

## IFMP WORKSHOP IN IONIAN UNIVERSITY, CORFU, GREECE

Monday 6/11/2017 12:00

### PET BASICS

Ivo Rausch, PhD

*Medical University Vienna, Centre Medical Physics and Biomedical Engineering, QIMP Group*

The discovery of radioactivity in the late 1890's by Henry Becquerel was the starting point of a wide range of new discoveries and application. One of those was the development of the radioactive tracer principle by George de Hevesy in 1911 which led to the first experiments using a radioactive tracer in humans in 1923. In the following decades the field progressed e.g. with the discovery of the positron or the development of cyclotrons and nuclear reactors. This made it possible to produce artificial radioactive sources in a large amount.

In 1951 Wrenn and colleges published the first application of positrons for brain tumours using coincident detection of the annihilation photons. This was the birth of the technique used in positron emission tomography (PET) and finally led to the development of the first PET scanner in 1975.

A PET relies on the simultaneous detection of two photons travelling in opposing direction originating from positron annihilation. Hence, if these two photons are detected, it is evident that the annihilation has taken place somewhere on a line (also referred to as line of response (LOR)) between the two detectors. In PET coincident photons are detected in a ring geometry or by extended opposing detector arrays from various angles around a positron source. A set of parallel LORs correspond to the projection of the activity distribution from a certain angle. Thereby, it is possible to reconstruct an image of the measured activity distribution using tomographic reconstruction techniques.

In a real setting, photons travelling through an extended object are attenuated according to the properties of its material. One big advantage of coincidence detection is that the probability of attenuation is solely dependent on the attenuation probability across the whole object along the respective LOR. This can be measured using a rotating transmission source e.g. a Ge/Ga 68 source or by computed tomography, used to correct attenuation of the annihilation photons.

Therefore, PET is principally able to quantitatively measure an activity distribution in an extended object.

# Positron emission tomography Basics

---

Ivo Rausch, PhD

Center for Medical Physics and Biomedical Engineering



# Overview

---

1. The Tracer Principle
2. The beta decay
3. Positron emission tomography
4. Reconstruction
5. Detectors
6. System design
7. PET/CT

# The tracer principle

Use of a radioactive compound to measure in-vivo processes

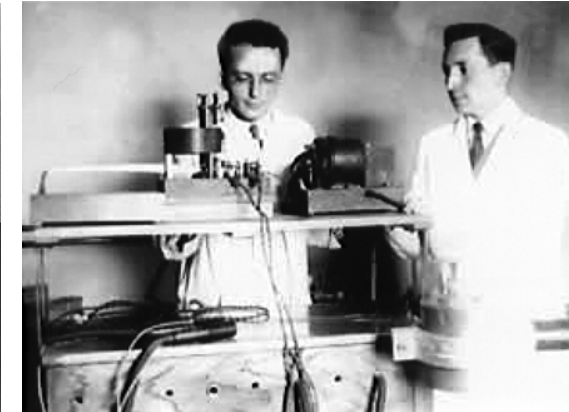
1913 First use of radioactive isotopes by George de Hevesy – works on Pb-salt solubility with a Pb-isotope.

1923 (De Hevesy) Pb-salt uptake in Plants

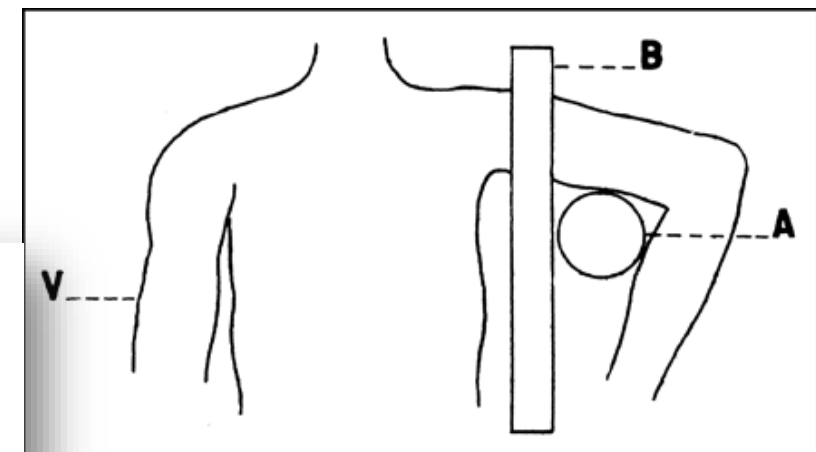
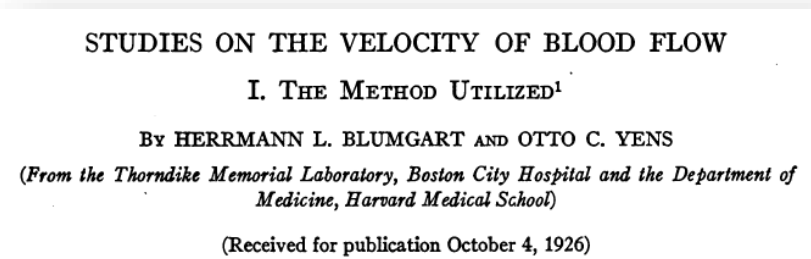
1924 Blumgart and Yens / Weiss – Bi 212 into arm of patient – measured arrival in other



www.nobelprize.org

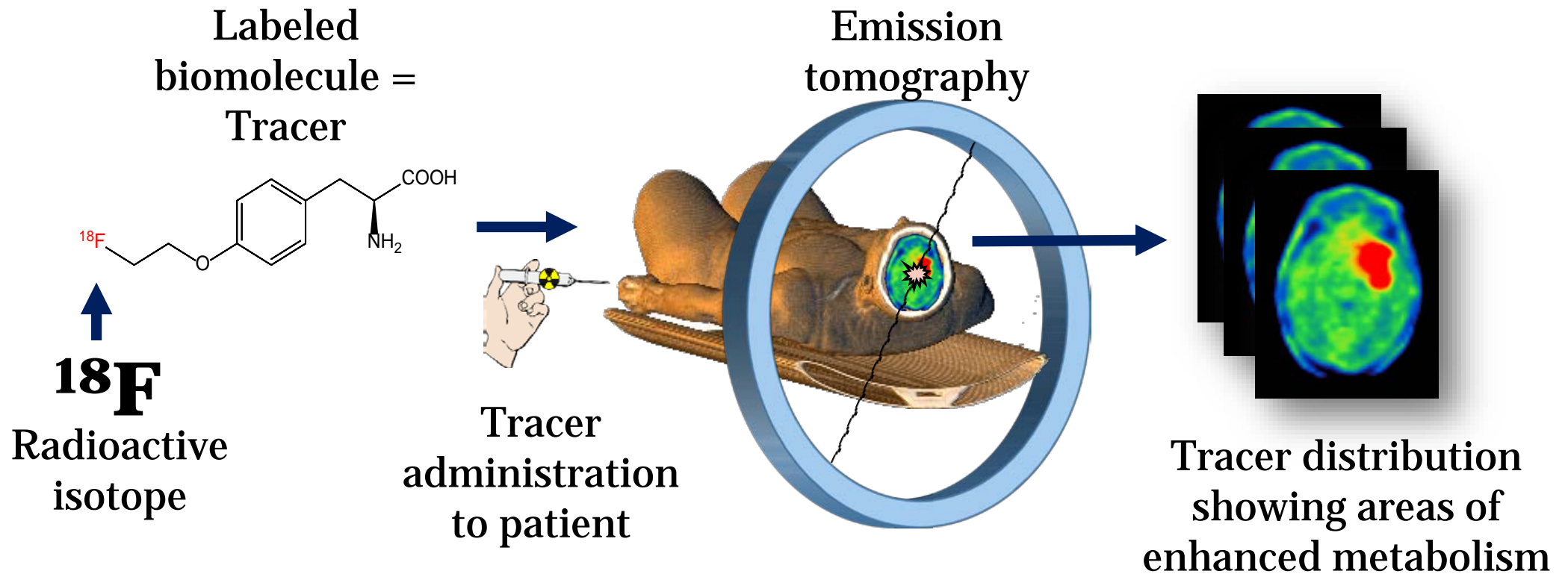


Patton, JNM 2003



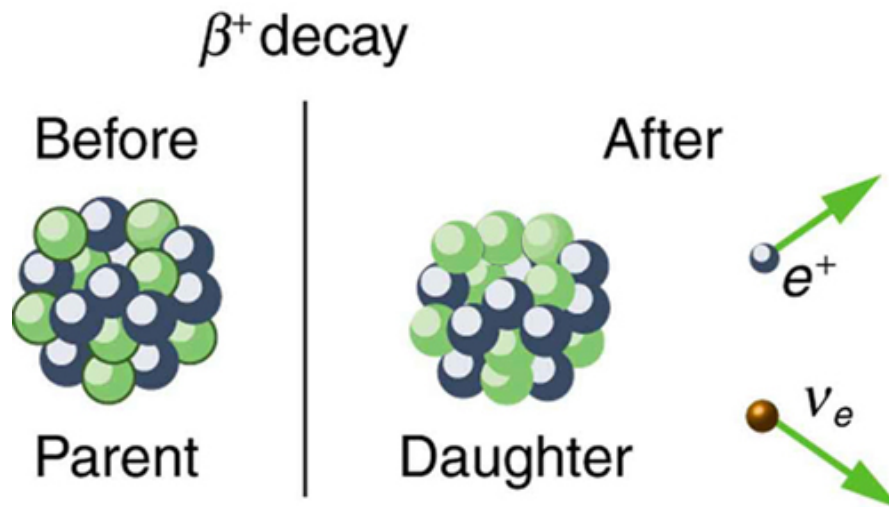
A radioactive tracer can be tracked to study dynamic processes

# Principle of Nuclear Medicine

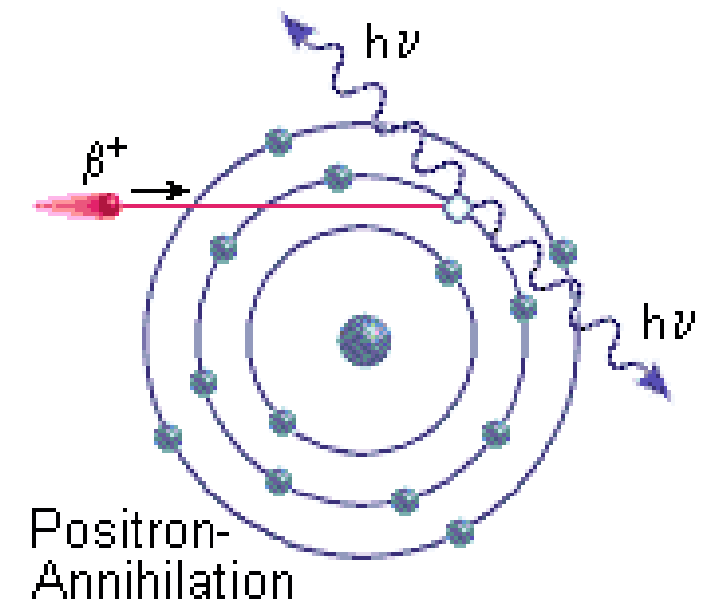


# The beta+ decay

For nuclei with a fixed mass number a proton can transform to a neutron =  $\beta^+$  (and conversely =  $\beta^-$ )



- $e^+$  antiparticle to  $e^-$  -> annihilation
  - $E = mc^2 = 2 \times 511\text{keV}$
  - Momentum conservation ->  $\sim 180^\circ$



Beta+ decay: Changing a proton into a neutron

# Coincidence counting

First described by Wrenn et al. (Science 1951) for localization of Brain tumors

$e^+$  decay leads to 2 perpendicular  $\gamma$ -rays

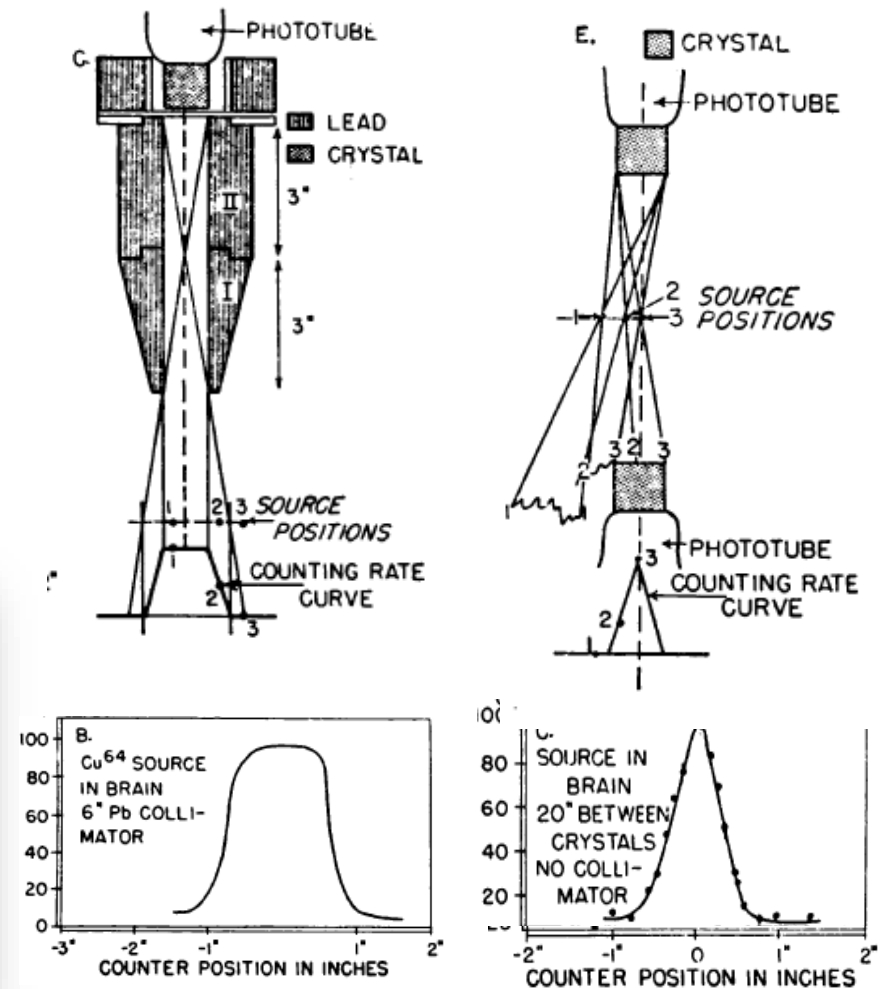
If detected, decay took place on a line between detectors

