

# EFT fit on top quark EW couplings

I. García, M. Perelló Roselló, M. Vos (IFIC - U. Valencia/CSIC)  
P. Roloff, R. Ström (CERN)  
G. Durieux (DESY), C. Zhang (IHEP)



## Acknowledging input/contributions from:

M. Boronat, J. Fuster, P. Gomis, E. Ros (IFIC - U. Valencia/CSIC)

R. Pöschl, F. Richard (Orsay, LAL)

# Outline

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- Introduction to quark couplings and EFT
- Observables sensitivities:
  - $A_{FB}$  + cross-section
  - Optimal CP-odd observables
  - Top quark polarization
  - Statistically optimal observables
- Full-simulation at CLIC380 and ILC500
- Full-simulation at high energies

# Introduction to quark couplings and EFT

# Top quark couplings

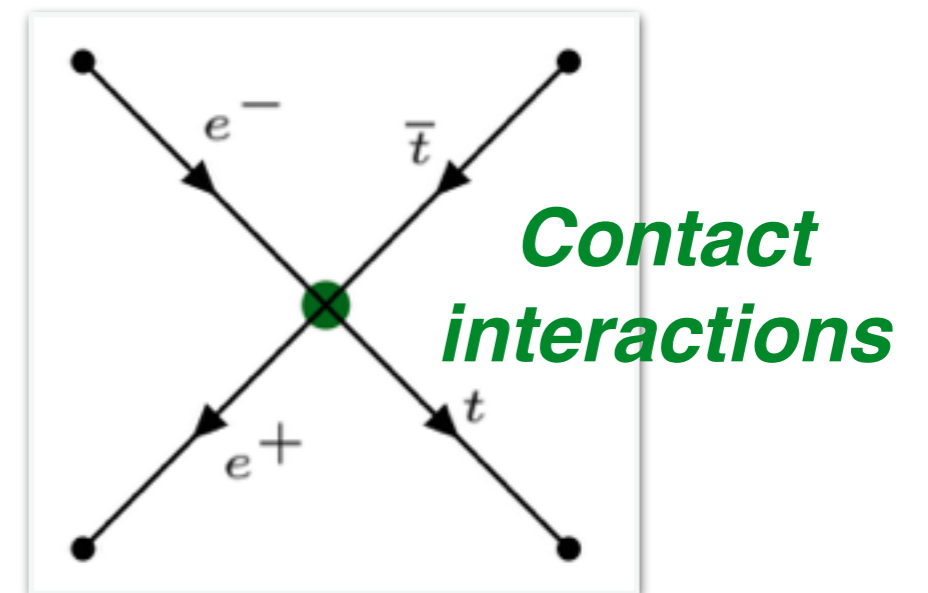
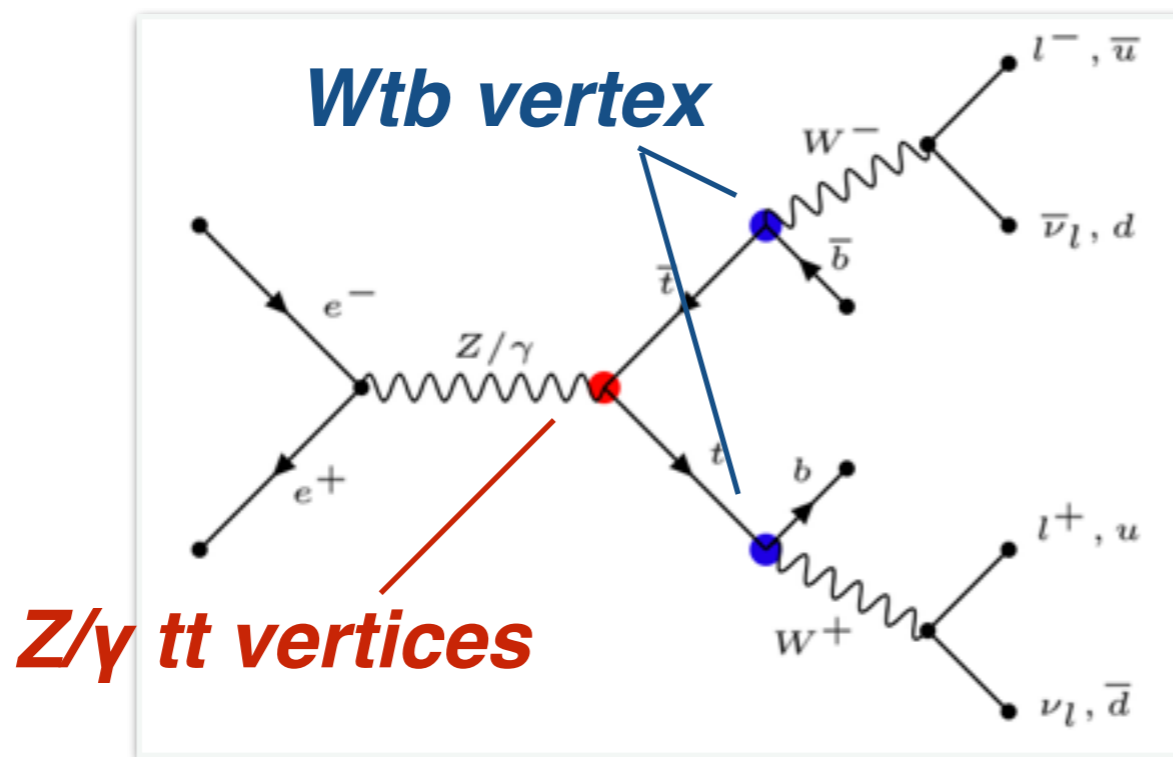
**Objective:** to study the potential of a global fit in the top EW sector.

## Form-factors

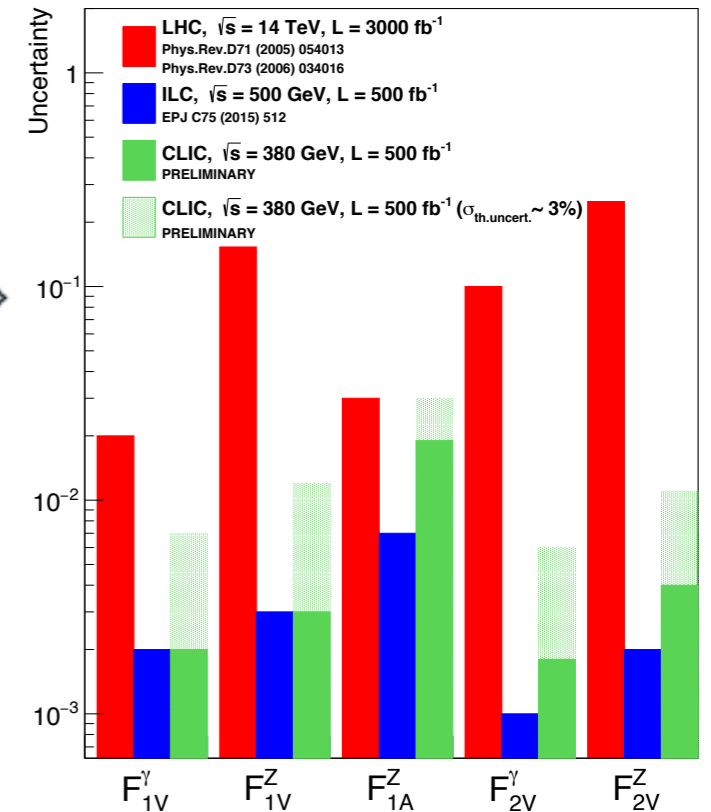
$$\Gamma_{\mu}^{t\bar{t}X}(k^2, q, \bar{q}) = ie \left\{ \gamma_{\mu} \left( \underbrace{F_{1V}^X(k^2)}_{\text{CP Conserving}} + \gamma_5 \underbrace{F_{1A}^X(k^2)}_{\text{CPV}} \right) - \frac{\sigma_{\mu\nu}}{2m_t} (q + \bar{q})^{\nu} \left( \underbrace{iF_{2V}^X(k^2)}_{\text{CP Conserving}} + \gamma_5 \underbrace{F_{2A}^X(k^2)}_{\text{CPV}} \right) \right\}$$

## Effective Field Theory

$$\mathcal{L}_{eff} = \mathcal{L}_{SM} + \frac{1}{\Lambda^2} \sum_i C_i O_i + \mathcal{O}(\Lambda^{-4})$$

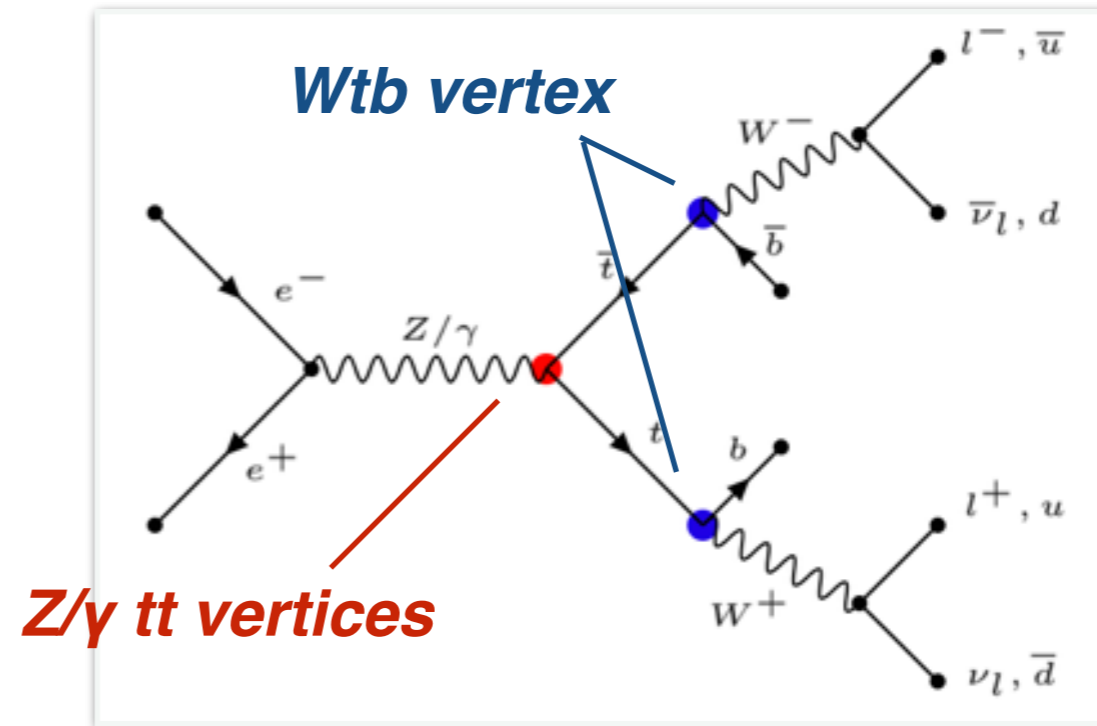


CLIC baseline document  
arXiv:1608.07537



# Dim-6 operators

$$\begin{aligned}
 O_{\varphi q}^1 &\equiv \frac{y_t^2}{2} \bar{q} \gamma^\mu q \varphi^\dagger i \overleftrightarrow{D}_\mu \varphi \\
 O_{\varphi q}^3 &\equiv \frac{y_t^2}{2} \bar{q} \tau^I \gamma^\mu q \varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi \\
 O_{\varphi u} &\equiv \frac{y_t^2}{2} \bar{u} \gamma^\mu u \varphi^\dagger i \overleftrightarrow{D}_\mu \varphi \\
 O_{\varphi ud} &\equiv \frac{y_t^2}{2} \bar{u} \gamma^\mu d \varphi^T \epsilon i D_\mu \varphi \\
 \\ 
 O_{uG} &\equiv y_t g_s \bar{q} T^A \sigma^{\mu\nu} u \epsilon \varphi^* G_{\mu\nu}^A \\
 O_{uW} &\equiv y_t g_W \bar{q} \tau^I \sigma^{\mu\nu} u \epsilon \varphi^* W_{\mu\nu}^I \\
 O_{dW} &\equiv y_t g_W \bar{q} \tau^I \sigma^{\mu\nu} d \epsilon \varphi^* W_{\mu\nu}^I \\
 O_{uB} &\equiv y_t g_Y \bar{q} \sigma^{\mu\nu} u \epsilon \varphi^* B_{\mu\nu}
 \end{aligned}$$

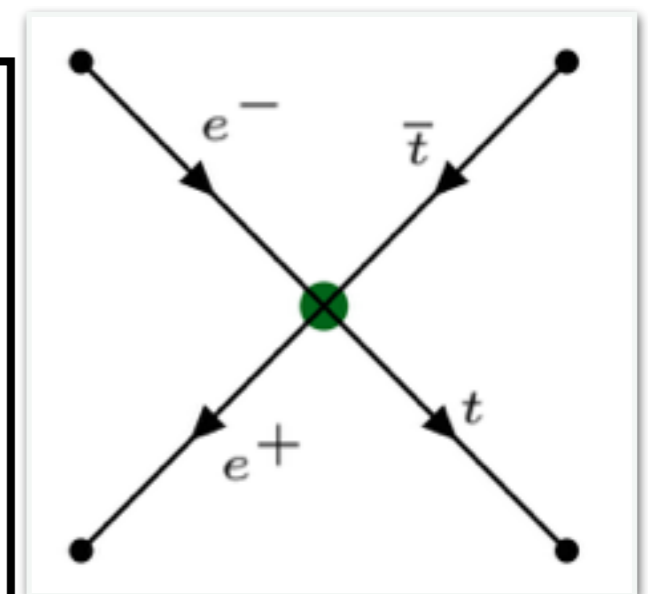


$$\begin{aligned}
 O_{lq}^1 &\equiv \bar{q} \gamma_\mu q \bar{l} \gamma^\mu l \\
 O_{lq}^3 &\equiv \bar{q} \tau^I \gamma_\mu q \bar{l} \tau^I \gamma^\mu l \\
 O_{lu} &\equiv \bar{u} \gamma_\mu u \bar{l} \gamma^\mu l \\
 O_{eq} &\equiv \bar{q} \gamma_\mu q \bar{e} \gamma^\mu e \\
 O_{eu} &\equiv \bar{u} \gamma_\mu u \bar{e} \gamma^\mu e
 \end{aligned}$$

## Contact interactions

$$O_{lequ}^T \equiv \bar{q} \sigma^{\mu\nu} u \epsilon \bar{l} \sigma_{\mu\nu} e$$

$$\begin{aligned}
 O_{lequ}^S &\equiv \bar{q} u \epsilon \bar{l} e \\
 O_{ledq} &\equiv \bar{d} q \bar{l} e
 \end{aligned}$$



# Change of basis

## Transformation between effective operators and form-factors:

$$\begin{aligned}
 F_{1,V}^Z - F_{1,V}^{Z,SM} &= \frac{1}{2} \left( \underline{C_{\varphi Q}^{(3)}} - \underline{C_{\varphi Q}^{(1)}} - C_{\varphi t} \right) \frac{m_t^2}{\Lambda^2 s_W c_W} = -\frac{1}{2} \underline{C_{\varphi q}^V} \frac{m_t^2}{\Lambda^2 s_W c_W} \\
 F_{1,A}^Z - F_{1,A}^{Z,SM} &= \frac{1}{2} \left( -\underline{C_{\varphi Q}^{(3)}} + \underline{C_{\varphi Q}^{(1)}} - C_{\varphi t} \right) \frac{m_t^2}{\Lambda^2 s_W c_W} = -\frac{1}{2} \underline{C_{\varphi q}^A} \frac{m_t^2}{\Lambda^2 s_W c_W} \\
 F_{2,V}^Z &= \left( \underline{\text{Re}\{C_{tW}\} c_W^2 - \text{Re}\{C_{tB}\} s_W^2} \right) \frac{4m_t^2}{\Lambda^2 s_W c_W} = \text{Re}\{ \underline{C_{uZ}} \} \frac{4m_t^2}{\Lambda^2} \\
 F_{2,V}^\gamma &= \left( \underline{\text{Re}\{C_{tW}\} + \text{Re}\{C_{tB}\}} \right) \frac{4m_t^2}{\Lambda^2} = \text{Re}\{ \underline{C_{uA}} \} \frac{4m_t^2}{\Lambda^2} \\
 [F_{2,A}^Z, F_{2,A}^\gamma] &\propto \underline{[\text{Im}\{C_{tW}\}, \text{Im}\{C_{tB}\}]}
 \end{aligned}$$

We can change to an alternative basis  
(**Vector/Axial - Vector**)

10 operators in the current global fit:

- 4 CP-conserving ttX vertices
- 2 CP-violating ttX vertices
- 4 contact interactions

## Conversion to V/A - V basis in contact interactions:

$$\begin{aligned}
 C_{lq}^V &\equiv C_{lu} + C_{lq}^{(1)} - C_{lq}^{(3)} & C_{eq}^V &\equiv C_{eu} + C_{eq} \\
 C_{lq}^A &\equiv C_{lu} - C_{lq}^{(1)} + C_{lq}^{(3)} & C_{eq}^A &\equiv C_{eu} - C_{eq}
 \end{aligned}$$

