

MUON (G-2) AND MEASUREMENT OF HADRONIC CROSS-SECTIONS AT CMD-3

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on behalf of CMD-3 collaboration

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*International Conference on Precision Physics of Simple Atomic
Systems - PSAS'2018, May 14-18, 2018*

Outline

- History and status of muon $g-2$
- Hadronic contribution and $R(s)$
- VEPP-2000 collider and CMD-3 detector
- Recent results

Muon g-2

- Anomalous magnetic moment: $a_\mu = \frac{g_\mu - 2}{2}$
- In the first order $a = 0$, non-zero value comes from higher order corrections
- a_e is measured to 0.24 ppb (*D. Hanneke et al., PRL 100 (2008) 120801*)

$$a_e = (115\,965\,218\,073 \pm 28) \times 10^{-14} \text{ (0.24 ppb)}$$

- But a_μ is much more sensitive to heavy fields

$$\Delta a_\mu / \Delta a_e \sim (m_\mu / m_e)^2 \approx 43000$$

- a_μ is measured to 0.54 ppm \rightarrow about 20 times more sensitive to BSM physics

a_e provides α , a_μ provides SM test

Muon g-2 in Standard Model

- **QED**: up to 5 loops (12672 diagrams!). **0.29 ppb**

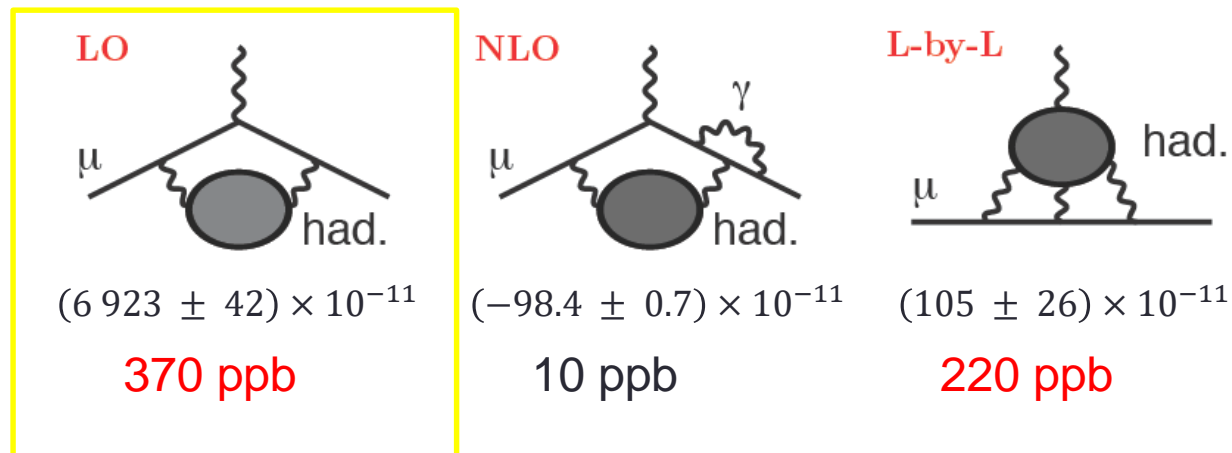
$$a_{\mu}^{QED} = 116\,584\,718.859 (.026)(.009)(.017)(.006) [.034] \times 10^{-11},$$

- **EW**: 2 loops, now Higgs mass is known. **9 ppb**

$$a_{\mu}(\text{EW}) = (153.6 \pm 1.0) \times 10^{-11}$$

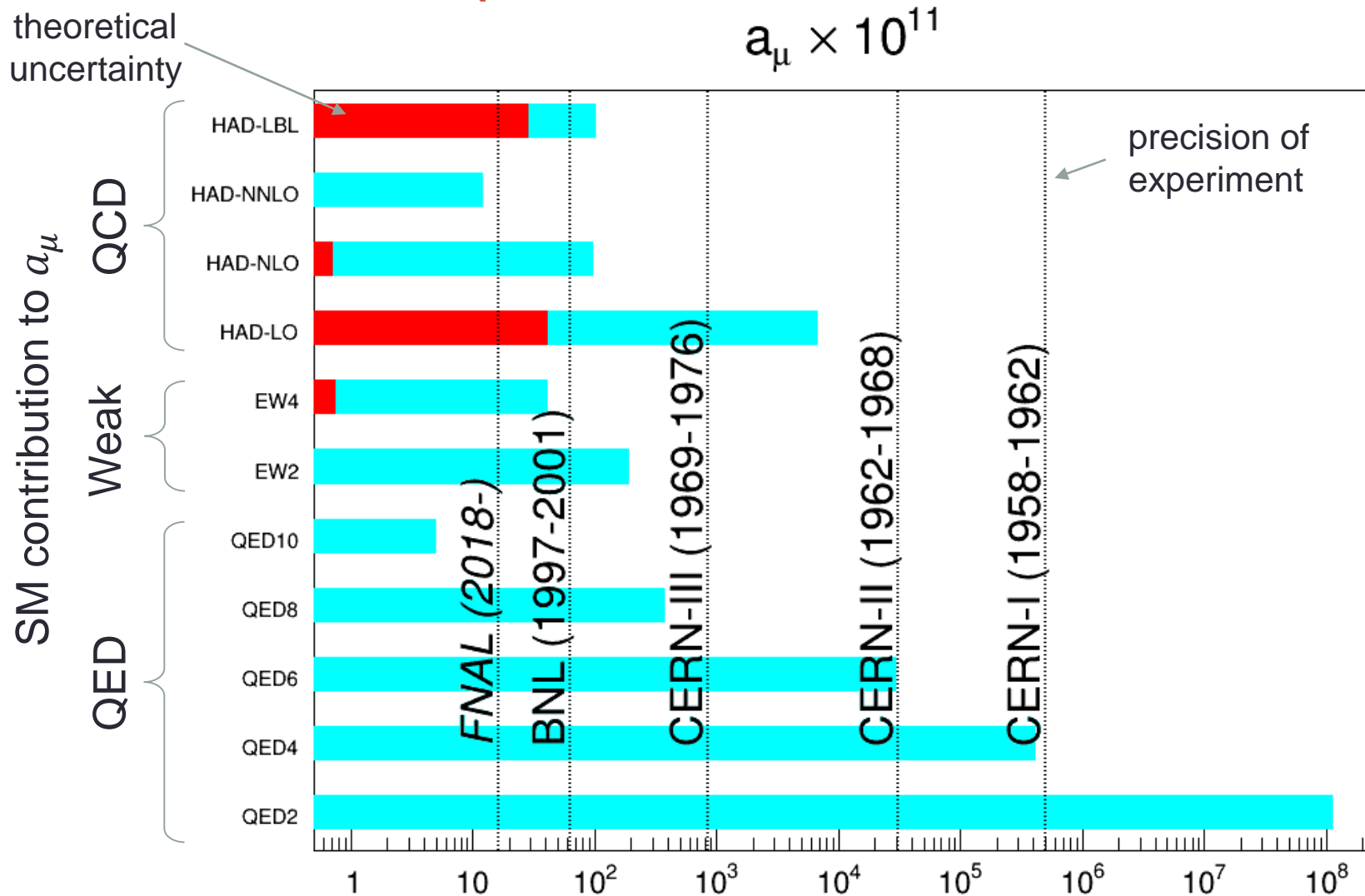
- **Hadronic**

$$a_{\mu}^{\text{had}} = a_{\mu}^{\text{had,VP LO}} + a_{\mu}^{\text{had,VP NLO}} + a_{\mu}^{\text{had,Light-by-Light}}$$



New experiment at FNAL: 140 ppb

History of a_μ measurements



Muon (g-2) today: experiment vs theory

$$a_{\mu}(exp) = 1\,165\,920\,89(63) \times 10^{-11} \\ (0.54 \text{ ppm})$$

$$a_{\mu}(th) = 1\,165\,918\,21(36) \times 10^{-11} \\ \text{KNT18} \quad (0.31 \text{ ppm})$$

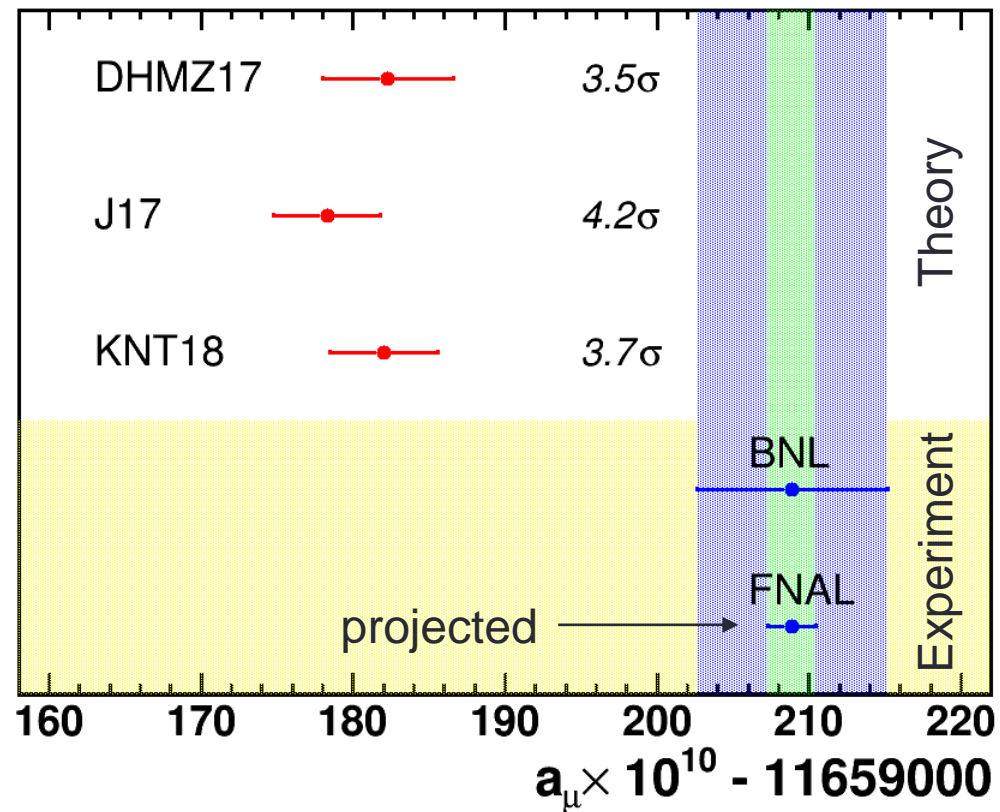
$$\Delta a_{\mu}(exp - th) = (268 \pm 73) \times 10^{-11}$$

Fermilab projections (conservative):

$$a_{\mu}(exp) \rightarrow \text{to } 0.14 \text{ ppm}$$

$$a_{\mu}(th) \rightarrow \text{to } 0.30 \text{ ppm}$$

$$\Delta a_{\mu}(exp - th) \rightarrow \text{to } \pm 40 \times 10^{-11}$$



New measurement at FNAL

A new experiment to measure muon ($g-2$) has started data taking in 2018 at Fermilab.

The experiment layout follows CERN-III and BNL design:

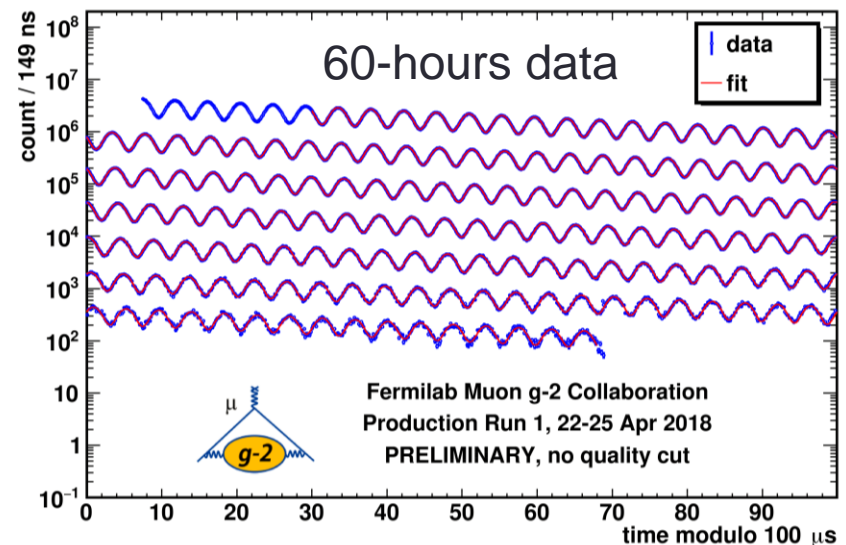
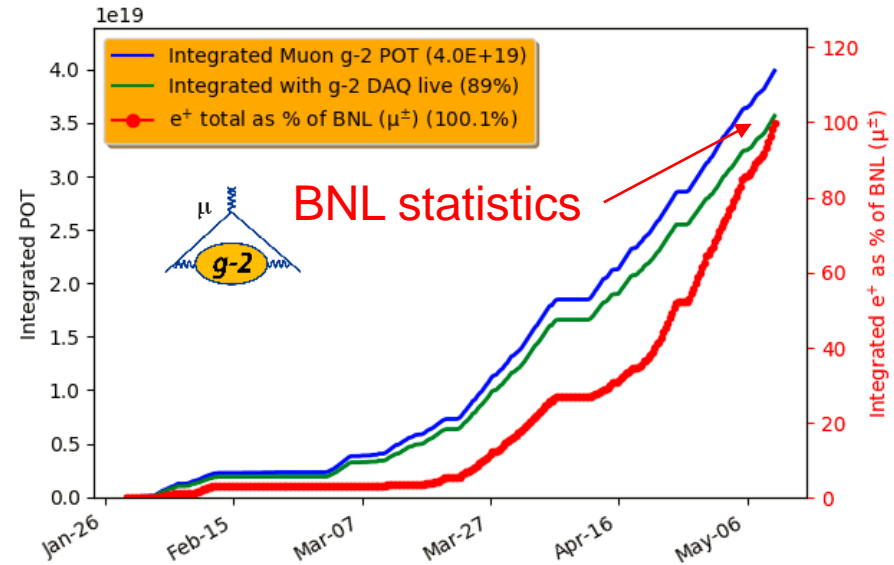
- Storage ring of 7 m radius with ultra uniform magnetic field and quadrupole focusing electric field
- Muons with “magic” momentum of 3.09 GeV/c

but with numerous improvements.

