

# Energy calibration for W physics

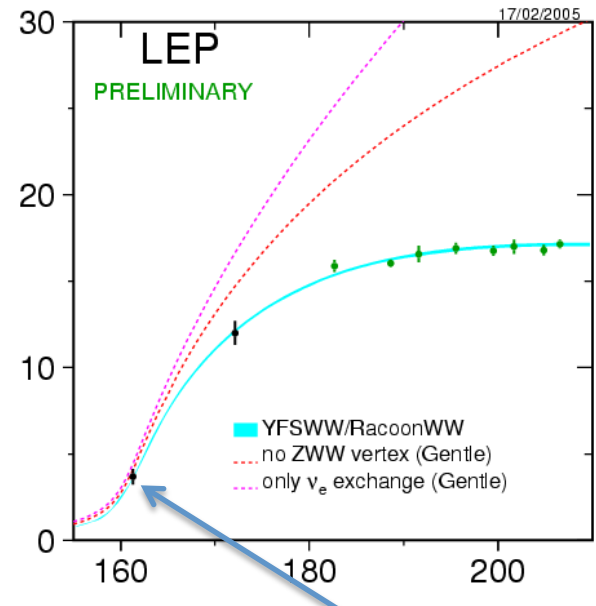
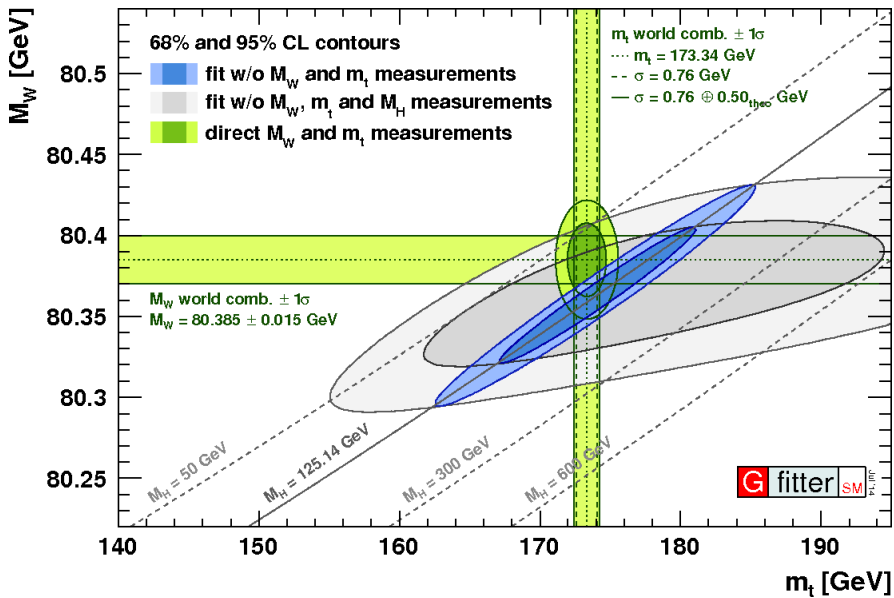


