

# Neutrino Flux Requirements for DUNE

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WG1: Neutrino Flux

October 16, 2017

# Outline

- LBNF beamline designs.
- Current flux uncertainties.
- Reducing the flux uncertainties

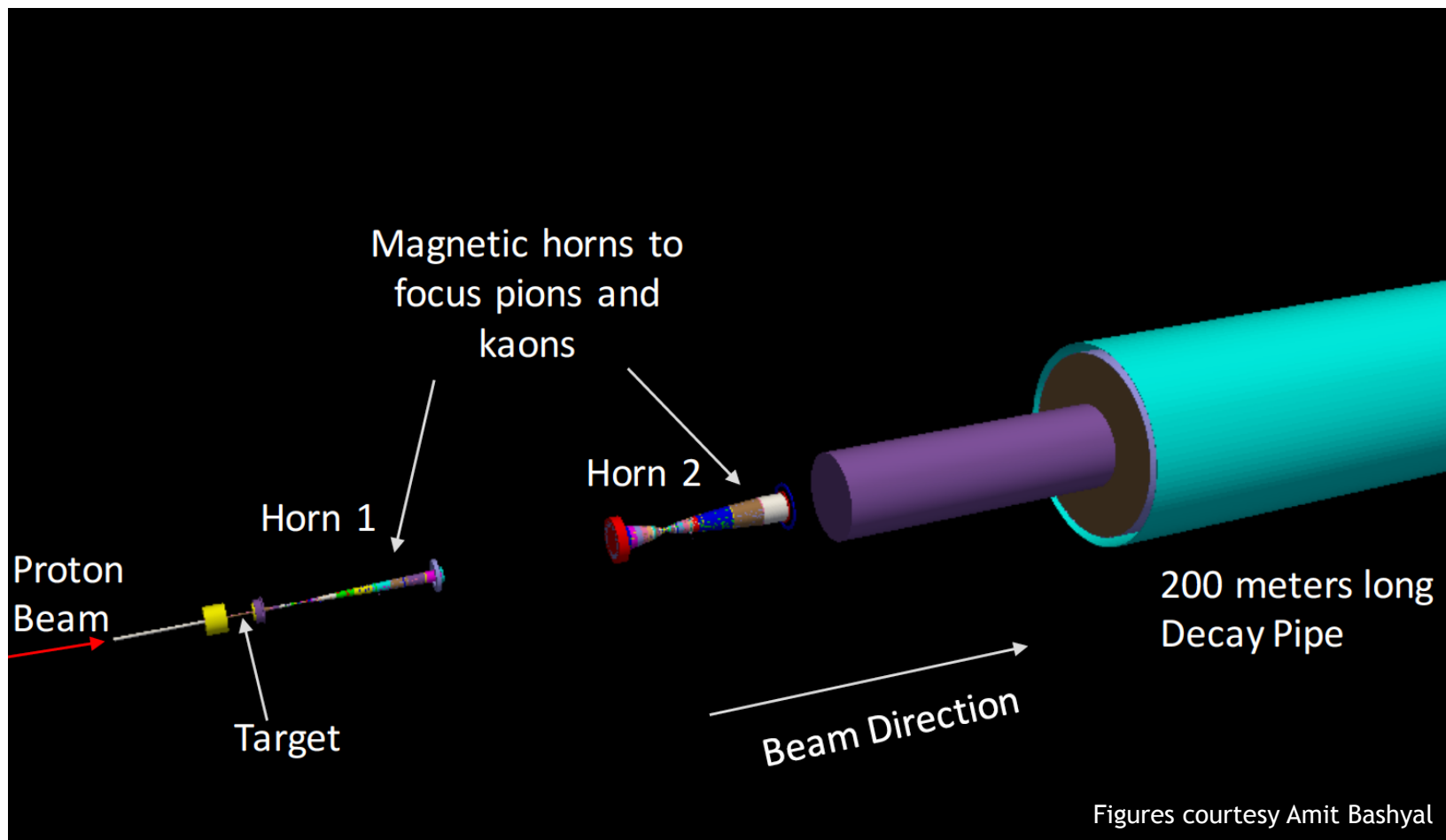
# LBNF Beamline Designs

# LBNF Beamline

- Primary proton beam in 60-120 GeV.
- Initial 1.2 MW beam power, upgradable to 2.4 MW.
- Wide-band beam on-axis with tunable energy spectrum.
- Decay pipe ~ 200 m long, He filled.
- Currently considering two different beamline designs:
  - Reference (NuMI-like).
  - Optimized (for CP violation).
- ***Decision regarding which one will go forward to preliminary design will be made soon.***

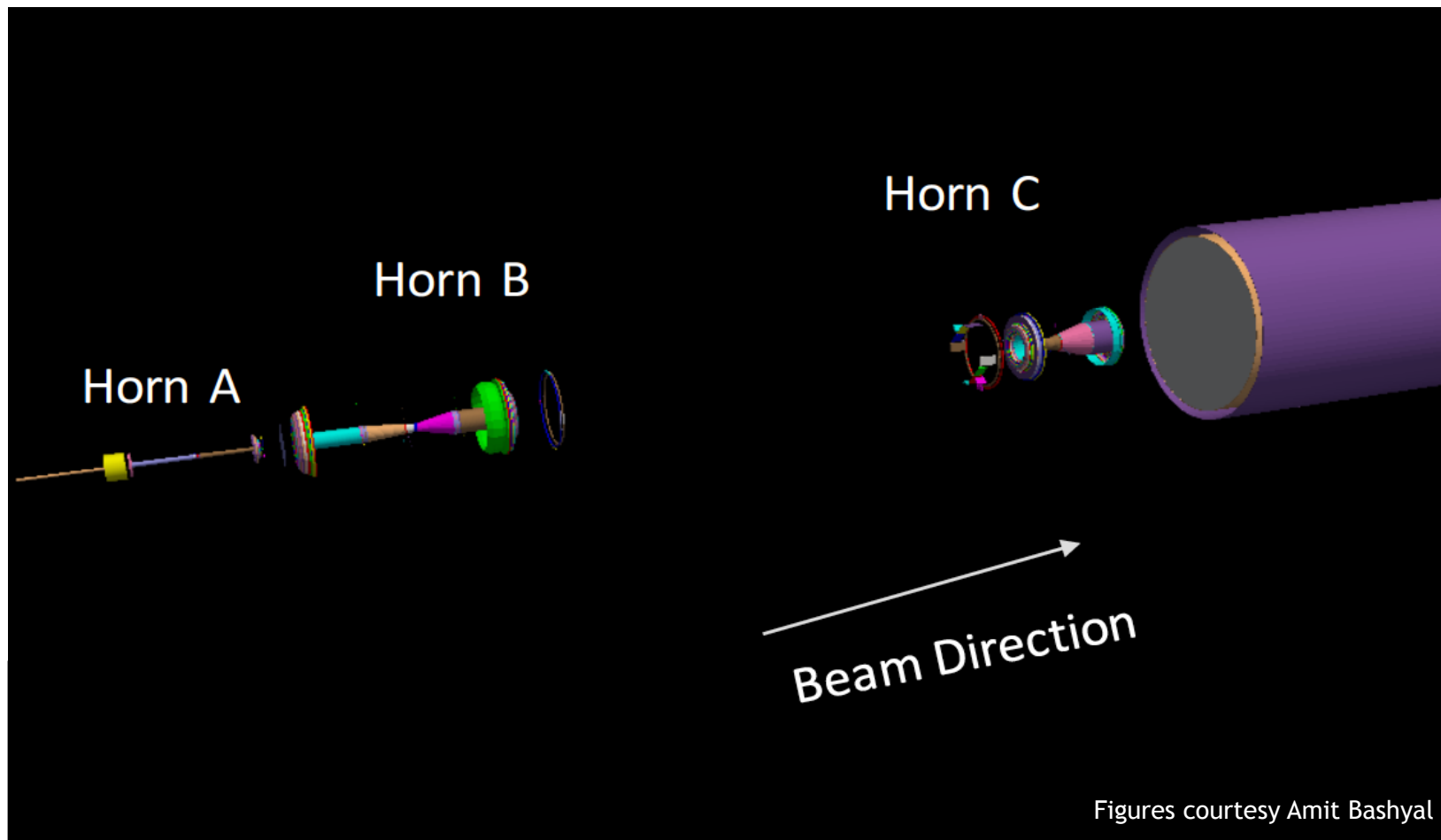
# LBNF Reference Beamline

- Two horns, nearly identical to those used in NuMI, run at slightly higher current (230 kA).
- 1 m long graphite fin target, similar to but not identical to NuMI target



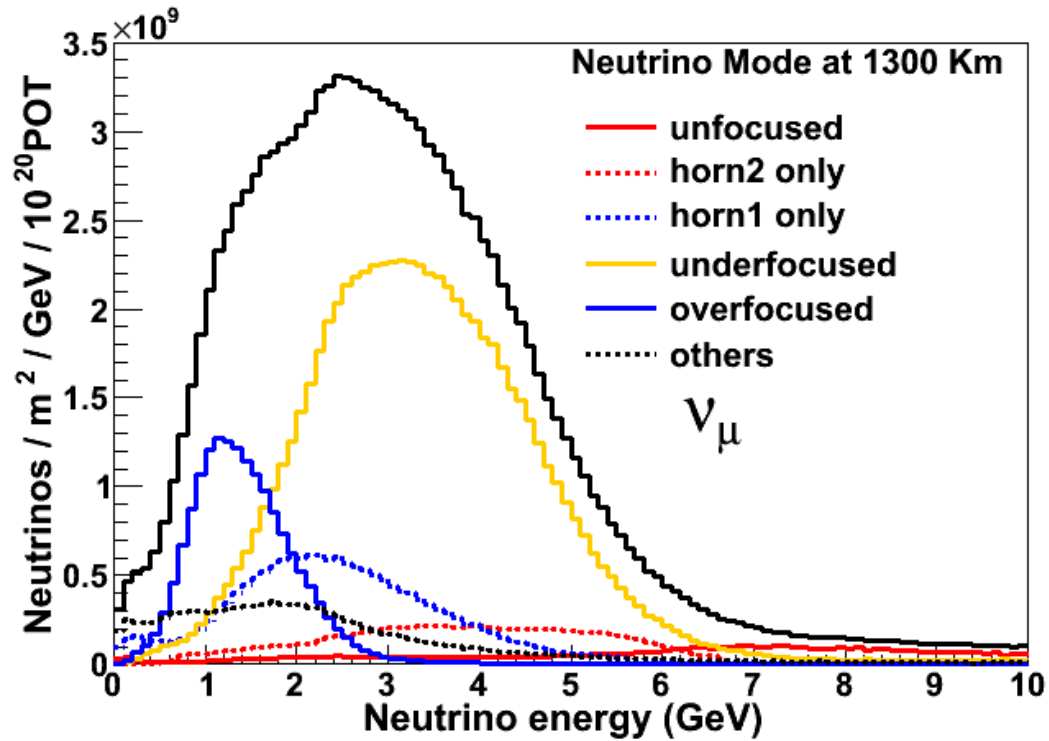
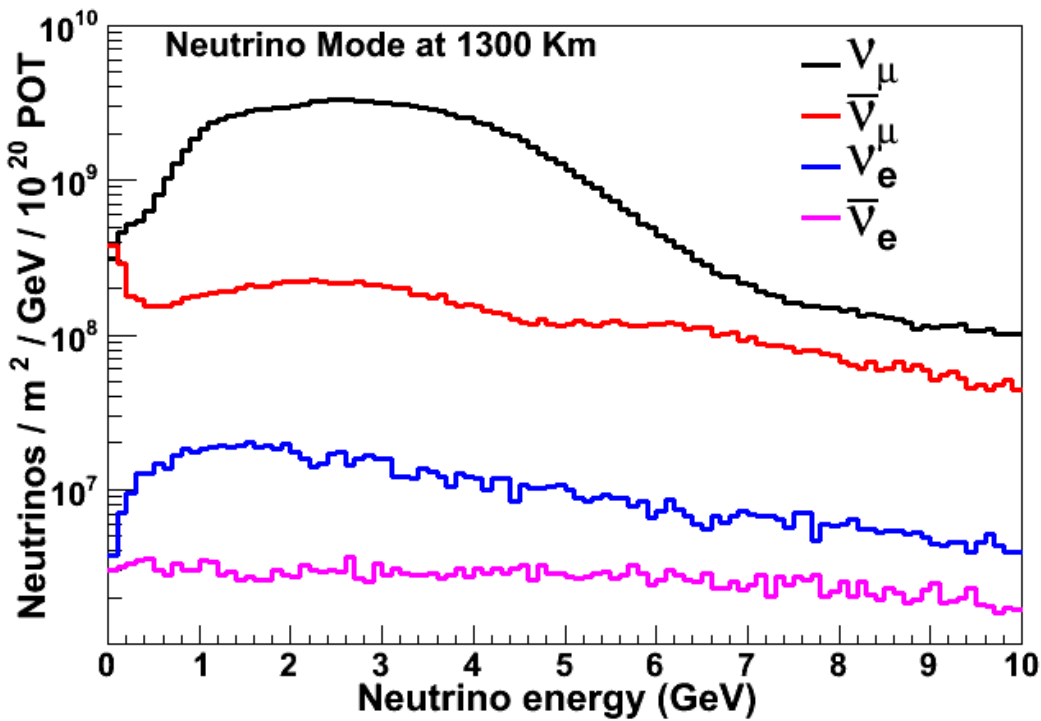
# LBNF Optimized Beamline

- Three horns, not similar to NuMI, run at 300 kA
- 2 m long graphite fin target, but development of alternative graphite cylindrical target design is ongoing at RAL

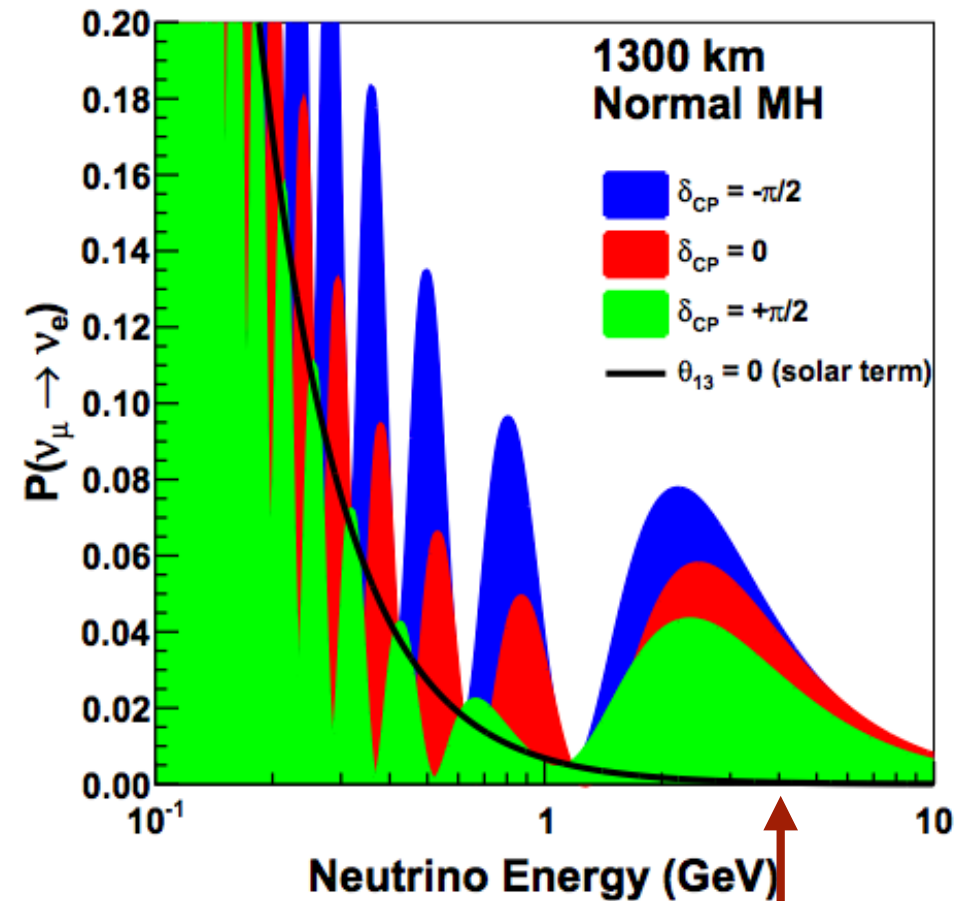
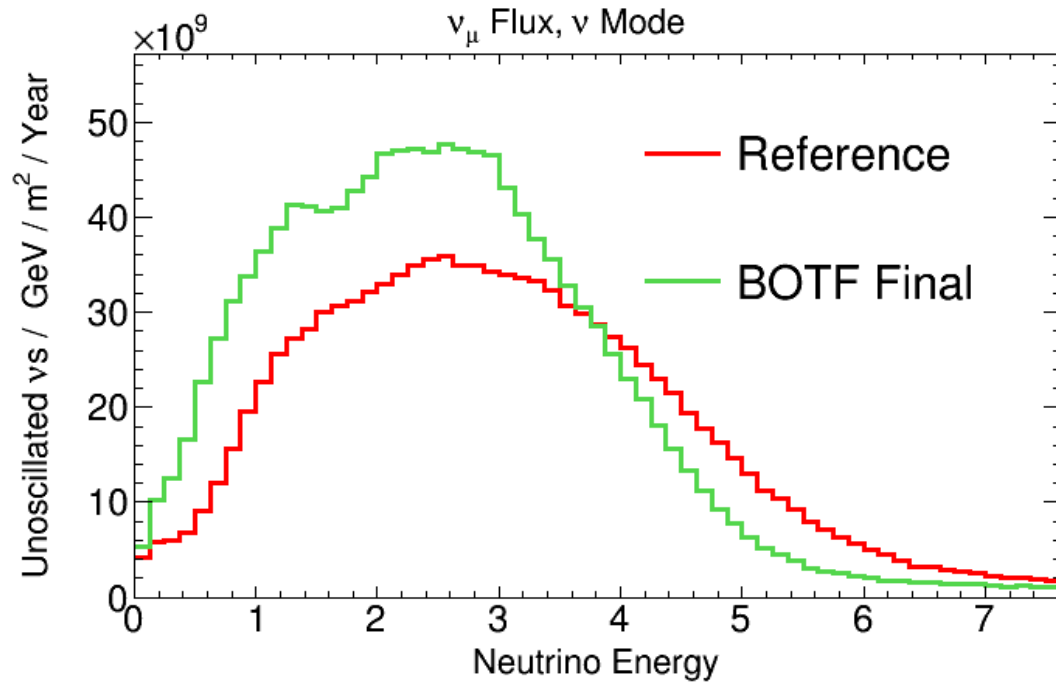


