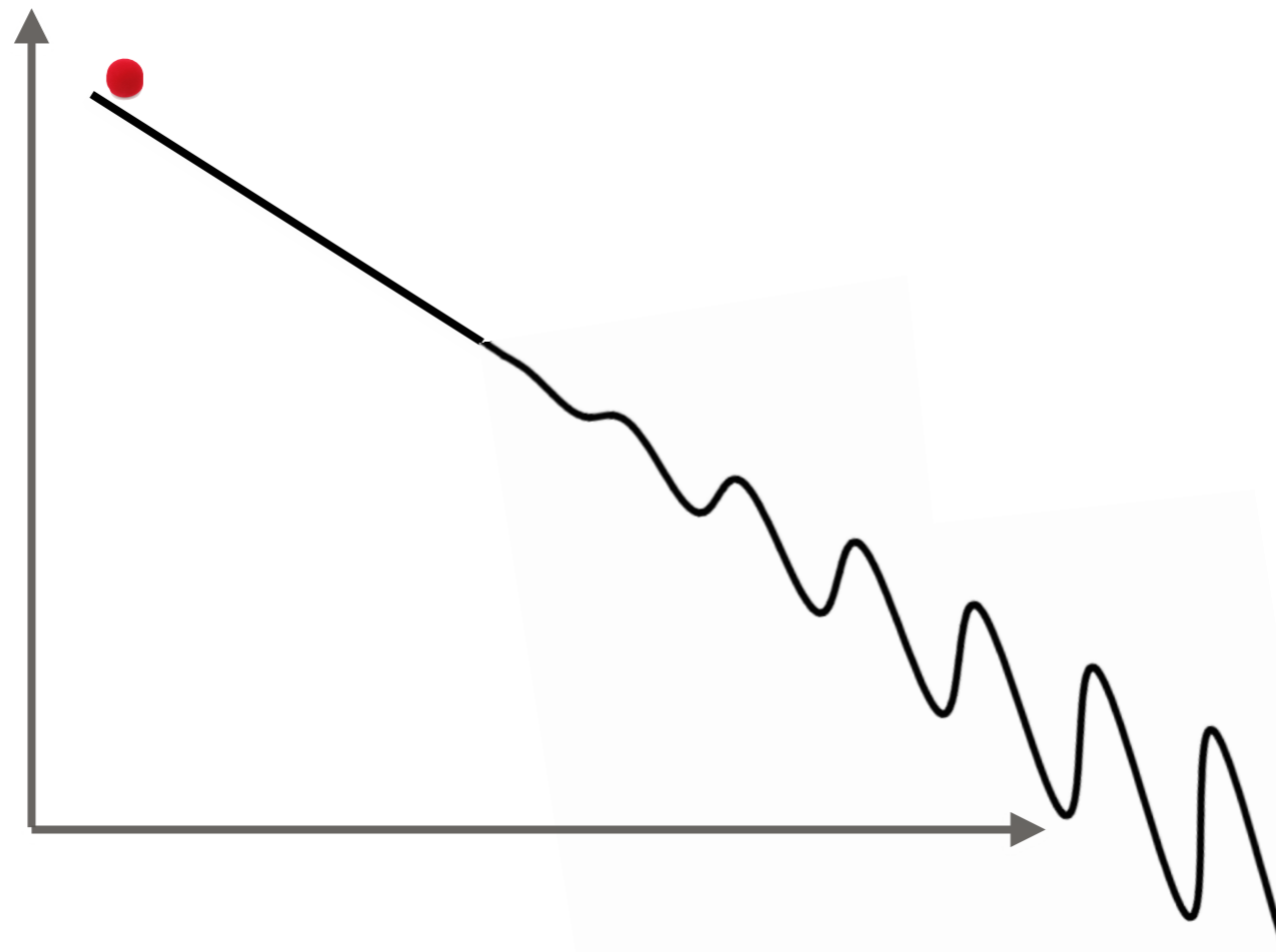


Relaxions



Institute for Advanced Study



Diego Redigolo

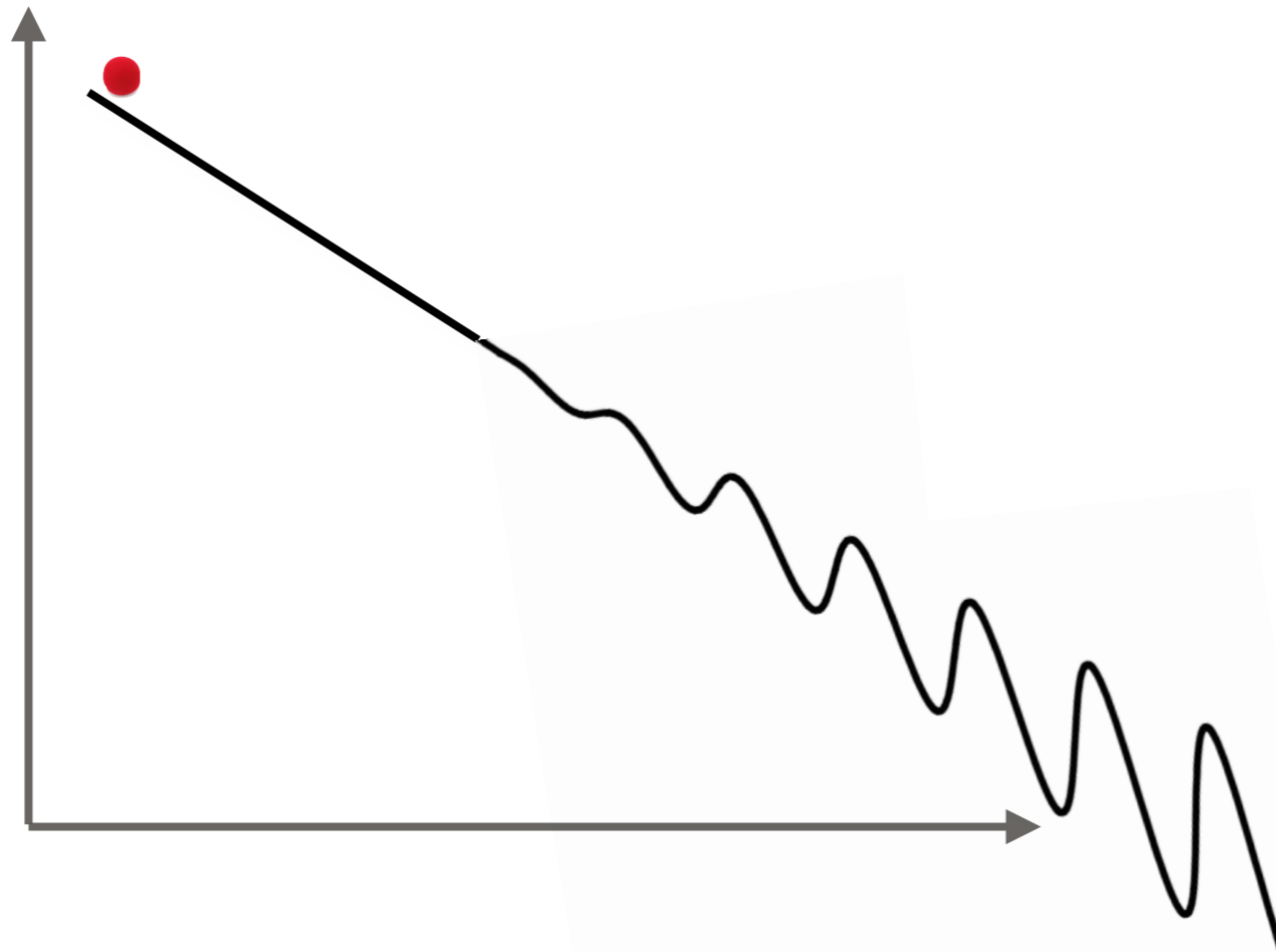
2/10/2018



Institute for Advanced Study



New playground for Naturalness



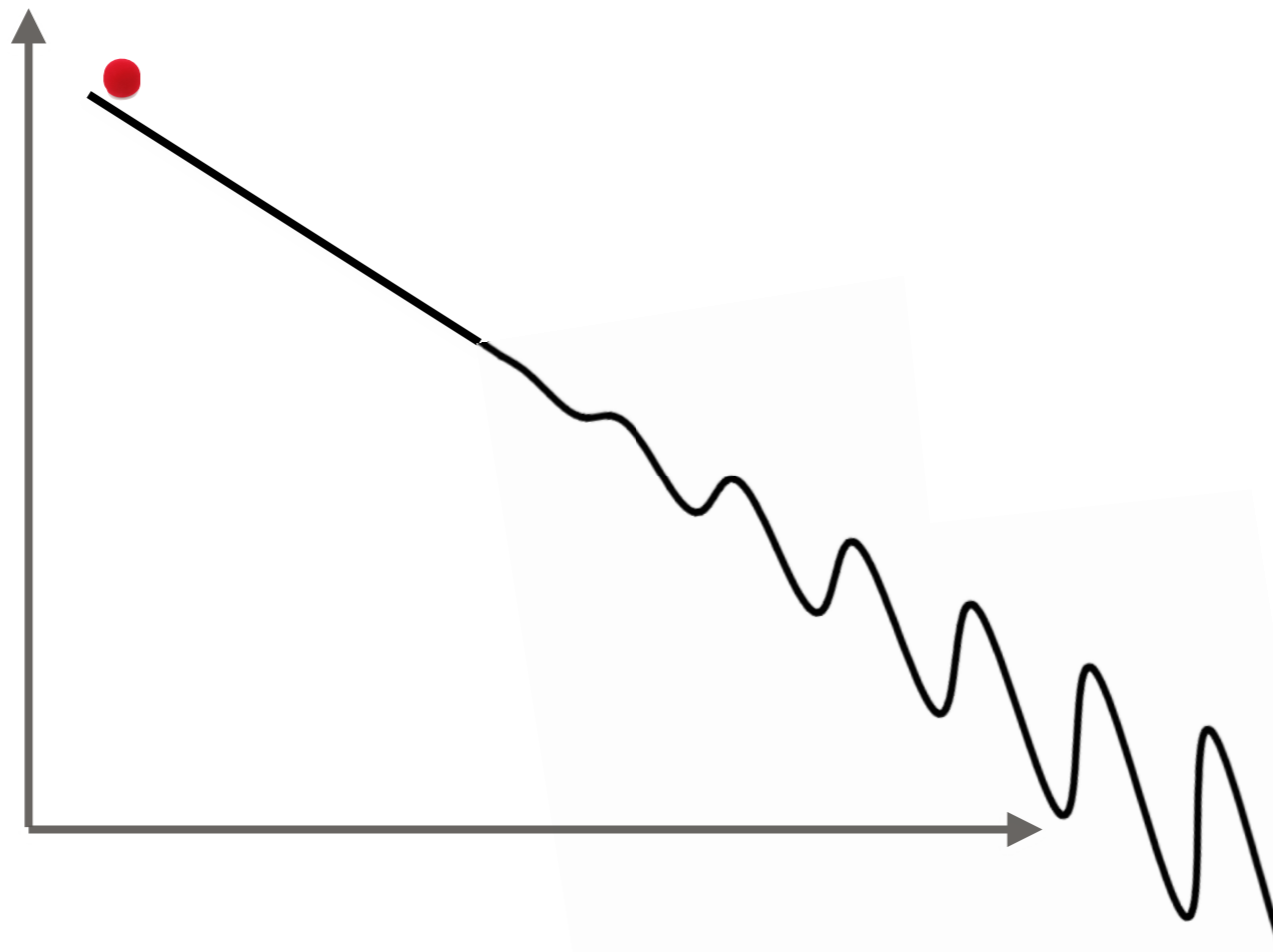
**new
theoretical
challenges**



**new
phenomenological
probes**

New playground for Naturalness

going on from David's talk



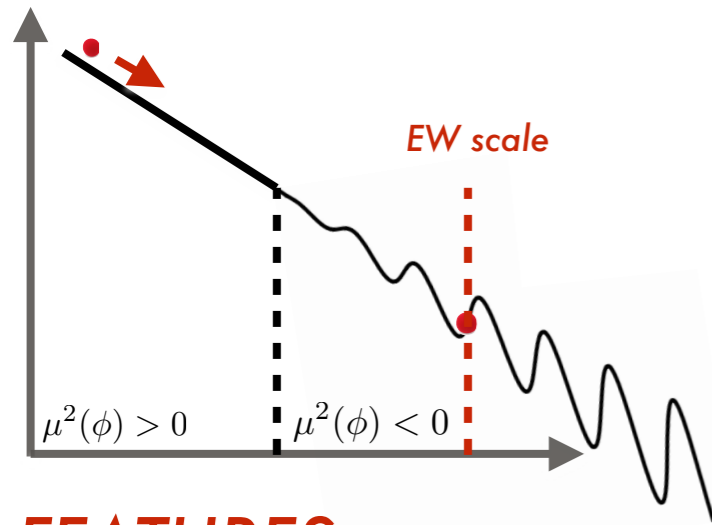
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The simplest version

(Graham, Kaplan & Rajendran '15)

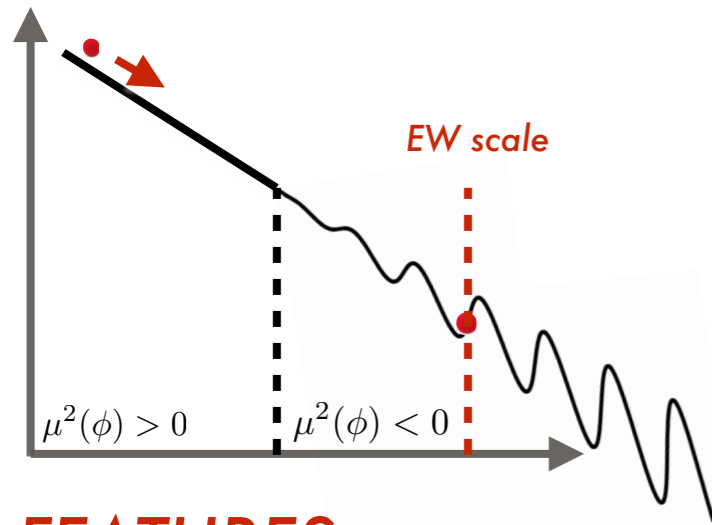


FEATURES:

- *classical rolling + Hubble friction set the Cosmo*
- *EWSB triggers potential barriers*
- *stopping point: Ratio of scales = Ratio of vevs*
- *abelian symmetry with $O(1)$ and $(1/3)^N$ charges*

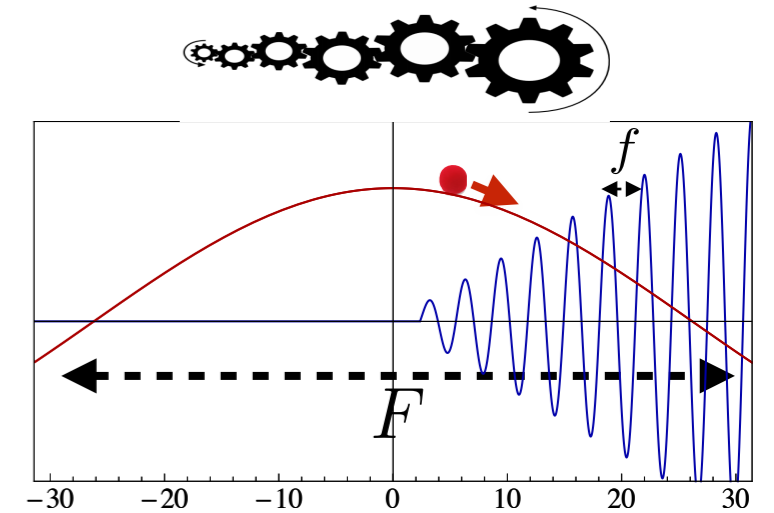
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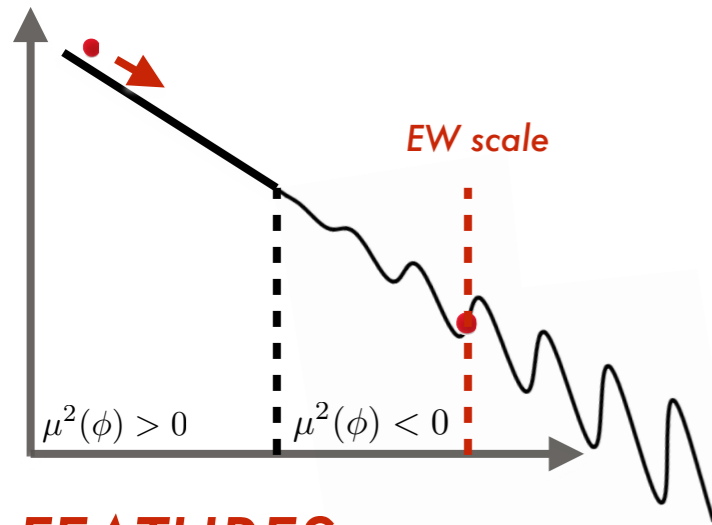
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$$\frac{\Lambda_{\text{UV}}^4}{F} \sin \frac{\phi_0}{F} = \frac{\Lambda_{\text{wig}}^4}{f} \sin \frac{\phi_0}{f}$$

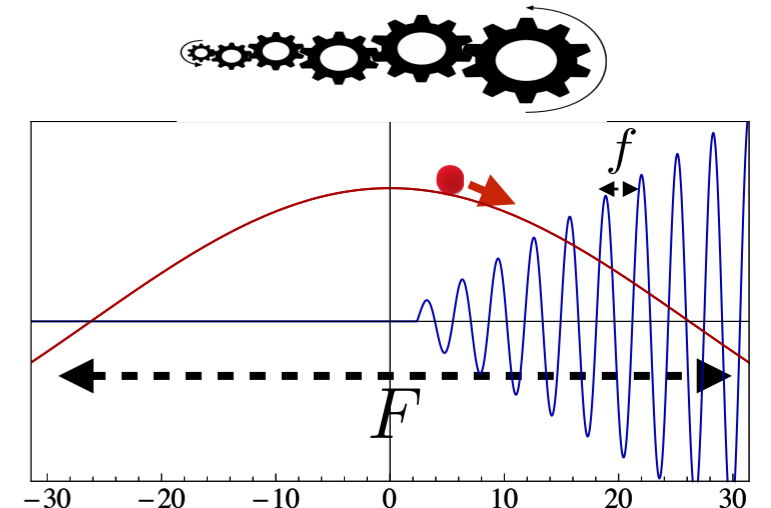
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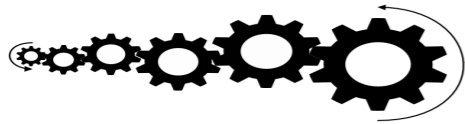
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CONSEQUENCES:

- works for generic initial conditions
- CP violating phase \longleftrightarrow Higgs-Relaxion mixing
- Lots of e-folds \longleftrightarrow Transplanckian field excursion

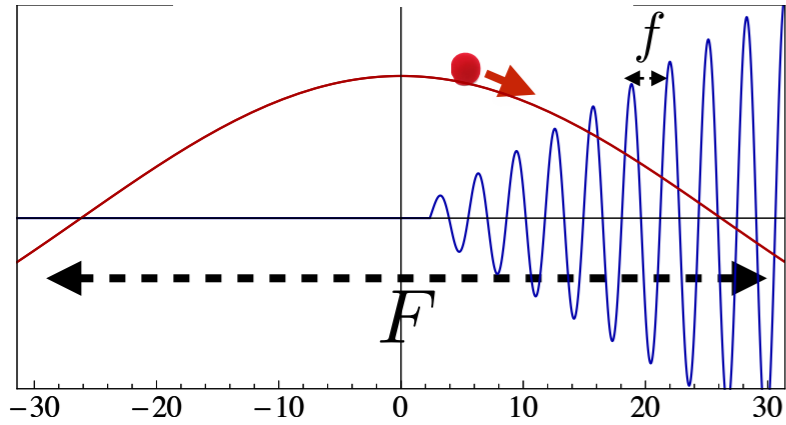
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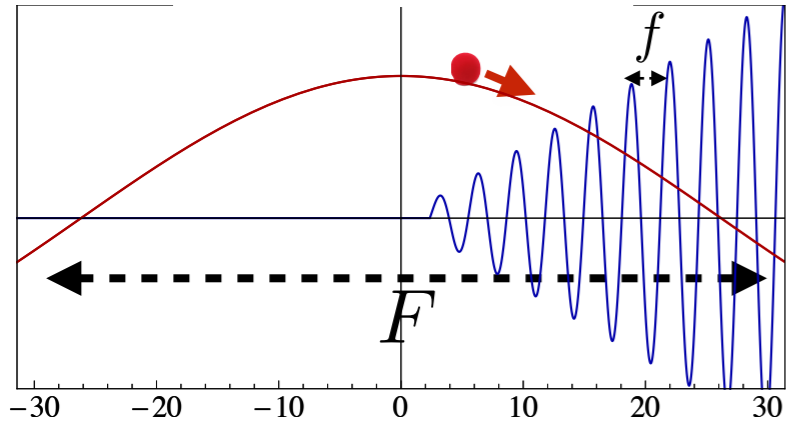
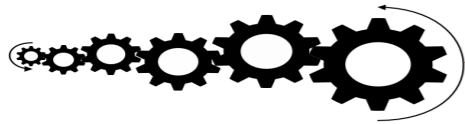


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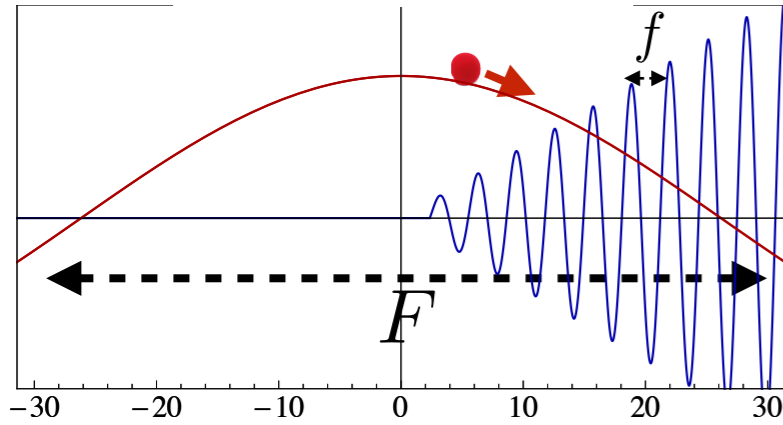
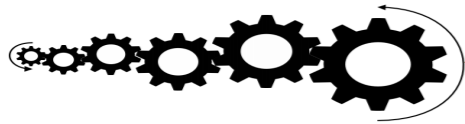
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if QCD anomaly generates the wiggles

$$\frac{\phi}{f} G\tilde{G} \longleftrightarrow m_{\pi}^2 f_{\pi}^2 \cos \frac{\phi}{f} \longleftrightarrow \theta_{\text{QCD}} \sim \mathcal{O}(1)$$

Then the relaxation is excluded by neutron EDM

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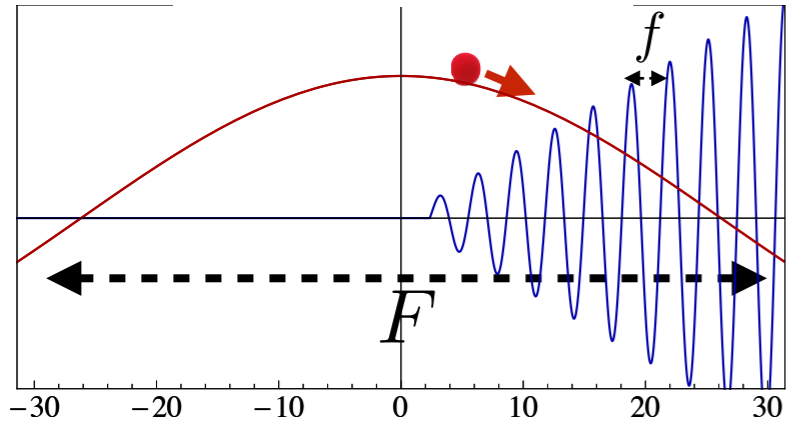
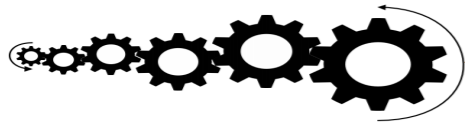
● changing the Cosmo:

★ smaller slope after inflation

Graham, Kaplan Rajendran '15

★ inflation between EW & QCD PT

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● changing the Field Theory:

★ ignoring CP: NP generates wiggles

Gupta, Komargodski, Perez, Ubaldi '15;
Espinosa, Panico, Pomarol, Pujolas, Servant '15
 ...

★ solving CP: Nelson-Barr relaxion

Davidi, Gupta, Perez, DR, Shalit '17

CHANGING THE COSMOLOGY

$$\frac{\Lambda_{\text{UV}}^4}{F} \sin \frac{\phi_0}{F} = \frac{\Lambda_{\text{wig}}^4}{f} \sin \frac{\phi_0}{f} \theta_{\text{QCD}}$$

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low cut-off (at most 30 TeV)

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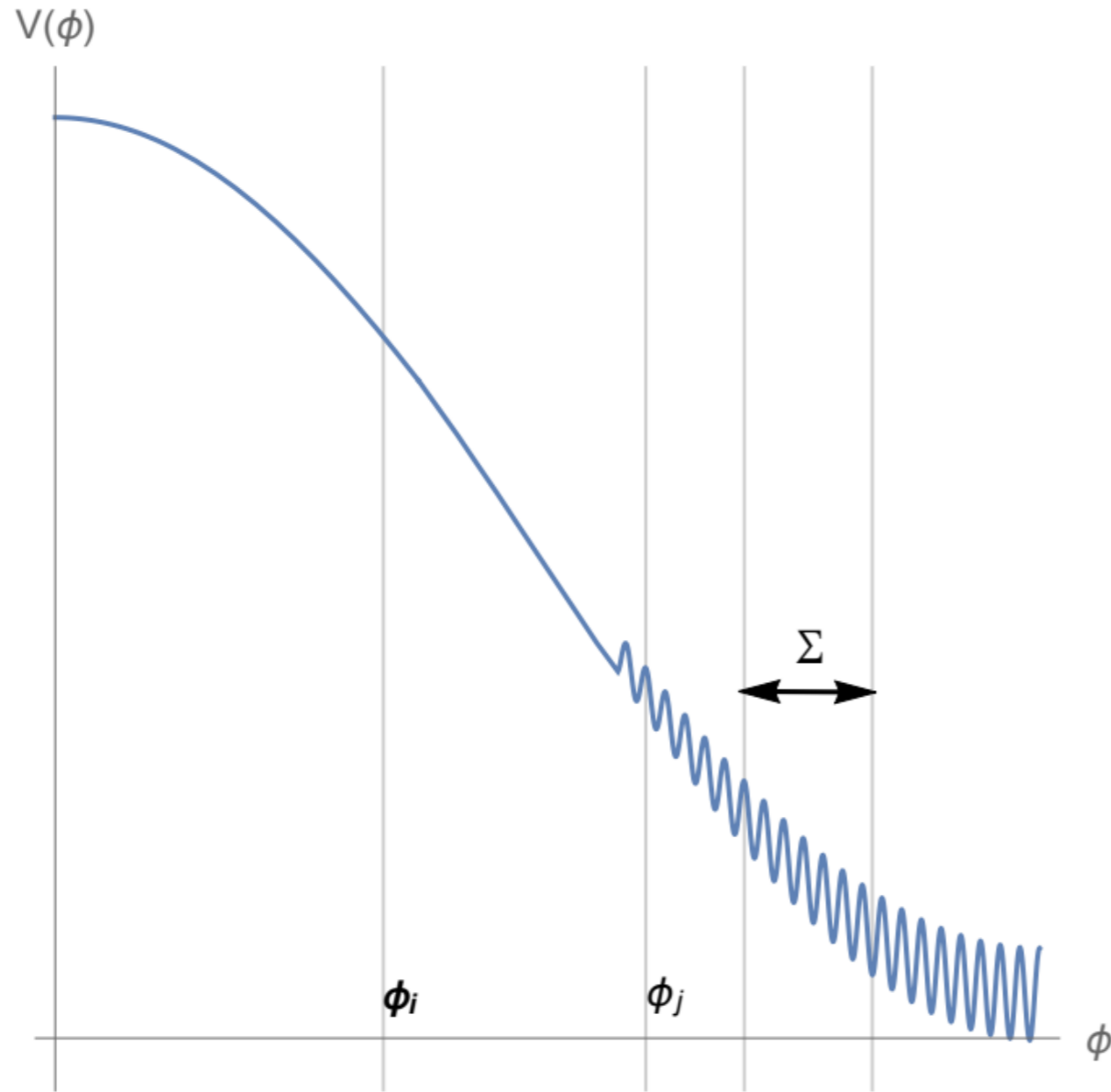
If we fix the L.H.S \longrightarrow wiggles during inflation \ll wiggles after inflation

Nelson & Prescod-Weinstein '17

$H_I \gtrsim 3 \text{ GeV}$ \longleftrightarrow high enough Hubble to suppress QCD wiggles with T-effects

CAN WE achieve that?

~~$\dot{\phi}_{\text{roll}} \lesssim H_I^2$~~ + $\Delta V_{\text{roll}} \lesssim V_{\text{infl}}$ \longleftrightarrow $\Lambda_{UV} \lesssim (H_I M_{Pl})^{1/2}$



CAN WE achieve that?

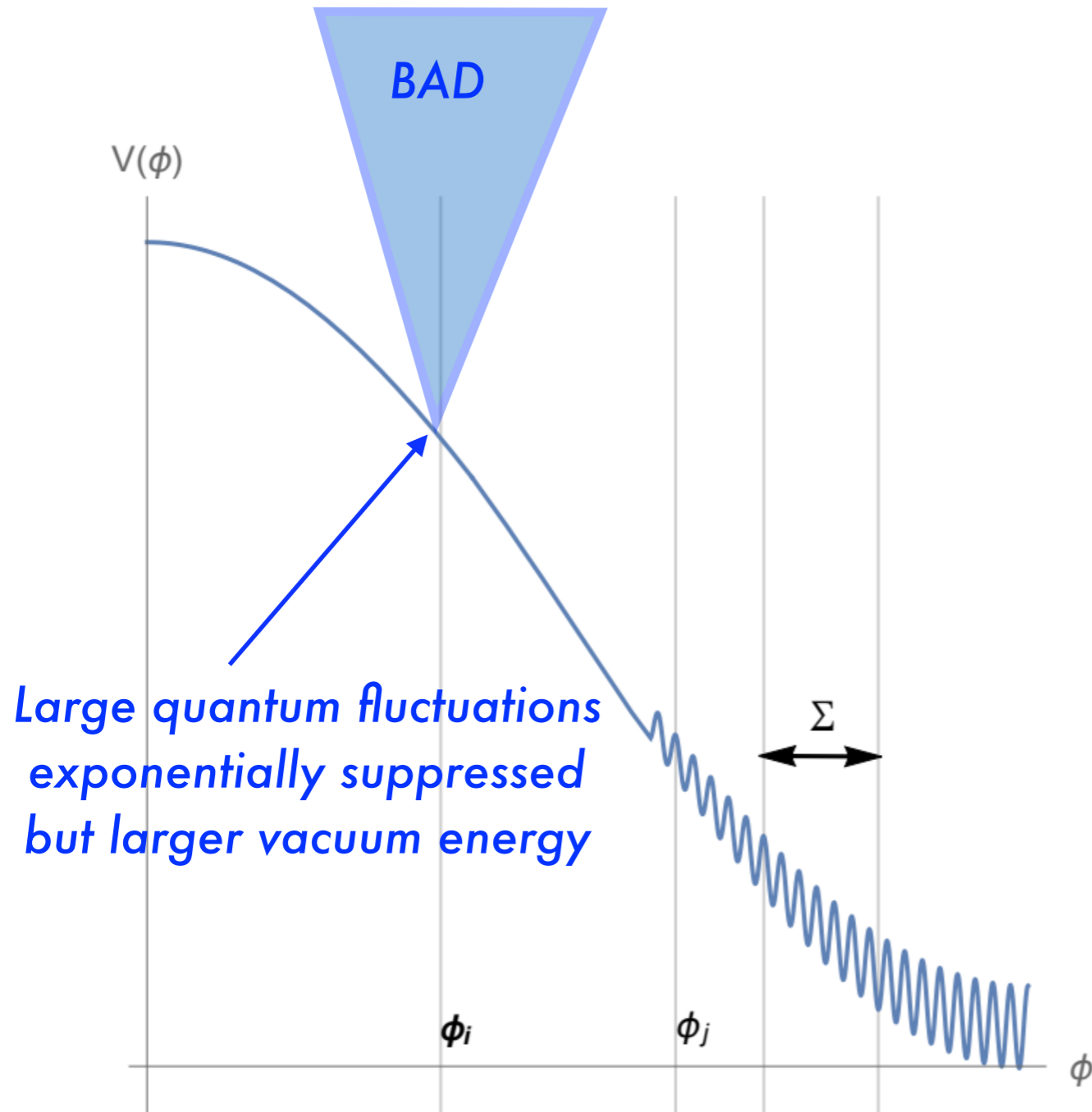
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+

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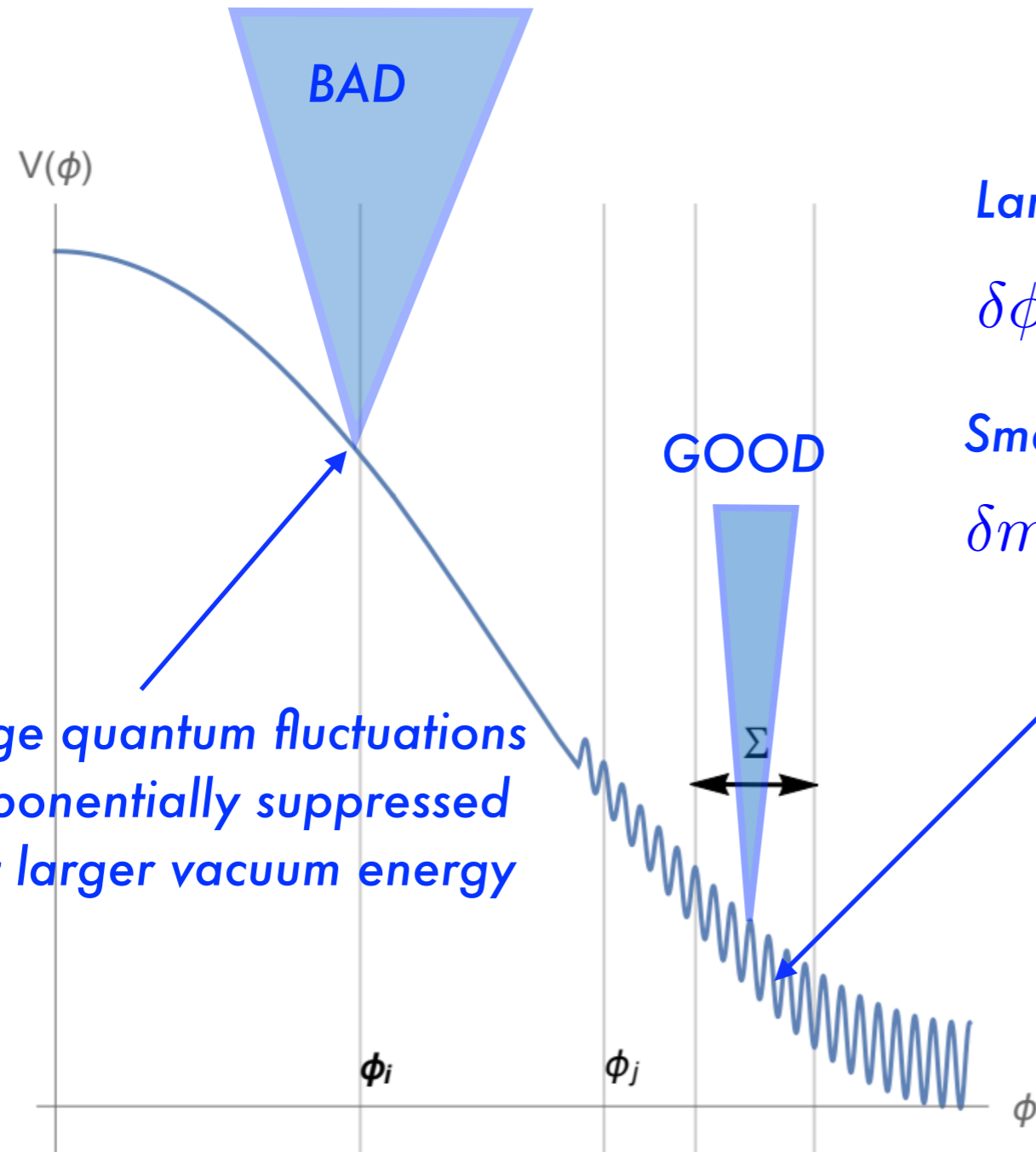
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Large quantum spread

$$\delta\phi \sim F \cdot \frac{H_I^2}{\Lambda_{UV}^2}$$

Small variation of the EW scale

$$\delta m^2 \sim H_I^2 \lesssim v^2$$

Large quantum fluctuations exponentially suppressed but larger vacuum energy

GOOD

Δ

ϕ_i

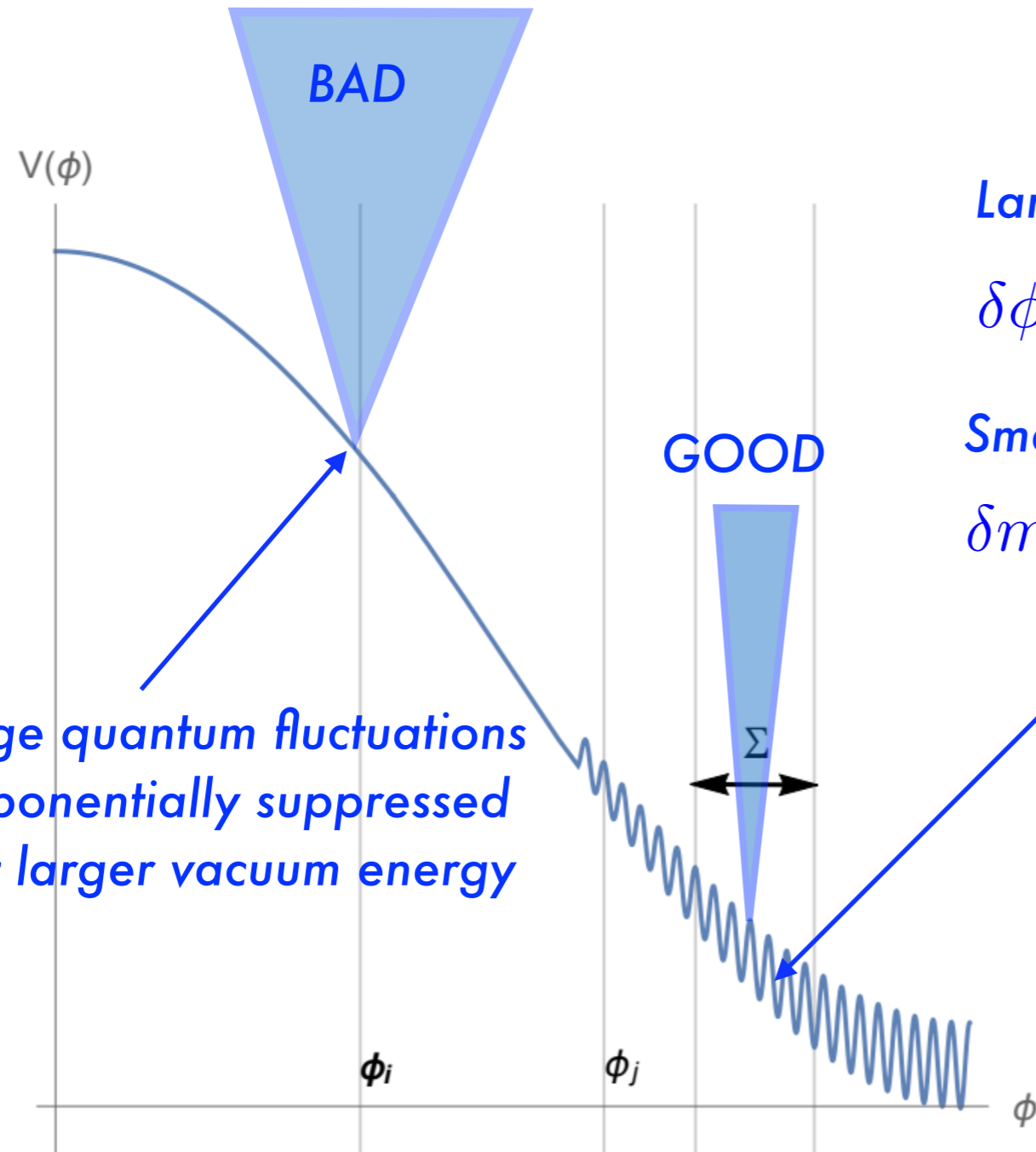
ϕ_j

ϕ

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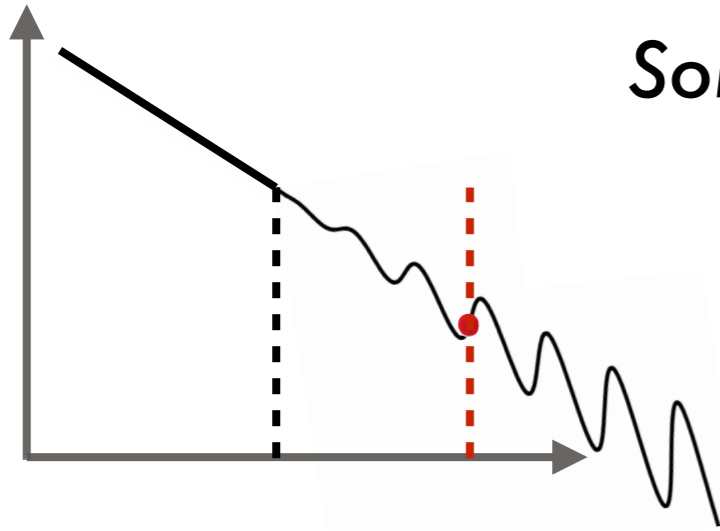
Volume BAD > Volume GOOD?

