

## Superradiant Transition and Diffraction radiation in the THz Region

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#### CrossMark

#### The SPARC linear accelerator based terahertz source

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Ultra-short electron beams, produced through the velocity bunching compression technique, are used to drive the SPARC linear accelerator based source, which relies on the emission of coherent transition radiation in the terahertz range. This paper reports on the main features of this radiation, as terahertz source, with spectral coverage up to 5 THz and pulse duration down to 200 fs, with an energy per pulse of the order of several micro-joule, and as electron beam longitudinal diagnostics. © 2013 American Institute of Physics. [http://dx.doi.org/10.1063/1.4794014]

The finite size of the screen (i.e., 30 mm x 30 mm), the vacuum chamber geometry (i.e., 63 mm vacuum window clear aperture, at 70 mm distance from the target, and 60 mm beam pipe radius) and the optics acceptance introduce a low frequency cut-off estimated to be 100 GHz



FIG. 1. Schematic layout of the SPARC test facility.





#### The SPARC linear accelerator based terahertz source

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$$
\sigma_t(Q)=AQ^B
$$

$$
S(t) = \frac{e^{-t^2/2\sigma_t^2}}{\sqrt{2\pi}\sigma_t} \leftrightarrow F(\omega) = e^{-\omega^2 A^2 Q^{2B}}
$$

 $\alpha$  .  $\alpha$ 

$$
I_{CTR} = \int_{\Delta\Omega} \int_0^\infty \frac{d^2I}{d\omega d\Omega} d\omega d\Omega \propto Q^{2-B}
$$







(a) Longitudinal bunch profile measured with the RFD in case of a 260 fs RMS bunch duration with 260 pC charge. (b) Corresponding measured CTR pulse energy density in μJ/THz as function of frequency (red squares). Dashed blue and solid olive curves correspond to the CTR pulse energy density calculated from the ideal GF formula and the generalized one, respectively, taking into account the measured form factor.

CTR autocorrelation function as measured through a Martin-Puplett interferometer. 3



#### Ultrabroadband terahertz source and beamline based on coherent transition radiation

S. Casalbuoni,<sup>1</sup> B. Schmidt,<sup>2</sup> P. Schmüser,<sup>2,3</sup> V. Arsov,<sup>2</sup> and S. Wesch<sup>2</sup> <sup>1</sup>Institute for Synchrotron Radiation, Research Center Karlsruhe, P.O. Box 3640, D-76021 Karlsruhe, Germany  ${}^{2}$ Deutsches Elektronen-Synchrotron DESY, Notkestrasse 85, 22607 Hamburg, Germany  $3$ Institut für Experimentalphysik, Universität Hamburg, Luruper Chaussee 149, 22607 Hamburg, Germany (Received 30 October 2008; published 25 March 2009)

Coherent transition radiation (CTR) in the THz regime is an important diagnostic tool for analyzing the temporal structure of the ultrashort electron bunches needed in ultraviolet and x-ray free-electron lasers. It is also a powerful source of such radiation, covering an exceptionally broad frequency range from about 200 GHz to 100 THz. At the soft x-ray free-electron laser FLASH we have installed a beam transport channel for transition radiation (TR) with the intention to guide a large fraction of the radiation to a laboratory outside the accelerator tunnel. The radiation is produced on a screen inside the ultrahigh vacuum beam pipe of the linac, coupled out through a diamond window and transported to the laboratory through an evacuated tube equipped with five focusing and four plane mirrors. The design of the beamline has been based on a thorough analysis of the generation of TR on metallic screens of limited size. The optical propagation of the radiation has been computed taking into account the effects of near-field (Fresnel) diffraction. The theoretical description of the TR source is presented in the first part of the paper, while the design principles and the technical layout of the beamline are described in the second part. First experimental results demonstrate that the CTR beamline covers the specified frequency range and preserves the narrow time structure of CTR pulses emitted by short electron bunches.

