

DA and first misalignment studies for the booster synchrotron

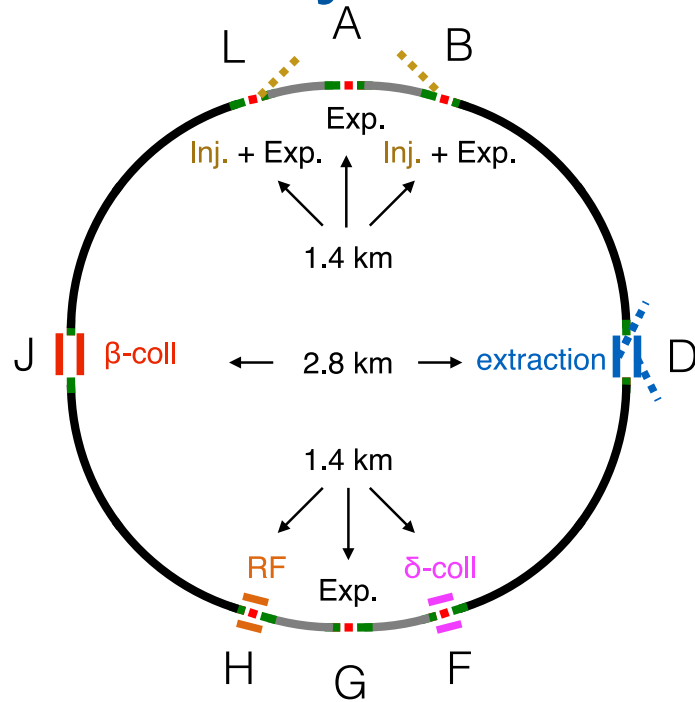


Bastian Haerer (CERN)
for the FCC-ee lattice design team

15th FCCee Injector Meeting
06 October 2017



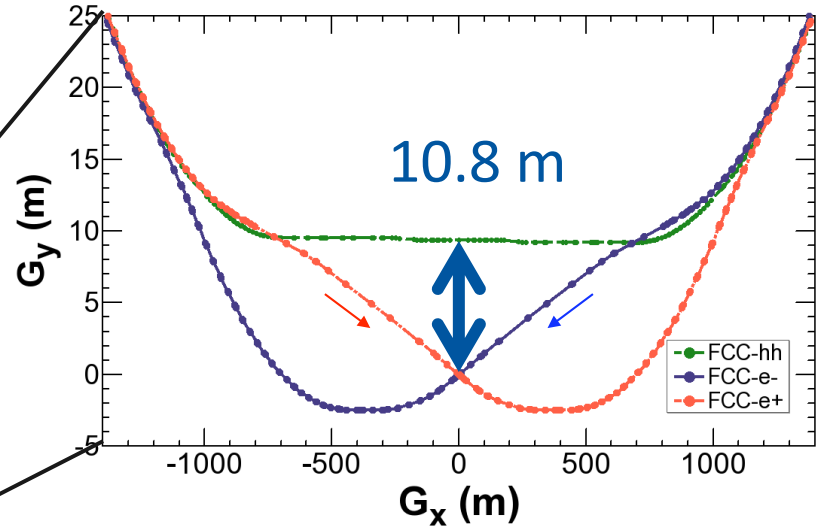
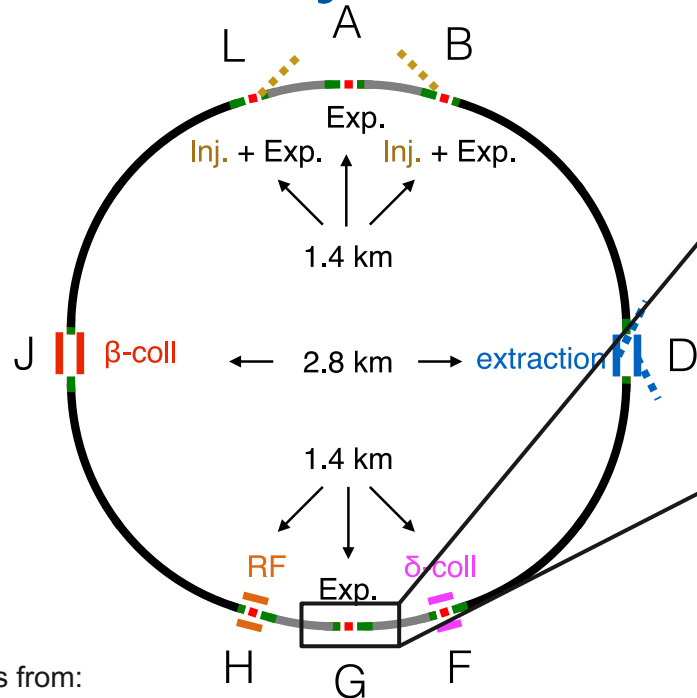
FCC Layout



Circumference: $C = 97.75$ km
Bending radius: $\rho = 10.5$ km

2 experimental straight sections (A & G)
2 RF sections in points D and J

FCC Layout



The layout of the booster follows the footprint of FCC-hh
 → inside the experiments

Images from:

D. Schulte, "New layout," Presentation in the FCC-hh General Design Meeting, Sep. 2016.

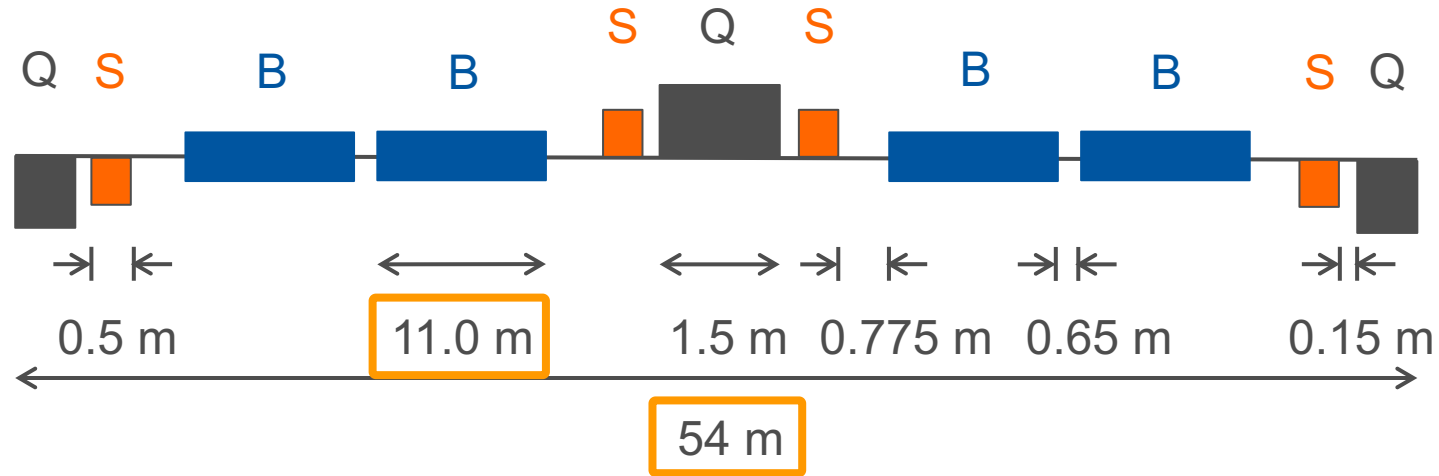
K. Oide *et al.*, "Design of beam optics for the future circular collider e+e- collider rings," Phys. Rev. Accel. Beams, vol. 19, p. 111005, Nov 2016.



