

**Transverse Effects in the  
Hollow Channel Plasma Accelerator**  
Carl A. Lindstrøm, University of Oslo

CLIC Novel Accelerator Working Group,  
CERN – Oct 13, 2017

# Transverse Effects in the Hollow Channel Plasma Accelerator

CLIC Novel Accelerator Working Group – Oct 13, 2017

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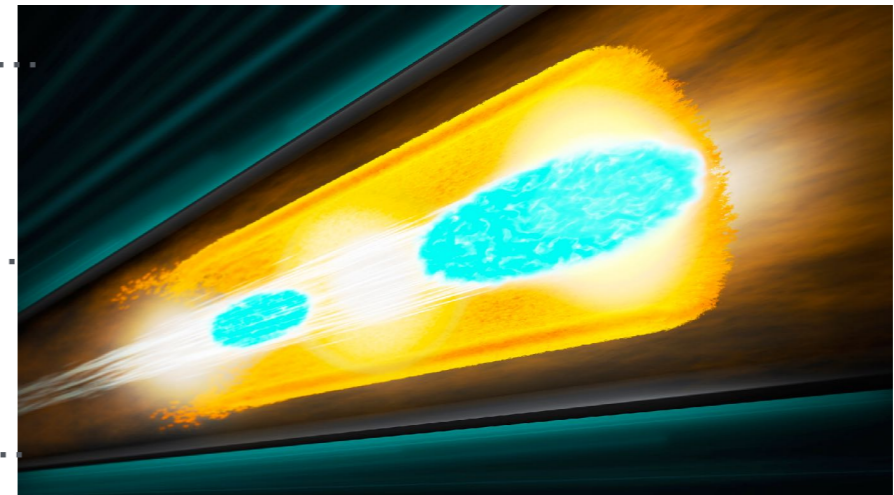
## Why use a hollow channel?

- Bigger picture:
  - If you want an **electron-positron collider**, you need **positron acceleration** (!)
  - You therefore need to charge-symmetrize your technology  
(or make another different, but equally good technology)
- Main reasons for using a hollow plasma channel are

**charge symmetry**  
(works also positrons)

**no focusing fields**  
(no tight beam matching)

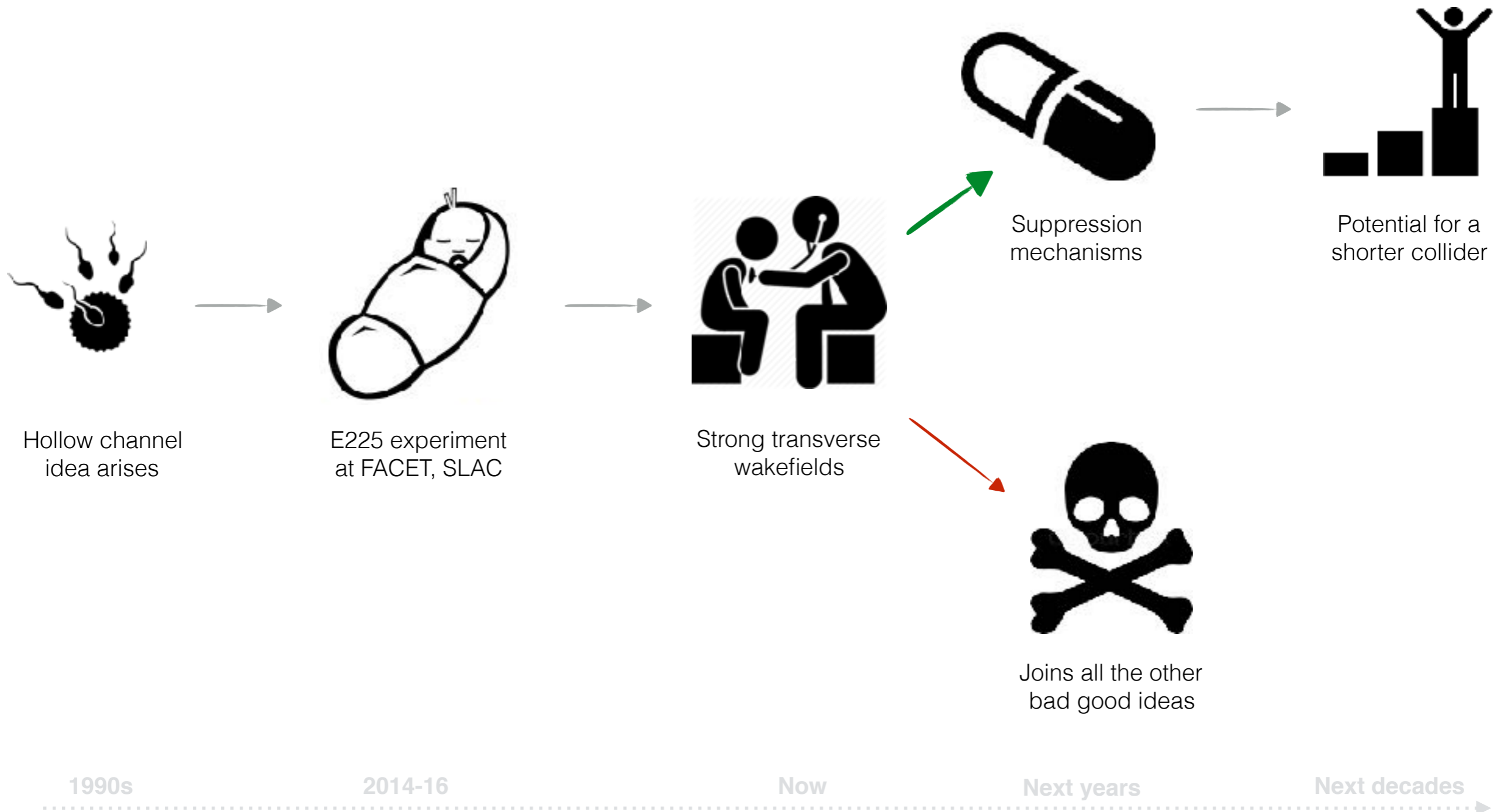
**no structure failure**  
(new channel every time)



- **However**, we soon discover that unless you are perfectly aligned, there is a **strong transverse wakefield**.

