

# Issues in Hadron Spectroscopy

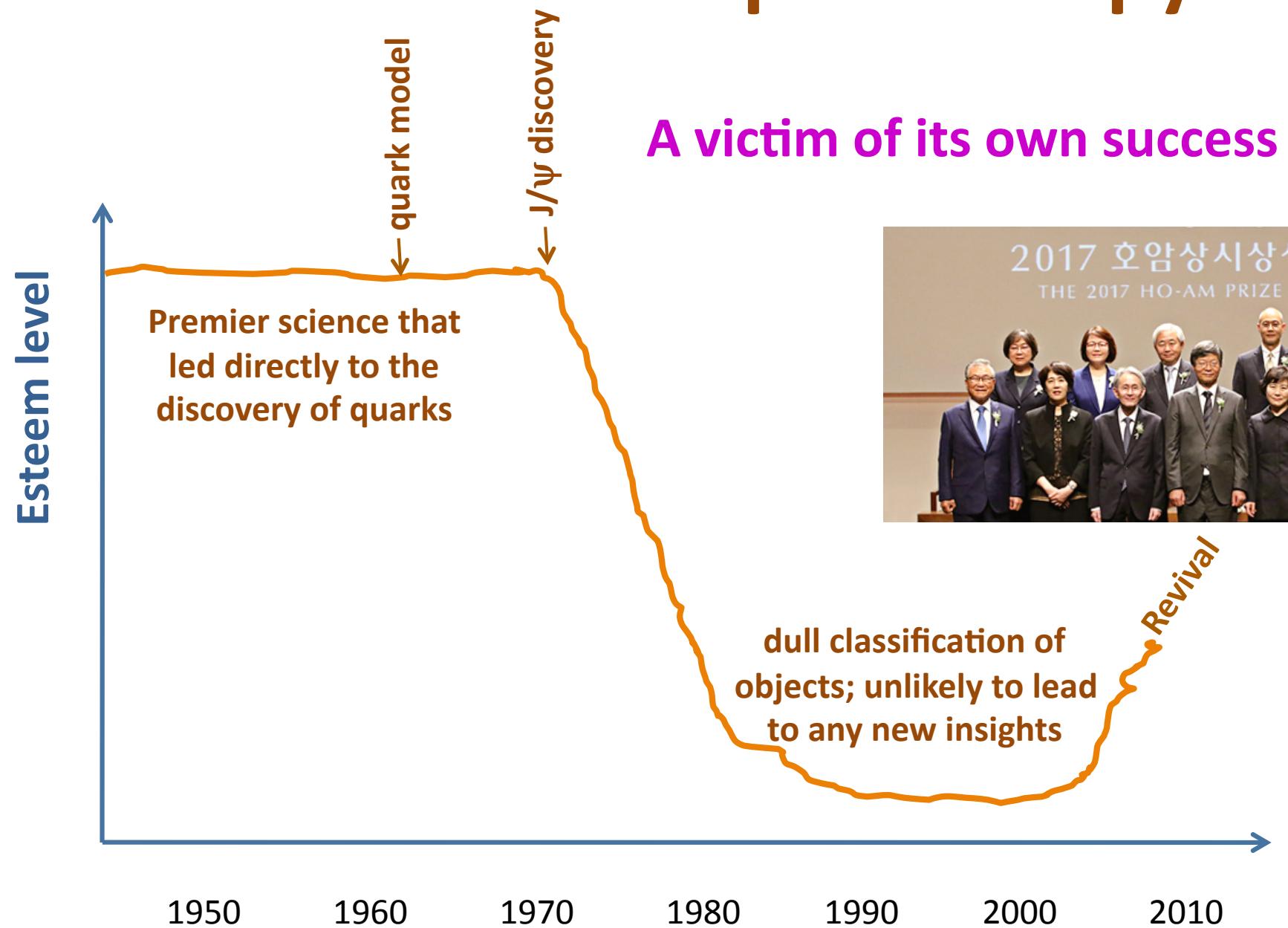
-- puzzling near-threshold anomalies --



Stephen Lars Olsen **ibS** Institute for Basic Science Daejeon, KOREA

Joint Symposium on Nuclear, Particle & Field, and Astrophysics (SYNPA2017)  
Chonnam University, Gwangju, KOREA, Nov. 17-18, 2016

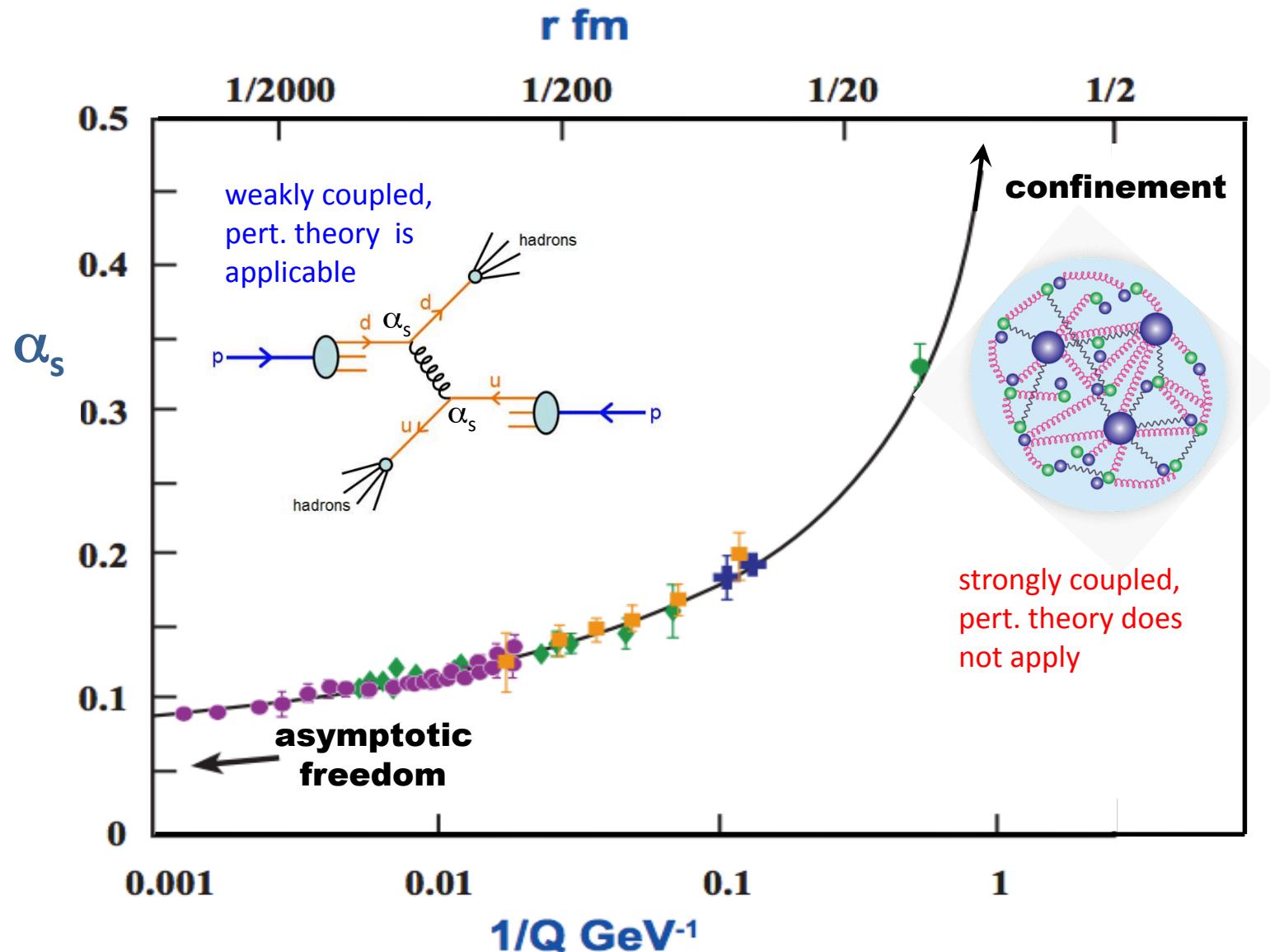
# Status of hadron spectroscopy:



A victim of its own success



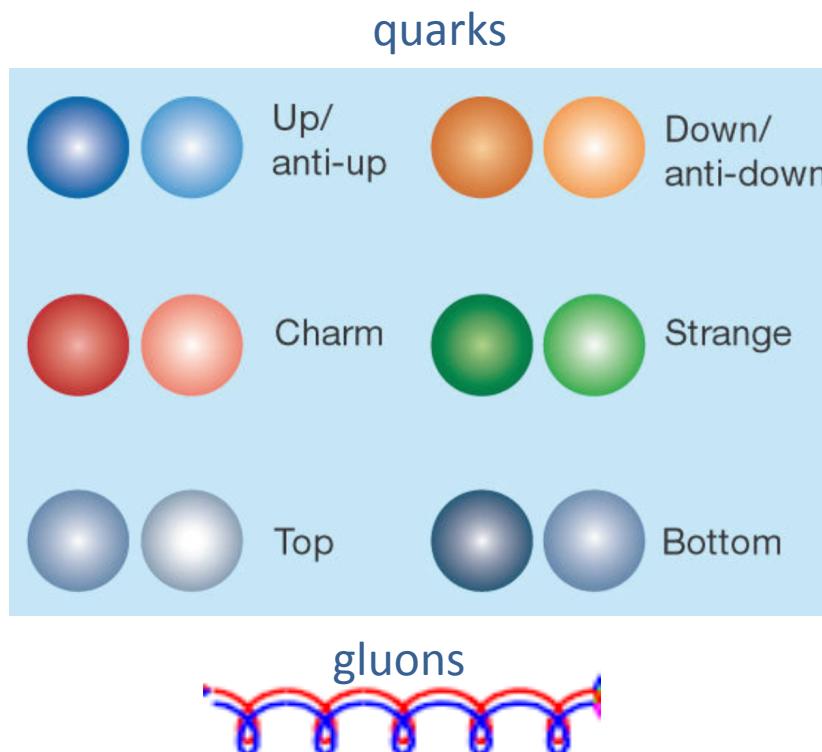
# QCD dilemma



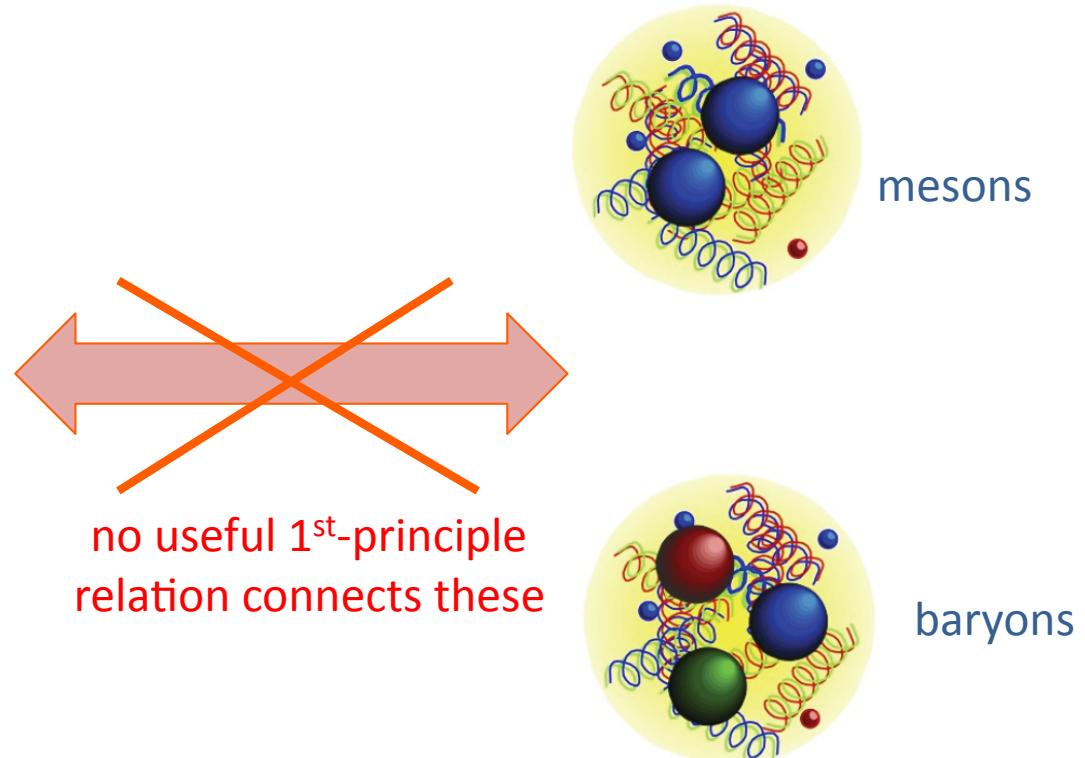
# “psychological” problem

-- theory is divorced from reality --

strongly interacting particles  
of the Standard Model



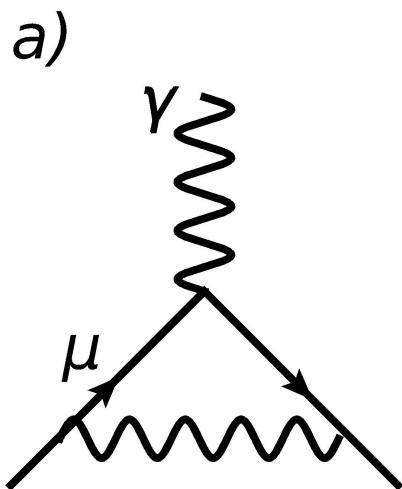
strongly interacting particles  
in Nature



# “practical” problem

– long-distance QCD effects limits on new physics searches –

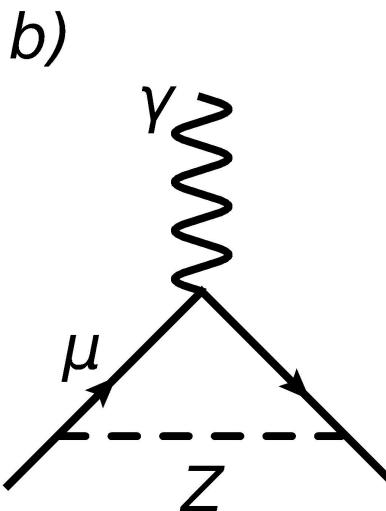
$(g-2)_\mu/2$ : experimental precision  $\delta_{\text{exp}} = \pm 6.3 \times 10^{-10}$



QED:  $11658472 \times 10^{-10}$   
 $(1.2 \times 10^{-3})$

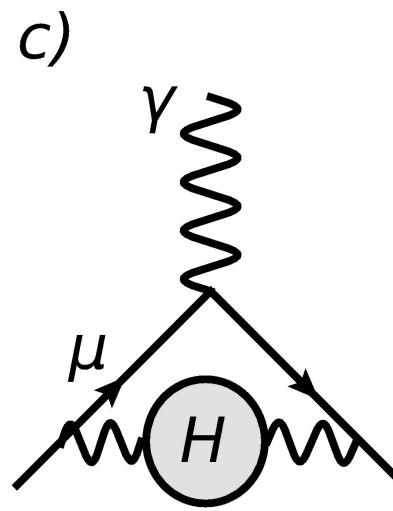
$$\delta_{\text{QED}} = \pm 0.02 \times 10^{-10}$$

12,672 diagrams!

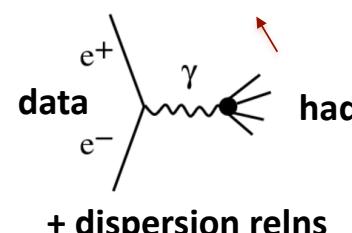


EW:  $15.4 \times 10^{-10}$

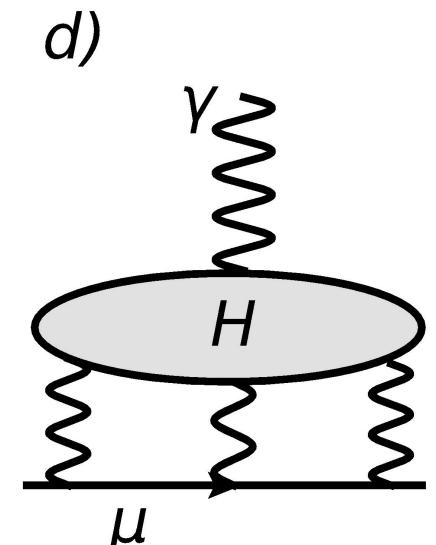
$$\delta_{\text{EW}} = \pm 0.2 \times 10^{-10}$$



LO+NLO had:  $682 \times 10^{-10}$



$$\delta_{\text{NLO}} = \pm 4.6 \times 10^{-10}$$



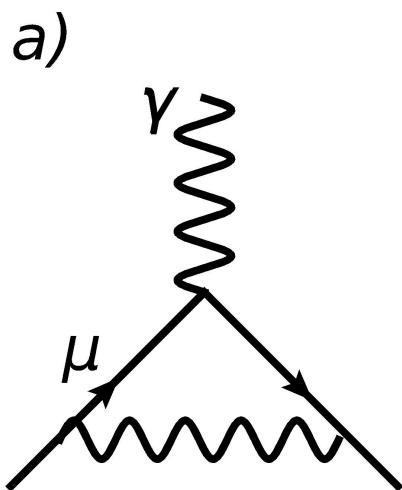
$\ell$ -by- $\ell$ :  $14 \times 10^{-10}$

$$\delta_{\ell\text{-by-}\ell} \approx \pm 3 \times 10^{-10}$$

# “practical” problem

– long-distance QCD effects limits on new physics searches –

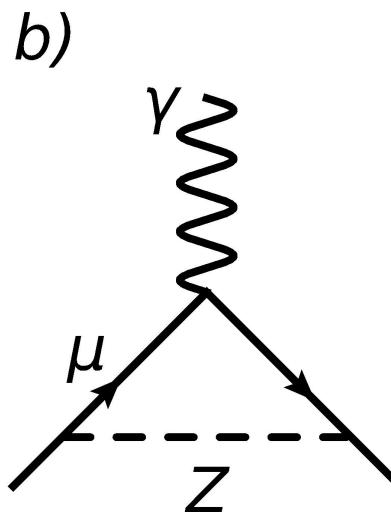
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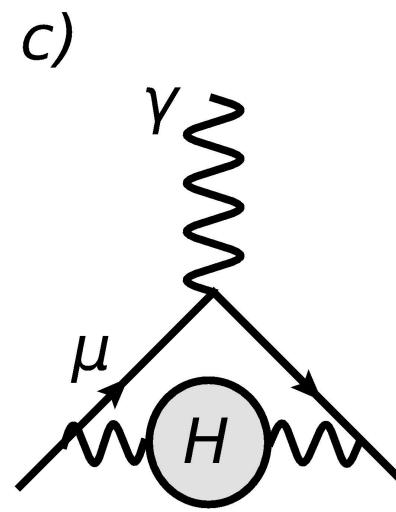
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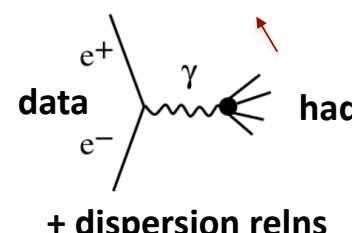


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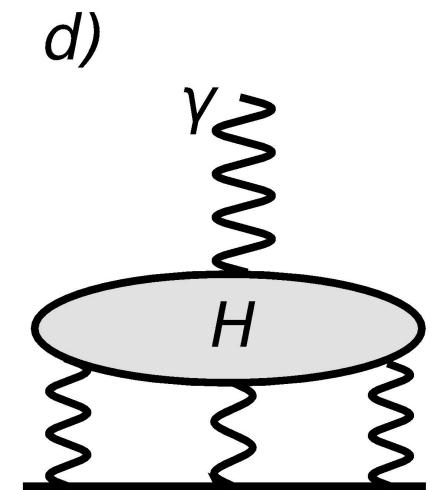
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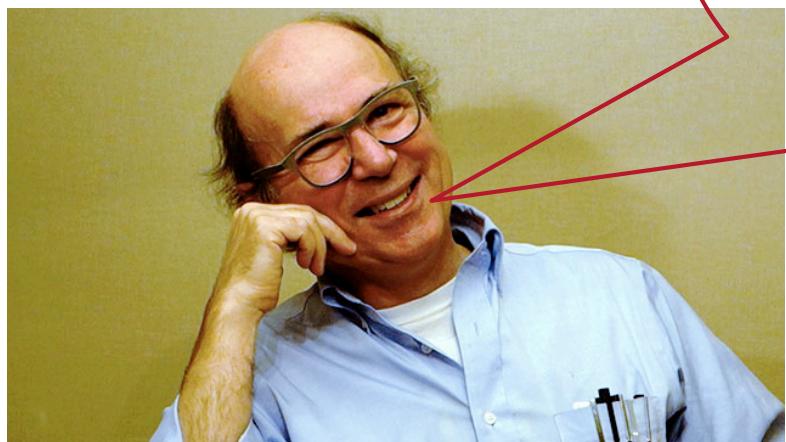
$\ell\text{-by-}\ell$ :  $14 \times 10^{-10}$

$\delta_{\ell\text{-by-}\ell} \approx \pm 3 \times 10^{-10}$

this will ultimately be  
the dominant SM error  
and larger than  $\delta_{\text{exp}}$

# A better understanding of long-distance QCD is essential

Frank Wilczek



We have something called a standard model, but its foundations are kind of *scandalous*. We have not known how to define an important part of it mathematically rigorously, ...

