



# LÉVY HBT STATUS AND OTHER PLANS WITH PHENIX, CMS AND NA61

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MÁTÉ CSANÁD @ DAY OF FEMTOSCOPY, NOV 2, 2018

EÖTVÖS UNIVERSITY, BUDAPEST, HUNGARY



NATIONAL RESEARCH, DEVELOPMENT  
AND INNOVATION OFFICE  
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PROGRAM  
FINANCED FROM  
THE NRDI FUND  
*MOMENTUM OF INNOVATION*

## 2/17 LEVY DISTRIBUTIONS IN HEAVY ION PHYSICS

- Expanding medium, increasing mean free path: anomalous diffusion

Metzler, Klafter, Physics Reports 339 (2000) 1-77, Csanad, Csorg, Nagy, Braz.J.Phys. 37 (2007) 1002

- Levy-stable distribution:

$$\mathcal{L}(\alpha, R; r) = \frac{1}{(2\pi)^3} \int d^3 q e^{iqr} e^{-\frac{1}{2}|qR|^\alpha}$$

- Generalized Gaussian from generalized central limit theorem
- $\alpha = 2$  Gaussian,  $\alpha = 1$  Cauchy

- Shape of the correlation functions with Levy source:

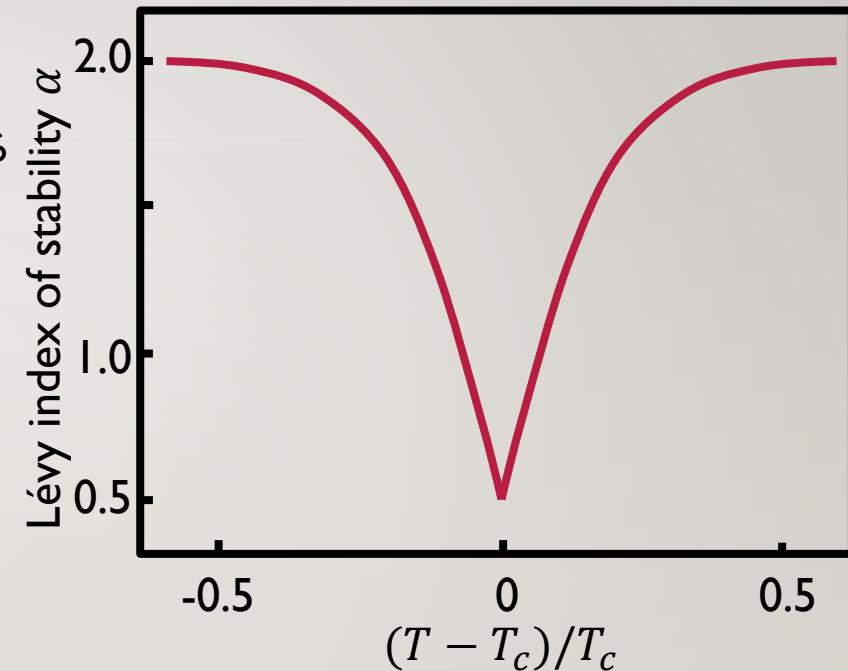
$$C_2(q) = 1 + \lambda \cdot e^{-|qR|^\alpha} \quad \begin{array}{l} \alpha = 2: \text{Gaussian} \\ \alpha = 1: \text{Exponential} \end{array}$$

- Critical behavior → described by critical exponents
- Spatial correlation  $\sim r^{(d-2-\eta)}$  → defines critical exponent
- Symmetric stable distributions (Levy) → spatial corr.  $\sim r^{1-\alpha}$
- $\alpha$  alpha can be associated with the critical exponent eta
- Csorg, Hegyi, Zajc, Eur.Phys.J. C36 (2004) 67, nucl-th/0310042

3/17

# Lvy index as a critical exponent?

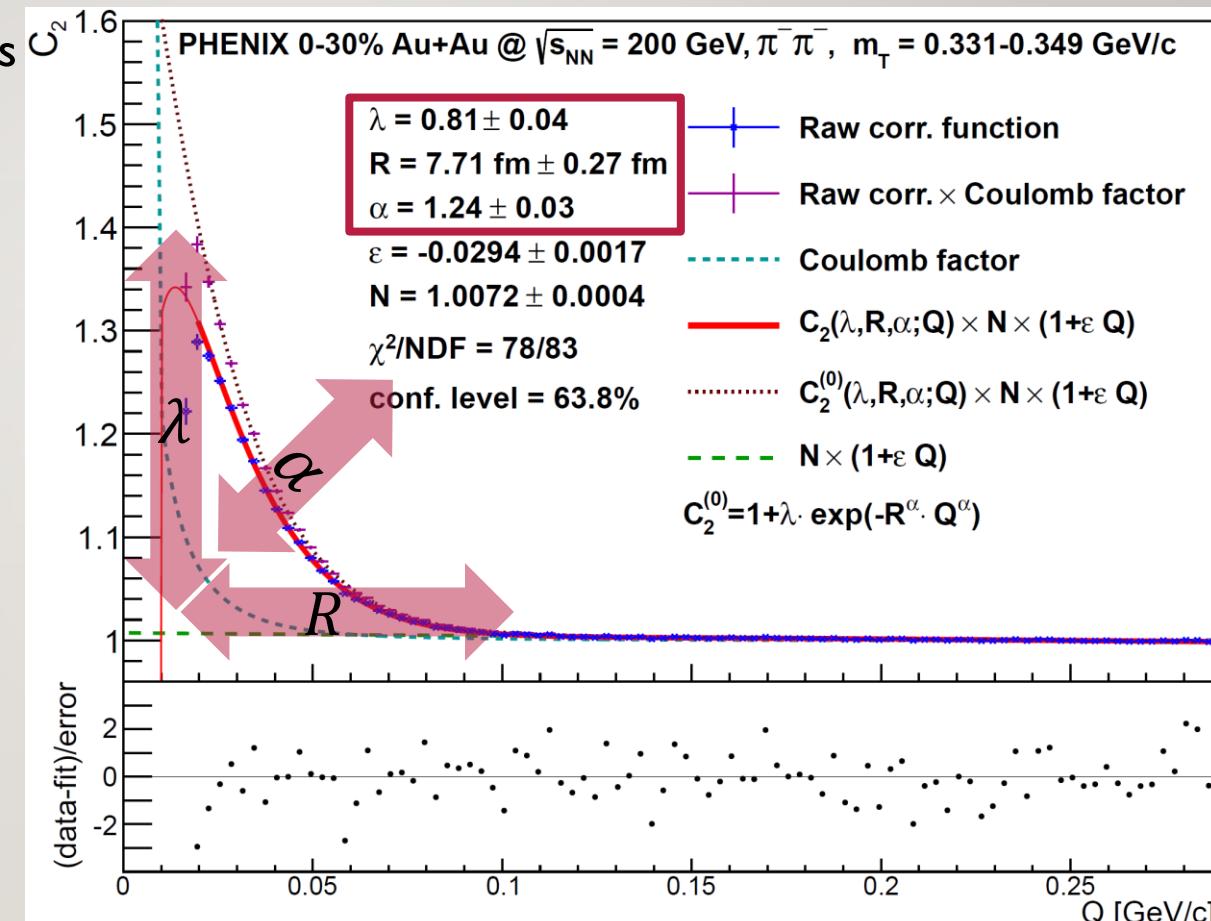
- QCD universality class  $\leftrightarrow$  3D Ising
  - Halasz et al., Phys.Rev.D58 (1998) 096007
  - Stephanov et al., Phys.Rev.Lett.81 (1998) 4816
- At the critical point:
  - Random field 3D Ising:  $\eta = 0.50 \pm 0.05$   
Rieger, Phys.Rev.B52 (1995) 6659
  - 3D Ising:  $\eta = 0.03631(3)$   
El-Showk et al., J.Stat.Phys.157 (4-5): 869
- Modulo finite size effects
- Distance from the critical point?
- Motivation for precise Lvy HBT!
- Change in  $\alpha_{\text{Lvy}}$  proximity of CEP?
- Non-static system, finite size effects may modify all this



