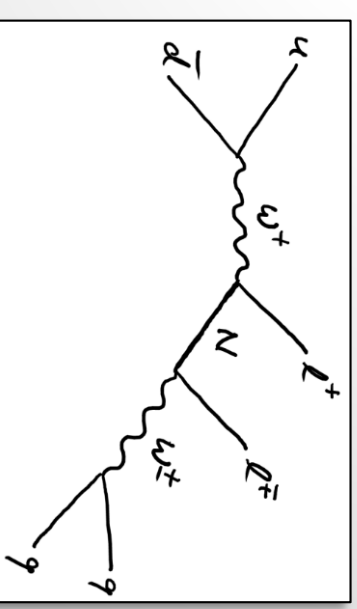
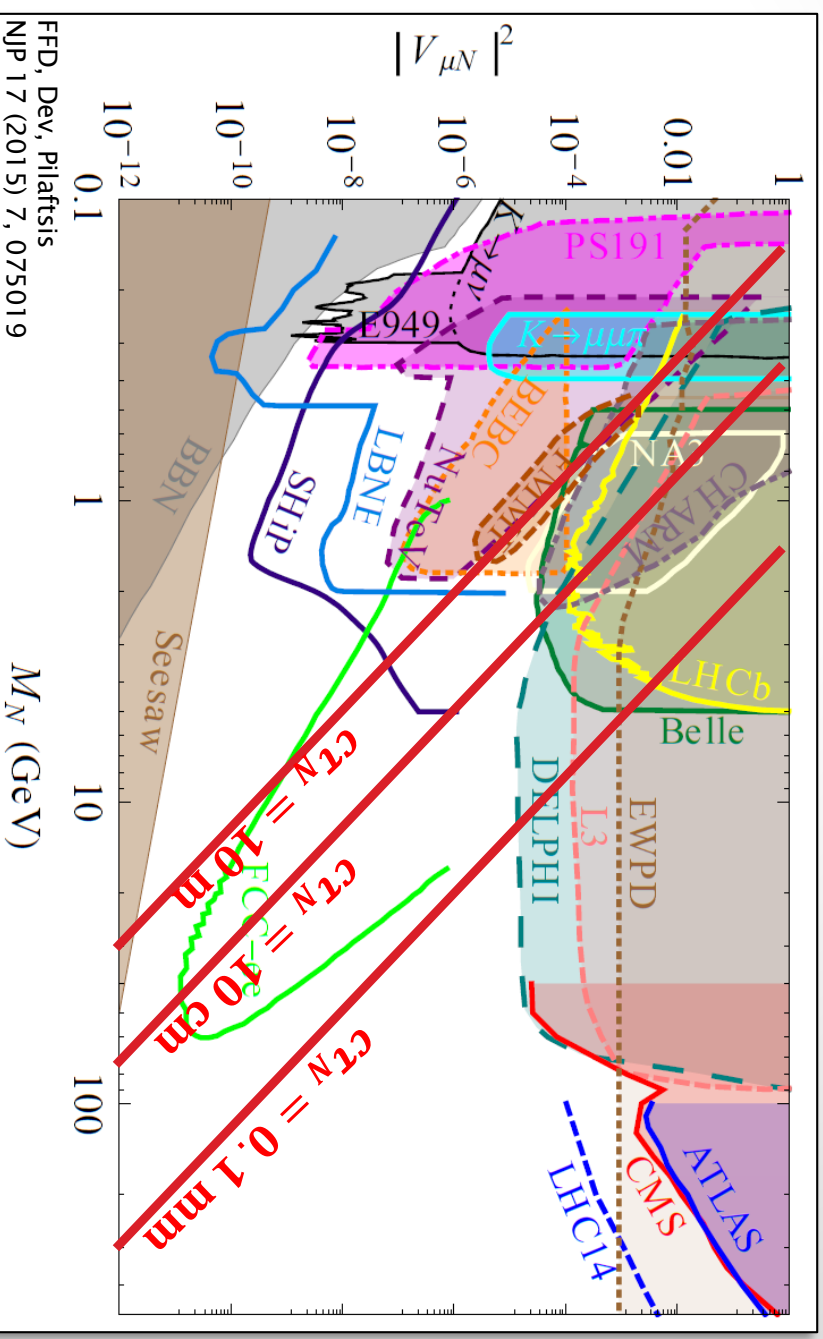
- Potentially large CLFV
- In the limit  $\mu \rightarrow 0$ , no LNV but CLFV