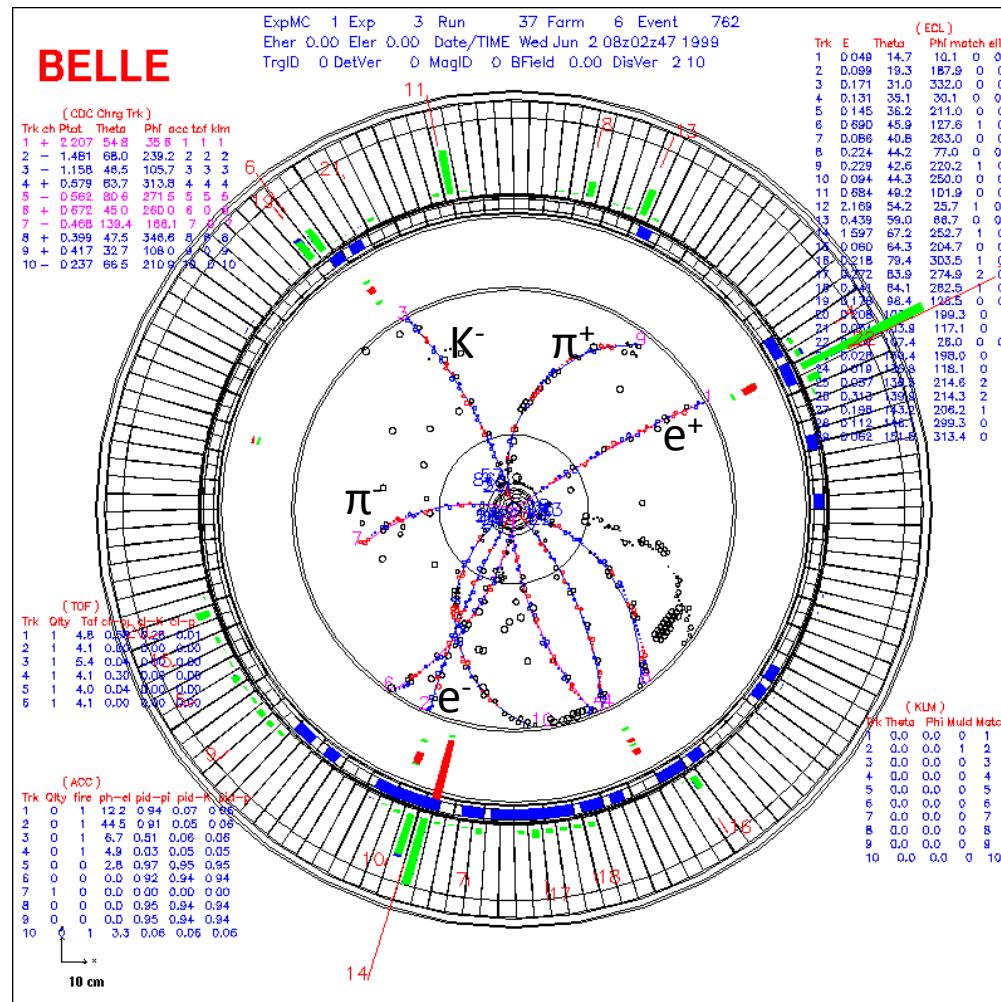
# Possible strategies for dealing with the “scandalous” situation

Theorists: abandon old ideas, try to dream up new ones

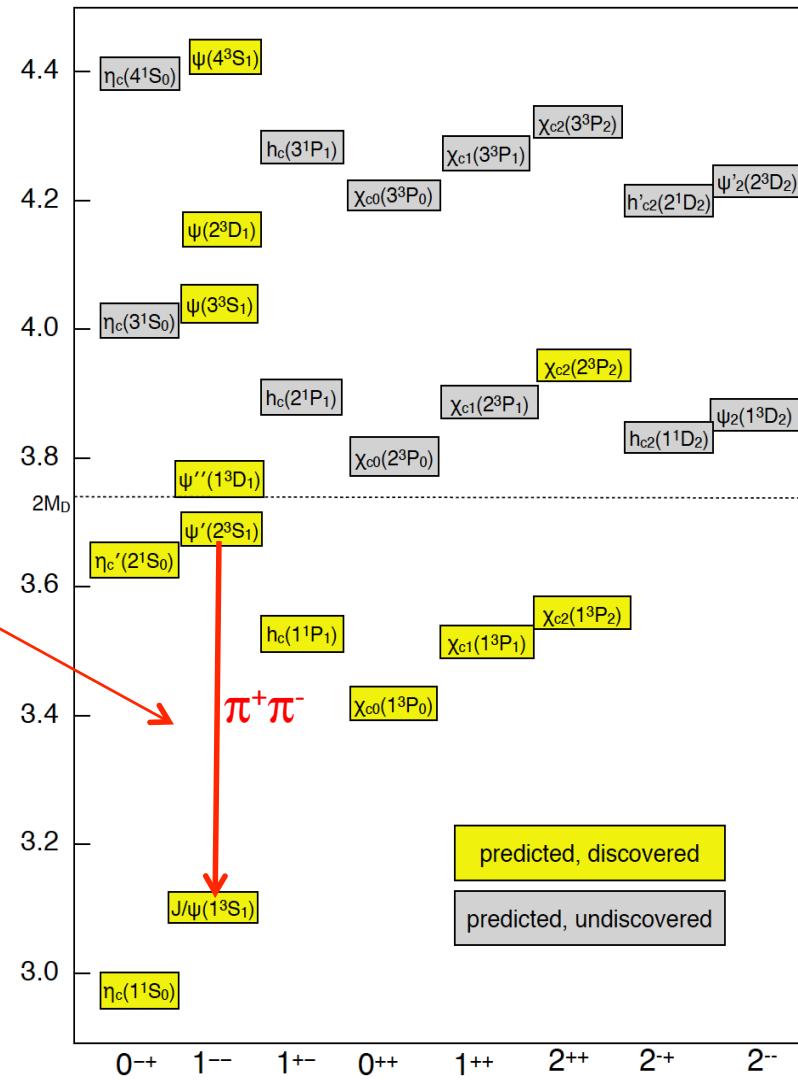
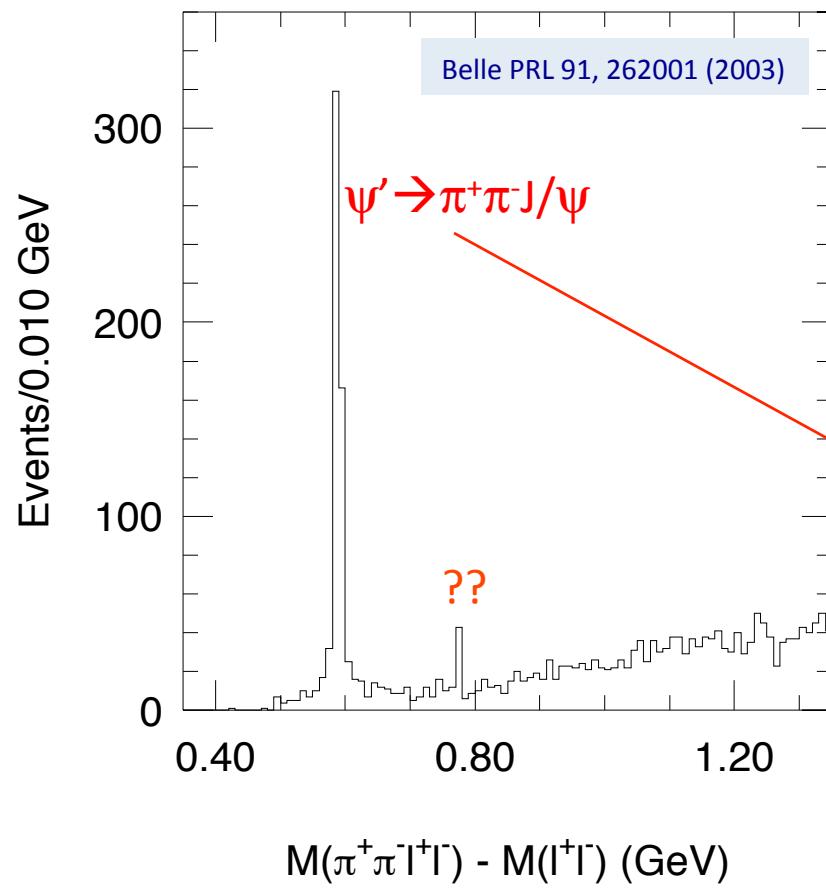
Experimenters: try to identify previously unrecognized patterns in the data

# $B^- \rightarrow K^- \pi^+ \pi^- J/\psi$ event in Belle

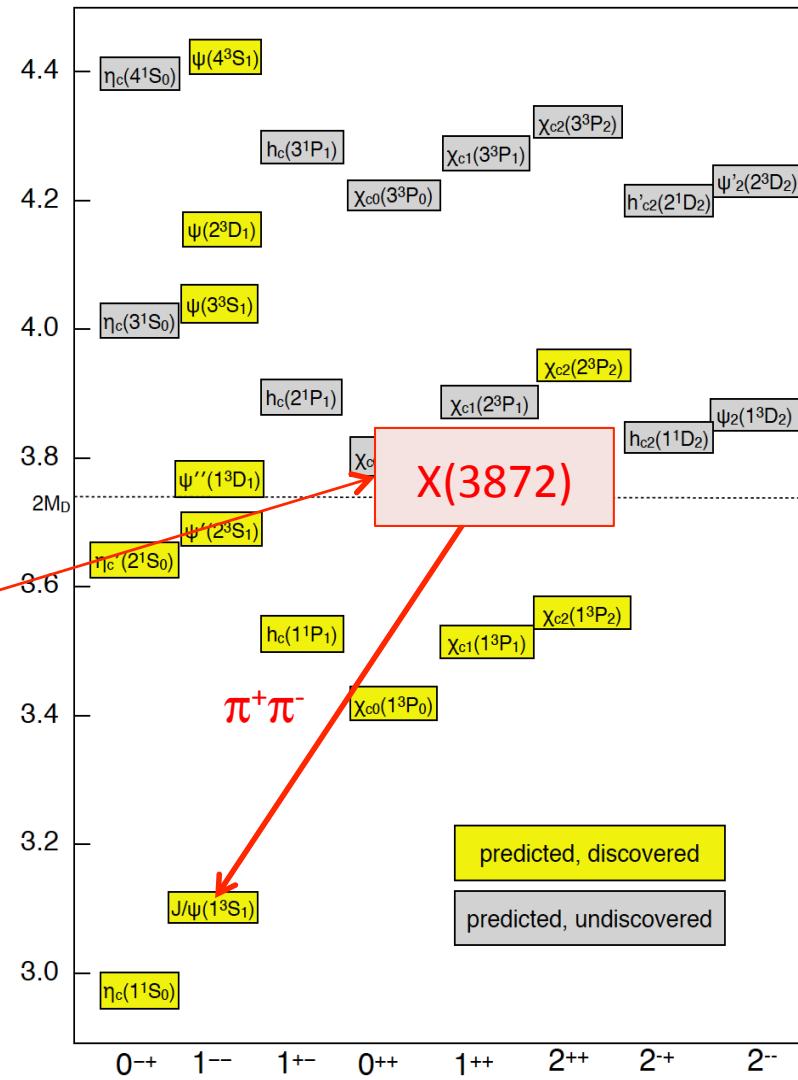
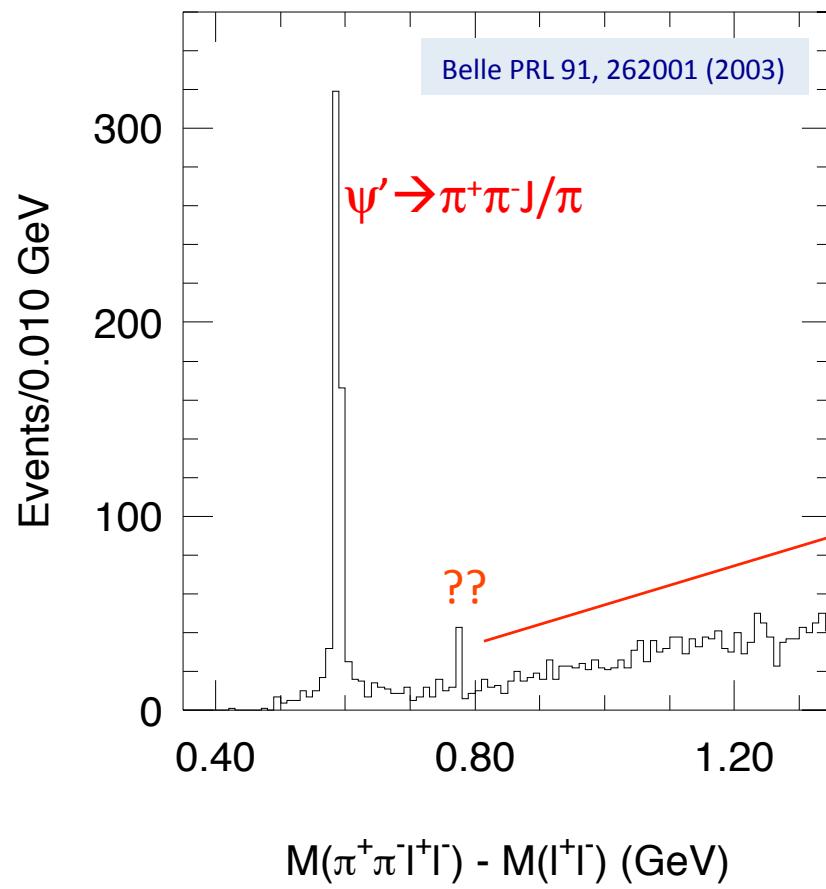
$\hookdownarrow e^+ e^-$



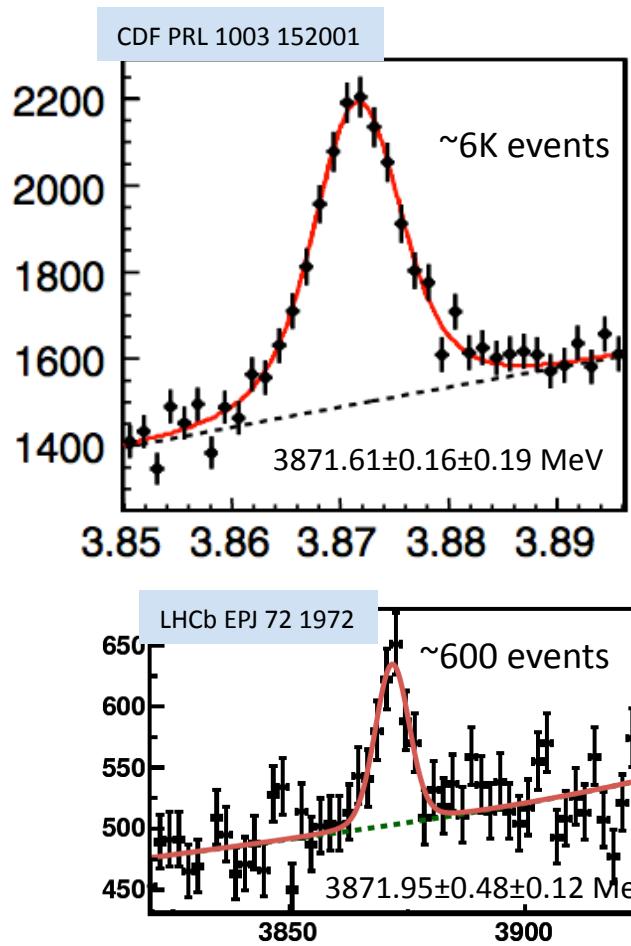
# $\mathcal{M}(\pi^+\pi^-J/\psi)$



# $\mathcal{M}(\pi^+\pi^- \text{J}/\psi)$



# X(3872) Mass

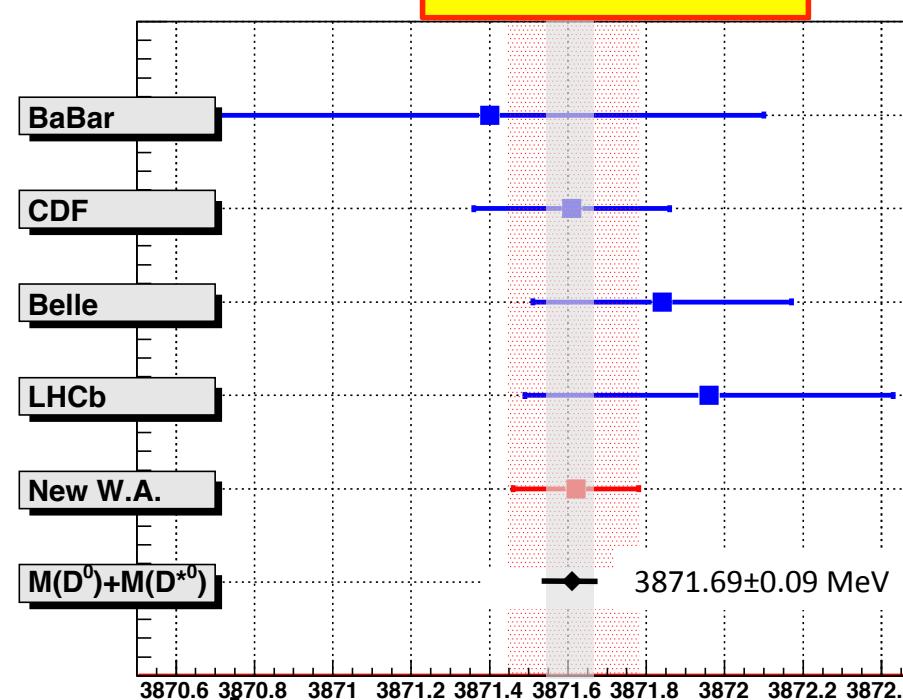


$M_{X(3872)}$  is indistinguishable from  $m_{D^0} + m_{D^{*0}}$

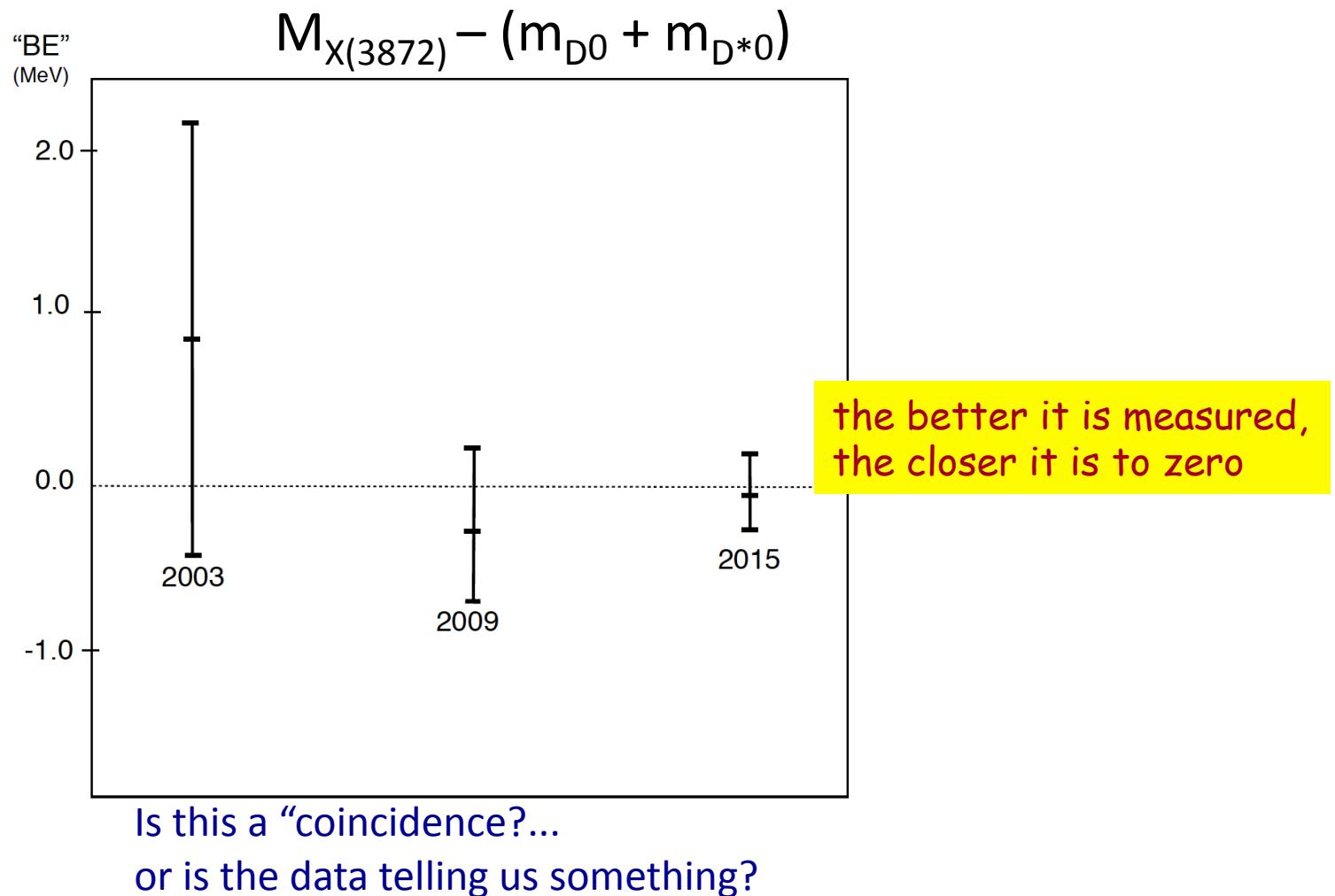
"B.E." =  $3 \pm 193$  keV

## X(3872) mass measurements

PDG14:  $3871.69 \pm 0.12$



# X(3872) “Binding Energy”



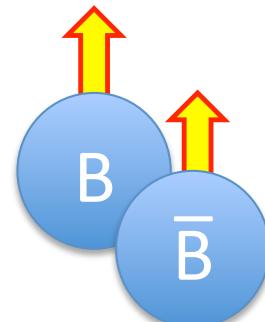
# Thresholds may be interesting



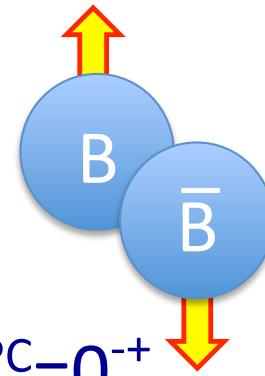
# Look at light baryon thresholds

baryon-antibaryon:

2 S-wave threshold states:



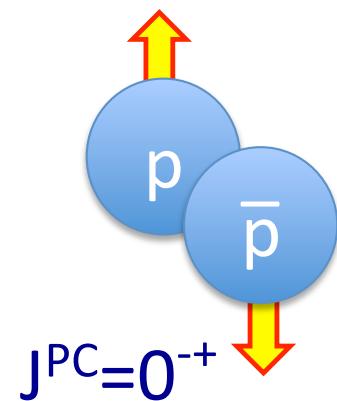
$$J^{PC}=1^{--}$$



$$J^{PC}=0^{-+}$$

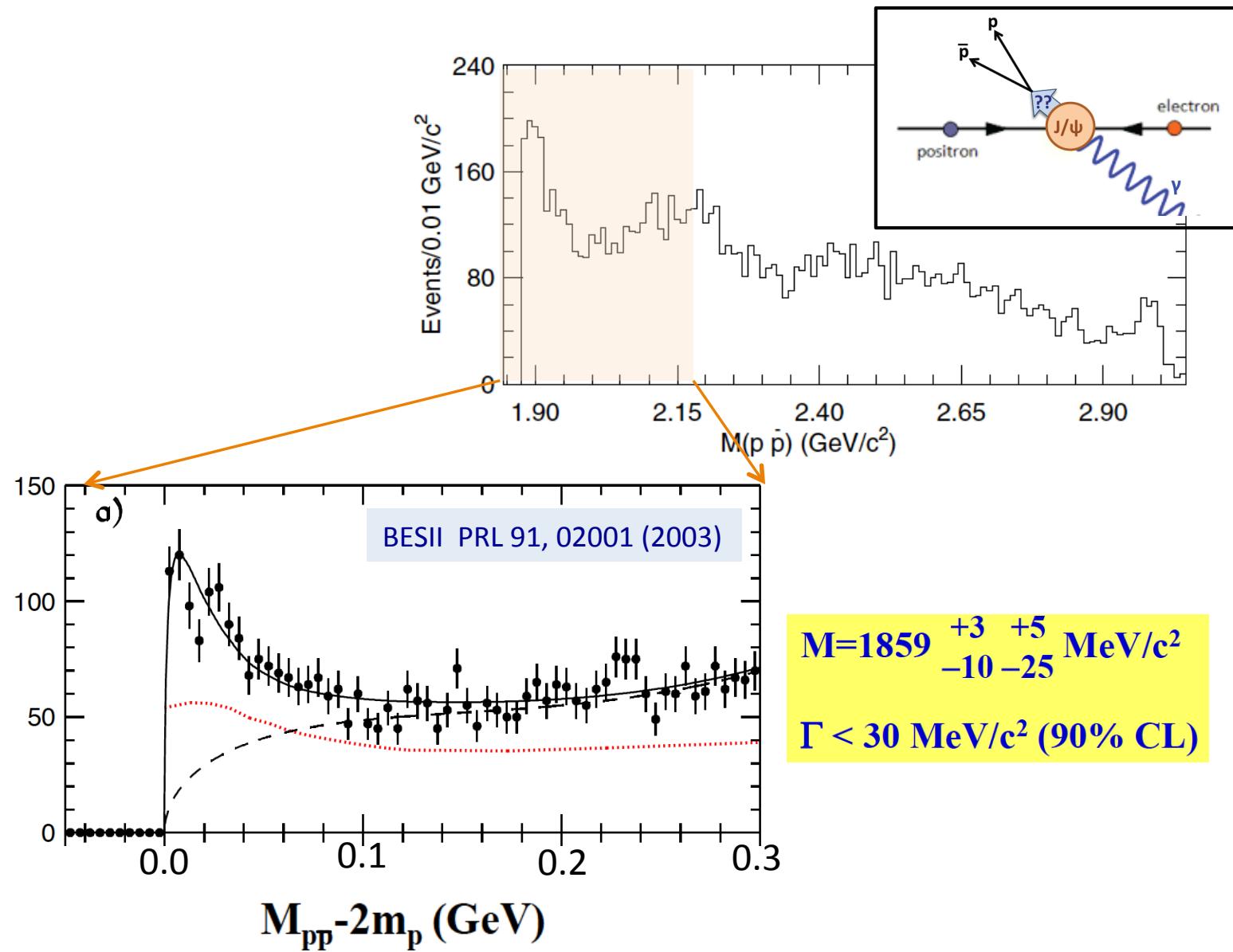


# $0^{-+}$ $p\bar{p}$ system

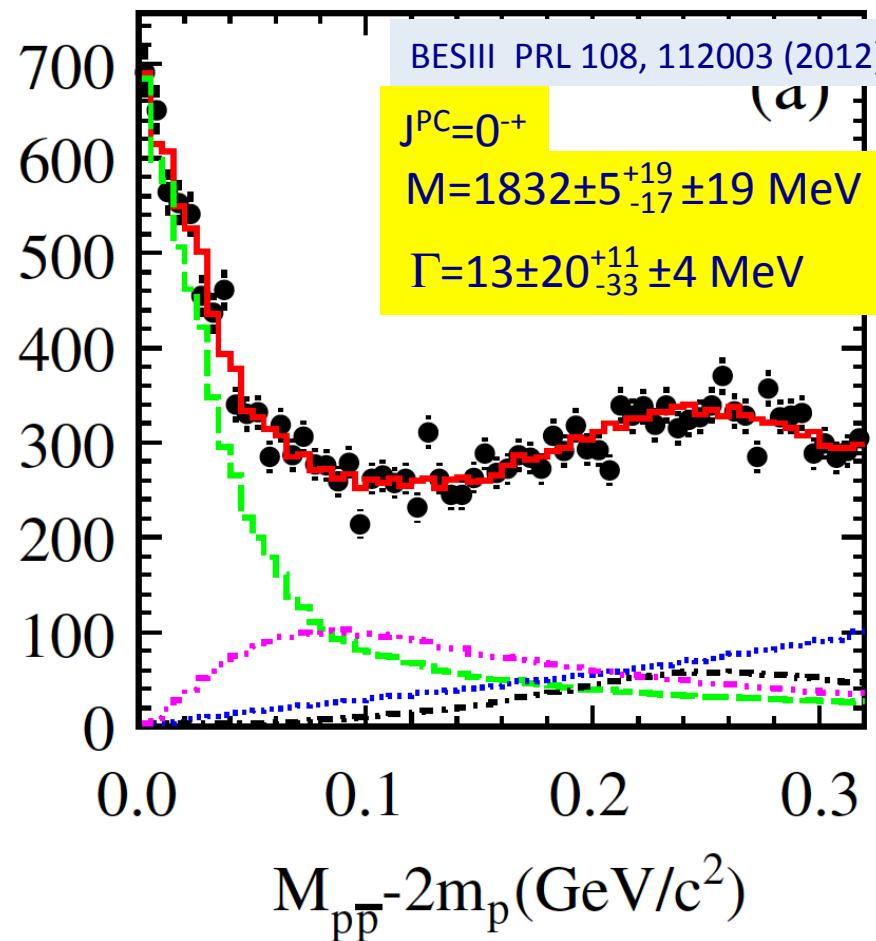


$$J/\psi (\psi') \rightarrow \gamma p\bar{p}$$

# $J/\psi \rightarrow \gamma p\bar{p}$ at BESII

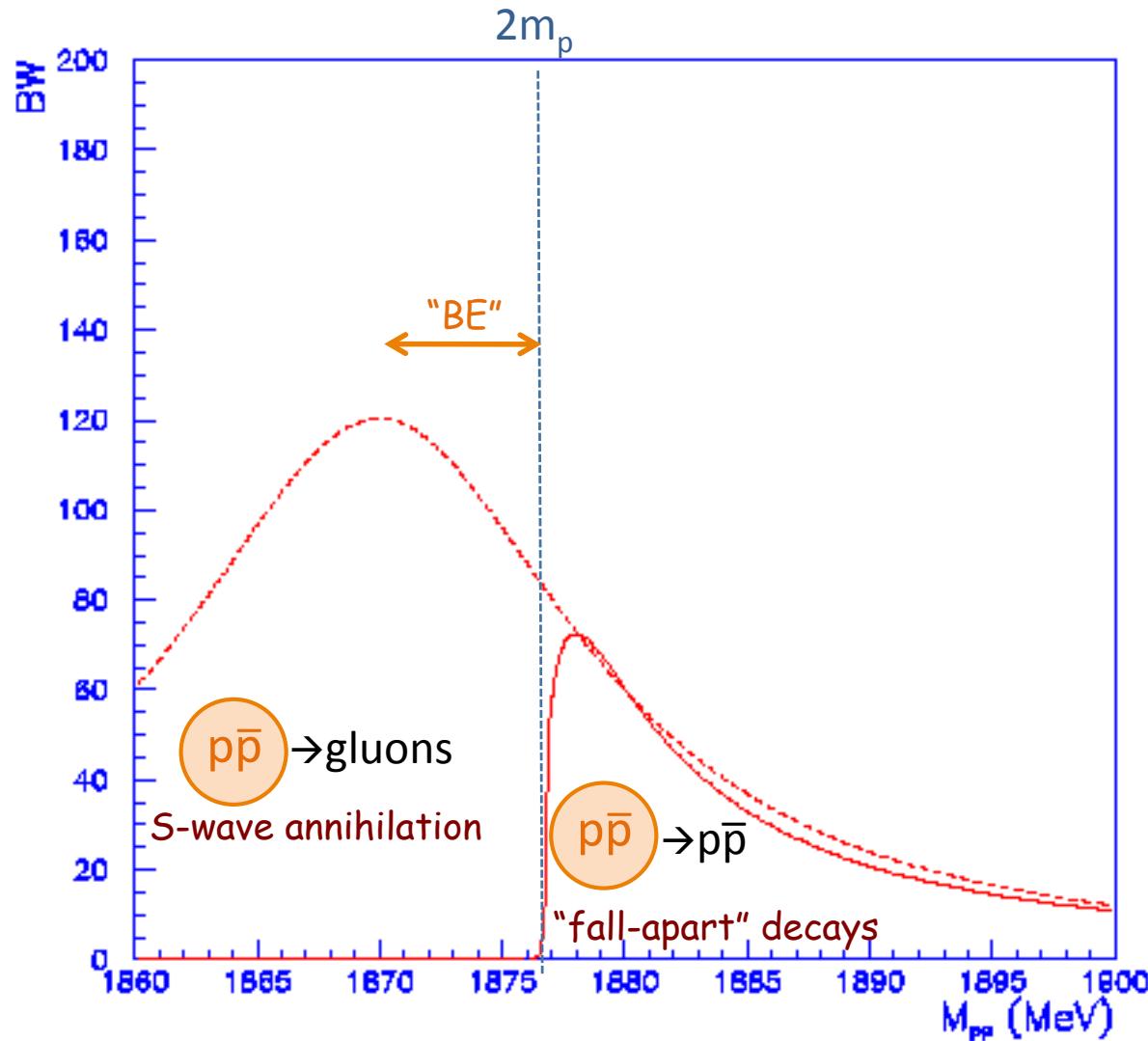


# $J/\psi \rightarrow \gamma p\bar{p}$ at BESIII (PWA)

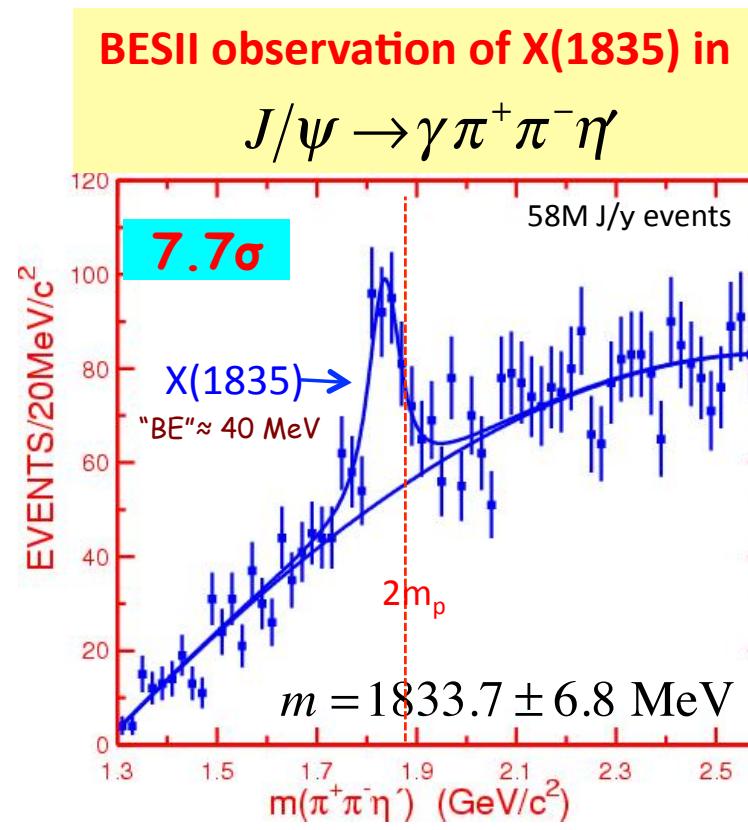
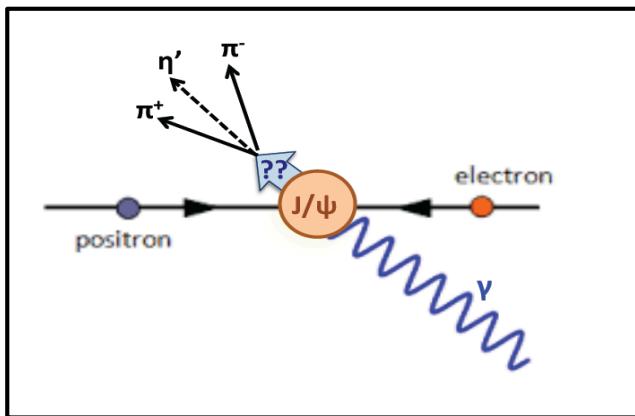


FSI included: A. Sibirtsev et al, PRD71, 054010 (2005)

# “protonium:” a $p\bar{p}$ bound state?



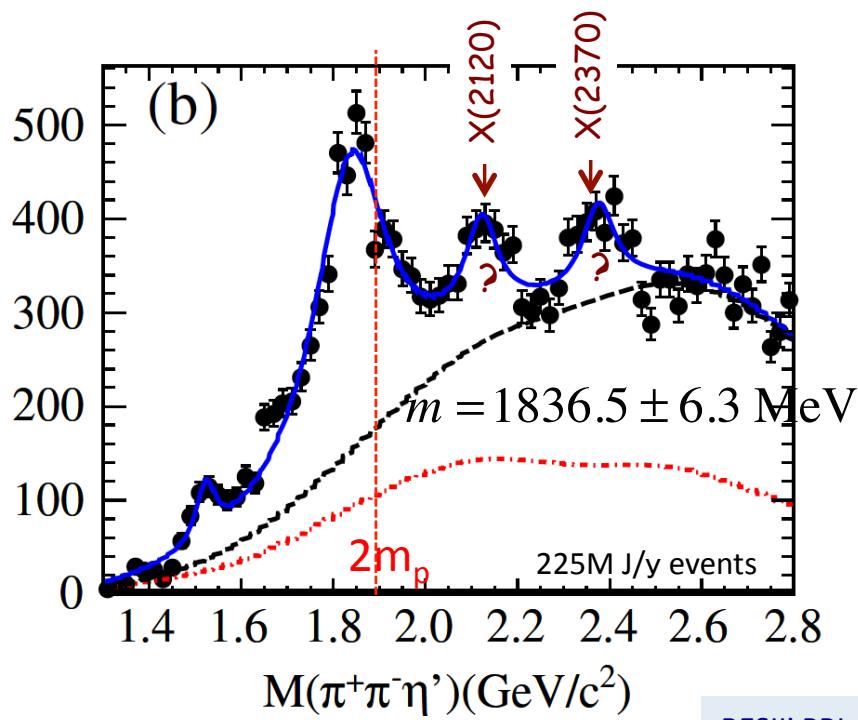
# $X(1835) \rightarrow \pi^+ \pi^- \eta'$ with 58M $J/\psi$ decays (BESII)



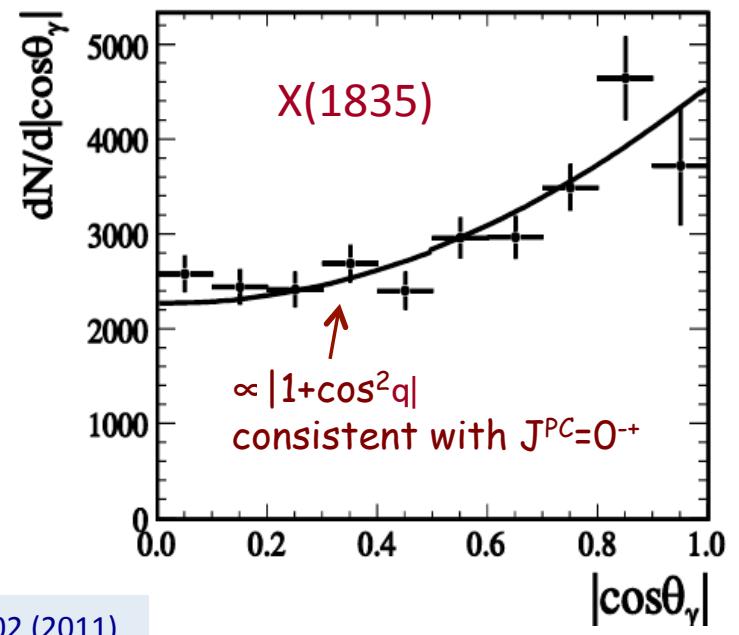
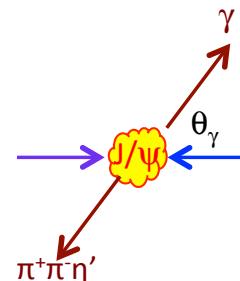
BESII PRL 95, 262001 (2005)

# $X(1835) \rightarrow \pi^+ \pi^- \eta'$ with 225M $J/\psi$ decays (BESIII)

BESIII observation of  $X(1835)$  in  
 $J/\psi \rightarrow \gamma \pi^+ \pi^- \eta'$

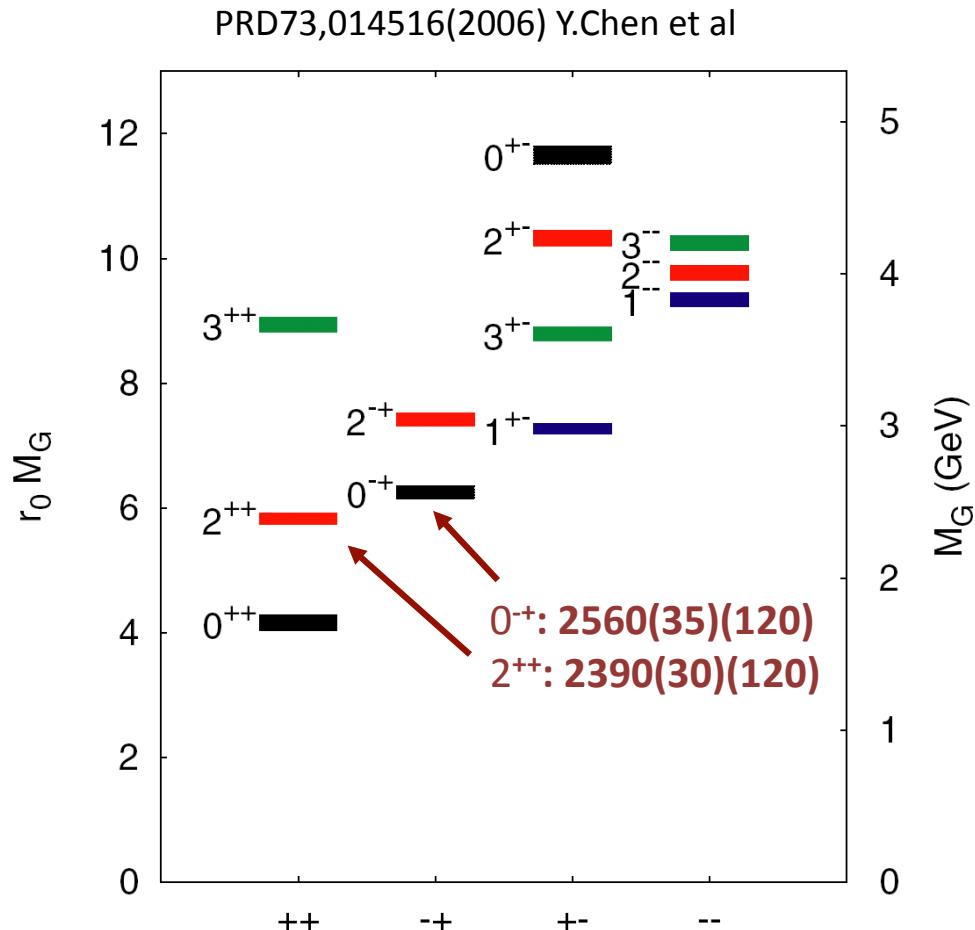


BESIII PRL 106, 072002 (2011)



# What are the new structures?

way above threshold, but narrow ( $\Gamma \approx 80$  MeV)!!

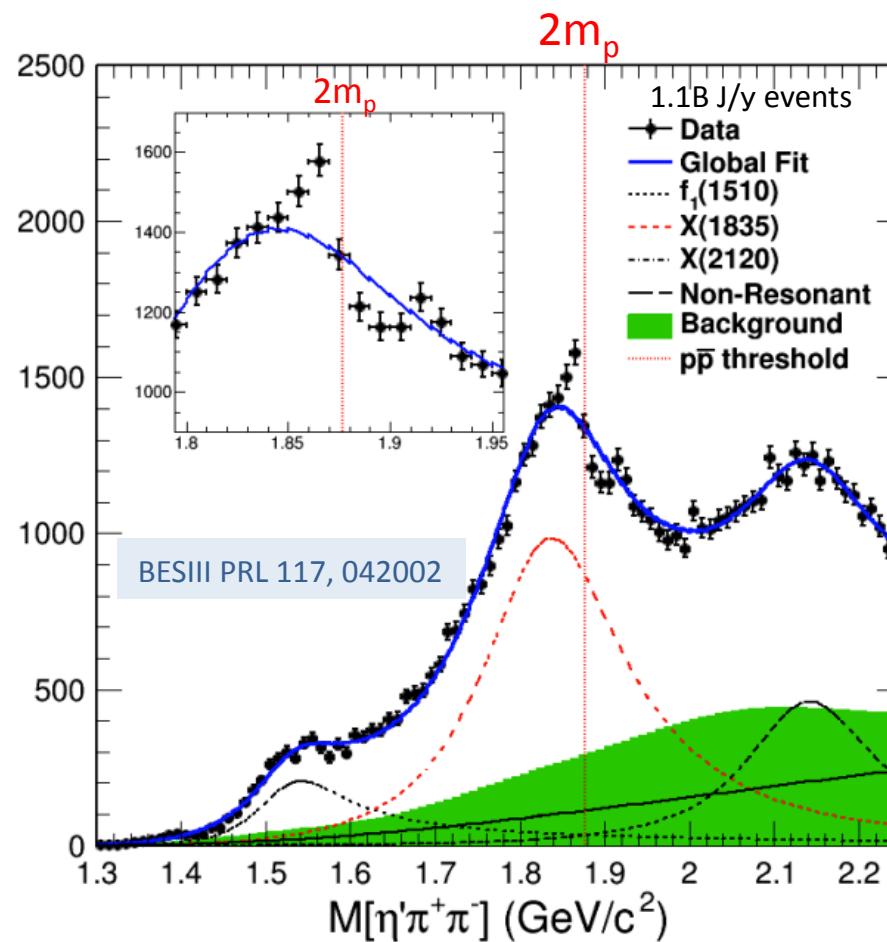


- ✓ first resonant structures observed in the 2.3 GeV region:
  - LQCD predicts that the lowest –lying pseudoscalar glueball: around 2.3 GeV
  - $J/\psi \rightarrow \eta' \pi^+ \pi^-$  is a good decay channel for finding  $0^+$  glueballs.
- ✓  $X(2120)/X(2370)$  possibilities:
  - pseudoscalar glueball ?
  - $\eta/\eta'$  radial excitations?

