



**UNIVERSITÉ
DE GENÈVE**

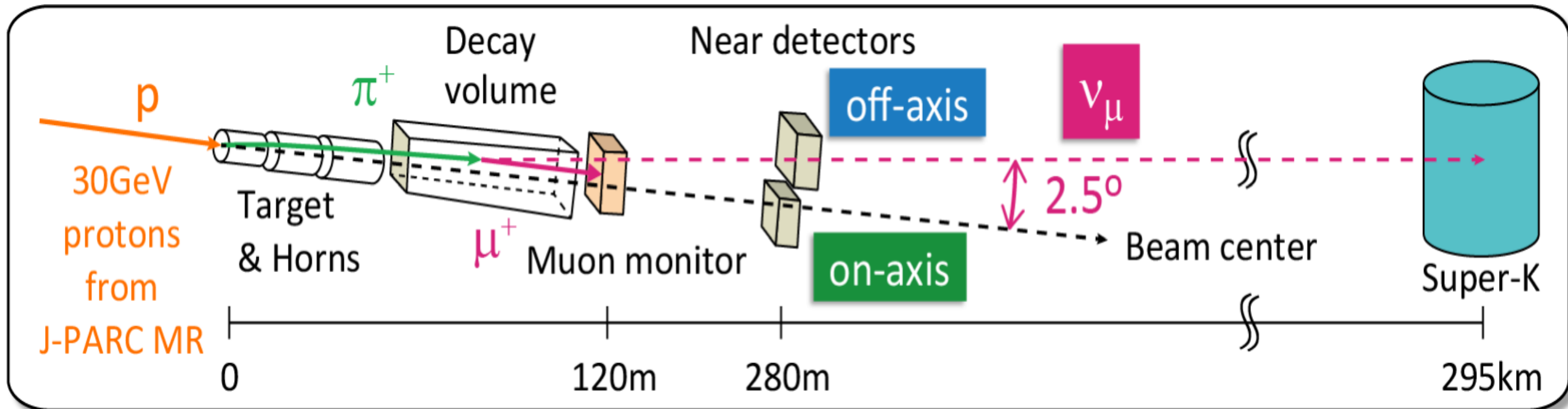
FACULTÉ DES SCIENCES



Overview of the T2K techniques

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CENF-ND Sensitivity Working Group (WG4)

Design principle: the off-axis angle



Near Detector: $N_{ND} \sim \Phi(E_\nu) \sigma(E_\nu) \epsilon_{ND}$

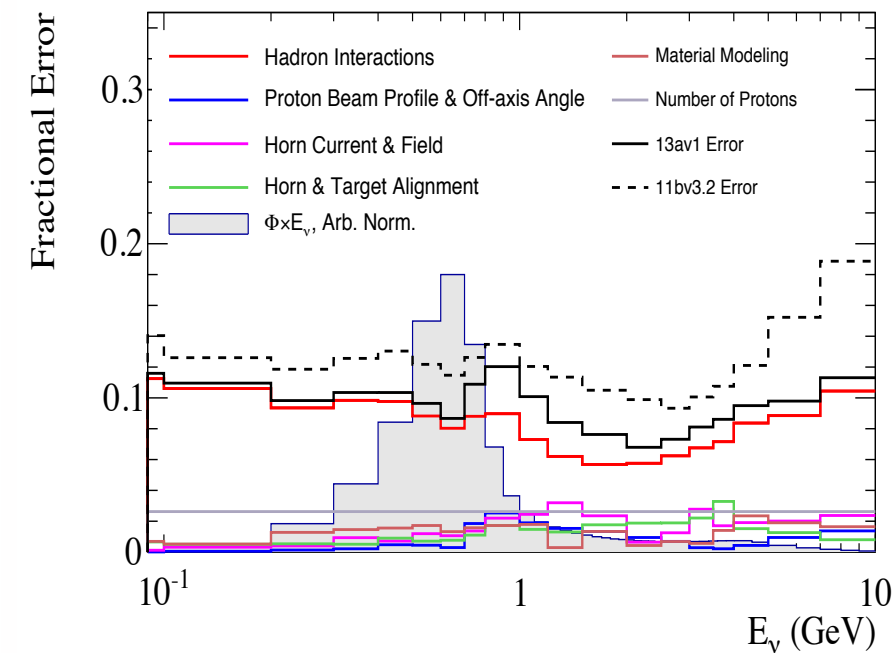
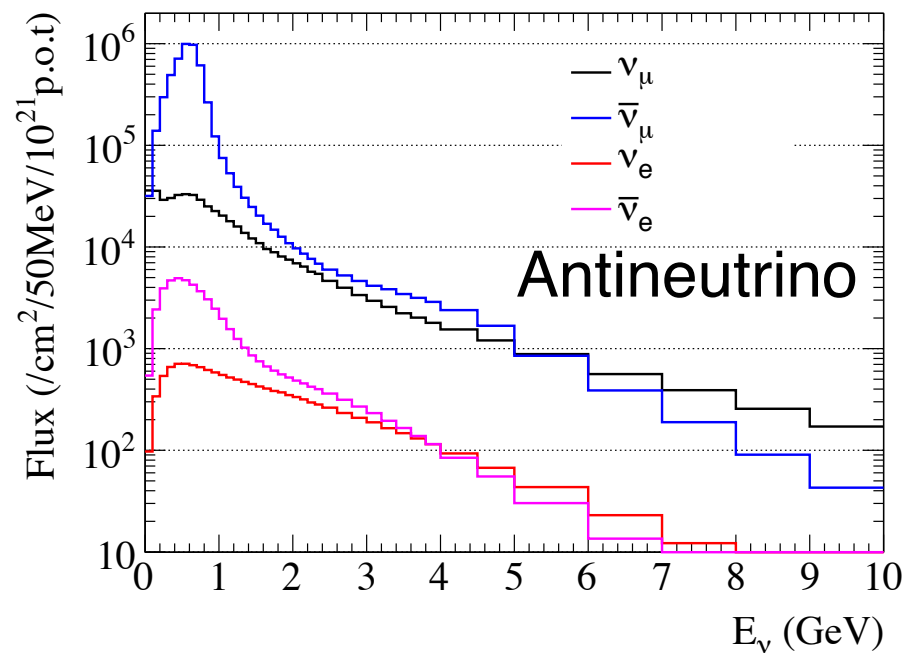
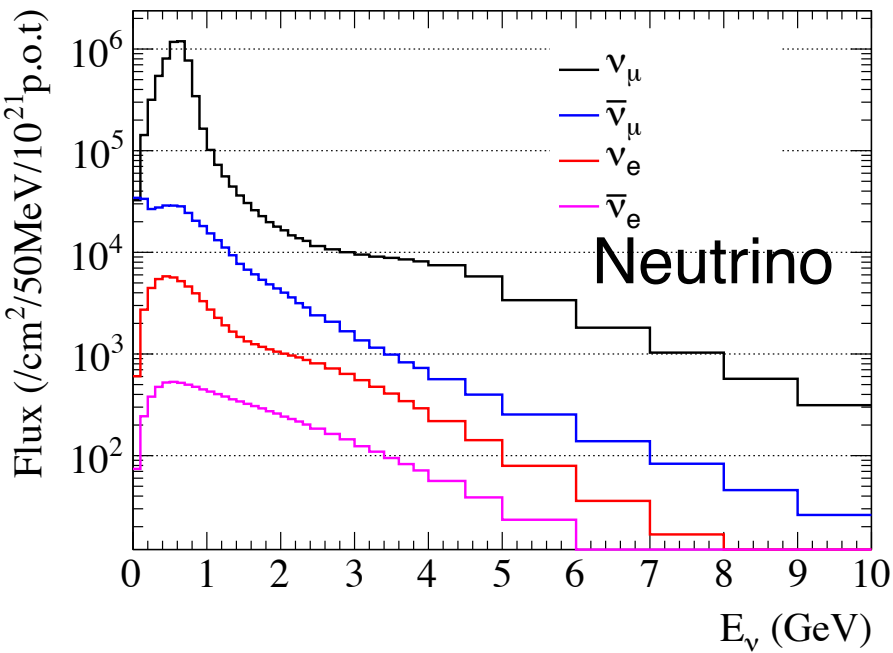
Flux Cross Section Detector Efficiency Oscillation probability

Far Detector: $N_{FD} \sim \Phi(E_\nu) \sigma(E_\nu) \epsilon_{FD} P_{osc}(E_\nu)$

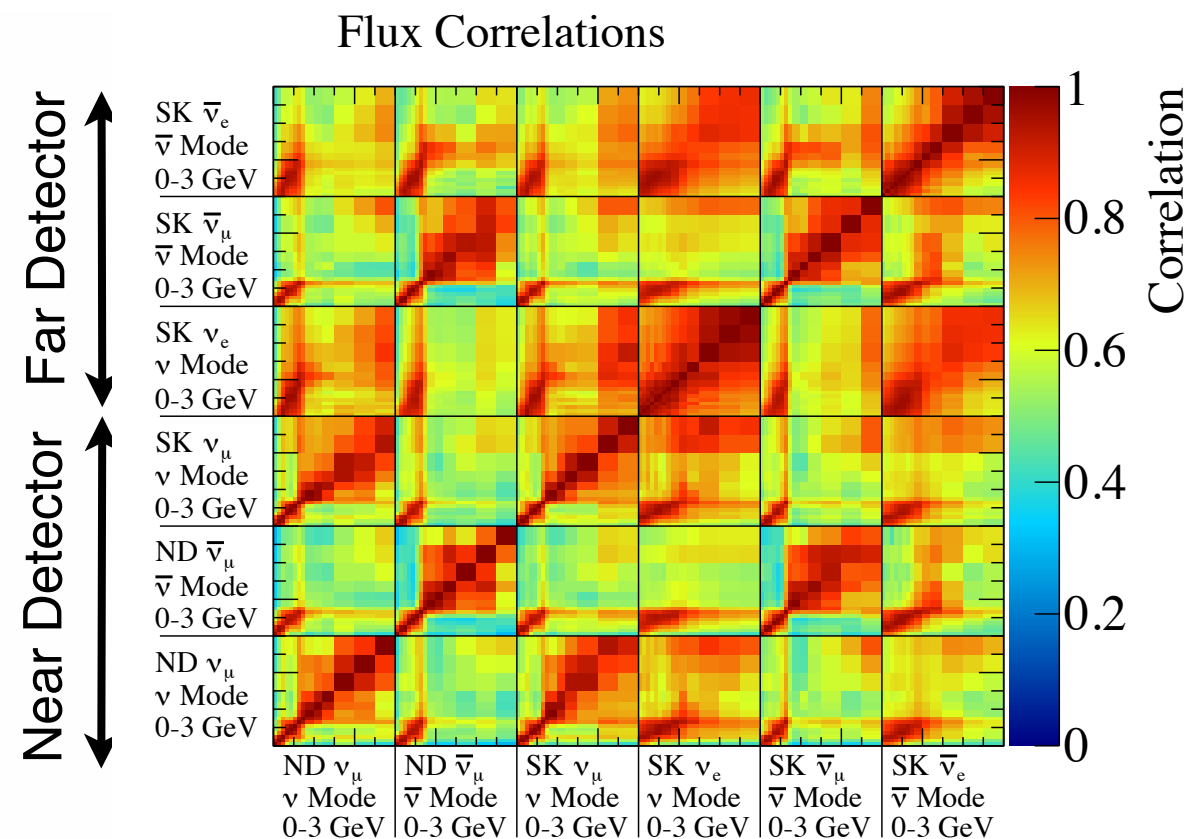
- Systematic errors enter the modeling of flux, cross section and detector
- To reduce errors on the models use the measurements at the Near Detector

Neutrino and antineutrino flux prediction

- Neutrino flux prediction tuned with hadron spectra measured at NA61/SHINE
- Flux systematic uncertainty reduced from $\sim 30\%$ to $\sim 10\%$ (thin target data)

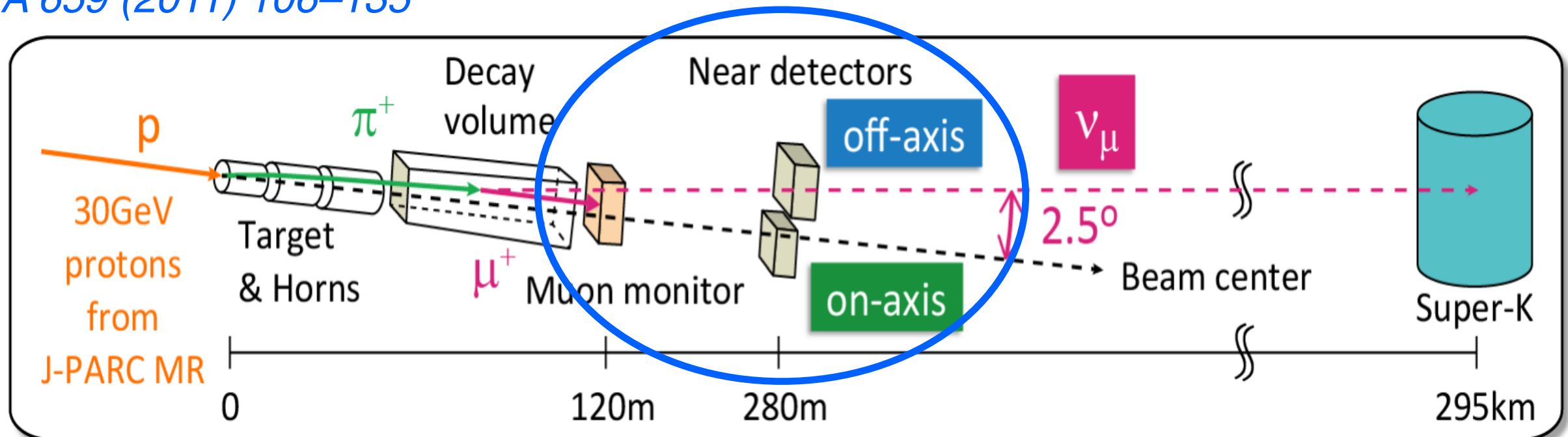


- Less than 1% intrinsic electron (anti)neutrino component at the peak
- $<10\%$ of wrong-sign background (ν_μ in $\bar{\nu}_\mu$ beam)
- Prediction of flux correlations between near / far detector, neutrino / antineutrino beam, ν_μ / ν_e is used

