Sources: Magnetohydrodynamic Waves

- Introduction to MHD waves (and beyond)

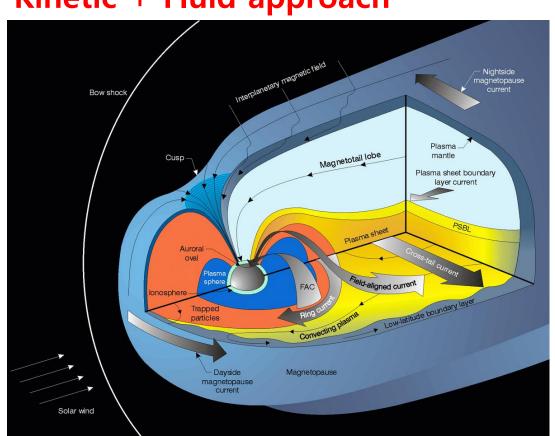
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Introduction

- Space: in situ experiment
- Space is NOT empty and well structured.
- Space has all kinds of dynamics:

Single-ptl + Kinetic + Fluid approach

L ~ 100,000km dL ~ 100km



Introduction

(ground)

Sea:
$$\sim 10^{+22} / cm^3$$

Air:
$$\sim 10^{+19} / cm^3$$

- collisions dominant

- diffusive
- neutral ptls
- mech. + gravit.

(space)

$$\sim 10^{-2} - 10^{+3} / cm^3$$

- collisions negligible
- well-structured
- plasma (ions, electrons)
- mech. + electromag.

cf) For CLIC beams,

$$n_e \, \Box \, 10^{12 \sim 13} \, / \, (1nm, 40nm, 150ns * c) \sim 10^{21} \, / \, cm^3$$



Background: from single-ptl to fluid

Single-ptl (e.g., f=ma)

$$\vec{X}(t), \ \vec{V}(t)$$
 $\vec{F} = m \frac{d\vec{V}}{dt} = q (\vec{E} + \vec{V} \times \vec{B})$

A few or many ptls (kinetic approach, f(x,v,t))

$$N(\vec{x}, \vec{v}, \vec{t}) = \sum_{j} \delta(\vec{x} - \vec{X}_{j}(t)) \delta(\vec{v} - \vec{V}_{j}(t)) \qquad f(\vec{x}, \vec{v}, t) \equiv \langle N(\vec{x}, \vec{v}, t) \rangle$$

Multi-fluids (multi-ions + electrons)

$$n_{j}(\vec{x}, t), \vec{V}_{j}(\vec{x}, t), P_{j}(\vec{x}, t), T_{j}(\vec{x}, t)$$
 $j = e, i$

- Single-fluid (MHD) $n(\vec{x}, t)$, $\vec{V}(\vec{x}, t)$, $P(\vec{x}, t)$, $T(\vec{x}, t)$
- Ideal MHD

Background: Multi-fluids (multi-ions + electrons)

- Multi-fluid equations

$$\frac{\partial n_j}{\partial t} + \nabla \cdot (n_j \mathbf{v_j}) = 0$$

$$m_j n_j \left[\frac{\partial \mathbf{v_j}}{\partial t} + (\mathbf{v_j} \cdot \nabla) \mathbf{v_j} \right] = n_j q_j (\mathbf{E} + \mathbf{v_j} \times \mathbf{B}) - \nabla p_j + \mathbf{R}_j \qquad j = i, e$$

$$p_j = C_j n_j^{\gamma_j}$$

- Ideal MHD equations

$$\frac{\partial n}{\partial t} + \nabla \cdot (n\mathbf{v}) = 0$$

$$mn\left[\frac{\partial \mathbf{v}}{\partial t} + (\mathbf{v} \cdot \nabla)\mathbf{v}\right] = \mathbf{j} \times \mathbf{B} - \nabla p$$

$$p = Cn^{\gamma}$$

$$\mathbf{E} + \mathbf{v} \times \mathbf{B} = 0$$

Approximations

- From N(x,v,t) to f(x,v,t):

Neglect the single-particle nature

$$r >> \lambda_D = \sqrt{\frac{\epsilon_o k_B T}{ne^2}}$$
 = the Debye length

 $\Lambda = n\lambda_D^3 >> 1$: the plasma parameter

cf) For CLIC beams: $r \square \lambda_D$, but $\Lambda \square 1$

-From f(x,v,t) {plasma kinetic eq.} to f(x,v,t) {Vlasov eq.}:

> Neglect collisions (resistivity) weak turbulence quasi-linear theory

- From f(x,v,t) to MF(x,t):

Neglect the velocity distribution ex) wave-particle interaction microscopic instabilities Landau damping non-thermal equilibrium

- From MF(x,t) to SF(x,t):

Neglect the electron inertia and the ion species ex) rapid EM & ES variations

$$\omega < \omega_{ci} = rac{eB}{m_i}$$
 lon gyro-frequency
$$r > r_{ci} = rac{v_\perp}{\omega_{ci}}$$
 lon gyro-radius

Application – Waves in space

<MHD waves>

- very low freq:

MHD waves

 $\omega \ll \Omega_i$

<multi-fluid waves>

- low freq:

Ion waves

 $\omega \sim \Omega_i$

- intermed. freq:

lon-electron waves

 $\Omega_i < \omega < \Omega_e$

- high freq:

Electron waves

 $\omega \sim \Omega_e$

<kinetic waves>

- e.g. higher harmonics, Bernstein waves, ...

<single-ptl resonances>

- e.g. bounce resonance, bounce-drift resonance, ...

Application – Waves in space

Maxwell eqs + Ohm's law



For instance, $\vec{B} = B \hat{z}$,

$$\vec{B}=B\,\hat{z}$$
 ,

$$\epsilon = \left(egin{array}{ccc} S & -iD & 0 \ iD & S & 0 \ 0 & 0 & P \end{array}
ight)$$

$$\vec{\nabla} \times (\vec{\nabla} \times \vec{E}) = -\frac{1}{c^2} \frac{\partial^2 \vec{E}}{\partial t^2} - \mu_o \frac{\partial \vec{J}}{\partial t}$$
$$= \frac{\omega^2}{c^2} \left(\mathbf{I} + \frac{i\sigma}{\omega \epsilon_o} \right) \cdot \vec{E}$$
$$= k^2 \epsilon \cdot \vec{E}$$

$$\epsilon = \begin{pmatrix} S & -iD & 0 \\ iD & S & 0 \\ 0 & 0 & P \end{pmatrix} \qquad \begin{array}{rcl} S & = & 1 - \sum_{j} \frac{\omega_{pj}^2}{\omega^2 - \omega_{cj}^2} \\ D & = & \sum_{j} \frac{|q_j|/q_j \ \omega_{cj}\omega_{pj}^2}{\omega(\omega^2 - \omega_{cj}^2)} \\ P & = & 1 - \sum_{j} \frac{\omega_{pj}^2}{\omega^2} \end{array}$$

$$\omega_{pj} = \sqrt{rac{n_j q_j^2}{m_j \epsilon_o}} ~~ \omega_{cj} = rac{|q_j|B}{m_j}$$