**Observables sensitivities**

# Observables sensitivity: $A_{\text{FB}}$ + cross-section

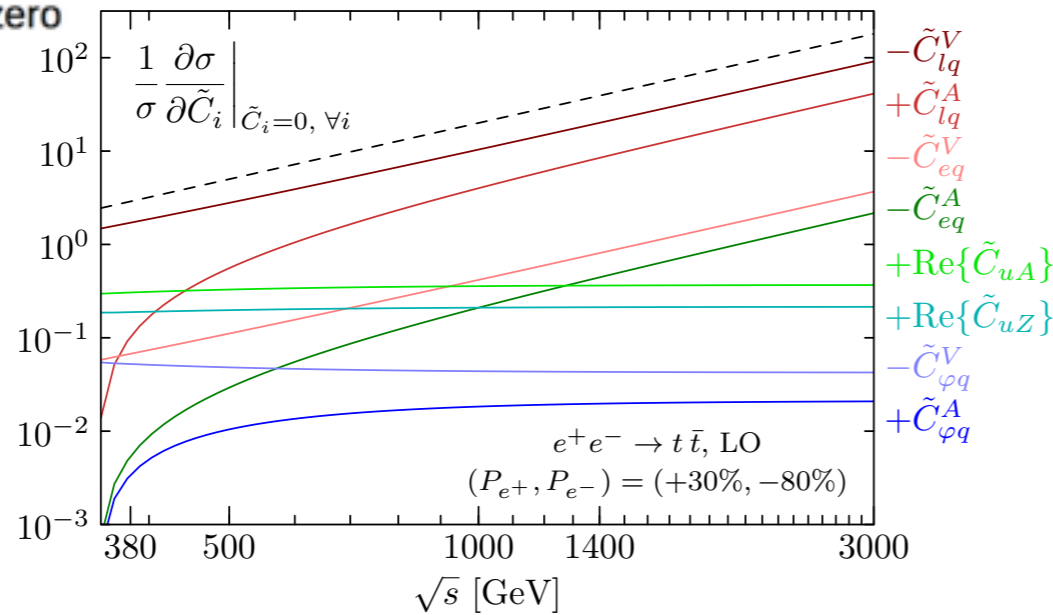
$$e^+e^- \rightarrow t\bar{t}, \text{ LO}$$

Durieux, Perelló, Vos, Zhang, to be published

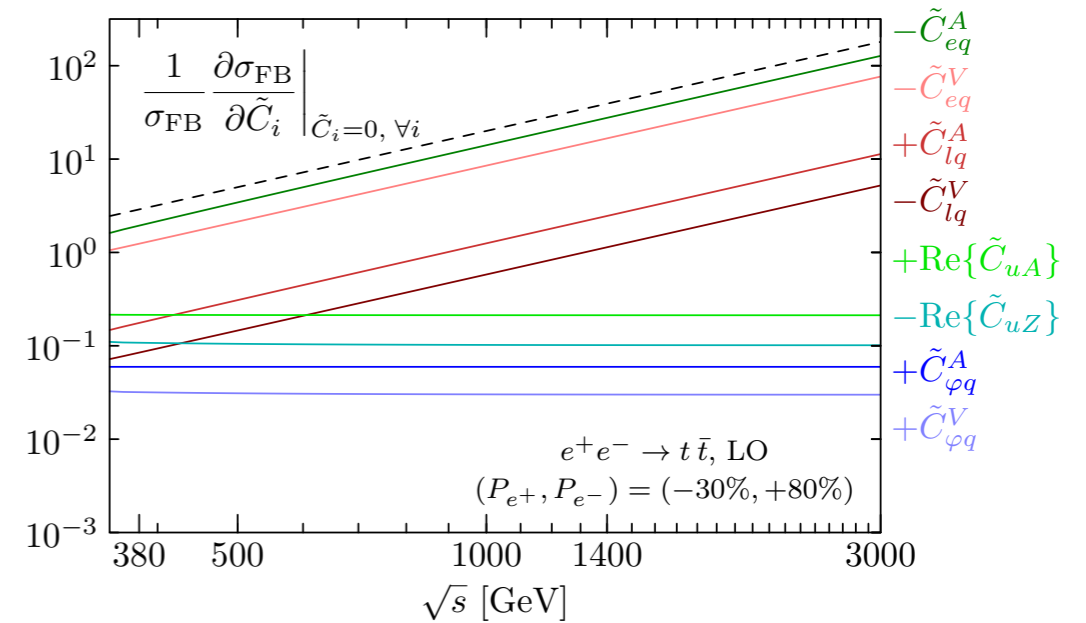
## Sensitivity:

Relative change in cross-section due to non-zero operator coefficient  
 $\Delta\sigma(C)/\sigma/\Delta C$

## Cross-section

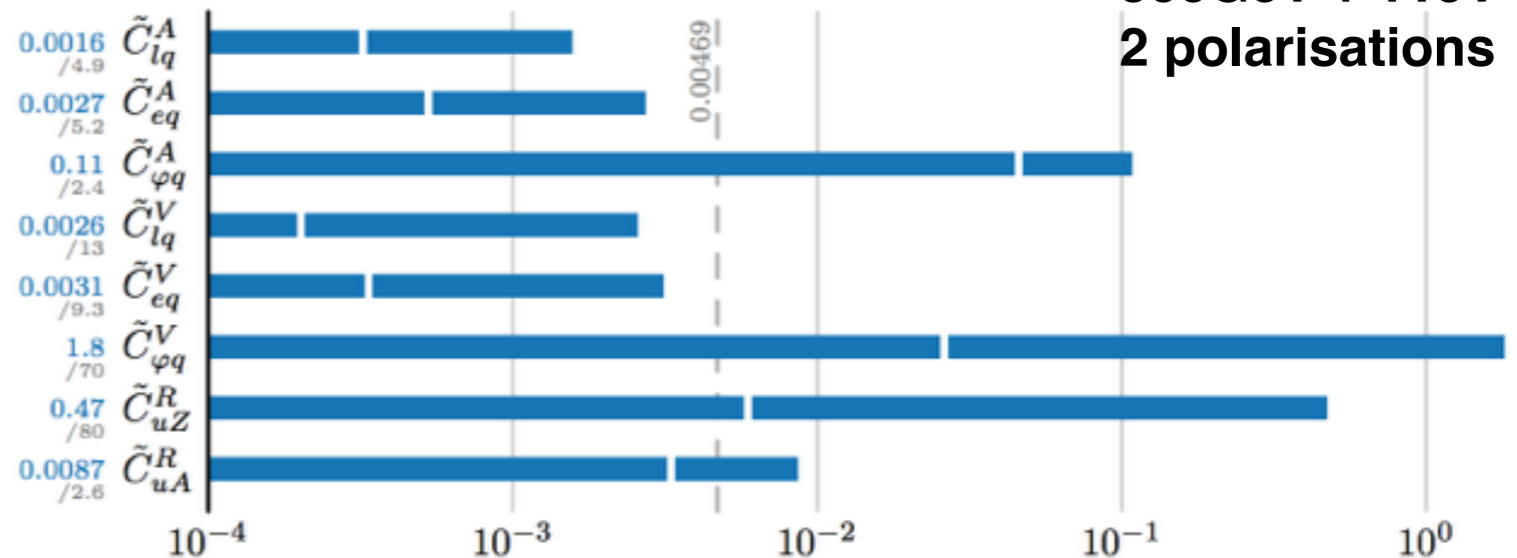


## Forward-backward asymmetry



(multi-) TeV operation provides better sensitivity to **contact-interaction operators**.

$\sigma + A^{\text{FB}}$ :



**Global constraints 500GeV + 1TeV for 2 polarisations**

- Very good individual limits (until de gap)
- Global limits (full bar) factor 3 to 80 worse



# Optimal CP-odd observables

The **CP-violating effects** in  $e^+e^- \rightarrow t\bar{t}$  manifest themselves in specific **top-spin effects**, namely **CP-odd top spin-momentum correlations and  $t\bar{t}$  spin correlations**.

- **CP-odd observables** are defined with the **four momenta available in  $t\bar{t}$  semi-leptonic decay channel**
- The way to **extract** the **CP-violating form factor** is to construct **asymmetries sensitive to CP-violation effects**

**arXiv:1710.06737**

Eur. Phys. J. C manuscript No.  
(preprint number: TTK-17-17, IFIC/17-26, ILD-PHYS-2017-001, CLICdp-PUB-2017-003 )

## CP-violating top quark couplings at future linear $e^+e^-$ colliders

W. Bernreuther<sup>1</sup>, L. Chen<sup>1,a</sup>, I. García<sup>2,b,c</sup>, M. Perelló<sup>2</sup>,  
R. Poeschl<sup>3</sup>, F. Richard<sup>3</sup>, E. Ros<sup>2</sup>, M. Vos<sup>2</sup>

<sup>1</sup>Institut für Theoretische Teilchenphysik und Kosmologie, RWTH Aachen University, 52056 Aachen, Germany

<sup>2</sup>Instituto de Física Corpuscular (IFIC, UVEG/CSIC), Apartado de Correos 22085, E-46071, Valencia, Spain

<sup>3</sup>Laboratoire de l'Accélérateur Linéaire (LAL), Centre Scientifique d'Orsay, 91898 Orsay Cédex, France

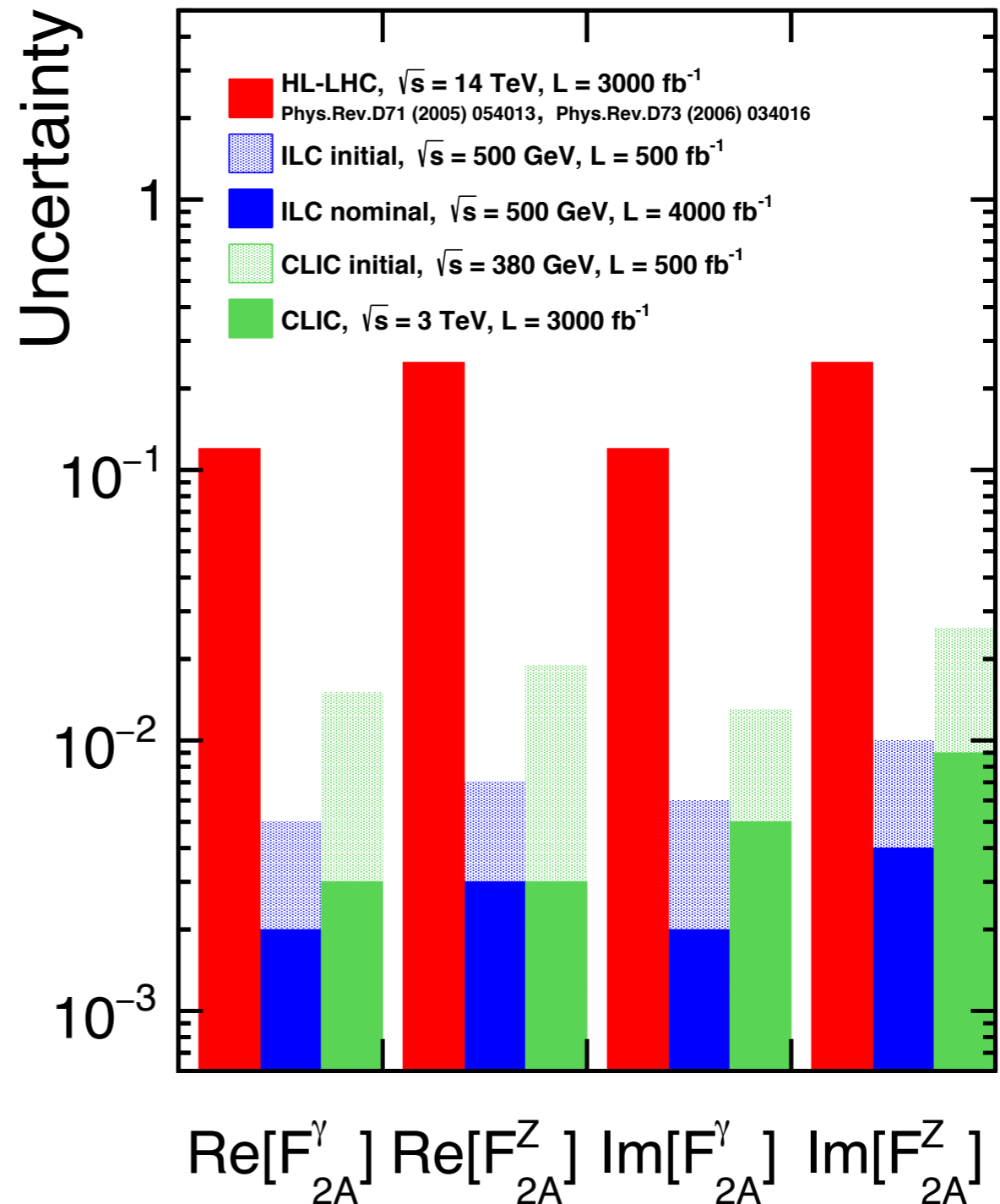
October 19, 2017

**Abstract** We study the potential of future lepton colliders to probe violation of the CP symmetry in the top quark sector. In certain extensions of the Standard Model, such as the two-Higgs-doublet model (2HDM), sizeable anomalous top quark dipole moments can arise, that may be revealed by a precise measurement of top quark pair production. We present results from detailed Monte Carlo studies for the ILC at 500 GeV and CLIC at 380 GeV and use parton-level simulations to explore the potential of high-energy operation. We find that precise measurements in  $e^+e^- \rightarrow t\bar{t}$  production with subsequent decay to lepton plus jets final states can provide sufficient sensitivity to detect Higgs-boson-induced CP violation in a viable two-Higgs-doublet model. The potential of a linear  $e^+e^-$  collider to detect CP-violating electric and weak dipole form factors of the top quark exceeds the prospects of the HL-LHC by over an order of magnitude.

**Keywords** CP violation · top physics ·  $e^+e^-$  collider

# Prospects of CPV optimal observables

- **ILC500** and **CLIC380** have a very similar sensitivity to form factors, reaching **limits of  $|F_{2A}^\gamma| < 0.01$** .
- Assuming that systematic uncertainties can be controlled to the required level, a luminosity upgrade of both machines **may bring a further improvement**.



# CPV observables in the global fit

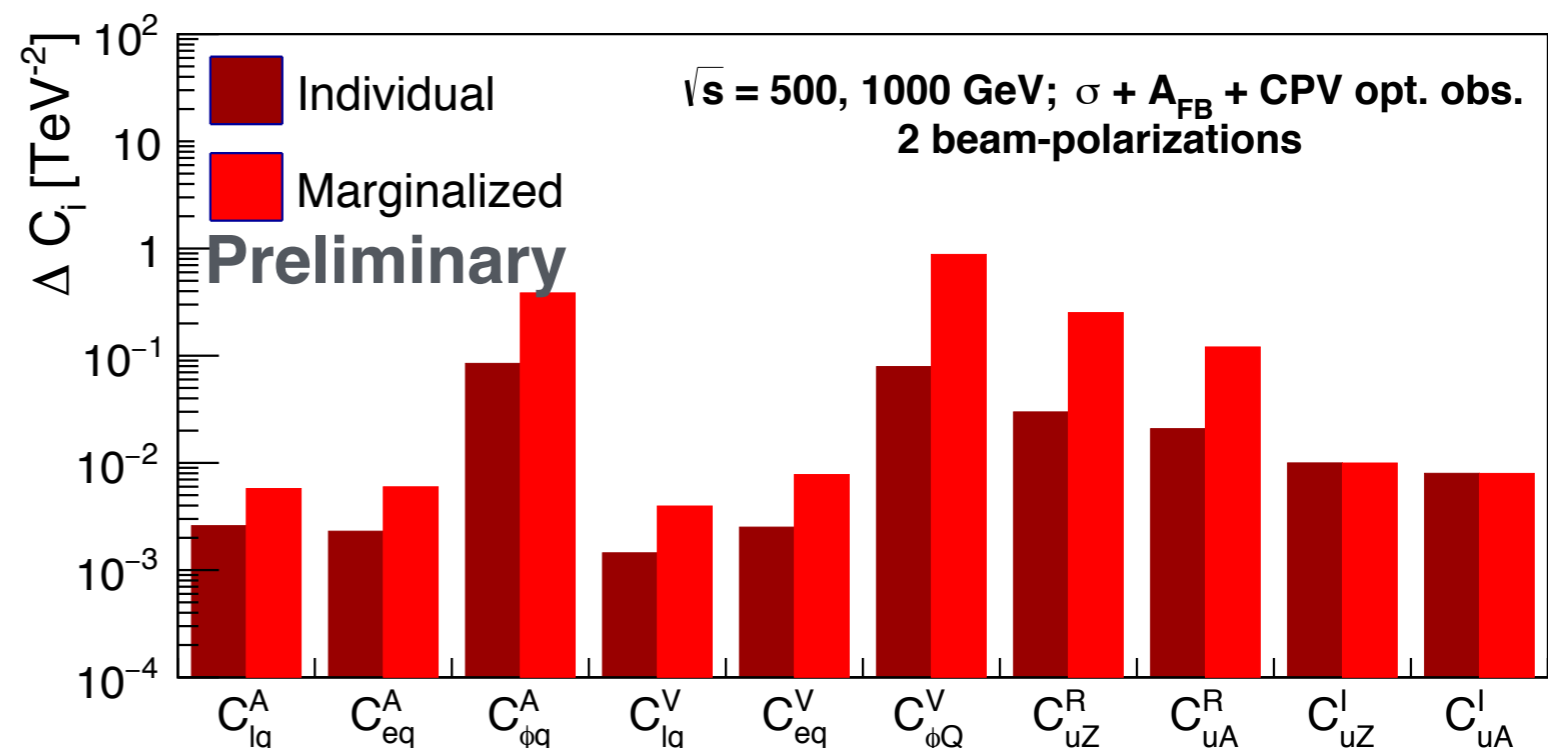
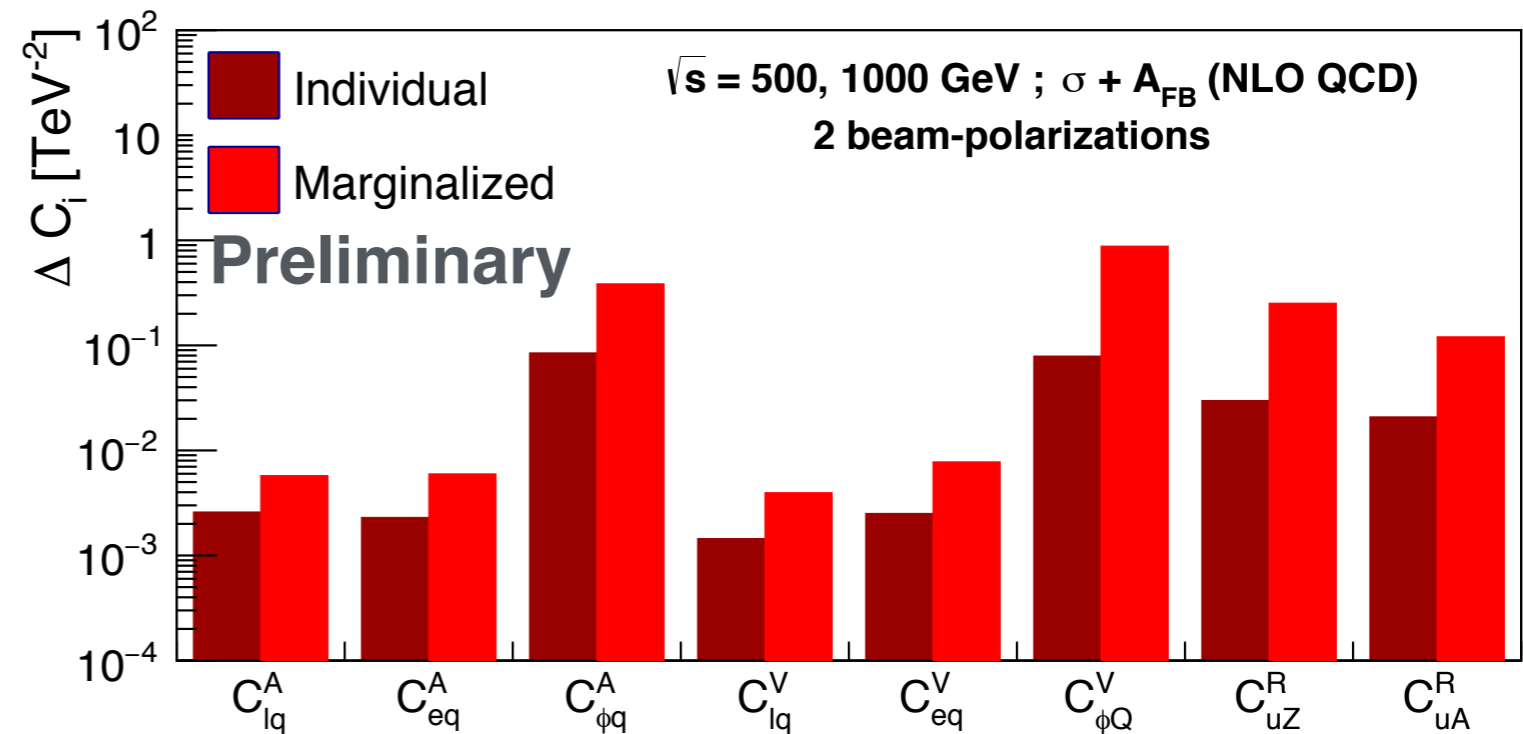
Including CPV observables  
in the EFT global fit...