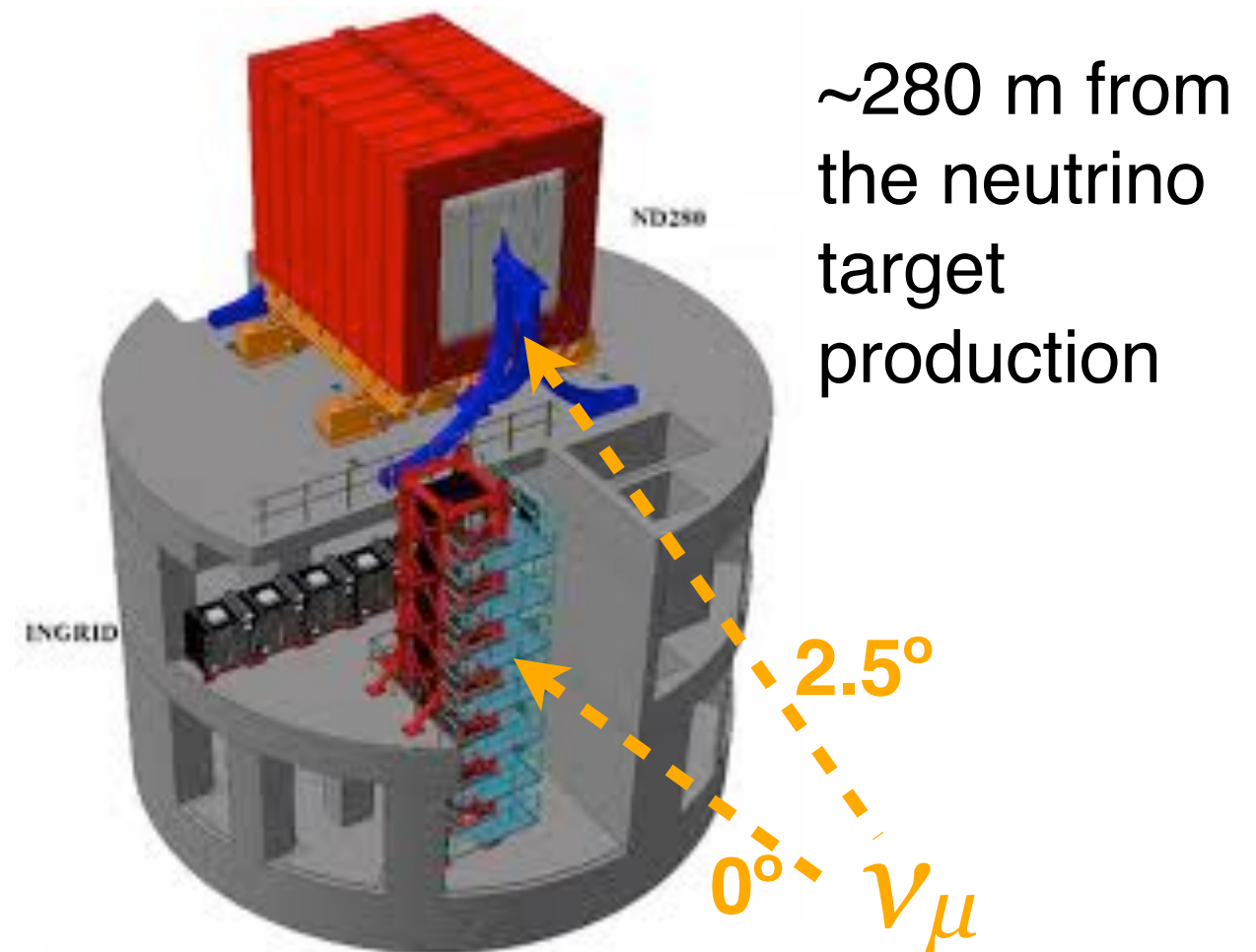


T2K near detector complex

NIM A 659 (2011) 106–135

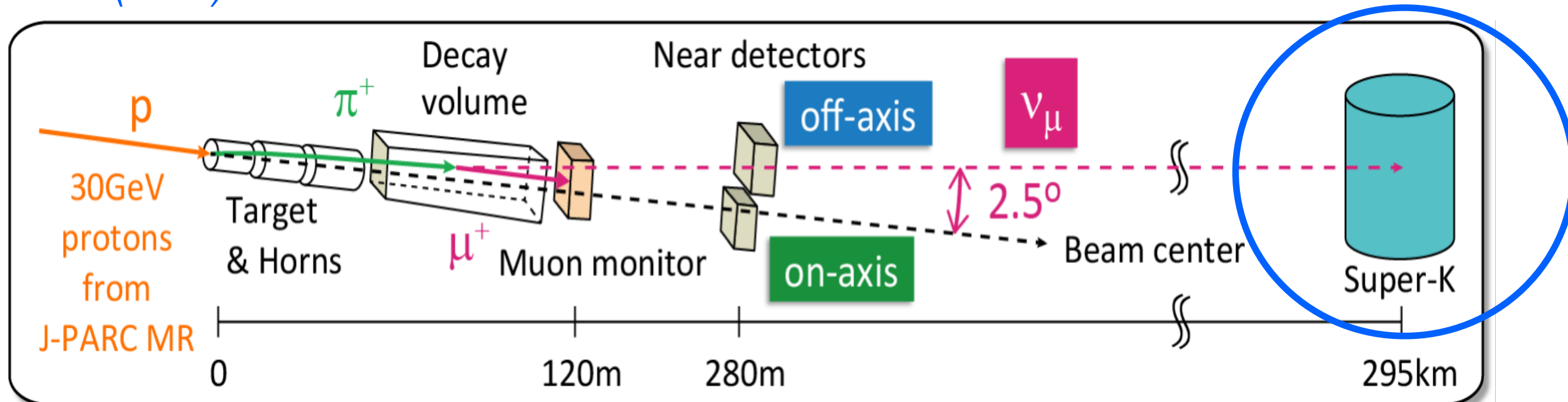


- **Muon monitor:**
 - spill-by-spill monitoring of the beam
- **On-axis detector:**
 - INGRID
 - measure beam intensity / direction
- **Off-axis detector:**
 - 2.5° off-axis magnetized detector
 - precise measurement of neutrino flux and cross section
 - measure wrong-sign background (20-30% ν_μ in $\bar{\nu}_\mu$ beam after interaction)

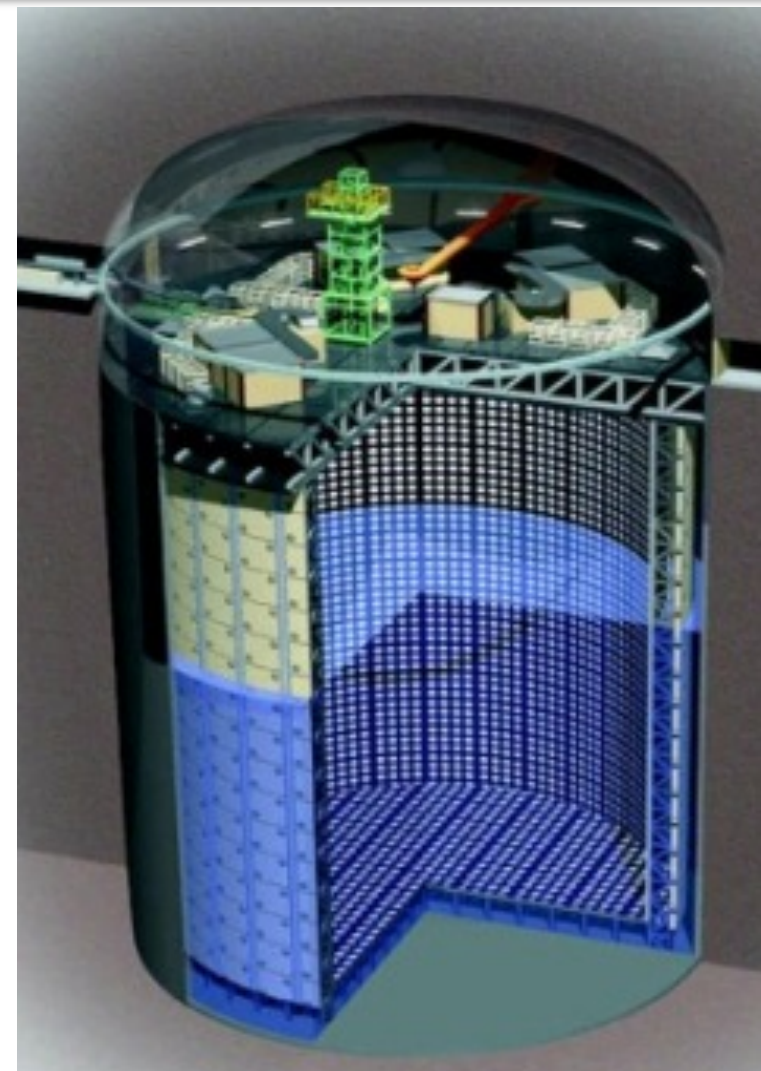


T2K near detector complex

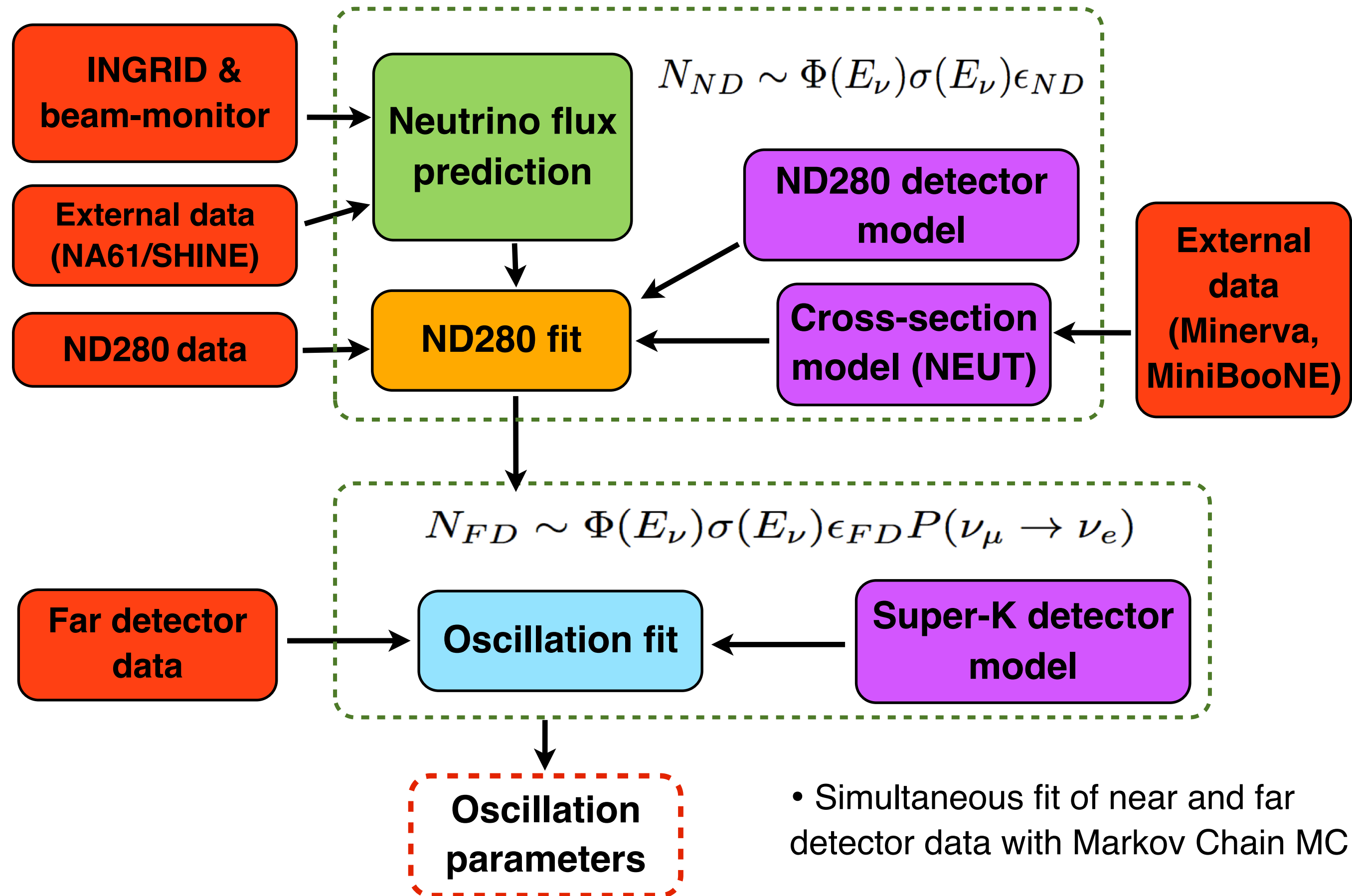
NIM A 659 (2011) 106–135



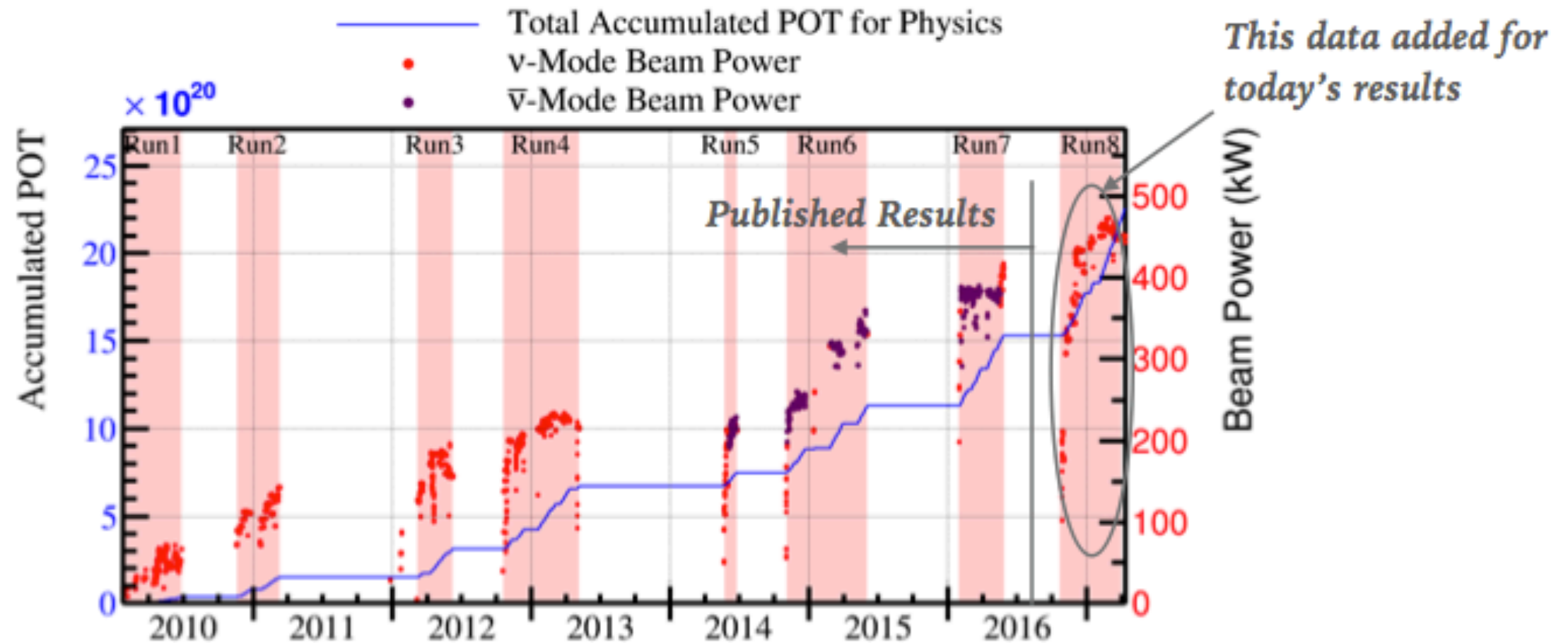
- Located in Mozumi mine
 - 2700 m.w.e overburden
- Water Cherenkov detector (50 kton)
- Fiducial mass 22.5 kton
- Inner detector
 - 11129 20-inch PMTs
- Outer veto detector
 - 1885 8-inch PMTs
 - determine fully-contained events
- T2K beam event: $\pm 500 \mu\text{s}$ window



Strategy for oscillation analyses



T2K data collection



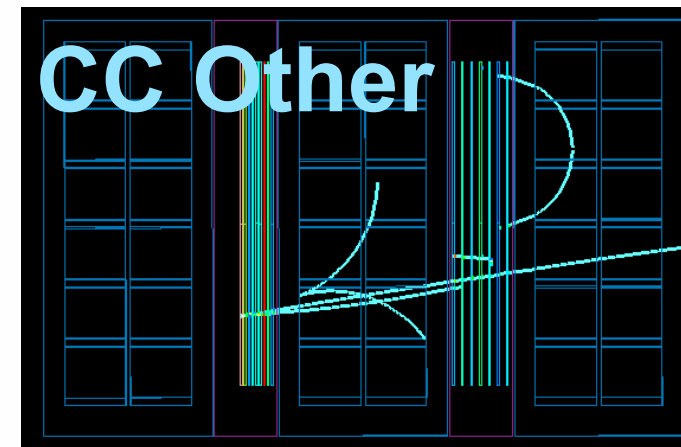
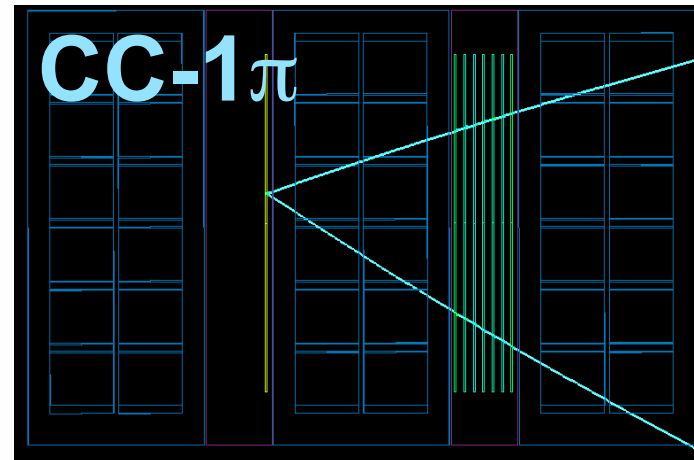
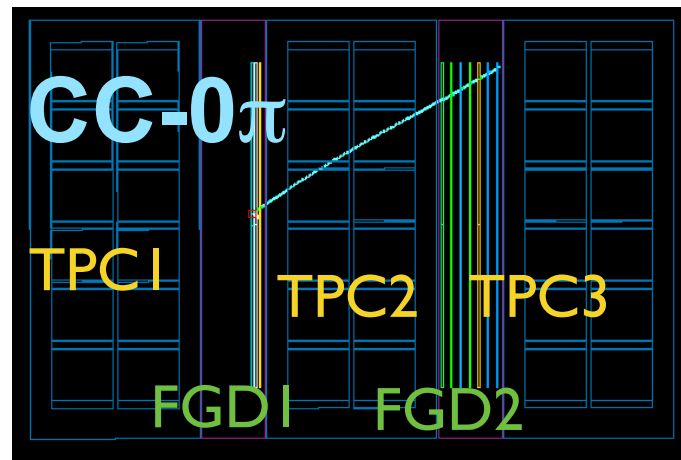
- Accumulated about 29% of the approved T2K protons-on-target (POT)
 - 14.7×10^{20} POT in neutrino mode
 - 7.6×10^{20} POT in antineutrino mode
- Phys. Rev. Lett. 118 (2017) no.15, 151801 - PRL Editor's Suggestion
- arXiv:1707.01048
- Stable operation with 470 kW beam power
- New results presented in August at KEK laboratory

