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# Conclusions

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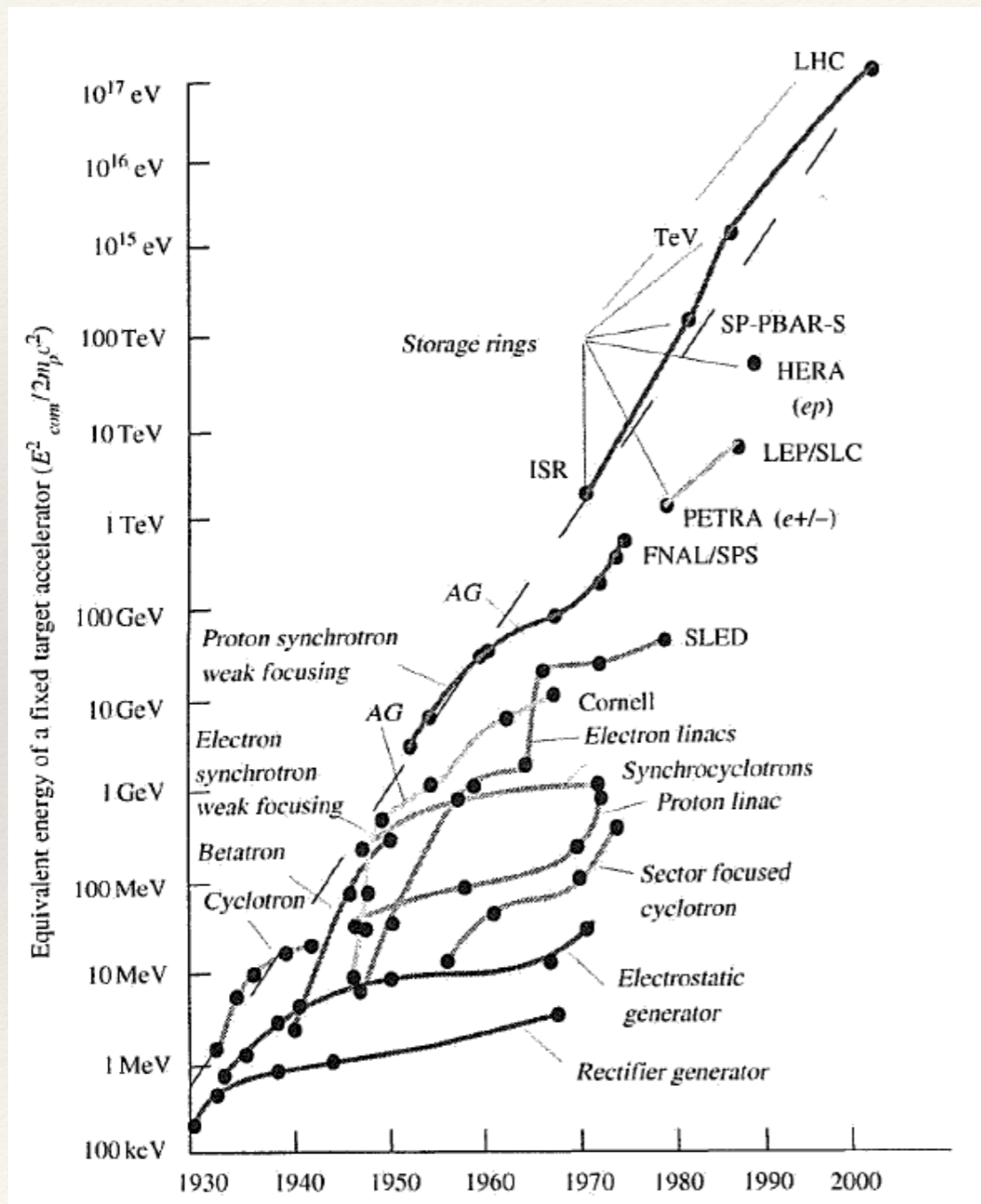
Pisa Future Colliders School,  
17-21 September 2018



R. Keith Ellis  
IPPP, Durham



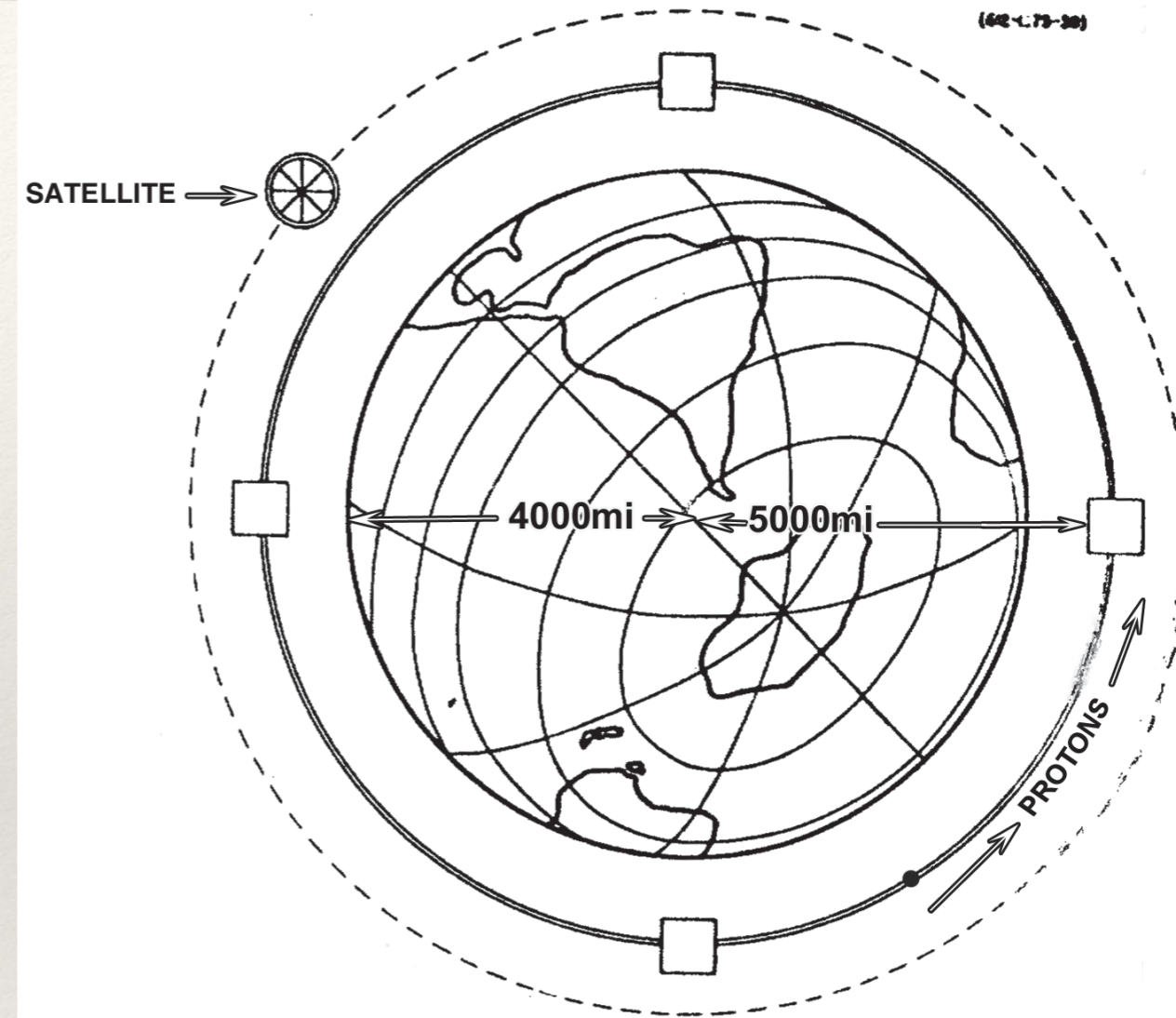
# The continuation of a 90-year adventure



- ❖ Accelerator progress over 90 years,
- ❖ For the colliders, the energy has been expressed in terms of the energy of an equivalent fixed target machine

# Global Accelerator (mark1)

- ❖ In January 1954, Enrico Fermi made a presentation in New York, on the occasion of Fermi stepping down as president of the APS, and being replaced by Bethe. The title of the presentation was **What can we learn from High-Energy Accelerators?** The following are quotations from Fermi's notes.
- ❖ Fermi starts off by "Congratulate Society on Loosing(sic) mediocre President and getting excellent(sic) one."
- ❖ "But to solve the mysteries, higher energy data are needed."
- ❖ "But cosmic rays above 25 GeV only at one per cm<sup>2</sup> at an inconvenient location."
- ❖ "For these reasons clamoring for higher and higher energies.."
- ❖ "Preliminary design...8000 km, 20,000 gauss" (2 Tesla)
- ❖ "Energy of  $5 \times 10^6$  GeV, cost \$170 Billion"
- ❖ "What we can learn impossible to guess. . .main element surprise. . .some things look for, but see others"
- ❖ ". . .Look for multiple production. . .antinucleons.. .strange particles. . .puzzle of long lifetimes. . .large angular momentum? . . .double formation?" (now called associated production).
- ❖ Fermi died in November 1954.



JAN. 29, 1954

FRIDAY AFTERNOON AT 2:00

McMillin Theatre

(H. A. BETHE AND P. E. KLOPSTEG presiding)

Joint Ceremonial Session of the APS and the AAPT

Retiring Presidential Address of the American Physical Society

P1. What Can We Learn with High-Energy Accelerators? ENRICO FERMI, University of Chicago.

Presentation of the Oersted Medal of the AAPT

Response of the Oersted Medallist

P2. The Metaphysics of a Physics Teacher. C. N. WALL, University of Minnesota.

# Bending magnetic field

❖ A synchrotron has a bending field produced by several magnets

❖ Field changes as momentum increases to keep particles in fixed orbit.

$$\frac{mv^2}{\rho} = evB \quad \implies p = eB\rho$$

❖ Balance of centrifugal force and Lorentz force for bending radius  $\rho$

$$\frac{pc}{e} [eV/c] = c [m/s] B [T] \rho [m] \quad \implies (pc/e) [TeV/c] = 0.299 B [T] \rho [km]$$

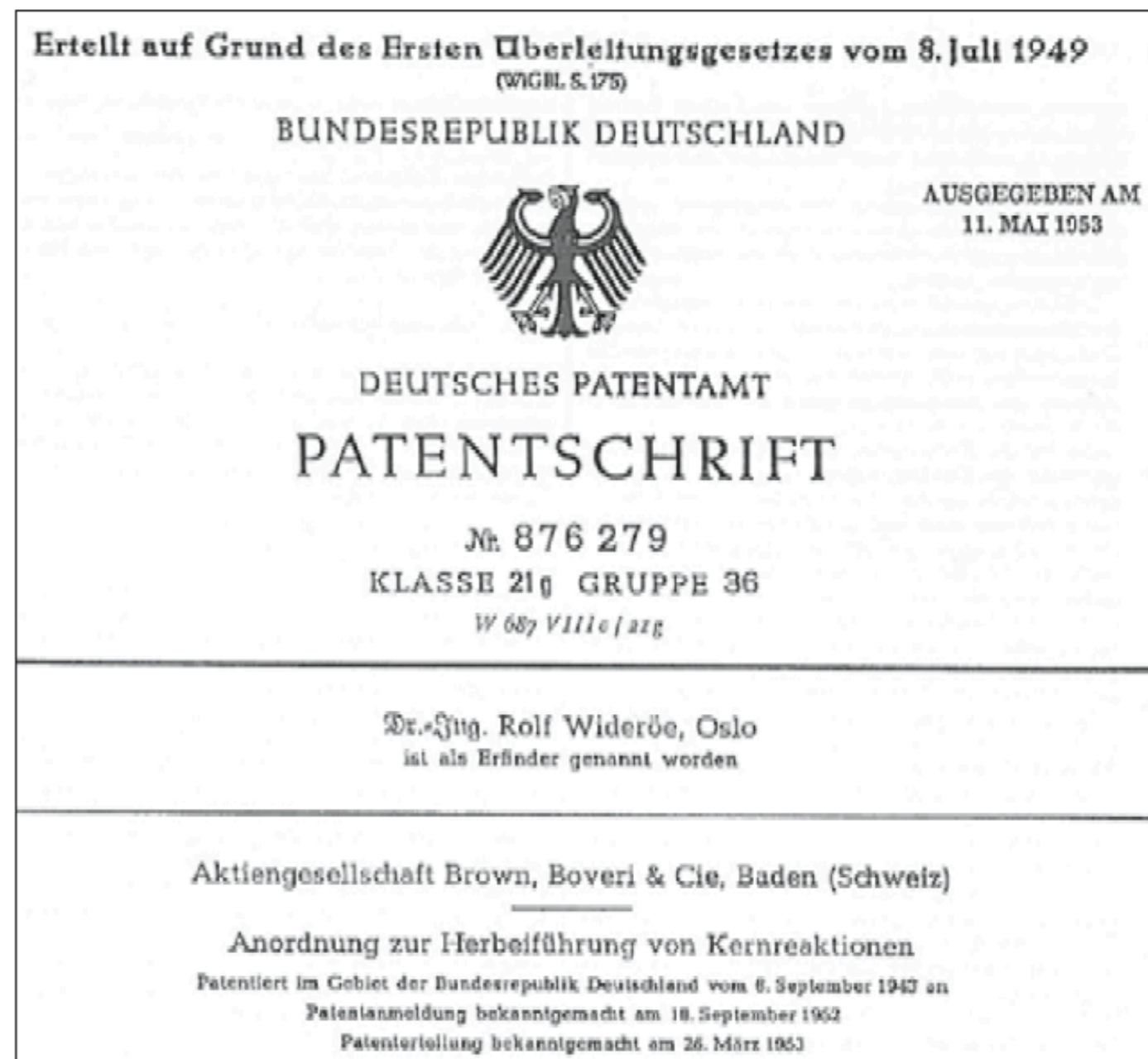
	p[TeV/c]	B[T]	$\rho$
Fermi Machine	5000	2	8000[km]
LHC14	7.0	8.33	2,800[m]
LHC27	13.5	16	2,800[m]
$\mu$ -Higgs factory	0.0625	8.33	50[m]
$\mu$ -collider	0.625	8.33	500[m]
100TeVpp	50	16	10.4[km]

Table 1: Bending radius of various proposed machines

Continuous (superconducting) magnetic fields have a practical limitation to ~20-30T.

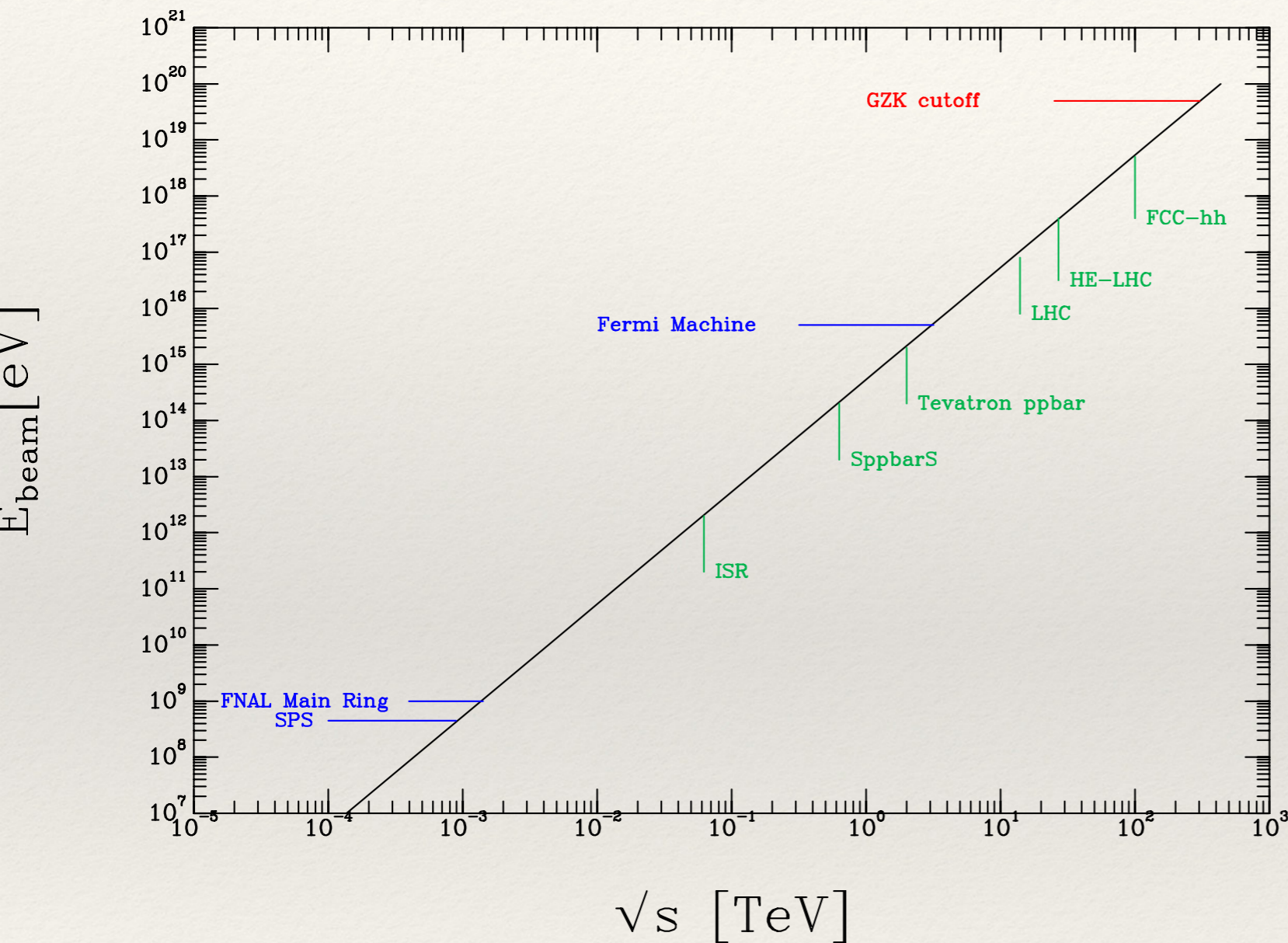
# Higher energies, higher fields

- ❖ Norwegian, Rolf Wideroe's German patent of 1943, (published only in 1953....), introduced the collider concept.
- ❖ (The first successful superconducting magnet was built by using niobium wire and achieved a field of 0.71T at 4.2K in 1954).
- ❖ Power consumption limits conventional magnets to about ~2T