$$[F_{2,A}^Z, F_{2,A}^\gamma] \propto [\text{Im}\{C_{uA}\}, \text{Im}\{C_{uZ}\}]$$

We still need to improve  
the marginalized fit

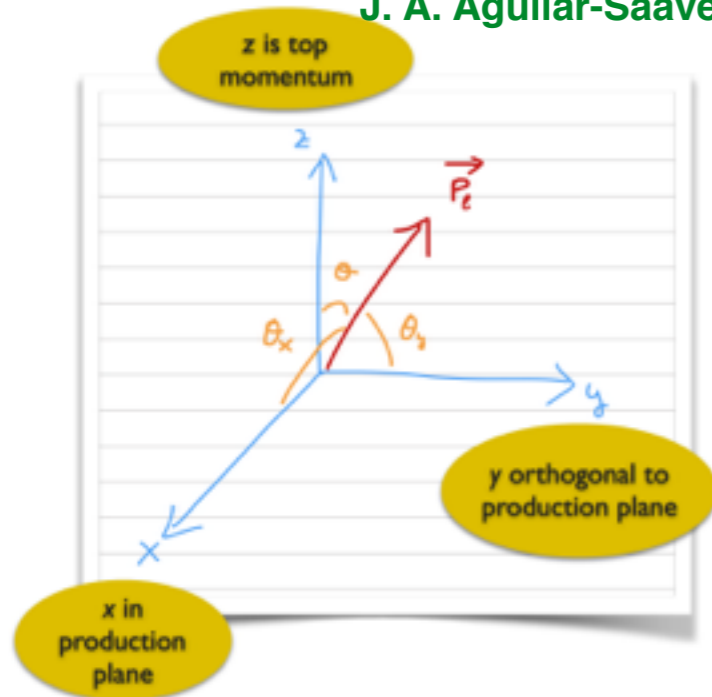
**Individual:** assuming variation in only 1 parameter  
each time.

**Marginalized:** assuming variation in all the  
parameters at the same time.



# Top quark polarization at different axes

J. A. Aguilar-Saavedra and J. Bernabeu. [arXiv:1005.5382].



$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \theta} = \frac{1}{2} (1 + \alpha P_3 \cos \theta)$$

$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \theta_x} = \frac{1}{2} (1 + \alpha P_1 \cos \theta_x)$$

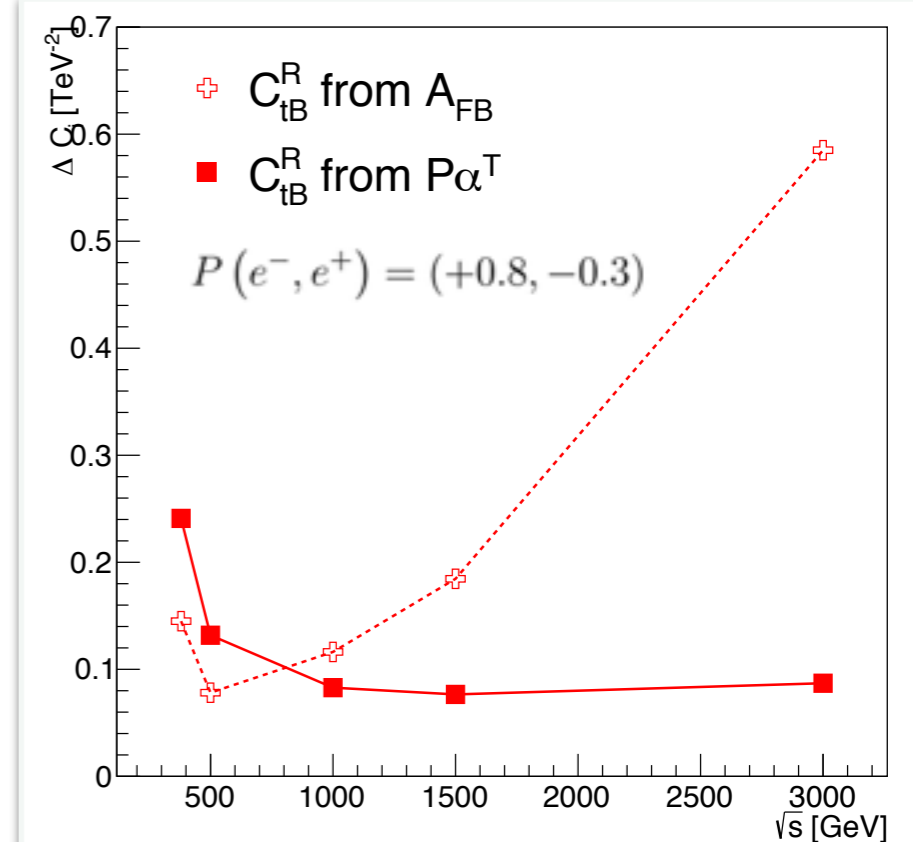
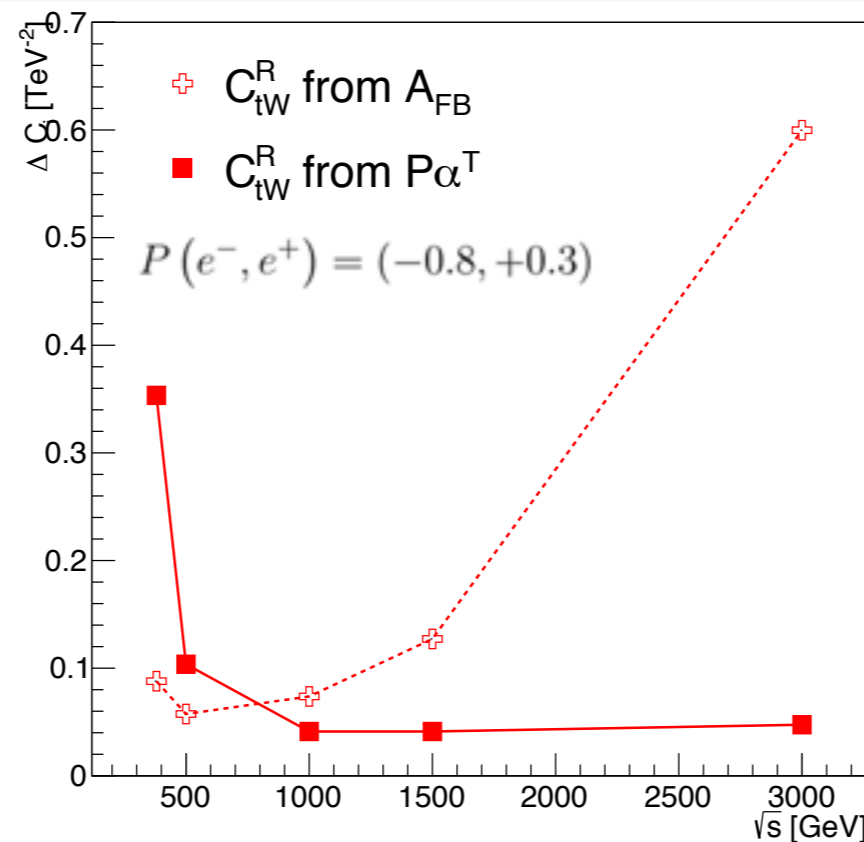
$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \theta_y} = \frac{1}{2} (1 + \alpha P_2 \cos \theta_y)$$

## Studied process

$$e^- e^+ \rightarrow t\bar{t} \rightarrow W^+ b W^- \bar{b} \rightarrow l \nu b \bar{b} q \bar{q}$$

Top polarization in the transverse axis (perpendicular to the top flight direction in the production plane) provides good sensitivity to the real part of dipoles operators (CtW and CtB).

Evolution of individual limits with center-of-mass energy



# Statistically optimal observables

G. Durieux @TopLC 2017:

<https://indico.cern.ch/event/595651/contributions/2573918/attachments/1473086/2280215/durieux-top-lc-2017.pdf>

## Statistically optimal observables

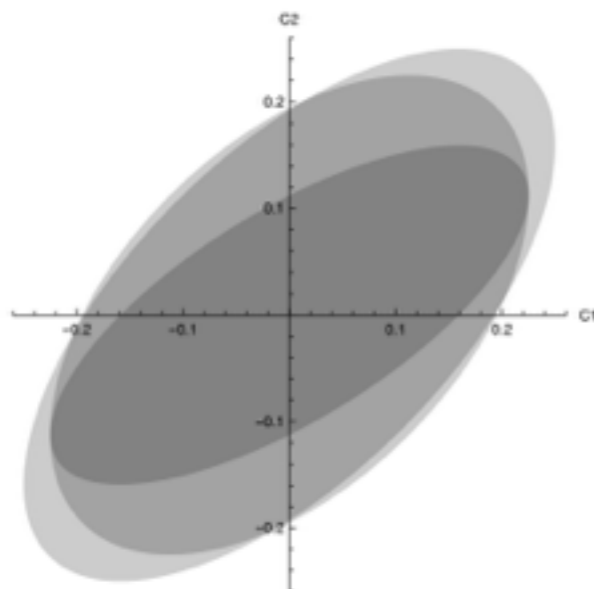
[Atwood,Soni '92]

[Diehl,Nachtmann '94]

minimize the one-sigma ellipsoid in EFT parameter space.

(joint efficient set of estimators, saturating the Rao-Cramér-Fréchet bound:  $V^{-1} = I$ )

For small  $C_i$ , with a phase-space distribution  $\sigma(\Phi) = \sigma_0(\Phi) + \sum_i C_i \sigma_i(\Phi)$ ,  
the statistically optimal set of observables is:  $O_i(\Phi) = \sigma_i(\Phi)/\sigma_0(\Phi)$ .



e.g.  $\sigma(\phi) = 1 + \cos(\phi) + C_1 \sin(\phi) + C_2 \sin(2\phi)$

1. asymmetries:  $O_i \sim \text{sign}\{\sin(i\phi)\}$

2. moments:  $O_i \sim \sin(i\phi)$

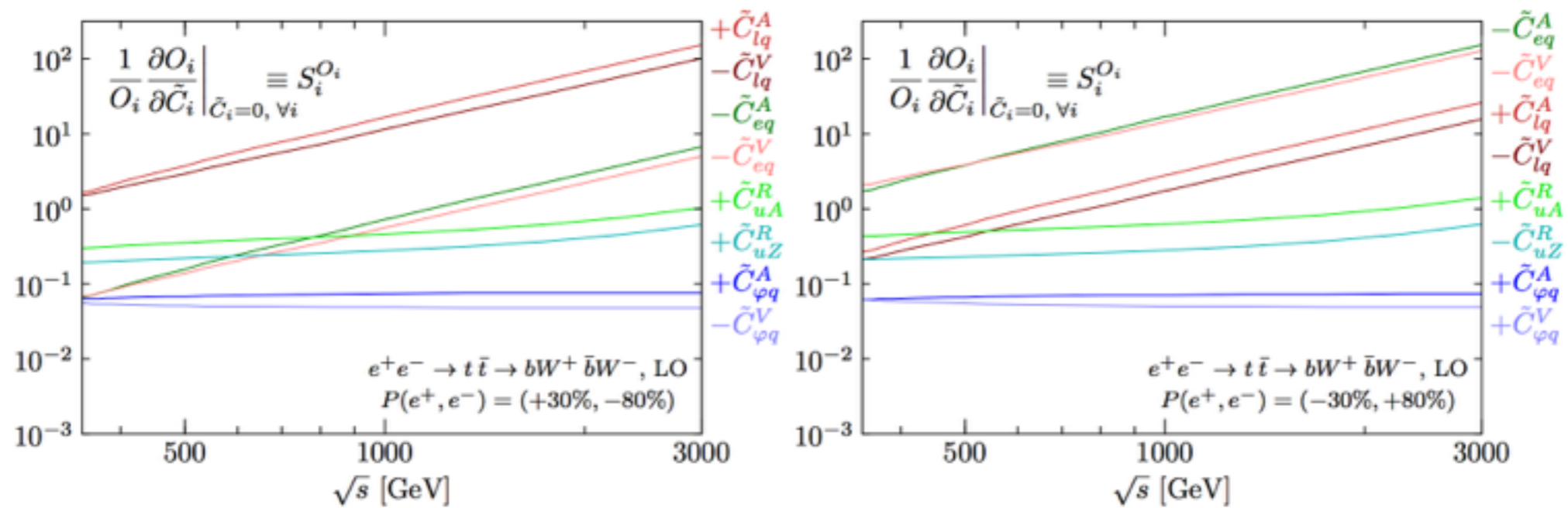
3. statistically optimal:  $O_i \sim \frac{\sin(i\phi)}{1 + \cos \phi}$

$\Rightarrow$  area ratios 1.9 : 1.7 : 1

Previous applications in  $e^+e^- \rightarrow t\bar{t}$ :

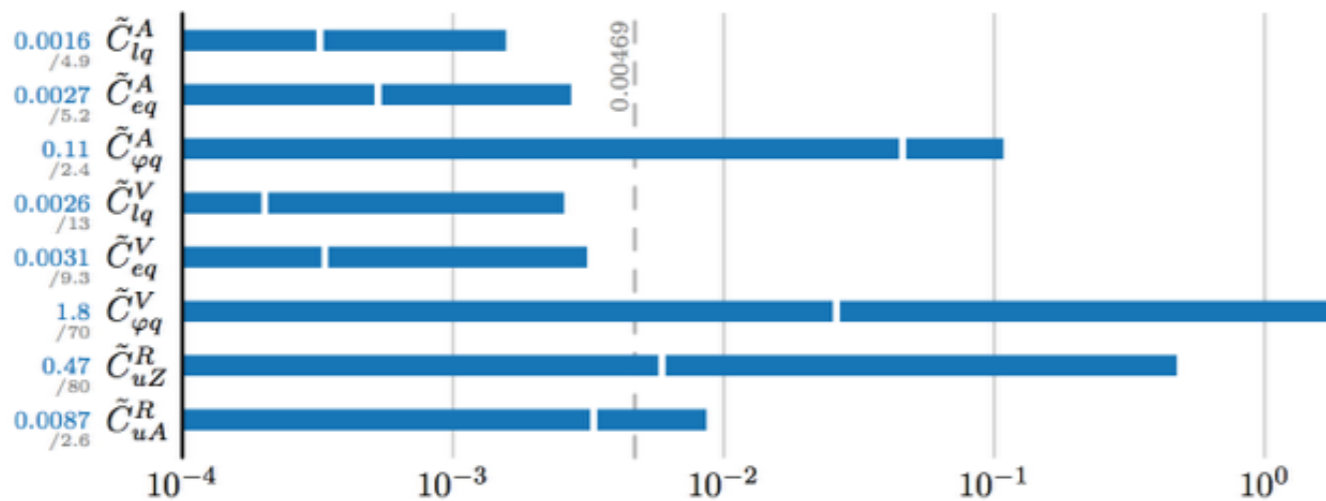
[Grzadkowski, Hioki '00] [Janot '15] [Khiem et al '15]