<https://kds.kek.jp/indico/event/25337/material/slides/0.pdf>

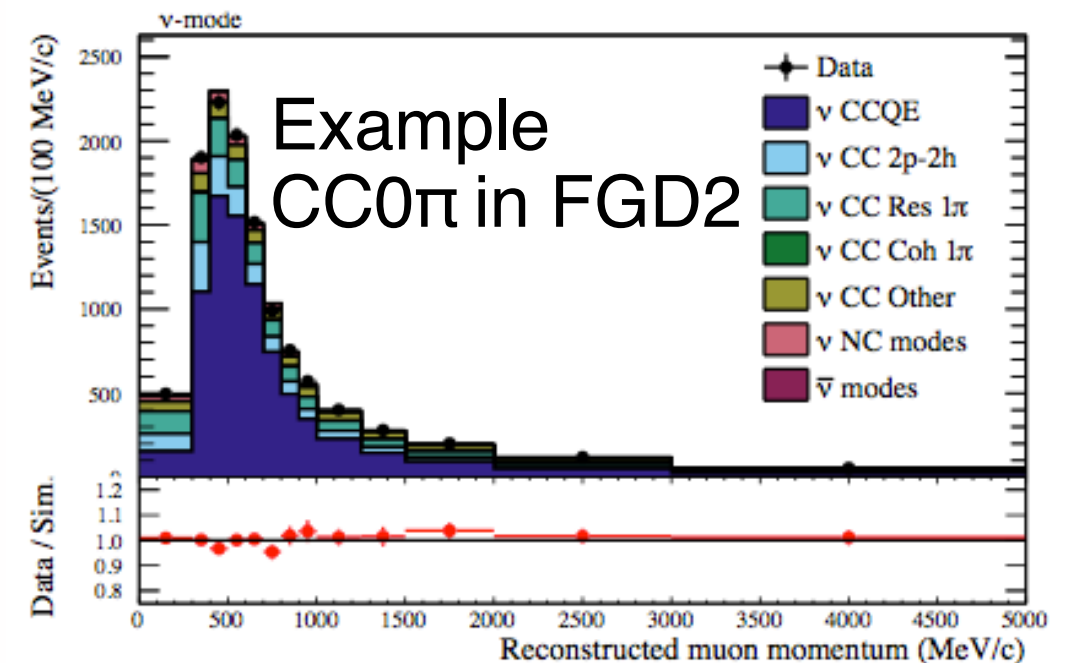
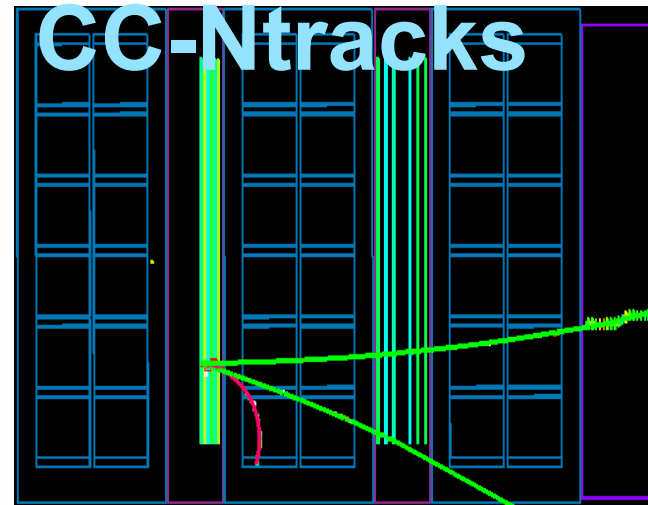
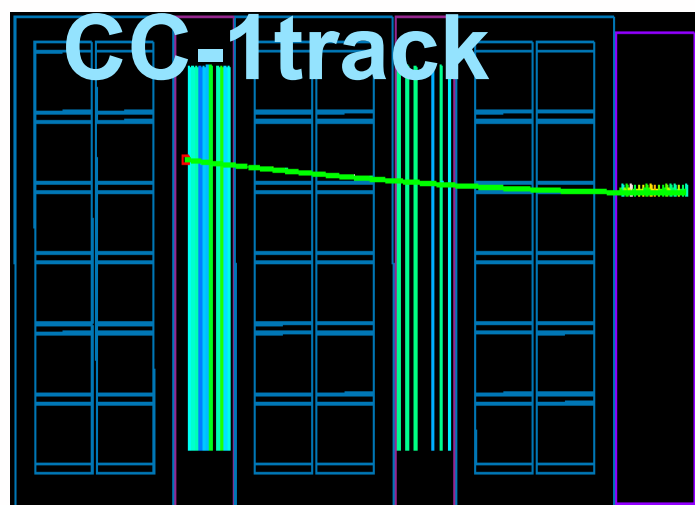
Near Detector Fit: the samples

- Antineutrino samples: 1 μ^+ candidates (CC-1track) + CC-Ntracks
- Neutrino samples: 1 μ^- candidates (CC-0 π) + 1 π^+ (CC-1 π) + CC other
- Simultaneous analysis of neutrino and antineutrino data (μ momentum/angle)
- Additional samples to measure wrong-sign background (ν_μ in $\bar{\nu}_\mu$ -bar)

Neutrino samples



Antineutrino samples

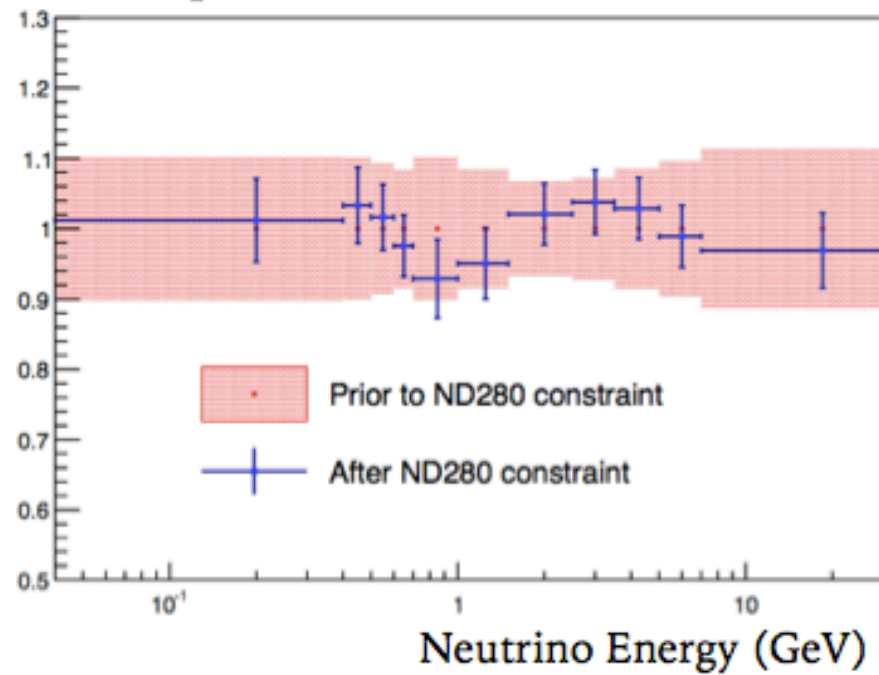


- Maximum binned likelihood fit
- Fit parameters are constrained by a gaussian penalty term (except a few)