Figures courtesy Amit Bashyal

# LBNF Reference Beamline



# LBNF Beamline Options



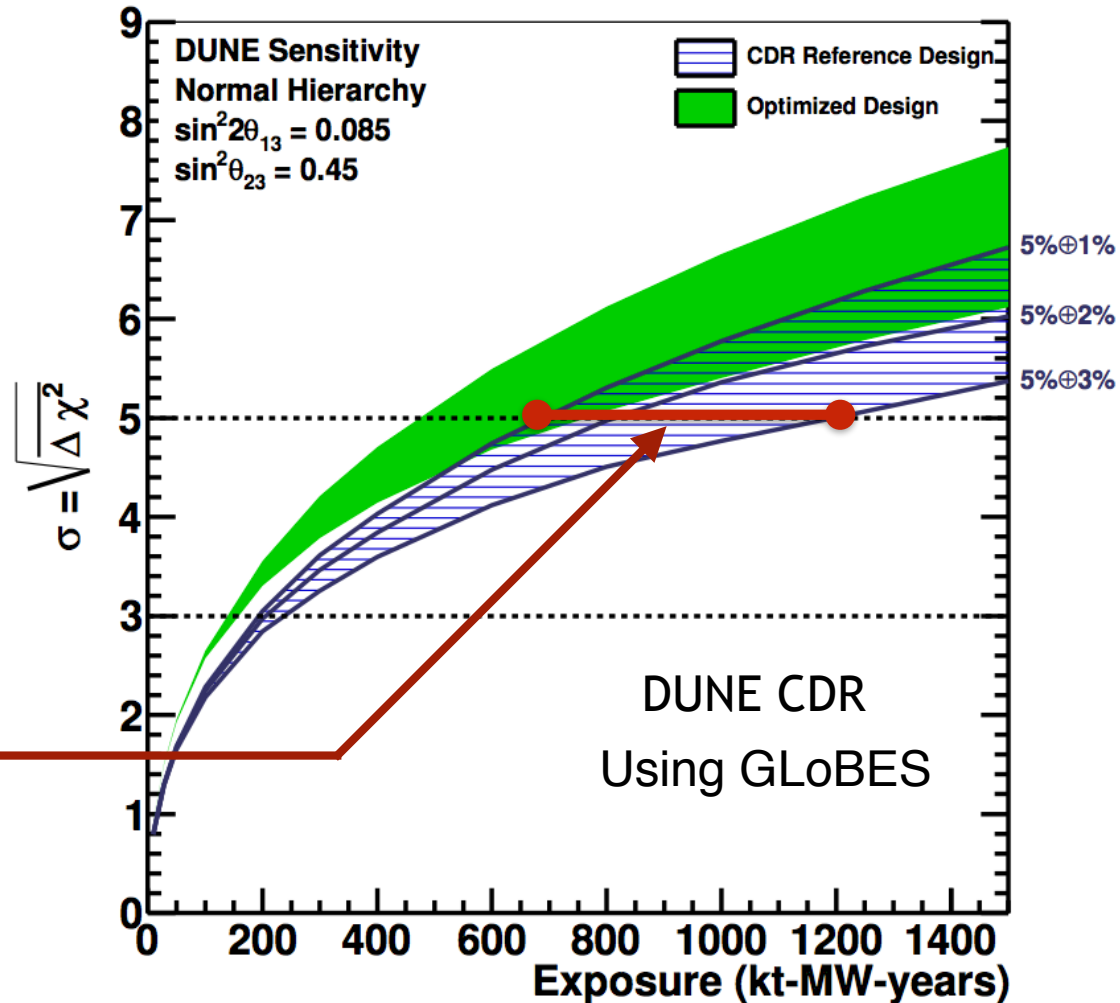


# LBNF/DUNE Long Baseline Physics

Assuming:

1. 5% uncertainties on the normalizations of the  $\nu_e$  appearance correlated with the  $\nu_\mu$  disappearance.
  2. Additional uncertainties of 1%, 2% or 3% that are uncorrelated with the  $\nu_\mu$  spectrum
- Going from 3% vs 1% uncertainty is equivalent to nearly doubling exposure time.

## 50% CP Violation Sensitivity

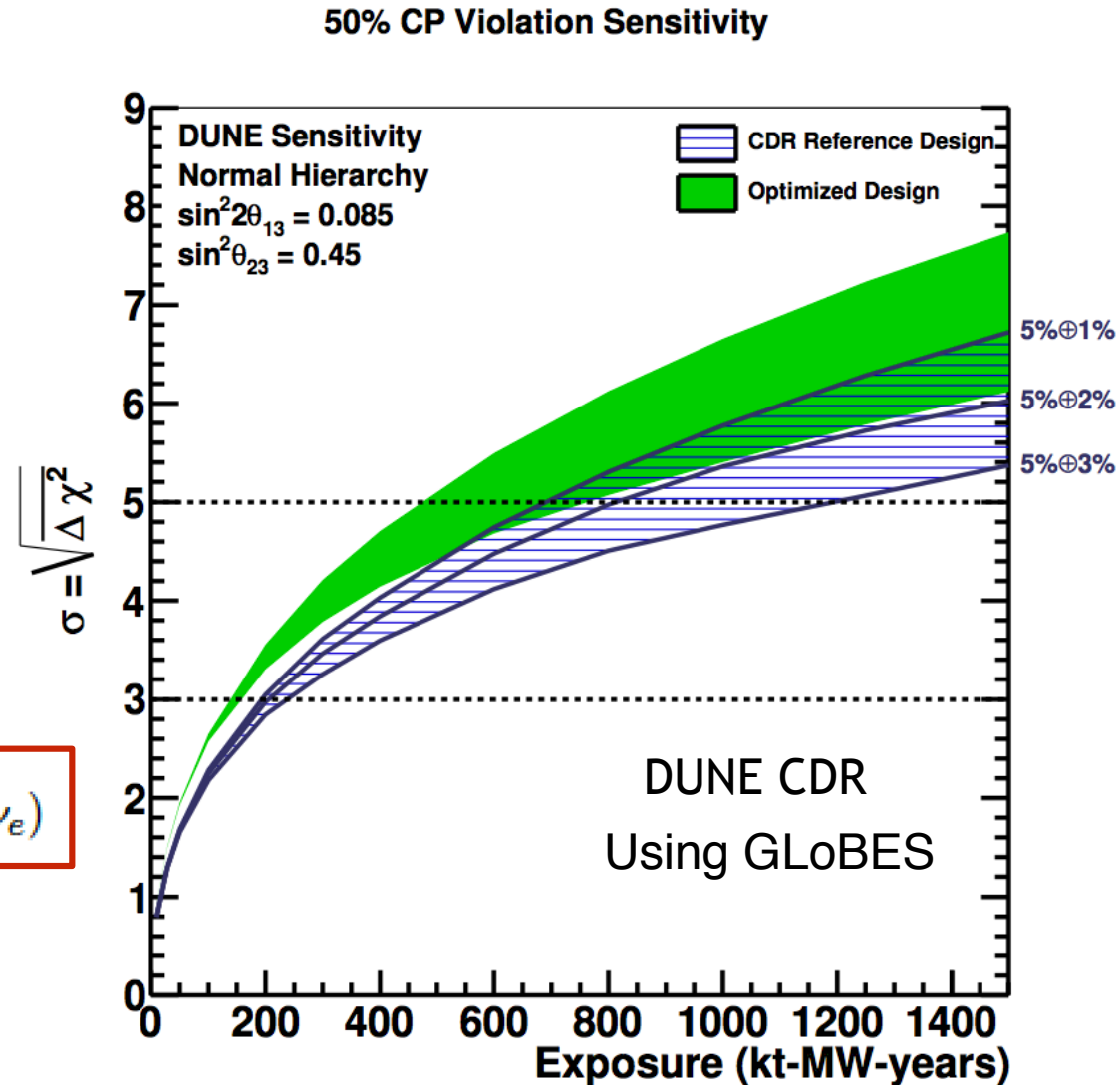


# LBNF/DUNE Long Baseline Physics

Flux uncertainties enter:

1. **Directly** (after constraint by the near detector) the uncertainty 1, that is correlated between  $\nu_e$  and  $\nu_\mu$ ,
2. **Indirectly** to the uncertainty 2, since flux uncertainties couple to uncertainties in cross sections:

$$N_{\nu_e}(E_\nu) = \phi_{\nu_\mu} \times \sigma(\nu_e) \times \epsilon(\nu_e) \times P(\nu_\mu \rightarrow \nu_e)$$

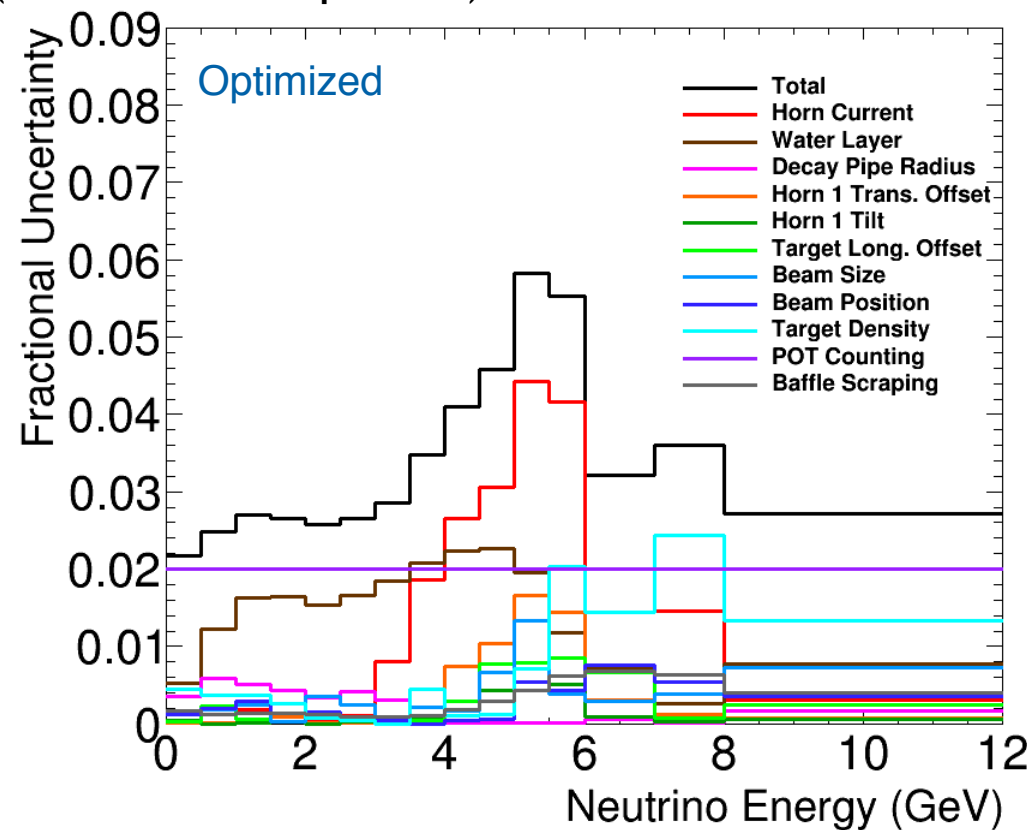
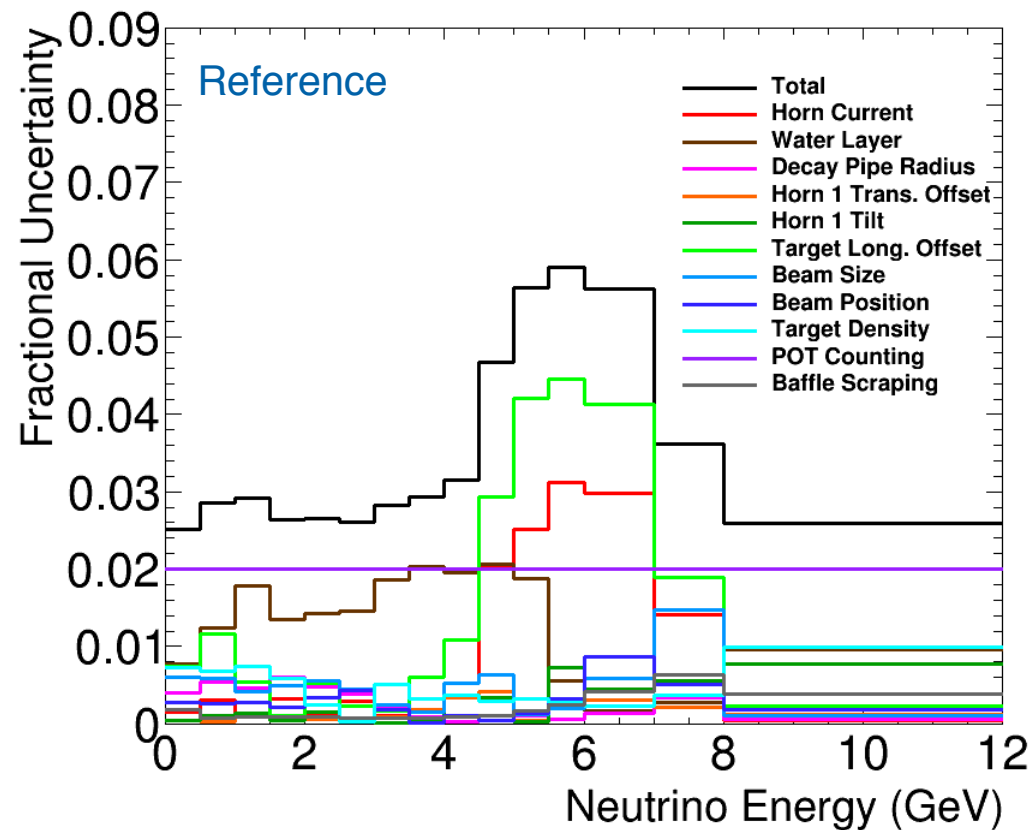


Final uncertainties should include the flux shape uncertainty as well.

# Current Flux Uncertainties

# Focusing Uncertainties

L. Fields ((NA61 Workshop 2017)



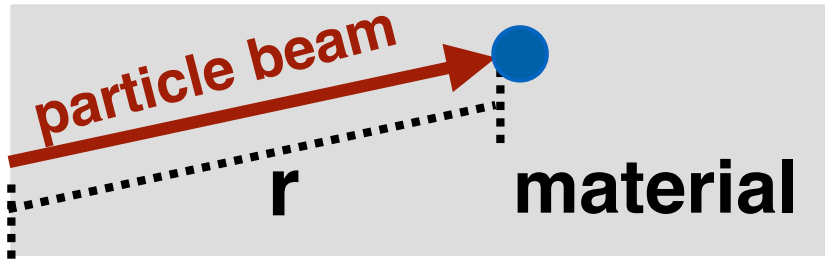
- **POT counting** and **water layer** are the most significant at the peak.
- **Horn current** and **target longitudinal offset** are the most significant at the falling edge for the reference design.

## HP Uncertainties

- DUNE uses PPFX (Package to Predict the Flux) developed by MINERvA that uses all relevant HP data (currently it corrects FTFP\_BERT G4 model).
- DUNE uses QGSP hadronic model and then only the uncertainties can be calculated using PPFX.
- PPFX calculates two kind of uncertainties related to the corrections of the HP:
  - 1. *Beam attenuation.***
  - 2. *Hadron production.***

# 1. Beam Attenuation

When the particle interacts in a volume

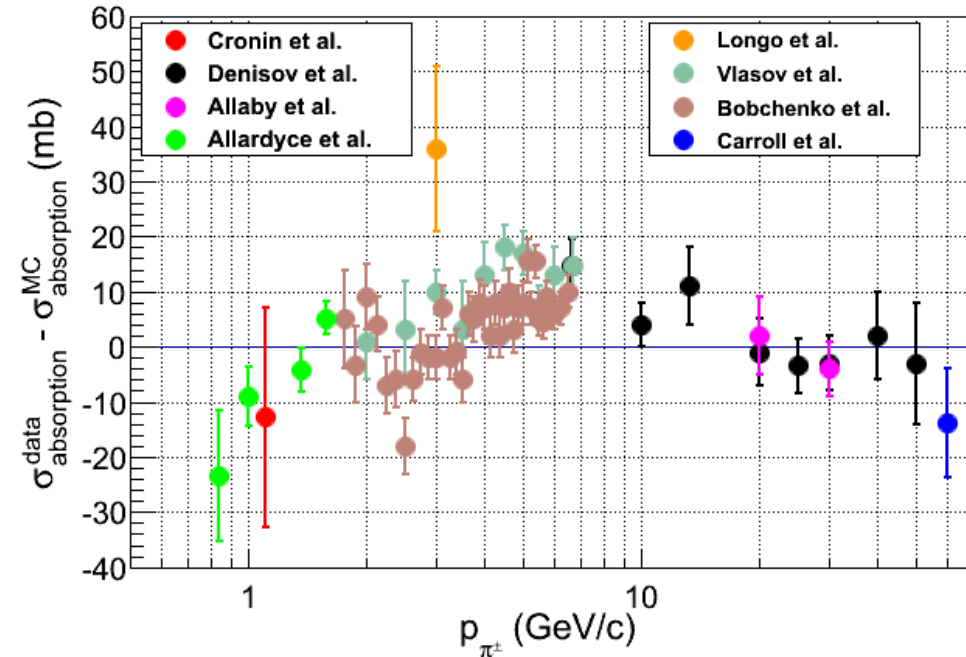


$$correction(r) = \frac{\sigma_{Data}}{\sigma_{MC}} e^{-r \frac{N_A \rho (\sigma_{Data} - \sigma_{MC})}{A}}$$

$N_A$ : Avogadro Number,  $\rho$ : density,  $A$ : mass number

When the particle passes through the volume without interacting the survival probability is calculated.