The experiment aims for **140 ppb** precision (x4 over BNL)

- x20 in statistics
- x2.8 in systematics

BNL level statistics has already been collected!



J-PARC $g-2$ experiment (E34)

3 GeV proton beam
(1MW, double pulses, 25Hz)

Production target

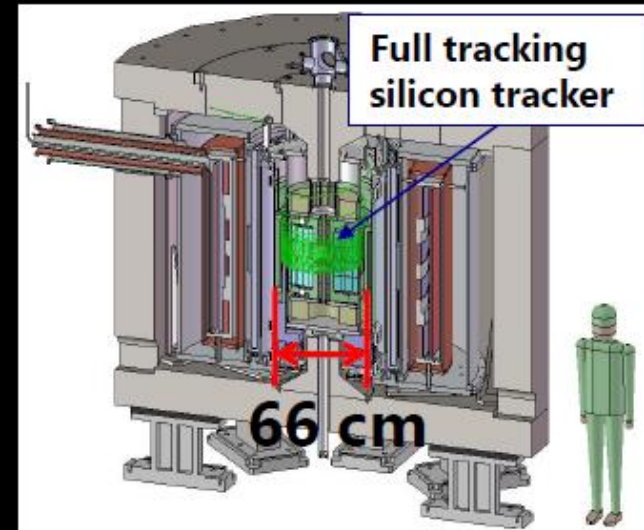
Surface muon beam (4 MeV)
 $\epsilon \sim 1000 \pi \text{ mm} \cdot \text{mrad}$

Muonium production target
(300 K \sim 25 meV)

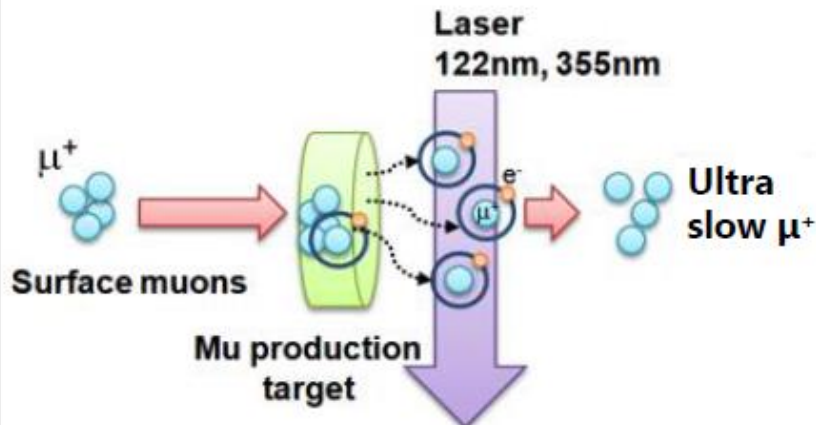
Ultra slow μ^+ production by Resonant Laser Ionization of Muonium ($\sim 10^6 \mu^+/\text{s}$)

Re-acceleration LINAC
($\sim 200 \text{ MeV}$)

$\epsilon \sim 1 \pi \text{ mm} \cdot \text{mrad} !$



Compact storage magnet
(3T, $\sim 1 \text{ ppm}$ local)



Target precision

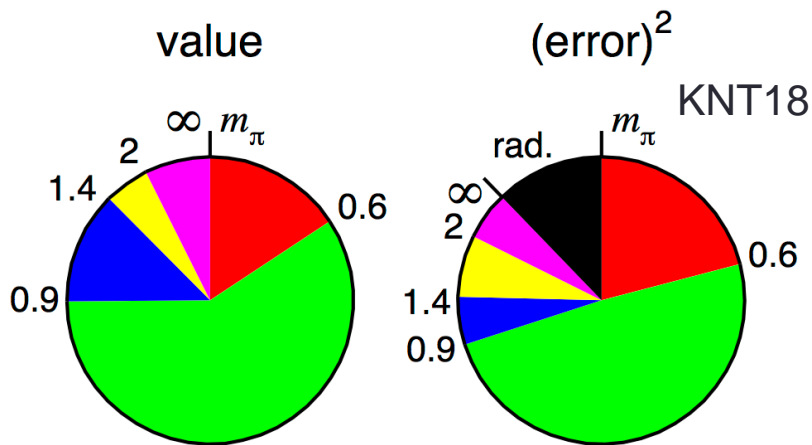
$$\Delta(g-2) = 0.1 \text{ ppm}$$

$$\Delta EDM = 10^{-21} \text{ e} \cdot \text{cm}$$

Leading order hadronic contribution

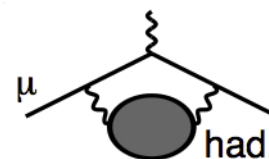
So far, the only method to calculate the hadronic contribution to necessary precision is via dispersion relation - by integrating experimental cross-section $\sigma(e^+e^- \rightarrow hadrons)$.

Weighting function $\sim 1/s$, therefore **lower energies ($\lesssim 2$ GeV) contribute the most.**



Contribution to the value and error of $a_\mu(had; LO)$ from various energy ranges (in GeV)

The diagram to be evaluated:



pQCD not useful. Use the **dispersion relation** and the **optical theorem**.

$$\text{had. blob} = \int \frac{ds}{\pi(s-q^2)} \text{Im} \text{had. blob}$$

$$2 \text{Im} \text{had. blob} = \sum_{\text{had.}} \int d\Phi \left| \text{had. blob} \right|^2$$

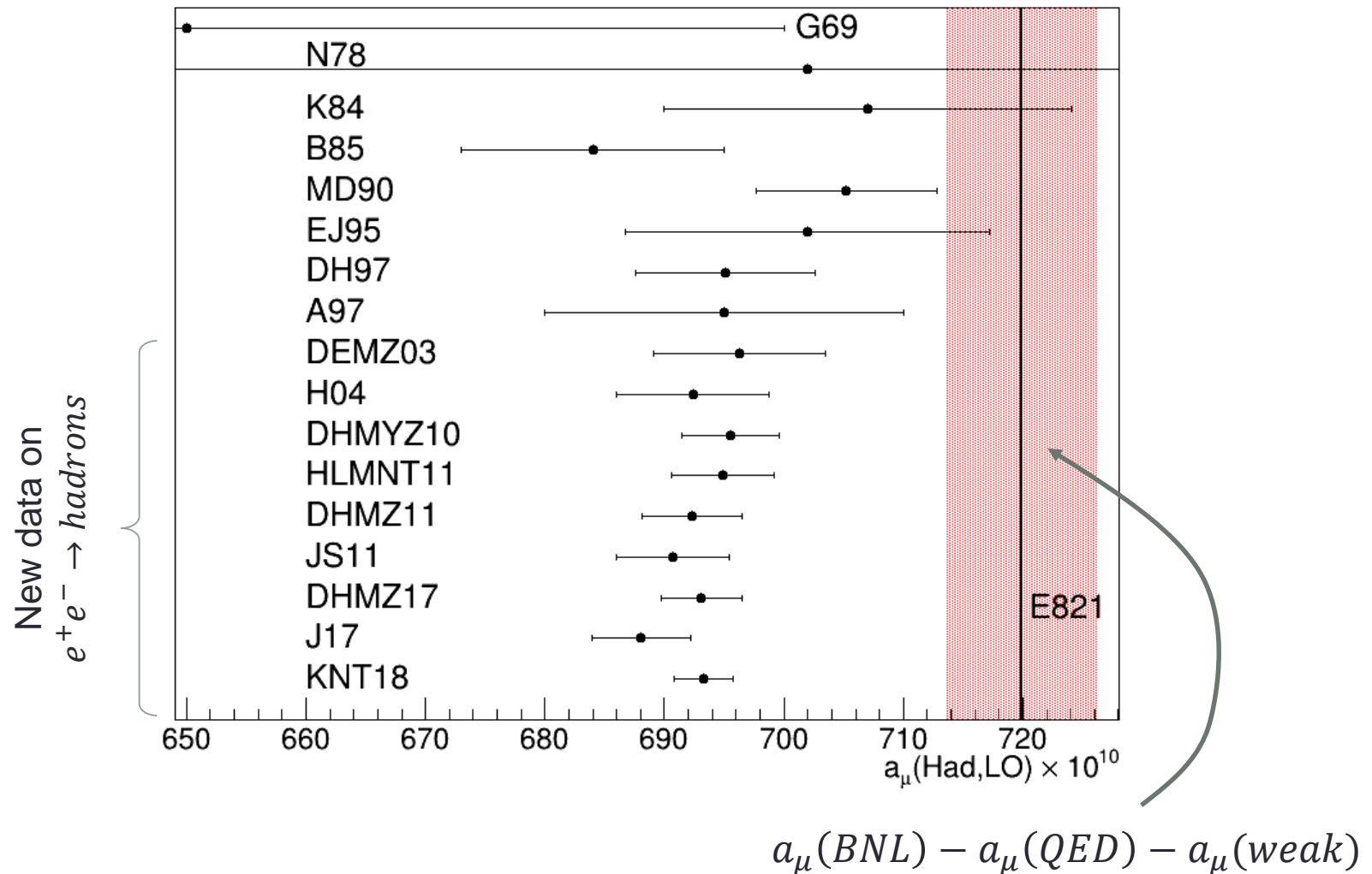
$$a_\mu(had; LO) = \frac{\alpha^2}{3\pi^2} \int \frac{ds}{s} R(s) K(s)$$

measured \rightarrow

$$R(s) = \frac{\sigma^0(e^+e^- \rightarrow \gamma^* \rightarrow hadrons)}{4\pi\alpha^2/3s}$$

FOM: 140 ppb at FNAL \leftrightarrow 0.25% in $R(s)$

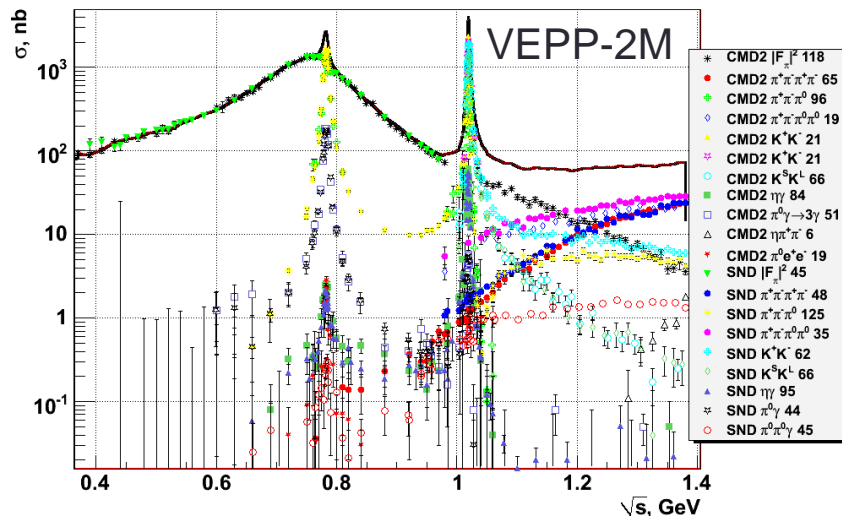
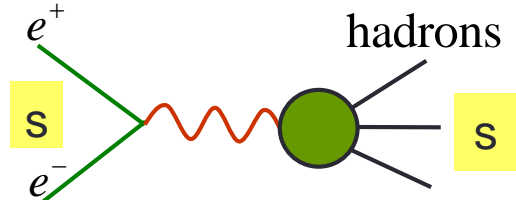
The history of $a_\mu(\text{had}; LO)$ calculation



Sources of $\sigma(e^+e^- \rightarrow \text{hadrons})$ data

Direct energy scan

- e^+e^- collider, tunable in energy
- Take data at each energy to identify $e^+e^- \rightarrow H$