Fields of progress

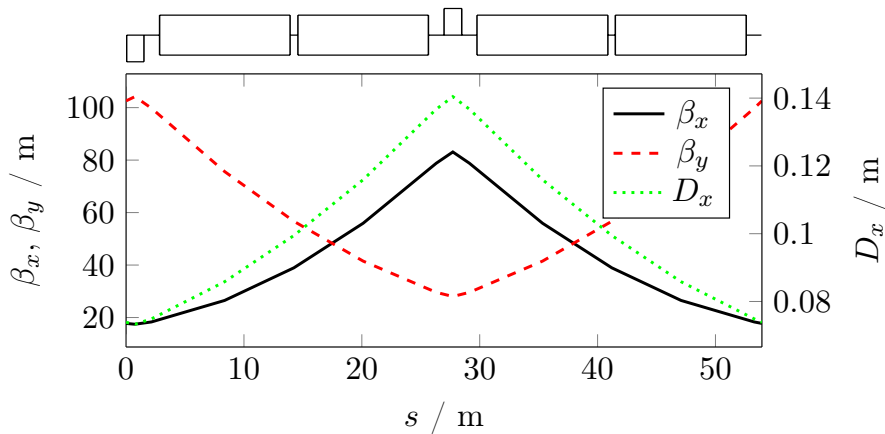
- Longer **FODO cell layout** in the arcs
- **Three optics** are investigated
- **Three sextupole schemes** & DA
- **Transverse misalignments** of quadrupoles

FODO cell of the FCC-ee booster



B = bending magnet, Q = quadrupole, S = sextupole

First optics for 80-175 GeV

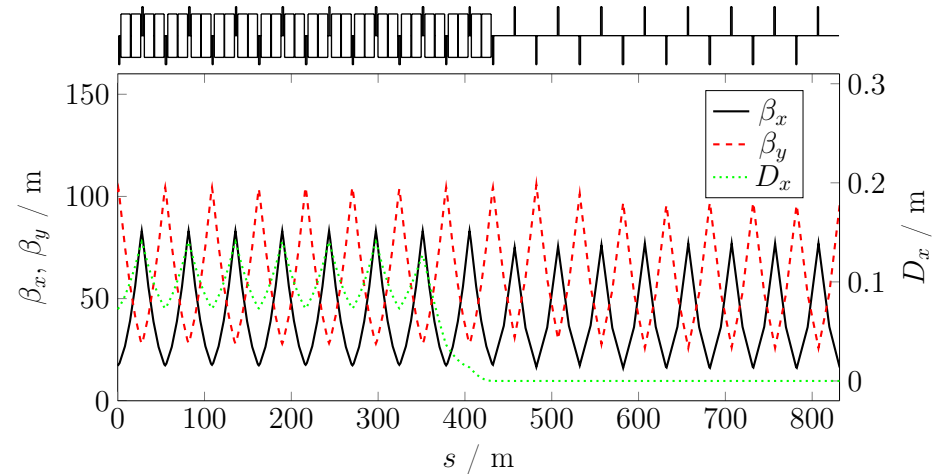


FODO cell:

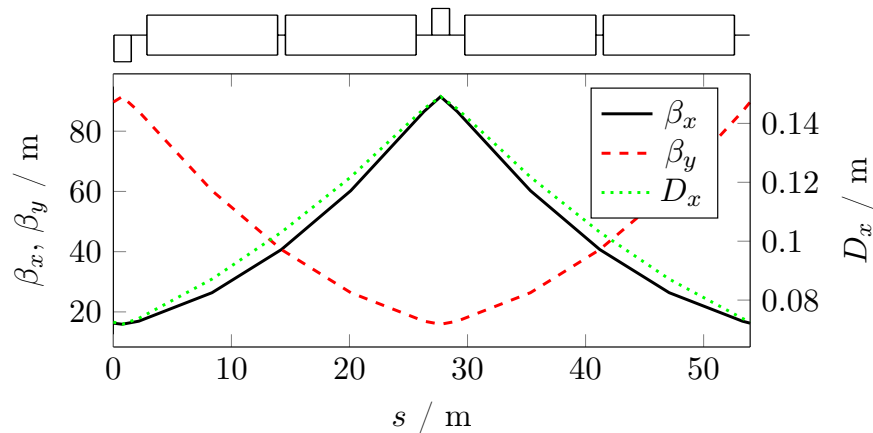
$L = 54$ m

$\varphi = 90^\circ/60^\circ$

**2-cell half-bend
dispersion suppressor**



Second optics for 80-175 GeV

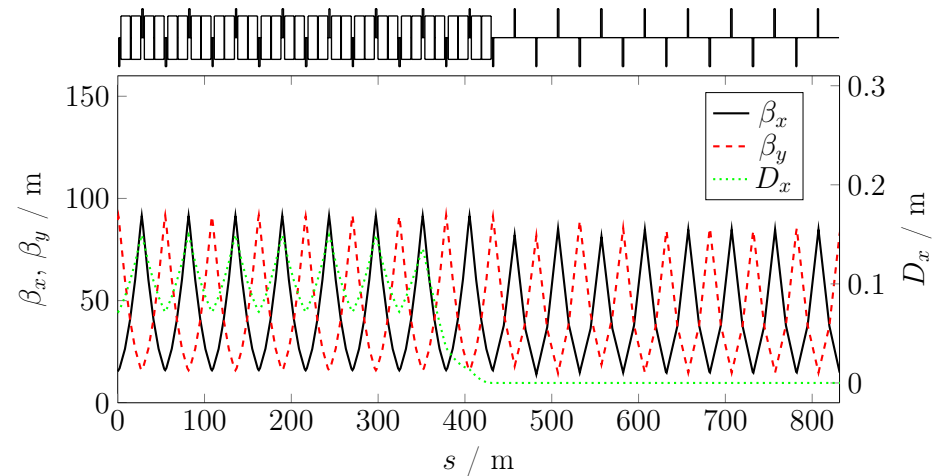


FODO cell:

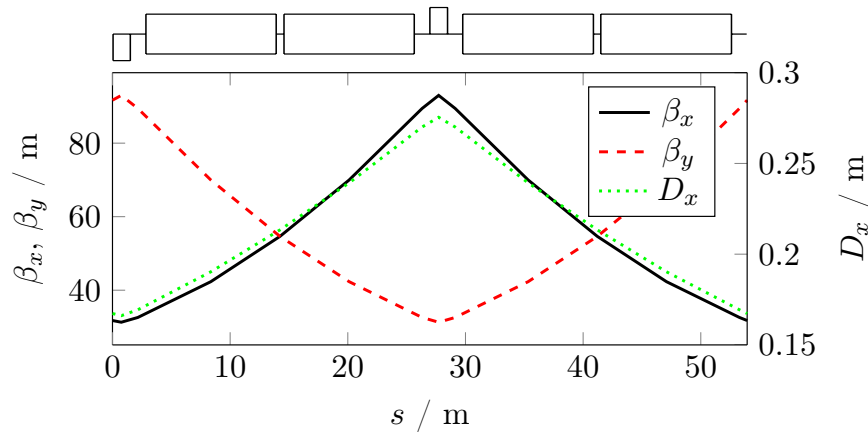
$$L = 54 \text{ m}$$

$$\varphi = 90^\circ/90^\circ$$

**2-cell half-bend
dispersion suppressor**



Optics for 45 GeV

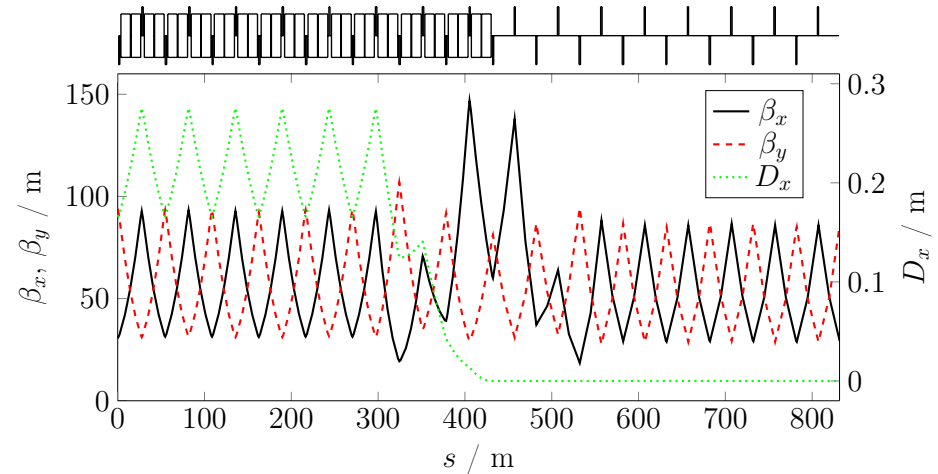


FODO cell:

$L = 54$ m

$\varphi = 60^\circ/60^\circ$

**Dispersion suppressor
supported by quadrupoles**



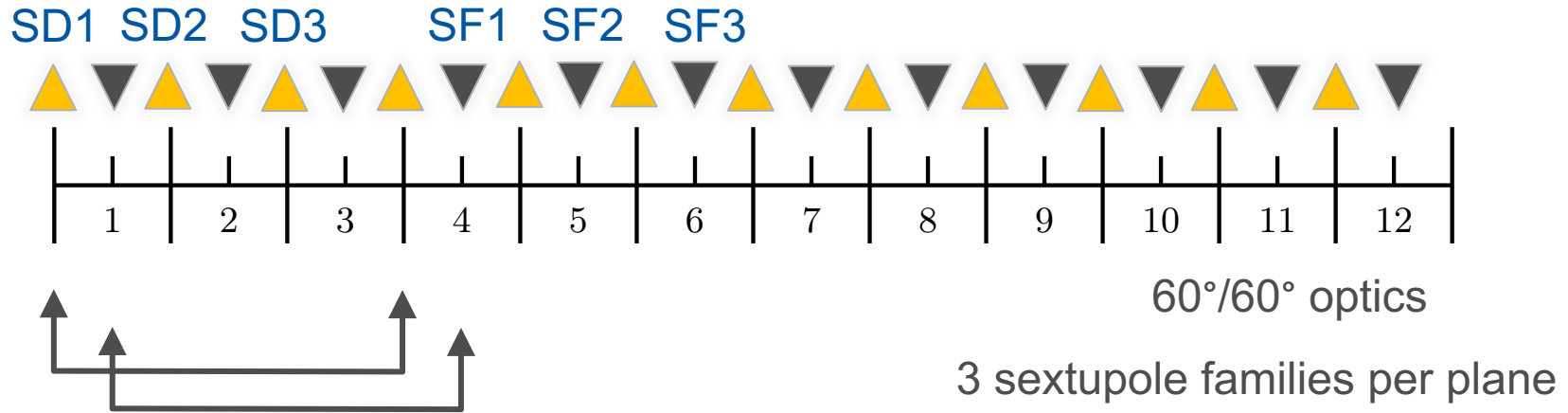
Parameters

	L = 50 m 90°/60°	L = 54 m 90°/60°	90°/90°	60°/60°
Q_x	487.08	457.225	459.225	306.225
Q_y	327.14	304.290	457.290	304.290
ξ_x	-542.010	-507.658	-584.643	-338.778
ξ_y	-450.449	-420.928	-582.910	-336.455
$\alpha_c / 10^{-6}$	5.6	6.5	6.7	13.7
ϵ_x (20 GeV)/nm rad	0.012	0.015	0.015	0.045
ϵ_x (45.5 GeV)/nm rad	0.062	0.075	0.078	0.235
ϵ_x (175 GeV)/nm rad	0.918	1.124	1.172	3.540

Dynamic aperture

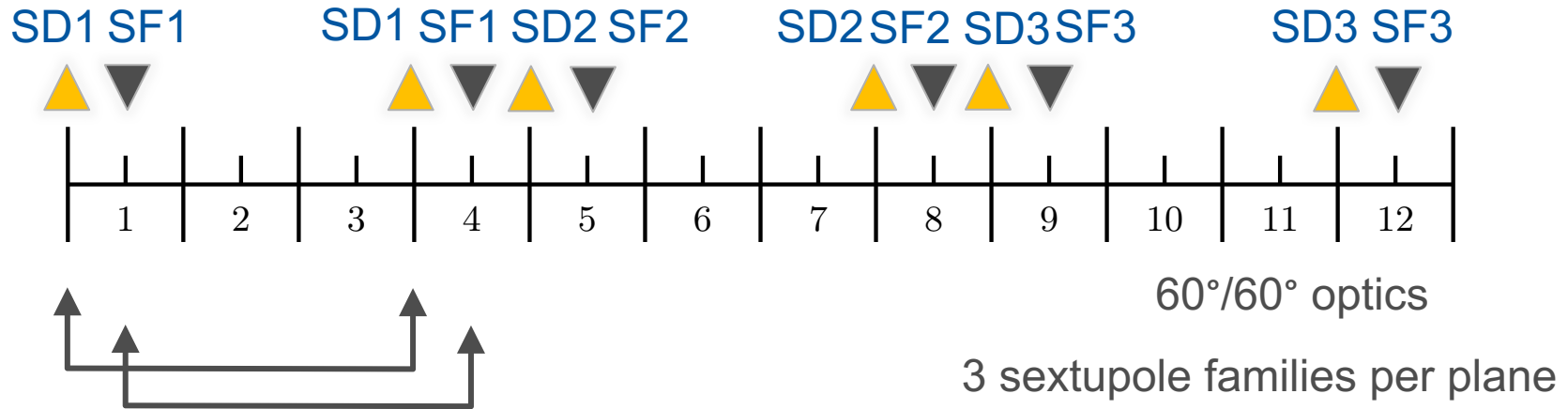
- All sextupoles in one plane are powered equally
- Only linear chromaticity corrected
- Different sextupole schemes:
 - interleaved
 - “partially” non-interleaved
 - “completely” non-interleaved

Interleaved sextupole scheme



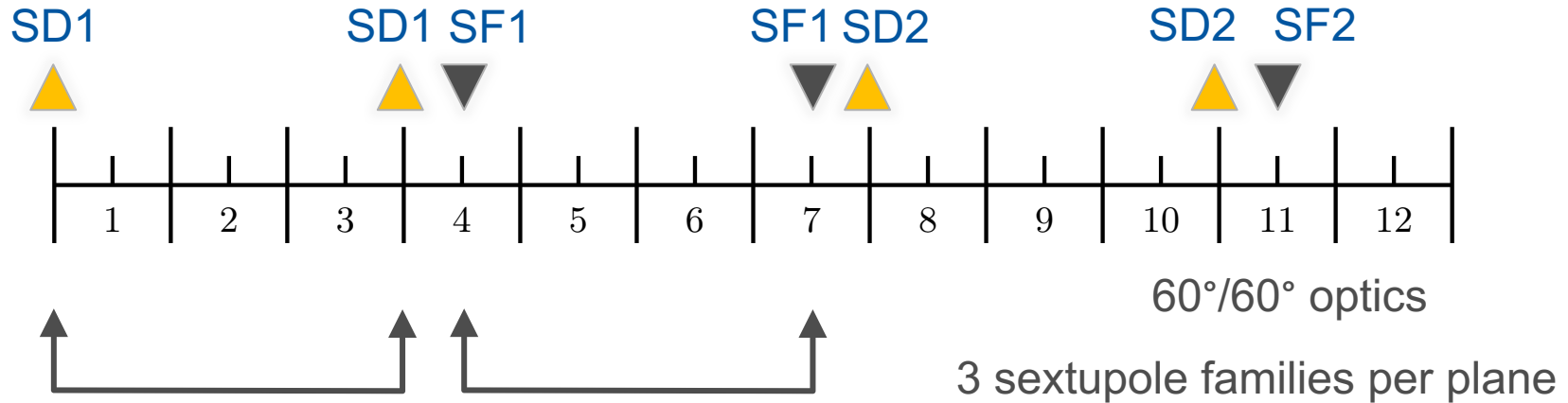
$$\mu_x = \mu_y = 180^\circ (\rightarrow -I \text{ transformation})$$