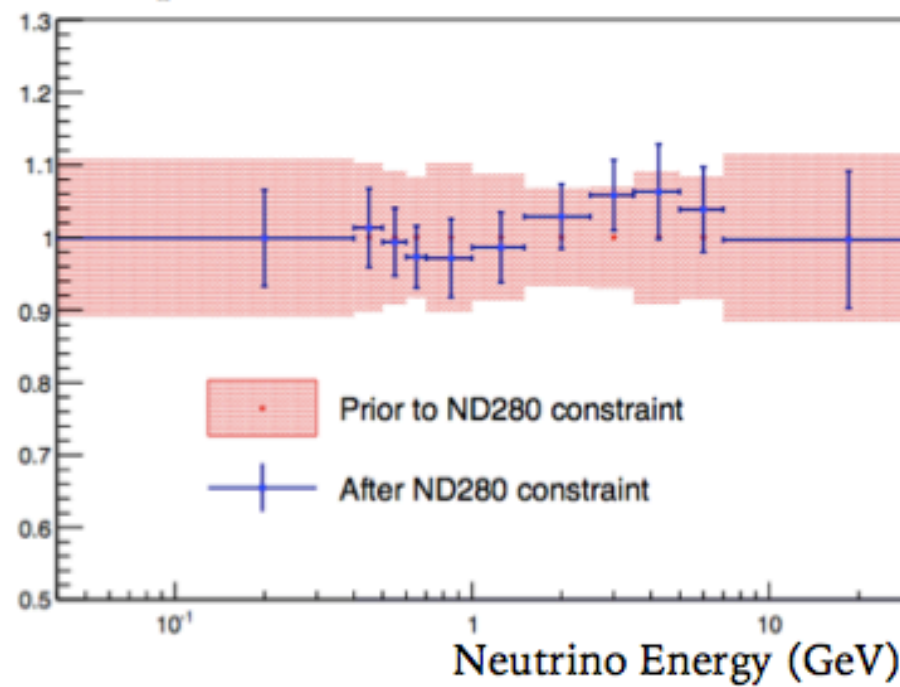
T2K Preliminary

Near Detector Fit: flux and cross-section uncertainties

Super-K Neutrino Mode Flux



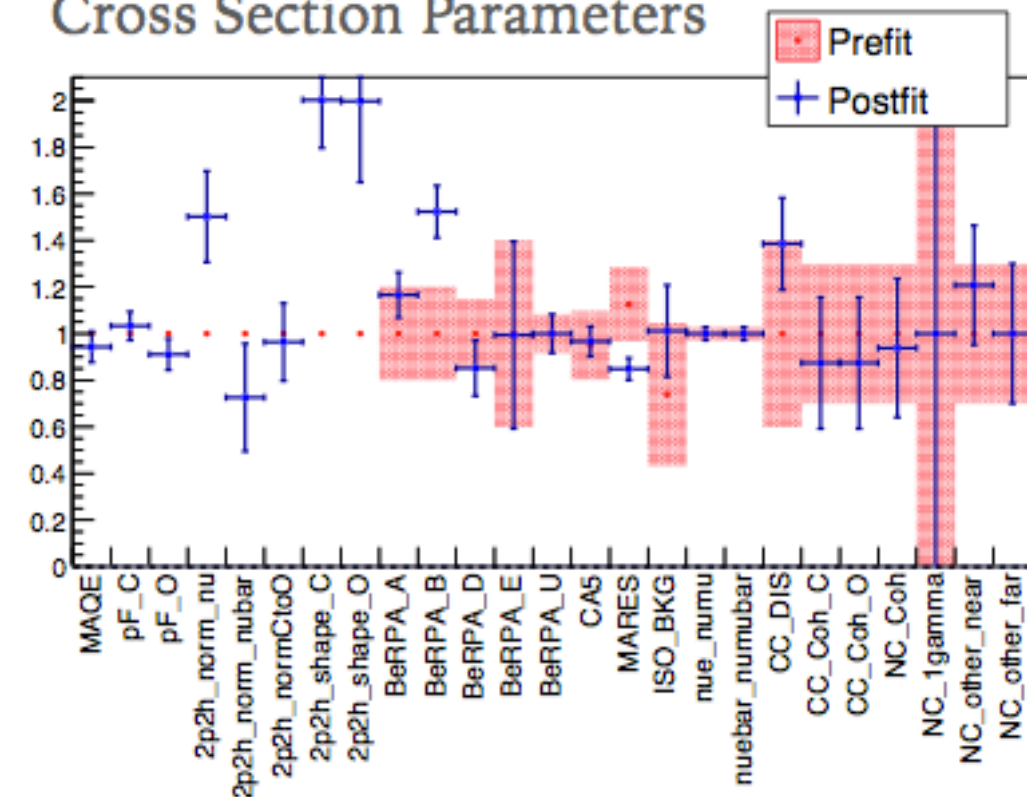
Super-K Antineutrino Mode Flux



Measure neutrino flux and cross section at ND280

T2K Preliminary

Cross Section Parameters



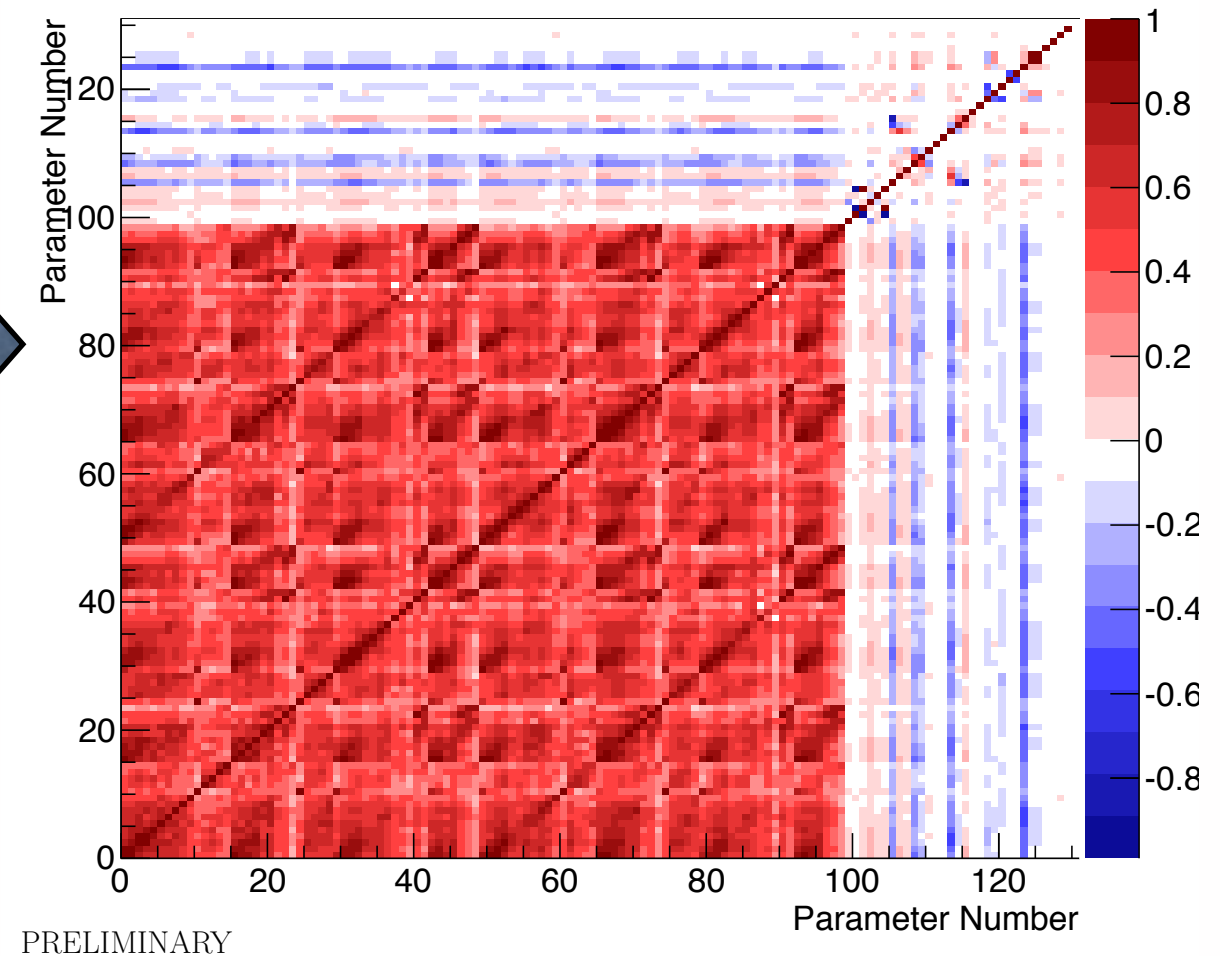
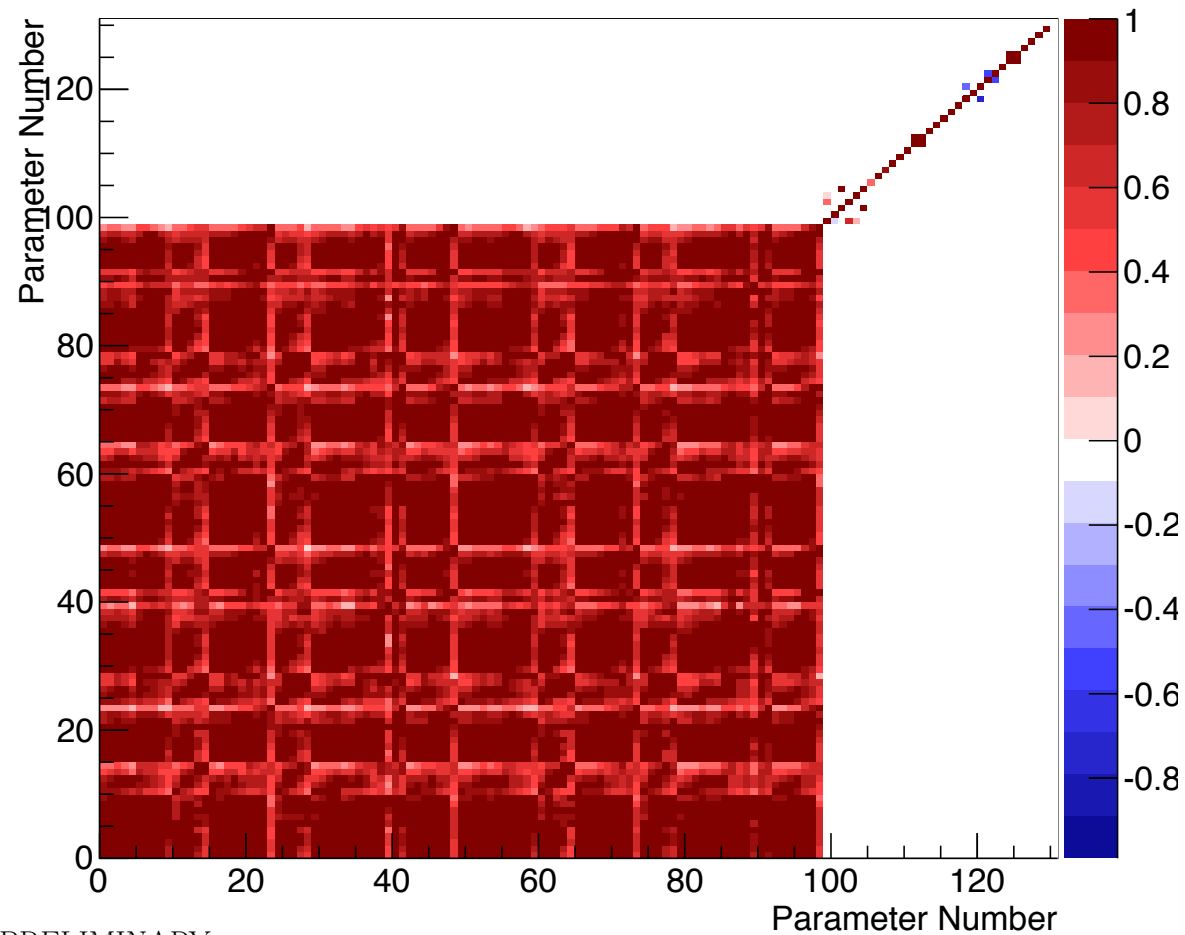
- Different fit parameters as a function of true, reco energy, flavor and interaction mode
 - normalization parameters (e.g. flux, xsec)
 - modelled with non-linear response functions (e.g. MAQE, 2p2h, RPA, etc...)
- The fit reproduces well data: p-value=0.47
- Best-fit parameter values and covariance matrix are obtained and used to constrain systematics in the oscillation measurement

Near Detector Fit: flux and cross-section uncertainties

T2K Preliminary

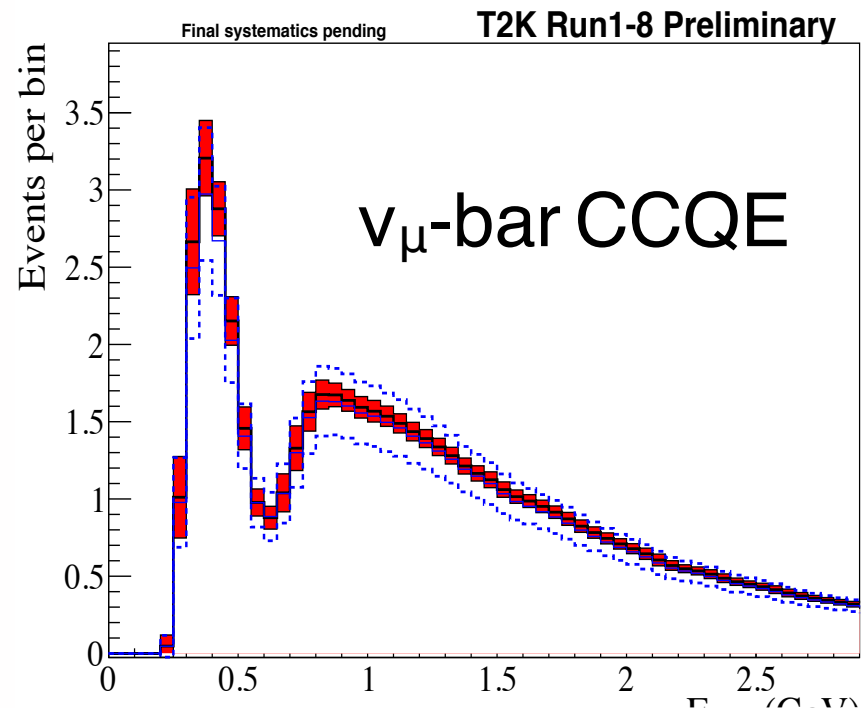
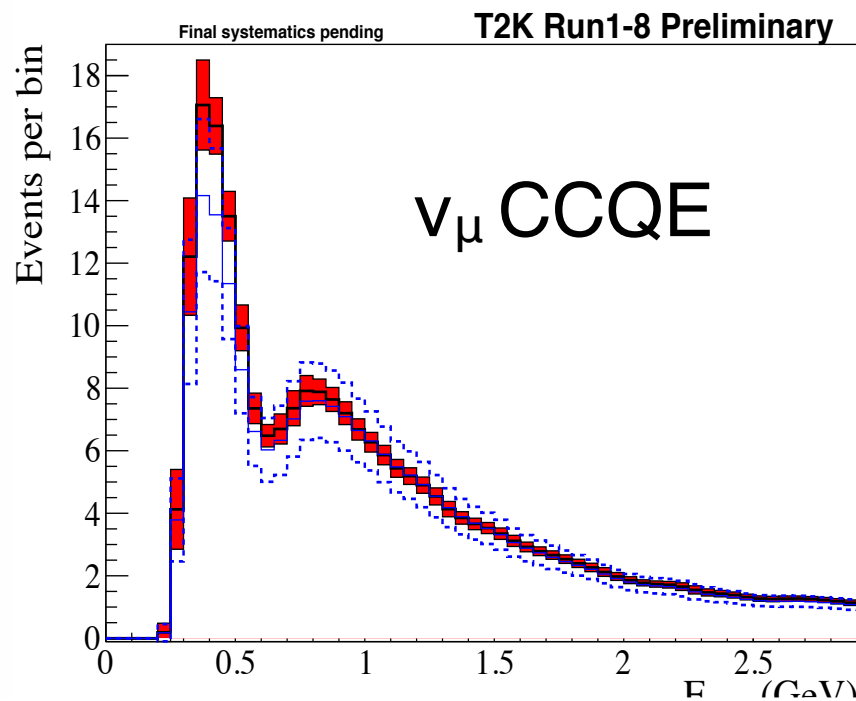
Prefit Correlation Matrix

Postfit Correlation Matrix

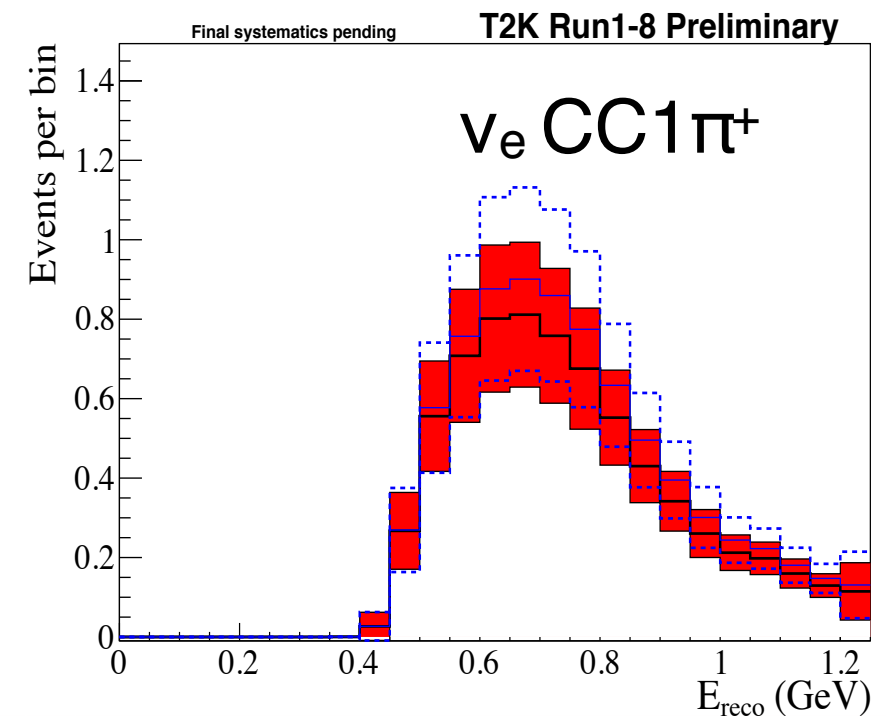
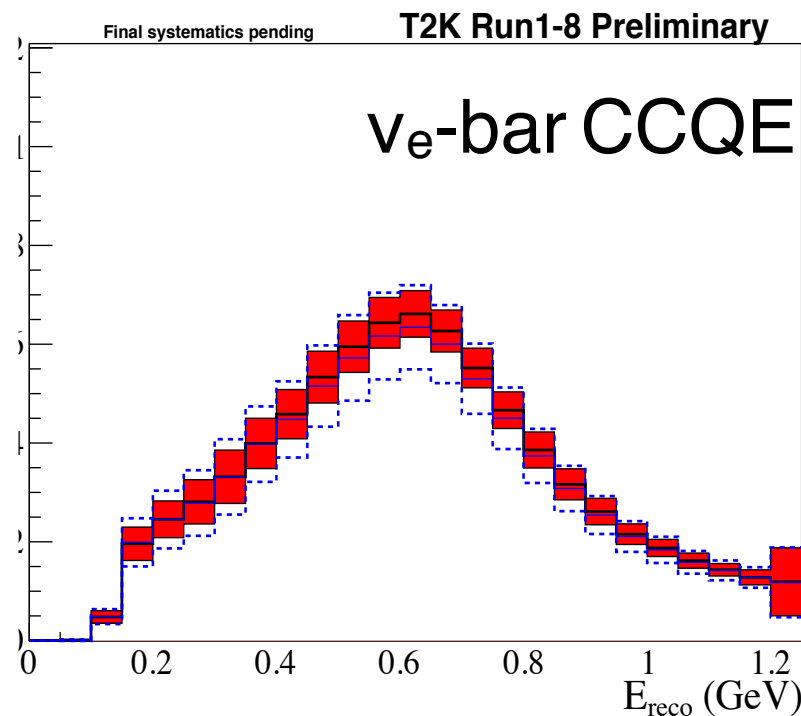
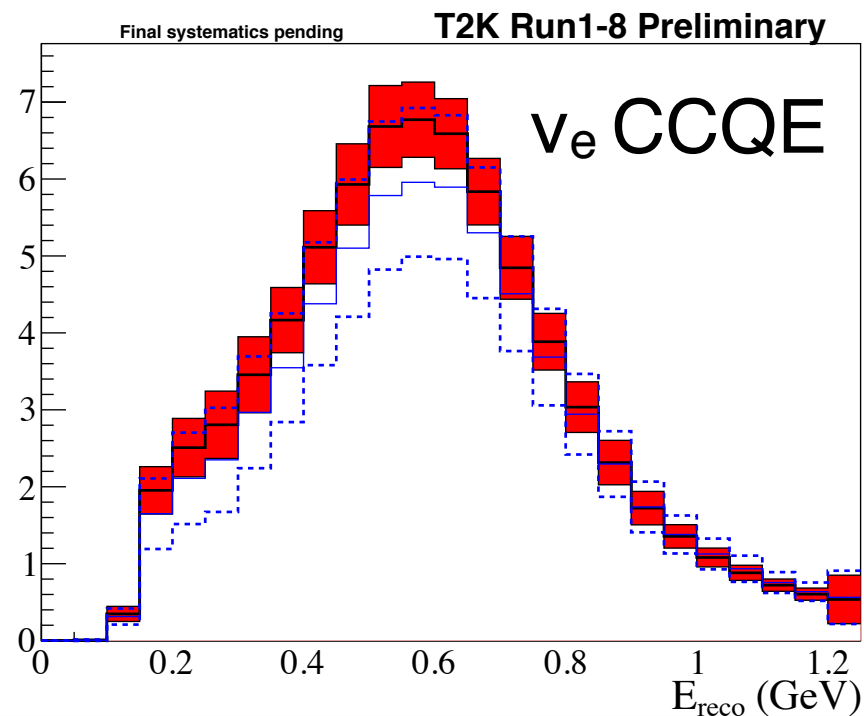


- Anti-correlations between neutrino flux and cross-section parameters
- The covariance matrix will be used to constrain the flux and cross-section systematic parameters in the neutrino oscillation analysis