# Statistically optimal observables sensitivities

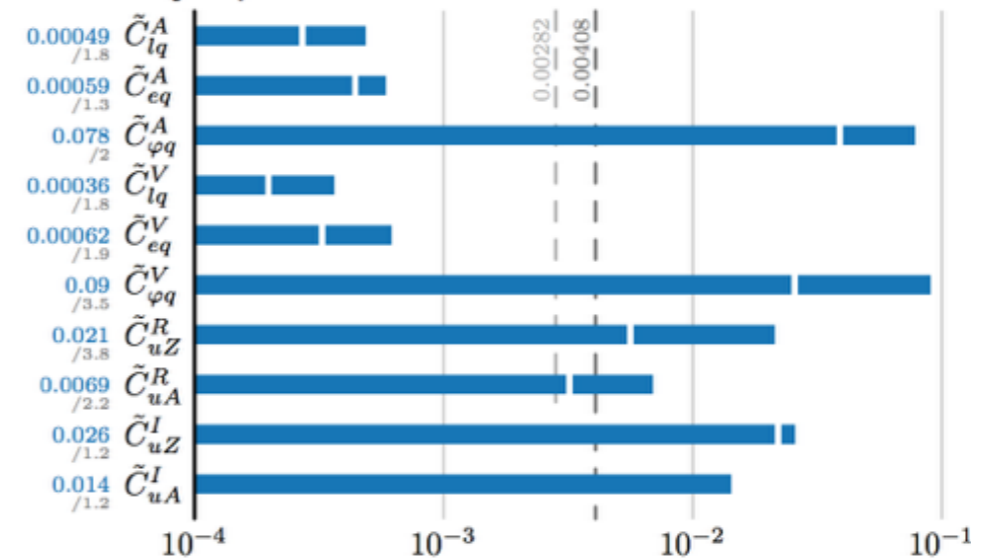


Comparison in the global limits (500GeV + 1TeV for 2 pols.):

$\sigma + A_{\text{FB}}$



Statistically optimal observables:

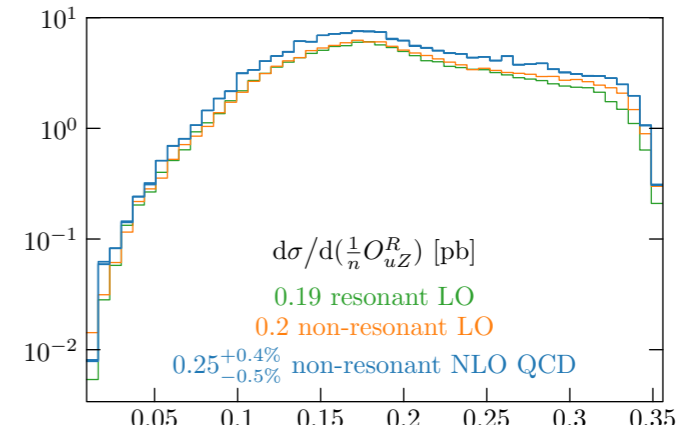
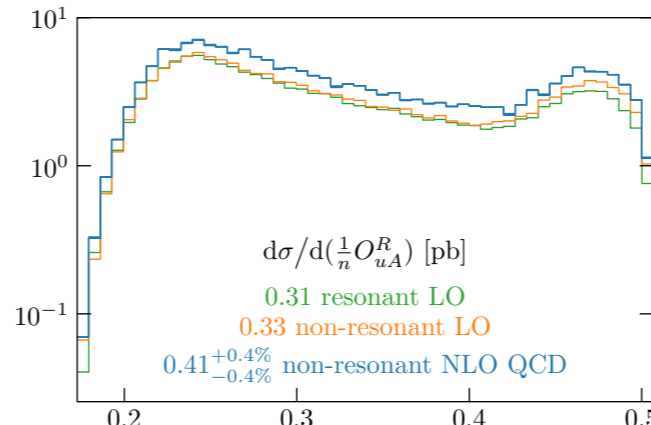
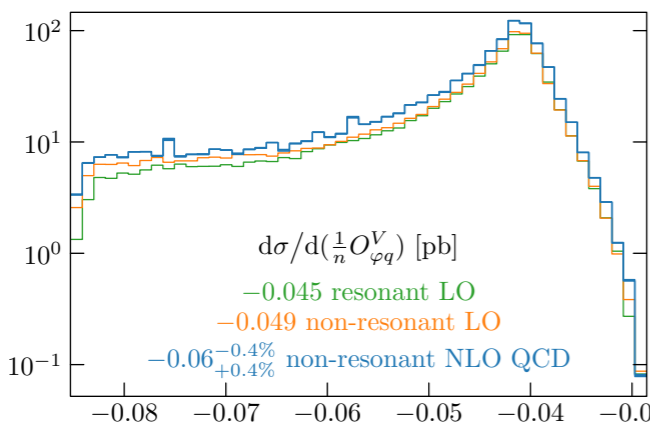
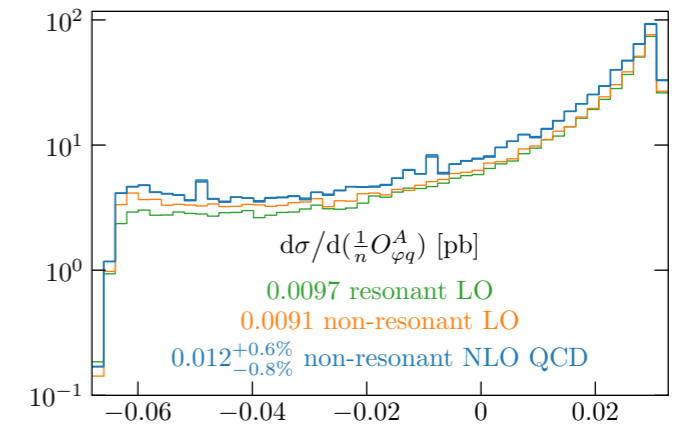
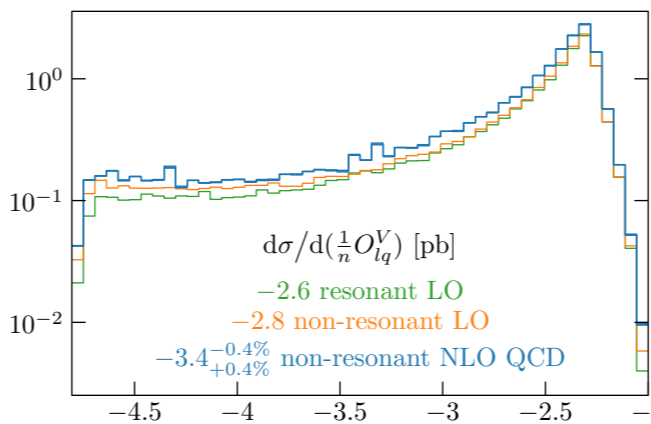
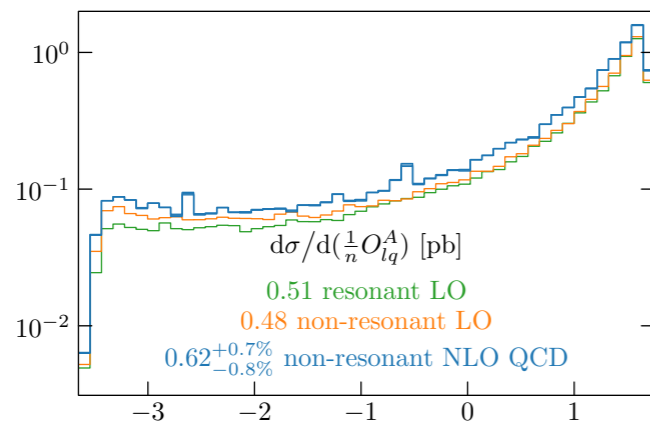
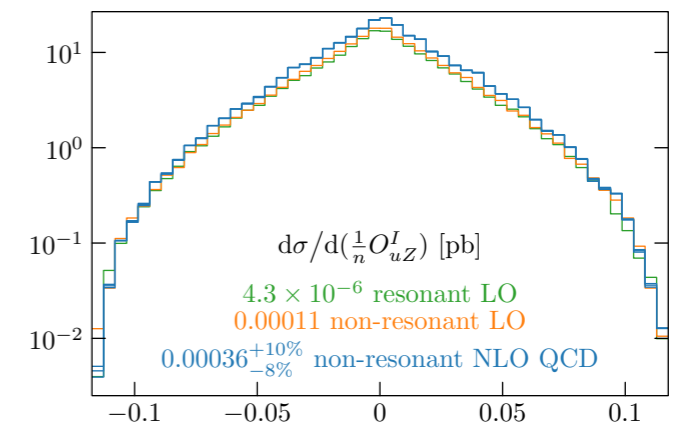
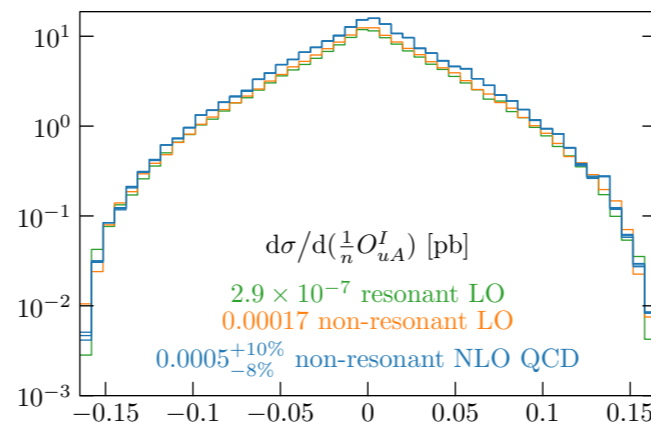
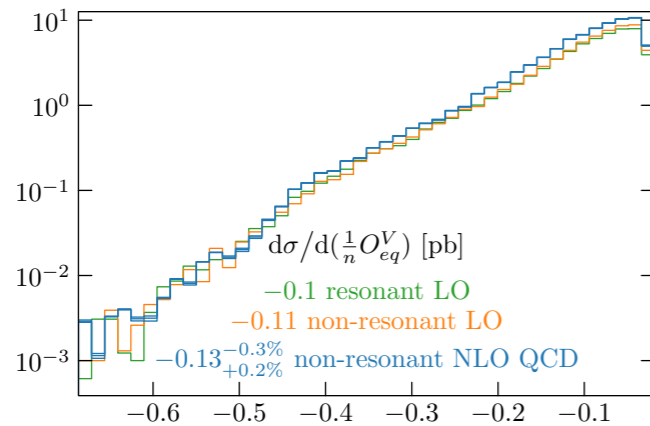
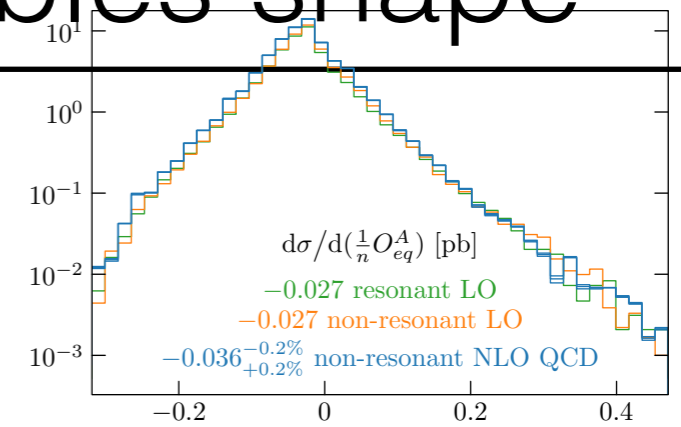


- **Even better individual limits**
- **Global limits within a factor 1.3 to 3.5**

# Statistically optimal observables shape

Example for 500 GeV ( $e^-, e^+$ ) = (-0.8, 0.3)

Theory uncertainties under study



# Full-simulation at CLIC380 and ILC500



# Full-simulation

Studied process

$$e^-e^+ \rightarrow t\bar{t} \rightarrow W^+bW^-\bar{b} \rightarrow l\nu b\bar{b}q\bar{q}$$

$$\sqrt{s} = \{380, 500, 1000, 1400, 3000\} \text{ GeV}$$

■ CLIC

■ ILC

	380 GeV	500 GeV	1 TeV	1.4 TeV	3 TeV
Pol (e-, e+)	(-0.8, 0)	(-0.8, +0.3)	(-0.8, +0.2)	(-0.8, 0)	(-0.8, 0)
	(+0.8, 0)	(+0.8, -0.3)	(+0.8, -0.2)	(+0.8, 0)	(+0.8, 0)
$\sigma$ [L,R] (fb)	792	930	256	113	25
$\sigma$ [R,L] (fb)	418	480	142	66	15
Lumi (fb-1)	500	500	1000	1500	3000

**Studies at CLIC380 and ILC500 included in I. Garcia thesis**

(<https://cds.cern.ch/record/2239794?ln=en>)

**ILC@500GeV L=500fb<sup>-1</sup>**

[arXiv:1505.06020]

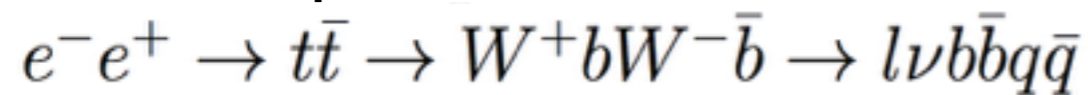
$\mathcal{P}_{e^-, e^+}$	$(\delta\sigma/\sigma)_{\text{stat.}} (\%)$	$(\delta A_{\text{FB}}^t/A_{\text{FB}}^t)_{\text{stat.}} (\%)$
-0.8, +0.3	0.47	1.8
+0.8, -0.3	0.63	1.3

**CLIC@380GeV L=500fb<sup>-1</sup>**

$\mathcal{P}_{e^-, e^+}$	$(\delta\sigma/\sigma)_{\text{stat.}} (\%)$	$(\delta A_{\text{FB}}^t/A_{\text{FB}}^t)_{\text{stat.}} (\%)$
-0.8, 0	0.47	3.8
+0.8, 0	0.83	4.6

# Full-simulation at CLIC@380 and ILC@500

Studied process



Same cuts used in previous studies which reduce background.

Signal selection:

- **Hadronic top in the range:  $120 < m_t < 230$**
- **Hadronic W:  $50 < m_W < 110$**
- **only 1 lepton per event**
- **2 b-tags (b-tag1 > 0.8 and b-tag2 > 0.5)**

Statistical uncertainties:

$$O_i = \left( \sum \sigma_i / \sigma_0 \right)_{\text{(normalization)}}$$

$$O_i = 1/n \left( \sum \sigma_i / \sigma_0 \right)_{\text{(distribution mean)}}$$

statistical uncertainty [%]	cross-section	lqA	eqA	pqA	lqV	eqV	pqV	ReuZ	ReuA	ImuZ*	ImuA*
380 (e-,e+) = (-0.8, 0)	0,8	3	5	3	0,1	0,5	0,1	0,2	0,1	1E-3	2E-3
380 (e-,e+) = (0.8, 0)	0,8	5	4	4	0,5	0,1	0,3	0,2	0,1	2E-3	2E-3
500 (e-,e+) = (-0.8, 0.3)	0,6	2	8	2	0,2	4	0,2	0,3	0,2	2E-3	4E-3
500 (e-,e+) = (0.8, -0.3)	0,8	6	2	2	2	0,4	0,7	0,7	0,3	4E-3	7E-3

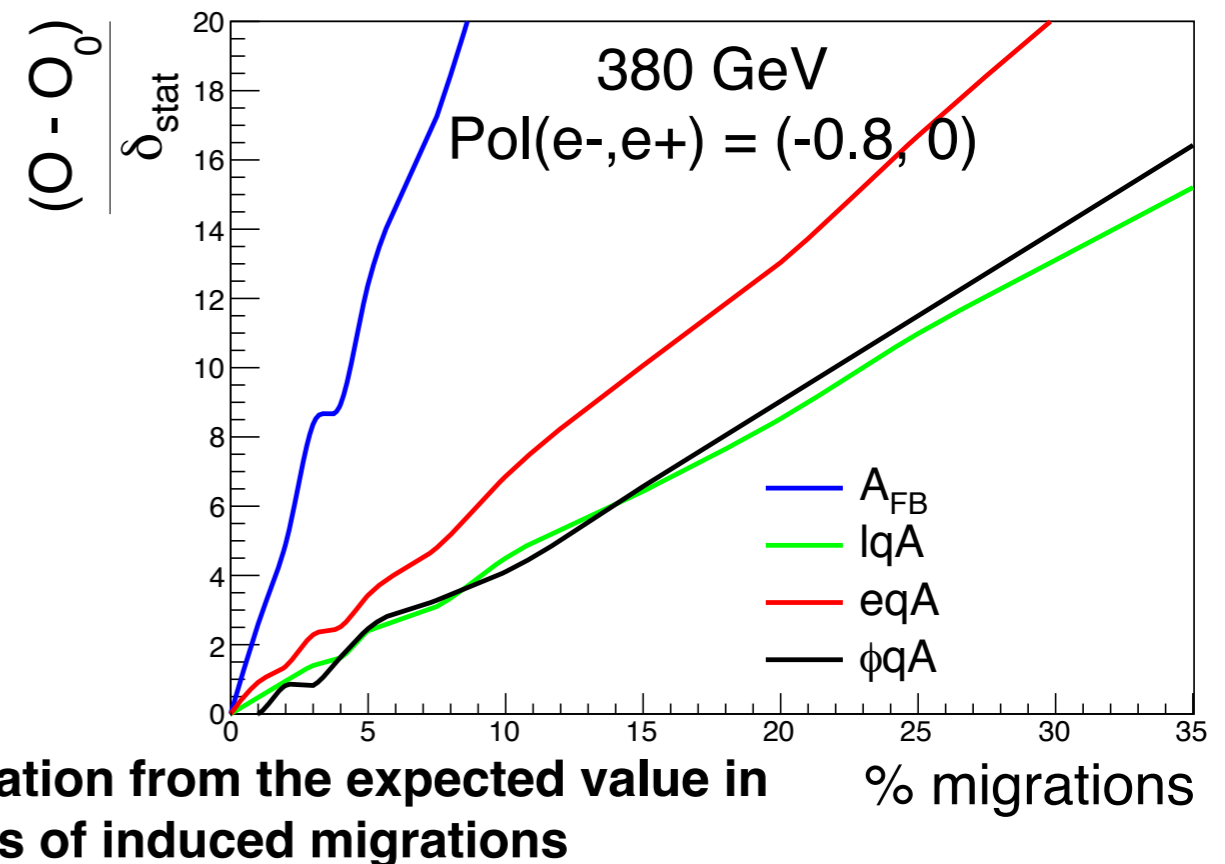
\*Absolute uncertainty

# Reconstruction effects

Need of a quality cut  
(mainly for reducing  
migrations - wrong  
W-b pairing)

$$\chi^2 = \left( \frac{\gamma_t - \gamma_t^0}{\sigma_{\gamma_t}} \right)^2 + \left( \frac{E_b^* - E_b^{*0}}{\sigma_{E_b^*}} \right)^2 + \left( \frac{\cos \theta_{bW} - \cos \theta_{bW}^0}{\sigma_{\cos \theta_{bW}}} \right)^2$$

	efficiency	quality cut chi2 < X	efficiency after quality cut
380L	37%	5	<b>18%</b>
380R	33,3%	40	<b>30,4%</b>
500L	34,4%	50	<b>29,4%</b>
500R	35%	50	<b>30,1%</b>