Application – Waves

- CMA diagram

<multi-fluid waves>

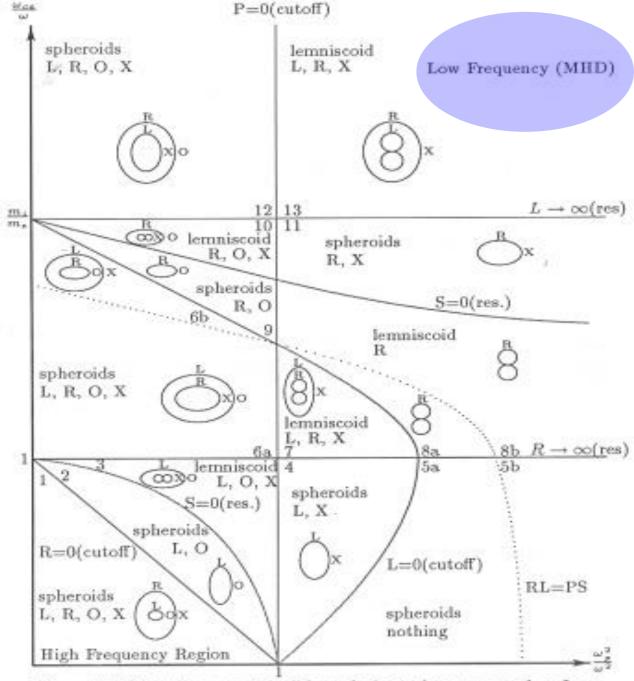
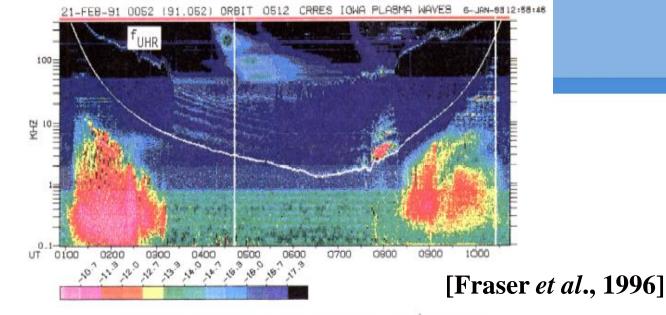
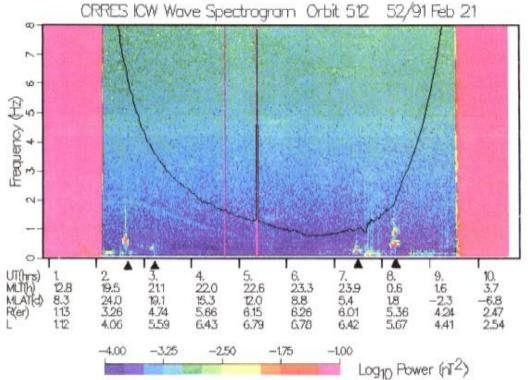


Figure 2.8: CMA diagram with all boundaries and wave normal surfaces.

Application – W

<electron waves>



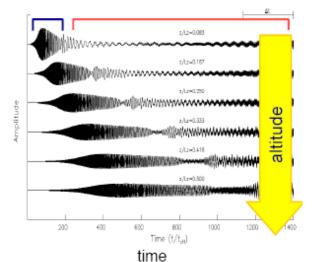


<multi-ion waves>

Plate 1. (Upper) CRRES EMIC wave dynamic spectrum for orbit 512 on February 21, 1991. The dark curve is the

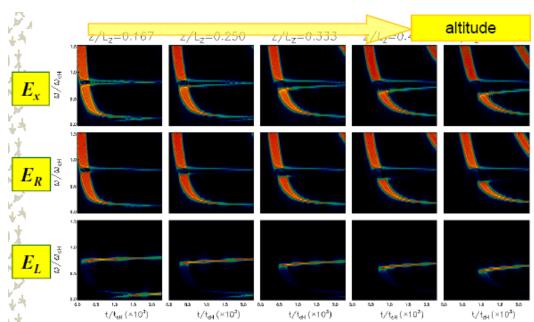
Application – Waves in space

- Two wave modes
 - First mode
 - Decreasing frequency with increasing time
 - Second mode ———
 - Appear after the reception of first wave modes
- Length of the wavetrains grows significantly with z.
- The time delay increases with z.



[Kim & Lee, 2005]

<ion-electron waves>

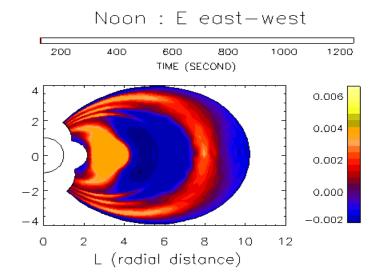


MHD waves

In uniform medium:

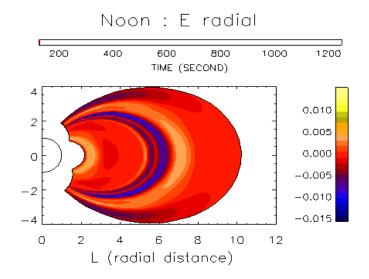
$$\omega = \frac{k V_A}{\sqrt{1 + \frac{i k^2}{\mu_o \omega \sigma}}}$$

- Compressional waves
- Magnetosonic waves
- Isotropic mode
- Three-dimensional



$$\omega = \frac{k_{\parallel} V_A}{\sqrt{1 + \frac{i k^2}{\mu_o \omega \sigma}}}$$

