



# Casimir And Non-Newtonian force EXperiment

# A parallel plate approach to physics

Vienna May 17, 2018

René Sedmik

Atominstitut, TU Vienna previously: VU Amsterdam

Stay tuned on our website cannex.vu.nl

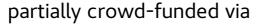








er Wissenschaftsfonds











### Casimir And Non-Newtonian force EXperiment

# A parallel plate approach to vacuum energy

Vienna May 17, 2018

René Sedmik

Atominstitut, TU Vienna previously: VU Amsterdam Stay tuned on our website cannex.vu.nl

















Dark energy and the cosmological constant

$$R_{\mu\nu} - \left(\frac{1}{2}\mathcal{R} - \Lambda\right)g_{\mu\nu} = \frac{8\pi}{c^4}T_{\mu\nu}$$

Einstein 1918: Absence of gravitational collapse



Phenomenological cosmological constant  $\Lambda$ 

#### Dark energy and the cosmological constant

$$R_{\mu\nu} - \left(\frac{1}{2}\mathcal{R} - \Lambda\right)g_{\mu\nu} = \frac{8\pi}{c^4}T_{\mu\nu}$$

Einstein 1918: Absence of gravitational collapse



Phenomenological cosmological constant  $\Lambda$ 

**Hubble 1927:** The universe expands



#### Dark energy and the cosmological constant

 $R_{\mu\nu} - \left(\frac{1}{2}\mathcal{R} - \Lambda\right)g_{\mu\nu} = \frac{8\pi}{c^4}T_{\mu\nu}$ 

Einstein 1918: Absence of gravitational collapse

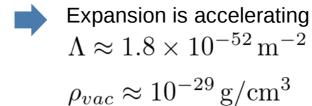
Phenomenological cosmological constant  $\Lambda$ 

**Hubble 1927:** The universe expands

 $\Lambda > 0$ 

Today:

- Redshift of Type 1a supernovae
- Anisotropy of the cosmic microwave background
- Large scale distribution



#### Dark energy and the cosmological constant

$$R_{\mu\nu} - \left(\frac{1}{2}\mathcal{R} - \Lambda\right)g_{\mu\nu} = \frac{8\pi}{c^4}T_{\mu\nu}$$

**Einstein 1918:** Absence of gravitational collapse



Phenomenological cosmological constant  $\Lambda$ 

**Hubble 1927:** The universe expands



- **Today:** Redshift of Type 1a supernovae
  - Anisotropy of the cosmic microwave background
  - Large scale distribution



Expansion is accelerating

$$\Lambda \approx 1.8 \times 10^{-52} \, \mathrm{m}^{-2}$$

$$\rho_{vac} \approx 10^{-29} \,\mathrm{g/cm^3}$$

#### Quantum mechanics (field theory)

Zero point energies of the EM (and other) fields:

$$\rho_{ZPE} \propto \int_{0}^{\lambda_c} dk \, k^3 = \lambda_c^4 \to \infty$$

#### Dark energy and the cosmological constant

$$R_{\mu\nu} - \left(\frac{1}{2}\mathcal{R} - \Lambda\right)g_{\mu\nu} = \frac{8\pi}{c^4}T_{\mu\nu}$$

**Einstein 1918:** Absence of gravitational collapse



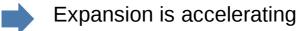
Phenomenological cosmological constant  $\Lambda$ 

**Hubble 1927:** The universe expands



- **Today:** Redshift of Type 1a supernovae
  - Anisotropy of the cosmic microwave background
  - Large scale distribution





$$\Lambda \approx 1.8 \times 10^{-52} \, \mathrm{m}^{-2}$$

$$\rho_{vac} \approx 10^{-29} \,\mathrm{g/cm^3}$$

#### Quantum mechanics (field theory)

Zero point energies of the EM (and other) fields:

$$\rho_{ZPE} \propto \int_{0}^{\lambda_c} dk \, k^3 = \lambda_c^4 \to \infty$$

**Cutoff at the Planck length:** 

$$\lambda_c \to 2\pi/\ell_P$$

$$\rho_{ZPE} \approx 10^{95} \,\mathrm{g/cm^3}$$

#### Dark energy and the cosmological constant

 $R_{\mu\nu} - \left(\frac{1}{2}\mathcal{R} - \Lambda\right)g_{\mu\nu} = \frac{8\pi}{c^4}T_{\mu\nu}$ 

Expansion is accelerating

**Einstein 1918:** Absence of gravitational collapse

Phenomenological cosmological constant  $\Lambda$ 

**Hubble 1927:** The universe expands

 $\Lambda > 0$ 

- **Today:** Redshift of Type 1a supernovae
  - Anisotropy of the cosmic microwave background
  - Large scale distribution

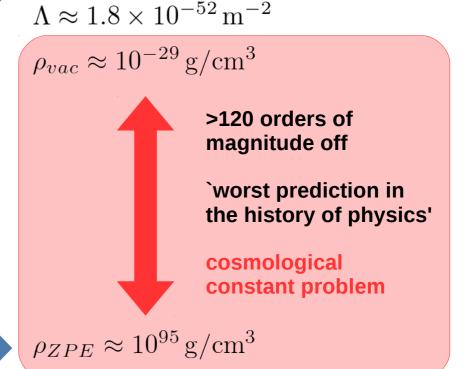
#### Quantum mechanics (field theory)

Zero point energies of the EM (and other) field:

$$\rho_{ZPE} \propto \int_{0}^{\lambda_c} dk \, k^3 = \lambda_c^4 \to \infty$$

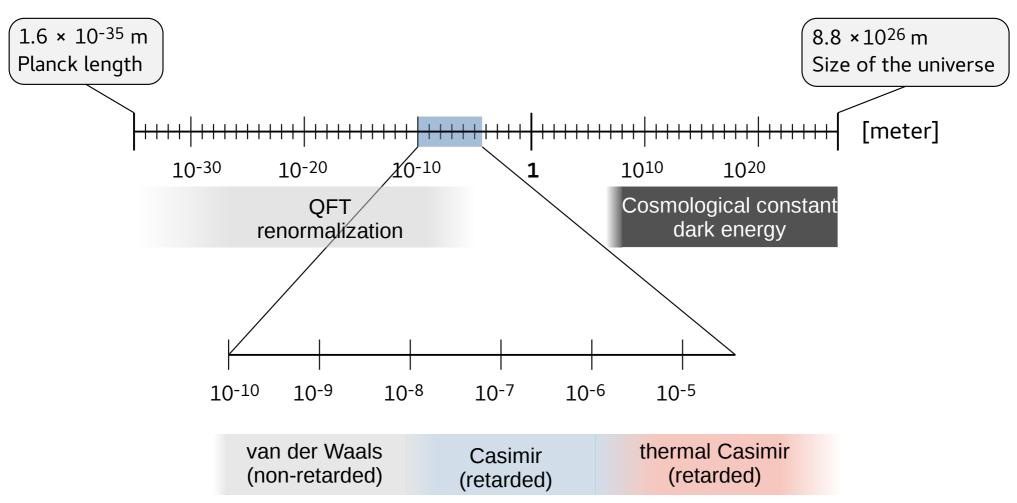
**Cutoff at the Planck length:** 

$$\lambda_c \to 2\pi/\ell_P$$



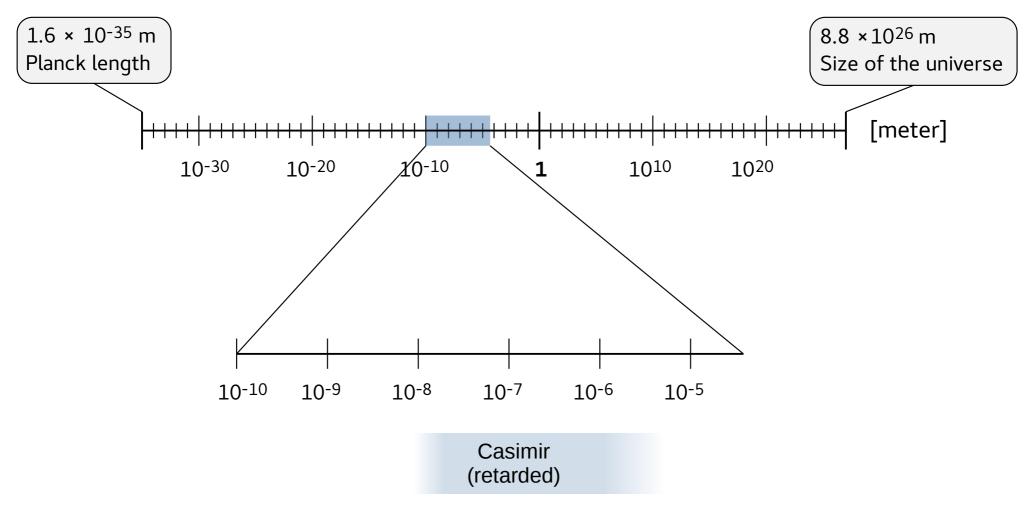
# Vacuum energy at different scales

#### Scale of the universe:



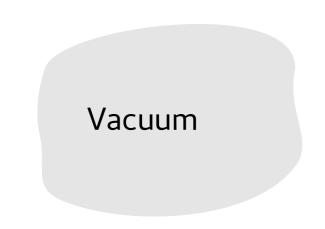
# Small surface separations: Casimir effect