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FIG. 7. Schematic optical design of the THz transfer line. The focusing elements F1 to F5 are shown as lenses with their respective positions and focal lengths.



and place it at the CTR distribution is closed to  $TEM<sub>10</sub>$  mode</u>

#### Ultrabroadband terahertz source and beamline based on coherent transition radiation

S. Casalbuoni,<sup>1</sup> B. Schmidt,<sup>2</sup> P. Schmüser,<sup>2,3</sup> V. Arsov,<sup>2</sup> and S. Wesch<sup>2</sup>



5



### **Coherent Transition radiation**

Intensity of coherent transition radiation (CTR) from a bunch with population  $N_e$ :

$$
\frac{d^2W_{CTR}}{d\omega \, d\Omega} = \frac{d^2W_{TR}}{d\omega \, d\Omega} [N_e + N_e (N_e - 1)] F(\omega)
$$

- Spectral-angular distribution of TR from a single electron

Ginzburg-Frank formula for ultrarelativistic charge is valid for far-field zone:

$$
\frac{d^2 W_{TR}}{d\omega\, d\Omega}=\frac{e^2}{\pi^2 c}\frac{\theta_x^2+\theta_y^2}{(\gamma^{-2}+\theta_x^2+\theta_y^2)^2}\qquad \theta_x,\ \theta_y\quad\text{-projection angles}
$$

Formfactor:

$$
F_L(\omega) = \left| \int S(r) \exp\left[-i\Delta\varphi\right] dr \right|^2, \quad \Delta\varphi = kr - \omega\Delta t = \frac{2\pi}{\lambda} \left(x\theta_x + y\theta_y + z/\beta\right)
$$

For ultrarelativistic case (neglecting by transverse formfactor):

**Coherent Transition radiation**  
\nIntensity of coherent transition radiation (CTR) from a bunch with population N<sub>e</sub>:  
\n
$$
\frac{d^2W_{TR}}{d\omega d\Omega} = \frac{d^2W_{TR}}{d\omega d\Omega} [N_e + N_e(N_e - 1)]F(\omega)
$$
\n
$$
\frac{d^2W_{TR}}{d\omega d\Omega} - \text{Spectral-angular distribution of TR from a single electron}
$$
\nGinzburg-Frank formula for ultrarelativistic charge is valid for far-field zone:  
\n
$$
\frac{d^2W_{TR}}{d\omega d\Omega} = \frac{e^2}{\pi^2 c} \frac{\theta_x^2 + \theta_y^2}{(\gamma - 2 + \theta_x^2 + \theta_y^2)^2} \qquad \theta_x, \theta_y \qquad \text{projection angles}
$$
\n
$$
\text{Comfactor:}
$$
\n
$$
F_L(\omega) = \left| \int S\left(r \right) \exp[-i\Delta \varphi] d\tau \right|^2, \quad \Delta \varphi = kr - \omega \Delta t = \frac{2\pi}{\lambda} \left( x\theta_x + y\theta_y + z/\beta \right)
$$
\nFor ultrarelativistic case (neglecting by transverse formfactor):  
\n
$$
F_L(\omega) = \exp\left[ -\frac{4\pi^2 \sigma_z^2}{\lambda^2} \right] = \exp\left[ -\left( \frac{2\pi \nu}{v_0} \right)^2 \right], \text{ where } v_0 = c/\sigma_z
$$



### **Pre-wave zone effect**

 $>> \gamma^2 \lambda$ .

 $\langle \gamma^2 \lambda, \gamma -$  Lorentz factor,  $\lambda$ 

Finite target sizes effect: *a*<γλ







### **Spectrum of the coherent transition radiation**

Far-field zone:

EXECUTE: The equation of the coherent transition radiation. The field zone:

\n
$$
\frac{dW_{\text{CTR}}}{d\omega} = 2\pi \int_{0}^{\theta_{\text{max}}} \theta \, d\theta \frac{d^{2}W_{\text{CTR}}}{d\omega d\Omega} \approx N_{e}^{2} F(\omega) \cdot \frac{\alpha h}{\pi} \left[ \log(1 + \gamma^{2} \theta_{\text{max}}^{2}) + \frac{1}{1 + \gamma^{2} \theta_{\text{max}}^{2}} - 1 \right], \quad \theta_{\text{max}} - \text{aperture}
$$
\nPre-wave zone:

\n
$$
\frac{dW_{\text{CTR}}}{d\omega} = c D^{2} \int_{N_{\text{symmetric}}} \left| \frac{d}{dt} (x_{d}, y_{d}) \right|^{2} dx_{d} dy_{d}
$$
\nCTR radiation losses

