

# EFT analysis of $B$ -decay anomalies

**J. Martin Camalich**



ZPW2018 - Flavours: light, heavy and dark

January 16th 2018

# Lepton-universality violation in $b \rightarrow c\tau\nu$ decays

# EFT of new-physics in $b \rightarrow c\tau\nu$

- Low-energy effective Lagrangian (no RH  $\nu$ )

$$\begin{aligned}\mathcal{L}_{\text{eff}}^{\ell} = & -\frac{G_F V_{cb}}{\sqrt{2}} [(1+\epsilon_L^{\ell}) \bar{c} \gamma_{\mu} (1-\gamma_5) \nu_{\ell} \cdot \bar{c} \gamma^{\mu} (1-\gamma_5) b + \epsilon_R^{\ell} \bar{c} \gamma_{\mu} (1-\gamma_5) \nu_{\ell} \cdot \bar{c} \gamma^{\mu} (1+\gamma_5) b \\ & + \bar{c} (1-\gamma_5) \nu_{\ell} \cdot \bar{c} [\epsilon_S^{\ell} - \epsilon_P^{\ell} \gamma_5] b + \epsilon_T^{\ell} \bar{c} \sigma_{\mu\nu} (1-\gamma_5) \nu_{\ell} \cdot \bar{c} \sigma^{\mu\nu} (1-\gamma_5) b] + \text{h.c.},\end{aligned}$$

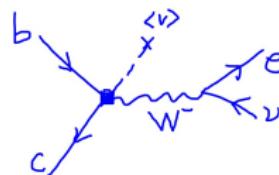
**Wilson coefficients:**  $\epsilon_{\Gamma}$  decouple as  $\sim v^2/\Lambda_{\text{NP}}^2$

- Matching to high-energy Lagrangian – SMEFT Cirigliano, Gonzalez-Alonso & Jenkins '10

- Symmetry relations for  $\epsilon_{\Gamma}$

- In charged-currents  $\epsilon_R^{\ell}$ :

$$\mathcal{O}_{Hud} = \frac{i}{\Lambda_{\text{NP}}^2} (\tilde{H}^\dagger D_\mu H) (\bar{u}_R \gamma^\mu d_R)$$

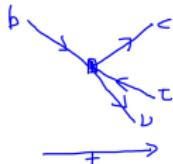


- RHC is lepton universal:  $\epsilon_R^{\ell} \equiv \epsilon_R + \mathcal{O}(\frac{v^4}{\Lambda_{\text{NP}}^4}) \Rightarrow \text{Cannot explain LUR } R_{D^{(*)}}!$

Down to 4 operators to explain  $R_{D^{(*)}}$ :  $\epsilon_L, \epsilon_S, \epsilon_P, \epsilon_T$

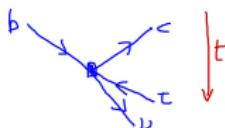
## The constraint of the $B_c$ -lifetime

- $B \rightarrow D^* \tau \nu$  receives a contribution from  $\epsilon_P$



$$\epsilon_P \langle D^*(k, \epsilon) | \bar{c} \gamma_5 b | \bar{B}(p) \rangle = -\frac{2\epsilon_P m_{D^*}}{m_b + m_c} A_0(q^2) \epsilon^* \cdot q$$

- $B_c \rightarrow \tau \nu$  also receives a **helicity-enhanced** contribution from  $\epsilon_P$ !



$$\frac{\text{Br}(B_c^- \rightarrow \tau \bar{\nu}_\tau)}{\text{Br}(B_c^- \rightarrow \tau \bar{\nu}_\tau)^{\text{SM}}} = \left| 1 + \epsilon_L + \frac{m_{B_c}^2}{m_\tau(m_b + m_c)} \epsilon_P \right|^2$$

- Use the lifetime of  $B_c$

- ▶ Very high experimental precision (1.5%):

$$\tau_{B_c} = 0.507(8) \text{ ps}$$

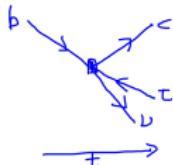
- ▶ **QCD:** "Most of the  $B_c$  lifetime comes from  $\bar{c} \rightarrow \bar{s}$  ( $\sim 65\%$ ) and  $b \rightarrow c$  ( $\sim 30\%$ )"