The fate of these large quantum fluctuations suffer from measure problems... Gupta '18

Something else than QCD generates the wiggles

Espinosa, Grojean, Panico, Pomarol, Pujolas, Servant '15

Komargodski, Gupta, Perez, Ubaldi '15

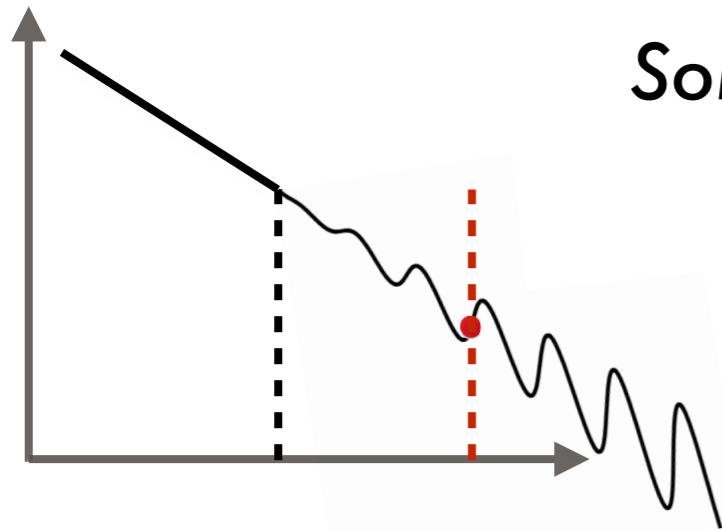


$$V_{\text{br}} = -M_{\text{br}}^2 H^\dagger H \cos \frac{\phi}{f} + r_{\text{br}} M_{\text{br}}^4 \cos \frac{\phi}{f}$$
$$\Lambda_{\text{wig}} \equiv \sqrt{M_{\text{br}} v}$$

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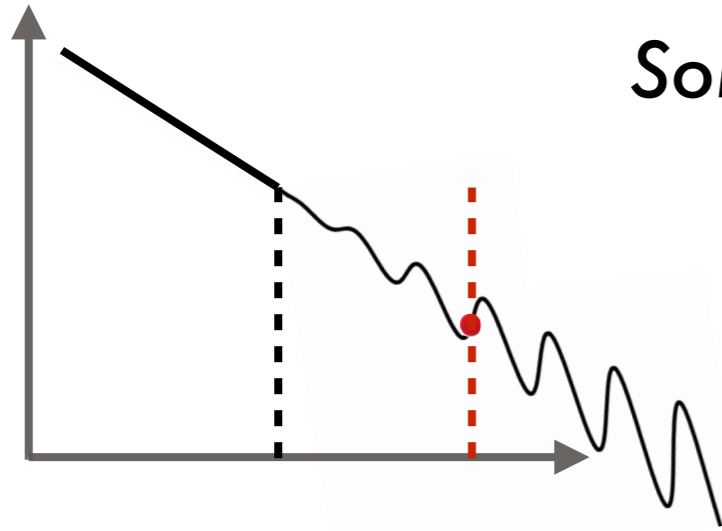


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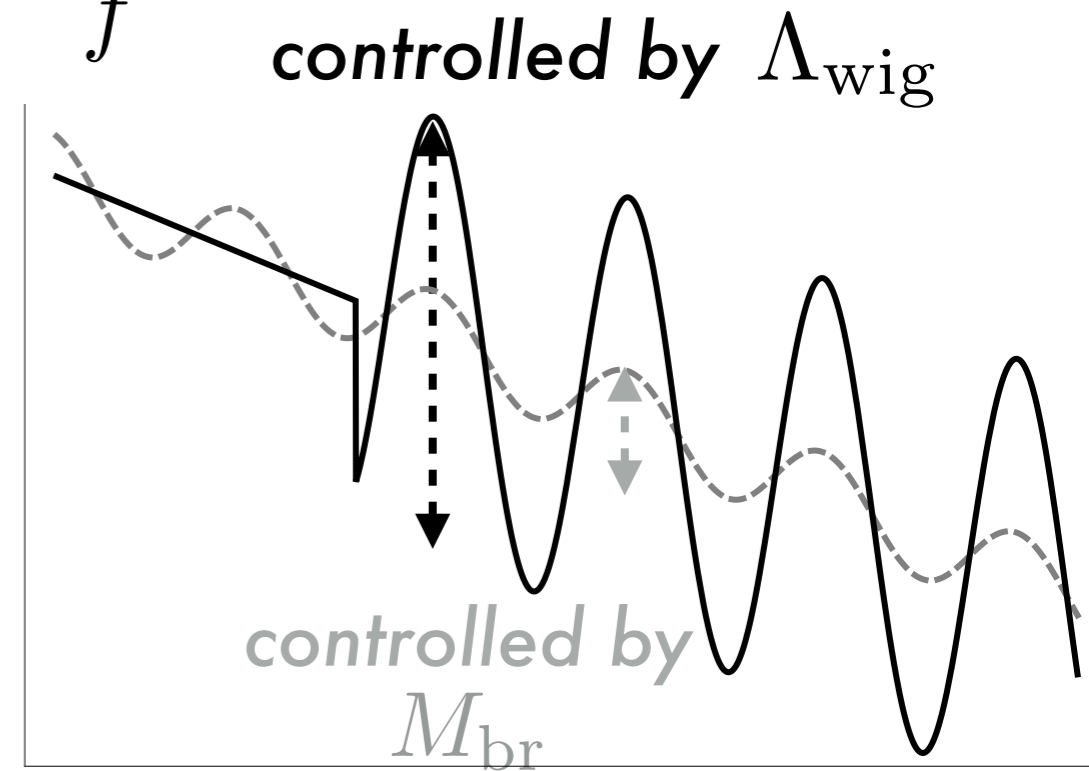
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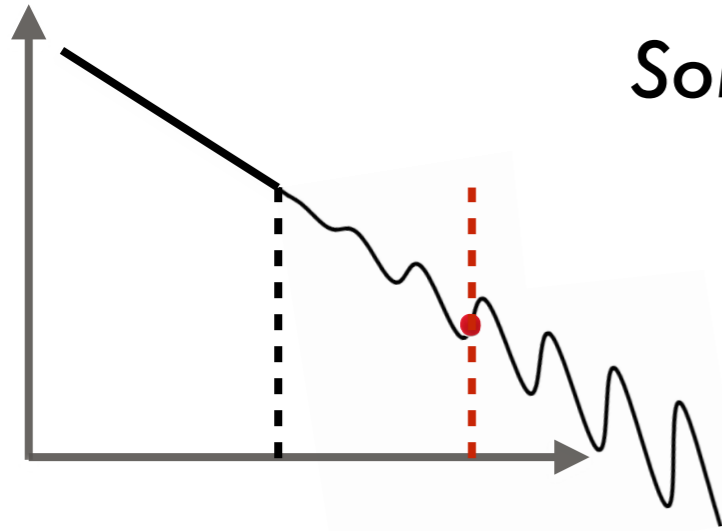
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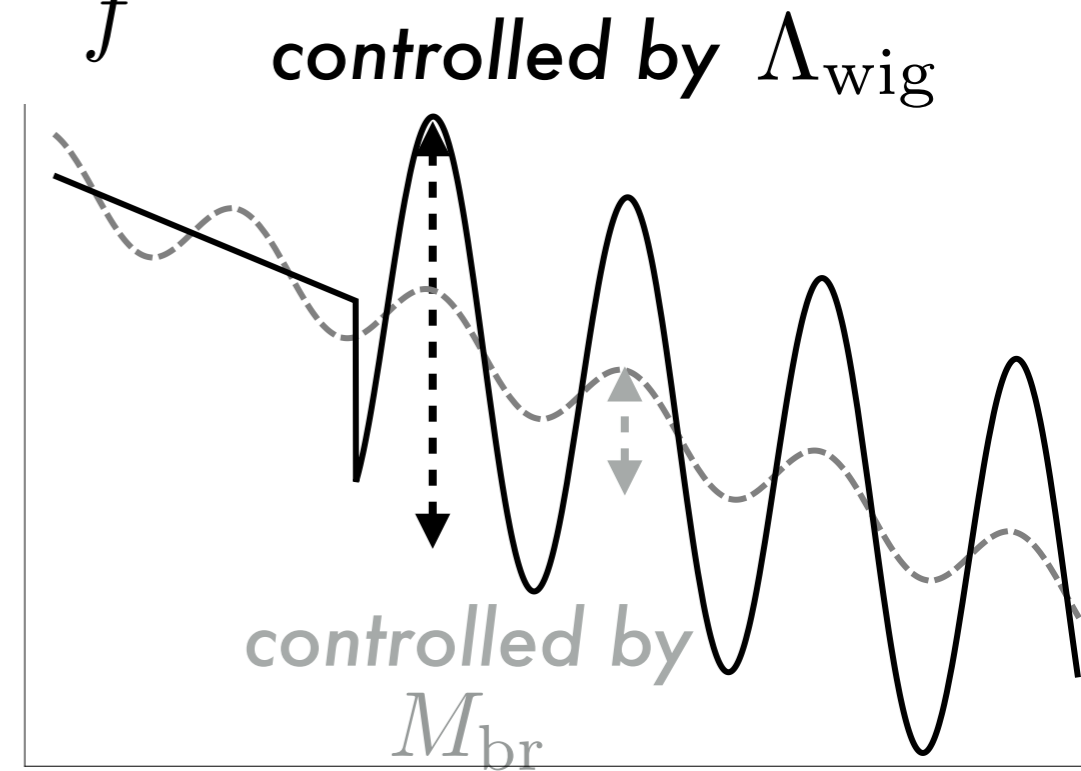
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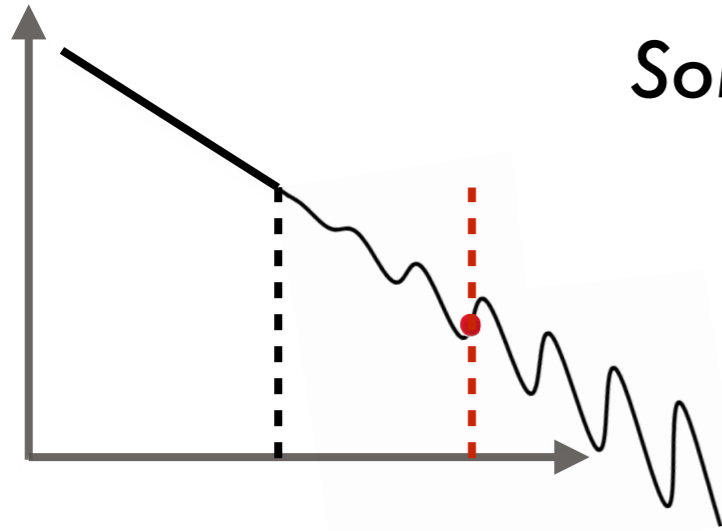
no loose theorem



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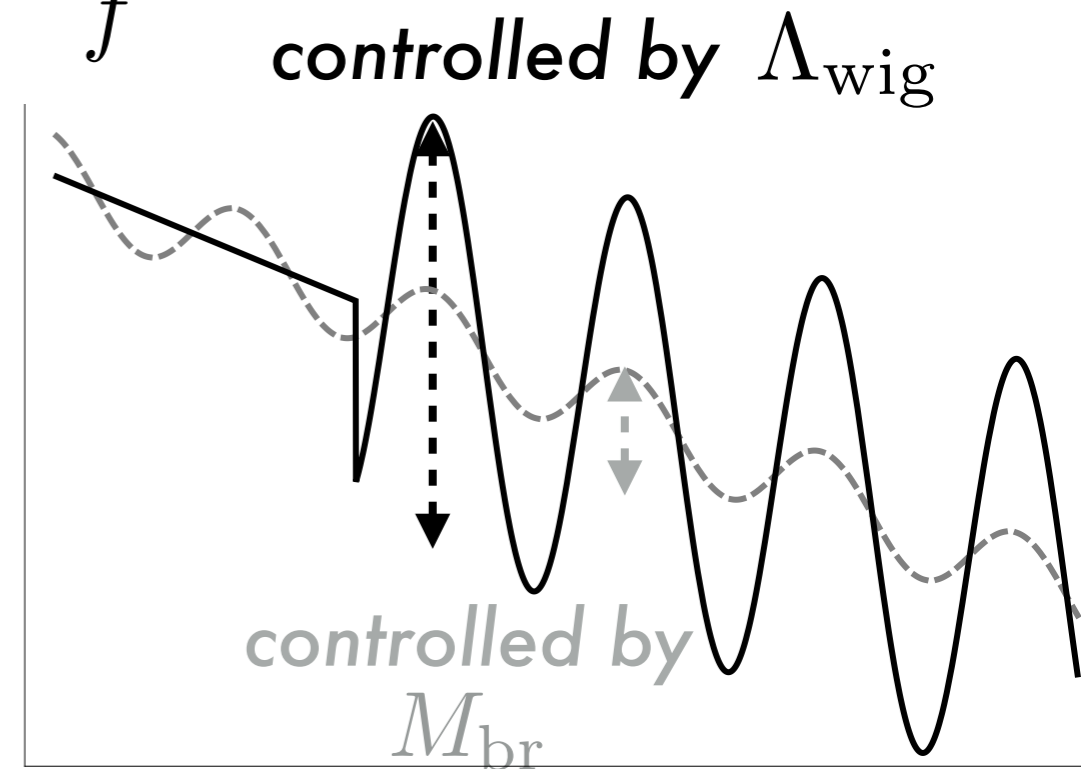


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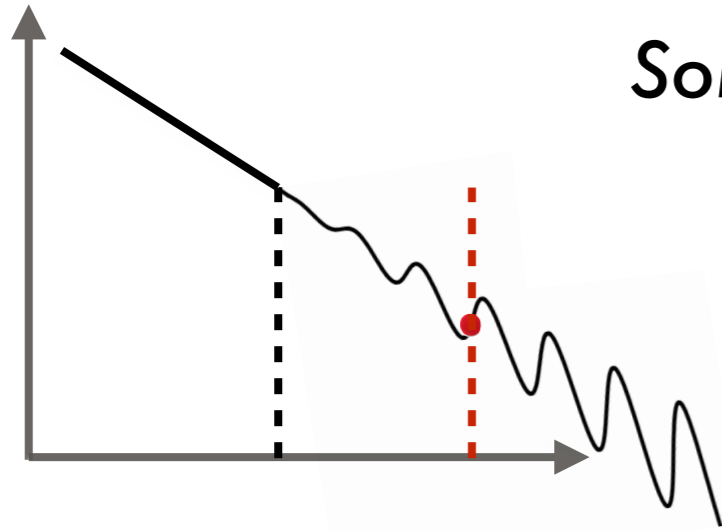
New states @ the EW scale $\mathcal{L}_{\text{NP}} \supset H f^{\text{SM}} f^{\text{NP}}$



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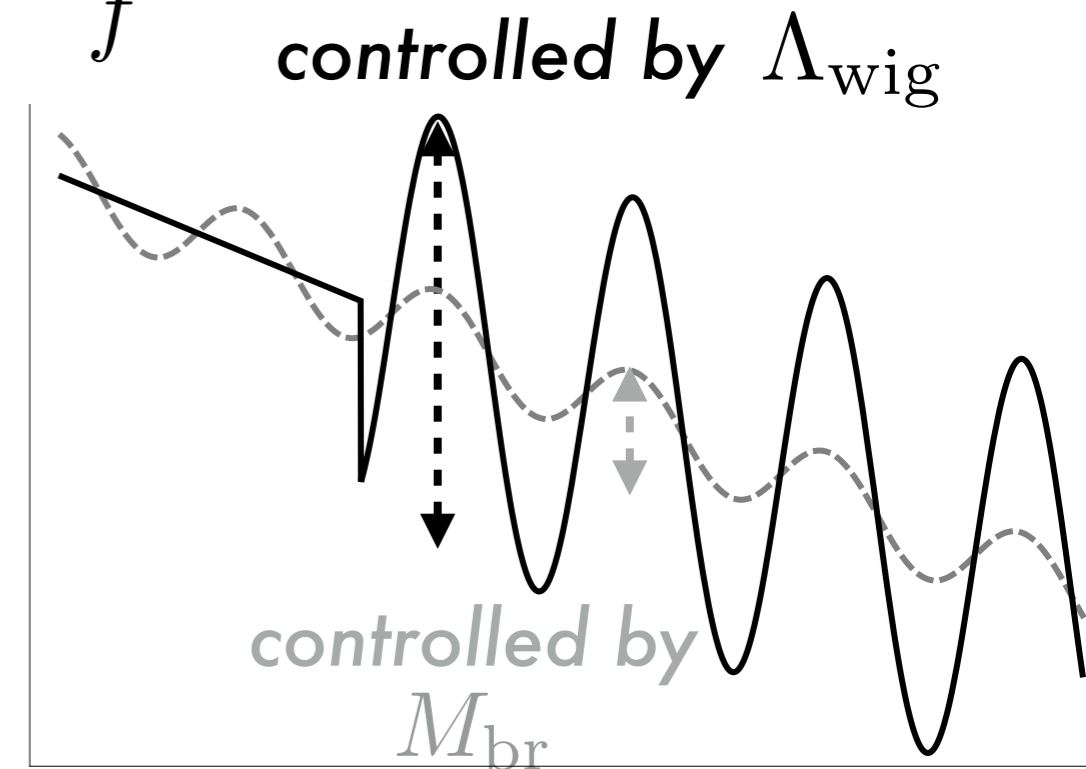
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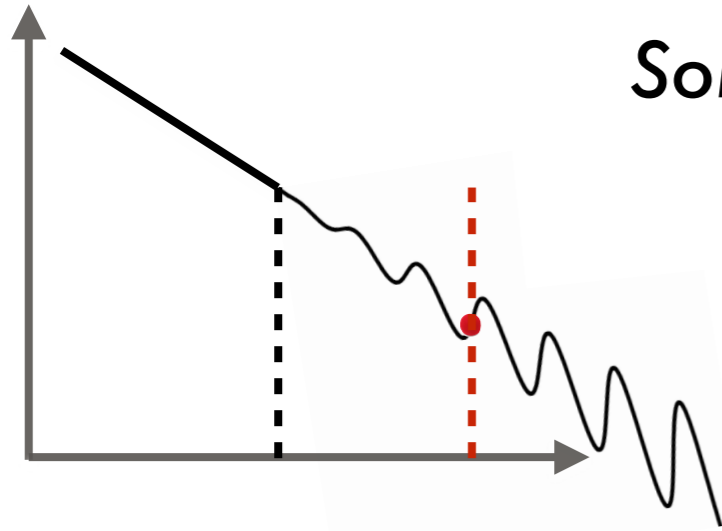
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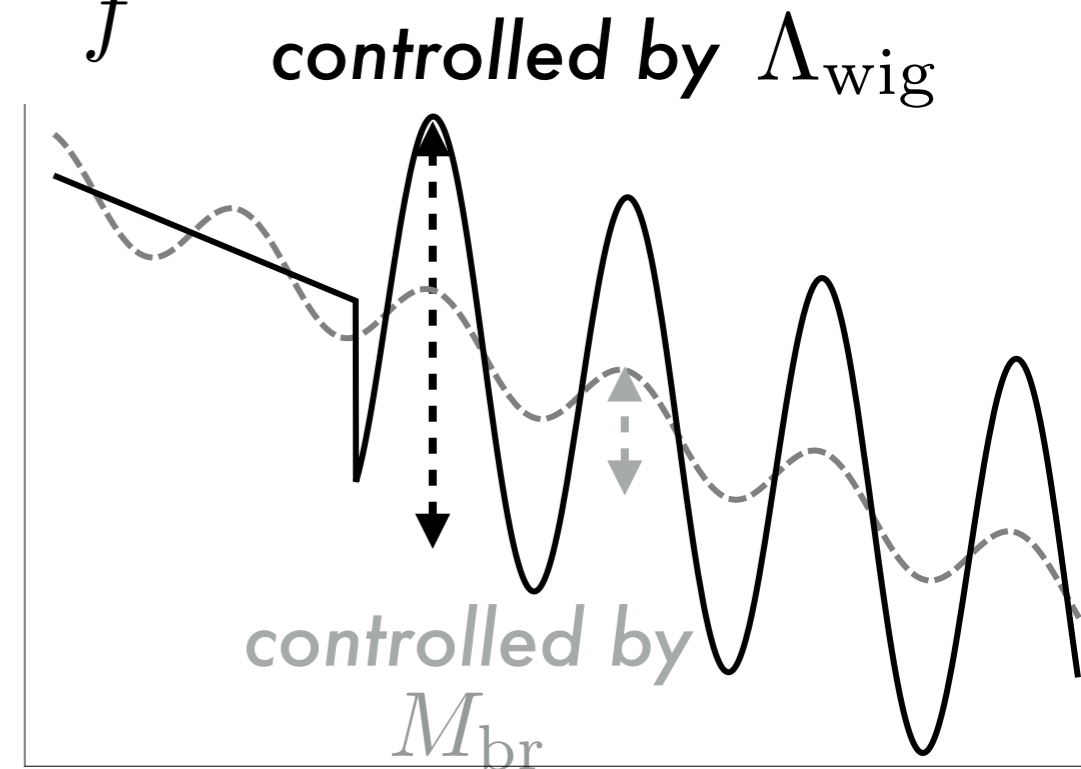
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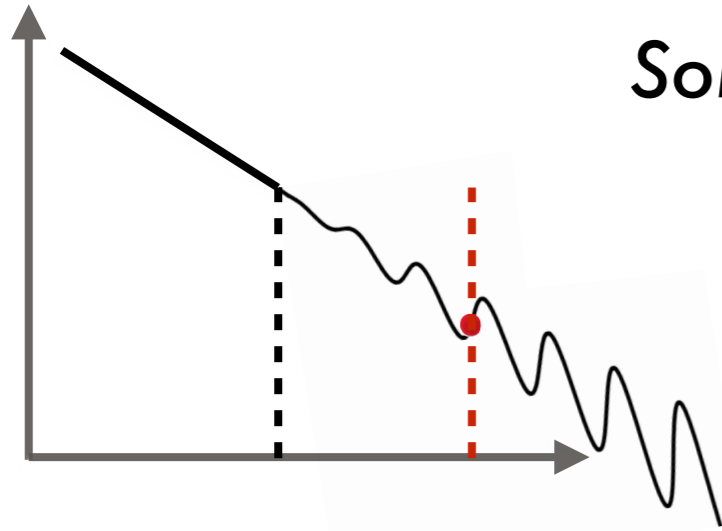
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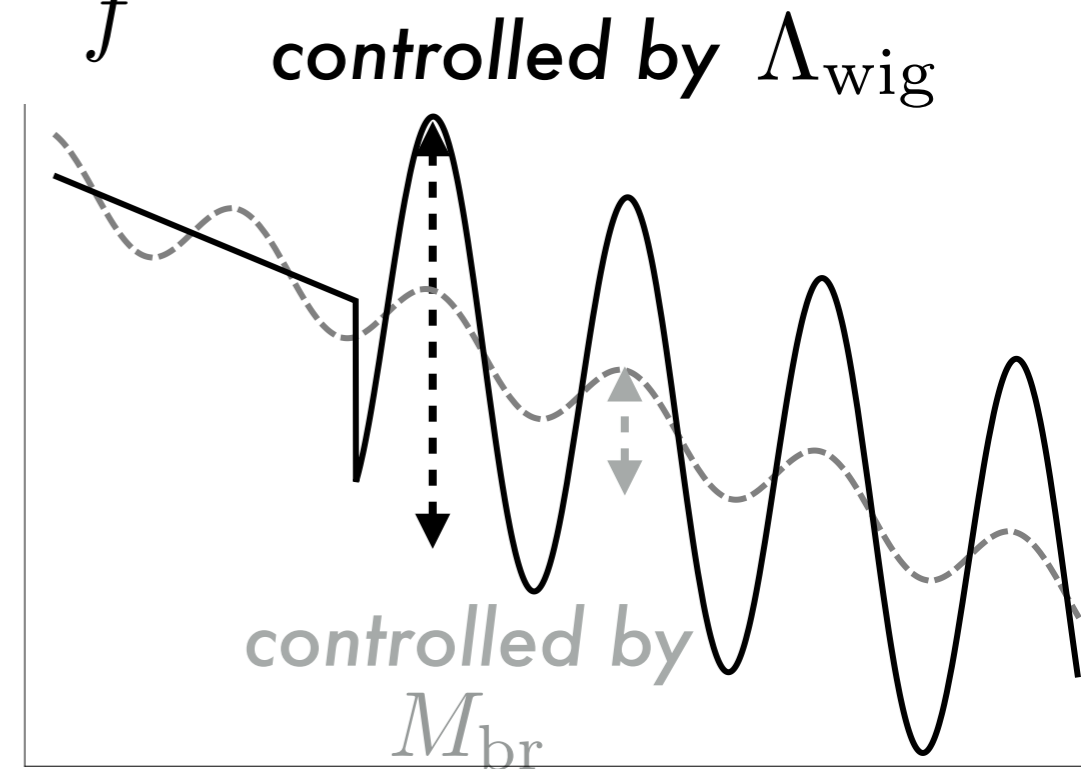
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We can test them @ collider **I will show a counter-example later...**



addressing strong CP

Something else than QCD generates the wiggles

+

Nelson-Barr sector generates the rolling

addressing strong CP

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Nelson-Barr sector generates the rolling

CP is a symmetry of the UV theory

it is spontaneously broken by the relaxion VEV

a discrete symmetry forbids the coupling to $G\tilde{G}$

Nelson-Barr solution to the
strong CP problem

(Nelson '84, Barr '84)

addressing strong CP

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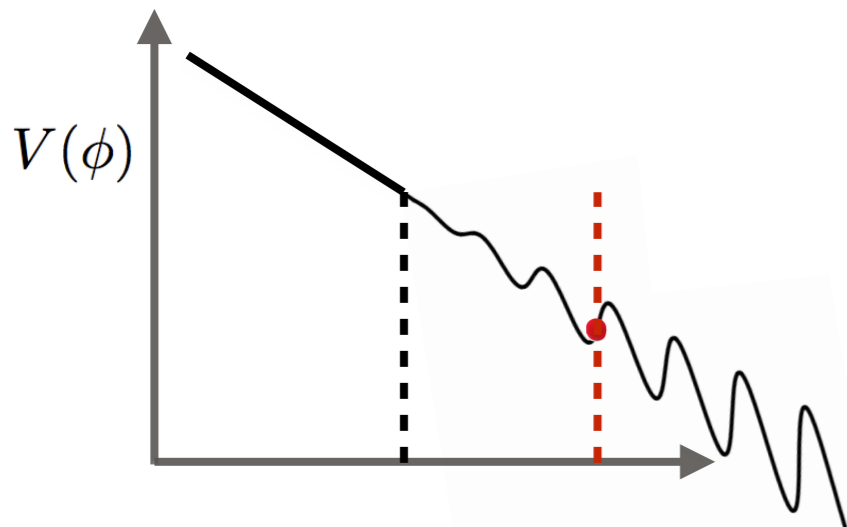
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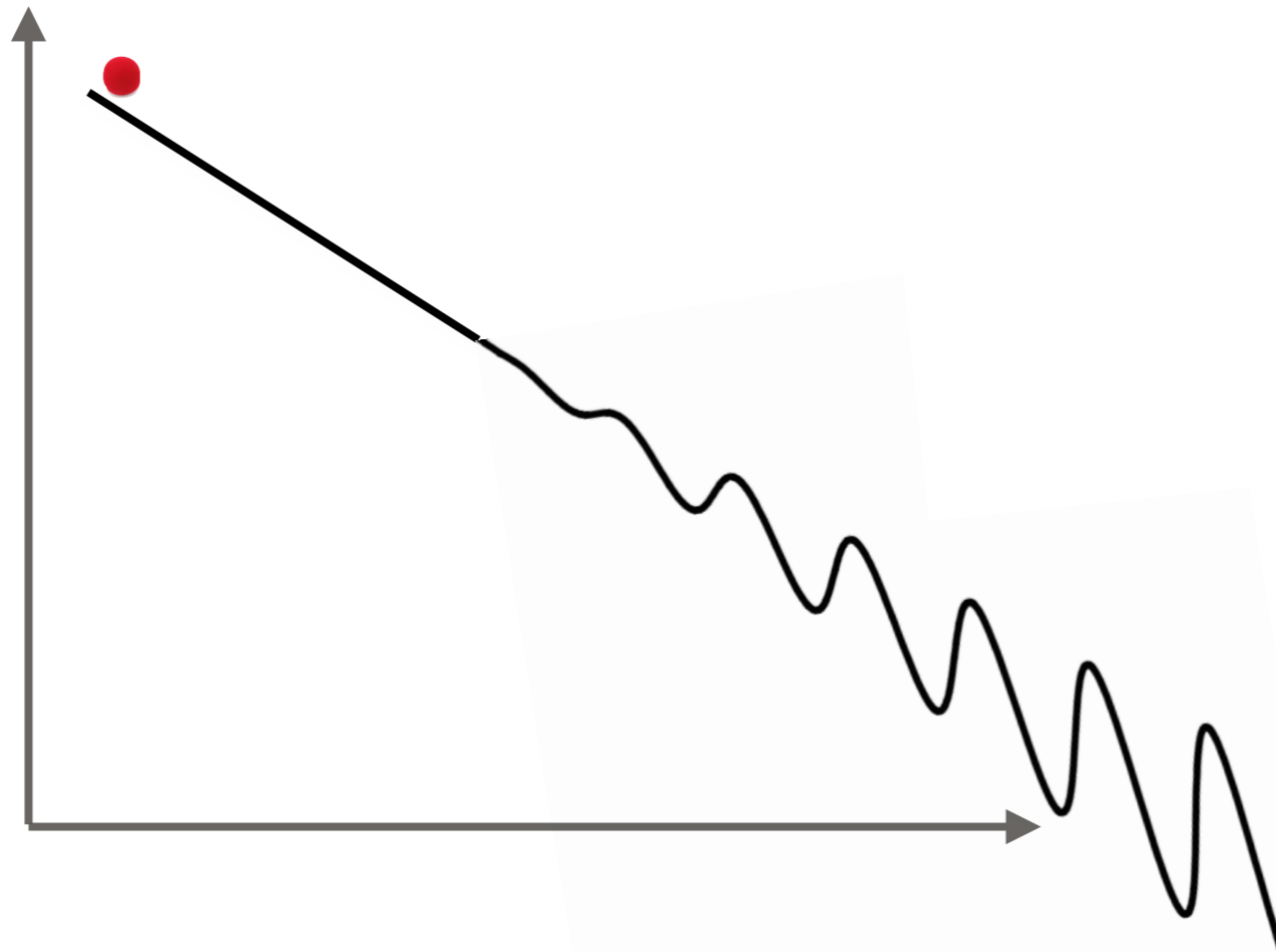
The U(1) on the N-site of the clockwork chain is broken explicitly $g_{u,d}\tilde{g}_{u,d}$



ϕ rolling potential:
$$V_{\text{roll}} = \frac{g_{u,d}\tilde{g}_{u,d}f^4}{16\pi^2} \cos \frac{\phi}{F}$$