Equivalent to a projection

## The Use of Positron-emitting Radioisotopes for the Localization of Brain Tumors<sup>1</sup>

Frank R. Wrenn, Jr.,<sup>2</sup> Myron L. Good, and Philip Handler

*Division of Neurosurgery, Departments of Physics and Biochemistry and Nutrition, Duke University, Durham, North Carolina*



Coincidence counting requires no collimation

# PET principle

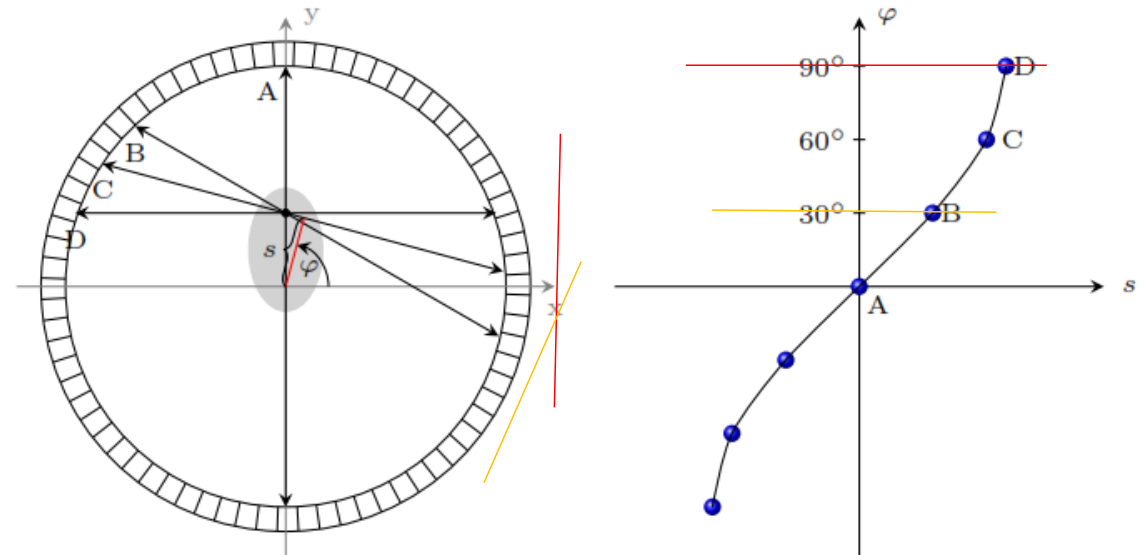
PET relies on detection of two photons from positron annihilations

Most common: ring geometry

Annihilation on a line (LOR) between the detectors

Parallel lines belong to same projection

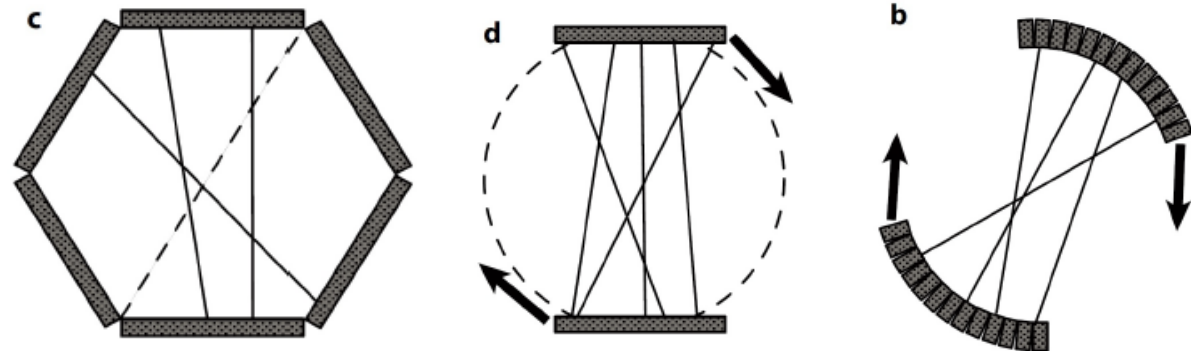
Data most common represented as “Sinograms”



(a) LORs in the scanner

(b) Sinogram

Courtesyv Albert Hirtl



Multiple projections are acquired using a detector ring



# The first PE(T)T

First described by Phelps et al.  
JNM 1975

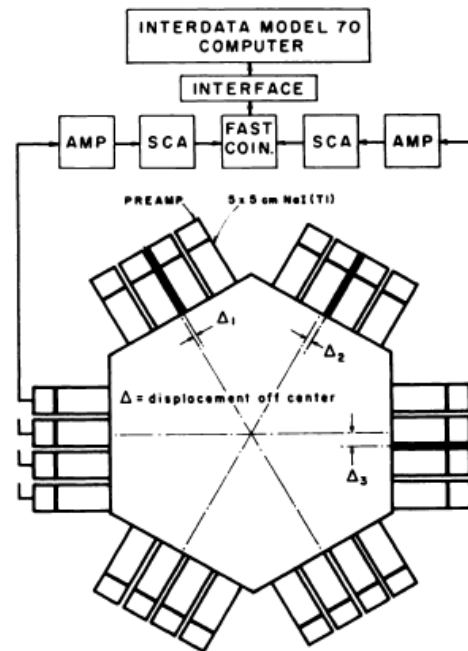
Prototype of a positron  
emission transaxial tomograph  
(PETT)

Tested on phantoms and dogs

Reconstructed using Fourier  
transformation and  
attenuation corrected using  
 $^{64}\text{Cu}$  source

## APPLICATION OF ANNIHILATION COINCIDENCE DETECTION TO TRANSAXIAL RECONSTRUCTION TOMOGRAPHY

Michael E. Phelps, Edward J. Hoffman, Nizar A. Mullani, and Michel M. Ter-Pogossian  
*Washington University School of Medicine, St. Louis, Missouri*



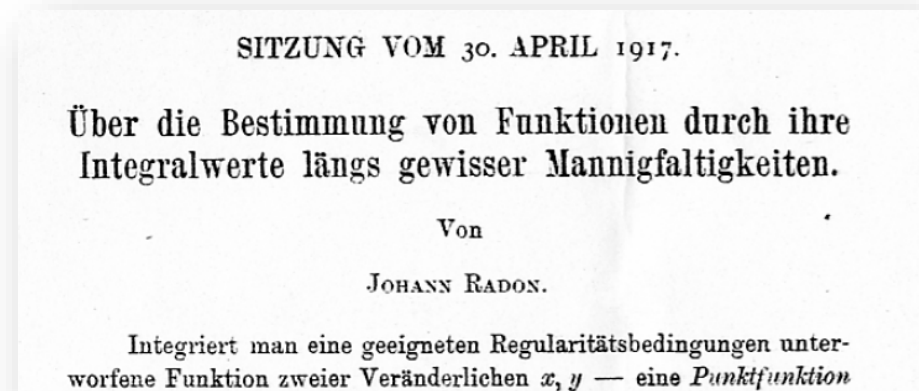
The first positron emission tomograph was described in 1975

# Image reconstruction

## General Problem:

Get a 2D image out of 1D projections

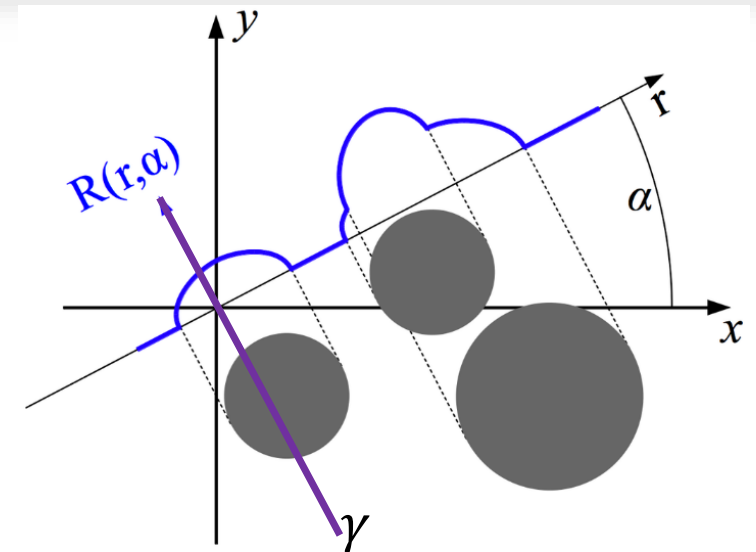
- In principle solved mathematically by Radon 1917
- Radon transformation



$$R(\alpha, r) = \int_{\gamma} f(x, y) d\gamma$$

Activity distribution

Projections



Line integral through activity concentration = Projection

Invers Radon transformation = FBP

# Image reconstruction: FBP

Back projection -> Blurred images

## Solution: FBP

Inverted radon transformation

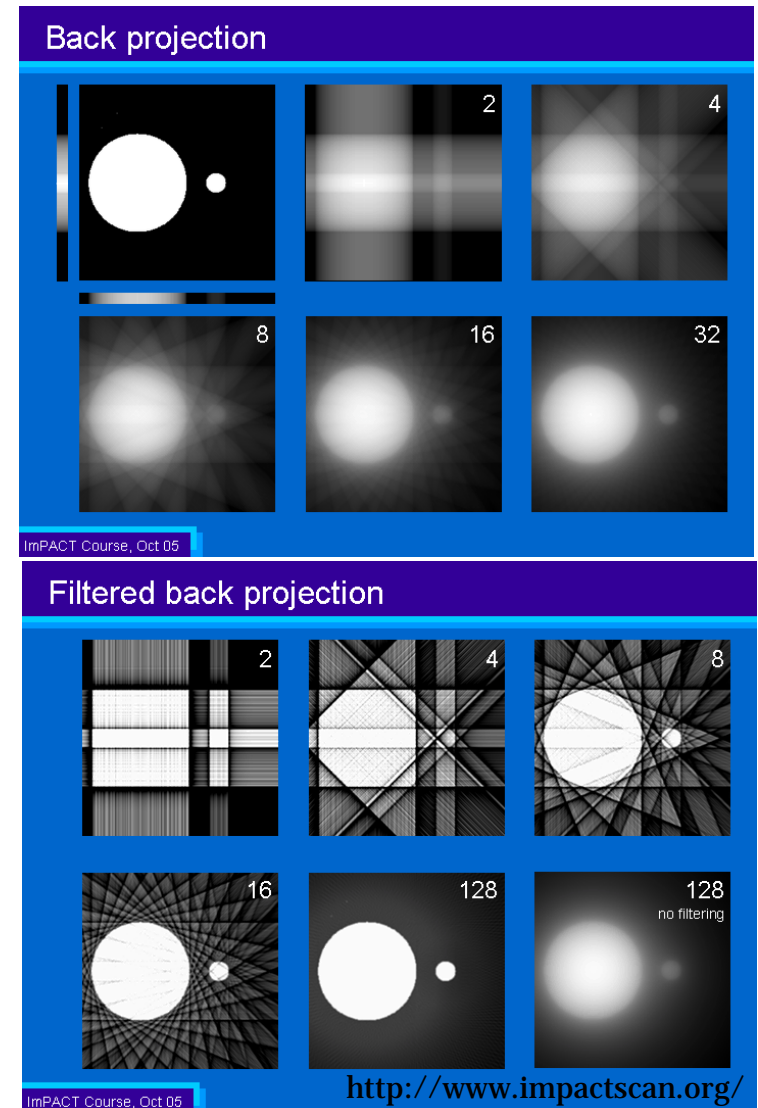
$$f(x, y) = \frac{1}{4\pi^2} \iint G(\alpha, \omega) e^{i\omega(x \sin \alpha - y \cos \alpha)} |\omega| d\omega d\alpha$$

**Filter!!!** (arrow pointing to  $|\omega|$ )

**Projections in Frequency space** (arrow pointing to  $G(\alpha, \omega)$ )

Filter:

- reduces low frequencies = blurring
- enhances high frequencies = sharp edges
- ! Enhances noise
- ! Limited # projections -> Cut of frequency



FBP is fast and easy but sensitive to noisy data

# Iterative Reconstruction

Getting a projection from an image can be written as a matrix multiplication

## Problem:

inversion of matrix not possible!!!