- Similar behaviour we observed in the  $A_{FB}$  reconstruction.
- From [arXiv:1505.06020](https://arxiv.org/abs/1505.06020): “It is expected that these ambiguities can be (partially) eliminated by an event-by-event determination of the charge of the b quark from the t decay.”
- Study of this b-charge determination in  $e^+e^- \rightarrow bb^-$ : [arXiv:1709.04289](https://arxiv.org/abs/1709.04289)

# Systematic uncertainties

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## Selection effects

Normalization: Biases around  $3\sigma$

Shape: Selection biases around  $1\sigma - 3\sigma$

**Residual uncertainty  
expected to be smaller  
than the effect**

## Reconstruction effects

Normalization: biases  $< 1\sigma$

Shape: Reconstruction biases around  $1\sigma - 2\sigma$

## Beam structure effects (using WHIZARD 2.6.0 for MC generation)

### Beamstrahlung (switching on/off CIRCE2 package)

Normalization:  $20\sigma$

Shape: Biases  $< 1\sigma$  in all cases

**Uncertainty to be estimated  
with Bhabha scattering study**

### ISR (Switching on/off ISR)

Normalization:  $20\sigma$

Shape: Biases around  $1\sigma - 2\sigma$

**Uncertainty from  
parameters variation  $< 1\%$**

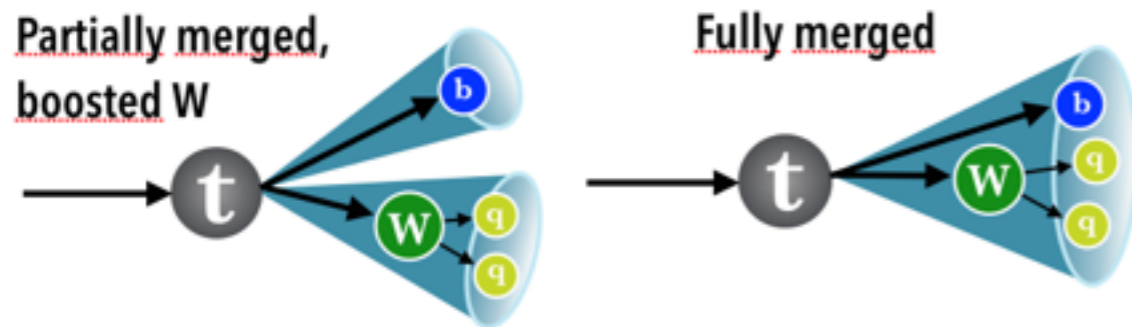
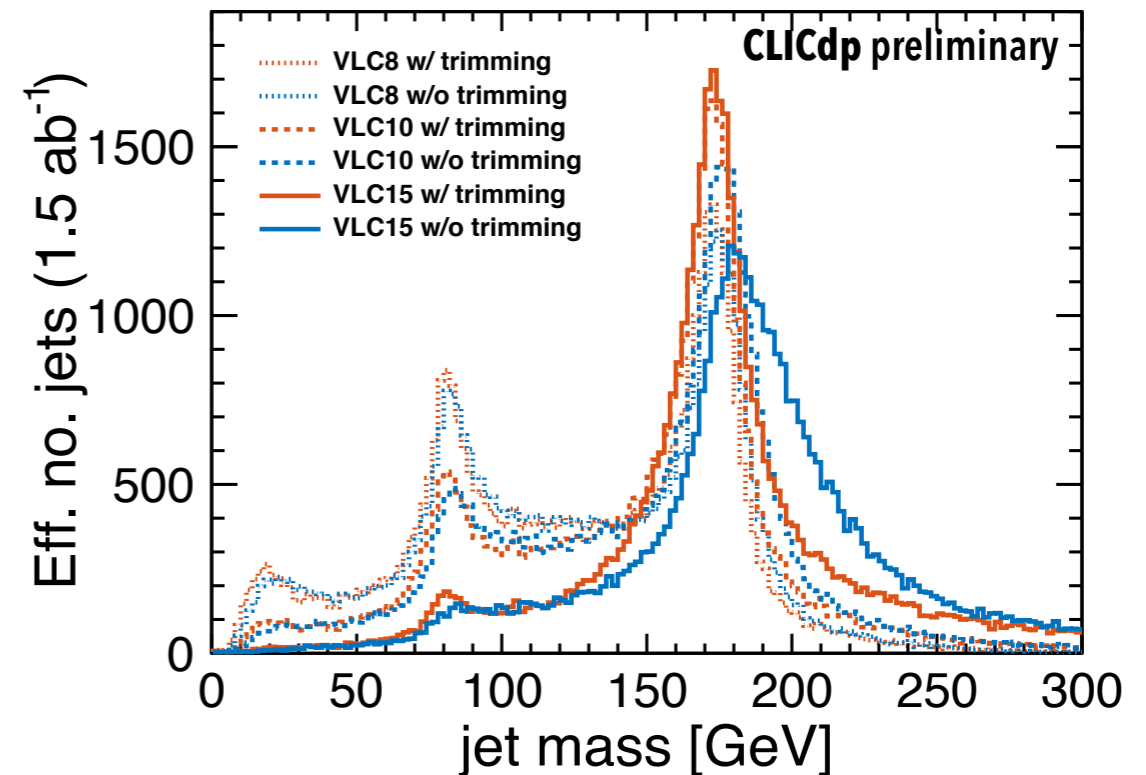
# Full-simulation at high energies

For a detailed explanation visit R. Ström's talk at CLICdp Collaboration Meeting: <https://indico.cern.ch/event/633975/contributions/2689114/>

# Boosted top reconstruction techniques

- Collimated decay products - Identify and correctly assign the top decay products
- **Resolved analysis** - Production near threshold (lower effective centre-of-mass due to ISR, beamstrahlung), use b-tagging, search for W, or 3 jets with a combined invariant mass near  $m_t$
- **Boosted analysis** - **Standard identification techniques may not work**: b-tagging not foreseen, tracks are very close to each other, W decay products not isolated from each other or b-jet,
  - Idea: tag tops by identifying prongy sub-structure

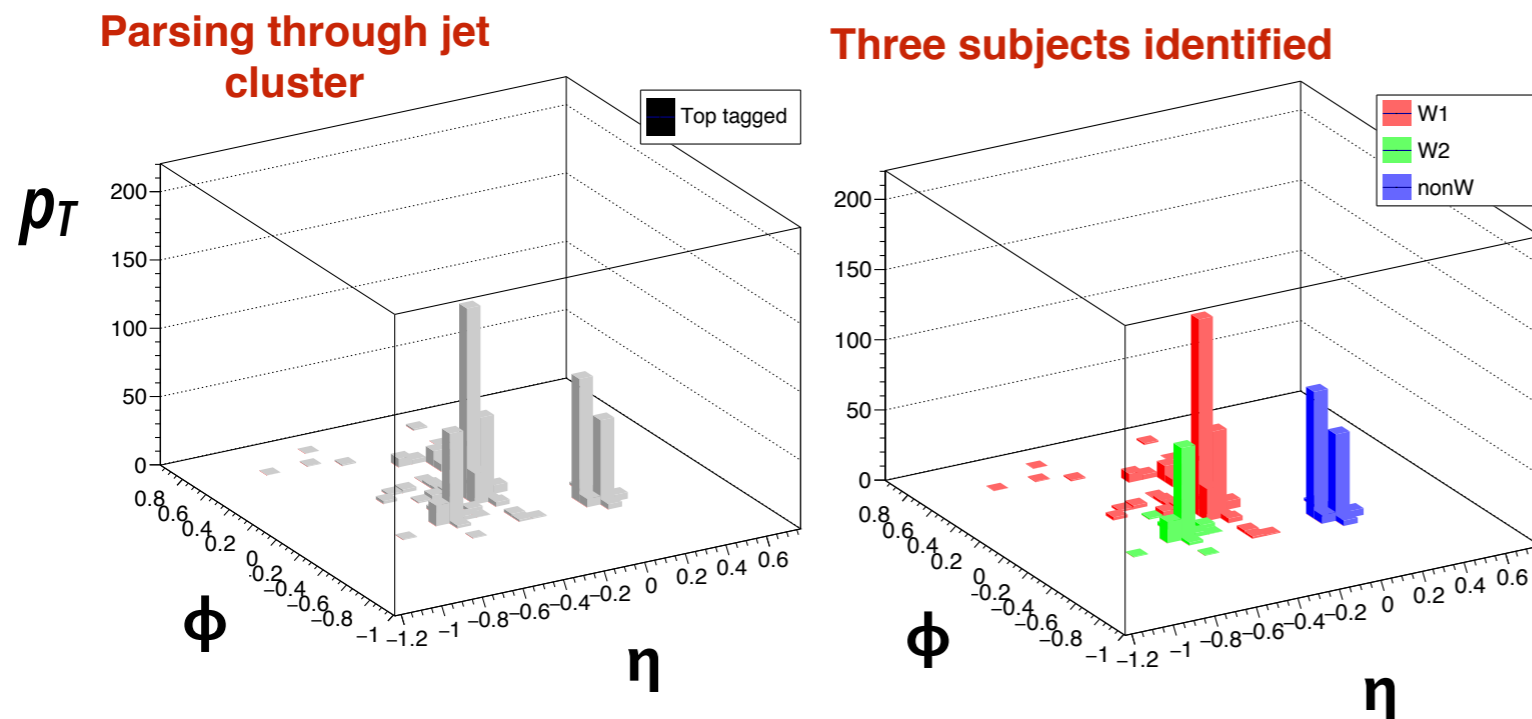
Optimization in jet clustering parameters by Rickard Ström  
Fully-hadronic decay mode reconstruction



- Jet clustering (incl. trimming)
- 2 exclusive large-R jets
- Jet tagging:
  - Parsing sub-structure (**method 1**)
  - Jet structure variables (**method 2**) - **not explained here, see Alasdair Winter's talk at CLIC WS 2017** (<https://indico.cern.ch/event/577810/contributions/2485031/>)
- Flavour-tagging (sub-jet, fat-jet)

# Parsing sub-structure (method 1)

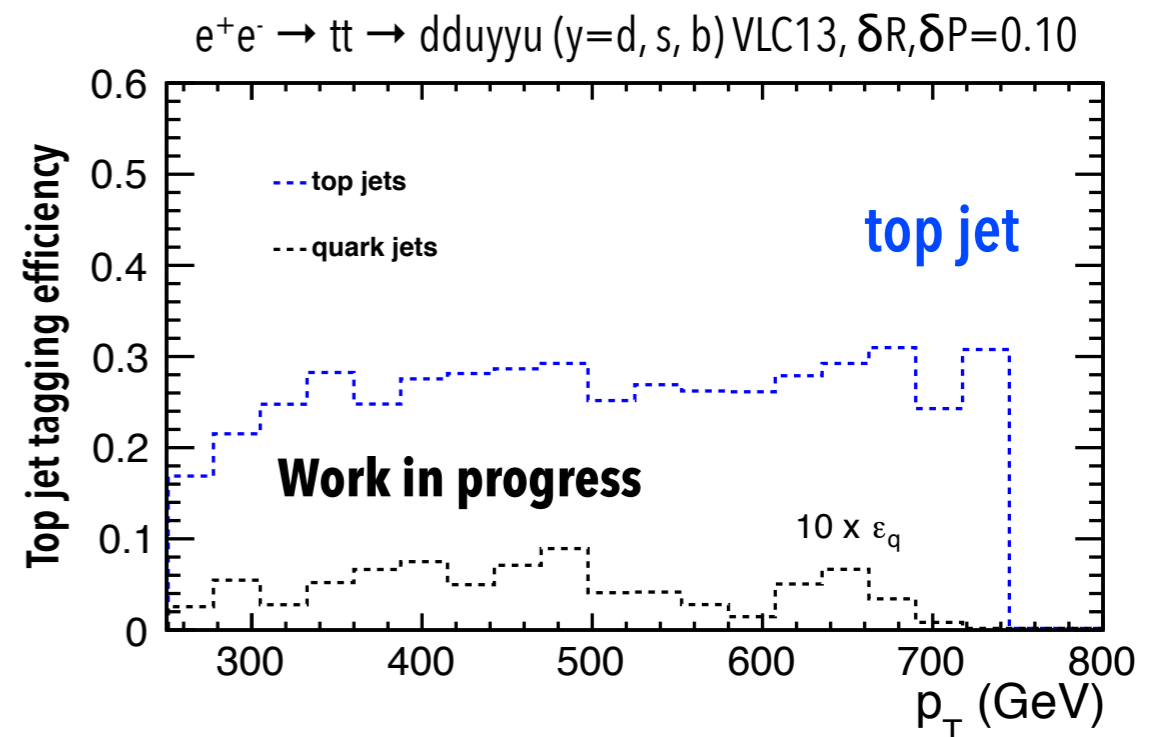
Jet de-clustering (FastJet extension), DOI: 10.1103/PhysRevLett.101.142001



- VLC jet clustering algorithm ( $R=1.5$ ,  $\beta=1$ ,  $\gamma=1$ ) + trimming
- "JH Top Tagger"
- kinematic cuts ( $m_t \in [145, 205]$  GeV,  $m_W \in [65, 95]$  GeV)

## JH Top Tagger - results

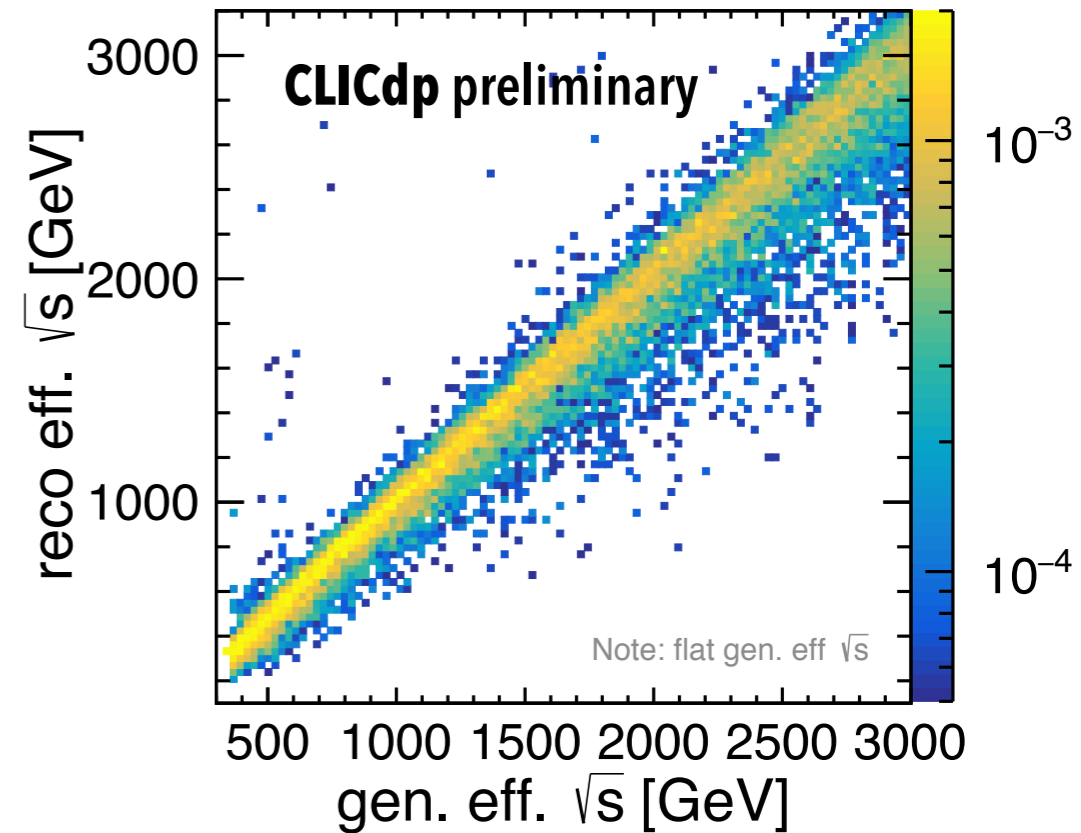
- Top quark mass recovered for sufficiently large- $R$  jet (efficiency drop for  $R < 1.3$ )
- Good discrepancy towards background processes without top
- More efficient than simple mass cut (still being optimised)