Paolo Azzurri – INFN Pisa

FCC-ee polarization workshop

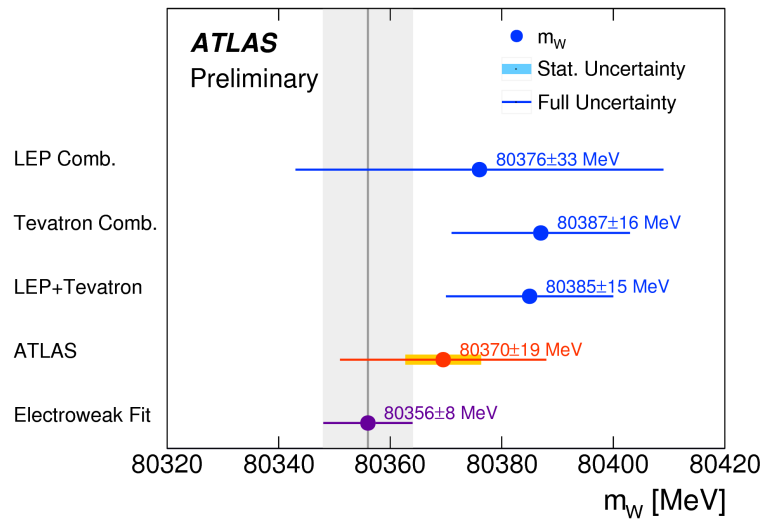
October 18<sup>th</sup> 2017

# WW threshold



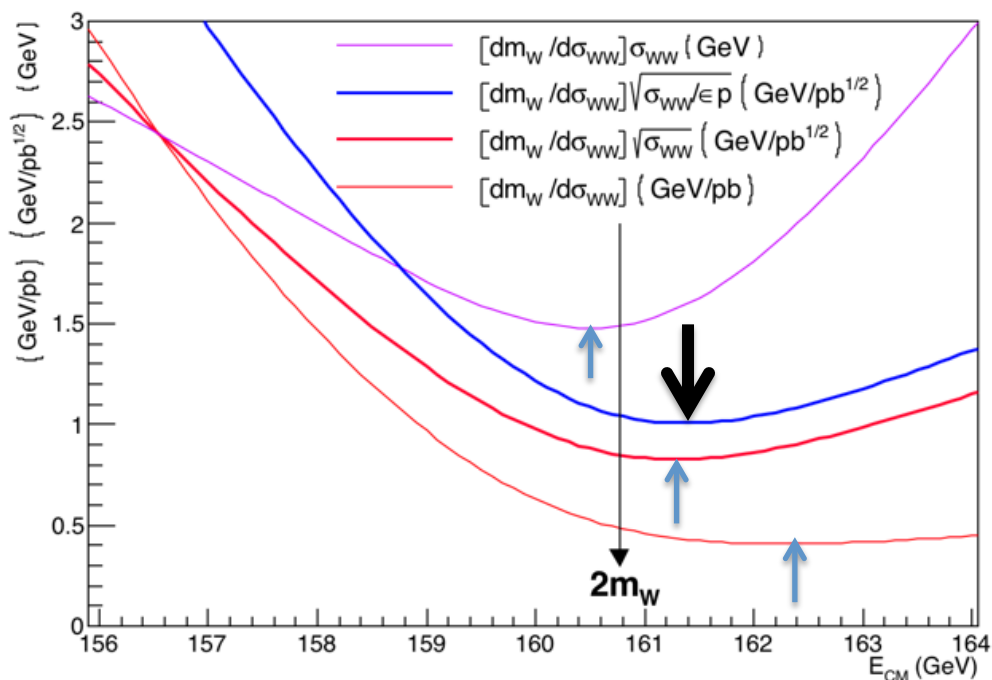
At LEP2  $\sqrt{s}=161$  GeV  $\sigma=4$ pb  
 $\epsilon=0.75$ ,  $\sigma_B=300$  fb  
 $p=0.9$  :  $\epsilon p \approx 0.68$  (@161)  
 $\rightarrow m_W=80.40 \pm 0.21$  GeV  
 with 11/pb @  $E_{\text{CM}}=161$  GeV

$$\Delta m_W = \left( \frac{d\sigma}{dm_W} \right)^{-1} \Delta \sigma$$



# $m_W$ from $\sigma_{WW}$ : sensitivity vs $E_{CM}$

$\sigma_{WW}$  with YFSWW3 1.18  
 $m_W=80.385$  GeV



**Max stat sensitivity at  $\sqrt{s} \sim 2m_W + 600$  MeV**

$\sqrt{\epsilon p}$  with fixed :  $\epsilon=0.75$  and  $\sigma_B=0.3$ pb

*statistical precision*  
 with  $L = 11/\text{pb} \rightarrow \Delta m_W \approx 350 \text{ MeV}$   
 with  $L = 8/\text{ab} \rightarrow \Delta m_W \approx 0.40 \text{ MeV}$

need syst control on :

- $\Delta\epsilon/\epsilon, \Delta L/L < 10^{-4}$
- $\Delta\sigma_B < 0.7 \text{ fb} (2 \cdot 10^{-3})$

and  
 $\Delta E(\text{beam}) < 0.40 \text{ MeV} (5 \cdot 10^{-6})$

# WW threshold $\Delta M_W$

$$\sigma = \left( \frac{N}{L} - \sigma_B \right) \frac{1}{\varepsilon}$$

$$\Delta m_W(\text{stat}) = \left( \frac{d\sigma}{dm_W} \right)^{-1} \frac{\sqrt{\sigma}}{\sqrt{L}} \frac{1}{\sqrt{\varepsilon p}}$$

$$\Delta \sigma_{WW} = \frac{\Delta \sigma_B}{\varepsilon}$$

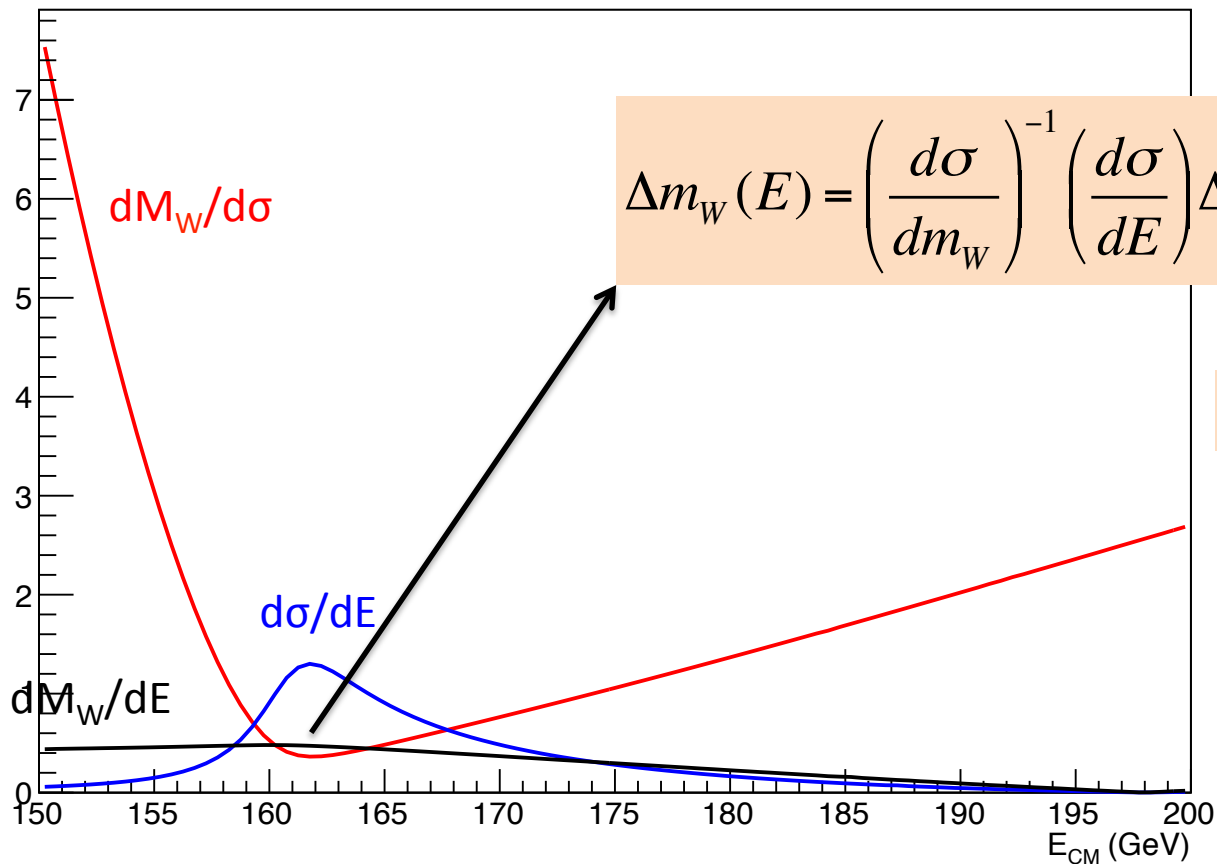
$$\Delta m_W(B) = \left( \frac{d\sigma}{dm_W} \right)^{-1} \frac{\Delta \sigma_B}{\varepsilon}$$