**Fig. 1:** The patent of R. Wideroe introducing colliding beams

# The power of the collider technique

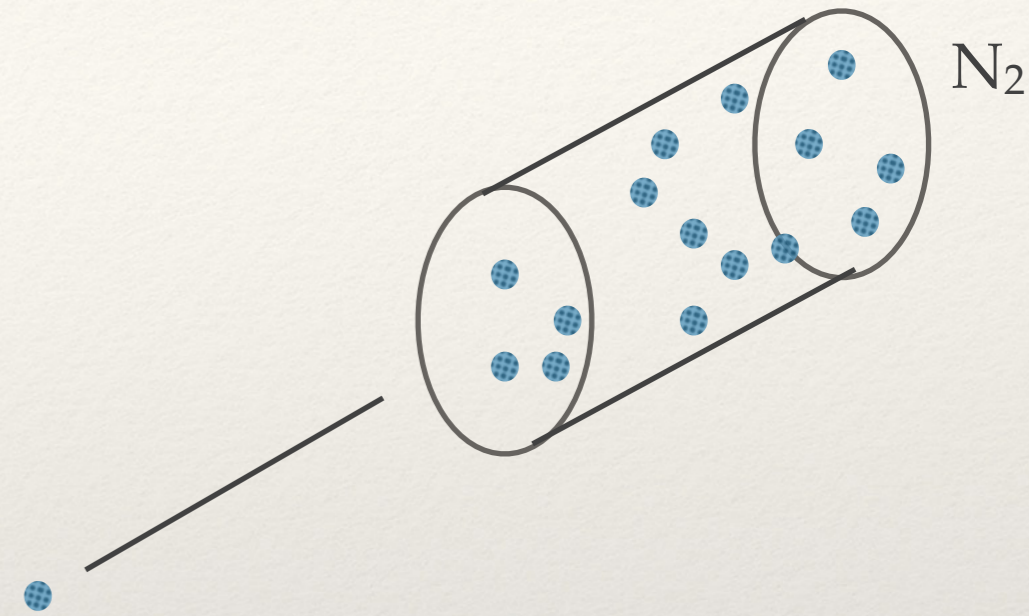


(The Greisen–Zatsepin–Kuzmin limit (GZK limit) is a theoretical upper limit on the energy of cosmic ray protons travelling from other galaxies through the intergalactic medium to our galaxy. The limit is set by slowing-interactions of the protons with the microwave background radiation over long distances ( $\sim 160$  million light-years)).

Current and future colliders have c.o.m energies fixed above that of the Fermi Machine, thanks to the colliding beam technique and the development of superconducting magnets.

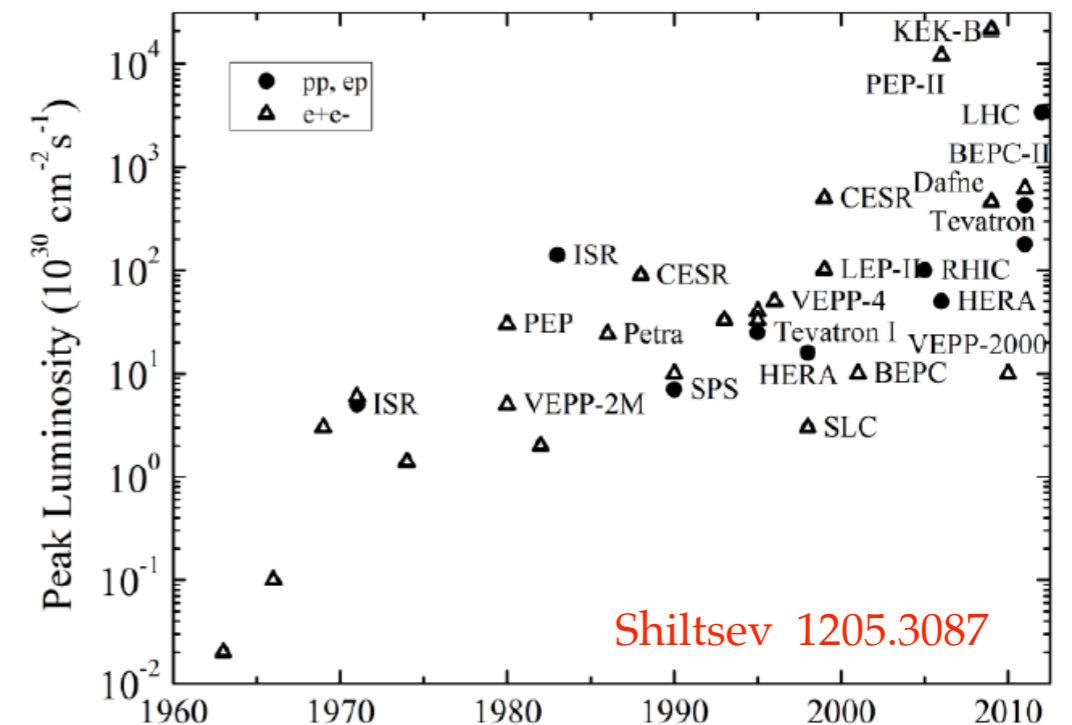
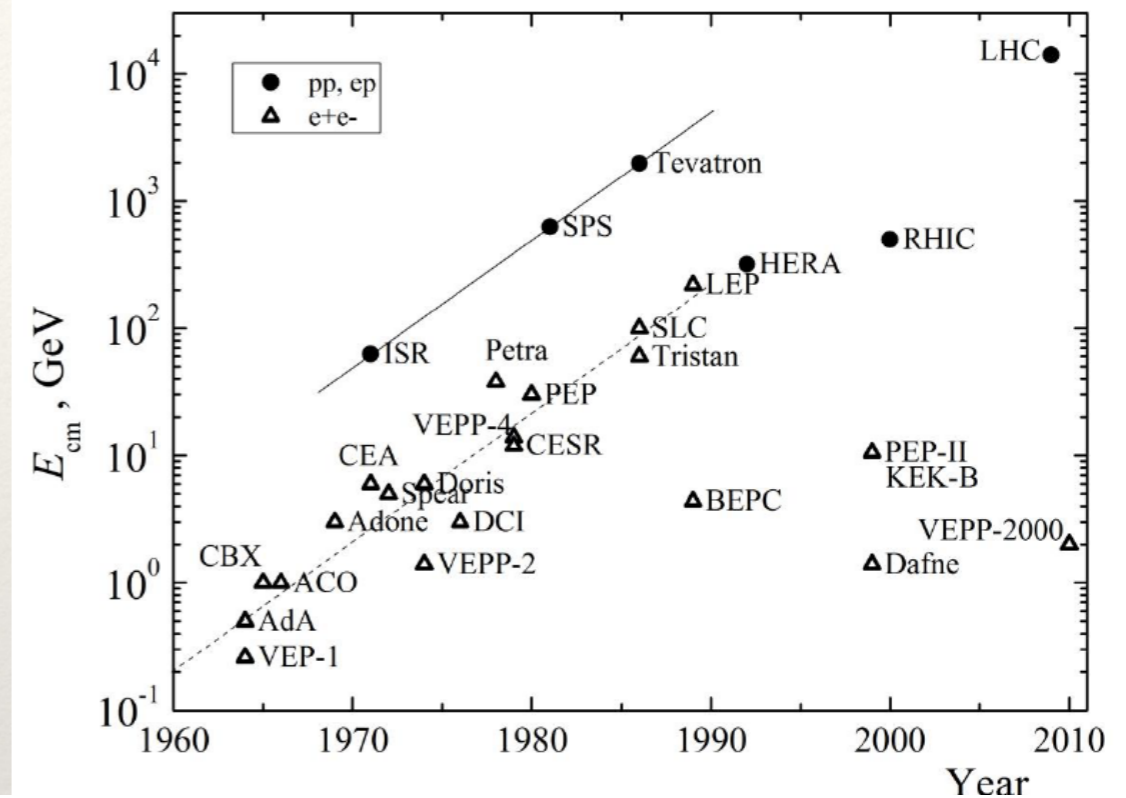
# Luminosity

- ❖ Cylindrical bunches have a cross sectional area  $A$  and contain  $N_1, N_2$  particles
- ❖ A given particle in Bunch 1 will interact with a fraction  $N_2 \frac{\sigma_{int}}{A}$
- ❖ Total number of such interactions is  $\frac{N_1 N_2 \sigma_{int}}{A}$
- ❖ If the frequency of bunch interactions is  $f$ , then the interaction rate is  $R = f \frac{N_1 N_2}{A} \sigma_{int}$
- ❖ Defining  $R = \mathcal{L} \sigma_{int}$  the luminosity per bunch is  $\mathcal{L} = f \frac{N_1 N_2}{A}$
- ❖ More sophisticated calculation for Gaussian beams, colliding head-on,  $N_b$  number of bunches gives  $\mathcal{L} = f \frac{N_1 N_2 N_b}{4\pi\sigma_x\sigma_y}$
- ❖  $\sigma_x, \sigma_y$  are the transverse sizes of the Gaussian.



# Credo

- ❖ Accelerator-based particle physics is the fundamental core of our subject - allows us to perform reproducible experiments.
- ❖ Historical precedent: 100-fold increase in energy for both hadron and lepton colliders (in ~60 years) accompanied by a similar increase in luminosity.
- ❖ Progress in the field will continue to require colliders with high energy and high luminosity.
- ❖ Does our advanced technological civilisation have another high-energy collider in its future? Certainly, yes.
- ❖ How, when and where?

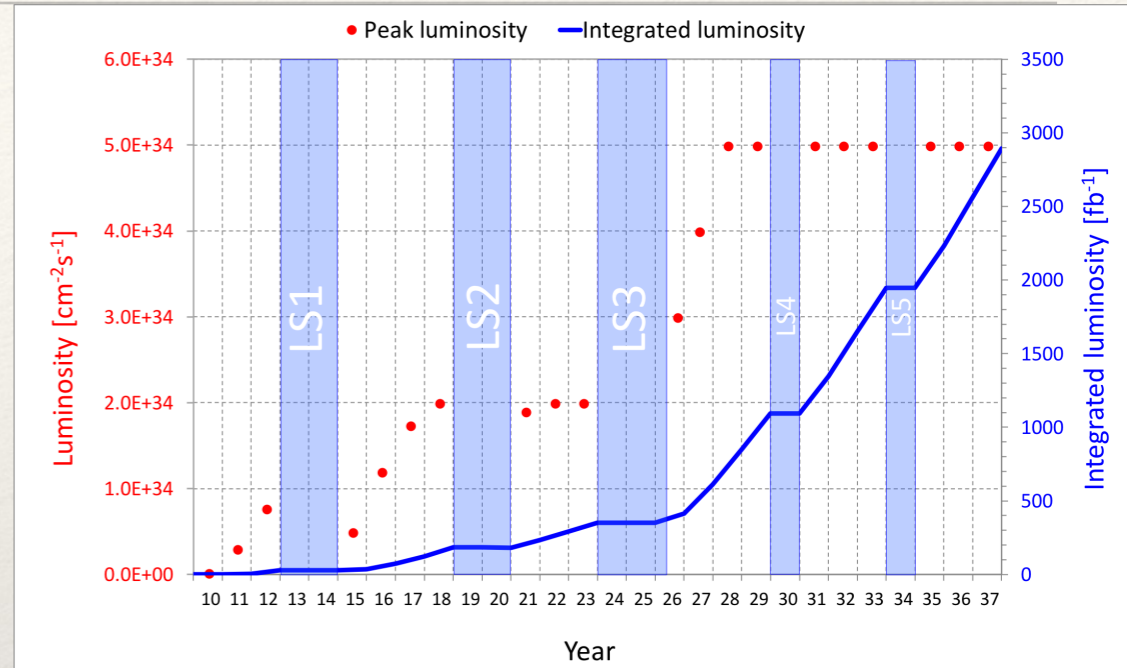


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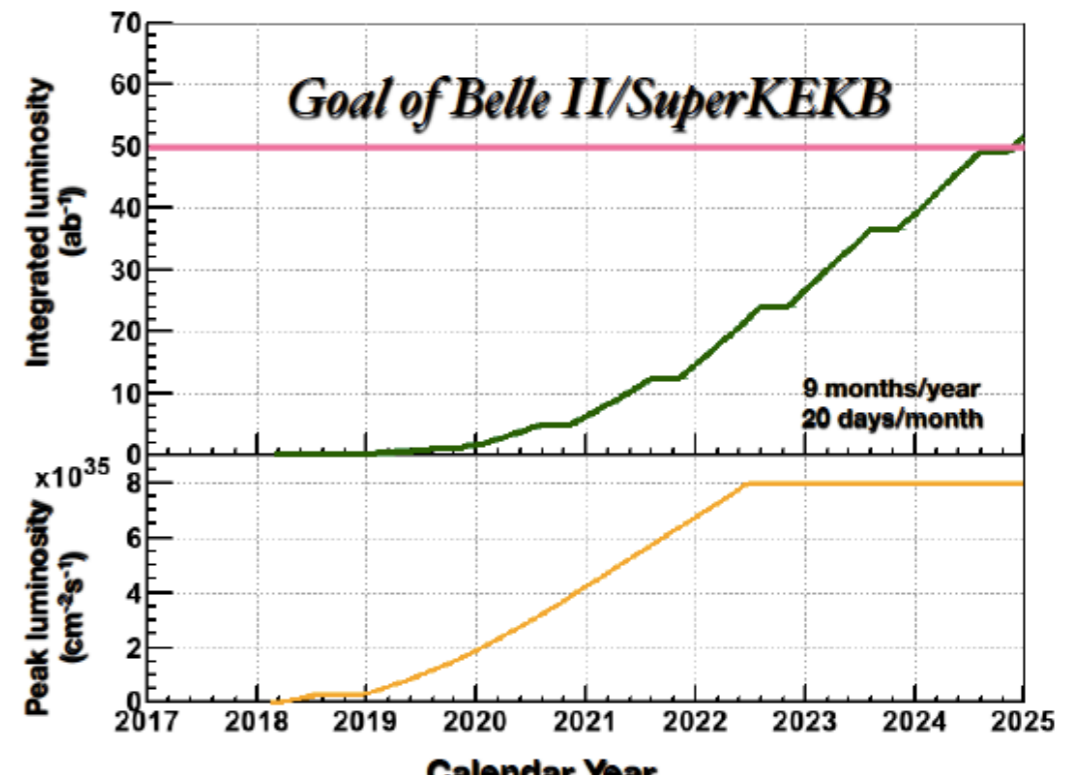


# Credo, part II

- ❖ The “short-term” future looks good too.
- ❖ HL-LHC will run from 2026-2037 (~20 years=half of an academic career).
  - ❖ HL-LHC includes dipole & quadrupole magnets based on Nb<sub>3</sub>Sn and crab cavities, both of which are important technical steps for the future.
- ❖ SuperKEKB now in operation, goal 50ab<sup>-1</sup>
- ❖ Exploration of the rare as well as the high energy, c.f. DUNE, start 2025



## SuperKEKB luminosity projection



Fermilab Program Planning 5-April-18

LONG-RANGE PLAN

		FY18	FY19	FY20	FY21	FY22	FY23	FY24	FY25	FY26	FY27	FY28	FY29	FY30
LBNF / PIP II	SANFORD FNAL				DUNE	DUNE	DUNE	DUNE	DUNE	DUNE	DUNE	DUNE	DUNE	DUNE
					LBNF	LBNF	LBNF	LBNF	LBNF	LBNF	LBNF	LBNF	LBNF	LBNF
NuMI	MI	MINERvA	MINERvA	NOvA	NOvA	NOvA	NOvA	NOvA	NOvA	NOvA	NOvA	NOvA	NOvA	NOvA
BNB	B	μBooNE	μBooNE	μBooNE	OPEN	OPEN	OPEN	OPEN	OPEN	OPEN	OPEN	OPEN	OPEN	OPEN
		CARUS	CARUS	CARUS	CARUS	CARUS	CARUS	CARUS	CARUS	CARUS	CARUS	CARUS	CARUS	CARUS
		SBND	SBND	SBND	SBND	SBND	SBND	SBND	SBND	SBND	SBND	SBND	SBND	SBND
Muon Complex		g-2	g-2	g-2										
		Mu2e	Mu2e	Mu2e	Mu2e	Mu2e	Mu2e	Mu2e	Mu2e	Mu2e	Mu2e	Mu2e	Mu2e	Mu2e
SY 120	MT	FTBF	FTBF	FTBF	FTBF	FTBF	FTBF	FTBF	FTBF	FTBF	FTBF	FTBF	FTBF	FTBF
	MC	FTBF	FTBF	FTBF	FTBF	FTBF	FTBF	FTBF	FTBF	FTBF	FTBF	FTBF	FTBF	FTBF
	NM4	OPEN	E1039	E1039	E1039	E1039	OPEN	OPEN	OPEN	OPEN	OPEN	OPEN	OPEN	OPEN

■ Construction / commissioning   
 ■ Run   
 ■ Subject to PAC review   
 ■ Shutdown

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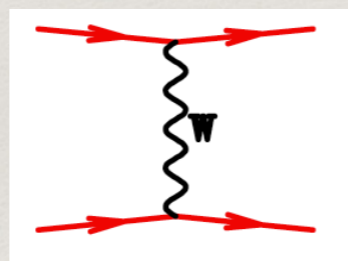
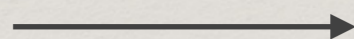
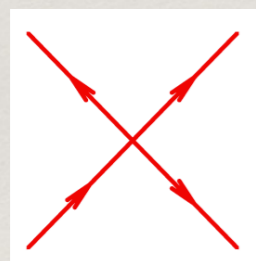
# A question of scale?