Joint neutrino and antineutrino analysis



- Costrained with ND280 data
- Not constrained by ND280 data



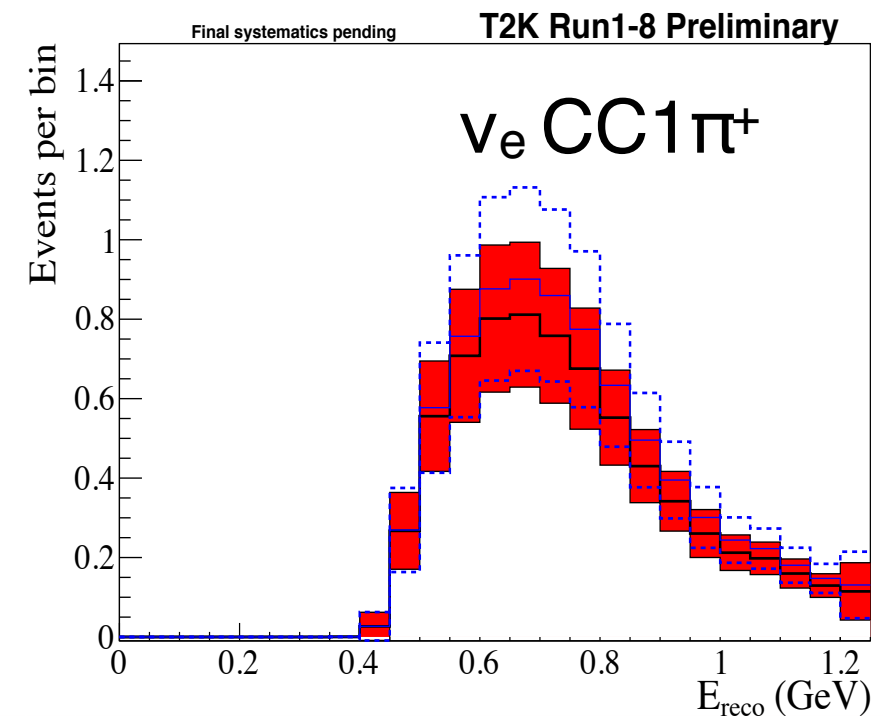
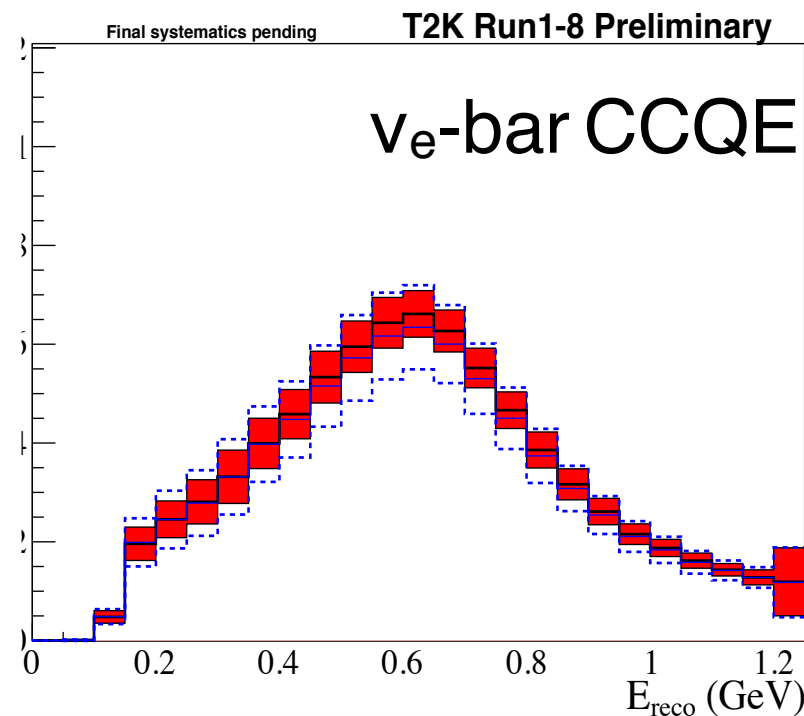
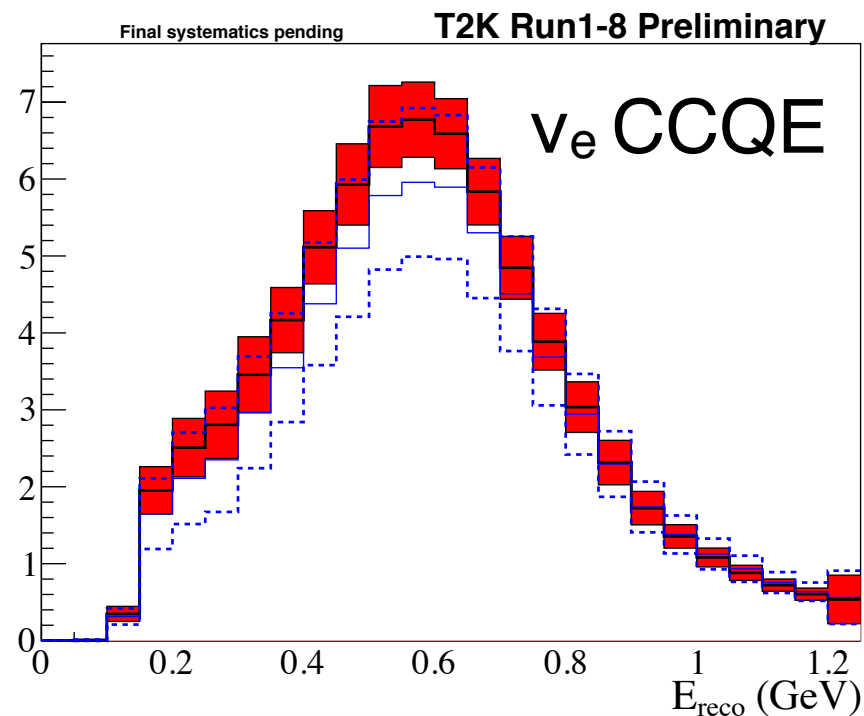
- Impact of systematic uncertainties that can be constrained by the ND280 data on the total Super-K # of events from $\sim 13\%$ to $\sim 3\%$ after the fit
- Statistical uncertainties still dominant (more details in backup)

Joint neutrino and antineutrino analysis

| Error Source | 1Rmu | | 1Re | | | |
|--|------|-----|-----|-----|-------------|---------|
| | FHC | RHC | FHC | RHC | FHC 1 d. e. | FHC/RHC |
| SK Detector | 1.9 | 1.6 | 3.0 | 4.2 | 16.5 | 1.6 |
| SK FSI+SI+PN | 2.2 | 2.0 | 2.9 | 2.5 | 11.3 | 1.6 |
| SK Detector+FSI+SI+PN | 2.9 | 2.5 | 4.2 | 4.8 | 19.2 | 2.1 |
| ND280 const. flux & xsec | 3.3 | 2.7 | 3.2 | 2.9 | 4.1 | 2.5 |
| $\sigma(\nu_e)/\sigma(\nu_\mu), \sigma(\bar{\nu}_e)/\sigma(\bar{\nu}_\mu)$ | 0.0 | 0.0 | 2.6 | 1.5 | 2.6 | 3.1 |
| NC1 γ | 0.0 | 0.0 | 1.1 | 2.6 | 0.3 | 1.5 |
| NC Other | 0.3 | 0.3 | 0.1 | 0.3 | 1.0 | 0.2 |
| Syst. Total | 4.4 | 3.8 | 6.3 | 6.4 | 19.6 | 4.7 |

- Costrained with ND280 data

- Not constrained by ND280 data

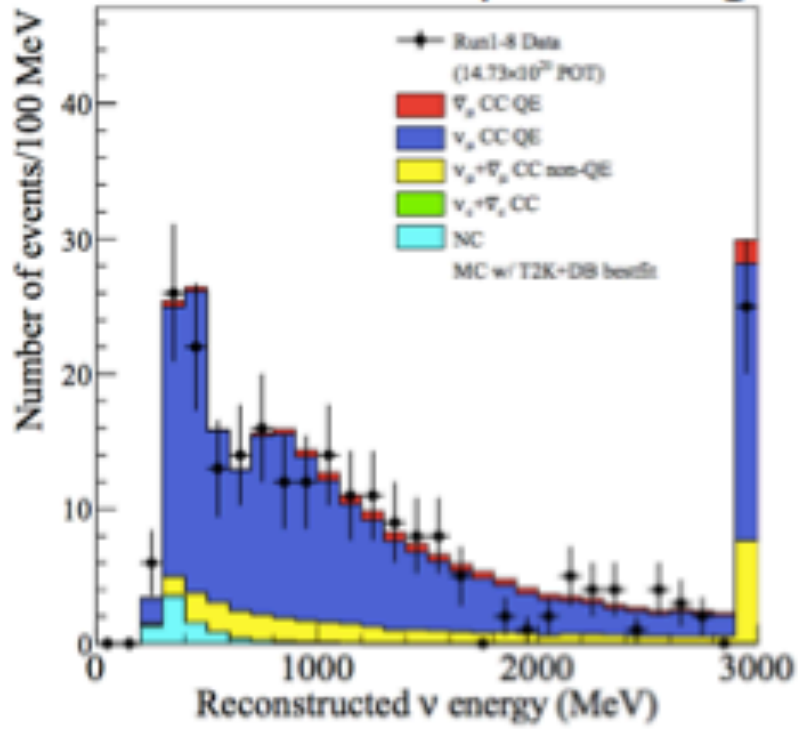


- Impact of systematic uncertainties that can be constrained by the ND280 data on the total Super-K # of events from $\sim 13\%$ to $\sim 3\%$ after the fit
- Statistical uncertainties still dominant (more details in backup)

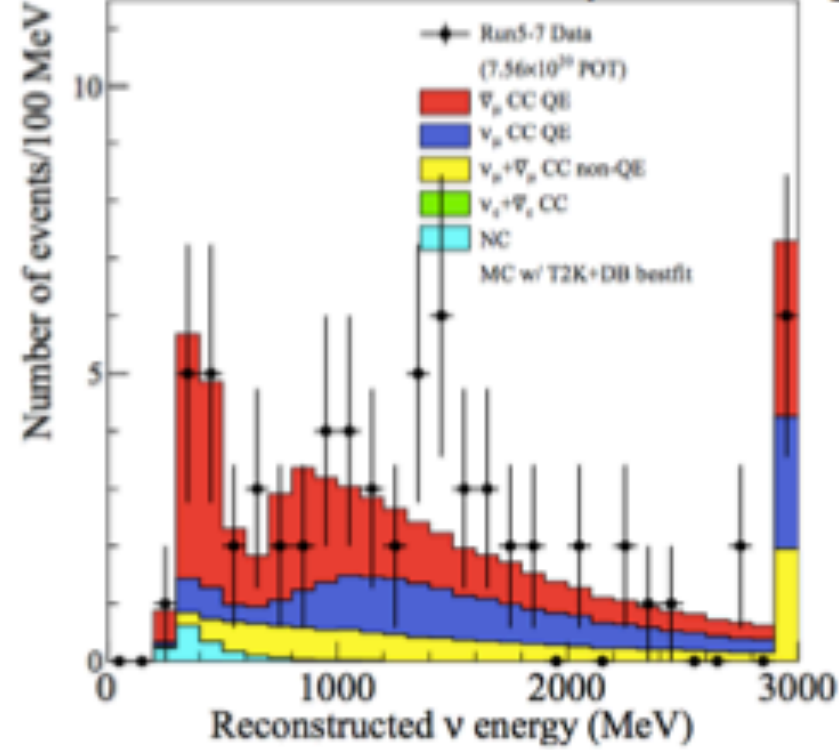
Joint neutrino and antineutrino analysis

- Joint fit of all 5 samples at the far detector

Neutrino CCQE 1 μ -like ring



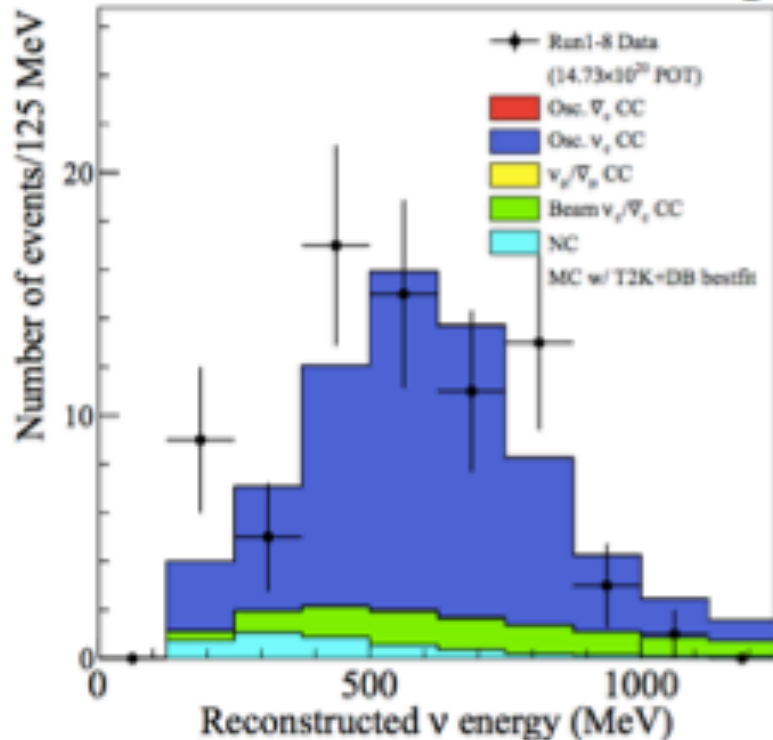
Antineutrino CCQE 1 μ -like ring



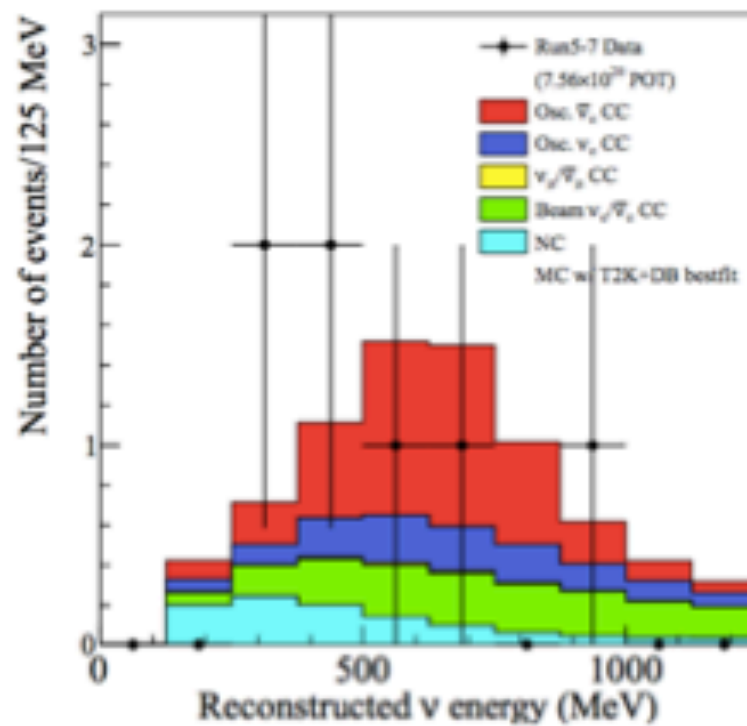
Observed spectra

T2K Preliminary

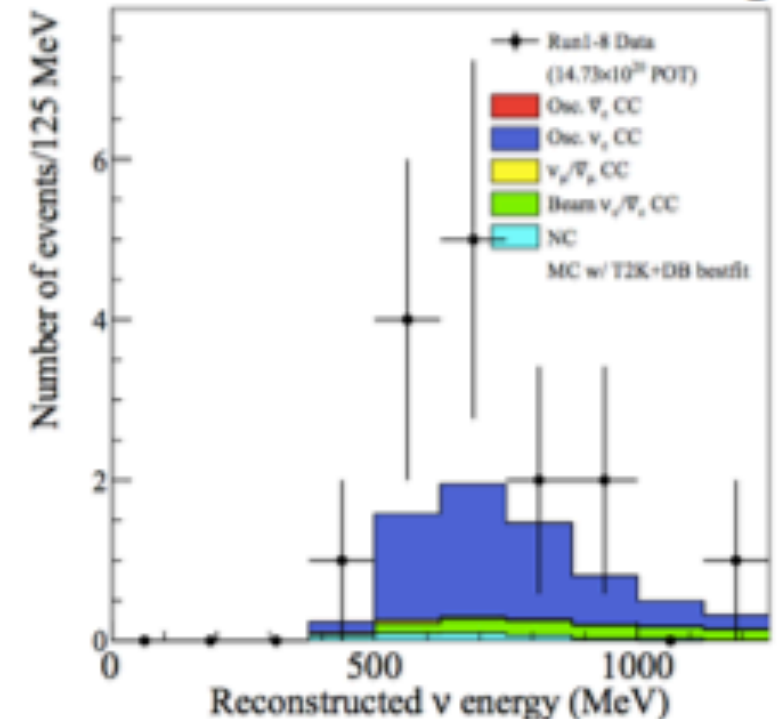
Neutrino CCQE 1 e -like ring



Antineutrino CCQE 1 e -like ring



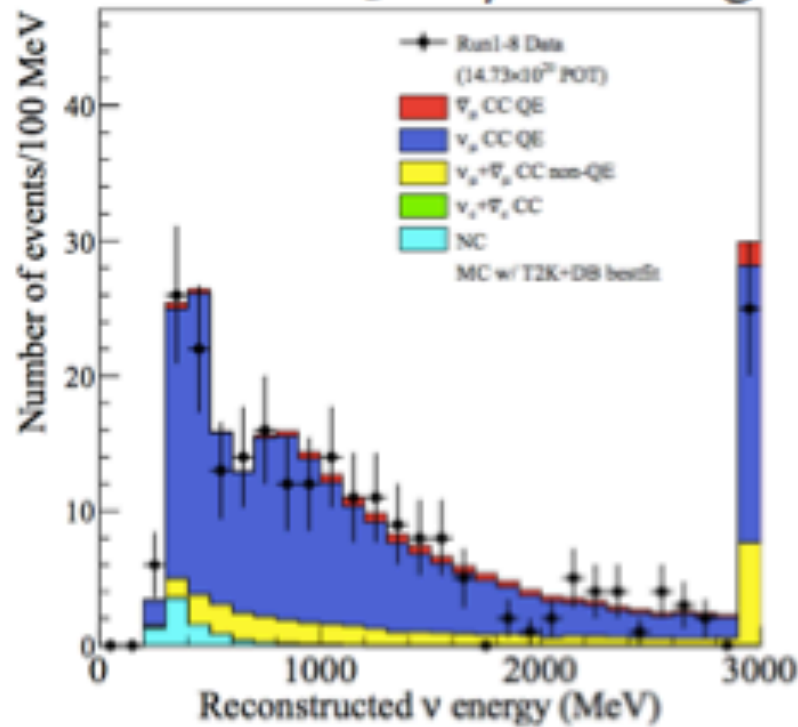
Neutrino CC1 π 1 e -like ring



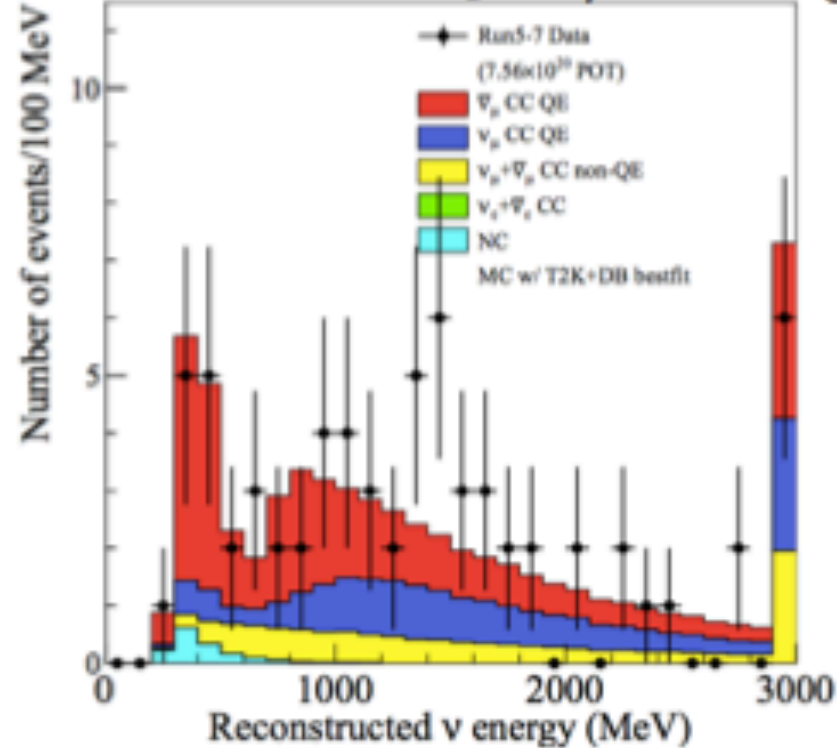
Joint neutrino and antineutrino analysis