Partly non-interleaved sextupole scheme



$$\mu_x = \mu_y = 180^\circ (\rightarrow -I \text{ transformation})$$

Non-interleaved sextupole scheme



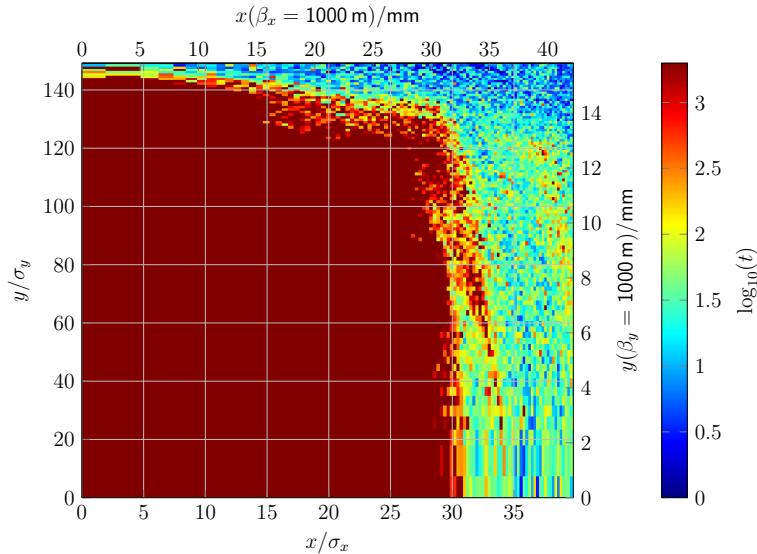
$$\mu_x = \mu_y = 180^\circ (\rightarrow -I \text{ transformation})$$

Dynamic aperture

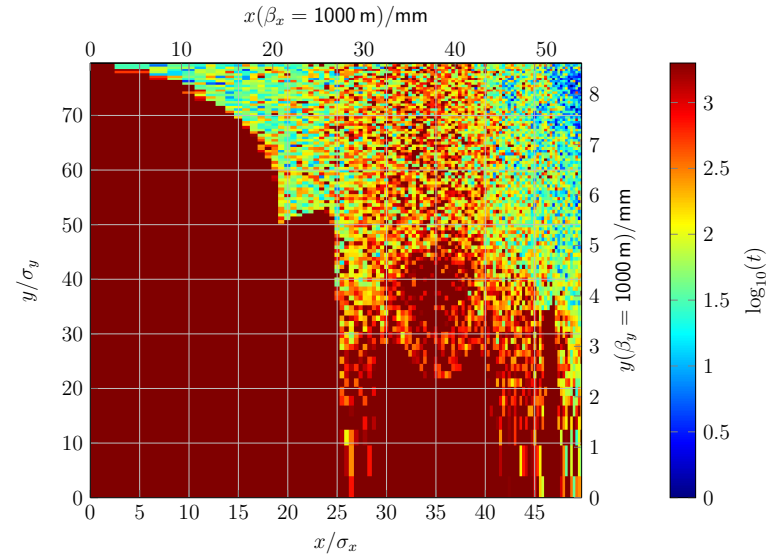
- Obtained through tracking with PTC
→ survival after 2000 turns
- No radiation, no damping
- Which sextupole scheme gives the best DA performance? → “completely” non-interleaved
- How large is the obtained DA?

Dynamic aperture (175 GeV)

Non-interleaved sextupole scheme, only linear chromaticity is compensated



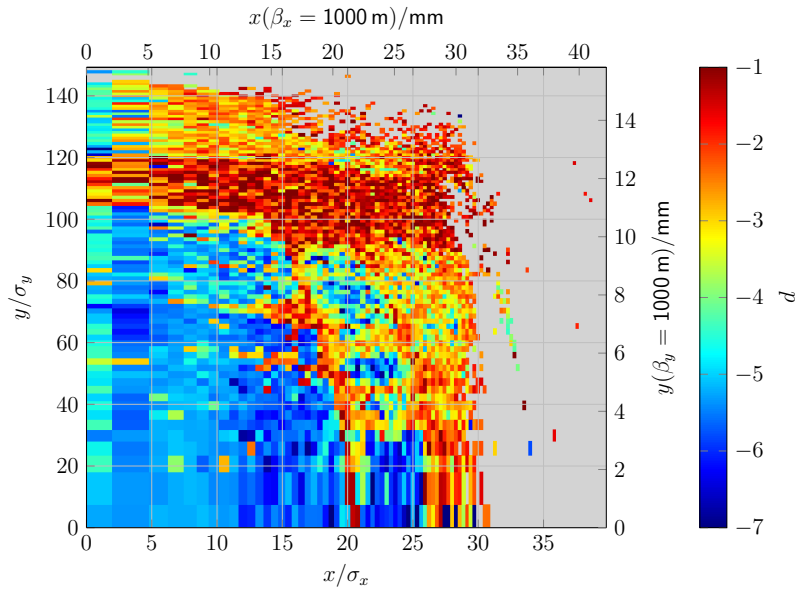
90°/60°



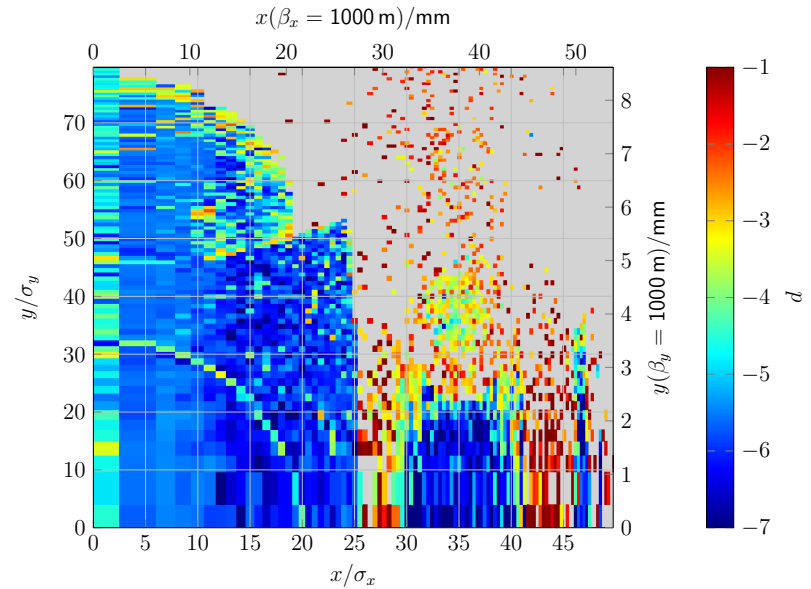
90°/90°

Diffusion rate

$$d = \log_{10} \left[\sqrt{(\nu_x^{(2)} - \nu_x^{(1)})^2 + (\nu_y^{(2)} - \nu_y^{(1)})^2} \right]$$