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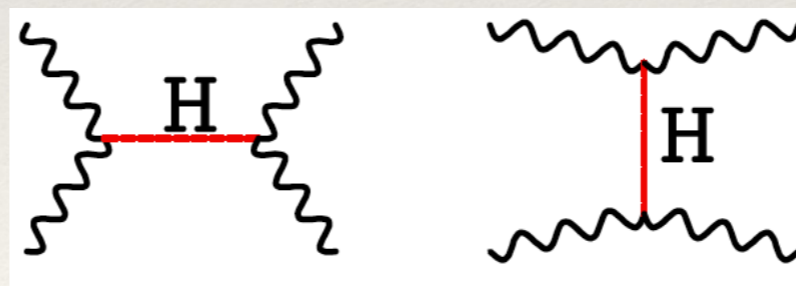
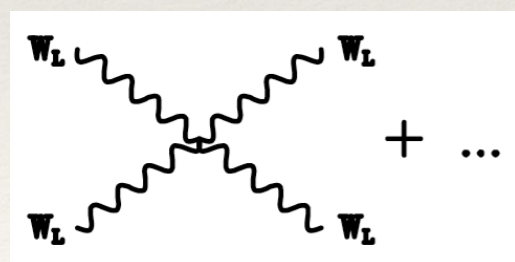
- ❖ In planning for future colliders it would be helpful to have an idea of the energy scale of potential next discoveries.
- ❖ This was very helpful in making the case for the LHC.
- ❖ No-lose theorems implied that below about 1 TeV,
  - ❖ There had to be either new physics (Higgs boson)
  - ❖ Or strong interaction dynamics.

# No-lose completion of the standard model

- ❖ To complete the standard model we have been aided by no-lose theorems, based on perturbative unitarity.
- ❖ Before some critical energy  $\sqrt{s_c}$ , new physics must enter,
- ❖ either a new particle which keeps the theory perturbative.
- ❖ or, new physics to describe the non-perturbative regime.



Necessity of W-boson



Necessity of H-boson

Now that the standard model is complete, there are no further no-lose theorems.  
In principle, the standard model could be valid to the Planck scale.

# Partial Wave Unitarity

❖ Partial wave expansion

$$T(s, t) = 16\pi \sum_J (2J + 1) a_J(s) P_J(\cos \theta)$$

❖ Lowest partial wave

$$a_0 = \frac{1}{32\pi} \int_{-1}^1 d(\cos \theta) T(s, \cos \theta)$$

❖ Expression for cross section

$$\sigma = \frac{16\pi}{s} \sum_J (2J + 1) |a_J(s)|^2 .$$

❖ Optical theorem

$$\sigma = \frac{1}{s} \text{Im} T(s, 0) = \frac{16\pi}{s} \sum_J (2J + 1) \text{Im} a_J(s) ,$$

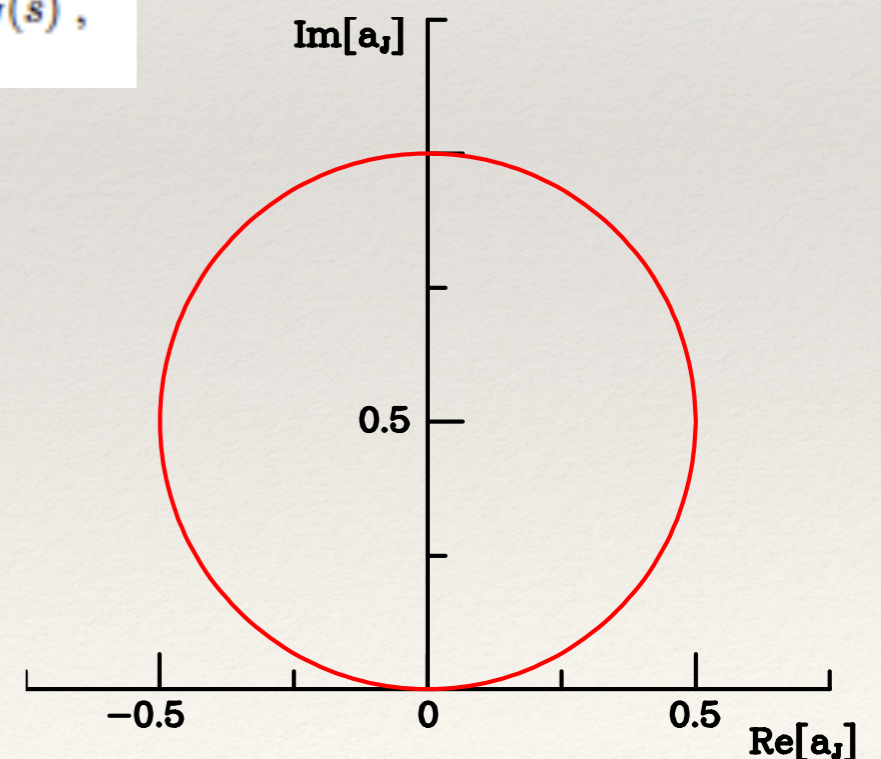
❖ Resultant bound on a

$$|a_J|^2 = \text{Im} a_J$$

❖ Unitarity circle

$$\text{Re} a_J^2 + \left( \text{Im} a_J - \frac{1}{2} \right)^2 = \frac{1}{4}$$

❖ Constraint  $\text{Re} a_0 < \frac{1}{2}$



# Perturbative Unitarity constraint on Fermi theory

- ❖ In Fermi's theory of beta decay the

Lagrangian is,  $\mathcal{L} = \frac{G_f}{\sqrt{2}} \bar{u}(p_u) \gamma^\mu \gamma_L u(p_d) \bar{u}(p_e) \gamma_\mu \gamma_L u(p_\nu)$

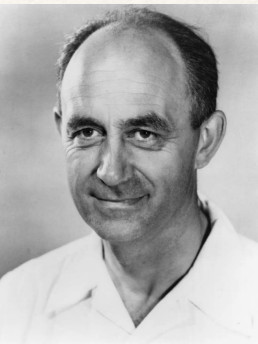
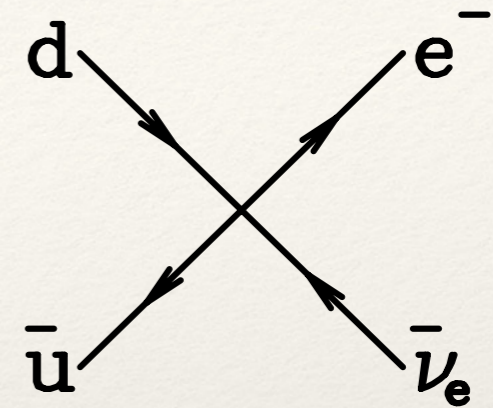
- ❖ At high energy the amplitude is  $T(s, \cos \theta) = \frac{G_f}{\sqrt{2}} s (1 - \cos \theta)$
- ❖ So the result for the J=0 partial wave is  $a_0 = \frac{G_f}{\sqrt{2}} \frac{s}{16\pi}$

- ❖ Constraint  $a_0 < \frac{1}{2}$  gives  $s_{critical} < \frac{8\pi\sqrt{2}}{G_F}$

- ❖ So that the constraint of perturbative unitarity places the limit on the Fermi theory of  $\sqrt{s_{critical}} < 1.75 \text{ TeV}$  This constraint is satisfied by the discovery of the W-boson with mass 81.4 GeV

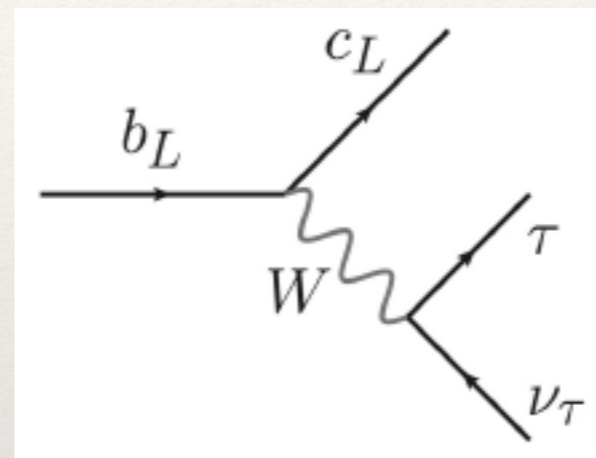
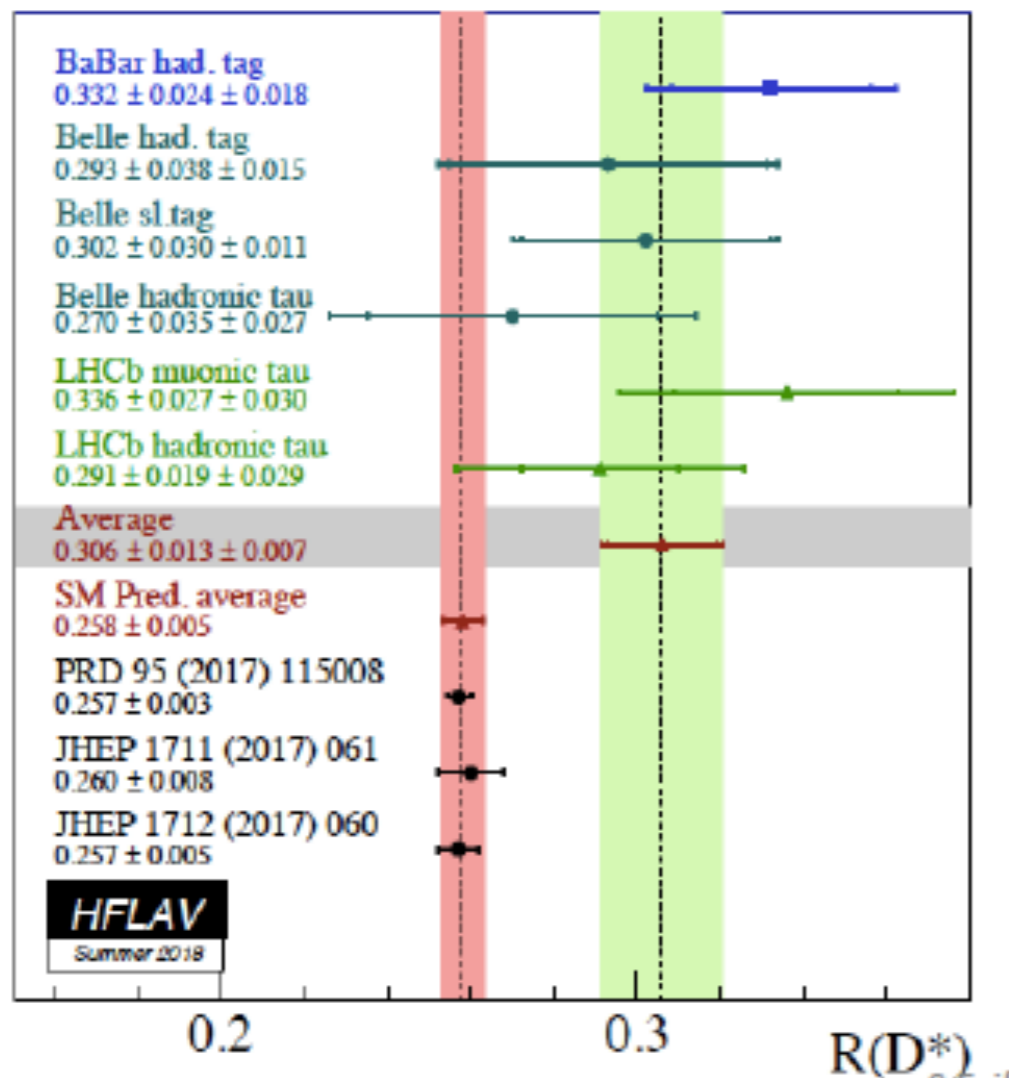
- ❖ A similar argument applied to WW scattering implies for the mass of Higgs boson

$$M_H < \sqrt{\left(\frac{8\sqrt{2}\pi}{3G_f}\right)} \approx 1 \text{ TeV}$$



# BSM physics? – B-physics Anomalies - tree level

$$R_{D^{(*)}} = \frac{BR(B \rightarrow D^{(*)} \tau \nu_\tau)}{BR(B \rightarrow D^{(*)} \mu \nu_\mu)}$$

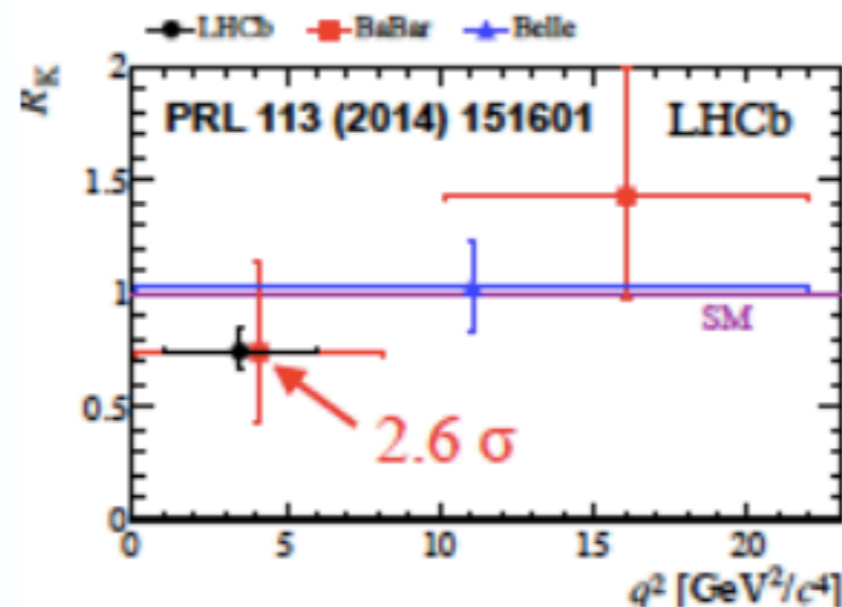
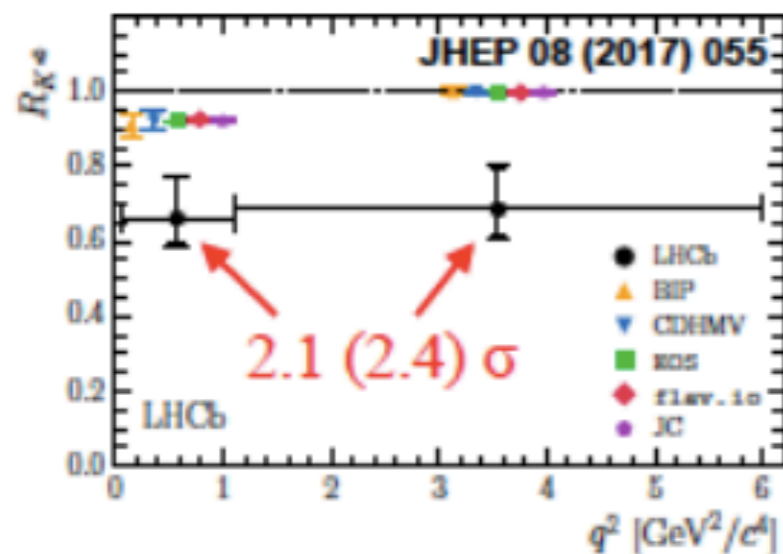


- ❖ 3.8 sigma anomaly in a tree process

# BSM physics: B physics anomalies – $R_{K^*}$ and $R_K$ (loop level)

Fajfer:ICHEP2018

$$R_{K^{(*)}} = \frac{BR(B \rightarrow K^{(*)}\mu\mu)}{BR(B \rightarrow K^{(*)}ee)} \Bigg|_{q^2 \in [q_{min}^2, q_{max}^2]}$$



- ❖ Flavor changing neutral current processes  $b \rightarrow s\ell\bar{\ell}$
- ❖ Also 3 sigma deviation in  $P5'$ , a variable constructed in such a way that theoretical uncertainties cancel out and are under control.

# Could B-physics be suggesting a new scale?

- ❖ The B-physics anomalies have not yet reached the level of 5 sigma.
- ❖ If they were to persist, perturbative unitarity can be used to set the scale of the new physics, just as it did for the Fermi theory.
- ❖ Unfortunately the loop-level perturbative unitarity constraints are not very stringent.
- ❖ Using the operator  $\mathcal{L} = \frac{1}{\Lambda_{D^*}^2} 2\bar{c}_L \gamma^\mu b_L \bar{\tau}_L \gamma_\mu \nu_L + \frac{1}{\Lambda_{R_K^*}^2} 2\bar{s}_L \gamma^\mu b_L \bar{\mu}_L \gamma_\mu \mu_L$
- ❖ Perturbative unitarity limits are  $s_c^{D^*} = 9.2 \text{ TeV}$  and  $s_c^{R_K^*} = 84 \text{ TeV}$





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# The next project

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- ❖ Every new machine needs to have a guaranteed deliverable, as well as the potential for serendipitous discovery.
- ❖ As a temporary goal, let us decide to find out as much about the Higgs boson as we can, and rate potential new machines on that basis.
- ❖ Everything changes if we see something new at the 1TeV scale.

# Higgs Physics provides guaranteed deliverables

- ❖ Mass of Higgs
- ❖ Total Width of Higgs
- ❖ Couplings of Higgs to all? particles
- ❖ (Higgs invisible width)
- ❖ Trilinear coupling of Higgs
- ❖ Composite or elementary?

$$\mathcal{V}(\phi^\dagger\phi) = \lambda (\phi^\dagger\phi)^2 - \mu^2\phi^\dagger\phi .$$

$$\mathcal{L}_{\text{Higgs}} = \frac{1}{2} (\partial_\mu h)^2 - \frac{1}{2} M_h h^2 - \lambda_3 \left( \frac{M_h^2}{2v} \right) h^3 - \lambda_4 \left( \frac{M_h^2}{8v^2} \right) h^4$$

$$\text{SM: } \lambda_3 = 1, \lambda_4 = 1$$

$H^0$

$J = 0$

Mass  $m = 125.09 \pm 0.24$  GeV  
Full width  $\Gamma < 0.013$  GeV, CL = 95%

## $H^0$ Signal Strengths in Different Channels

See Listings for the latest unpublished results.