$$\cos \frac{\phi_0}{F} \sim \delta_{\text{CKM}} \sim \mathcal{O}(1)$$

New playground for Naturalness

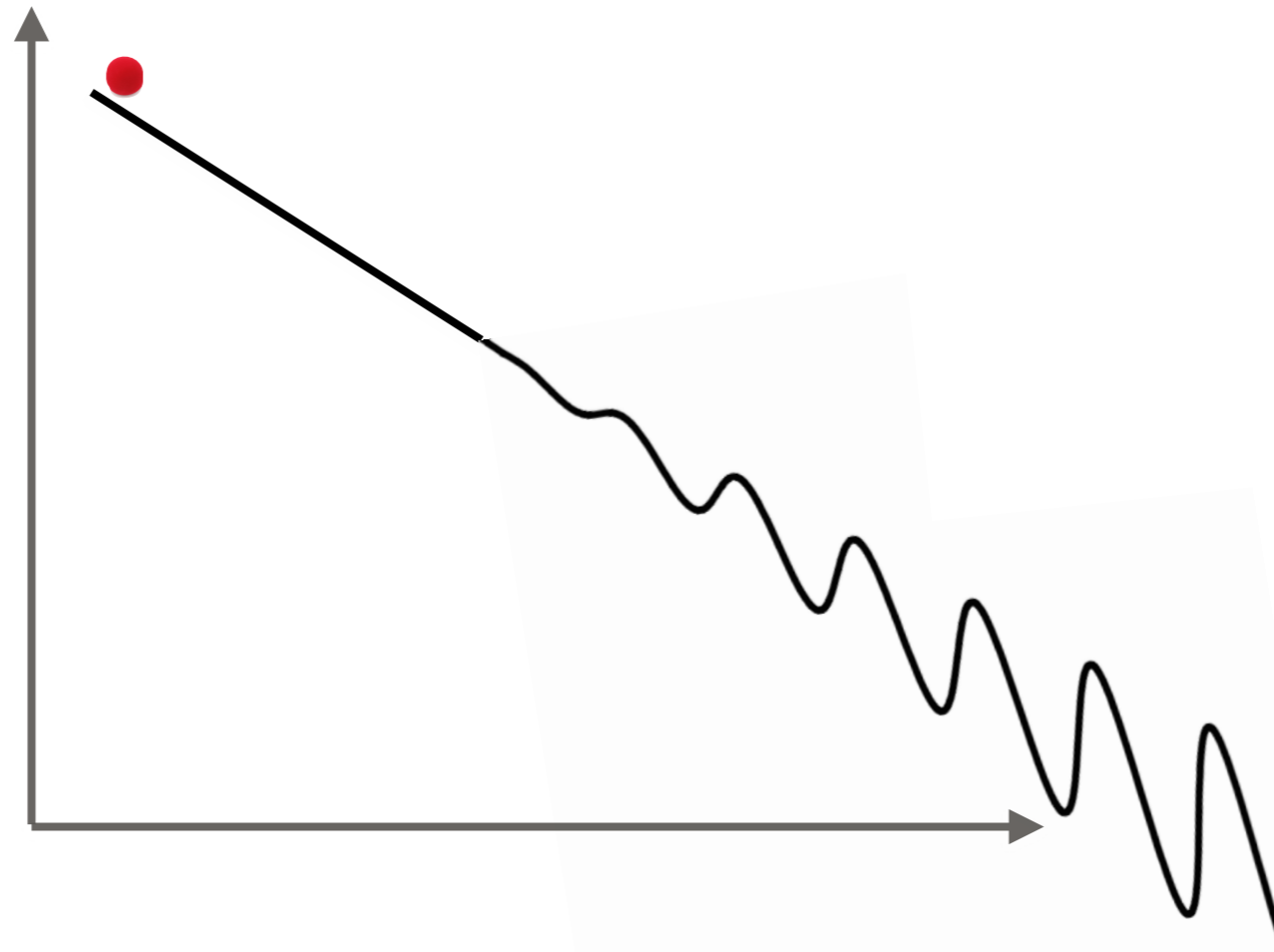


**new
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New playground for Naturalness



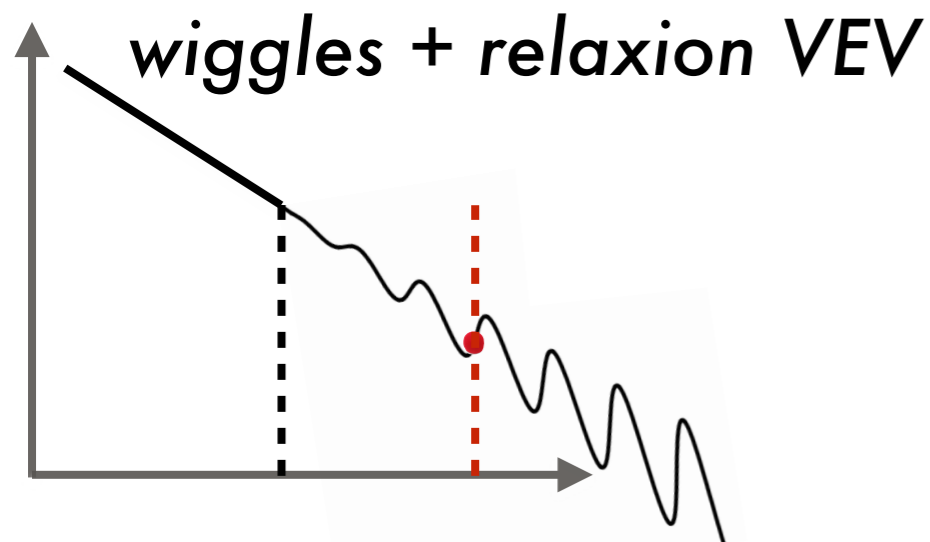
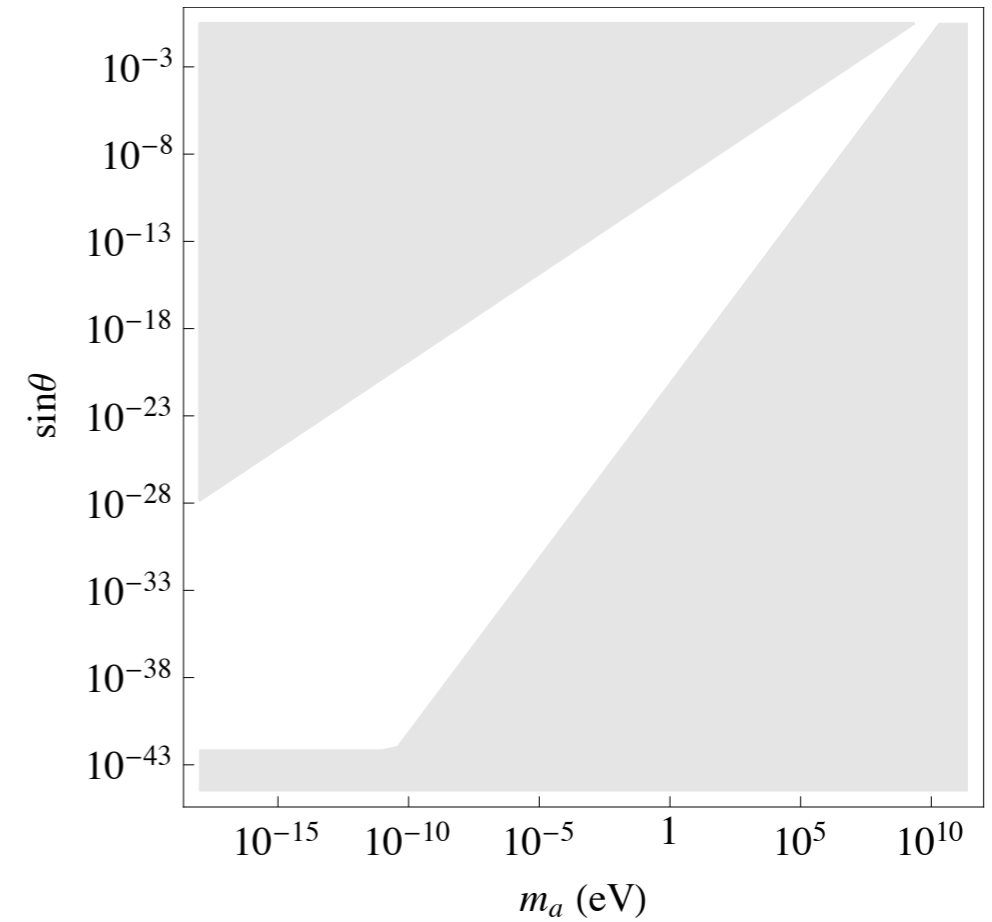
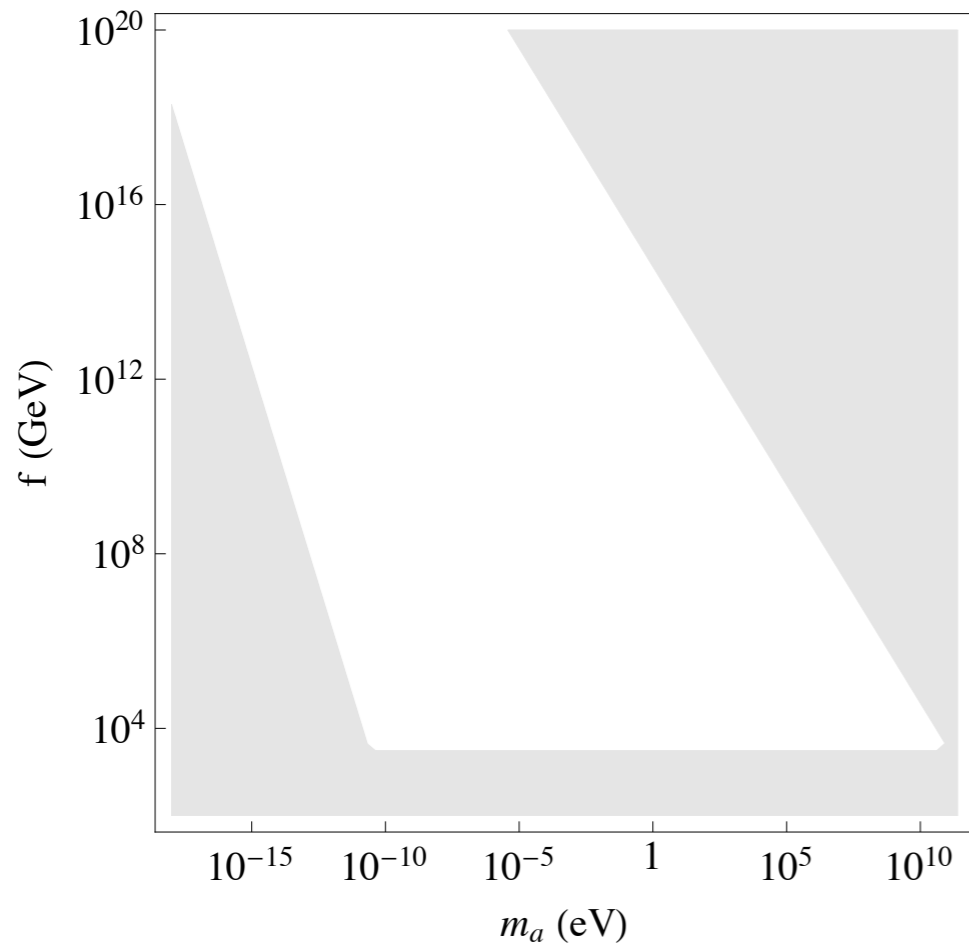
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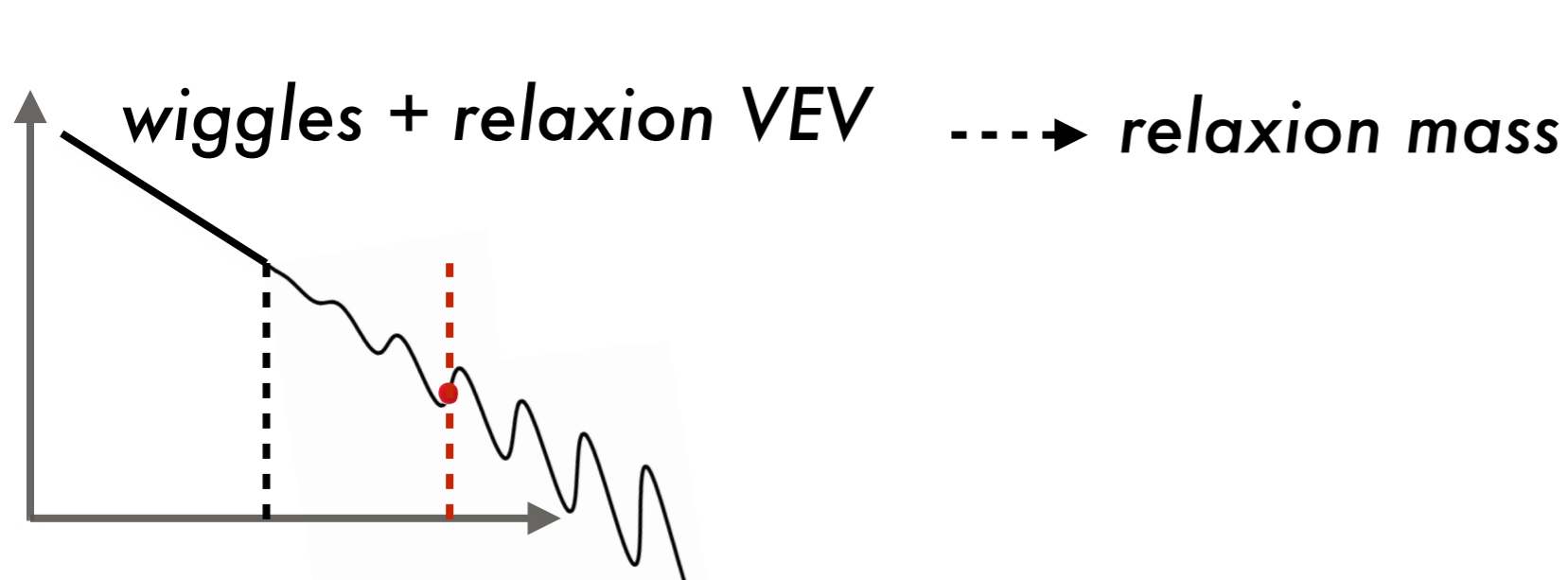
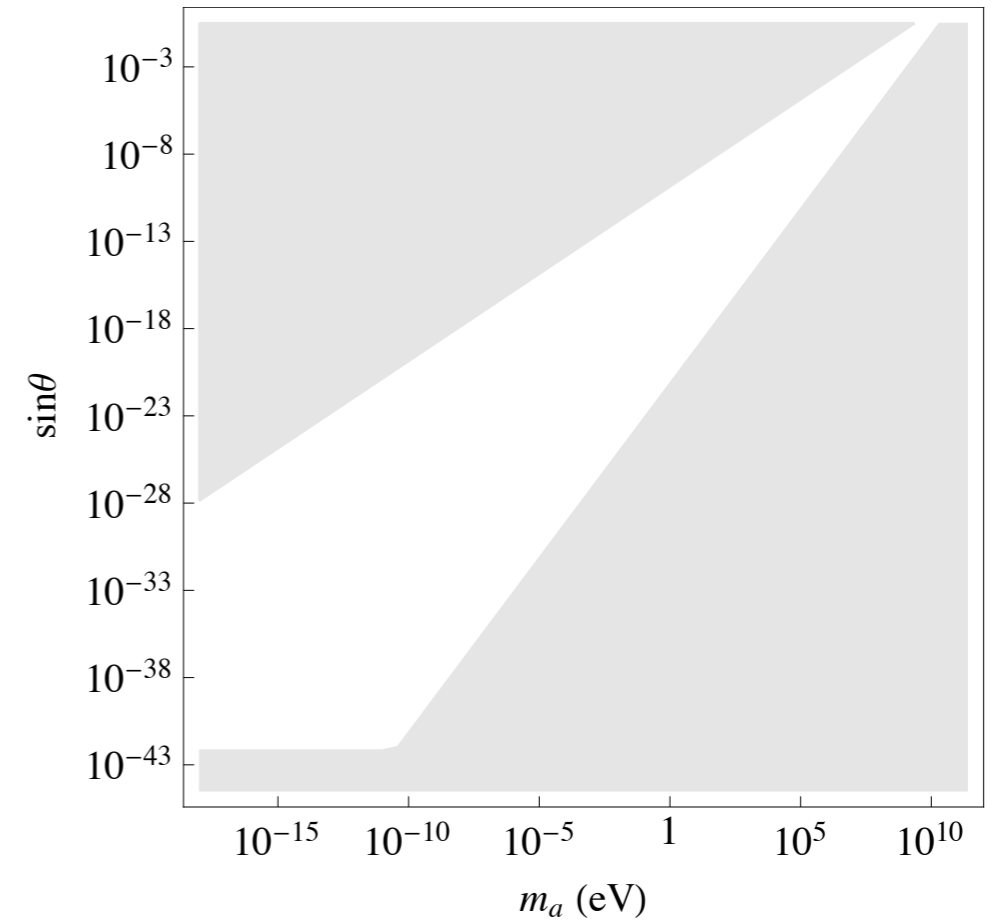
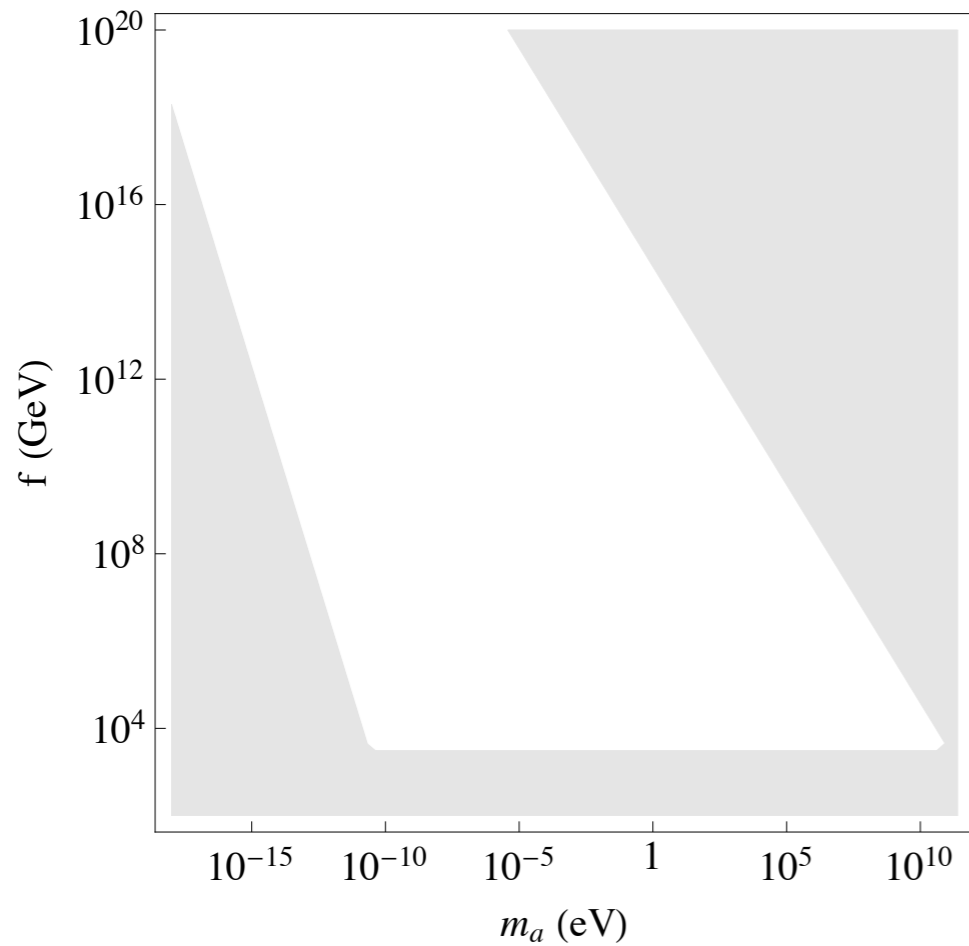
The relaxion parameter space

Model-independent PHENO depends on explicit breaking from wiggles



The relaxion parameter space

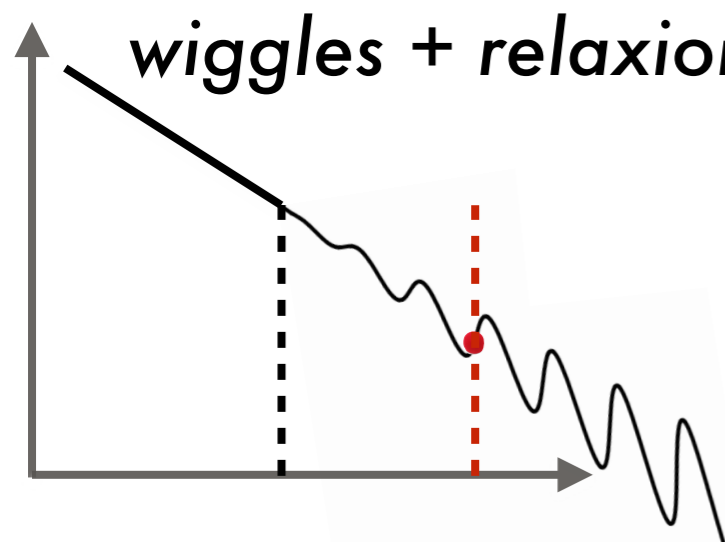
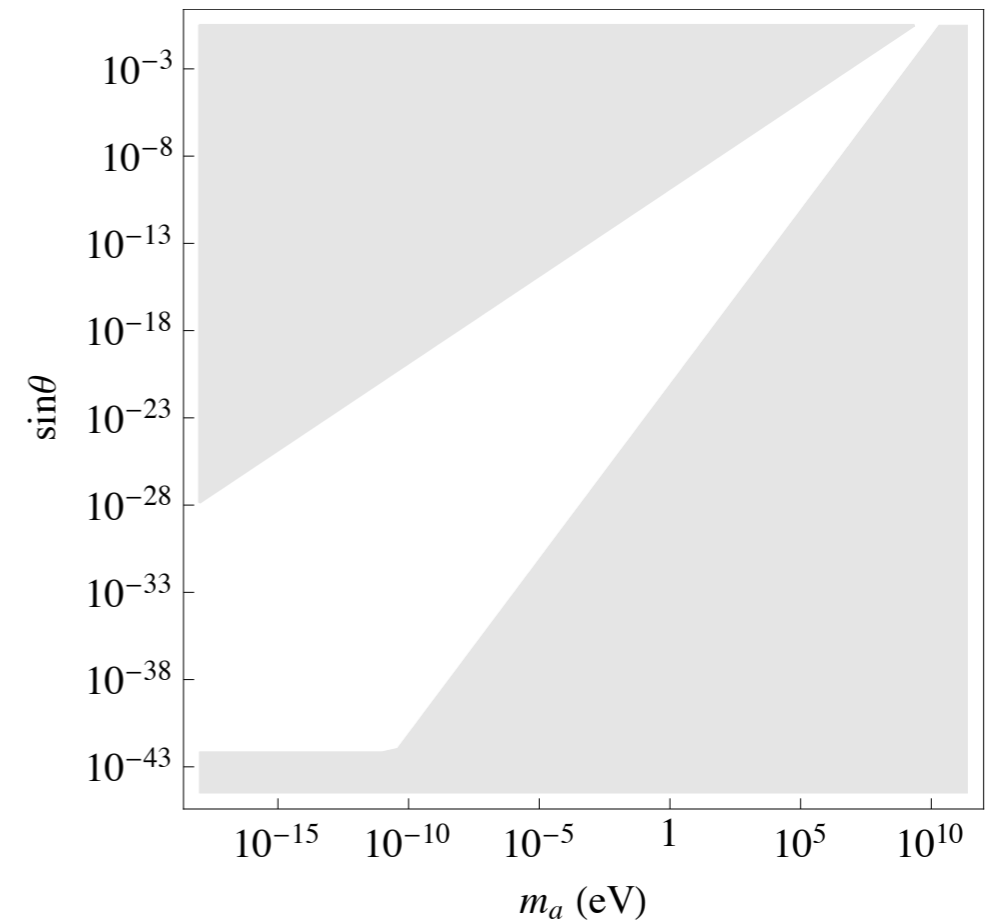
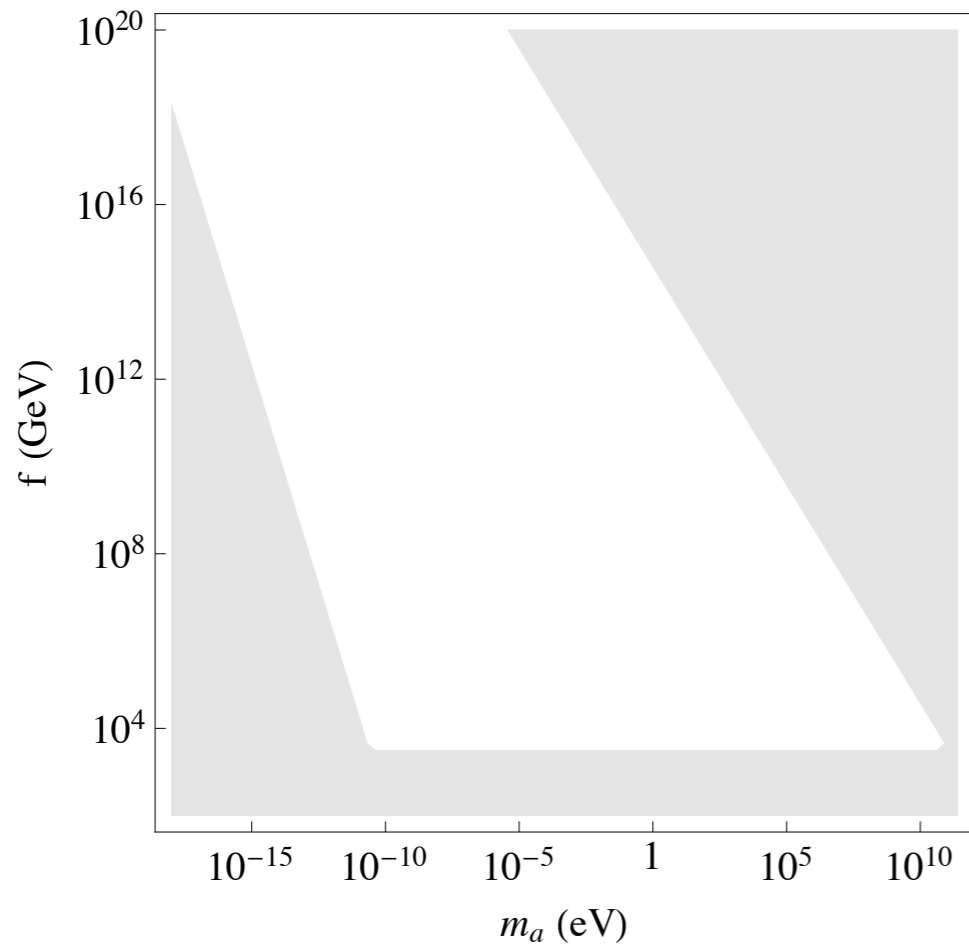
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$$m_a \simeq \frac{\overbrace{M_{\text{br}}^2}}{f}$$

The relaxion parameter space

Model-independent PHENO depends on explicit breaking from wiggles



wiggles + relaxion VEV

---> relaxion mass

$$m_a \simeq \frac{\overbrace{M_{\text{br}}^2}}{f}$$

---> relaxion-Higgs mixing

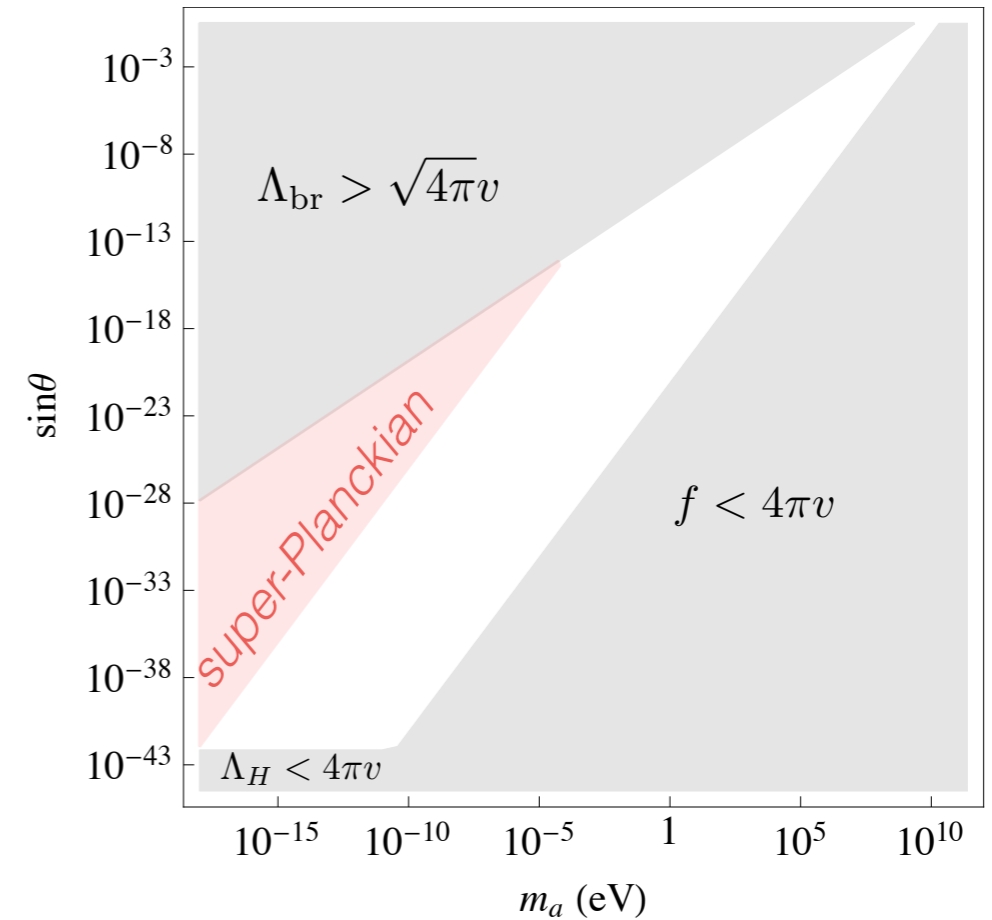
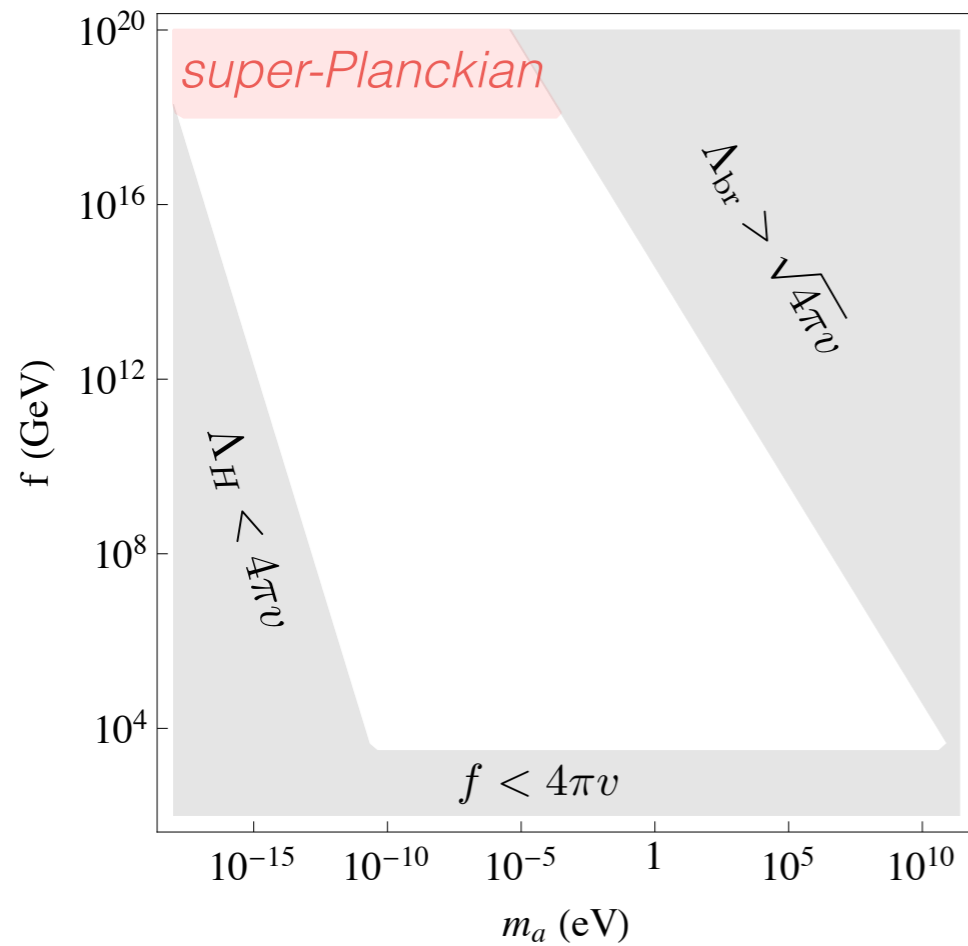
$$\sin \theta \simeq \frac{v}{f} \cdot \frac{\overbrace{M_{\text{br}}^2}}{m_h^2}$$

Flacke, Gupta, Frugiuele, Fuchs, Perez '16

Choi and Im '17

The relaxion parameter space

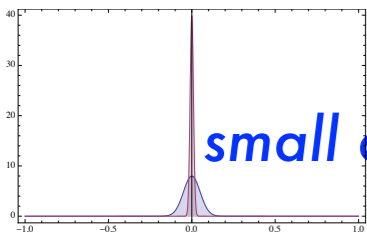
Model-independent boundaries



inflation OK

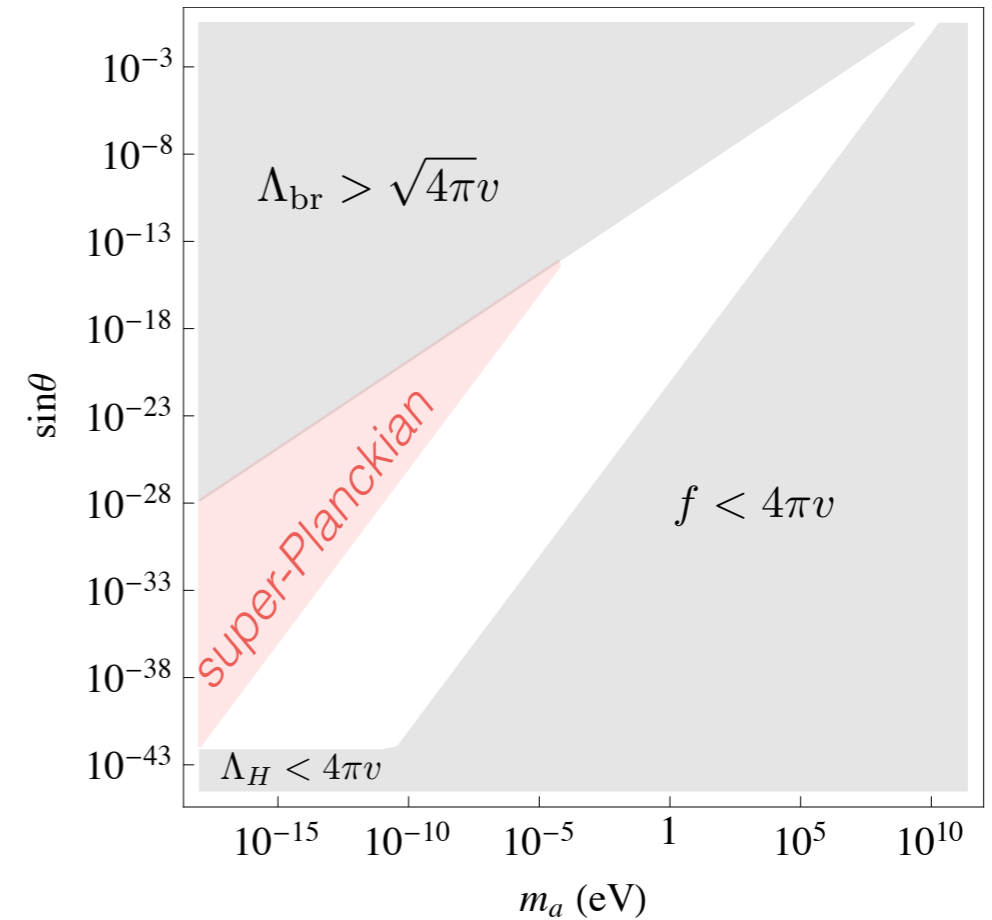
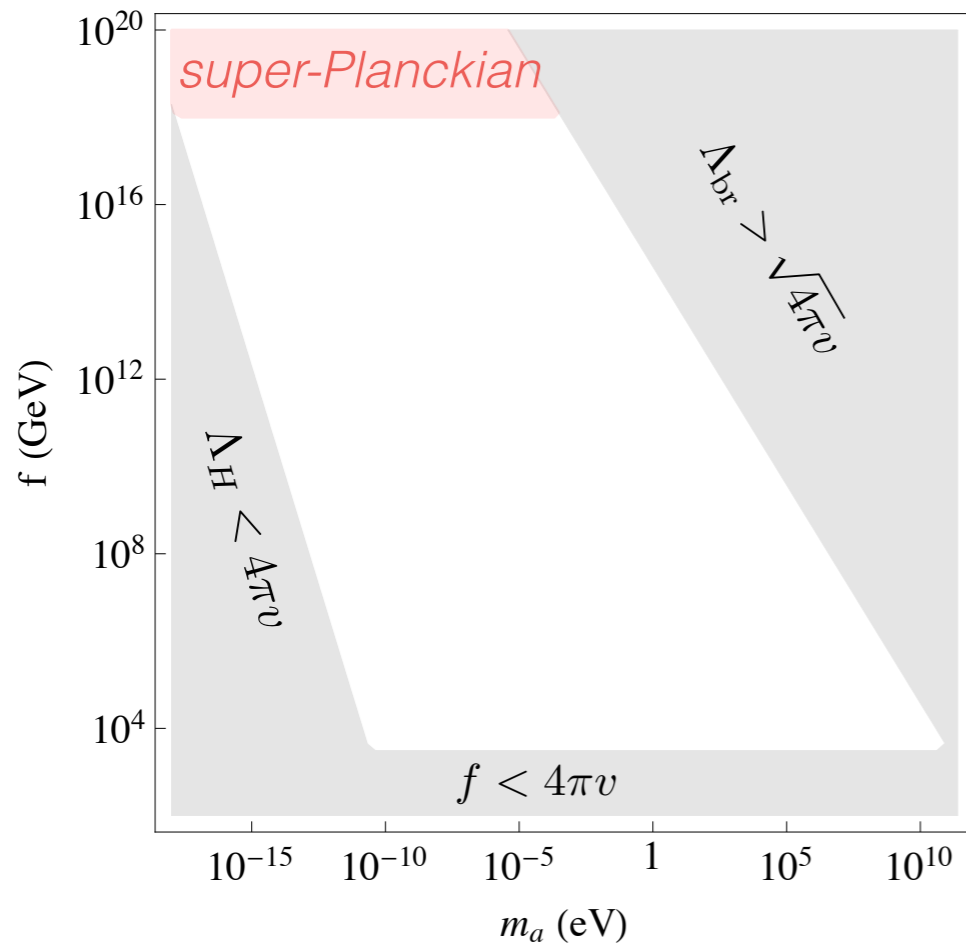
$$\Lambda_{\text{roll}}^4 \lesssim H_I^2 M_{\text{Pl}}^2$$

small quantum spread $\dot{\phi} \gtrsim H_I^2$



The relaxion parameter space

Model-independent boundaries

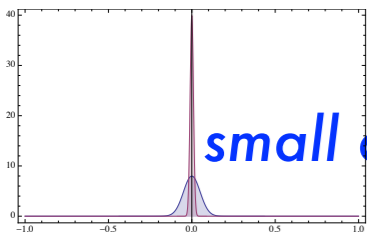


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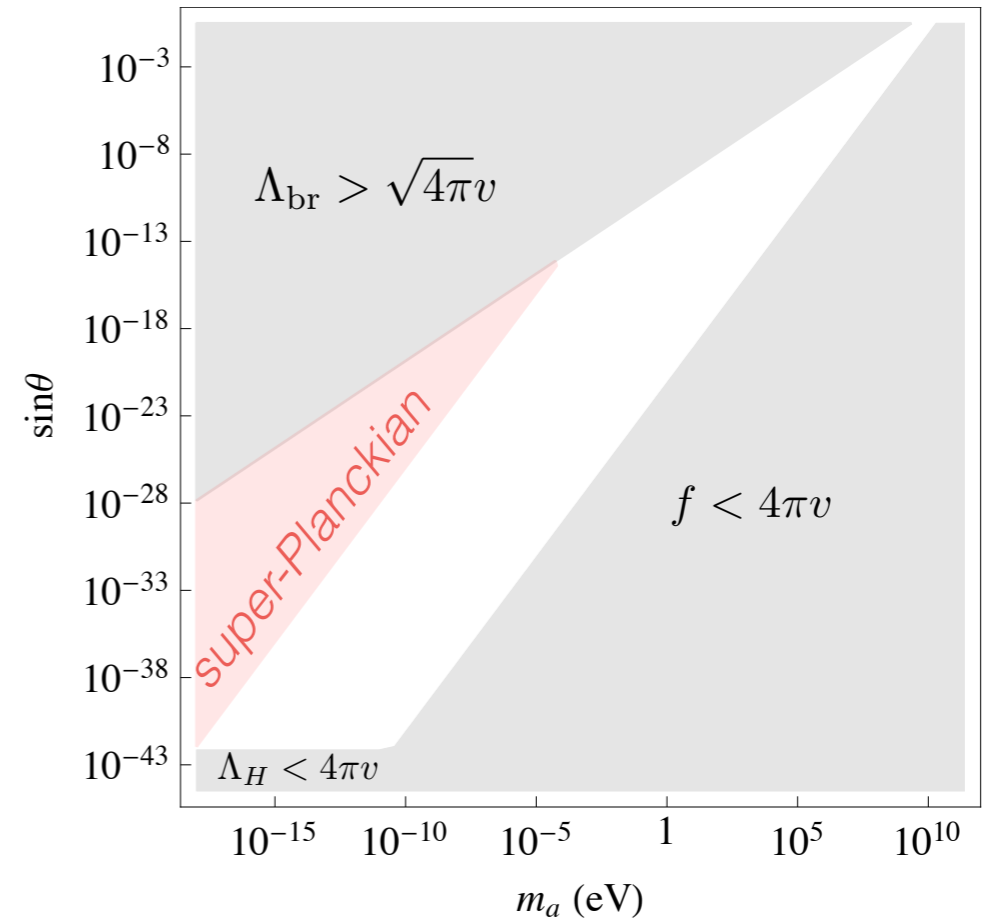
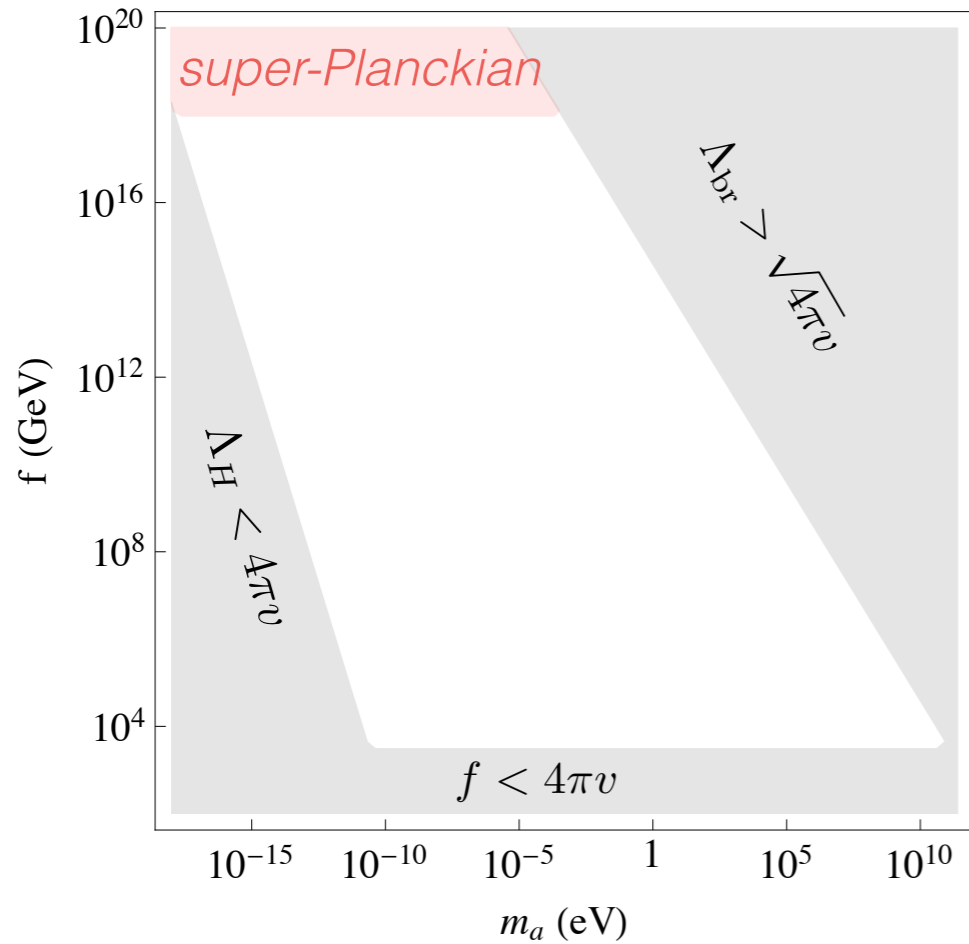
small quantum spread $\dot{\phi} \gtrsim H_I^2$

$$\left\{ \begin{array}{l} 4\pi v \lesssim \Lambda_H \lesssim \left(\frac{M_{\text{Pl}}}{r_{\text{roll}}} \right)^{1/2} \left(\frac{\Lambda_{\text{br}}^4}{f} \right)^{1/6} \\ \sqrt{\frac{M_{\text{Pl}}}{f}} \cdot 10^{-18} \text{ eV} \lesssim m_a \lesssim v \end{array} \right.$$