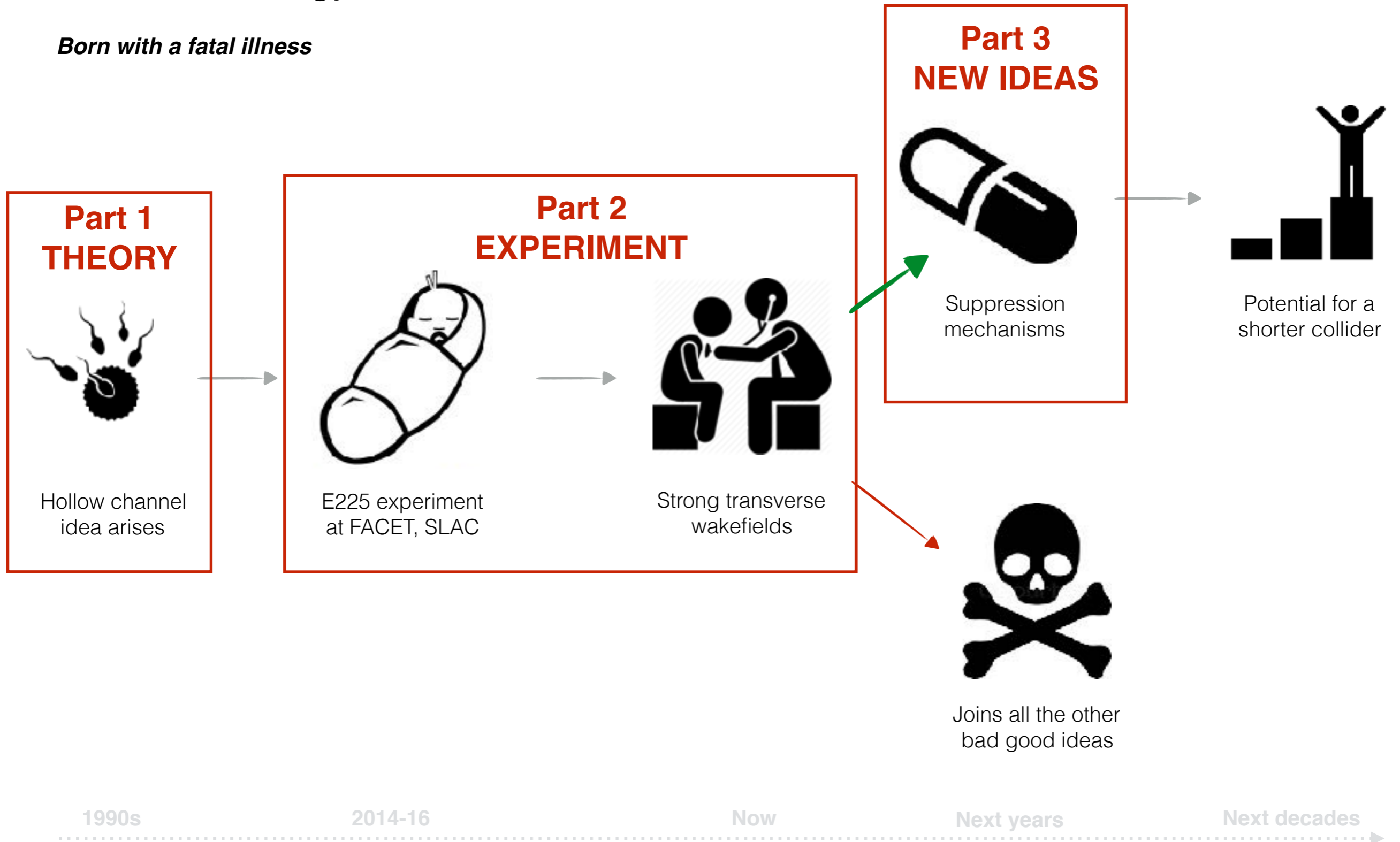
# A useful analogy

## *Born with a fatal illness*



# A useful analogy

*Born with a fatal illness*



# **PART 1: Conception**

Hollow plasma channel  
transverse wakefield theory

# Linear model

- Assume:
  - plasma electrons are not moving (just slightly perturbed)
  - that the plasma behaves as a dielectric medium

- The most significant longitudinal wakefield (for acceleration):

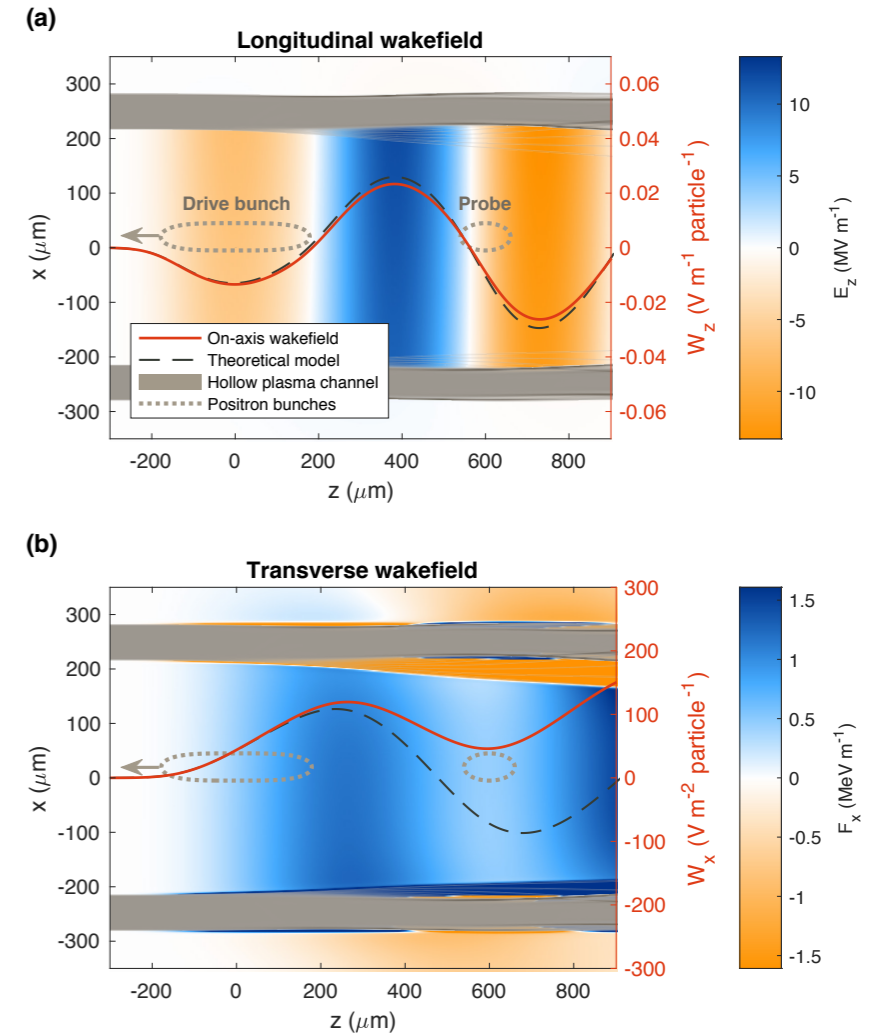
$$W_{z0}(z) = \frac{ek_p\chi_{\parallel}^2}{2\pi\epsilon_0a} \frac{B_{00}(a,b)}{B_{10}(a,b)} \cos(\chi_{\parallel}k_pz)\Theta(z)$$

- The most significant transverse wakefield is a dipole mode:

$$W_{x1}(z) = -\frac{e\Delta x\chi_{\perp}}{\pi\epsilon_0a^3} \frac{B_{11}(a,b)}{B_{21}(a,b)} \sin(\chi_{\perp}k_pz)\Theta(z)$$

- When the response is non-linear, we turn to particle-in-cell (PIC) simulations.