4/17

# EXAMPLE $C_2(Q_{LCMS})$ CORRELATION FUNCTION

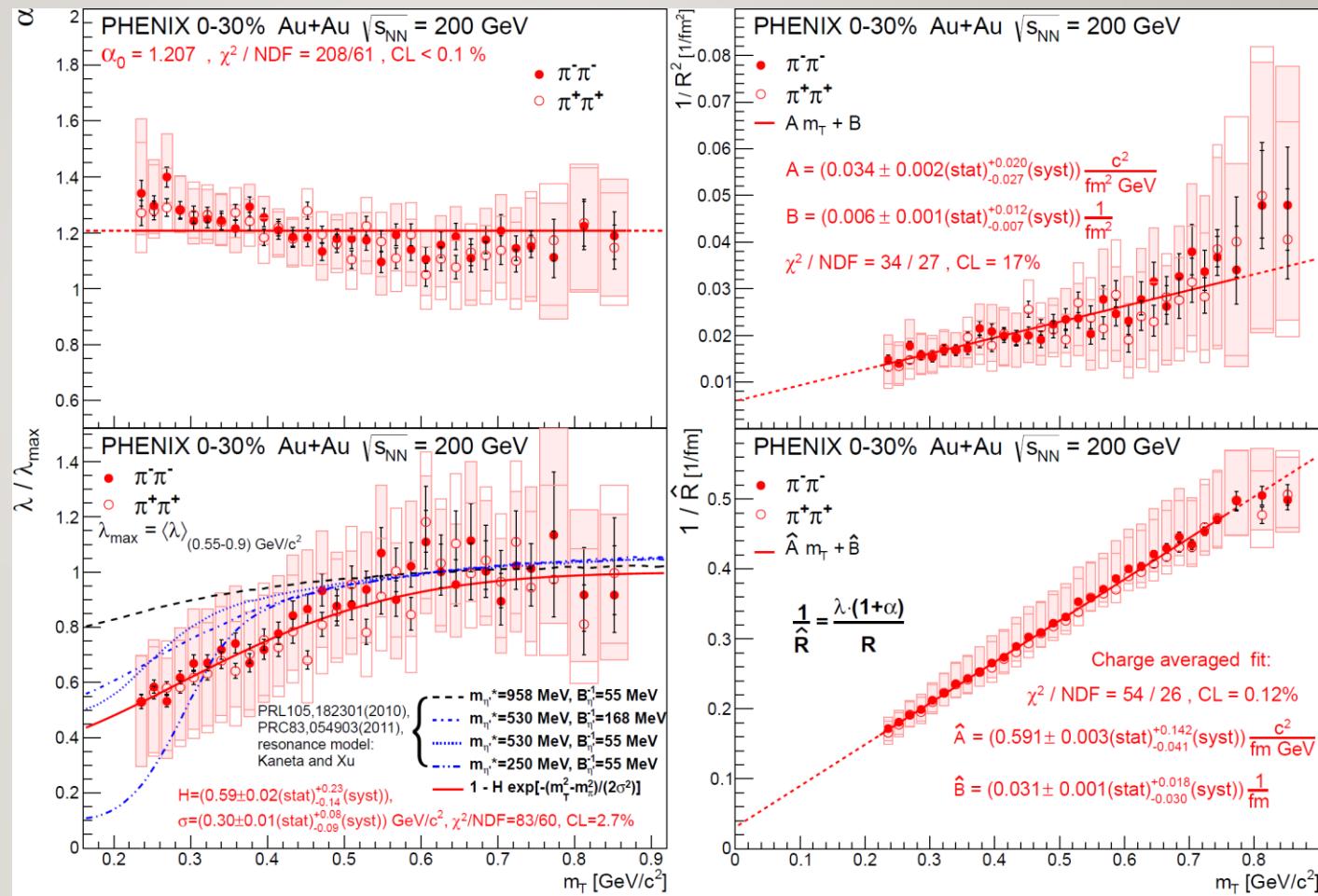
- Measured in 31  $m_T$  bins
- Fitted with Coulomb-incorporated function
- Coulomb-factor displayed separately
- All fits converged
- Confidence levels all acceptable
- $\chi$  values scatter around 0 properly
- Physical parameters:  $R, \lambda, \alpha$  measured versus pair  $m_T$



PHENIX, arXiv:1709.05649

# 5/17 PHYSICAL FIT PARAMETER RESULTS

- $\alpha$ : between 0.5 and 2.0
- $R$ : hydro scaling
- $\lambda$ : „hole”, compatible with mass modification
- $\hat{R}$ : new scaling variable



6/17

# LEVY HBT STATUS FROM 39 TO 200 GEV

- Bose-Einstein correlation functions measured from 39 to 200 GeV
- Levy fits yield statistically acceptable description
- Fine  $m_T$  binned Levy source parameters ( $R, \lambda, \alpha$ )
  - Nearly constant  $\alpha$ , away from 2, 1 and 0.5  $\leftrightarrow$  distance to CEP?
  - Linear scaling of  $I/R^2$  vs  $m_T$   $\leftrightarrow$  hydro?
  - Low- $m_T$  decrease in  $\lambda(m_T)$   $\leftrightarrow$  chiral restoration, in-medium  $\eta'$  mass?
- New, empirically found scaling parameter  $\hat{R} = \frac{R}{\lambda \cdot (1+\alpha)}$
- Centrality and collision energy dependence also explored
  - No  $\alpha$  decrease down to 39 GeV, non-monotonic  $\alpha$  vs  $N_{\text{part}}$  dependence
  - “Hole” in  $\lambda(m_T)$  present down to 39 GeV (c.f. SPS result without hole!)
  - No change in  $I/R^2$  and  $I/\hat{R}$  scaling with centrality and  $\sqrt{s_{NN}}$

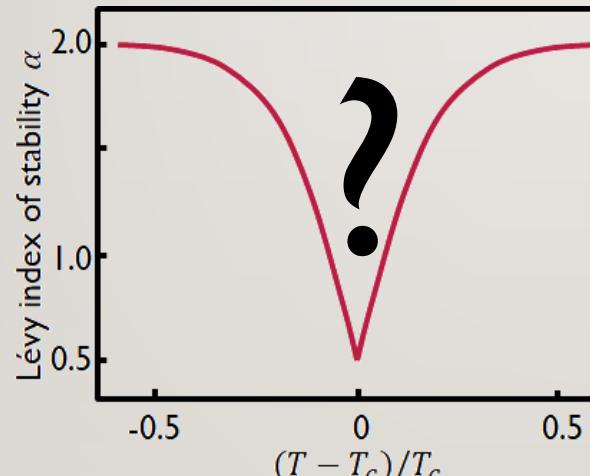
7 / 17

# OPEN QUESTIONS

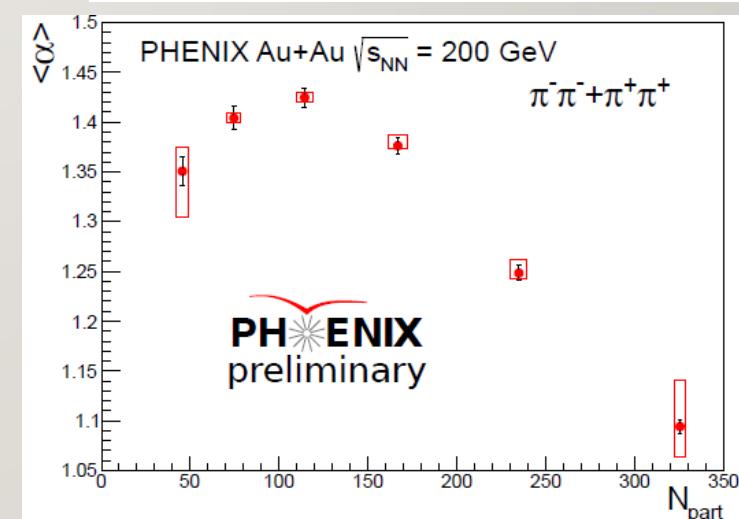
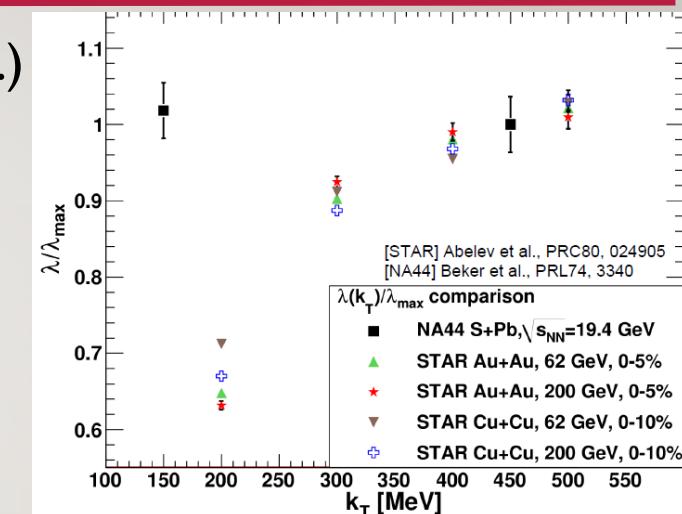
- Collision energy and centrality dependence?
  - Non-monotonicity in  $\alpha(\sqrt{s_{NN}})$  or  $\alpha(\text{centrality})$ ? Hole in  $\lambda(m_T)$  at low  $\sqrt{s_{NN}}$ ? Really due to  $\eta'$ ?
  - Lower energies (<39 GeV) currently analyzed, filtering  $\eta'$  decay products investigated
- How does the shape look in 3D (out-side-long)?
  - Is the Lvy exponent still around unity?
  - How are the radii modified as compared to Gaussian ones? The  $1/R^2 \sim mT$  scaling still valid?
  - $R_{\text{out}}^2 - R_{\text{side}}^2$  non-monotonicity modified if  $R$  is the Lvy scale?
- What about kaons?
  - What is the Lvy exponent for kaons?
  - Kaons have smaller total cross-section thus larger mean free path, heavier tail?
  - Does  $m_T$  scaling hold for Lvy scale  $R$ ?
- Correlation strength versus core-halo picture: are there other effects?
  - Three-particle correlations may show if coherence or other effects play a role
  - Other effects may also play a role (finite meson sizes, random field phase shift, etc)

# 8/17 COLL. ENERGY & CENTRALITY DEPENDENCE

- D. Kincses, S. Lks (supervisors: M. Cs. + T. Cs.)
- Hole in  $\lambda(m_T)$  at lower energies?
  - Filtering of  $\eta'$  decay products to be investigated, based on Eur. Phys. J.A (2011) 47: 76
- Non-monotonicity in  $\alpha$  vs centrality or  $s_{NN}$ ?