Combined Final States =  $1.10 \pm 0.11$

$$WW^* = 1.08^{+0.18}_{-0.16}$$

$$ZZ^* = 1.29^{+0.26}_{-0.23}$$

$$\gamma\gamma = 1.16 \pm 0.18$$

$$b\bar{b} = 0.82 \pm 0.30 \quad (S = 1.1)$$

$$\mu^+\mu^- = 0.1 \pm 2.5$$

$$\tau^+\tau^- = 1.12 \pm 0.23$$

$$Z\gamma < 9.5, \text{ CL} = 95\%$$

$$t\bar{t}H^0 \text{ Production} = 2.3^{+0.7}_{-0.6}$$

PDG-May 2017

# How precisely do we need to know Higgs couplings?

- ❖ A hard question
- ❖ As precisely as possible?
- ❖ As precisely as theoretical errors on couplings?
- ❖ Beyond the level of sensitivity associated with the non-observation of BSM particles at the LHC?
- ❖ eg MSSM

Process	Cross section (pb)	Relative uncertainty in percent		
		Total	Scale	PDF
Gluon fusion	49.3	+19.6 -14.6	+12.2 -8.4	+7.4 -6.2
VBF	4.15	+2.8 -3.0	+0.7 -0.4	+2.1 -2.6
WH	1.474	+4.1 -4.4	+0.3 -0.6	+3.8 -3.8
ZH	0.863	+6.4 -5.5	+2.7 -1.8	+3.7 -3.7

$$\begin{aligned}\kappa_V &\sim 1 - 0.5\% \left( \frac{400 \text{ GeV}}{M_A} \right)^4 \cot^2 \beta \\ \kappa_t &\sim 1 - \mathcal{O}(10\%) \left( \frac{400 \text{ GeV}}{M_A} \right)^2 \cot^2 \beta \\ \kappa_b = \kappa_\tau &\sim 1 + \mathcal{O}(10\%) \left( \frac{400 \text{ GeV}}{M_A} \right)^2.\end{aligned}$$

# Higgs and Flavor

$$y_F = \frac{\sqrt{2}m_f}{v}$$

❖ Proportionality

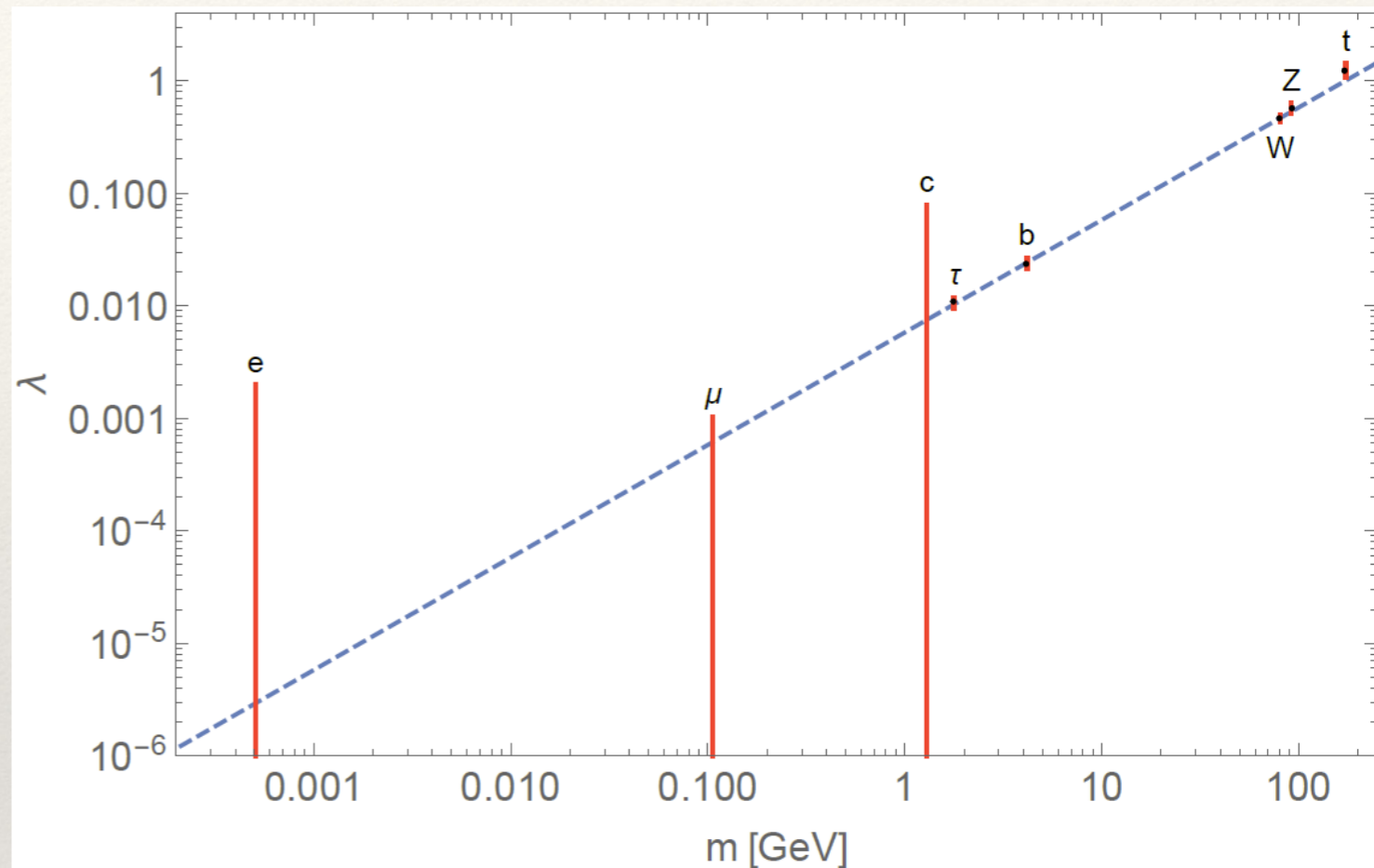
$$y_i/y_j = m_i/m_j$$

❖ Factor of proportionality

$$y_i/m_i = \sqrt{2}/v$$

❖ Diagonality

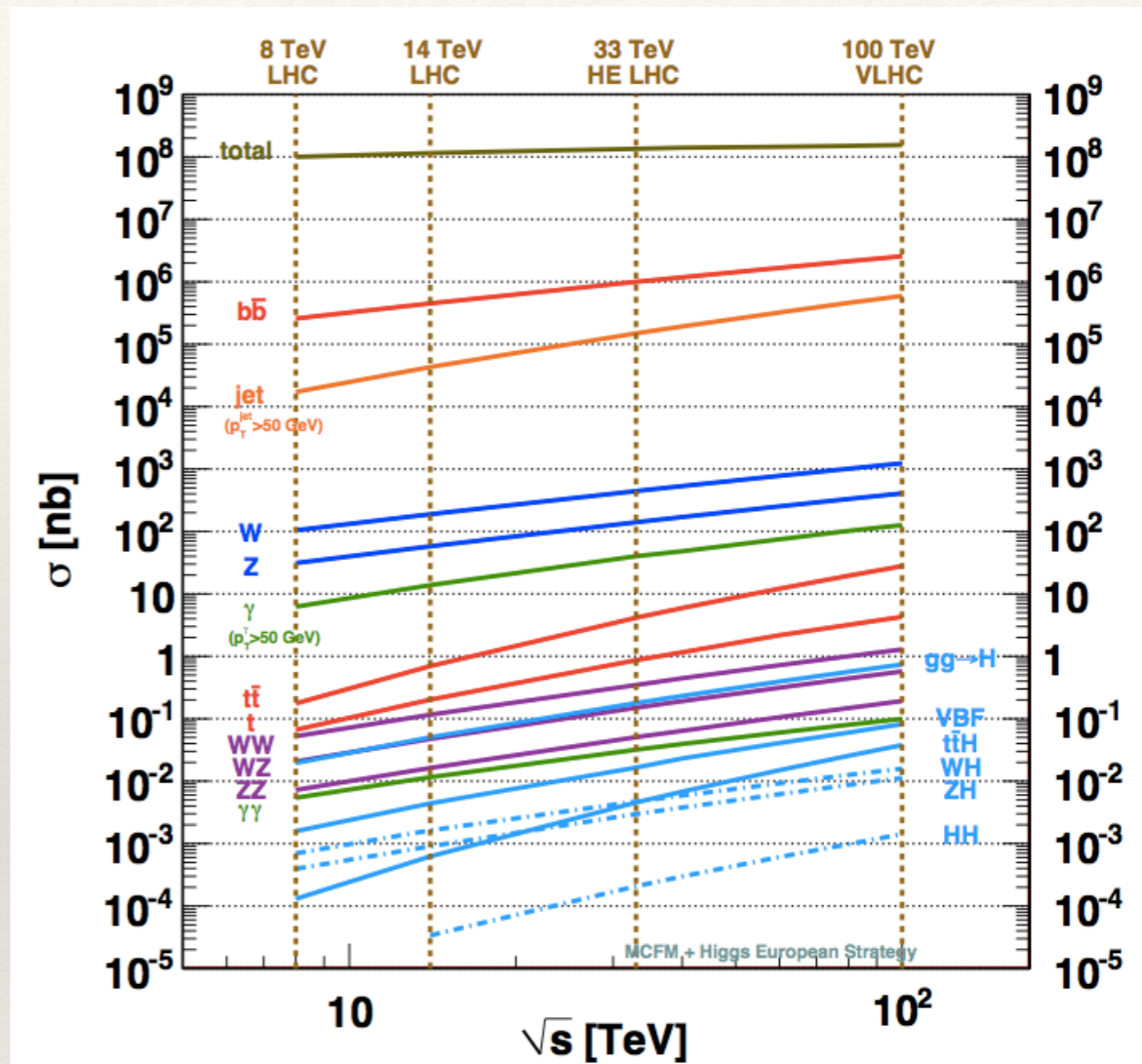
$$y_{ij} = 0 \text{ for } i \neq j$$



Yossi Nir private communication.

# Hadron colliders as Higgs Factories

- ❖ Real factories vs lepton colliders
- ❖ Millions rather than thousands of H-bosons
- ❖ Signal to background
- ❖ Growth with energy (esp.  $ttH$ ).
- ❖ Access to Higgs pair production.



	$ggF$	$VBF$	$VH$	$ttH$
$H \rightarrow \text{all}$ ( $3000 \text{ fb}^{-1}$ @ 14 TeV)	$149.7 \times 10^6$	$12.54 \times 10^6$	$7.14 \times 10^6$	$1.833 \times 10^6$
Cross section [pb] ( $\sqrt{s} = 14 \text{ TeV}$ )	50.35	4.40	2.53	0.623
Cross section [pb] ( $\sqrt{s} = 33 \text{ TeV}$ )	178.3	15.47	7.053	4.377
Cross section [pb] ( $\sqrt{s} = 100 \text{ TeV}$ )	740.3	82.0	27.16	37.9

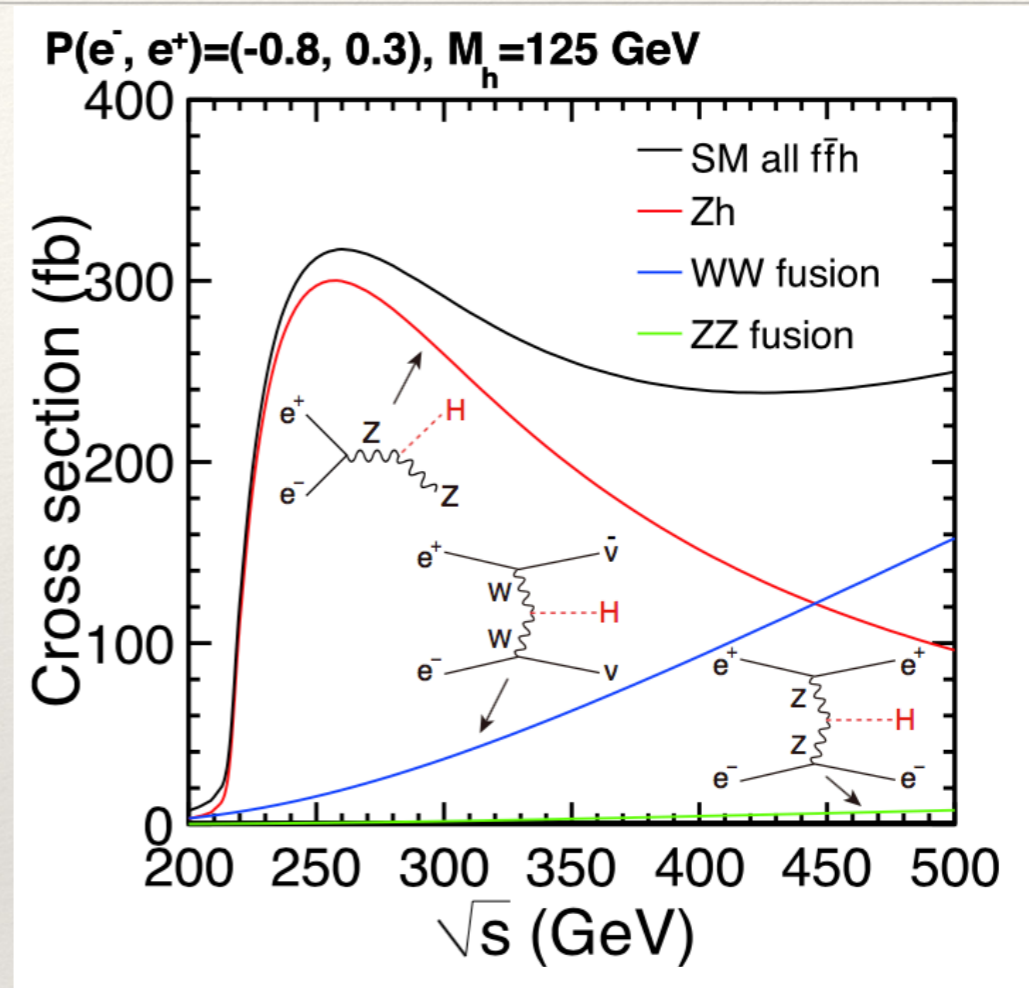
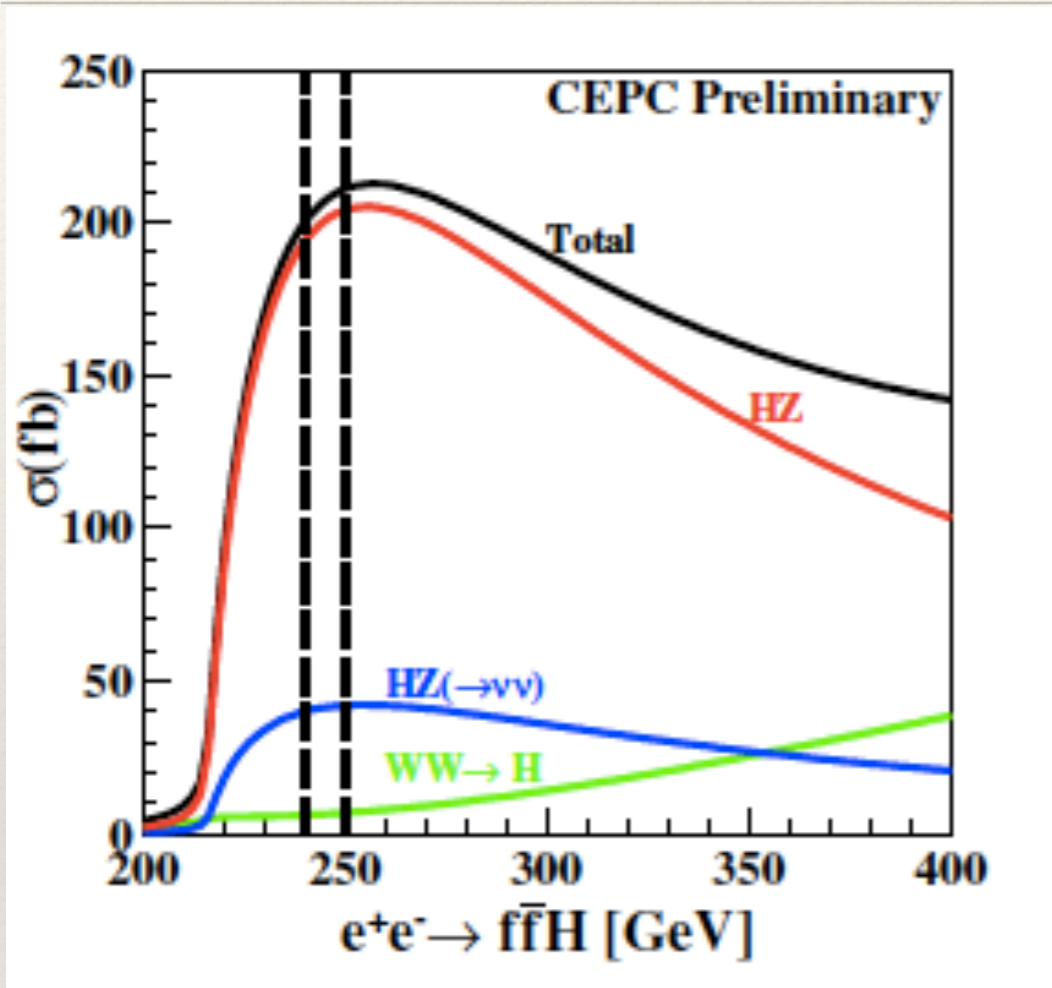
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# Low energy Higgs factories

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- ❖ The physics of electron positron colliders is independent of whether the machine is circular or linear.
- ❖ What differs is the luminosity (and possibly polarization in the case of the linear collider).
- ❖ Muon collider has access to s-channel production.

# $e^+e^-$ collider generalities: Higgs physics



- ❖ WW fusion production ten times smaller at 250 than 500.
- ❖ ~40% increase in ZH cross section with polarization(-0.8,+0.3)
- ❖ Polarization is useful to identify certain sub-processes.