#### Scale of the universe:



#### The Casimir effect in a nutshell

#### Intuitive:

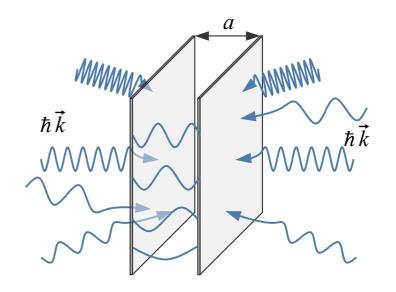


continuous spectrum

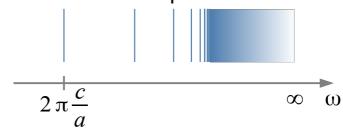


Energy:  $E_{vac} = \infty$ 

Difference:  $E_{||} - E_{vac} < 0$  finite



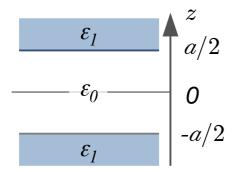
discrete spectrum



$$E_{||} = \infty$$

#### The Casimir effect in a nutshell

#### Reality (simplest possible case):



- materials with dielectric functions  $\varepsilon_r(\omega)$
- extrapolate to zero frequency

$$\varepsilon_r(\omega) = \varepsilon_0 - \frac{\omega_p^2}{\omega^2 + i\gamma\omega}$$

 need to Wick-rotate by using the Kramers-Kronig relation

$$\varepsilon(i\xi) = 1 + \frac{2}{\pi} \int_0^\infty d\omega \frac{\omega \operatorname{Im} \varepsilon_r(\omega)}{\omega^2 + \xi^2}$$

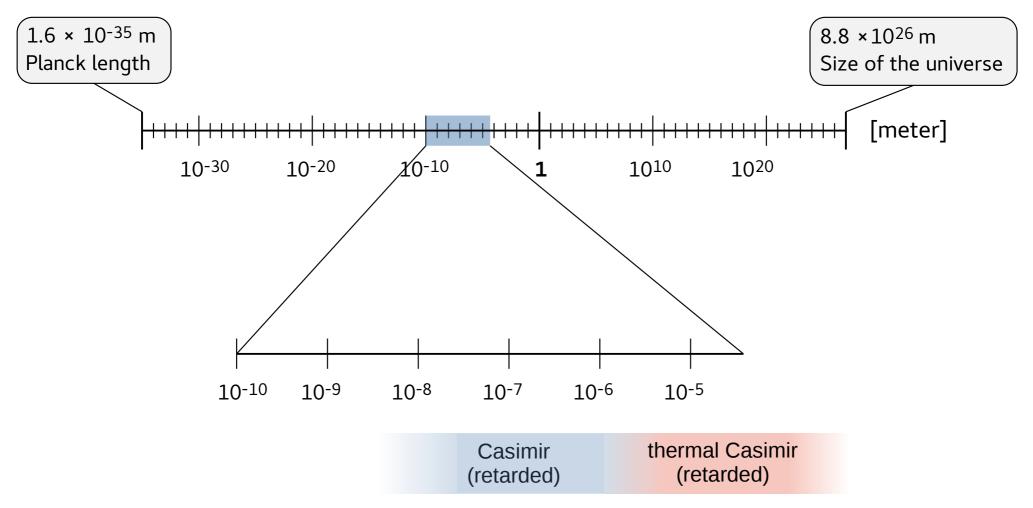
• Compute the energy (force): Lifshitz equation

$$\frac{E_{||}(a)}{A} = \frac{\hbar}{(2\pi)^2 c^2} \int_{1}^{\infty} dp \int_{0}^{\infty} d\xi \, p\xi^2 \left[ \ln \frac{\Delta_{\perp}(i\xi, a)}{\Delta_{\perp, \infty}(i\xi)} + \ln \frac{\Delta_{||}(i\xi, a)}{\Delta_{||, \infty}(i\xi)} \right], \quad F(a) = -\frac{\partial E_{||}(a)}{\partial a}$$

$$\frac{\Delta_{\perp}(p, i\xi, a)}{\Delta_{\perp, \infty}(p, i\xi)} = 1 - \left(\frac{K_1 \varepsilon_0(i\xi) - K_0 \varepsilon_1(i\xi)}{K_1 \varepsilon_0(i\xi) + K_0 \varepsilon_1(i\xi)}\right)^2 e^{-2a\frac{\xi}{c}K_0}, \quad K_j(p, i\xi) = \sqrt{p^2 - 1 + \varepsilon_j(i\xi)}$$

# Large surface separations: Thermal Casimir effect

#### Scale of the universe:



### More fundamental: The nature of virtual photons

#### Dissipation at zero frequency or not? Drude vs. plasma debate

$$\begin{array}{ccc} \text{Drude} & \text{plasma} \\ \varepsilon_r(\omega) = \varepsilon_0 - \frac{\omega_p^2}{\omega^2 + \mathrm{i} \gamma \omega} & \varepsilon_r(\omega) = \varepsilon_0 - \frac{\omega_p^2}{\omega^2} & \gamma & \text{relaxation frequency} \\ & & & & & & & & & & & \\ \end{array}$$

- Recent data suggests: No dissipation for virtual photons (short distance)!
  Bimonte et al, Phys. Rev. B 93, 184434 (2016)

  - Situation at large distance ( $\gtrsim 2 \mu m$ ) unclear

### More fundamental: The nature of virtual photons

#### Dissipation at zero frequency or not? Drude vs. plasma debate

Drude 
$$\varepsilon_r(\omega) = \varepsilon_0 - \frac{\omega_p^2}{\omega^2 + \mathrm{i} \gamma \omega}$$

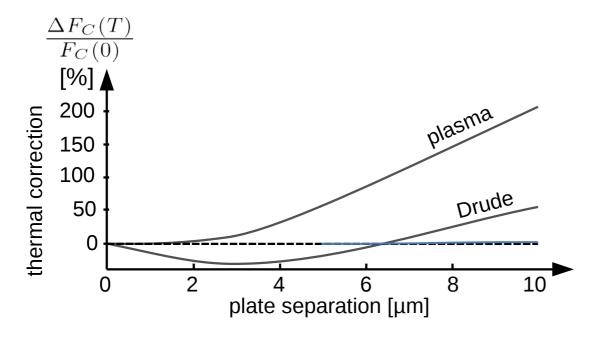
plasma 
$$\varepsilon_r(\omega) = \varepsilon_0 - \frac{\omega_p^2}{\omega^2}$$

plasma frequency relaxation frequency (dissipation)

- Recent data suggests: No dissipation for virtual photons (short distance)!
  Bimonte et al, Phys. Rev. B 93, 184434 (2016)

  - Situation at large distance ( $\geq 2 \mu m$ ) unclear

#### What is different at larger separation?



At *d*>10 μm less than 10<sup>-7</sup> N/m<sup>2</sup>

### Only possible with parallel plates.

M.. Bordag et al "Advances in the Casimir effect", Oxford Science Publications, (2009).

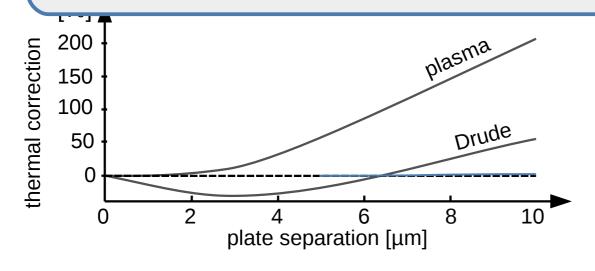
Review: Klimchitskaya et al., Int. J. Mod. Phys. Conf. Ser. 3(2011), 515

# More fundamental: The nature of virtual photons

Dissipation at zero frequency or not? Drude vs. plasma debate

# **CANNEX Task List:**

1. Force/Gradient measurements at separation >6 μm, vacuum, accuracy ~1pN/0.1 μN/m



At *d*>10 μm less than 10<sup>-7</sup> N/m²

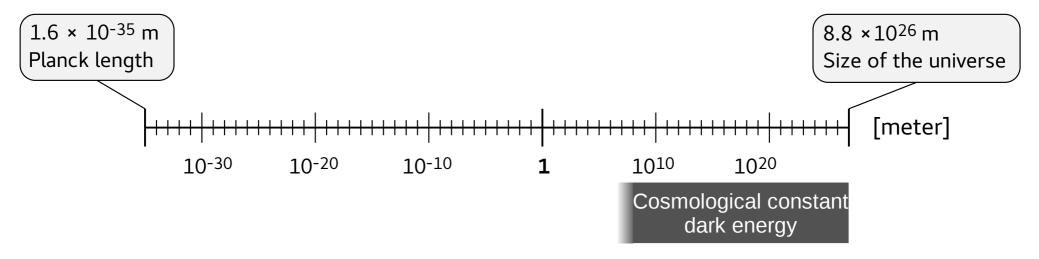
# Only possible with parallel plates.