The relaxion parameter space

Model-independent boundaries

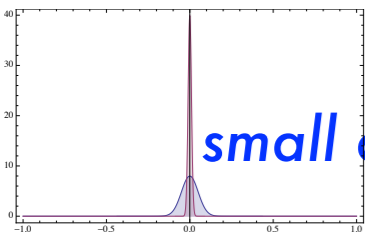


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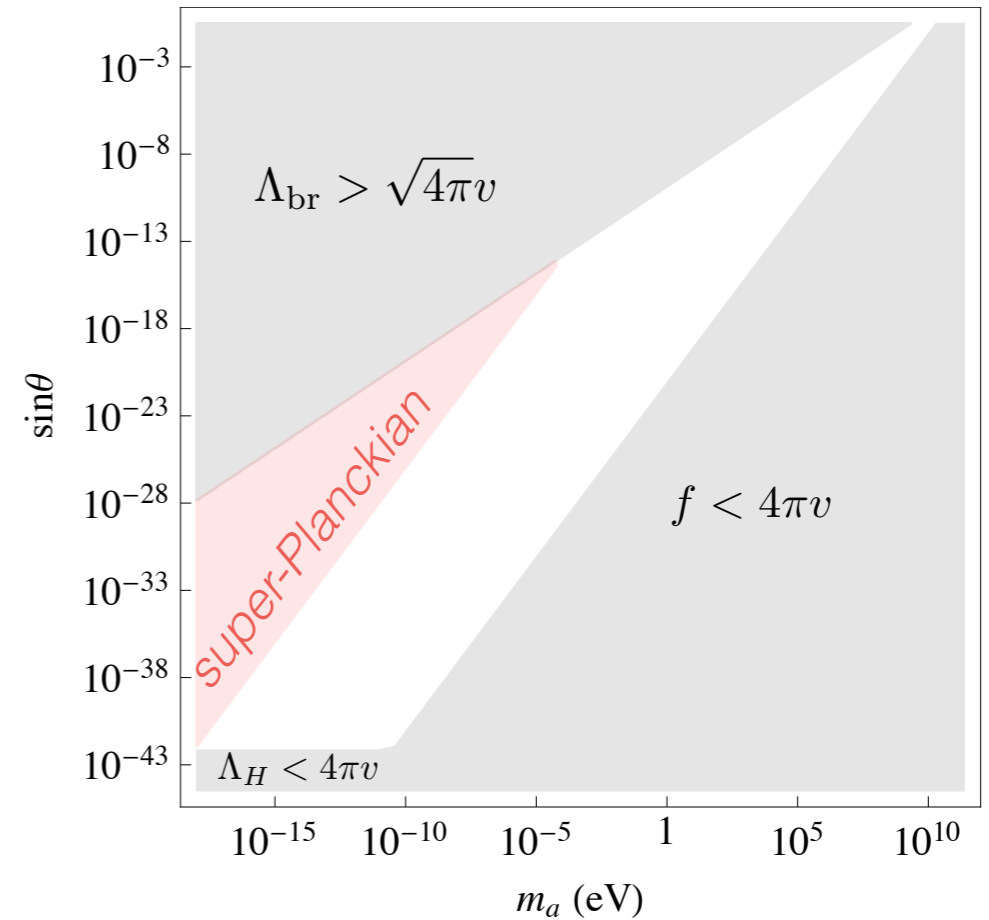
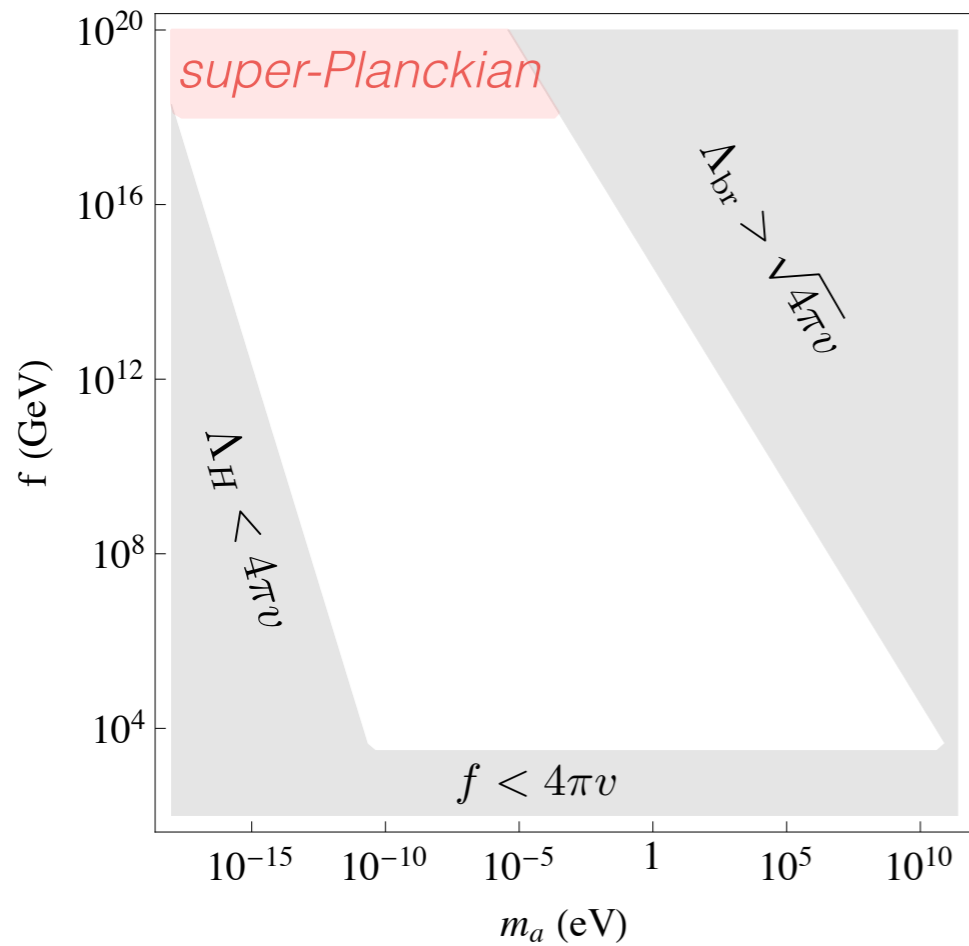
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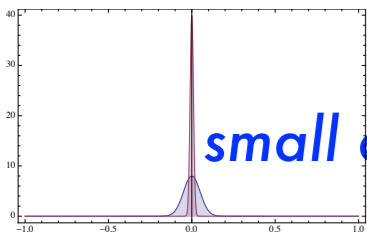


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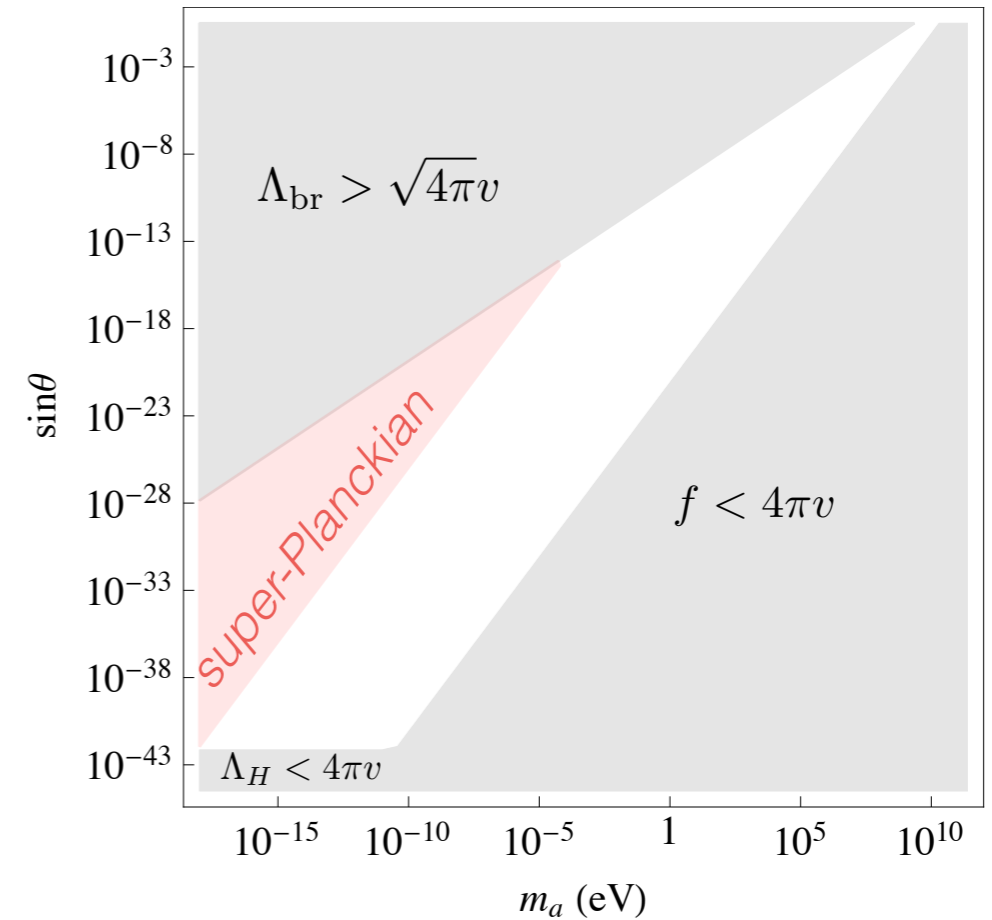
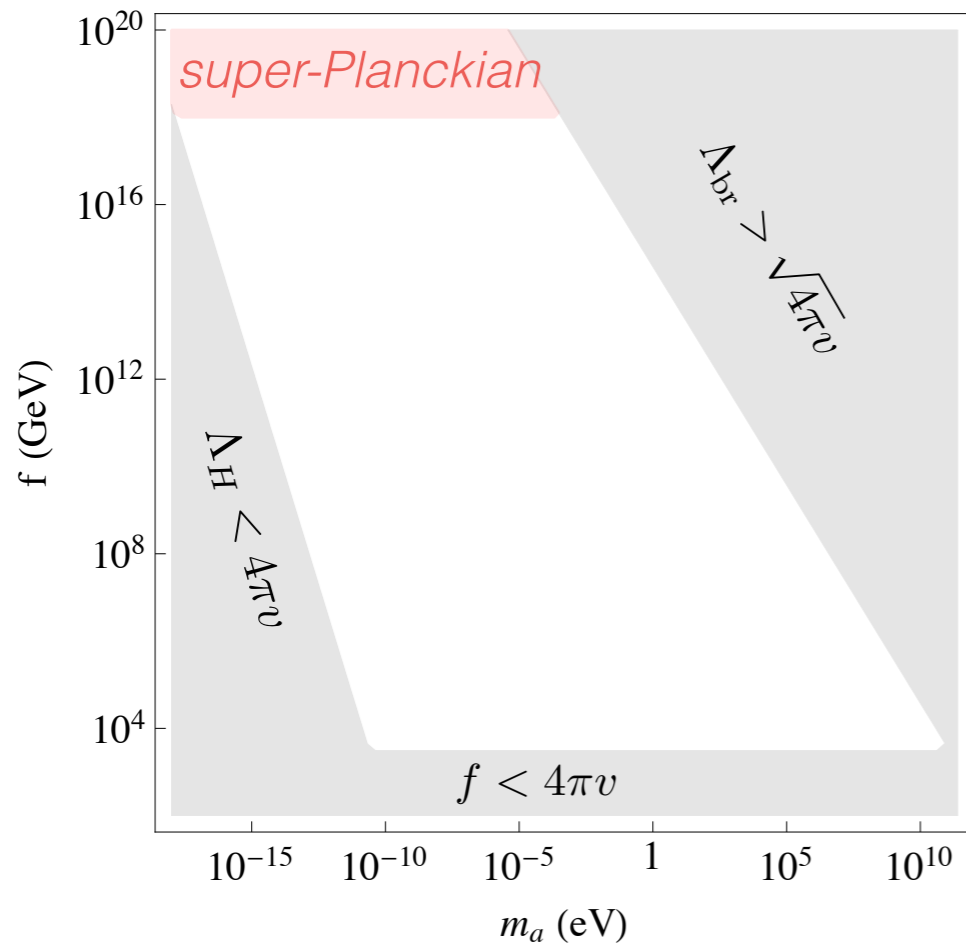
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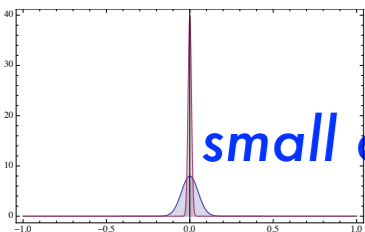


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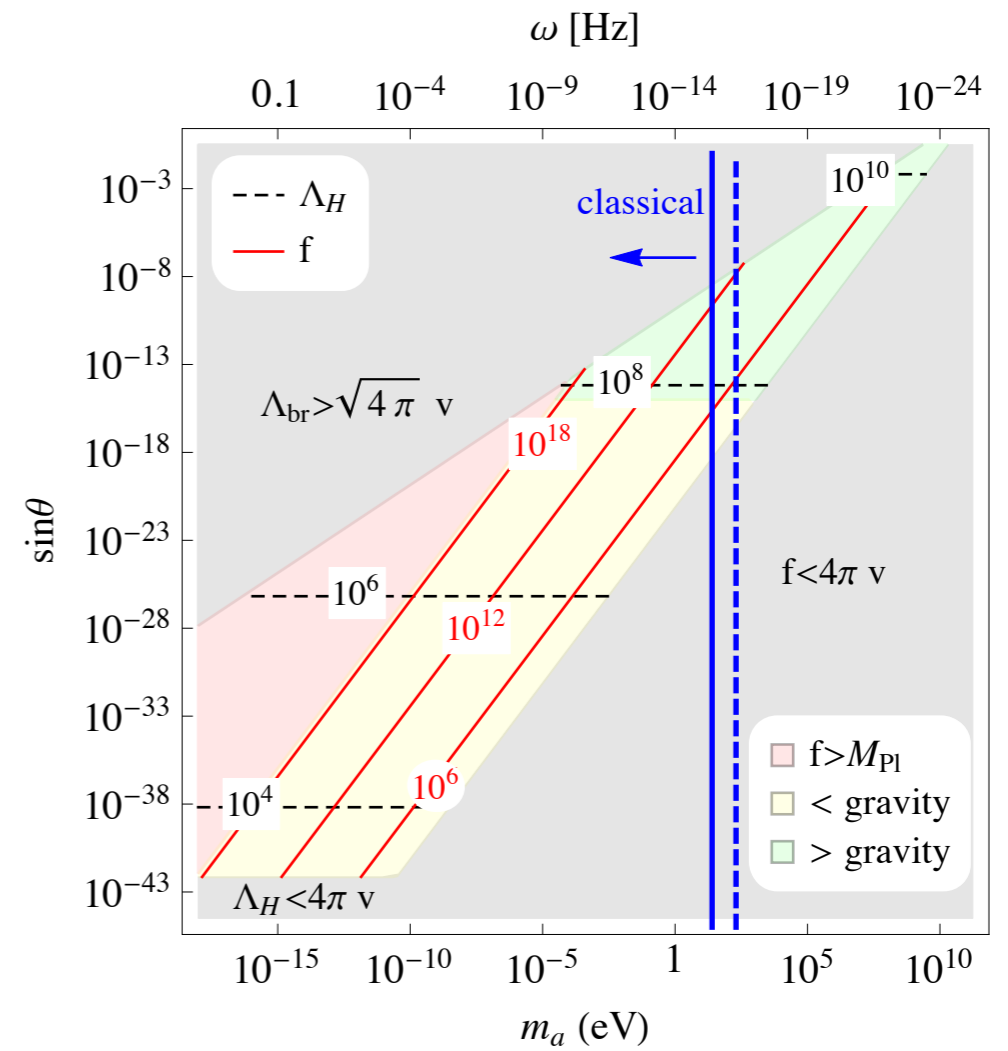
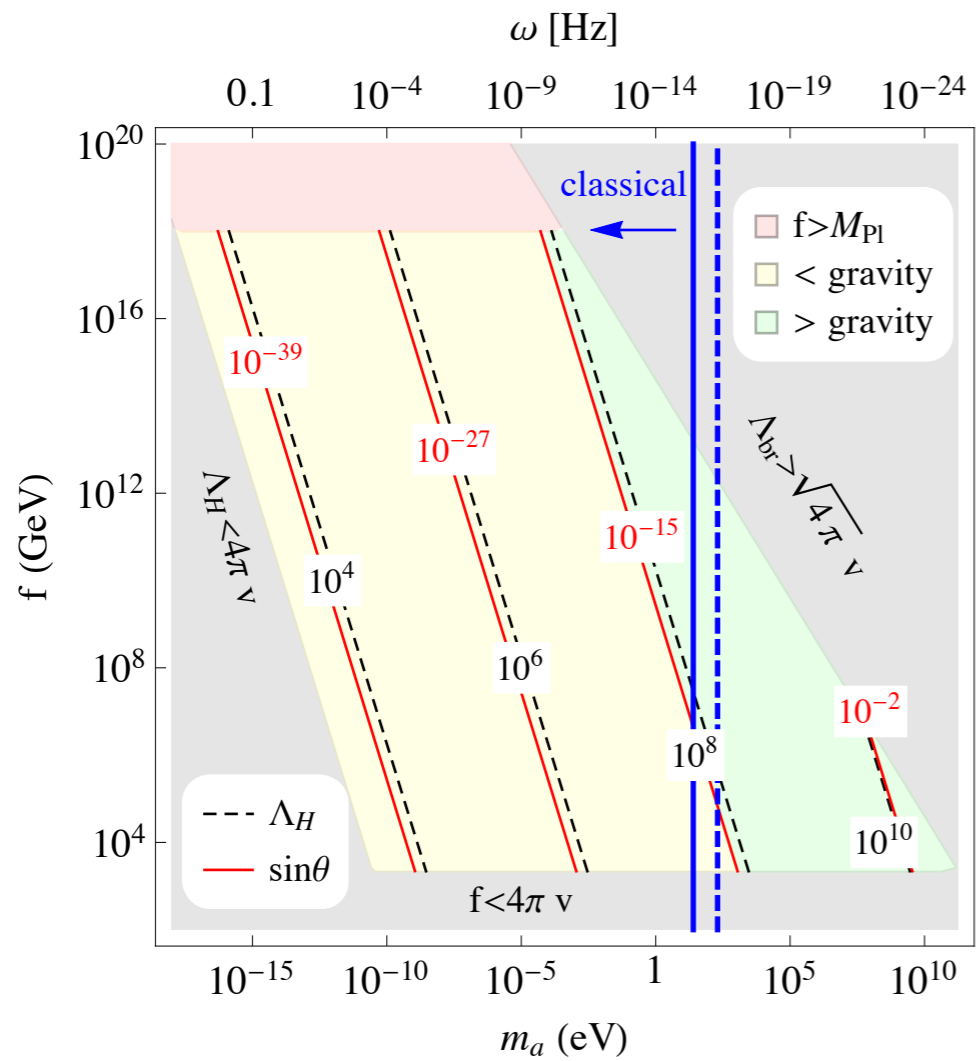
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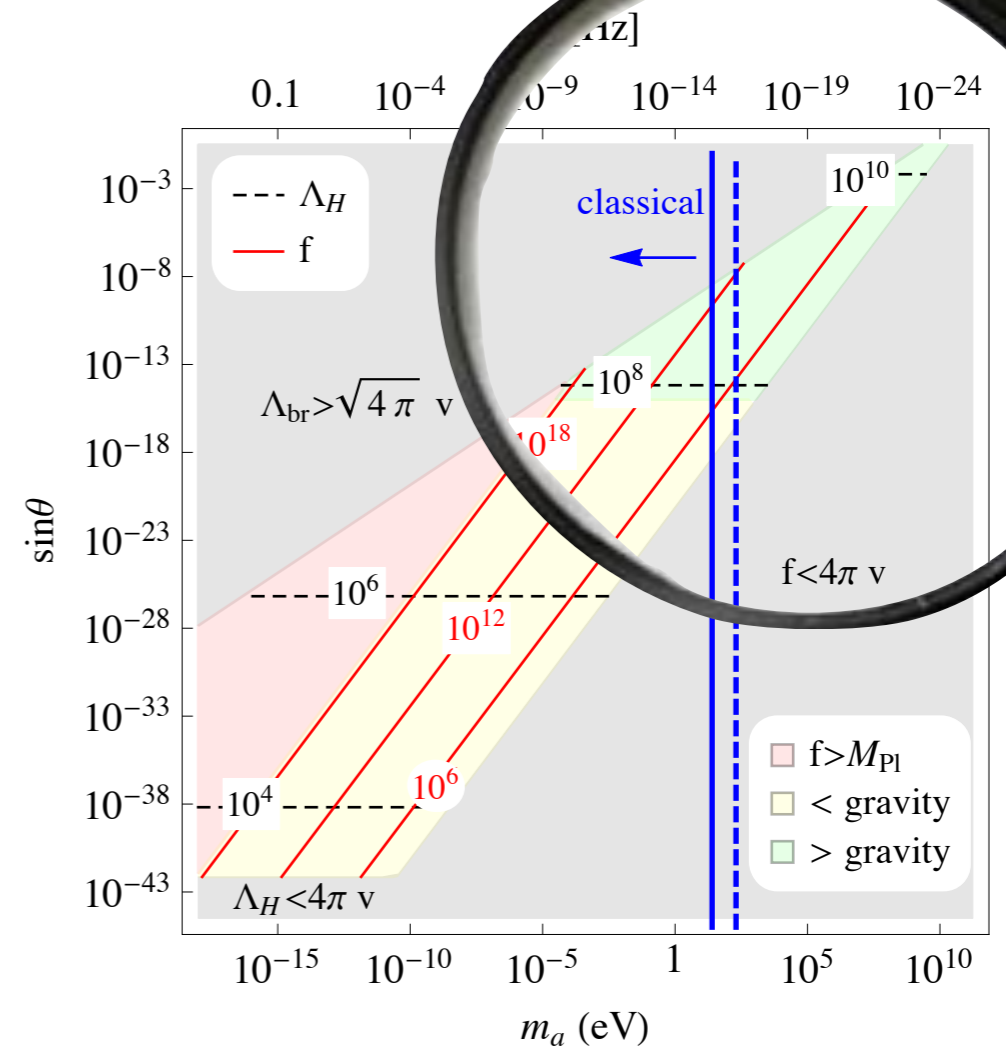
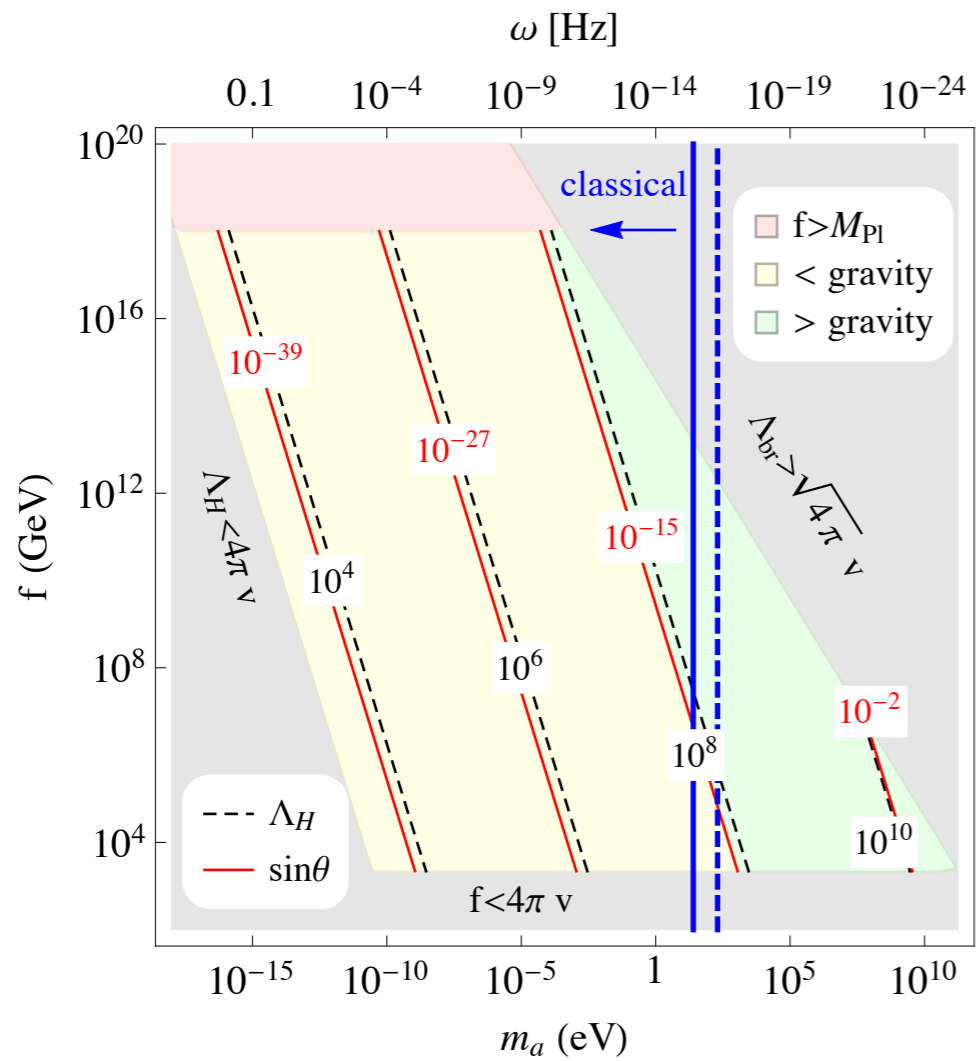
The relaxion parameter space



highest cut-off \longleftrightarrow highest mixing

TESTABLE SETUP

The relaxion parameter space

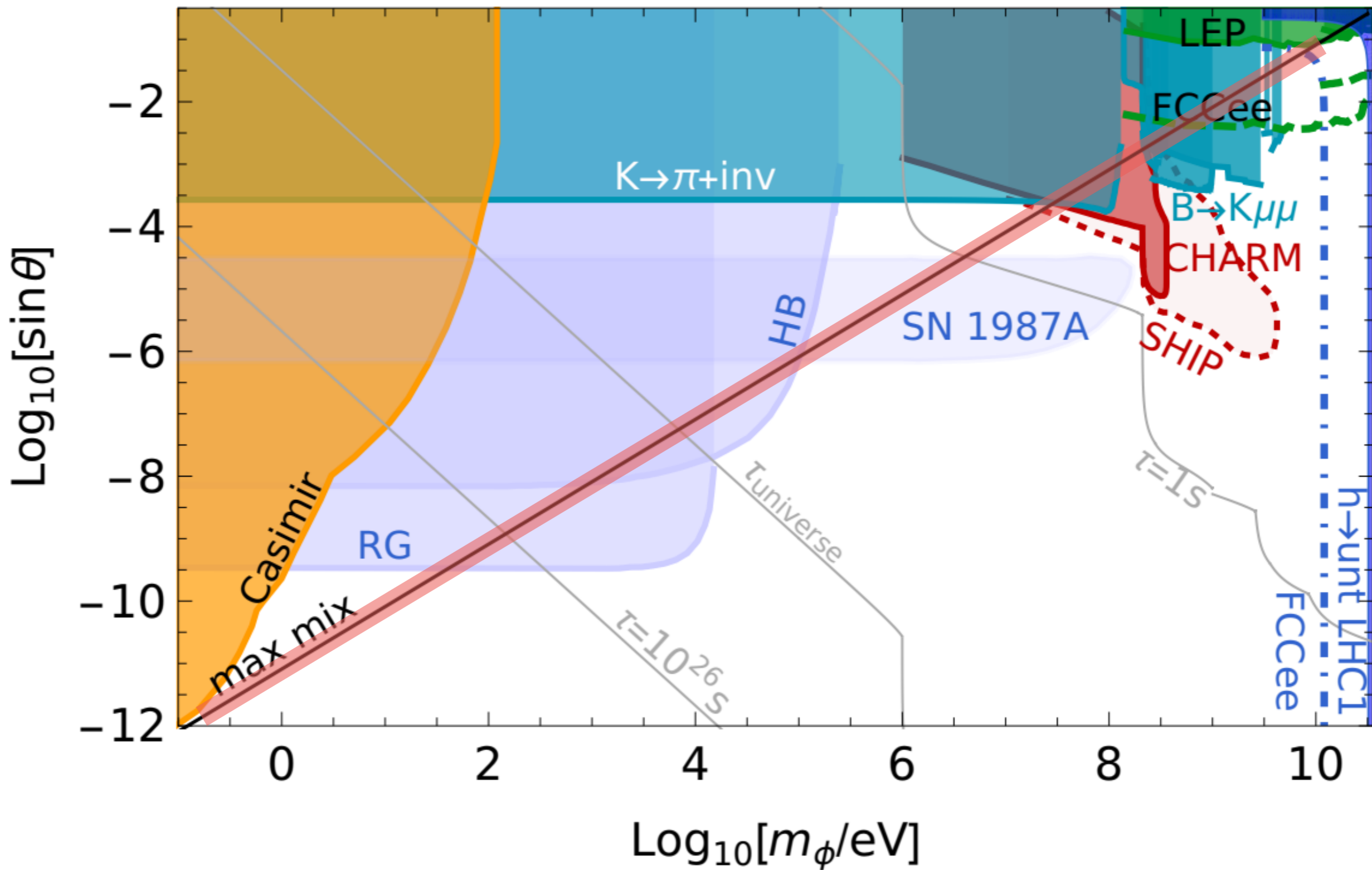


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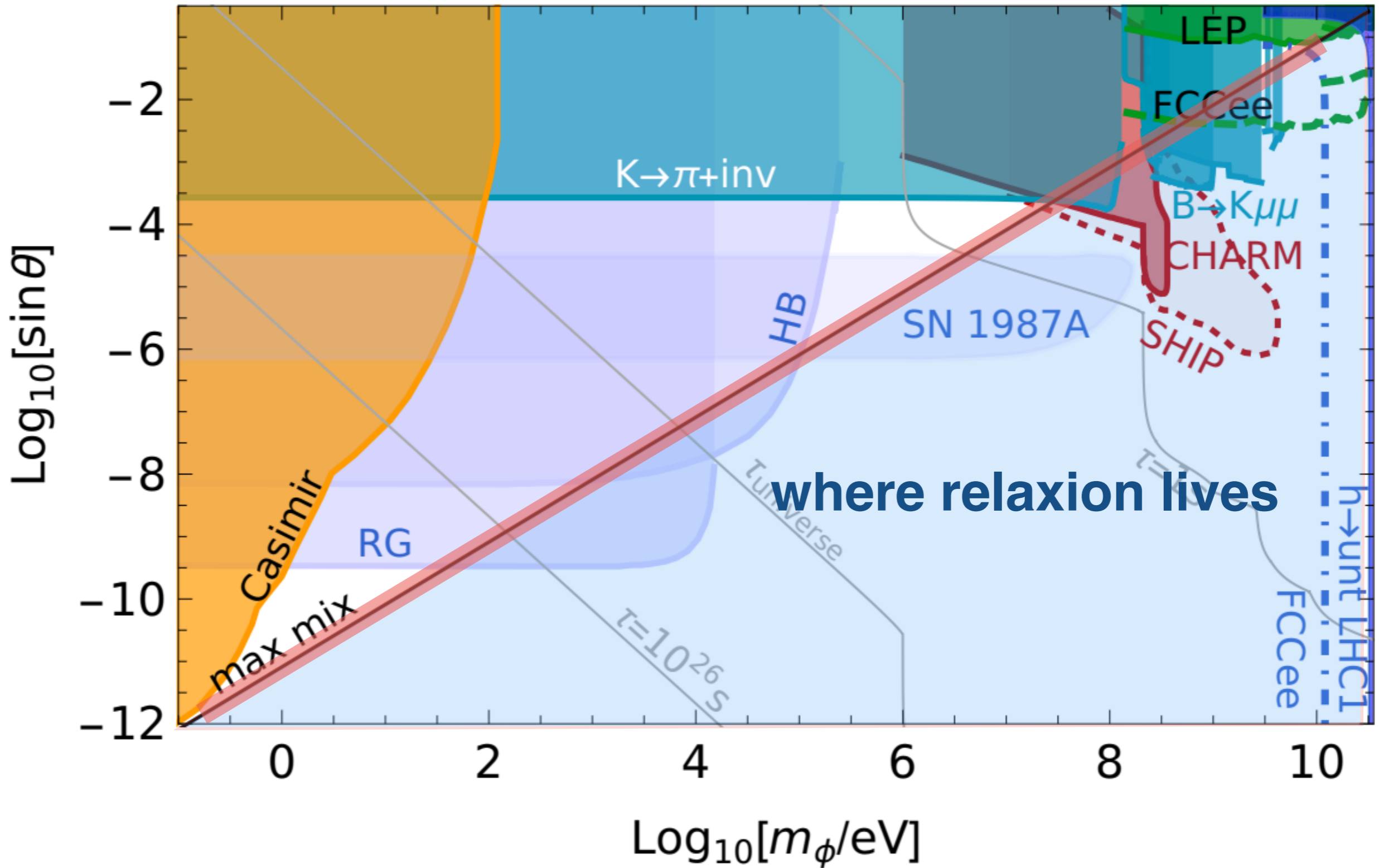
The Phenomenology is the one of a light Higgs portal

Frugiuele, Fuchs, Perez, Schlaffer '18



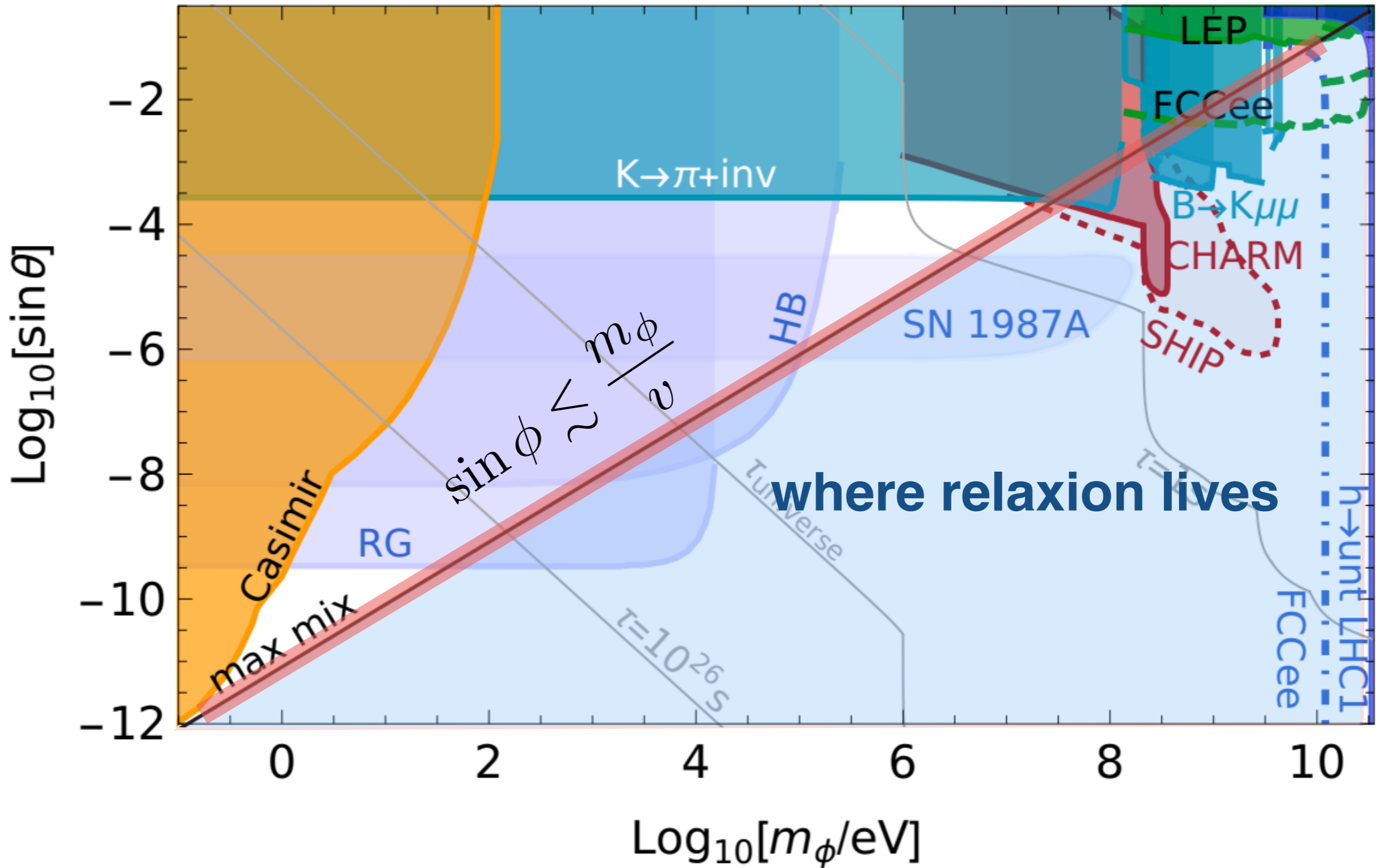
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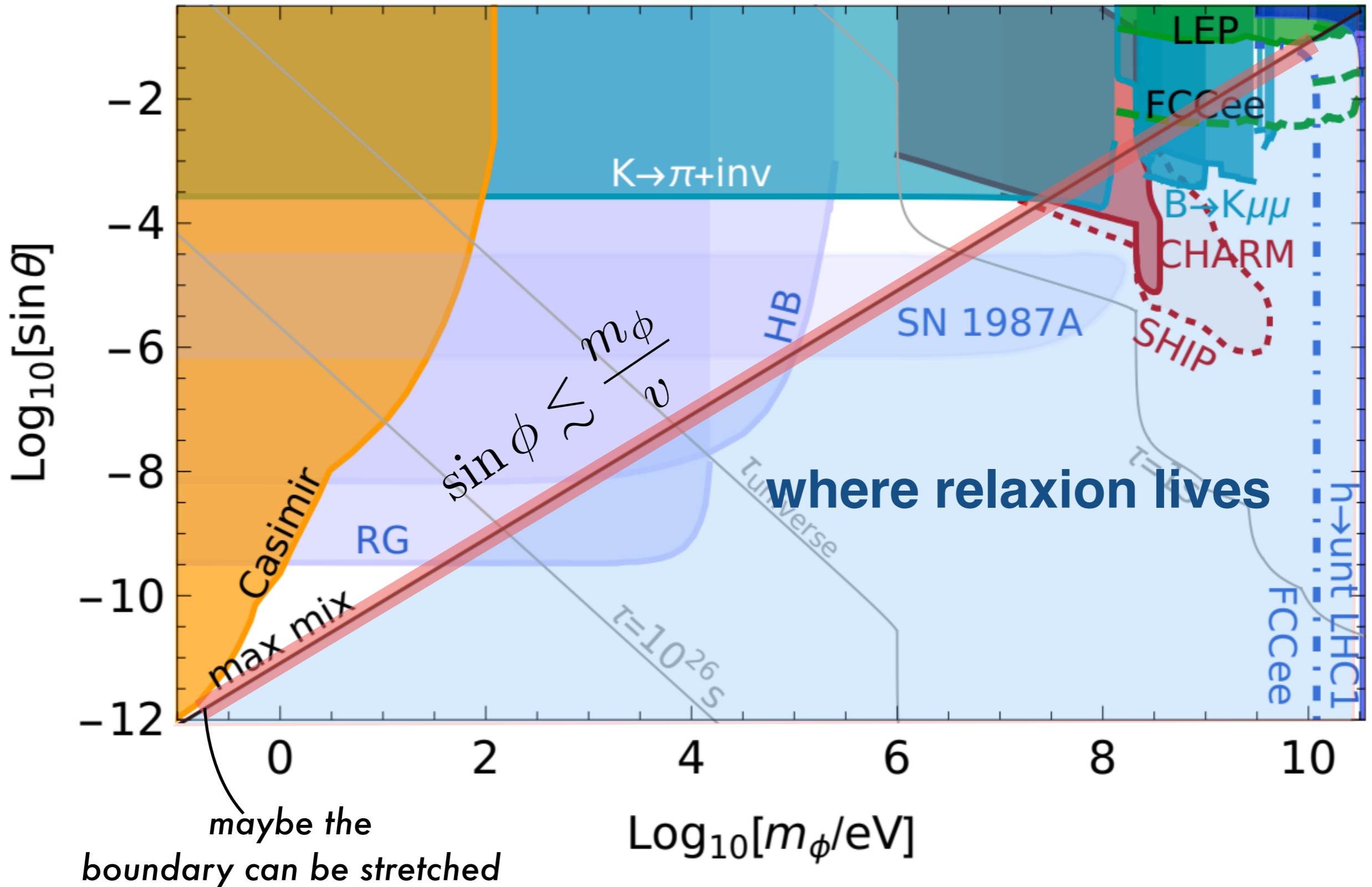
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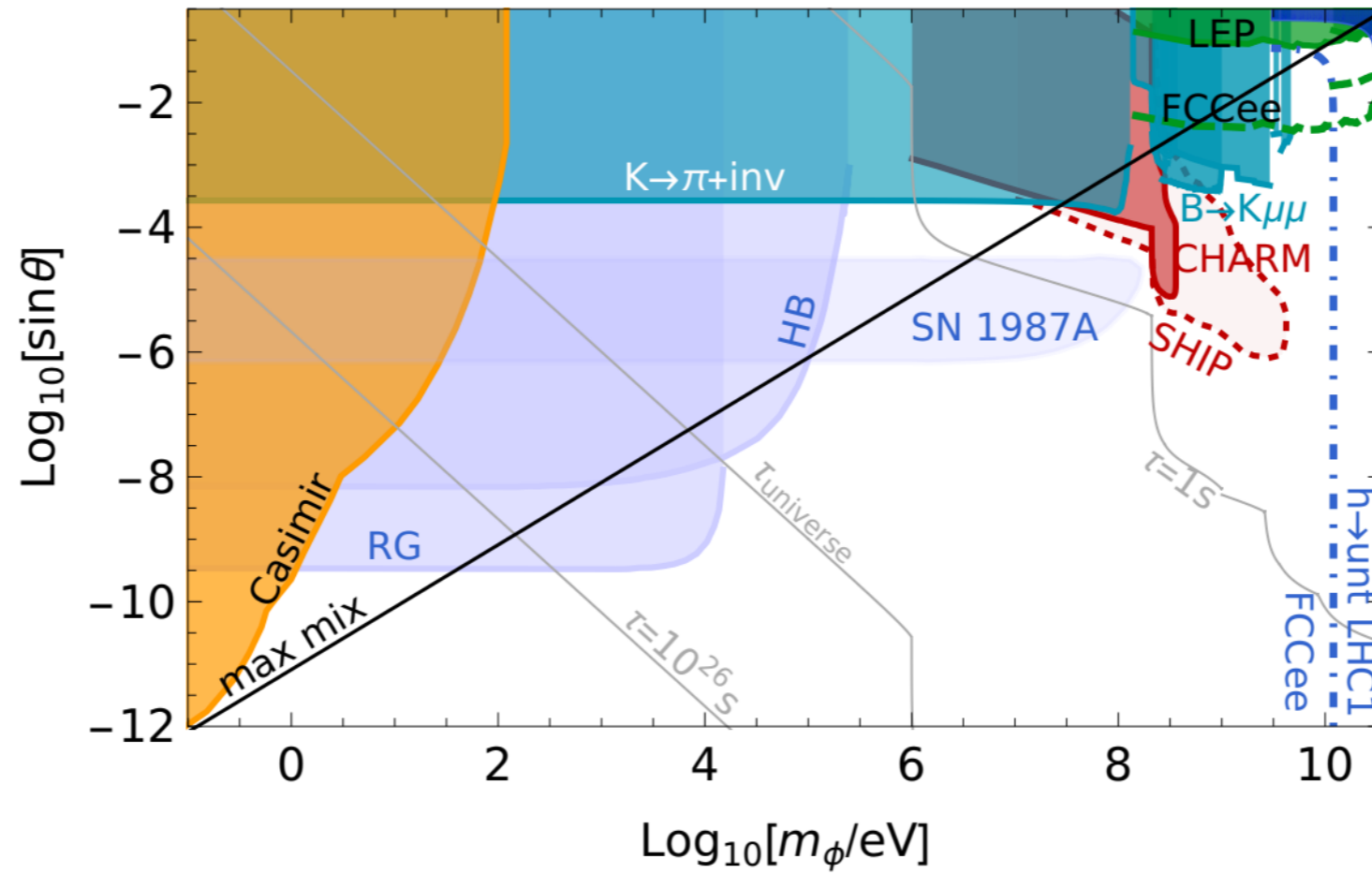