PRD82,074026,2010 J.F. Liu, G.J. Ding and M.L.Yan  
PRD83:114007,2011 (J.S. Yu, Z.-F. Sun, X. Liu, Q. Zhao)

# $X(1835) \rightarrow \pi^+ \pi^- \eta'$ with 1.1B $J/\psi$ events (BESIII)

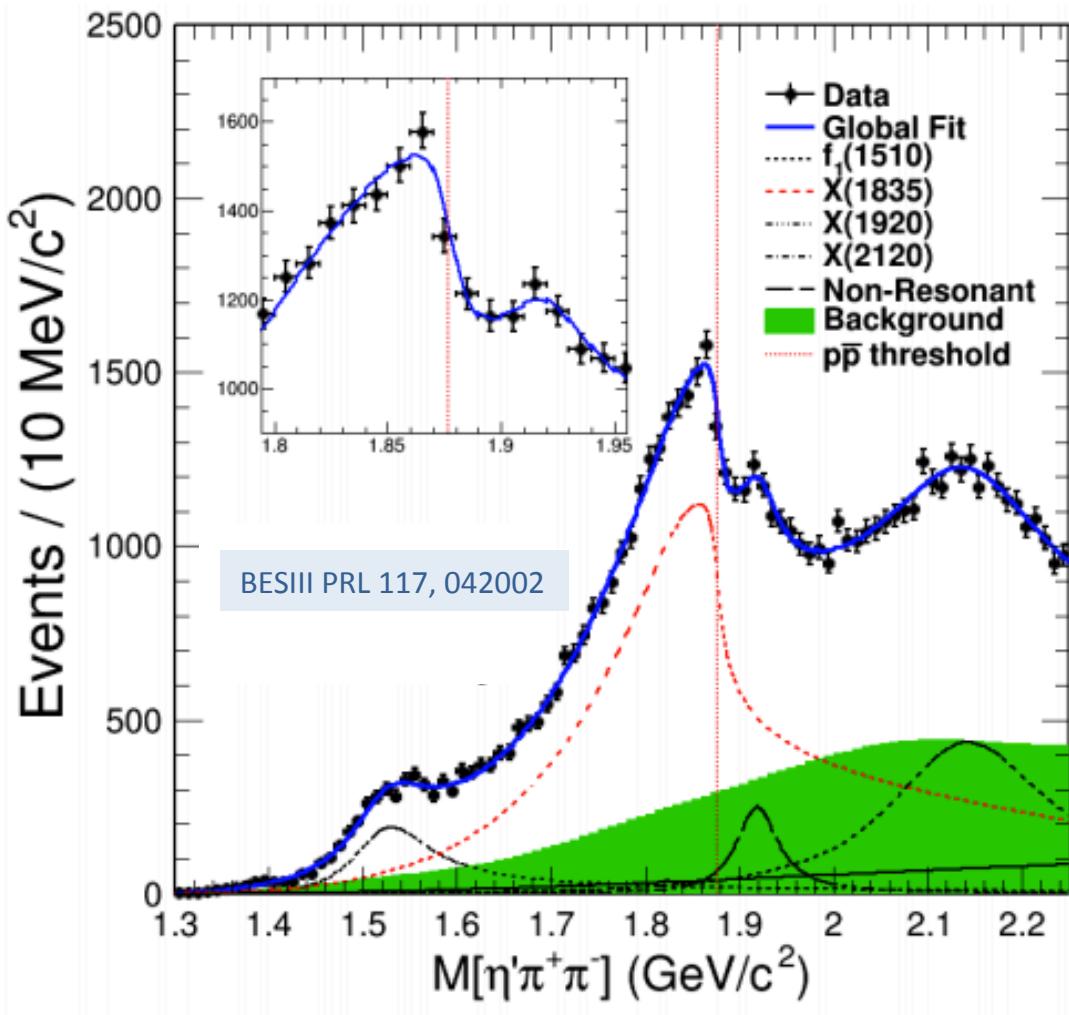
$$J/\psi \rightarrow \gamma \pi^+ \pi^- \eta'$$



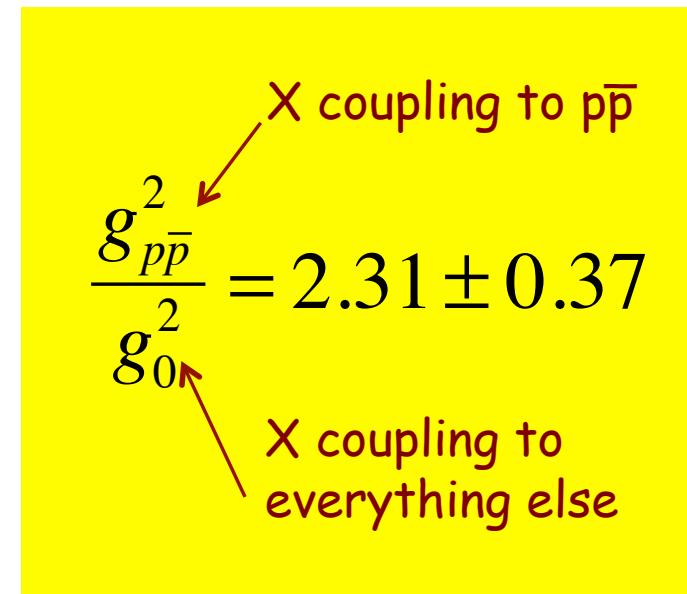
# Flatté formula fit:

$$T = \frac{\sqrt{\rho_{out}}}{\mathcal{M}^2 - s - i \sum_k g_k^2 \rho_k}, \sum_k g_k^2 \rho_k \simeq g_0^2 (\rho_0 + \frac{g_{p\bar{p}}^2}{g_0^2} \rho_{p\bar{p}})$$

S.M. Flatté PLB 63, 224 (1976)

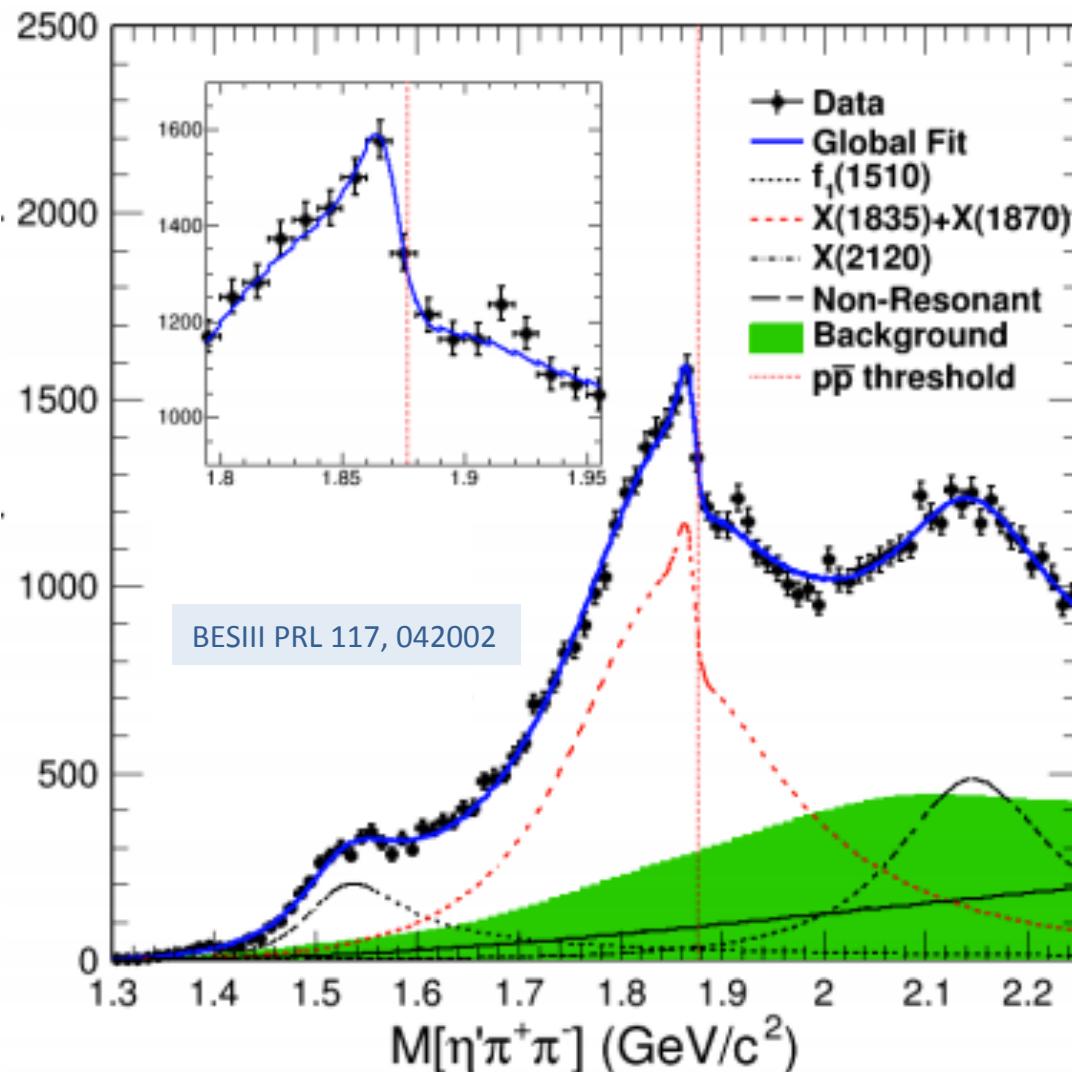


Fit results:



# Two-resonance fit

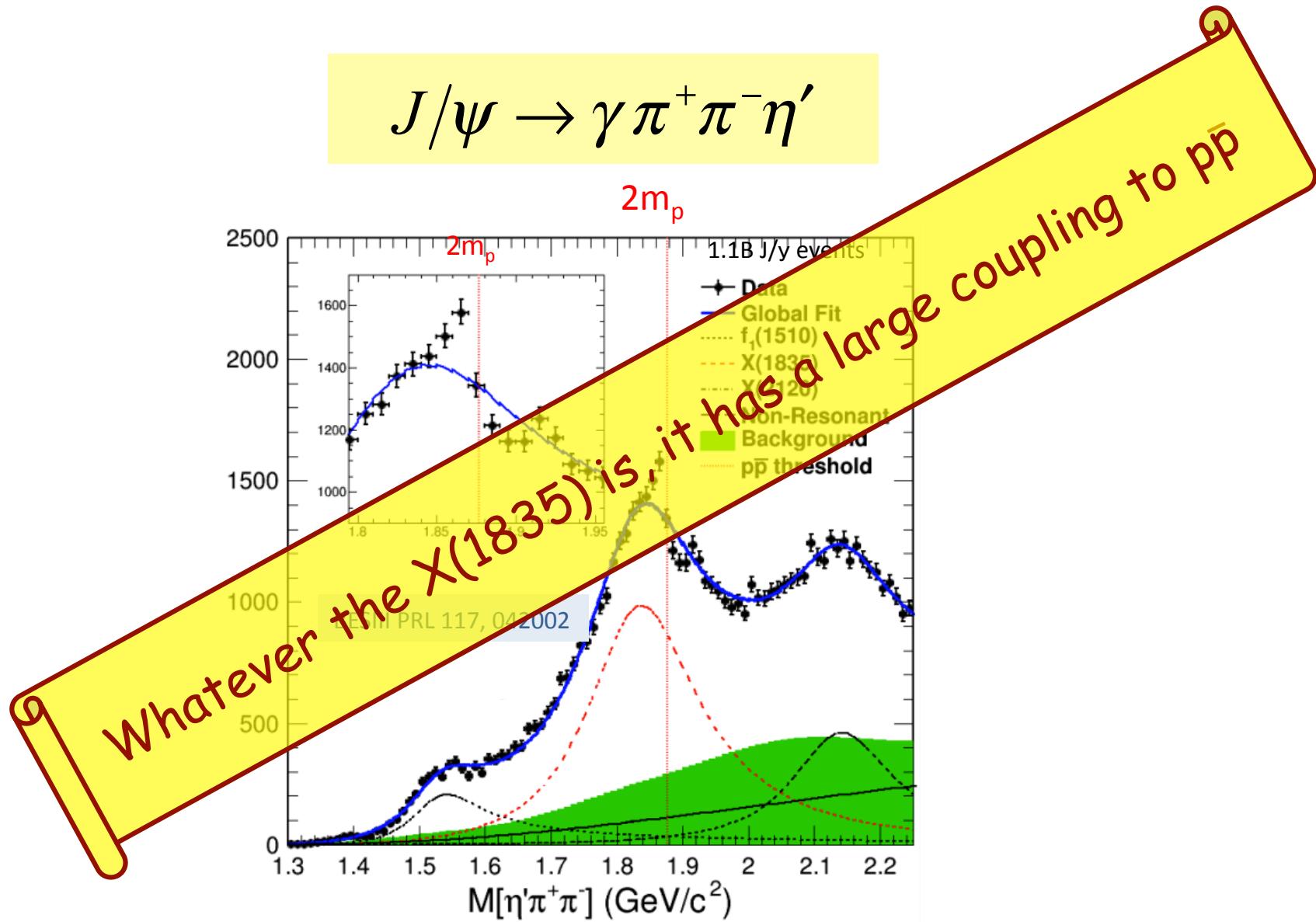
$$T = \frac{\sqrt{\rho_{out}}}{M_1^2 - s - iM_1\Gamma_1} + \frac{\beta \cdot e^{i\theta} \cdot \sqrt{\rho_{out}}}{M_2^2 - s - iM_2\Gamma_2}$$



**1<sup>st</sup> resonance (X(1835)):**  
 $M_1 = 1825.3 \pm 2.4^{+17.3}_{-2.4}$  MeV  
 $\Gamma_1 = 245 \pm 16$  MeV

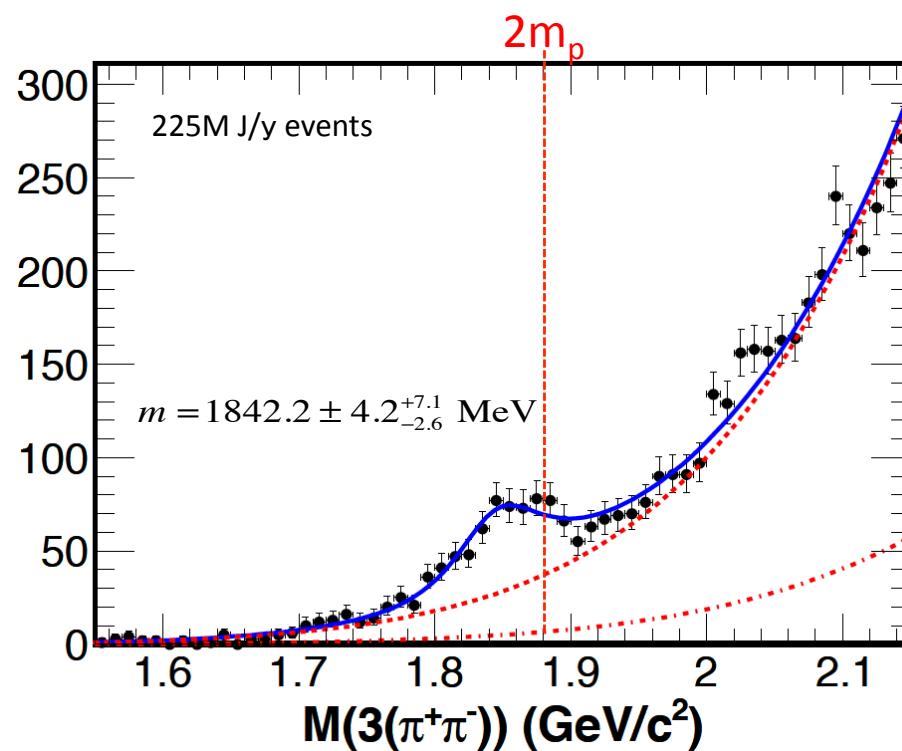
**2<sup>nd</sup> resonance (X(1870)):**  
 $M_2 = 2m_p - 6.3 \pm 3.2$  MeV  
 $\Gamma_2 = 13.0 \pm 6.7$  MeV

# $X(1835) \rightarrow \pi^+ \pi^- \eta'$ with 1.1B $J/\psi$ events



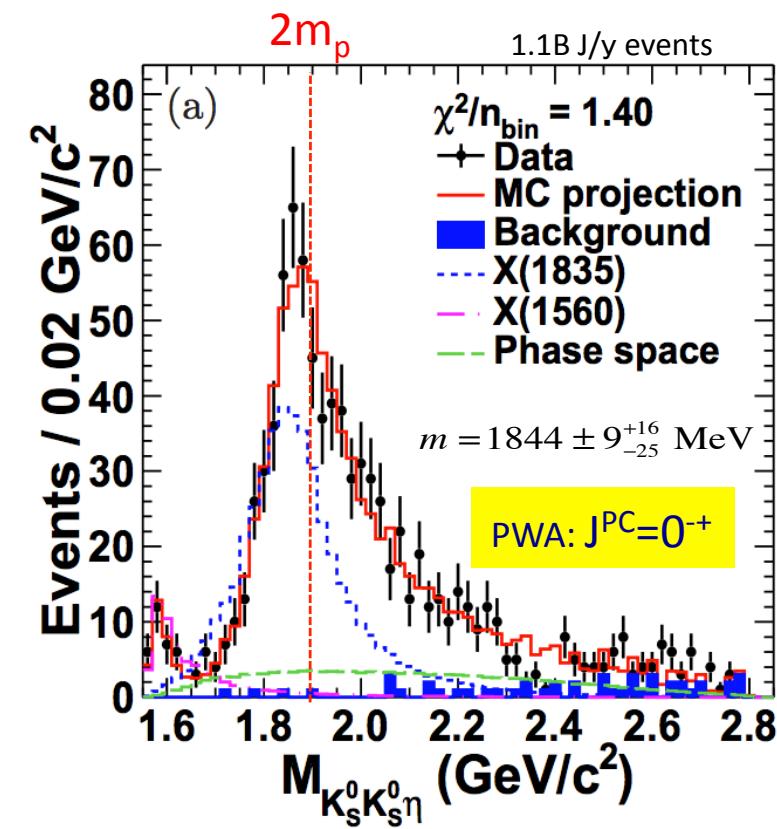
# X(1835) in other channels (BESIII)

$J/\psi \rightarrow \gamma 3(\pi^+ \pi^-)$



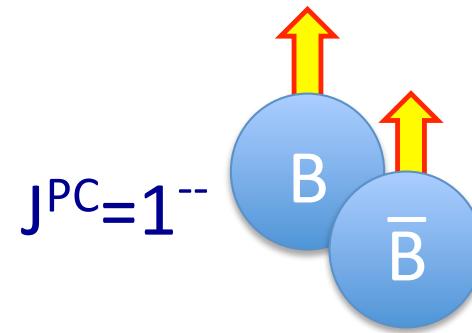
BESIII PRD 88, 091502 (2013)

$J/\psi \rightarrow \gamma K_S^0 K_S^0 \eta$

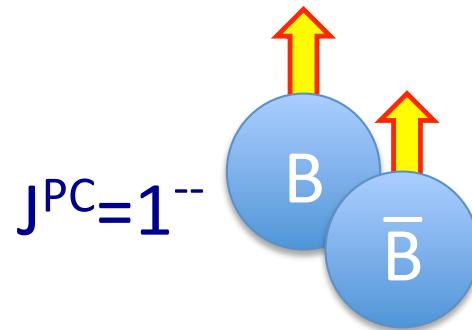


BESIII PRL 115, 091803 (2015)

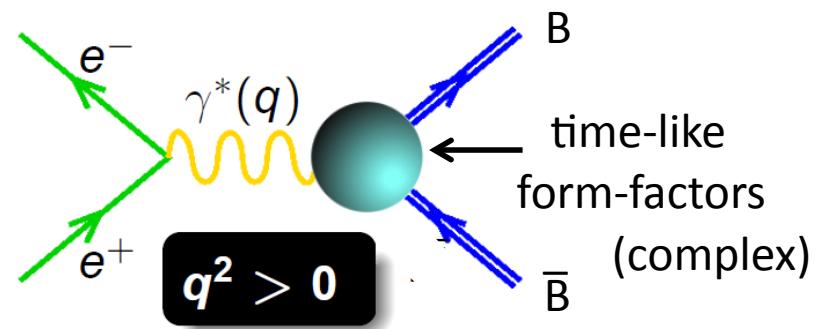
# $1^{--}$ baryon-antibaryon systems



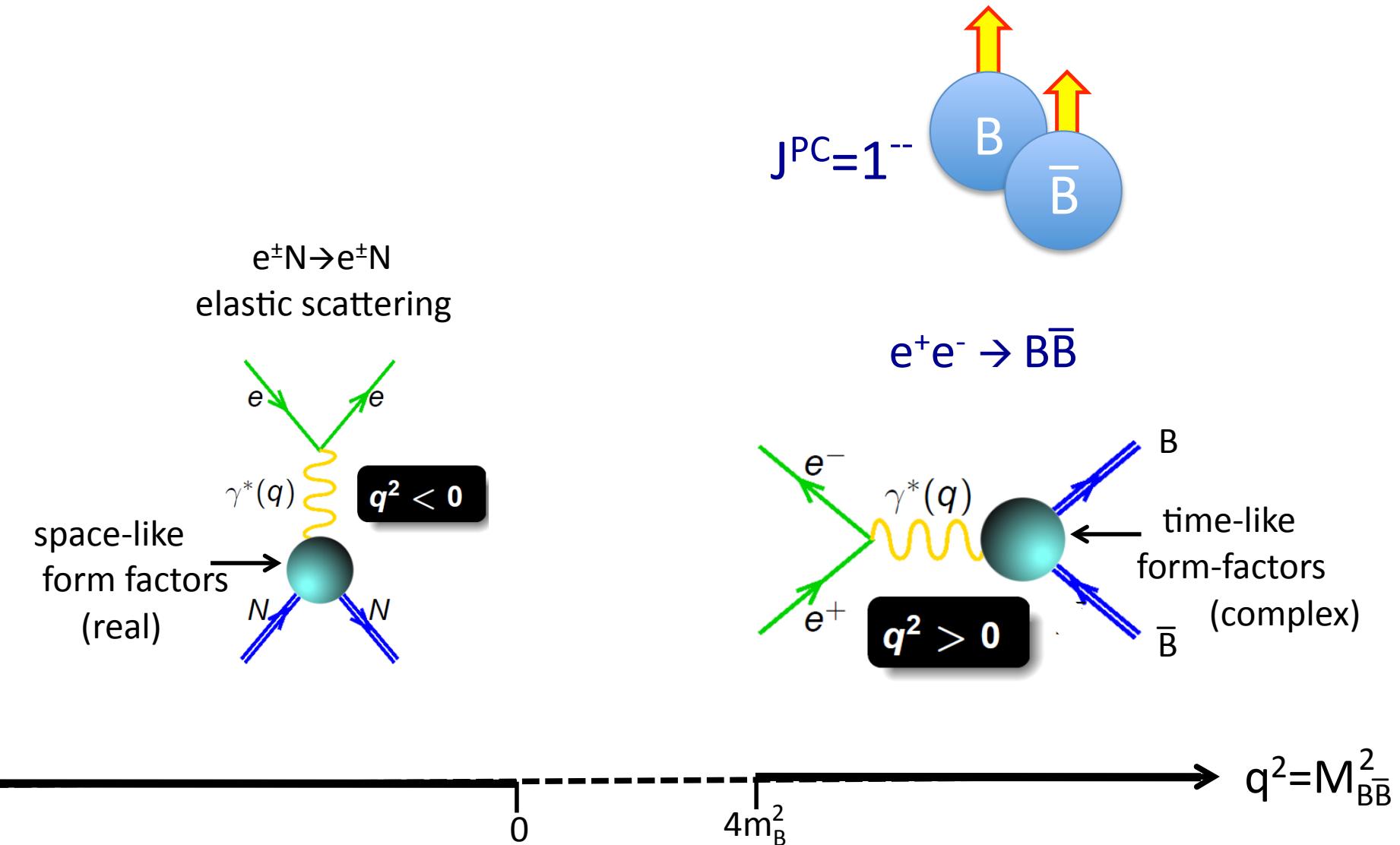
# $1^{--}$ baryon-antibaryon systems



$$e^+e^- \rightarrow B\bar{B}$$

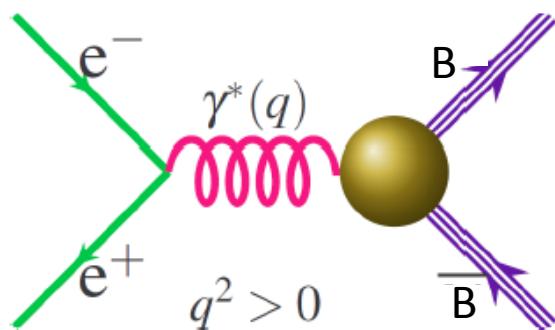


# $1^{--}$ baryon-antibaryon systems



# $e^+e^- \rightarrow p\bar{p}, n\bar{n} (\Lambda\bar{\Lambda})$ near threshold

$e^+e^- \leftrightarrow N\bar{N}, \Lambda\bar{\Lambda}, \dots$



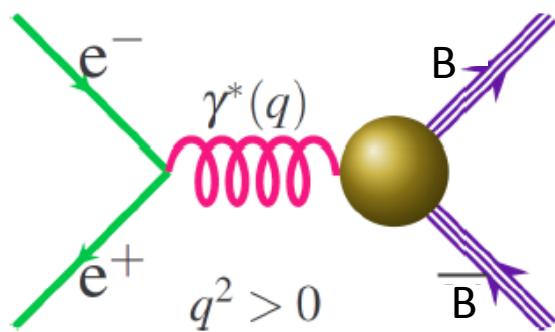
time-like form-factors

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2 \beta C}{4m_{B\bar{B}}^2} \left[ (1 + \cos^2 \theta) |G_M(m_{B\bar{B}})|^2 + \frac{1}{\tau} \sin^2 \theta |G_E(m_{B\bar{B}})|^2 \right]$$

$$\tau = \frac{m_{B\bar{B}}^2}{4m_B^2} \quad \beta = \sqrt{1 - \frac{1}{\tau}}$$

# $e^+e^- \rightarrow p\bar{p}, n\bar{n} (\Lambda\bar{\Lambda})$ near threshold

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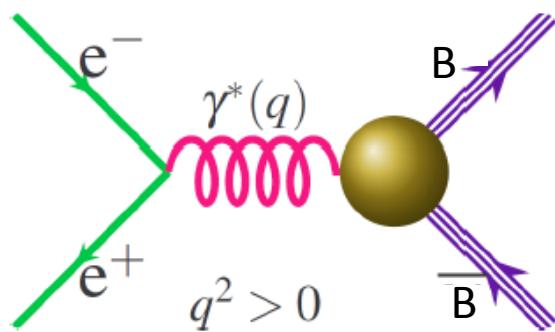
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$$\tau = \frac{m_{B\bar{B}}^2}{4m_B^2} \quad \beta = \sqrt{1 - \frac{1}{\tau}} \quad C = \text{Coulomb correction}$$