- Incompressional waves
- Alfven waves
- Anisotropic
- One-dimensional



* In a nonuniform plasma,

$$rac{\omega}{\omega_{cj}} \ll 1$$
 and $ho(x), V_A(x) = rac{B}{\mu_o
ho(x)}$

$$S \approx \frac{c^2}{V_A^2}$$

 $D \approx 0$

 $P \rightarrow \infty$

Ey: Compressional waves

$$Ez = 0$$

$$\left(\frac{d}{dx}\frac{D}{D-k_y^2}\frac{dE_y}{dx}\right) + D E_y = 0$$

- MHD waves: Asymptotic solutions

At resonances,

$$E_x \propto \frac{1}{x - x_0}$$
 $E_y \propto ln|x - x_0|$

$$E_y \propto ln|x-x_0|$$

$$\frac{\omega^2}{V_A^2} - k_z^2 = \alpha (x - x_0) = C (\omega - \omega_0)$$

$$E_y(x,t\to\infty) \propto \frac{1}{2\pi} \int_{-\infty}^{\infty} \ln|\omega-\omega_0| e^{-i\omega t} d\omega = -\frac{1}{2t} e^{-i\omega_0 t}$$

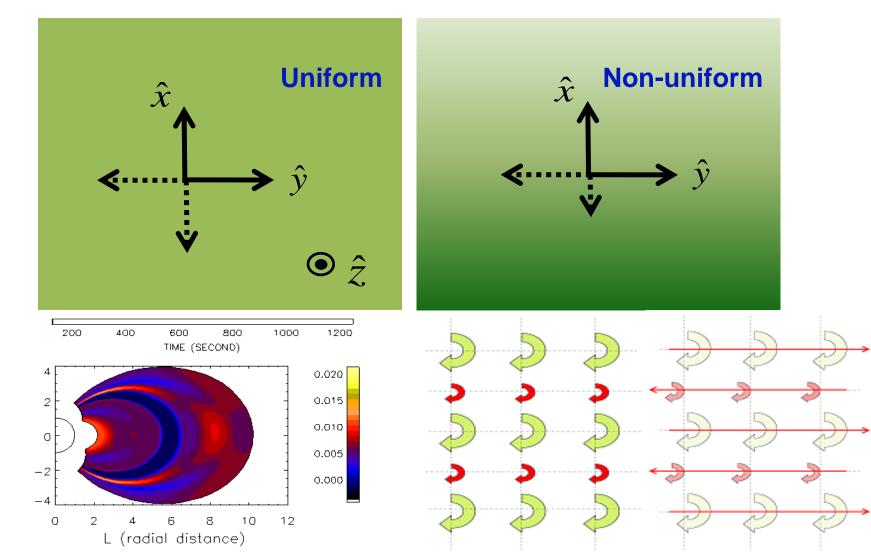
Ey is being damped to Ex (even if no dissipations)

Compressional waves damp, shear Alfven waves grow.

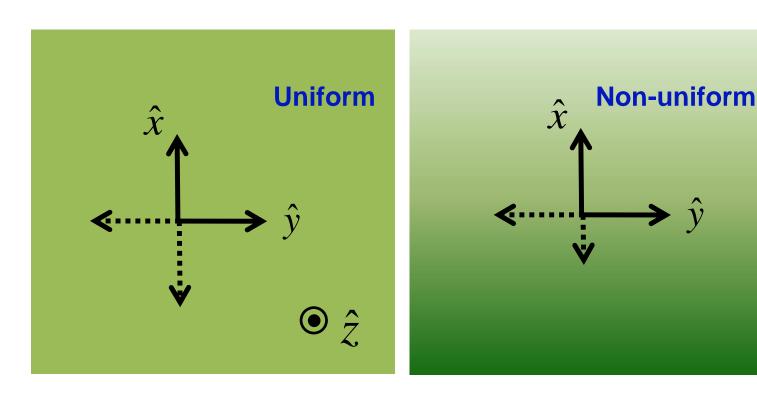
Resonant absorption of Alfven waves = Field line resonances

Mode conversion

- Two degrees of freedom become differential in nonuniform plasmas.
- In terms of wave (collective) motion, azimuthal or shear motion is stable.



 $\vec{E} + \vec{v} \times \vec{B}_o = 0$ is valid for collective, but relatively low frequency wave motion.



- When inhomo. lies perpendicular to B-field, the azimuthal (shear) motion Vy or radial Ex or azimuthal By are expected to be stable(and dominant?).



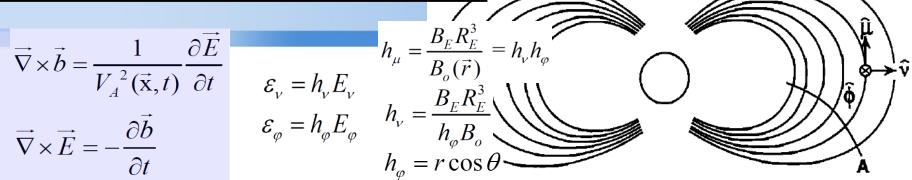
* Torodial & Poloidal modes

$$\vec{\nabla} \times \vec{b} = \frac{1}{V_A^2(\vec{\mathbf{x}}, t)} \frac{\partial \vec{E}}{\partial t}$$

$$\vec{\nabla} \times \vec{E} = -\frac{\partial \vec{b}}{\partial t}$$

$$\varepsilon_{v} = h_{v} E_{v}$$

$$\varepsilon_{\varphi} = h_{\varphi} E_{\varphi}$$



$$(\mu, \nu, \varphi)$$

In the dipole coordinate
$$(\mu, \nu, \varphi)$$

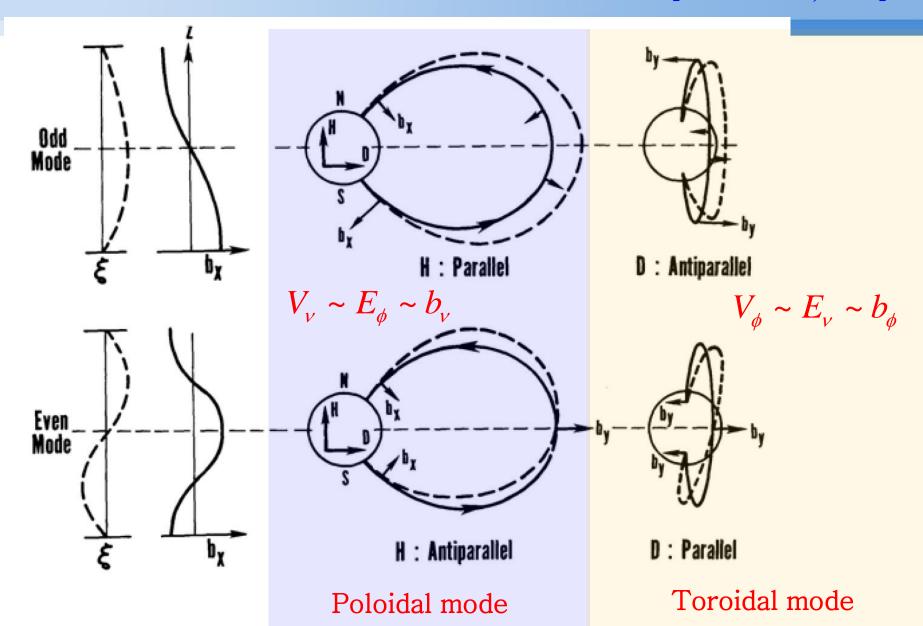
$$\frac{\partial \beta_{\mu}}{\partial t} = -\left\{\frac{\partial \varepsilon_{\varphi}}{\partial \nu} - \frac{\partial \varepsilon_{\nu}}{\partial \varphi}\right\} = -\left\{\frac{\partial \varepsilon_{\varphi}}{\partial \nu} + im\varepsilon_{\nu}\right\}$$