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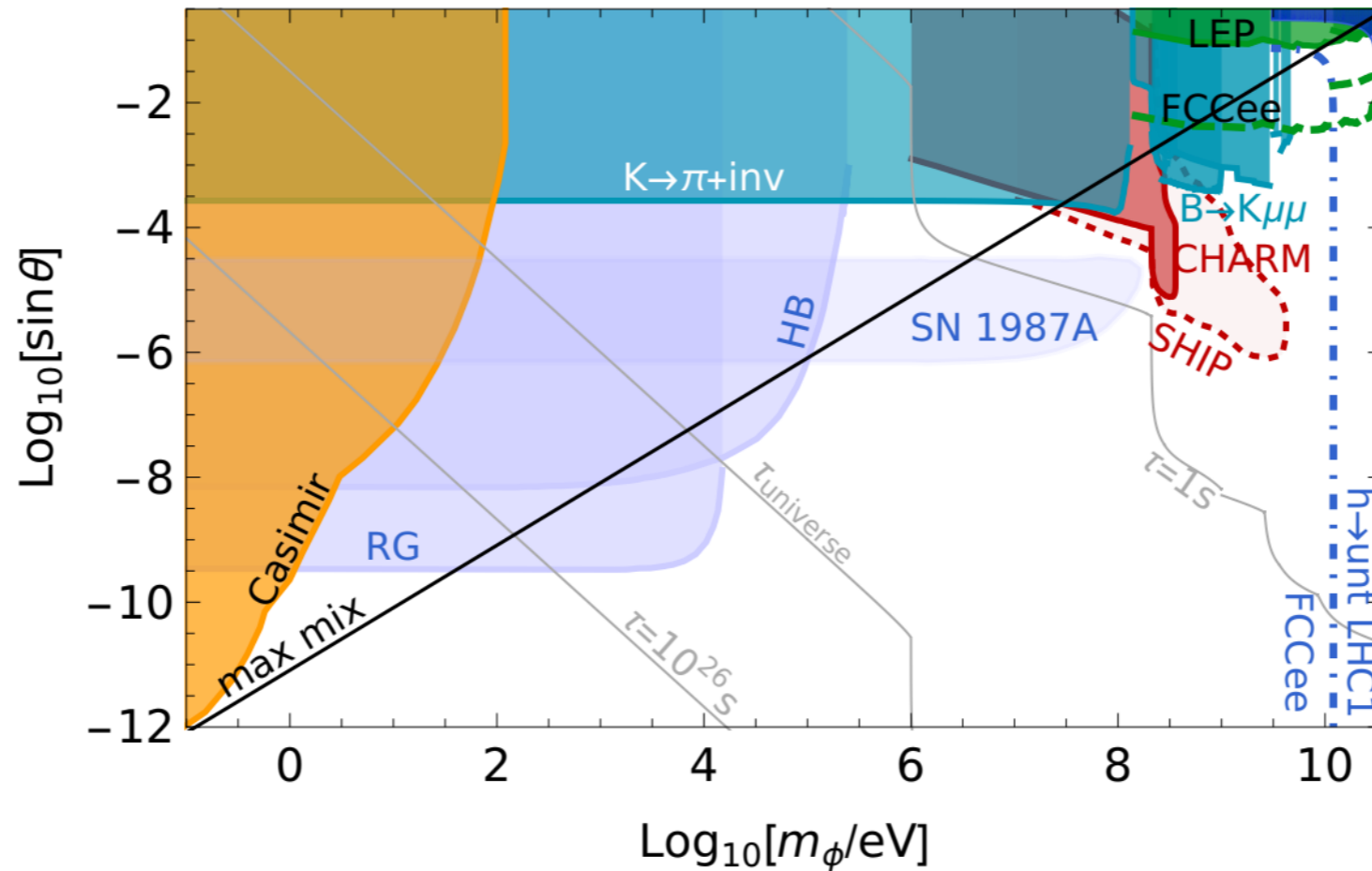


Different probes depending on the mass range



Different probes depending on the mass range

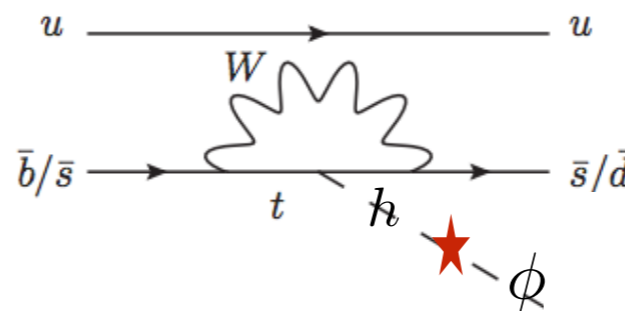
$$m_\phi > 0.1 \text{ GeV}$$



● Proton Beam Dump

$$N_{\text{dec}} \approx N_\phi \cdot \text{BR}(\phi \rightarrow l^+ l^-) \cdot e^{-\frac{L}{\tau}}$$

● Flavor transitions



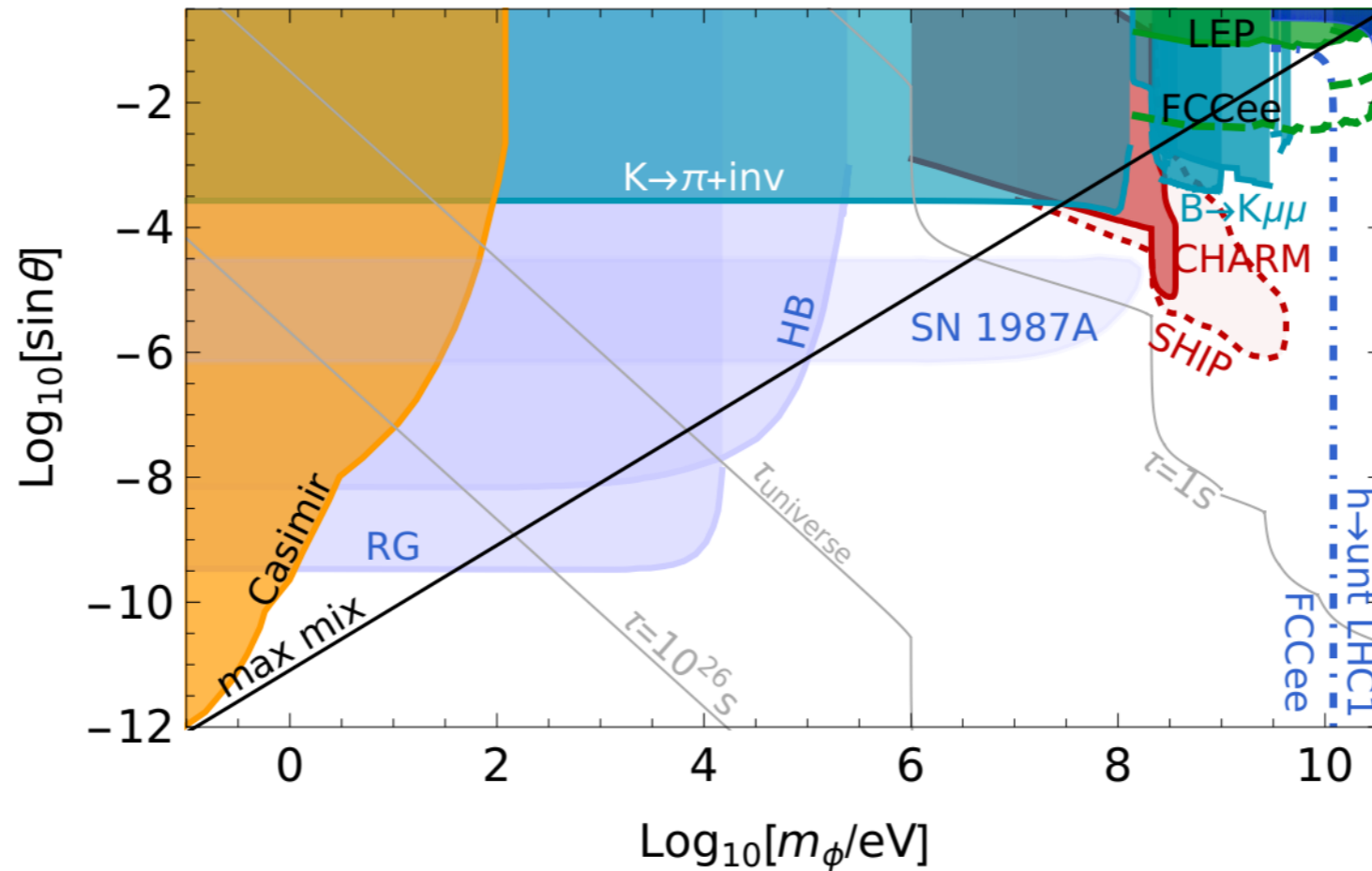
● colliders

$$\mu_h = \mu_h^{\text{SM}} \cos^2 \gamma$$

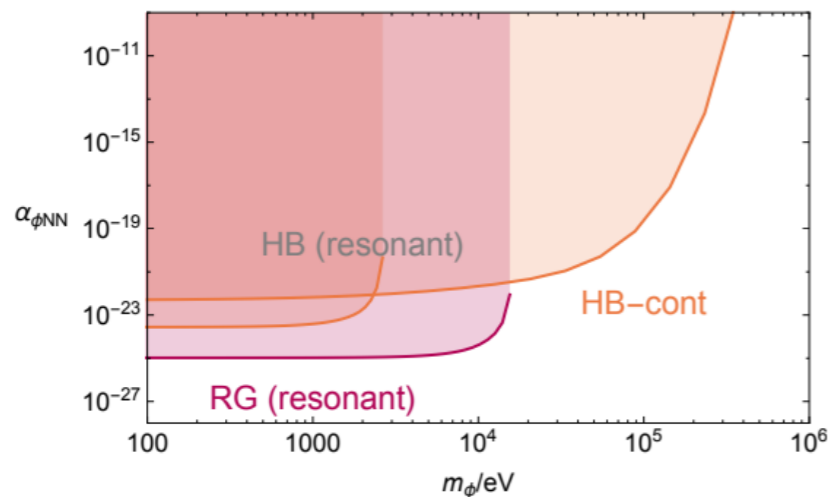
$$Z \rightarrow f \bar{f} \phi$$

Different probes depending on the mass range

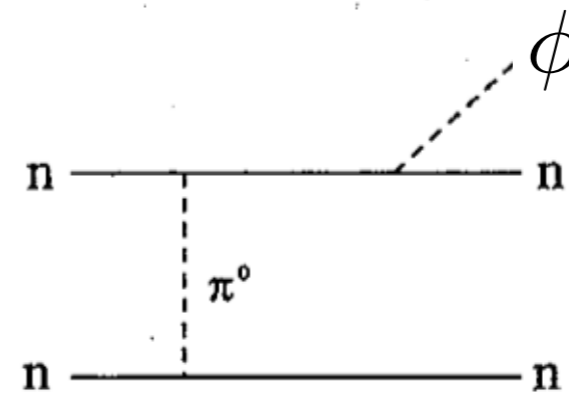
$$0.1 \text{ KeV} < m_\phi < 0.1 \text{ GeV}$$



● Star cooling *Hardy, Lasenby '17*



● Supernova neutrino flux

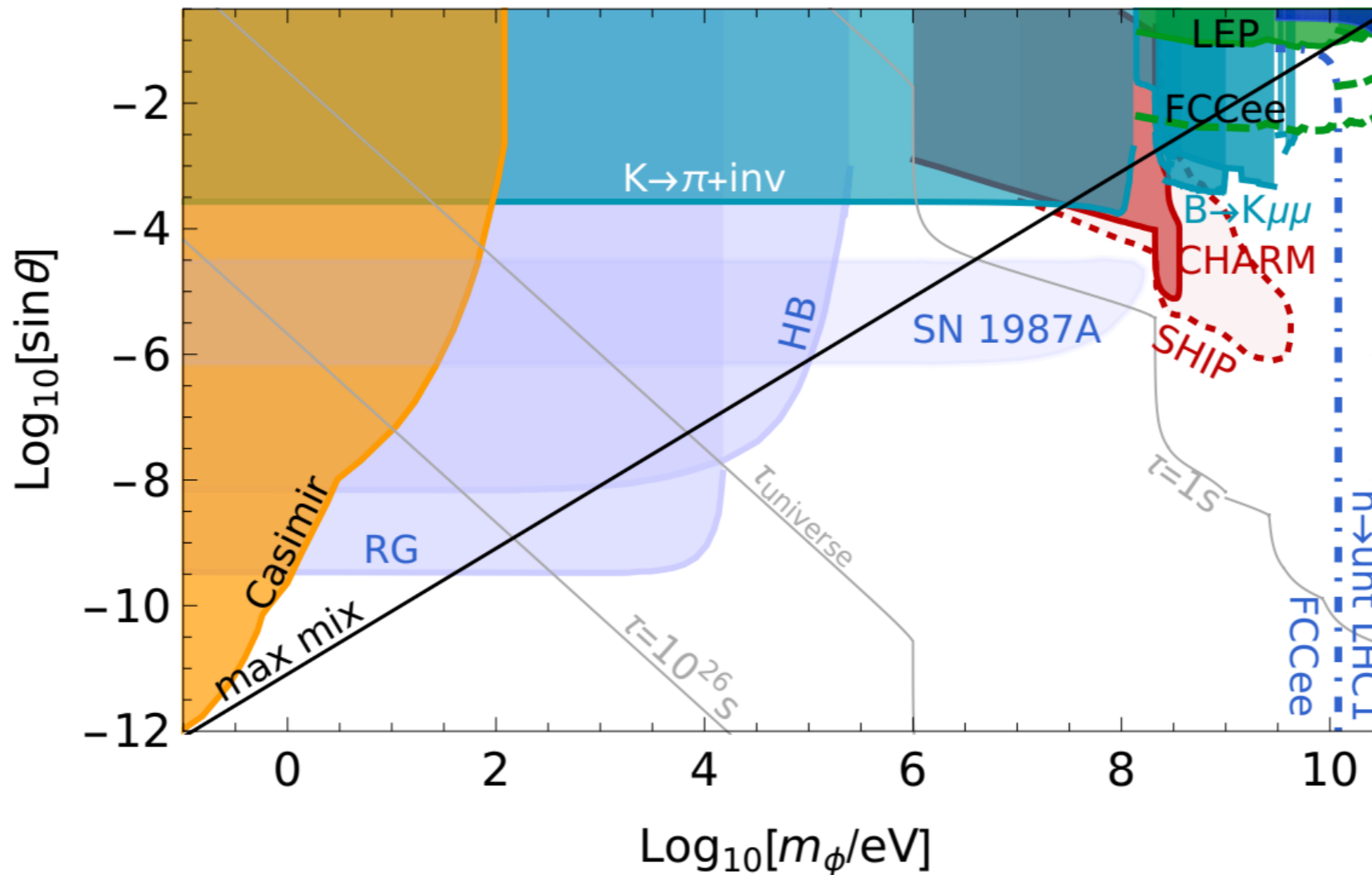


$$L_{NP} \lesssim 3 \cdot 10^{52} \text{ erg/s}$$

Ishizuka, Yoshimura '90

Different probes depending on the mass range

$$m_\phi < 100 \text{ eV}$$



- **5th force experiments** *see Andrew's talk*

$$V(r) = \frac{\alpha_{\text{eff}}}{r} e^{-m_\phi r}, \quad \text{through Higgs mixing we induce a long range force}$$

The Nelson Barr relaxation

narrows down the relaxation parameter space

$$V_{\text{roll}} = \frac{g_{u,d} \tilde{g}_{u,d} f^4}{16\pi^2} \cos \frac{\phi}{F}$$

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see M. Dine & P. Draper '15
L. Vecchi '14

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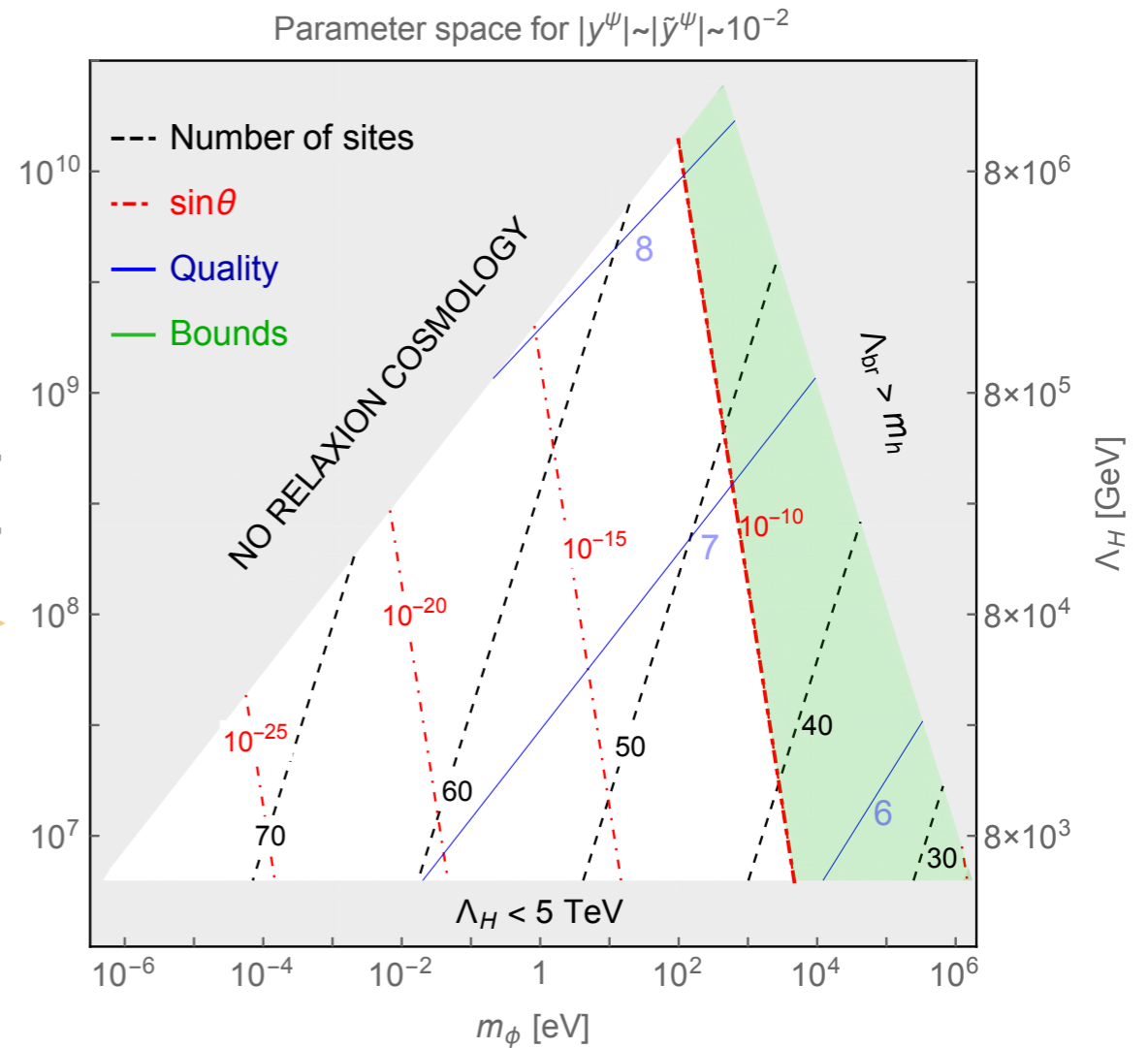
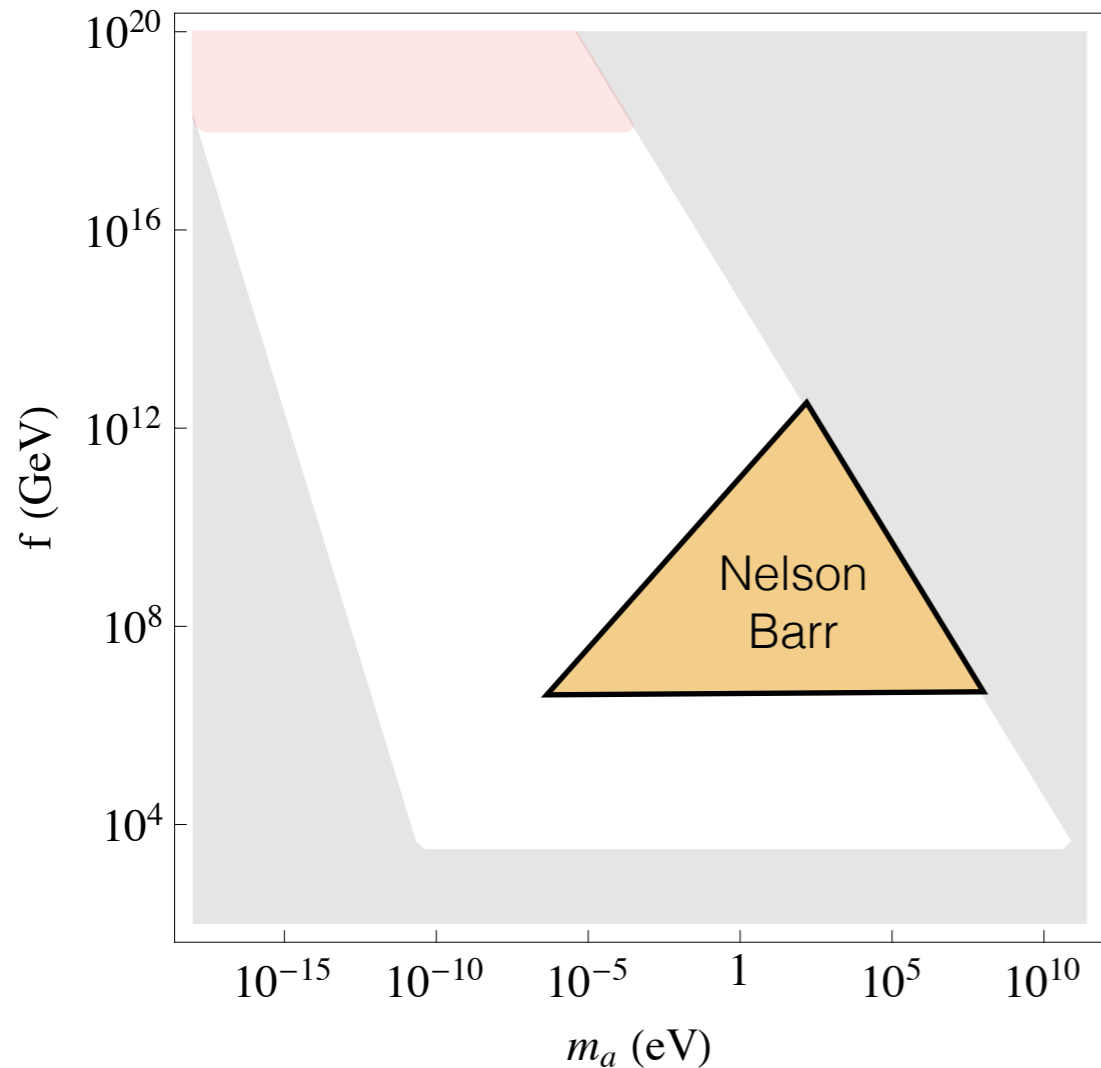
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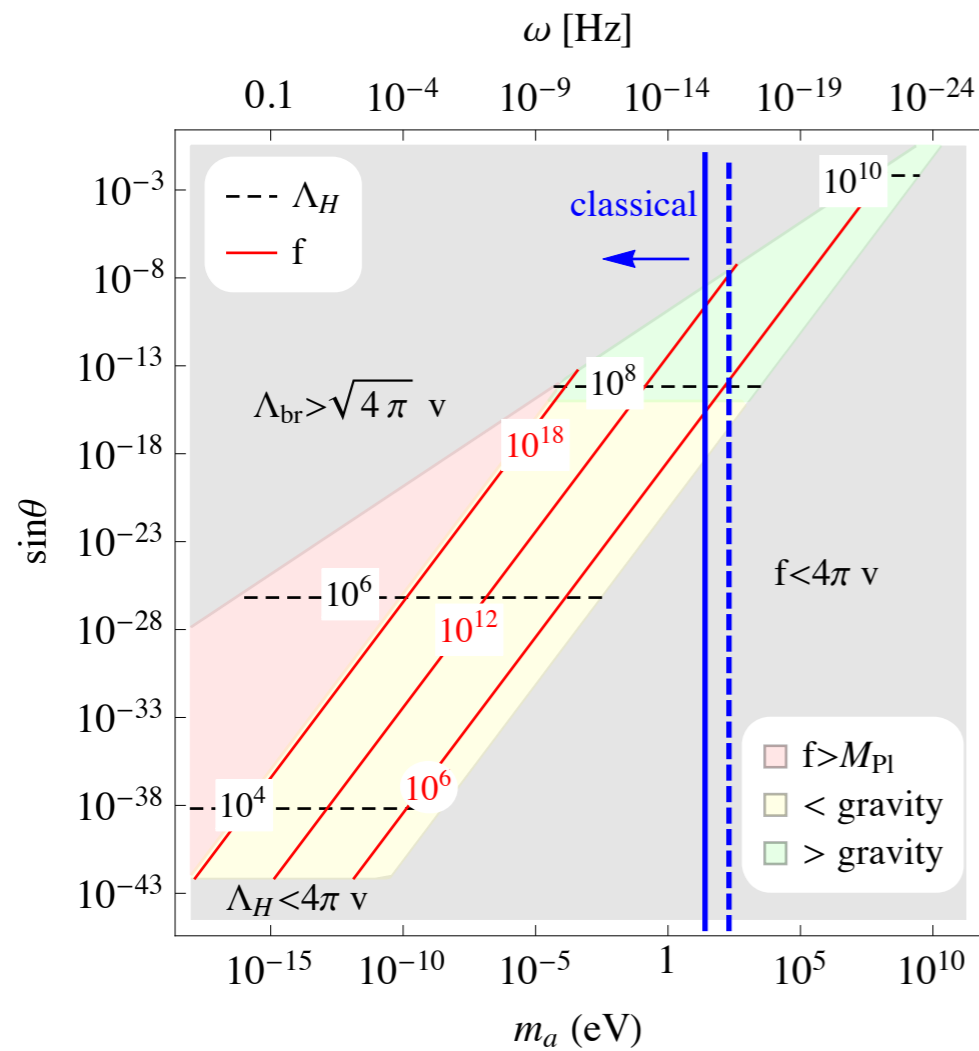


Davidi, Gupta, Perez, DR, Shalit '17

Can the Relaxion be a relic?

if produced cold (misalignment, during inflation, other?...) it would be a classical background

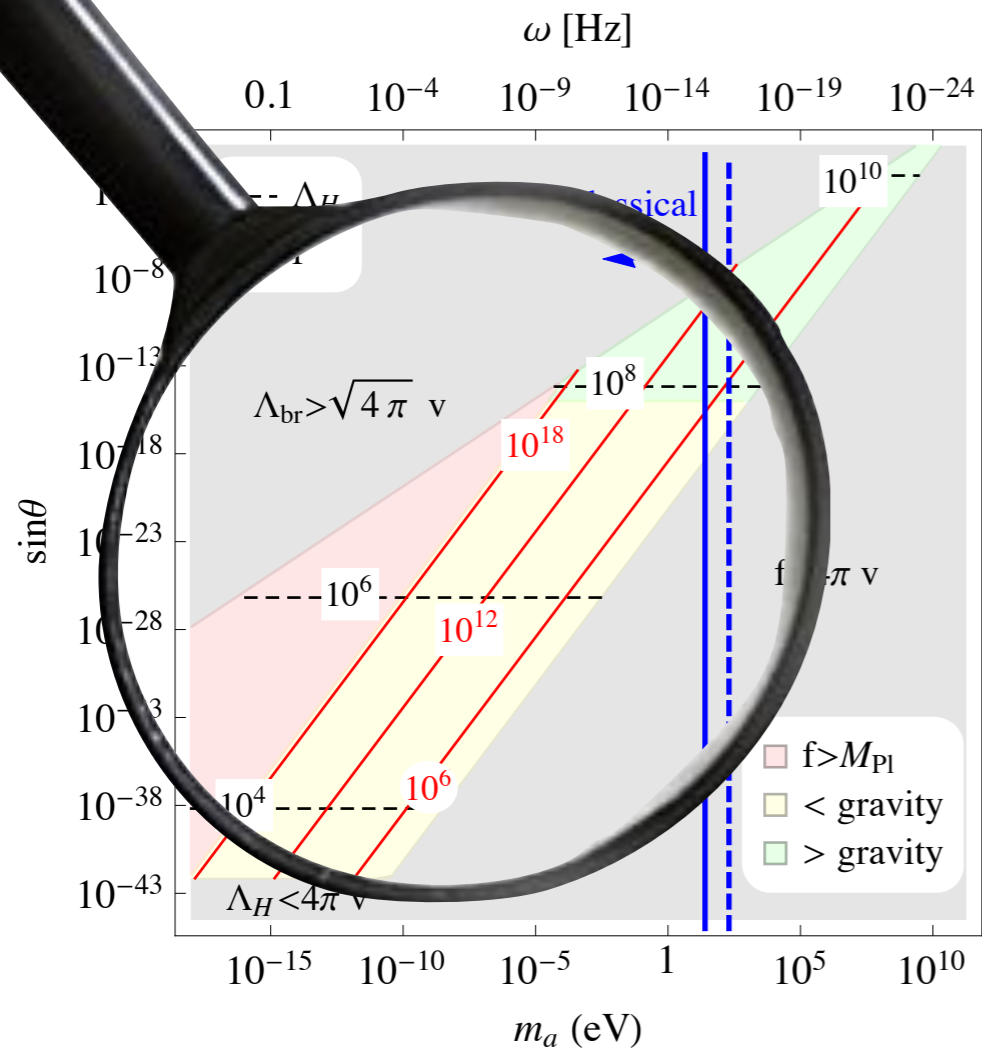
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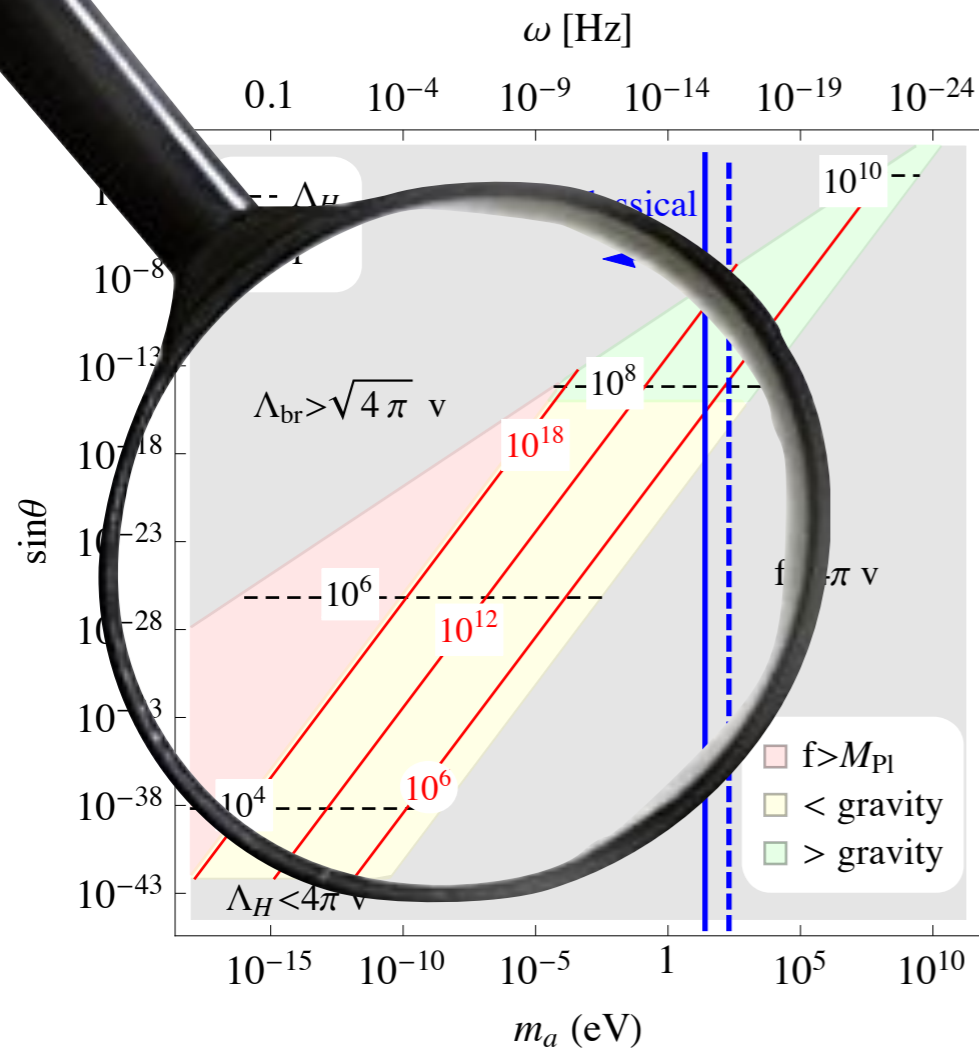
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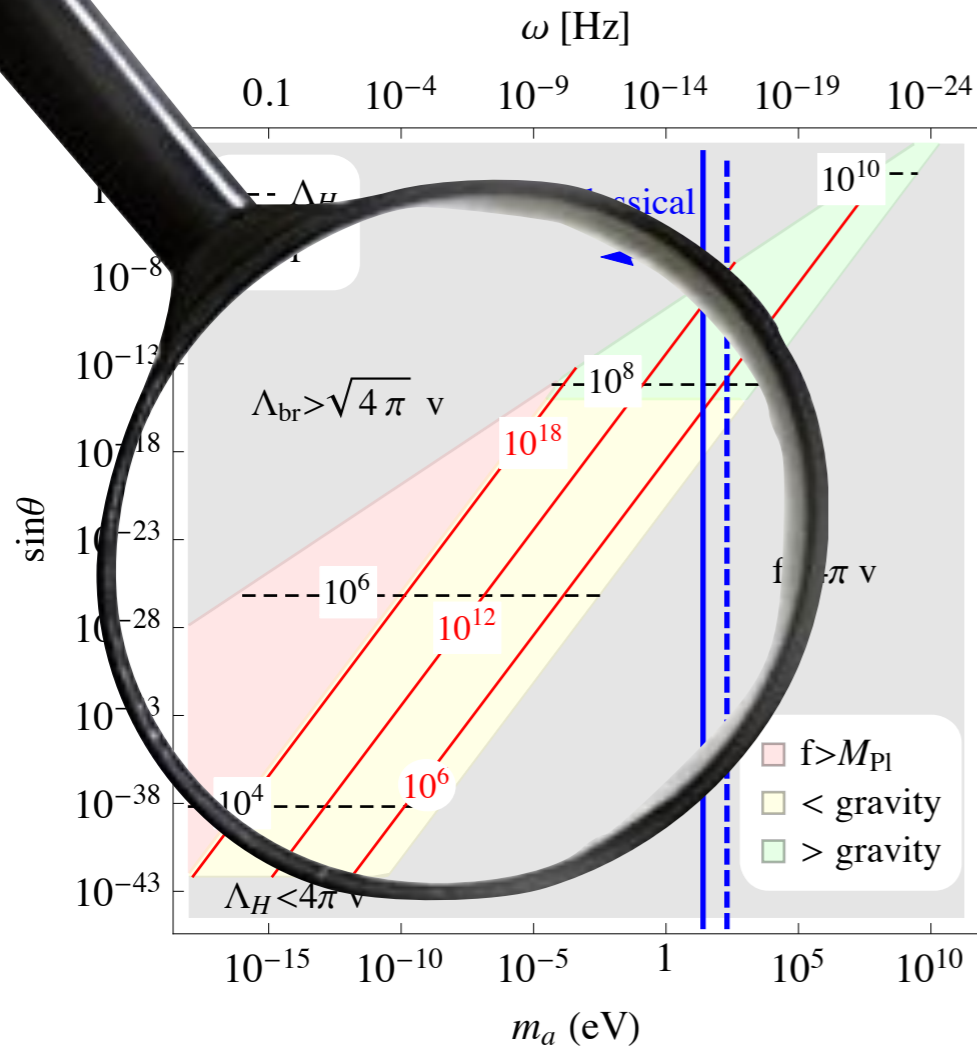
this might enhance detectability in the near future

- atomic clock experiments
- absorption
- ...