$$\Delta \sigma_{WW} = \sigma \left( \frac{\Delta \varepsilon}{\varepsilon} \oplus \frac{\Delta L}{L} \right)$$

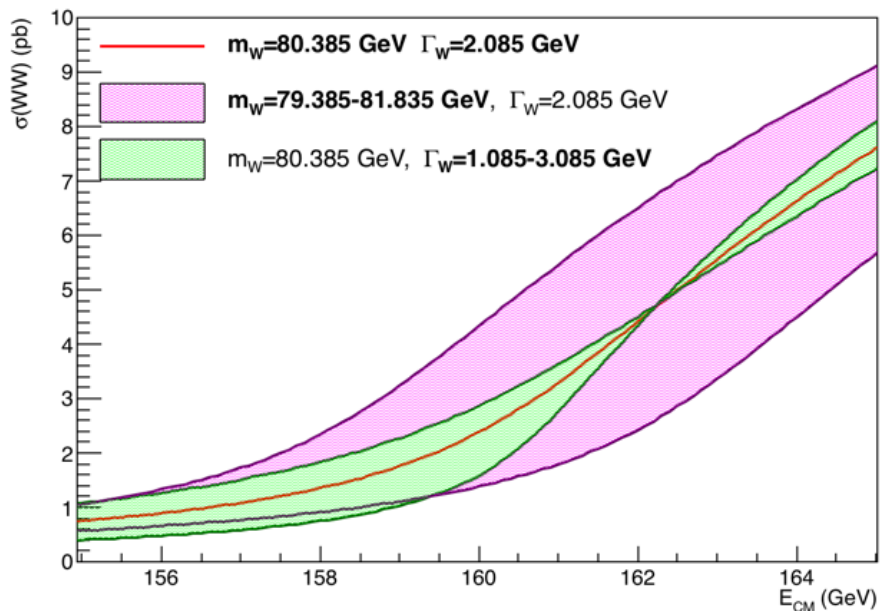
$$\Delta m_W(\varepsilon) = \left( \frac{d\sigma}{dm_W} \right)^{-1} \left( \frac{\Delta \varepsilon}{\varepsilon} + \frac{\Delta L}{L} \right)$$

$$\Delta m_W(E) = \left( \frac{d\sigma}{dm_W} \right)^{-1} \left( \frac{d\sigma}{dE} \right) \Delta E$$

# $dM_W/dE_{CM}$



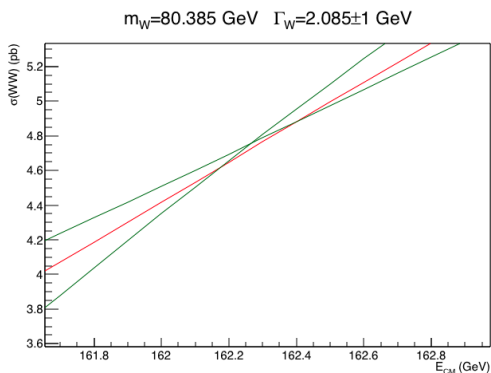
# $\Gamma_W$ from $\sigma_{WW}$



Measure  $\sigma_{ww}$  in two energy points  $E_1, E_2$  with a fraction  $f$  of lumi in  $E_1$   
 $\rightarrow$  determine both  $m_W$  &  $\Gamma_W$

Determine  $f, E_1, E_2$  such to minimise  $(\Delta\Gamma_W, \Delta m_W)$  with some target

Evaluate loss of  $\Delta m_W$  precision in the single parameter ( $m_W$ ) determination wrt scenario of running only at an optimal  $E_0=161$  point