\n
$$
10^{8} \left[ \frac{1 - \sigma_{z} = 500 \text{ um}}{10^{4}} \right]
$$
\n
$$
10^{9} \left[ \frac{3}{1 - \sigma_{z} = 75 \text{ um}} \right]
$$
\nLosses per bunch for  $\theta_{\text{max}}$ :

\n
$$
2 \left[ \frac{dW_{\text{CTR}}}{d\omega} \right] \cdot \frac{dW_{\text{CTR}}}{d\omega} \cdot \frac{2}{\sigma_{z}} \cdot \frac{2}{\sigma_{z}} \cdot \frac{1}{\sigma_{z}} \cdot \frac{dW_{\text{CTR}}}{d\omega} \cdot \frac{2}{\sigma_{z}} \cdot \frac{1}{\sigma_{z}} \cdot \frac{1}{\sigma_{z
$$



#### CTR radiation losses

return of the coherent transition radiation  
\nfield zone:  
\n
$$
\int \frac{\partial h}{\partial t} \left[ \log(1 + \gamma^2 \theta_{\text{max}}^2) + \frac{1}{1 + \gamma^2 \theta_{\text{max}}^2} - 1 \right], \quad \theta_{\text{max}} - \text{aperture}
$$
\n
$$
\int^2 \int_{N_{\text{symverse}}} \left| \frac{dF}{d(x_d, y_d)} \right| dx_d dy_d
$$
\nCTR radiation losses  
\n
$$
= 100, N_e = 10^8
$$
\n
$$
-\sigma_z = 500 \text{ um}
$$
\n
$$
-\sigma_z = 250 \text{ um}
$$
\n
$$
-\sigma_z = 250 \text{ um}
$$
\n
$$
-\sigma_z = 75 \text{ um}
$$
\n
$$
\Delta W_{\text{CR}} : N_e^2 \frac{dE}{d\sigma_z}
$$
\nFor Q=0.5 nC,  
\n
$$
\int \sigma_Z = 500 \mu m, \Delta W_{\text{CTR}} \sim 1200 \eta J, \quad \nu < 0.05 \text{ THZ}
$$
\n
$$
\sigma_Z = 100 \mu m, \Delta W_{\text{CTR}} \sim 6000 \eta J, \quad \nu < 0.4 \text{ THZ}
$$



### **DR in the far-field zone**





#### **DR in the pre-wave zone** [A. Potylitsyn, NATO Science Series, V.199, 2009]

DR distribution on the windows surface

1IC  
\n**DR in the pre-wave zone** [A. Potylitsyn, NATO Science Series, V.199, 2009]  
\n1DR distribution on the windows surface  
\n
$$
E_{x,y}^{DR}(x_y, y_y) = const \iint_{S_y} dx_r dy_y \frac{\{x_\tau, y_\tau\} \left(1 + 0.57 \sqrt{x_\tau^2 + y_\tau^2} - 0.04 \left(x_\tau^2 + y_\tau^2\right) \right) \exp\left[-\sqrt{x_\tau^2 + y_\tau^2}\right]}{x_\tau^2 + y_\tau^2} * \exp\left[i\frac{\left(x_\tau^2 + y_\tau^2\right)}{4\pi R} - i\left(x_\tau x_y + y_\tau y_y\right)\right],
$$
\nwhere  $R = \frac{D}{y^2\lambda}$ ,  $x_y(y_y) = \frac{2\pi x_y(y_y)}{y\lambda}$ ,  $x(y) = \frac{\gamma}{D}X(Y)$   
\nΔS<sub>T</sub>- target area,  
\nX<sub>T</sub>, Y<sub>T</sub>- coordinate on the target surface,  
\nX<sub>D</sub>, Y<sub>D</sub>- coordinate on the exit window surface,

where 
$$
R = \frac{D}{\gamma^2 \lambda}
$$
,  $x_T(y_T) = \frac{2\pi X_T(Y_T)}{\gamma \lambda}$ ,  $x(y) = \frac{\gamma}{D} X(Y)$ 

∆*S*T- target area,

- *X*<sup>T</sup> *,Y*T- coordinate on the target surface,
- *X*<sup>D</sup> *,Y*D- coordinate on the exit window surface,



### **DR from a flat target (pre-wave zone):**

 $\gamma = 300$ ,  $a = 30$  mm,  $\lambda = 0.3$  mm,  $D = 200$  mm



DR distribution in the pre-wave zone is much broader in comparison with far-field zone



### **Focusing of the DR**

The pre-wave zone effect (broadening of the DR cone) can be eliminated using a parabolic focusing DR target



Calculations are performed using the same formula with the target surface element **EXECUTE:**<br> **EXEC** 

$$
dS = dx_r dy_r \sqrt{x_r^2 + y_r^2 + 4f^2}/2f
$$

Where *f* is the target focal distance, *f=*2D

The simulation scheme and some definitions.