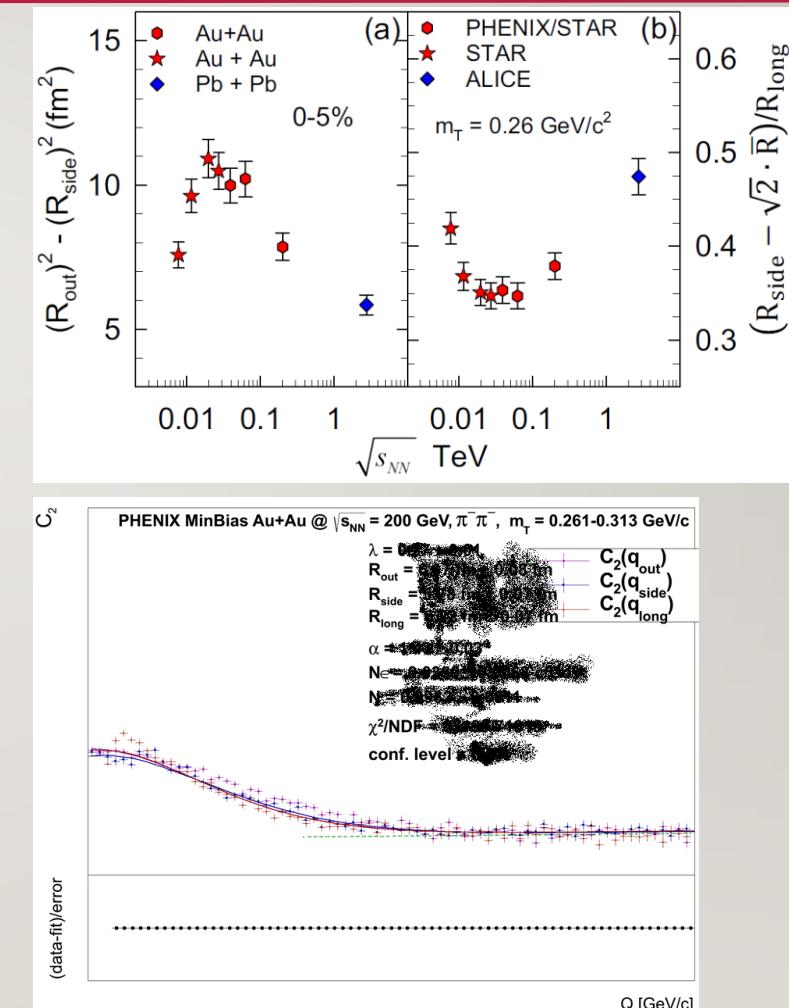


- New prelim. (15-27 GeV) and PPG(s) by mid 2018



# 9/17 3D ANALYSIS

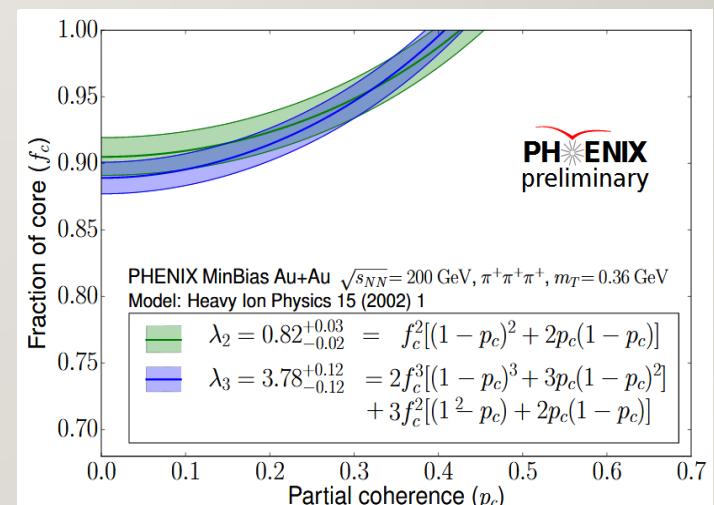
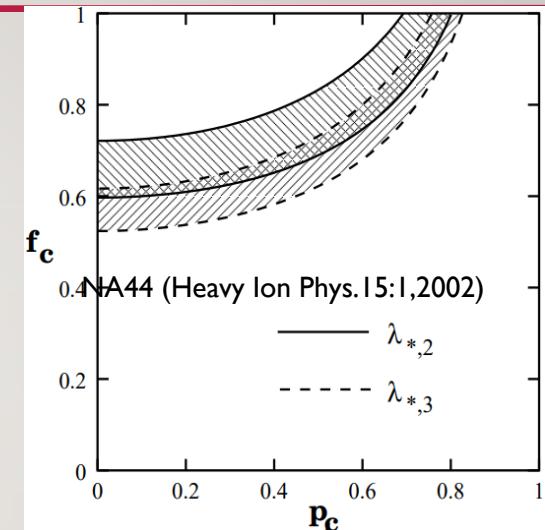
- B. Kurylis (supervisor: M. Cs. and D. K.)
- Lvy radii at 200 GeV:
  - $R_{\text{out}} \approx R_{\text{side}}$  still true for Lvy scales?
  - $1/R^2 \sim m_T$  scaling still true?
- How do Lvy radii change with energy?
  - Non-monotonicity still there in  $R_{\text{out}}^2 - R_{\text{side}}^2$ ?
  - $\alpha$  versus energy in 3D: same as for 1D?
- Analysis started with 200 GeV data
- Many issues still
  - Fits harder to visualize in 3D
  - Coulomb effect complicated in 3D
- Preliminary before QM18



10/17

# THREE-PION CORRELATIONS

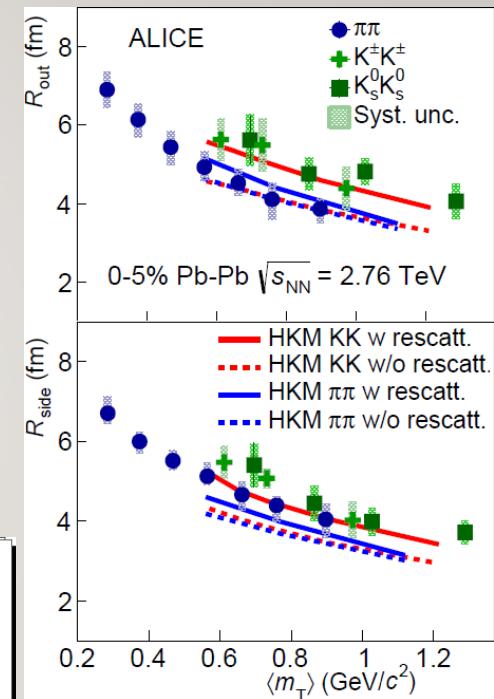
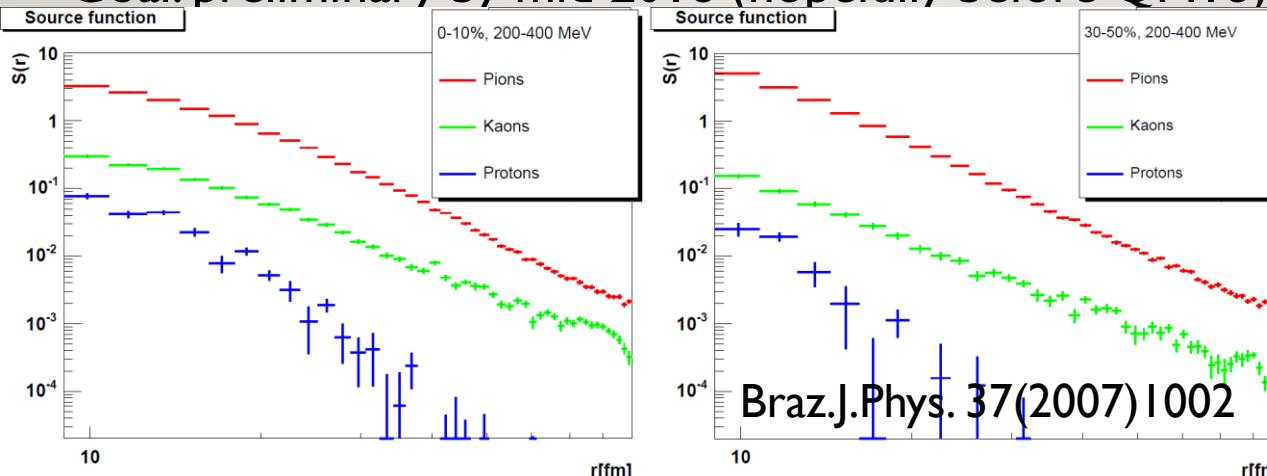
- J. Baskay & A. Bagoly (supervisor: M. Cs.)
- Recall:  $\lambda_2 = f_C^2$  only if no other effects!
- E.g. if there is partial coherence ( $p_C$ ):
  - $\lambda_2 = f_C^2[(1 - p_C)^2 + 2p_C(1 - p_C)]$
  - $\lambda_3 = 2f_C^3[(1 - p_C)^3 + 3p_C(1 - p_C)^2] + 3f_C^2[(1 - p_C)^2 + 2p_C(1 - p_C)]$
- Coherence effects:  
centrality dependent!
- Measure in 0-30% and maybe 40-70%?
- Finalize data
- PPG formation by mid 2018



II / 17

# KAON ANALYSIS

- D. Joti (supervisor: M. Nagy and M. Cs.)
- Kaon: PID possible, recalibrators by M. Nagy suitable
- Transverse mass scaling of Lvy HBT radii for kaons?
- HRC prediction for kaons:
  - Smaller cross-section, larger mean free path, heavier tail
- Goal: preliminary by mid 2018 (hopefully before QM18)