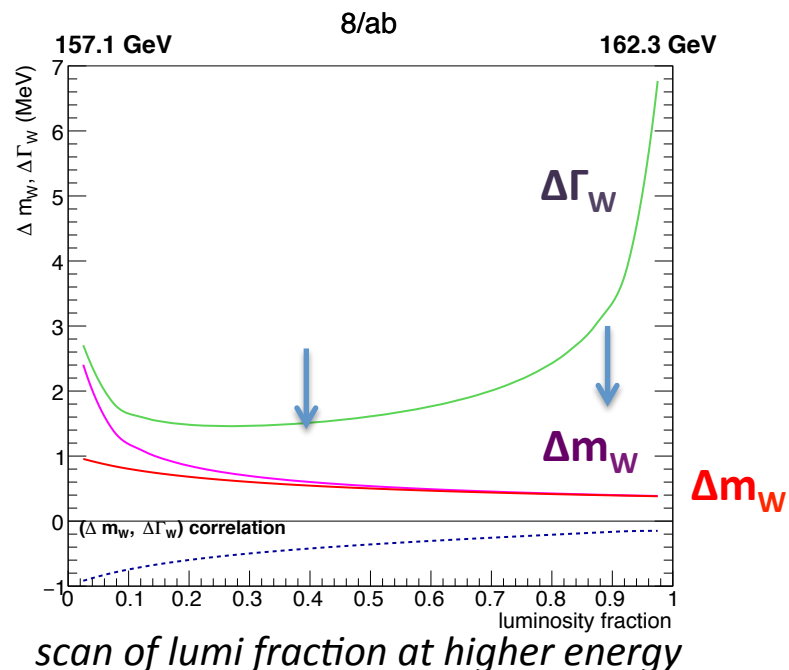
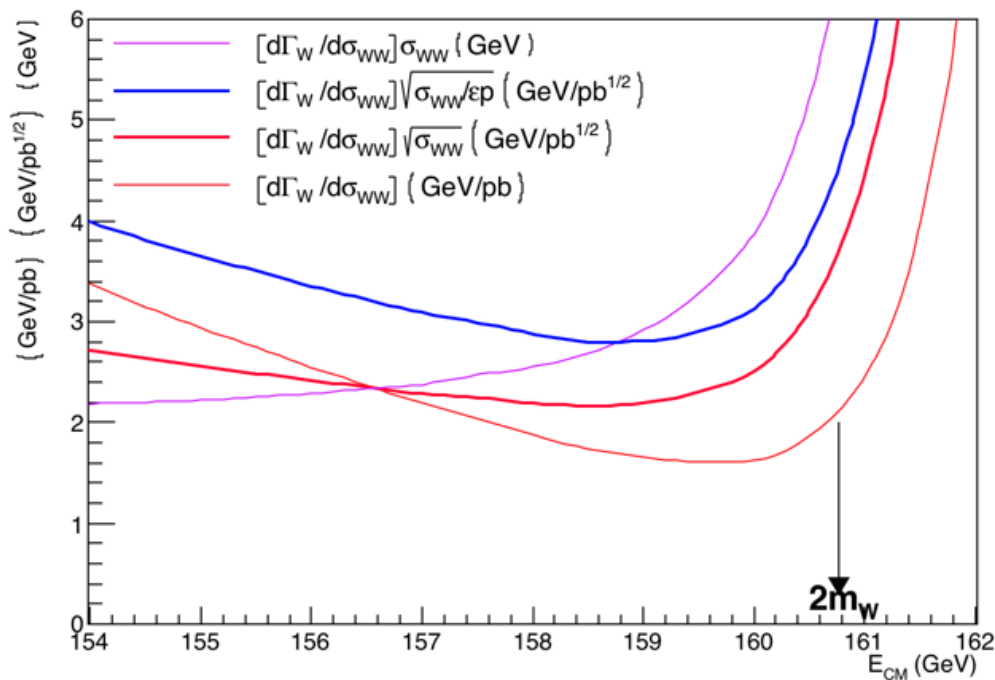
$$\frac{d\sigma_{WW}}{d\Gamma_W} = 0$$

$$\text{at } E_{CM} \sim \mathbf{162.3 \text{ GeV}}$$

$$\sim 2m_W + 1.5 \text{ GeV}$$

# $m_W$ & $\Gamma_W$ from $\sigma_{WW}$

$m_W=80.385$  GeV  $\Gamma_W=2.085$  GeV



$\Delta m_W, \Delta \Gamma_W$ : error on W mass and width from fitting both

$\Delta m_W$ : error on W mass from fitting only  $m_W$

min  $\Delta m_W + \Delta \Gamma_W$

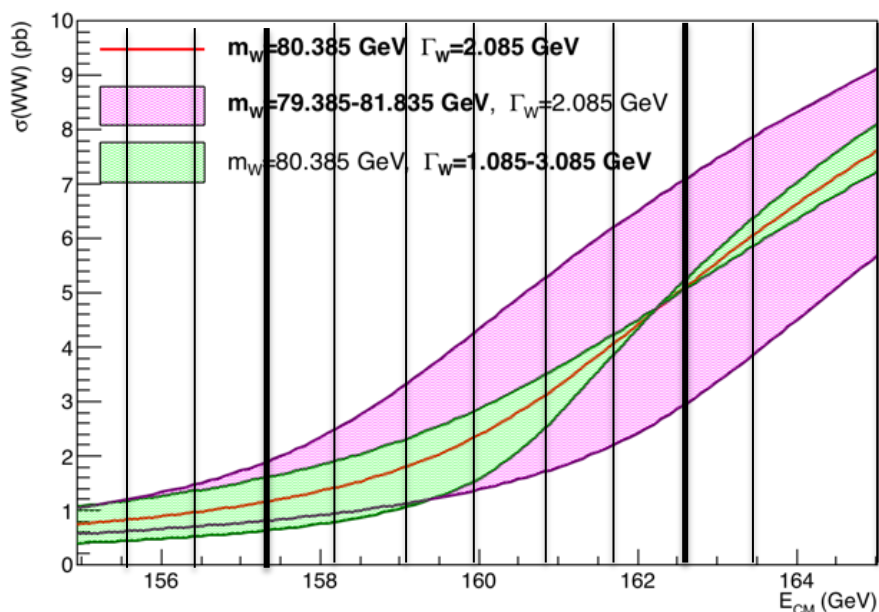
with  $E_1=157.1$  GeV  $E_2=162.3$  GeV  $f=0.4$