QuickPIC simulation:



$$\chi_{\parallel} = \sqrt{\frac{2B_{10}(a,b)}{2B_{10}(a,b) - k_p a B_{00}(a,b)}}$$

$$\chi_{\perp} = \sqrt{\frac{2B_{21}(a,b)}{4B_{21}(a,b) - k_p a B_{11}(a,b)}}$$

$$B_{ij}(a,b) = I_i(k_p a)K_j(k_p b) + (-1)^{i-j+1} I_j(k_p b)K_i(k_p a)$$

## Comparing numbers to conventional wakefields

- Typical CLIC transverse wakefields per offset in structures:  
 **$\sim 1\text{-}100 \text{ V/pC/m/mm}$**
- Hollow channel (500  $\mu\text{m}$  diameter at  $3 \times 10^{15} \text{ cm}^{-3}$ ):  
 **$\sim 150 \text{ V/m}^2/\text{particle} = \sim 1\,000\,000 \text{ V/pC/m/mm}$**

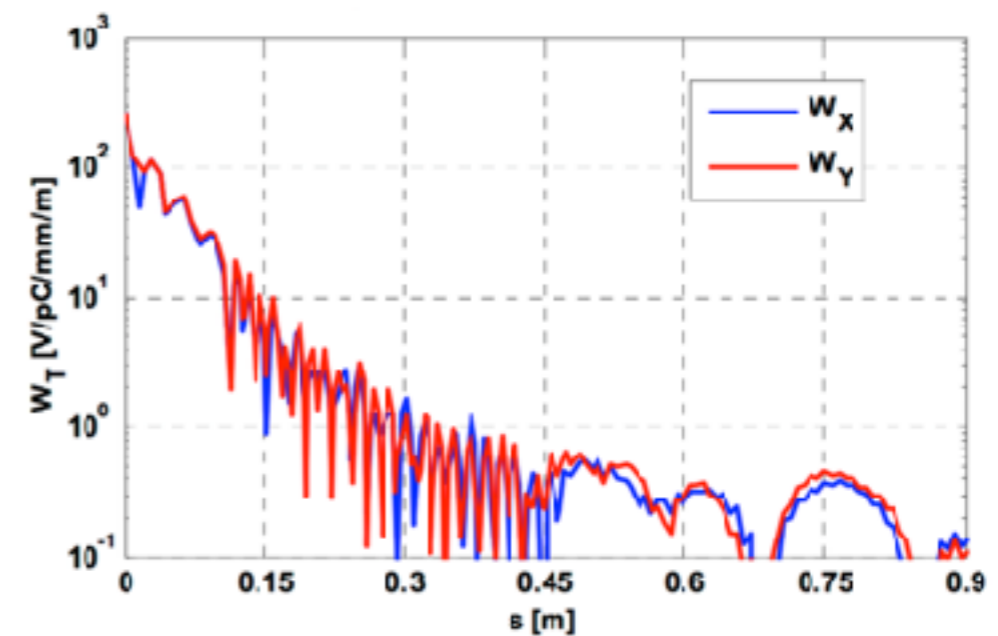
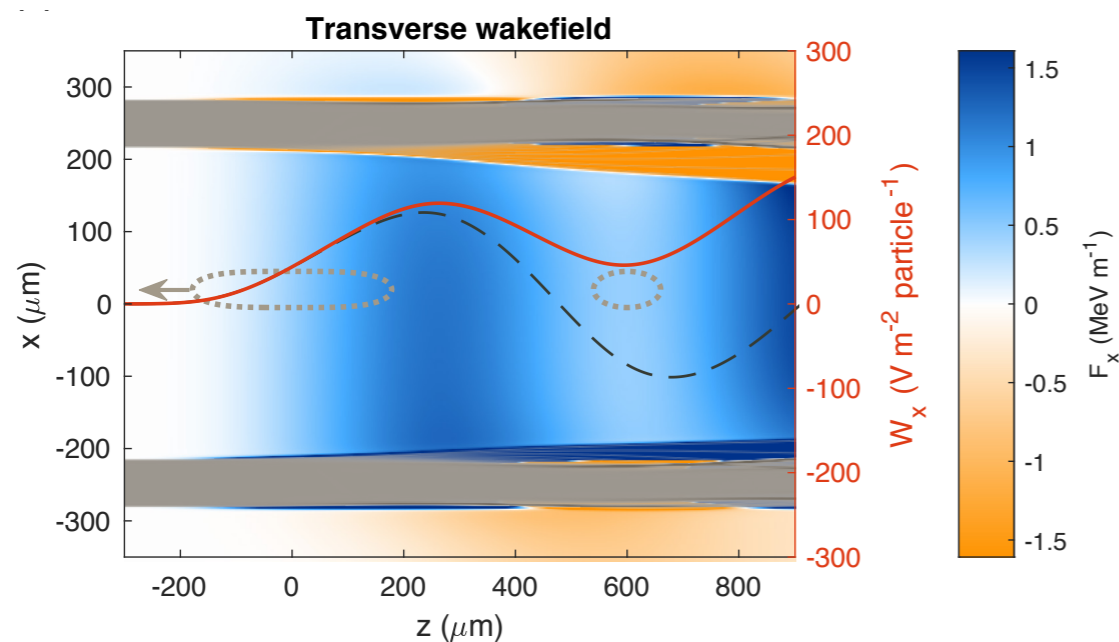


Figure 8: The envelope of the transverse wakefields for both planes is shown. The CLIC bunch spacing is 0.15 m.