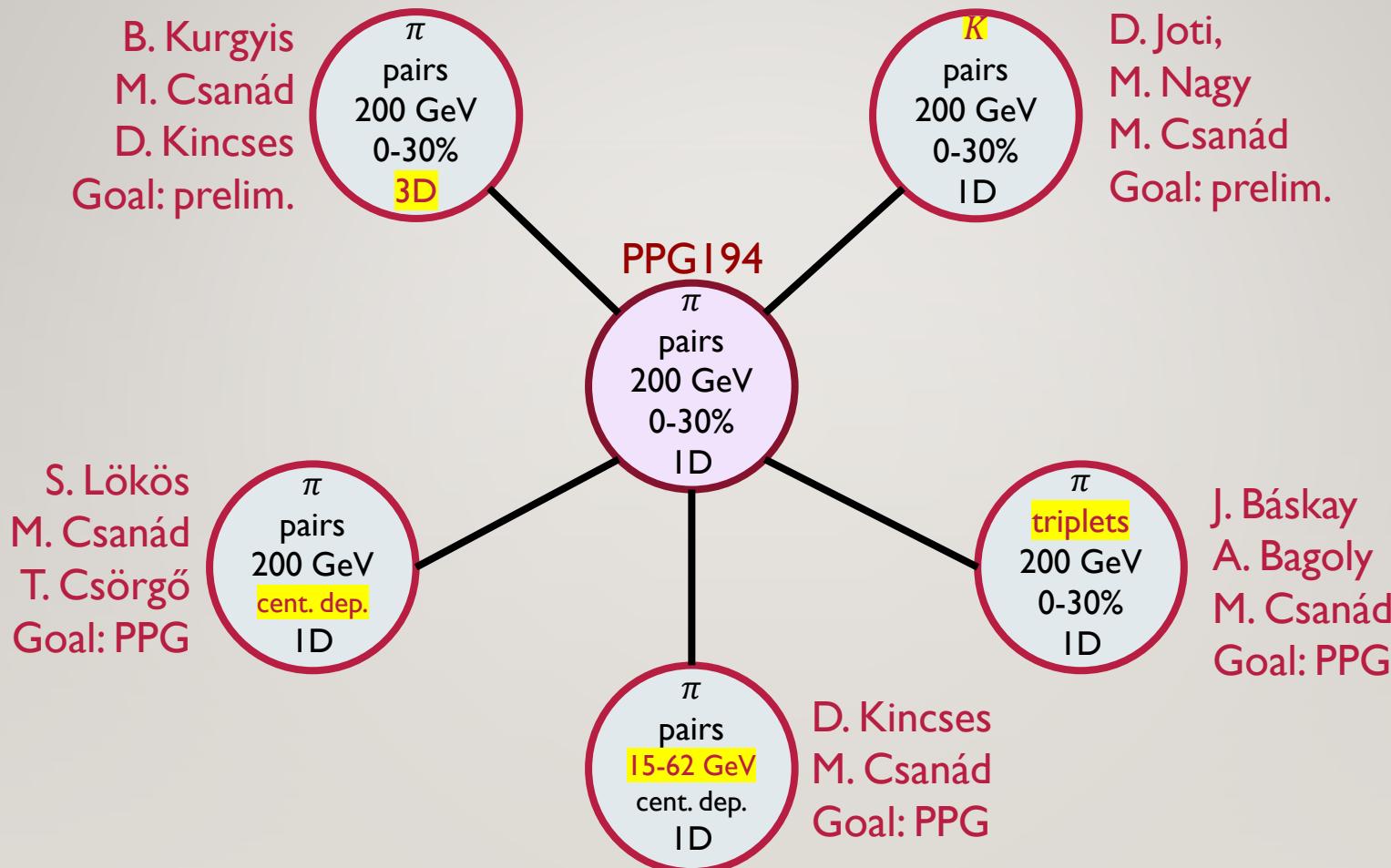
ALICE Coll.  
arXiv:1709.01731

# 12/17 PLANNING

- $\sqrt{s_{NN}}$  & centrality dependence: S. Lks, D. Kincses (M. Cs., T. Csrg)
  - Preliminary results available for 39-200 GeV, various centralities
  - Goal: preliminary for 15-27 GeV, PPG formation for final analysis (early 2018)
- How does the shape look in 3D: B. Kurylis (M. Cs., D. Kincses)
  - Analysis started, hope to reach preliminary in early 2018
- Kaon Lvy HBT: D. Joti (M. Nagy, M. Cs.)
  - Analysis started, hope to reach preliminary by mid 2018
- 3pion HBT: core-halo picture and coherence: J. Bskay and A. Bagoly (M. Cs.)
  - Preliminary obtained in early 2017, goal: PPG formation by mid 2018
- Additional phenomenological work needed: refinements for Coulomb
  - Work ongoing by B. Gazdag (not PHENIX-related, supervised by M. Nagy and M. Cs.)

13/17

# ONE-PAGE SUMMARY OF PHENIX HBT PLANS





14  
/17

# NA61 AND CMS LEVY HBT PLANS

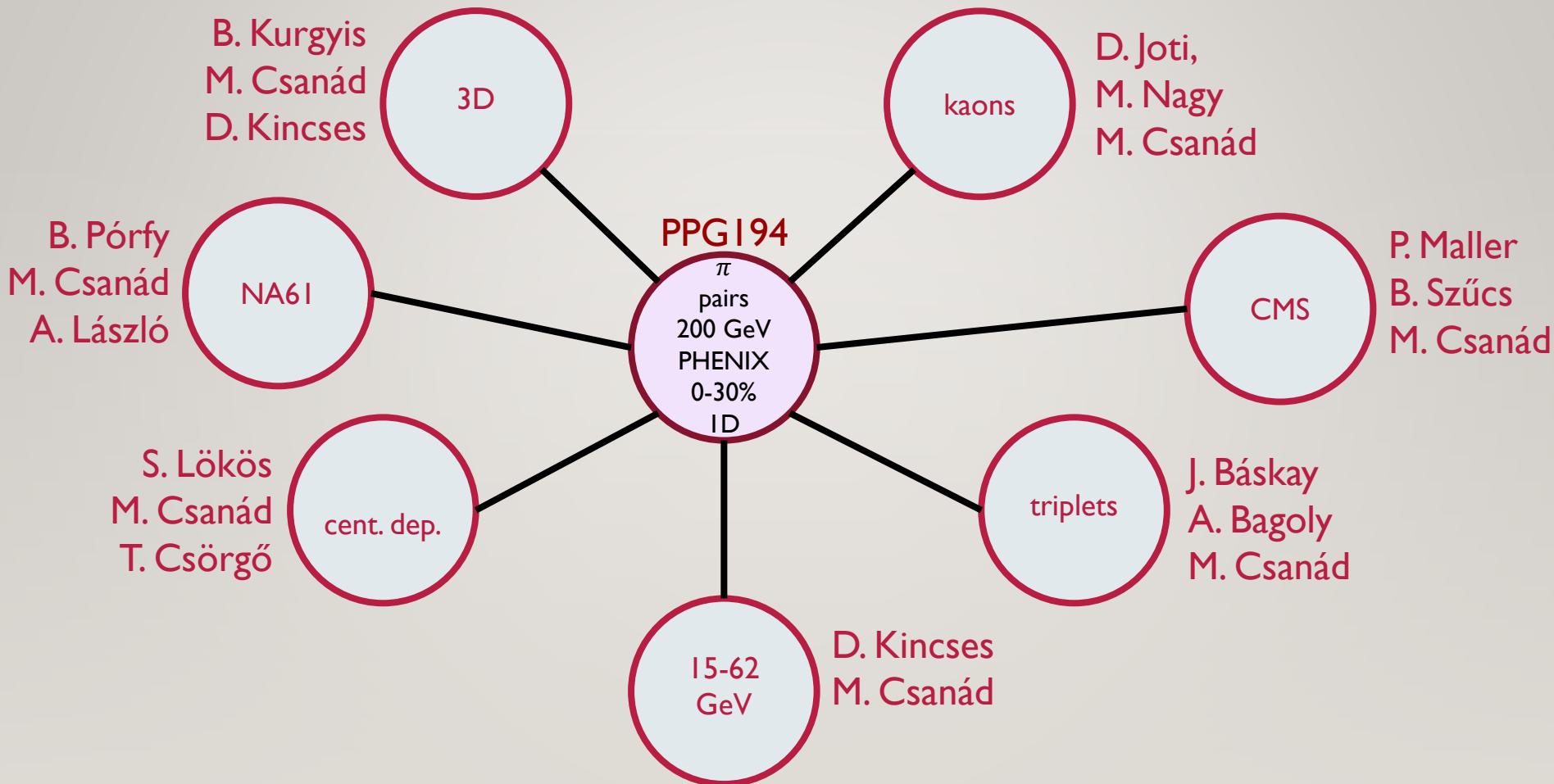
## NA61

- First step is 3D Levy analysis for a well calibrated energy and system
- Main analyzer: B. Porf y (supervisors: M. Cs. and A. Laszl)

## CMS

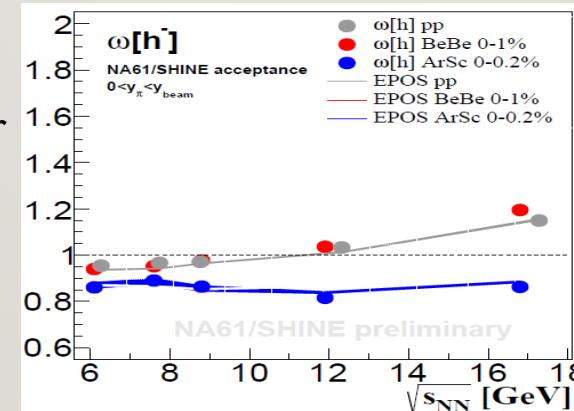
- First step is 1D or 3D Levy analysis for PbPb
- Two- and three-particle correlations also to be analyzed
- Main analyzers: B. Szucs and P. Maller (supervisor: M. Cs. and ???)
- Proton-proton analysis by Sandra Padula: under finalization, no real Levy or dip analysis

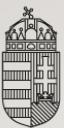
# 15<sub>/17</sub> SUMMARY OF SPS-RHIC-LHC HBT PLANS



# 16/17 OTHER NA61 RESULTS (FOR THE FK GRANT)

- FTPC system operational (pA spectra for NA61 neutrino analysis)
- 17.3 GeV pp and pPb analysis ongoing
  - Centrality dependent midrapidity  $p_T$  spectra
  - Model independent  $R_{AA}$  analysis performed
  - Main analyzer: K. Mrton (PhD topic, superv.: A. L.)
- Xe+La energy scan data taking underway
  - Large signal expected if there is a critical point
  - Scaled variance  $\omega$
  - No anomaly so far