$\Delta m_W=0.62$   $\Delta \Gamma_W=1.5$   $\Delta m_W=0.56$  (MeV)

$\rightarrow \Delta \alpha_s \approx (3 \pi/2) \Delta \Gamma/\Gamma \approx 0.003$

# with half-integer spin tunes

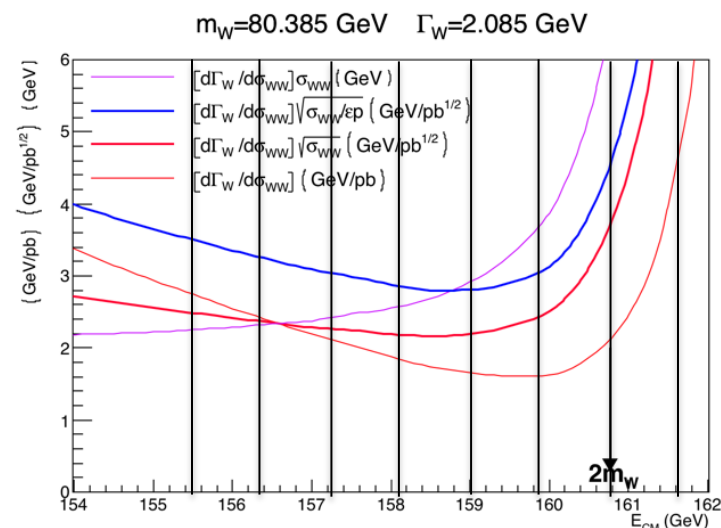
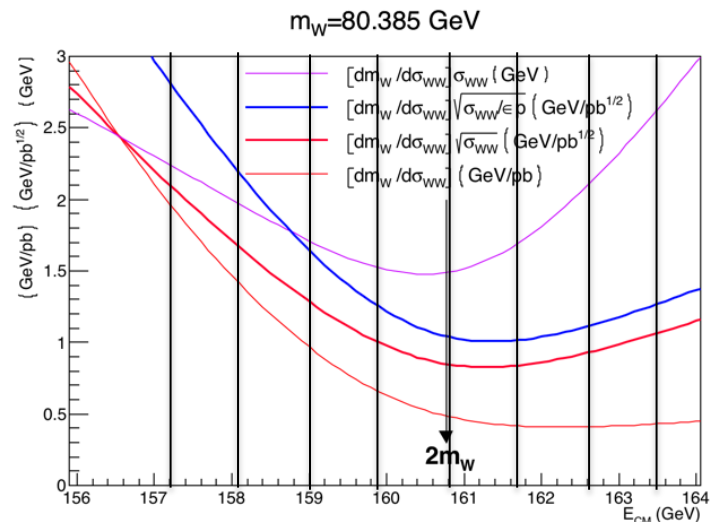
limiting data taking points to  
 $E_{CM} = (2n+1)*0.4406486 \text{ GeV}$



$\min \Delta m_W + \Delta \Gamma_W$

with  $E_1=157.3 \text{ GeV}$   $E_2=162.6 \text{ GeV}$   $f=0.4$   
 $\Delta m_W=0.65$   $\Delta \Gamma_W=1.6$   $\Delta m_W=0.60 \text{ (MeV)}$

**~10% loss of stat precision**





# acc & bkg control

decay	efficiency	purity	bkg	[LEP1996]
$l\nu l\nu$	70-80%	80-90%	<b>50fb</b> ( $\tau\tau, \gamma\gamma \rightarrow \tau\tau, Z\gamma^* \rightarrow \nu\nu ll$ )	
$e\nu qq$	85%	~90%	<b>30fb</b> ( $qq, Zee, Z\gamma^*$ ) <b>-10fb</b> ( $W\nu\nu$ )	
$\mu\nu qq$	90%	~95%	<b>10fb</b> ( $Z\gamma^*, qq$ )	
$\tau\nu qq$	50%	80-85%	<b>50fb</b> ( $qq, Z\gamma^*$ )	
$qqqq$	90%	~90%	<b>~200fb</b> ( $qq (qqqq, qqgg)$ )	

2-fermion :  $\tau\tau, qq$   
 4-fermion :  $\gamma\gamma \rightarrow \tau\tau, ll\nu\nu, Zee, W\nu\nu$

some 4f bkg is identical to the signal final state  $\rightarrow$  CC03-4f interferences

measure directly the **backgrounds** with very different S/B levels **at different  $E_{CM}$  points**

concern is mostly on the four-jet background

**measure forward electrons ( $\theta \geq 0.1$  rad)** for Zee W $\nu\nu$  : determine forward pole  $d\sigma/d\theta$  and WW interference effects

acceptance down to  $\theta=0.1$  [ $\cos\theta=0.995$ ] would also cover forward jets