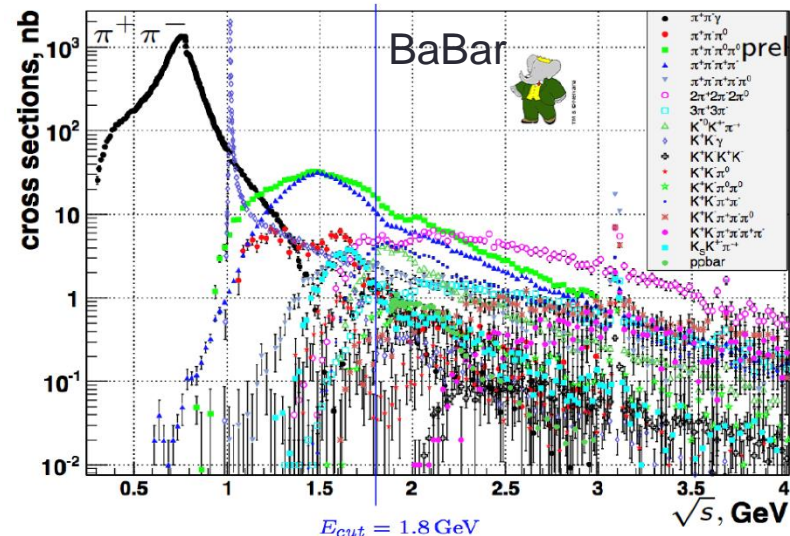
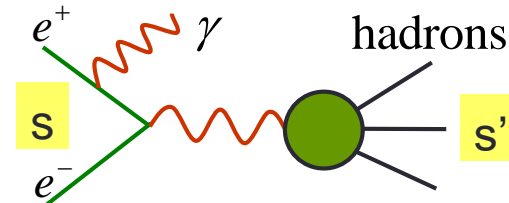


Direct: CMD-2 and SND (Novosibirsk), (2003-2008)

ISR: BaBar (2009-2017), KLOE (2009-2017), BES-III (2016)

Initial state radiation method (ISR)

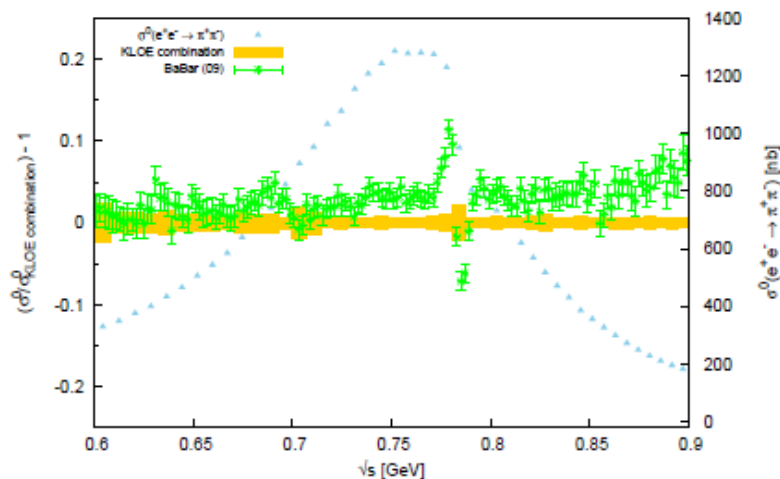
- e^+e^- collider with high luminosity at fixed energy (“factory”)
- Take data at single energy to identify $e^+e^- \rightarrow H + \gamma$ and extract $\sigma(e^+e^- \rightarrow H)$ at lower energies



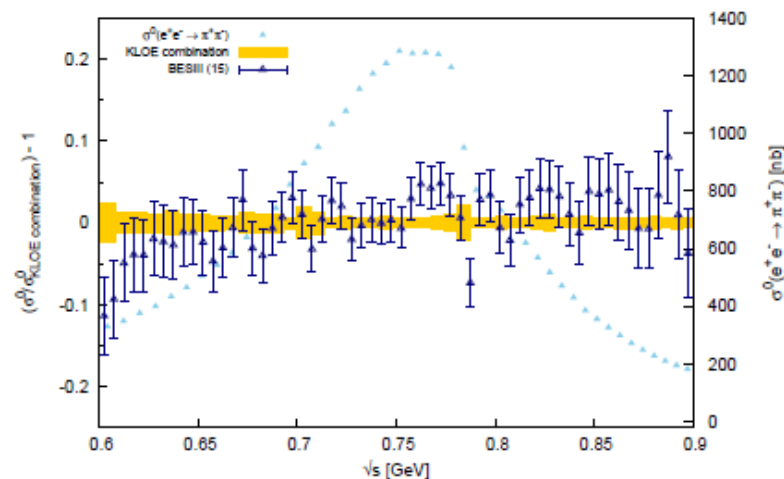
$E_{cut} = 1.8 \text{ GeV}$

Comparison of $e^+e^- \rightarrow \pi^+\pi^-$ data

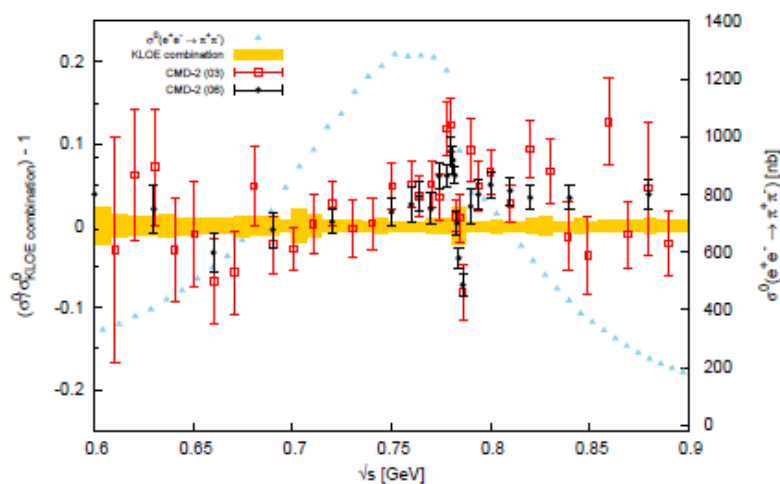
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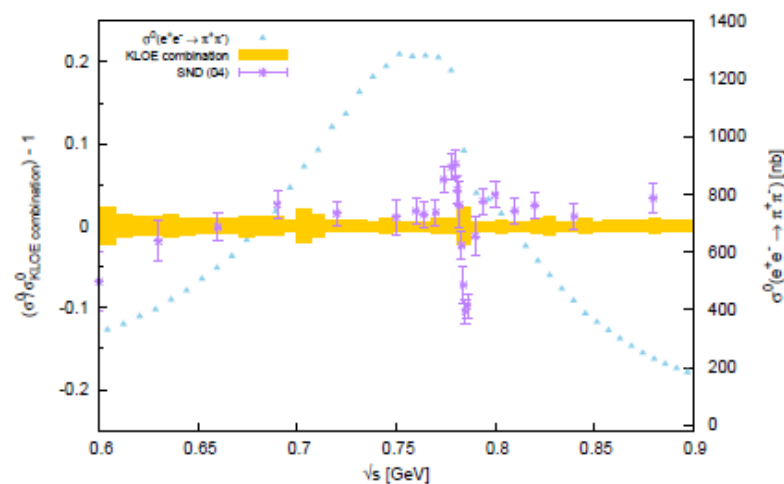
(b) KLOE combination vs. BaBar



(c) KLOE combination vs. BESIII



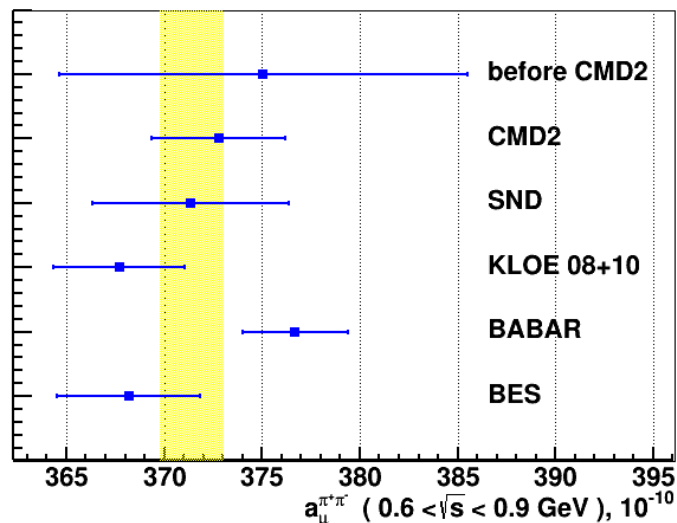
(d) KLOE combination vs. CMD-2



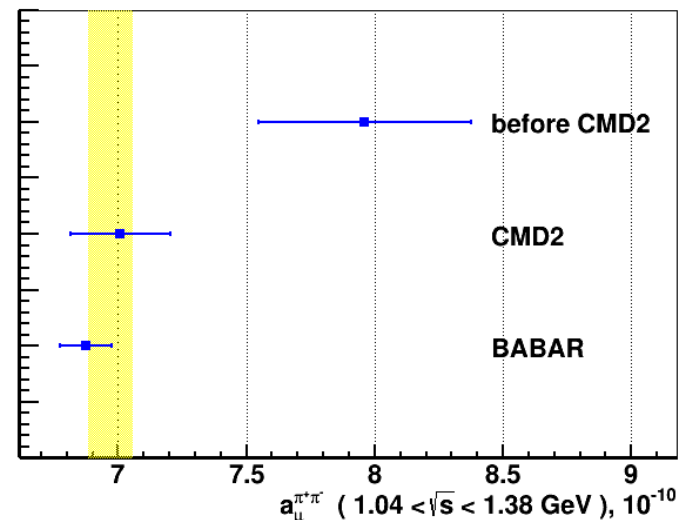
(e) KLOE combination vs. SND

Comparison of contributions to $a_\mu(\text{had}; LO)$

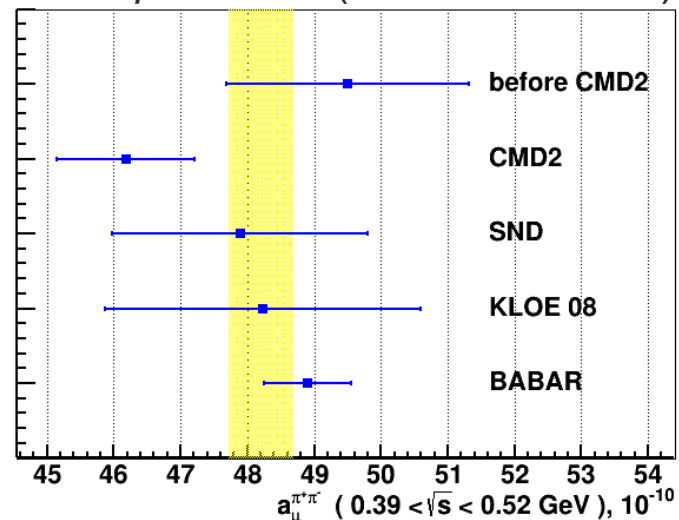
ρ meson (0.6-0.9 GeV)



Above ϕ meson (1.04-1.38 GeV)



Below ρ meson (0.39-0.52 GeV)



Compared are values of integral:

$$a_\mu(\text{had}; LO) = \frac{\alpha^2}{3\pi^2} \int_{E_{min}}^{E_{max}} \frac{ds}{s} \frac{\sigma^0(e^+e^- \rightarrow \pi^+\pi^-)}{4\pi\alpha^2/3s} K(s)$$

calculated in different energy ranges and with various data sets

VEPP-2000 and R(s)

Now $a_\mu^{had,LO}$ calculation is dominated by ISR measurements

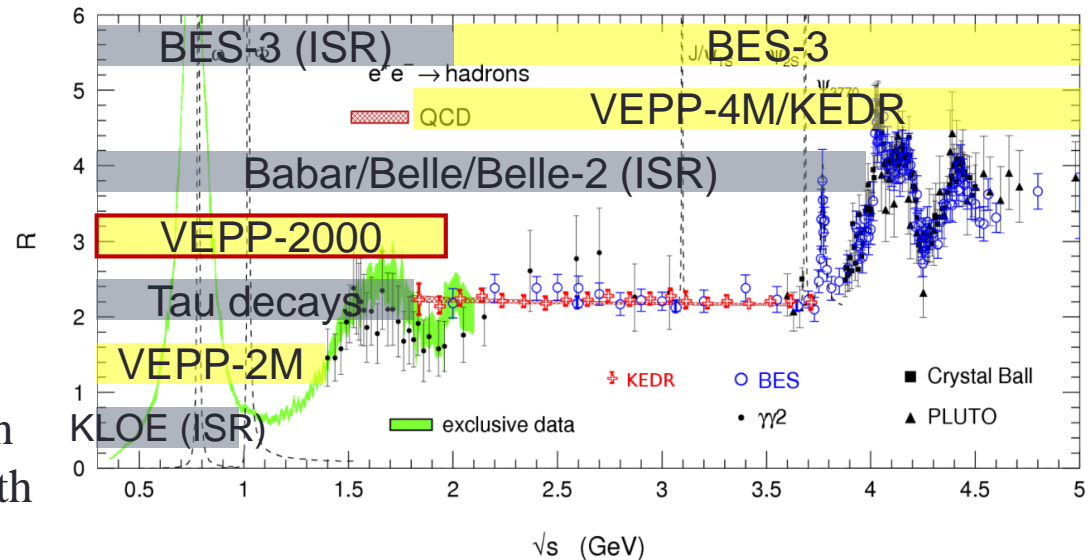
ISR and direct scan were never compared to the required level of precision except for $e^+e^- \rightarrow \pi^+\pi^-$, where some discrepancies are observed

VEPP-2000 goal: provide direct scan measurement of R(s) up to 2 GeV with high statistics and low systematic

In perfect world we want:

- $a_\mu^{had,LO}$ from direct scan to 0.4%
 - $a_\mu^{had,LO}$ from ISR to 0.4%
 - $a_\mu^{had,LO}$ from lattice to 0.4%
- and they should agree.