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17

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December 4-8., Budapest, Hungary

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<http://zimanyischool.kfki.hu/17>





# 18 BACKUP

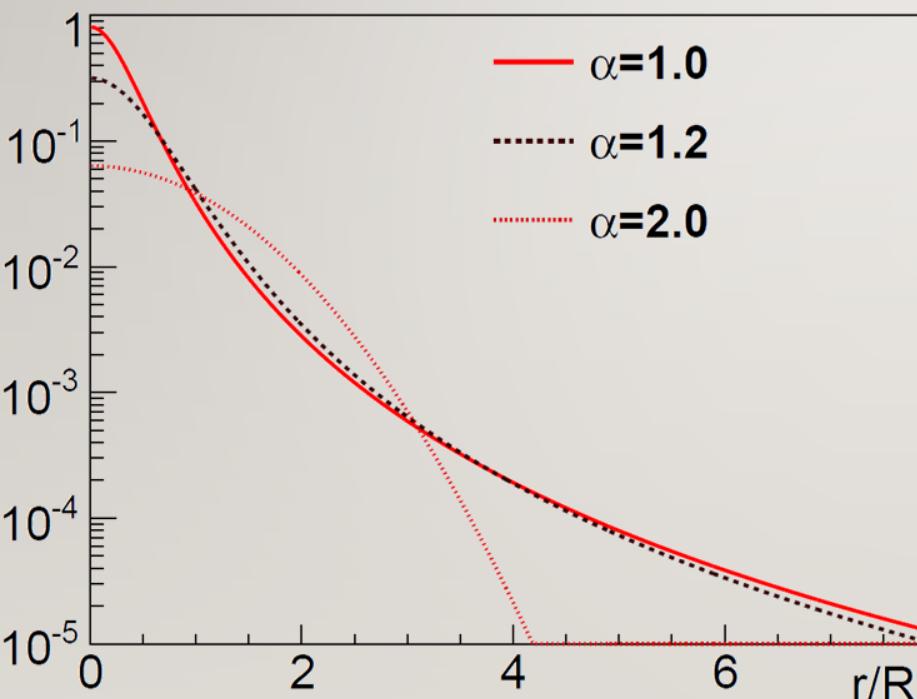
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19/17

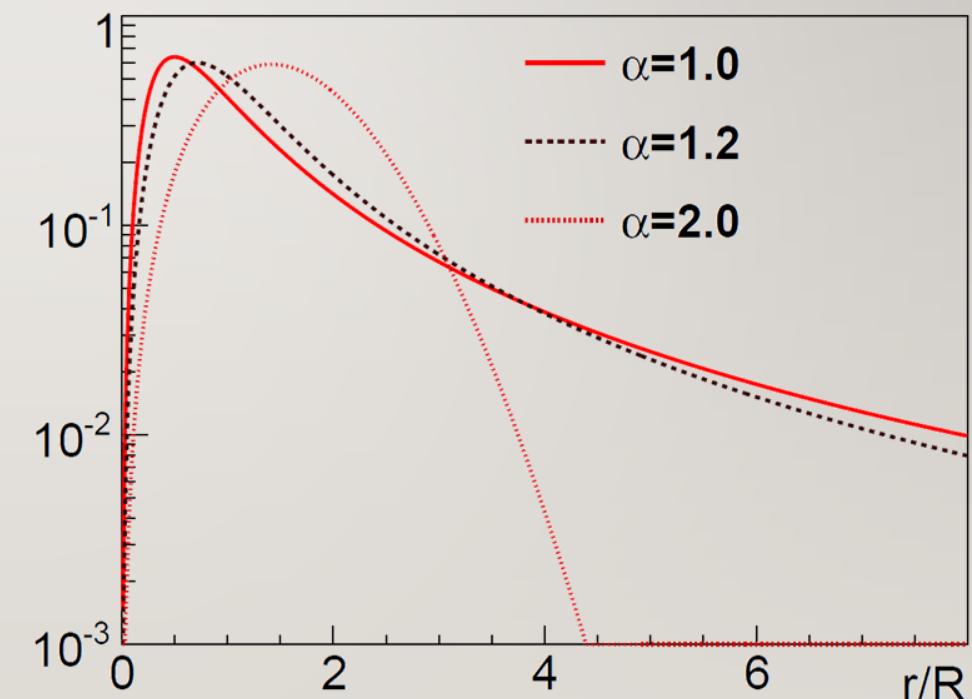
# LEVY VERSUS GAUSS VERSUS EXPONENTIAL

- No tail if  $\alpha = 2$ , power law if  $\alpha < 2$

$$R^3 S_{\text{core}}(r)$$



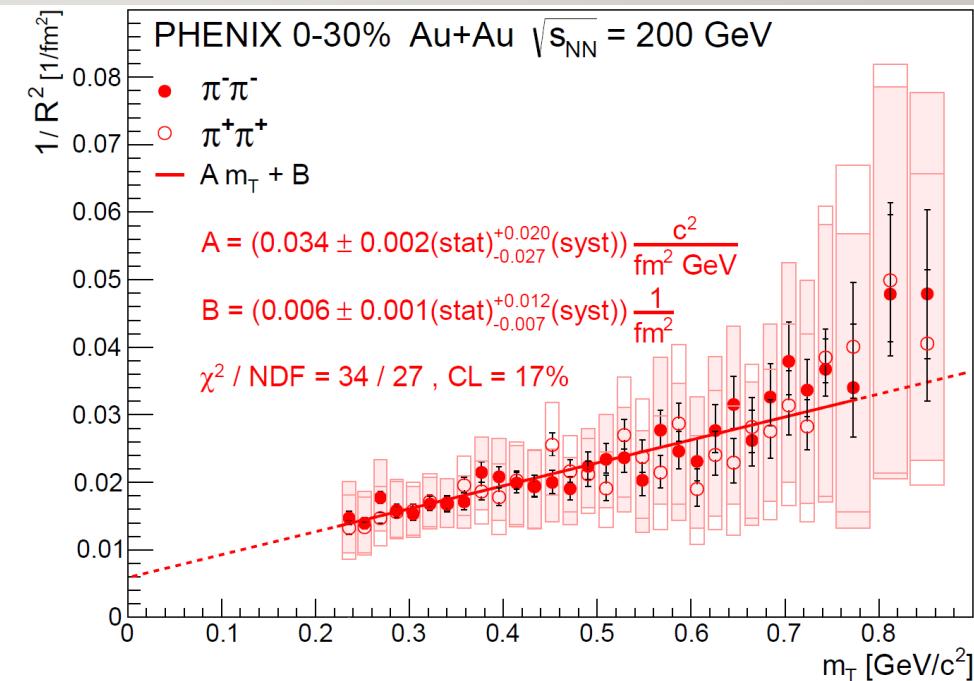
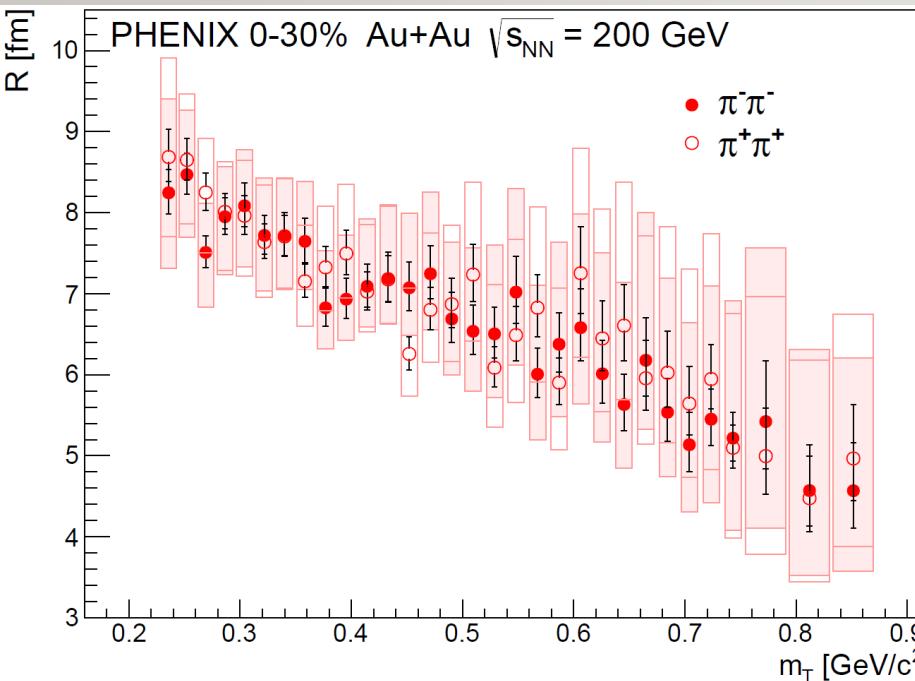
$$R4\pi r^2 S_{\text{core}}(r)$$



# 20<sub>/17</sub> 200 GEV LEVY HBT ANALYSIS

- Dataset used for the analysis:
  - Run-10, Au+Au,  $\sqrt{s_{NN}} = 200 \text{ GeV}$ ,  $7.3 \cdot 10^9$  events
  - Additional offline requirements: vertex less than 30 cm away from center
  - Particle identification:
    - time-of-flight data from PbSc East/West, TOF East/West, momentum, flight length
    - $2\sigma$  cuts on  $m^2$  distribution
  - Single track cuts:  $2\sigma$  matching cuts in TOF & PbSc for pions
  - Pair-cuts:
    - A random member of pairs assoc. with hits on same tower were removed
    - customary shaped cuts in  $\Delta\phi - \Delta z$  plane for Drift Chamber, PbSc East/West, TOF East/West
- ID corr. func. as a function of  $|k|_{LCMS}$  in various  $m_T$  bins
  - $k_{LCMS}$  is 3-momentum difference in longitudinal co-moving system
  - Levy fits for 31  $m_T$  bins ( $0.228 < m_T < 0.871 \text{ GeV}/c$ ) with Coulomb effect