$$\begin{split} &\left\{\frac{1}{V_{A}^{2}}\frac{\partial^{2}}{\partial t^{2}} - \frac{1}{h_{\varphi}^{2}}\frac{\partial}{\partial\mu}\left(\frac{1}{h_{v}^{2}}\frac{\partial}{\partial\mu}\right)\right\}\varepsilon_{v} = -\frac{1}{h_{\varphi}^{2}}\frac{\partial}{\partial\varphi}\left\{\frac{\partial\varepsilon_{\varphi}}{\partial\nu} - \frac{\partial\varepsilon_{v}}{\partial\varphi}\right\} \\ &\left\{\frac{1}{V_{A}^{2}}\frac{\partial^{2}}{\partial t^{2}} - \frac{1}{h_{v}^{2}}\frac{\partial}{\partial\mu}\left(\frac{1}{h_{\varphi}^{2}}\frac{\partial}{\partial\mu}\right)\right\}\varepsilon_{\varphi} = \frac{1}{h_{v}^{2}}\frac{\partial}{\partial\nu}\left\{\frac{\partial\varepsilon_{\varphi}}{\partial\nu} - \frac{\partial\varepsilon_{v}}{\partial\varphi}\right\} \\ &\left\{\frac{\partial\varepsilon_{\varphi}}{\partial\nu} - \frac{1}{\partial\varphi}\frac{\partial}{\partial\varphi}\left(\frac{1}{h_{\varphi}^{2}}\frac{\partial}{\partial\nu}\right)\right\}\varepsilon_{\varphi} = \frac{1}{h_{v}^{2}}\frac{\partial}{\partial\nu}\left\{\frac{\partial\varepsilon_{\varphi}}{\partial\nu} - \frac{\partial\varepsilon_{v}}{\partial\varphi}\right\} \\ &= \frac{1}{h_{v}^{2}}\frac{\partial}{\partial\nu}\left\{\frac{\partial\varepsilon_{\varphi}}{\partial\nu} + im\varepsilon_{v}\right\} \end{split}$$

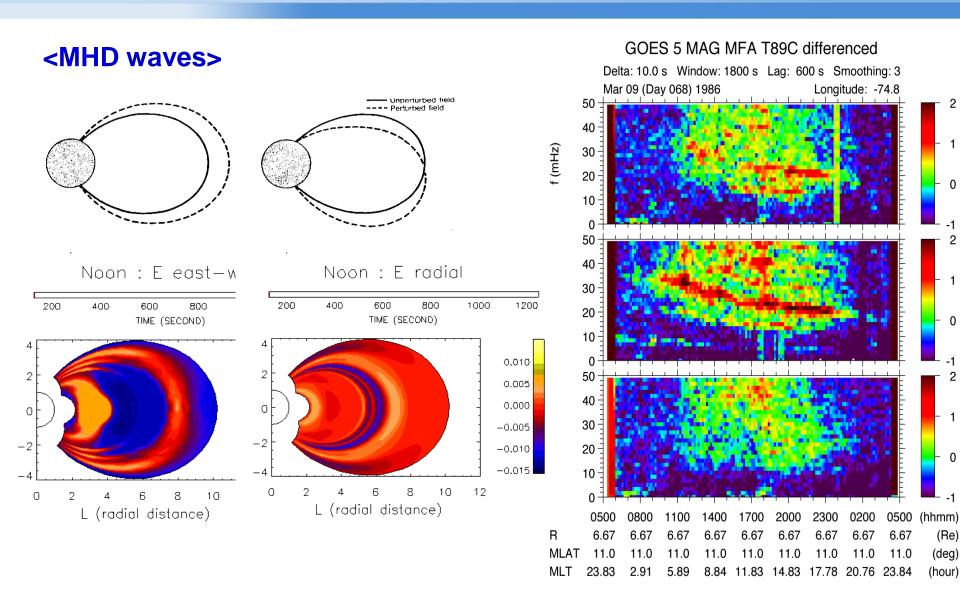


$$\left\{ \frac{1}{V_A^2} \frac{\partial^2}{\partial t^2} - \frac{1}{h_{\varphi}^2} \frac{\partial}{\partial \mu} \left(\frac{1}{h_{\nu}^2} \frac{\partial}{\partial \mu} \right) \right\} \varepsilon_{\nu} = 0 \quad \text{Toroidal: } m = 0$$

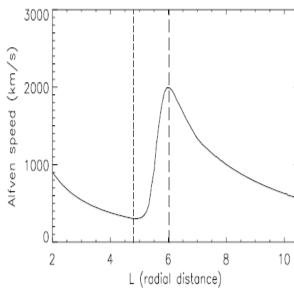
$$\left\{ \frac{1}{V_A^2} \frac{\partial^2}{\partial t^2} - \frac{1}{h_{\nu}^2} \frac{\partial}{\partial \mu} \left(\frac{1}{h_{\varphi}^2} \frac{\partial}{\partial \mu} \right) \right\} \varepsilon_{\varphi} = 0 \quad \text{Poloidal: } m \to \infty$$