**DR from a focusing target**



DR angular distribution on the exit window is closed to the  $TEM<sub>00</sub>$  mode distribution and can be</u>



#### Observation of coherently enhanced tunable narrow-band terahertz transition radiation from a relativistic sub-picosecond electron bunch train

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We experimentally demonstrate the production of narrow-band  $(\delta f/f \approx 20\%$  at  $f \approx 0.5$  THz) transition radiation with tunable frequency over [0.37, 0.86] THz. The radiation is produced as a train of sub-picosecond relativistic electron bunches transits at the vacuum-aluminum interface of an aluminum converter screen. The bunch train is generated via a transverse-to-longitudinal phase space exchange technique. We also show a possible application of modulated beams to extend the dynamical range of a popular bunch length diagnostic technique based on the spectral analysis of coherent radiation. © 2011 American Institute of Physics. [doi:10.1063/1.3604017]



The rf gun is surrounded by three solenoidal lenses (L1, L2, and L3) that control the beam's transverse size and divergence. The beam is then accelerated in a 1.3-GHz superconducting rf cavity (the booster cavity) to  $\sim$  14 MeV. Downstream of the booster cavity, the 500-pC bunch is intercepted by a multislit mask consisting of 48-μm wide slits with 1-mm spacing thereby producing a transversely segmented beam with total charge of  $\sim$ 15 pC. The beam is transported, with a set of quadrupole magnets, to the phase space exchange (PEX) beamline which consists of a liquid-nitrogen-cooled deflecting cavity operating on the TM110-like  $\pi$ -mode at 3.9 GHz.



### **Superradiant CTR and CDR from a train of bunches**

ant CTR and CDR from a train of bunche  
\n
$$
S_L(z) = \frac{1}{N_b \sqrt{\pi} \sigma_z} \sum_{n=1}^{N_b} \exp \left[ -\frac{(z - n\lambda_0)^2}{\sigma_z^2} \right],
$$
\n
$$
U_0
$$
 is the distance between microbunch,  $N_b$  is the number  
\n
$$
V_0 = \exp \left[ -\sigma_z^2 \omega^2/c^2 \right] \frac{1}{N_b^2} \frac{\sin^2 (N_b \lambda_0 \omega/2c)}{\sin^2 (\lambda_0 \omega/2c)},
$$
\nSCTR spectrum is determined by the last factor:  
\nne number of bunches  $N_b$ :  $\Delta v/v = 1/N_b$   
\n
$$
N_e + N_e (N_e - 1) \left[ N_b^2 F_L(\omega) \frac{d^2 W_{TR}}{d\omega d\Omega} \approx N_e^2 N_b^2 F_L(\omega) \frac{d^2 W_{TR}}{d\omega d\Omega} \right]
$$

**adiant CTR and CDR from a train of bunches**  
\n
$$
S_L(z) = \frac{1}{N_b \sqrt{\pi} \sigma_z} \sum_{n=1}^{N_b} \exp \left[ -\frac{(z - n\lambda_0)^2}{\sigma_z^2} \right],
$$
\n
$$
ch, \lambda_0 \text{ is the distance between microbunch}, N_b \text{ is the number of 1}
$$
\n
$$
F_L(\omega) = \exp \left[ -\sigma_z^2 \omega^2/c^2 \right] \frac{1}{N_b^2} \frac{\sin^2 (N_b \lambda_0 \omega/2c)}{\sin^2 (\lambda_0 \omega/2c)},
$$
\n
$$
h \text{ the SCTR spectrum is determined by the last factor: } v_0 = \lambda_0 \text{ by the number of bunches } N_b : \Delta v/v = 1/N_b
$$
\n
$$
\frac{CTR}{\Omega} = \left[ N_e + N_e \left( N_e - 1 \right) \right] N_b^2 F_L(\omega) \frac{d^2 W_{TR}}{d \omega d \Omega} \approx N_e^2 N_b^2 F_L(\omega) \frac{d^2 W_{TR}}{d \omega d \Omega}
$$
\n
$$
s \text{ the charge of segmented initial bunch passed trough a slit}
$$