Bigi PLB371 (1996) 105, Beneke *et al.* PRD53(1996)4991, ...

$$\tau_{B_c}^{\text{OPE}} = 0.52^{+0.18}_{-0.12} \text{ ps}$$

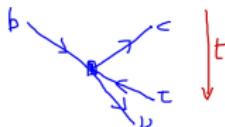
# The constraint of the $B_c$ -lifetime

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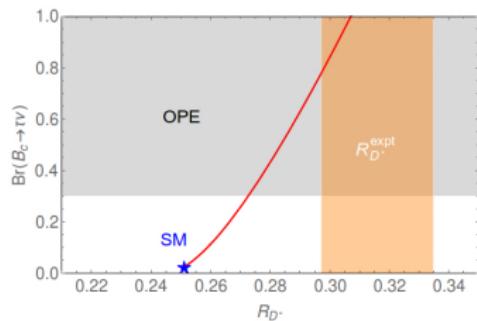


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$\tau_{B_c}$  makes **implausible ANY**  
“scalar solution”  
(e.g. 2HDM) to the  $R_{D^*}$  anomaly!

Alonso, Grinstein&JMC, arXiv: 1611.06676

(see also Xin-Qiang Li *et al.*, JHEP 1608 (2016) 054)

## Searches for $B_c \rightarrow \tau\nu$ at LEP

- BR( $B_c \rightarrow \tau\nu$ ) measured in a  $e^+e^-$  collider at the  $Z$  pole Akeroyd&Chen, 1708.04072
  - Searches of  $B^- \rightarrow \tau^-\nu$  above  $B_c \bar{B}_c$  threshold really measure

Mangano&Slabospitsky, PLB410(1997)299

$$\overbrace{\text{LEP}}^{\text{BR}_{\text{eff}}} = \overbrace{\text{Belle \& BaBar}}^{\text{BR}(B \rightarrow \tau\nu)} + \underbrace{\frac{f_c}{f_u}}_{\text{TH.input}} \text{BR}(B_c \rightarrow \tau\nu)$$

- $B_c$  contribution suppressed by  $f_c/f_u \sim 10^{-3}\text{-}10^{-2}$  but enhanced by  $\frac{|V_{cb}|^2}{|V_{ub}|^2} \frac{f_{B_c}^2}{f_B^2} \sim 700$

- $f_c/f_u$ : Fraction of hadronization into  $B_c$  over  $B$ 
  - Traded by experimental data and **computable TH. input**

$$R_\ell = \frac{f_c}{f_u} \frac{\text{BR}(B_c \rightarrow J/\psi \mu \nu)}{\text{B} \rightarrow J/\psi K}$$

- $R_\ell$  measured by **CDF** and reconstructed from **LHCb** data

# Searches for $B_c \rightarrow \tau\nu$ at LEP

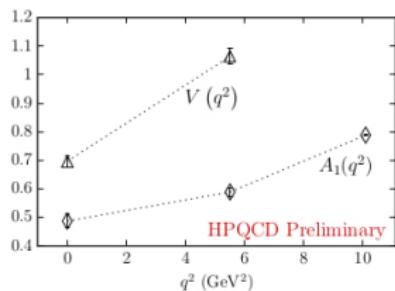
- Model calculations predict  $\text{BR}(B_c \rightarrow J/\psi \mu\nu) \in 1 - 7\%$ !

	pQCD	WSL[9]	EFG[7]	ISK[6]	HNV[5]	DV[4]
$V^{B_c \rightarrow J/\Psi}$	0.42	0.74	0.49	0.83	0.61	0.91
$A_0^{B_c \rightarrow J/\Psi}$	0.59	0.53	0.40	0.57	0.45	0.58
$A_1^{B_c \rightarrow J/\Psi}$	0.46	0.50	0.50	0.56	0.49	0.63
$A_2^{B_c \rightarrow J/\Psi}$	0.64	0.44	0.73	0.54	0.56	0.74

Wang, Fang&Xiao, arXiv: 1212.5903

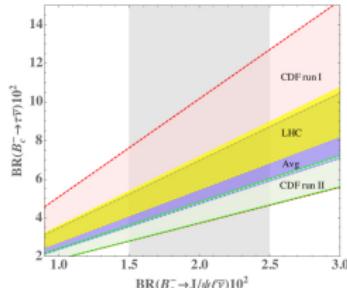
## Ongoing efforts in LQCD!