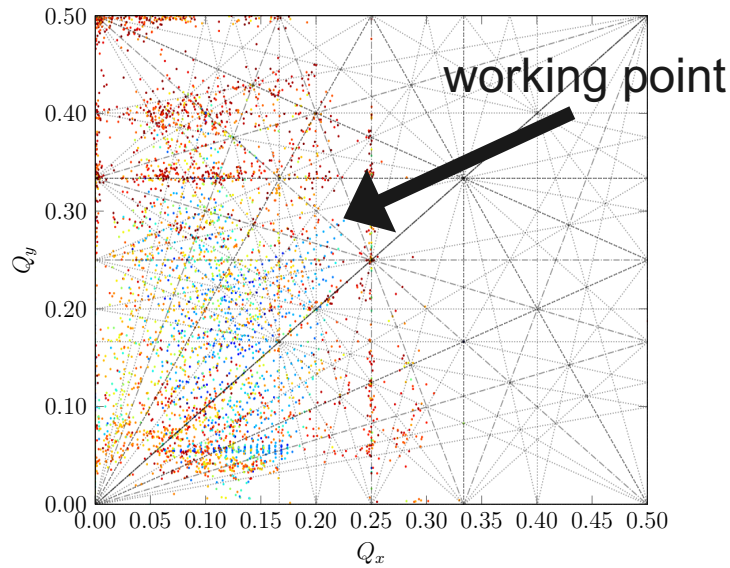


90°/60°

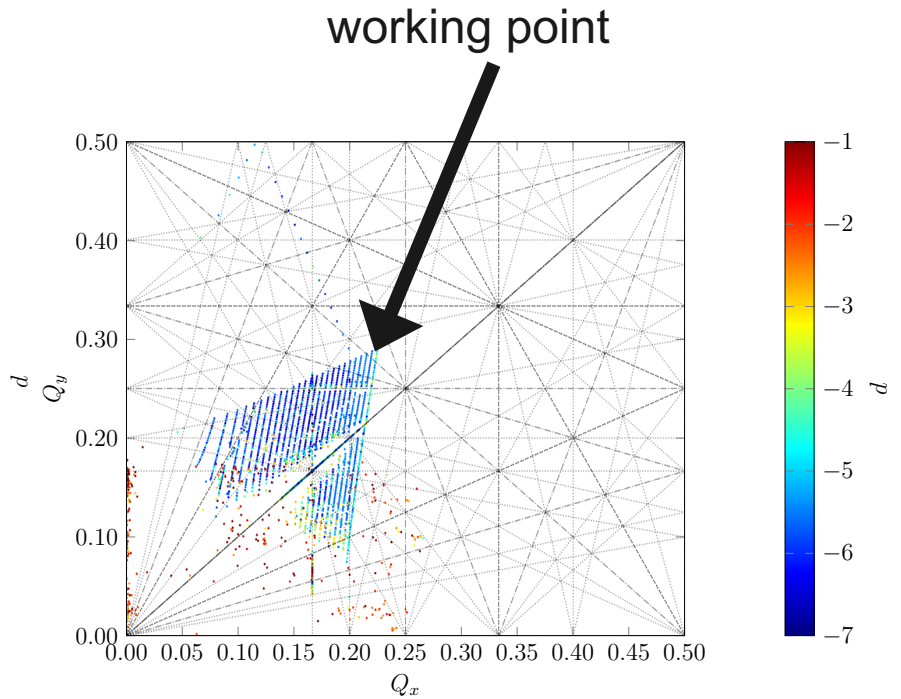


90°/90°

Tune footprint

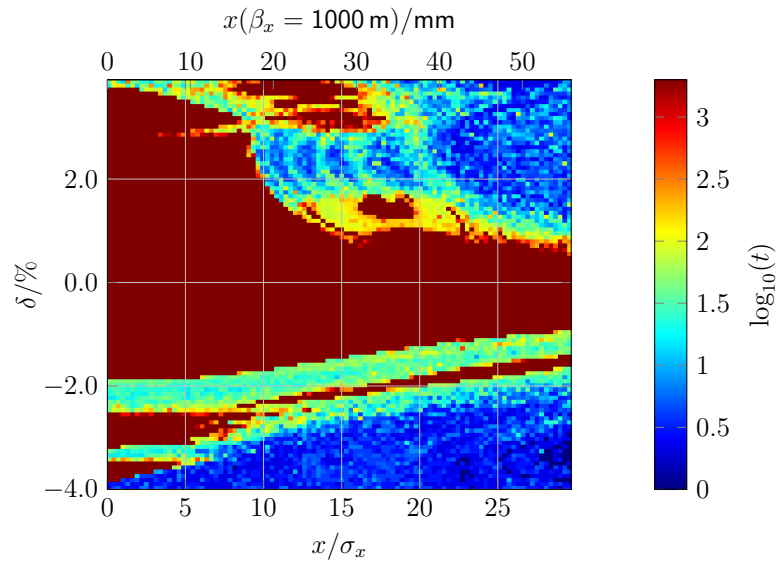
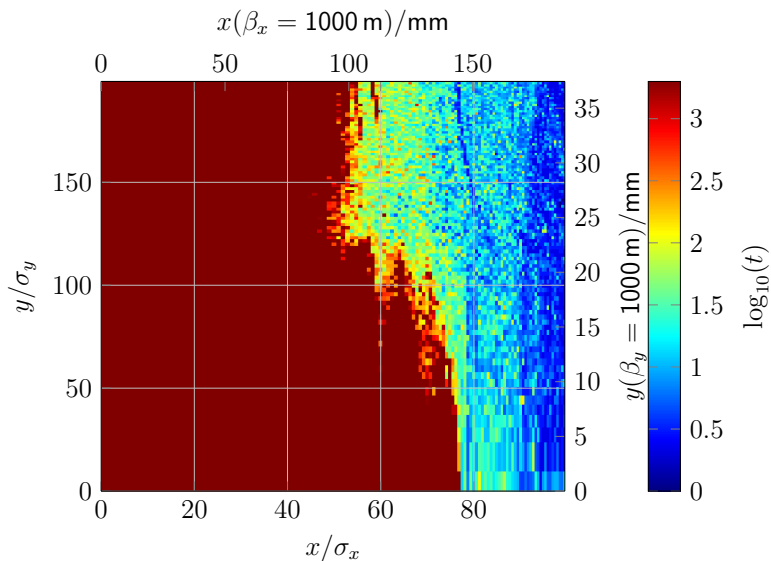