CDR from a train of  $\exp \left[-\frac{(z-n\lambda_0)^2}{\sigma_z^2}\right]$ ,<br>
exp $\left[-\frac{(z-n\lambda_0)^2}{\sigma_z^2}\right]$ ,<br>
exp $\frac{1}{N_b^2} \frac{\sin^2(N_b\lambda_0\omega/2c)}{\sin^2(\lambda_0\omega/2c)}$ ,<br>
is determined by the las<br>
nches  $N_b$ :  $\Delta v/v = I/N_b$ <br>  $\omega \frac{d^2 W_{TR}}{d\omega d\Omega} \approx N_e^2 N_b^2 F_L(\omega) \frac{d$ from a train of bund<br>  $\frac{(z-n\lambda_0)^2}{\sigma_z^2}$ <br>
microbunch,  $N_b$  is the num<br>  $\frac{\sin^2(N_b\lambda_0\omega/2c)}{\sin^2(\lambda_0\omega/2c)}$ ,<br>
ermined by the last fact<br>  $N_b : \Delta v/v = 1/N_b$ <br>  $\frac{d^2W_{TR}}{\sigma_s^2}$ and CDR from a train of bunches<br>  $\frac{N_b}{\pi \sigma_z} \sum_{n=1}^{N_b} \exp \left[ -\frac{(z - n\lambda_0)^2}{\sigma_z^2} \right]$ ,<br>
ance between microbunch,  $N_b$  is the number of bunch in a train<br>  $\frac{2}{\epsilon} \omega^2/c^2 \frac{1}{N_b^2} \frac{\sin^2(N_b \lambda_0 \omega/2c)}{\sin^2(\lambda_0 \omega/2c)}$ ,<br>
ctrum **R** from a train of bunches<br>  $\left[-\frac{(z-n\lambda_0)^2}{\sigma_z^2}\right]$ ,<br>
een microbunch,  $N_b$  is the number of bunch in a train<br>  $\frac{1}{N_b^2} \frac{\sin^2(N_b\lambda_0 \omega/2c)}{\sin^2(\lambda_0 \omega/2c)}$ ,<br>
determined by the last factor:  $\nu_0 = \lambda_0/c$ <br>
es  $N_b$ :  $\Delta \nu/\nu$ TR and CDR from a train of bunches<br>  $=\frac{1}{N_b\sqrt{\pi}\sigma_z}\sum_{n=1}^{N_b}\exp\left[-\frac{(z-n\lambda_0)^2}{\sigma_z^2}\right]$ <br>
e distance between microbunch,  $N_b$  is the number of bunch in a train<br>  $\text{sp}[-\sigma_z^2 \omega^2/c^2]\frac{1}{N_b^2}\frac{\sin^2(N_b\lambda_0\omega/2c)}{\sin^2(\lambda_0\omega/2c)}$ **i** CDR from a train of bunches<br>  $\sum_{n=1}^{N_b} \exp \left[ -\frac{(z - n\lambda_0)^2}{\sigma_z^2} \right]$ ,<br>
between microbunch,  $N_b$  is the number of bunch in a train<br>  $\left[ c^2 \right] \frac{1}{N_b^2} \frac{\sin^2 (N_b \lambda_0 \omega/2c)}{\sin^2 (\lambda_0 \omega/2c)}$ ,<br>
m is determined by the last and CDR from a train of b<br>  $\frac{1}{2\pi\sigma_z}\sum_{n=1}^{N_b}\exp\left[-\frac{(z-n\lambda_0)^2}{\sigma_z^2}\right]$ ,<br>
ince between microbunch,  $N_b$  is the<br>  $\frac{1}{2} \omega^2/c^2\right] \frac{1}{N_b^2} \frac{\sin^2(N_b\lambda_0\omega/2c)}{\sin^2(\lambda_0\omega/2c)}$ ,<br>
ctrum is determined by the last<br>
of bunch **R** from a train of bunches<br>  $\left[-\frac{(z-n\lambda_0)^2}{\sigma_z^2}\right]$ ,<br>
een microbunch,  $N_b$  is the number of b<br>  $\frac{1}{N_b^2} \frac{\sin^2(N_b\lambda_0\omega/2c)}{\sin^2(\lambda_0\omega/2c)}$ ,<br>
determined by the last factor:  $v_0 = \lambda$ <br>
es  $N_b$ :  $\Delta v/v = 1/N_b$ <br>  $\frac{l^2W_{TR}}{l\$ **CTR and CDR from a train of bunches**<br>  $z_j = \frac{1}{N_b\sqrt{\pi}\sigma_z} \sum_{n=1}^{N_b} \exp\left[-\frac{(z - n\lambda_0)^2}{\sigma_z^2}\right]$ ,<br>
the distance between microbunch,  $N_b$  is the number of  $\exp[-\sigma_z^2 \omega^2/c^2] \frac{1}{N_b^2} \frac{\sin^2(N_b\lambda_0 \omega/2c)}{\sin^2(\lambda_0 \omega/2c)}$ ,<br> **TR ant CTR and CDR from a train of bunches**<br>  $S_L(z) = \frac{1}{N_s \sqrt{\pi} \sigma_z} \sum_{\epsilon=1}^{N_b} \exp\left[-\frac{(z - n \lambda_0)^2}{\sigma_z^2}\right]$ <br>  $\lambda_0$  is the distance between microbunch,  $N_b$  is the number of bunch in a train<br>  $\omega$ ) = exp $\left[-\sigma_z^2 \omega^2/c^2\right] \frac$ **and CDR from a train of bunches**<br>  $S_L(z) = \frac{1}{N_b \sqrt{\pi \sigma_z}} \sum_{\kappa=1}^{N_b} \exp \left[ -\frac{(z - n\lambda_0)^2}{\sigma_z^2} \right]$ <br>  $\psi_0$  is the distance between microbunch,  $N_b$  is the number of bunch in a train<br>  $D = \exp \left[ -\sigma_z^2 \omega^2/c^2 \right] \frac{1}{N_b^2} \frac{\sin$ The fundamental frequency in the SCTR spectrum is determined by the last factor:  $v_0 = \lambda_0/c$ Monochromaticity is defined by the number of bunches  $N_b$ :  $\Delta v/v=1/N_b$ **rradiant CTR and CDR from a train of bunch**<br>  $S_{\ell}(z) = \frac{1}{N_{\ell}} \sum_{\sqrt{\pi}}^{\infty} \exp\left[-\frac{(z - n\lambda_0)^2}{\sigma_{z}^2}\right]$ <br>
unch,  $\lambda_0$  is the distance between microbunch,  $N_{\ell}$  is the num<br>  $F_{\ell}(\omega) = \exp\left[-\sigma_{z}^2 \omega^2/c^2\right] \frac{1}{N_{\ell}^$ 