- Joint fit of all 5 samples at the far detector

Neutrino CCQE 1 μ -like ring



Antineutrino CCQE 1 μ -like ring



Observed spectra

T2K Preliminary

- Marginalize all the systematic parameters and oscillation parameters “not of interest”

- $\pi(\mathbf{a})$ is the prior used to marginalize

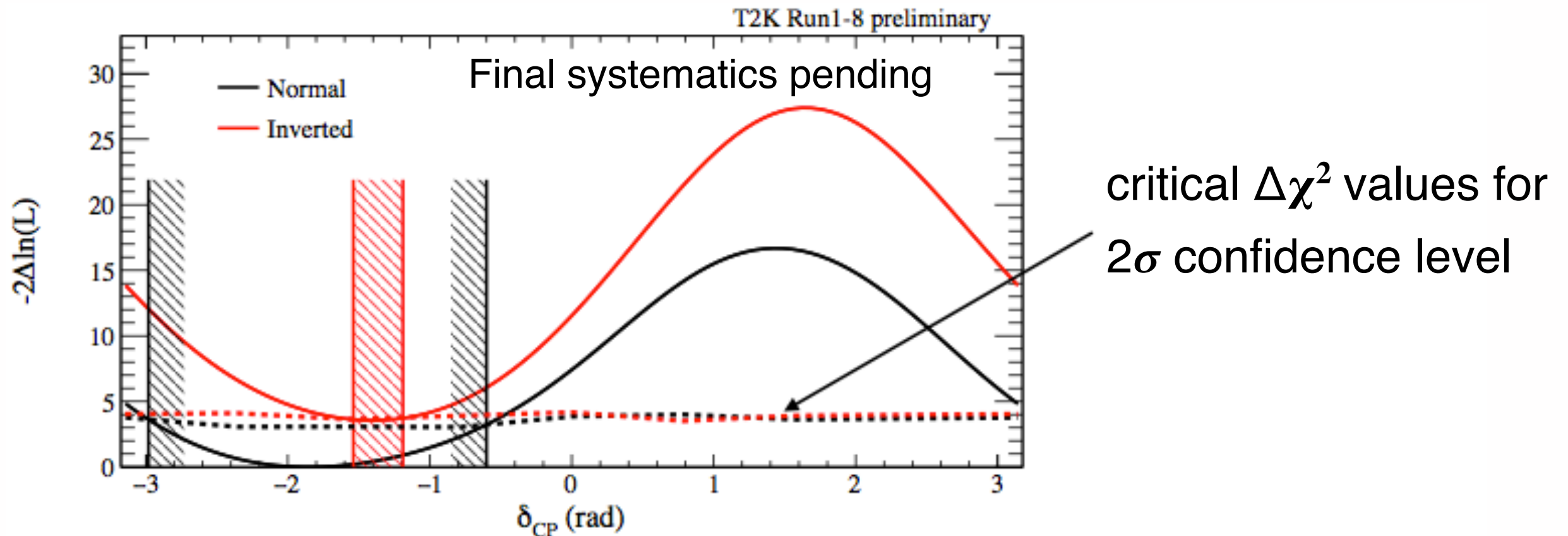
$$\lambda_{marg}(\vec{\theta}) = \int_A \lambda(\vec{\theta}; \mathbf{a}) \pi(\mathbf{a}) d\mathbf{a} = \frac{1}{n} \sum_{i=1}^n \lambda(\vec{\theta}; \mathbf{a}_i)$$

- ND fit covariance matrix for flux and xsec
- Covariance matrix evaluated with SuperK atmospheric data for detector systematics
- PDG or flat priors for neutrino oscillation parameters (reactors for $\sin^2 2\theta_{13}$)

Results

- Feldman-Cousins to get the right coverage

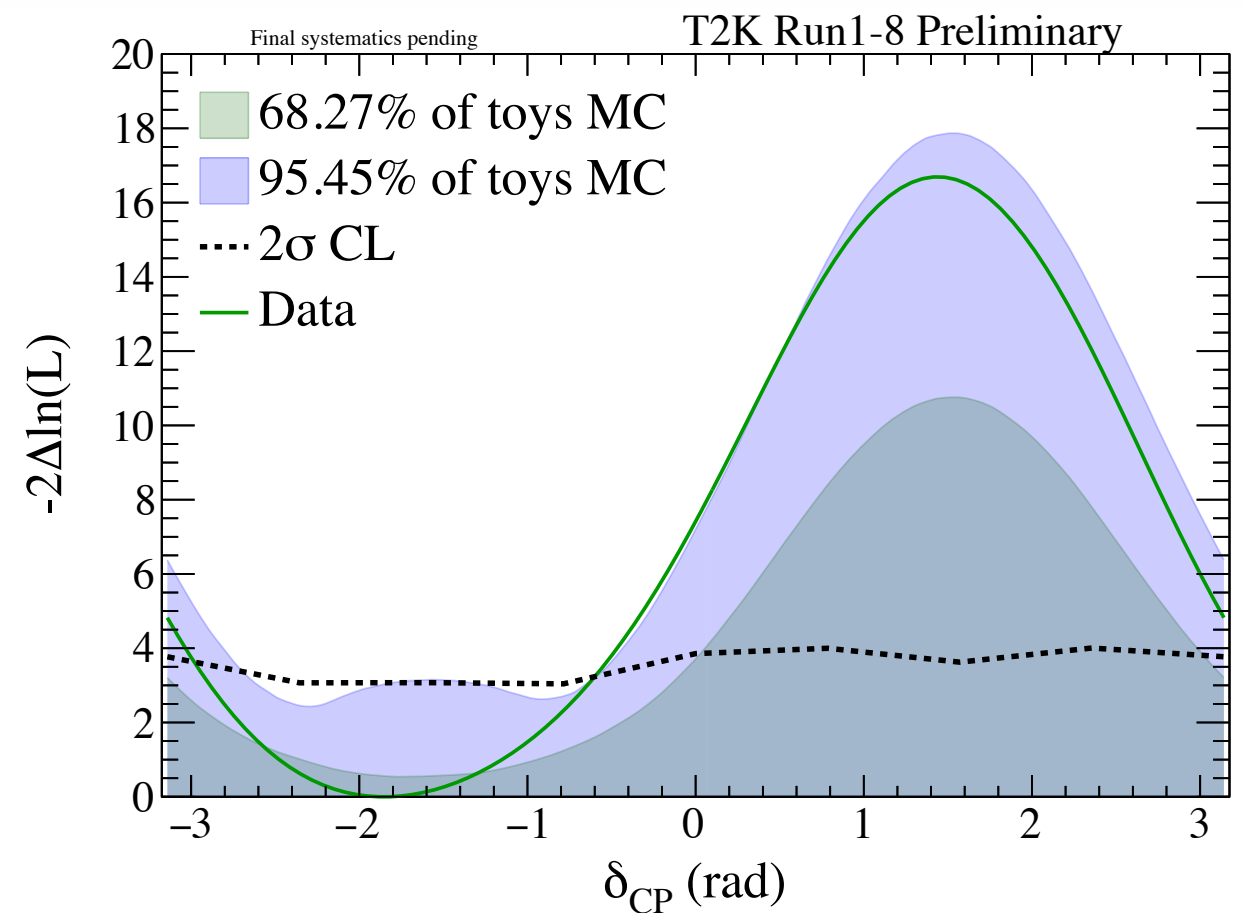
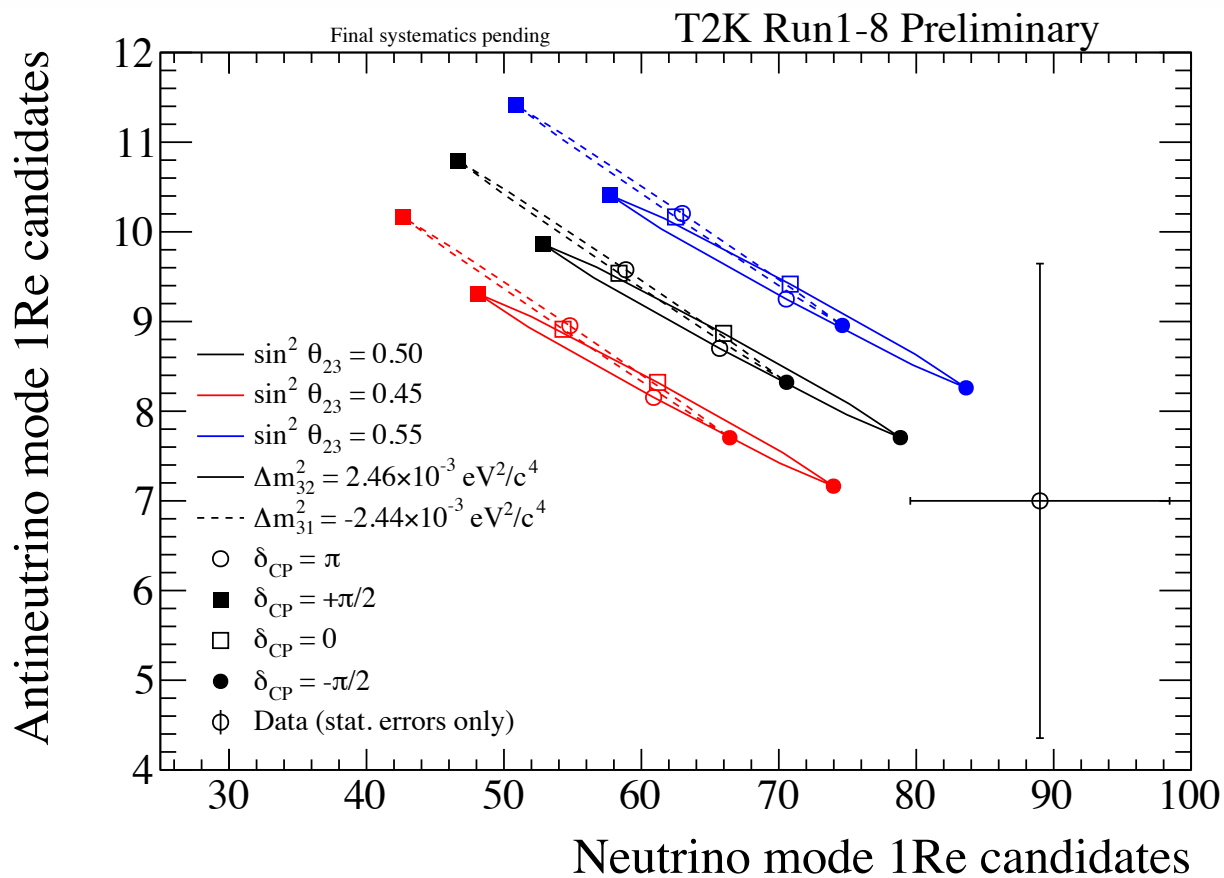
2σ confidence level



- Best-fit δ_{CP} is -1.833 radians
 - Normal Ordering is favored by the T2K data
 - CP conserving values (0, π) are excluded with a significance of 2σ
- Bayesian joint fit of Near and Far detector (MCMC): validation of the near to far detector extrapolation

Measured Vs Sensitivity

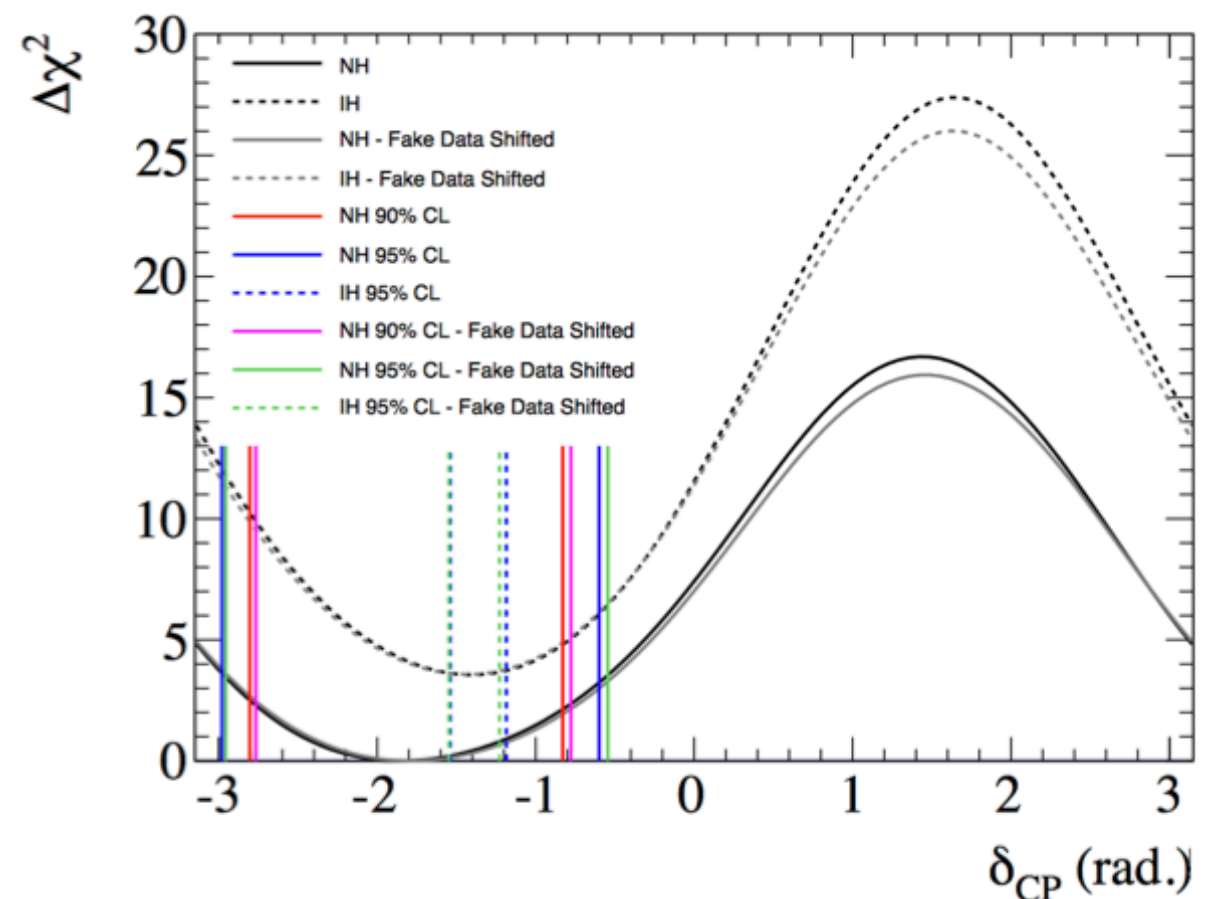
- Data constrain δ_{CP} more than the sensitivity
- How likely can this happen?
- Perform many pseudo-experiments at $\delta_{CP} = -\pi/2$ and Normal Ordering