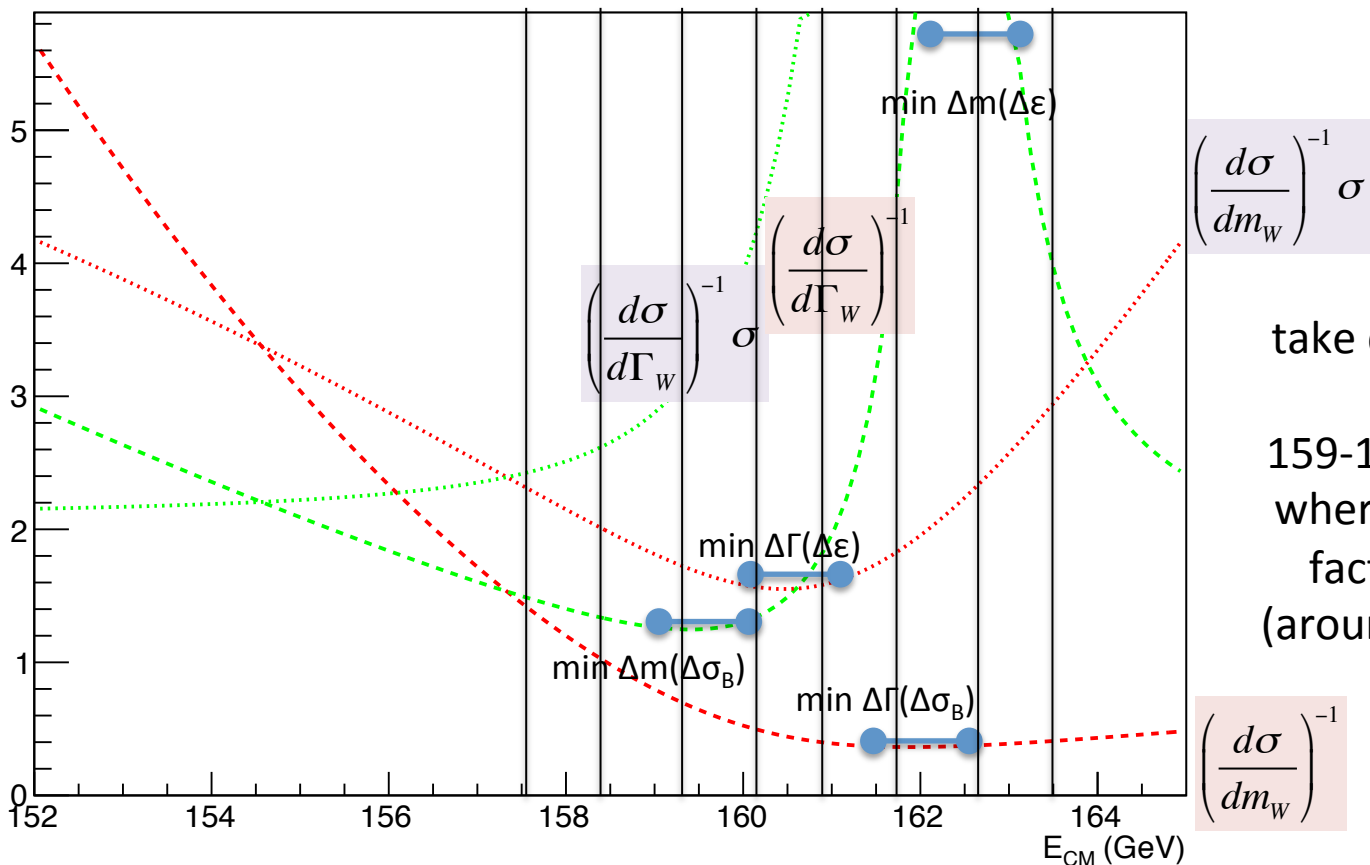
limiting **correlated** systs can cancel out taking data at more  $E_{CM}$  points where

$$\left(\frac{d\sigma}{d\Gamma_w}\right)^{-1} \left(\frac{d\sigma}{dm_w}\right)^{-1} \left(\frac{d\sigma}{dm_w}\right)^{-1} \sigma \left(\frac{d\sigma}{d\Gamma_w}\right)^{-1} \sigma$$

differential factors are equal

# $m_W$ & $\Gamma_W$ from $\sigma_{WW}$

optimal E points with limiting **correlated** systs



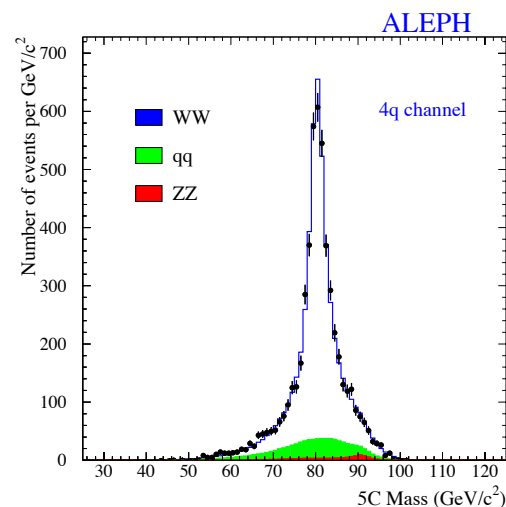
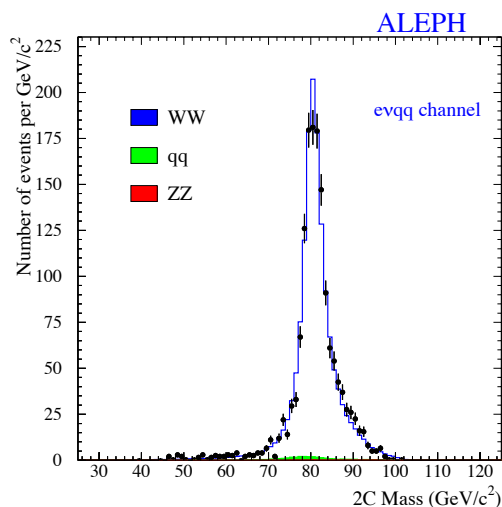
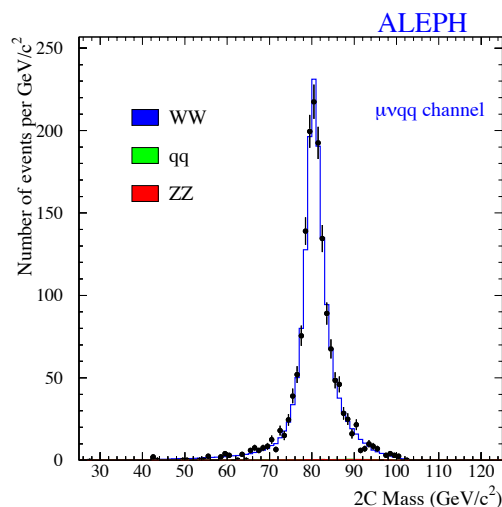
take data at different  $E_{CM}$  points  
159-160-161-162-163  
where the derivative factors are equal (around their minima)