- Preliminary results to select models



HPQCD Collaboration, PoS LATTICE2016 (2016) 281

- Constrains  $\text{BR}(B_c \rightarrow \tau\nu) < 10\%$



Akeroyd&Chen, 1708.04072

# New-physics solutions and challenges: The left-handed operator

- Left-handed  $\epsilon_L = 0.13$ : Universal enhancement of the  $b \rightarrow c\tau\nu$  rates by 30%

**SMEFT operators:**  $Q_{\ell q}^{(1)} = \frac{1}{\Lambda^2} (\bar{Q}_L \gamma^\mu Q_L) (\bar{L}_L \gamma_\mu L_L), \quad Q_{\ell q}^{(3)} = \frac{1}{\Lambda^2} (\bar{Q}_L \gamma^\mu \vec{\tau} Q_L) \cdot (\bar{L}_L \gamma_\mu \vec{\tau} L_L)$

- ▶ **Warning ☠ Radiative LUV contributions in  $\tau$  and  $Z$  decays!**

Ferruglio *et al.* PRL118 (2017), 011801



- ▶ **Problem with 3<sup>rd</sup> generation:** Non-trivial flavor str. [Battazzo \*et al.\* arXiv:1706.07808](#)
- ▶ **Model dependence:** EFT only gives log parts (mixing)

- It can also solve  $b \rightarrow s\ell\ell$  anomaly! [Bhattacharya \*et al.\* '14, Alonso, JMC & Grinstein. '15, ...](#)

- ▶ **Lepton flavor structure:**

- ★ Large enhancements  $\tilde{C}_{\tau\tau} \gg \tilde{C}_{\mu\mu}$  ruled out by  $B \rightarrow K^{(*)}\nu\nu$  unless  $C_{\tau\tau}^{(1)} \simeq C_{\tau\tau}^{(3)}$
- ★ **Vector Leptoquark**  $U_1^\mu$  (3,1,2/3) produces this! [Alonso, JMC & Grinstein. '15, Barbieri \*et al.\* '15, ...](#)

# Tensor and scalar operators

- ▶ Mixing in  $H^3\psi^2$  operators that **modify Yukawas** Jenkins *et al.*, arXiv: 1310.4838

- Tensor  $\epsilon_T = 0.38$

- ▶ **EW+QED corrections:** Large mixing tensor into scalars

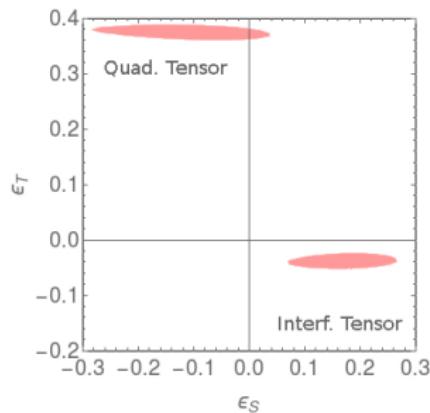
$$\begin{pmatrix} w_{ledq} \\ w_{\ell equ} \\ w_{\ell equ}^{(3)} \end{pmatrix}_{(\mu = m_Z)} = \begin{pmatrix} 1.19 & 0. & 0. \\ 0. & 1.20 & -0.185 \\ 0. & -0.00381 & 0.959 \end{pmatrix} \begin{pmatrix} w_{ledq} \\ w_{\ell equ} \\ w_{\ell equ}^{(3)} \end{pmatrix}_{(\mu = 1 \text{ TeV})}$$

Gonzalez-Alonso, JMC & Mimouni arXiv: 1706.00410

- ▶ **No explicit models** that give *only* tensor operators

- Tensor & Scalar

- ▶ Fit to current values of  $R_{D^{(*)}}$



- ▶ **New solution:**  $\epsilon_T$  interferes constructively in  $R_{D^*}$

- ★ **Best Fit:**  $\epsilon_S = 0.17$ ,  $\epsilon_T = -0.04$
- ★ **Scalar Leptoquark**  $S_1 (\bar{3}, 1, 1/3)$  produces

$$\epsilon_T(M) = -\frac{\epsilon_{S_L}(M)}{4}$$

- ★  $\epsilon_P \sim 0.2$  produces  $\text{BR}(B_c \rightarrow \tau\nu) \sim 6\%$