# 21 / 17 LEVY SCALE PARAMETER R



- Similar decreasing trend as Gaussian HBT radii
- Hydro behavior not invalid
- The linear scaling of  $1/R^2$ , breaks for high  $m_T$

22/17

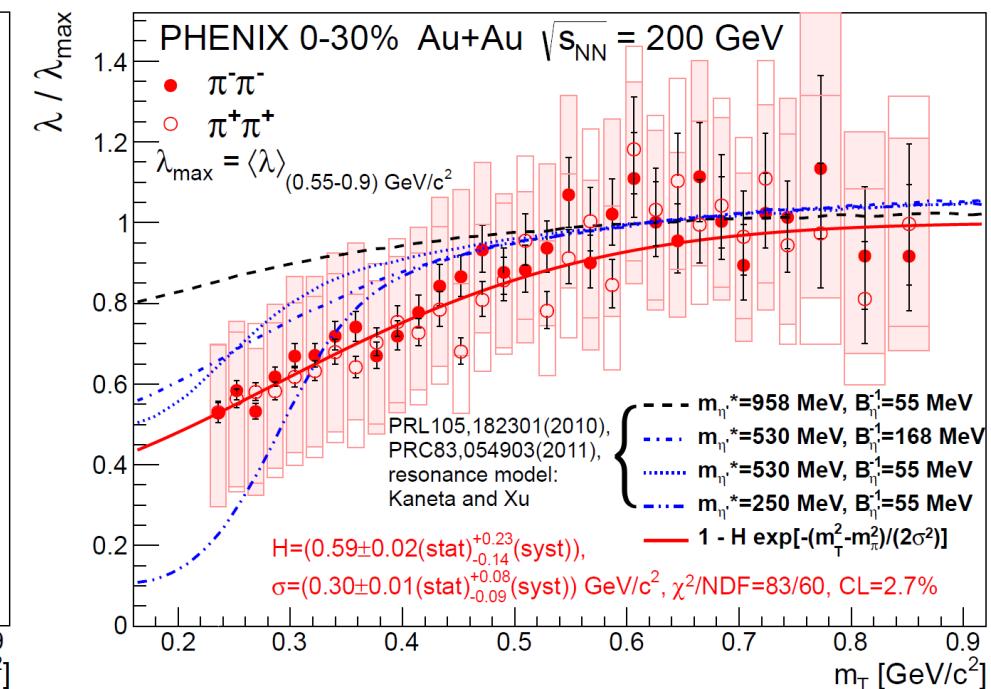
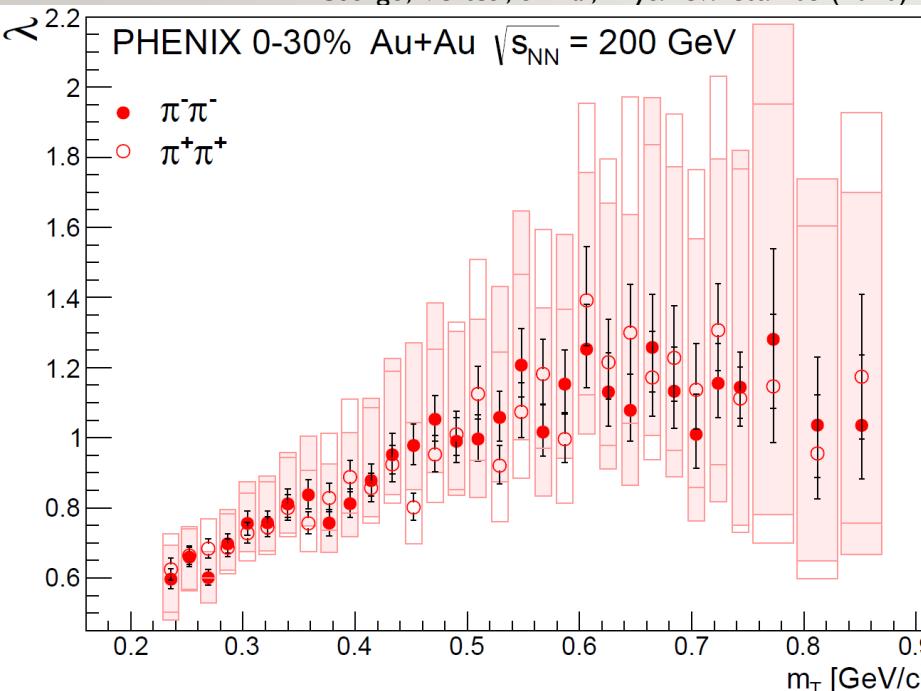
# CORRELATION STRENGTH $\lambda(m_T)$

- $\lambda(m_T)$ : core/(core+halo) fraction, may be connected to chiral restoration
  - Decreased  $\eta'$  mass  $\rightarrow \eta'$  enhancement  $\rightarrow$  halo enhancement
  - Kinematics:  $\eta'$  decay pions will have low  $m_T$   $\rightarrow$  decreased  $\lambda(m_T)$  at low  $m_T$
  - Compatibility with unmodified in-medium  $\eta'$  mass?

Kapusta, Kharzeev, McLerran, Phys.Rev. D53 (1996) 5028, hep-ph/9507343

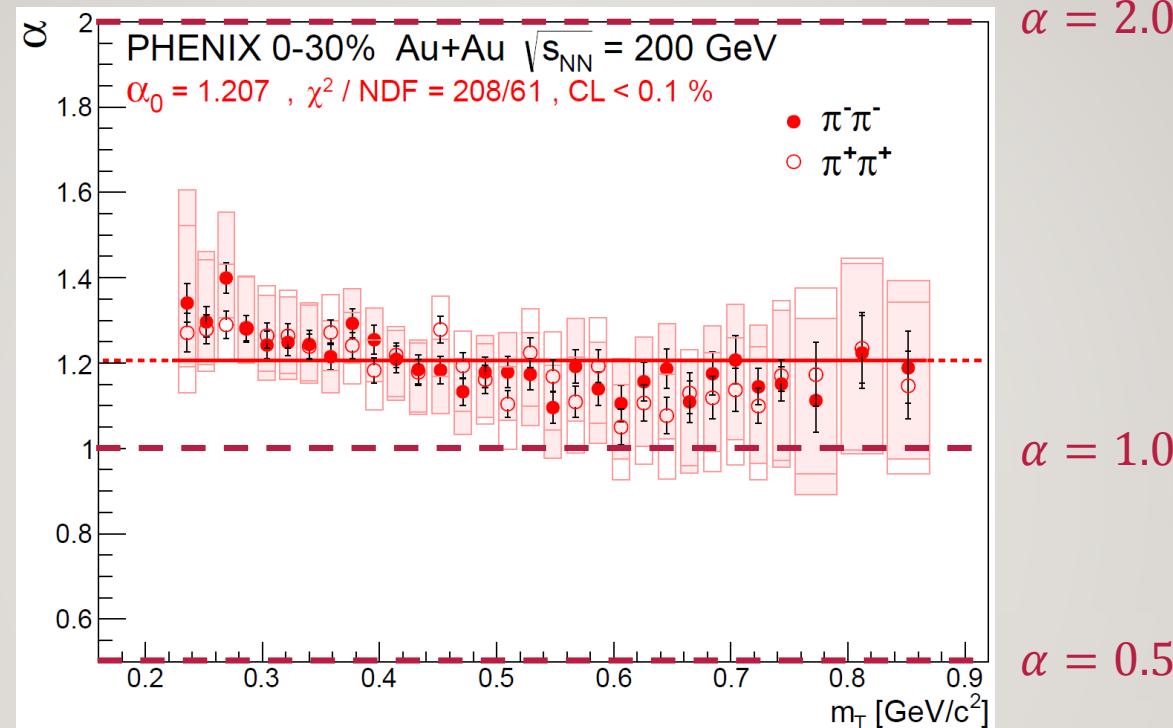
Vance, Csorg, Kharzeev, Phys.Rev.Lett. 81 (1998) 2205, nucl-th/9802074