- Example: Absorption cross section of pion on Aluminum



**Reference (Geant4):**

$$\sigma_{absorption} = 344 \text{ mbar}$$

- Most of the cross-section discrepancies are less than 6%.

## 2. Hadron Production

For thin target data (NA49 for instance):

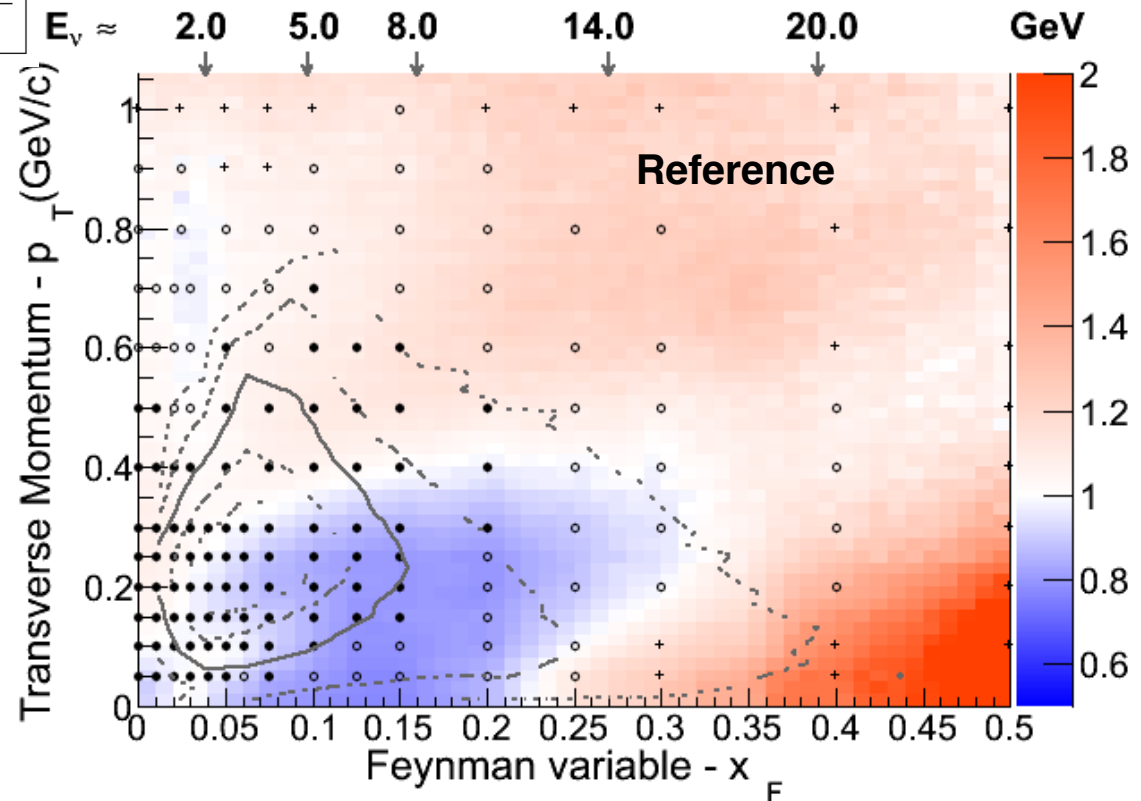
$pC \rightarrow \pi^+ X$

$$\text{correction}(x_F, p_T, E) = \frac{f_{\text{Data}}(x_F, p_T, E = 158 \text{ GeV}) \times \text{scale}(x_F, p_T, E)}{f_{\text{MC}}(x_F, p_T, E)}$$

( $f = Ed^3\sigma/dp^3$ : invariant production cross section)

- The **scale** allows us to use NA49 for proton on carbon in 12-120 GeV (calculated with FLUKA).
- It was checked by comparing with NA61 at 31 GeV (negligible difference).

Contours: 2.5, 10, 25, 50 and 75 % of the  $\pi$  yields.

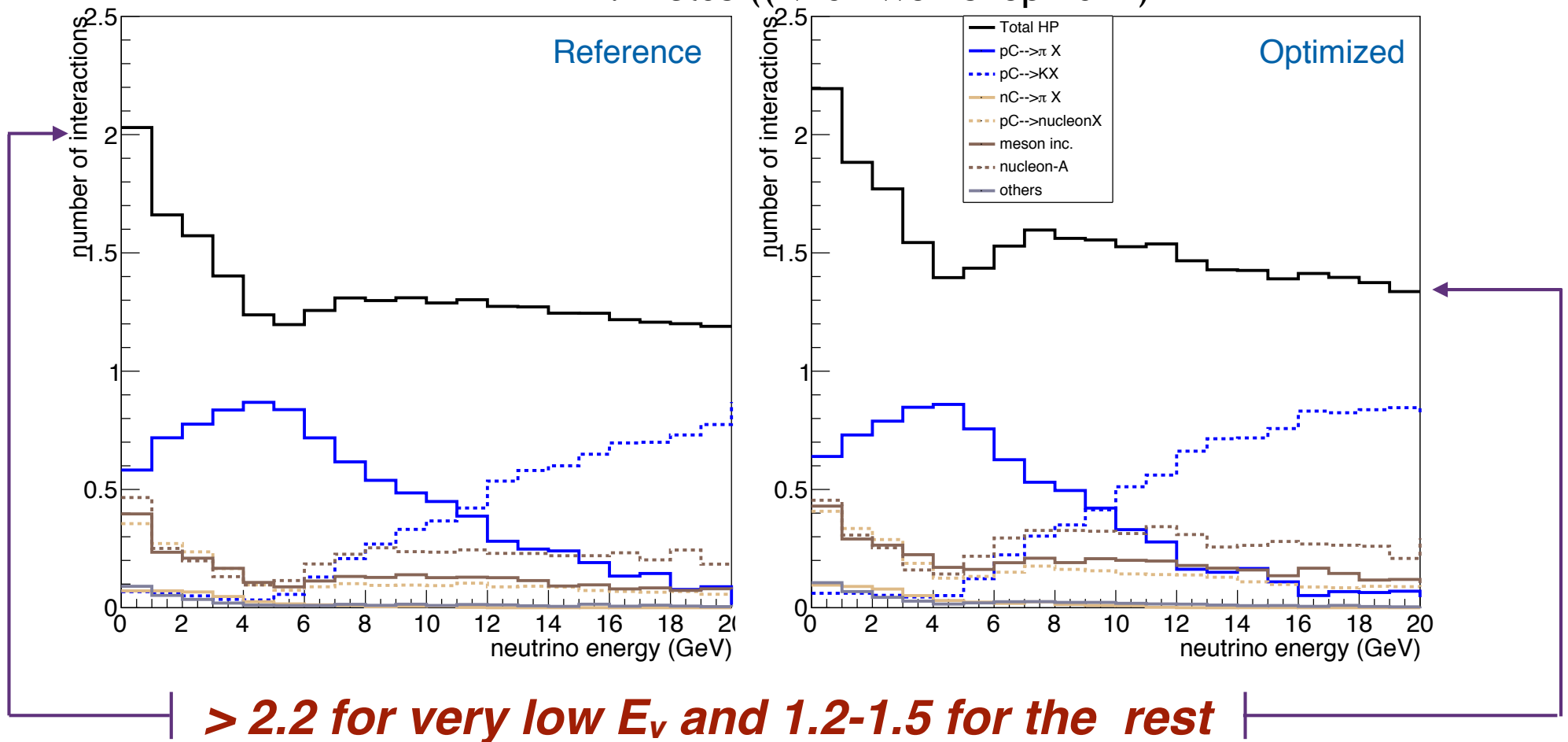


$$x_F = \frac{2p_L^*}{\sqrt{s}} \quad \text{Systematic uncertainties} = 3.8\% \text{ (added in quadrature).}$$

# Hadron Production Needs

- $\pi$ ,  $K$  and **nucleons** productions from  $pC$  based on data (mainly NA49).
- **nucleon-A**: quasi-elastics, extension from carbon to other materials, etc.
- No data applied to meson incidents: assuming large uncertainties.

L. Fields ((NA61 Workshop 2017)

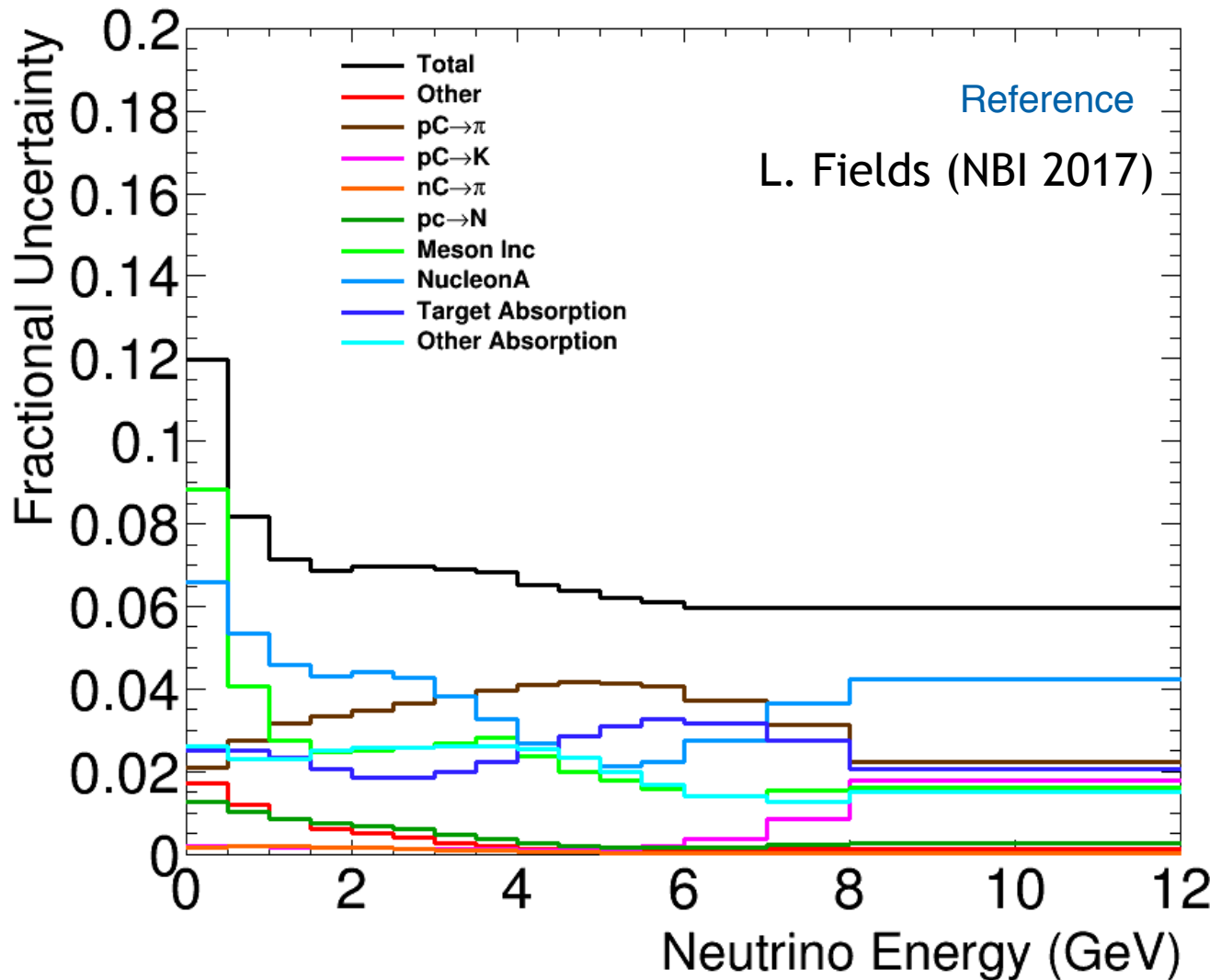


> 2.2 for very low  $E_\nu$  and 1.2-1.5 for the rest



# Hadron Production Uncertainties

- Same procedure as MINERvA applied to DUNE beam simulation
- Total HP uncertainty  $\sim 7\%$  in the peak and 12% for very low energies.



# Hadron Production Uncertainties

Particle production in proton carbon interactions:

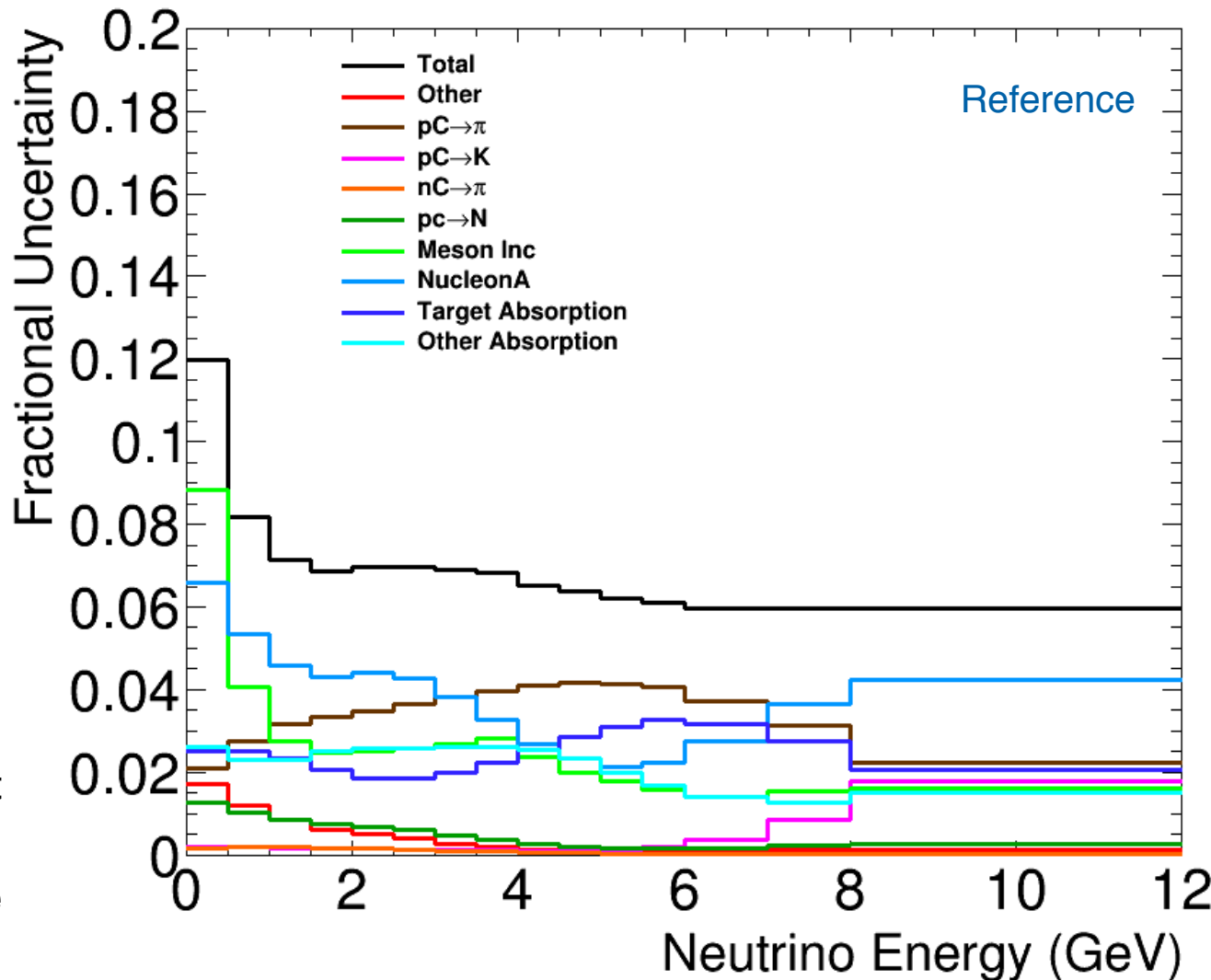
- **Pions** ( $pC \rightarrow \pi$ )
- **Kaons** ( $pC \rightarrow K$ )
- **Nucleons** ( $pC \rightarrow N$ )

All covered by external data (mainly NA49).

(for high energy kaons, a combination of NA49 + MIPP  $k/\pi$  )

The magnitude of this uncertainty depends both on uncertainties reported by experiments.

The correlations of the datasets are not reported by experiments. We assumed 100% for the systematics (conservative approach from MINERvA).