# Full-simulation at CLIC@1.4 and CLIC@3 TeV

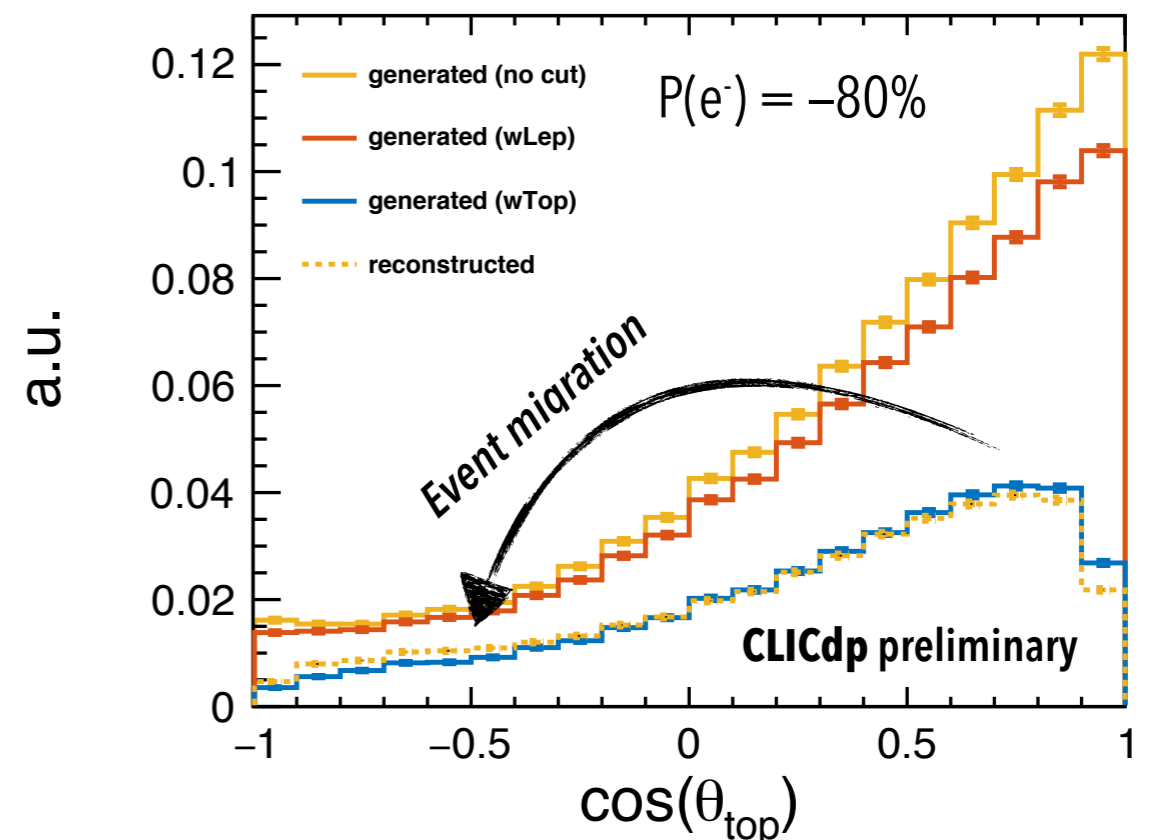
## Event selection

- Technical cut (gen. level) in  $\sqrt{s}$ ' (same cut can be done at reconstruction level)
- 1 isolated lepton, 1 top tagged jet ("JH Top Tagger")
- Flavour tagging (fat-jet / sub-jet)  $\rightarrow$  BDT
- Exploiting kinematics of semi-leptonic side  $\rightarrow$  BDT



## Top quark $A_{FB}$ results

- Less migration is observed for  $P(e^-) = +80\%$   
Backgrounds substantially reduced
- Relative error on  $A_{FB}$ :
  - $P(e^-) = -80\%$ :  $\sim 2\%$  (signal only)
  - $P(e^-) = +80\%$ :  $\sim 3\%$  (signal only)
- Both methods yield a similar result

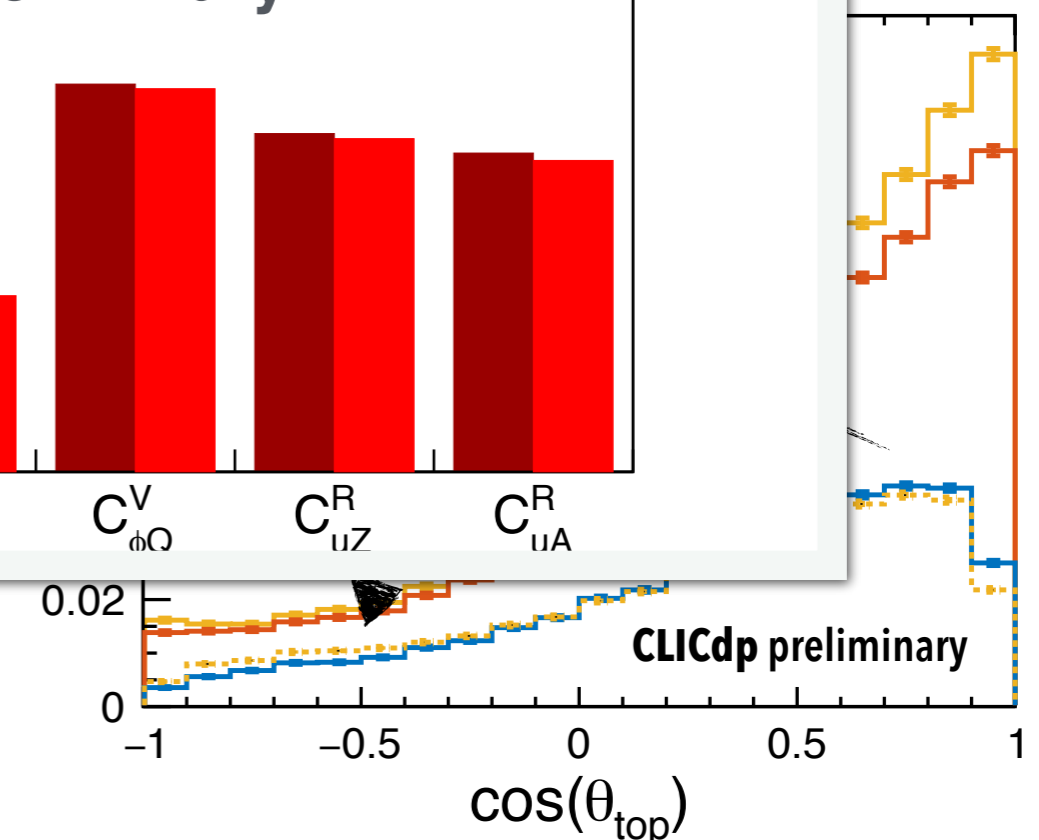
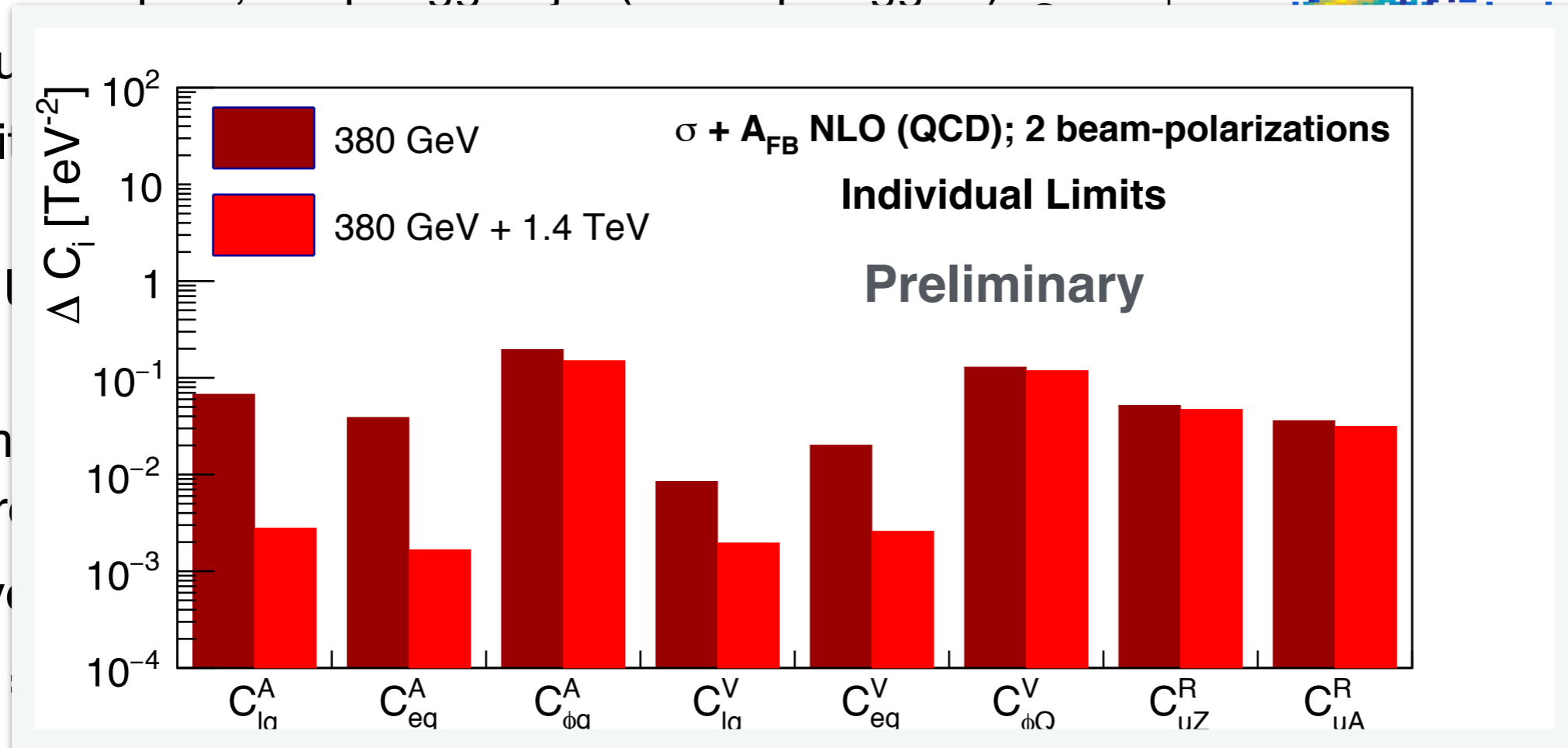
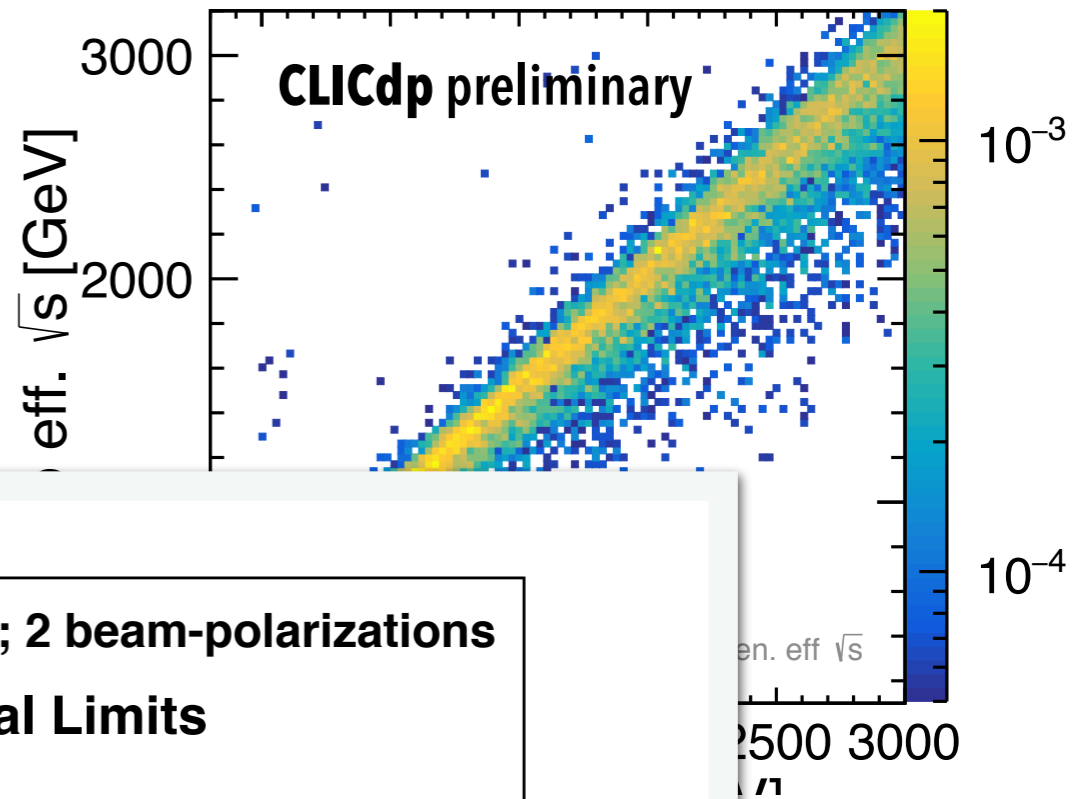




# Full-simulation at CLIC@1.4 and CLIC@3 TeV

## Event selection

- Technical cut (gen. level) in  $\sqrt{s}$ ' (same cut can be done at reconstruction level)
- 1 isolated lepton, 1 top tagged jet ("JH Top Tagger")
- Flavour
- Exploit
- Top quark
- Less m
- Backgr
- Relative
- $P(e^-)$
- $P(e^-) = +80\%$ :  $\sim 3\%$  (signal only)
- Both methods yield a similar result



# Conclusions

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- Cross-section +  $A_{FB}$  are not enough for global EFT fit. Top polarization at different axes and CP-odd observables help in the operators disentangling.
- Optimal observables seem to be the proper solution and are found to be robust
- Reconstruction new techniques at high energies are making progress providing first results for  $A_{FB}$  @CLIC1400.

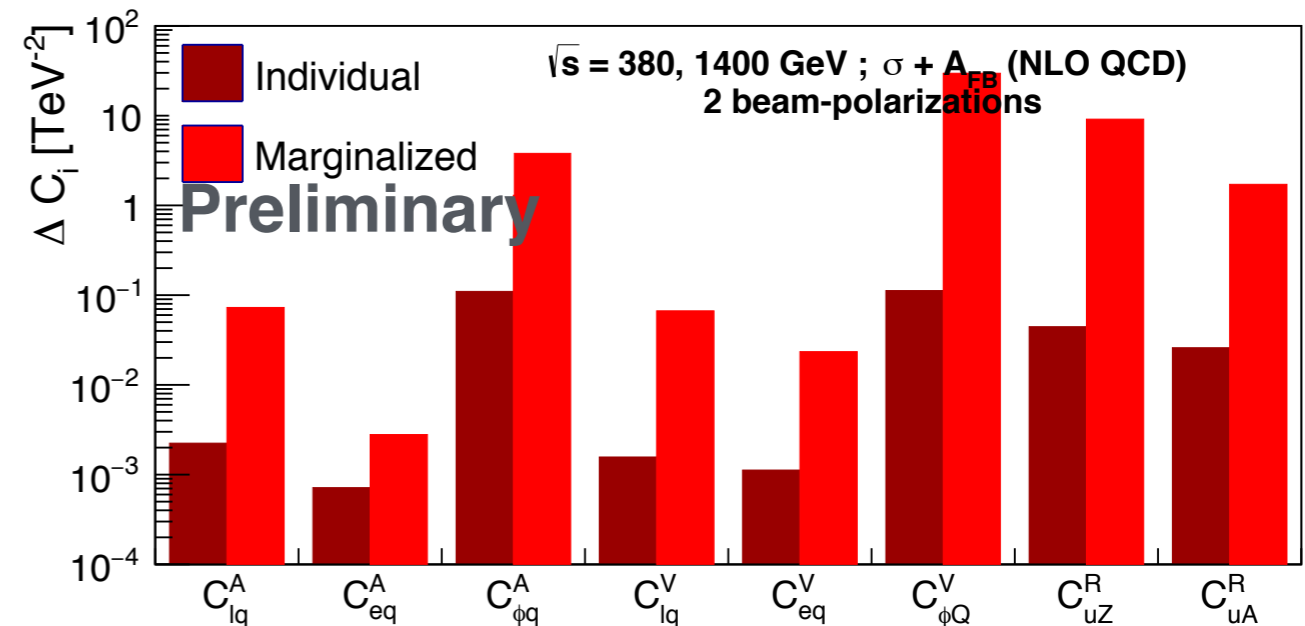
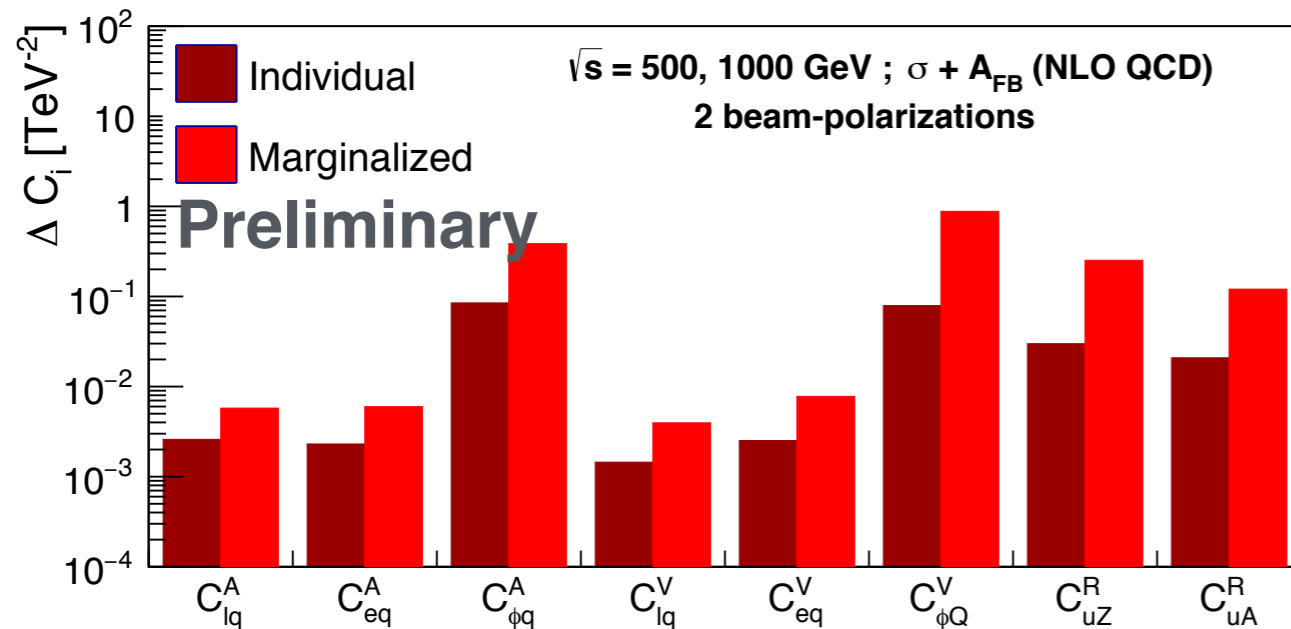
**Back up**

# Global Fit: $A_{FB} + \sigma$

Studied process  $e^-e^+ \rightarrow W^+bW^-\bar{b}$  @NLO [Motivation from arXiv:1411.2355]

ILC: **500 GeV + 1 TeV**

CLIC: **380 GeV + 1.4 TeV + (3) TeV**



**Individual:** assuming variation in only 1 parameter each time.

**Marginalized:** assuming variation in all the parameters at the same time.

Similar behaviour at  $e^-e^+ \rightarrow t\bar{t}$  @LO and  $e^-e^+ \rightarrow W^+bW^-\bar{b}$  @NLO (QCD)

Low uncertainties are achieved, but we can do it better

We should improve the marginalized fit

# Some technical numbers at reconstruction

<https://cds.cern.ch/record/2239794?ln=en>

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**CLIC380** (Repository <https://twiki.cern.ch/twiki/bin/view/CLIC/MonteCarloSamplesForTopPhysics>)

- Jet clustering: VLC algorithm ( $R=1.6$ ,  $\beta = 0.8$ ,  $\gamma = 0.8$ ).