# $e^+e^- \rightarrow p\bar{p}, n\bar{n} (\Lambda\bar{\Lambda})$ near threshold

$e^+e^- \leftrightarrow N\bar{N}, \Lambda\bar{\Lambda}, \dots$



time-like form-factors

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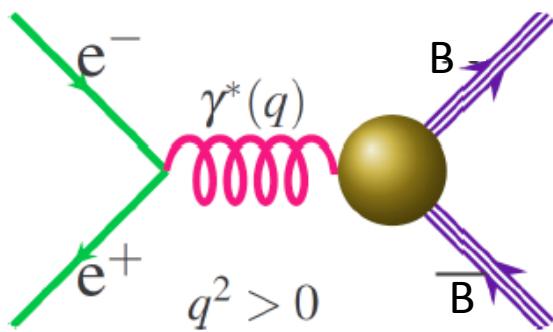
for  $p\bar{p}$ :  $C = \frac{\pi\alpha/\beta}{1 - \exp(-\pi\alpha/\beta)} \rightarrow \frac{\pi\alpha}{\beta}$

for  $n\bar{n}$  ( $\Lambda\bar{\Lambda}$ ):  $C = 1$

in point-like approx

# $e^+e^- \rightarrow p\bar{p}, n\bar{n} (\Lambda\bar{\Lambda})$ near threshold

$$e^+e^- \leftrightarrow N\bar{N}, \Lambda\bar{\Lambda}, \dots$$



time-like form-factors

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2 \beta C}{4m_{B\bar{B}}^2} \left[ (1 + \cos^2 \theta) |G_M(m_{B\bar{B}})|^2 + \frac{1}{\tau} \sin^2 \theta |G_E(m_{B\bar{B}})|^2 \right]$$

$$\tau = \frac{m_{B\bar{B}}^2}{4m_B^2} \quad \beta = \sqrt{1 - \frac{1}{\tau}}$$

for  $p\bar{p}$ :  $C = \frac{\pi\alpha/\beta}{1 - \exp(-\pi\alpha/\beta)} \rightarrow \frac{\pi\alpha}{\beta}$   
 for  $n\bar{n}$  ( $\Lambda\bar{\Lambda}$ ):  $C = 1$

in point-like approx

If the form-factors are analytic: as  $\tau \rightarrow 1$   $|G_E| \rightarrow |G_M|$  and  $\frac{d\sigma}{d\Omega} \rightarrow$  isotropic

Integrated cross section:

$$\sigma_{B\bar{B}}(m_{B\bar{B}}) = \frac{4\pi\alpha^2\beta C}{3m_{B\bar{B}}^2} \left[ |G_M(m_{B\bar{B}})|^2 + \frac{1}{2\tau} |G_E(m_{B\bar{B}})|^2 \right] = \frac{4\pi\alpha^2\beta C}{3m_{B\bar{B}}^2} |G_{eff}(m_{B\bar{B}})|^2 (1 + 1/2\tau)$$

“effective” form-factor

# effective form factor

$$|G_{eff}| = \sqrt{\frac{2\tau |G_M|^2 + |G_E|^2}{2\tau + 1}}$$

## numerology

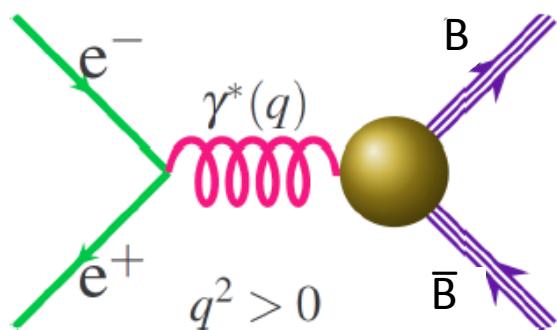
$$\sigma_{B\bar{B}}(m_{B\bar{B}}) = \frac{4\pi\alpha^2\beta C}{3m_{B\bar{B}}^2} |G_{eff}(m_{B\bar{B}})|^2 (1+1/2\tau) = 98.6 \text{ nb} \frac{\beta C}{m_{B\bar{B}}^2 / m_p^2} |G_{eff}(m_{B\bar{B}})|^2 (1+1/2\tau)$$

$$\frac{4\pi\alpha^2}{3m_p^2} = 98.6 \text{ nb}; \quad \text{at threshold: } \begin{aligned} \tau &\rightarrow 1 \\ m_{B\bar{B}} &\rightarrow 2m_B \\ |G_{eff}| &\rightarrow |G_M| \end{aligned}$$

# $e^+e^- \rightarrow p\bar{p}, n\bar{n} (\Lambda\bar{\Lambda})$ near threshold

Integrated cross section

$$e^+e^- \leftrightarrow N\bar{N}, \Lambda\bar{\Lambda}, \dots$$

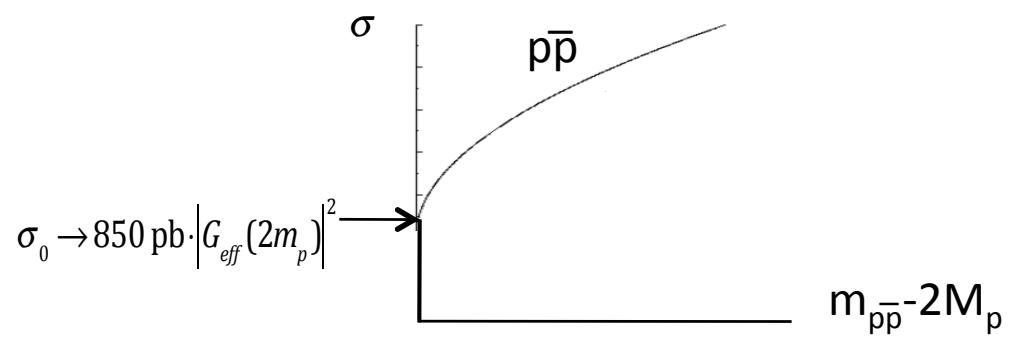
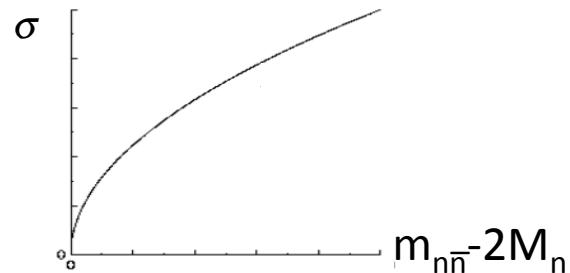


$$\sigma_{B\bar{B}}(m_{B\bar{B}}) = 98.6 \text{ nb} \frac{\beta C}{m_{B\bar{B}}^2/m_p^2} |G_{eff}(m_{B\bar{B}})|^2 (1 + 1/2\tau)$$

$$\text{for } p\bar{p}: C = \frac{\pi\alpha/\beta}{1 - \exp(-\pi\alpha/\beta)} \rightarrow \frac{\pi\alpha}{\beta}$$

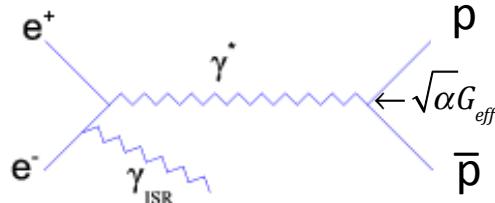
$$\sigma_{p\bar{p}}(m_{p\bar{p}} \rightarrow 2m_p) \rightarrow 0.85 \text{ nb} |G_{eff}(2m_p)|^2$$

for  $n\bar{n} (\Lambda\bar{\Lambda})$ :  $C=1$

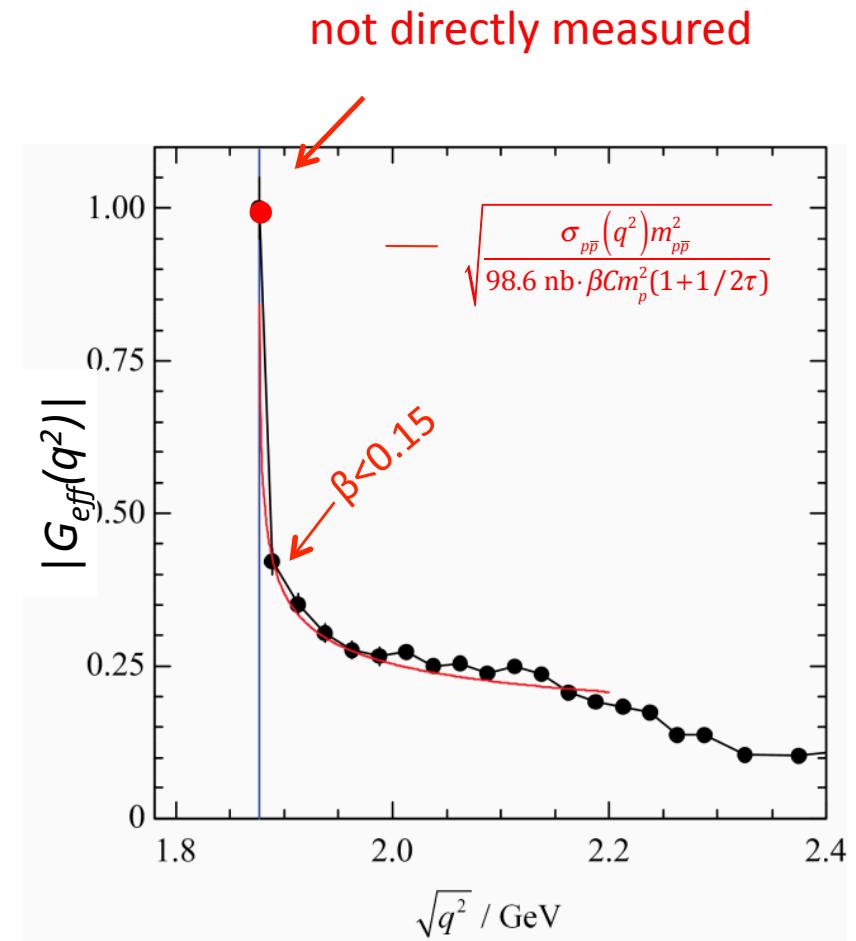
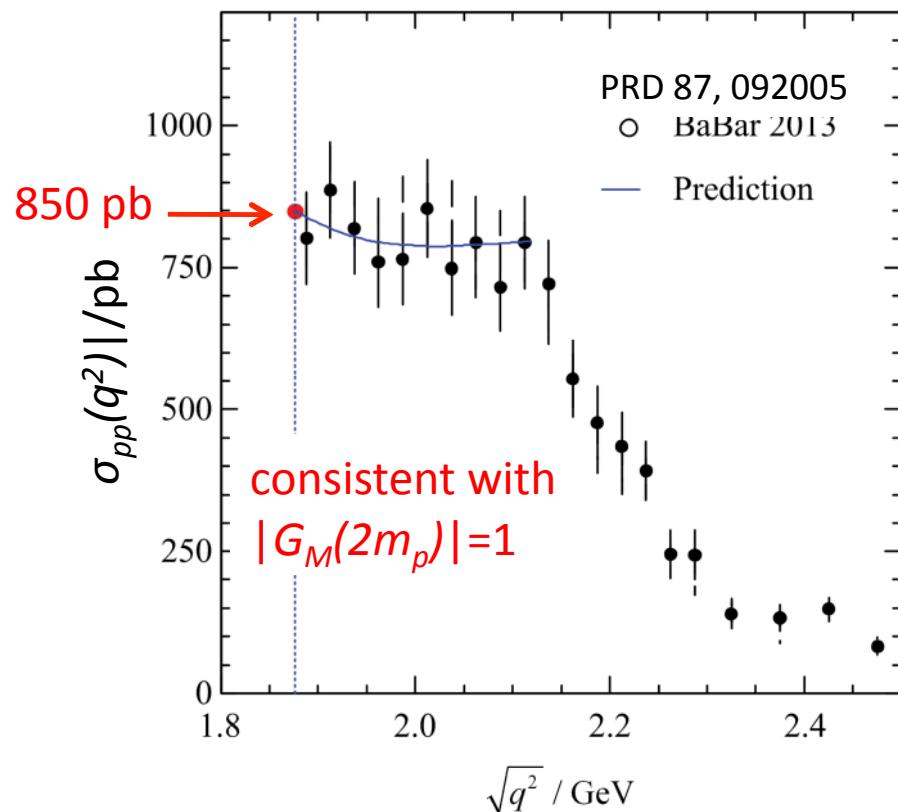


# $\sigma(e^+e^- \rightarrow p\bar{p})$ threshold data

--from BaBar, using initial-state-radiation--

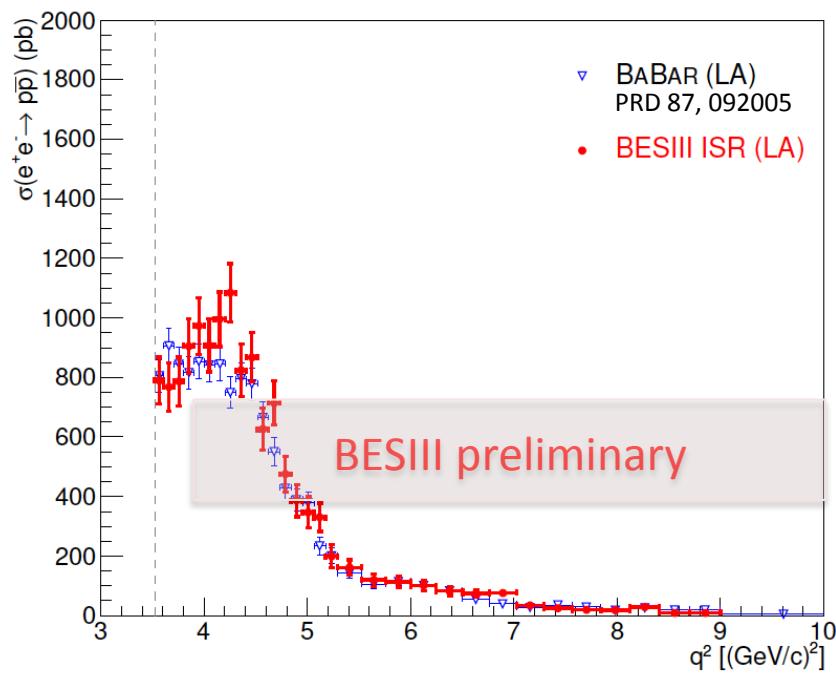


$\sigma(e^+e^- \rightarrow \gamma_{\text{ISR}} p\bar{p})$

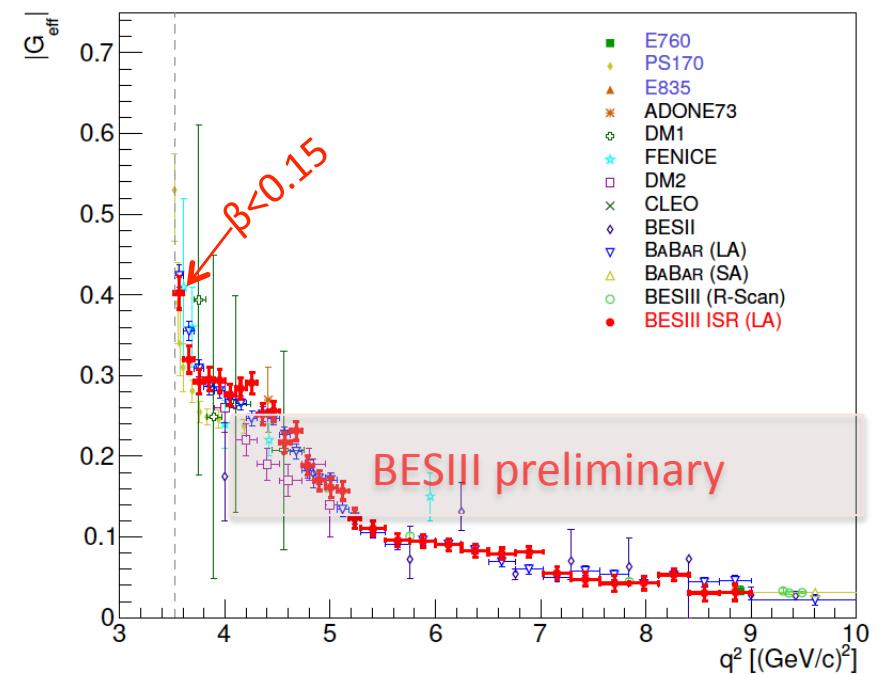


# Preliminary BESIII data confirms BaBar

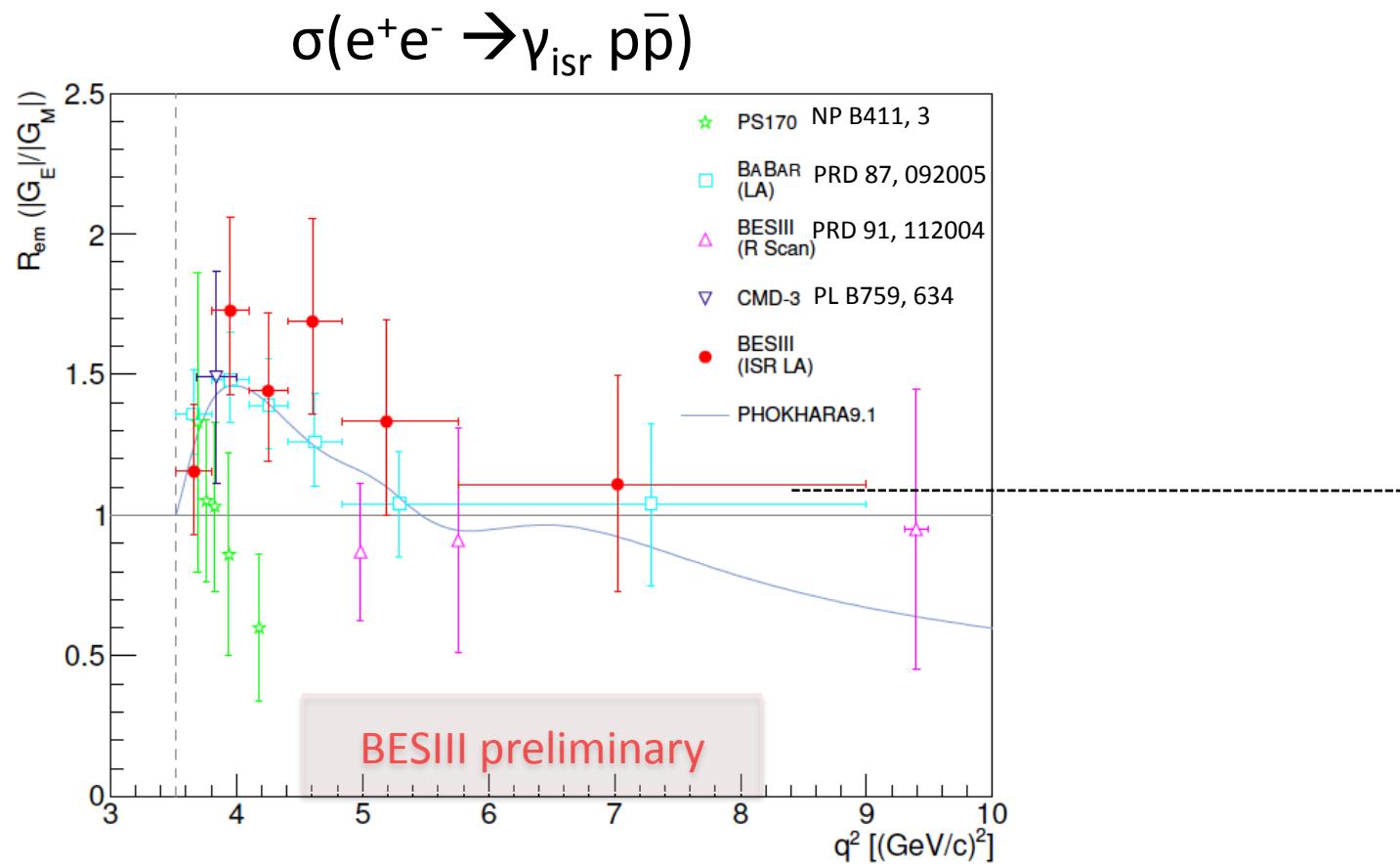
$$\sigma(e^+e^- \rightarrow \gamma_{\text{ISR}} p\bar{p})$$



$$|G_{eff}|$$

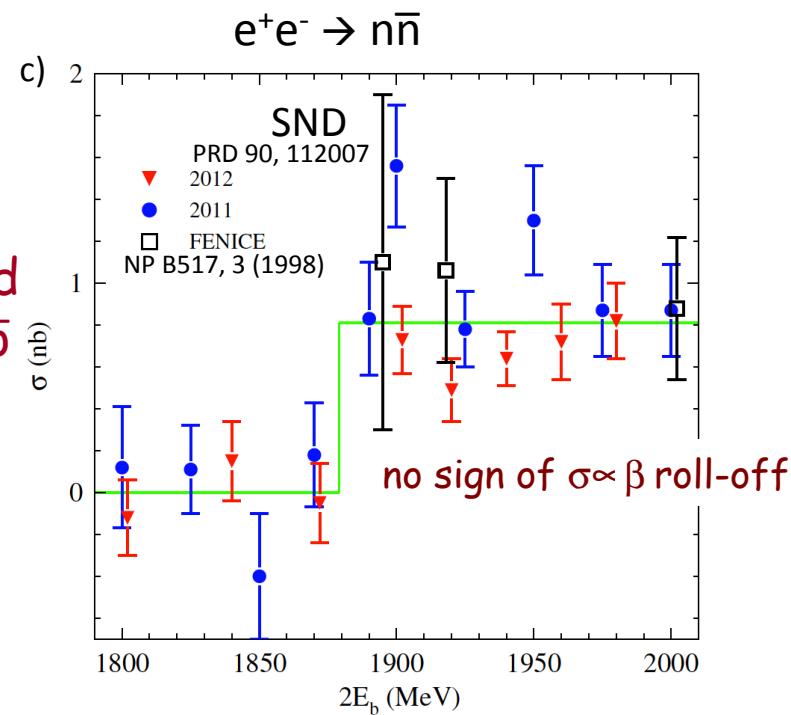


$$|G_E(2m_p)|/|G_M(2m_p)| \rightarrow 1$$

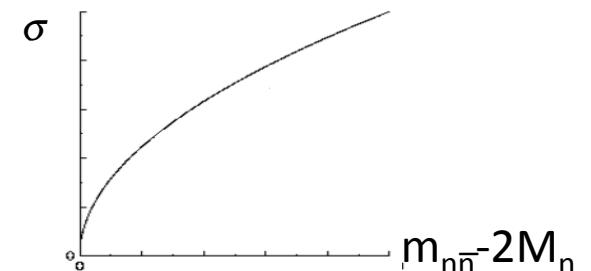


# $\sigma(e^+e^- \rightarrow n\bar{n})$ near threshold

~ same size threshold jump as seen for  $p\bar{p}$

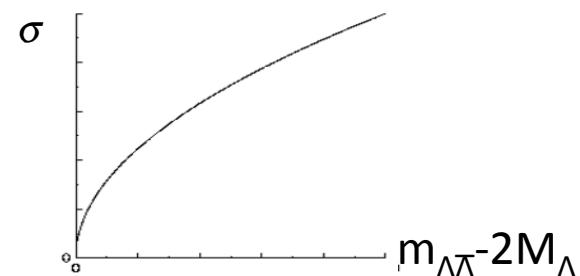


for  $n\bar{n}$ ,  $C=1$ ;  $\sigma \propto \beta$



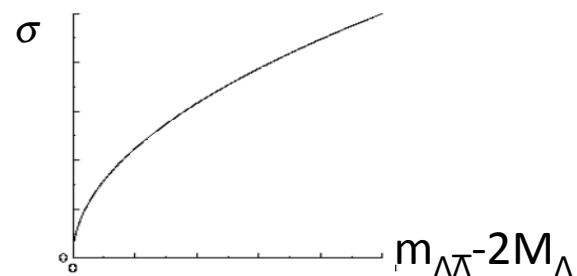
$e^+e^- \rightarrow \gamma^* \rightarrow \Lambda\bar{\Lambda}$  at threshold