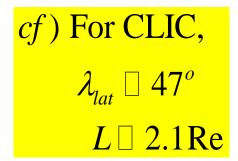
Application – Waves in space

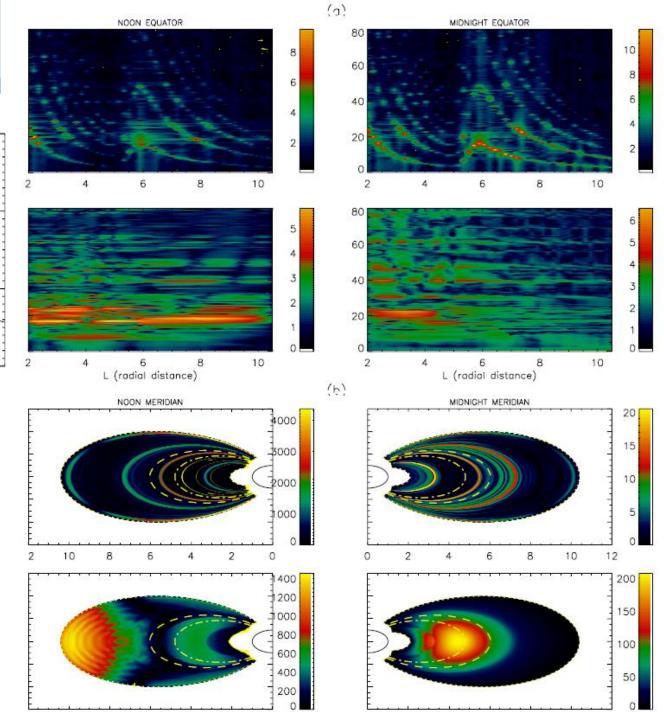


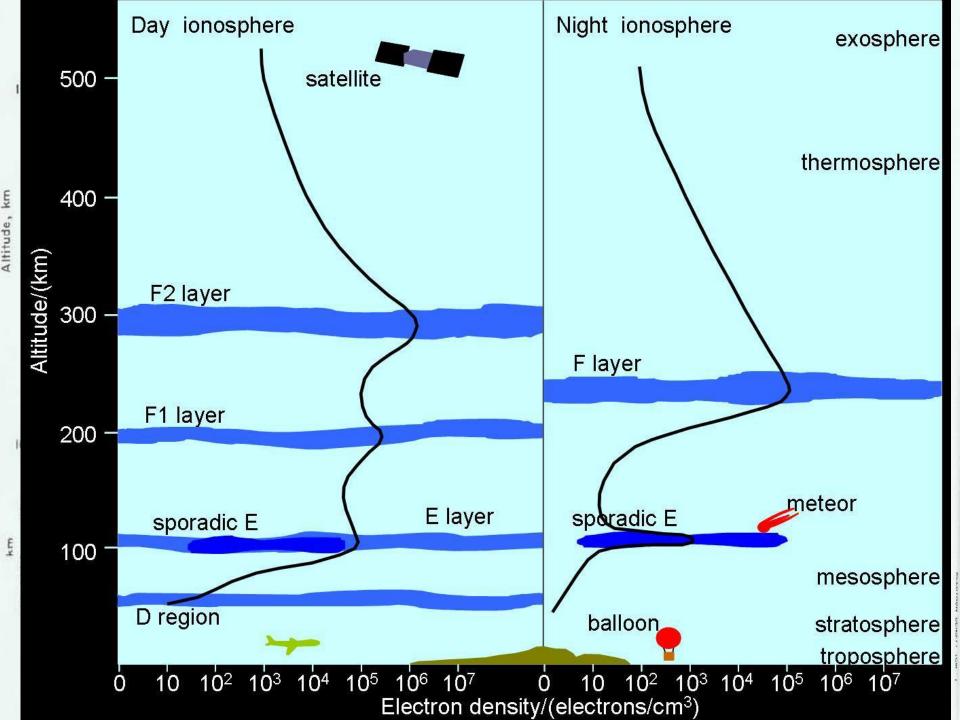
- 3-D dipole MHD waves



[e.g., Lee et al., 2004]







* Assume: $\overrightarrow{v}_n = 0$

$$\overrightarrow{v_n} = 0$$

- Eqs of motion:

$$m_i \frac{\partial \overrightarrow{v_i}}{\partial t} = e \left(\overrightarrow{E} + \overrightarrow{v_i} \times \overrightarrow{B} \right) - m_i v_{in} \overrightarrow{v_i}$$

$$m_e \frac{\partial \overrightarrow{v_e}}{\partial t} = -e \left(\overrightarrow{E} + \overrightarrow{v_e} \times \overrightarrow{B} \right) - m_e v_{en} \overrightarrow{v_e}$$

$$\overrightarrow{J} = \overrightarrow{\sigma} \cdot \overrightarrow{E} = \begin{pmatrix} \sigma_P & -\sigma_H & 0 \\ \sigma_H & \sigma_P & 0 \\ 0 & 0 & \sigma_{\parallel} \end{pmatrix} \cdot \begin{pmatrix} E_{\chi} \\ E_{y} \\ E_{z} \end{pmatrix}$$

$$\overrightarrow{J} = \sigma_{\parallel} \overrightarrow{E}_{\parallel} + \sigma_{P} \overrightarrow{E}_{\perp} - \sigma_{H} \frac{\overrightarrow{E} \times \overrightarrow{B}}{B}$$

where

$$\sigma_{p} = \epsilon_{o} \sum_{j} \frac{\omega_{pj}^{2} (\nu_{jn} - i\omega)}{(\nu_{jn} - i\omega)^{2} + \omega_{cj}^{2}}$$

$$\sigma_{H} = -\epsilon_{o} \sum_{j} \frac{\epsilon_{j} \omega_{pj}^{2} \omega_{cj}}{(\nu_{jn} - i\omega)^{2} + \omega_{cj}^{2}}$$

$$\sigma_{\parallel} = \epsilon_{o} \sum_{j} \frac{\omega_{pj}^{2} \omega_{cj}}{(\nu_{jn} - i\omega)^{2} + \omega_{cj}^{2}}$$

If $\omega \ll \nu_{jn}$

$$\sigma_{p} \cong \epsilon_{o} \sum_{i} \frac{\omega_{pj}^{2} v_{jn}}{v_{jn}^{2} + \omega_{cj}^{2}} = \left(\frac{v_{en}}{v_{en}^{2} + \omega_{ce}^{2}} + \frac{m_{e}}{m_{i}} \frac{v_{in}}{v_{in}^{2} + \omega_{ci}^{2}}\right) \frac{n_{e}e^{2}}{m_{e}}$$

$$\sigma_{H} \simeq -\epsilon_{o} \sum_{i} \frac{\epsilon_{j} \, \omega_{pj}^{2} \, \omega_{cj}}{|v_{jn}|^{2} + |\omega_{cj}|^{2}} = \left(\frac{\omega_{ce}}{|v_{en}|^{2} + |\omega_{ce}|^{2}} - \frac{m_{e}}{m_{i}} \, \frac{|\omega_{ci}|}{|v_{in}|^{2} + |\omega_{ci}|^{2}} \right) \frac{n_{e} e^{2}}{m_{e}}$$