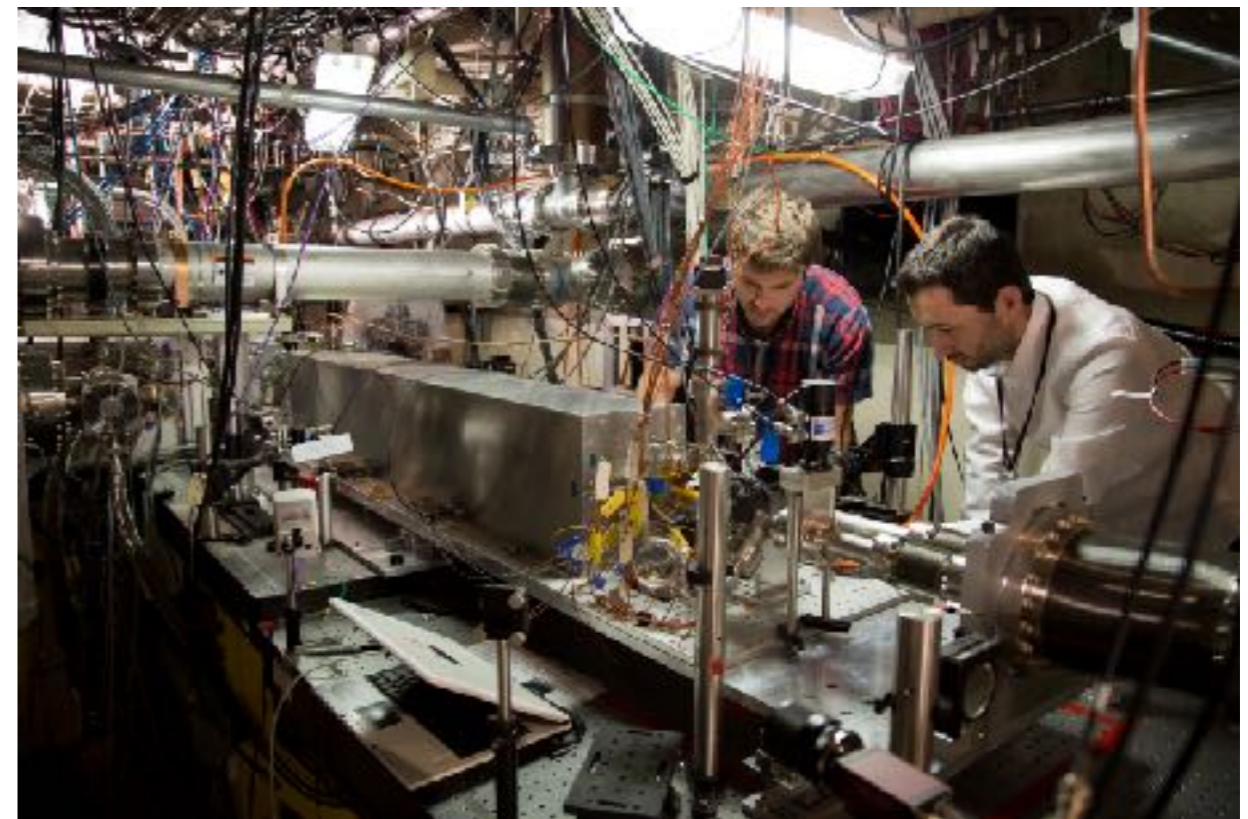


# **PART 2: Diagnosis**

Experiments at FACET, SLAC

## The E225 experiment

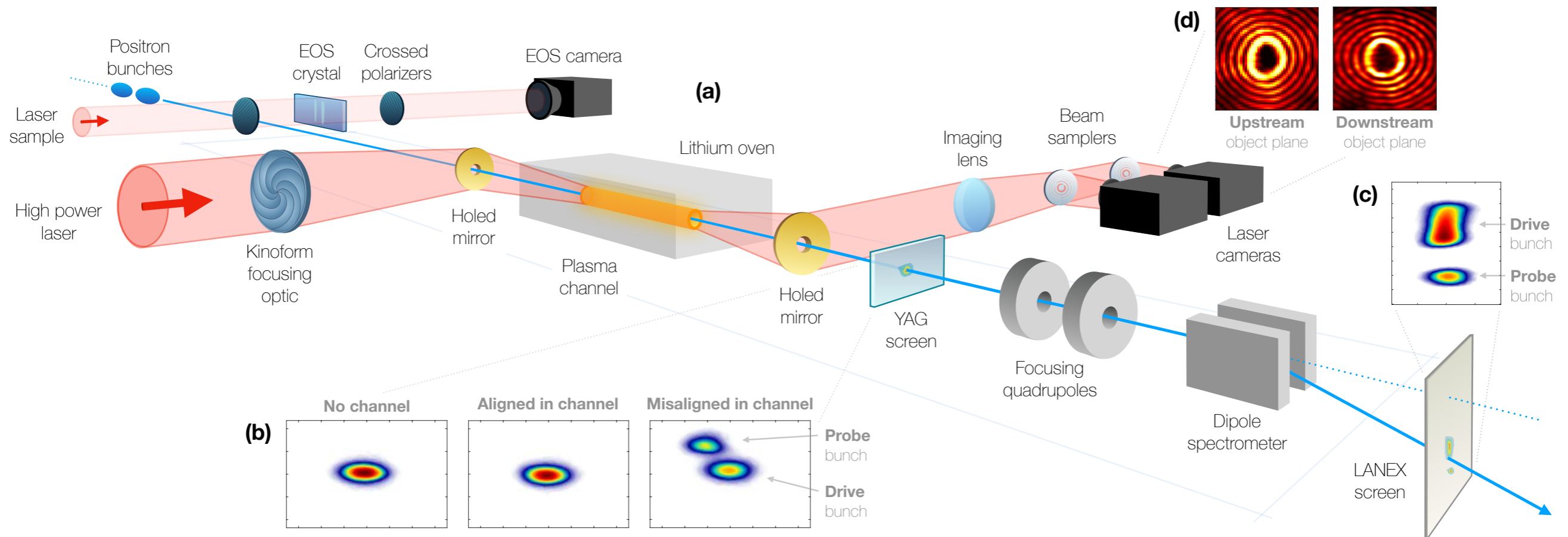
- One of these experiments was the E225 Hollow Channel experiment, **lead by Spencer Gessner**.
- **E225 successfully demonstrated acceleration** of a trailing positron bunch in a positron driven hollow plasma channel.
- Transverse wakefields were also measured in the E225 experiment.



**Spencer Gessner (left) and Sebastien Corde (right) at FACET tunnel, SLAC.**

*Image source: SLAC National Accelerator Laboratory*

## E225 – Experimental setup

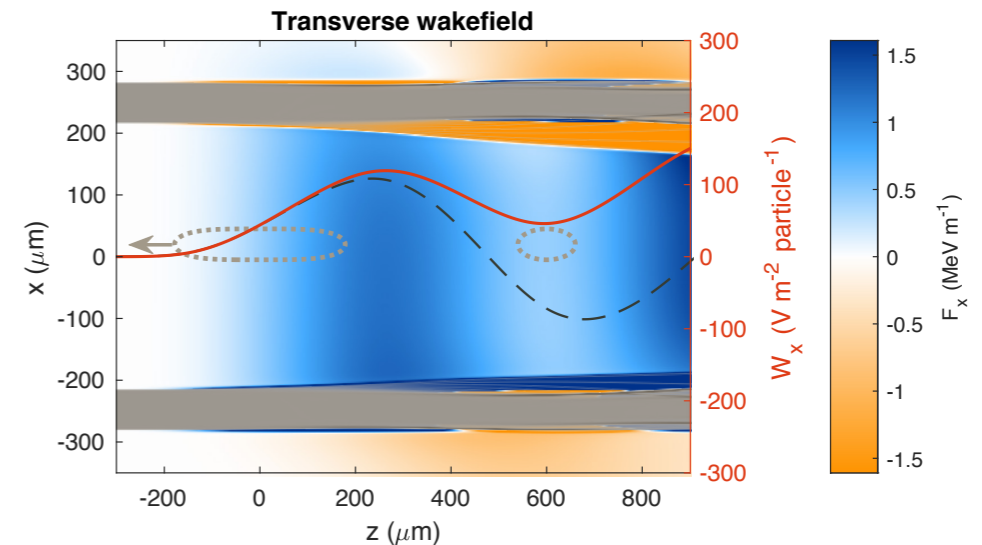


- The SLAC linac provided **two 20 GeV bunches**, made from one bunch using a beam notching device.
- The FACET laser (up to 10 TW, 60 fs pulses) was adjusted down to ensure **no ionisation in the channel**.
- A lithium oven was set to give a neutral gas density of  $3 \times 10^{16} \text{ cm}^{-3}$  (but was necessarily fully ionized).