for  $\Lambda\bar{\Lambda}$ , C=1;  $\sigma \propto \beta$



$e^+e^- \rightarrow \gamma^* \rightarrow \Lambda\bar{\Lambda}$  at threshold

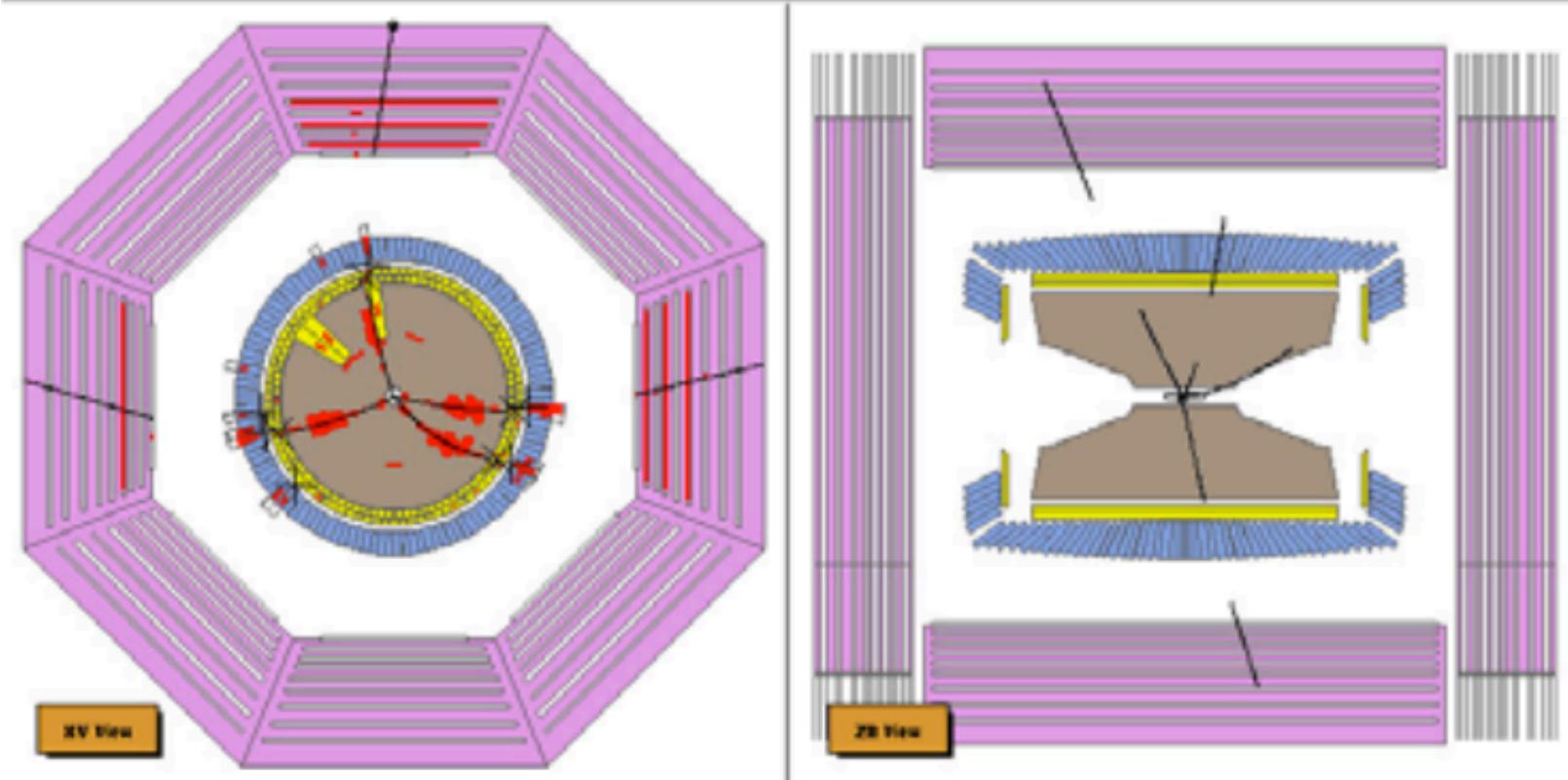
for  $\Lambda\bar{\Lambda}$ ,  $C=1$ ;  $\sigma \propto \beta$



but 1<sup>st</sup> some experimental physics

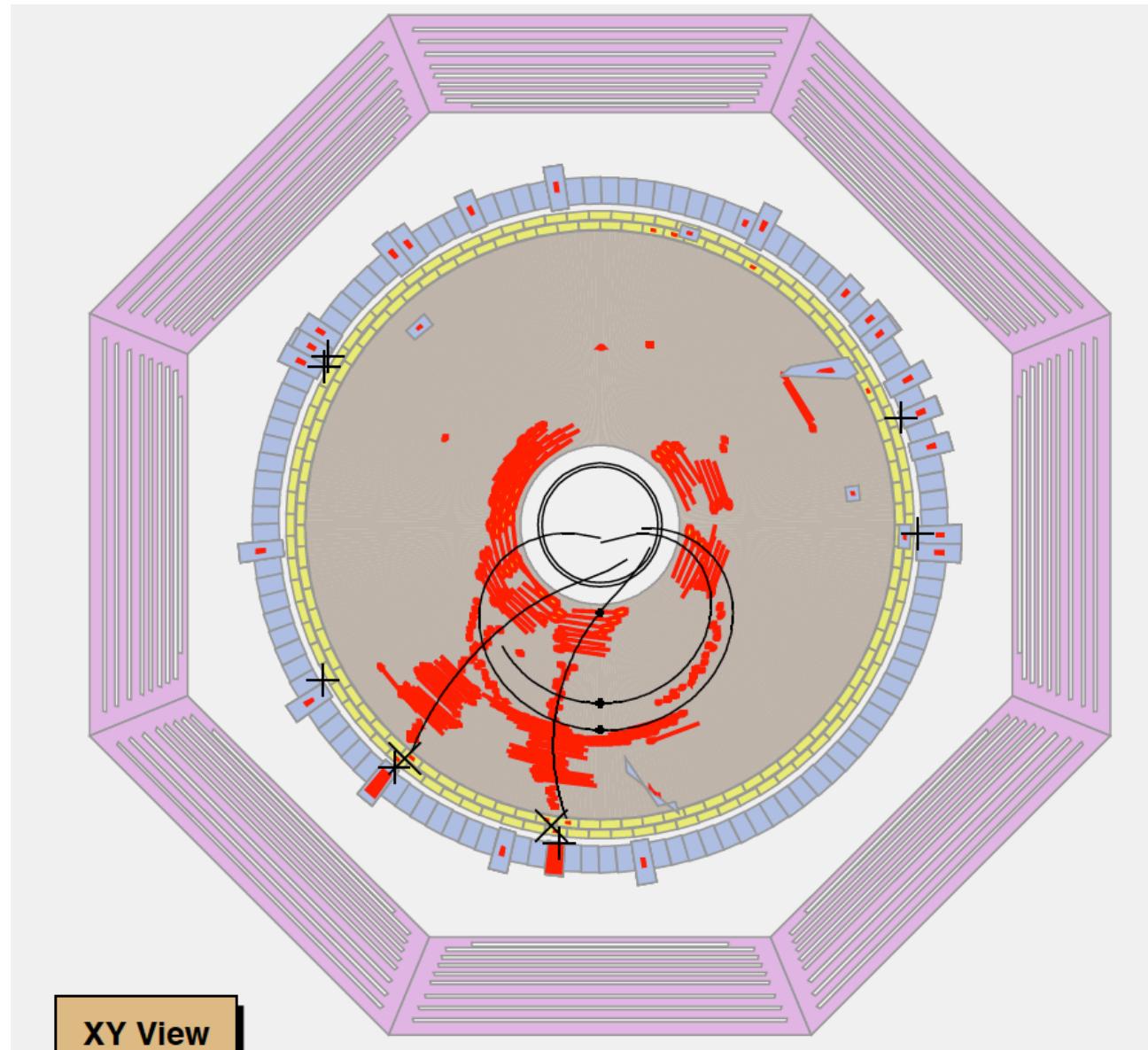
# First event in BESIII

July 20, 2007

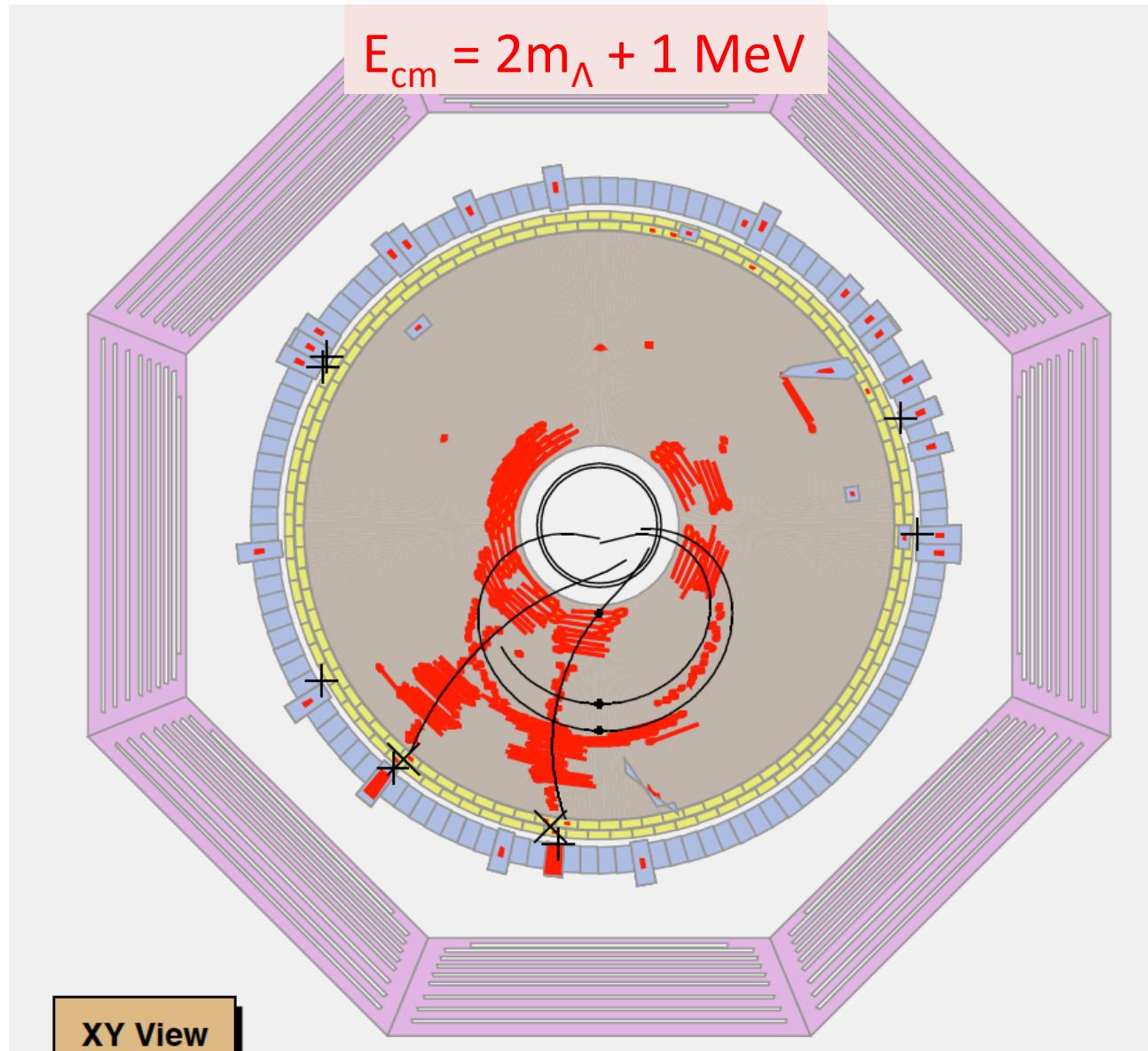


First collision event

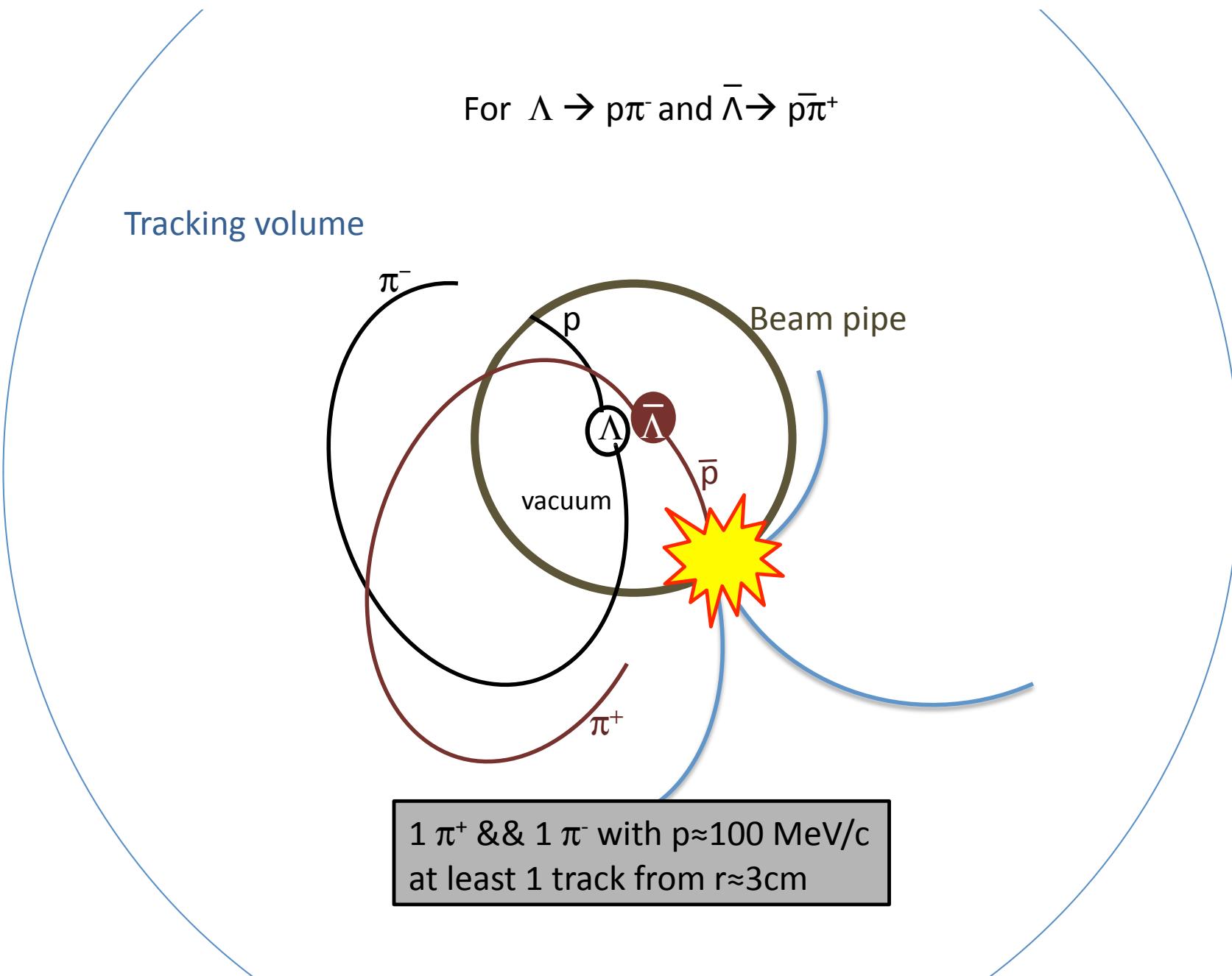
# events we don't usually show in public



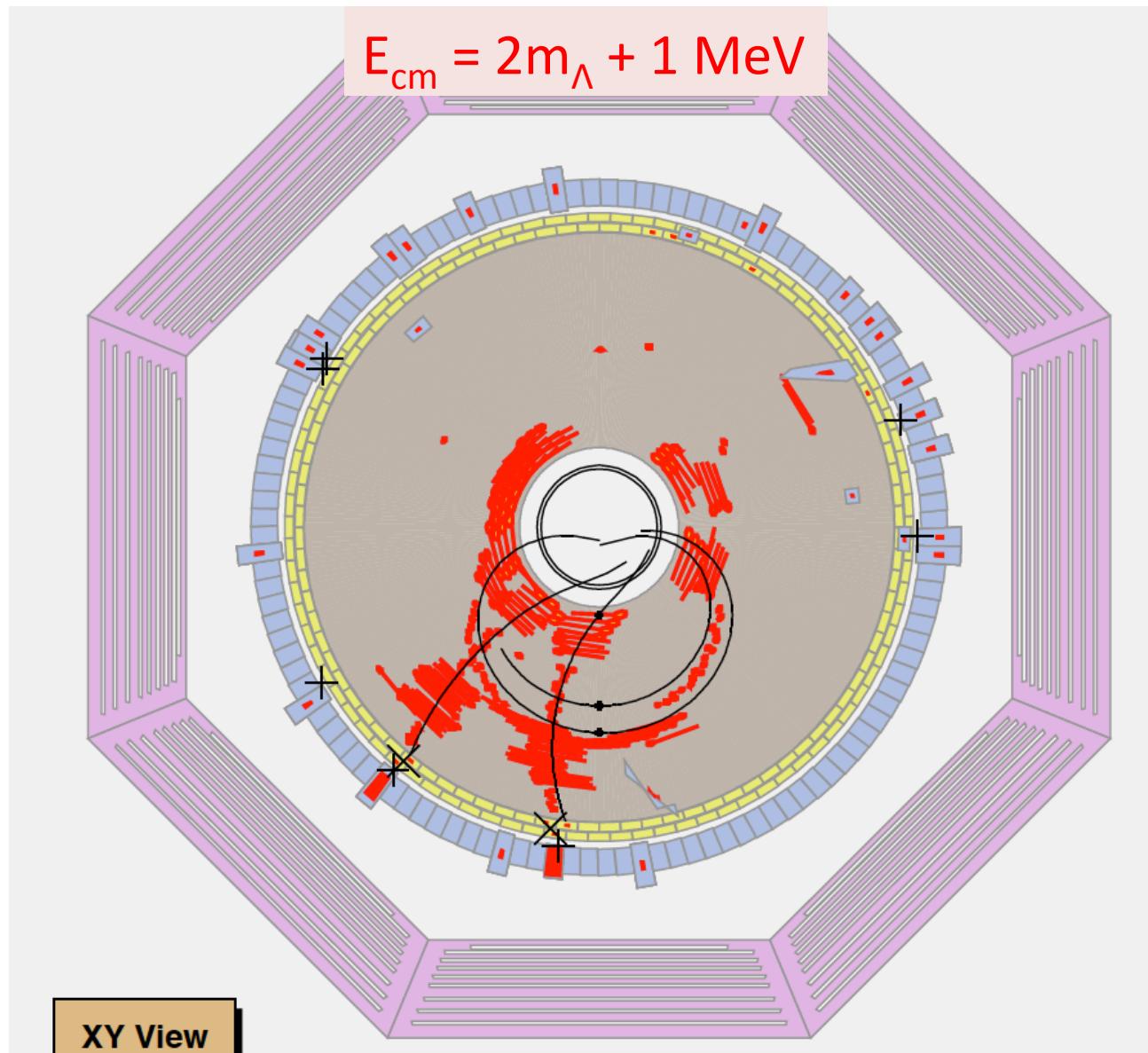
# events we don't usually show in public



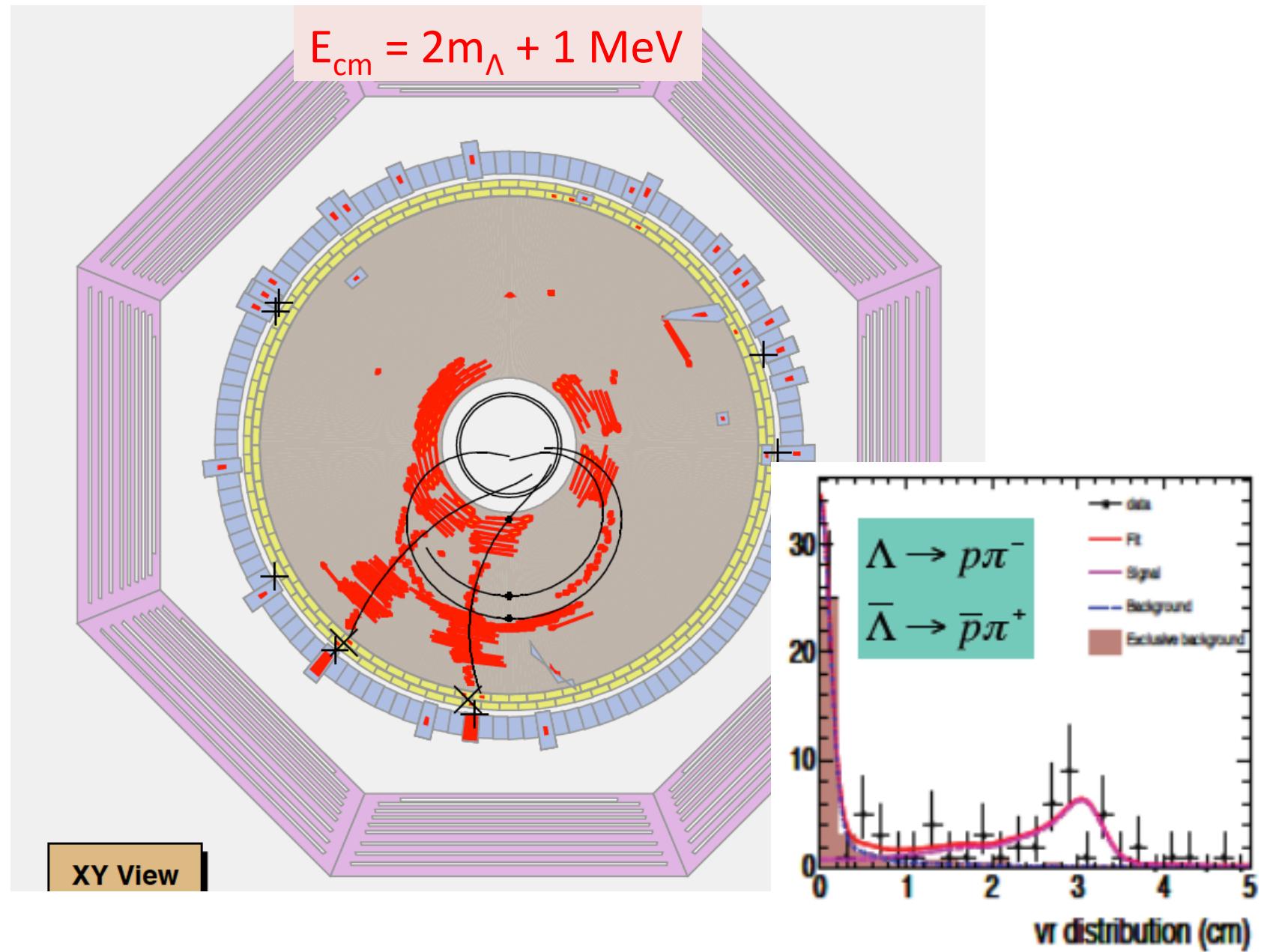
# What would a $\Lambda\bar{\Lambda}$ at rest look like in BESIII