**ILC500**

- Jet clustering: VLC algorithm ( $R=1.2$ ,  $\beta = 0.8$ ,  $\gamma = 0.8$ ).

Collider	ILC	CLIC
Sample	$e^+e^- \rightarrow l^\pm \nu b \bar{b} q' \bar{q}$	$e^+e^- \rightarrow 6f (t\bar{t} \text{ compatible})$
$\sqrt{s}$ [GeV]	500	380
Luminosity [ $\text{fb}^{-1}$ ]	500	500
$P(e^-), P(e^+)$	$\mp 1, \pm 1$	$\mp 0.8, 0$
Detector model	ILD_o1_v05 [54]	CLIC_ILD_CDR [53]
Number of BX	1	300
Background	1.7 $\gamma\gamma \rightarrow \text{hadrons} / \text{BX}$	0.0464 $\gamma\gamma \rightarrow \text{hadrons} / \text{BX}$

[53] L. Linssen, A. Miyamoto, M. Stanitzki and H. Weerts, Physics and Detectors at CLIC: CLIC Conceptual Design Report, 1202.5940.

[54] H. Abramowicz et al., The International Linear Collider Technical Design Report - Volume 4: Detectors, 1306.6329.

# CPV: Optimal CP-odd observables

The **CP-violating effects** in  $e^+e^- \rightarrow t\bar{t}$  manifest themselves in specific **top-spin effects**, namely **CP-odd top spin-momentum correlations and  $t\bar{t}$  spin correlations**.

$$e^+(\mathbf{p}_+, P_{e^+}) + e^-(\mathbf{p}_-, P_{e^-}) \rightarrow t(\mathbf{k}_t) + \bar{t}(\mathbf{k}_{\bar{t}})$$

$$t \bar{t} \rightarrow \ell^+(\mathbf{q}_+) + \nu_\ell + b + \bar{X}_{\text{had}}(\mathbf{q}_{\bar{X}})$$

$$t \bar{t} \rightarrow X_{\text{had}}(\mathbf{q}_X) + \ell^-(\mathbf{q}_-) + \bar{\nu}_\ell + \bar{b}$$

- **CP-odd observables** are defined with the **four momenta available in  $t\bar{t}$  semi-leptonic decay channel**

$$\mathcal{O}_+^{Re} = (\hat{\mathbf{q}}_{\bar{X}} \times \hat{\mathbf{q}}_+^*) \cdot \hat{\mathbf{p}}_+,$$

$$\mathcal{O}_+^{Im} = -\left[1 + \left(\frac{\sqrt{s}}{2m_t} - 1\right)(\hat{\mathbf{q}}_{\bar{X}} \cdot \hat{\mathbf{p}}_+)^2\right] \hat{\mathbf{q}}_+^* \cdot \hat{\mathbf{q}}_{\bar{X}} + \frac{\sqrt{s}}{2m_t} \hat{\mathbf{q}}_{\bar{X}} \cdot \hat{\mathbf{p}}_+ \hat{\mathbf{q}}_+^* \cdot \hat{\mathbf{p}}_+$$

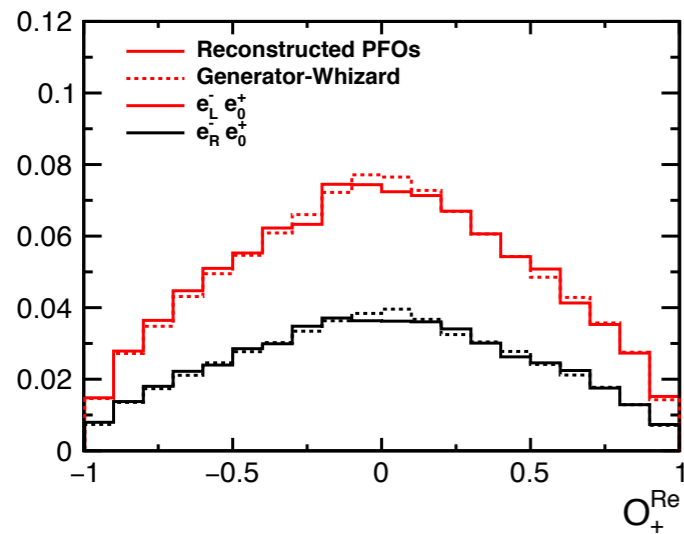
- The way to **extract** the **CP-violating form factor** is to construct **asymmetries sensitive to CP-violation effects**

$$\mathcal{A}^{Re} = \langle \mathcal{O}_+^{Re} \rangle - \langle \mathcal{O}_-^{Re} \rangle = c_\gamma(s) \text{Re}F_{2A}^\gamma + c_Z(s) \text{Re}F_{2A}^Z$$

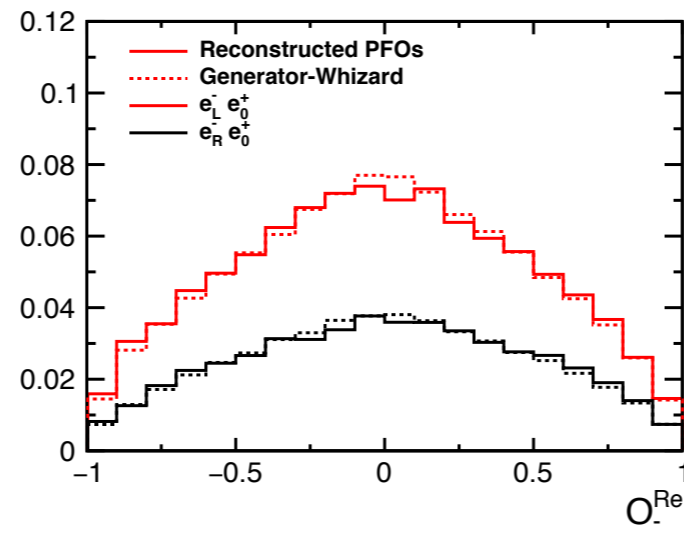
$$\mathcal{A}^{Im} = \langle \mathcal{O}_+^{Im} \rangle - \langle \mathcal{O}_-^{Im} \rangle = \tilde{c}_\gamma(s) \text{Im}F_{2A}^\gamma + \tilde{c}_Z(s) \text{Im}F_{2A}^Z$$

$$\begin{array}{cc} \mathcal{A}_{\gamma,Z}^{Re L} & \mathcal{A}_{\gamma,Z}^{Re L} \\ \mathcal{A}_{\gamma,Z}^{Im R} & \mathcal{A}_{\gamma,Z}^{Im R} \end{array}$$

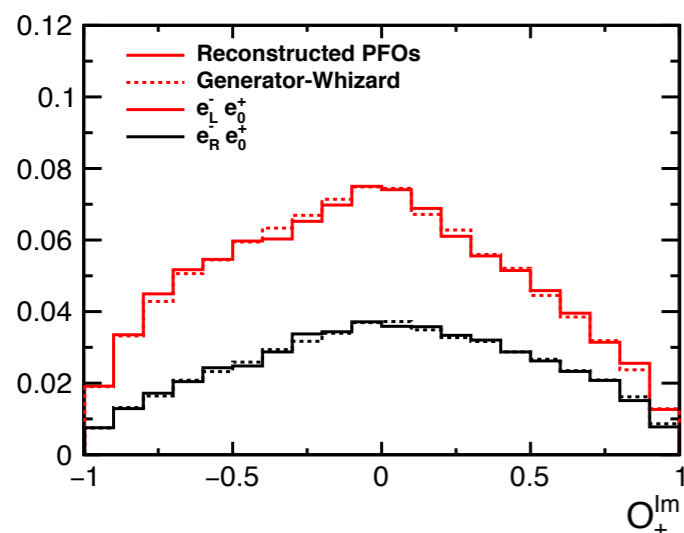
# CPV: Full-simulation: CLIC@380GeV



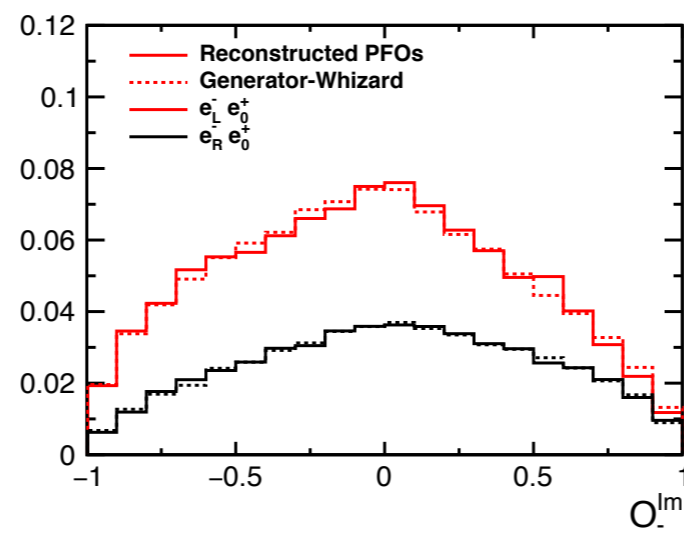
(a)  $\mathcal{O}_+^{Re}$



(b)  $\mathcal{O}_-^{Re}$



(c)  $\mathcal{O}_+^{Im}$



(d)  $\mathcal{O}_-^{Im}$

- Distributions are **centered at zero**
- **Differences** between reconstructed and generated events are **very small**.
- Any **distortions** in the reconstructed distributions are **expected to cancel in the asymmetries**  $A_{Re}$  and  $A_{Im}$
- **Asymmetries** are **compatible with zero** within the statistical error

polarization	$e_L^- (P_{e^-} = -0.8)$	$e_R^- (P_{e^-} = +0.8)$
$\mathcal{A}^{Re}$	$-0.00006 \pm 0.003$	$0.0072 \pm 0.003$
$\mathcal{A}^{Im}$	$0.0004 \pm 0.003$	$-0.0019 \pm 0.003$

# CPV: Coefficients vs sqrt(s)

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**The sensitivity of  $A_{\text{Re}}/A_{\text{Im}}$  to  $F_{2A}$  increases strongly with the c.o.m. energy**

$$P_{e^-} = -1, P_{e^+} = +1$$

c.m. energy $\sqrt{s}$ [GeV]	$c_\gamma(s)$	$c_Z(s)$	$\tilde{c}_\gamma(s)$	$\tilde{c}_Z(s)$
380	0.245	0.173	0.232	0.164
500	0.607	0.418	0.512	0.352
1000	1.714	1.151	1.464	0.983
1400	2.514	1.681	2.528	1.691
3000	5.589	3.725	10.190	6.791

$$P_{e^-} = +1, P_{e^+} = -1$$

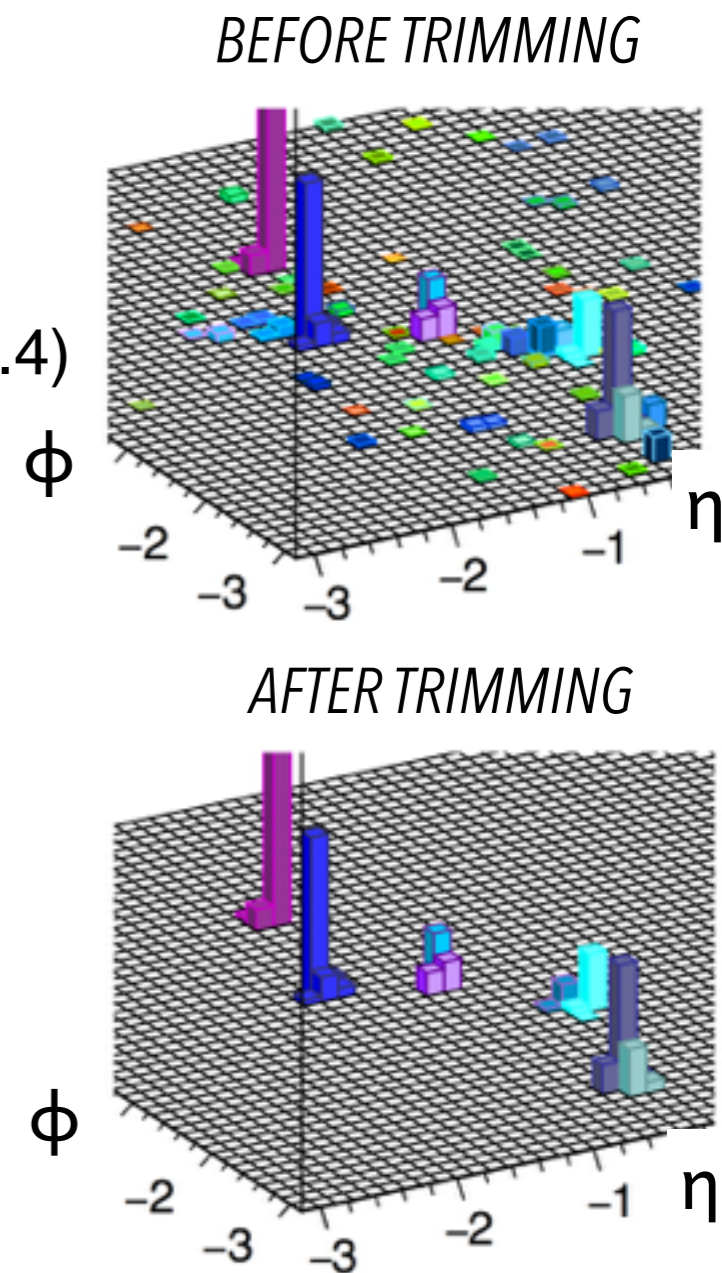
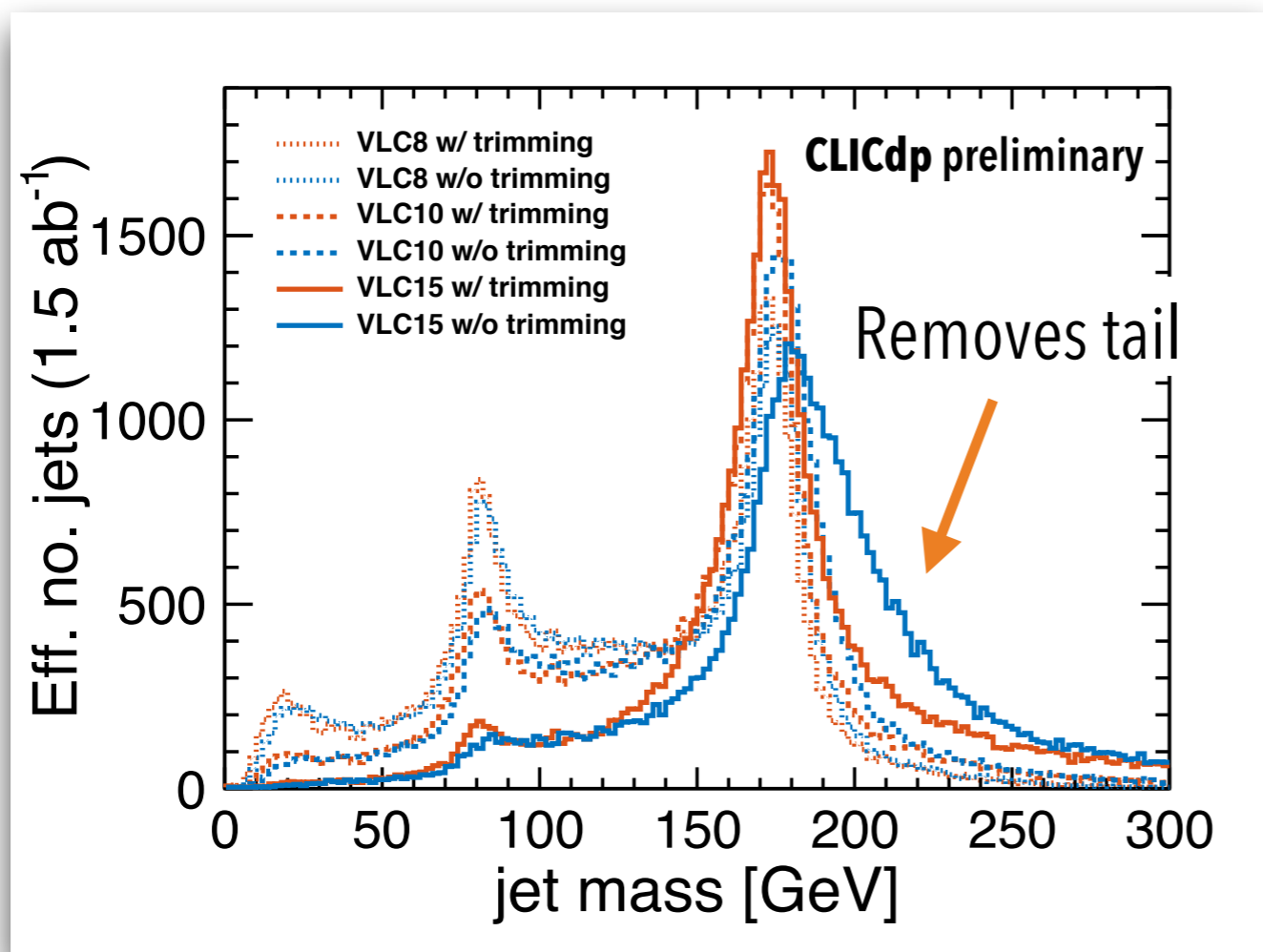
c.m. energy $\sqrt{s}$ [GeV]	$c_\gamma(s)$	$c_Z(s)$	$\tilde{c}_\gamma(s)$	$\tilde{c}_Z(s)$
380	-0.381	0.217	0.362	-0.206
500	-0.903	0.500	0.761	-0.422
1000	-2.437	1.316	2.081	-1.124
1400	-3.549	1.909	3.569	-1.920
3000	-7.845	4.205	14.302	-7.667