Polarisation	Scaling factor			1608.07538
	$P(e^-) : P(e^+)$	$e^+e^- \rightarrow ZH$	$e^+e^- \rightarrow H\nu_e\bar{\nu}_e$	
unpolarised		1.00	1.00	1.00
-80% : 0%		1.12	1.80	1.12
-80% : +30%		1.40	2.34	1.17
-80% : -30%		0.83	1.26	1.07
+80% : 0%		0.88	0.20	0.88
+80% : +30%		0.69	0.26	0.92
+80% : -30%		1.08	0.14	0.84

We will have a much better idea of this tables by the end of the year and maybe we already do (cf Kado).

# Comparison of precision on Higgs couplings

Parameter	HL-LHC	FCC-ee	FCC-ee	ILC	CLIC	CEPC	$\mu$ -Coll
$\sqrt{s}$ [TeV]	14	350	240	250	1400	240	125
Lum/IP[E34]	5	1.9	8.5	1.35	1.5	2	0.01?
total[ab <sup>-1</sup> ]	3+(3)	1.3+1.3	5+5	2	1.5	2+2	0.002?
years[Sn'm'ss]	6	6.8	5.9	15	10	10	2?
$\Delta m_h$ [MeV]	$\sim 100$			14	47	5.9	0.06
$\Gamma_h$ [%]	-	1.2	2.4	3.9	3.7	2.7	3.6
$\Delta g_{hZZ}$ [%]	4	0.15	0.16	0.38	0.8	0.26	
$\Delta g_{hWW}$ [%]	4.5	0.19	0.85	1.8	0.9	1.2	2.2
$\Delta g_{hbb}$ [%]	11	0.42	0.88	1.8	1.0	1.3	2.3
$\Delta g_{h\tau\tau}$ [%]	9	0.54	0.94	1.9	1.7	1.4	2.3
$\Delta g_{h\gamma\gamma}$ [%]	4.1	1.5	1.7	1.1	5.7	4.7	5
$\Delta g_{hcc}$ [%]	-	0.71	0.71	2.4	2.3	1.7	10
$\Delta g_{hgg}$ [%]	6.5	0.8	0.80	2.2	1.8	1.5	-
$\Delta g_{htt}$ [%]	8.5	-	-	-	4.2	-	-
$\Delta g_{h\mu\mu}$ [%]	7.2	6.2	6.4	5.6	14.1	8.6	2.1
$\Delta\Gamma_{\text{invis}}$ [%]	$\sim 10$			0.32			
$\Delta g_{hhh}$ [%]	-400,1200	-	-	-	40	-	
References	ATL-PHYS-PUB -2014-016	1308.6176	1308.6176	1710.07621 1711.00568	1608.07538	IHEP-CEPC-DR -2015-01	1304.5270 1308.2143

Many questionable and/or dated numbers!

Table inspired by talk of M Klute, Higgs couplings,2015



# Higgs physics at lepton-proton colliders

Parameter	LHeC	DLHeC	FCC-ep
total[ab <sup>-1</sup> ]	1	1	1 (10 for $g_{hhh}$ )
$E_p$ [TeV]	7	14	50
$\sqrt{s}$ [TeV]	1.3	1.8	3.5
Polarized e beam	Yes	Yes	Yes
$\Delta g_{hbb}$ [%]	0.5	0.3	0.2
$\Delta g_{hcc}$ [%]	4	2.8	1.8
$\Delta g_{htt}$ [%]	17		
$\Delta g_{hhh}$ [%]			-17,+25
References	1702.03426,Wang EPS2017	Wang EPS2017	1509.04016

- ❖ Limited study of potential of these machines for Higgs physics

# Hadron-colliders

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# How fast can we proceed to higher energy at LHC

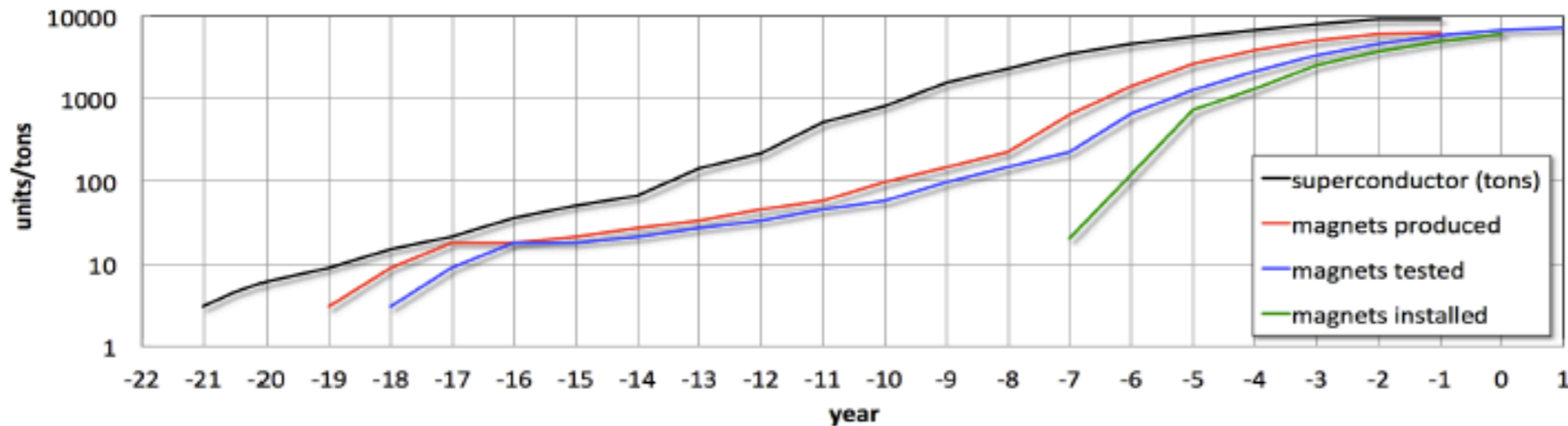
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- ❖ Given the apparent absence so far of new physics so far, (with less than 2% of final data sample fully analyzed), one might wish to move to higher energy ASAP.
- ❖ The possibility of going to 15 TeV (with the current magnets operated at higher field) late in Run 3 is being studied.
- ❖ the feasibility and cost of substituting some fraction of the magnets, (say 1/3), with higher field magnets to go beyond 15 TeV is being studied.

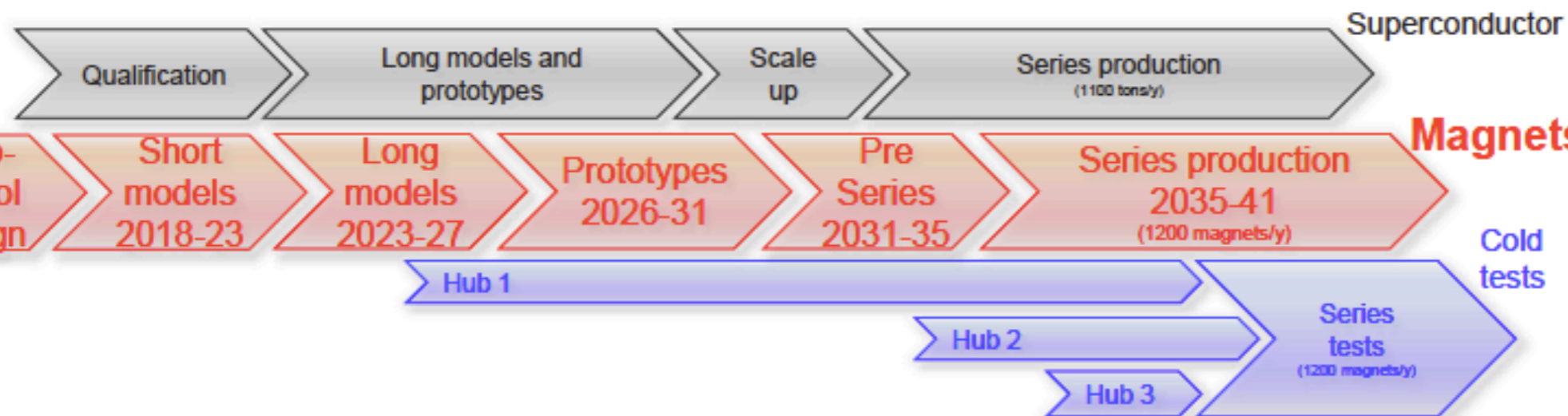
# 16 Tesla Technically-driven magnet schedule



## 16 T magnet R&D schedule



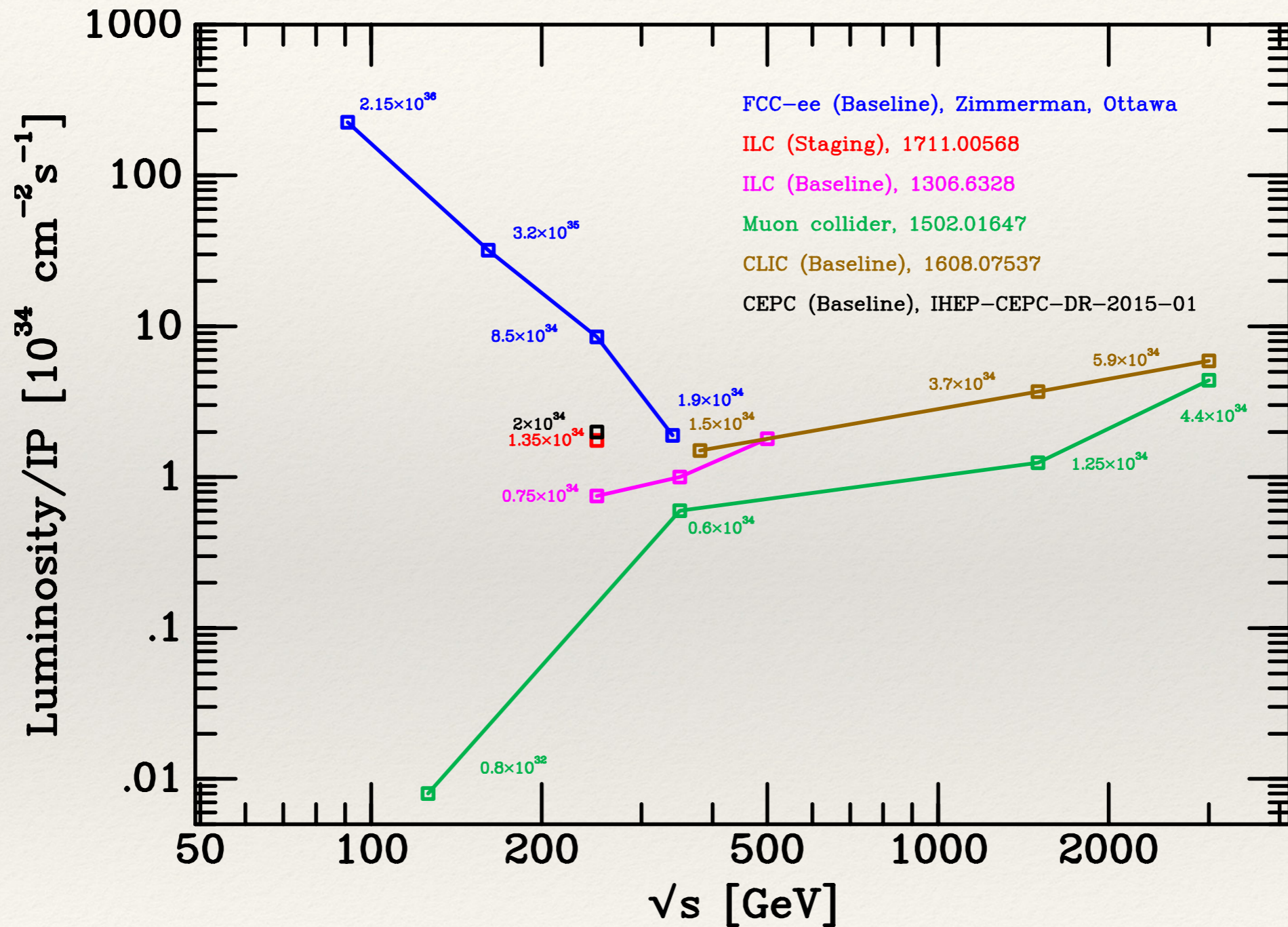
Total duration of magnet program:  
**~20 years**



Would follow on HL-LHC Nb3Sn program with long models with industry from 2023/24

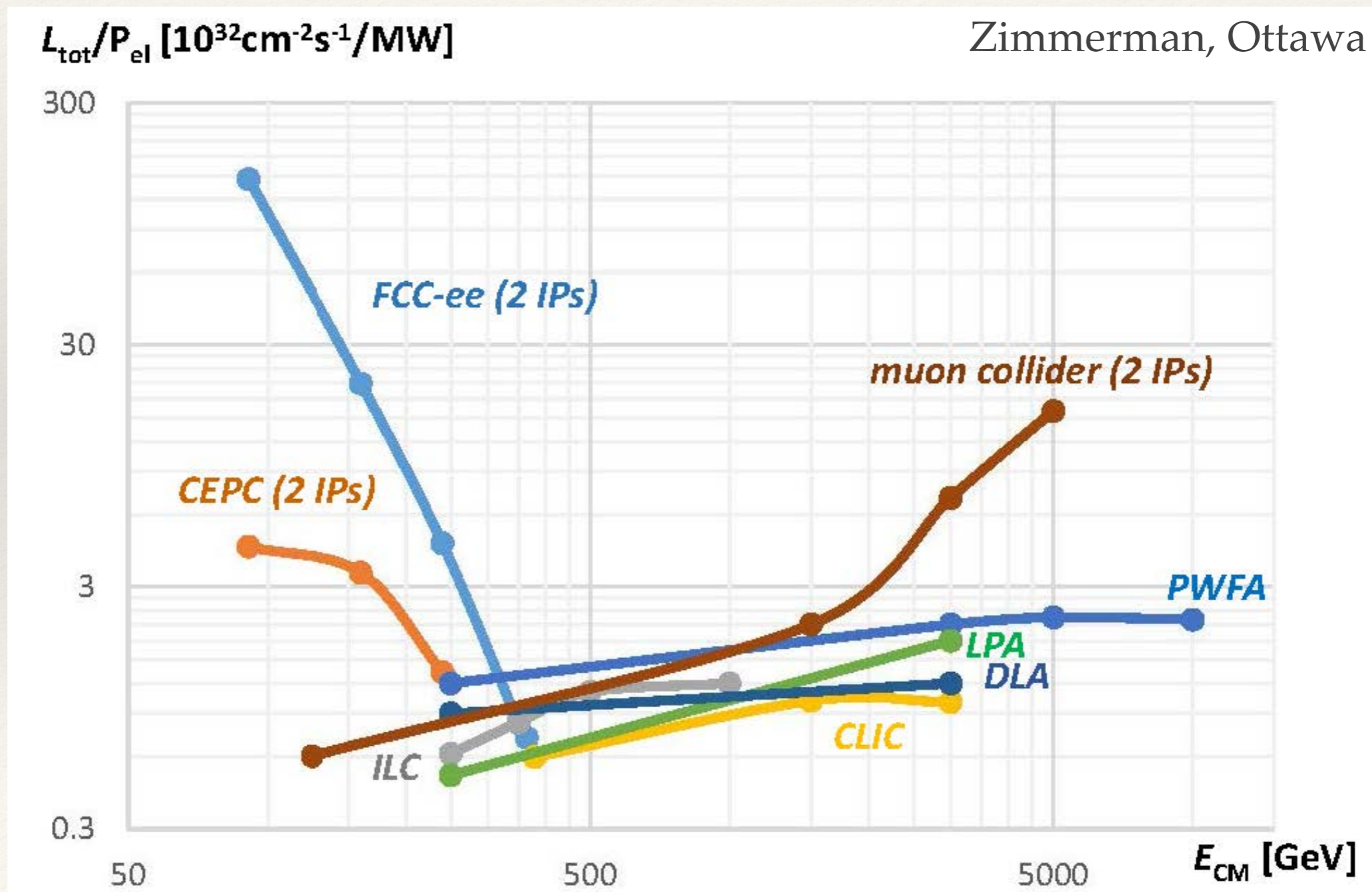
# Lepton-colliders

# Luminosity at lepton colliders



# Lepton colliders

- ❖ Luminosity per Megawatt, wall plug power



# Measuring the total width at $e^+e^-$ collider

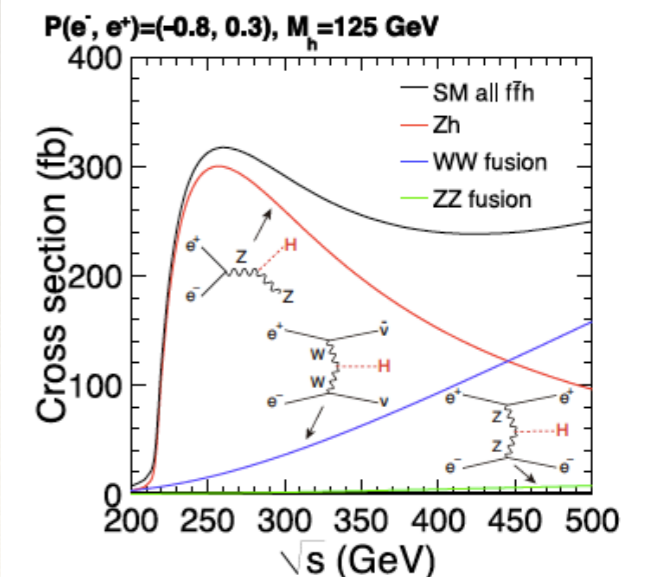
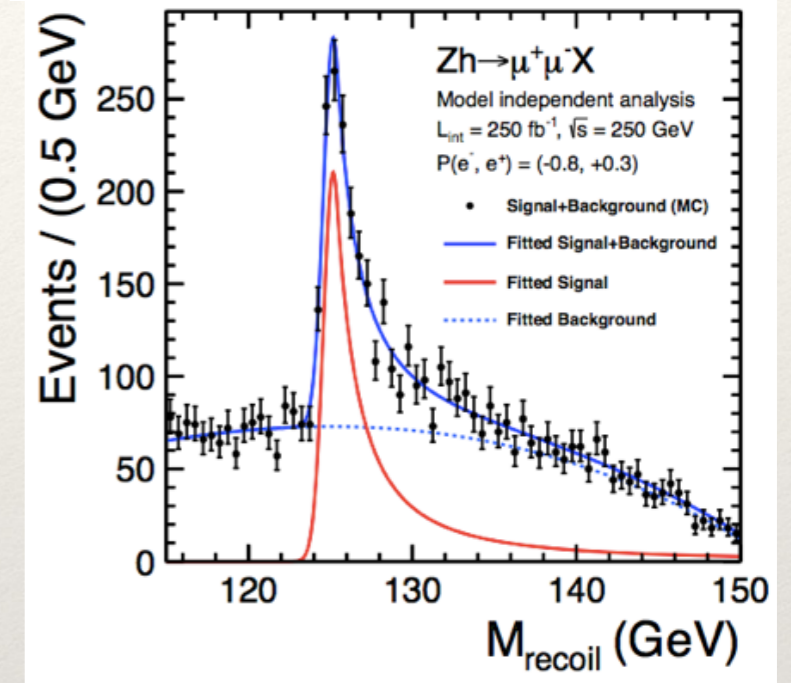
- ❖ It is possible to identify a Higgs event without looking at the Higgs at all.
- ❖ Total width is given by the quotient of partial width and branching to a given final state.