## Adding new channels: $B_c \rightarrow J/\psi \tau \nu$

$$R_{J/\psi}^{\text{LHCb}} = 0.71 \pm 0.17 \pm 0.18$$

Greg's talk yesterday

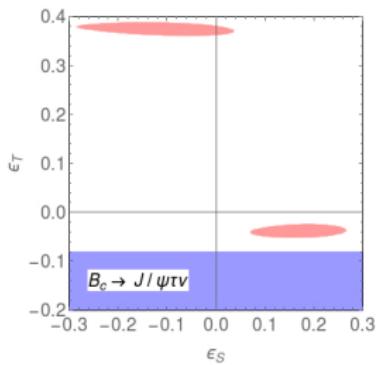
- Comparison with SM **NOW** is subtle because of **model dependence**

Mode	This paper	[8, 30]	[11]	[15]	[16]	[31]	[32]
$B_c^- \rightarrow J/\psi \ell \nu$	$6.7^{+2.1+1.0+0.9}_{-1.2-0.4-0.6}$	1.9	2.37	1.5	1.49	1.20	2.07
$B_c^- \rightarrow J/\psi \tau \nu$	$0.52^{+0.16+0.08+0.08}_{-0.09-0.03-0.05}$	0.48	0.65	0.4	0.37	0.34	0.49

$$R_{J/\psi}^{\text{SM}^*} \sim 0.24 - 0.29$$

Qiao&Zhu, 1208.5916

- Goes in the *right* direction of NP but effect is **large**



- For the LH solution one predicts

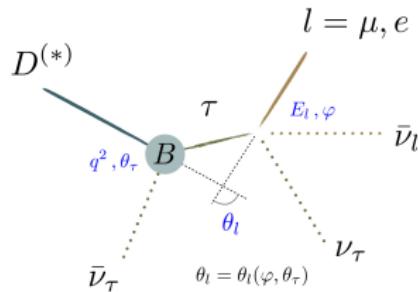
$$R_{J/\psi}^{\text{LH}^*} \sim 0.35 - 0.4$$

(see also Watanabe, arXiv: 1709.08644)

- Besides more data, **LQCD input urgently needed!**

# Adding new observables: Kinematic distributions ( $\tau^- \rightarrow \ell^- \bar{\nu}_\ell \nu_\tau$ )

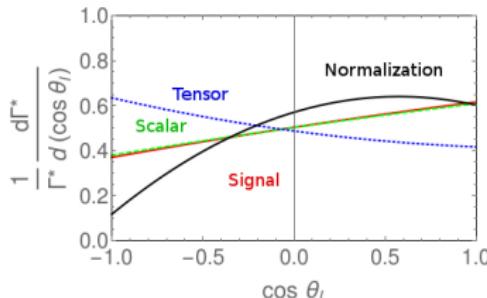
Alonso, Kobach, JMC, PRD94(2016)no.9,094021; Alonso, JMC, Westhoff, PRD95(2017)no.9,093006



- Integrate analytically the  $\tau$  and  $\nu$ 's angular phase-space:

$$\frac{d^3 r_5}{dq^2 dE_\ell d(\cos \theta_\ell)} = \mathcal{B}[\tau_\ell] \mathcal{N} [I_0(q^2, E_\ell) + I_1(q^2, E_\ell) \cos \theta_\ell + I_2(q^2, E_\ell) \cos^2 \theta_\ell]$$

- Angular distribution help discriminate **signal**, **normalization**, **NP**



$\tau^- \rightarrow \pi^- \nu_\tau$  as a  $\tau$  polarimeter

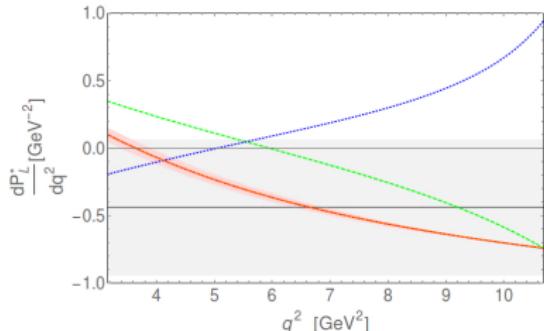
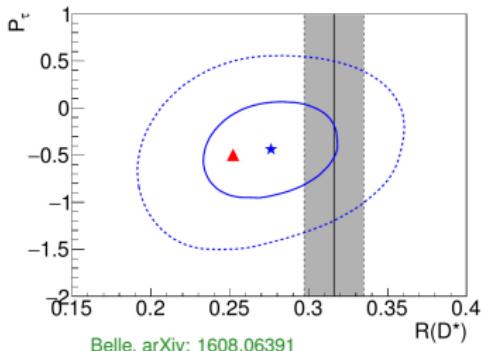
$$\frac{dP_L}{dq^2} = \frac{d\Gamma_{B,+}/dq^2 - d\Gamma_{B,-}/dq^2}{d\Gamma_B/dq^2}$$