$$\sigma_{\parallel} \cong \epsilon_o \sum_{i} \frac{|\omega_{pj}|^2}{|\nu_{jn}|} = \left(\frac{1}{|\nu_{en}|} + \frac{m_e}{m_i} \frac{1}{|\nu_{in}|}\right) \frac{n_e e^2}{m_e}$$

since
$$\frac{\sigma_P(j)}{\sigma_H(j)} \approx \frac{\nu_{jn}}{\omega_{cj}}$$

$$\frac{\omega_{ce}}{\omega_{ci}} = \frac{m_i}{m_e} = 1836$$

$$\frac{v_{en}}{v_{in}} = \sqrt{\frac{m_i}{m_n}} = \sqrt{1836} \cong 43$$

$\omega_{cj} \ll \nu_{jn}$ $\sigma_{P}(j) \gg \sigma_{H}(j)$ $\sigma_{Cj} \gg \nu_{jn}$ $\sigma_{D}(j) \ll \sigma_{H}(j)$

$$\omega_{cj} \gg \nu_{jn} \qquad \sigma_{P}(j) \ll \sigma_{H}(j)$$

There are 3 choices:







: both H currents dominant

* Ionosphere: Composition

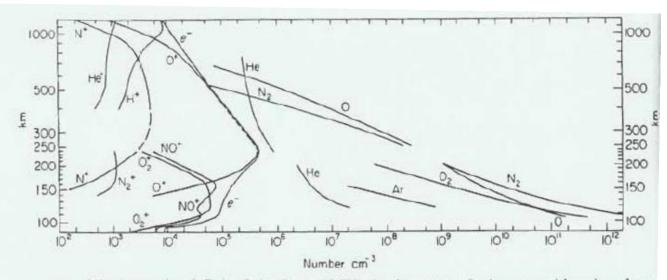
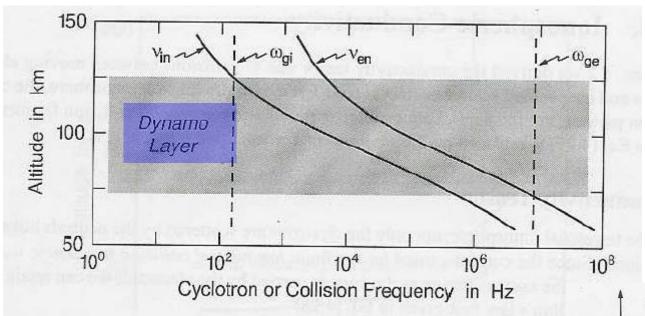


Fig. 1.2. International Quiet Solar Year (IQSY) daytime atmospheric composition, based on mass spectrometer measurements above White Sands, New Mexico (32°N, 106°W). The helium distribution is from a nighttime measurement. Distributions above 250 km are from the Elektron II satellite results of Istomin (1966) and Explorer XVII results of Reber and Nicolet (1965). [C. Y. Johnson, U.S. Naval Research Laboratory, Washington, D.C. Reprinted from Johnson (1969) by permission of the MIT Press, Cambridge, Massachusetts. Copyright 1969 by MIT.]



$$\omega_{ci} \ll \nu_{in} \ll \nu_{en} \ll \omega_{ce}$$

(After Baumjohann & Treumann, 1996)

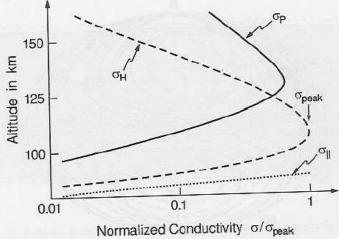
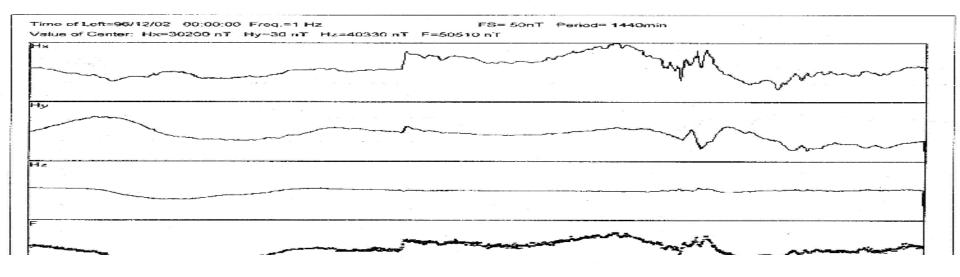
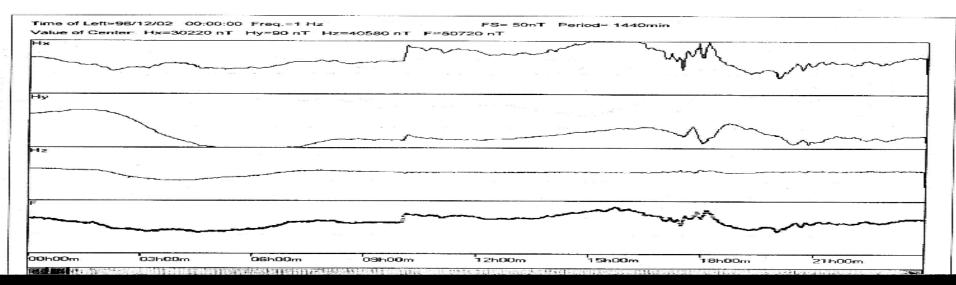


Fig. 4.11. Height profiles of normalized conductivities.

* CME observations at the two near-by stations (< 60km)