Csorg, Vrtesi, Sziklai, Phys.Rev.Lett. 105 (2010) 182301, arXiv:0912.5526



23/17

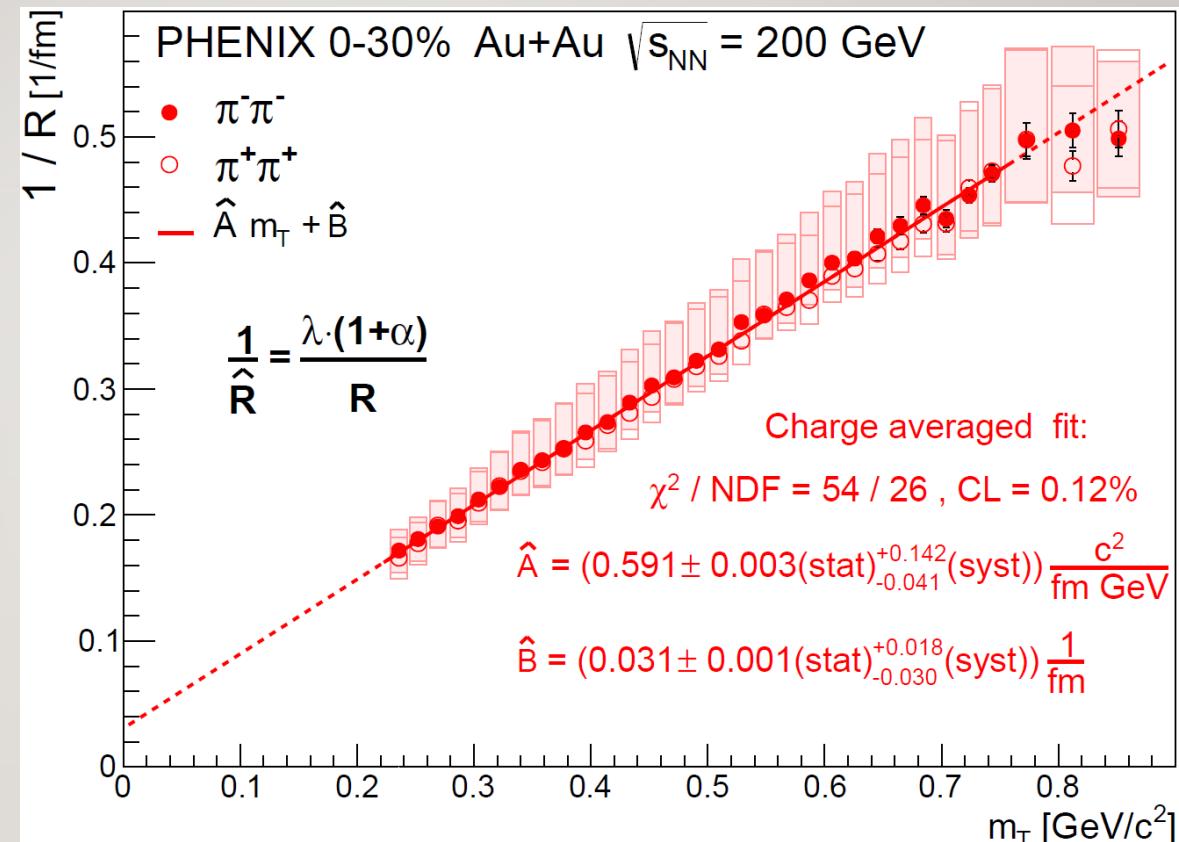
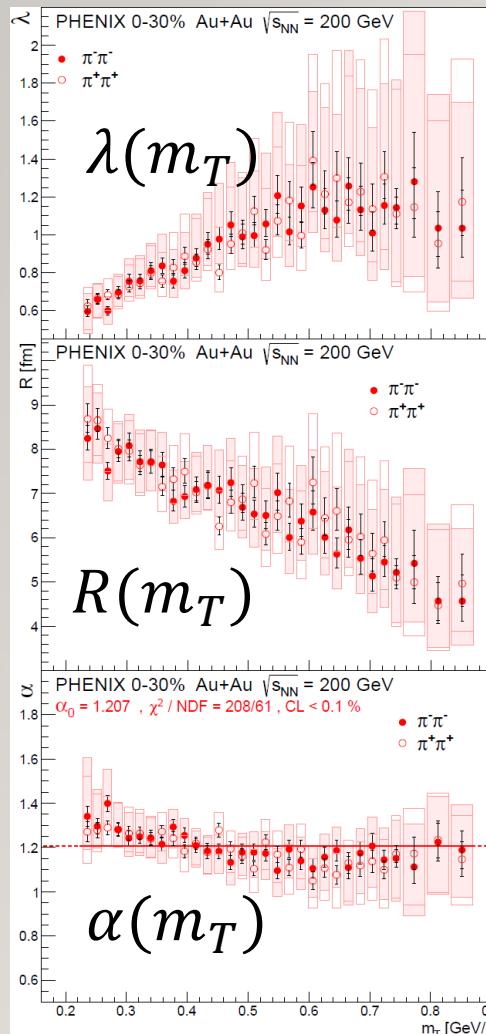
# LEVY EXPONENT $\alpha$



- Measured value far from Gaussian ( $\alpha = 2$ ), inconsistent with expo. ( $\alpha = 1$ )
- Also far from the random field 3D Ising value at CEP ( $\alpha = 0.5$ )
- More or less constant (at least within systematic uncertainties)
- Trend observable with statistical uncertainties only

24<sub>/17</sub>

# NEWLY DISCOVERED SCALING PARAMETER $\widehat{R}$

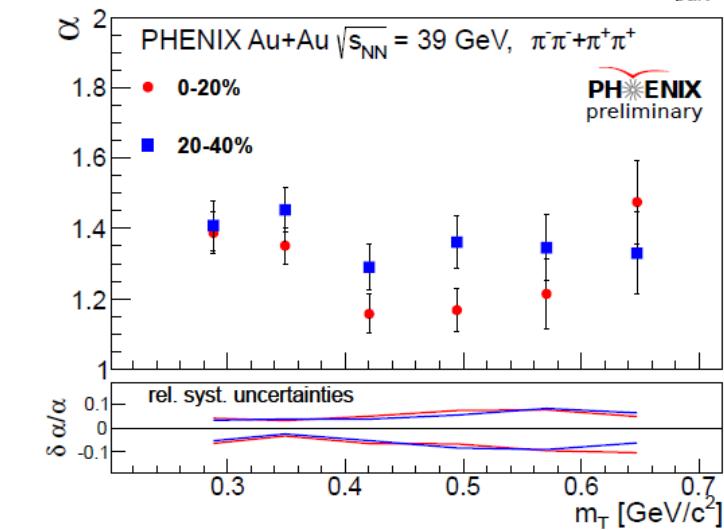
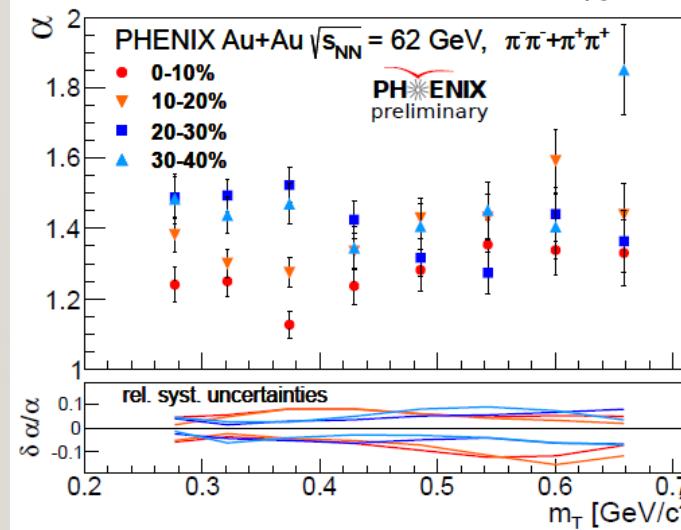
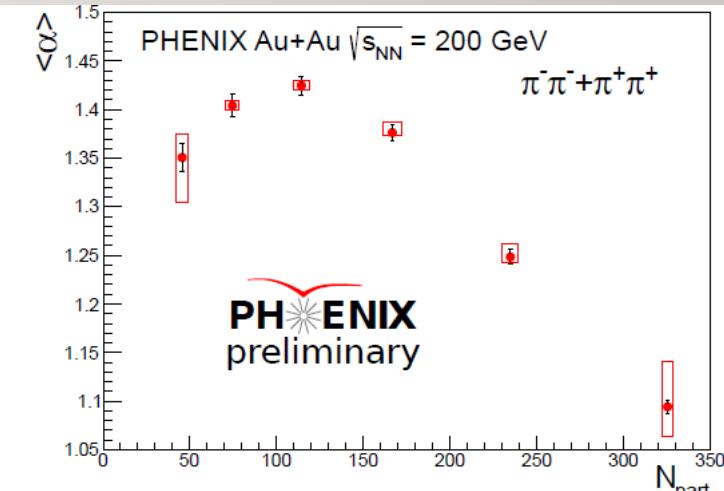
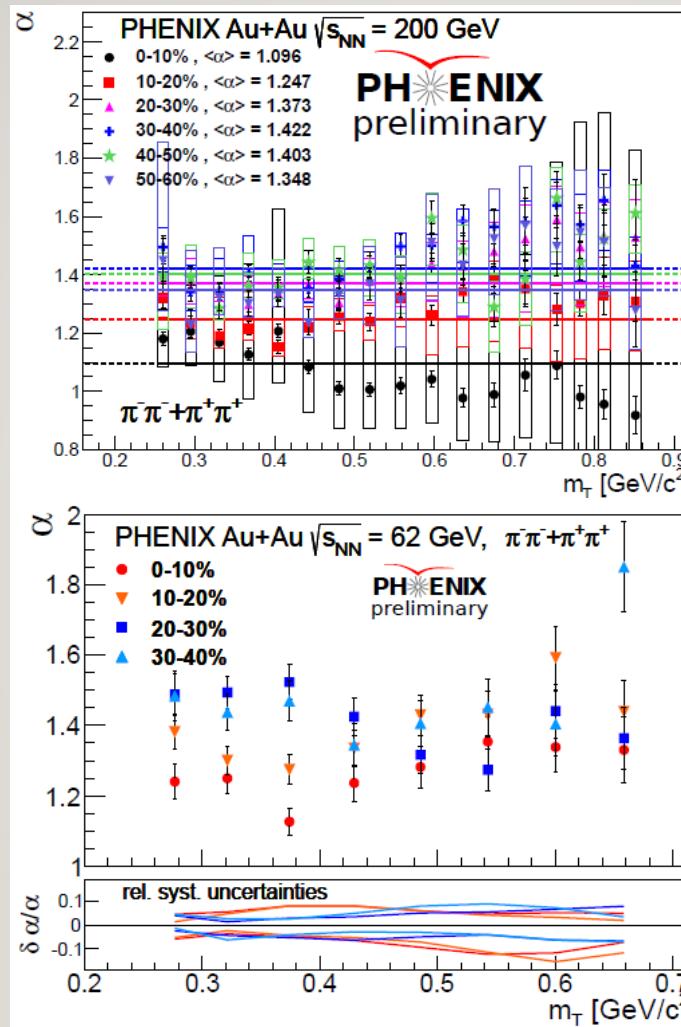


