

# Constraints to Triplet Higgs model from oscillation experiments

Katri Huitu, Timo J. Kärkkäinen,  
Jukka Maalampi and Sampsa Vihonen

University of Helsinki, University of Jyväskylä

*timo.j.karkkainen@helsinki.fi*

20 October 2017

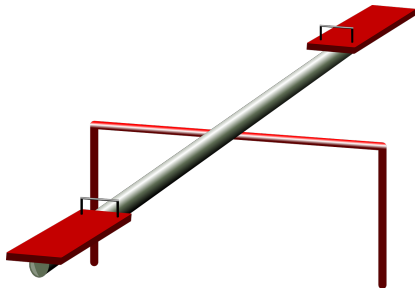
---

arXiv: 1601.07730, 1710.01080, 1711.XXXXX.

Work in progress.

# Neutrino mass $\Rightarrow$ Standard model is incomplete!

- Triplet Higgs model as a neutrino mass generation mechanism.
- Lepton number violation and subleading effects to neutrino oscillation.
- Constraints on  $\frac{M_\Delta}{|\lambda_\phi|}$  and small  $\lambda_\phi$  ( $\Delta\phi\phi$  coupling).



# Triplet seesaw model contributes to neutrino oscillation

Magg, Wetterich, Schechter, Valle, Cheng, Li, Lazarides, Mohapatra,  
Senjanović, Gelmini, Roncadelli... (1980)

- $SU(2)_L \times U(1)_Y$  electroweak model + scalar triplet field  
 $\Delta = (\Delta_1, \Delta_2, \Delta_3) \sim (\mathbf{3}, 2)$  with  $L = -2$ .

# Triplet seesaw model contributes to neutrino oscillation

Magg, Wetterich, Schechter, Valle, Cheng, Li, Lazarides, Mohapatra,  
Senjanović, Gelmini, Roncadelli... (1980)

- $SU(2)_L \times U(1)_Y$  electroweak model + scalar triplet field  
 $\Delta = (\Delta_1, \Delta_2, \Delta_3) \sim (\mathbf{3}, 2)$  with  $L = -2$ .
- Can be understood as an effective theory of the left-right symmetric  $SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} < SO(10)$

# Triplet seesaw model contributes to neutrino oscillation

Magg, Wetterich, Schechter, Valle, Cheng, Li, Lazarides, Mohapatra,  
Senjanović, Gelmini, Roncadelli... (1980)

- $SU(2)_L \times U(1)_Y$  electroweak model + scalar triplet field  
 $\Delta = (\Delta_1, \Delta_2, \Delta_3) \sim (\mathbf{3}, 2)$  with  $L = -2$ .
- Can be understood as an effective theory of the left-right symmetric  $SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} < SO(10)$
- All the other nonstandard degrees of freedom in LR model except the triplet scalar are assumed **too heavy** to have observable effects in oscillation and CLFV experiments.

# Triplet seesaw model contributes to neutrino oscillation

Magg, Wetterich, Schechter, Valle, Cheng, Li, Lazarides, Mohapatra, Senjanović, Gelmini, Roncadelli... (1980)

- $SU(2)_L \times U(1)_Y$  electroweak model + scalar triplet field  
 $\Delta = (\Delta_1, \Delta_2, \Delta_3) \sim (\mathbf{3}, 2)$  with  $L = -2$ .
- Can be understood as an effective theory of the left-right symmetric  $SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} < SO(10)$
- All the other nonstandard degrees of freedom in LR model except the triplet scalar are assumed **too heavy** to have observable effects in oscillation and CLFV experiments.