• 1996.12.02 09:30 - 10:30(UT) at Icheon, Yongin station





daily variations

OOH

01H

02H 03H 04H

05H

06H

07H

08H

09H 10H 11H

12H

13H

14H 15H 16H

17H

18H 19H

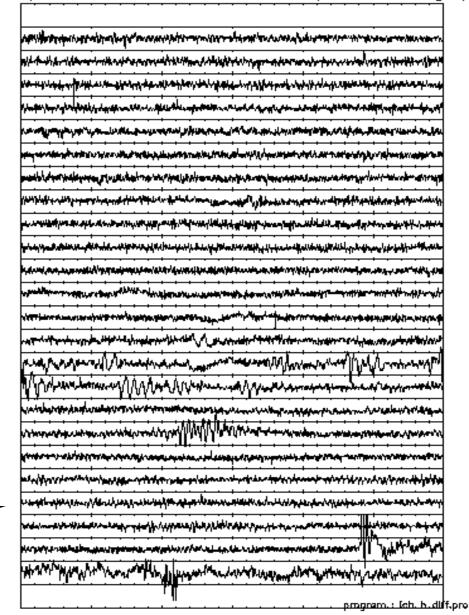
21H 22H

23H

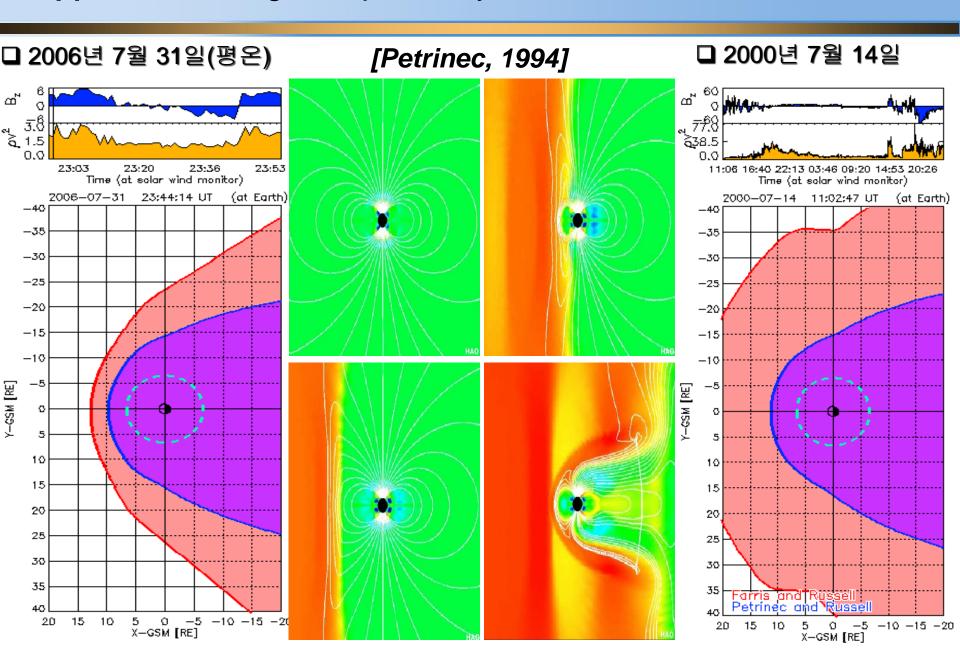
97/11/06 이천 전파연구소 관측자료

Magnetic Field Data of Branch of RRL ICHON (dH/dT-comp) 97/11/06

Compensation Field 30250 nT 0.25 nT/di(4sec averaged)



Application - Magnetospheric dynamics

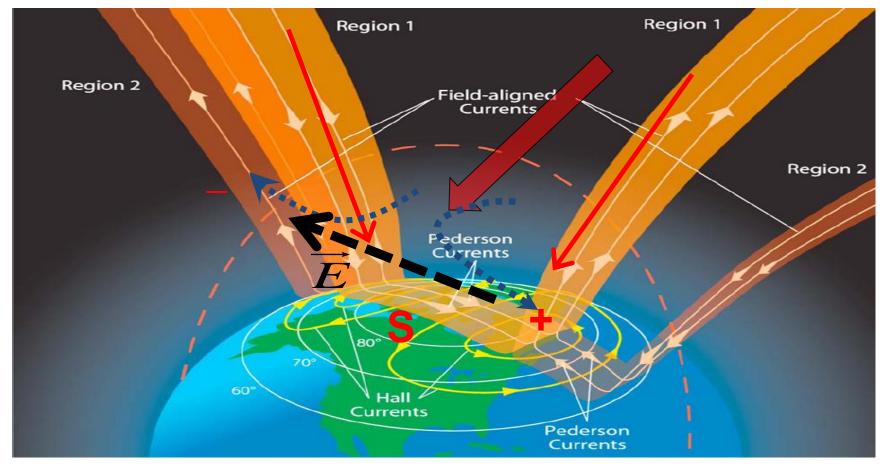


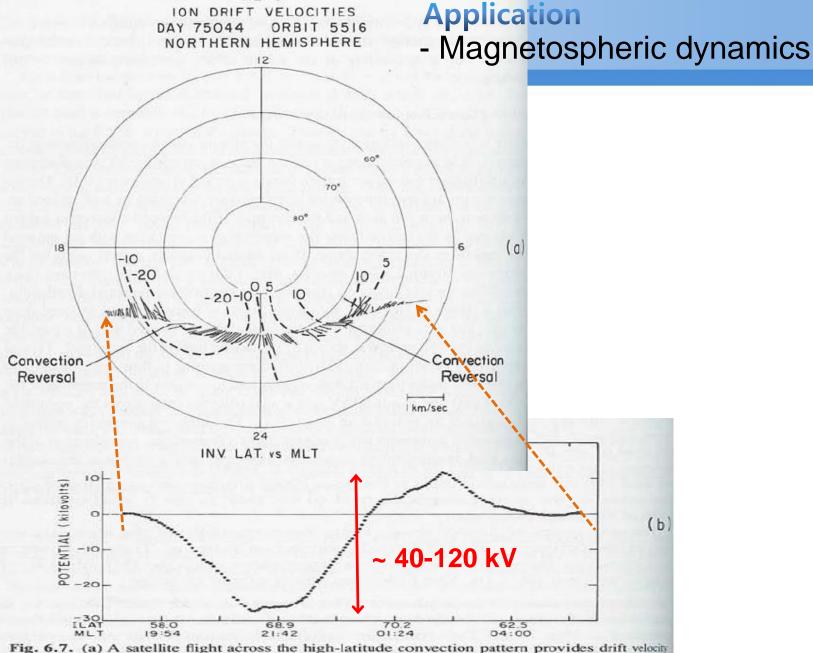
Application - Magnetospheric dynamics

* MHD Dynamo:

$$\vec{E} + \vec{V} \times \vec{B} = 0$$
 (ideal MHD eq.)

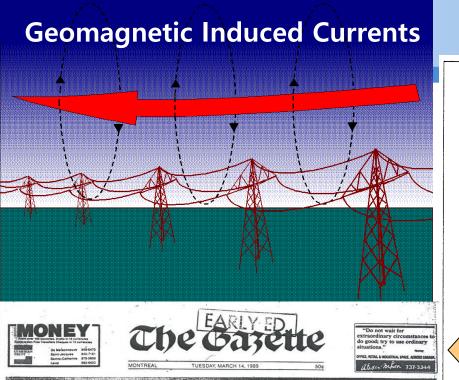
- EM energy generates mechanical energy or
- Mechanical energy generates EM energy





ION DRIFT VELOCITIES

profiles, which are shown along with the inferred convection pattern. (b) The potential distribution resulting from this convective flow pattern shows maxima and minima at the polar cap boundaries and a total potential difference of about 60 kV across the polar cap. [After Heelis and Hanson (1980)] Reproduced with permission of the American Geophysical Union.]