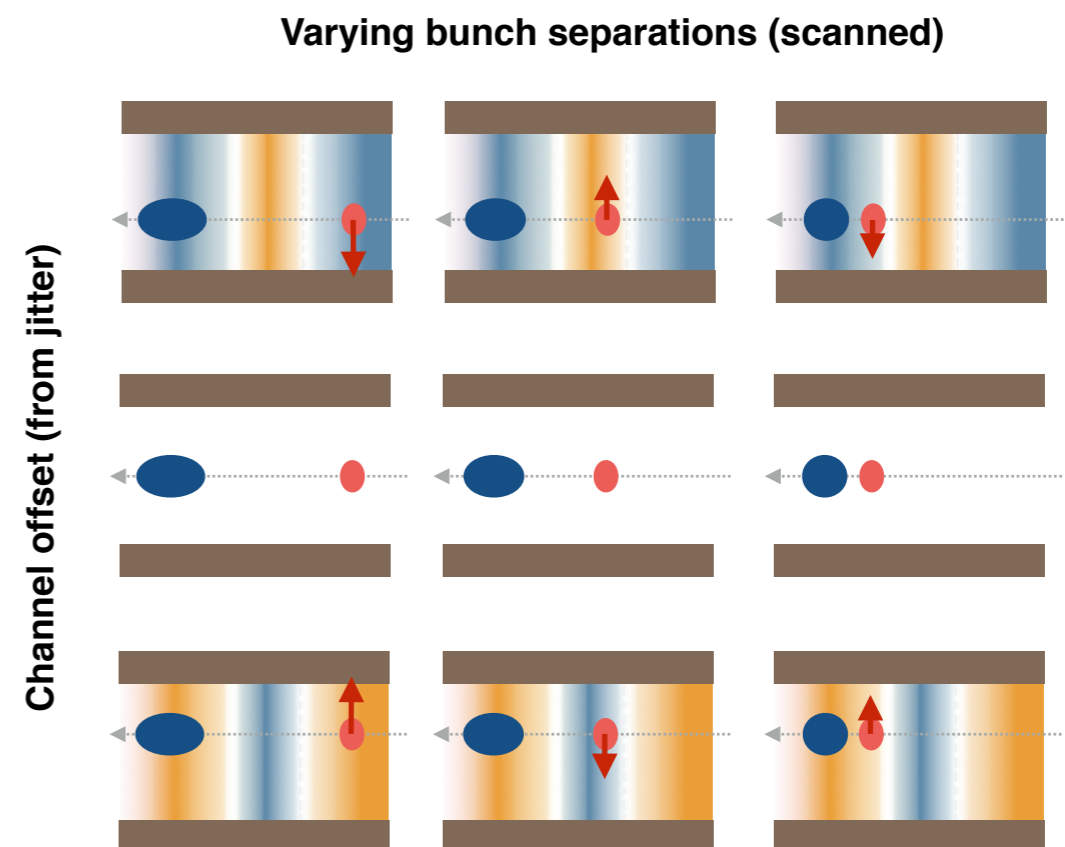
# The experiment

- Our **goal** was to **measure the how the transverse wakefield varied longitudinally**.
- The probe bunch observing the wakefield is deflected angularly (kicked) when the channel and the drive bunch are relatively offset.
- The experiment performed was:  
**Transverse channel offsets for various bunch separations**
  - The channel (250  $\mu\text{m}$  radius) was offset by transverse laser jitter (20-40  $\mu\text{m}$  rms)
  - The bunch separation was varied by stretching the bunch and adjusting the notching device.
- Diagnostics:
  - Laser offset imaged downstream (**laser cameras**).
  - Probe kick measured on a **spectrometer** (in the non-dispersed plane).
  - Bunch separation measured using an **electro-optical sampler**.

Prediction:



Experiment (2D "scan"):



## Another independent measurement

- An independent measurement is beneficial (due to high complexity).
- It is possible to estimate the transverse wakefield per offset from the measured longitudinal wakefield, via the Panofsky-Wenzel theorem and the linear model.