The Lagrangian relevant to nonstandard neutrino oscillation is

$$\mathcal{L}_\Delta = \mathcal{L}_Y + \mathcal{L}_\ell = Y_{\alpha\beta} L_{\alpha L}^T C i\sigma_2 \Delta L_{\beta L} + \lambda_\phi \phi^T i\sigma_2 \Delta^\dagger \phi + \text{h.c.},$$

where the triplet is represented by  $2 \times 2$  matrix form

$$\Delta = \frac{1}{\sqrt{2}} \sigma_i \Delta_i = \begin{pmatrix} \frac{\Delta^+}{\sqrt{2}} & \Delta^{++} \\ \Delta^0 & -\frac{\Delta^+}{\sqrt{2}} \end{pmatrix},$$

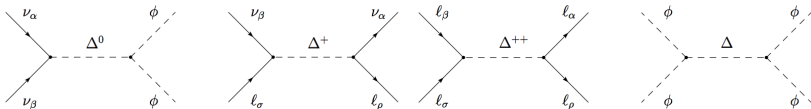
# Interactions between $\nu$ , $\ell$ and SM Higgs mediated by $\Delta$

The model features an  $L$ -breaking term in the Lagrangian:

$$\mathcal{L}_\ell = \lambda_\phi \phi^T i\sigma_2 \Delta^\dagger \phi + \text{h.c.}$$

where the trilinear dimension-1 coupling  $\lambda_\phi$  can be naturally small, since at the limit  $\lambda_\phi \rightarrow 0$  the symmetry of the theory is enhanced. Written in terms of component fields, the Yukawa term is

$$\mathcal{L}_Y = Y_{\alpha\beta} \left[ \Delta^0 \overline{\nu_{\alpha R}^C} \nu_{\beta L} - \frac{1}{\sqrt{2}} \Delta^+ \left( \overline{\ell_{\alpha R}^C} \nu_{\beta L} + \overline{\nu_{\alpha R}^C} \ell_{\beta L} \right) - \Delta^{++} \overline{\ell_{\alpha R}^C} \ell_{\beta L} \right] + \text{h.c.}$$



# Low-energy Lagrangians of triplet model

Malinský, Ohlsson, Zhang (2008) [arXiv:0811.3346](https://arxiv.org/abs/0811.3346)

Assuming triplet masses  $M_\Delta$  are degenerate, and large compared with momenta of the processes, the amplitudes are described by effective Lagrangians

$$\mathcal{L}_\nu^m = \frac{Y_{\alpha\beta} \lambda_\phi v^2}{M_\Delta^2} (\overline{\nu_{\alpha R}^C} \nu_{\beta L}) = -\frac{1}{2} (m_\nu)_{\alpha\beta} \overline{\nu_{\alpha R}^C} \nu_{\beta L},$$

$$\mathcal{L}_{\text{NSI}} = \frac{Y_{\sigma\beta} Y_{\alpha\rho}^\dagger}{M_\Delta^2} (\overline{\nu_{\alpha L}} \gamma_\mu \nu_{\beta L}) (\overline{\ell_{\rho L}} \gamma^\mu \ell_{\sigma L}).$$



# Low-energy Lagrangians of triplet model

Malinský, Ohlsson, Zhang (2008) arXiv:0811.3346

Assuming triplet masses  $M_\Delta$  are degenerate, and large compared with momenta of the processes, the amplitudes are described by effective Lagrangians

$$\mathcal{L}_\nu^m = \frac{Y_{\alpha\beta} \lambda_\phi v^2}{M_\Delta^2} (\overline{\nu_{\alpha R}^C} \nu_{\beta L}) = -\frac{1}{2} (m_\nu)_{\alpha\beta} \overline{\nu_{\alpha R}^C} \nu_{\beta L},$$

$$\mathcal{L}_{\text{NSI}} = \frac{Y_{\sigma\beta} Y_{\alpha\rho}^\dagger}{M_\Delta^2} (\overline{\nu_{\alpha L}} \gamma_\mu \nu_{\beta L}) (\overline{\ell_{\rho L}} \gamma^\mu \ell_{\sigma L}).$$