We're sorry Hydro will be kept on short leash: Bourassa for the delay

Hydro blames sun for power failure



It says solar storm overloaded system

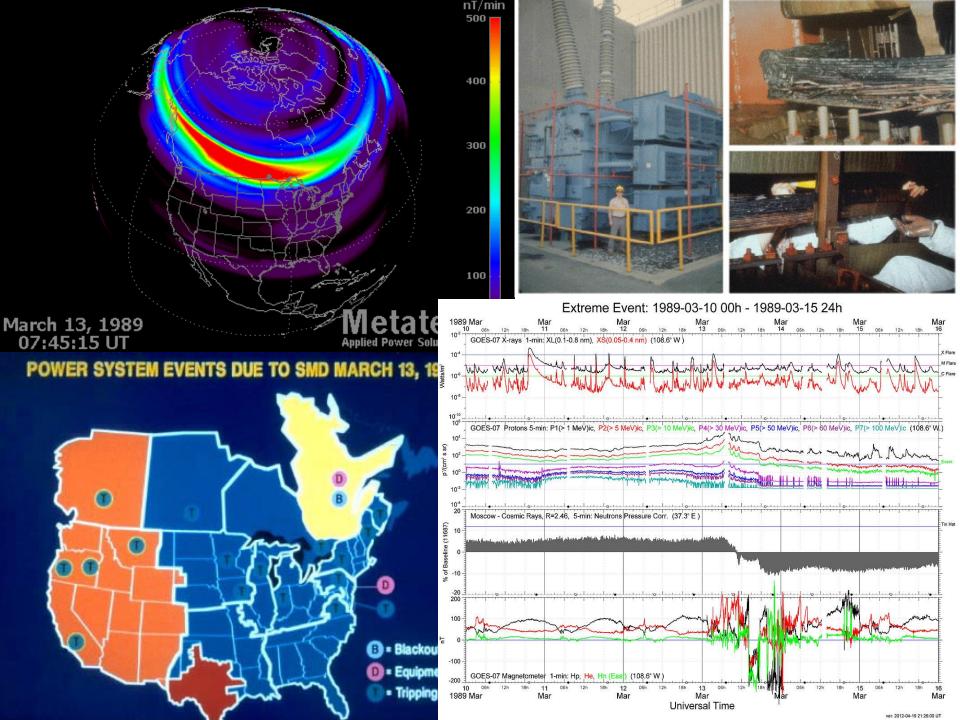
the stars

Officials at the utility are citing a magnetic storm — touched off by an explosion on the sun and

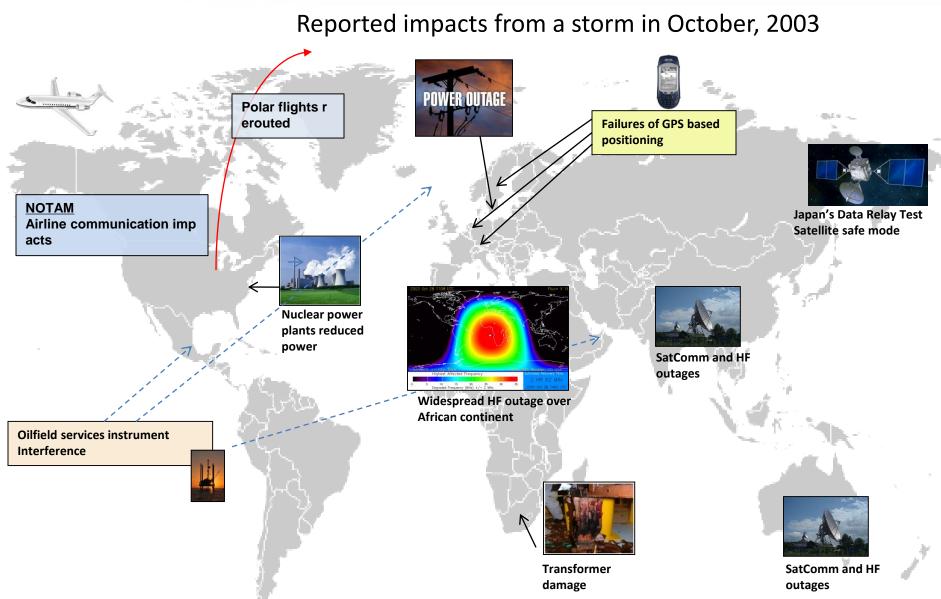
Giant generator



JAMES BAY COMPLEX (15 000 MW) CHURCHILL FALLS LG 2 COMPLEX LG 4 TILLY (5 600 MW) RADISSON DE CHURCH ILL LEMOYNE MONTAGNA IS ALBANEL MANIC - OUTARDES COMPLEX 34% (8 100 MW) ARNAUD 32% MICOUA CH I BOUGAMAU CHAMOUCHOUANE (2)MAN I COUAGAN **=** 26% 400 km SAGUENAY La VERENDRYE LAURENTIDE LEVIS (2) QUEBEC GRAND-APPALACHES AREA BRULE MONTREAL **LEGEND** CHÉNIER AREA DES CANTONS 735 kV Substation **CHATE AUGUAY** DC Converter 1 - DUVERNAY 3 after Boteler, 2011] Series Compensation 3 - CARIGNAN Synchronous Condensers Static Var Compensators N.Y.P.A. Nepool



Space Weather: Global feature





International Space Environment Service

ISES | URSIgram Codes | Reports | Regional Warning Centres | Info | Geo-Calendar

Regional Warning Centres



Australia (Sydney)

Belgium (Brussels)

Brazil (São José dos Campos)

Canada (Ottawa)

China (Beijing)

Czech Republic (Prague)

India (New Delhi)

Japan (Tokyo)



http://www.spaceweather.org/

Summary

- The near-Earth space provides a broad range of temporal and spatial phenomena from single-ptl to MHD, which can be confirmed in *in situ* observations.
- MHD disturbances & waves tend to effectively affect geomagnetic variations in the sense that relatively large-scale EM variations occur with considerable amplitude.
- In terms of spatial and temporal scales over CLIC's criterion, it seems that natural sources from "Space" such as dB~nT over dT~1 sec can be well incorporated (Space Weather should be monitored, though).
- In addition, local conductivity variation should be checked in advance by comparing B(t) at the two "Ground" ends.