90°/60°



90°/90°

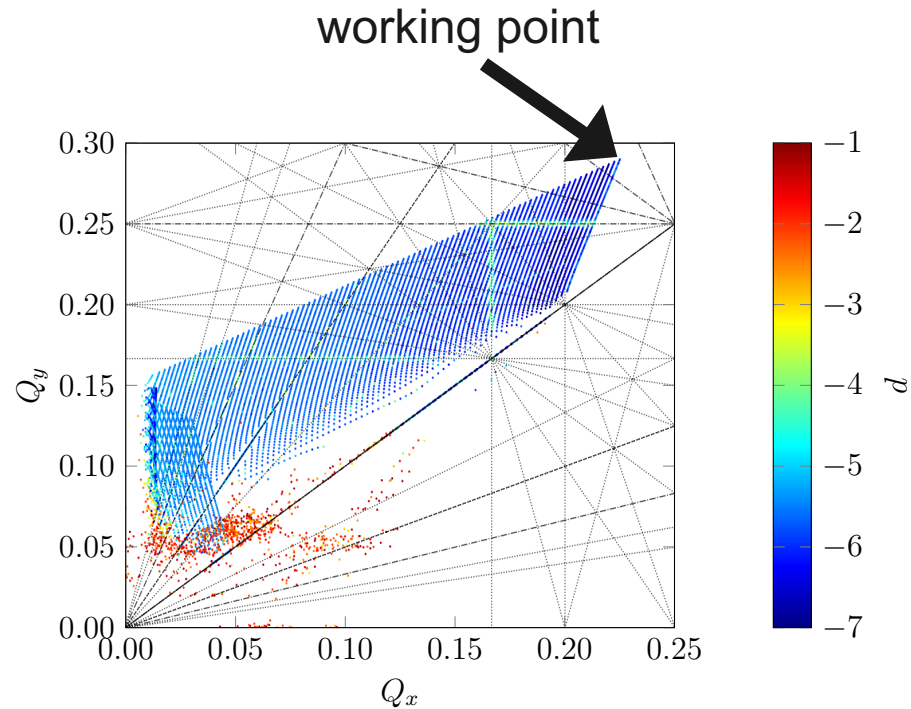
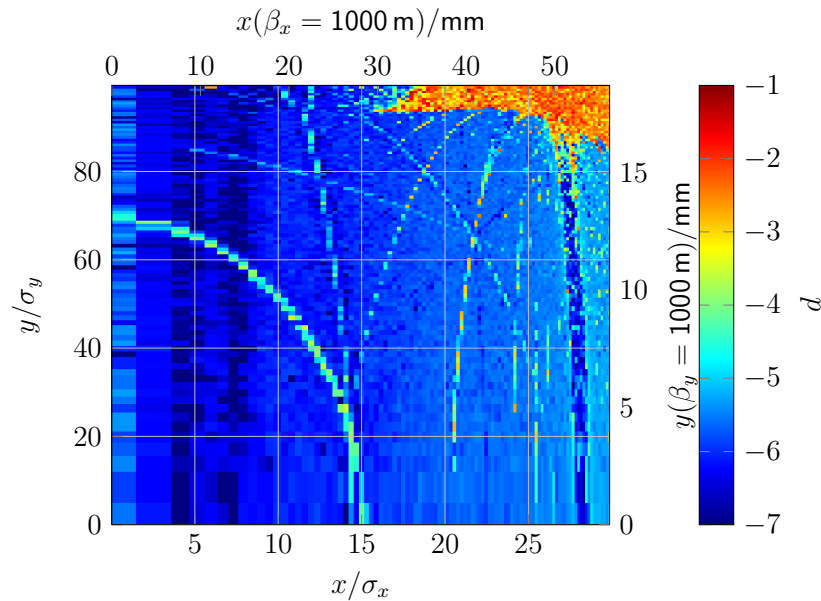
Dynamic aperture 60°/60° optics



Non-interleaved sextupole scheme
Only linear chromaticity is compensated

175 GeV

60°/60° optics



$$d = \log_{10} \left[\sqrt{(\nu_x^{(2)} - \nu_x^{(1)})^2 + (\nu_y^{(2)} - \nu_y^{(1)})^2} \right]$$

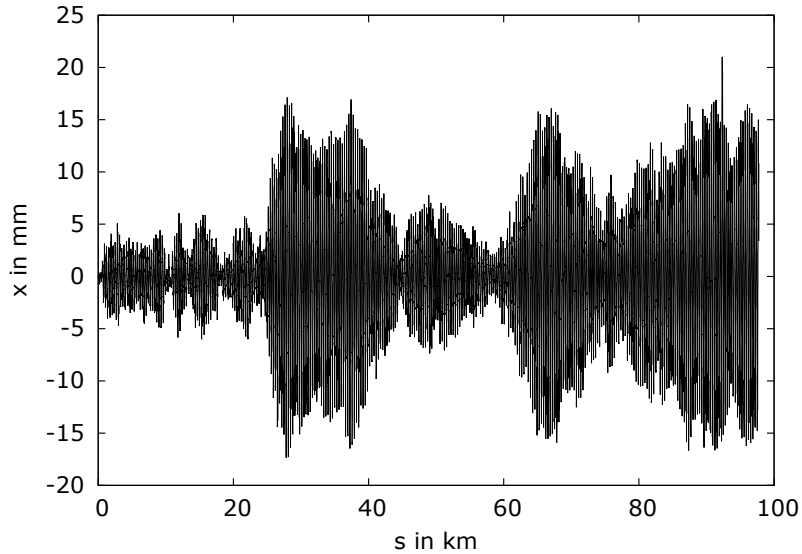
tune footprint

Transverse misalignments of quadrupoles

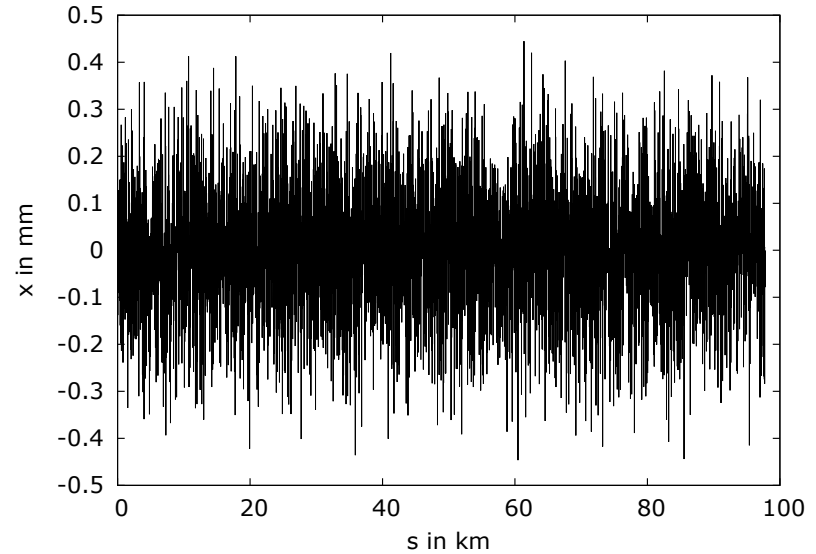
- Gaussian distributed, truncated at 3σ
- $10\ \mu\text{m}$, $50\ \mu\text{m}$, $100\ \mu\text{m}$ & $150\ \mu\text{m}$
- 100 seeds each
- Orbit correction in two iterations (SVD, micado)
- $60^\circ/60^\circ$ and $90^\circ/90^\circ$ optics with non-interleaved sextupole scheme