# Heavy Sterile Neutrinos

- ▶ Constraints on coupling to leptons  $|V_{lN}|$
- ▶ Neutrinoless Double Beta Decay
  - GERDA
  - stringent for pure Majorana  $N$
- ▶ Peak Searches in Meson Decays
  - $\pi, K \rightarrow e\nu$
  - Belle
- ▶ Beam Dump Experiments
  - e.g. PS191, CHARM
  - LBNE
- ▶ LNV Meson Decays
  - $K \rightarrow e e \pi$
  - SHiP
- ▶ Z Decays
  - LEP: L3, Delphi
  - FCC-ee
- ▶ Electroweak Precision Tests
  - EWPD: Fit of electroweak precision observables, lepton universality observables

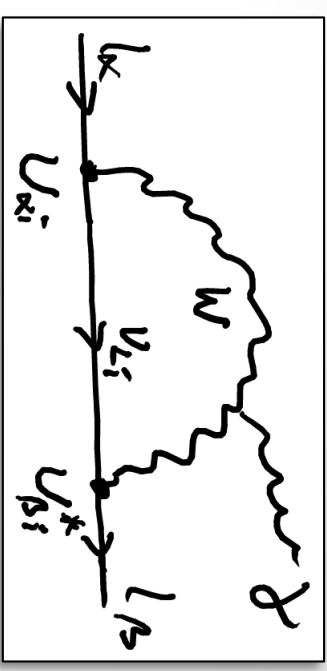


# Heavy Sterile Neutrinos

## CLFV in the Seesaw Mechanism

- Light neutrino exchange
- Negligible due to small neutrino masses

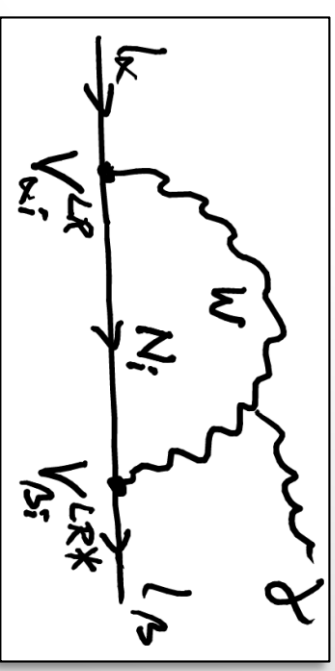
$$Br(\mu \rightarrow e\gamma) = \frac{3\alpha}{32\pi} \left| \sum_i U_{\mu i}^* U_{ei} \frac{\Delta m_{1i}^2}{m_W^2} \right|^2 \approx 10^{-56}$$



## Heavy neutrino exchange

- Sizable for TeV scale heavy neutrinos and large LR mixing  $V^{LR} \approx 10^{-2}$

$$Br(\mu \rightarrow e\gamma) \approx 4 \times 10^{-3} \left| \sum_i V_{\mu i}^{LR*} V_{ei}^{LR} G\left(\frac{m_{N_i}^2}{m_W^2}\right) \right|^2 \approx 10^{-11} \left(\frac{V^{LR}}{10^{-2}}\right)^4$$



$$\mathcal{U}^\nu = \begin{pmatrix} U & V^{LR} \\ (V^{LR})^\dagger & U^R \end{pmatrix}$$