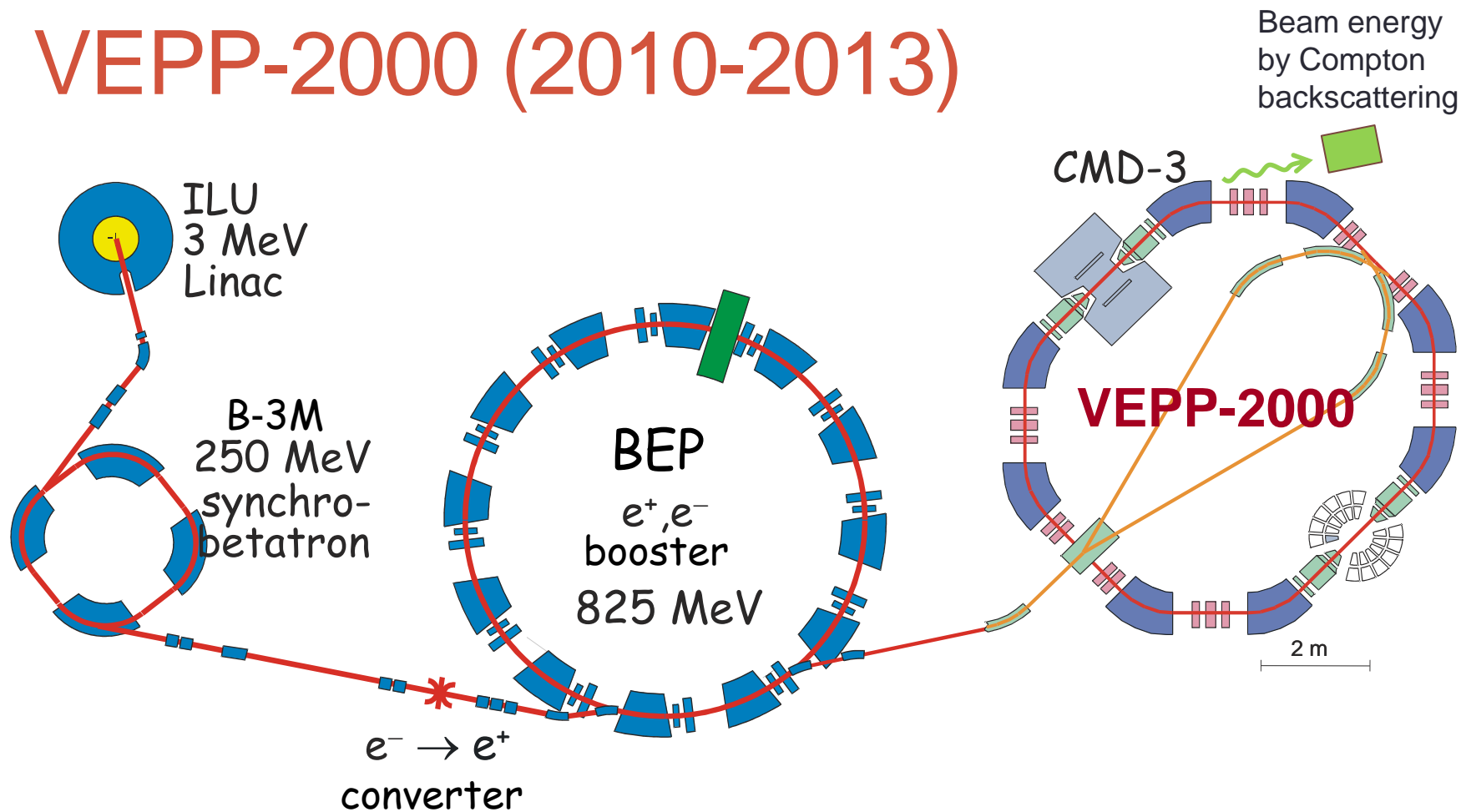
$$R(s) = \frac{\sigma(e^+e^- \rightarrow hadrons)}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}$$



Lets set the scale:

- $\Delta a_\mu(exp - th)$ corresponds to $\approx 4\% \cdot a_\mu^{had,LO}$
- FNAL precision of 140 ppb corresponds to $\approx 0.25\% \cdot a_\mu^{had,LO}$

VEPP-2000 (2010-2013)



C.m. energy range is 0.32-2.0 GeV; unique optics – “round beams”

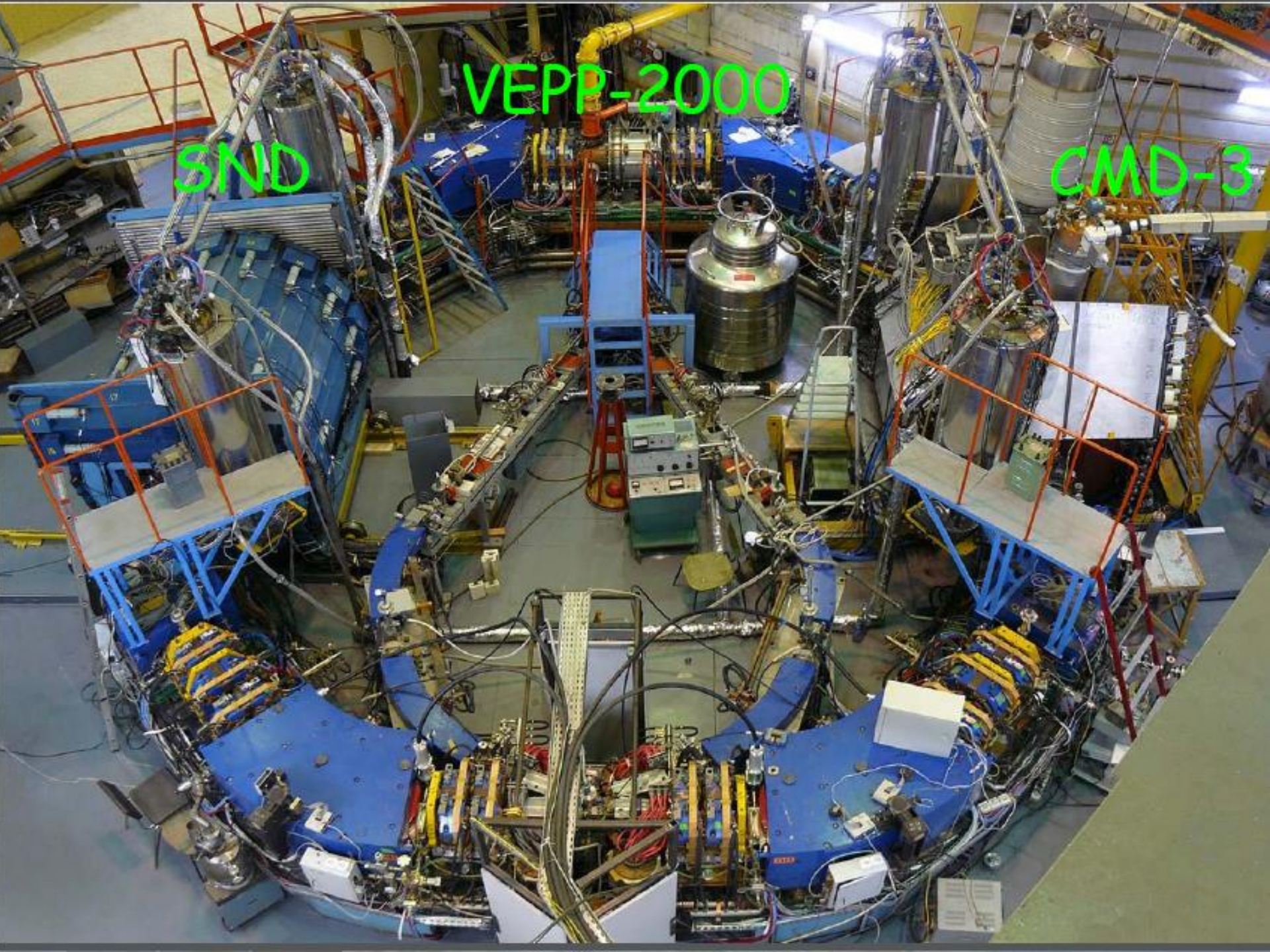
Design luminosity is $L = 10^{32} 1/cm^2 s @ \sqrt{s} = 2 \text{ GeV}$

Experiments with two detectors, CMD-3 and SND, started by the end of 2010

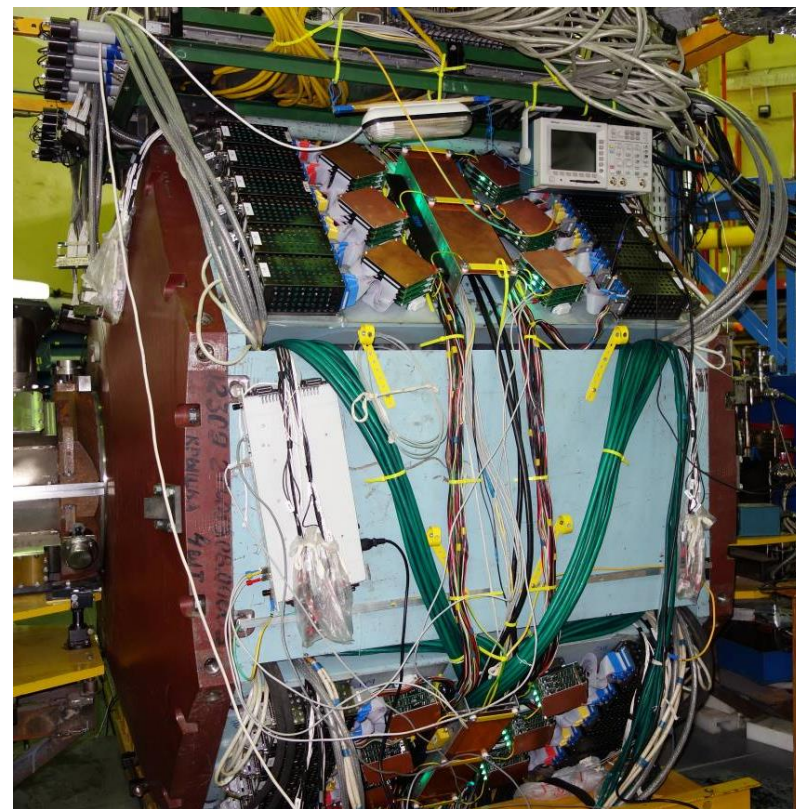
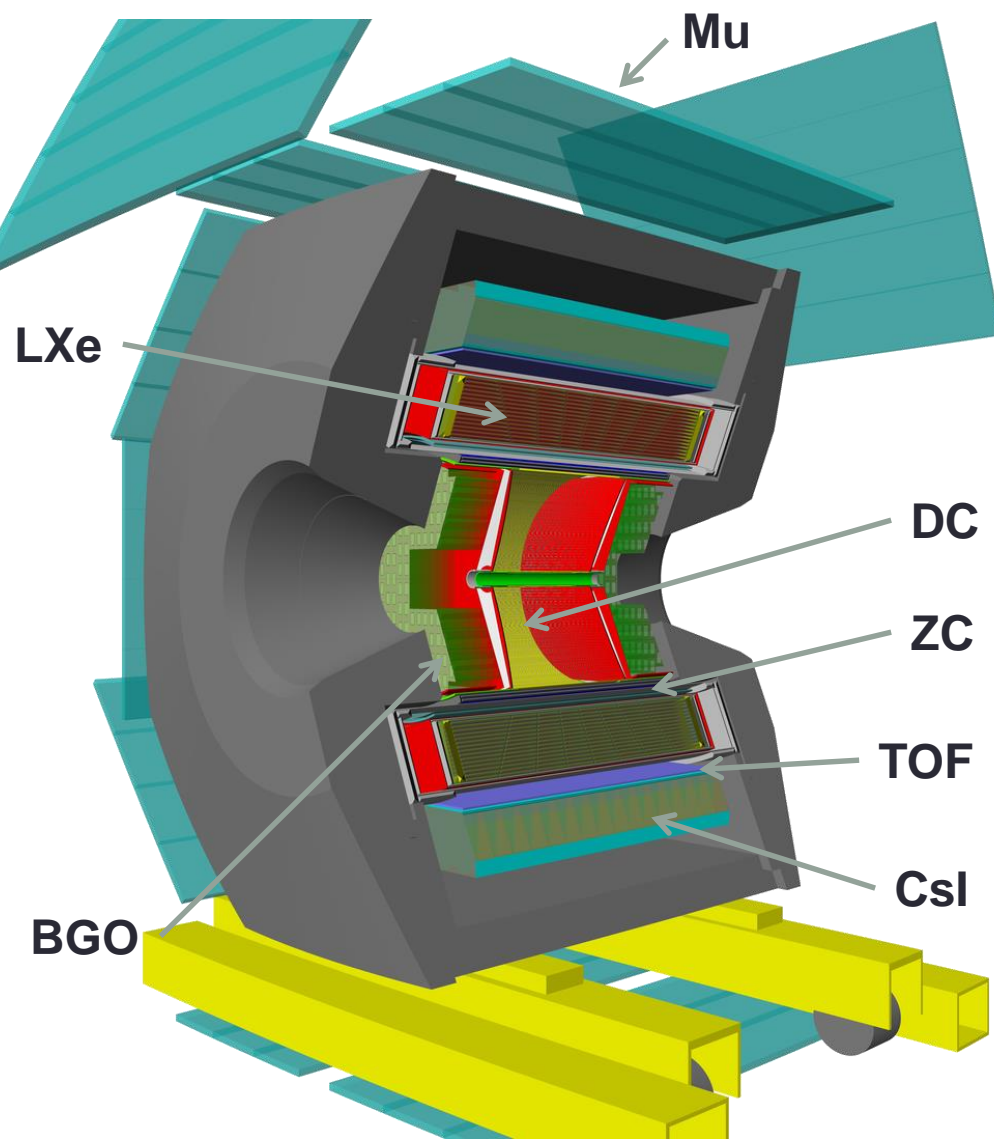
VEPP-2000