Horizontal orbit

150 μm , seed 1000

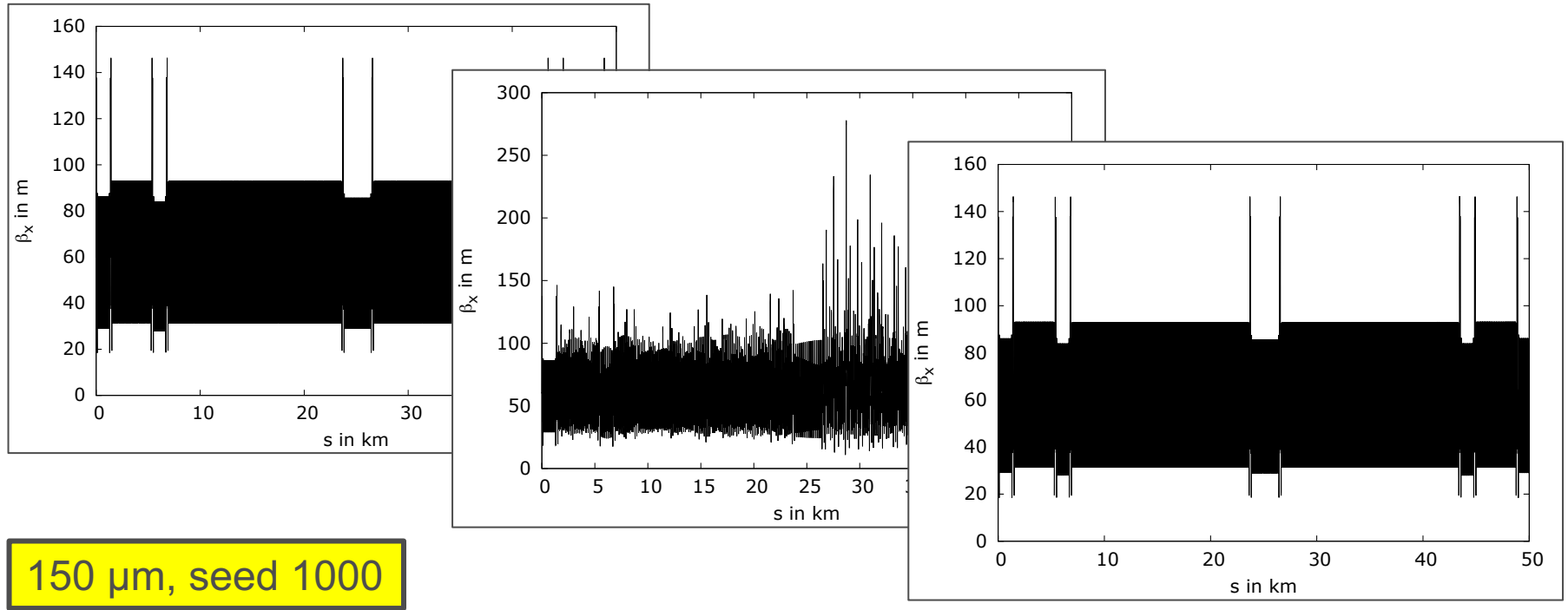


before orbit correction



after orbit correction

Optics distortions (60°/60°)



150 μm , seed 1000

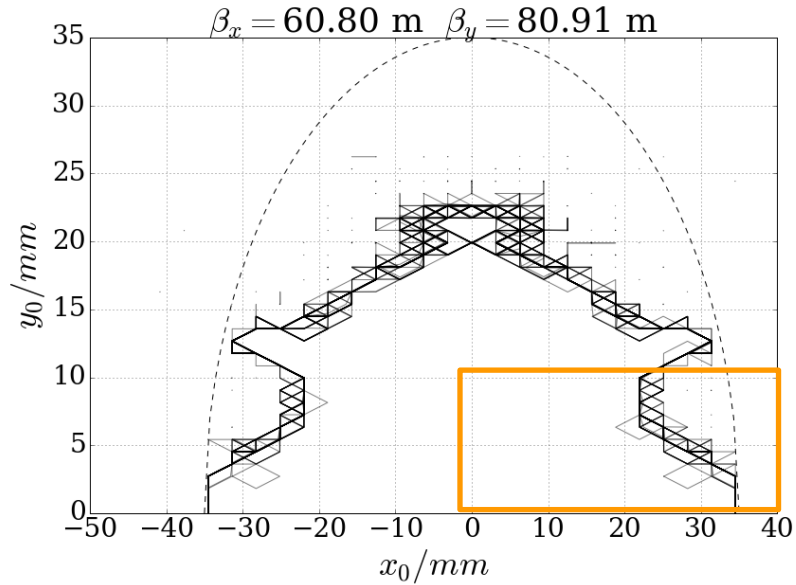
Emittances (60°/60°)

	Ideal ϵ_x /nm rad	Misaligned ϵ_x /nm rad
20 GeV	0.045	0.045
45 GeV	0.230	0.230
175 GeV	3.642	3.640

	Misaligned ϵ_y /nm rad	ϵ_y/ϵ_x
20 GeV	4.4×10^{-7}	9.8×10^{-6}
45 GeV	2.3×10^{-6}	9.9×10^{-6}
175 GeV	4.0×10^{-5}	1.1×10^{-5}

- No coupling from sextupole misalignment or roll angles considered yet

DA with misalignments

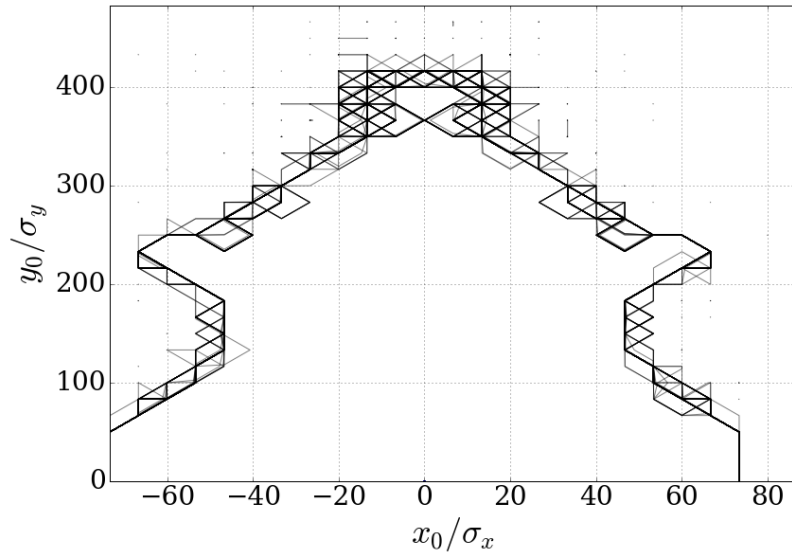


- $60^\circ/60^\circ$ optics
- $150 \mu\text{m}$
- 100 seeds

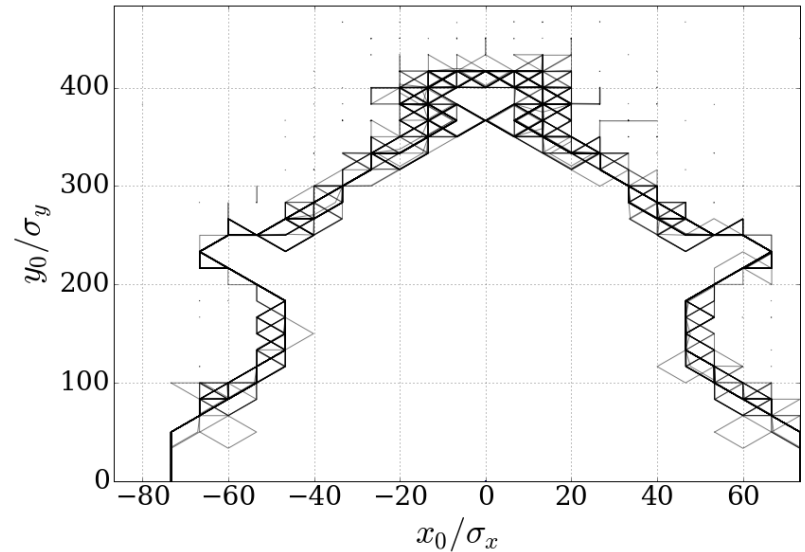
Previously shown part:

→ No reduction of DA because of transverse misalignments

DA with misalignments

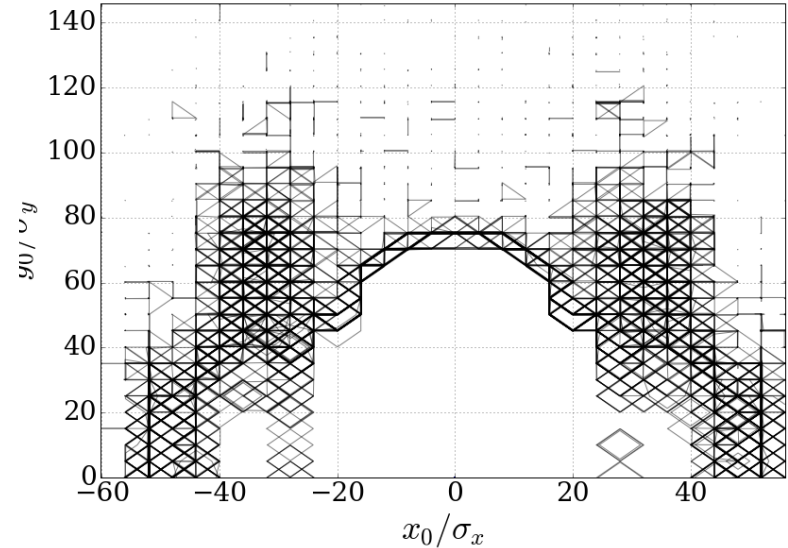
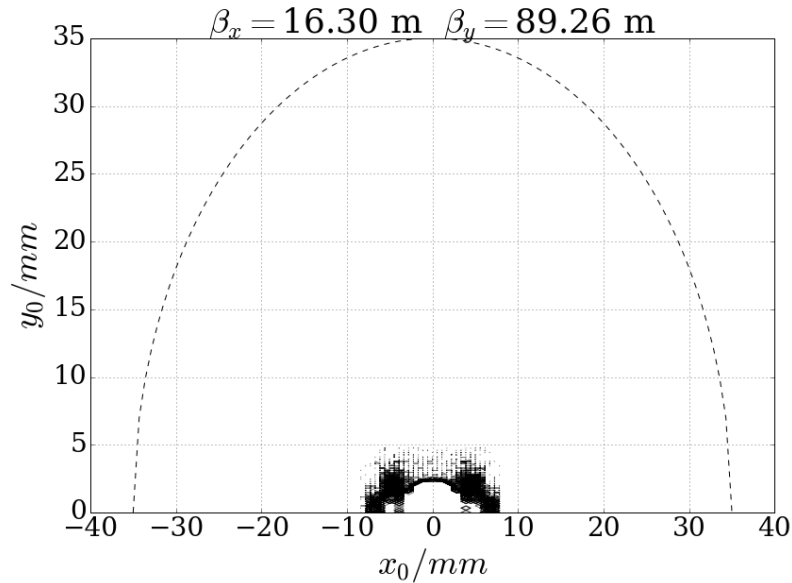


10 μm , 100 seeds



150 μm , 100 seeds

DA with misalignments II



- $90^\circ/90^\circ$ optics: $150 \mu\text{m}$, 100 seeds

Summary

- Lattice with 54 m cell length in the arcs provides **larger momentum compaction factor**
- **Three different optics** are considered: $90^\circ/60^\circ$, $60^\circ/60^\circ$ & $90^\circ/90^\circ$
- **25-75 σ dynamic aperture for all optics**
 - Multi-family sextupole scheme allows to modify higher orders of chromaticity and detuning with amplitude, if needed
- Transverse misalignments **of quadrupoles create no considerable optics distortions**

Next steps

- Contribution to coupling from roll angles and sextupole misalignments
- More realistic RF scheme
→ are there news?
- Estimation of instabilities due to low beam energy and small vertical emittance
→ Touschek effect, what else?

Thank you for your attention!

Acknowledgements:

Thanks to T. Tydecks for the tracking calculations!

Detuning with amplitude

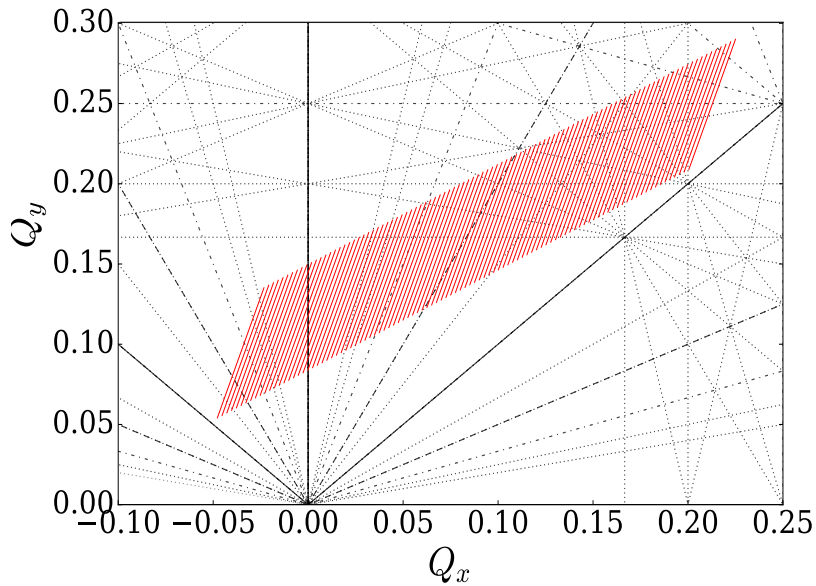
- Detuning in first order given by

$$Q_x = Q_{x,0} + \alpha_{xx}J_x + \alpha_{xy}J_y$$

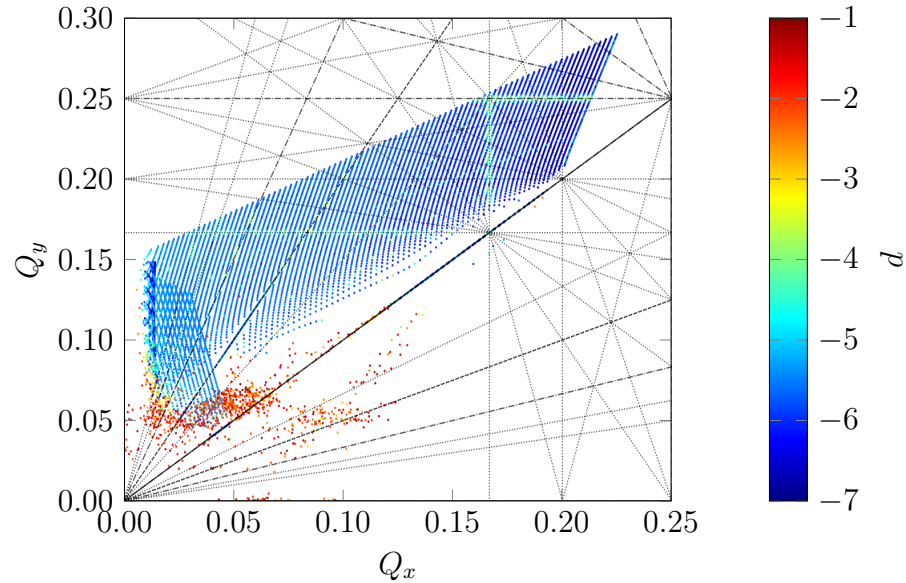
$$Q_y = Q_{y,0} + \alpha_{yx}J_x + \alpha_{yy}J_y$$

- α_{ij} are the detuning coefficients, J the action
- Detuning coefficients (also higher orders) can be quickly calculated with PTC_normal

Tune footprints of 60°/60° optics



Analytic calculation based on first order PTC_normal results



Tracking results