- Data $\Delta\chi^2$ falls within the 95.45% of the pseudo-experiments
- 30% of pseudo-experiments exclude $\delta_{CP}=0$ at 2σ
- 25% of pseudo-experiments exclude $\delta_{CP}=\pi$ at 2σ

Effect of different models on oscillation analysis

- Neutrino interaction models are constantly updated
- Check robustness of T2K results against potential mis-modeling, due to models not yet included in the MC
- Generate fake data sets consistent with variations of the cross-section model (data-driven or different assumptions in the model)
- Fit the fake data set with the MC currently used in the oscillation analysis (both near and far detector)
- Evaluate potential biases on the measured neutrino oscillation parameters
- Full study performed with the 2016 model and statistic
- Work in progress
- Details of the 2016 studies can be found in [arXiv:1707.01048](https://arxiv.org/abs/1707.01048)



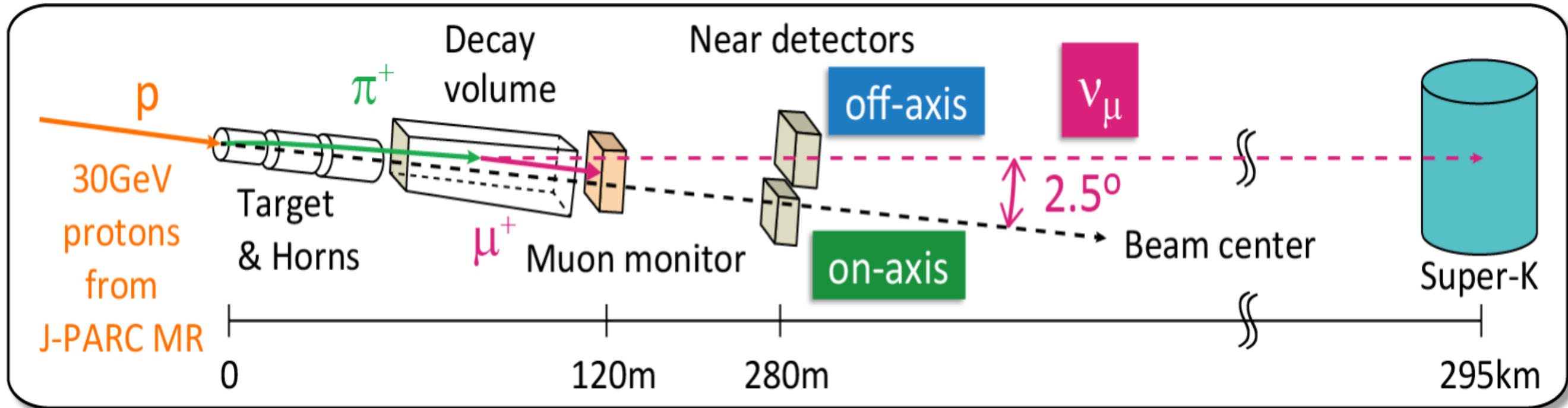
No significant impact on the δ_{CP} measured intervals

How can we improve the sensitivity?

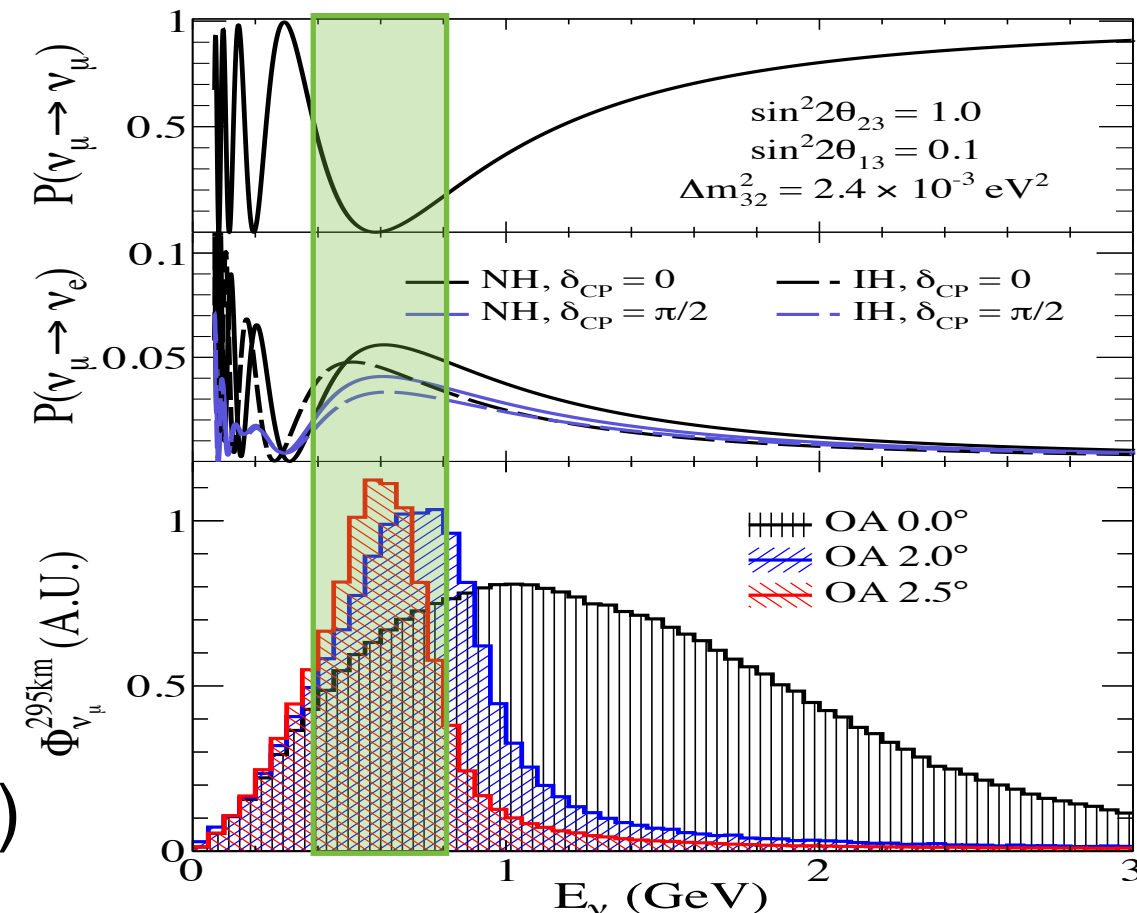
- More precise measurements of the unoscillated neutrino interactions
 - full acceptance
 - lowest momentum threshold
 - more data
- Continue interactions with theoreticians: “we” need improved models (and generators), “they” need more and better data
 - new cross-section measurements (T2K has an extensive program)
 - fake data studies
- Higher statistics analysis (e.g. T2K-II, Hyper-K, DUNE) may require optimized statistical tools and more CPU resources...

BACKUP

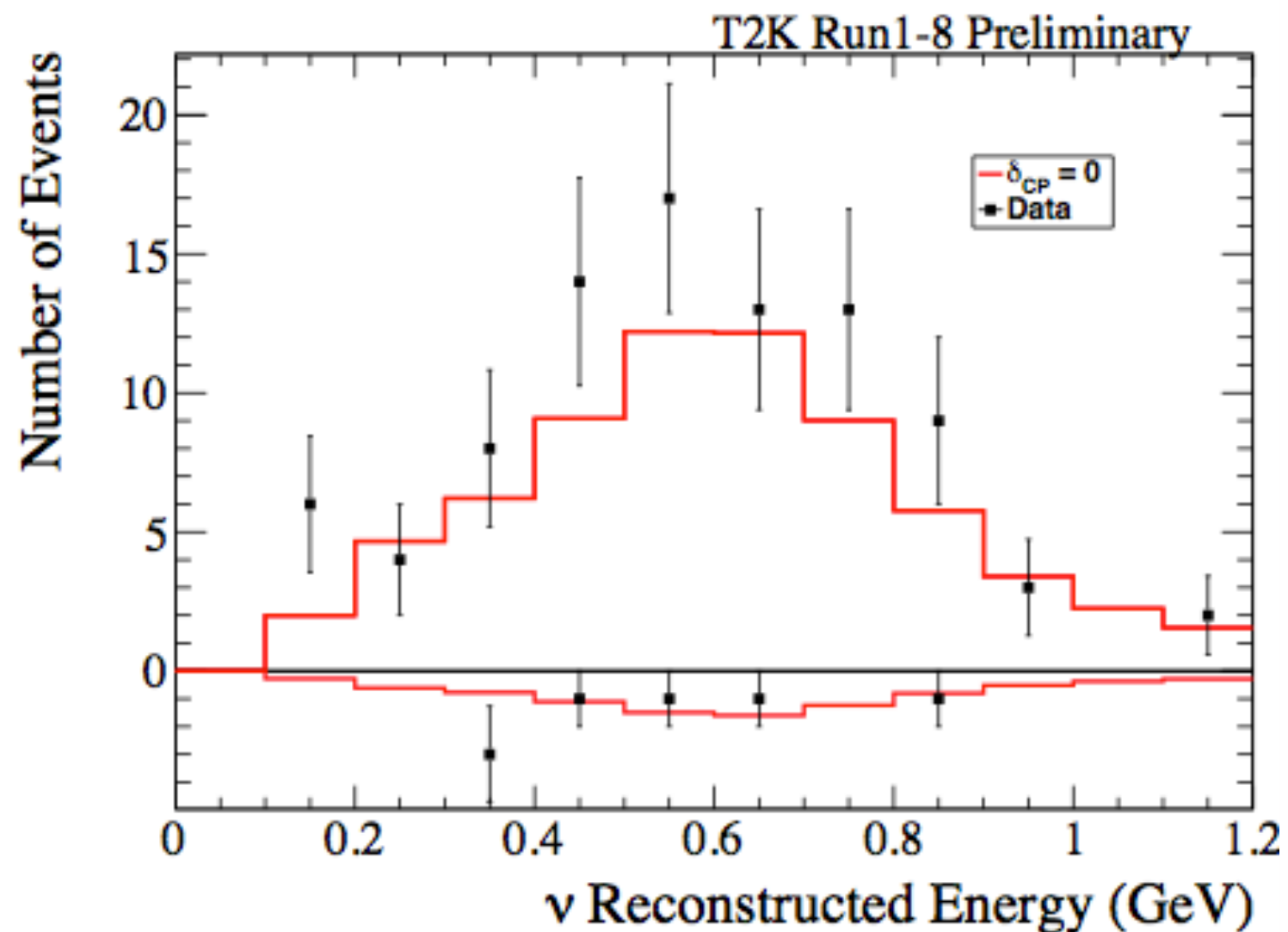
Design principle: the off-axis angle



- 30 GeV proton beam on 90 cm long graphite target
- ν_μ and $\bar{\nu}_\mu$ produced by pion and kaon decay:
 - $\pi^+ \rightarrow \mu^+ + \nu_\mu$
 - $\pi^- \rightarrow \mu^- + \bar{\nu}_\mu$
- Invert magnet polarity to produce a $\bar{\nu}_\mu$ beam
- First off-axis neutrino beam experiment (2.5°)
 - narrow spectrum peaked at 0.6 GeV, on the expected oscillation maximum



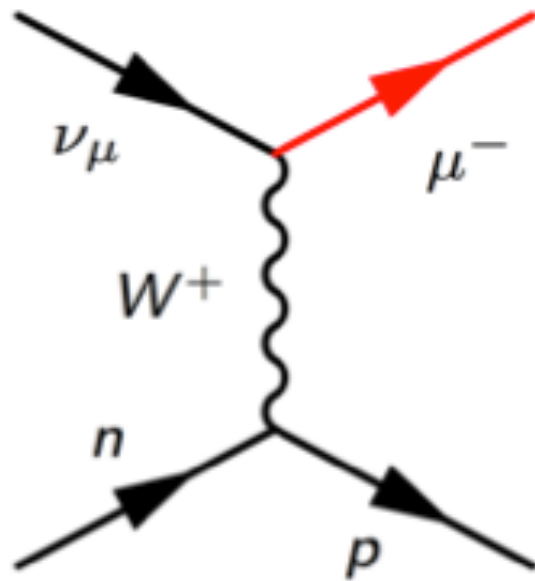
| | Set A | Set B |
|---------------------|-------------------------------------|-------------------------------------|
| $\sin^2\theta_{12}$ | 0.304 | 0.304 |
| $\sin^2\theta_{23}$ | 0.528 | 0.45 |
| $\sin^2\theta_{13}$ | 0.0219 | 0.0219 |
| Δm^2_{12} | $7.53 \times 10^{-5} \text{ eV}^2$ | $7.53 \times 10^{-5} \text{ eV}^2$ |
| Δm^2_{23} | $2.509 \times 10^{-3} \text{ eV}^2$ | $2.509 \times 10^{-3} \text{ eV}^2$ |
| δ_{CP} | -1.601 | 0 |



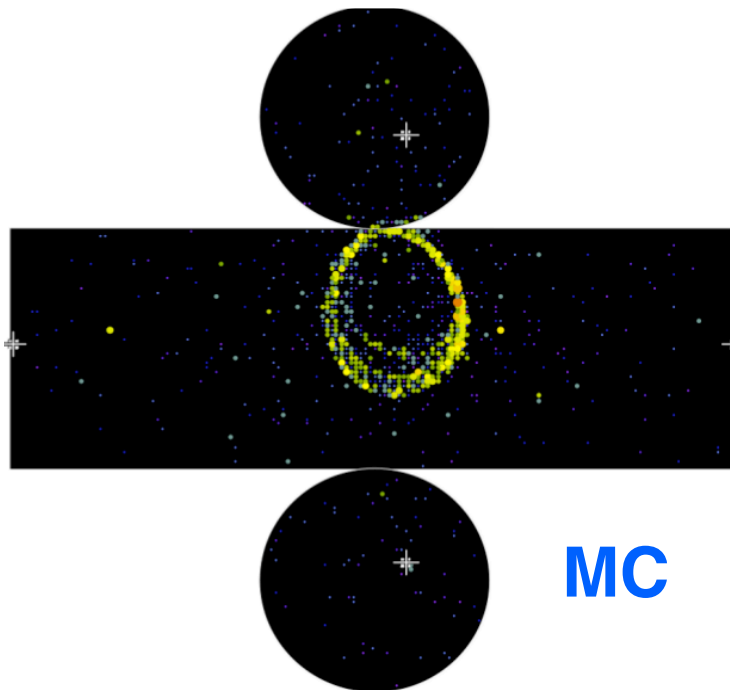
| Sample | Predicted Rates (pars except δ_{CP} take set A values) | | | | Observed Rates |
|---|---|-------------------|-----------------------|---------------------|----------------|
| | $\delta_{CP} = -\pi/2$ | $\delta_{CP} = 0$ | $\delta_{CP} = \pi/2$ | $\delta_{CP} = \pi$ | |
| CCQE 1-Ring e-like ν -mode | 73.5 | 61.5 | 49.9 | 62.0 | 74 |
| CC1 π 1-Ring e-like ν -mode | 6.92 | 6.01 | 4.87 | 5.78 | 15 |
| CCQE 1-Ring e-like $\bar{\nu}$ -mode | 7.93 | 9.04 | 10.04 | 8.93 | 7 |
| CCQE 1-Ring μ -like ν -mode | 267.8 | 267.4 | 267.7 | 268.2 | 240 |
| CCQE 1-Ring μ -like $\bar{\nu}$ -mode | 63.1 | 62.9 | 63.1 | 63.1 | 68 |