# Hadron Production Uncertainties

Extending the data coverage:

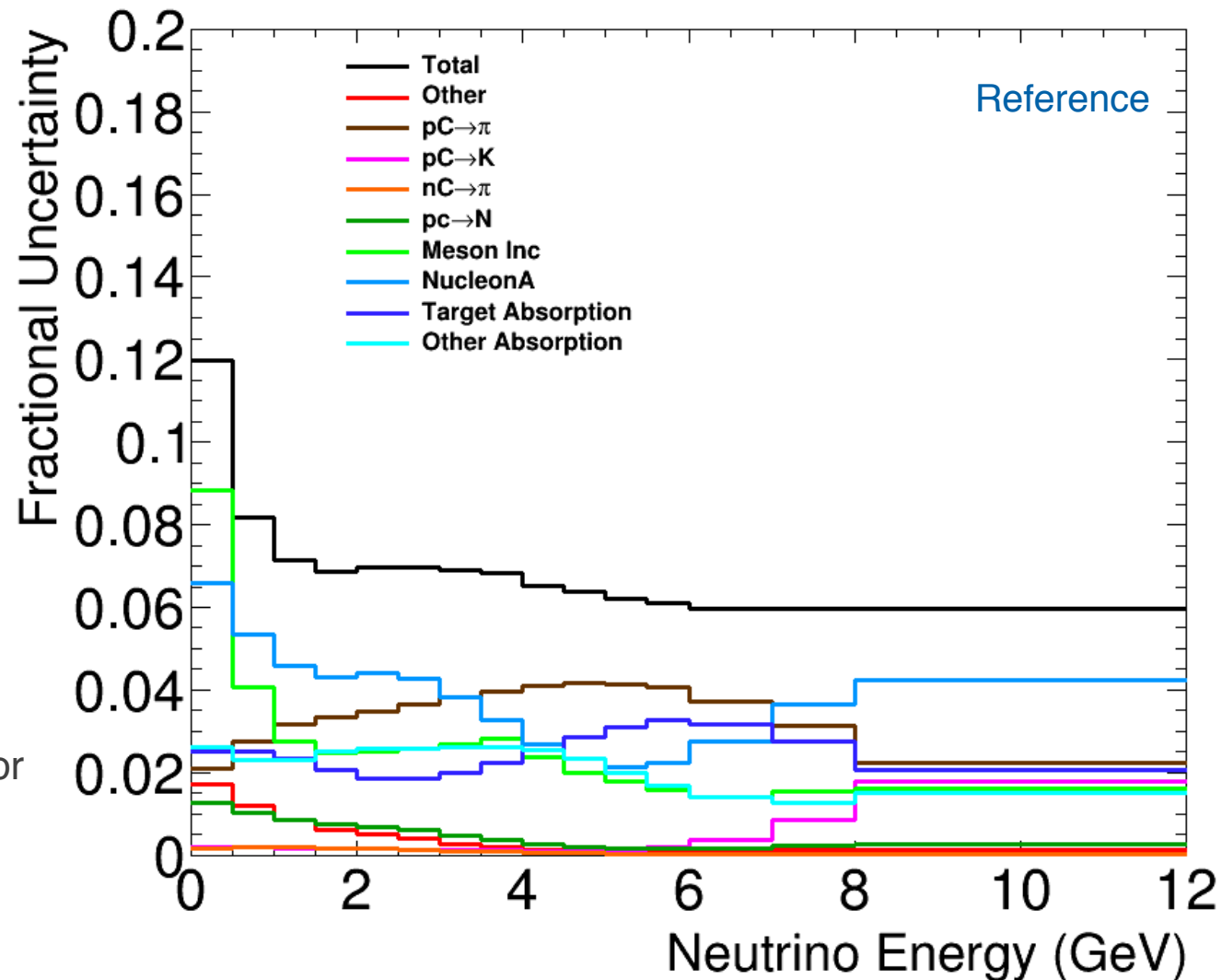
- **Nucleon interactions (NucleonA)**

Constrain these interactions with pC adding an additional uncertainty found by comparing A dependence of Barton, Skubic and Eichten.

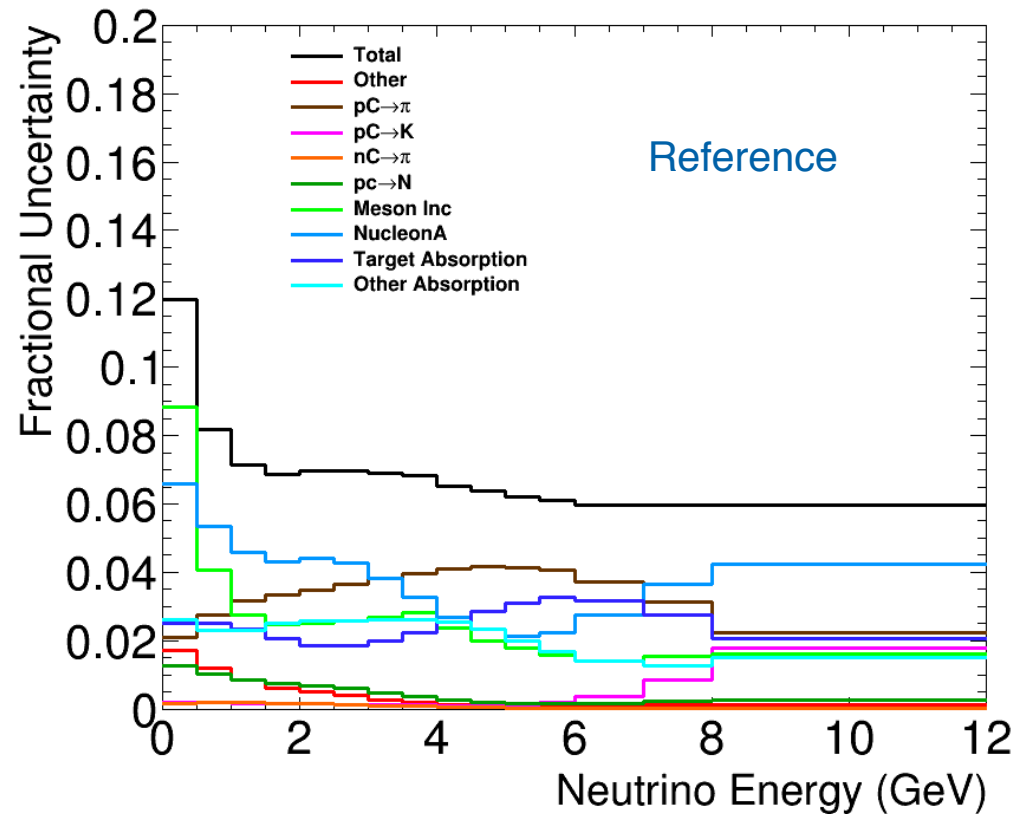
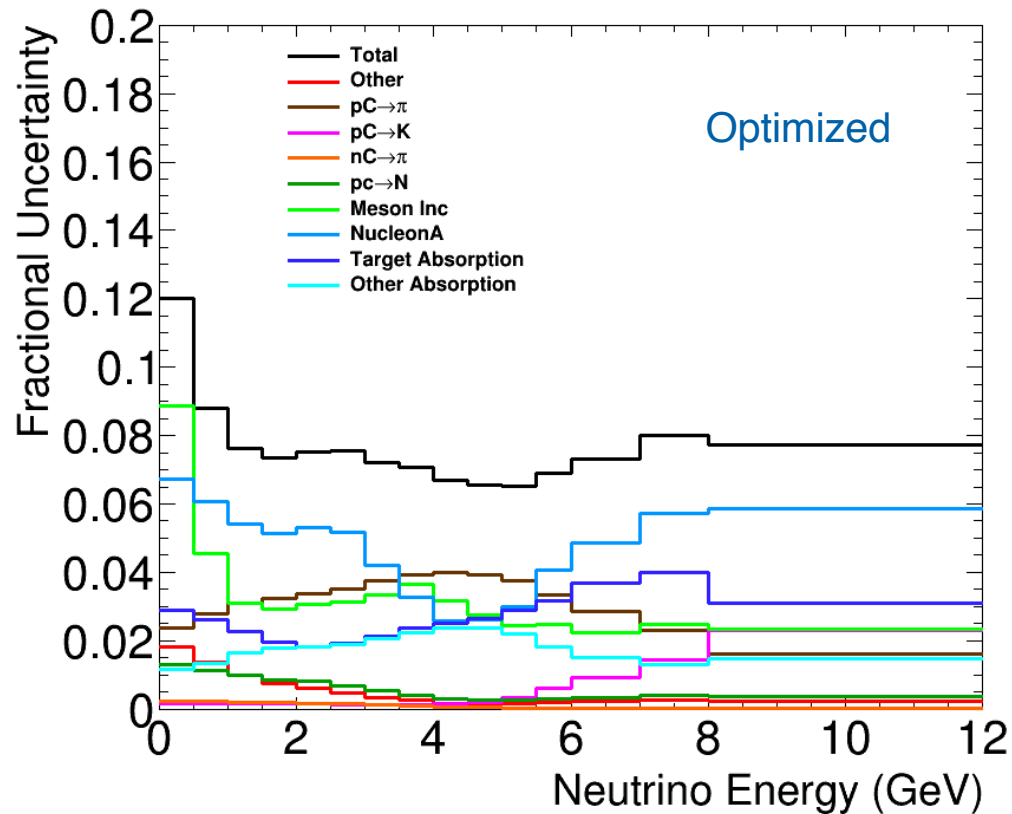
When there is not data coverage, like:

- **Incident Mesons (Meson Inc)**

Guided by the agreement with other datasets: processes categorized by meson and produced particle. 40% error assigned in 4  $x_F$  bins.



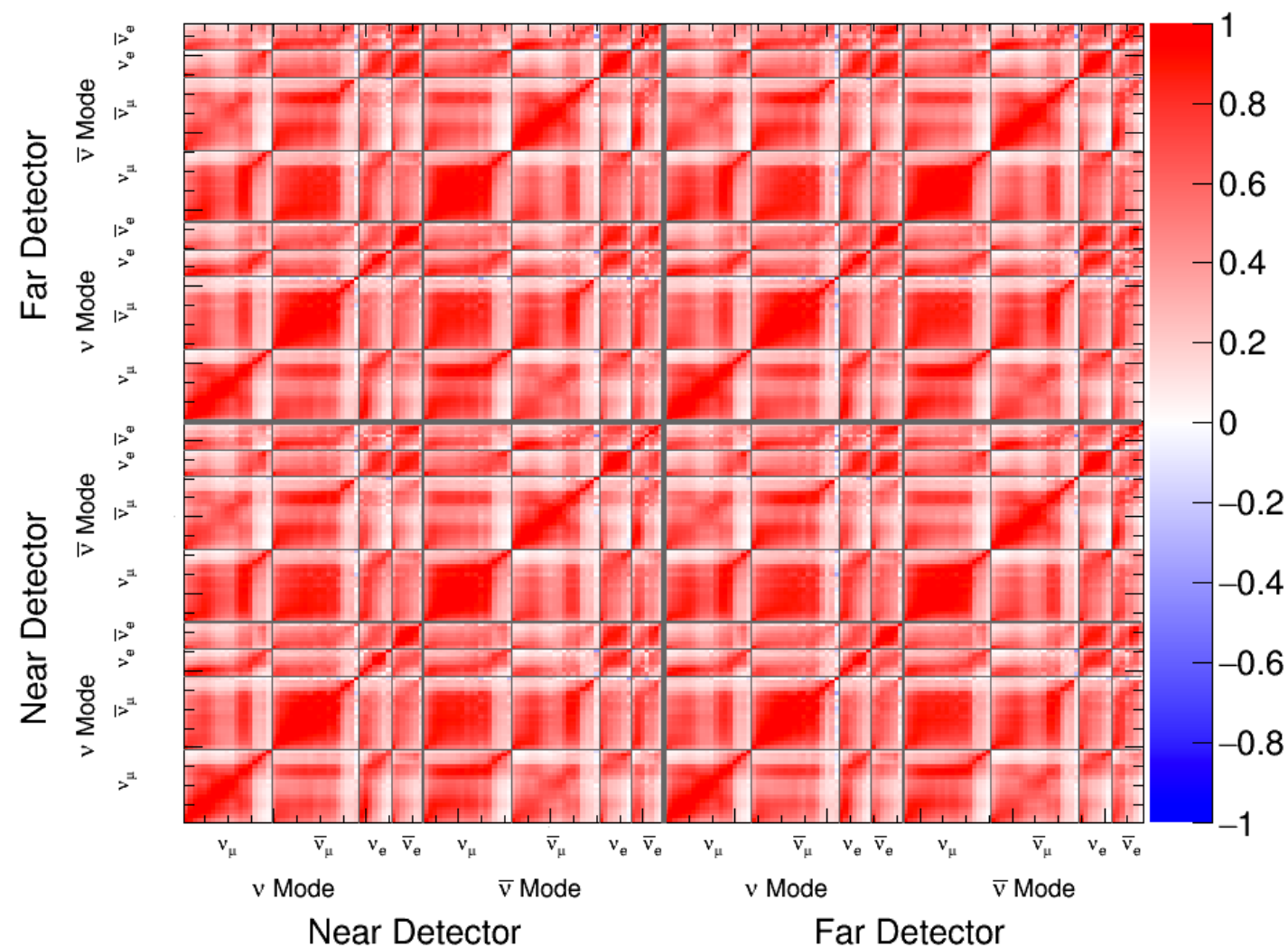
# Reference and Optimized Beam Uncertainties



Very similar in focusing peak; Optimized has slightly larger uncertainties at high energy, primarily due to having more interactions not covered by data

# Beam Uncertainty Correlation Matrix for the Optimized beam

Optimized



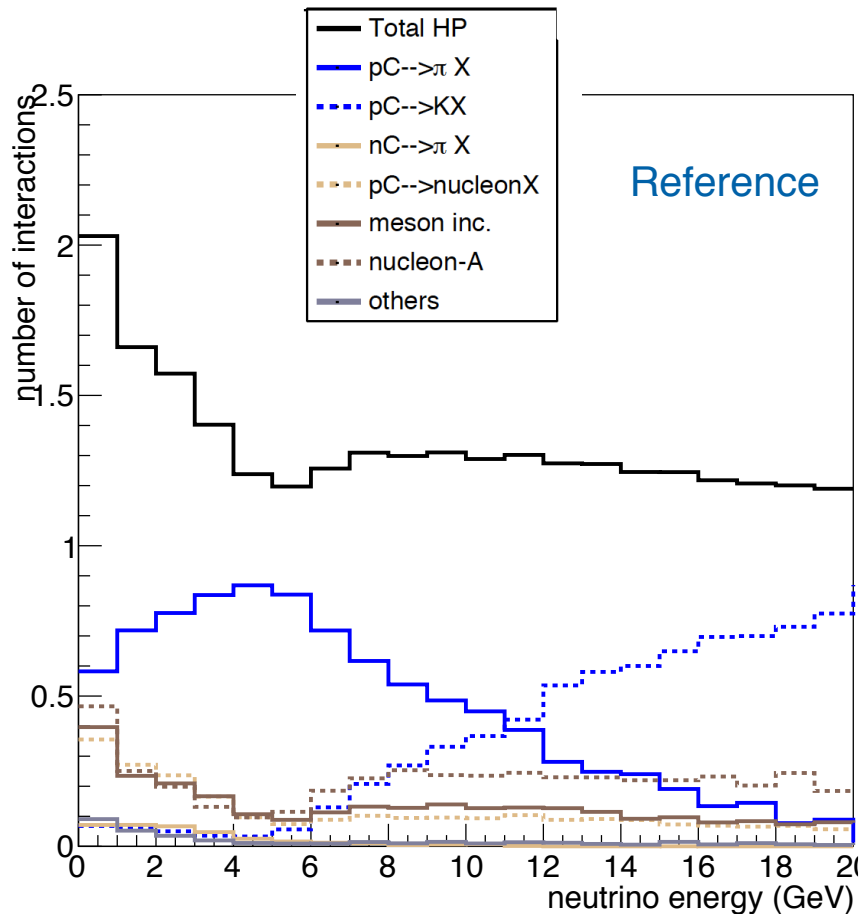
- Fluxes are **highly correlated** across most bins
- **Focusing regions and high energy bins** are the exceptions
- Depends strongly on **correlations of underlying datasets**; in many cases, we have to guess at these.

L. Fields (NA61 Workshop 2017)

## Reducing the flux uncertainties

# How can we reduce the a priori uncertainties

## More thin target data



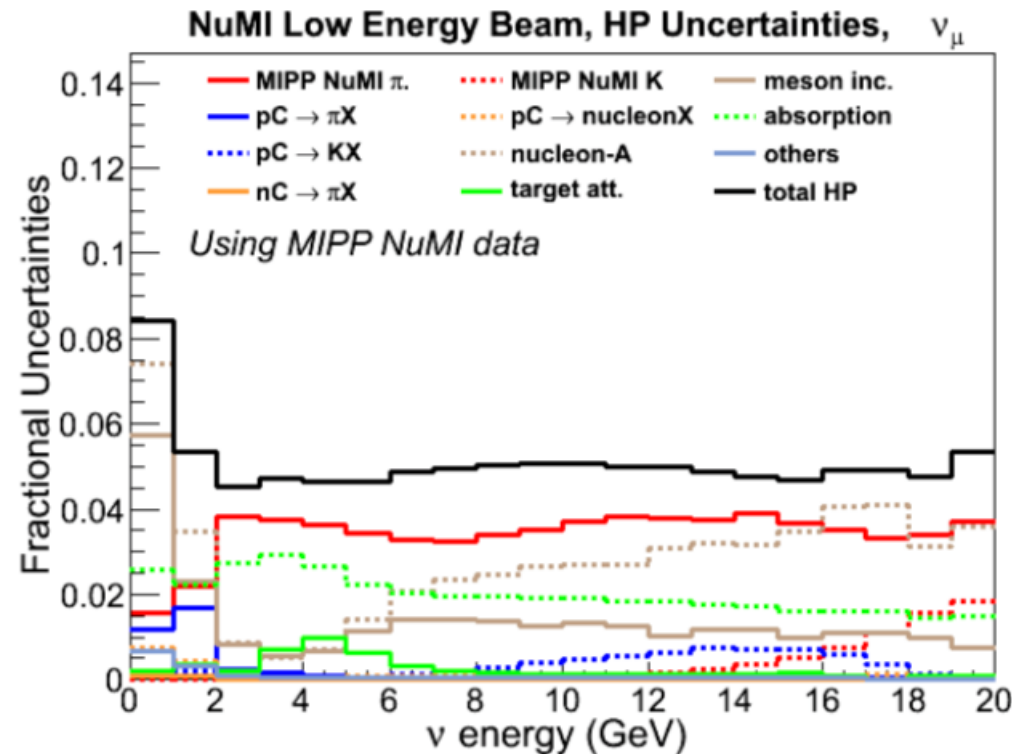
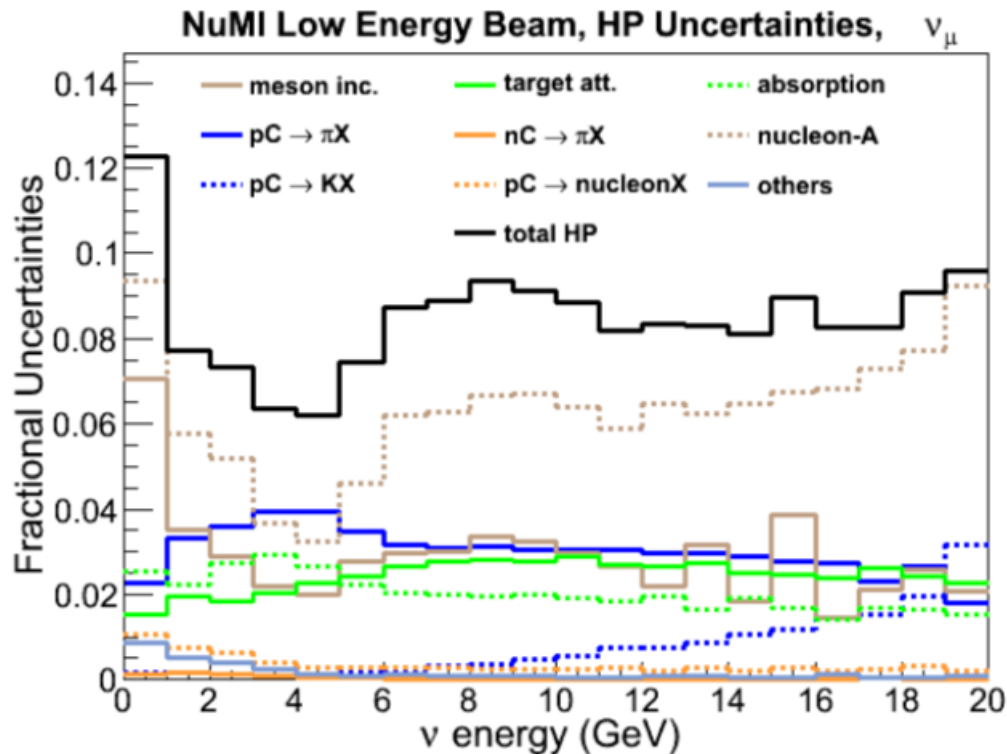
- **Inelastic cross-sections** of  $\pi$ , K and protons in different materials (C, Fe, Al, He).
- **Differential cross-sections** in different materials
  - $\pi \rightarrow \pi$  at a wide range 10-60 GeV.
  - $pA \rightarrow \pi (K) X$ , where  $X \neq C$
- **Proton quasi elastic cross-sections**

# How can we reduce the a priori uncertainties

## Replica target data: MINERvA experience.

- ~ 5% using MIPP NuMI target data primarily.