Now solving the Yukawa coupling from neutrino Majorana mass term, we obtain the following result:

$$\begin{aligned} \mathcal{L}_{\text{NSI}} &= 2\sqrt{2}G_F \frac{M_\Delta^2}{8\sqrt{2}G_F v^4 \lambda_\phi^2} (m_\nu)_{\sigma\beta} (m_\nu^\dagger)_{\alpha\rho} (\overline{\nu_{\alpha L}} \gamma_\mu \nu_{\beta L}) (\overline{\ell_{\rho L}} \gamma^\mu \ell_{\sigma L}) \\ &= 2\sqrt{2}G_F \varepsilon_{\alpha\beta}^{\rho\sigma} (\overline{\nu_{\alpha L}} \gamma_\mu \nu_{\beta L}) (\overline{\ell_{\rho L}} \gamma^\mu \ell_{\sigma L}) \end{aligned}$$

# Determining upper limit of $\frac{M_\Delta}{|\lambda_\phi|}$

$\mathcal{L}_{\text{NSI}}$  affects neutrino propagation in matter. Neutrino oscillation experiments are sensitive to  $\varepsilon_{\alpha\beta}^m$  and  $\varepsilon_{\alpha\alpha}^m - \varepsilon_{\beta\beta}^m$ , where  $\varepsilon_{\alpha\beta}^m \equiv \varepsilon_{\alpha\beta}^{ee}$ .

We calculate the upper bound for  $M_\Delta/|\lambda_\phi|$  by maximizing the matrix element products  $(m_\nu)_{\sigma\beta}(m_\nu^\dagger)_{\alpha\rho}$  and their differences by varying all relevant oscillation parameters within their current experimental bounds.

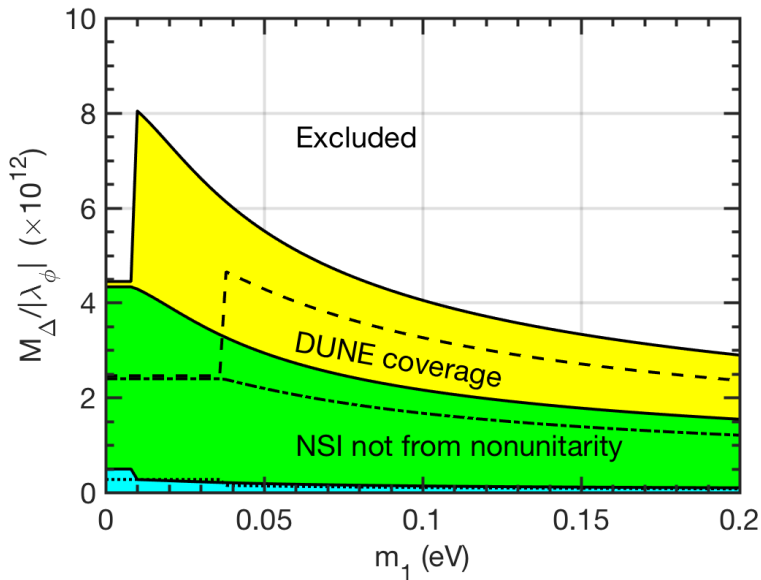
# Determining upper limit of $\frac{M_\Delta}{|\lambda_\phi|}$

$\mathcal{L}_{\text{NSI}}$  affects neutrino propagation in matter. Neutrino oscillation experiments are sensitive to  $\varepsilon_{\alpha\beta}^m$  and  $\varepsilon_{\alpha\alpha}^m - \varepsilon_{\beta\beta}^m$ , where  $\varepsilon_{\alpha\beta}^m \equiv \varepsilon_{\alpha\beta}^{ee}$ .