Super-Kamiokande events

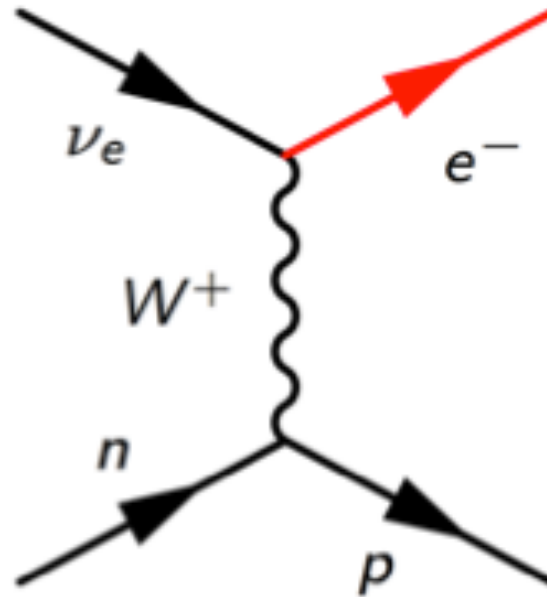
ν_μ CCQE



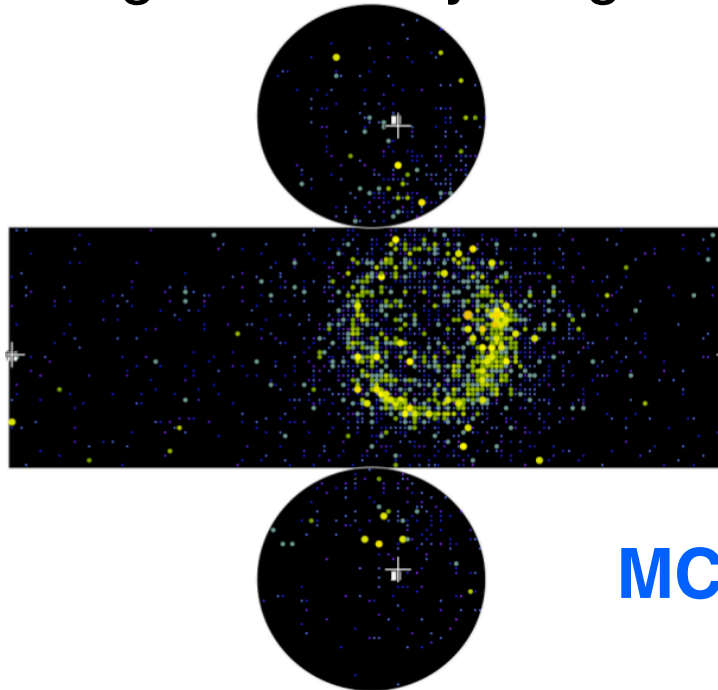
- 1 Cherenkov ring (protons below threshold)
- Low scattering
- Ring with sharp edge



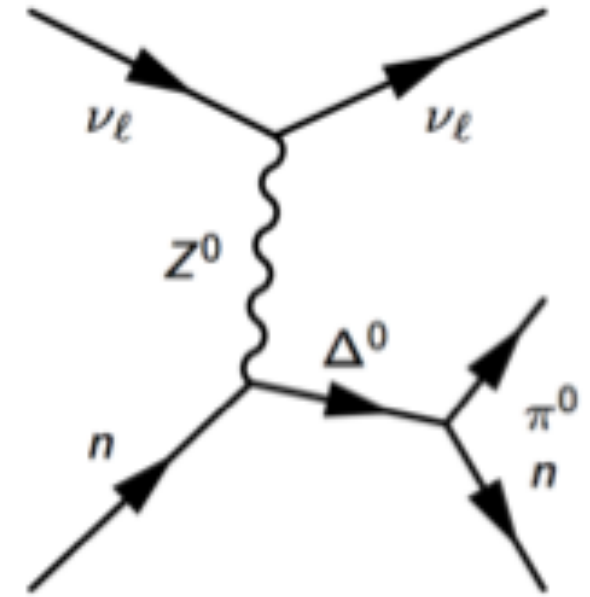
ν_e CCQE



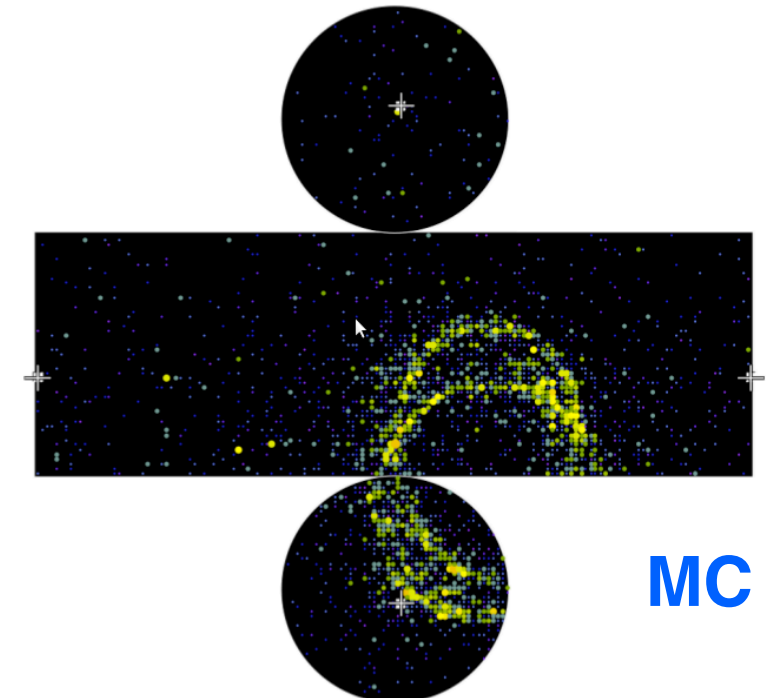
- 1 Cherenkov ring
- Multiple scattering
- EM shower
- Ring with “fuzzy” edge



Background



- 2 Cherenkov rings
- EM shower from $\pi^0 \rightarrow \gamma\gamma$
- Can be misidentified as an electron



- Probability to misidentify a muon as an electron is smaller than 1%

Neutrino oscillations at T2K

$$P(\nu_\mu \rightarrow \nu_\mu) \simeq 1 - (\cos^4 \theta_{13} \sin^2 2\theta_{23}) \sin^2 \left(\Delta m_{31}^2 \frac{L}{4E} \right)$$

- Precise measurement of $\sin^2 2\theta_{23}$
- Test of CPT by comparing measured $\nu_\mu \rightarrow \nu_\mu$ with $\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$

E ~ 0.6 GeV
L ~ 295 km

$$P(\nu_\mu \rightarrow \nu_e) \simeq \sin^2 2\theta_{13} \times \sin^2 \theta_{23} \times \frac{\sin^2[(1-x)\Delta]}{(1-x)^2} \quad \text{Phys. Rev. D64 (2001) 053003}$$

Leading term

CP violating $\ominus \alpha \sin \delta_{CP} \times \sin^2 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} \times \sin \Delta \frac{\sin[x\Delta]}{x} \frac{\sin[(1-x)\Delta]}{(1-x)}$
 “+” for antineutrino

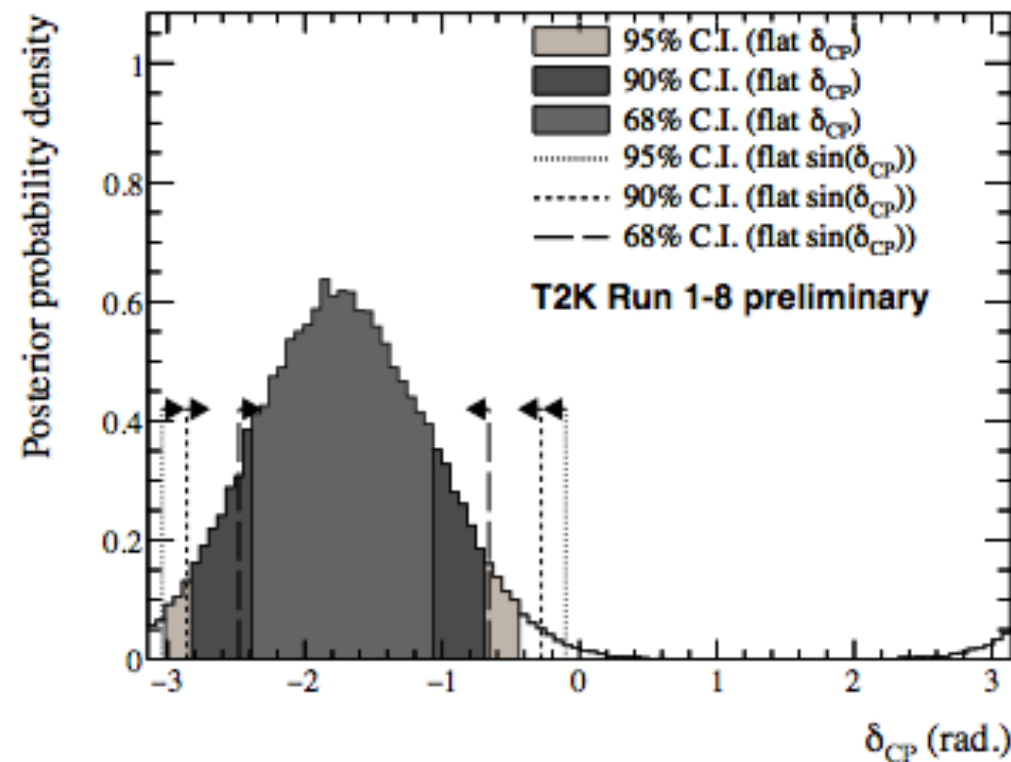
CP conserving $\alpha \cos \delta_{CP} \times \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} \times \cos \Delta \frac{\sin[x\Delta]}{x} \frac{\sin[(1-x)\Delta]}{(1-x)}$
 $+ O(\alpha^2)$

$$x = \frac{2\sqrt{(2)G_F N_e E}}{\Delta m_{31}^2} \quad \alpha = \left| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \right| \sim \frac{1}{30} \quad \Delta = \frac{\Delta m_{31}^2 L}{4E}$$

- The leading term defines the octant $\theta_{23} > 45^\circ$ or $\theta_{23} < 45^\circ$
- All mass splittings and mixing angles have been measured to be non-zero:
second order term can violate the CP symmetry if $\sin \delta_{CP} \neq 0$

Bayesian analysis

- Produce posterior probability distributions and credible intervals in Bayesian analysis
- Two choices for priors: flat in δ_{CP} and flat in $\sin(\delta_{CP})$



The 2σ confidence interval:

Flat prior on δ_{CP} : $[-3.02, -0.44]$ radians

Flat prior on $\sin(\delta_{CP})$: $[-3.04, -0.10]$ radians

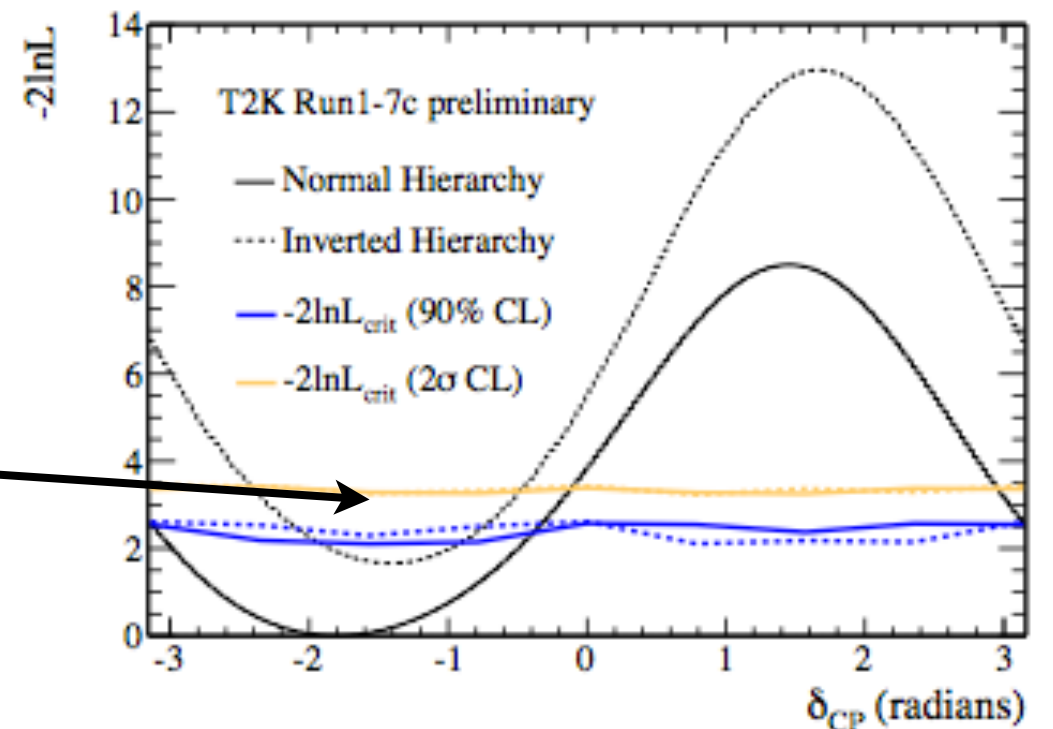
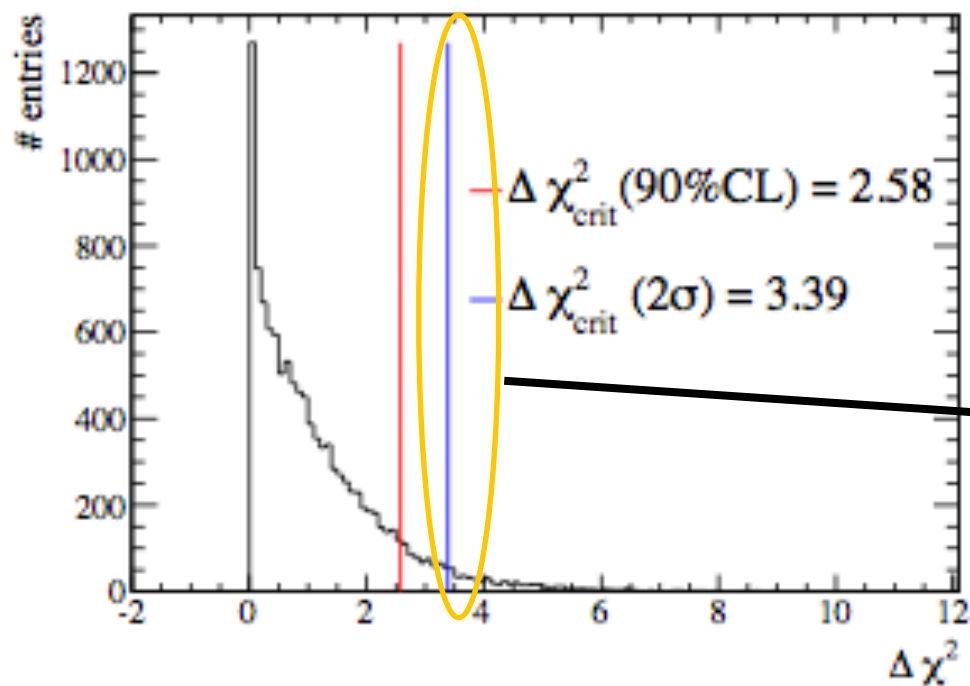
CP conserving values $(0, \pi)$ fall outside of the 2σ intervals

| | $\sin^2\theta_{23} < 0.5$ | $\sin^2\theta_{23} > 0.5$ | Sum |
|------------------------------|---------------------------|---------------------------|-------|
| NH ($\Delta m^2_{32} > 0$) | 0.193 | 0.674 | 0.868 |
| IH ($\Delta m^2_{32} < 0$) | 0.026 | 0.106 | 0.132 |
| Sum | 0.219 | 0.781 | |

Statistical methods

- Hybrid Bayesian-Frequentist analysis (confidence intervals):
 - scan $\Delta\chi^2 = -2\ln\lambda_{\text{marg}}$ surface as a function of e.g. δ_{CP}
 - if $\Delta\chi^2 > \Delta\chi^2_{\text{crit}}$ --> excluded at X%CL
 - Use Feldman-Cousins method: MC method to evaluate $\Delta\chi^2_{\text{crit}}$
 - Two analyses: VALOR using Ereco- Θ (primary analysis) and p- Θ

(b) $\Delta\chi^2$ distribution. $\delta_{\text{CP}}^{\text{true}} = -\pi/2$.



Statistical methods

- Hybrid Bayesian-Frequentist analysis (confidence intervals):

- scan $\Delta\chi^2 = -2\ln\lambda_{\text{marg}}$ surface as a function of e.g. δ_{CP}
- if $\Delta\chi^2 > \Delta\chi^2_{\text{crit}}$ --> excluded at X%CL
- Use Feldman-Cousins method: MC method to evaluate $\Delta\chi^2_{\text{crit}}$
- Two analyses: VALOR using Ereco- Θ , ρ - Θ analysis

- Fully Bayesian analysis (credible intervals):

- Markov Chain MC
- Bayesian intervals: weighted by the prior on δ_{CP}
- Using Ereco- Θ
- Joint fit of Near and Far detector: validation of the near to far detector extrapolation

Agreement between
all the 3 analyses