M.. Bordag et al "Advances in the Casimir effect", *Oxford Science Publications*, (2009).

Review: Klimchitskaya *et al*, Int. J. Mod. Phys. Conf. Ser. **3**(2011), 515

### Very large scales: 1 AE to the size of the universe

#### Scale of the universe:



### Very large scales: 1 AE to the size of the universe

#### dark matter

indication: grav. pull theory: unknown contents: unknown

part: 27%

#### dark energy

indication: acceleration

theory: unknown contents: unknown

part: 68%



#### visible universe

indication: em radiation, gravity

theory:  $\mathcal{L}_{\mathrm{SM}}$ 

contents: particles of the SM

part: 5%

#### proposition:

add a new scalar particle with Yukawa coulings

J. Khoury and A.Weltman,

Phys. Rev. Lett. 93 (2004) 171104

#### **New dynamics:**

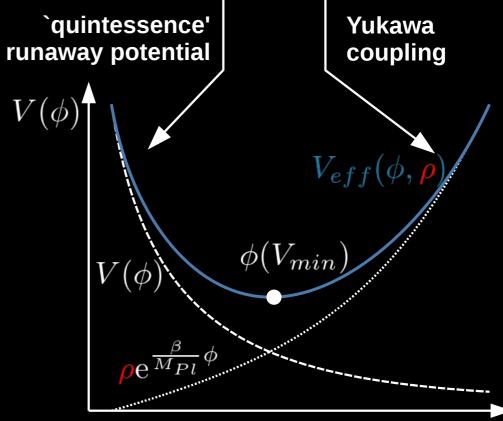
$$\mathcal{L}_{\phi} = \sqrt{-g} \left[ \mathcal{R} \frac{M_{Pl}^2}{2} - \frac{(\partial \phi)^2}{2} - V(\phi) \right]$$

#### Yukawa couplings:

$$\mathcal{L}_{EM} = \frac{-e^{\frac{\beta_{\gamma}}{M_{Pl}}\phi}}{4} F_{\mu\nu} F^{\mu\nu}$$

**Result 1: effective potential** 

$$V_{eff} = V(\phi) + \rho e^{\frac{\beta}{M_{Pl}}\phi}$$



#### **New dynamics:**

$$\mathcal{L}_{\phi} = \sqrt{-g} \left[ \mathcal{R} \frac{M_{Pl}^2}{2} - \frac{(\partial \phi)^2}{2} - V(\phi) \right]$$

#### Yukawa couplings:

$$\mathcal{L}_{EM} = \frac{-e^{\frac{\beta_{\gamma}}{M_{Pl}}\phi}}{4} F_{\mu\nu} F^{\mu\nu}$$

**Result 1: effective potential** 

**Result 2: `Newtonian' potential:** 

$$V_{eff} = V(\phi) + \rho e^{\frac{\beta}{M_{Pl}}\phi}$$

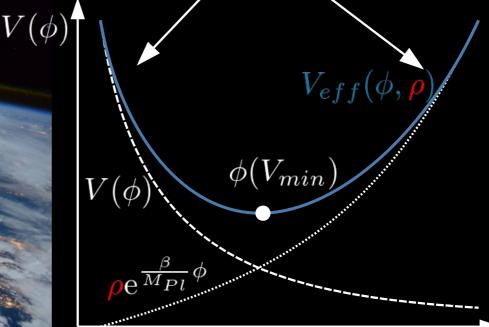
$$V(r) \propto \beta \frac{M}{M_{Pl}} \frac{\mathrm{e}^{-\sqrt{\partial V_{eff}(\rho)/\partial \phi^2}r}}{r}$$

`quintessence' runaway potential

Yukawa coupling

 $\rho \ll 1 \Rightarrow$  strong interaction





#### **New dynamics:**

$$\mathcal{L}_{\phi} = \sqrt{-g} \left[ \mathcal{R} \frac{M_{Pl}^2}{2} - \frac{(\partial \phi)^2}{2} - V(\phi) \right]$$

#### Yukawa couplings:

$$\mathcal{L}_{EM} = \frac{-e^{\frac{\beta_{\gamma}}{M_{Pl}}\phi}}{4} F_{\mu\nu} F^{\mu\nu}$$

**Result 1: effective potential** 

**Result 2: `Newtonian' potential:** 

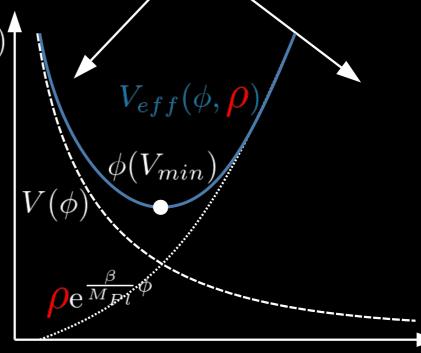
$$V(r) \propto \beta \frac{M}{M_{Pl}} \frac{\mathrm{e}^{-\sqrt{\partial V_{eff}(
ho)/\partial \phi^2 r}}}{r}$$

$$V_{eff} = V(\phi) + \rho e^{\frac{\beta}{M_{Pl}}\phi}$$

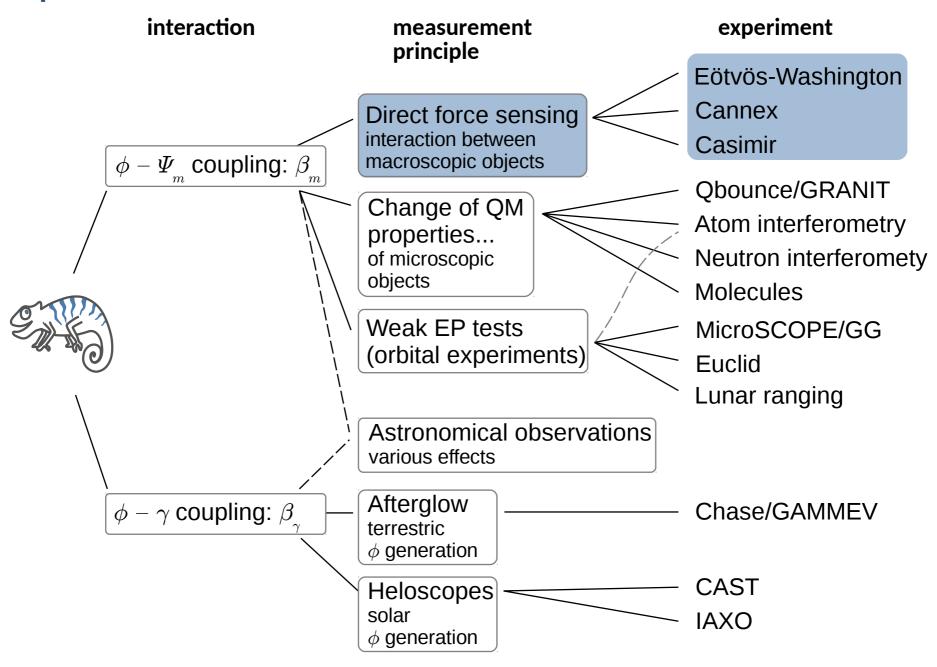
`quintessence' runaway potential Yukawa coupling