$$
\frac{d^2W_{\text{SCTR}}}{d\omega d\Omega} = \left[ N_e + N_e \left( N_e - 1 \right) \right] N_b^2 F_L(\omega) \frac{d^2W_{\text{TR}}}{d\omega d\Omega} \approx N_e^2 N_b^2 F_L(\omega) \frac{d^2W_{\text{TR}}}{d\omega d\Omega}
$$

The charge  $e \cdot N_e \cdot N_b$  is the charge of segmented initial bunch passed trough a slit mask

A mask with spacing 300 um and the slit width 75 um can provide transparency  $\sim 20\%$  (for instance  $N_b=6$ ,  $N_e \sim 20$  pC)







#### **Superradiant CTR spectra from a train of bunches**





![](_page_19_Picture_0.jpeg)

### **Summary**

- **Focused CDR provides transverse distribution similar to TEM<sup>00</sup> mode**
- **TR/ DR generated by a train of short electron bunches becomes monochromatic with the fundamental frequency defined by the distance between bunches**
- **Monochromaticity of the radiation is defined by the number of bunches in a train**   $(\Delta \nu/\nu_e=1/N_b)$
- **Intensity of the radiation is proportional squared number of bunches and squared charge of each microbunch (superradiant radiation)**
- **For Nb=6 and Qb≈20 pC SCDR monochromatic pulse energy density can achieve the ∆W/∆ν~0.04 μJ/THz at ν~1 THz (for the broadband SPARC source ∆W/∆ν~0.1 μJ/THz)**

![](_page_20_Picture_0.jpeg)

# **THANK FOR YOUR ATTENTION!**

![](_page_20_Picture_2.jpeg)