**Slope** in  $E_\pi$  of  $d\Gamma_4 \Rightarrow$  **Longitudinal Polarization**

$$\frac{d^2\Gamma_4}{dq^2 dE_\pi} = \frac{\mathcal{B}[\tau\pi]}{|\vec{p}_\tau|} \frac{d\Gamma_B}{dq^2} \left[ 1 + \xi(E_\pi, q^2) \frac{dP_L}{dq^2} \right], \quad \xi(E_\pi, q^2) = \frac{1}{\beta_\tau} \left( 2 \frac{E_\pi}{E_\tau} - 1 \right)$$

M. Davier *et al.* PLB306, 411 (1993), Tanaka&Watanabe, PRD82, 034027 (2010)

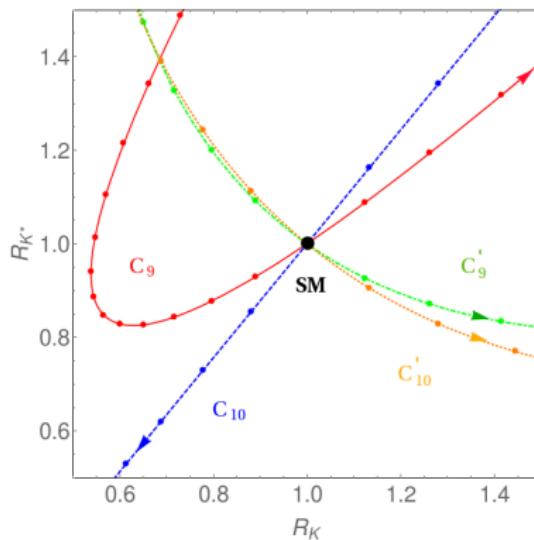
- Applied to the  $BD^*$  channel by *Belle*



# Lepton-universality violation in $b \rightarrow sll$ decays

## ● New physics in muons

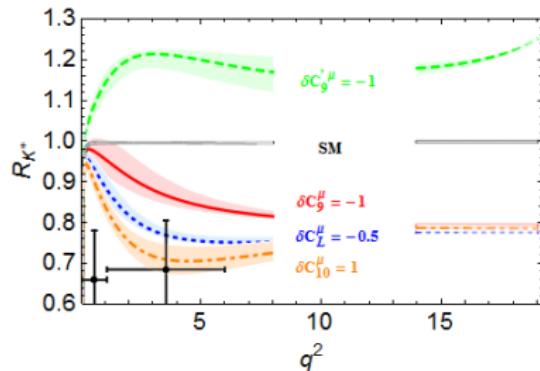
- ▶ No  $b \rightarrow sll$  **tensor operators** in the SMEFT
- ▶ **Scalar operators** severely constrained by  $B_s \rightarrow \mu\mu$  Alonso, Grinstein, JMC, PRL113 (2014) 241802



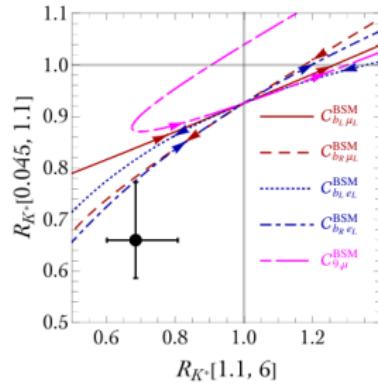
Geng, Grinstein, Jäger, JMC, Ren, Shi, arXiv: 1704.05446

## ● Nodes indicate steps of $\Delta C^\mu = +0.5$

- ▶ **Primed operators**  $C'_{9,10}$ : Monotonically decreasing dependence  $R_{K^*}(R_K)$ !