Adaptivity: Chameleon force





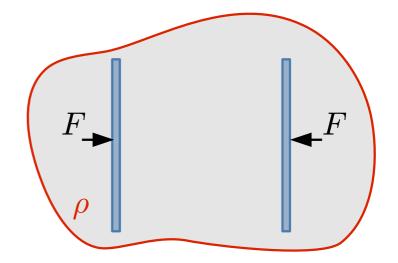
# Prospects for chameleon detection



#### **Principle:**

Measure at **constant plate separation** the change in the force for **different gas density**  $\rho$  Brax, van de Bruck, Davis, Shaw, Iannuzzi, *PRL.* **104,** 241101(2010)

$$F(\rho) = F_{ES} + F_C + F_G$$
$$\Delta F(\rho) = F(\rho) - F(0)$$

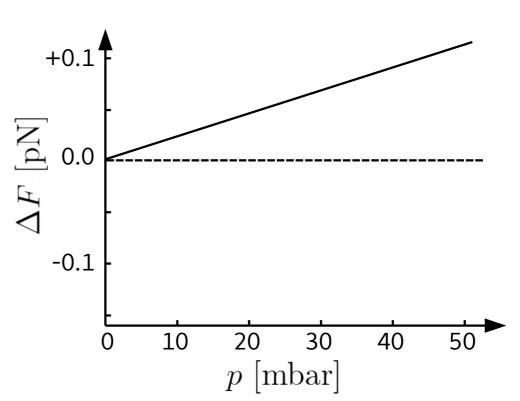


#### **Assumptions:**

- Xe gas
- plate area 1 cm<sup>2</sup>

• 
$$V(\phi) = \Lambda^4 \left( 1 + \frac{\Lambda^n}{\phi^n} \right)$$

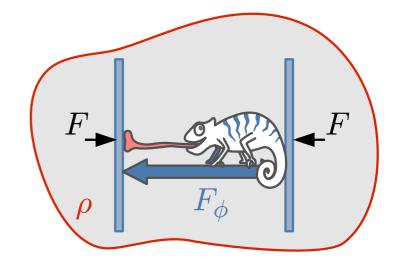
•  $\Lambda=$  2.4 meV



#### **Principle:**

Measure at **constant plate separation** the change in the force for different gas density  $\rho$ Brax, van de Bruck, Davis, Shaw, Iannuzzi, PRL. 104, 241101(2010)

$$F(\rho) = F_{ES} + F_C + F_G + F_{\phi}$$
$$\Delta F(\rho) = F(\rho) - F(0)$$

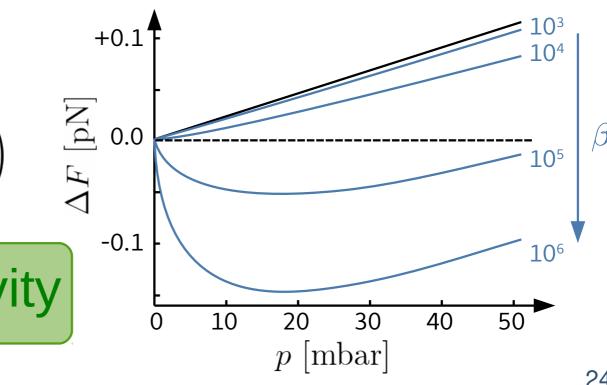


#### **Assumptions:**

- Xe gas
- plate area 1 cm<sup>2</sup>

• 
$$V(\phi) = \Lambda^4 \left( 1 + \frac{\Lambda^n}{\phi^n} \right)$$

•  $\Lambda=$  2.4 meV

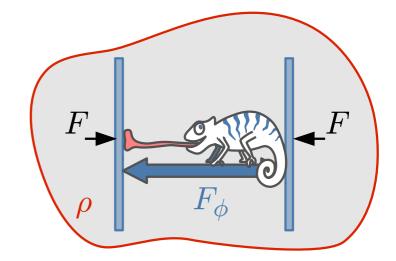


high sensitivity

#### **Principle:**

Measure at **constant plate separation** the change in the force for different gas density  $\rho$ Brax, van de Bruck, Davis, Shaw, Iannuzzi, PRL. 104, 241101(2010)

$$F(\rho) = F_{ES} + F_C + F_G + F_{\phi}$$
$$\Delta F(\rho) = F(\rho) - F(0)$$



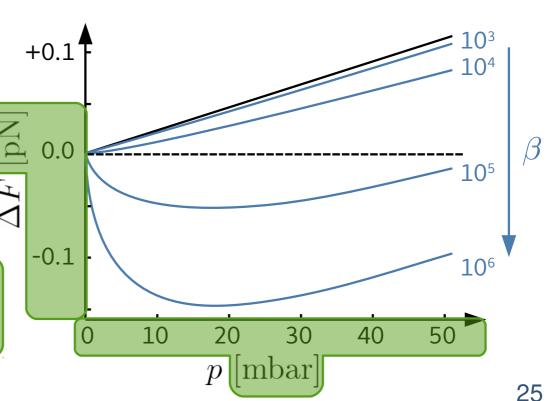
#### **Assumptions:**

- Xe gas
- plate area 1 cm<sup>2</sup>

• 
$$V(\phi) = \Lambda^4 \left( 1 + \frac{\Lambda^n}{\phi^n} \right)$$

•  $\Lambda=$  2.4 meV





# **CANNEX Task List:**

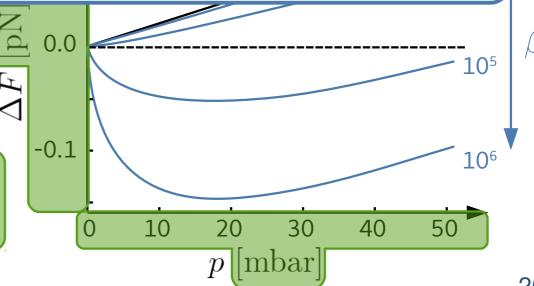
- 1. Force/Gradient measurements at separation >6 μm, vacuum, accuracy ~1pN/0.1 μN/m
- 2. Force measurements at constant separation, modulated gas density, precision <0.1 pN

piate area 1 cm²

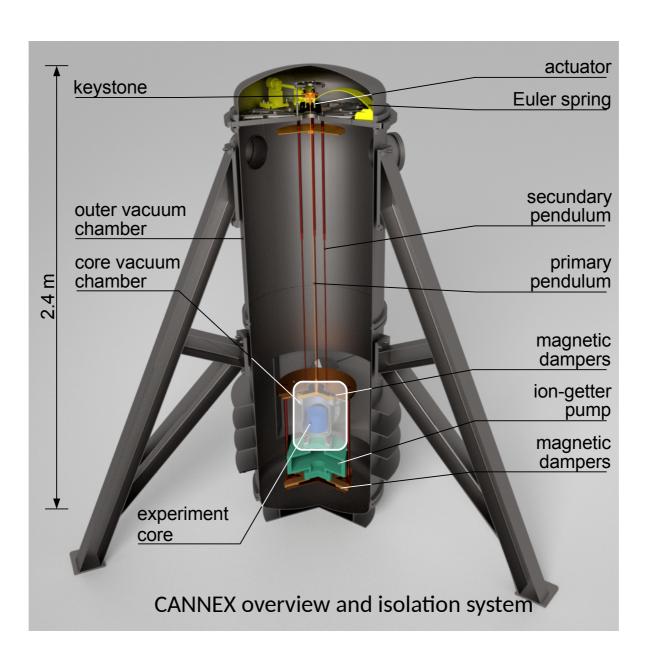
• 
$$V(\phi) = \Lambda^4 \left( 1 + \frac{\Lambda^n}{\phi^n} \right)$$

•  $\Lambda=$  2.4 meV





# Setup (located at VU Amsterdam)

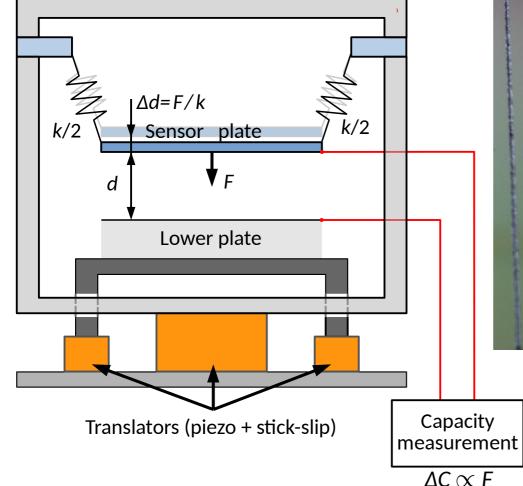


# Force detection (one year ago)

Principle:

Implementation: upper plate (sensor)

Measure capacitively the displacement of a spring.