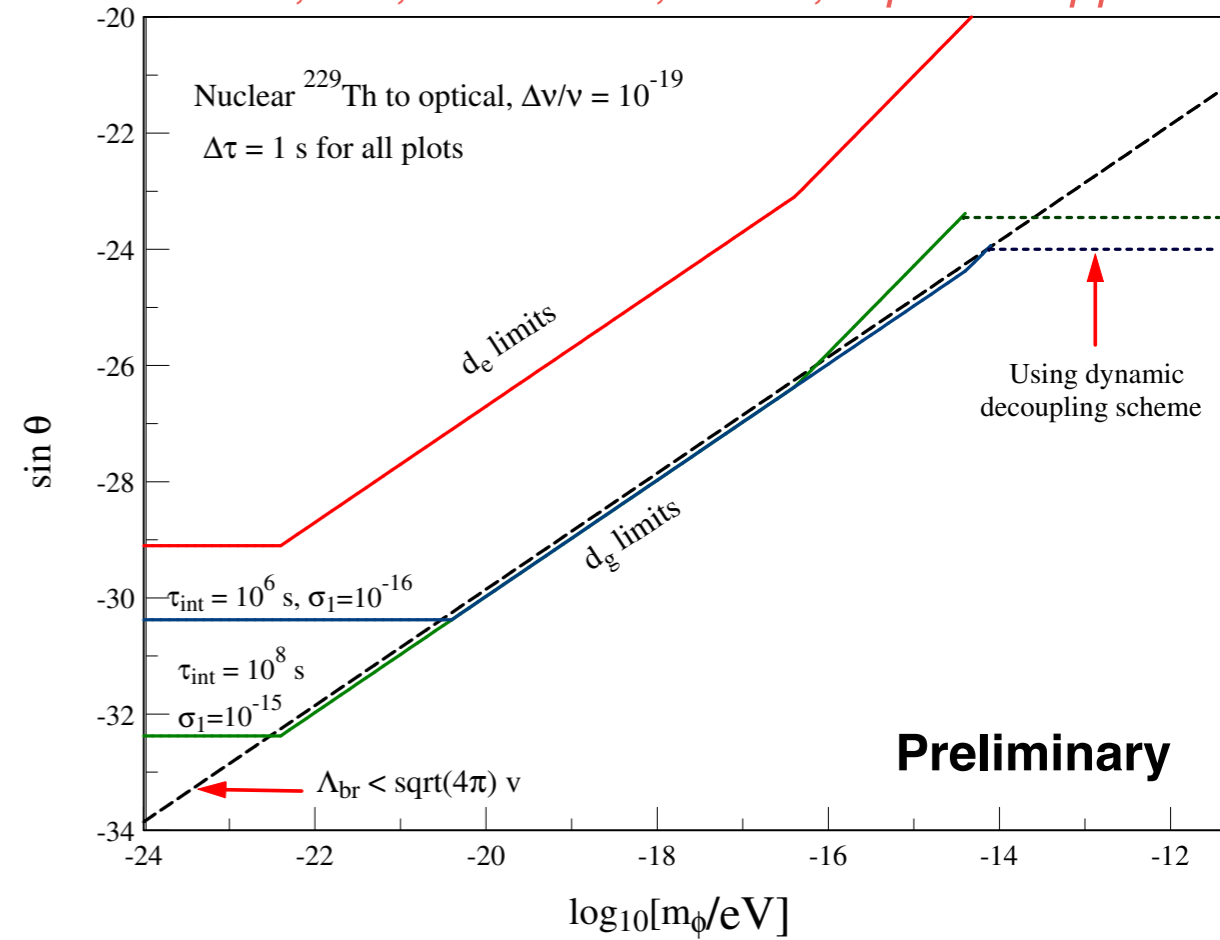
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Perez, DR, Safronova, Ubaldi, Zupan to appear



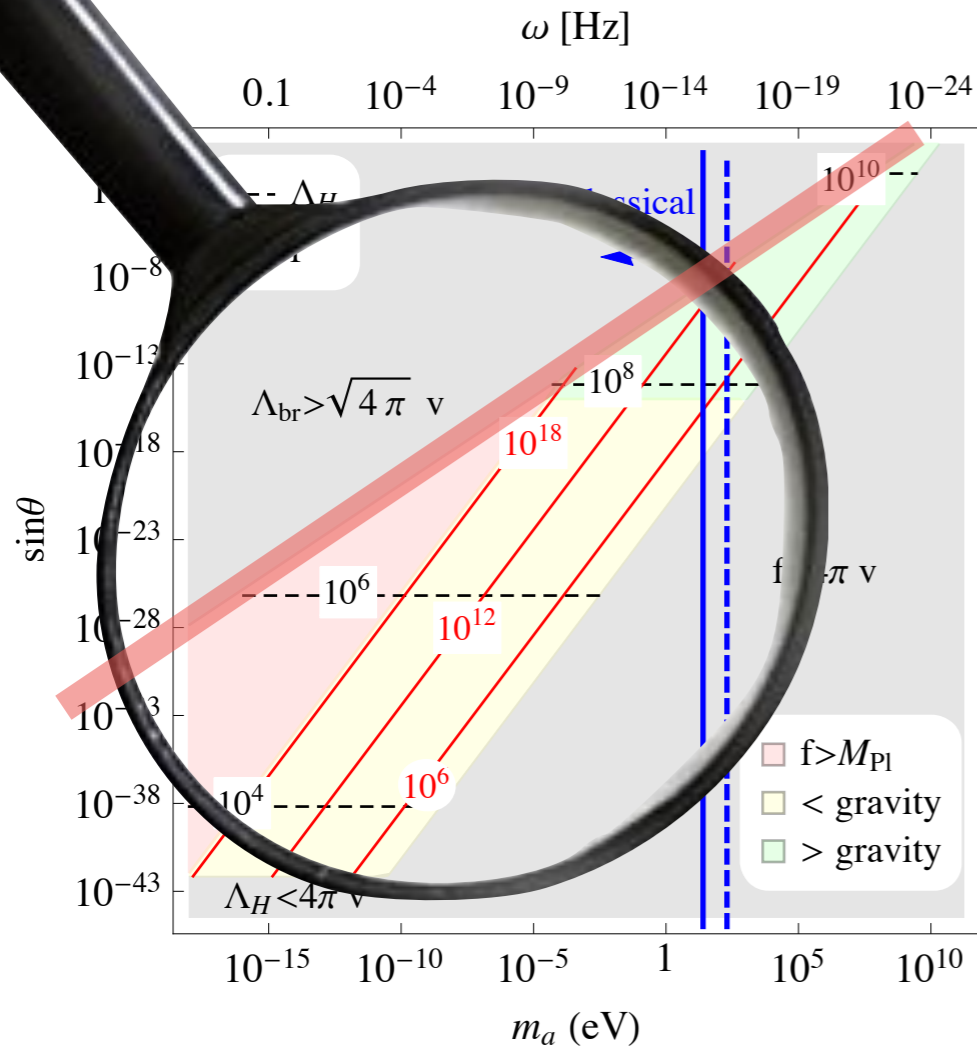
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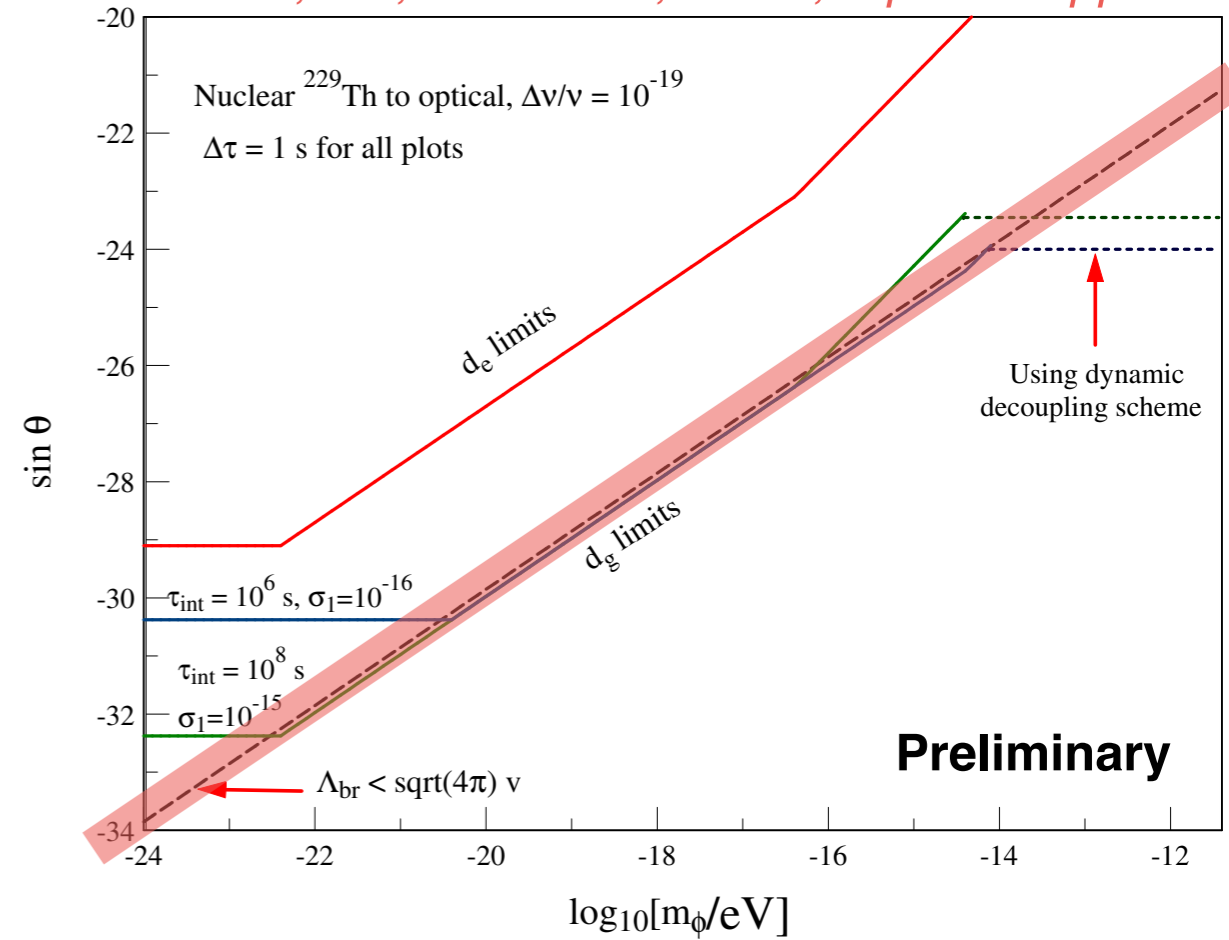
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It touches the boundary of the parameter space!

Wiggles without EW states

(Davidi, Gupta, Perez, DR, Shalit '18)


We use sterile neutrinos $\mathcal{L}_{\text{NP}} \supset Y_N \tilde{H} L N^c$

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Froggatt-Nielsen texture to ensure $\left\{ \begin{array}{l} \Lambda_{\text{br}} \gtrsim M_{\text{br}} \text{ (where } M_{\text{br}} \text{ is the scale of sterile neutrinos)} \\ \text{neutrino masses for free} \end{array} \right.$



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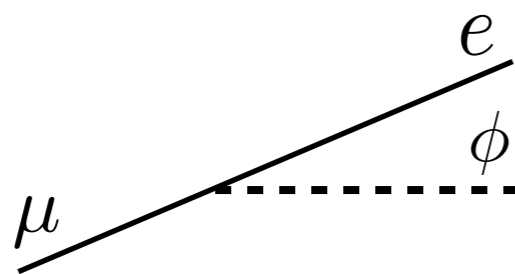
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FV lepton decays

VS

star cooling



$$\Gamma(\mu \rightarrow e\phi) \simeq \frac{m_e^2 m_\mu}{16\pi f^2}$$

Compton	
Pair Annihilation	
Electromagnetic Bremsstrahlung	

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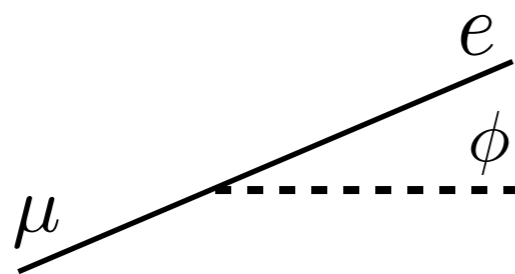
$$\mathcal{L}_\phi \supset \frac{iv\phi}{f} (L_j + e_k^c) (Y_e)_{jk} e_j e_k^c$$

This is an axion-like coupling!

FV lepton decays

VS

star cooling

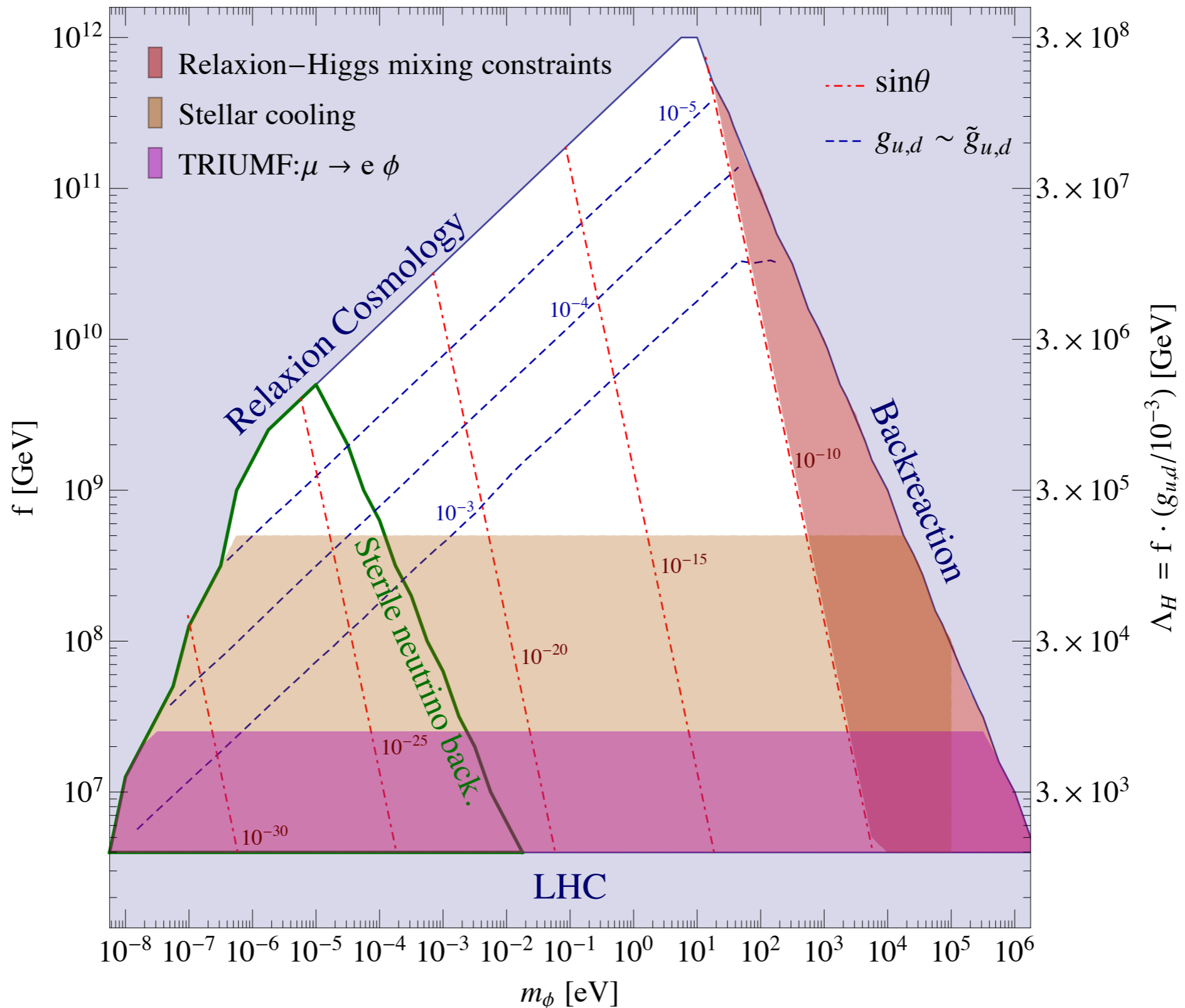


$$\Gamma(\mu \rightarrow e\phi) \simeq \frac{m_e^2 m_\mu}{16\pi f^2}$$

Compton	
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Star cooling gives the most stringent bound!

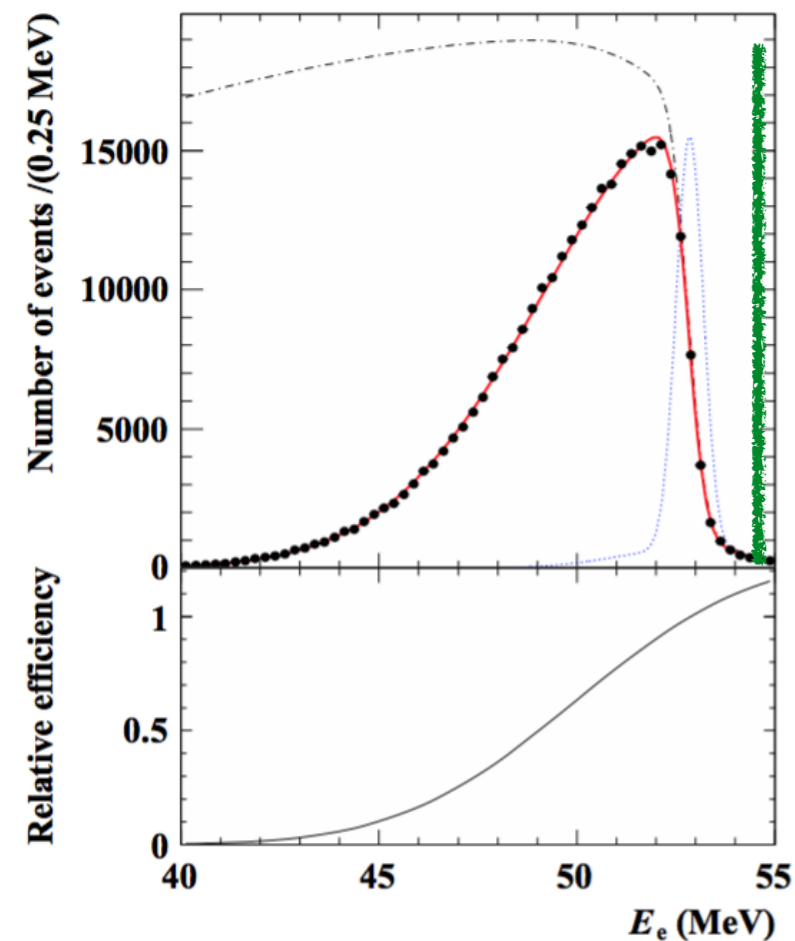
Davidi, Gupta, Perez, DR, Shalit '17



Can we increase the sensitivity of future experiments?

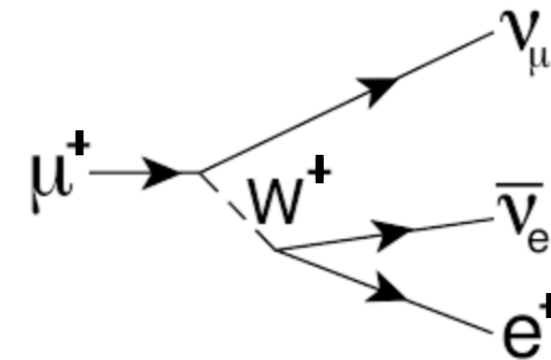
Learning from the past...

$$\text{TRIUMF (1988)} \approx 10^7 \mu \quad \left| \quad \text{BR}(\mu \rightarrow e + a) \lesssim 3 \cdot 10^{-6} \quad \right| \quad f_a \gtrsim 10^7 \text{ GeV}$$



The signal is a line at $E_e \approx \frac{m_\mu}{2}$

The background comes from



The peak of the Michel spectrum depend on the muon polarization

IT IS ZERO in the OPPOSITE direction to the muon polarization!

More recent experiments...

CRYSTAL BOX (1988)

$10^{12} \mu$

$$\text{BR}(\mu \rightarrow e + a + \gamma) \lesssim 1 \cdot 10^{-9}$$

$$f_a \gtrsim 10^6 \text{ GeV}$$

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MEG with $10^{14} \mu$? **no analysis but naively:** $\text{BR}(\mu \rightarrow e + a + \gamma) \lesssim 1 \cdot 10^{-9} \cdot \frac{1}{\sqrt{100}}$

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MEG II ?

Mu3e ?

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MEG II ?

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GENERAL LESSON HERE:

- Flavor experiment can be extremely good at probing light new states
- They compete/complement with astro in some region of the par. space
- Optimised searches on many motivated final states need still to be done

(more examples @ NA62 and LHCb)

See talk by Filippo Sala

NA62 highly constraint the quark FV interactions

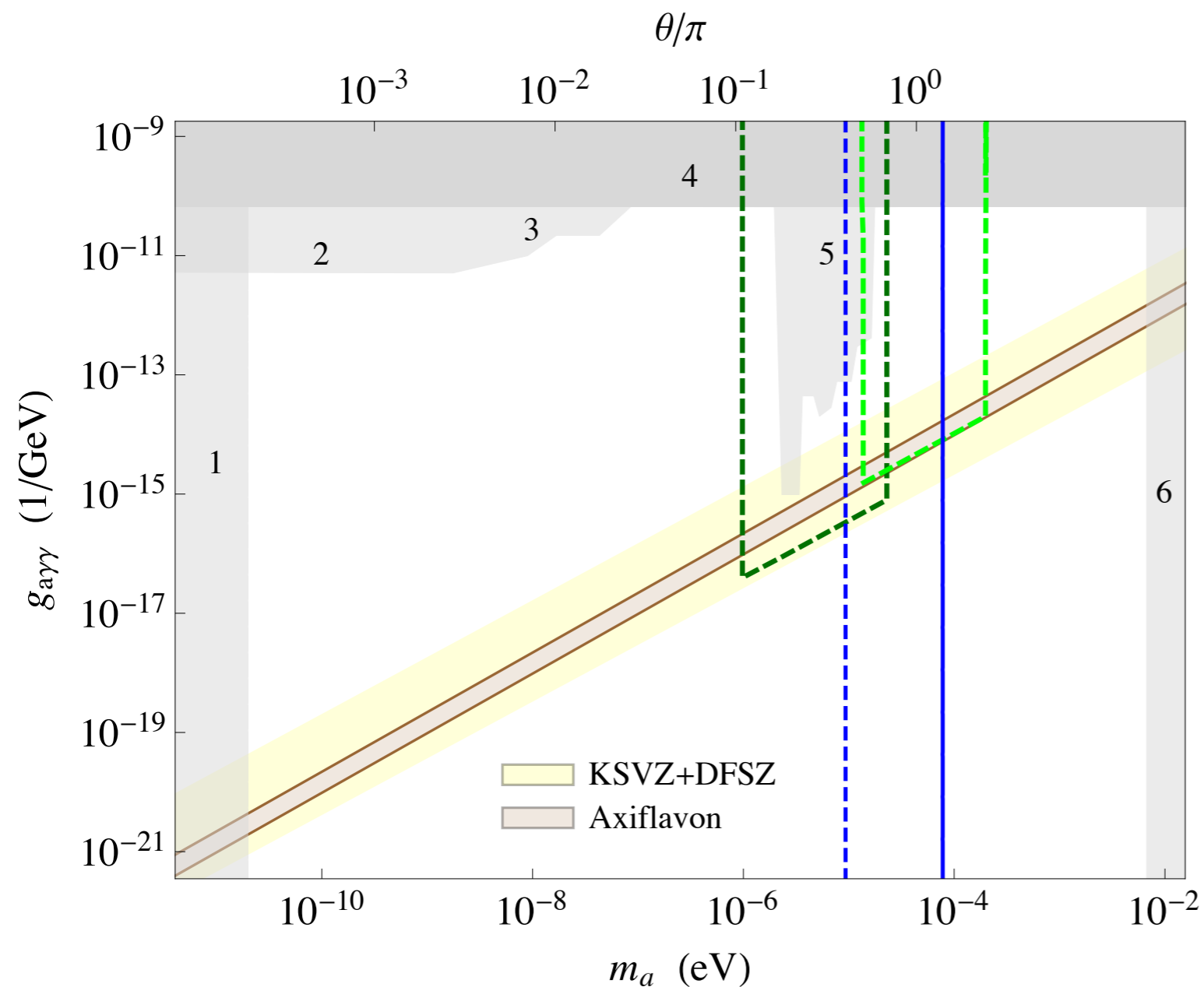
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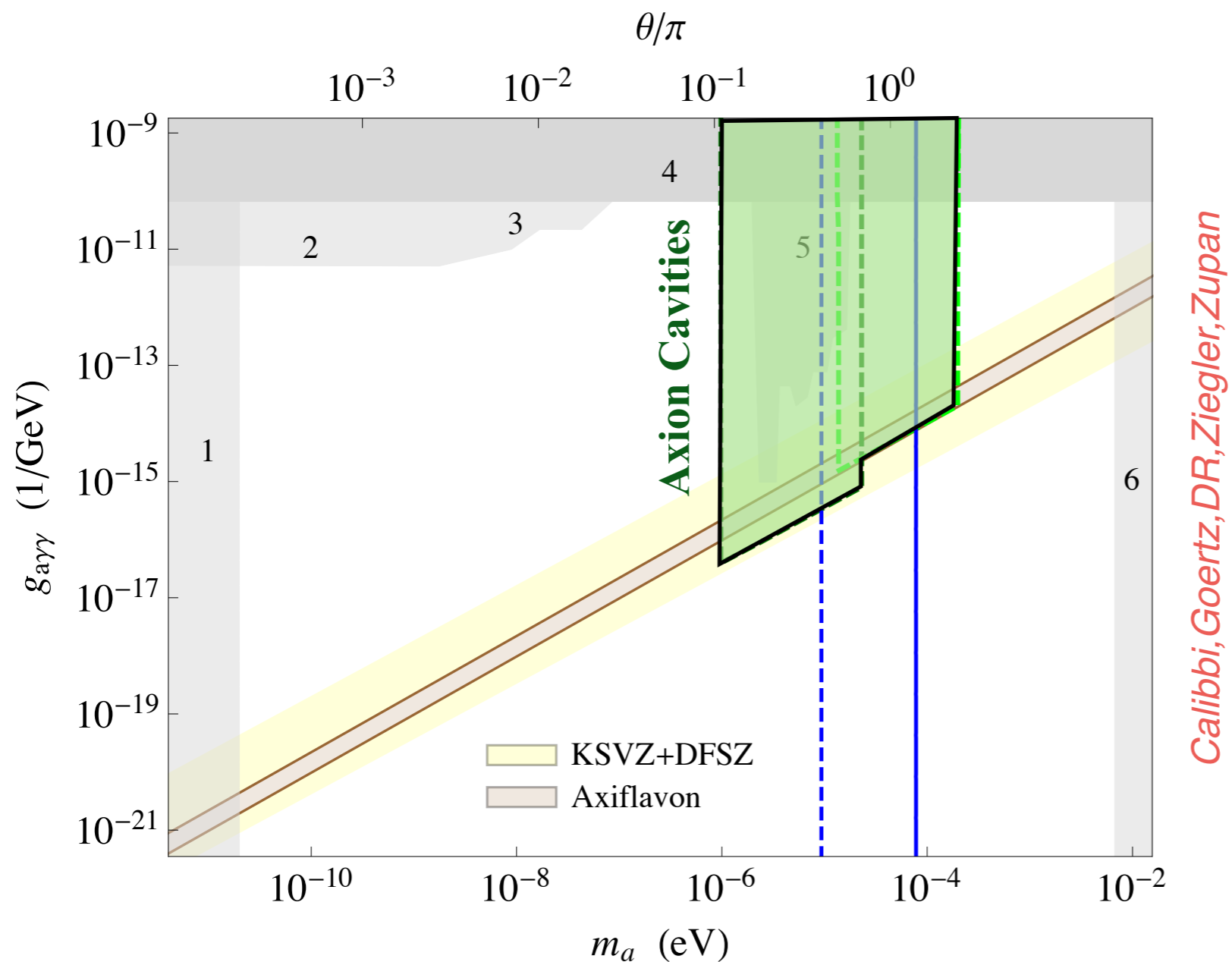


Calibbi, Goertz, DR, Ziegler, Zupan

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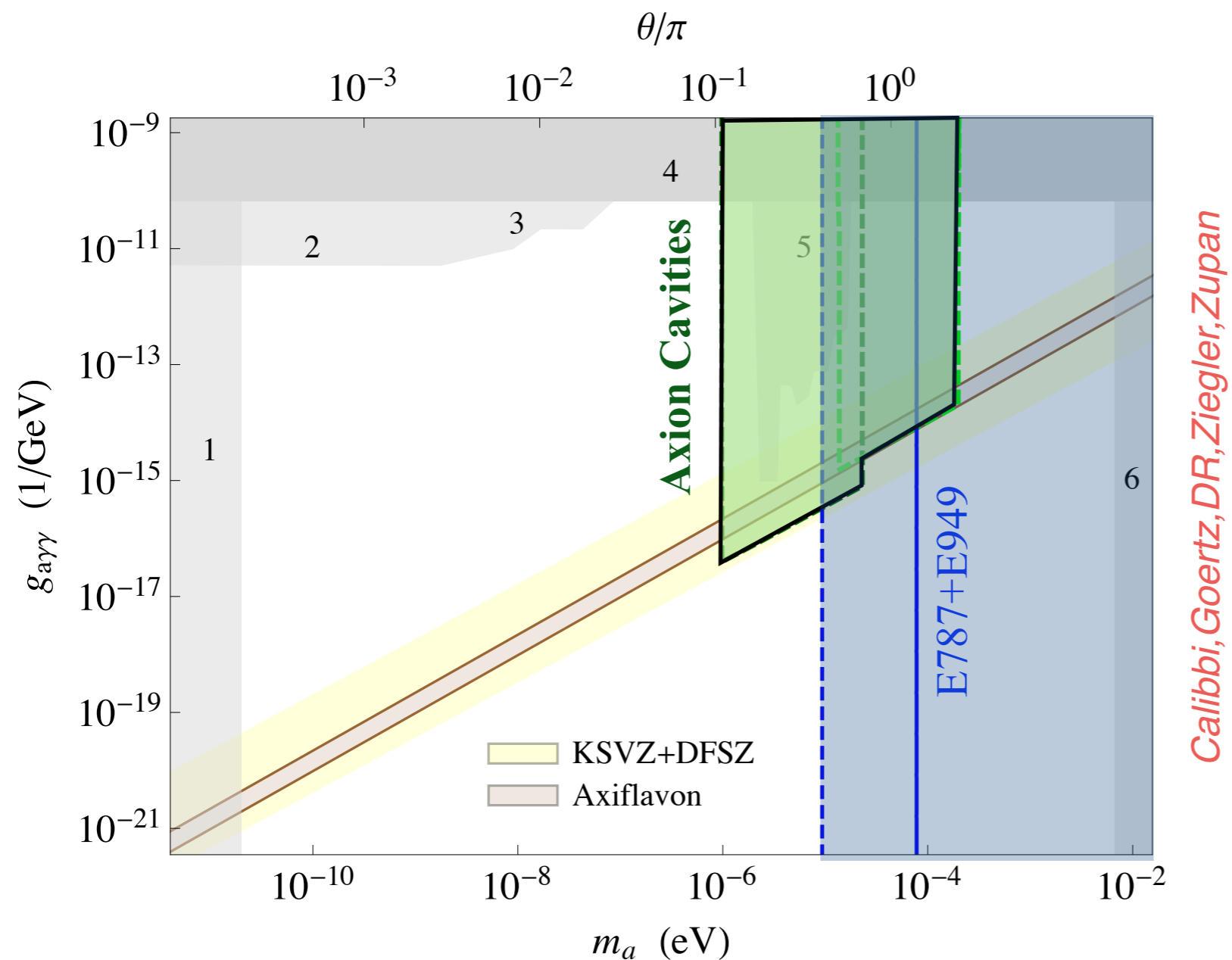
FV Kaon decays are super-powerful probes of NP $f \gtrsim 10^{11}$ GeV



NA62 highly constraint the quark FV interactions

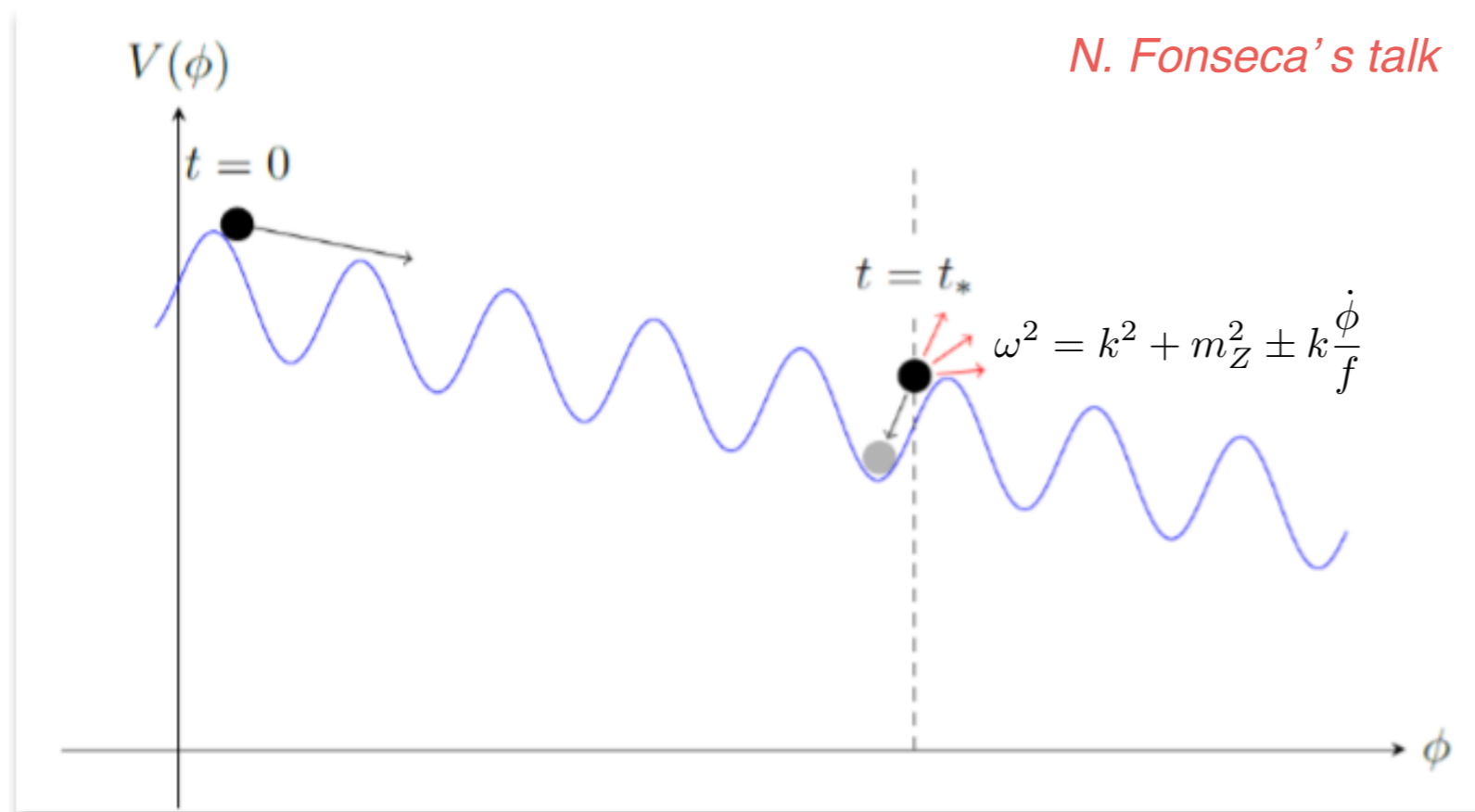
$$\mathcal{L}_\phi \supset \frac{iv\phi}{f} (Q_j + u_k^c) (Y_u)_{jk} u_j u_k^c$$

FV Kaon decays are super-powerful probes of NP $f \gtrsim 10^{11}$ GeV



The “thermal” relaxation

A. Hook, G. Marquez Tavares '16



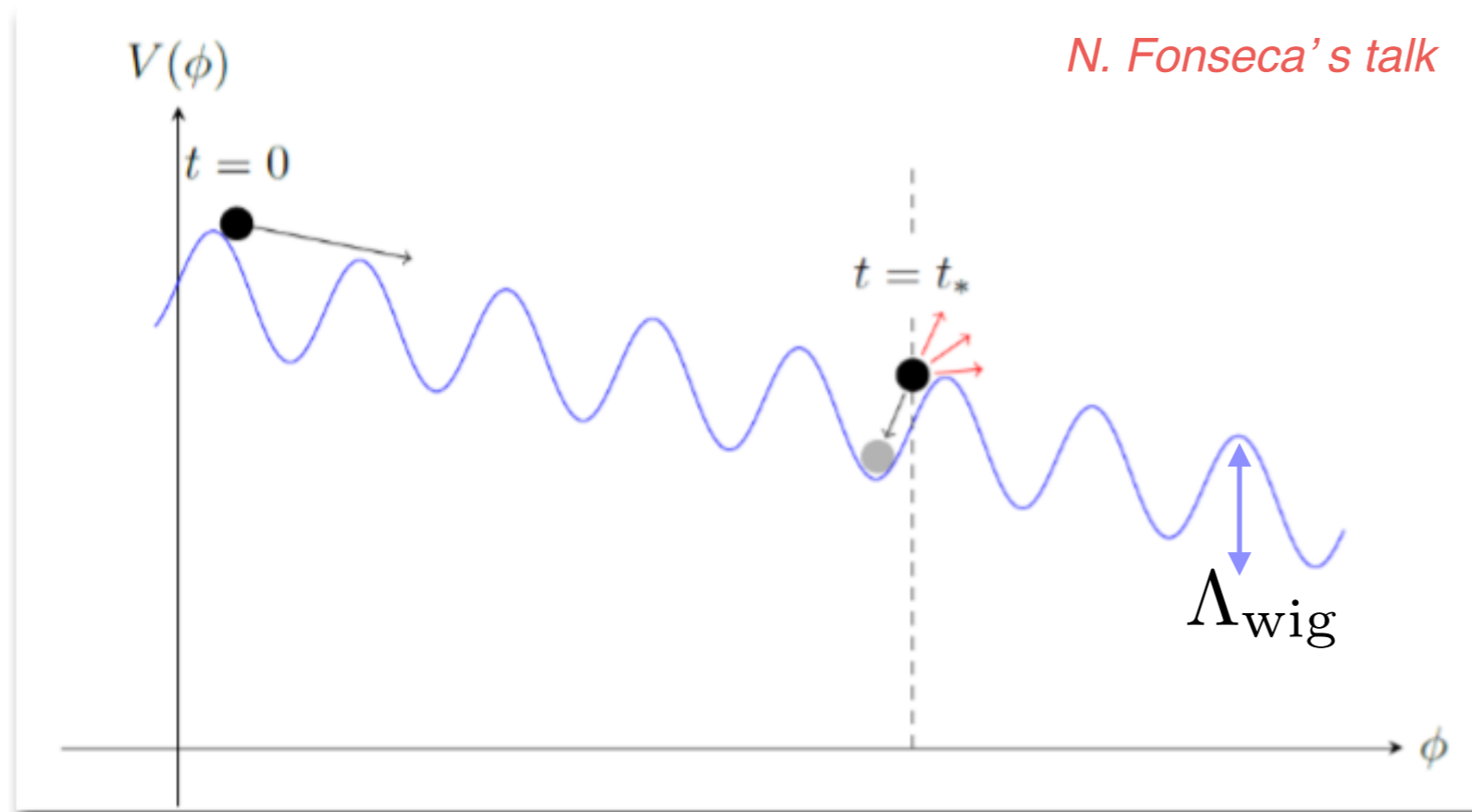
$$\mathcal{L} \supset -\frac{\phi}{f} \left(\alpha_Y B \tilde{B} - \alpha_2 W \tilde{W} \right)$$

FEATURES:

- *classical rolling + production of massive gauge bosons*
- *EW VEV goes down and enhance particle production*
- *particle production relevant* $\dot{\phi}_s \sim f v$
- *no coupling to photons*