- Empirically found scaling parameter
- Linear in  $m_T$
- Physical interpretation: open question

25/17

# LEVY EXPONENT $\alpha$ AT 200 GEV

- Slightly non-monotonic vs  $m_T$
- Non-monotonic vs  $N_{\text{part}}$
- No significant change vs  $\sqrt{s_{\text{NN}}}$



rel. syst. uncertainties

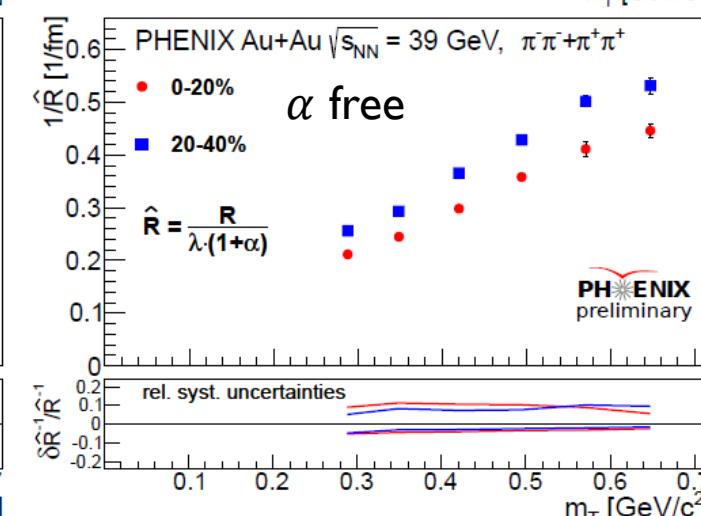
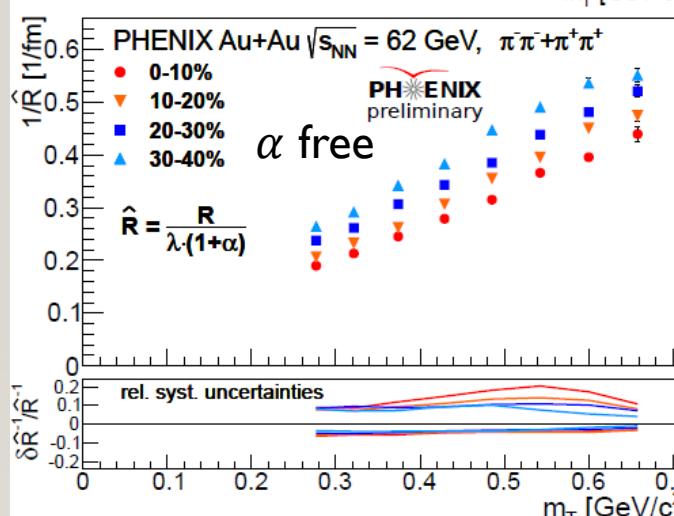
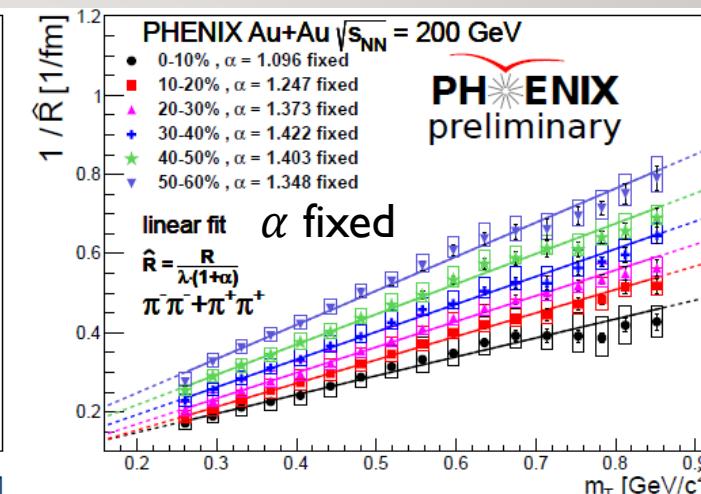
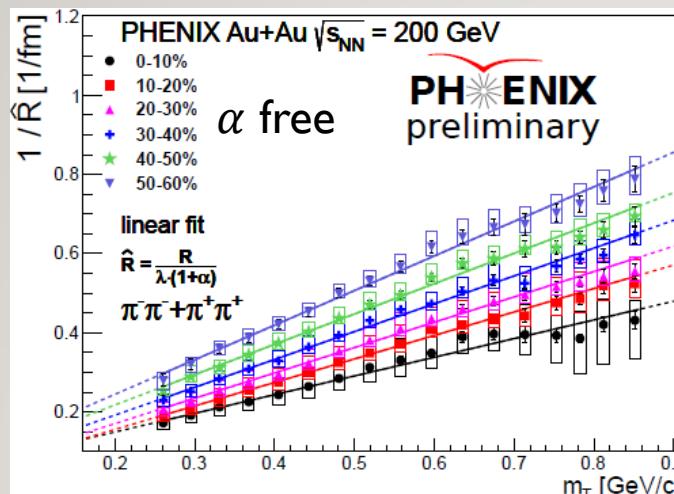
 $\delta \alpha/\alpha$  vs  $m_T$  [ $\text{GeV}/c^2$ ]

rel. syst. uncertainties

 $\delta \alpha/\alpha$  vs  $m_T$  [ $\text{GeV}/c^2$ ]

26/17

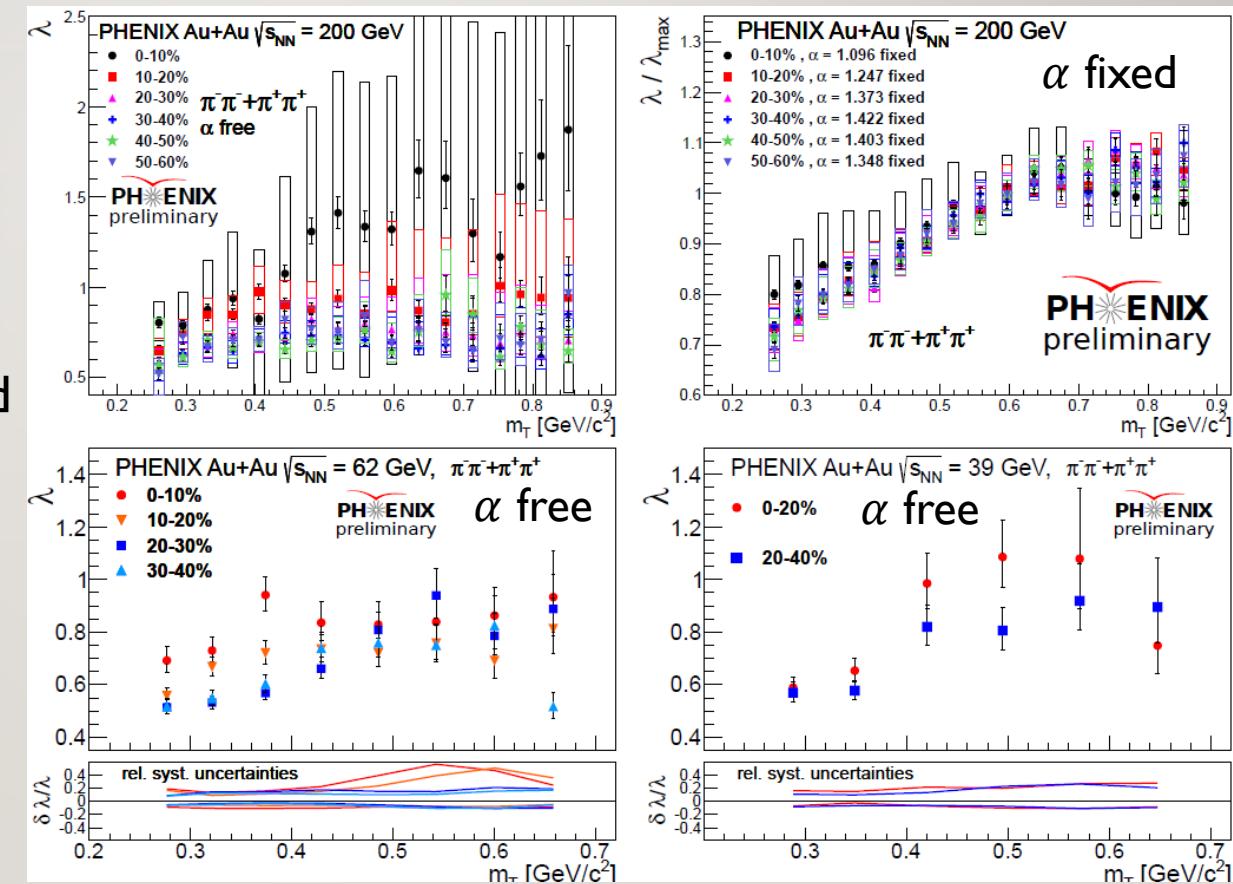
# $\hat{R}$ SCALING: ALL ENERGIES AND CENTRALITIES



27/17

# HOLE IN $\lambda(m_T)$ : ALL INVESTIGATED ENERGIES

- Hole apparent for  $\sqrt{s_{NN}} \geq 39$  GeV, all centralities
- Due to reduced  $\eta'$  mass?
- Sign for chiral restoration?
- To be cross-checked with photons, dileptons, etc.



28/17

# LEVY R: SIMILAR HYDRO TRENDS FOR ALL CASES