Custom-fabricated Silicon membrane

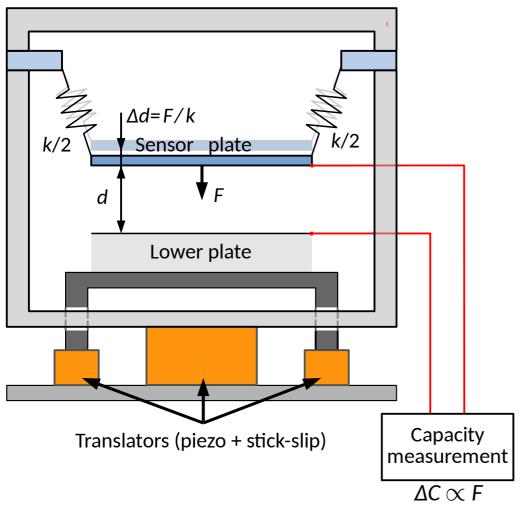
Force constant:  $0.22\pm0.02$  N/m Disk area:  $1.0834\pm0.0005$  cm<sup>2</sup>

Waviness(disk) < 15 nm (whole area)

# Force detection

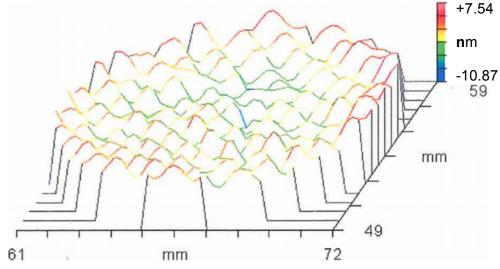
### Principle:

Measure optically the displacement of a spring.



Implementation lower plate:





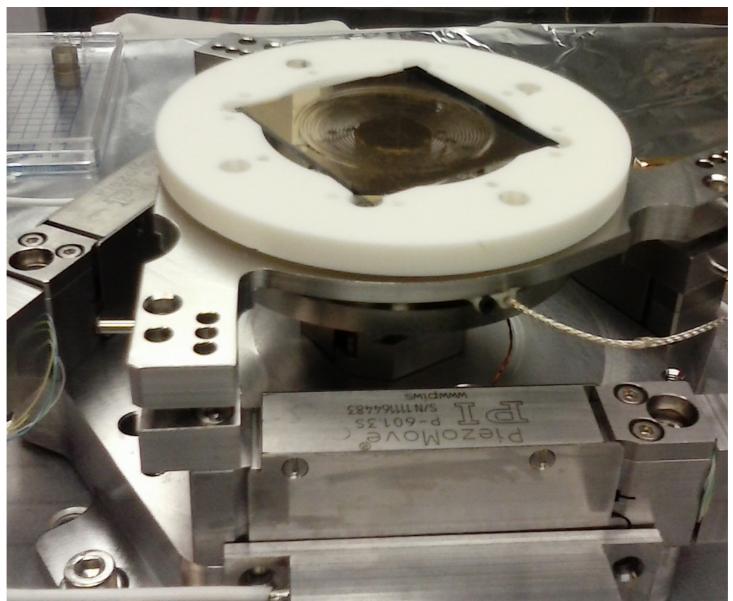
Custom-fabricated SiO<sub>2</sub> disk

Thickness 6 mm
Disk area 1 cm<sup>2</sup>

Waviness(disk) < 18 nm (whole area)

# Force detection

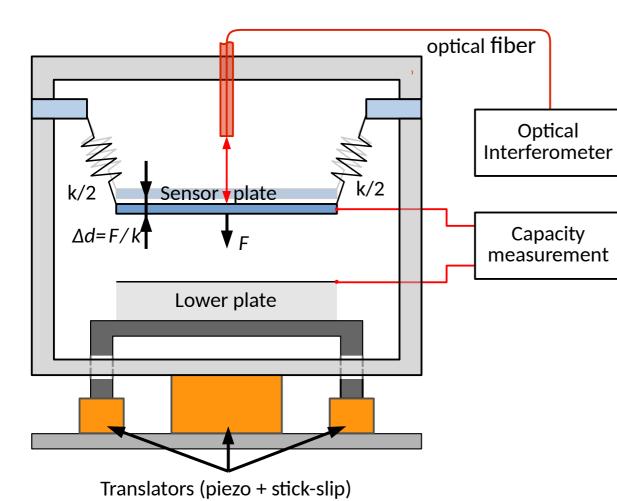
Implementation: core



# Force detection

### Principle:

optically Measure capacitively the displacement of a spring.



#### **Casimir:**

resonance frequency shift

$$\omega_0 = \sqrt{\frac{k}{m} - \frac{1}{m} \frac{\partial F(d)}{\partial d}}$$

#### **Chameleon:**

adiabatic pressure modulation

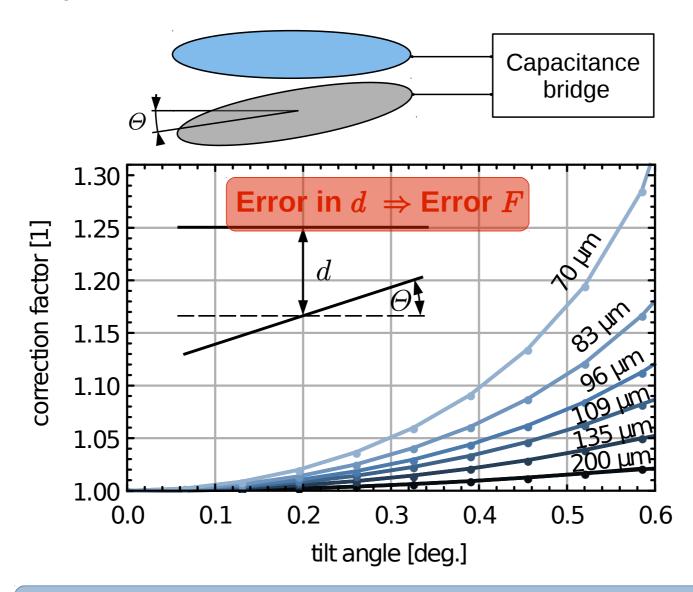
$$\Delta F_{\phi} \approx \frac{\partial F_{\phi}(p)}{\partial p} \Delta p$$

#### **Homodyne detection**

→ Able to measure below the thermal noise level

# Parallelism: Importance

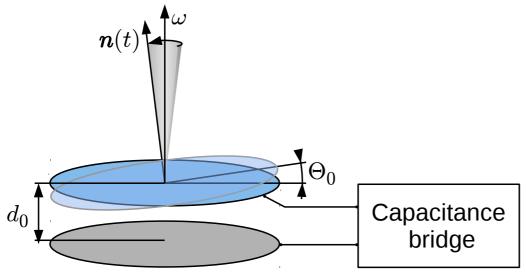
parallel plates with small tilt  $\Theta$ 



Target 0.1 pN: max deviation 0.1 µrad

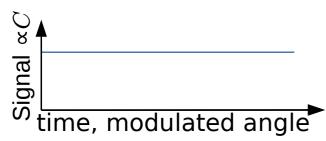
# Parallelism control: Principle

assume: parallel plates



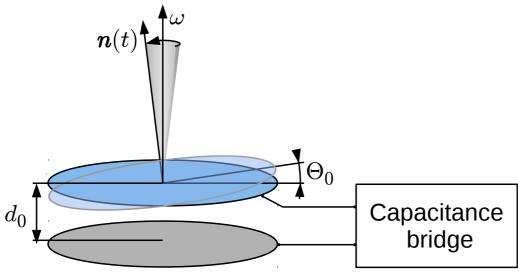
$$\Theta(t) = \Theta_0 = \text{const.}$$

$$C(t) = \varepsilon_0 \frac{R^2 \pi}{d} \left[ 1 + \left( \frac{R}{2d} \Theta(t) \right)^2 \right] + \mathcal{O}\left(\Theta(t)^4\right)$$

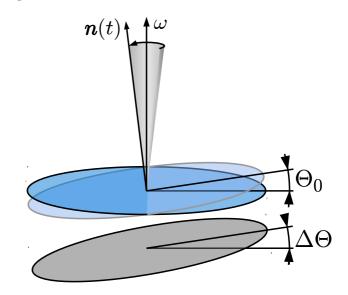


# Parallelism control: Principle

#### assume: parallel plates



#### plates with relative tilt $\Delta\Theta$



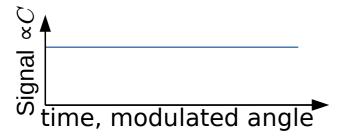
$$\Theta(t) = \Theta_0 = \text{const.}$$