SND

CMD-3

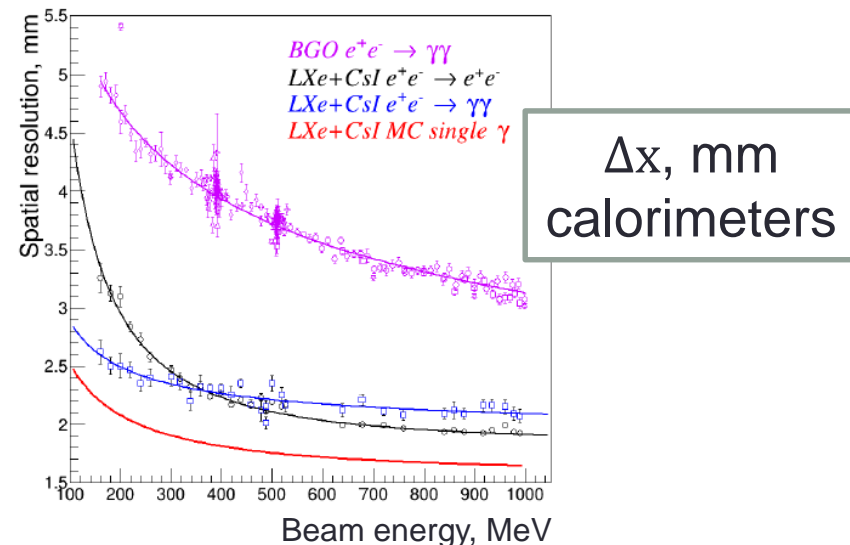
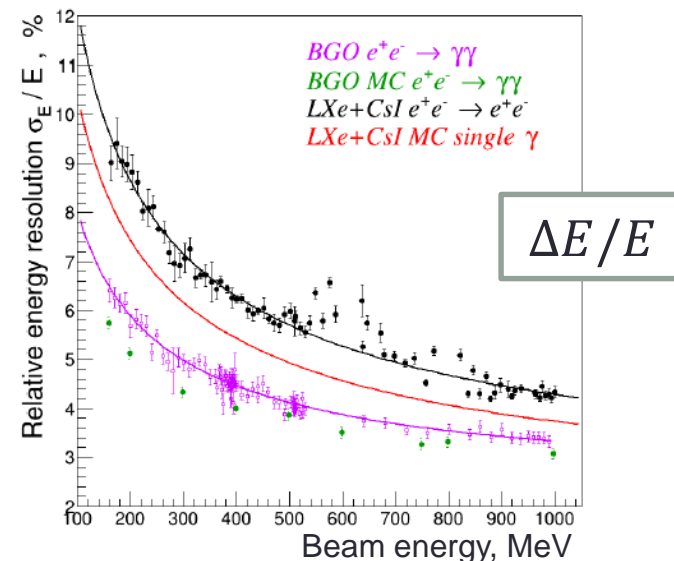
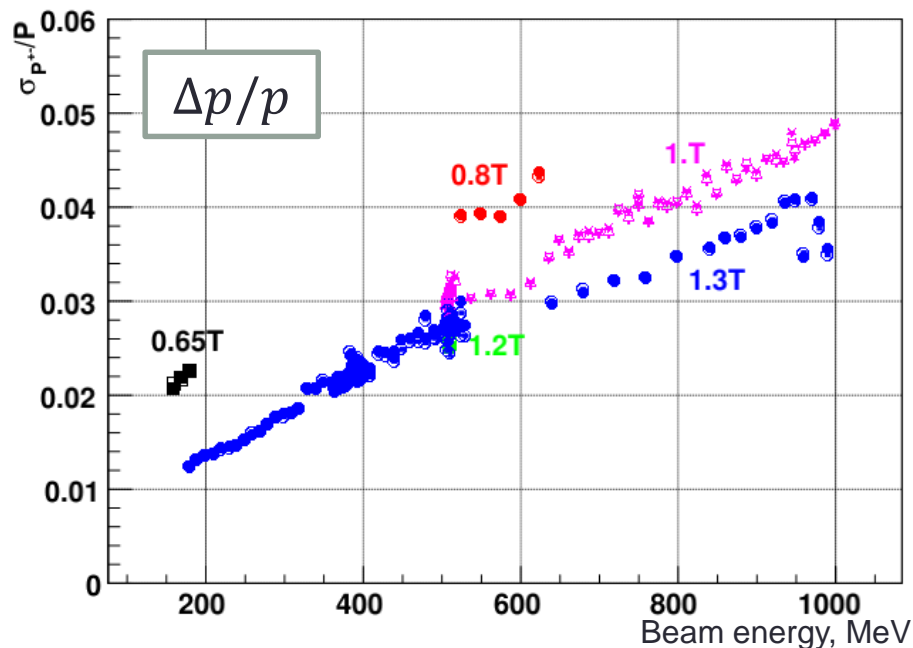


Detector CMD-3

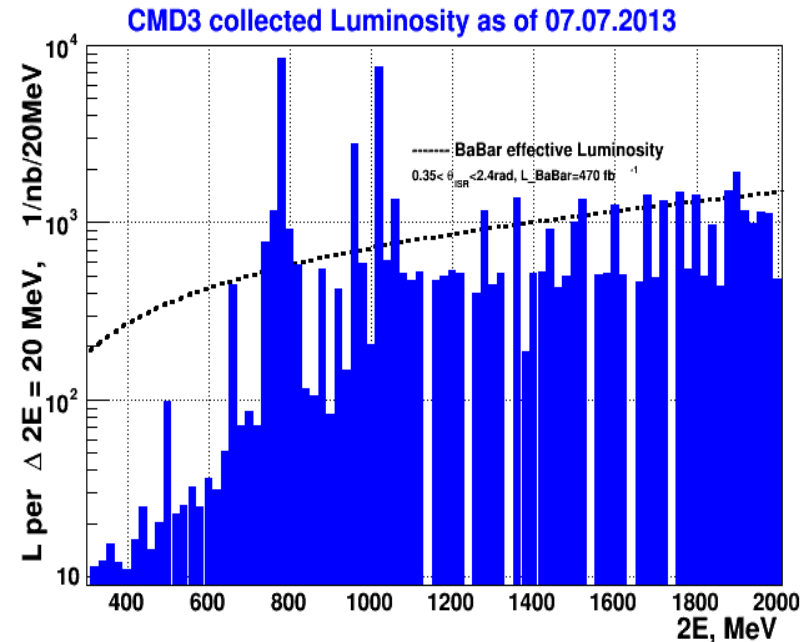
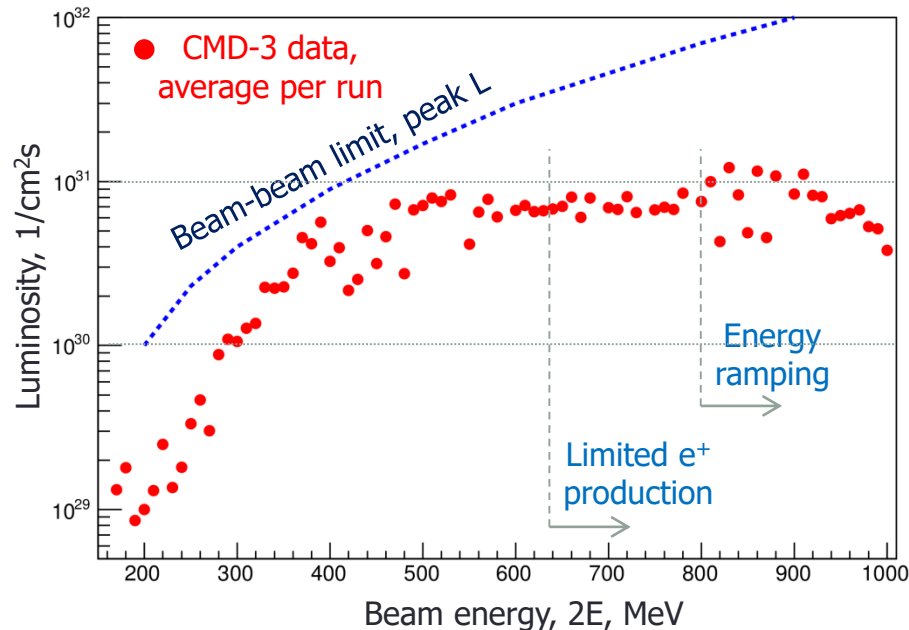


CMD-3 Performance (2011-2013)

- 1.0-1.3 T magnetic field
- Tracking: $\sigma_{R\phi} \sim 100 \mu$, $\sigma_z \sim 2 - 3$ mm
- Combined EM calorimeter (LXE, CsI, BGO), $13.5 X_0$
 - $\sigma_E/E \sim 3\% - 10\%$
 - $\sigma_{\Theta} \sim 5$ mrad



Collected luminosity in 2011-2013



About 60 pb⁻¹ collected per detector

$\omega(782)$	8.3 $1/\text{pb}$
$2E < 1 \text{ GeV}$ (except ω)	9.4 $1/\text{pb}$
$\phi(1019)$	8.4 $1/\text{pb}$
$2E > 1.04 \text{ GeV}$	34.5 $1/\text{pb}$

The luminosity was limited by a deficit of positrons and limited energy of the booster.

The VEPP-2000 upgrade has started in 2013.

VEPP-2000 upgrade (2013-2016)



Collider upgrades:

- x10 more intense positron source
- booster up to 1 GeV (match VEPP-2000)

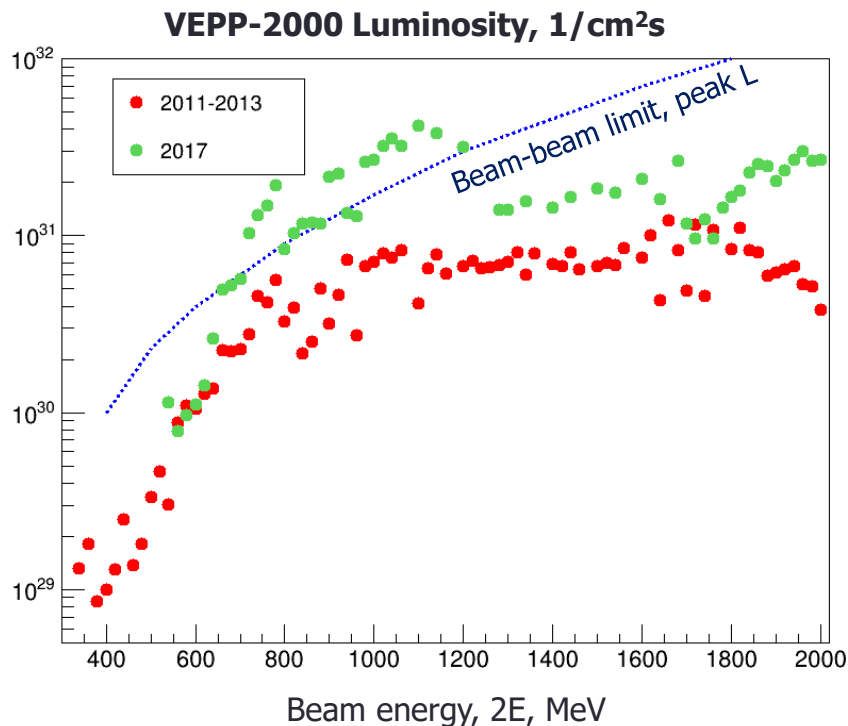
CMD-3 upgrades:

- New electronics for Lxe calorimeter
- New TOF system
- DAQ and electronics upgrades

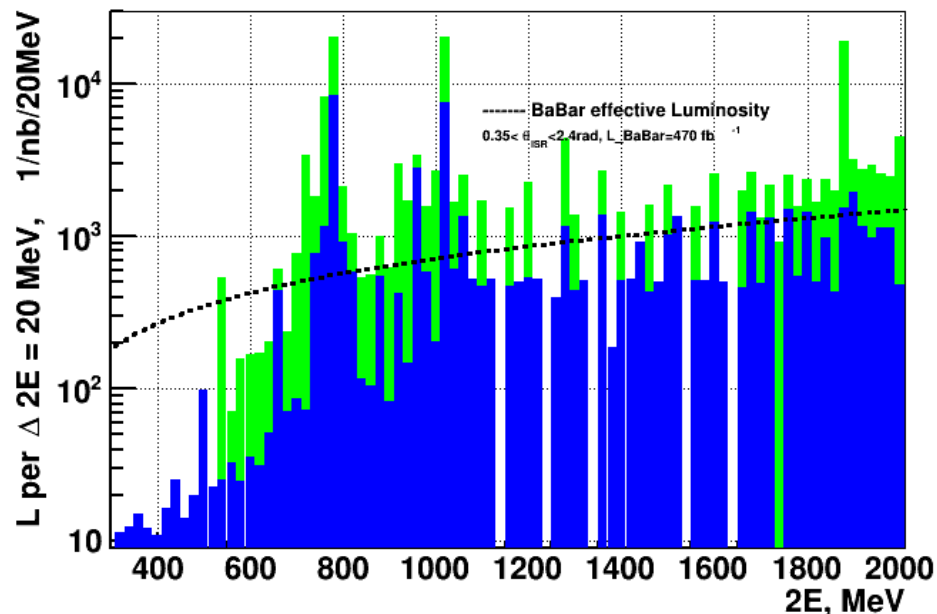
Detectors resumed data taking by the end of 2016