Geng, Grinstein, Jäger, Martin Camalich, Ren, Shi, arXiv: 1704.05446



D'Amico *et al.* 1704.05438

## Very clean null-tests of the SM!

Discussion Diego Guadagnoli this morning!

- **Warning 🧐:** Value at ultralow- $q^2$  is difficult to accommodate with UV physics

# Top-down approach: Fits for UV completions

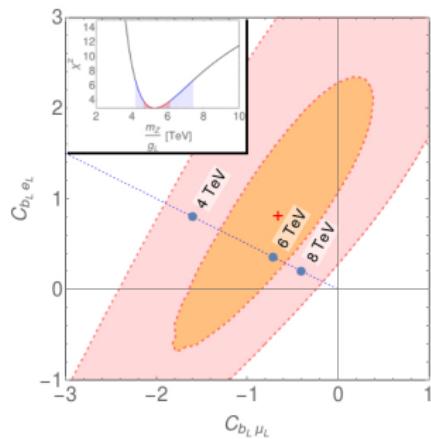
- **Gauged flavor symmetries** Altmannshofer *et al.* arXiv:1403.1269, Alonso *et al.* arXiv:1704.08158, ...

- **Gauge**  $SU(3)_L \times SU(3)_R$  Cline&JMC arXiv:1706.08510

- ★ Dynamically generate Flavor and UV consistent (no Landau poles)
    - ★ *Baroque* field content for gauge anomalies/SSB-structure, and *ad-hoc* flavor structure

- **Couplings to the leptons**

$$V_l^L T^8 V_l^{L\dagger} \cong \frac{1}{2\sqrt{3}} \begin{pmatrix} 1 & \epsilon_1 & \epsilon_2 \\ \epsilon_1^* & -2 & \epsilon_3 \\ \epsilon_2^* & \epsilon_3^* & 1 \end{pmatrix}$$



**Coupling to both electrons and muons!**

- Couplings to electrons opens up much more stringent phenomenology!

# Precision probes of lepton nonuniversal $C_{9,10}^\ell$

Geng, Grinstein, Jäger, Martin Camalich, Ren, Shi, arXiv: 1704.05446

- Can we pin down specific contributions to electrons/muons?
- Go to the angular analysis of  $B \rightarrow K^* \ell \ell \dots$

$$I_6^{(\ell)} = N C_{10}^\ell q^2 \beta_\ell^2(q^2) |\vec{k}| \left( \text{Re}[H_{V-}^{(\ell)}(q^2)] V_-(q^2) + \text{Re}[H_{V+}^{(\ell)}(q^2)] \frac{H_{A+}^{(\ell)}(q^2)}{C_{10}^\ell} \right)$$

- ▶ The  $H_{V,A+}$  amplitudes are suppressed at low  $q^2$ !
- ▶ Photon-pole enhancement of  $H_{V-}^{(\ell)}(q^2)$  at low  $q^2$ !

$$R_6[a,b] \approx \frac{C_{10}^\mu}{C_{10}^e} \times \frac{\int_a^b |\vec{k}| q^2 \beta_\mu^2 \text{Re}[H_{V-}^{(\mu)}(q^2)] V_-(q^2)}{\int_a^b |\vec{k}| q^2 \text{Re}[H_{V-}^{(e)}(q^2)] V_-(q^2)}$$

$R_6$  is an optimal  $C_{10}$  LUV analyser!

- Combine this with  $B_s \rightarrow \mu\mu$  to separate  $C_{10}^{e,\mu}$ !

# Conclusions

- **Interesting times ahead!**
- “Instant” workshop at CERN last May

### Instant workshop on B meson anomalies

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17 May 2017, 09:00 → 19 May 2017, 16:30 Europe/Zurich

4-3-006 - TH Conference Room (CERN)

Jorge Martin Camalich (CERN), Jure Zupan (University of Cincinnati), Marco Nardecchia (CERN)

**Description** In light of recent anomalies in B physics there is an increased interest in the theory community on its implications. As a quick response we are organizing an "Instant workshop on B meson anomalies" at CERN from May 17-May 19 2017.

- **Check recordings @ <https://indico.cern.ch/event/633880/>**

**CERN-TH Institute programmed for the next year**

“From flavor anomalies to direct discovery of New Physics”  
*Oct. 22nd to Nov. 2nd 2018 (tentative)*

# THANKS!