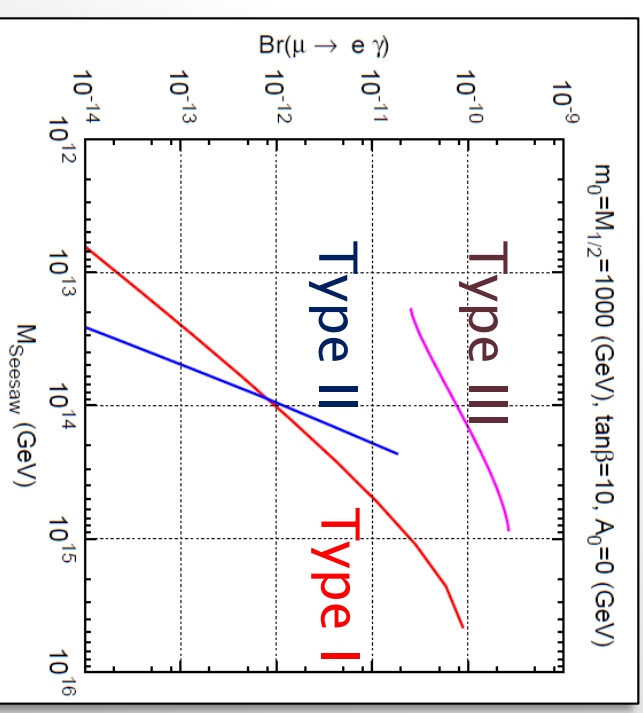
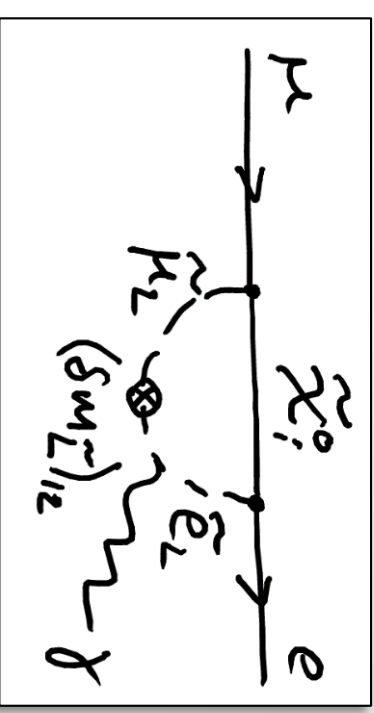
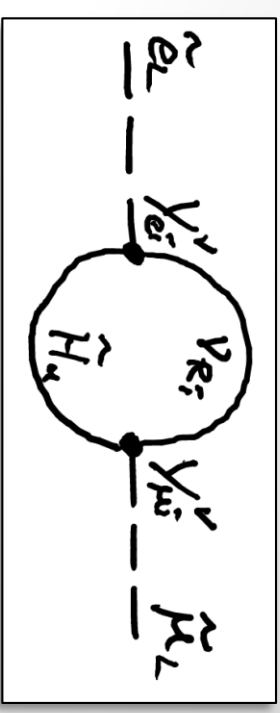
# SUSY Seesaw

- Neutrino flavour mixing radiatively induces slepton flavour mixing (Borzumati, Masiero '86)

- Correlation between slepton and neutrino flavour mixing (Type I)

$$(\delta m_L^2) = \begin{pmatrix} \delta_{11} & \delta_{12} & \delta_{13} \\ \delta_{12}^* & \delta_{22} & \delta_{23} \\ \delta_{13}^* & \delta_{23}^* & \delta_{33} \end{pmatrix} \propto (Y^{\nu\dagger} \cdot Y^\nu) \log(M_X/M_{\nu R})$$

- Induces observable charged LFV rates despite high scale Seesaw  $M_{\nu R} \approx 10^{14}$  GeV