*Panofsky-Wenzel theorem:*

$$\frac{\partial W_x}{\partial z} = \frac{\partial W_z}{\partial x}$$

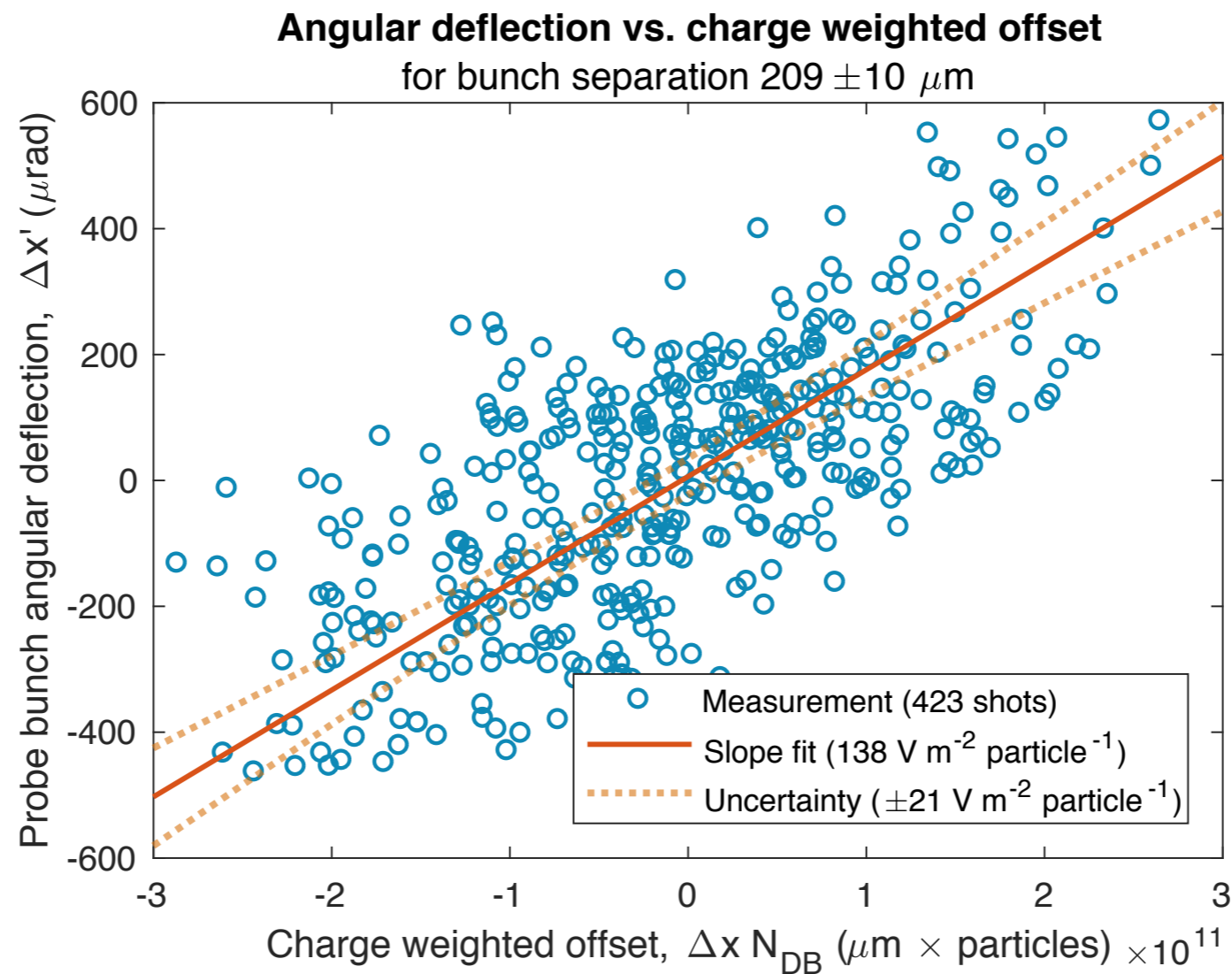
Integrate (++)  
→

*Estimate of transverse from longitudinal wakefield:*

$$\frac{W_x(z)}{\Delta x} \approx -\frac{\kappa(a, b)}{a^2} \int_0^z W_z(z') dz' \quad \text{where} \quad \kappa(a, b) = \frac{4\chi_{\perp}^2 - 2}{\chi_{\parallel}^2 - 1}$$

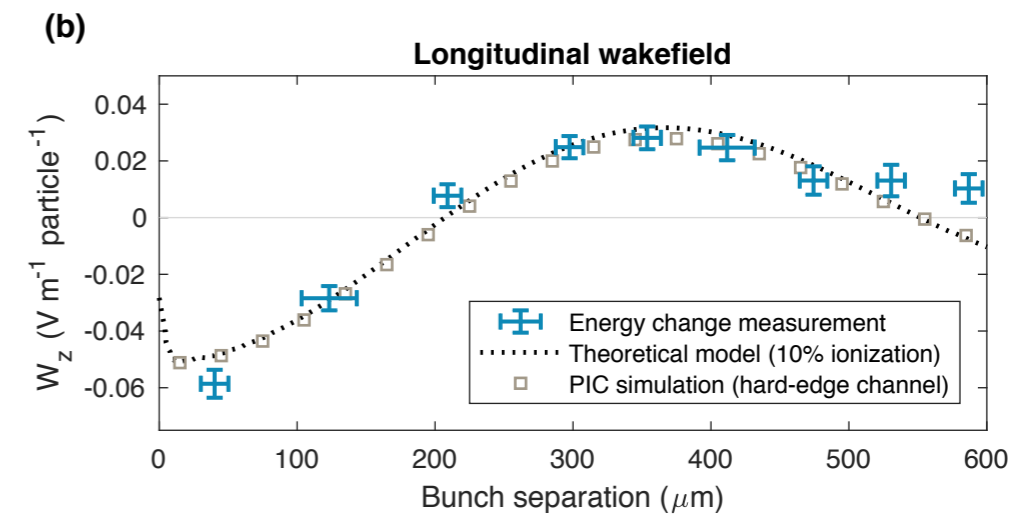
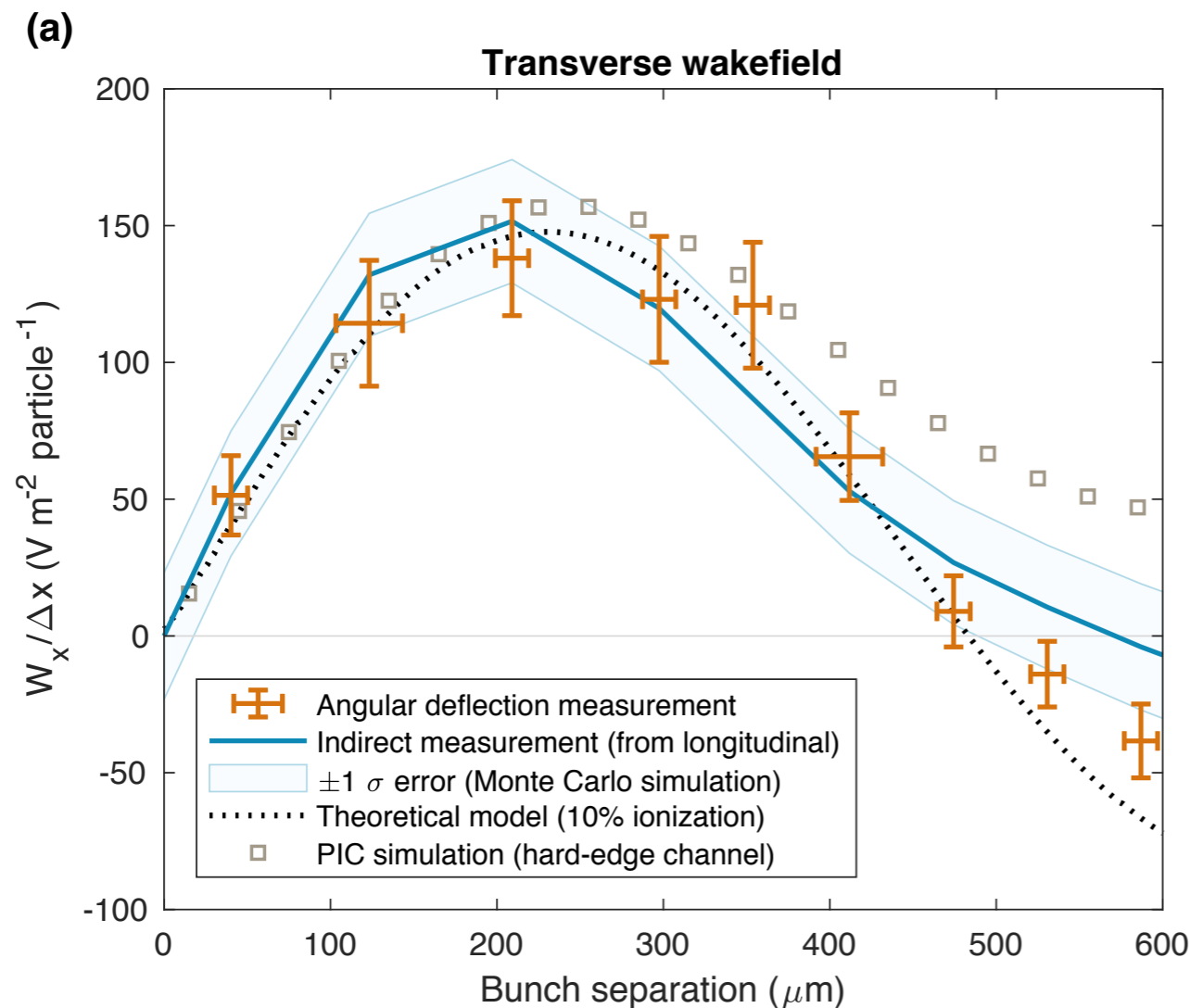
- Not perfect: Assumes linear model, breaks down far behind the drive bunch.
- Provides verification of numerical calibrations, etc.
- The longitudinal wakefield was measured by the energy change of the probe bunch (on a spectrometer).