## Solution:

Iteratively finding the image which fits the measured projections

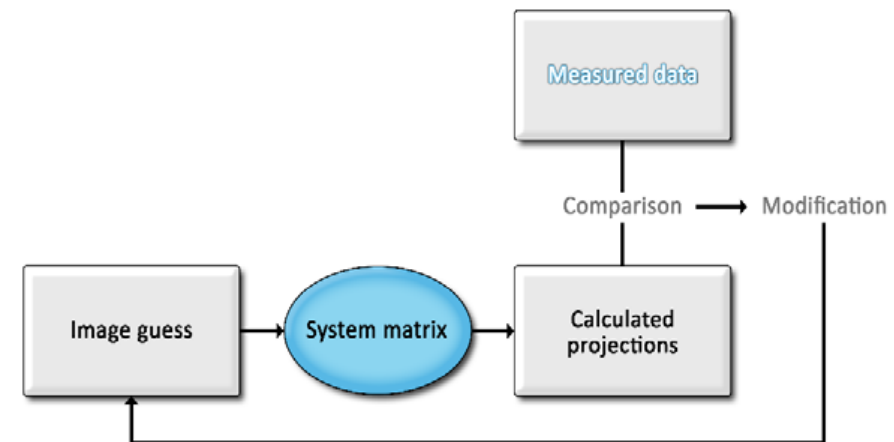
## Advantages:

- less affected by noise
- physical properties (scattering, absorption, resolution...) can be directly implemented into system-matrix

System-matrix: representing the PET

$$g_i = \sum_{j=1}^K c_{ij} \lambda_j$$

Projection  $\rightarrow$   $g_i$   $\leftarrow$  Image (activity distribution)  $\lambda_j$



Changing a activity distribution until it fits the measured data

# The OS-EM algorithm

## Maximum likelihood expectation maximisation

Algorithm for iterative reconstruction described by Sepp and Vardi 1982

Image update:

comparing and correcting with all projections

- slow convergence

## Ordered Subset:

A compromise described by Hudson and Larkin 1994: a subset of projections is taken for correction

- Good noise properties + fast convergence

## Maximum Likelihood Reconstruction for Emission Tomography

L. A. SHEPP AND Y. VARDI

Previous models for emission tomography (ET) do not incorporate timing information and correct for positron physics of ET from that of transmission tomography. We discuss methods to speed up reconstruction in a simple way. We discuss methods to speed up reconstruction in a simple way.

## Accelerated Image Reconstruction Using Ordered Subsets of Projection Data

H. Malcolm Hudson and Richard S. Larkin

We define ordered subset processing for standard fast Fourier transforms. Related approaches to the standard fast Fourier transforms. Related approaches to the standard fast Fourier transforms.

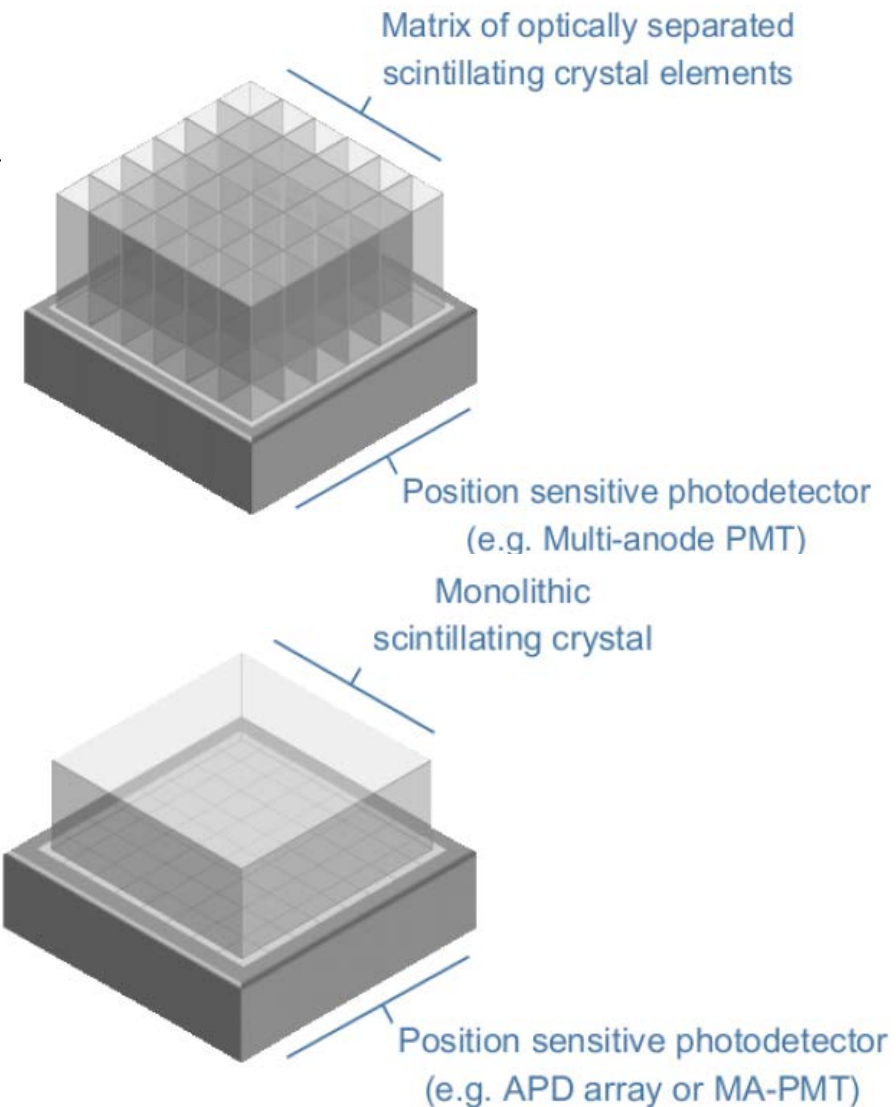
EM is the how to update the image, OS is for acceleration

# PET detectors

Transfer 511keV photons into electric signal

Most common devices consist of:

- **Scintillator:**  
converts high energy photons into visible light
- **Photo detector:**  
converts visible light into electric signal



A detector converts a 511 keV photon into an electrical signal

# Scintillator materials

Scintillator material needs certain properties

High interaction property with 511keV

➤ Density -> stopping power

High light output

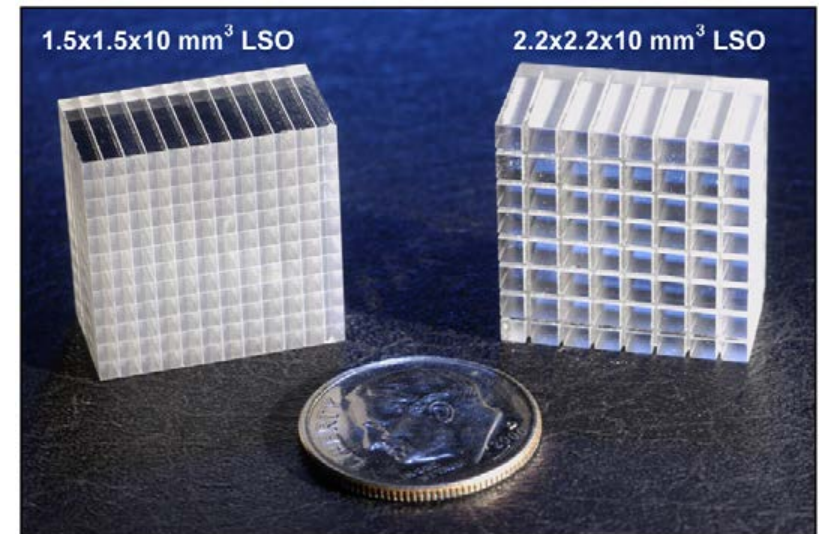
➤ Energy resolution

➤ Spatial resolution

Fast scintillation

➤ Dead time

➤ Timing resolution



Scintillator	Decay time (ns)	Attenuation coefficient (cm <sup>-1</sup> )	Light output (photons/MeV)
NaI(Tl)	230	0.35	41000
BGO	300	0.95	7000
GSO	60	0.70	10000
BaF <sub>2</sub>	2	0.45	2000
LYSO, LSO	40	0.86	26000
LaBr <sub>3</sub>	20	0.47	60000

Fast scintillators with high light output

# Photo multiplier tubes (PMTs)

Most commonly used

1. Photocathode: converts visible light quants into free electrons
2. Electric field: accelerates electrons towards the dynode (an anode)
3. Dynode: electron impact causes secondary electron production (amplification)
4. Anode: collects the electrons -> electric signal

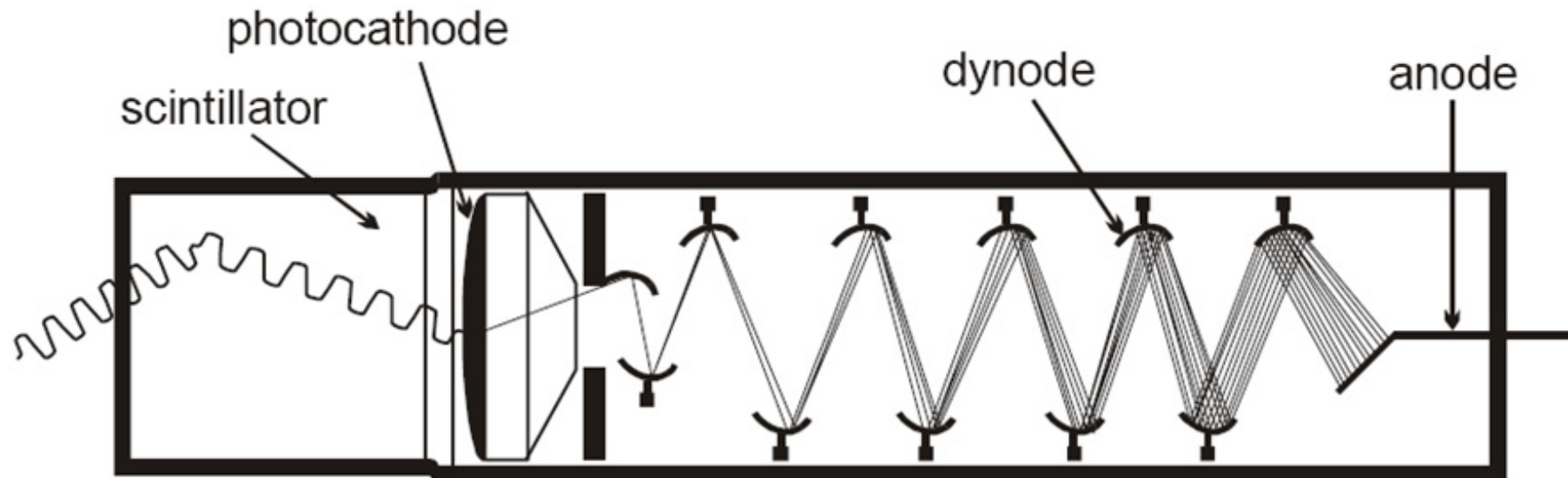


Image: <http://nsspi.tamu.edu/nsep/>

Electron acceleration and amplification



# Alternatives to PMTs

APD: Averslange photo detectors

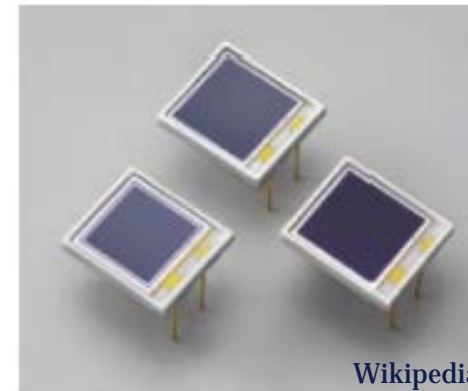
- Based on semiconductors
- + better spatial resolution
- low gain
- slow compared to PMTs