Esteves et al. '11

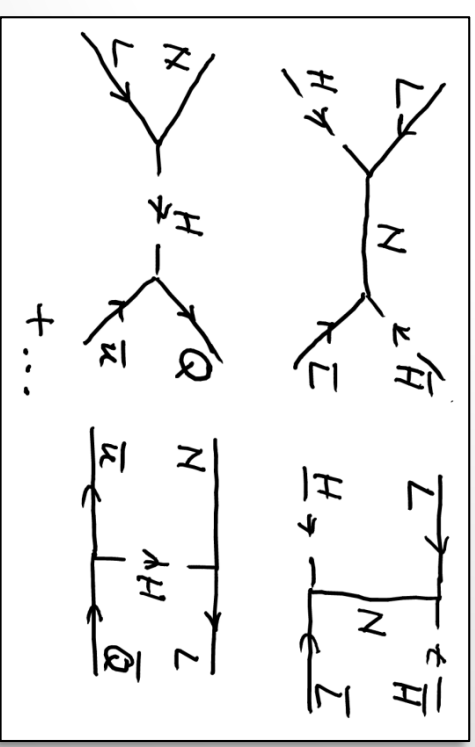
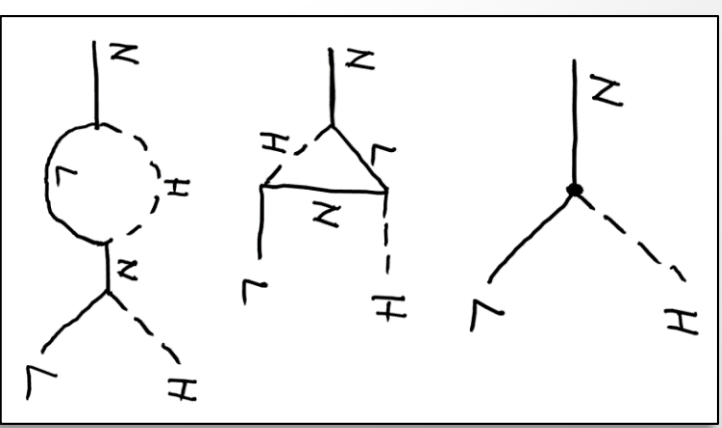
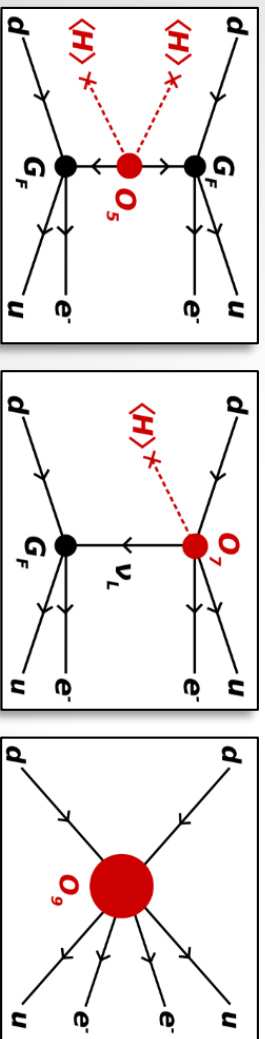
# Baryon Asymmetry

## Generation and Washout

- ▶ Classic Example: High-Scale Leptogenesis
  - Generation via heavy neutrino decays
  - Competition with LNV washout processes
  - Conversion to baryon asymmetry
  - EW sphaleron processes at  $T \approx 100$  GeV
  - Observed asymmetry

$$\eta_B \equiv \frac{n_B - n_{\bar{B}}}{n_\gamma} = (6.20 \pm 0.15) \times 10^{-10}$$