Phys. Rev. D 94, 092005 (2016)



**Checking the consistency with the low- $\nu$  measurement, MINERvA decided to use a prediction based only on thin target corrections**



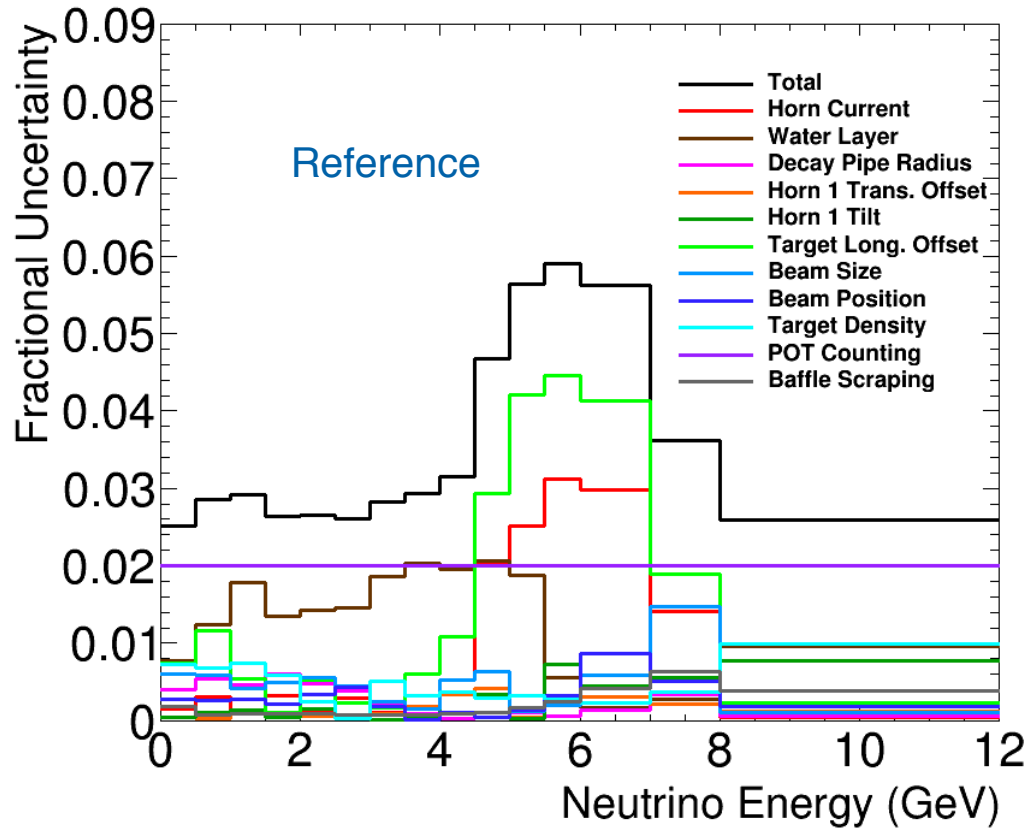
# LBNF Flux Spectrometer

A concept to measure hadron production after the horns (See Paul Le Brun's talk)

# Reducing the Focusing Uncertainties

*After reducing the HP, the focusing uncertainties will become dominant.*

- **POT counting** and **water layer** are the most significant at the peak.
- **Horn current** and **target longitudinal offset** are the most significant at the falling edge for the reference design.



# Conclusions

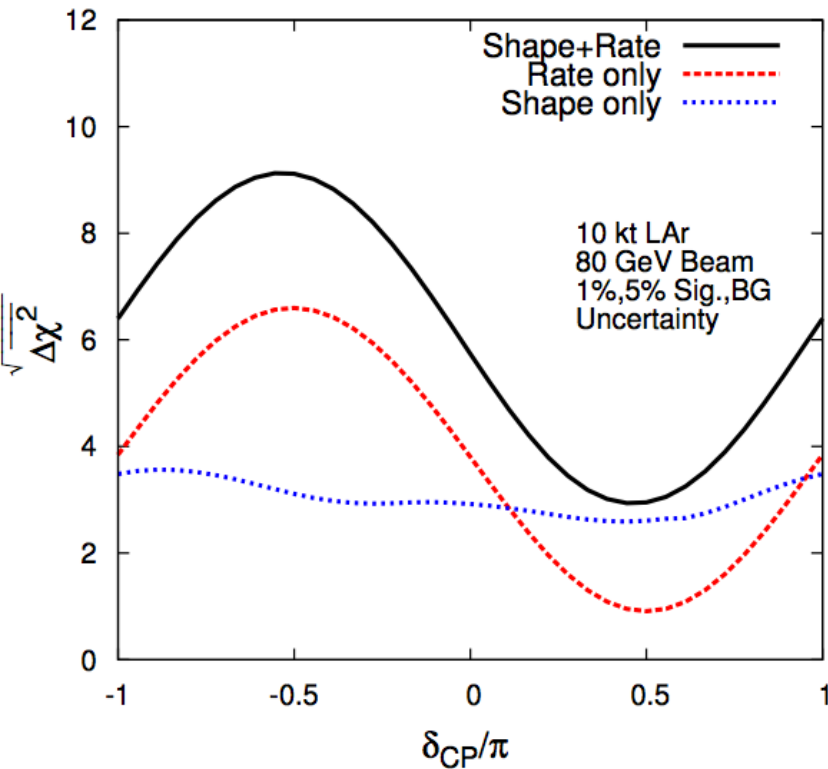
- Reducing the HP uncertainties is possible with dedicated experiments:
  - **Replica target data** would be the best option but **timescale** is a challenge (DUNE expects to receive beam in 2026) and it is likely that no replica will be available.
  - **Thin target data** would likely to have big impact on DUNE.

**backup**

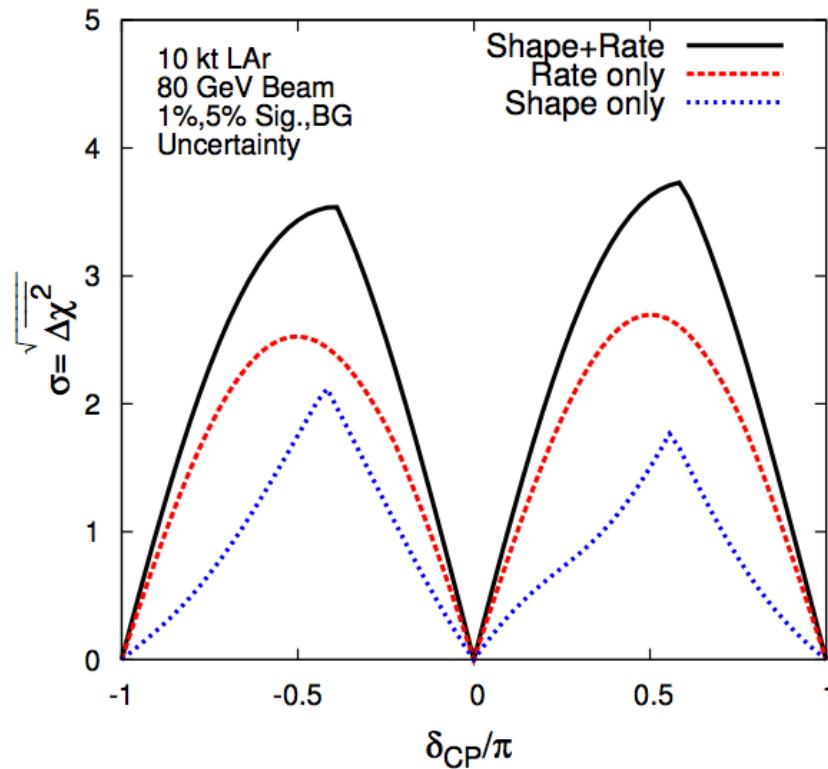
# LBNF/DUNE Long Baseline Physics

Respect to the shape (flux shape can have a big impact):

MH Significance vs  $\delta_{CP}$  (NH)

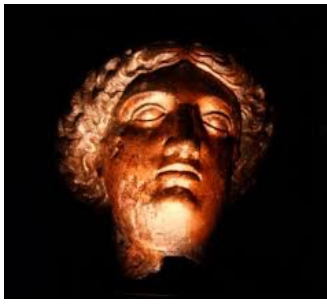


CPV Significance vs  $\delta_{CP}$  (NH)



LBNE Physics  
Book

This omission means that systematics likely have **an even bigger impact** than shown on previous page (which is already impressive!)



# MINERvA Strategy for Predicting the Flux

1. Calculate an a-priori flux

*Accounting for every optical modeling uncertainty.*

*Correcting the hadron production in the beam line to constrain to external hadron production data.*

2. Use in-situ measurements

*Checking our results with the low recoil event rates (low-nu method): flux shape measurement.*

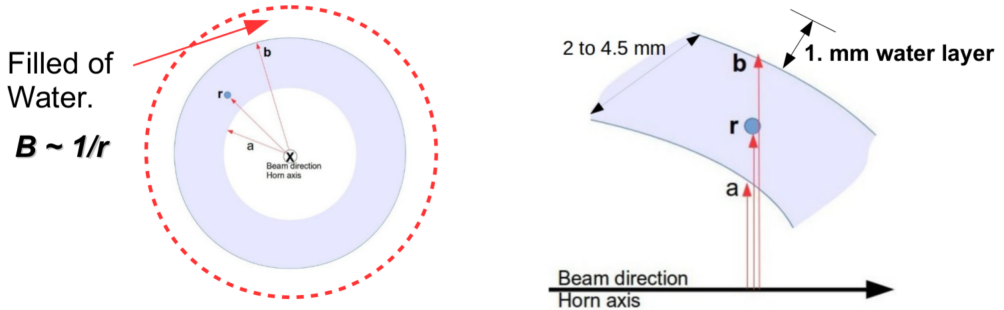
*Applying an additional constraint from the neutrino - electron scattering events.*

3. Package to Predict the Flux

*Develop every tool in such a way they can be used by any experiment at NuMI (PPFX).*

# Some geometrical improvements

## Effect of 1mm water layer around the Horn 1 inner conductor

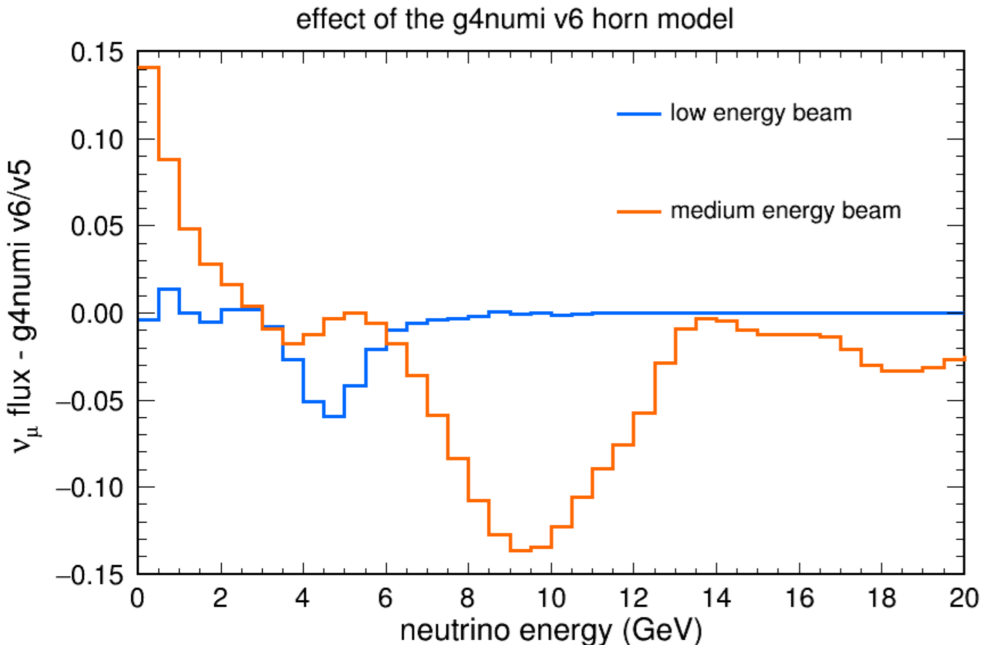
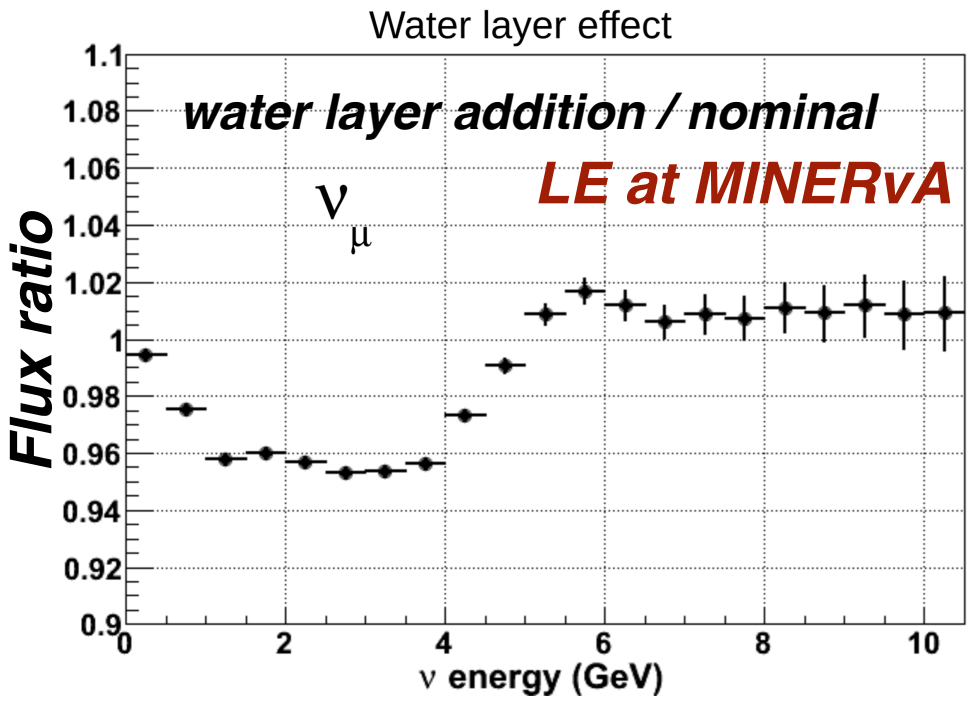


● 4% effect around the LE flux peak.

● More accurate description of the inner conductor (IC) of Horn 1 designed for LBNF

- Improved segmentation of the IC surface
- Check the neck shape (cylinder).

● 5% (14%) effect in the LE (ME) falling edge of the flux peak at MINERvA.

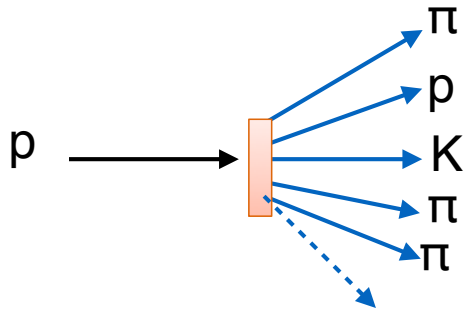


(Implemented by Paul Le Brun)

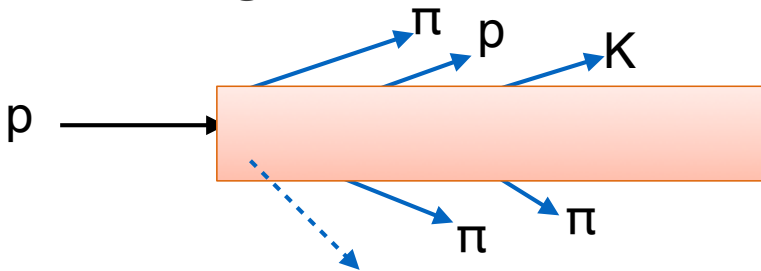
# External Data? What Sort of Data is Available?