SiPM: Silicon Photomultiplier

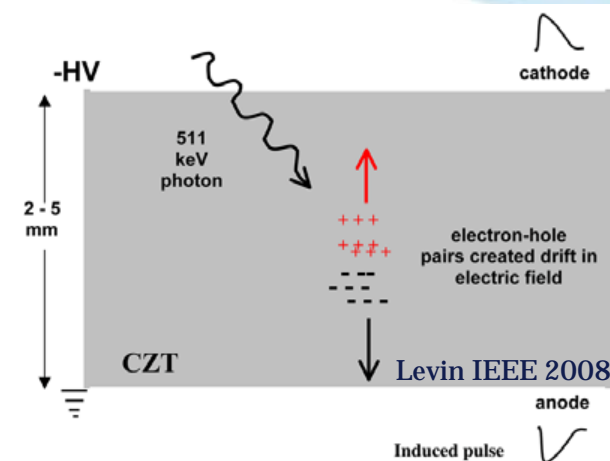
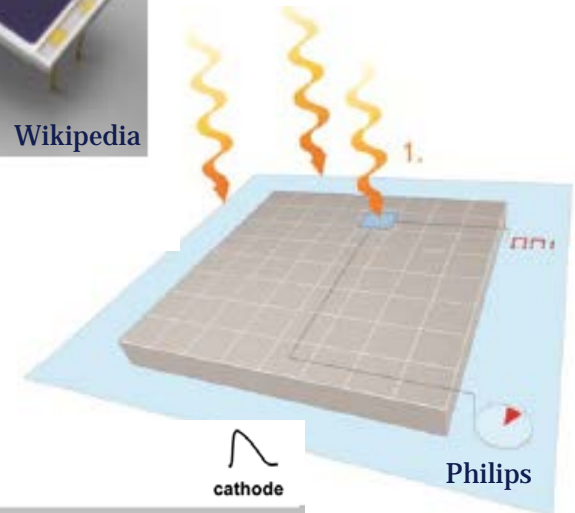
- Grid of APDs operated in “Geiger-mode”
- + analog or digital readout
- + fast

Direct semiconductor detectors

- + high spatial resolution
- low efficiency



APD



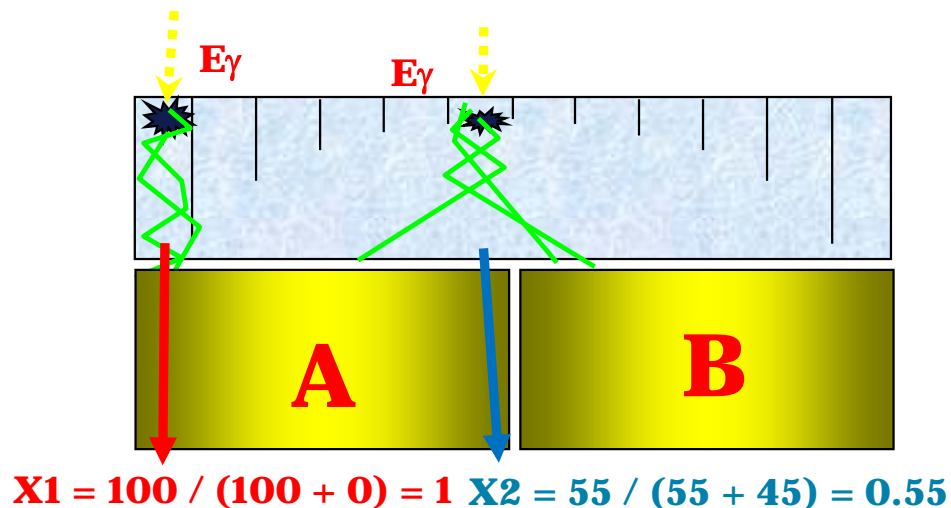
There are alternatives to PMTs based on semiconductors

# PET system design

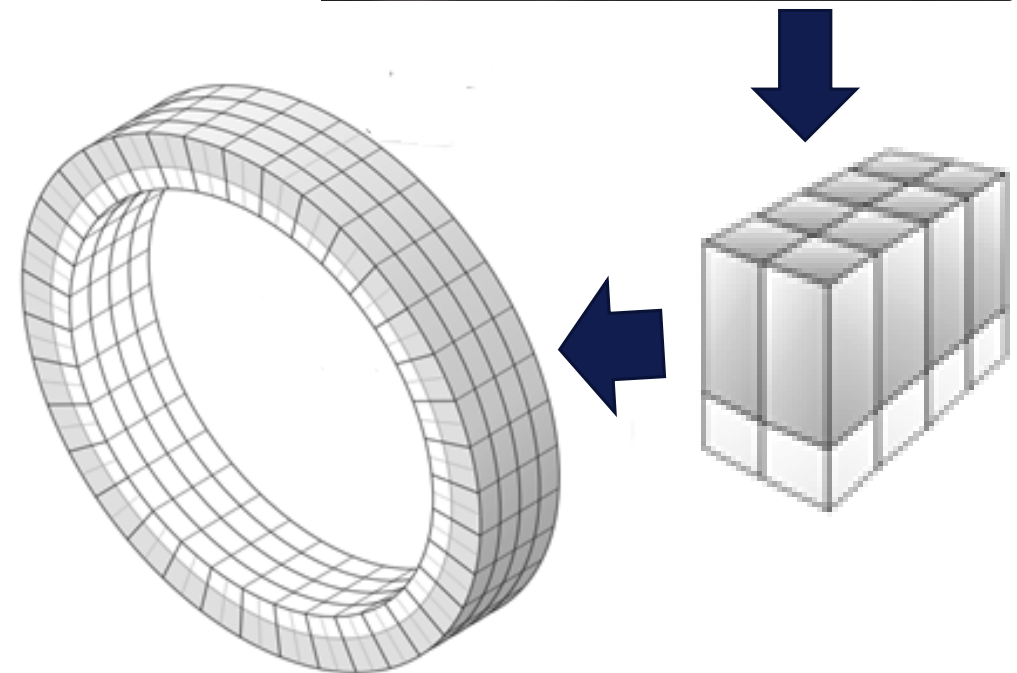
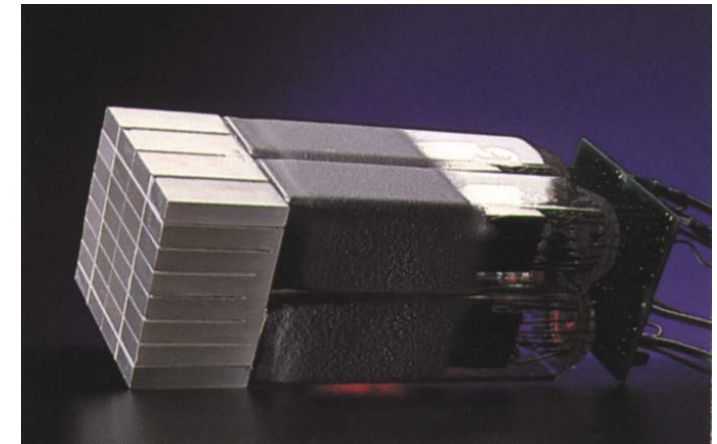
One scintillator crystal mounted on four PMT

➤ Detector block

Position of photon interaction – Anger logic



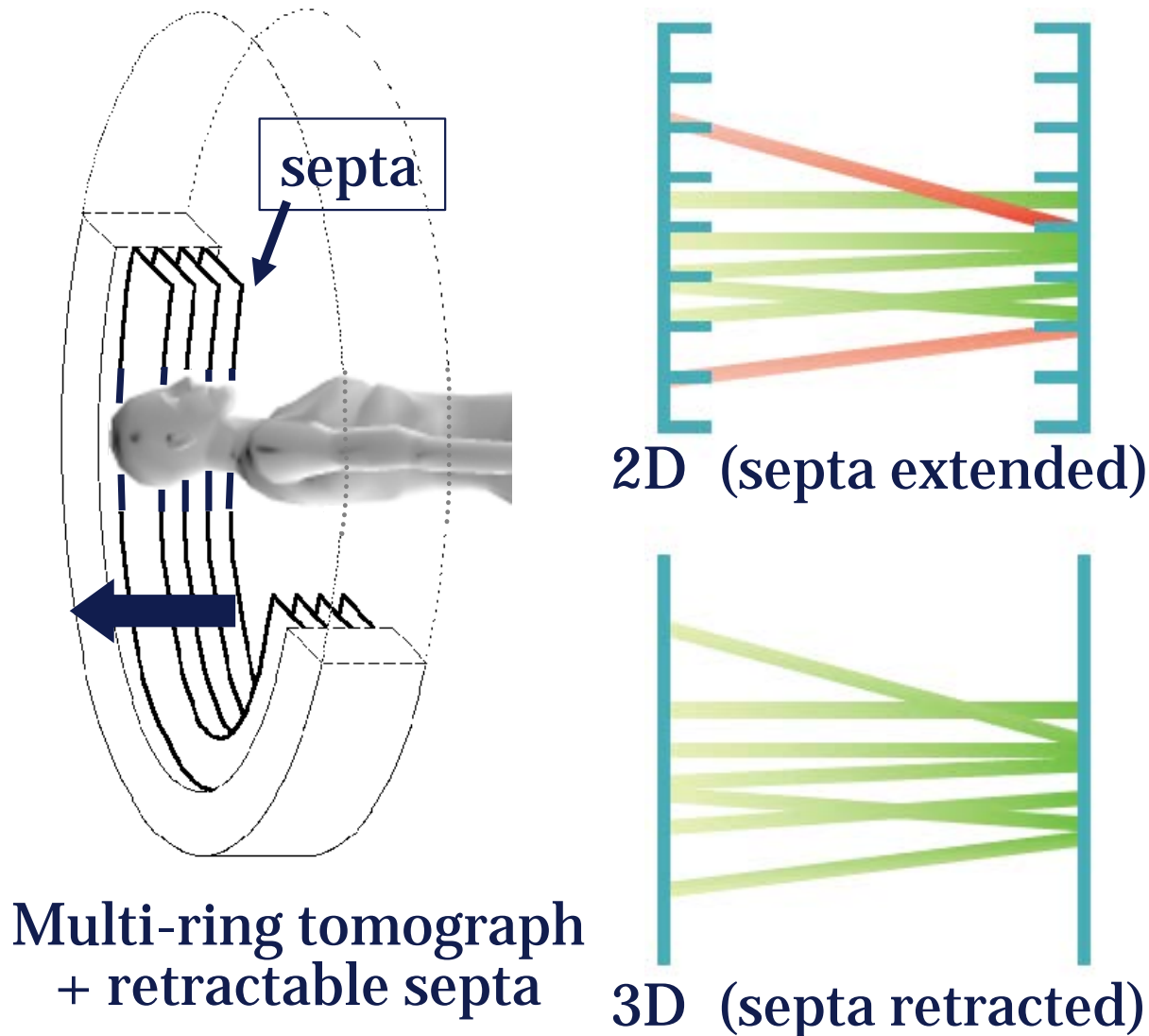
Courtesy: Mauritio Conty



All clinical PET/CT today are whole-body ring systems

# 2D- vs 3D PET

Courtesy T.Beyer (Vienna)



- increased sensitivity
- increased background
- increased deadtime
- out-of-field activity
- 3D reconstruction
- non-uniform response
- BGO works for brain
- LSO/GSO for whole-body