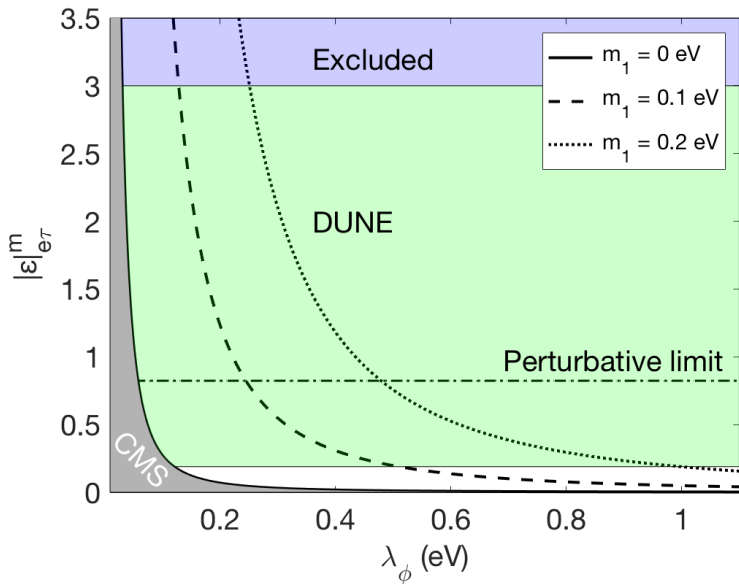
We calculate the upper bound for  $M_\Delta/|\lambda_\phi|$  by maximizing the matrix element products  $(m_\nu)_{\sigma\beta}(m_\nu^\dagger)_{\alpha\rho}$  and their differences by varying all relevant oscillation parameters within their current experimental bounds.

$$\left| \frac{M_\Delta^2}{\lambda_\phi^2} \right| = \left| -\frac{8\sqrt{2} G_F v^4 \varepsilon_{\alpha\beta}^m}{(m_\nu)_{e\beta}(m_\nu^\dagger)_{\alpha e}} \right|,$$
$$m_\nu^2 = U \begin{pmatrix} m_1^2 & 0 & 0 \\ 0 & m_2^2 & 0 \\ 0 & 0 & m_3^2 \end{pmatrix} U^\dagger + A \begin{pmatrix} 1 + \varepsilon_{ee}^m & \varepsilon_{e\mu}^m & \varepsilon_{e\tau}^m \\ \varepsilon_{e\mu}^{m*} & \varepsilon_{\mu\mu}^m & \varepsilon_{\mu\tau}^m \\ \varepsilon_{e\tau}^{m*} & \varepsilon_{\mu\tau}^{m*} & \varepsilon_{\tau\tau}^m \end{pmatrix},$$

# Constraining $M_{\Delta}/|\lambda_{\phi}|$ from oscillations and DUNE



# $M_\Delta$ and $\varepsilon_{\alpha\beta}^m$ bounds $\Rightarrow$ constraints for $\lambda_\phi$



- We have presented a novel method to constrain the triplet seesaw model by looking for effective limits for  $\varepsilon_{\alpha\beta}^m$  and maximizing the neutrino mass matrix elements.
- DUNE will constrain upper limits of  $\frac{M_\Delta}{|\lambda_\phi|}$  by  $\sim 50\%$ .
- For a triplet mass  $M_\Delta \sim 750$  GeV we get limits for trilinear  $\Delta\phi\phi$  coupling.
  - Currently  $\lambda_\phi \gtrsim 0.03$  eV.
  - DUNE is sensitive to  $\lambda_\phi \lesssim 0.12$  eV.

- Huitu, Kärkkäinen, Maalampi and Vihonen: *Constraining the nonstandard interaction parameters in long baseline neutrino experiments*, Phys. Rev. D **93**, 053016 (2016), arXiv:1601.07730.
- Malinský, Ohlsson, Zhang (2008) arXiv:0811.3346
- Valle et al. arXiv:1503.08879
- Y. Grossman, Phys. Lett. **B359**, 141 (1995), arXiv:hep-ph/9507344.
- NuFit 3.0 (as of November 2016), JHEP **11** (2014) 052 arXiv:1409.5439
- Blennow, Coloma, Fernandez-Martinez, Hernandez-Garcia and Lopez-Pavon, JHEP **04** (2017) 153.