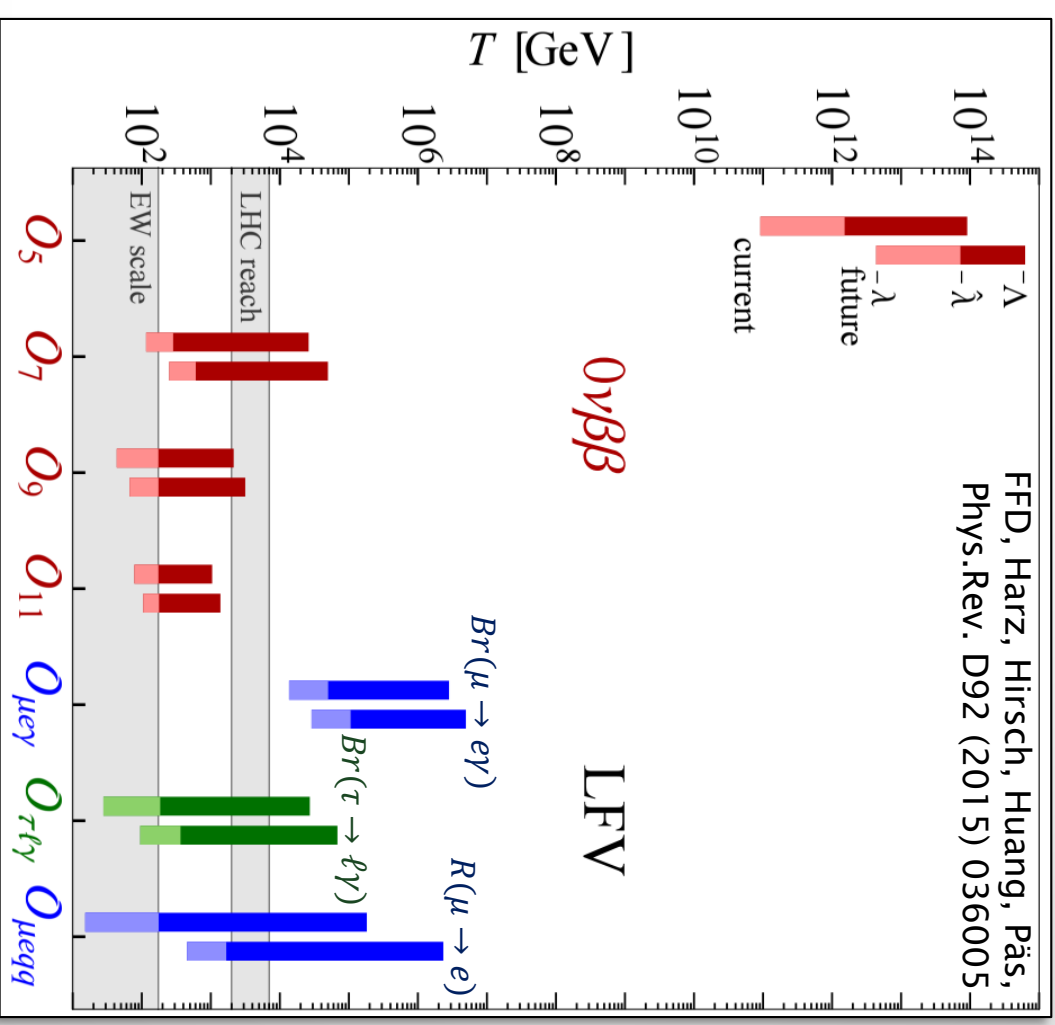
- ▶ What if we observe lepton number violating processes in  $0\nu\nu\beta$ ?



# Baryon Asymmetry

## Lepton Asymmetry Washout

- ▶ Compare  $0\nu\beta\beta$  rate with lepton asymmetry washout in the early Universe
- ▶ Observation of lepton number violation
  - gives information at what temperatures operators are in equilibrium
  - corresponds to highly effective washout  $\Gamma_W/H \gg 1$
  - **can falsify high-scale baryogenesis scenarios**



# Conclusion

- ▶ **Neutrinos much lighter than other fermions**
  - LNV! Dirac or Majorana? Lepton Number Violation?
- ▶ **LNV and LFV are crucial probes for BSM physics**
  - Test mechanisms and scale of neutrino mass generation
  - How is lepton number/flavour approximately protected
    - High scale, small couplings, symmetry?
- ▶ **Neutrinoless double beta decay**
  - Discovery → Majorana  $\nu$  → Physics near GUT scale? LNV @ TeV?
  - Exclusion → Dirac  $\nu$ ? → Fine-tuned SM?
- ▶ **Strong Synergy with LHC+LFV searches**
  - LHC can deep-probe anatomy of  $0\nu\beta\beta$  LNV operators
  - Observation of LNV+LFV would strongly constrain baryogenesis