State-of-the-art PET: 3D (no septa) for increased sensitivity

# Attenuation correction (AC)

Attenuation correction is essential for quantitative PET data



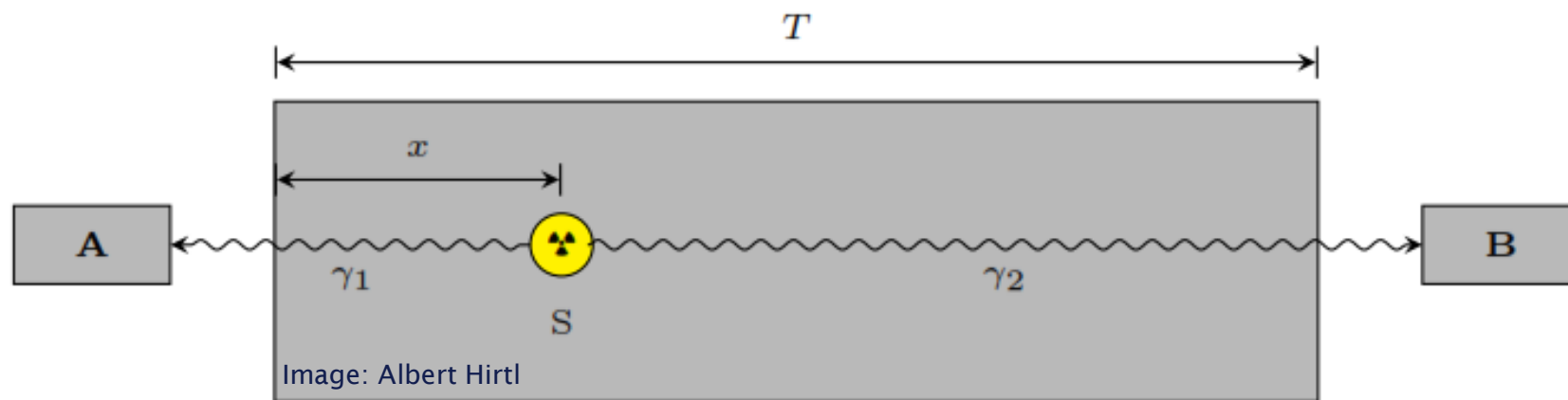
Non-attenuation corrected



Attenuation corrected

# Attenuation correction (AC)

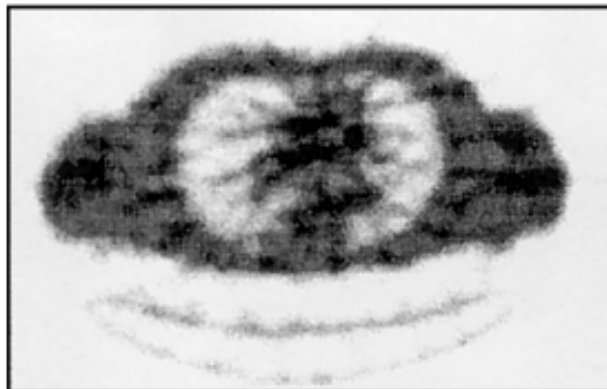
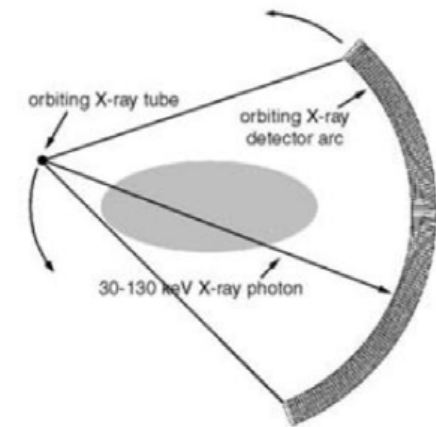
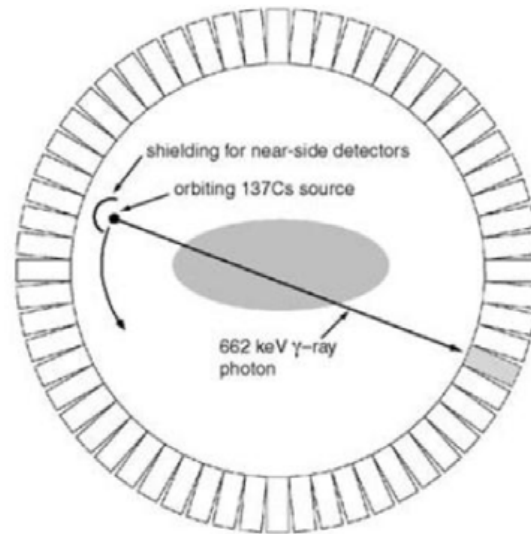
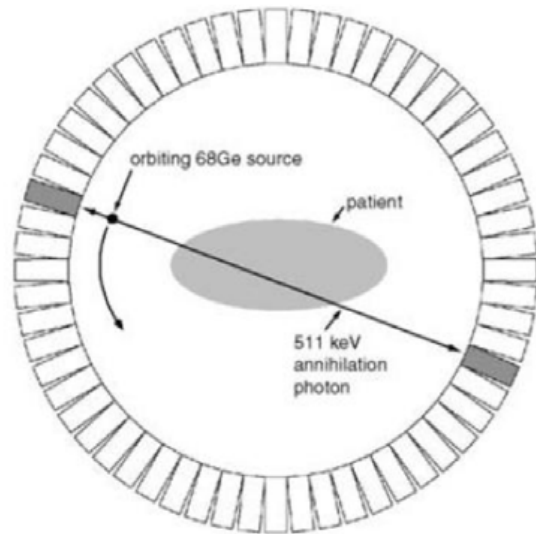
Both annihilation photons need to be detected for a valid event



$$P_{detect} = P_{detect\gamma_1} \cdot P_{detect\gamma_2} = e^{-\mu x} \times e^{-\mu(T-x)} = e^{-\mu T}$$

Probability dependent on total attenuation through the object

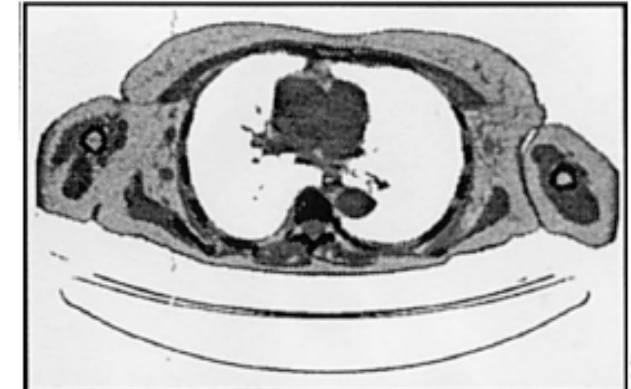
# Attenuation correction



(a)  $^{68}\text{Ge}/^{68}\text{Ga}$  positron source



(b)  $^{137}\text{Cs}$  gamma-ray source



(c) 120 kVp x-ray source

AC is done using a transmission scan

# Type of events in a PET system

## True coincidences are usable

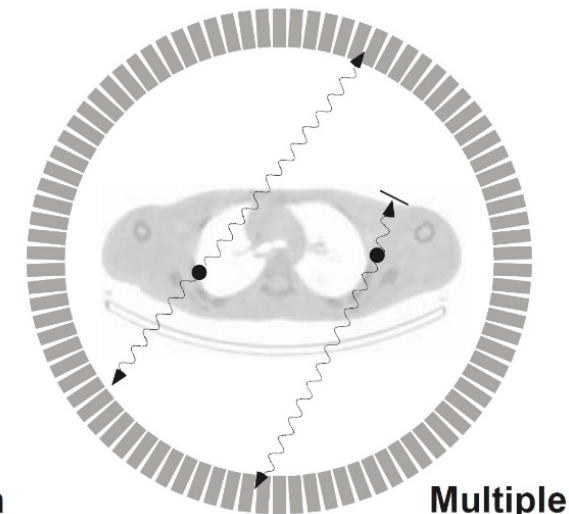
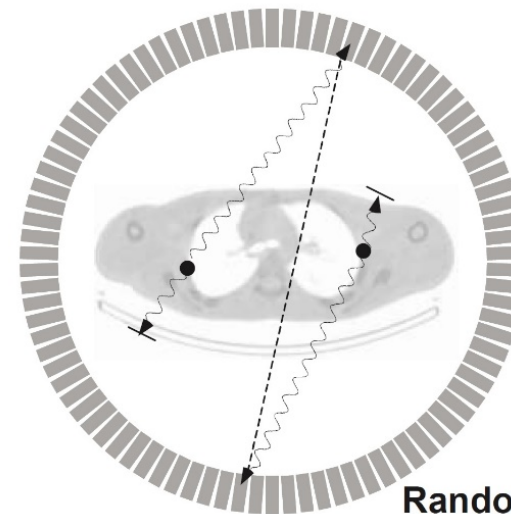
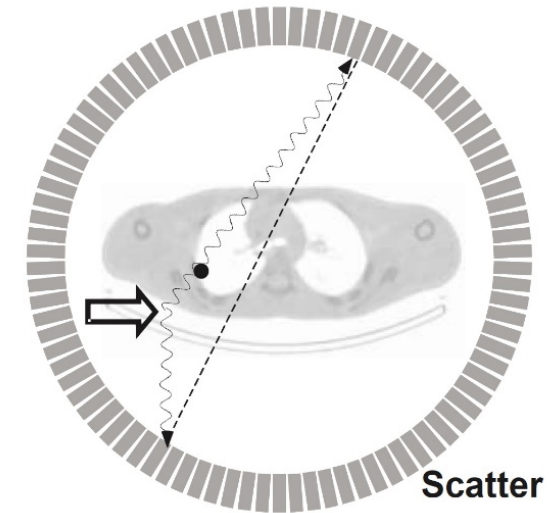
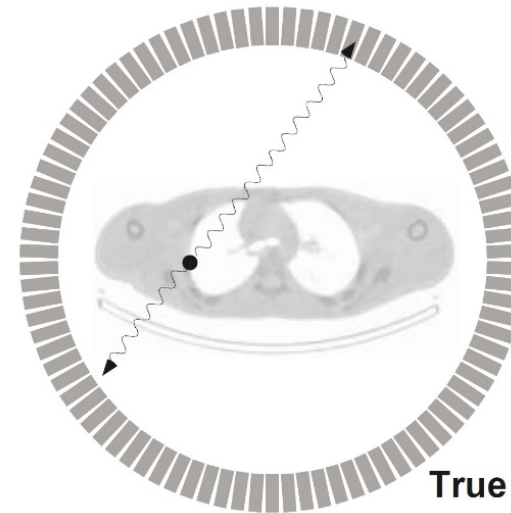
- Time window  $\sim 4\text{ns}$
- Energy window  $\sim 450\text{keV}-630\text{keV}$

## Scatter

- minimized by energy window
- Correction by simulation

## Random

- Minimized by timing window
- Correction by estimation from delayed timing window



Not every count is a usable count

# Limiting Factors

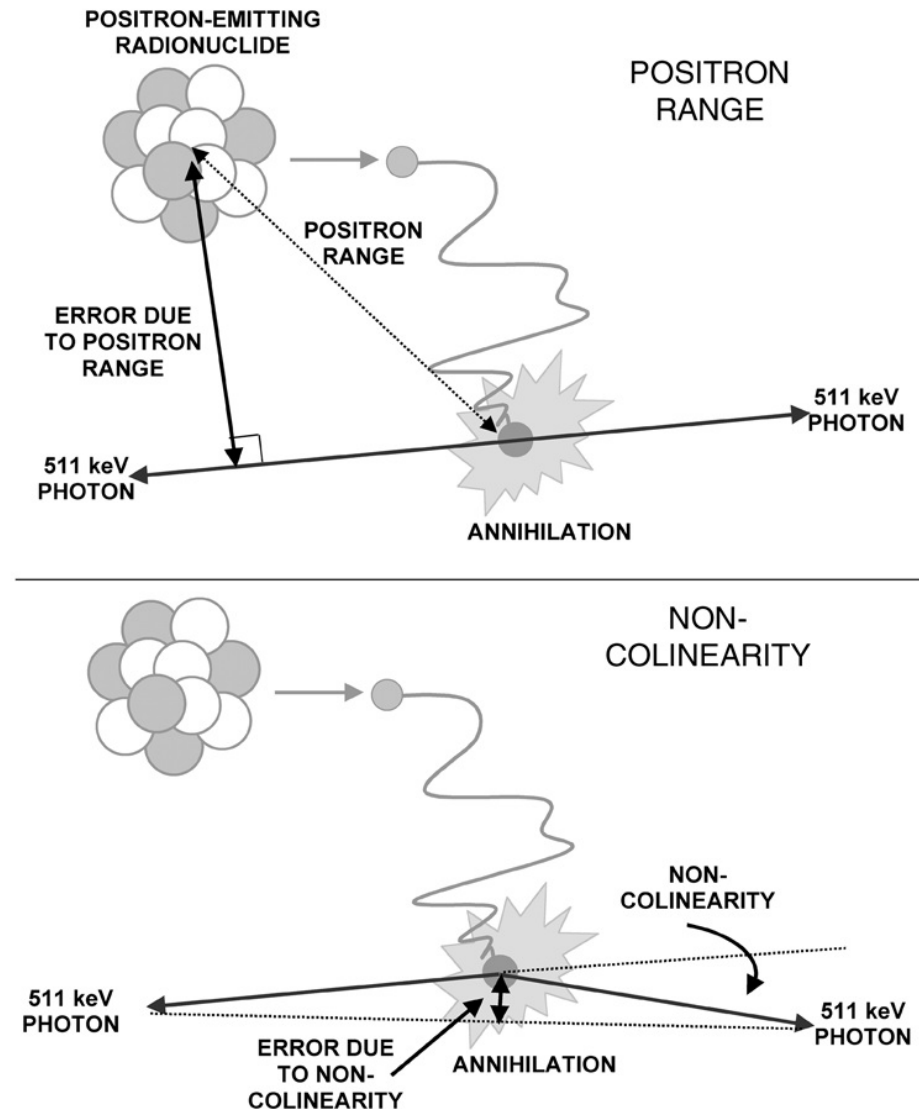
## Positron Range:

Depending on  $E_{\text{kin}}$  of positron

Nuclide	Mean range
18-F	0.6 mm
68-Ga	2.9 mm
11-C	1.1 mm

## Non collinearity:

- Residual momentum of positron causes deviation from  $180^\circ$ -preservation of momentum
- Nearly Gaussian (FWHM $\sim 0.5^\circ$ )
- Depending on ring diameter