- Hadron production data at the relevant energies for NuMI (references in the backup slides):

## Thin Target Data



## Thick Target Data



- Inelastic/absorption
  - Belletinni, Denisov, etc. cross sections of  $pC$ ,  $\pi C$ ,  $\pi Al$  etc.
  - **NA49:  $pC$  @ 158 GeV.**
  - NA61  $pC$  @ 31 GeV.
- Hadron Production:
  - Barton:  $pC \rightarrow \pi^\pm X$  @ 100 GeV  $x_F > 0.3$  .
  - **NA49:  $pC \rightarrow \pi^\pm X$  @ 158 GeV  $x_F < 0.5$  .**
  - NA49:  $pC \rightarrow n(p)X$  @ 158 GeV for  $x_F < 0.95$  .
  - NA49:  $pC \rightarrow K^\pm X$  @ 158 GeV for  $x_F < 0.2$  .
  - NA61:  $pC \rightarrow \pi^\pm X$  @ 31 GeV .
  - MIPP:  $\pi/K$  from  $pC$  at 120 GeV for  $p_Z > 20 \text{ GeV}/c$ .
- MIPP: proton on a spare NuMI target at 120 GeV:
  - $\pi^\pm$  up to 80 GeV/c.
  - $K/\pi$  for  $p_Z > 20 \text{ GeV}/c$ .

**Checking the consistency with the MINERvA low-nu measurement, we decided to use a prediction based only on thin target correction**



# 1. Beam Attenuation

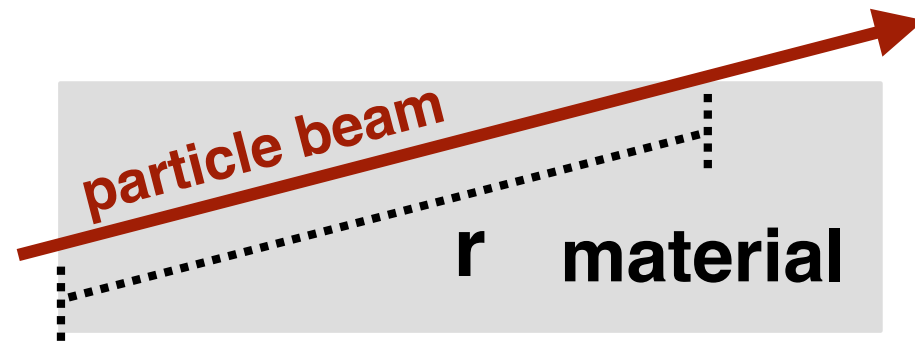
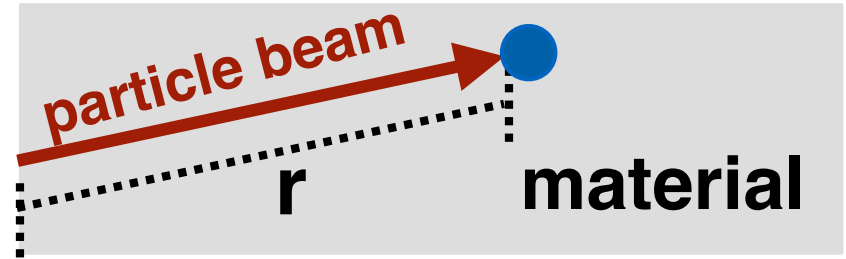
When the particle interacts in a volume

$$\text{correction}(r) = \frac{\sigma_{Data}}{\sigma_{MC}} e^{-r \frac{N_A \rho (\sigma_{Data} - \sigma_{MC})}{A}}$$

$N_A$ : Avogadro Number,  $\rho$ : density,  $A$ : mass number

When the particle passes through the volume without interacting

$$\text{correction}(r) = e^{-r \frac{N_A \rho (\sigma_{Data} - \sigma_{MC})}{A}}$$



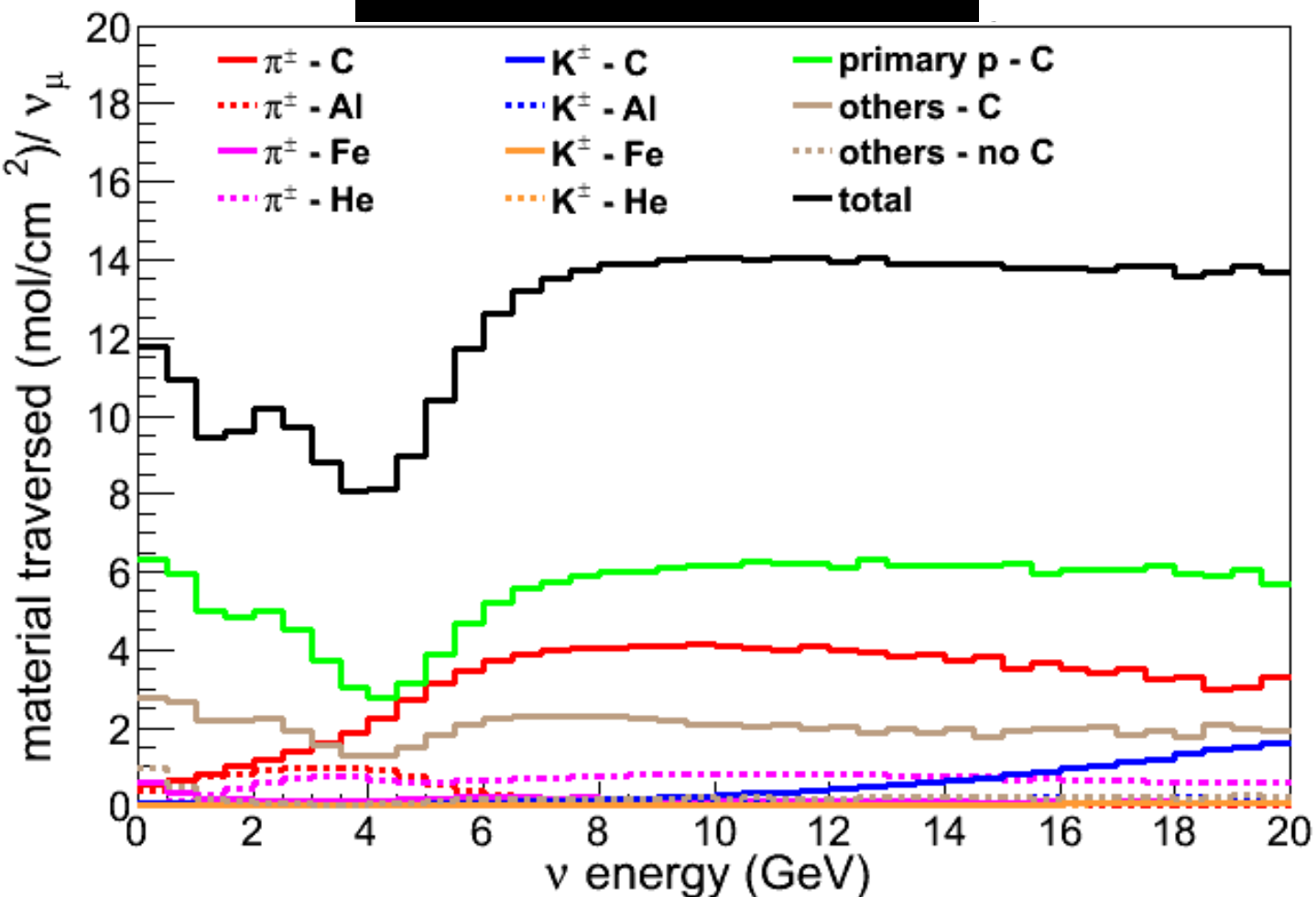
Two variables are important here:

- The amount of material:  $rN_A\rho/A$ .
- The  $\sigma_{Data}$  and  $\sigma_{MC}$  disagreement.

# Amount of Material Traversed

- Muon neutrino parent:

## LE Mode at MINERvA



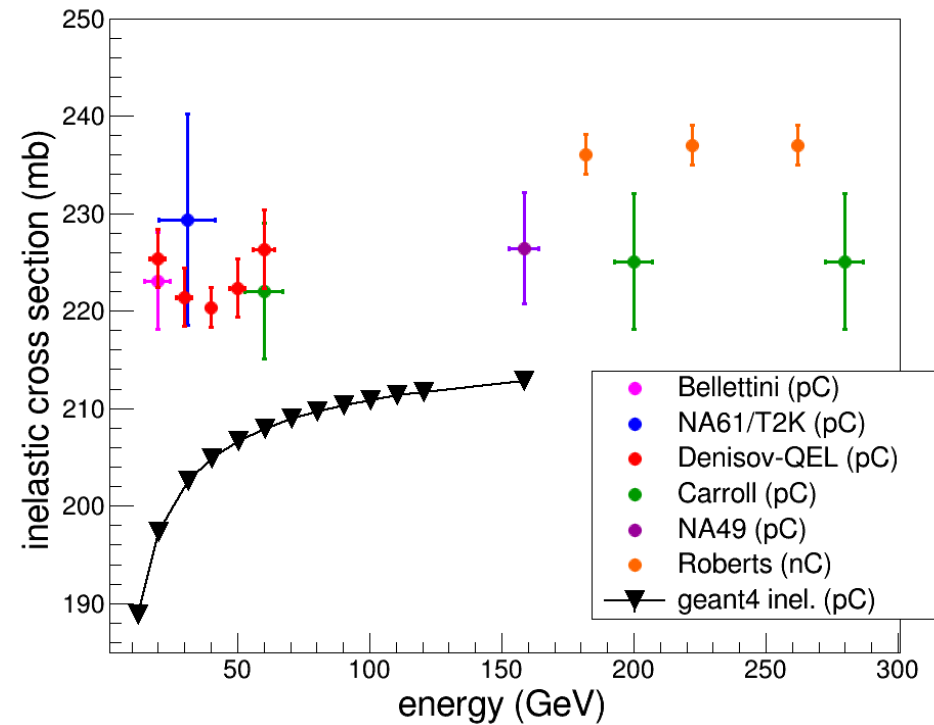
### References:

- C: 6 mol/cm<sup>2</sup> ≈ 40 cm
- Al: 1 mol/cm<sup>2</sup> ≈ 10 cm
- He: 1 mol/cm<sup>2</sup> ≈ 500 m

# Data - MC Comparison

## Inelastic cross section

### Proton on Carbon

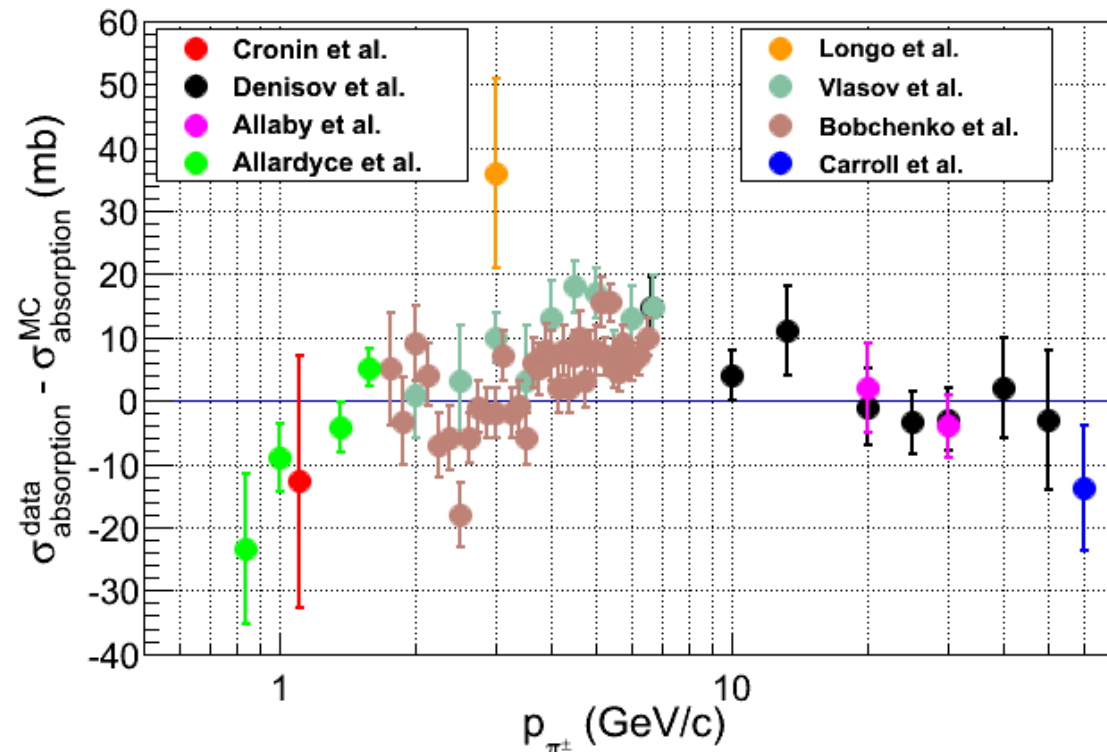


Reference (Geant4):

$$\sigma_{absorption} = 243.2 \text{ mbar}$$

## Absorption cross section

### Pion on Aluminum



Reference (Geant4):

$$\sigma_{absorption} = 344 \text{ mbar}$$

$$\sigma_{total} = \sigma_{elastic} + \underbrace{\sigma_{inelastic} + \sigma_{quasi-elastic}}_{\sigma_{absorption}}$$

## 2. Hadron Production

**For thin target data (NA49 for instance):**

$$\text{correction}(x_F, p_T, E) = \frac{f_{\text{Data}}(x_F, p_T, E = 158 \text{ GeV}) \times \text{scale}(x_F, p_T, E)}{f_{\text{MC}}(x_F, p_T, E)}$$

(  $f = E d^3 \sigma / dp^3$ : invariant production cross section)

- The **scale** allows us to use NA49 for proton on carbon in 12-120 GeV (calculated with FLUKA).
- It was checked by comparing with NA61 at 31 GeV (negligible difference).

**For thick target data (MIPP):**

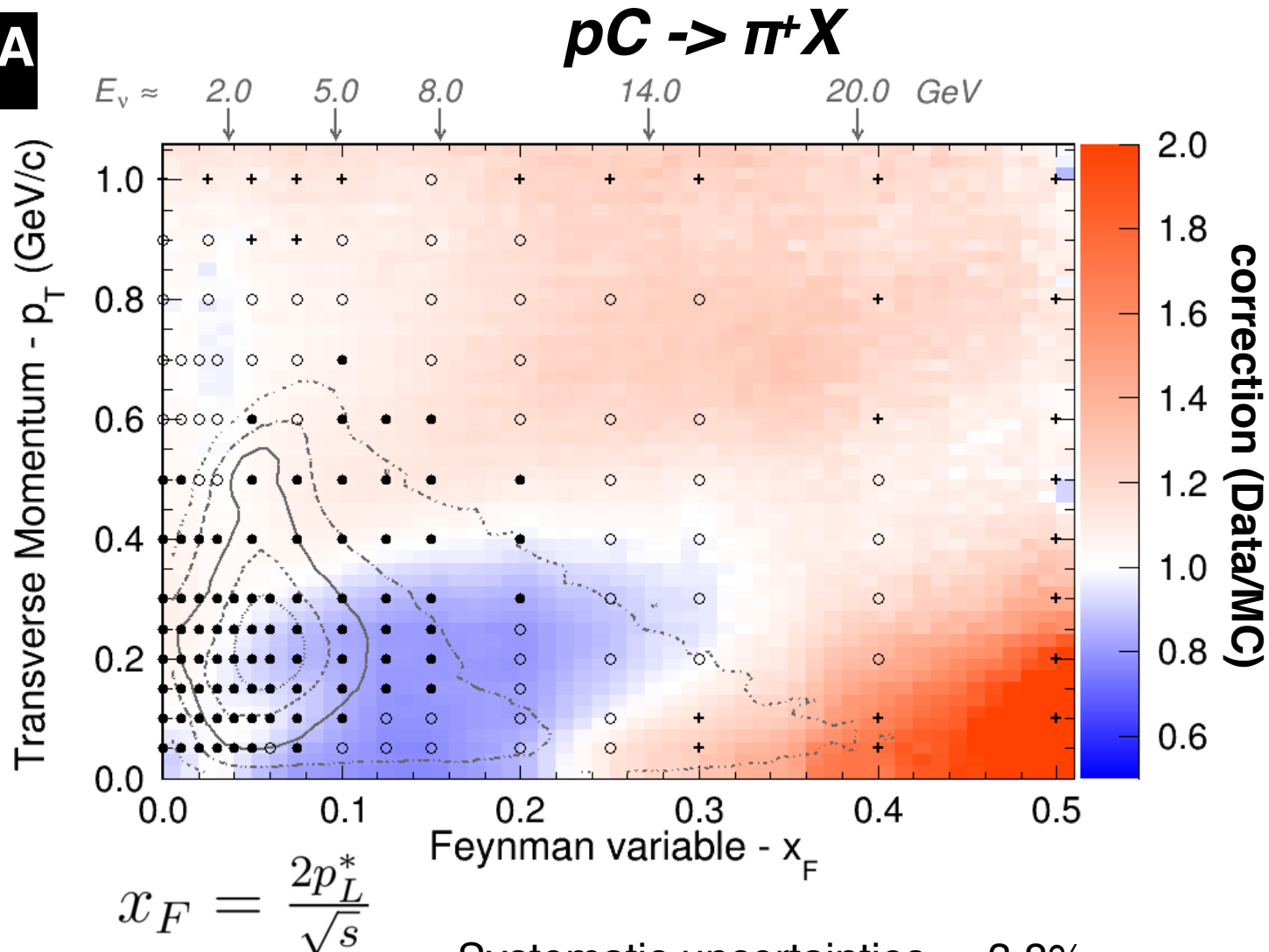
$$\text{correction}(p_Z, p_T) = \frac{n_{\text{Data}}(p_Z, p_T)}{n_{\text{MC}}(p_Z, p_T)}$$

**Example: NA49 Data/MC comparison** (closed circles = statistical error < 2.5%, Open circles = statistical error 2.5-5.0%, Crosses > 5%).

## LE Mode at MINERvA

Contours: 2.5, 10, 25, 50 and 75 % of the pion yields.

- Systematics are highly correlated bin-to-bin.
- Systematics and statistical errors are considered uncorrelated each other.



Systematic uncertainties = 3.8%  
(added in quadrature).