$$\Gamma_{tot} = \frac{\Gamma(H \rightarrow ZZ)}{BR(H \rightarrow ZZ)} = \frac{\sigma(e^+e^- \rightarrow ZH)\Gamma(H \rightarrow ZZ)}{\sigma(e^+e^- \rightarrow ZH) \cdot BR(H \rightarrow ZZ)}$$

- ❖ The partial width is controlled by the HZZ coupling, just like the total cross section
- ❖ The total width can be measured with the same precision as

$$\frac{\sigma_{HZ}^2}{\sigma_{HZ} \cdot BR(H \rightarrow ZZ)}$$

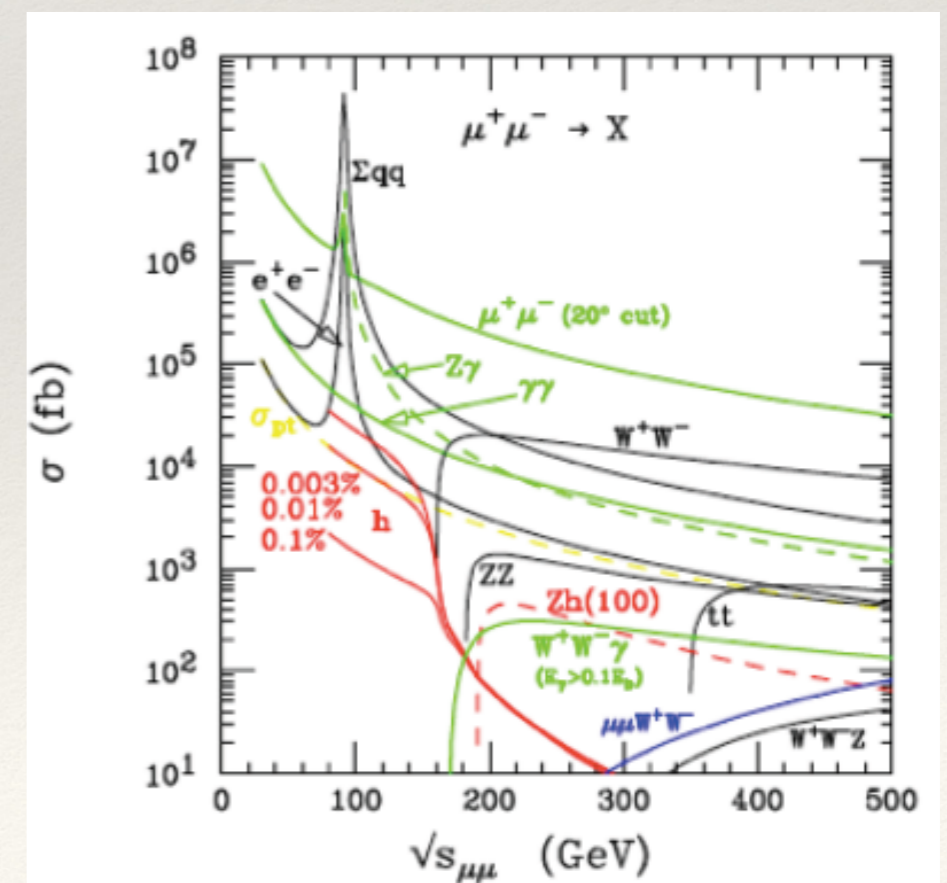
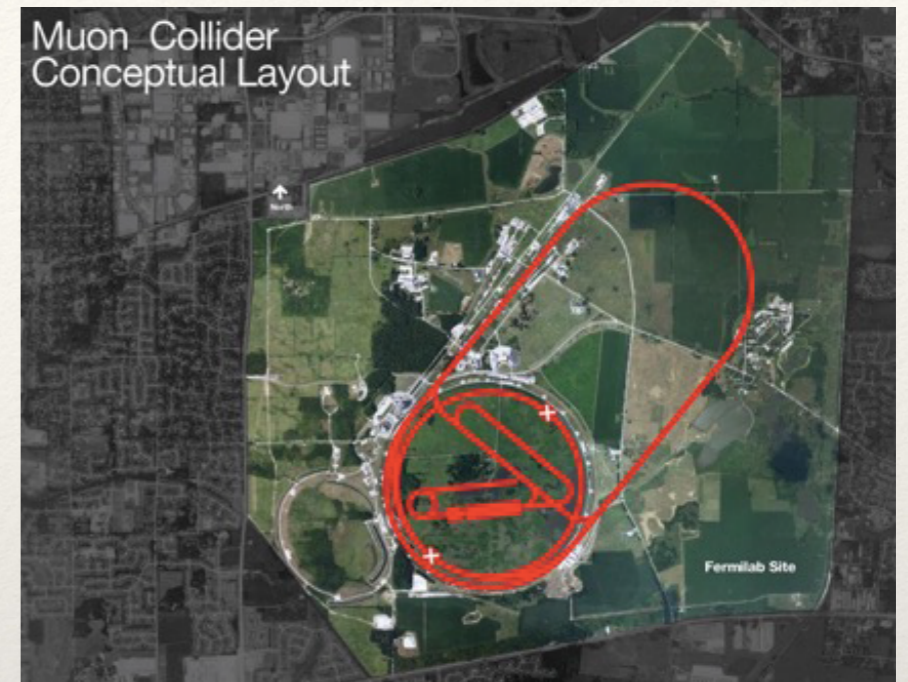
$$m_{recoil}^2 = (\sqrt{s} - E_{\ell\ell})^2 - |\vec{p}_{\ell\ell}|^2$$





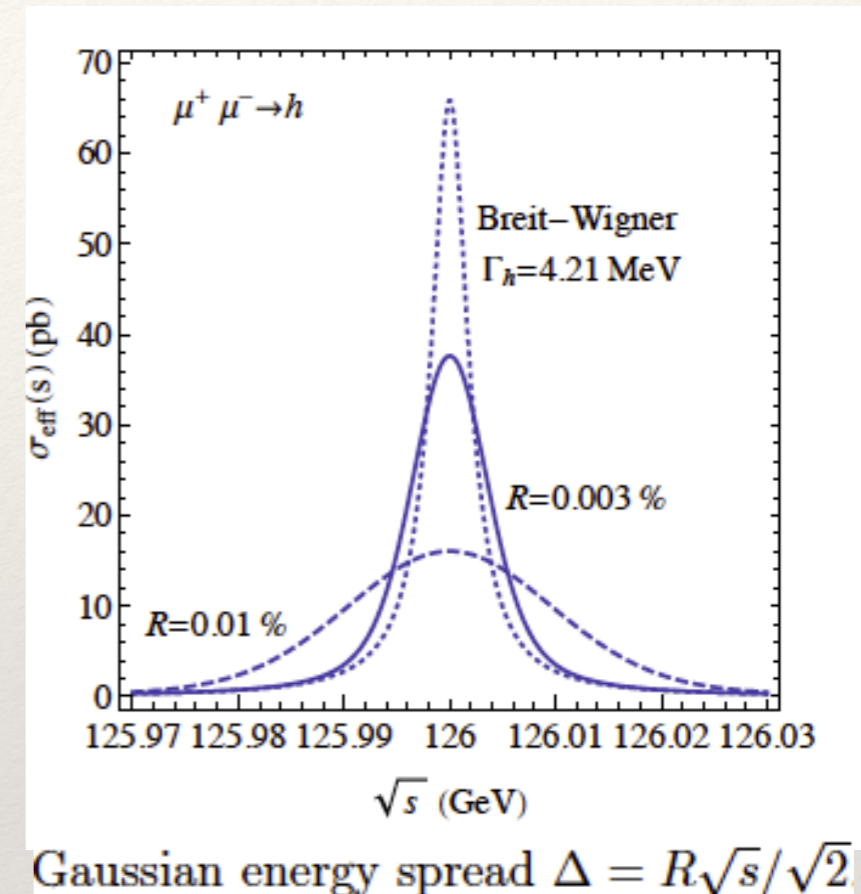
# Muon collider Higgs Factory

- ❖ Compact, fits on CERN site; Higgs factory ring radius 50m.
- ❖ Advantages associated with circular geometry
- ❖ Multipass acceleration, multipass collisions, more than one detector
- ❖ Narrow energy spread, negligible synchrotron radiation. Higgs signal depends on resolution.
- ❖ Picobarn cross section for s-channel Higgs production, direct measurement scan of Higgs width.
- ❖ Follow on program, neutrino factory, no energy constraints limiting scaling to Multi-TeV energy.



# Muon collider

- ❖ Effective production cross section,  $\sigma(\mu^+\mu^-\rightarrow H, \sqrt{s}=125\text{GeV})\approx 15\text{pb}$ , but dependent on resolution.
- ❖ cf,  $\sigma(e^+e^-\rightarrow ZH, \sqrt{s}=240\text{GeV})=200\text{-}300\text{fb}$
- ❖ Ring size small, presenting the hope that cost scales with size.
- ❖ Detector issues, decaying beam particle, “machine detector interface”.
- ❖ Follow on program, Nustorm, Intense muon beams for Lepton-Flavour violation, neutrino factory, high energy muon collider.....



$$\frac{dL(\sqrt{s})}{d\sqrt{\hat{s}}} = \frac{1}{\sqrt{2\pi}\Delta} \exp\left[-\frac{(\sqrt{\hat{s}} - \sqrt{s})^2}{2\Delta^2}\right],$$

$$\sigma_{\text{eff}}(s) = \int d\sqrt{\hat{s}} \frac{dL(\sqrt{s})}{d\sqrt{\hat{s}}} \sigma(\mu^+\mu^-\rightarrow h\rightarrow X)$$

$$\propto \begin{cases} \Gamma_h^2 B / [(s - m_h^2)^2 + \Gamma_h^2 m_h^2] & (\Delta \ll \Gamma_h), \\ B \exp\left[-\frac{(m_h - \sqrt{s})^2}{2\Delta^2}\right] (\Gamma_h / \Delta) / m_h^2 & (\Delta \gg \Gamma_h). \end{cases}$$

Economics: the dismal science

# Phenomenological Model of Accelerator costs

- ❖ Total project cost [TPC] divided into three components

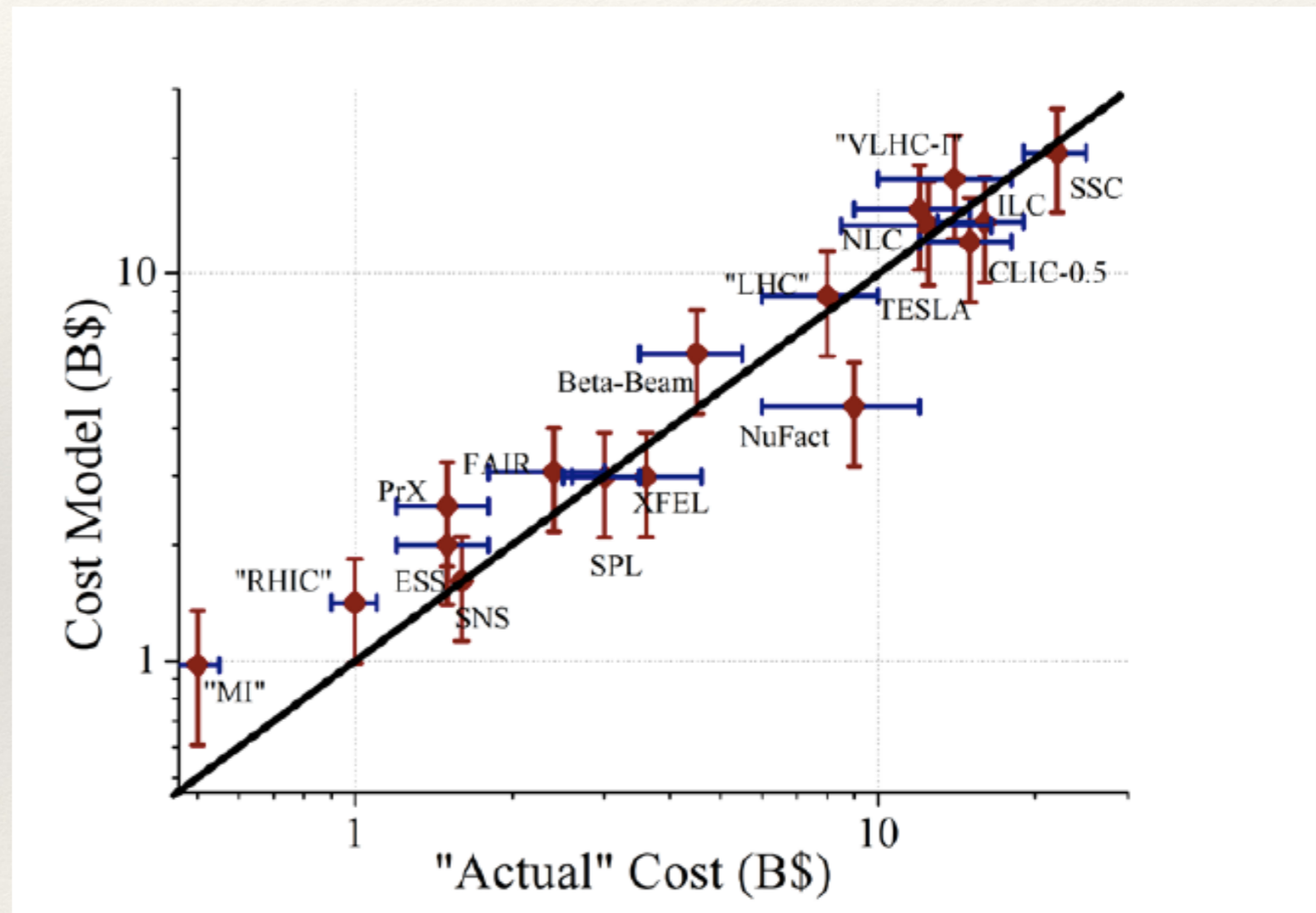
$$\text{TPC} = \alpha \left( \frac{L}{10[\text{km}]} \right)^{\frac{1}{2}} + \beta \left( \frac{E}{1[\text{TeV}]} \right)^{\frac{1}{2}} + \gamma \left( \frac{P}{100[\text{MW}]} \right)^{\frac{1}{2}}$$

- ❖ Civil Engineering and construction
- ❖ Accelerator components
- ❖ Facility Infrastructure
- ❖ Phenomenological formula parametrised in terms of tunnel length[L], centre-of-mass Energy[E] and total site AC power [P]
- ❖ Coefficient beta is technology dependent

$$\begin{aligned} \alpha &= \$2B \\ \gamma &= \$2B \\ \beta &= \$1B \text{ (NCmagnets),} \\ \beta &= \$2B \text{ (SCmagnets),} \\ \beta &= \$8B \text{ (NCRF),} \\ \beta &= \$10B \text{ (SCRf)} \end{aligned}$$

# Validation of cost model

- ❖ US accounting  $\approx$  3x European accounting
- ❖ Model good to about 30%
- ❖ Lots of inverted commas around Actual!



# How much is plausible/possible?

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- ❖ The CERN subscription is about \$1B / year. (20% higher now).
- ❖ World-wide spending is about \$3B / year, of which only a fraction is available for projects
- ❖ Spending \$1B / year over ten years would allow us to complete a \$10B project.

# Estimated costs of future facilities

- ❖ Costs are in American accounting, i.e. including all labour costs. In European accounting this would be a factor  $\sim 2-2.5$  smaller.

	$E[\text{TeV}]$	$L[\text{km}]$	$P[\text{MW}]$	$\alpha\beta\gamma$ TPC [\\$B]	Civil construction cost [\\$B]
$Ce^+e^-C$	0.25	54	$\sim 500$	10.2	4.6
FCC-ee	0.25	100	$\sim 300$	10.9	6.3
ILC	0.5	36	163	13.1	3.8
CLIC	3	60	$\sim 560$	23.5	4.9
$\mu$ collider	6	20	$\sim 230$	12.9	2.8
LHC-33	33	0	$\sim 100$	4.8	0?
SppC(China)	50	54	$\sim 300$	25.5	4.6
FCC-pp	100	100	$\sim 400$	30.3	6.3

These are Shiltsev's numbers, in no way approved by any of the proponents of these machines.

- ❖ Power usage is substantial. Rate of energy usage,  $\sim 1$  kW / person.
- ❖ A small nuclear power station gives 500MW of power.

Parameters for CepC, ILC, HE-LHC, SppC have now changed.