## Observed data (deflection vs. channel offset)



- For each bunch separation, a correlation between channel offset and probe bunch angular deflection was observed.
- The **slope of this correlation is proportional to the transverse wakefield per offset** at the z-location of the probe bunch.

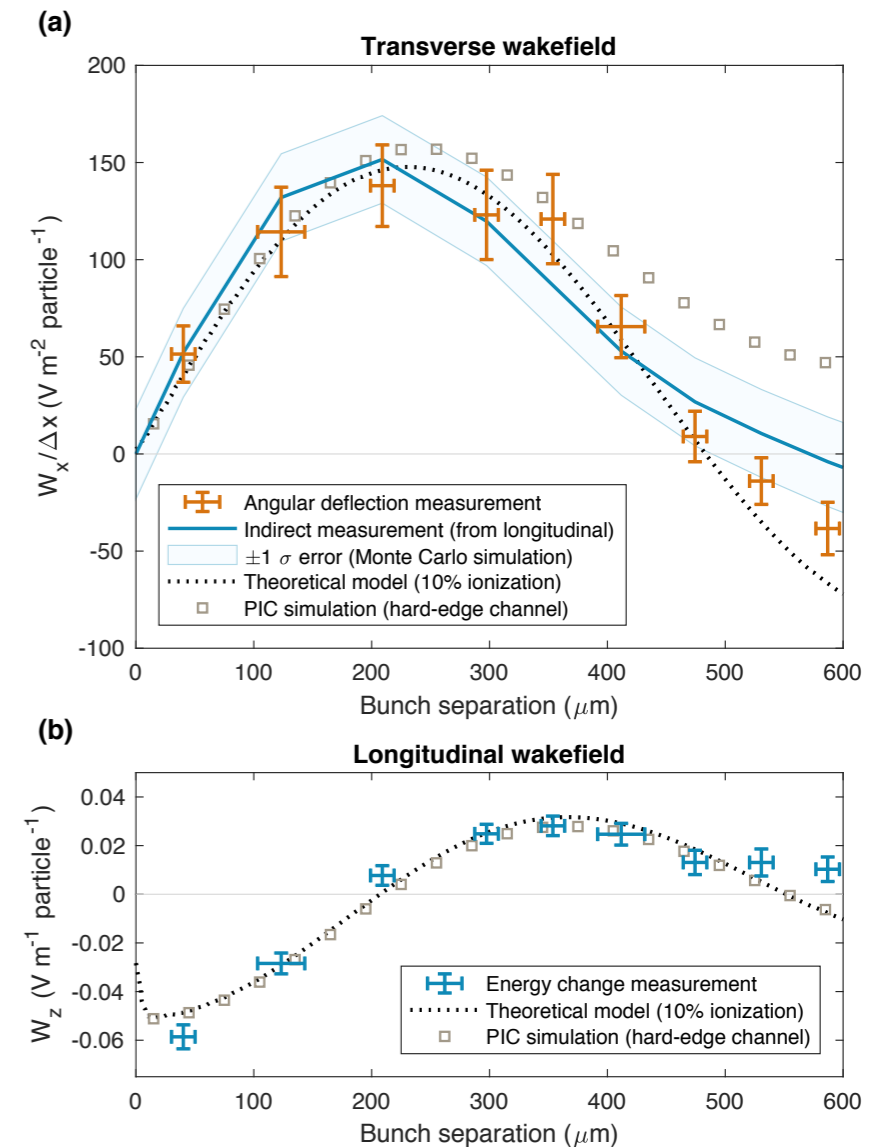
# Final experimental results



- Plasma density determined by a wavelength fit (10% ionization =  $3 \times 10^{15} \text{ cm}^{-3}$ )
- Good fit, largely consistent with theory. Some discrepancy at larger separations.

## Implications

- **Overall, the measurement agrees with the theoretical models.**
- Simulation-based parameter scans indicate that the discrepancy at large separations can possibly be explained by using a more complex radial plasma shape (not possible to exclude with our diagnostics).
- Implication: There is indeed a strong transverse wakefield.
- Submitting these results to Physical Review Letter.