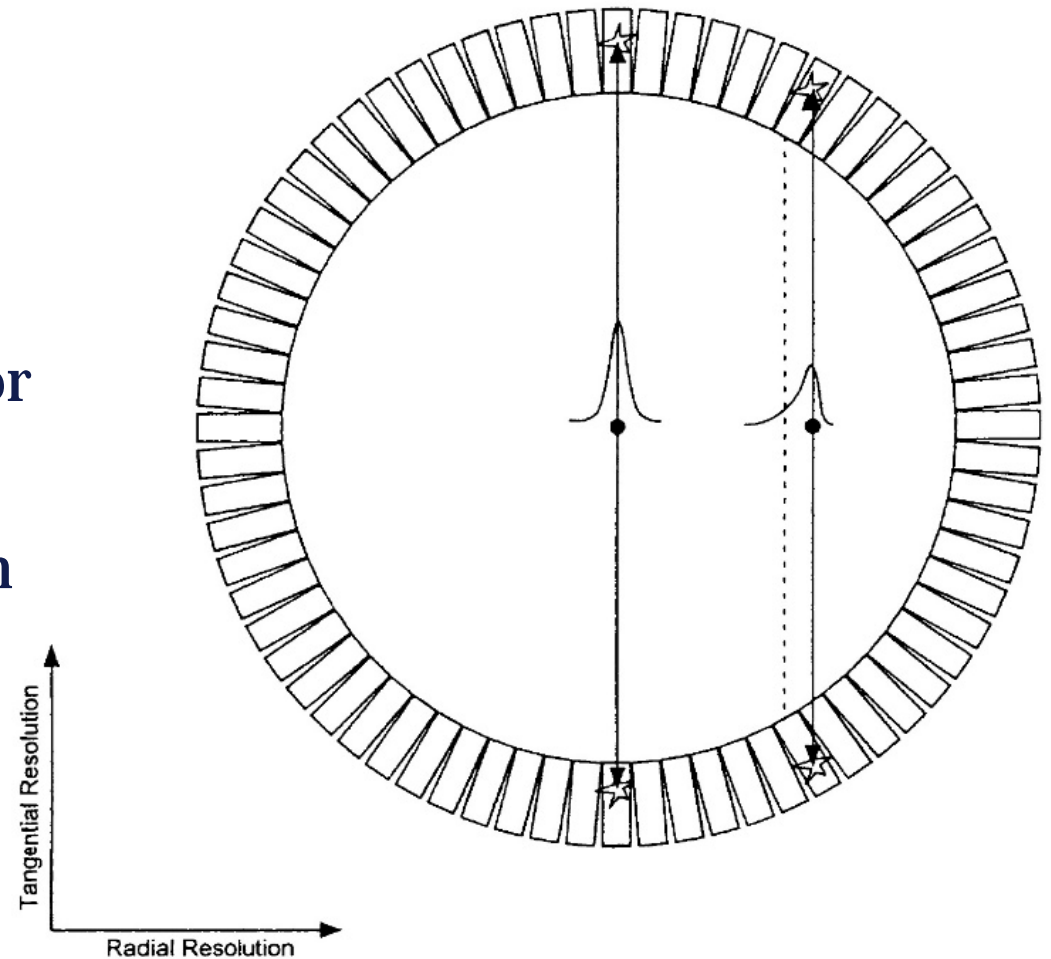
Positron emission  $\neq$  positron annihilation



# Limiting factors

## Detector parallax:

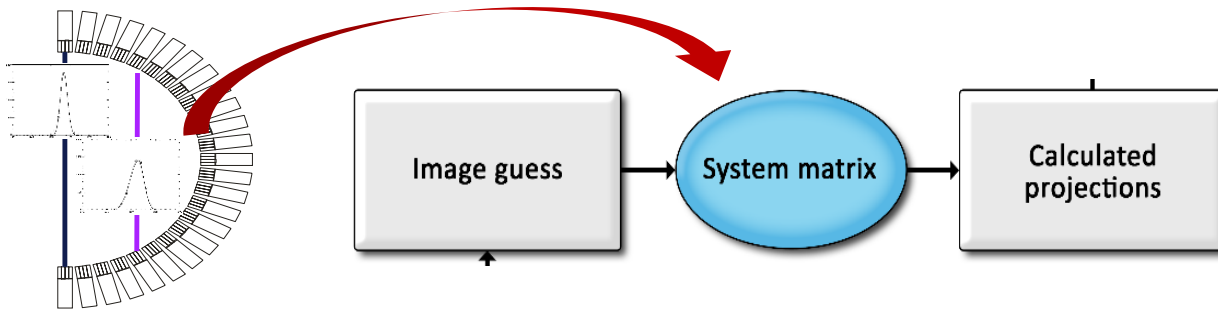
- Detectors shifted in angle
- Photon passing first scintillator -> wrong LOR
- asymmetric response function



Resolution depends on system design and geometry

# Point spread function (PSF)

## Incorporation of the PSF into system matrix

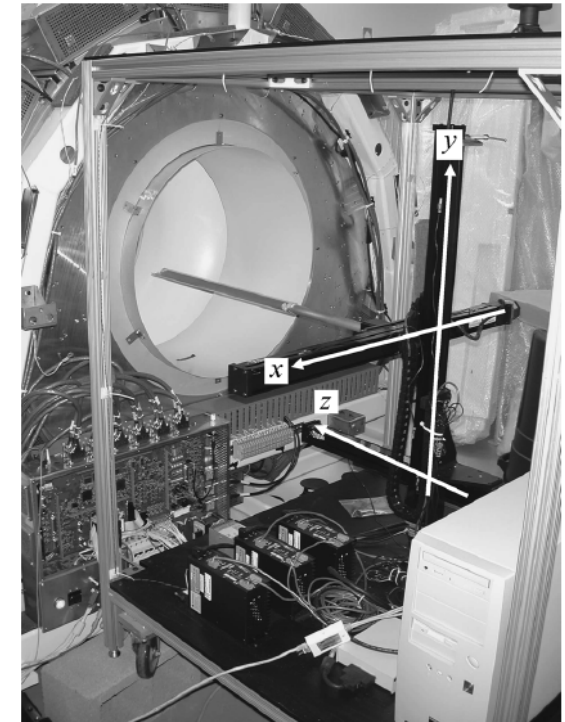


PSF: measured, MC simulations, modelled

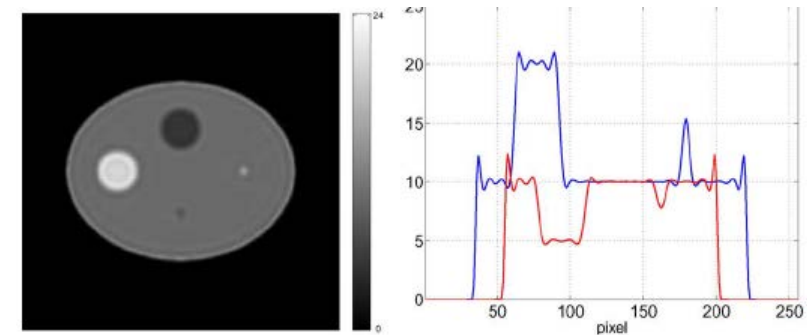
➤ accounting for varying spatial resolution

E.g. Siemens TrueX Algorithm (now “HD PET”)

- + better resolution -> detectability of small volumes
- Gibbs artifacts at sharp edges



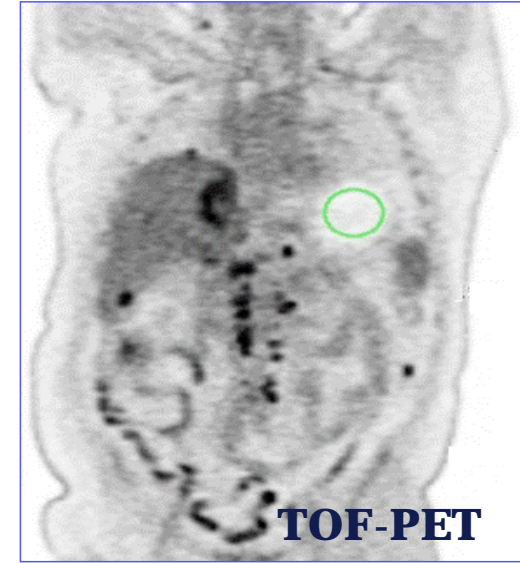
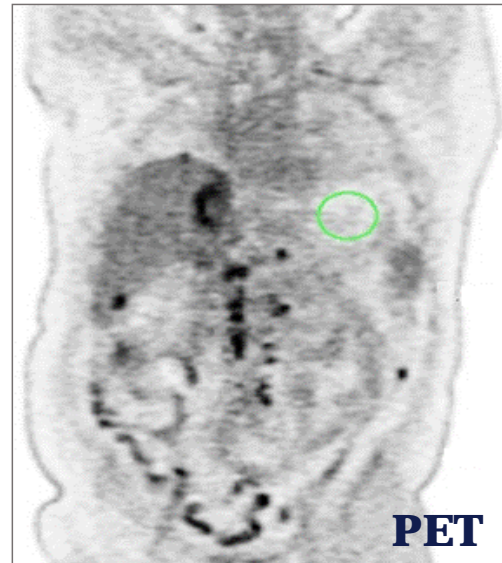
Panin et al. IEEE 2006



Tong et al. IEEE 2011

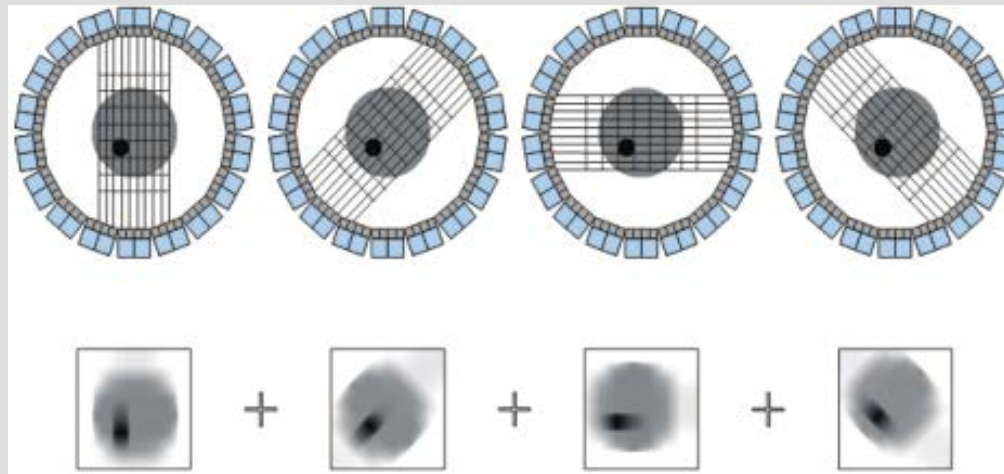
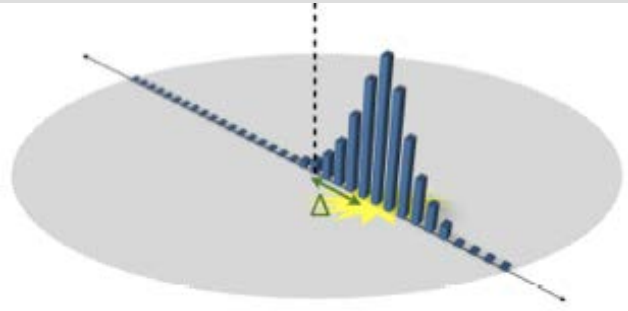
# Time-of-flight

$$SNR_{TOF} \cong \sqrt{\frac{D}{\Delta x}} \cdot SNR_{conv}$$



BMI  
30

## Time-of-flight PET

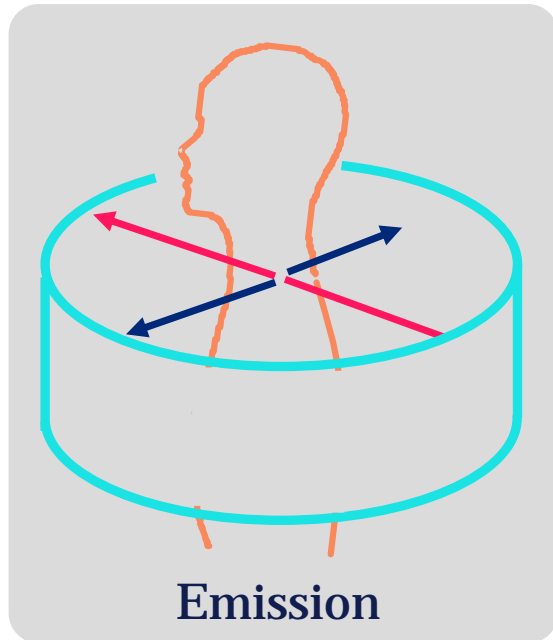


TOF-PET improves SNR (not spatial resolution)

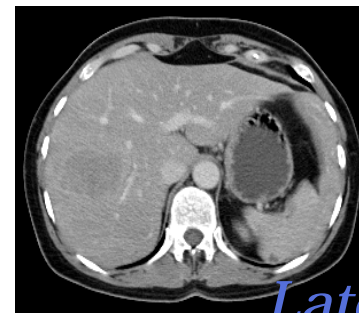
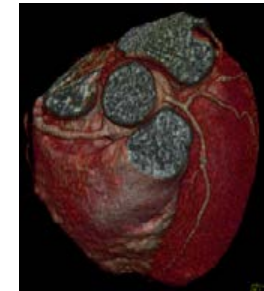
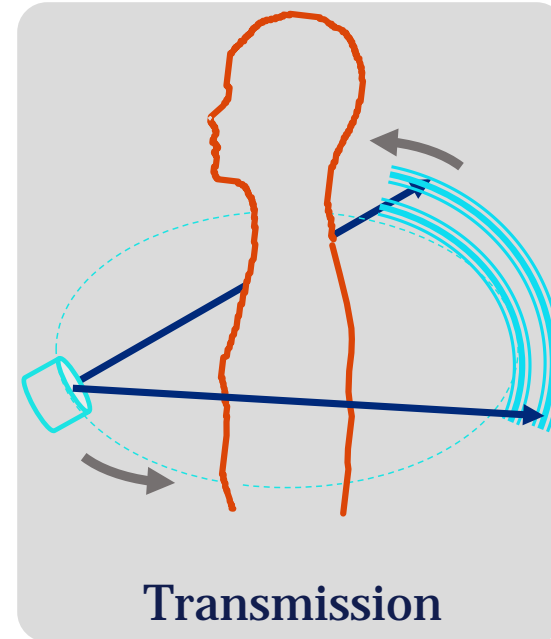
# Why PET/CT?