2017 data taking

2017
2011-2013



CMD3 collected Luminosity as of 15.05.2018



In 2017: big improvement in luminosity

Below 1 GeV: $>50 \text{ pb}^{-1}$ collected and counting

0.55 – 1.00 GeV	$> 50 \text{ 1/pb}$
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Above 1 GeV: $\sim 50 \text{ pb}^{-1}$ collected

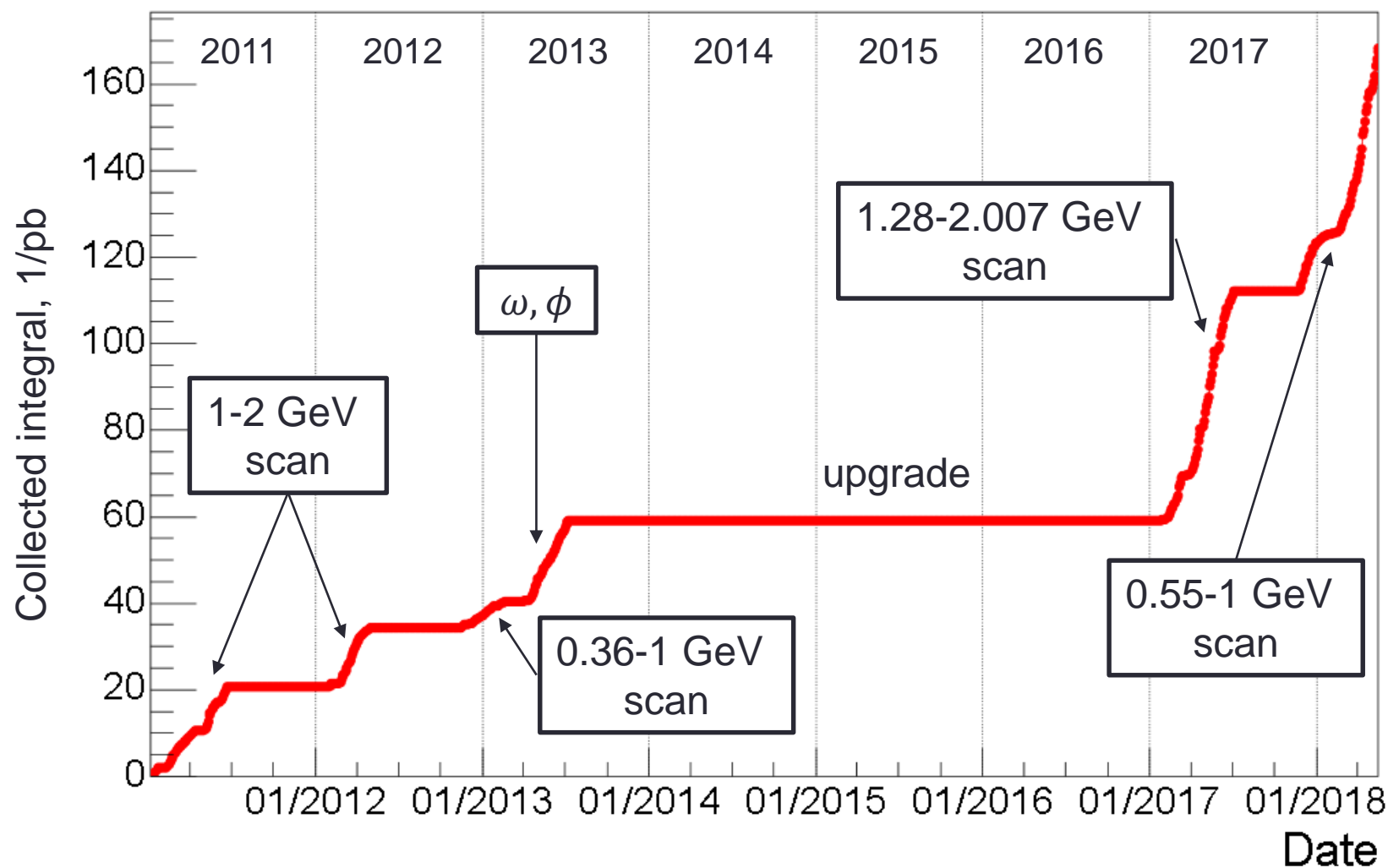
2.007 GeV ($e^+e^- \rightarrow D^{0*}$)	4 $1/\text{pb}$
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$p\bar{p}$ and $n\bar{n}$ threshold	14 $1/\text{pb}$
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Overall:

1.28 – 2.007 GeV	50 $1/\text{pb}$
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Overview of CMD-3 data taking runs



Exclusive channels $e^+e^- \rightarrow hadrons$

At VEPP-2000 we do **exclusive** measurement of $\sigma(e^+e^- \rightarrow hadrons)$.

- 2 charged

$$e^+e^- \rightarrow \pi^+\pi^-, K^+K^-, K_S K_L, p\bar{p}$$

published
in progress

- 2 charged + γ 's

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0, \pi^+\pi^-\eta, K^+K^-\pi^0, K^+K^-\eta, K_S K_L \pi^0, \pi^+\pi^-\pi^0\eta, \\ \pi^+\pi^-\pi^0\pi^0, \pi^+\pi^-\pi^0\pi^0\pi^0, \pi^+\pi^-\pi^0\pi^0\pi^0\pi^0$$

- 4 charged

$$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-, K^+K^-\pi^+\pi^-, K_S K^*$$

- 4 charged + γ 's

$$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-\pi^0, \pi^+\pi^-\eta, \pi^+\pi^-\omega, \pi^+\pi^-\pi^+\pi^-\pi^0\pi^0, K^+K^-\eta, K^+K^-\omega$$

- 6 charged

$$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-\pi^+\pi^-$$

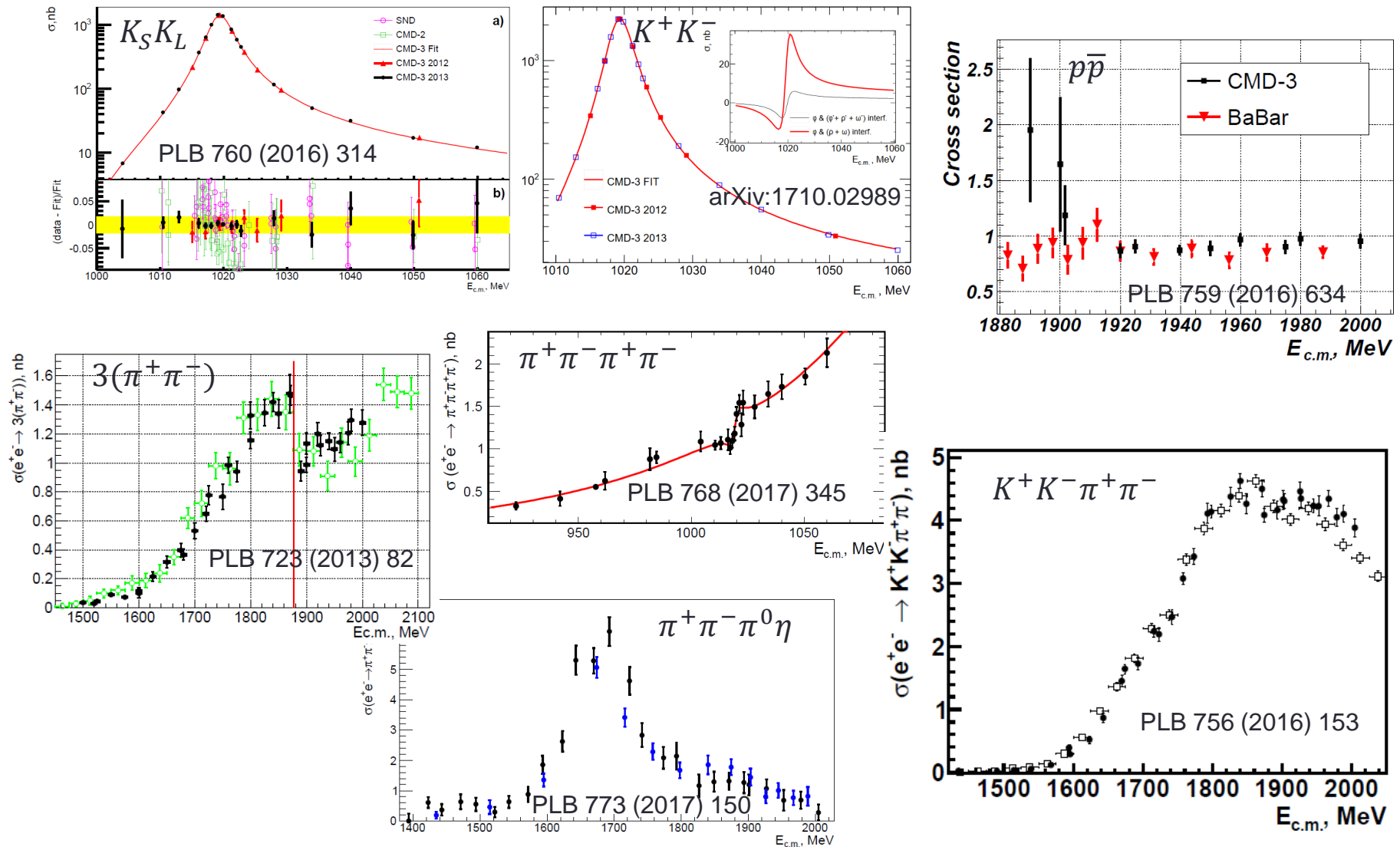
- γ 's only

$$e^+e^- \rightarrow \pi^0\gamma, \eta\gamma, \pi^0\pi^0\gamma, \pi^0\eta\gamma, \pi^0\pi^0\pi^0\gamma, \pi^0\pi^0\eta\gamma$$

- other

$$e^+e^- \rightarrow n\bar{n}, \pi^0 e^+e^-, \eta e^+e^-$$

CMD-3 published results from 2011-2013



Overview of the $e^+e^- \rightarrow \pi^+\pi^-$ analysis

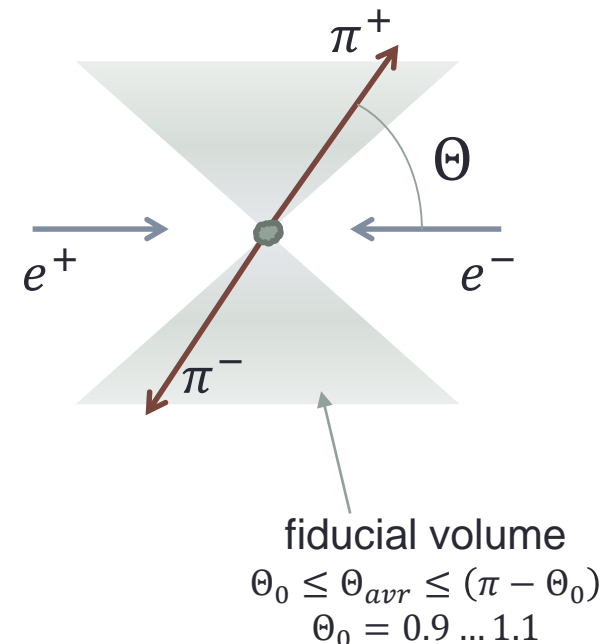
- We select events with 2 back-to-back tracks in the detector at large angle
- Selected event sample consists of e^+e^- , $\mu^+\mu^-$, $\pi^+\pi^-$ pairs and background (mostly cosmic)

Key pieces of analysis to reach high precision:

- $e/\mu/\pi$ separation
- radiative corrections
- various pion-specific corrections