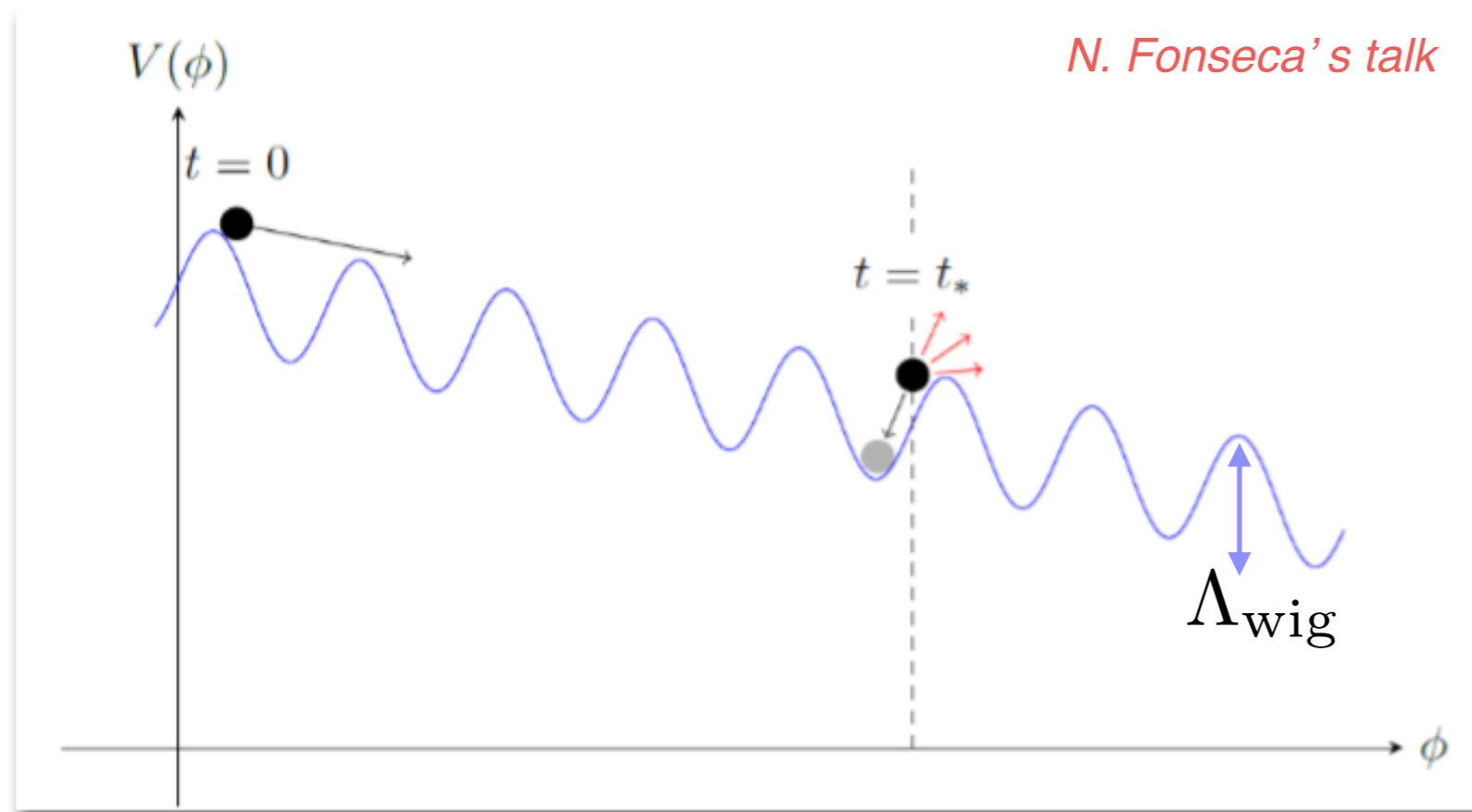
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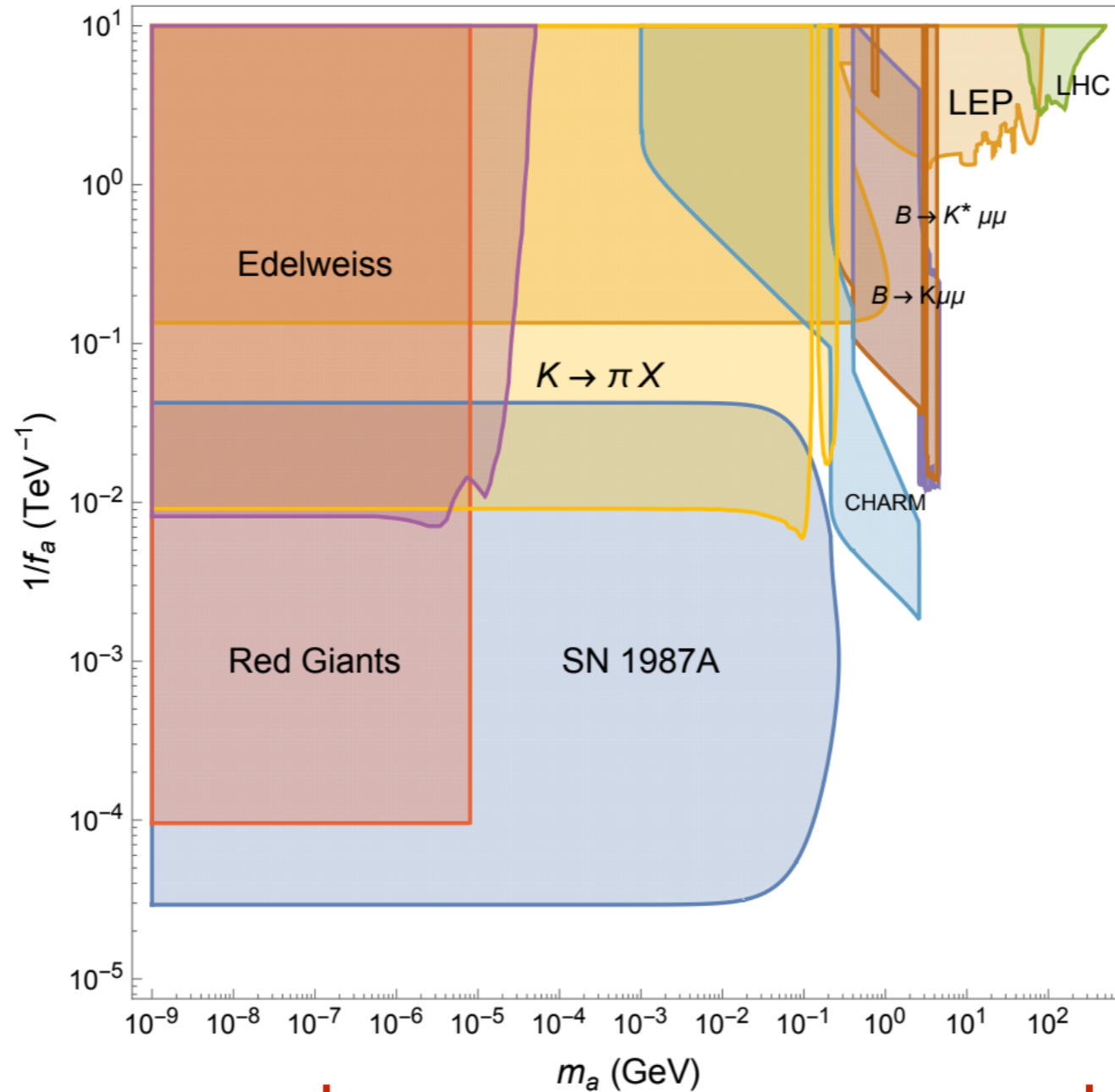
A. Hook, G. Marquez Tavares '16



- $F \lesssim M_{\text{Pl}}$
- $\Lambda_{\text{UV}} \lesssim \sqrt{M_{\text{Pl}} v} \cdot \left(\frac{\Lambda_{\text{wiggles}}}{f} \right)^2$
- $\dot{\phi}_i^2 \gtrsim \Lambda_{\text{wig}}^4$, $\dot{\phi}_f^2 \gtrsim \Lambda_{\text{wig}}^4$
- $F \lesssim \left(\frac{T_{\text{RH}}}{\Lambda_{\text{UV}}} \right)^2 \cdot M_{\text{Pl}}$

CONSEQUENCES:

- *Subplanckian field excursion*
- *Large wiggles* \longleftrightarrow *heavy relaxation*
- *non-generic initial velocity* \longleftrightarrow *tuning in the initial conditions?*
- *relaxation without inflation* *N. Fonseca, E. Morgante, G. Servant '18*

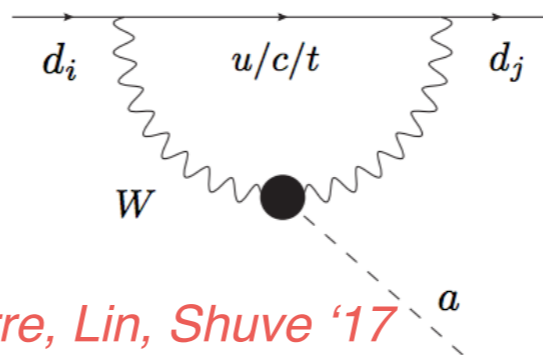


● **Bolometers/Red Giants**

production of axion
in the Sun

$$e + Ze \rightarrow Ze + e + a$$

● **Flavor transitions**



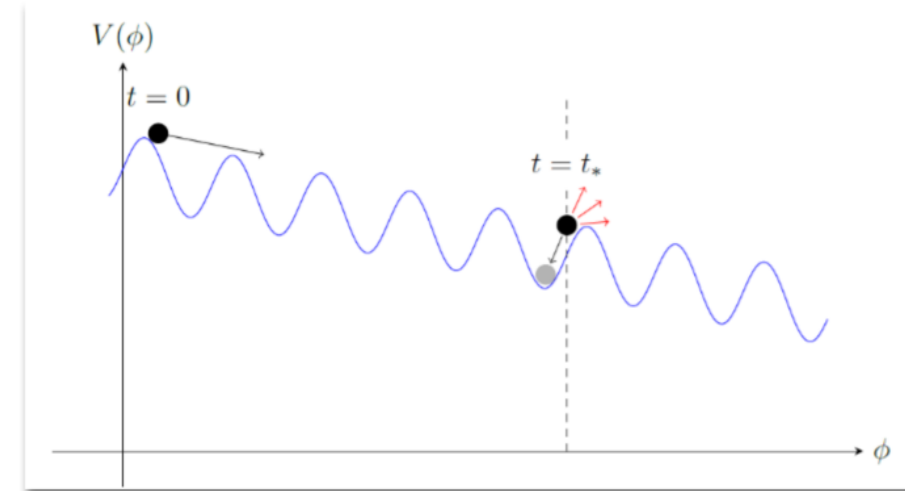
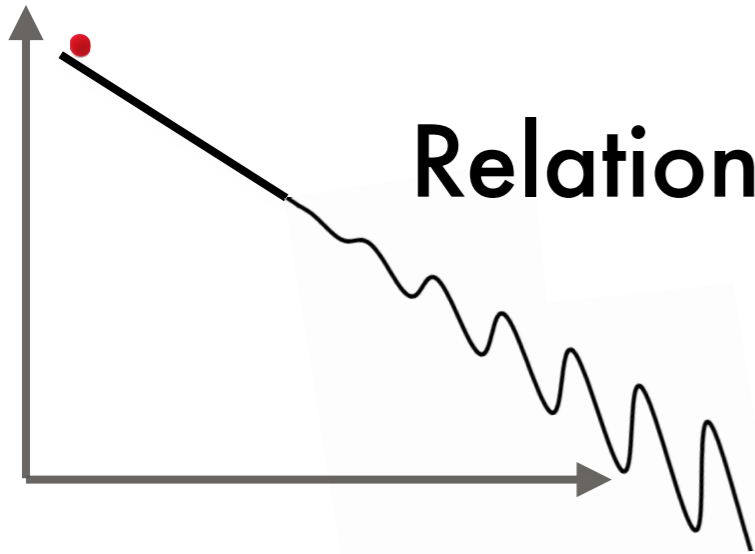
Izaguirre, Lin, Shuve '17

● **colliders**

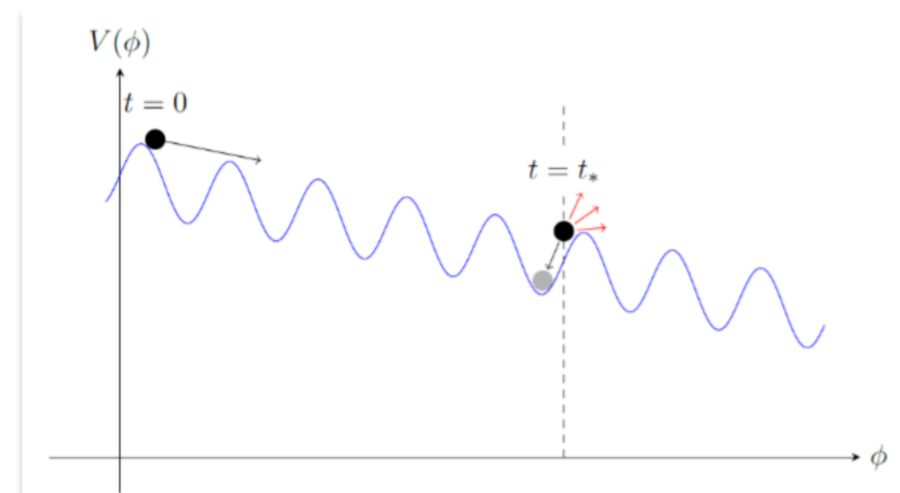
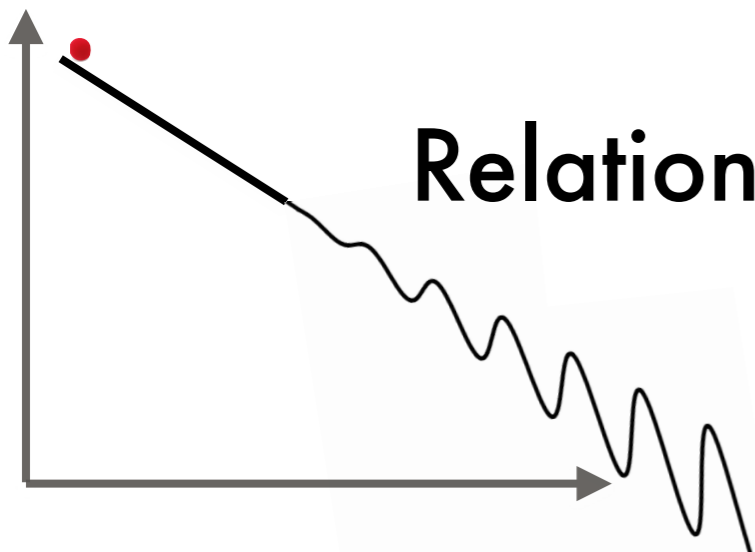
$$pp \rightarrow Z2\gamma$$

$$pp \rightarrow 3W$$

Relation as playground for Naturalness



Relation as playground for Naturalness



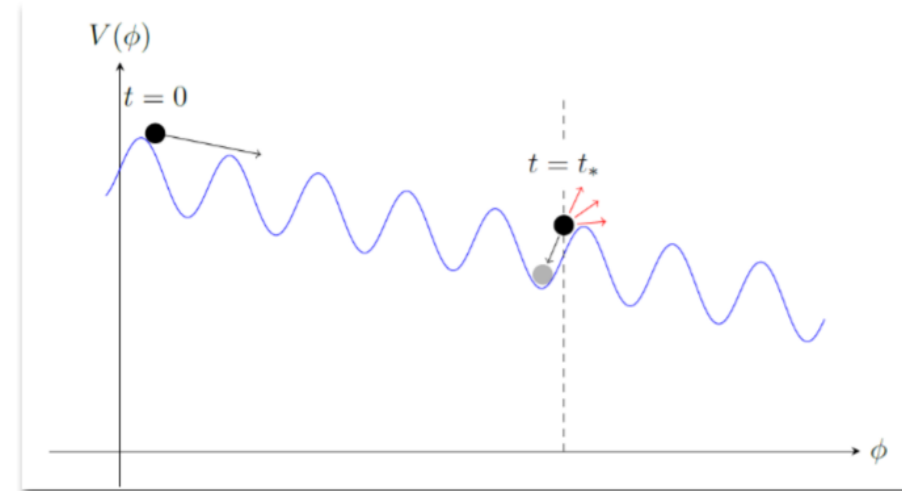
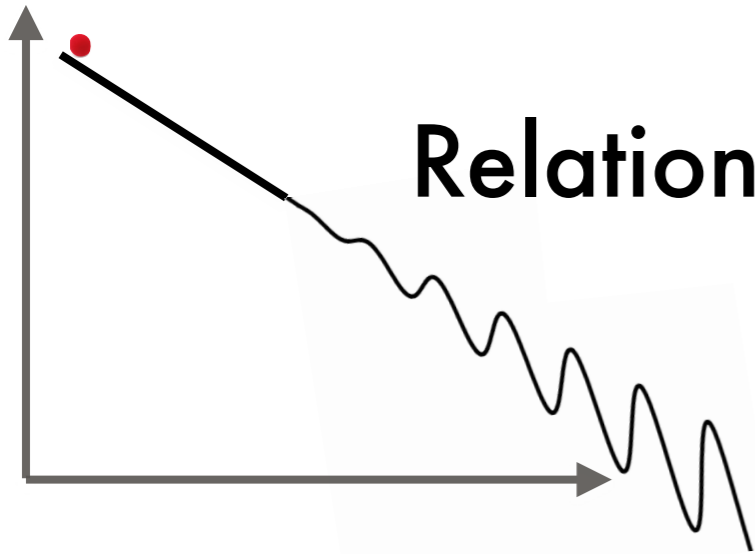
**new
theory
challenges**

- *Raises new cosmological and field theory questions*

CC? Is there a bound on small global charges?

inflation? baryogenesis? relaxion DM?

Relation as playground for Naturalness



new
theory
challenges

- *Raises new cosmological and field theory questions*

CC? Is there a bound on small global charges?

inflation? baryogenesis? relaxion DM?

new pheno
probes

- *Switches the focus to very light weakly coupled states*
- *Higgs portal phenomenology for the original relaxion*
- *ALP phenomenology for the thermal relaxion*

BACKUP

How Atomic Clock experiments work?

Arvanitaki, Dimopoulos, Van Tilburg

$$\phi(t, \vec{x}) = \phi_0 \cos(m_\phi t - \vec{k}_\phi \cdot \vec{x} + \dots)$$

$$\phi_0 \approx \frac{1}{m_\phi} \sqrt{2\xi_\phi \rho_{DM}}$$

Fluctuations on the fundamental constant of Nature

The mass controls the frequency

$$\frac{\delta(f_A/f_B)}{(f_A/f_B)} \simeq [d_{m_e} - d_g + M_A d_{\hat{m}} + d_e(\xi_A - \xi_B)] \kappa \phi(t)$$

$$\overset{\text{1 sec}}{\Delta\tau} < \frac{2\pi}{m_\phi} < \overset{\text{3.25 years}}{\tau_{\text{int}}} \longrightarrow m_\phi \lesssim 10^{-15} \text{ eV}$$

Backreaction from NP sector

$$\mathcal{L} = -y_1 e^{i\frac{2n\phi}{f_{UV}}} \epsilon^{\alpha\beta} h_\alpha L_\beta N - y_2 h^{\dagger\alpha} L_\alpha^c N - m_L \epsilon^{\alpha\beta} L_\alpha L_\beta^c - \frac{m_N}{2} NN + \text{h.c.}$$



$$V_{\text{CW}}(\phi) \simeq -\frac{1}{4\pi^2} m_L m_N y_1 y_2 |h^0|^2 \cos\left(\frac{\phi}{f}\right) \log\left(\frac{\Lambda^2}{\tilde{m}^2}\right), \quad \text{VS} \quad V_{\text{CW}}^{2\text{-loop}}(\phi) \sim -\frac{1}{4\pi^2} m_L m_N y_1 y_2 \left(\frac{\Lambda_c^2}{16\pi^2}\right) \cos\left(\frac{\phi}{f}\right)$$

screen the Higgs loop

$$\Delta\mathcal{L} = m_D NN^c - \frac{m_{N^c}}{2} N^c N^c \dashrightarrow m_N \approx \frac{m_D^2}{m_{N^c}}$$

no quadratic divergences above m_{N^c} $m_L \approx m_N \lesssim m_{N^c} \approx 4\pi v$

Backreaction from neutrino sector

$$\begin{aligned}\mathcal{L}_N^{\text{br}} &= y_{jk}^D \cdot \left(\frac{\hat{\Phi}_0}{\Lambda_n} \right)^{|[N_j]+[N_k^c]|\cdot -1} \hat{\Phi}_0 N_j N_k^c + \frac{1}{2} M_{jk}^M N_j N_k + \text{h.c.} \\ &\supseteq M_{jk}^D \cdot U_0^{[N_j]+[N_k^c]} N_j N_k^c + \frac{1}{2} M_{jk}^M N_j N_k + \text{h.c.},\end{aligned}$$

The potentials:

$$\begin{aligned}V_D &\sim \frac{\text{Tr}(M^D M^{D\dagger} \overline{M}^M \overline{M}^{M\dagger})}{16\pi^2} \log \frac{m_{\text{clock}}^2}{M^2} \\ V_{\text{br}} &\sim H^\dagger H \left[\frac{\text{Tr}(Y^n M^{D\dagger} \overline{M}^M \overline{M}^{M\dagger} M^D Y^{n\dagger})}{16\pi^2 M^2} + \dots \right]\end{aligned}$$

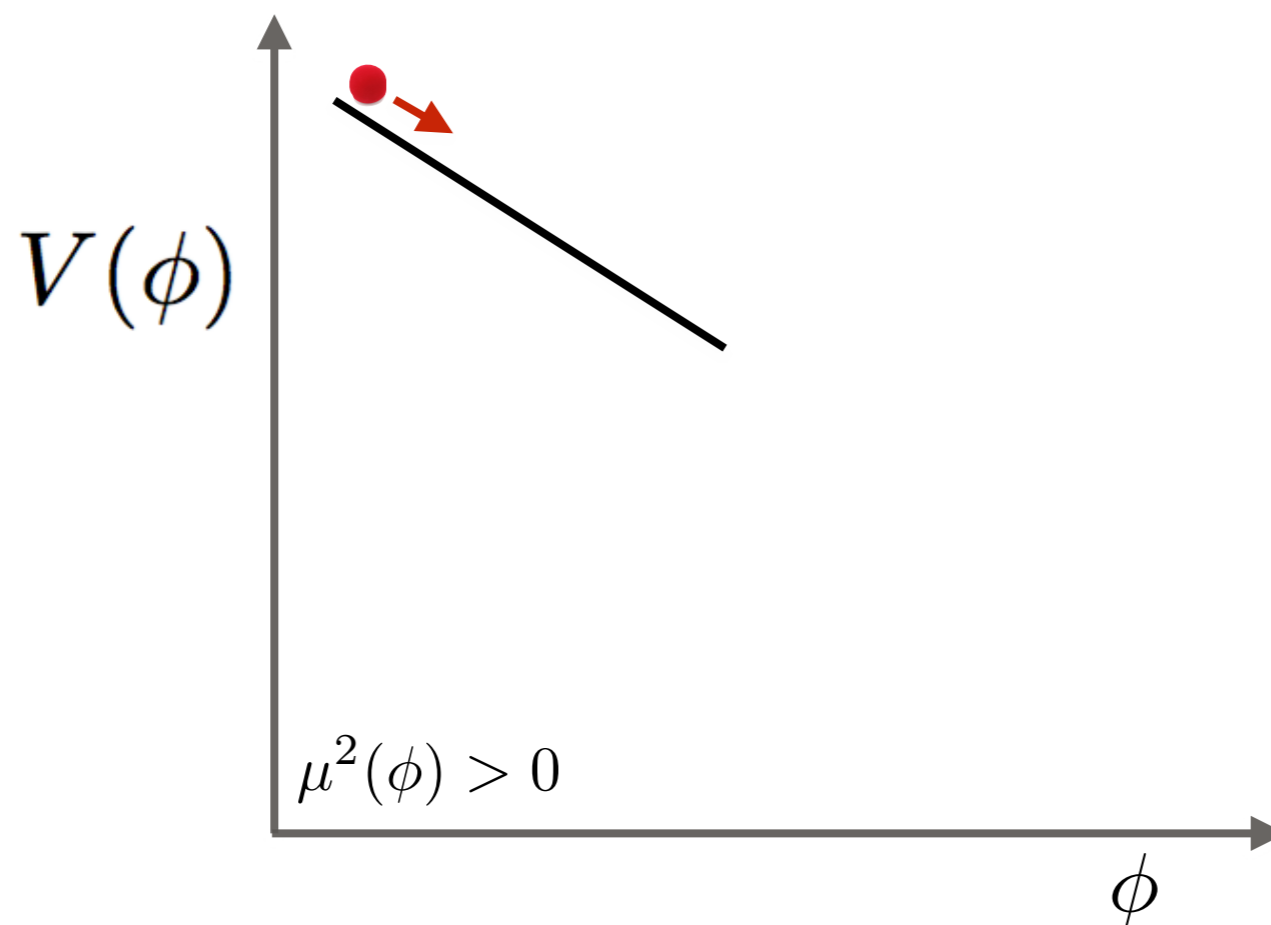
The trick: $V_D < V_{\text{br}} \dashrightarrow M_D$ diagonal

The consequence: $\Lambda_{\text{br}} \sim \left(\frac{y_N^2 v^2 M^2}{16\pi^2} \right)^{1/4} \sim \left(\frac{m_\nu M^3}{16\pi^2} \right)^{1/4} \lesssim 10 \text{ MeV}.$

I

The Relaxion rolling

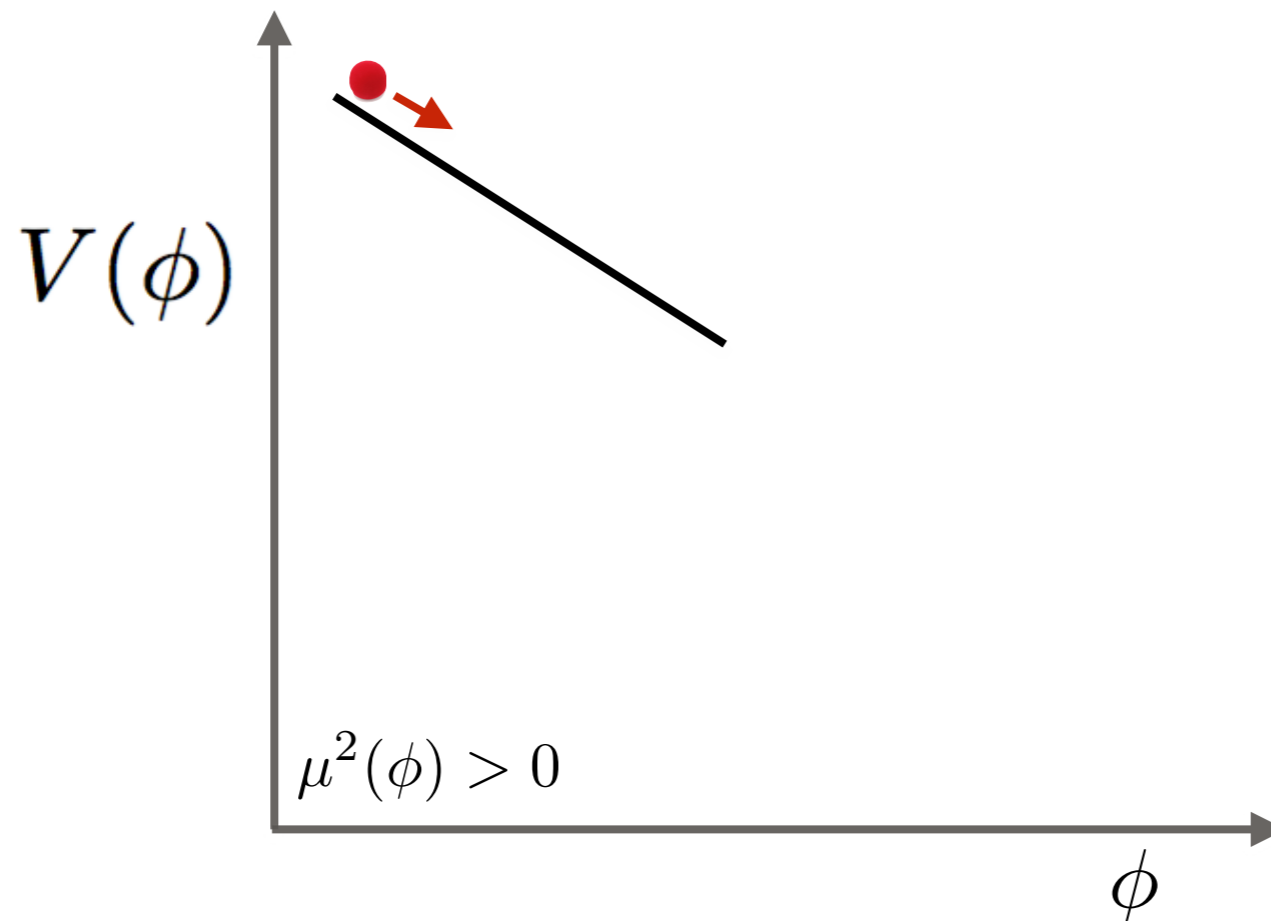
(Graham, Kaplan & Rajendran)



I

The Relaxion rolling

(Graham, Kaplan & Rajendran)



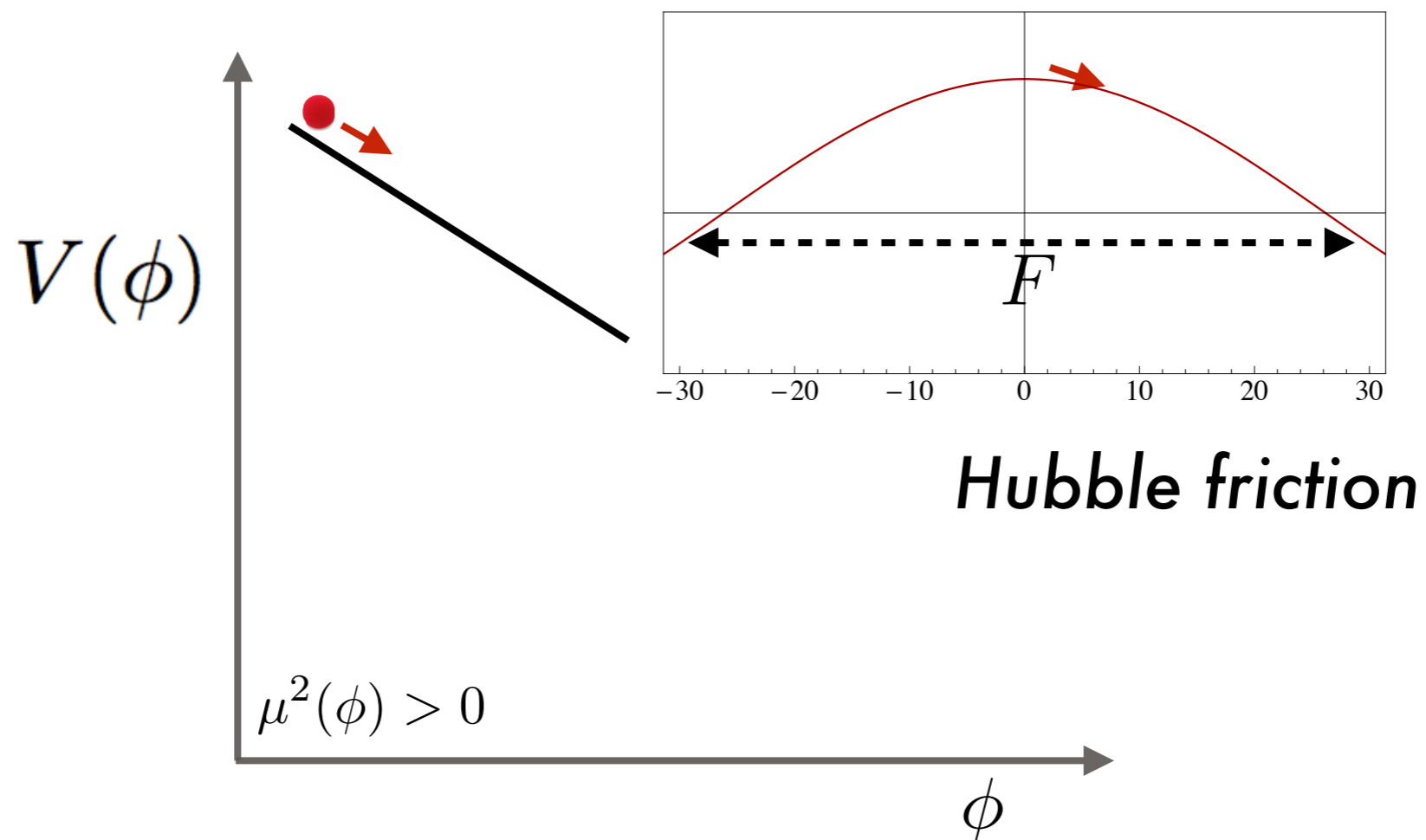
ϕ rolling potential:

$$\Lambda_{\text{roll}}^4 \cos \frac{\phi}{F}$$

I

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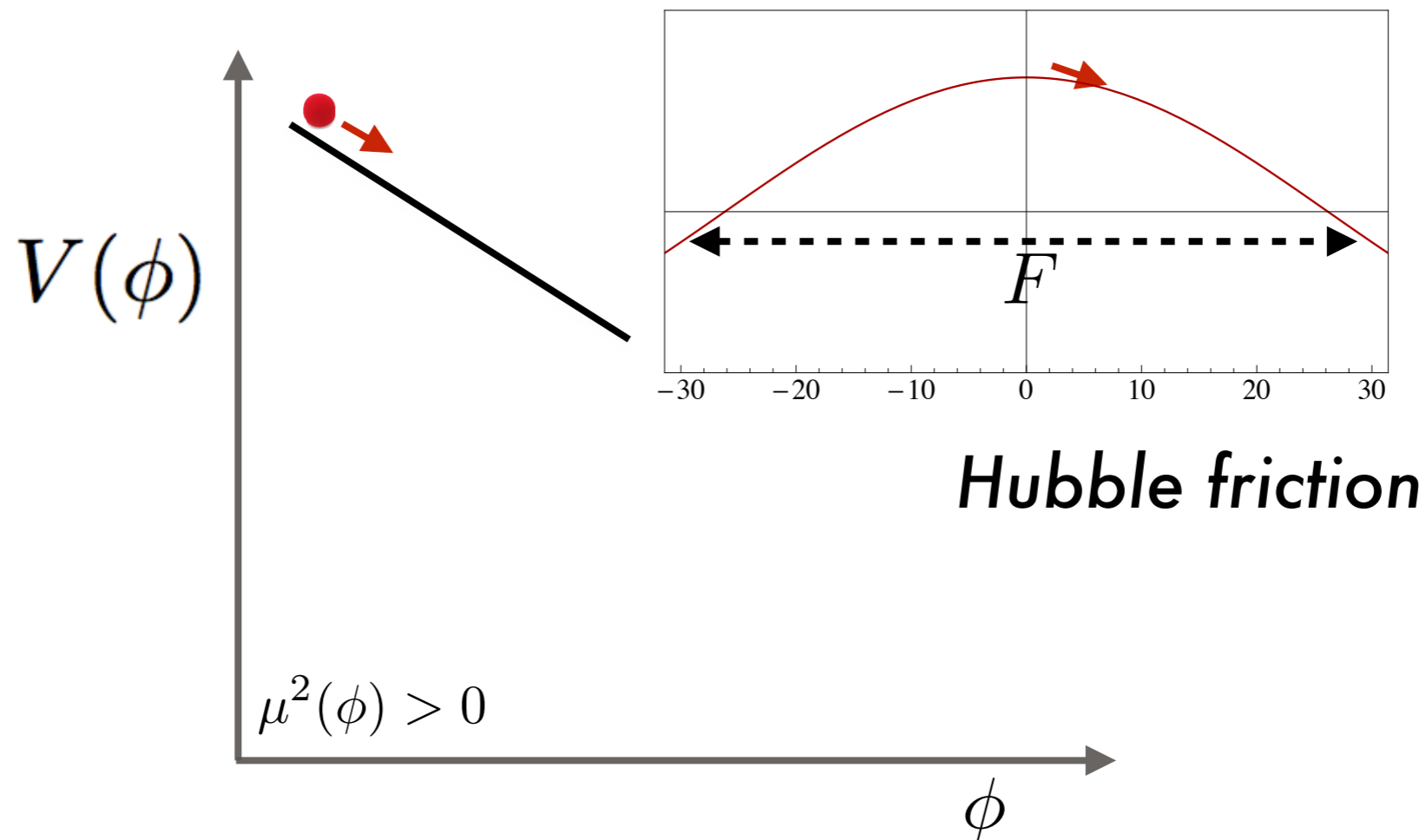
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The Relaxion rolling

(Graham, Kaplan & Rajendran)



Hubble friction

ϕ - dependent Higgs mass

$$\underbrace{\Lambda_H^2 \left(\kappa - \cos \frac{\phi}{F} \right)}_{\mu^2(\phi)} H^\dagger H$$

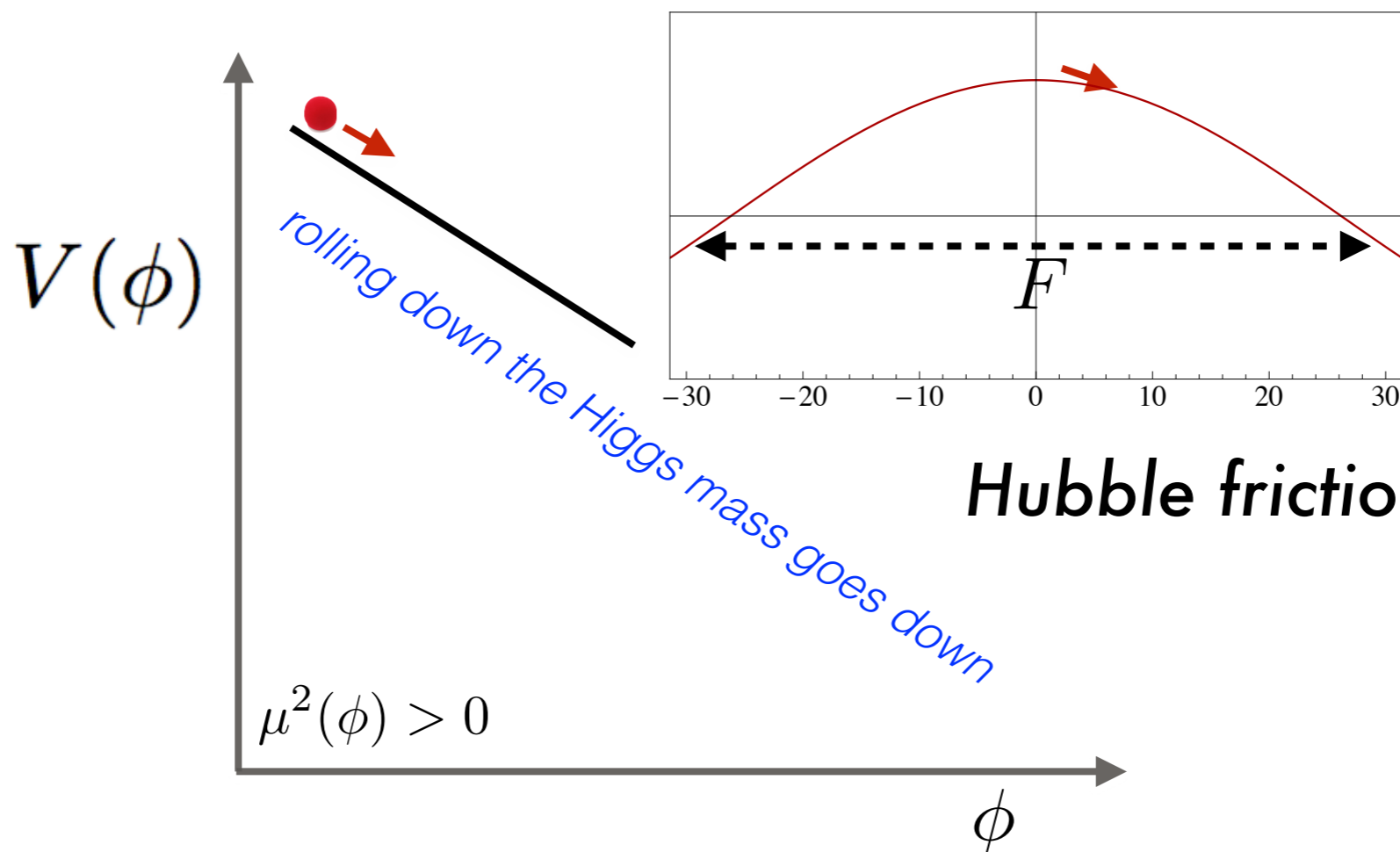
ϕ rolling potential:

$$\Lambda_{\text{roll}}^4 \cos \frac{\phi}{F}$$

I

The Relaxion rolling

(Graham, Kaplan & Rajendran)