# reco mass of the W boson

full  $m_W$  reco with kinematic fit. main ingredients :

$E_{CM}$  – jet/lepton angles – (jet boost )

$$M_Z^2 = s \frac{\beta_1 \sin \theta_1 + \beta_2 \sin \theta_2 - \beta_1 \beta_2 |\sin(\theta_1 + \theta_2)|}{\beta_1 \sin \theta_1 + \beta_2 \sin \theta_2 + \beta_1 \beta_2 |\sin(\theta_1 + \theta_2)|}$$



ALEPH Eur.Phys.J.C47:309 (2006) : 683 /pb  $\sim 10\text{k}$  WW events

*ignoring low energy particles in the qq qq channel*

$m_W = 80440 \pm 43(\text{stat.}) \pm 24(\text{syst.}) \pm 9(\text{FSI}) \pm 9(\text{LEP}) \text{ MeV}$

$\Gamma_W = 2140 \pm 90(\text{stat.}) \pm 45(\text{syst.}) \pm 46(\text{FSI}) \pm 7(\text{LEP}) \text{ MeV}$

# reco mass of the W boson

8/ab@160GeV + 5/ab@240GeV

→ 30M+ 80M W-pairs

→  $\Delta m_W$  (stat)= 0.5 MeV

→  $\Delta m_W$  (syst)  $\leq$  1 MeV ?

WW events produced near threshold also carry (reduced) kin information on  $m_W$

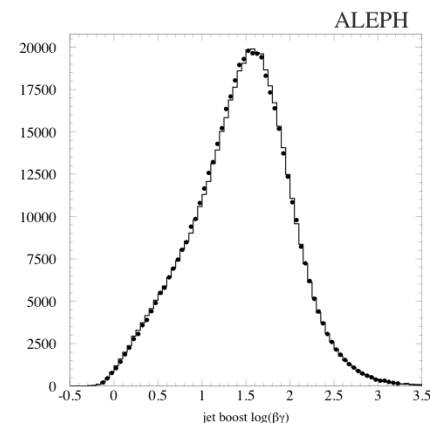
Is  $\Delta E_{\text{beam}} < 1\text{MeV}$  at  $E_{\text{CM}} = 240\text{ GeV}$  possible ?

With Z $\gamma$  events ?

$\Delta E_{\text{beam}} \sim 15\text{MeV}(\text{stat})$  @LEP

Table 9: Summary of the systematic errors on  $m_W$  and  $\Gamma_W$  in the standard analysis averaged over 183-209 GeV for all semileptonic channels. The column labelled  $l\nu q\bar{q}$  lists the uncertainties in  $m_W$  used in combining the semileptonic channels.