Thanks to Bernreuther



# High energies: Jet trimming

- **Jet trimming** is a complementary way to reduce the impact from beamstrahlung
- **Pre-clustering into micro-jets**
  - Inclusive clustering with minimum  $p_T$  threshold
  - generalised kt algorithm ( $\sim kt$  for  $e^+e^-$  + beam jets)
  - $p_T$  threshold and micro-jet radius optimised ( $E_{th}=5$  GeV,  $R=0.4$ )



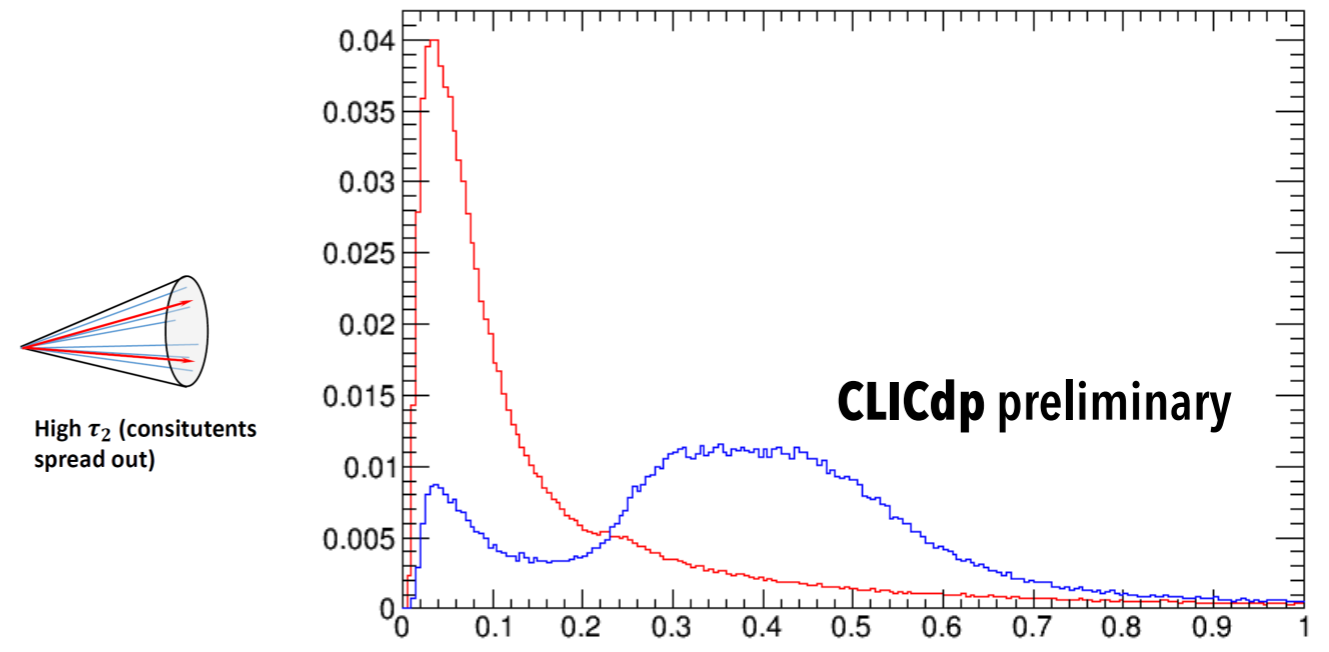
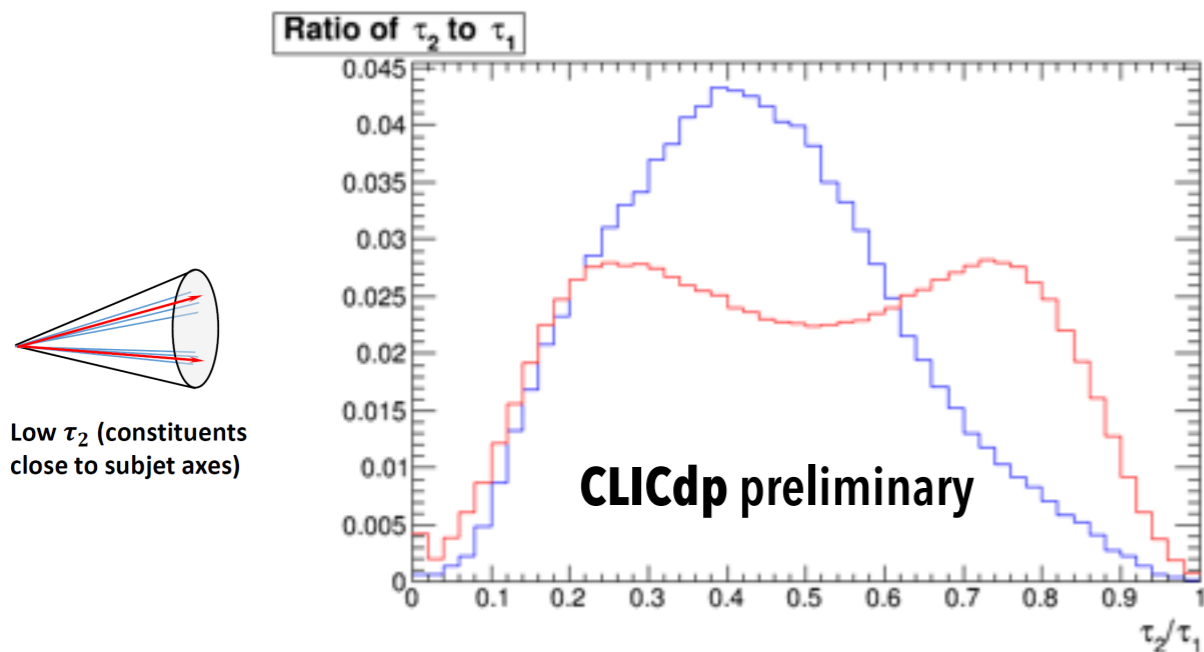
# High energies: Jet structure variables (method 2)

- Multiplicity - re-cluster fat jets into N “microjets” with kt algorithm R=0.05
- “N-subjettiness” - jet shape variable to measure consistency of jet to have N subjets [J.Thaler, K.Tilburg, [arXiv:1011.2268](https://arxiv.org/abs/1011.2268)]
- Angular distribution of subjets - re-cluster fat jet into 3 subjets and measure angular separation (identifies forced splitting)

$$\tau_N = \frac{1}{d_0} \sum_k p_{T k} \times \Delta R_k^{\min}$$

with  $d_0 \equiv \sum_k p_{T k} \times R$

$p_{T k}$ :  $p_T$  of constituent k  
 $\Delta R_k^{\min}$ : distance between constituent k & axis of closest subjet  
 $R$ : large-R jet distance parameter

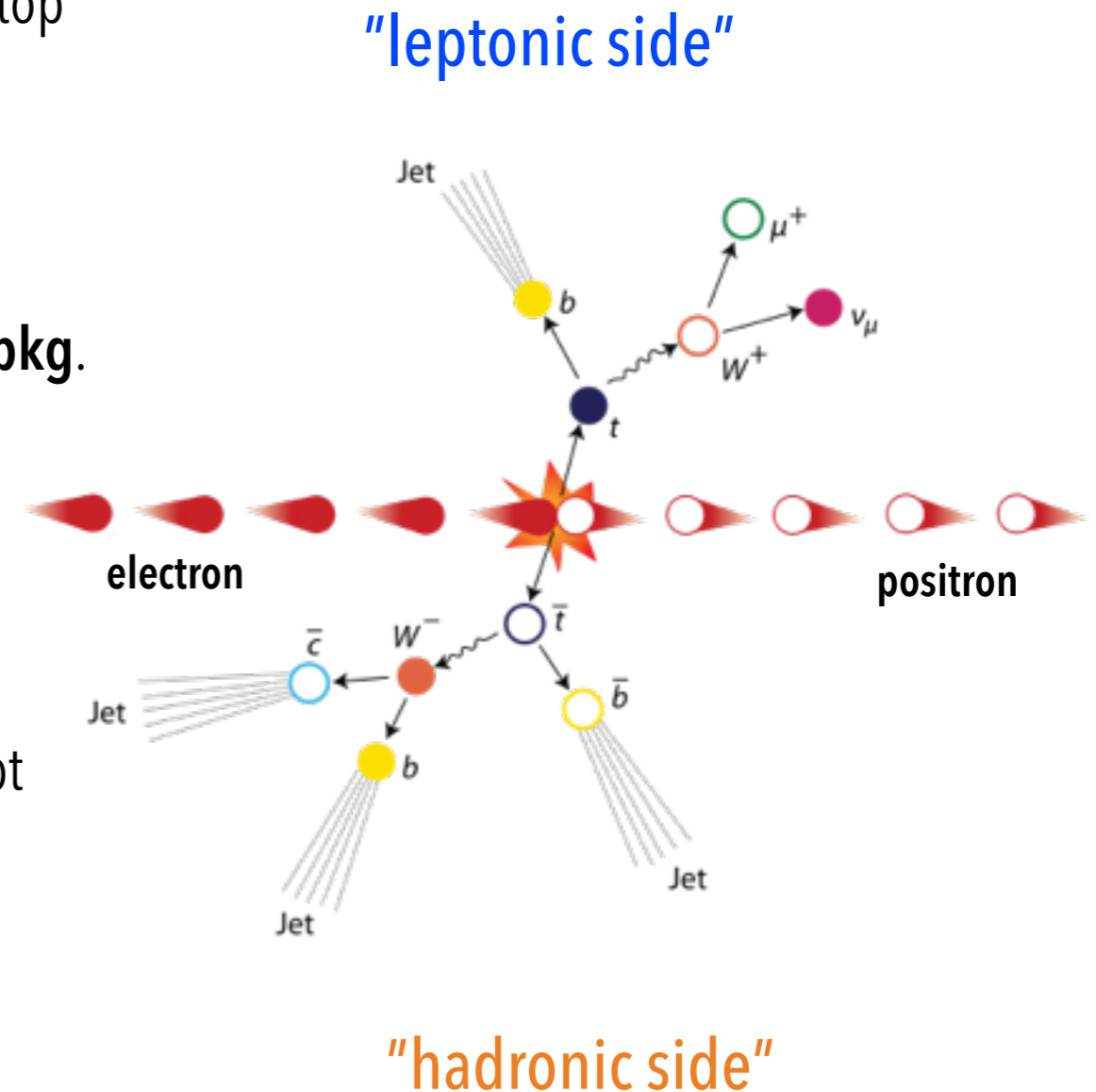


# High energies: General analysis strategy $t\bar{t} \rightarrow q\bar{q}q\bar{q}l\nu$

- Analysis concept studied at a benchmark collision energy of 1.4 TeV using CLIC-ILD
- Signal definition: semi-leptonic  $t\bar{t}$  ( $t\bar{t} \rightarrow q\bar{q}q\bar{q}l\nu$ )
- Use lepton charge to reconstruct the charge of the top/anti-top

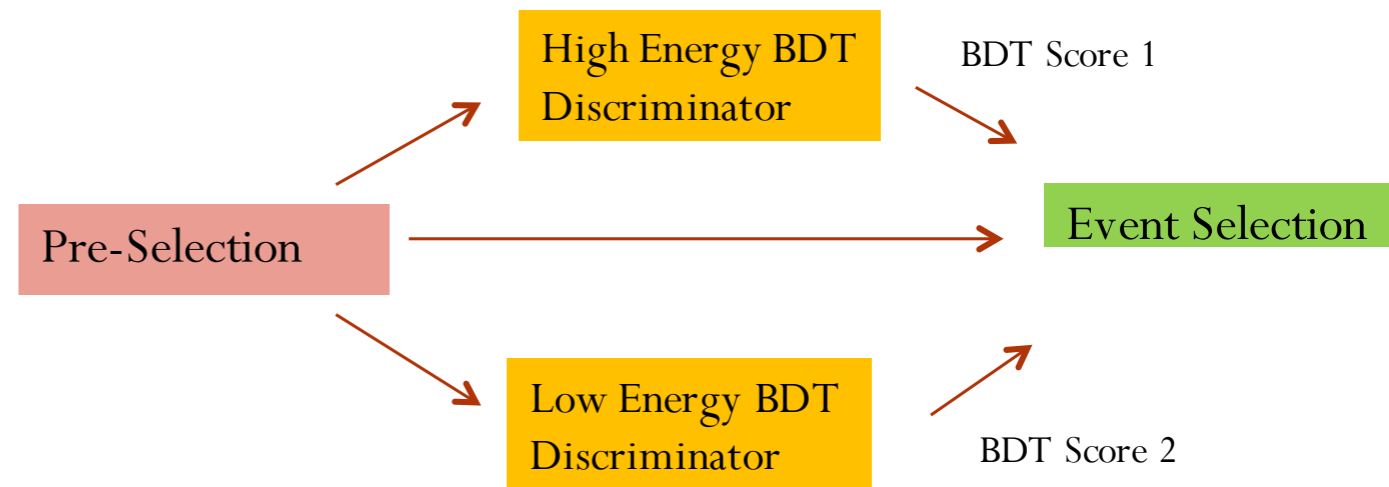
Event generation, detector simulation and reconstruction

- The results based on detailed MC studies incl. relevant **SM bkg.** processes
- Event generation using **WHIZARD** 1.95
- Fragmentation and hadronisation using **PYTHIA** 6.4
- **GEANT4** based simulations of the CLIC\_ILD detector concept
- **Pile-up** from gamma+gamma  $\rightarrow$  hadrons included
- Full reconstruction of the simulated events.
- **Particle flow** reconstruction using PandoraPFA
- $\Rightarrow$  Particle Flow Objects (PFO)



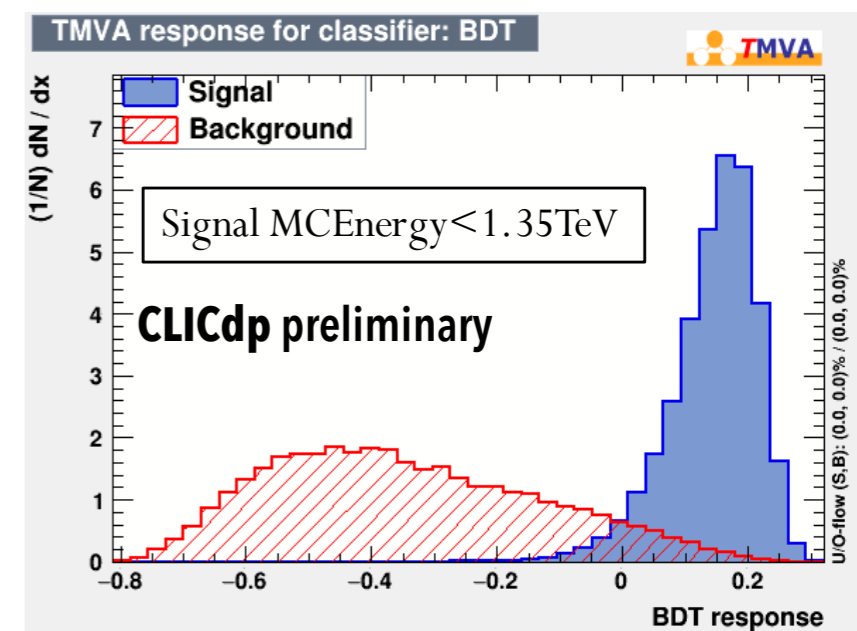
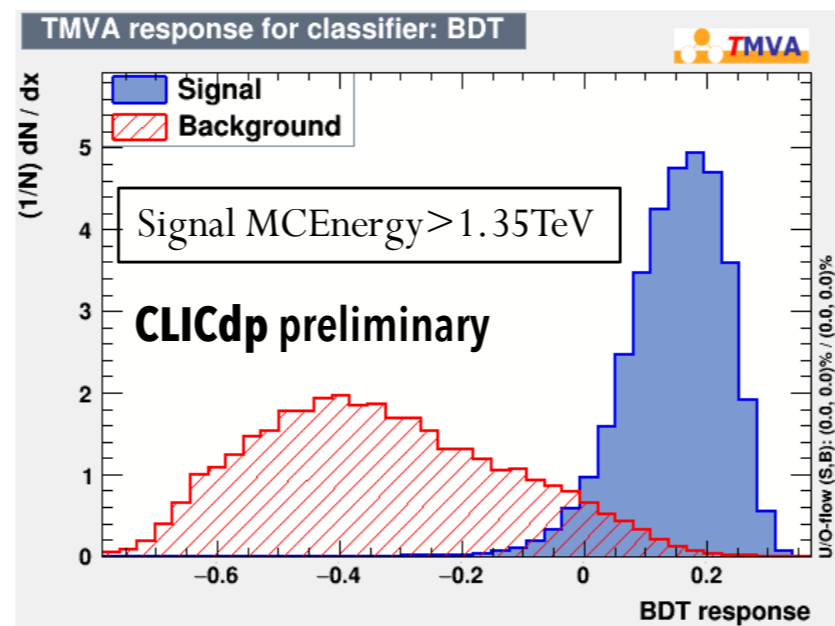
# High energies: Event selection - Method 2

- Technical cut (gen. level): two regions (different BDTs)
- 1 isolated lepton (based on Pandora PID)
- Pre selection (hadronic = highest jet energy)
- Jet structure variables in BDT (top tagging)



## Pre selection:

- Visible  $p_T > 200$  GeV
- Hadronic top:  $E > 100$  GeV
- Leptonic top  $p_T > 20$  GeV
- $Y_{23} < 7, Y_{34} < 9$



**$e^+e^- \rightarrow tt \rightarrow qq\bar{q}\bar{q}lv$ :**  
 LE: 31% efficiency  
 HE: 42% efficiency  
 (purity  $\sim 60\%$ )

# $\sqrt{s}'$ reconstruction at CLIC@1.4 and 3 TeV

- Agreement between  $\sqrt{s}'$ -generated and  $\sqrt{s}'$ -reconstructed is good
- Since the  $\sqrt{s}'$ -generated is very peaked around the nominal energy plots are re-normalised into using a flat  $\sqrt{s}'$ -generated distribution.