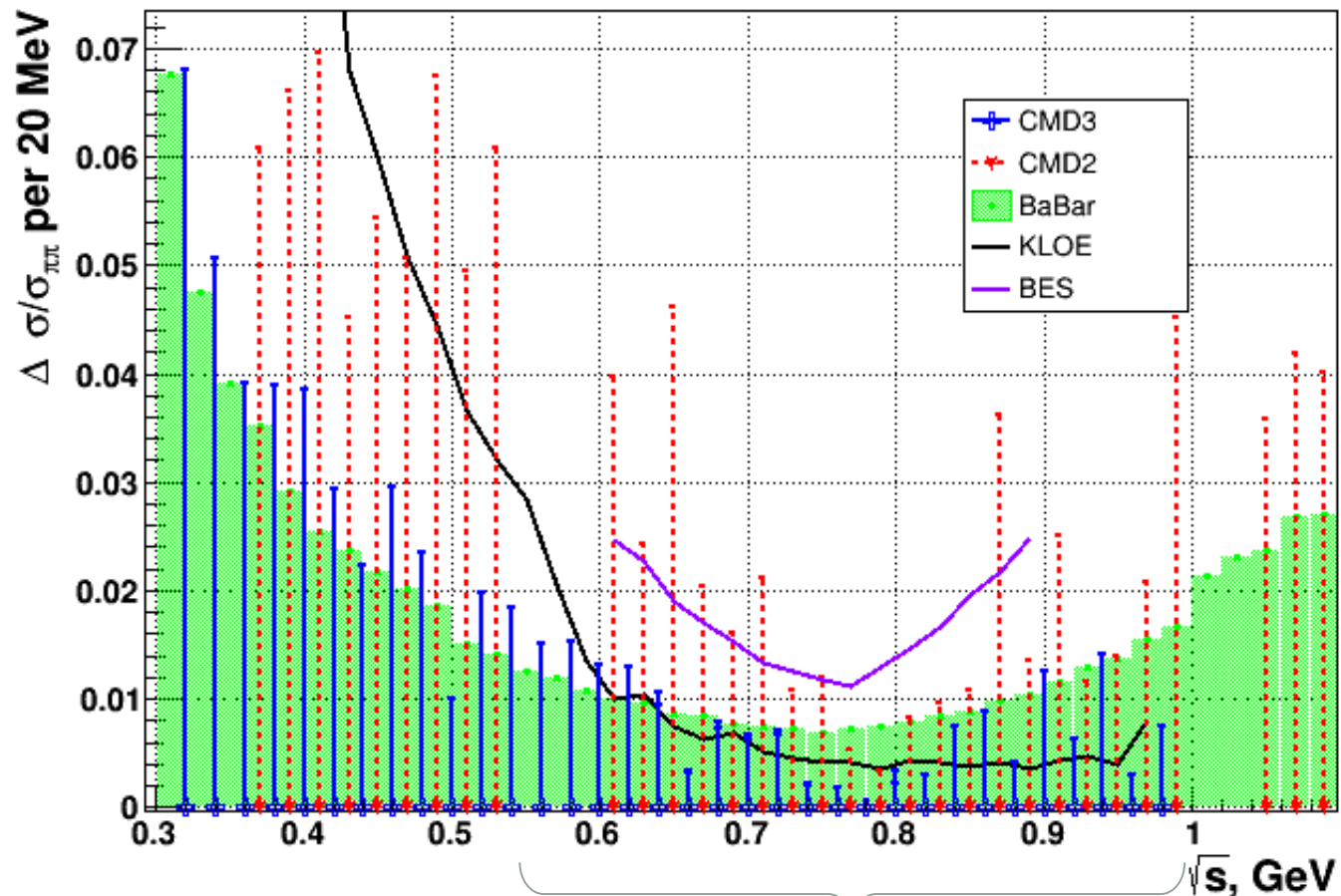
Available data:

- 0.32-1.0 GeV (below ϕ):
 - **2013 energy scan** – data analysis well in progress
 - 2017-2018 energy scan – we are taking data now
- 1.0-2.0 GeV (above ϕ):
 - 2011-2012 energy scan – no beam energy monitoring
 - 2017 energy scan – data analysis just starting



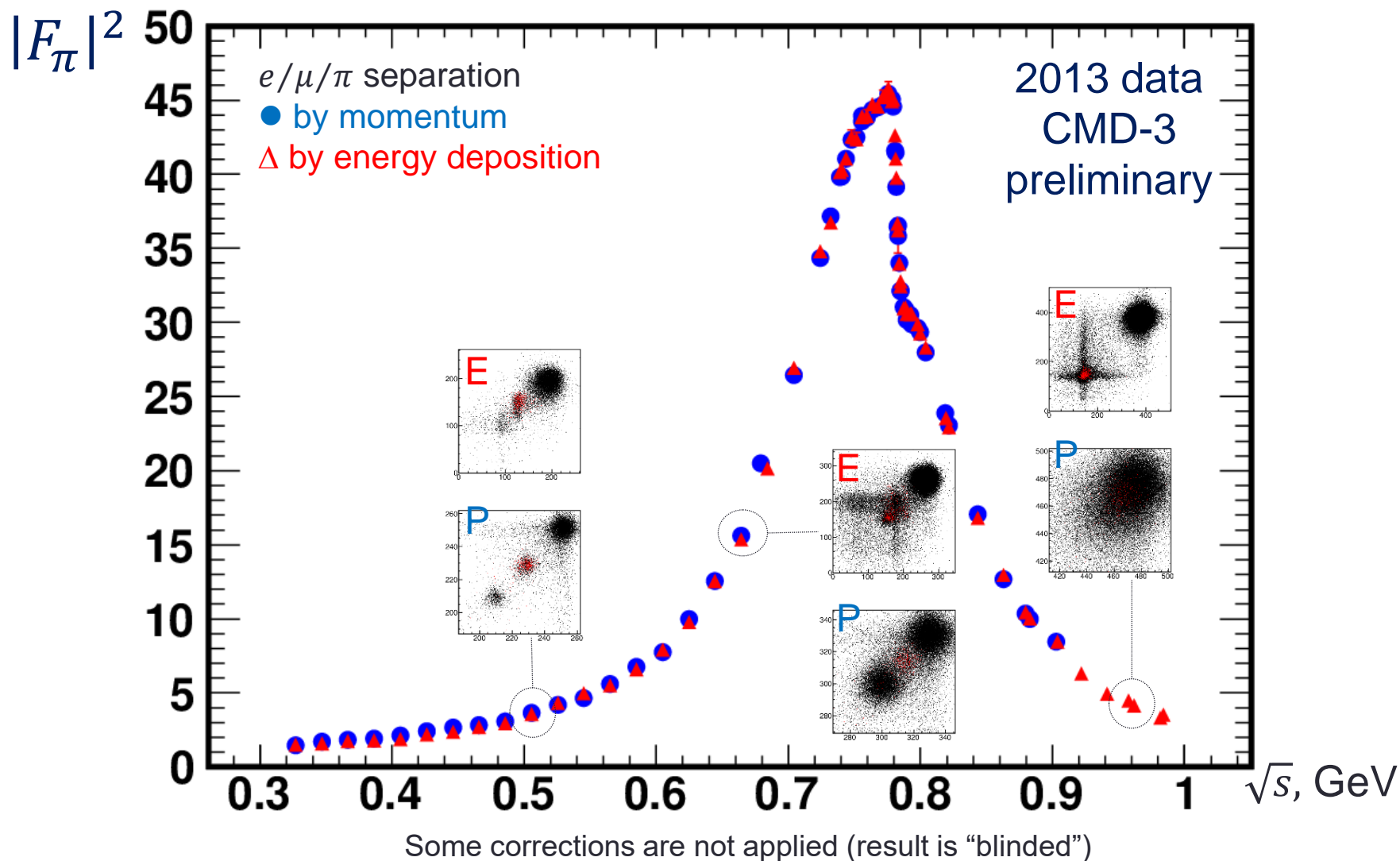
$e^+e^- \rightarrow \pi^+\pi^-$: statistics

Statistical accuracy $\Delta\sigma/\sigma$ in 20 MeV bins



Already collected x2-3 data in 2017-2018

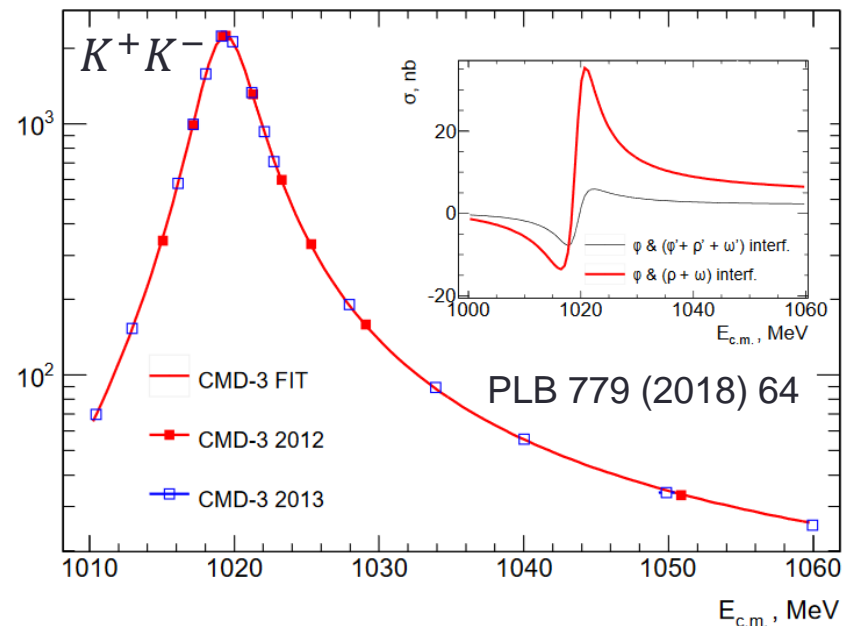
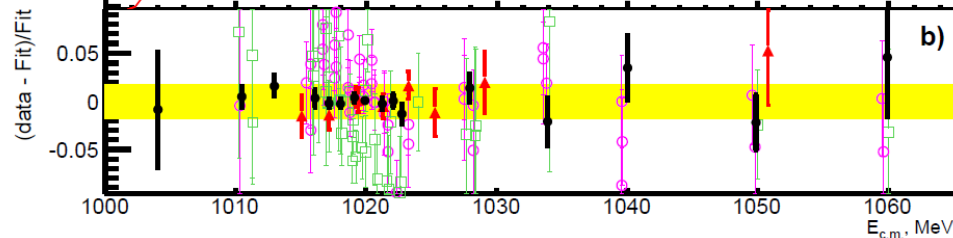
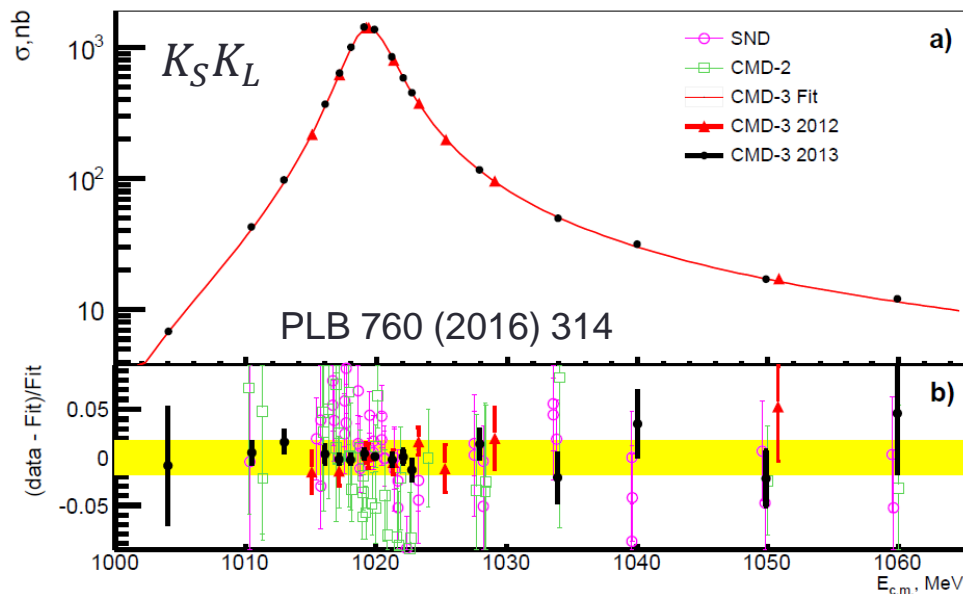
Preliminary result (“blinded”)



$e^+e^- \rightarrow \pi^+\pi^-$: systematics

Source	Goal	Current estimation	Comment
Radiative correction	0.2%	0.2% (cross-section) 0.0-0.4% (mom.separation)	To-do: more MCGPJ improvement, comparison to data
Event separation	0.2%	0.1-0.5% (mom.separation) ~1.5% (energy separation)	To-do: improve energy separation
Fiducial volume	0.1%	ok	Two independent subsystems to fix fiducial volume
Beam energy	0.1%	ok	Continuous monitoring via Compton backscattering
Pion corrections (decay, nucl.int.)	0.1%	0.1% - nucl.interations 0.6-0.3% - decays al low energies	To-do: improve reconstruction of decay events
Combined	0.33%	0.4-0.9% (mom.sep.) 1.5% (energy sep.)	