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# HE-LHC advantages

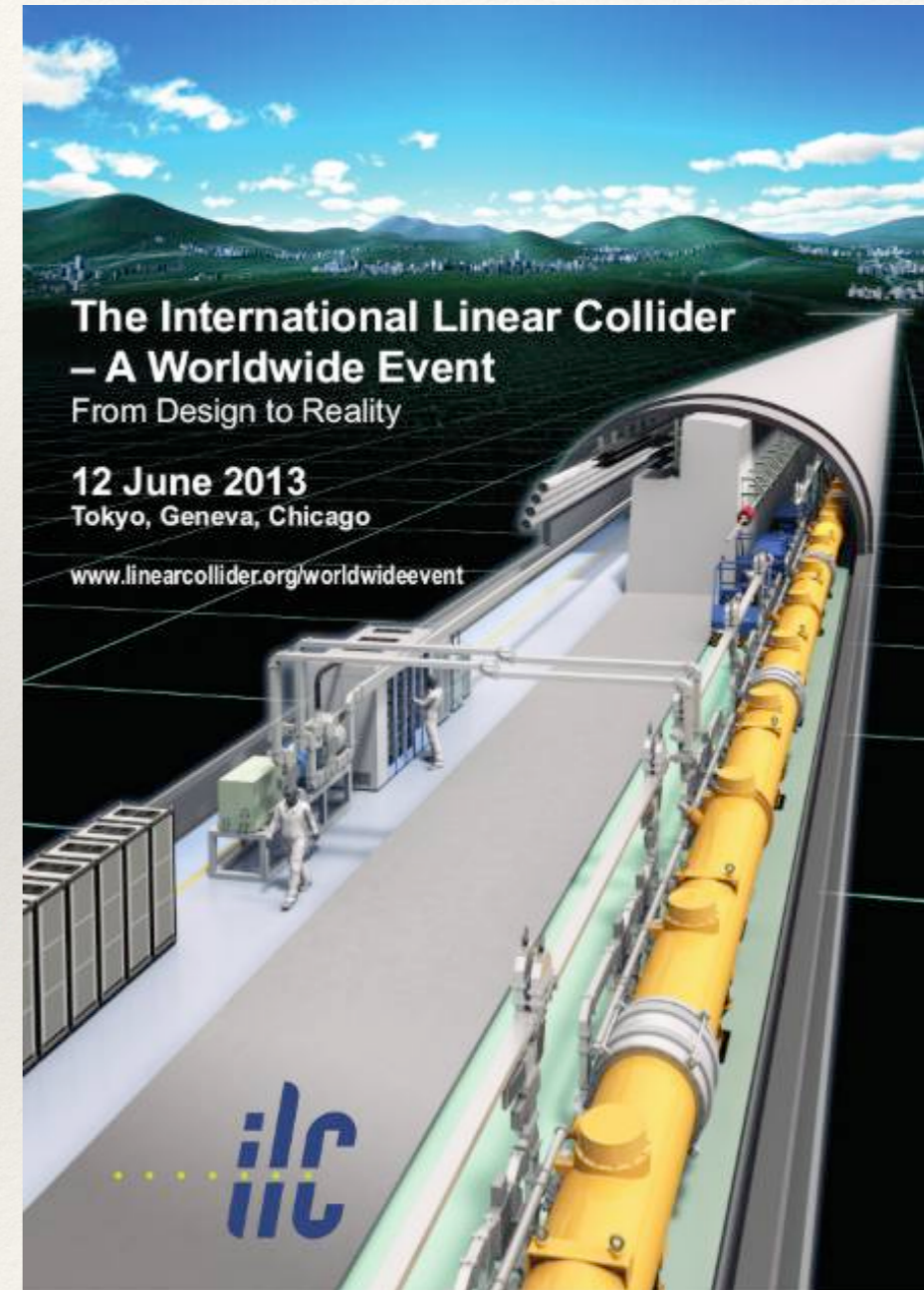
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- ❖ The tunnel is already there.
- ❖ Communality of Magnet R&D program with FCC-hh
- ❖ Achievable with current level of CERN budget?



# ILC advantages

- ❖ A very challenging machine, which now benefits from 20 years of R&D.
- ❖ Measurement of Higgs width, using missing mass technique (Common to all  $e^+e^-$  colliders).
- ❖ Polarization increases  $ZH$  cross section 40% and helps in analysis.
- ❖ Japan may pay a substantial fraction of the cost.



# FCC( $e^+e^-$ ) Advantages

- ❖ Luminosity (superior to ILC).
- ❖ Access to physics at the  $\sqrt{s}=91,240,350$  GeV
- ❖ Tunnel for further use
- ❖ TDR in 2018.
- ❖ c.f. CEPC, although limitation on energy consumption gives lower projected luminosity



# CLIC Advantages

- ❖ All the advantages of other e<sup>+</sup>e<sup>-</sup> machines, including polarization.
- ❖ Possible path to high energy, projected energies,  $\sqrt{s}=380,1500,3000$  GeV

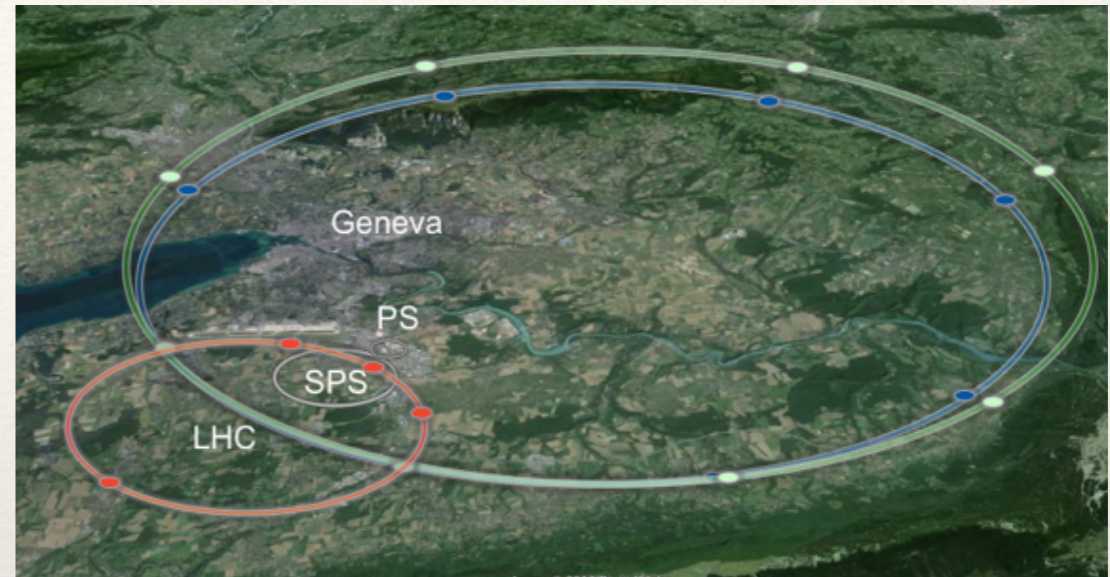
Parameter	Unit			
C.ofM. energy	GeV	380	1500	3000
L/year	fb <sup>-1</sup>	180	444	720

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# FCC(hh) advantages

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- ❖ Large jump in energy
- ❖ The highest energy hadron-hadron machines have always been considered discovery machines, and have not failed us, (SpS (W,Z), Tevatron (Top), LHC(Higgs)).



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# Muon collider advantages

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- ❖ R&D program, with physics at every step, Nustorm, Higgs factory, Neutrino Factory, High-energy lepton collider.
- ❖ Access to high energy lepton collider.
- ❖ Small size, leading to possibility of small civil construction, perhaps lower cost.

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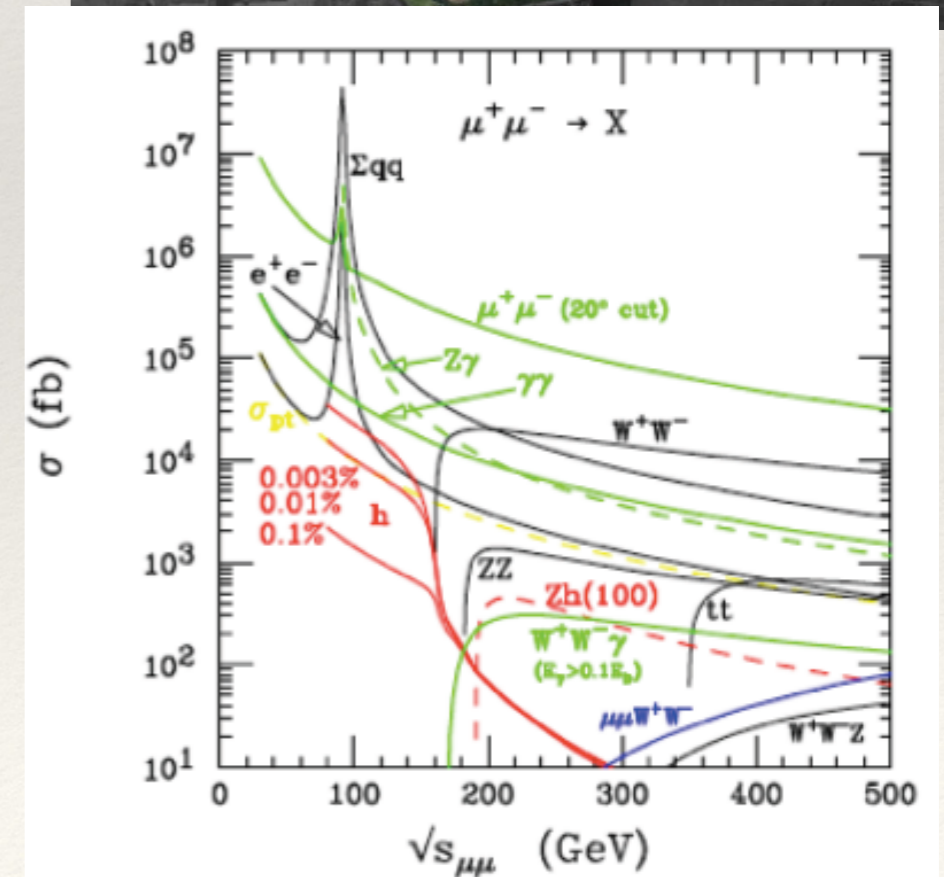
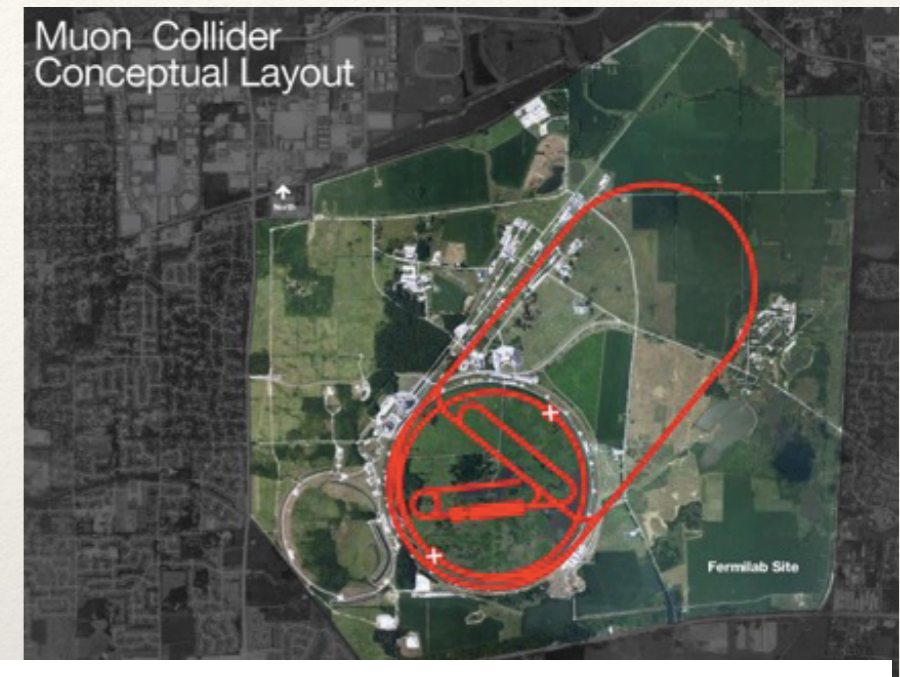
# LHC-ep advantages

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- ❖ the only possible TeV scale collider one can build in Europe at affordable cost in the next decade
- ❖ it brings fundamental new physics for the 2030's
- ❖ it maximises the LHC physics return
- ❖ it opens a wide perspective for accelerator R and D, energy recovery linac.
- ❖ prospect for some Higgs physics in a cleaner environment than LHC.
- ❖ A complementary machine for all energies, collide 60GeV polarized beam with HL-LHC, HE-LHC, FCC-hh.

# Muon collider Higgs Factory

- ❖ Compact, fits on CERN / Fermilab site
- ❖ Advantages associated with circular geometry
- ❖ Multipass acceleration, multipass collisions, more than one detector
- ❖ Narrow energy spread, negligible synchrotron radiation. Higgs signal depends on resolution.
- ❖ Enhanced cross section for s-channel Higgs production, direct measurement scan of Higgs width.
- ❖ A separate ring for every energy (Z,H,ttbar)?
- ❖ No obvious constraints limiting scaling to Multi-TeV energy.



# Schematic of muon complex

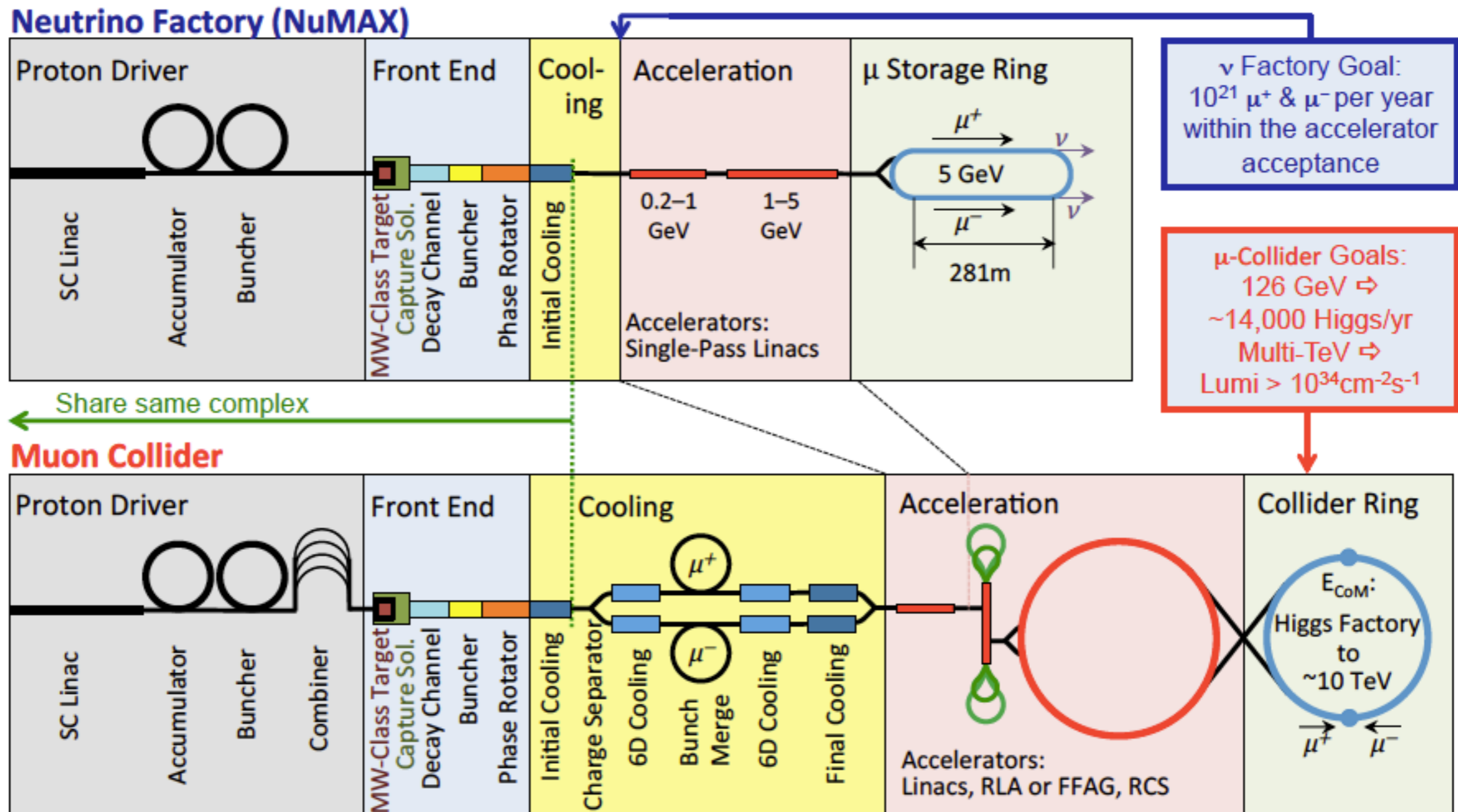
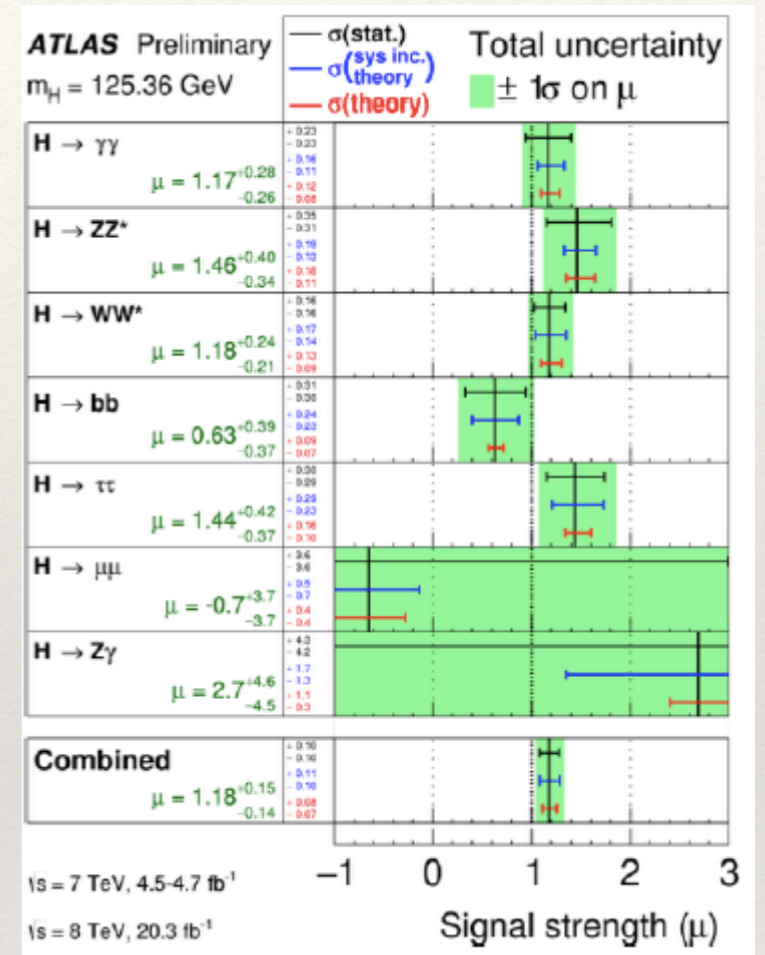


Figure 1: A block diagram showing the key systems needed for a long-baseline neutrino factory capability and a muon collider capability. Much of the infrastructure for each capability could be shared, thus enabling a cost effective multipurpose facility.