# If There is not Direct Data

## Extending the data coverage

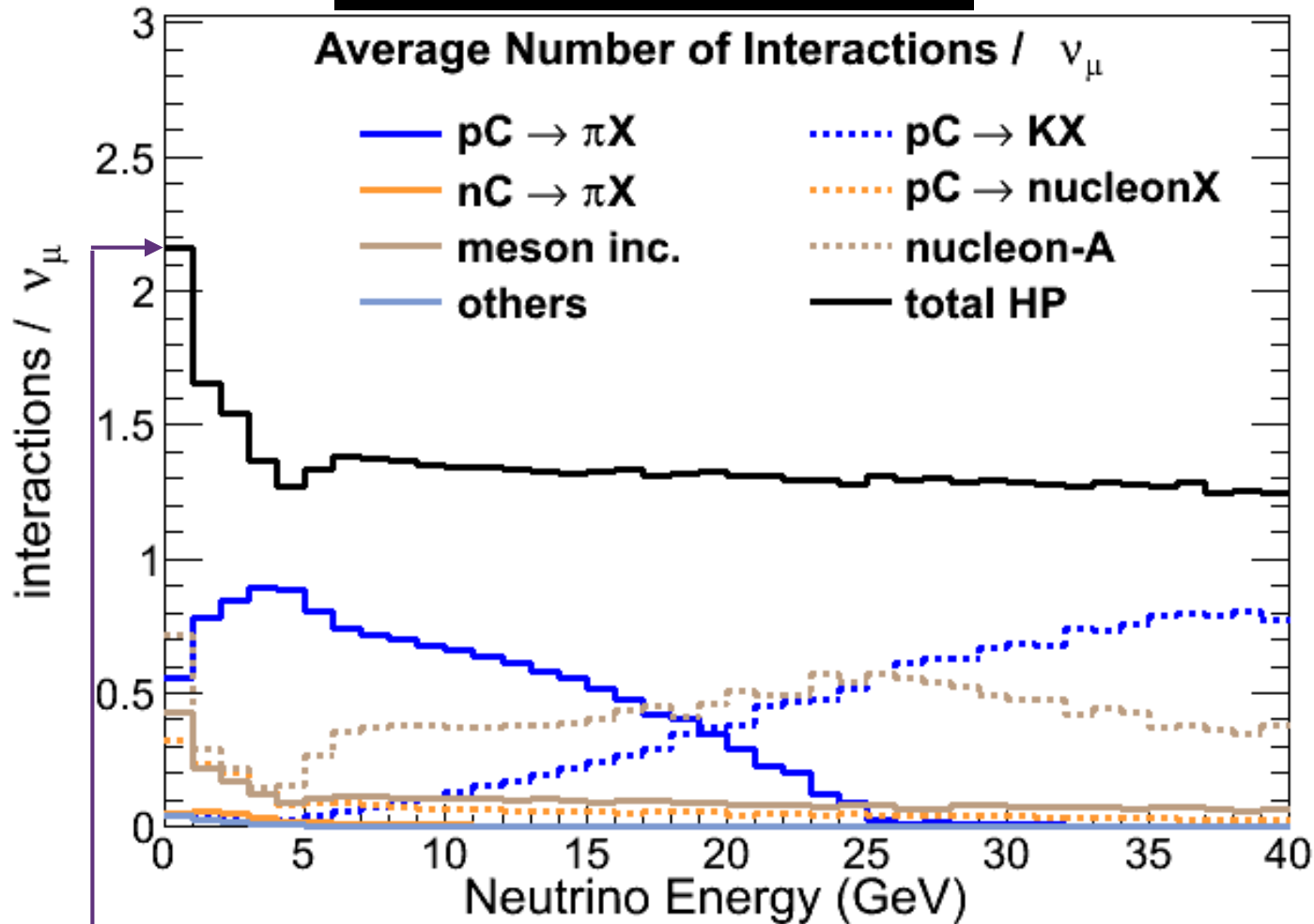
- Constrain pA interactions with pC adding an additional uncertainty found by comparing A dependence of Barton, Skubic and Eichten.
- Use theoretical guidance (isospin arguments, quark counting arguments, etc.)

## What if data is not available?

- Guided by the agreement with other datasets: processes categorized by projectile and produced particle. 40% error assigned in 4  $x_F$  bins.

# Average Number of Interactions

## LE Mode at MINERvA



**~2.2 for very low  $E_\nu$  and ~1.4 for the rest**

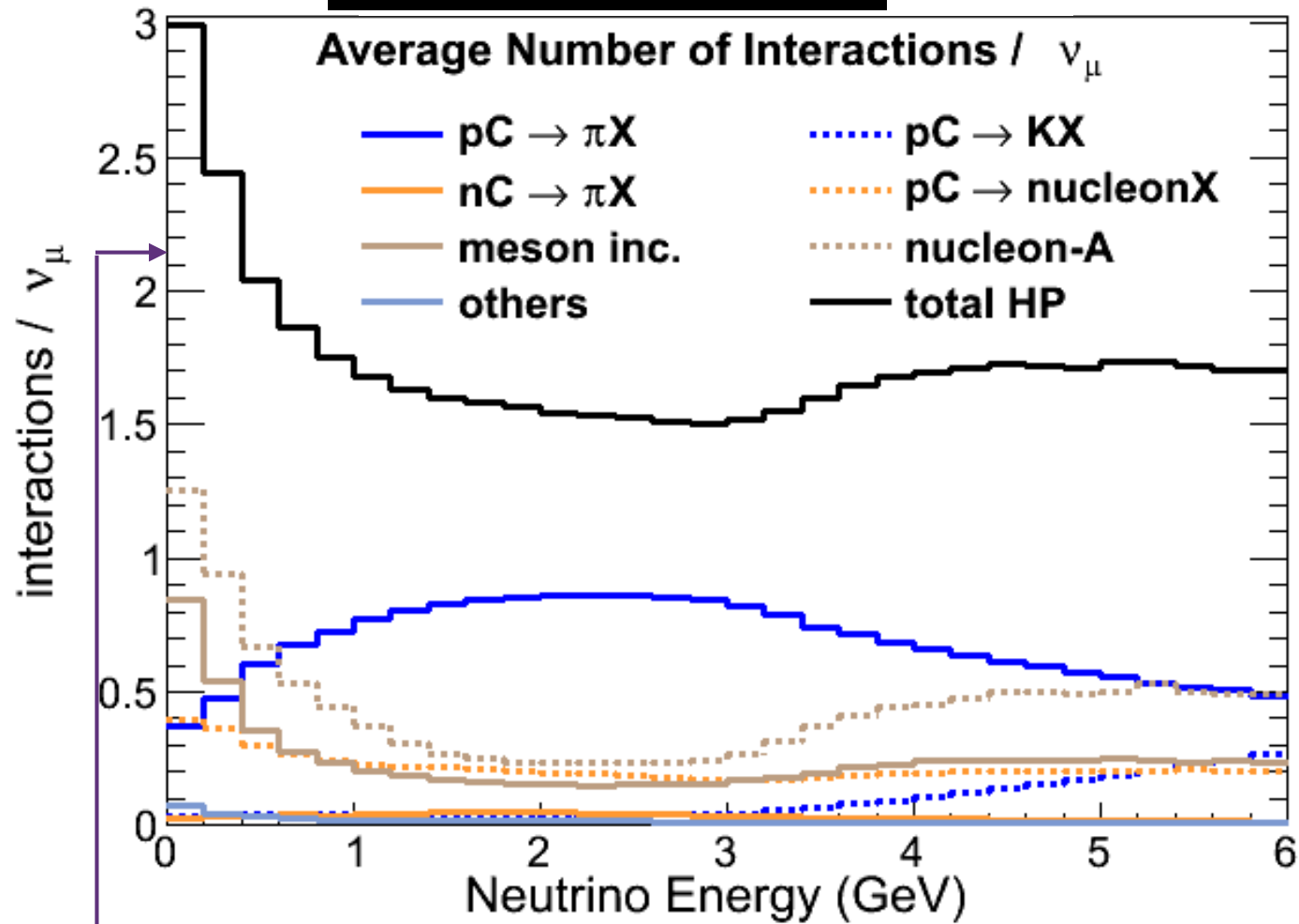
$\pi$ ,  $K$  and nucleons productions from  $pC$  based on data (mainly NA49).

We assume large uncertainties for meson incident.

- **nucleon-A** (quasi-elastics, extension from carbon to other materials, production outside data coverage, etc).

# Average Number of Interactions

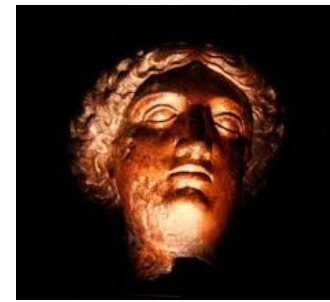
## At NOvA



*~3.0 for low  $E_\nu$  and ~1.5-1.6 for the rest*

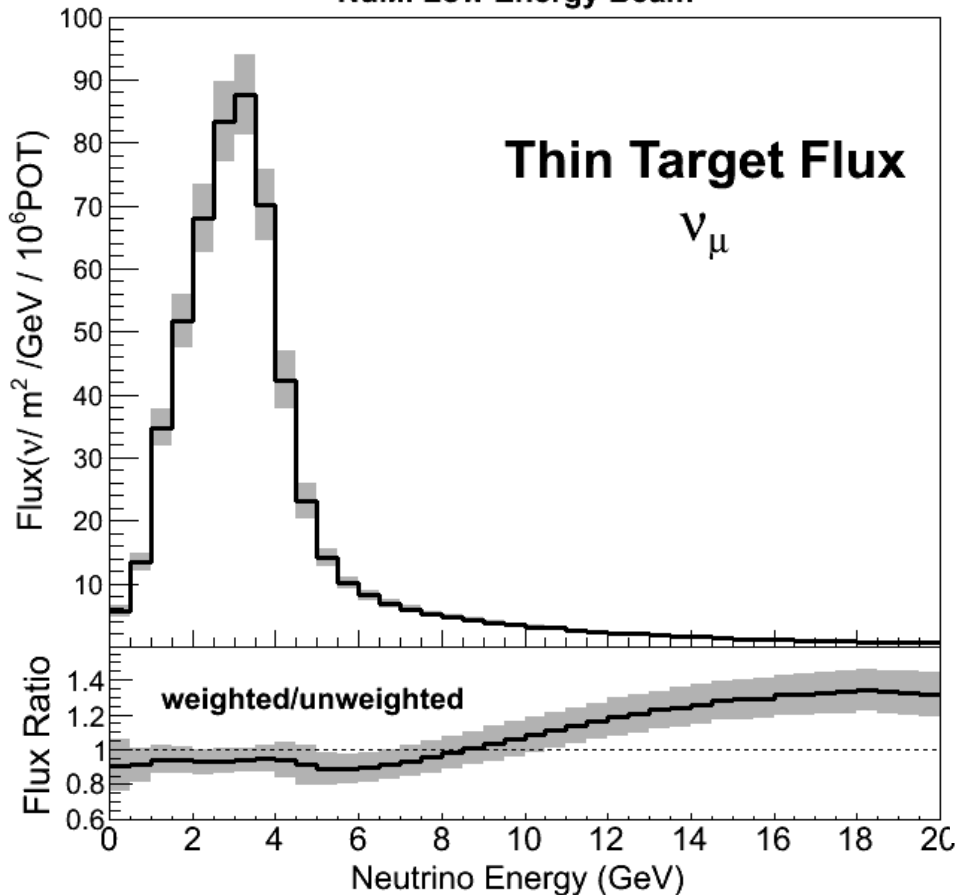


# A Priori Flux Results for LE MINERvA

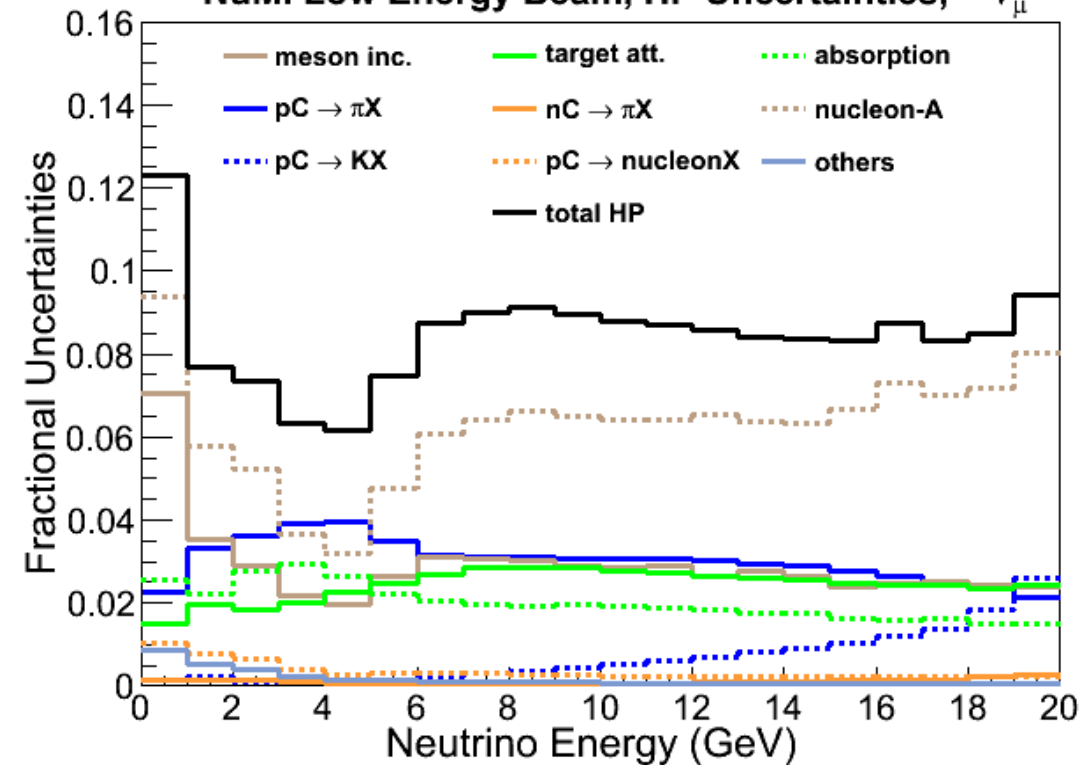


- MINERvA published the flux prediction for LE NuMI beam based on **thin target data correction**

NuMI Low Energy Beam



NuMI Low Energy Beam, HP Uncertainties,  $\nu_\mu$

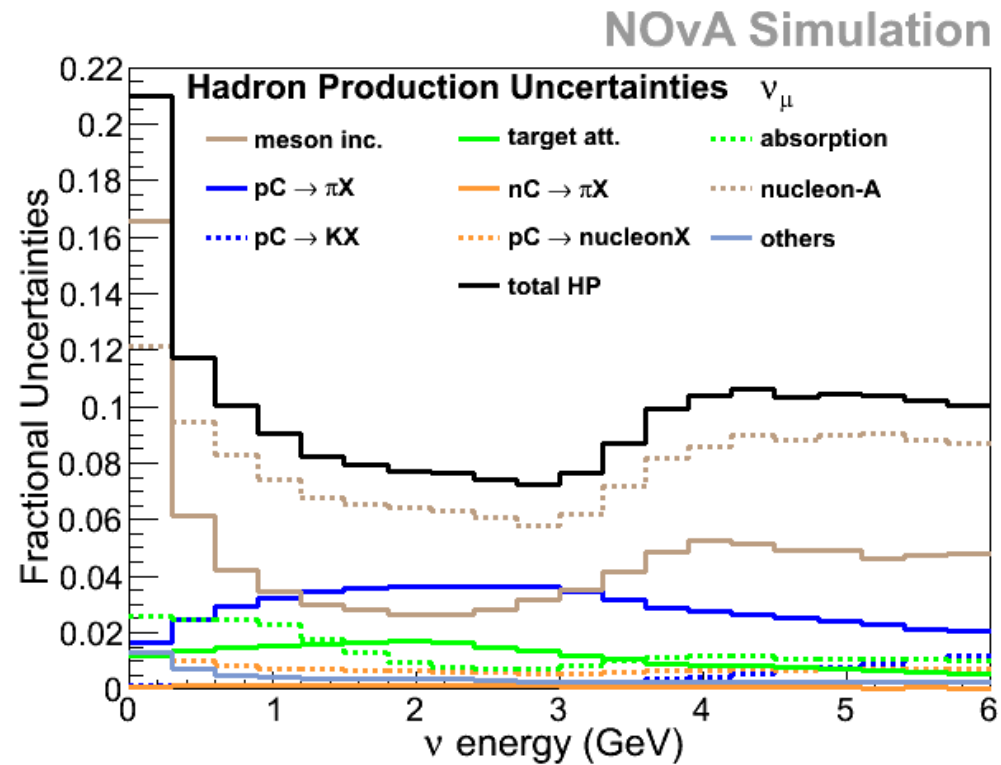
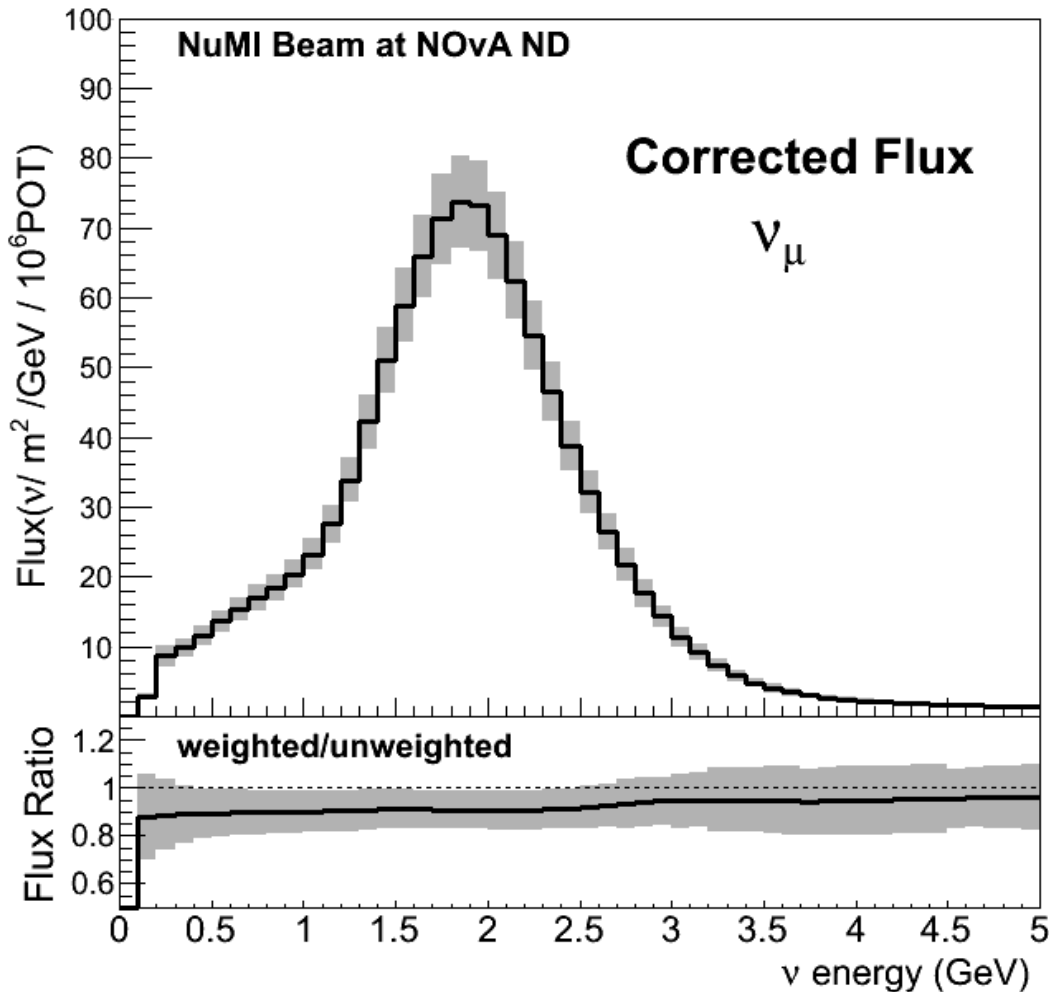