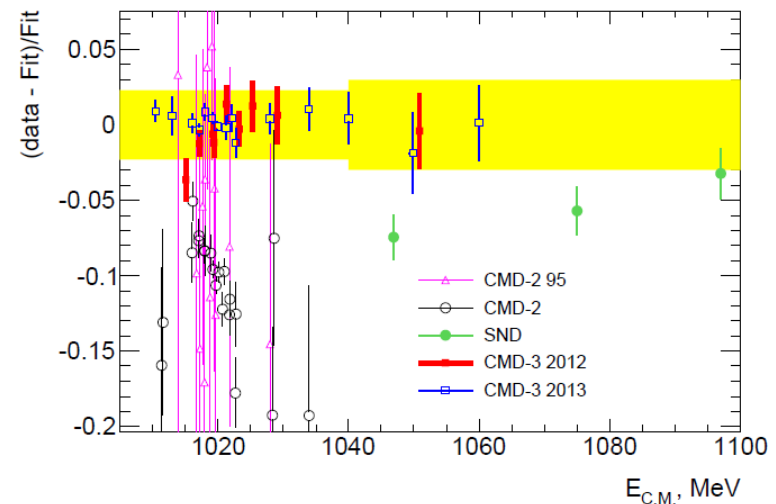
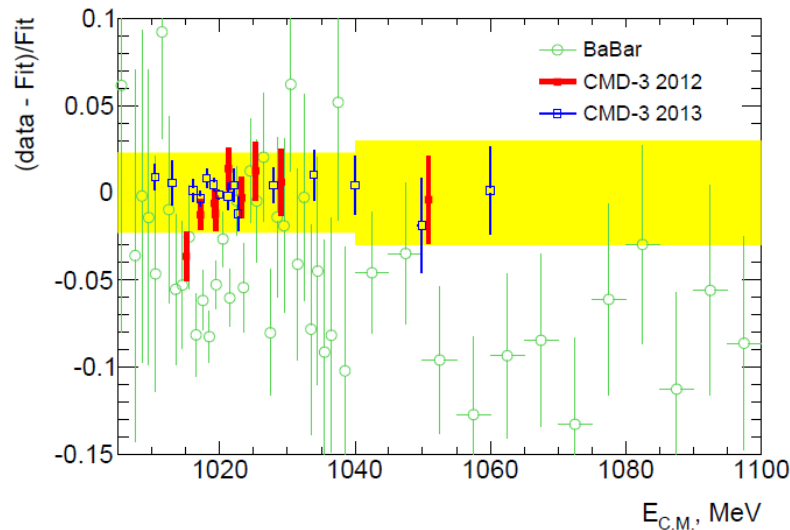
$K_S K_L$ and $K^+ K^-$ @ $\varphi(1020)$



Recent result from CMD-3:

- $K_S K_L$ at φ , systematic precision 1.8%
- $K^+ K^-$ at φ , systematic precision 2.0% (2.8%)

K^+K^- : comparison with other measurements



$K_S K_L$ at φ is consistent between different experiments, but there is discrepancy in $K^+ K^-$ channel.

New CMD-3 $K^+ K^-$ cross-section is above CMD-2 and BaBar, but is consistent with isospin symmetry:

$$R = \frac{g_{\varphi K^+ K^-}}{g_{\varphi K_S K_L} \sqrt{Z(m_\varphi)}} = 0.990 \pm 0.017$$

- $R_{SND} = 0.92 \pm 0.03 (2.6\sigma)$
- $R_{CMD-2} = 0.943 \pm 0.013 (4.4\sigma)$
- $R_{BaBar} = 0.972 \pm 0.017 (1.5\sigma)$

Possible explanation: CMD-2 trigger correction was underestimated; due to different trigger configuration there is no such correction at CMD-3

$K_S K_L$ and $K^+ K^-$: $\rho - \varphi$ interference

$\rho - \varphi$ interference can be directly observed:

$$R_{c/n} = \sigma(e^+e^- \rightarrow K^+K^-) \times \frac{p_{K^0}^3(s)}{p_{K^\pm}^3(s)} \times \frac{1}{Z(s)} - \delta \times \sigma(e^+e^- \rightarrow K_S K_L)$$

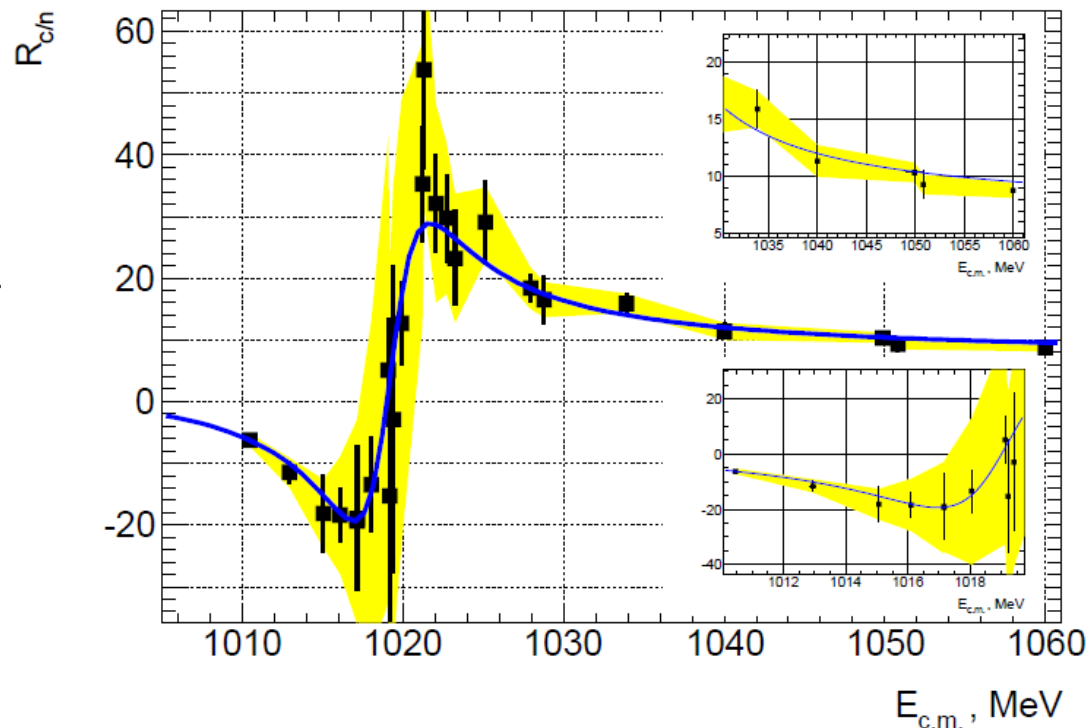
- $r_{\rho,\omega} = 0.91 \pm 0.04$

deviation of SU(3) relations

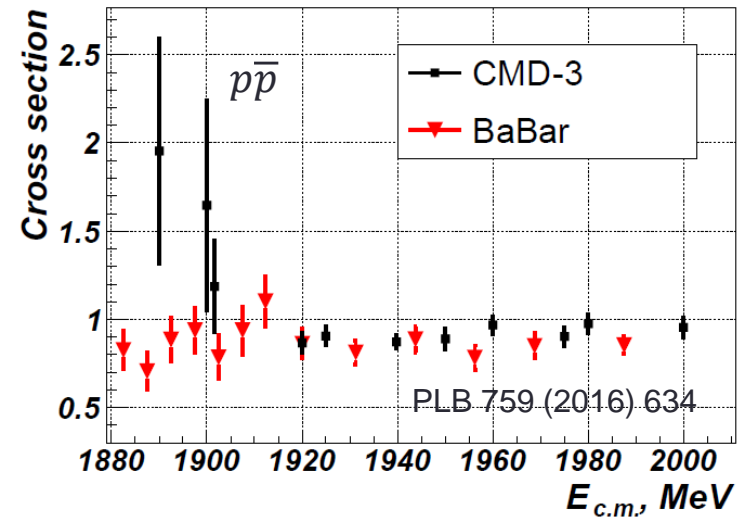
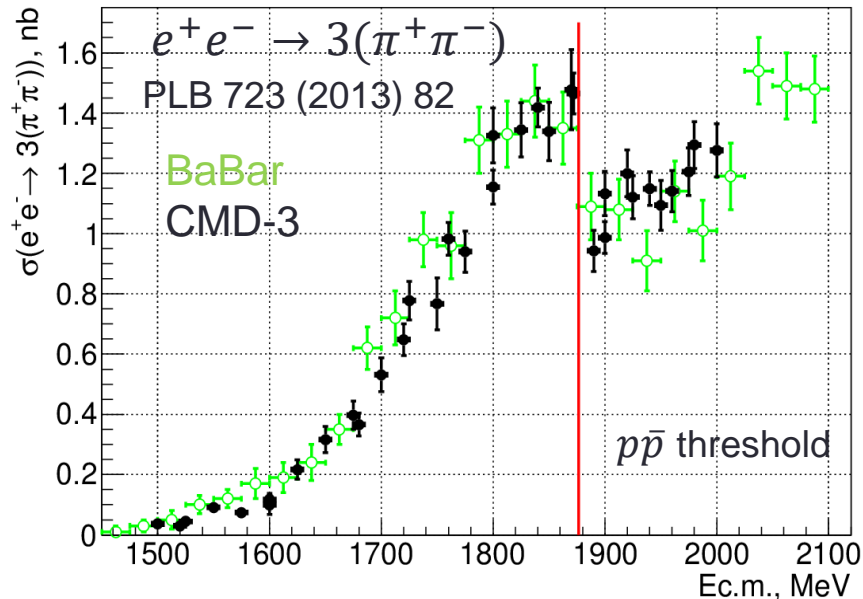
$$g_{\omega K^+ K^-} = g_{\rho K^+ K^-} = -g_{\varphi K^+ K^-} / \sqrt{2}$$

- $\delta = 0.989 \pm 0.003$

test of systematic errors



$R(s)$ at $N\bar{N}$ threshold



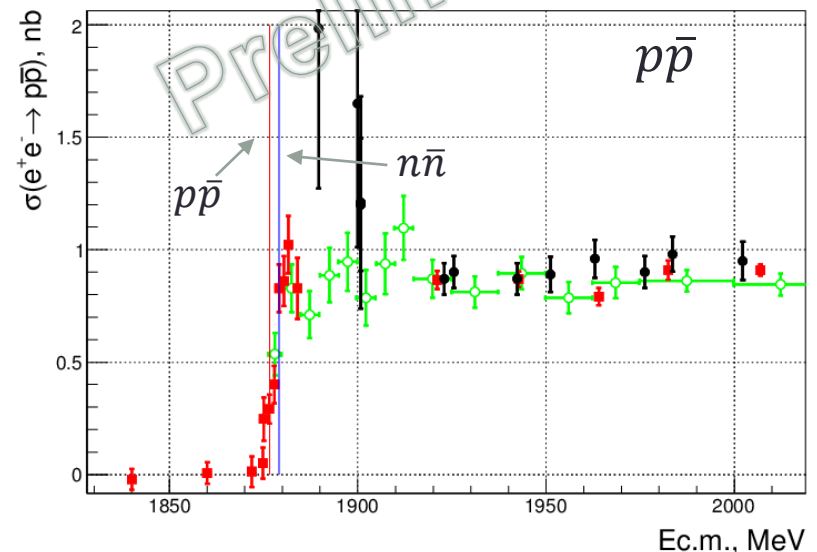
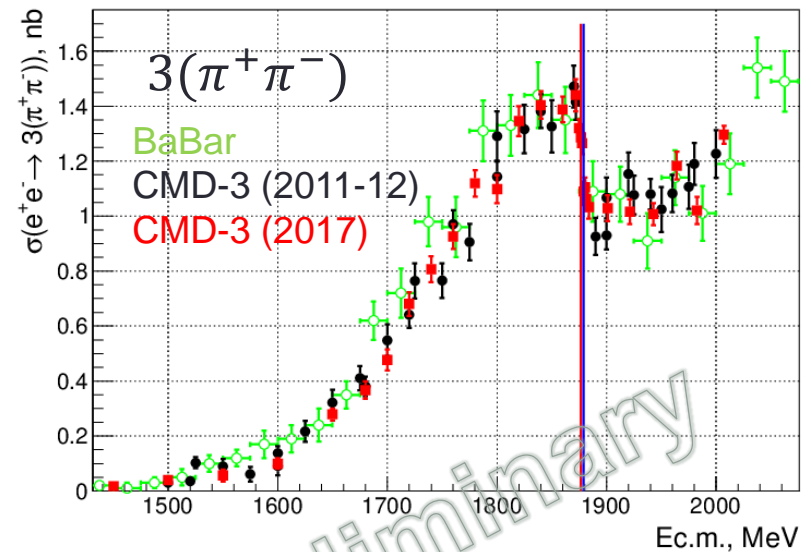
One of first results from CMD-3:

- Sudden drop of $e^+e^- \rightarrow 3(\pi^+\pi^-)$ cross section at $N\bar{N}$ threshold
- Confirmed, that $p\bar{p}$ production cross section increases quickly at threshold
- Preliminary studies of dynamics of $e^+e^- \rightarrow 3(\pi^+\pi^-)$, hint of energy dependent dynamics in 1.7-1.9 GeV energy range

2017: $e^+e^- \rightarrow 3(\pi^+\pi^-)$ at $N\bar{N}$ threshold

In 2017, CMD-3 collected 13 1/pb in the narrow energy range around $N\bar{N}$ threshold

- the sharp rise of $e^+e^- \rightarrow p\bar{p}$ cross-section is confirmed
- the sharp drop of $e^+e^- \rightarrow 3(\pi^+\pi^-)$ cross-section is confirmed
- we see the similar cross-section drop in other channels ($K^+K^-\pi^+\pi^-$) and don't see it in $\pi^+\pi^-\pi^+\pi^-$



Conclusion

- We are eagerly waiting for the result of the new measurement of muon (g-2) at Fermilab
- The goal of two experiments at VEPP-2000, CMD-3 and SND, is to provide exclusive measurement of $e^+e^- \rightarrow hadrons$ from 0.32 to 2.0 GeV. In particular, it is used to calculate the hadronic contribution to muon (g-2).
- In 2011-2013 CMD-3 has collected 60 1/pb in the whole energy range $0.32 \leq \sqrt{s} \leq 2.0$ GeV, available at VEPP-2000.
- In 2013-2016 the collider and the CMD-3 detector have been upgraded and the data taking was resumed in 2017. >100 1/pb were collected so far.
- Data analysis of exclusive modes of $e^+e^- \rightarrow hadrons$ is in progress. Many results have been published.