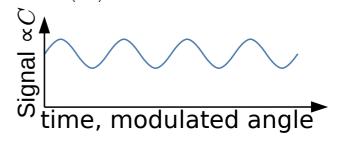
$$C(t) = \varepsilon_0 \frac{R^2 \pi}{d} \left[ 1 + \left( \frac{R}{2d} \Theta(t) \right)^2 \right] + \mathcal{O}\left(\Theta(t)^4\right)$$

$$\Theta(t) = \Theta_0 = \text{const.}$$

$$\Theta(t) = \Theta_0 + \Delta\Theta \cos \omega t$$

$$C(t) = \varepsilon_0 \frac{R^2 \pi}{d} \left[ 1 + \left( \frac{R}{2d} \Theta(t) \right)^2 \right] + \mathcal{O}\left(\Theta(t)^4\right) \quad C(t) \approx \varepsilon_0 \frac{R^2 \pi}{d} \left( 1 + \left( \frac{R}{2d} \right)^2 \left(\Theta^2 + \Delta\Theta^2 + 2\Theta\Delta\Theta \cos \omega t \right) \right]$$





Idea: Use feedback circuit to compensate  $\Delta\Theta$ 

# Parallelism control: Performance

### Proof of principle/preliminary results

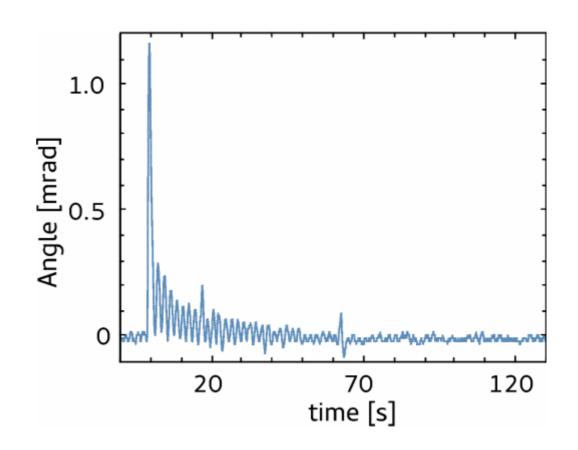
#### **Step response**

under very bad conditions

- First test
  - in air
  - without anti-vibration
  - with thick testing plates
- 6 μm single-sided step
- nominal distance 90 µm

#### **Long-term stability**

- Same conditions
- 3 µrad(RMS)



#### **Target**

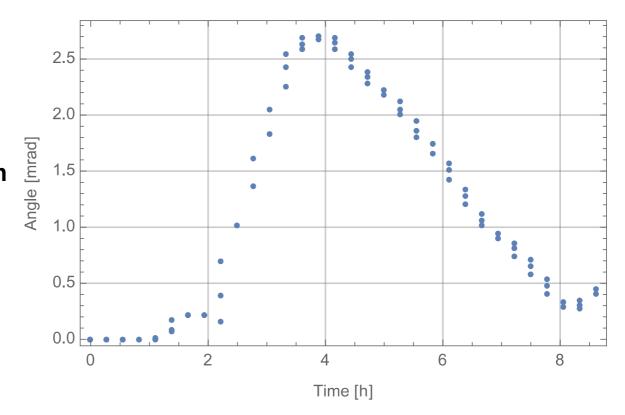
- Assumptions: vacuum, anti-vibration
- 0.1 µrad (~1 nm total tilt)

# Parallelism control: Performance

### Proof of principle/preliminary results

#### **Practical operation**

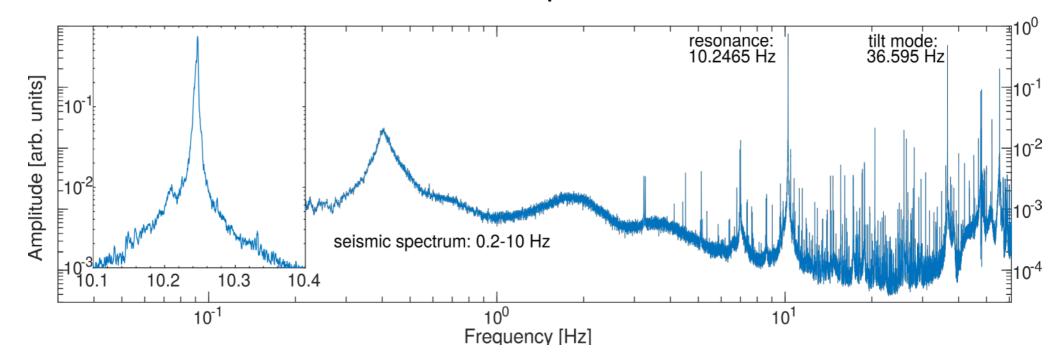
- · Works as expected
- currently
   ~200 μrad long term



**Limiting factor: Vibrations, Drift** 

### Force detection

### Sensor characterization: noise spectrum



#### Custom-fabricated Silicon membrane

Force constant: 0.22±0.02 N/m

Eigenfrequency:  $10.2465 \text{ Hz} \pm 0.1 \text{ mHz}$ 

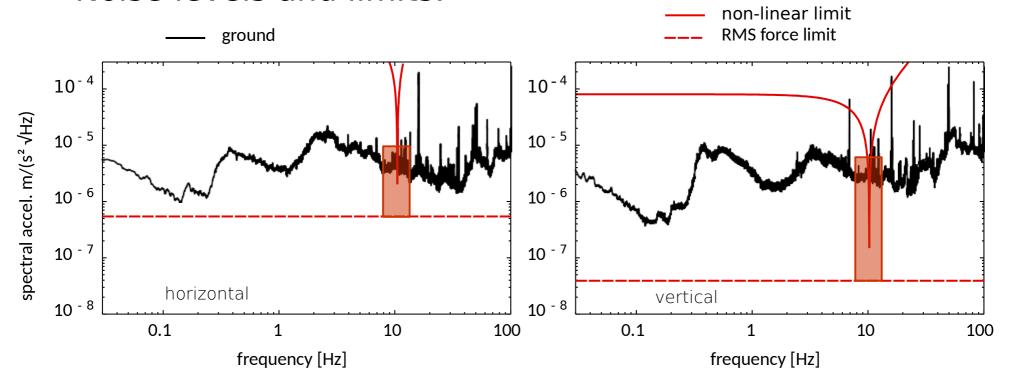
Q-factor: 5 k—15 k

Disk area:  $1.0834\pm0.0005$  cm<sup>2</sup>

Waviness(disk) < 15 nm (whole area)

# Vibrations 1: The background

### Noise levels and limits:



#### 2 limits:

**1:** non-linearities: 
$$F(d + \delta d) \approx F(d) + \delta d\partial_d F(d) + 1/2 \delta d^2 \partial_d^2 F(d)$$

2: equivalent RMS noise: 
$$\delta a_{n,RMS}(F) \gtrsim \int_{f_0 - f_{BW}/2}^{f_0 + f_{BW}/2} \delta a_n \approx \sqrt{f_{BW}} \delta a_n(f_0)$$
 f<sub>BW</sub> < 0.1 pN @ d=10 µm

f<sub>BW</sub> ~ 5 mHz

# Vibrations 2: The unlucky first system

single

### **Vertical seismic:**

- GAS\* filter
- $_{ullet}$  active  $\mathcal{H}_{\infty}$  feedback

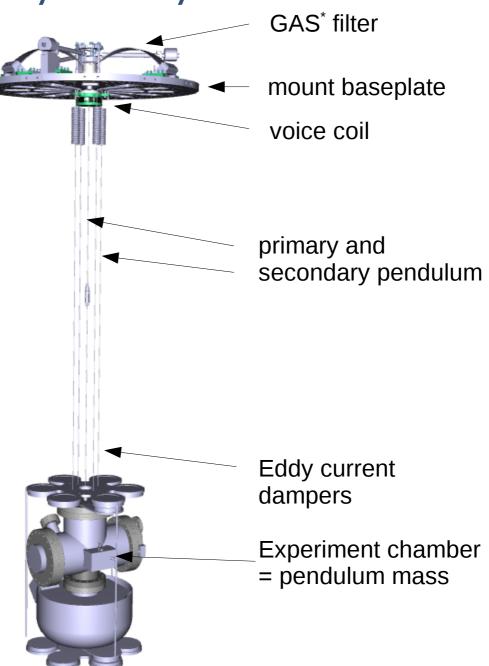
still missing

#### **Horizontal seismic:**

- double-pendulum
- Eddy current dampers

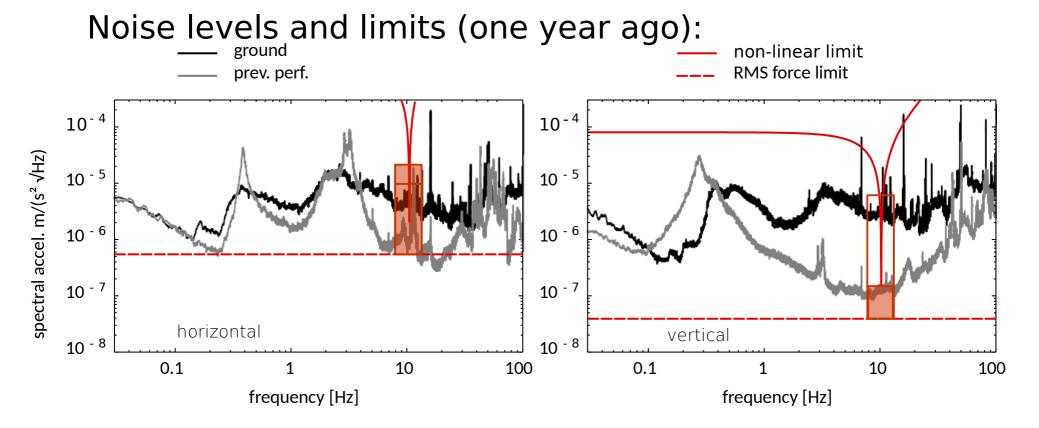
#### **Acoustic:**

 rigid all-enclosing vacuum chamber 10<sup>-5</sup> mbar (not shown)