# Muon-collider Higgs Factory

- ❖ Coupling  $g_{H\mu\mu}$  not yet measured.
- ❖ Muon cooling needs a demonstration of technological feasibility (MICE experiment, LEMMA proposal).
- ❖ No access to  $t$ - $t$ - $H$  and  $H$ - $H$ - $H$  couplings
- ❖ Decay backgrounds at High energy

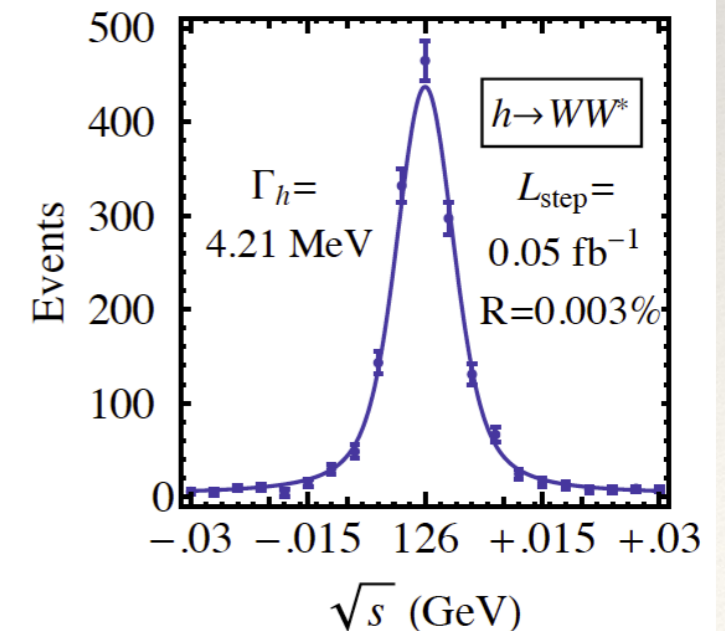
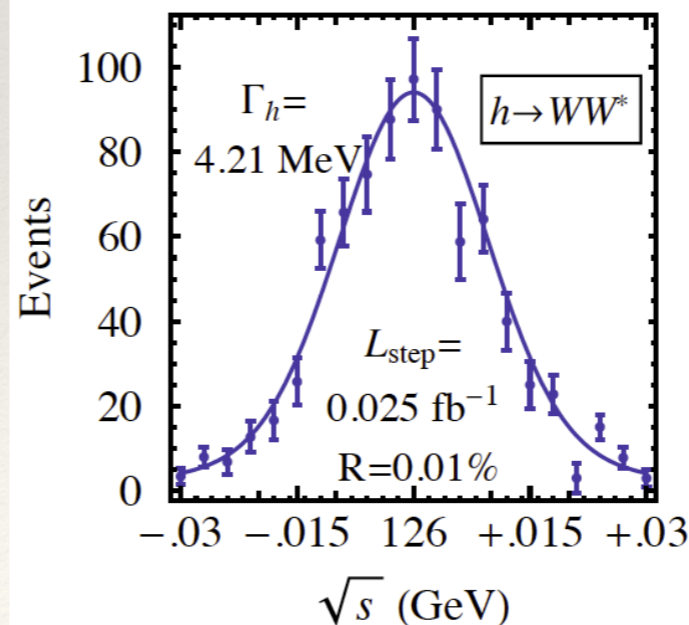
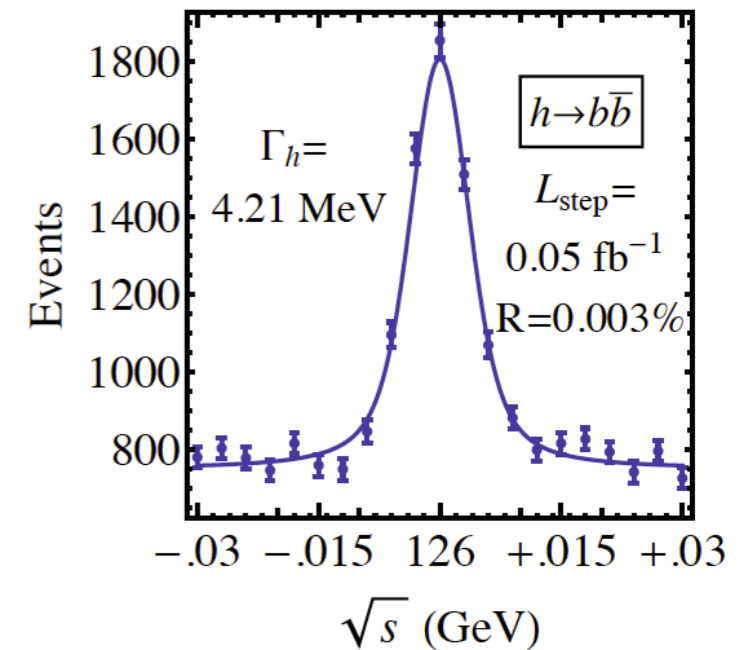
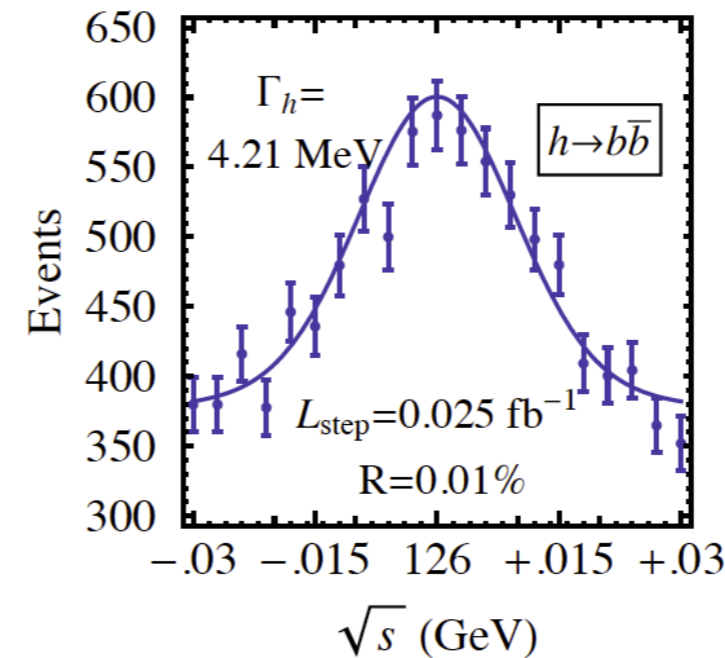


ATLAS-CONF-2015-044

# Measuring the Higgs width at Muon collider

1210.7803

With a beam energy resolution of  $R=0.01\%$  ( $0.003\%$ ) and integrated luminosity of  $0.5 \text{ fb}^{-1}$ , a muon collider would enable us to determine the Standard-Model-like Higgs width to  $0.35 \text{ MeV}$  by combining two complementary channels of the  $WW^*$  and  $b\bar{b}$  final states



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# Cern machine parameter list.

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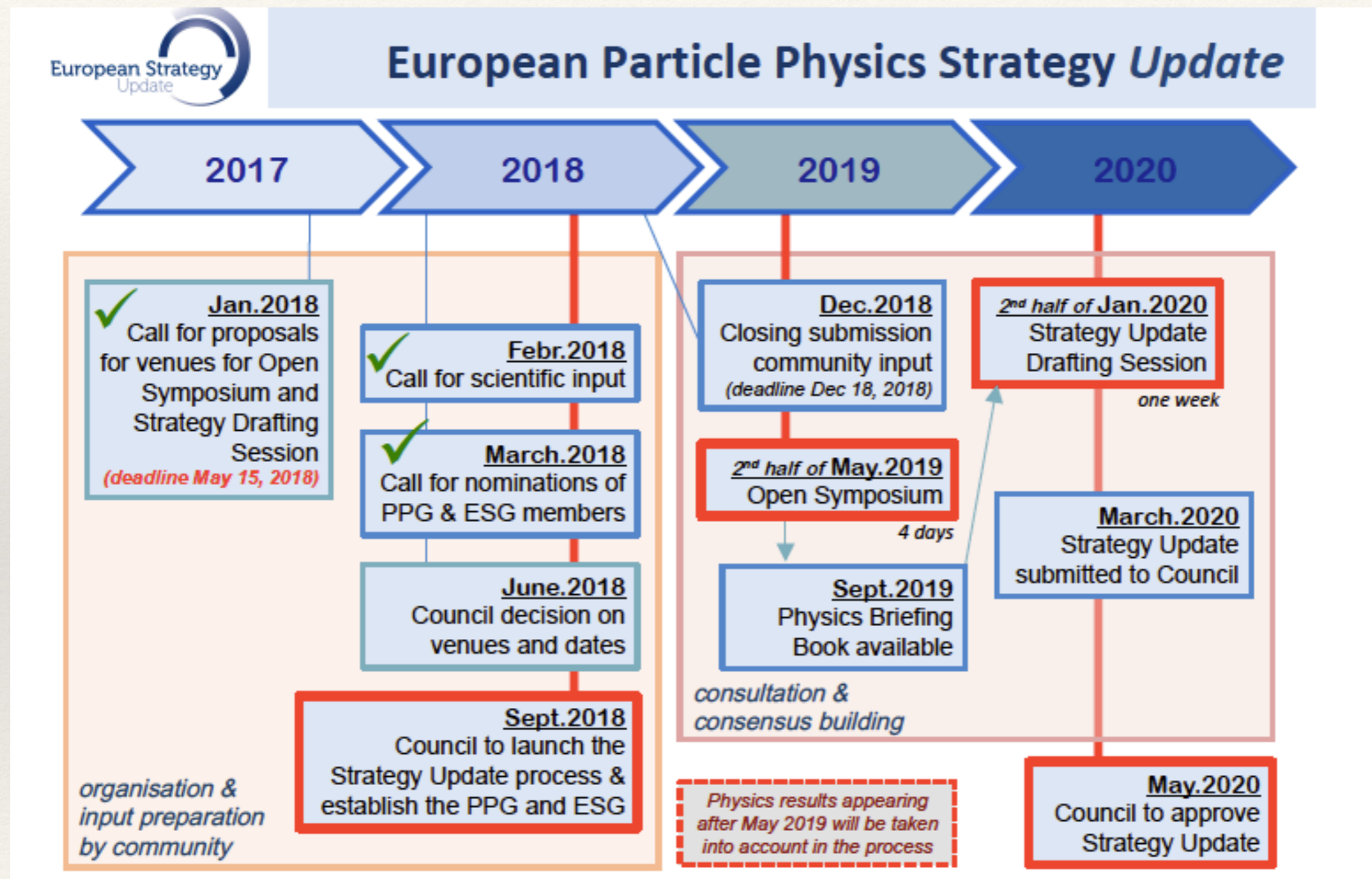
- ❖ To aid in the strategy update process, the CERN accelerator people have produced a document
- ❖ Machine parameters and projected luminosity: performance of proposed future colliders at CERN.
- ❖ Realistic assumptions about availability and luminosity
- ❖ Beyond the “Snowmass year” approximation.

# Projections for the CERN hadron machines

Parameter	Unit	FCC-hh	HE-LHC	HL-LHC	LHC
C.ofM.Energy	TeV	100	27	14	14
Bunch population	$10^{11}$	1	2.2	1.12	1.15
Peak Events / crossing	-	170(1000)	460	135	27
Luminosity / day	$\text{fb}^{-1}$	2.0(8.0)	5.0	1.9	0.4
Luminosity / year(160 days)	$\text{fb}^{-1}$	250(1000)	500	350	55



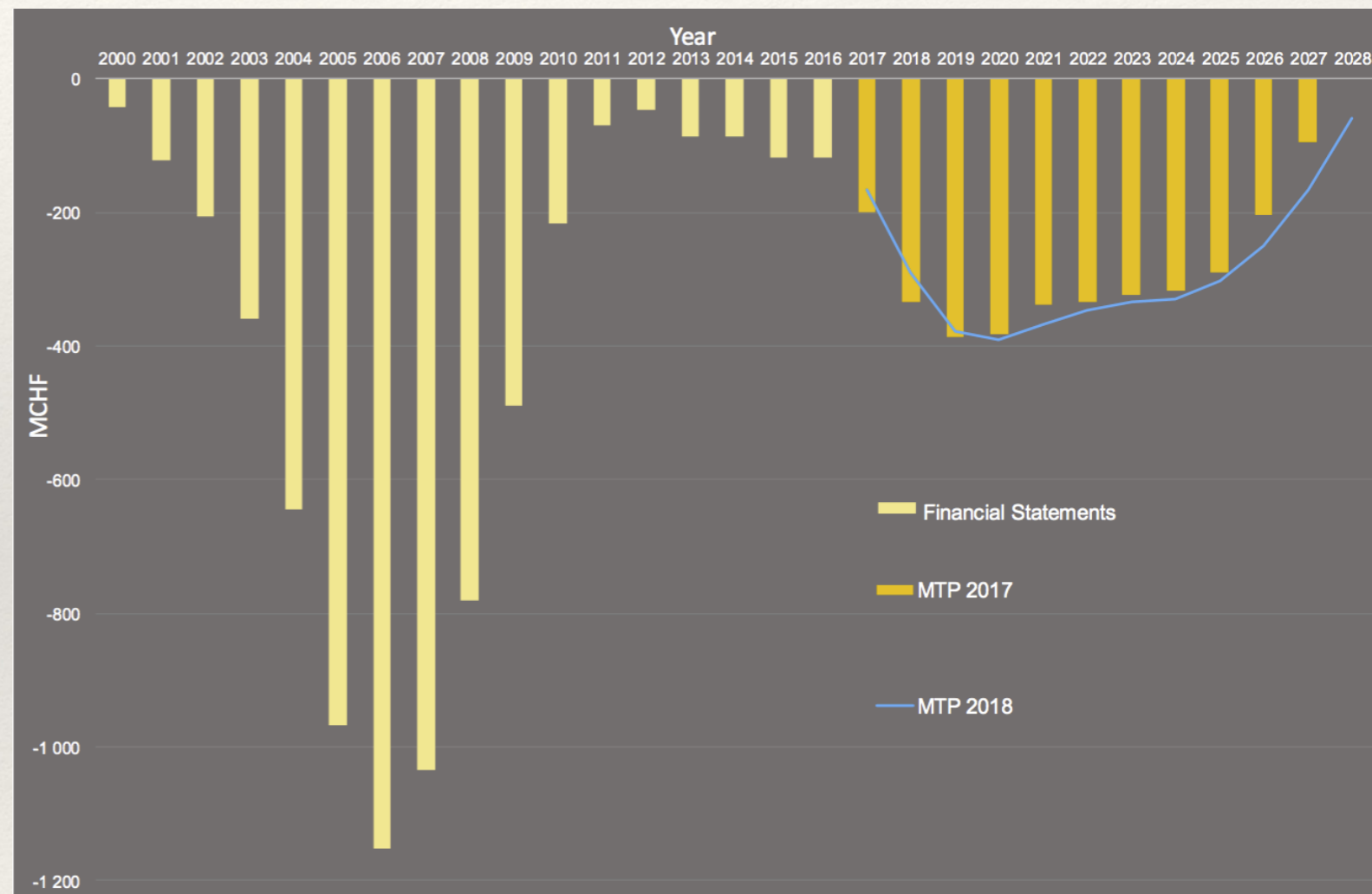
# However you are not alone.



- ❖ You may want to take note of the open symposium/town meeting in May 2019.

# Real decisions to be made

- ❖ Cern is entering into a 6-7 year period of financial deficit to pay for the HL-LHC upgrade.
- ❖ Because of the financial situation, there is not money to support both magnet R&D and CLIC TDR preparation, to be ready to start a project in 2027-2028



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# Conclusions

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- ❖ Human ingenuity (colliders, superconducting magnets) have allowed the field to progress. There is no reason to think that the reservoir of human ingenuity has run dry.
- ❖ Our field has made bold decisions in the past, ISR, SppbarS, Tevatron and LHC.
- ❖ Vigorous R&D on alternative acceleration techniques is mandatory.
- ❖ We have real decisions to make soon.



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# Bibliography

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- ❖ Projections for future Higgs at HL-LHC, 1307.7135v2(CMS),ATL-PHYS-PUB-2014-016, partial update CMS PAS FTR-16-002.
- ❖ Physics case for ILC250, 1710.07621,
- ❖ International linear collider staging report, 1711.00568
- ❖ Higgs Physics at CLIC, 1608.07538
- ❖ Higgs Physics at FCC-ee, 1308.6176
- ❖ Higgs Physics at CEPC, IHEP-CEPC-DR-2015-01
- ❖ Higgs measurements at a muon collider, 1304.5270.
- ❖ Machine parameters and projected luminosity performance of proposed future colliders at CERN, CERN/SPC/1114.