## **PART 3: Finding a cure**

New ideas  
for fixing the hollow channel

Fundamental problem:  
**transverse wakefields**

## Ideas for transverse wakefield suppression

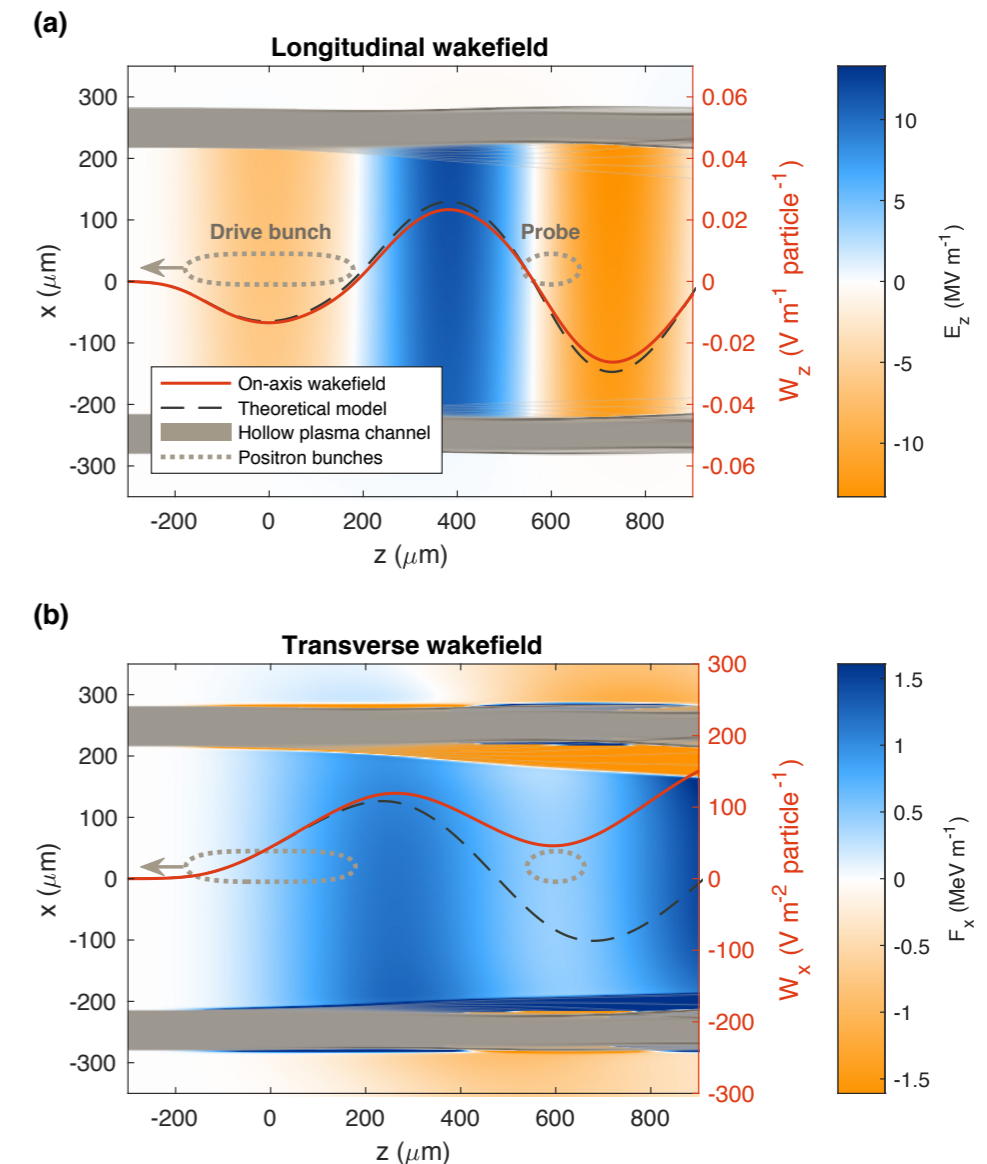
- Conventional BNS damping  
=> Requires very large energy spreads
- External focusing  
=> Requires very strong focusing  
=> Solenoids do not scale well with energy ( $1/\gamma^2$ , but kick scales with  $1/\gamma$ )  
=> Does not help unless perfectly aligned and at center
- Near hollow channels (low density plasma)  
=> Breaks the chiral symmetry
- Tailoring the wakefield in a locally controlled manner



## Clarification on what needs to be damped

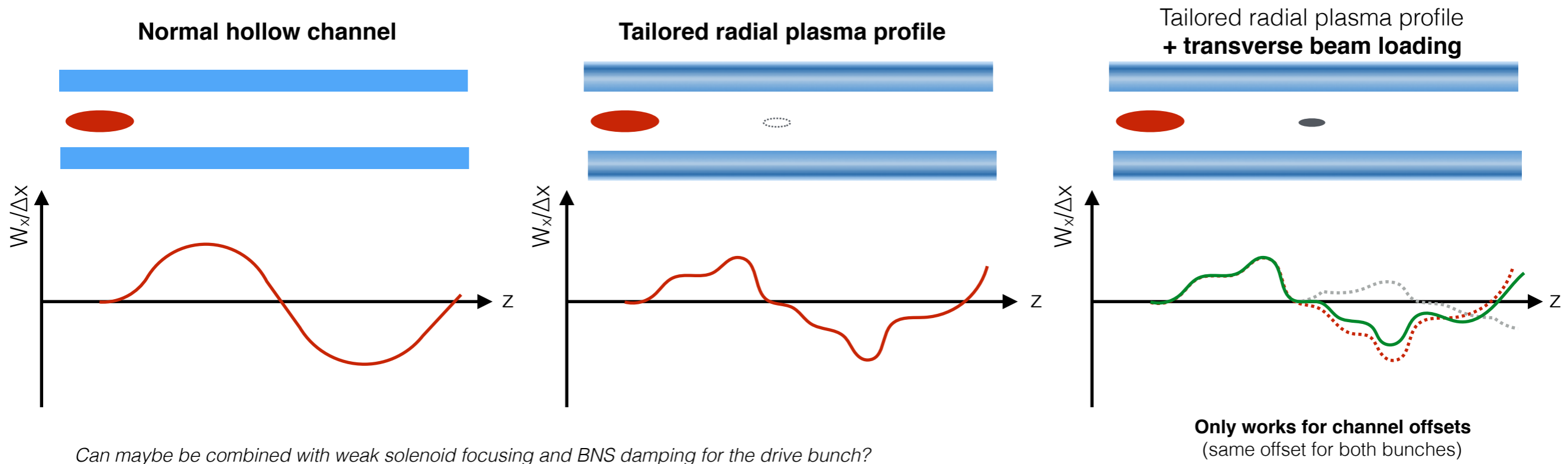
- Two different problems
  - Transverse instability of the drive beam (feedback loop)
  - Transverse deflection of accelerated beam caused by drive beam wakefield
  - Transverse instability of the accelerated beam (from its own transverse wakefield)
- The drive beam only needs to **survive one stage**. It does not need to preserve its emittance.
- The accelerated beam can in principle be placed on the **zero crossing** of the transverse wakefield from the driver.
- The self-wakefield can in principle be used to transversely **beam load** the transverse wakefield of the driver (at the zero crossing).
- Now we just need to make a hollow channel with all the above + high accelerating gradient + high efficiency

**EASY PEASY!**



# Tailored radial plasma profiles

- Currently just at the speculative stage: Hollow plasmas are naturally not high-Q cavities: can we use this to our advantage?
- A strength of plasma channels compared to structure-based channels: Many degrees of freedom to play with (radial distribution of plasma density)
- This work will benefit from a theoretical model for arbitrary radial plasma profiles  $n(r)$  – (as an alternative a brute force PIC simulation search)
- If it actually works, the next step is to somehow make this plasma profile (with the kinoform of all kinoforms?)



## Conclusions

- Strong wakefields is a big challenge for the hollow channel
- We did an experiment at FACET to diagnose the problem
- Experiments correspond well with theory (but still some discrepancies)
- We have ideas on how to fix it (with radially tailored plasma profiles?)
- Will be pursued at FACET-II

*A Haiku of Hope*



*We do not de-clare  
the ho-llow cha-nnel dead yet.  
First try all id-eas.*

**Thank you for your attention!**