\*Geometric anti-spring

# Vibrations 2: The unlucky first system



New problem: resonances

⇒ Could not approach

separations  $< 50 \mu m$ 

### Vibrations 3: The hopeful update:

#### **Vertical seismic:**

- GAS\* filter (Euler springs)
- active feedback

#### **Horizontal seismic:**

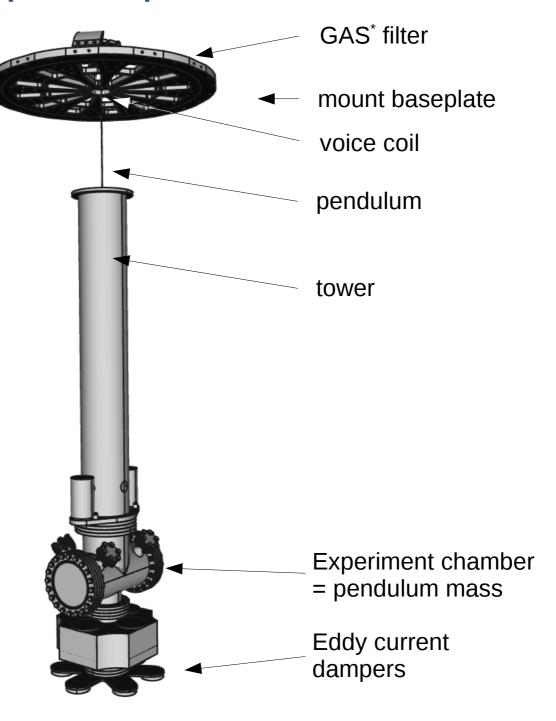
- single-pendulum thinner wire
- Eddy current dampers

#### **Tilt seismic:**

- tower on core chamber
- Eddy current dampers

#### **Acoustic:**

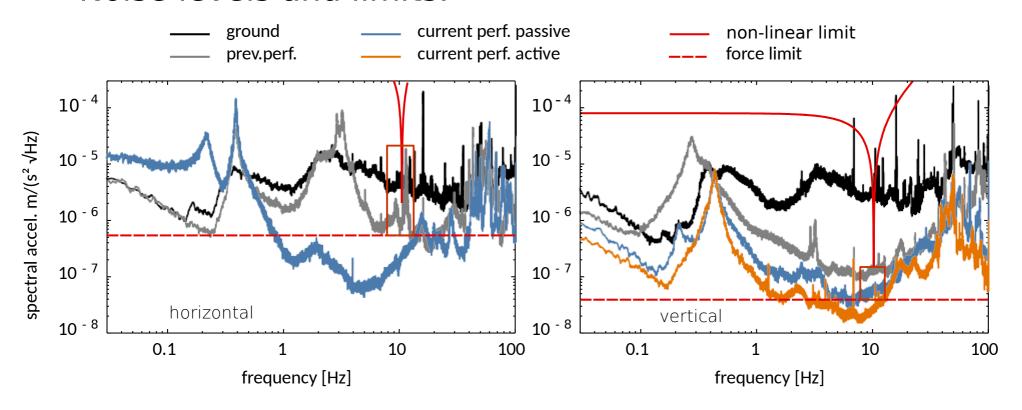
 rigid all-enclosing vacuum chamber 10<sup>-5</sup> mbar (not shown)



<sup>\*</sup>Geometric anti-spring

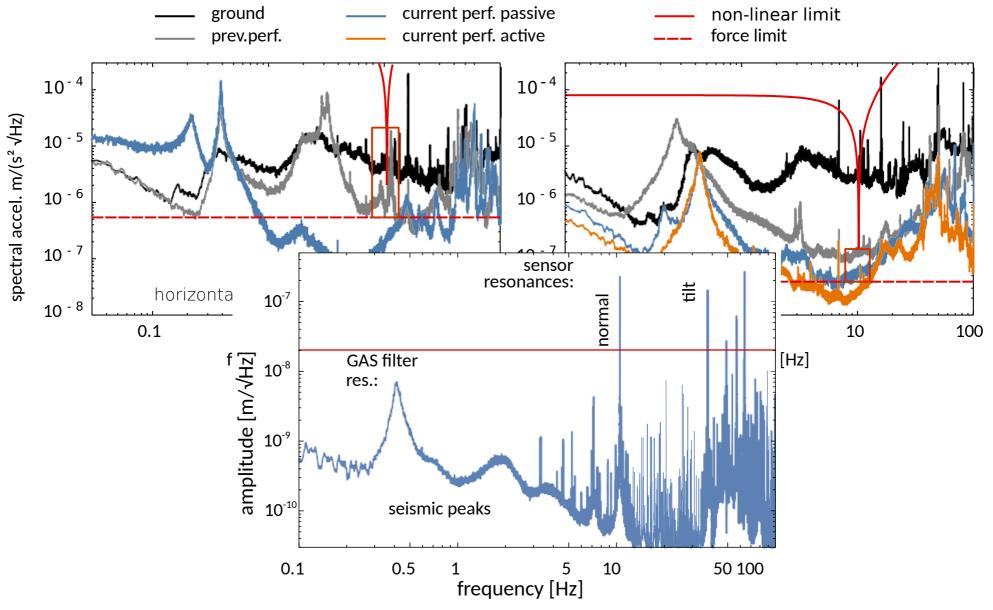
# Vibrations 3: The hopeful update

### Noise levels and limits:



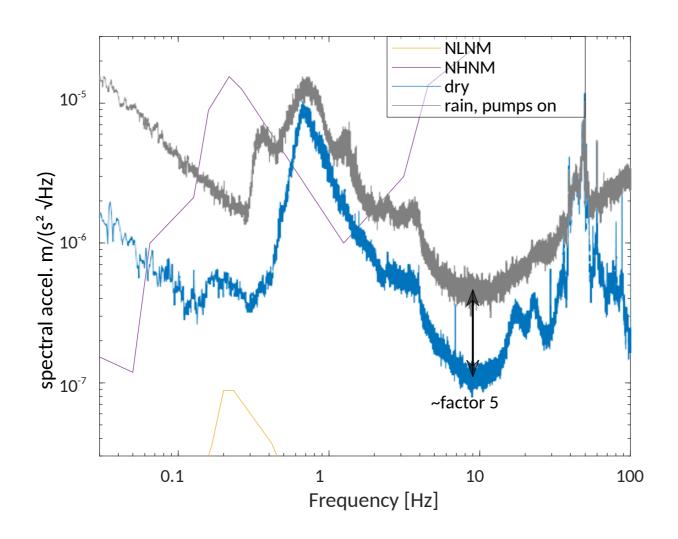
# Vibrations 3: The hopeful update

### Noise levels and limits:

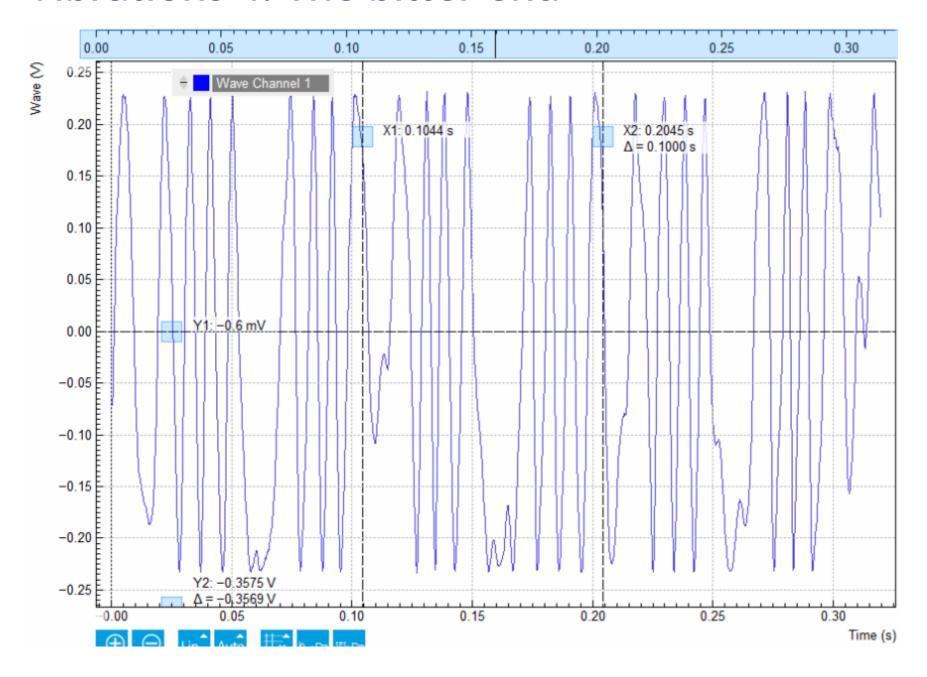


Still an improvement of 30 required (depending on the background)

# Vibrations 4: The bitter end



### Vibrations 4: The bitter end



# Remote operation

Setup completely automized.