Phys. Rev. D 94, 092005 (2016)

# A Priori Flux Results for NOvA Near Detector



- The same procedure has been fully implemented by NOvA for its a priori flux prediction in NOvA
- NOvA Simulation



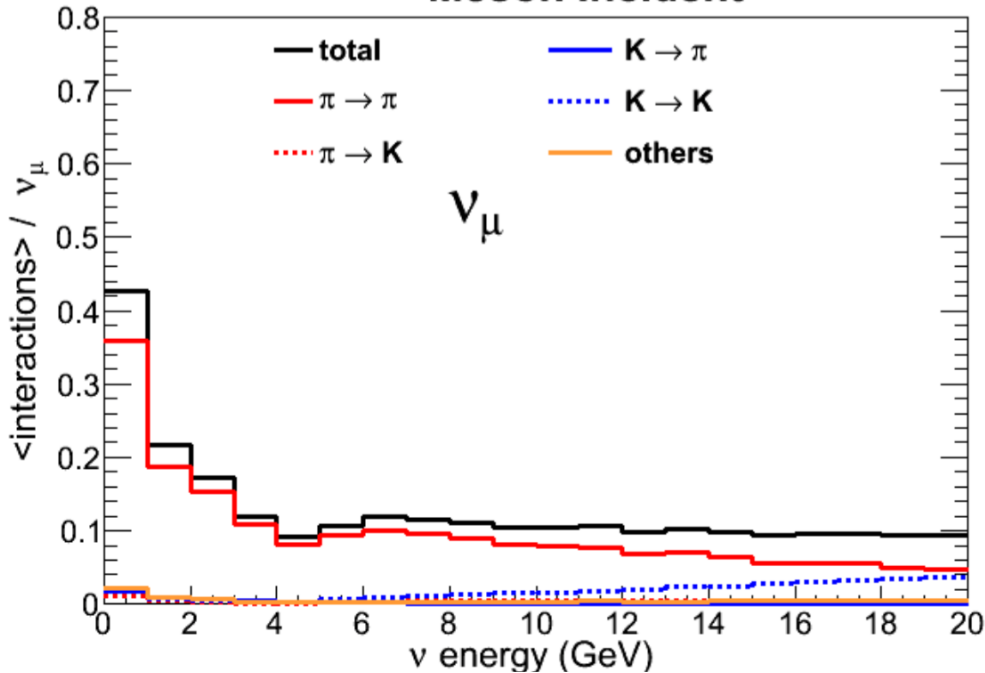
# Conclusions

- For NOvA, MINERvA (and MINOS+) and other experiments it is crucial to have a precise measurement of the flux with small uncertainties.
- The hadron production is the main source of uncertainties. Applied all relevant existing data to constrain the flux reduce the uncertainties.
- We develop an open and free computational tool called **PPFX** to share our result with other NuMI experiments.
  - Currently use by MINERvA and NOvA .
  - It has been adapted for DUNE and it is being used by the ND systematics

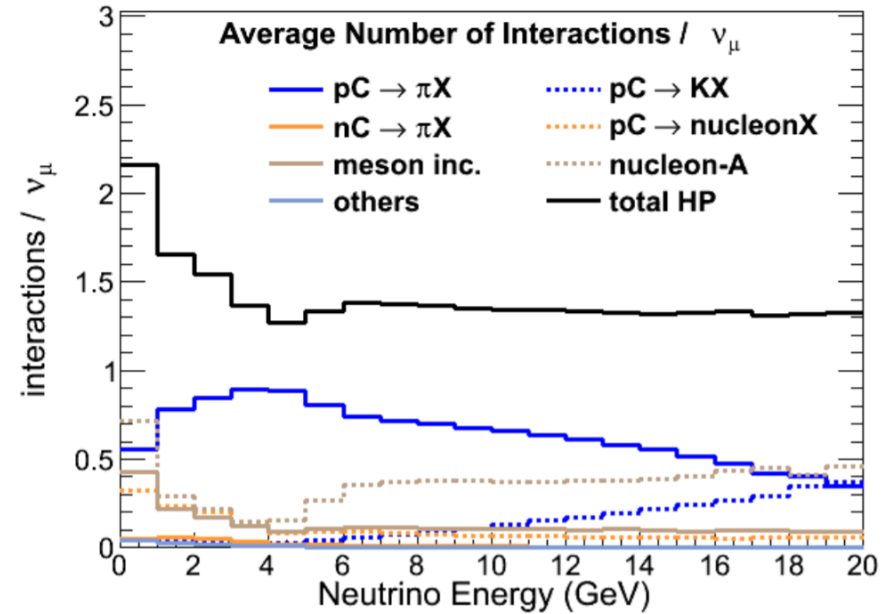
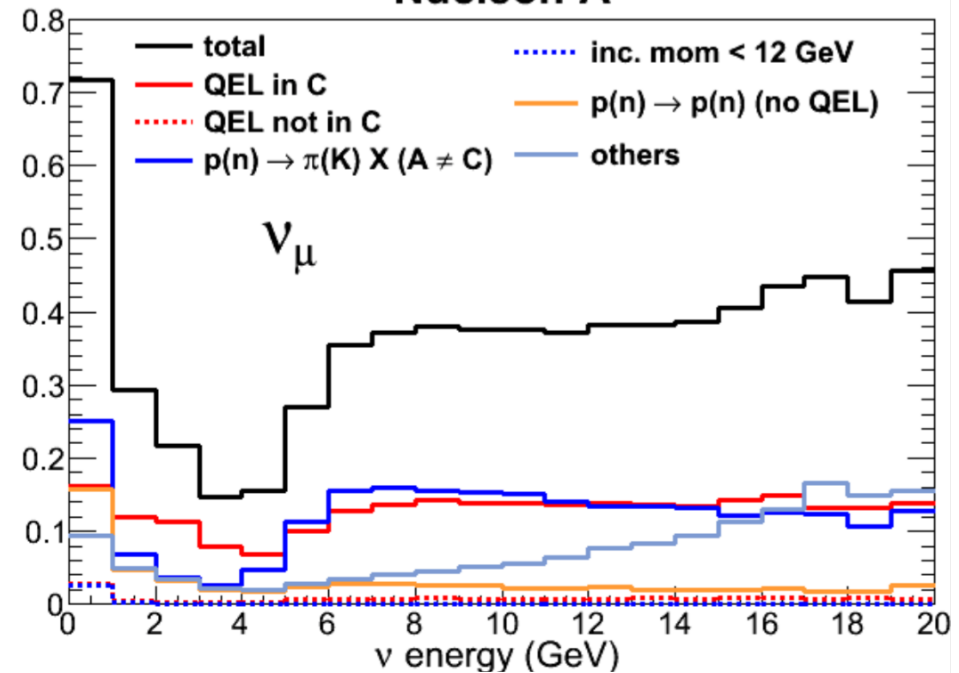
# Conclusions FOR MINERvA

- This work also indicates where additional data is needed
  - $\pi \rightarrow \pi$  at 30 GeV.
  - proton quasi-elastic cross section.
  - $pX \rightarrow \pi(K)X$  (A not C).

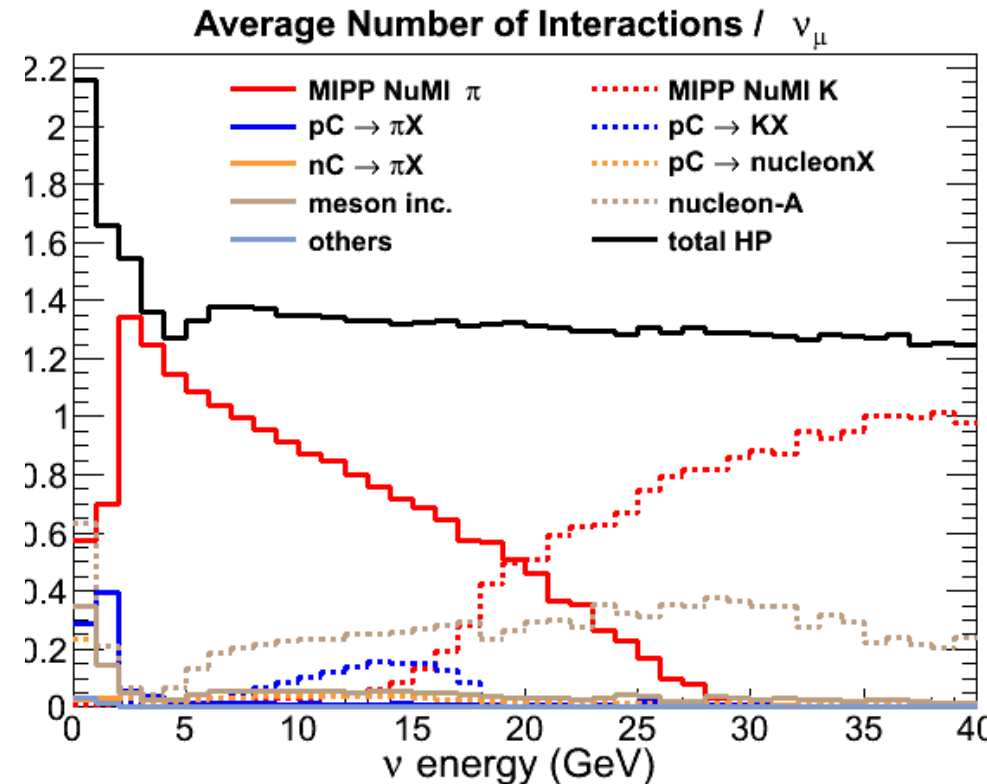
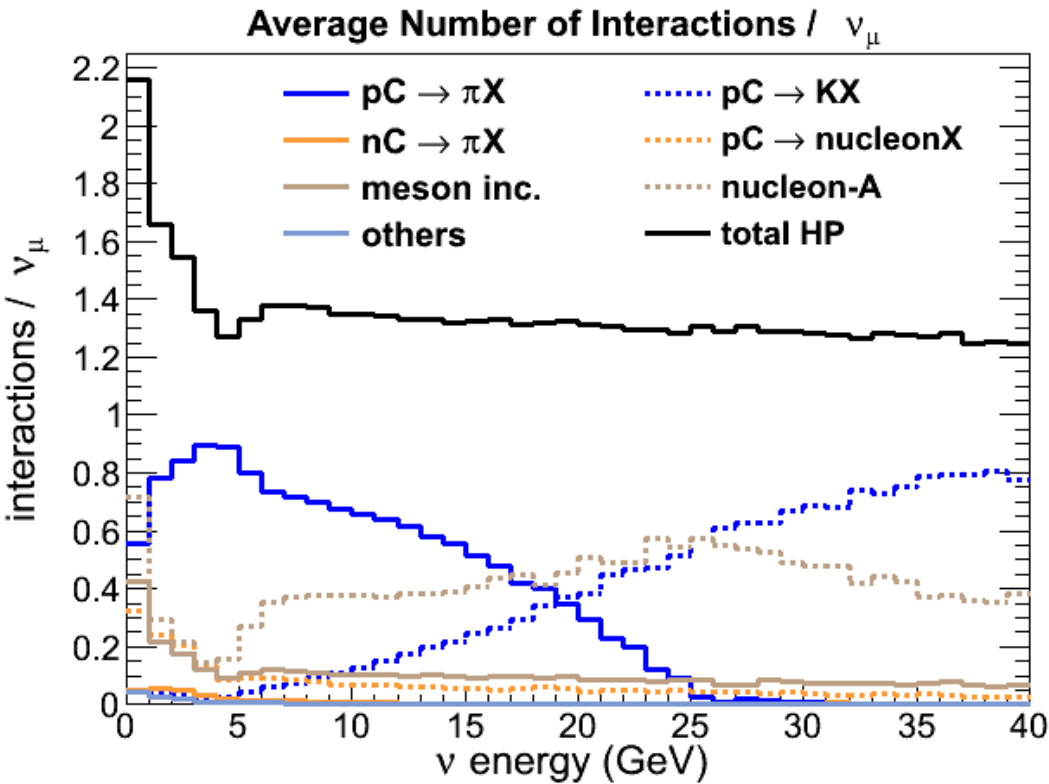
Meson Incident



Nucleon-A



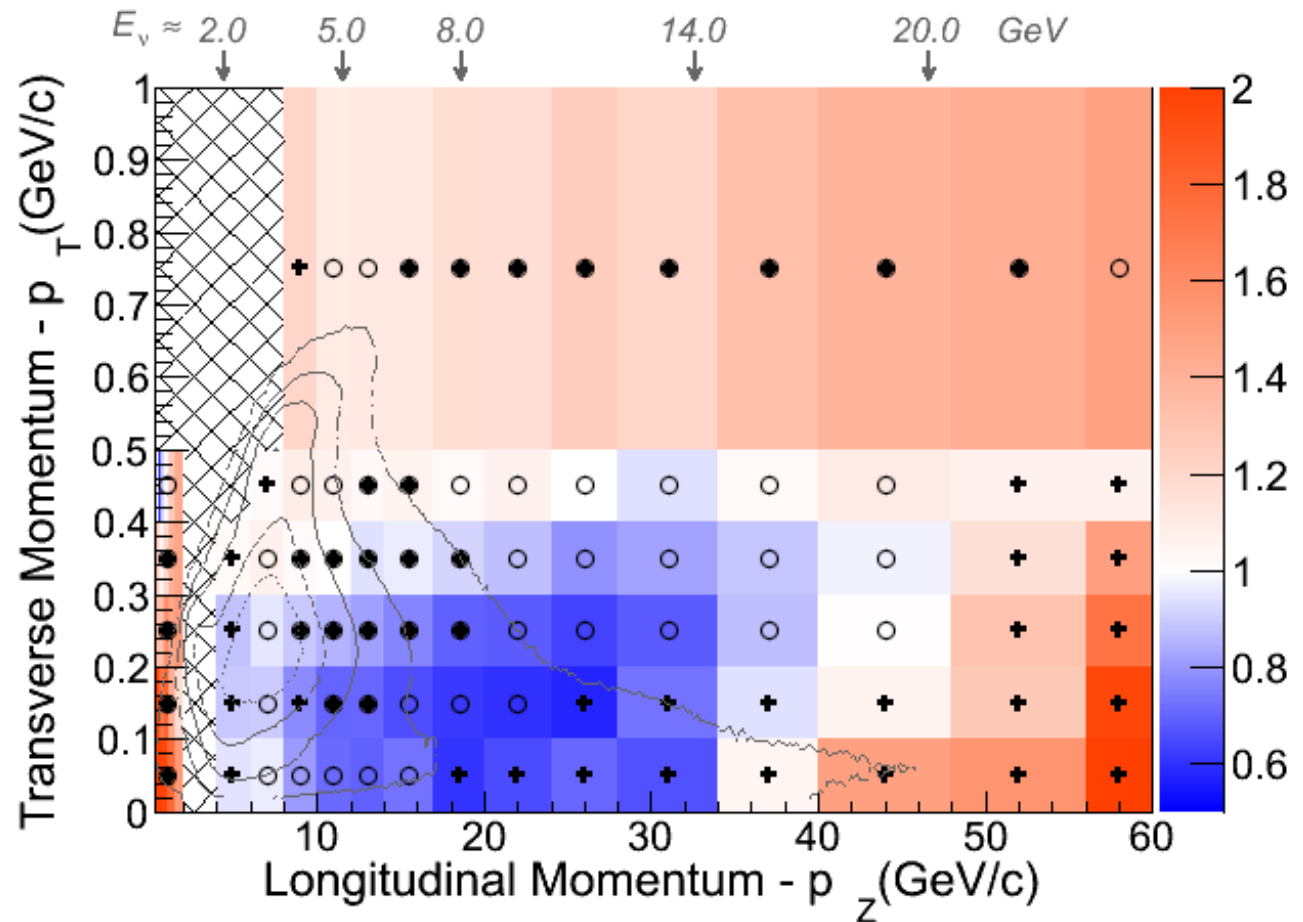
# Advantage to use thick target data



**MIPP NuMI Data/MC comparison** (closed circles = statistical error < 2.5%, Open circles = statistical error 2.5-5.0%, Crosses > 5%).

## LE Mode On-Axis

$p\text{NuMI} \rightarrow \pi^+ X$



systematic uncertainties = 3.8%  
(added in quadrature).

*Contours: 2.5, 10, 25, 50 and 75 % of the pion yields.*

- Systematics are highly correlated bin-to-bin.
- Systematics and statistical errors are considered uncorrelated each other.

# Focusing Components