Courtesy T.Beyer (Vienna)

## Positron Emission Tomography



## Computed Tomography



*Functional anatomy*  
*Changes in metabolism*  
*High functional resolution*  
*Early detection is possible*

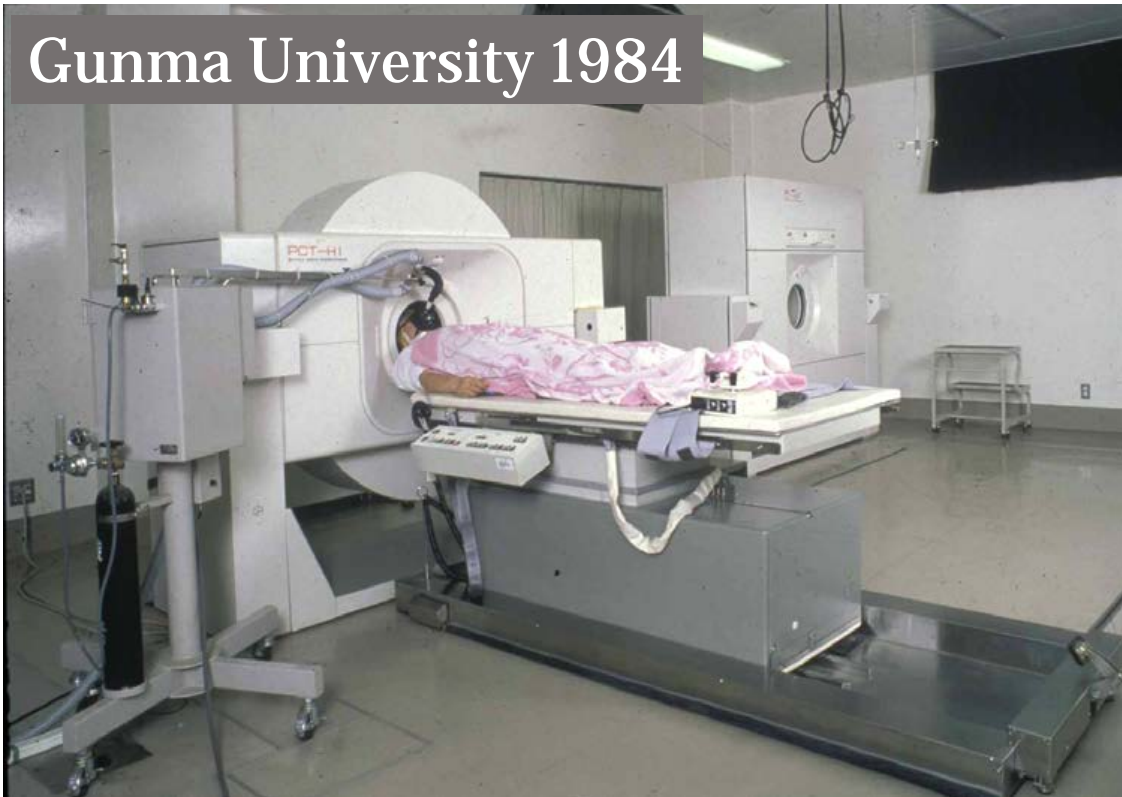
*Spatial anatomy*  
*Changes in anatomy*  
*High spatial resolution*  
*Late(r) anatomical changes*

**PET/CT is *function plus anatomy***

# Early PET/CT development

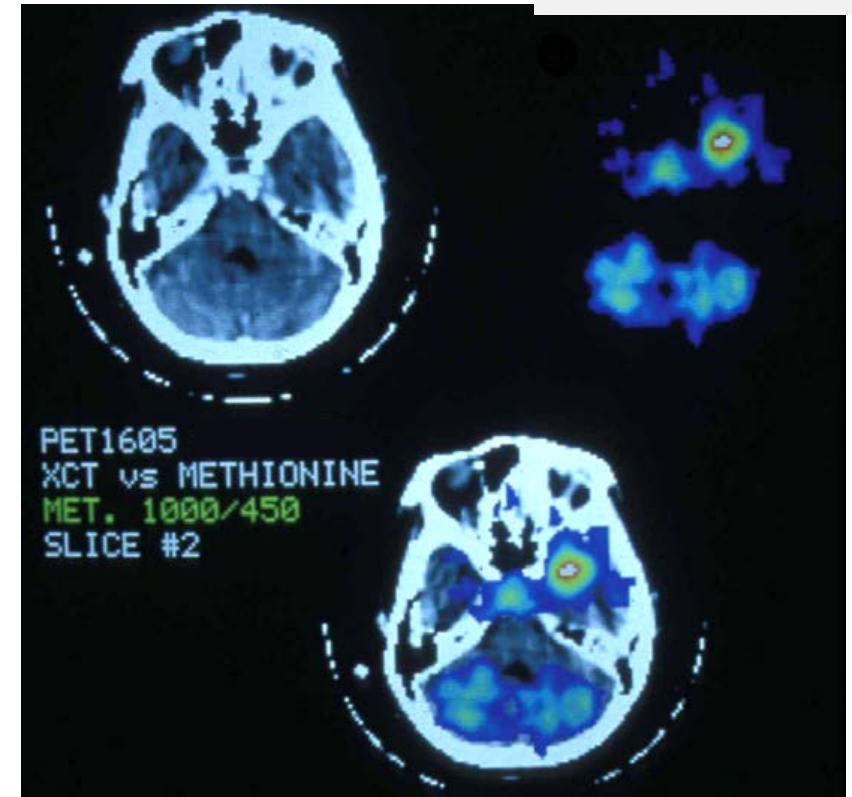
Courtesy T.Beyer (Vienna)

Gunma University 1984



A combined CT and PET system developed by Prof. Teruo Negai (Dept of Radiology, Gunma University, Japan) in 1984.

The device incorporated CT and PET scanners from Hitachi Inc and the patient bed moved on floor-mounted rails between the PET and CT.



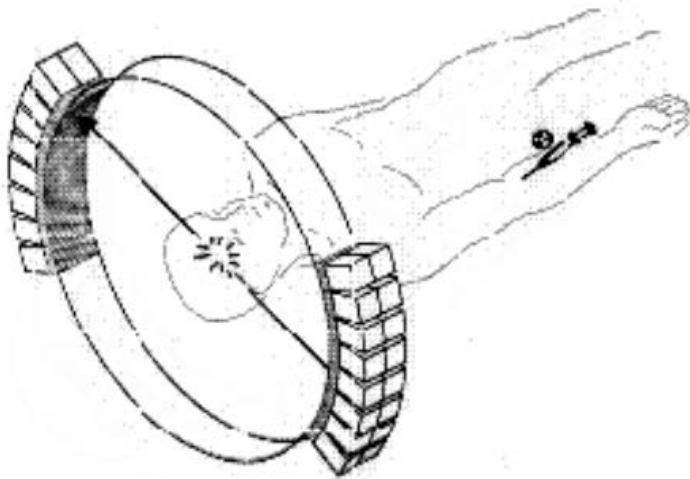
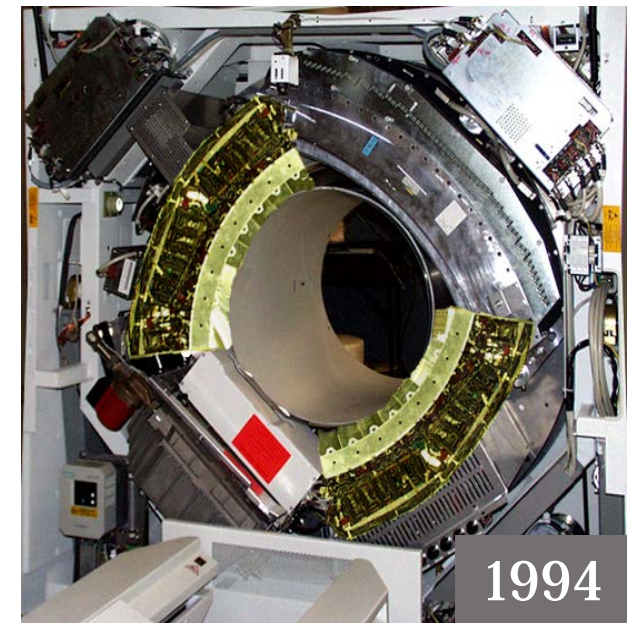
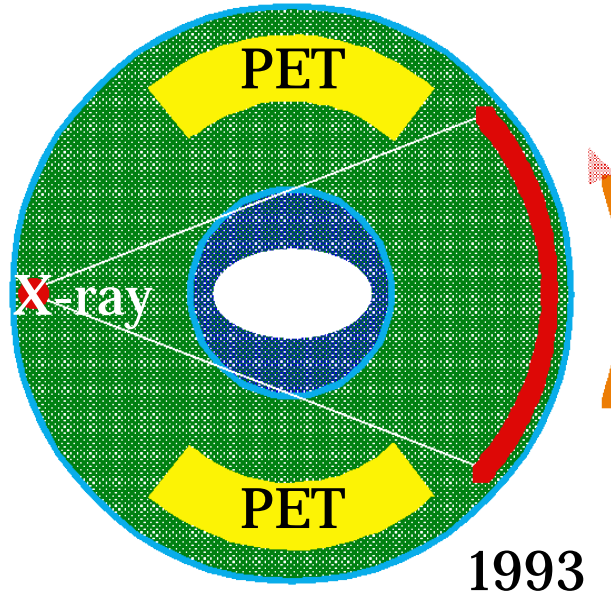
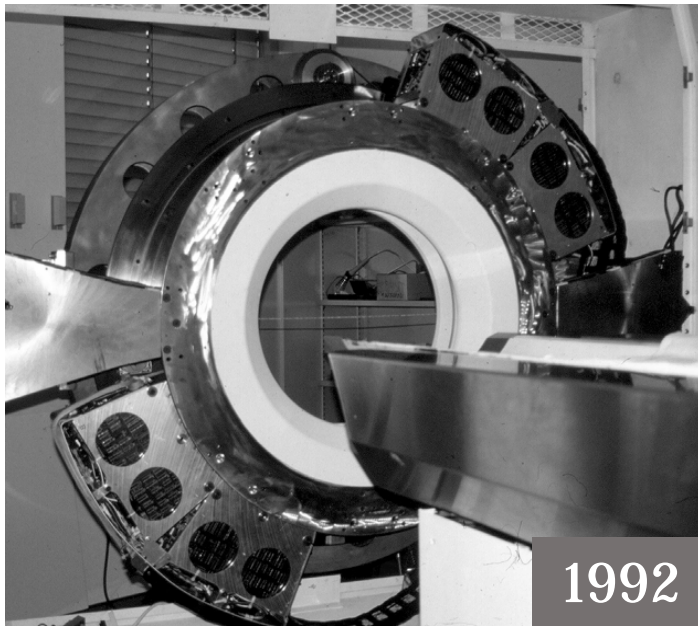
Fusion images of a patient with a brain tumor.

$^{11}\text{C}$ -methionine PET and CT acquired in the same examination.