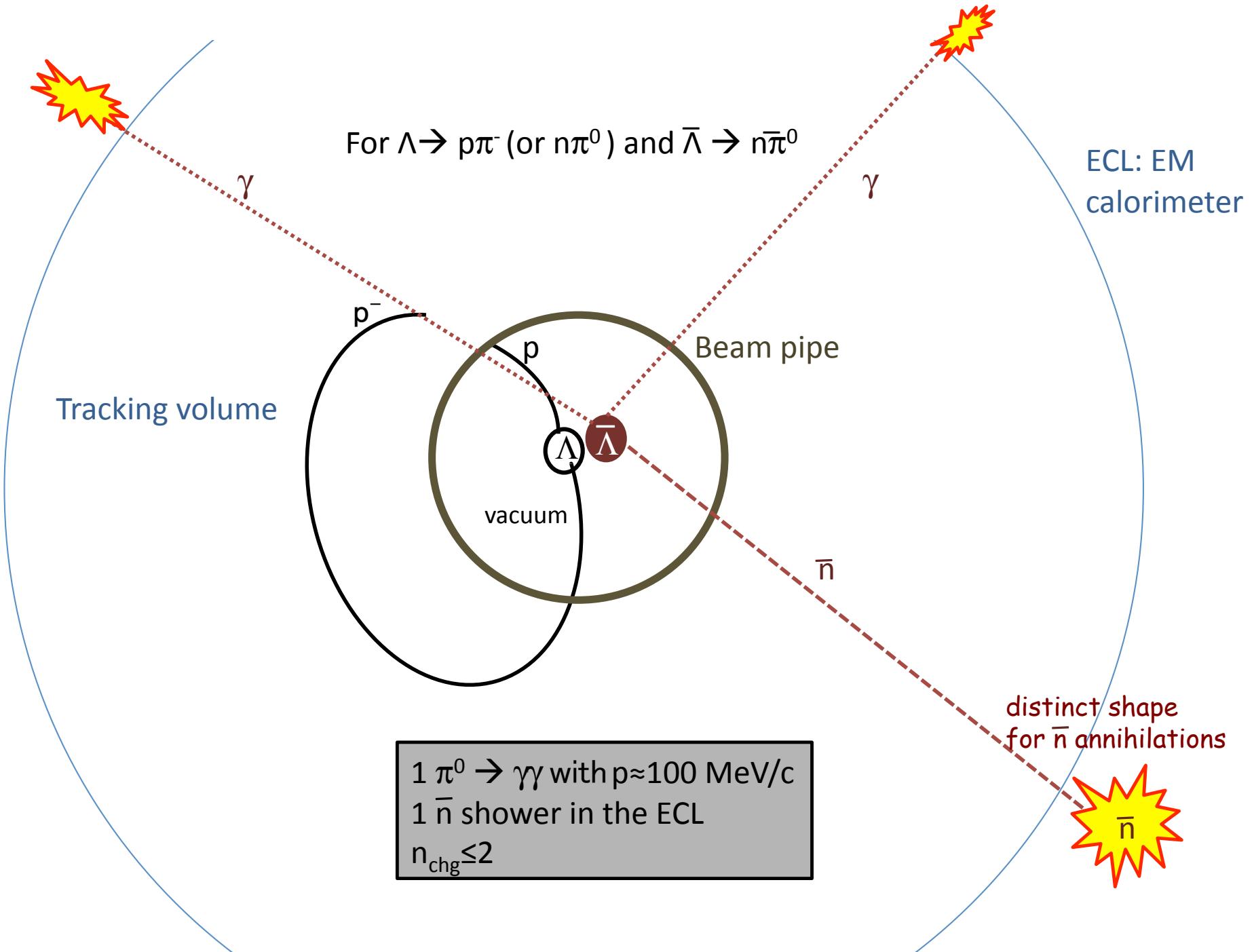
# about like this



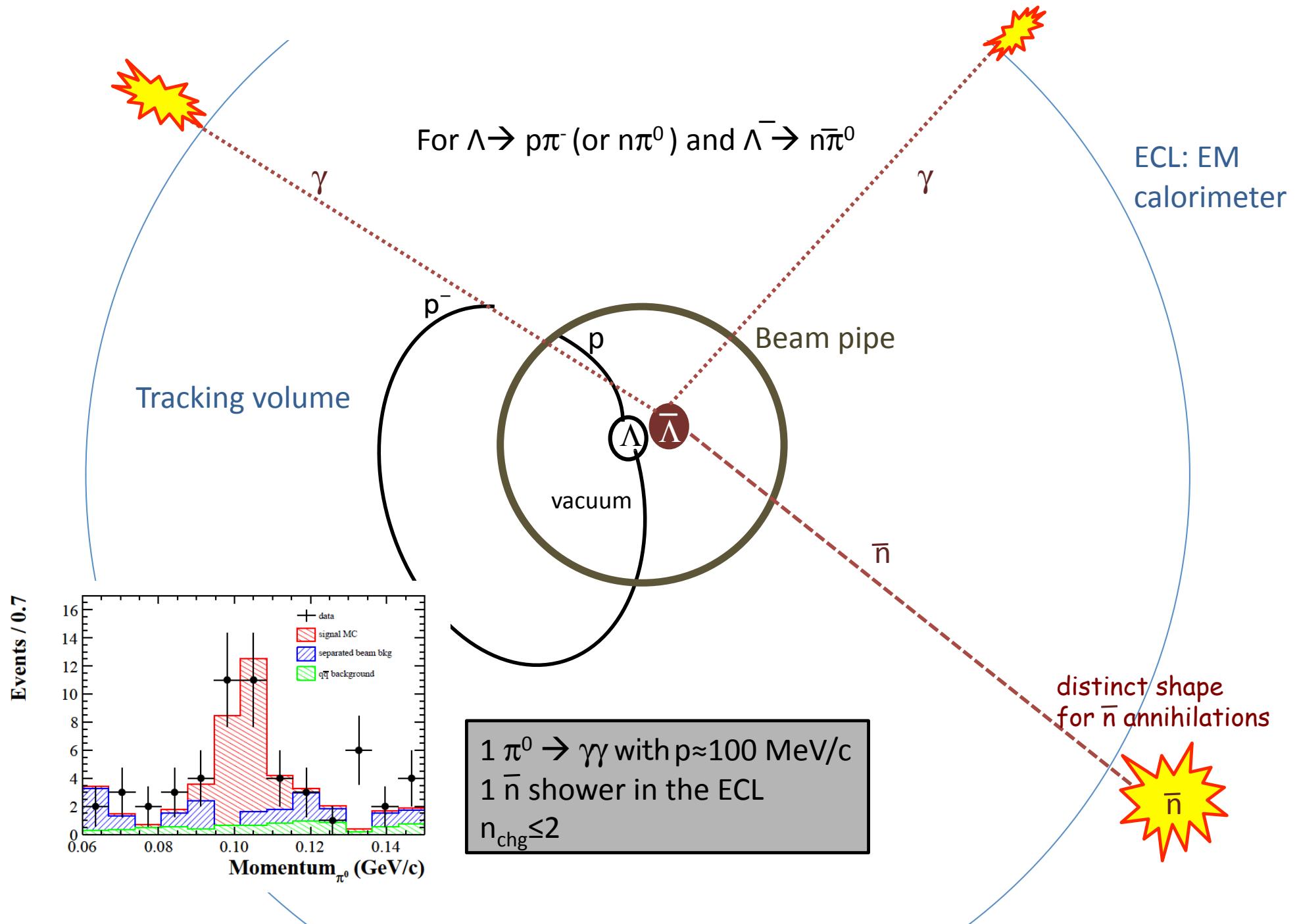
# about like this



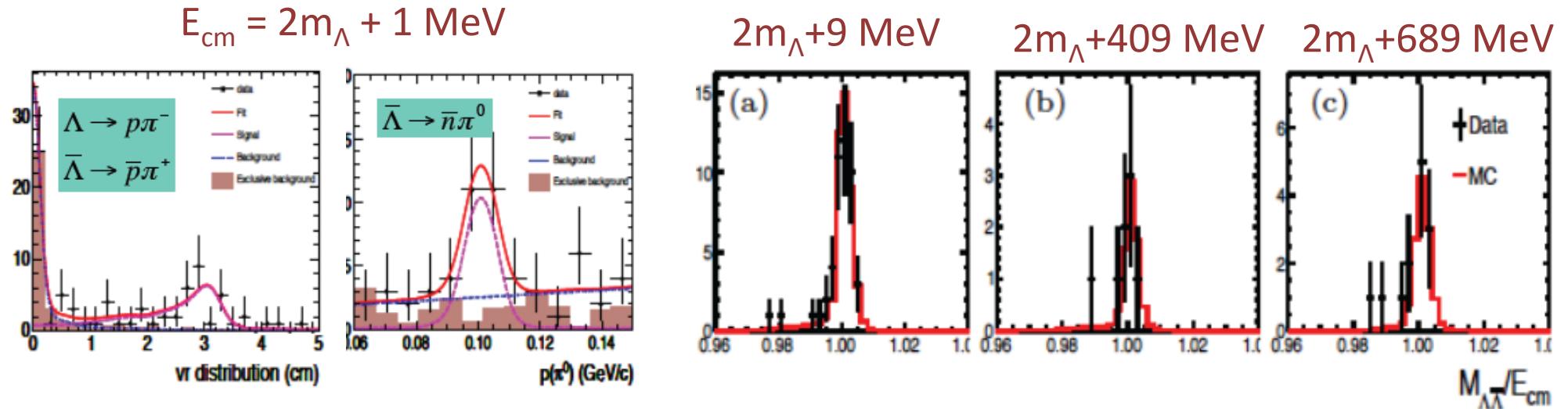
# What would a $\Lambda\bar{\Lambda}$ at rest look like in BESIII



# What would a $\Lambda\bar{\Lambda}$ at rest look like in BESIII



# BESIII $e^+e^- \rightarrow \Lambda\bar{\Lambda}$ measurements



$\sqrt{s}$ (GeV)	$\mathcal{L}_{int}$ (pb $^{-1}$ )	$N_{obs}$	$\epsilon(1+\delta)$ (%)	$\sigma^B$ (pb)	$ G $ ( $\times 10^{-2}$ )
2.2324 <sub>1</sub>	2.63	$43 \pm 7$	12.9	$312 \pm 51^{+72}_{-45}$	$61.9 \pm 4.6^{+11.6}_{-9.0}$
2.2324 <sub>2</sub>	2.63	$22 \pm 6$	8.25	$288 \pm 96^{+64}_{-36}$	
2.2324 <sub>c</sub>				$305 \pm 45^{+66}_{-36}$	
2.400	3.42	$45 \pm 7$	25.3	$128 \pm 19 \pm 18$	$12.7 \pm 0.9 \pm 0.9$
2.800	3.75	$8 \pm 3$	36.1	$14.8 \pm 5.2 \pm 1.9$	$4.10 \pm 0.72 \pm 0.26$
3.080	30.73	$13 \pm 4$	24.5	$4.2 \pm 1.2 \pm 0.5$	$2.29 \pm 0.33 \pm 0.14$

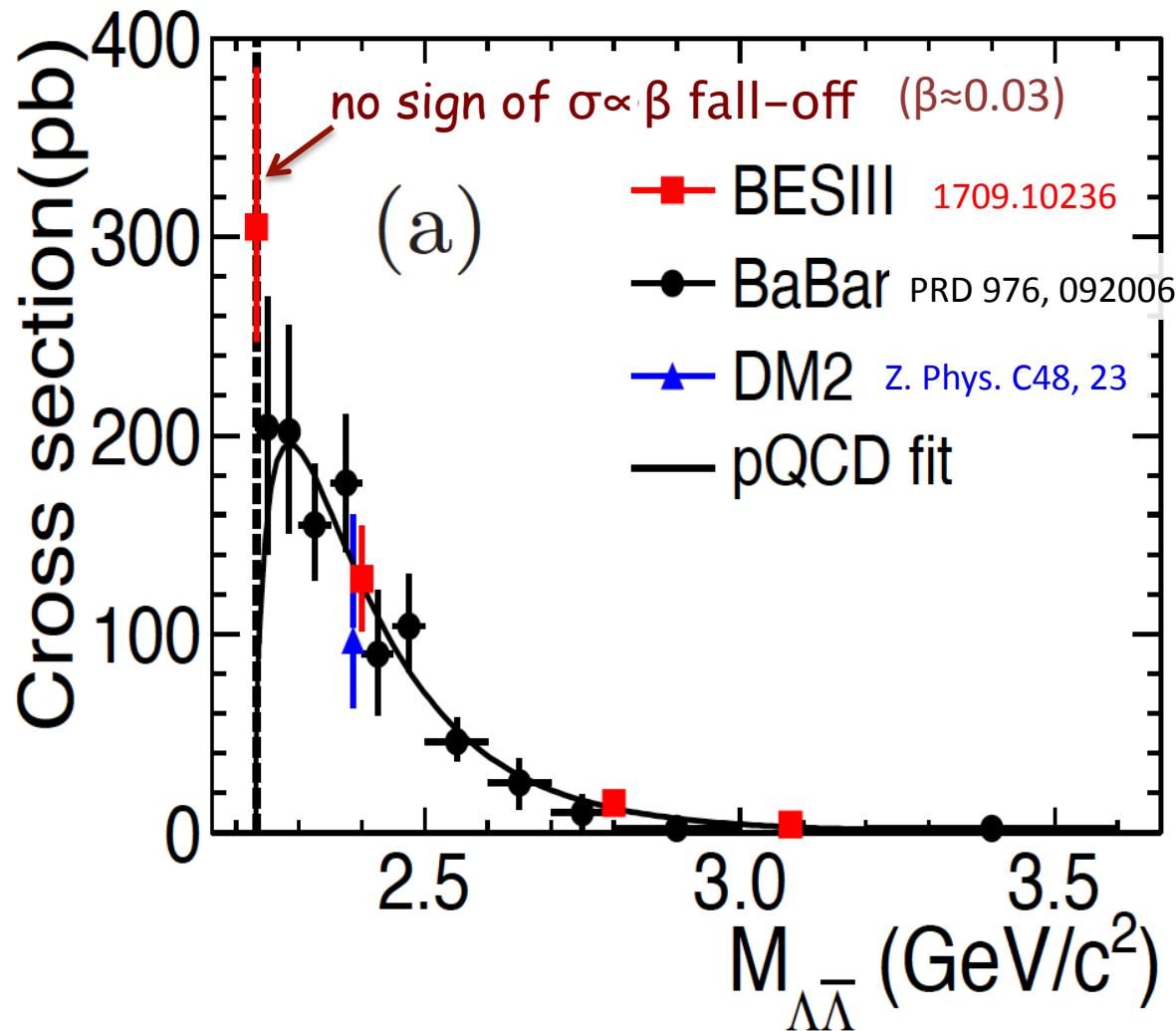
conventional analyses at higher energies { }

two methods are consistent

BESIII 709.10236

# Cross section: $e^+e^- \rightarrow \gamma^* \rightarrow \Lambda\bar{\Lambda}$

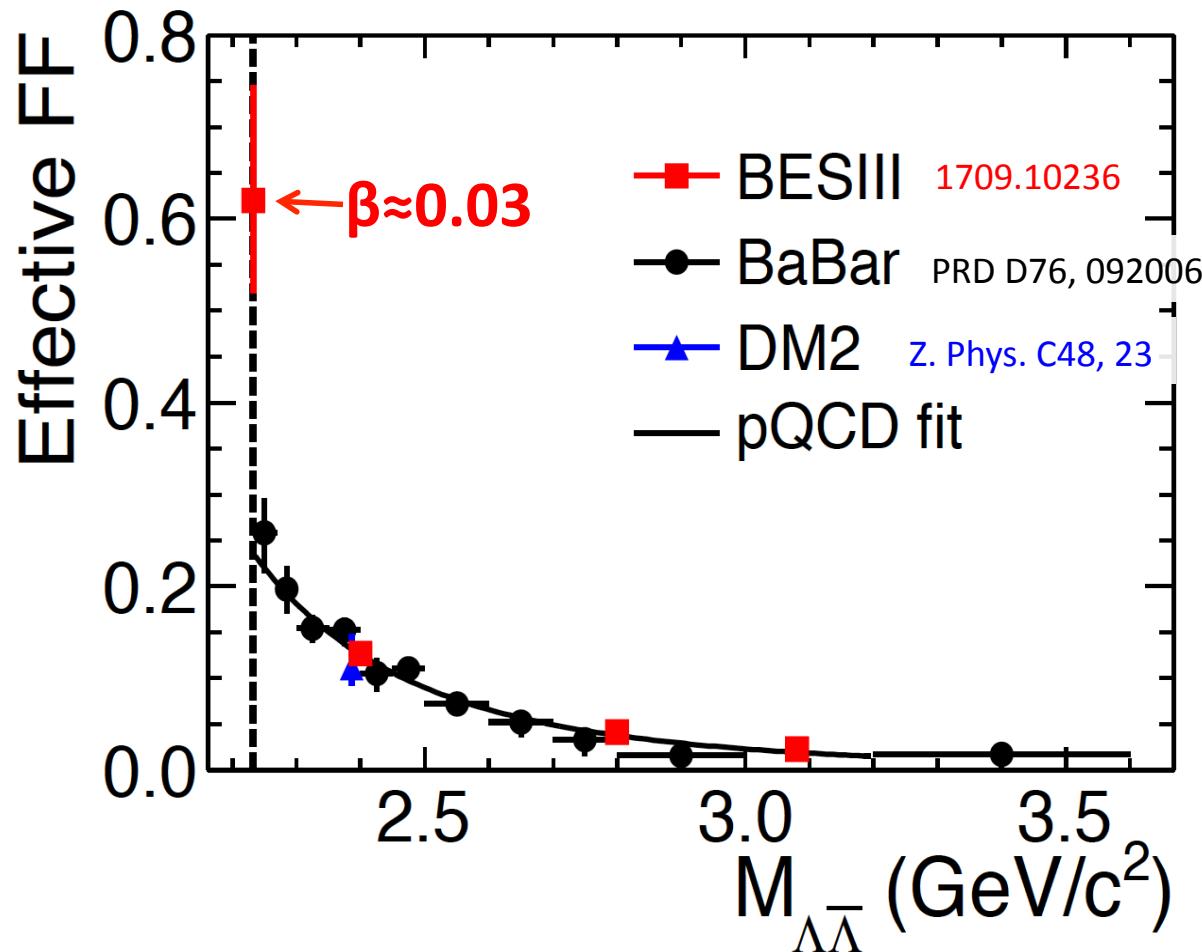
$$\sigma_{\Lambda\bar{\Lambda}}(m) = \frac{4\pi\alpha^2\beta}{3m^2} \left[ |G_M(m)|^2 + \frac{1}{2\tau} |G_E(m)|^2 \right] = \frac{4\pi\alpha^2\beta}{3m^2} |G_{eff}(m)|^2 (1 + 1/2\tau)$$



# Effective time-like form-factor of the $\Lambda$

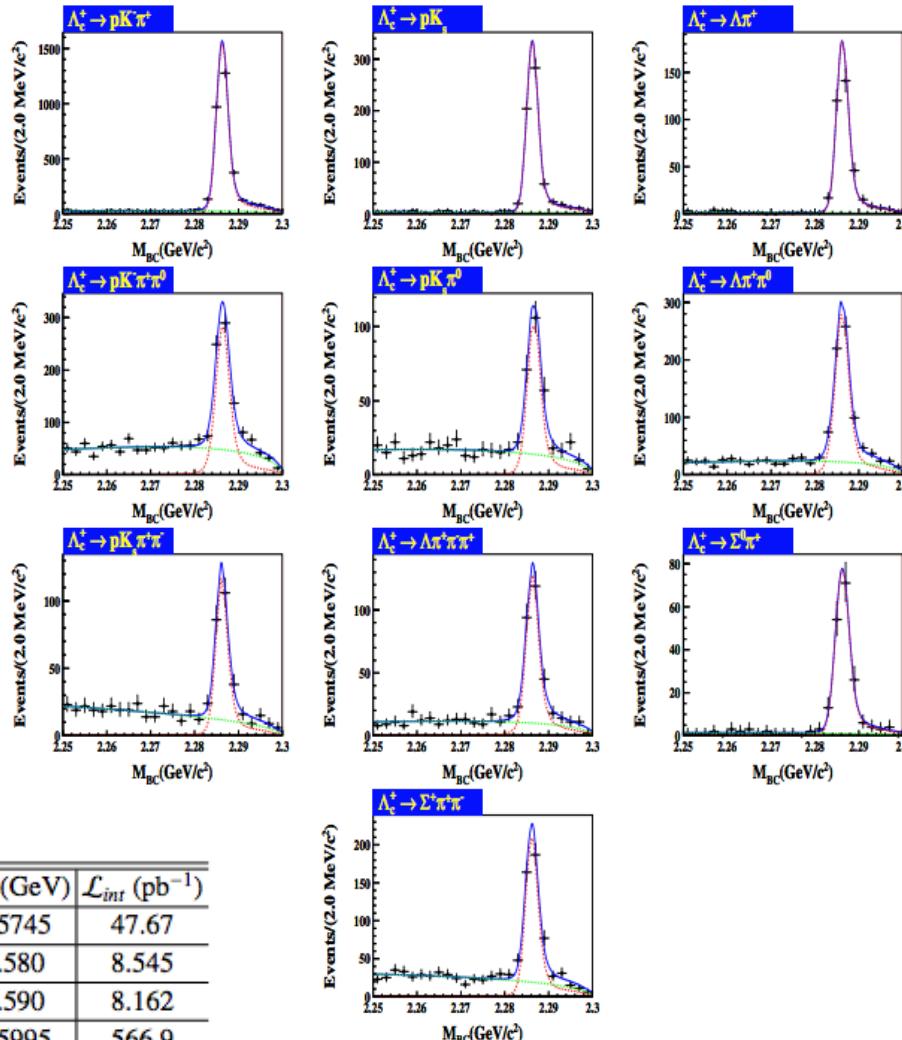
$$|G_{eff}(m_{\Lambda\bar{\Lambda}})| = \sqrt{\frac{3m_{\Lambda\bar{\Lambda}}^2 \sigma_{\Lambda\bar{\Lambda}}}{4\pi\alpha^2 \beta (1+1/2\tau)}}$$

diverging?



$$e^+ e^- \rightarrow \Lambda_c \bar{\Lambda}_c$$

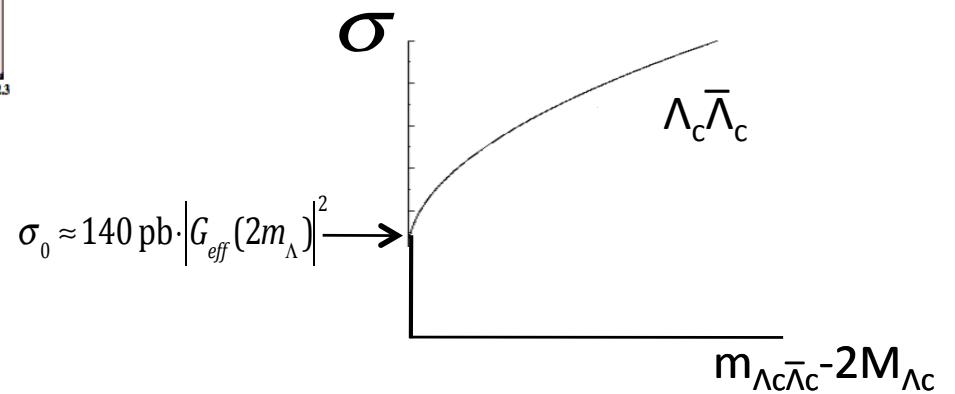
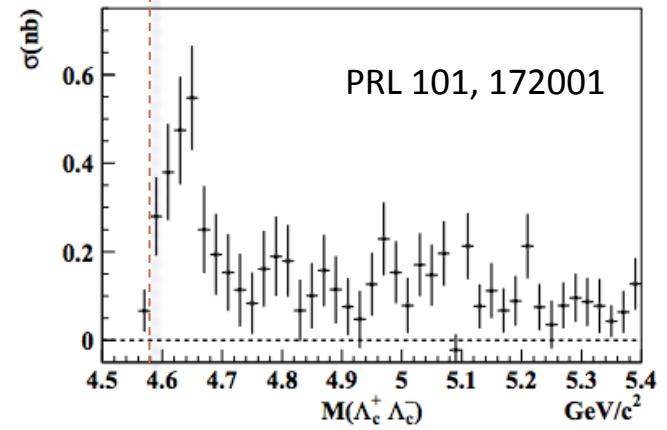
Detect one  $\Lambda_c$ ; use 10 different decay modes