Hubble friction $\dot{\phi}_{\text{roll}} \sim \frac{\Lambda_{\text{roll}}^4}{3H_I F}$

ϕ -dependent Higgs mass

$$\underbrace{\Lambda_H^2 \left(\kappa - \cos \frac{\phi}{F} \right)}_{\mu^2(\phi)} H^\dagger H \simeq (\kappa \Lambda_H^2 - \underbrace{g\phi}) H^\dagger H$$

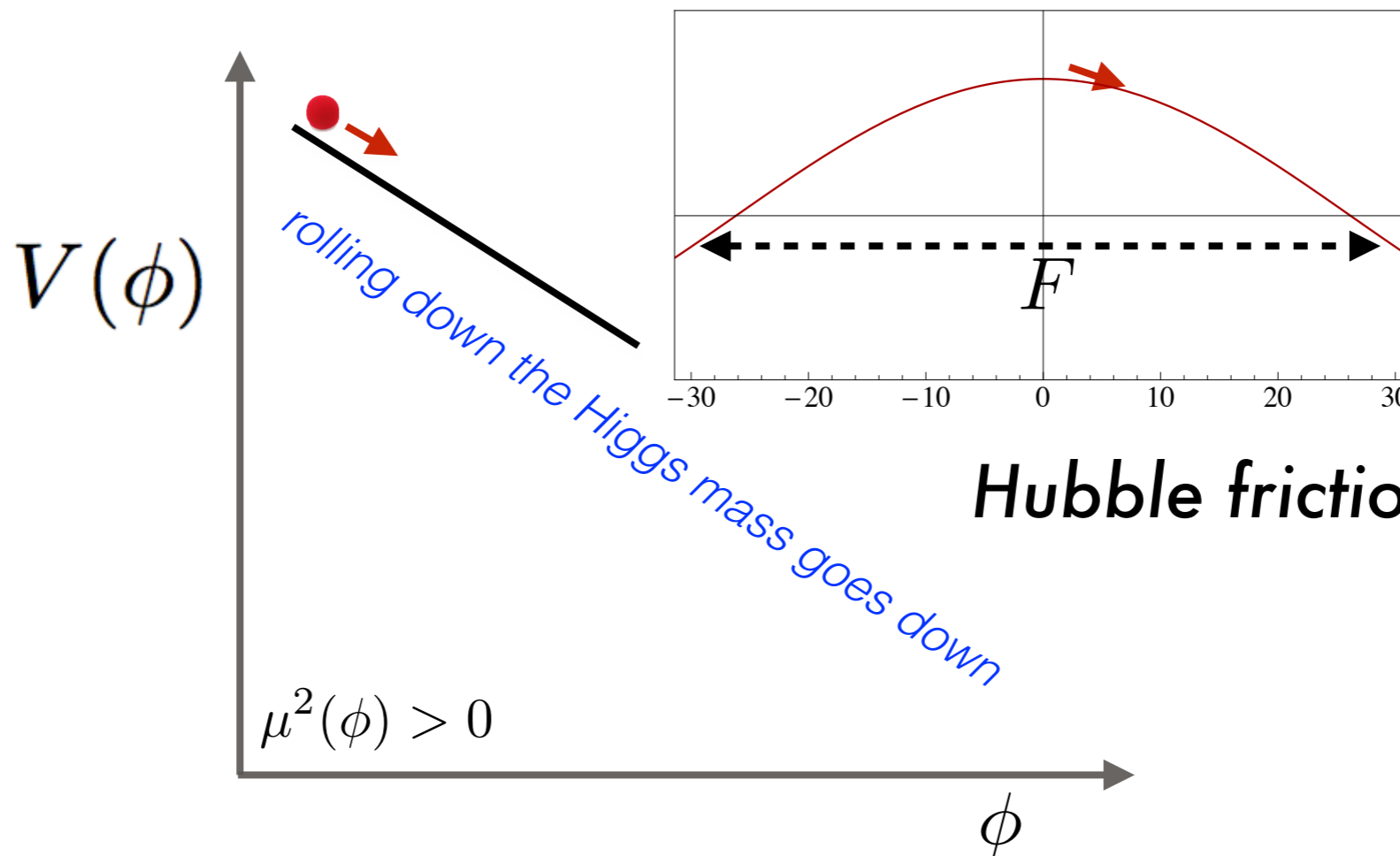
ϕ rolling potential:

$$\Lambda_{\text{roll}}^4 \cos \frac{\phi}{F} \simeq \underbrace{g\Lambda_H^3 \phi}$$

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The Relaxion rolling

(Graham, Kaplan & Rajendran)



Hubble friction $\dot{\phi}_{\text{roll}} \sim \frac{\Lambda_{\text{roll}}^4}{3H_I F}$

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$$\underbrace{\Lambda_H^2 \left(\kappa - \cos \frac{\phi}{F} \right)}_{\mu^2(\phi)} H^\dagger H \simeq \left(\kappa \Lambda_H^2 - \underbrace{g\phi}_{\frac{g}{\Lambda_H} \ll 1} \right) H^\dagger H$$

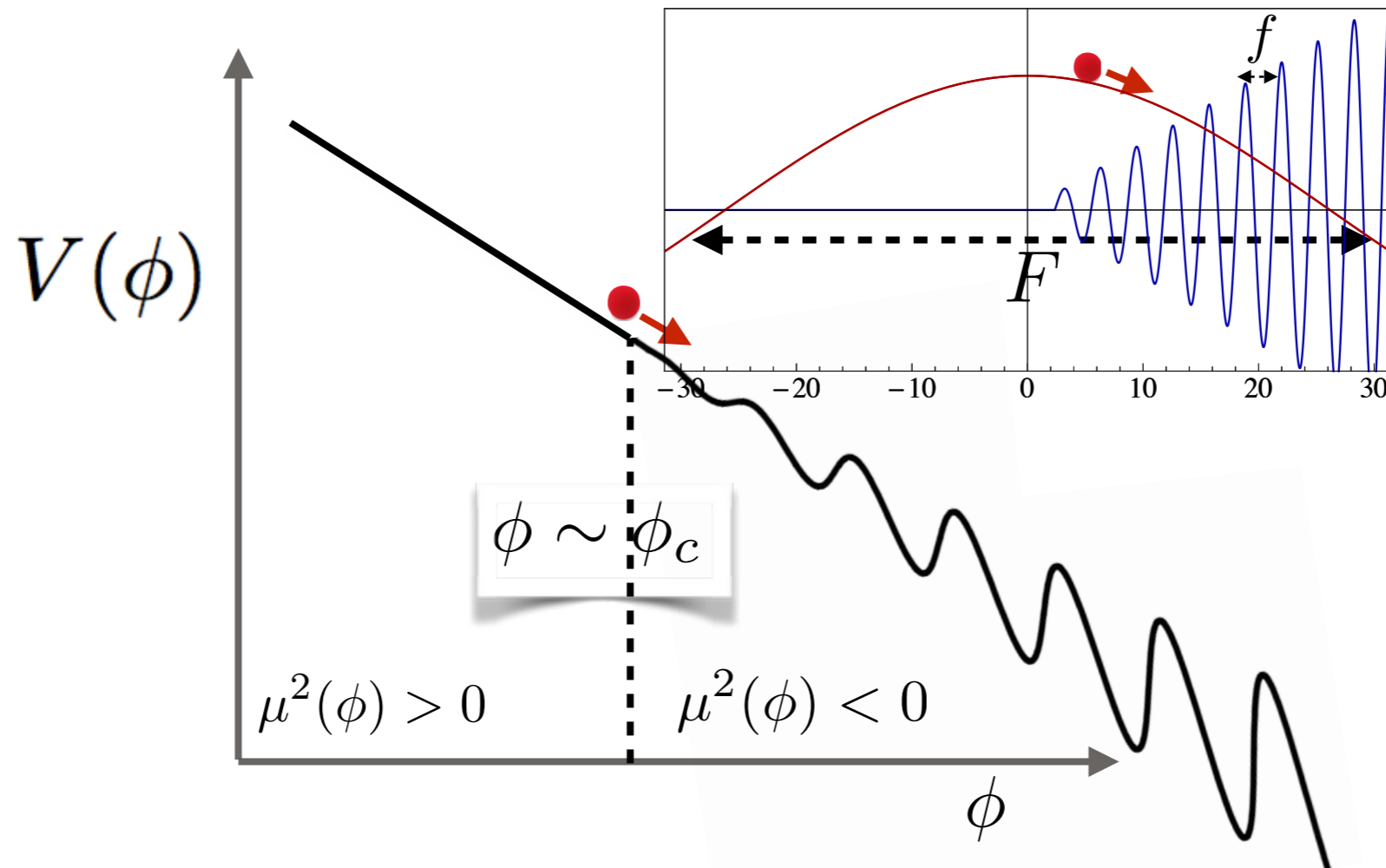
ϕ rolling potential:

$$\Lambda_{\text{roll}}^4 \cos \frac{\phi}{F} \simeq \underbrace{g\Lambda_H^3 \phi}_{\text{Hubble friction}} \times \underbrace{r_{\text{roll}}^2}_{\text{scanning pace}}$$

the pace of the scanning: $r_{\text{roll}} \equiv \frac{\Lambda_{\text{roll}}^2}{\Lambda_H^2} \gtrsim \frac{1}{4\pi}$

II

The Relaxion wiggles



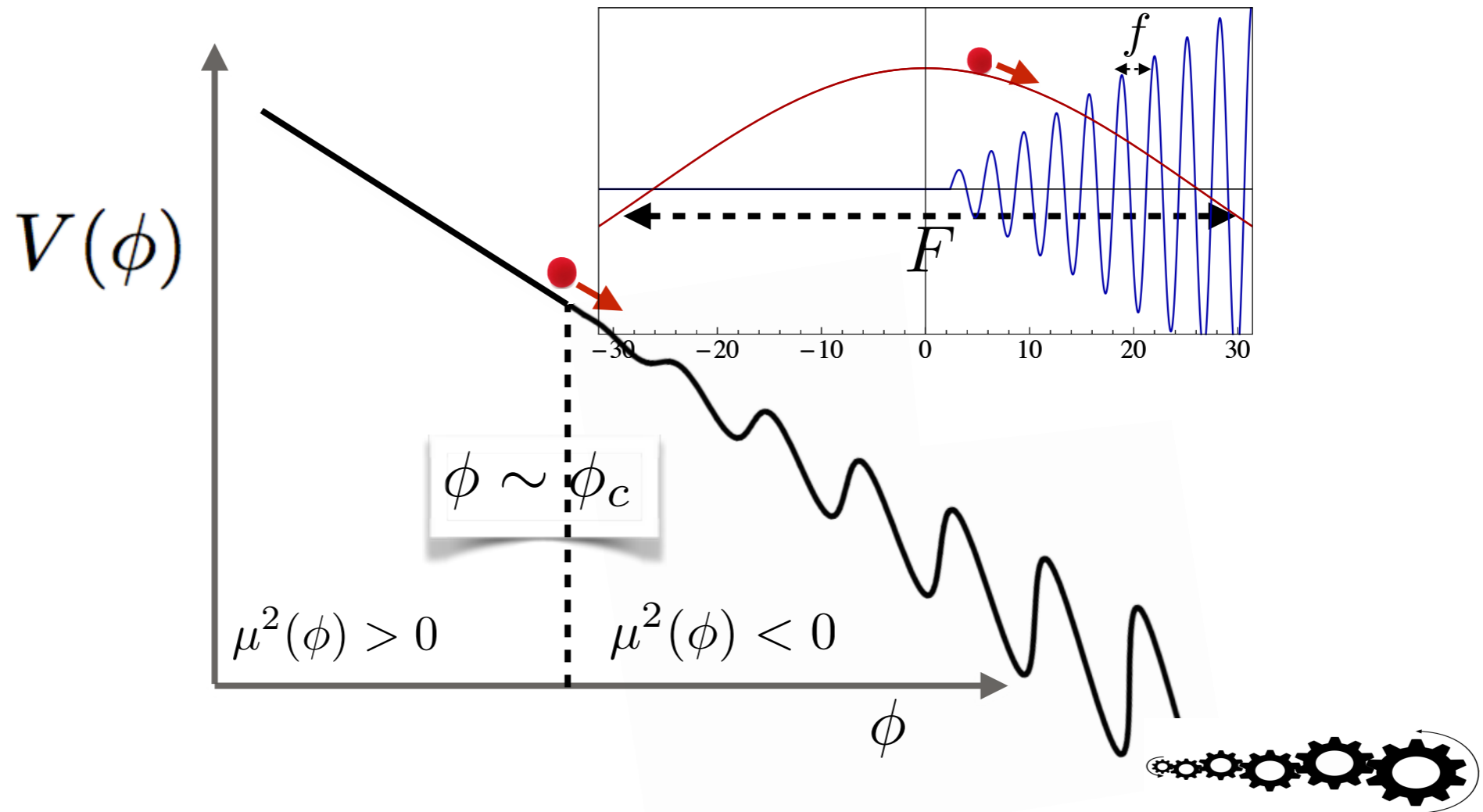
ϕ gets a "backreaction" potential after EWSB

Periodicity of this potential smaller than the "rolling"

$$\Lambda_{\text{br}}^4 \cos \frac{\phi}{f}$$

II

The Relaxion wiggles



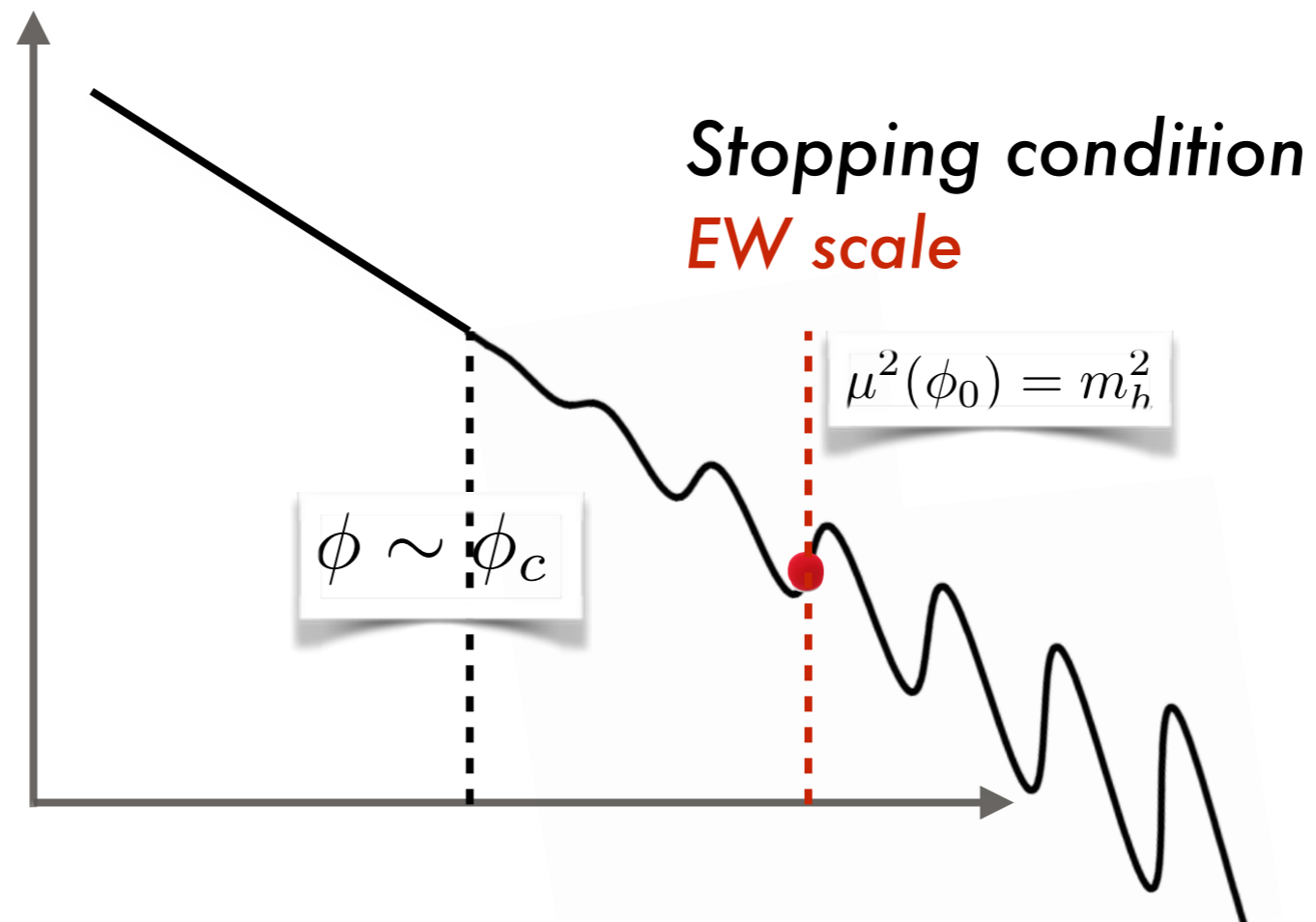
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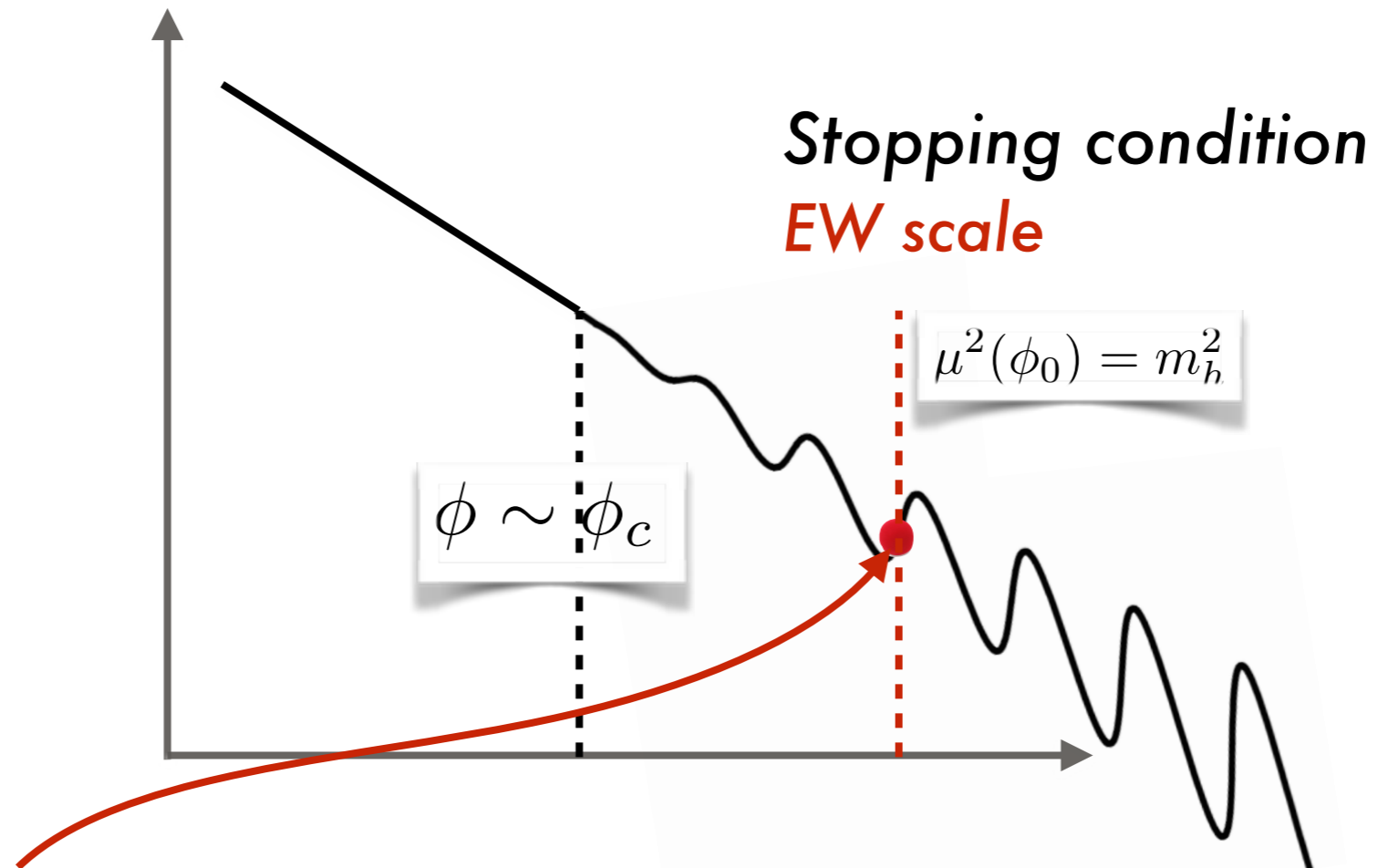
$$\Lambda_{\text{br}}^4 \cos \frac{\phi}{f} \} \Lambda_{\text{br}} \text{ model dependent}$$

$$f/F \simeq Q \ll 1$$

I + II = rolling + wiggles



I + II = rolling + wiggles



Stopping condition
EW scale

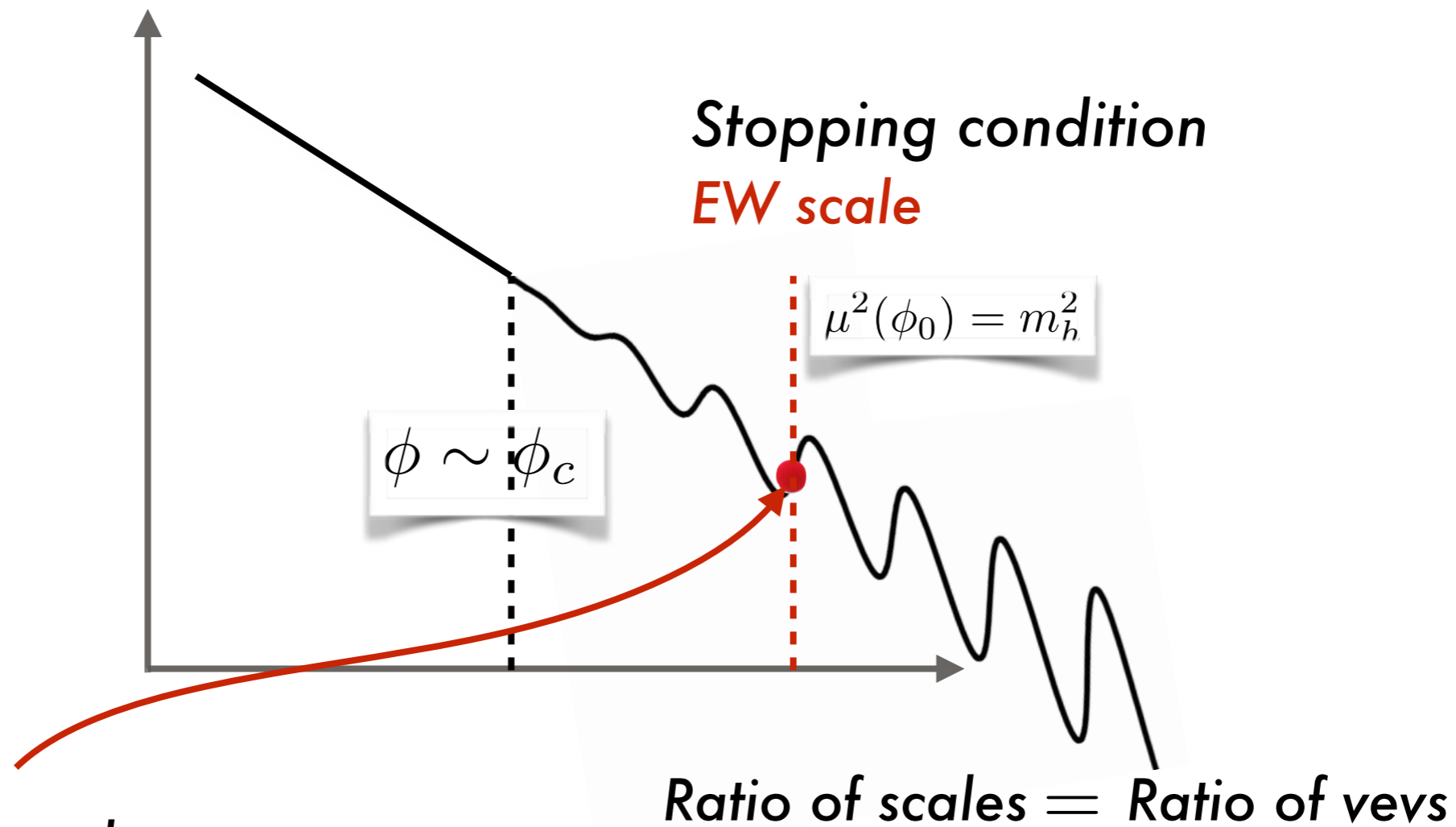
$$\phi \sim \phi_c$$

$$\mu^2(\phi_0) = m_h^2$$

CP violating phase

$$\sin \frac{\phi_0}{f} \sim \sin \frac{\phi_0}{F} \sim \mathcal{O}(1)$$

I + II = rolling + wiggles

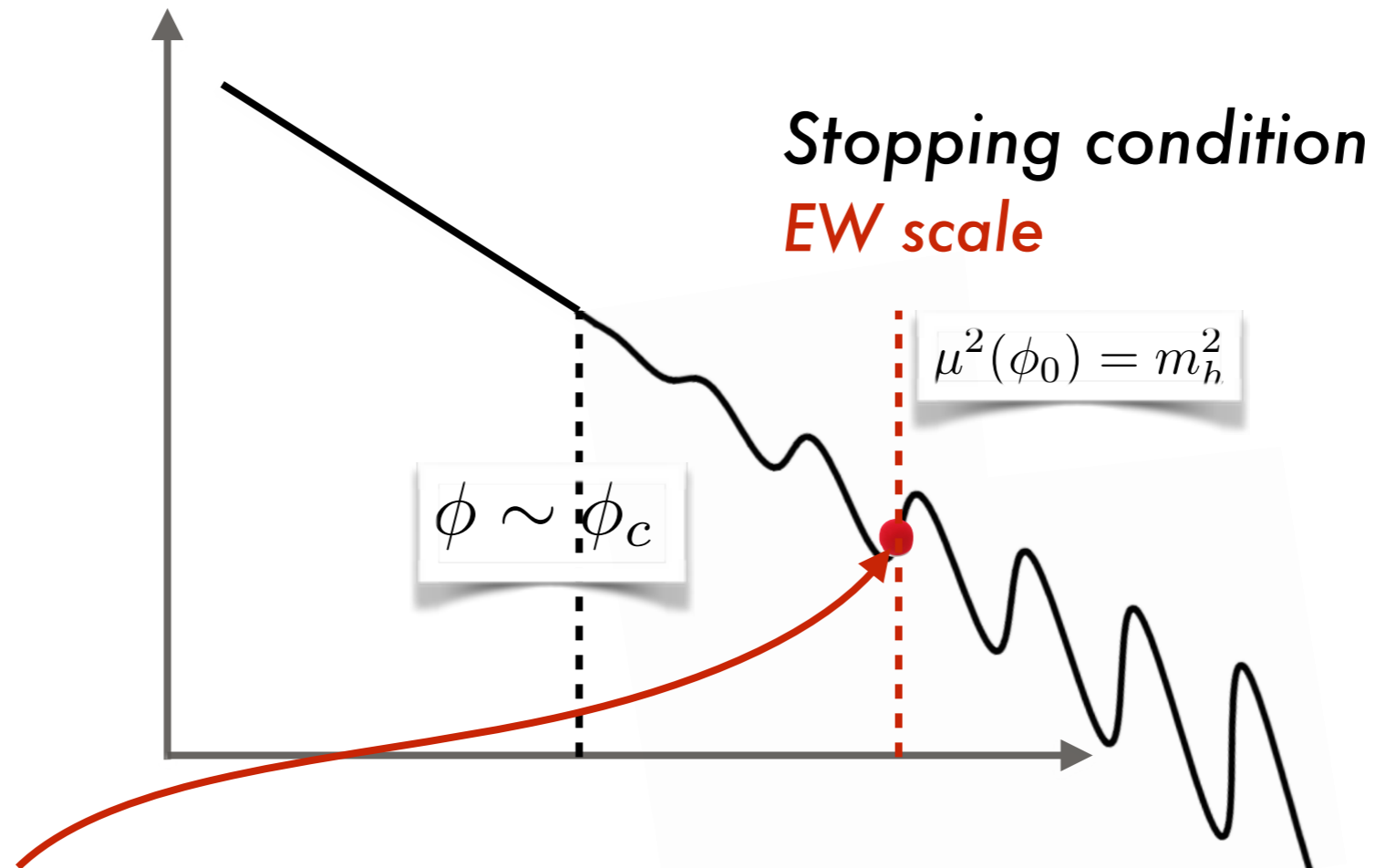


CP violating phase

$$\sin \frac{\phi_0}{f} \sim \sin \frac{\phi_0}{F} \sim \mathcal{O}(1)$$

$$\frac{\Lambda_{\text{roll}}}{\Lambda_{\text{br}}} \sim \left(\frac{F}{f} \right)^{1/4}$$

I + II = rolling + wiggles



CP violating phase

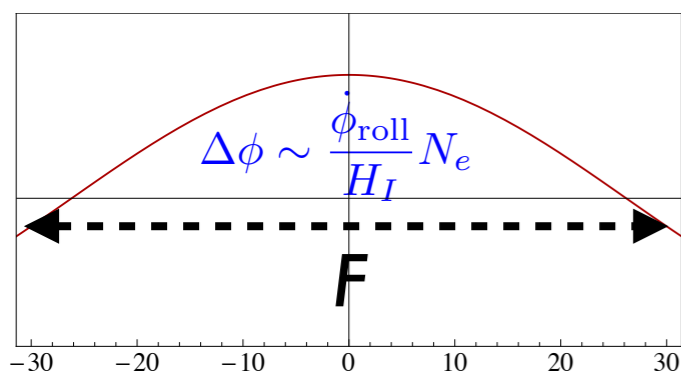
$$\sin \frac{\phi_0}{f} \sim \sin \frac{\phi_0}{F} \sim \mathcal{O}(1)$$

Ratio of scales = Ratio of vevs

$$\frac{\Lambda_{\text{roll}}}{\Lambda_{\text{br}}} \sim \left(\frac{F}{f} \right)^{1/4} \simeq 1/Q \gg 1$$

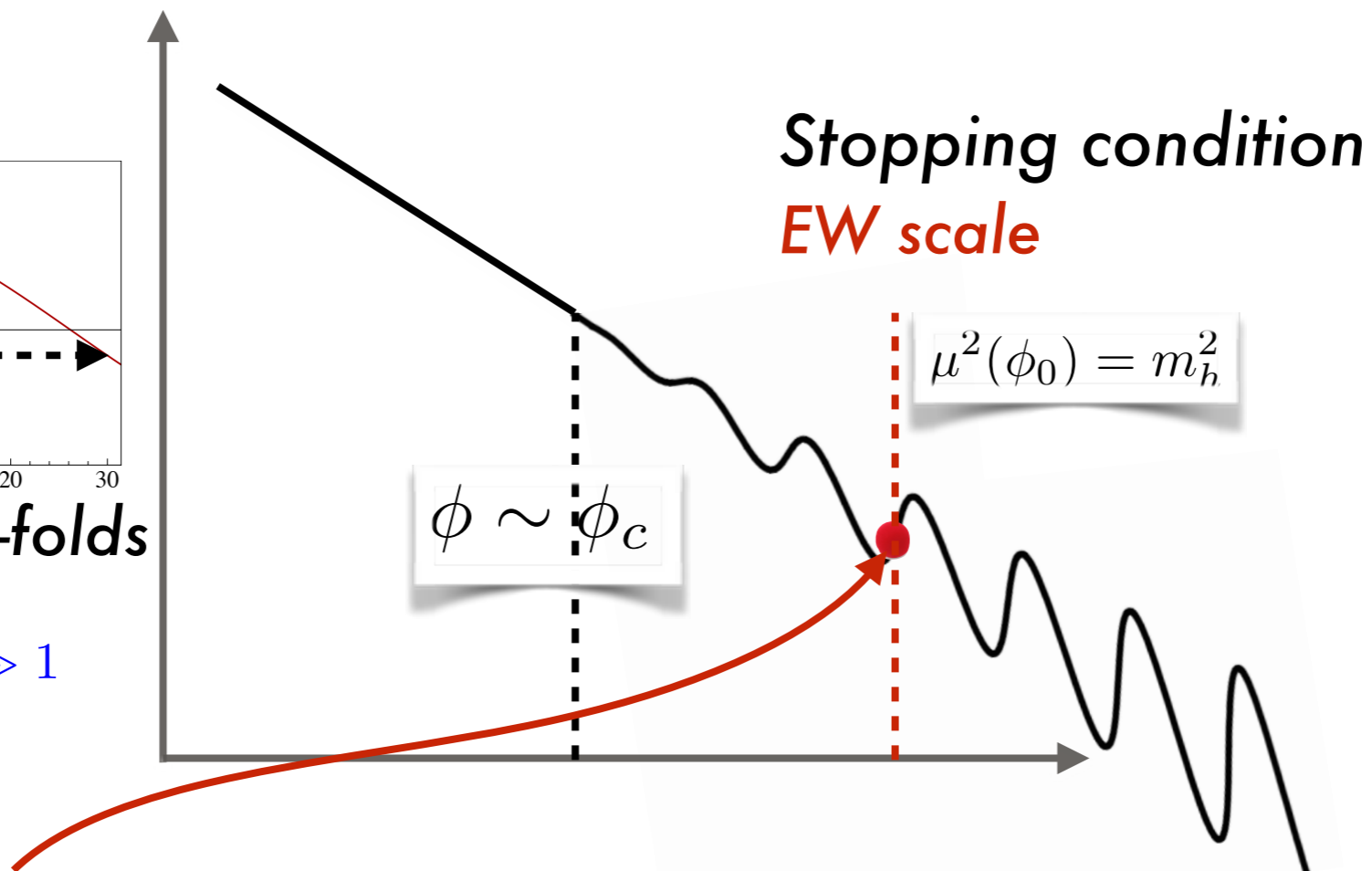
I + II = rolling + wiggles

Price to pay:



huge number of e-folds

$$N_e \sim \left(\frac{FH_I}{\Lambda_{\text{roll}}^2} \right)^2 \gg 1$$



Ratio of scales = Ratio of vevs

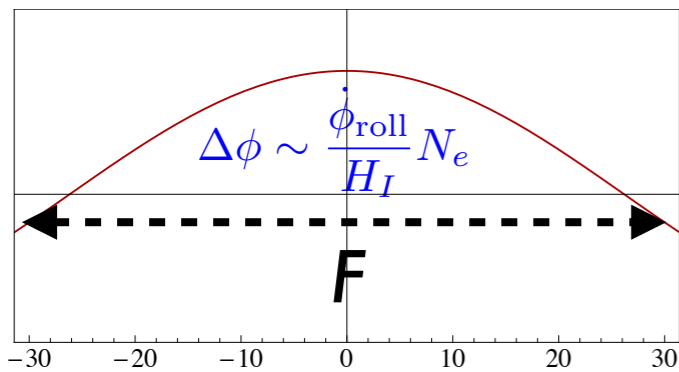
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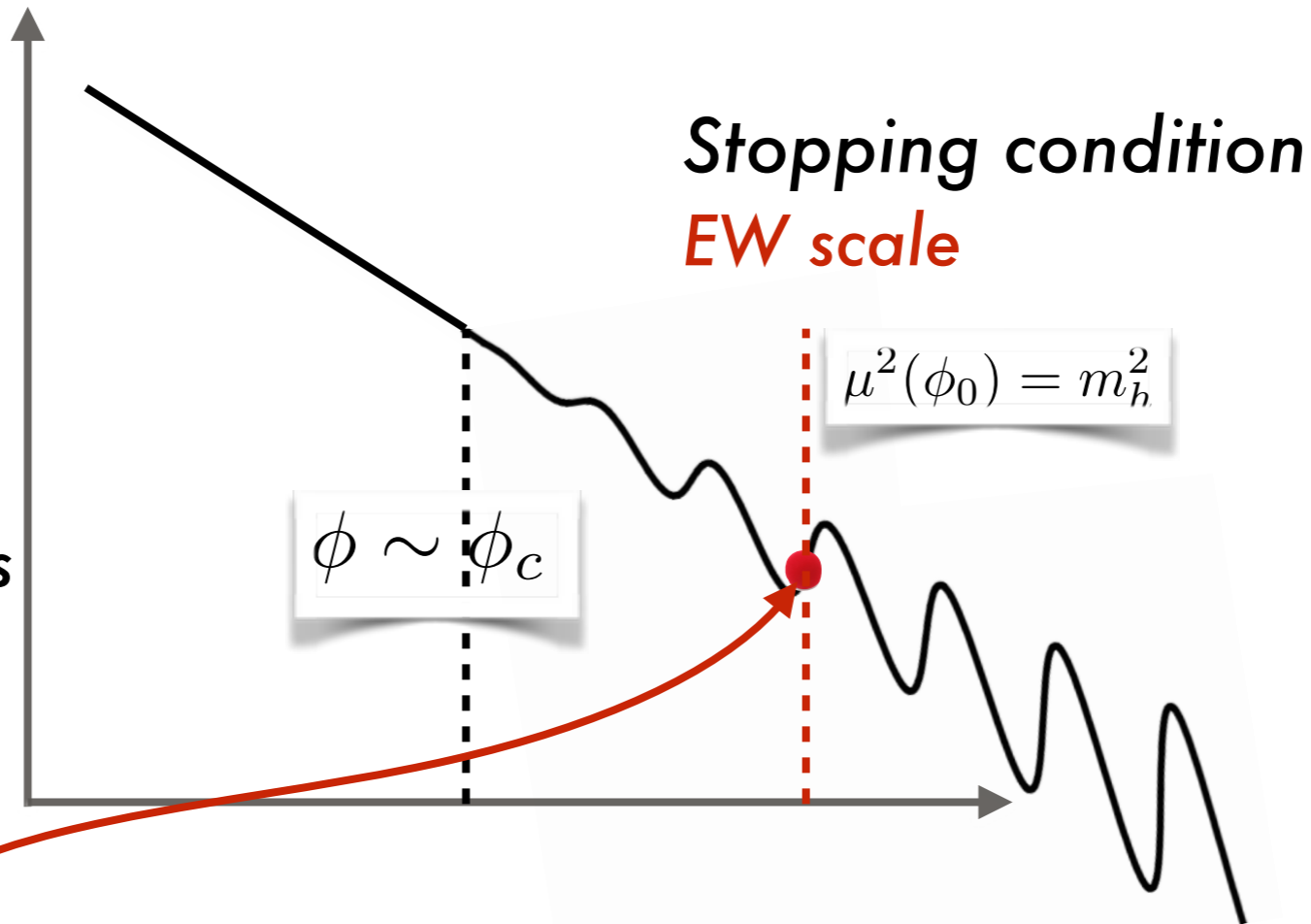
I + II = rolling + wiggles

Price to pay:



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$$N_e \sim \left(\frac{F H_I}{\Lambda_{\text{roll}}^2} \right)^2 \gg 1$$



Ratio of scales = Ratio of vevs

$$\frac{\Lambda_{\text{roll}}}{\Lambda_{\text{br}}} \sim \left(\frac{F}{f} \right)^{1/4} \simeq 1/Q \gg 1$$

CP violating phase

$$\sin \frac{\phi_0}{f} \sim \sin \frac{\phi_0}{F} \sim \mathcal{O}(1)$$

there is a price to pay for the large pace $\frac{\Lambda_H}{\Lambda_{\text{br}}} \simeq 1/\sqrt{r_{\text{roll}}} \cdot 1/Q$