Courtesy Prof. Y Sasaki

# Prototyping PET/CT

Courtesy T.Beyer (Vienna)



A rotating PET scanner using BGO detectors,  
Townsend DW et al, JNM 30, 1993

## The evolution of a PET/CT concept:1992-4

- Routine oncology imaging (whole-body)
- Complementary PET/CT
- Accurate, fast CT-based quantitation

# The SMART PET/CT

Courtesy T.Beyer (Vienna)



SMART

→ Somatom CT

→ Advanced Rotating Tomograph (PET)

← 110 cm →

← 60 cm →

168 cm



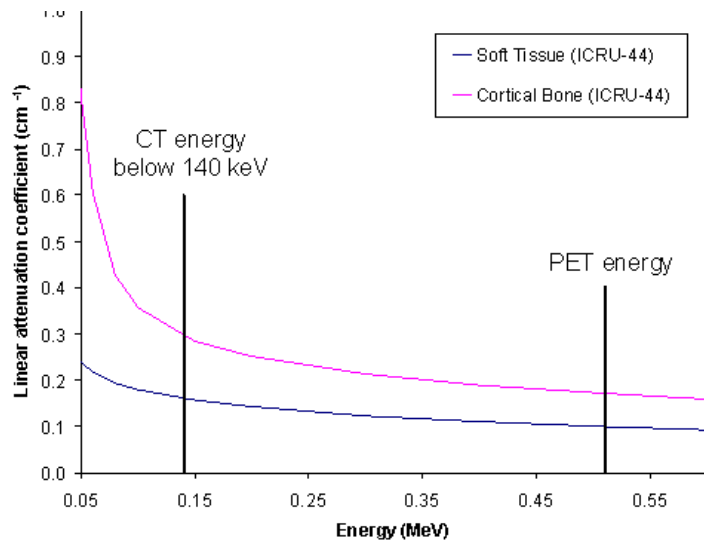
Patient handling system

CT

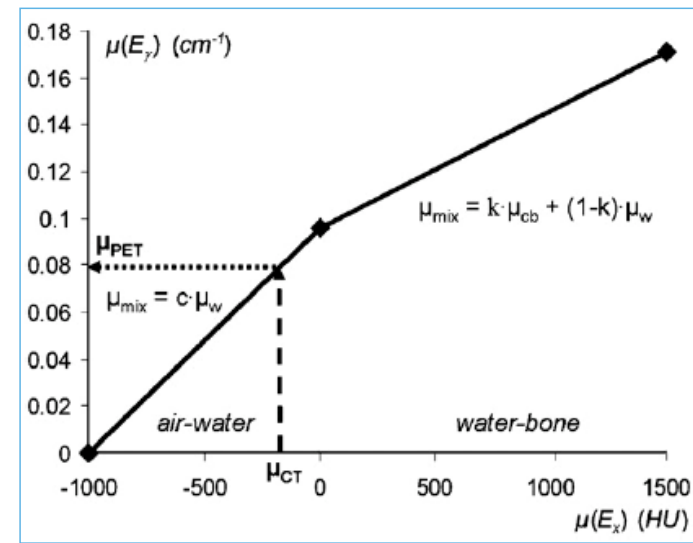
PET

# CT based AC

Courtesy T.Beyer (Vienna)

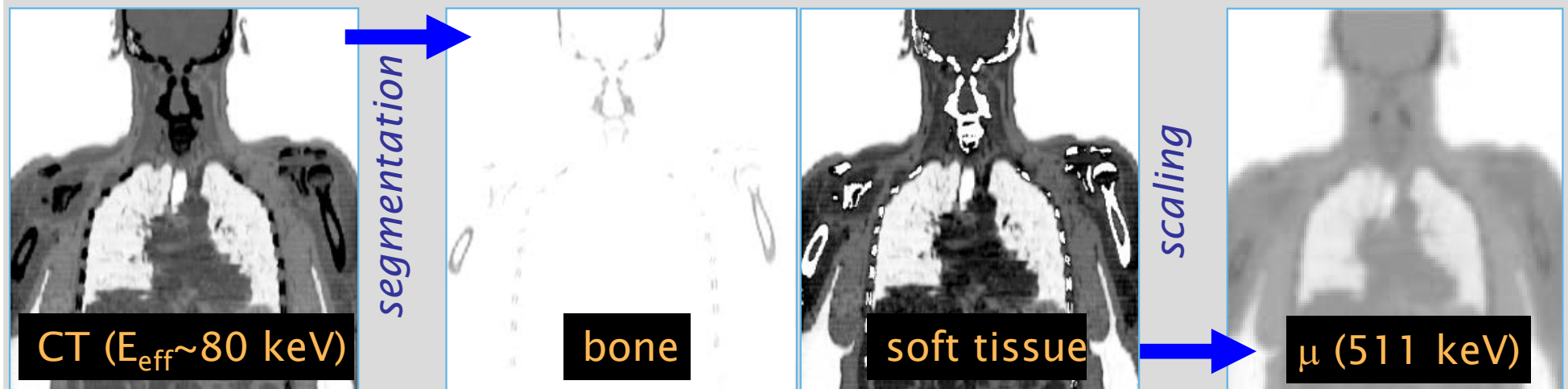


Kinahan P et al, Sem Nuc Med XXXIII, 2003



Townsend DW, PMB 53: R1-39, 2007

## bi-linear segmentation-scaling approach to CT-AC





# Early PET/CT concepts

Courtesy T.Beyer (Vienna)

1998-2000

300 oncology patients

~50% with CT

contrast

Torso exam in 60 min

CT: 80 cm = 4 min,

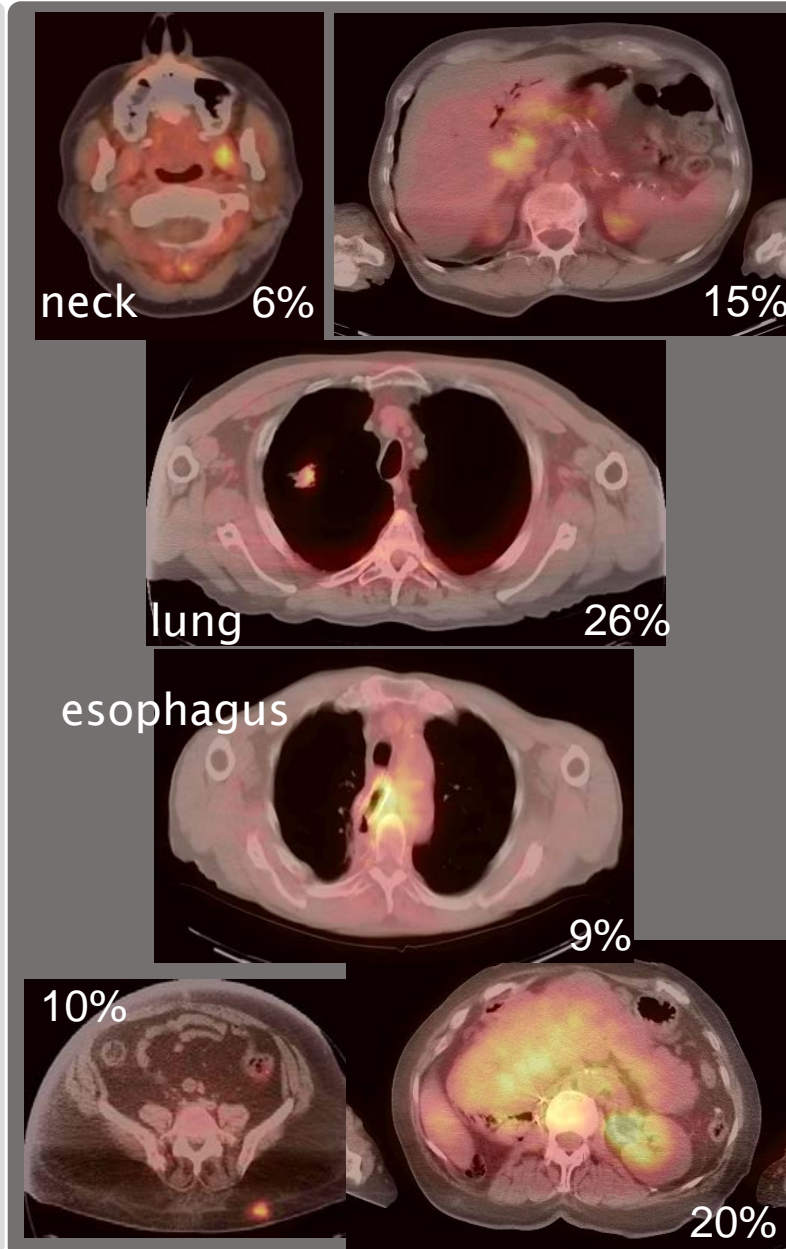
PET: 7 beds = 50 min

BGO: 7x7x20 mm<sup>3</sup>

1-slice CT, 15 kW

Power of fused images

CT-based artifacts



# PET/CT systems

Courtesy T.Beyer (Vienna)

## Discovery VCT



CT: 16-128 slices

70 cm patient port

250 kg table weight limit

170 cm co-scan range

24 rings of LYSO(Ce)

4.2 x 6.3 x 25 mm<sup>3</sup>

Time-of-flight

15.1 cm axial FOV

70 cm transaxial FOV

PET resolution model

## Ingenuity TF



CT: 16-128 slices

70 cm (85 cm) patient port

215 kg table weight limit

190 cm co-scan range

44 rings of LYSO(Ce)

4.0 x 4.0 x 22 mm<sup>3</sup>

Time-of-flight

18 cm axial coverage

67 cm transaxial FOV

PET resolution model

## AnyScan



16-slice CT

70 cm diameter patient port

250 kg table weight limit

360 cm co-scan range

24 rings of LYSO(Ce)

3.9 x 3.9 x 20 mm<sup>3</sup>

23 cm axial coverage

55 cm transaxial FOV

## Biograph mCT



CT: 20-128

78 cm patient port

250 kg table weight limit

170 cm co-scan range

52 rings of LSO (Ce) crystals

4.0 x 4.0 x 20 mm<sup>3</sup>

Time-of-flight

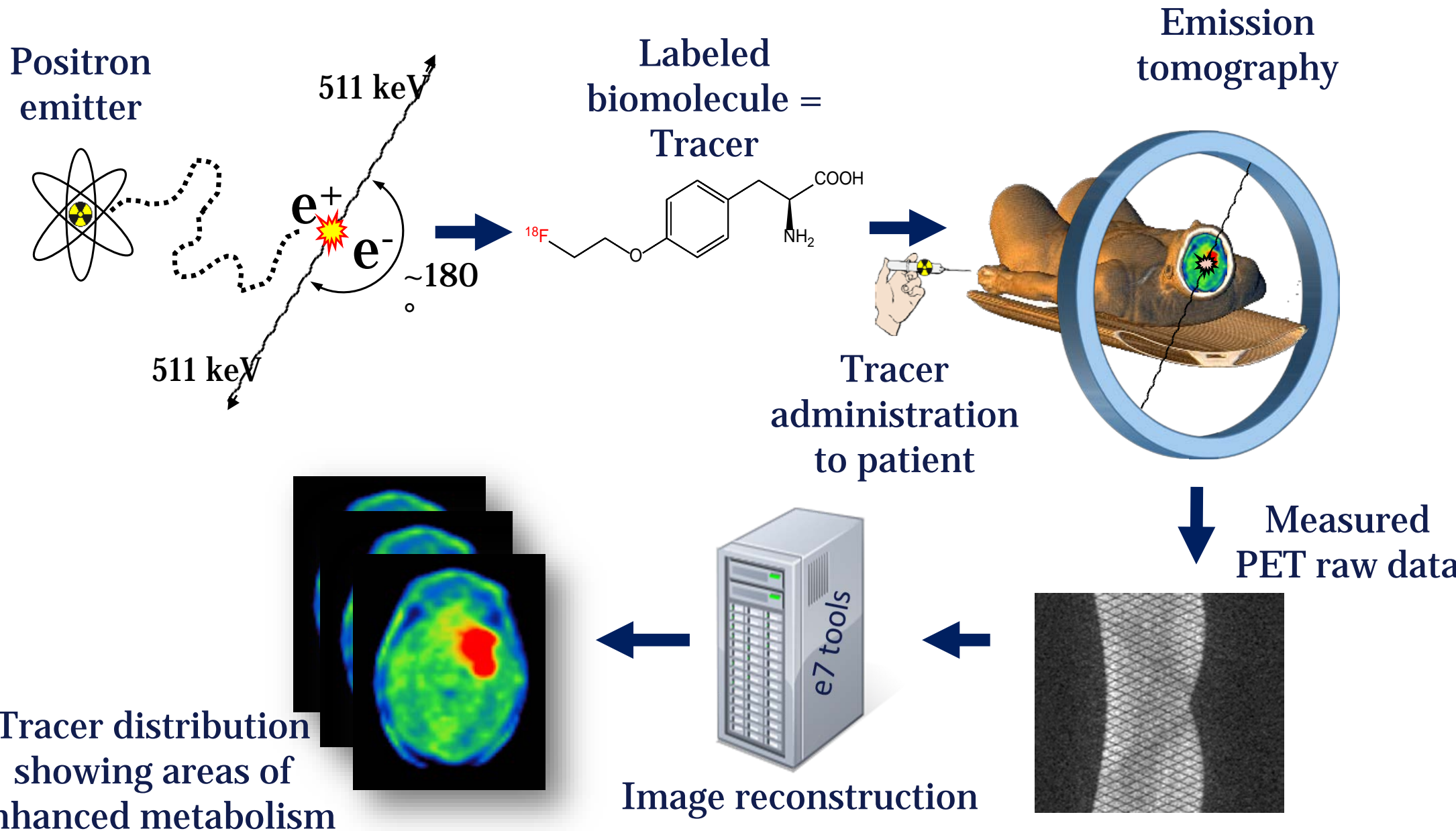
21.6 cm axial coverage

70 cm transaxial FOV

PET resolution model

**High-end PET combined with high-end, multi-slice CT**

# Summary





[ivo.rausch@meduniwien.ac.at](mailto:ivo.rausch@meduniwien.ac.at)