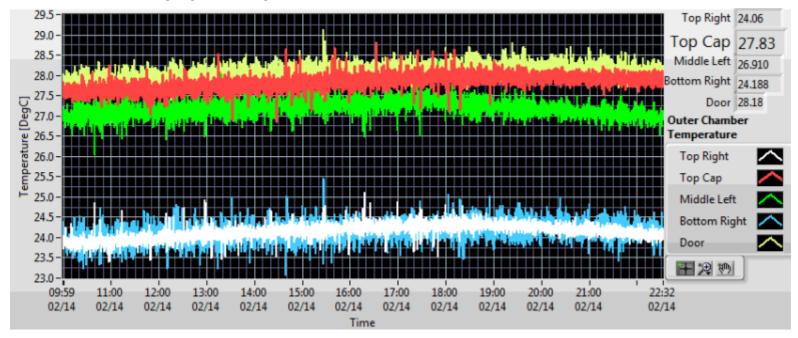
Data acquisition without physical access to the setup. What can go wrong?

# Remote operation

### Setup completely automized.

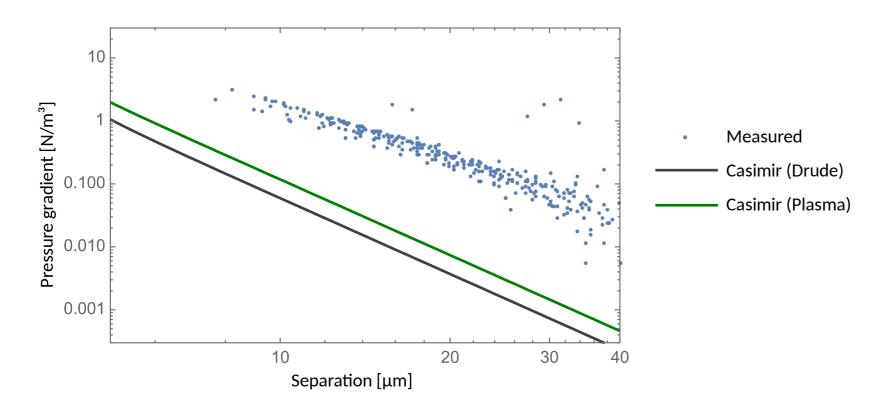
Data acquisition without physical access to the setup. What can go wrong?

Rain water pipe rupture → Lab flooded → Thermal controls broken



Required stability (sensor spring constant) in sensor spring constant: < 10 mKActual stability  $\sim 500 \text{ mK}$ 

# However, there is hope



First evaluation. Preliminary!

#### **Calibrated / Measured Parameters**

Parallelism (calibrated): < 200 µrad

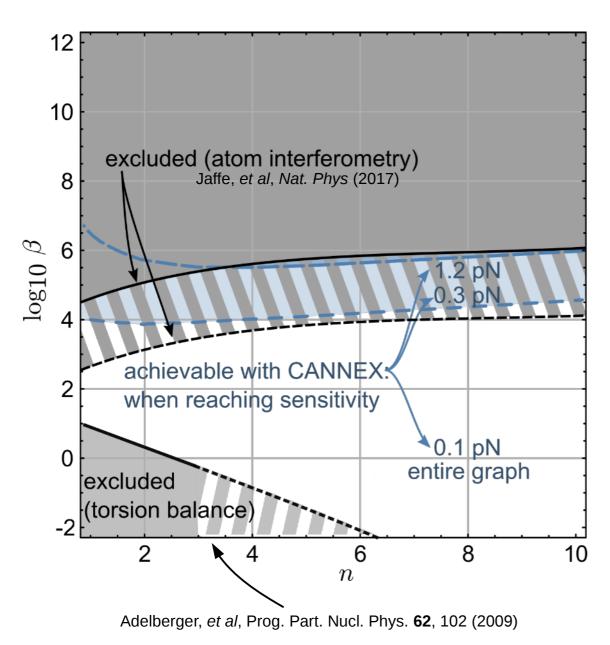
Residual electrostatic potential:  $< 8 \mu V$ 

Drift < 500 nm/h

Total thermal drift error  $< 2.5 \mu m/run$ 

### What could we reach?

### New limits...



### **Assumptions:**

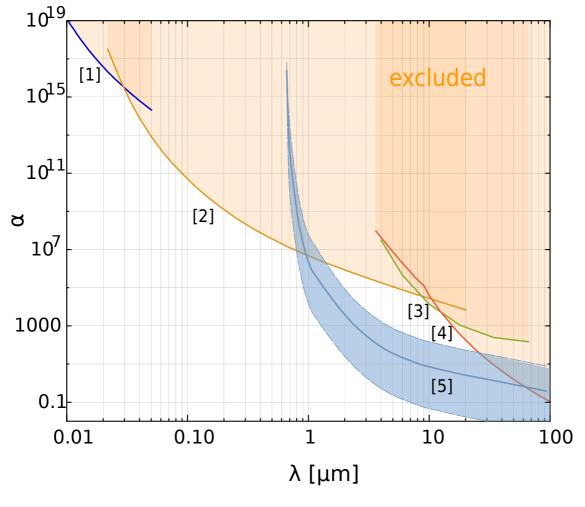
- $V(\phi) = \Lambda^4 \left( 1 + \frac{\Lambda^n}{\phi^n} \right)$
- Active vibration insulation
   > 30dB at 1 Hz
- Sensitivity limited only by
  - 1) Brownian sensor noise
  - 2) C-bridge electronic noise

# Room for improvements:

- Even better vibration insulation (6 axis, two-staged)
- Optical readout
- Sensor design with larger mass

### What could we reach?

### New limits possible... $\alpha = 2\beta^2$ $\lambda = m_{\phi}^{-1}$



- [1] Sushkov et al, PRL **107**, 171101 (2011)
- [2] Chen et al, PRL, **116**, 221102 (2016)
- \_\_ [3] Gerarci er al, PRD 78, 022002 (2008)
  - \_ [4] Kapner et al, *PRL*, **98**, 021101 (2007)
- [5] Cannex (estimated) d=10 μm, 0.1pN

### **Assumptions:**

• 
$$V(\phi) = -G \frac{m_1 m_2}{d} \left( 1 + \alpha e^{-d/\lambda} \right)$$

- Sensitivity limited only by
  - 1) Brownian sensor noise
  - 2) C-bridge electronic noise
- PRELIMINARY!

Room for improvements:

- Even better vibration insulation (6 axis, two-staged)
- 3 interferometer optical readout
- Sensor design with larger mass

### **Outlook & Conclusion**

#### **Refurbished Cannex:**



#### **Improvements:**

6 axis active feedback system to cancel resonances

Fully optical measurements

Pressure modulation system



#### **Measurements:**

Frequency shift force measurements 10-30 µm, 1 pN

Pressure modulation measurement at 10 µm, 0.1 pN



#### **Possible Results:**

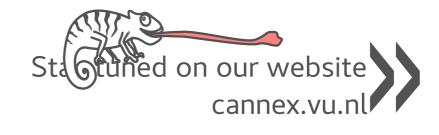
Exclusion of Chameleon forces  $n \le 10$ ,  $\beta > 10^{-2}$ 

Indication if virtual photons behave differently from real ones

Possibly new limits on Yukawa forces

# Acknowledgments

# Thank you for your attention!





VU:

René Sedmik

Lex v. d. Gracht

Rogier Elsinga

Nikhef:

Alessandro Bertolini

Paris Saclay:

Philippe Brax





and