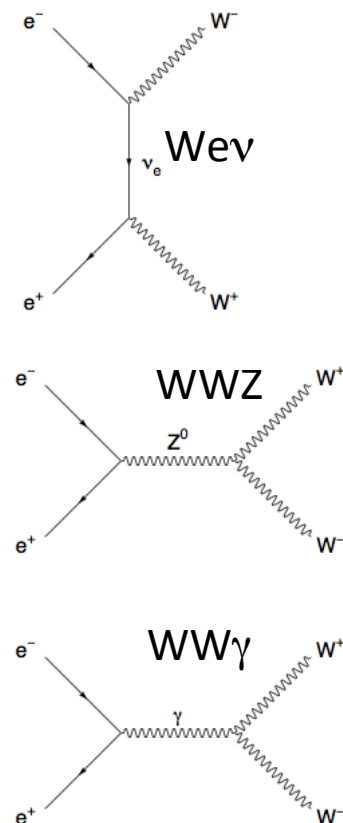
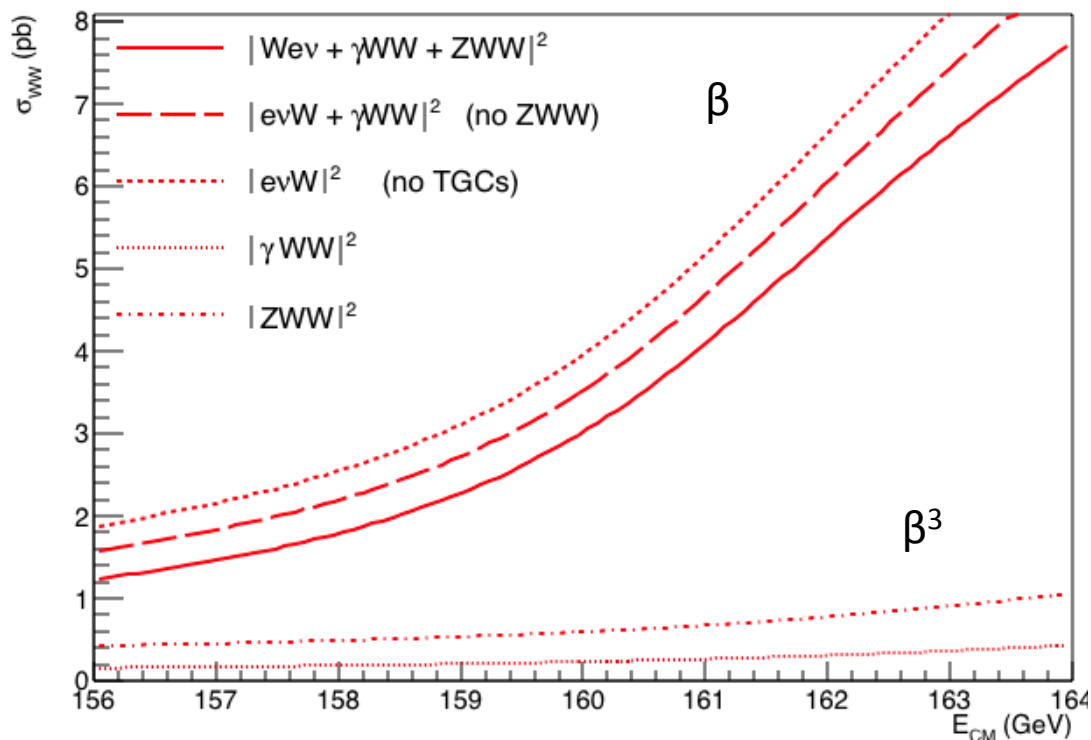
Source	$\Delta m_W$ (MeV/ $c^2$ )				$\Delta \Gamma_W$ (MeV)			
	$e\nu q\bar{q}$	$\mu\nu q\bar{q}$	$\tau\nu q\bar{q}$	$l\nu q\bar{q}$	$e\nu q\bar{q}$	$\mu\nu q\bar{q}$	$\tau\nu q\bar{q}$	$l\nu q\bar{q}$
$e+\mu$ momentum	3	8	-	4	5	4	-	4
$e+\mu$ momentum resolu	7	4	-	4	65	55	-	50
Jet energy scale/linearity	5	5	9	6	4	4	16	6
Jet energy resolu	4	2	8	4	20	18	36	22
Jet angle	5	5	4	5	2	2	3	2
Jet angle resolu	3	2	3	3	6	7	8	7
Jet boost	17	17	20	17	3	3	3	3
Fragmentation	10	10	15	11	22	23	37	25
Radiative corrections	3	2	3	3	3	2	2	2
LEP energy	9	9	10	9	7	7	10	8
Calibration ( $e\nu q\bar{q}$ only)	10	-	-	4	20	-	-	9
Ref MC Statistics	3	3	5	2	7	7	10	5
Bkgnd contamination	3	1	6	2	5	4	19	7



lepton and jet uncertainties from (Z) calibration data

# TGCs (also at threshold)

$SU(2) \otimes U(1)$  Gauge Cancellations



without TGCs

$\sigma_{WW} +40\% @157\text{GeV} +25\% @162\text{GeV}$

while  $\Delta\sigma/\sigma \approx 0.5 \cdot 10^{-3}$

LEP2 limits :  $\kappa, \lambda < 2-6 \cdot 10^{-2}$

# Conclusions

- The WW threshold  $\sigma$  lineshape is a great opportunity to measure both  $m_W$  and  $\Gamma_W$  at the (sub)-MeV level with FCCee
  - optimal points to take data are  $\sqrt{s}=2m_W+1.5$  GeV ( **$\Gamma$ -insensitive**) and  $\sqrt{s}=2m_W-2-3$  GeV ( **$-\Gamma$ off shell**)
  - limiting data taking ECM points to half-integer spin tunes will bring a very limited degradation to the optimal stat sensitivity.
- Direct  $m_W$  reconstruction would also necessitate  $E_{\text{beam}}$  at the MeV level
  - making use of radiative Z-returns events can provide precise  $E_{\text{beam}}$  constraints (leading to an effective  $m_W/m_Z$  determination)
  - we can probably make use also of W-pairs collected near threshold to perform a direct reconstruction  $m_W$  measurement

Work in progress by **Marina Beguin**, stay tuned

- Many other W-physics topics (W BRs, TGCs ...) should not have stringent  $E_{\text{CM}}$  requirements

# $m_W$ & $\Gamma_W$ from $\sigma_{WW}$

Uncertainty propagation

$$\begin{cases} \Delta\sigma_1 = a_1\Delta m + b_1\Delta\Gamma \\ \Delta\sigma_2 = a_2\Delta m + b_2\Delta\Gamma \end{cases}$$

$$a_1 = \frac{d\sigma_1}{dm}$$

$$b_1 = \frac{d\sigma_1}{d\Gamma}$$

$$a_2 = \frac{d\sigma_2}{dm}$$

$$b_2 = \frac{d\sigma_2}{d\Gamma}$$

$$\Delta m = -\frac{b_2\Delta\sigma_1 - b_1\Delta\sigma_2}{a_2b_1 - a_1b_2}$$

$$\Delta\Gamma = \frac{a_2\Delta\sigma_1 - a_1\Delta\sigma_2}{a_2b_1 - a_1b_2}$$

$\Delta m, \Delta\Gamma$  linear correlation with uncorrelated  $\Delta\sigma_1, \Delta\sigma_2$

$$r = -\frac{1}{\Delta m \Delta\Gamma} \frac{a_2b_2\Delta\sigma_1^2 + a_1b_1\Delta\sigma_2^2}{(a_2b_1 - a_1b_2)^2}$$