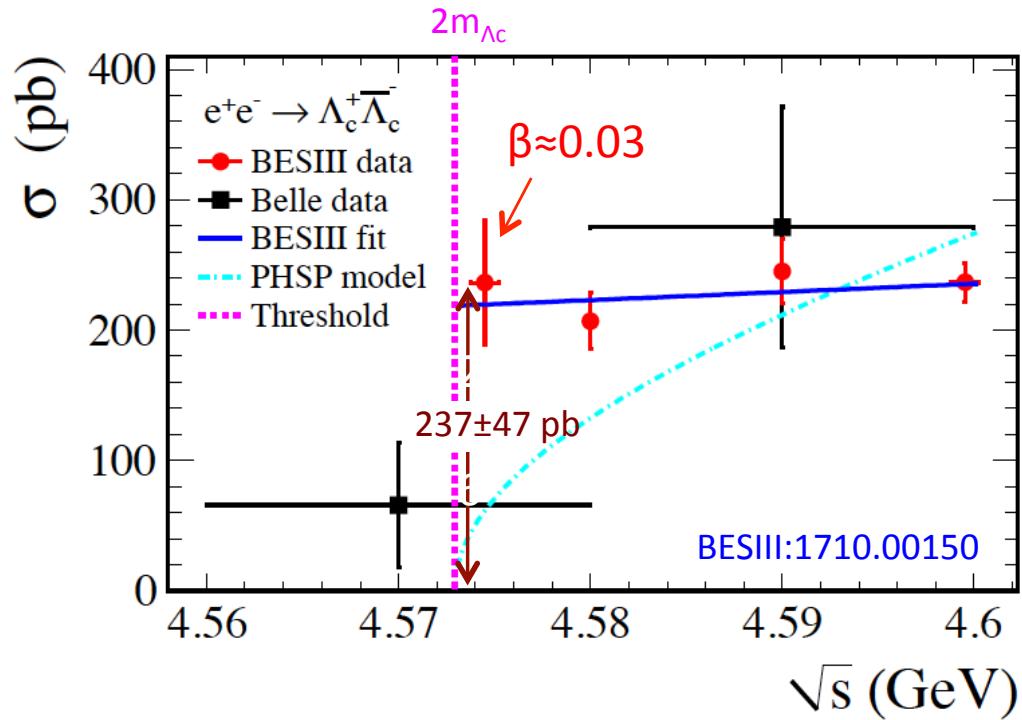
$\sqrt{s}$ (GeV)	$\mathcal{L}_{int}$ ( $\text{pb}^{-1}$ )
4.5745	47.67
4.580	8.545
4.590	8.162
4.5995	566.9

expectations:

$\sigma(e^+ e^- \rightarrow \Lambda_c \bar{\Lambda}_c)$  vis ISR from Belle

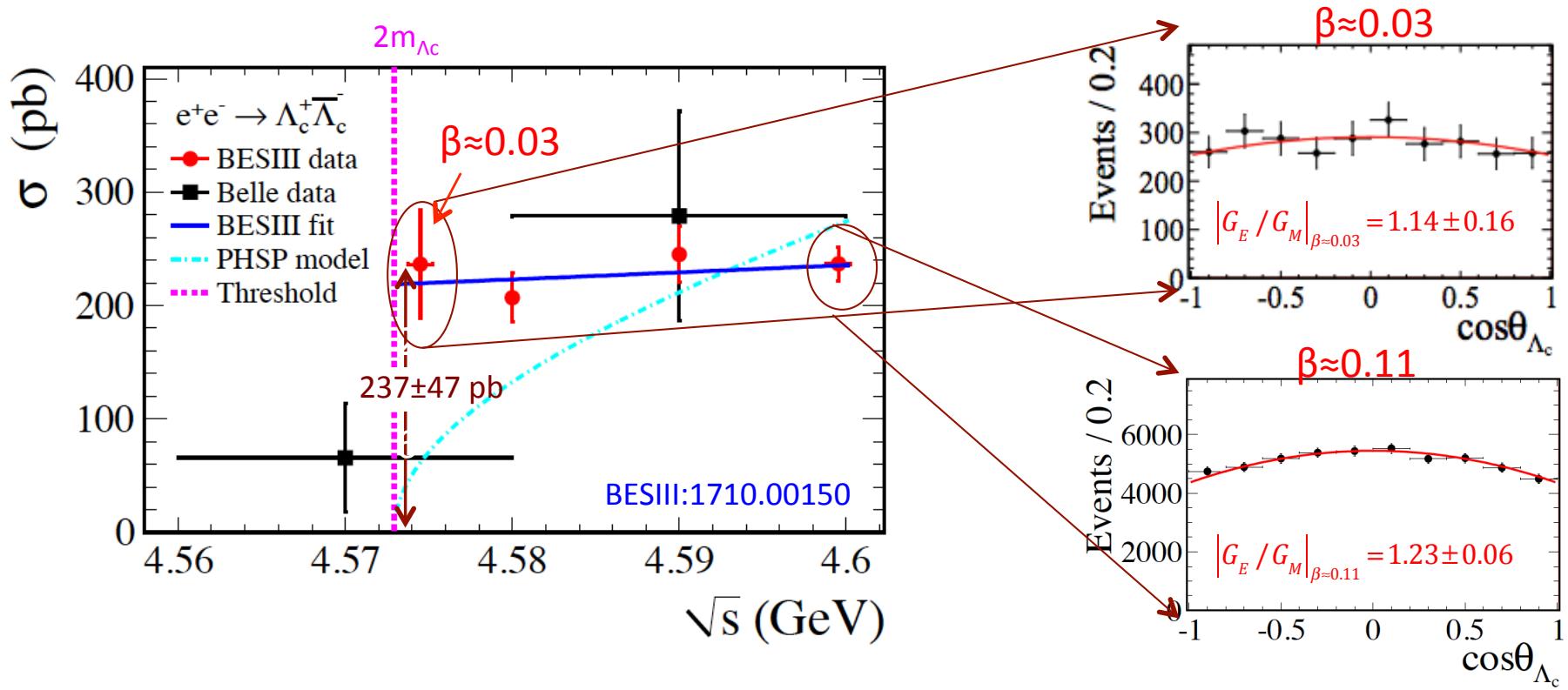


# $e^+e^- \rightarrow \Lambda_c^+\bar{\Lambda}_c^-$ results



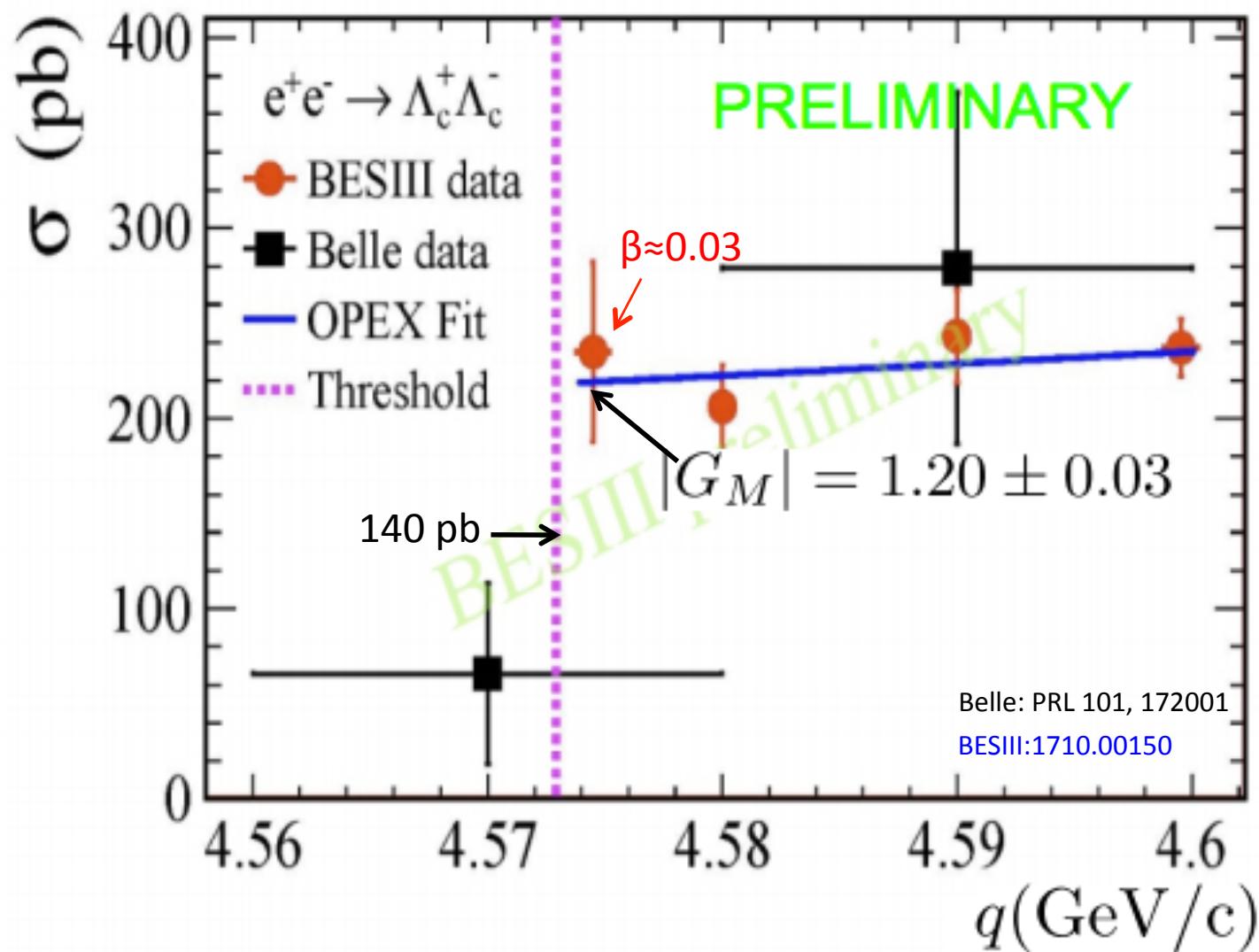
	$\sqrt{s}$ (MeV)	$\mathcal{L}_{\text{int}}$ ( $\text{pb}^{-1}$ )	$f_{\text{ISR}}$	$\sigma$ (pb)
$2m_{\Lambda_c} + 1.6 \text{ MeV}$	4574.5	47.67	0.45	$236 \pm 11 \pm 46$
	4580.0	8.545	0.66	$207 \pm 17 \pm 13$
	4590.0	8.162	0.71	$245 \pm 19 \pm 16$
	4599.5	566.9	0.74	$237 \pm 3 \pm 15$

# $e^+e^- \rightarrow \Lambda_c^+\bar{\Lambda}_c^-$ results



$\sqrt{s}$ (MeV)	$\mathcal{L}_{\text{int}}$ ( $\text{pb}^{-1}$ )	$f_{\text{ISR}}$	$\sigma$ (pb)
$2m_{\Lambda_c} + 1.6$ MeV			
4574.5	47.67	0.45	$236 \pm 11 \pm 46$
4580.0	8.545	0.66	$207 \pm 17 \pm 13$
4590.0	8.162	0.71	$245 \pm 19 \pm 16$
4599.5	566.9	0.74	$237 \pm 3 \pm 15$

# $|G_M(2m_{\Lambda_c})| > 1!$

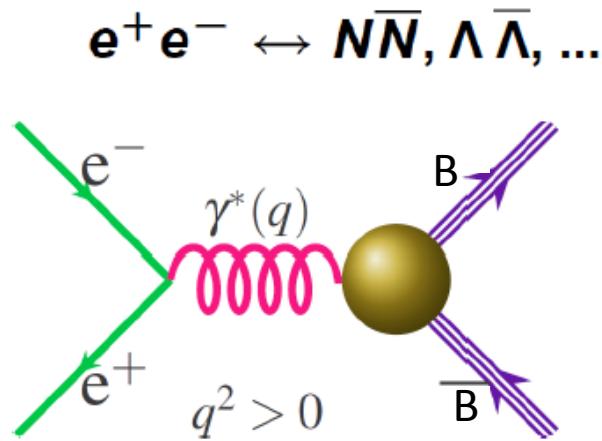


question to theorists:

Is the Coulomb factor reliable?

question to theorists:

# Is the Coulomb factor reliable?



$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2 \beta C}{4m_{B\bar{B}}^2} \left[ (1 + \cos^2 \theta) |G_M(m_{B\bar{B}})|^2 + \frac{1}{\tau} \sin^2 \theta |G_E(m_{B\bar{B}})|^2 \right]$$

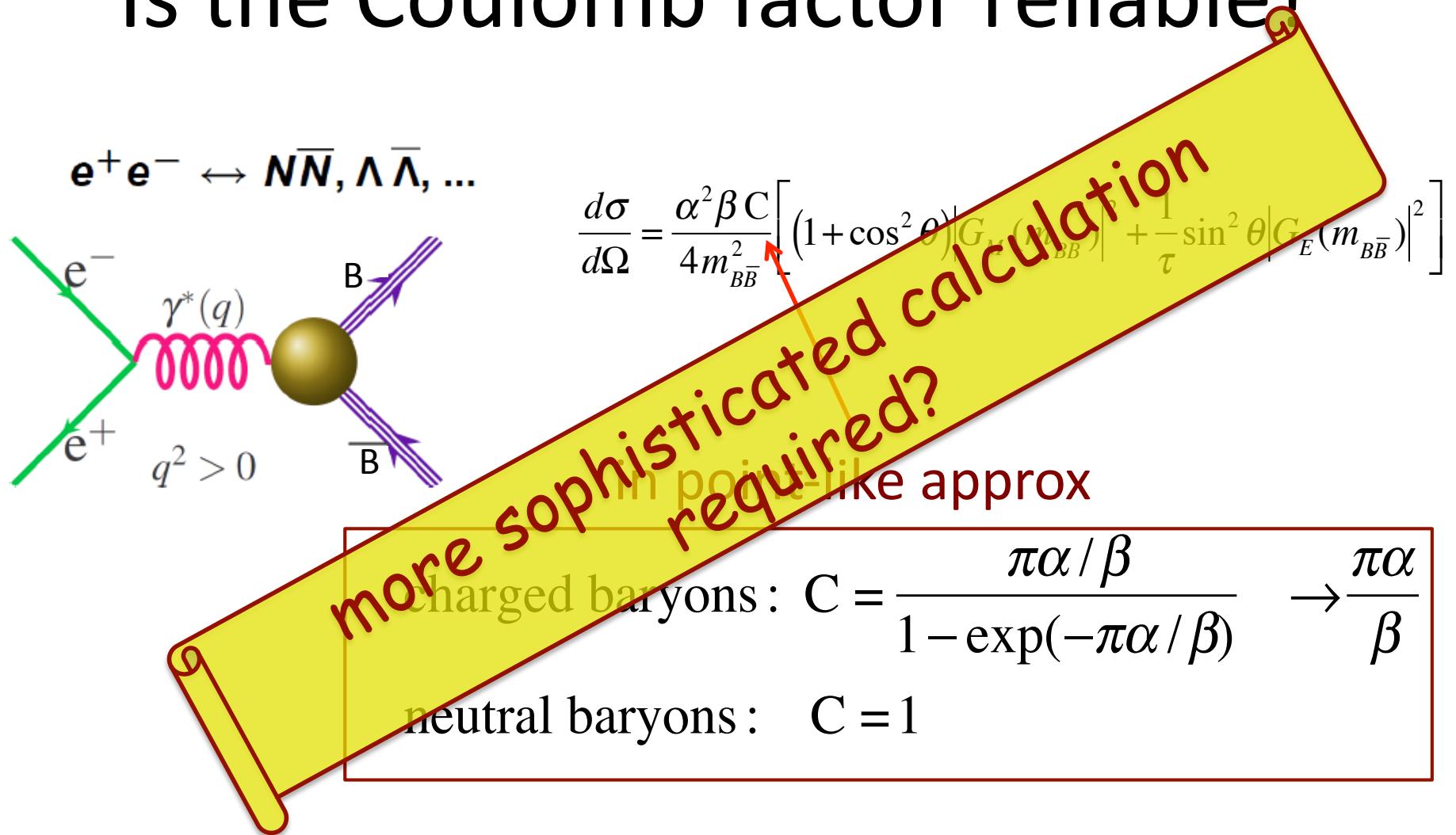
in point-like approx

charged baryons :  $C = \frac{\pi\alpha/\beta}{1 - \exp(-\pi\alpha/\beta)} \rightarrow \frac{\pi\alpha}{\beta}$

neutral baryons :  $C = 1$

question to theorists:

# Is the Coulomb factor reliable?



# B $\bar{B}$ threshold measurement prospects

BESIII data “in the can”

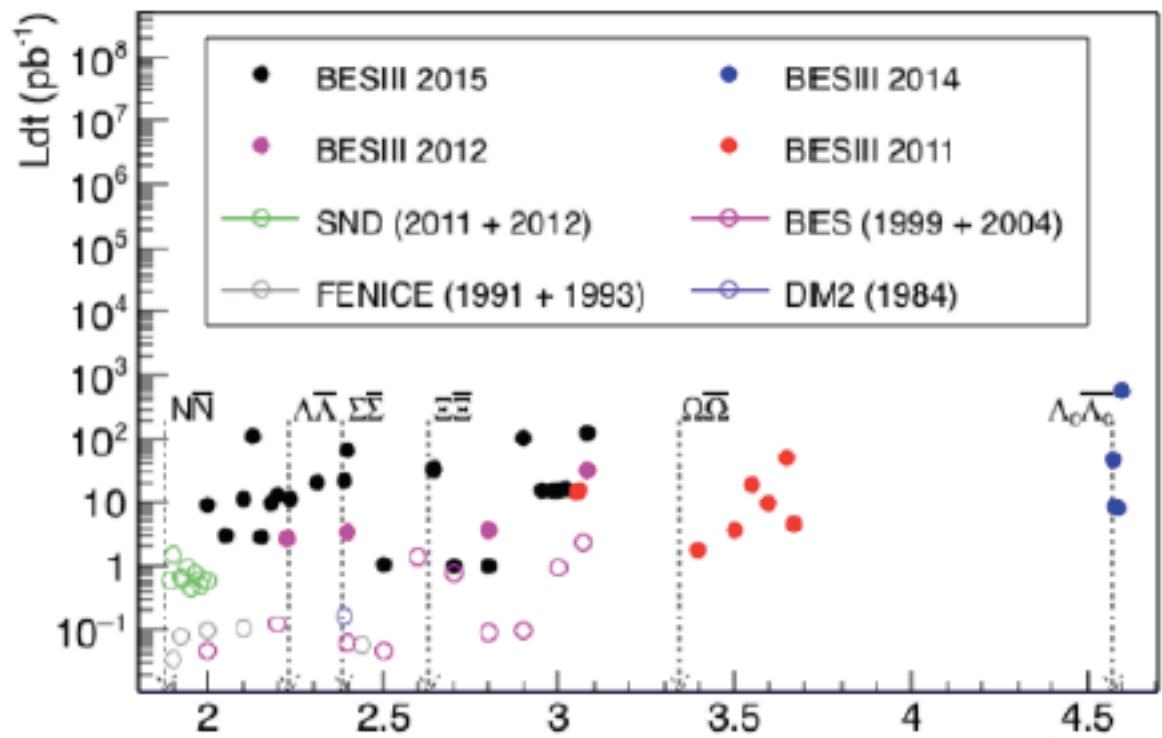
- & under analysis -

Scan data 2015 between 2 and 3.08 GeV (552 pb $^{-1}$ )

$e^+e^- \rightarrow \Lambda\bar{\Sigma}^0, \bar{\Sigma}^0\Sigma^0$  measured  
by BaBar: no extraction of R



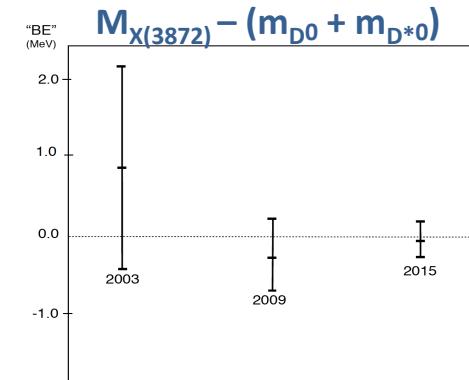
$e^+e^- \rightarrow \Lambda\bar{\Sigma}^0, \bar{\Sigma}^0\Sigma^0, \bar{\Sigma}^-\Sigma^+, \bar{\Sigma}^+\Sigma^-,$   
 $\Xi^0\Xi^0, \Xi^+\Xi^-, \Omega^+\Omega^-$



# Comments

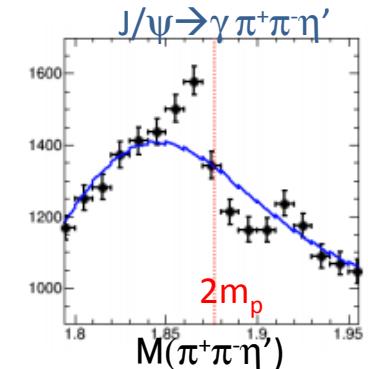
## ◆ $M(X(3872))$ is right at the $D^0\bar{D}^{*0}$ threshold

- ◆ the better it is measured, the closer it gets
- ◆ coincidence or physics?
- ◆ motivates studies of other S-wave thresholds



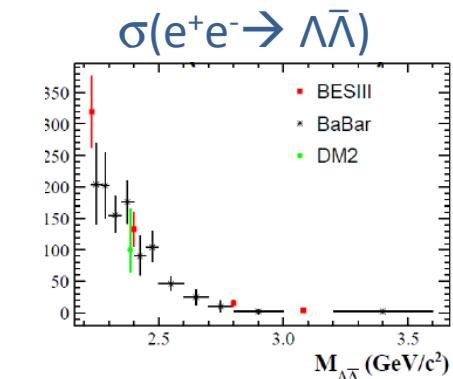
## ◆ a $0^{-+}$ $p\bar{p}$ bound state?

- ◆ seen in  $J/\psi \rightarrow \gamma p\bar{p}$  &  $\pi^+\pi^-\eta'$
- ◆ needs simultaneous multi-channel analyses



## ◆ $1^{--}$ $n\bar{n}$ , $\Lambda\bar{\Lambda}$ & $\Lambda_c\bar{\Lambda}_c$ puzzles @ threshold

- ◆ need more data, closer to thresholds
- ◆ and other channels
- ◆ and theory (especially for Coulomb corrections)
- ◆  $|G_M|$  @ threshold: useful probes of long-distance QCD?



# Thresholds *are* interesting



# Thresholds are interesting



# Acknowledgement



Thanks to my colleague **Rinaldo Baldini** (INFN-Frascati), who taught me all I know about time-like form factors and got me & BESIII colleagues involved in the subject

Thank you

감사합니다

# Backup Slides

