

# Theory status of diboson processes

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# Outline

- Introduction
- Diboson production at NNLO
- The *MATRIX* framework
- Results
- EW corrections and anomalous couplings
- Summary

# Introduction

Vector boson pair production is a benchmark process at hadron colliders

- background to Higgs and new physics searches
- important to set limits on anomalous couplings
- new nice data available from the LHC whose accuracy will soon be comparable with theoretical uncertainties

Up to very recently the accuracy was limited to NLO QCD



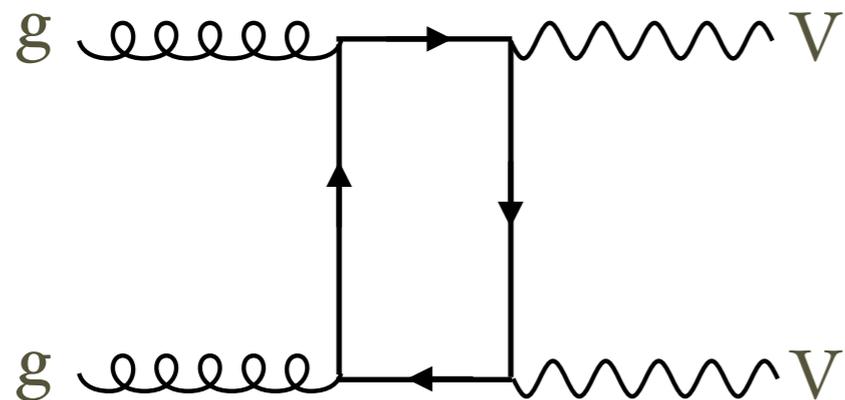
Extension to NNLO highly desirable to meet the increasing experimental precision

# Introduction



Both s and t channel contributions at Born level

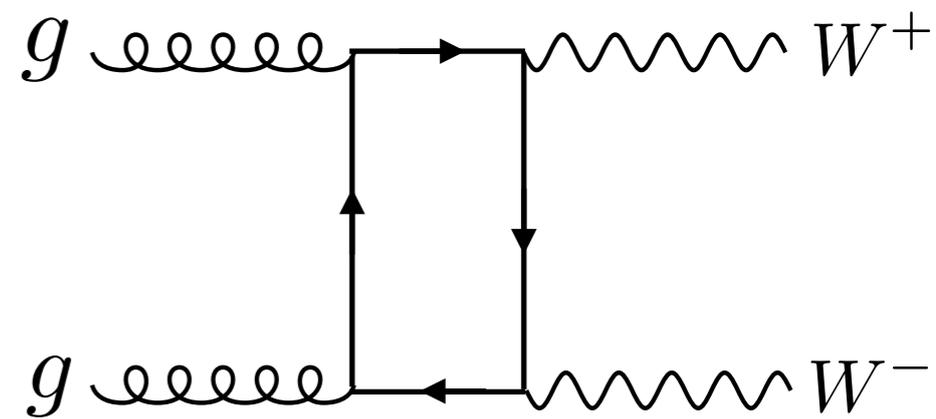
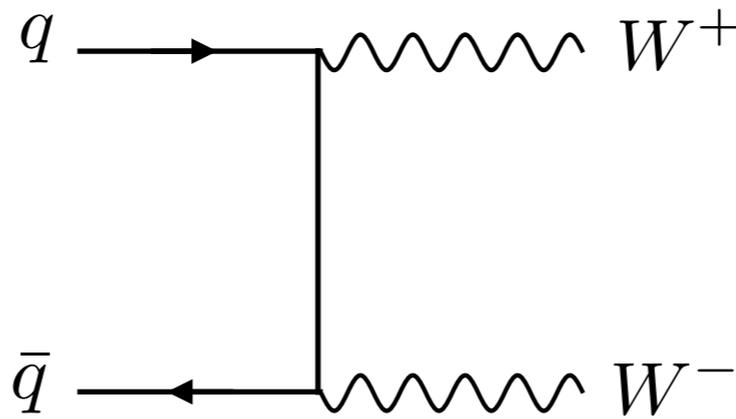
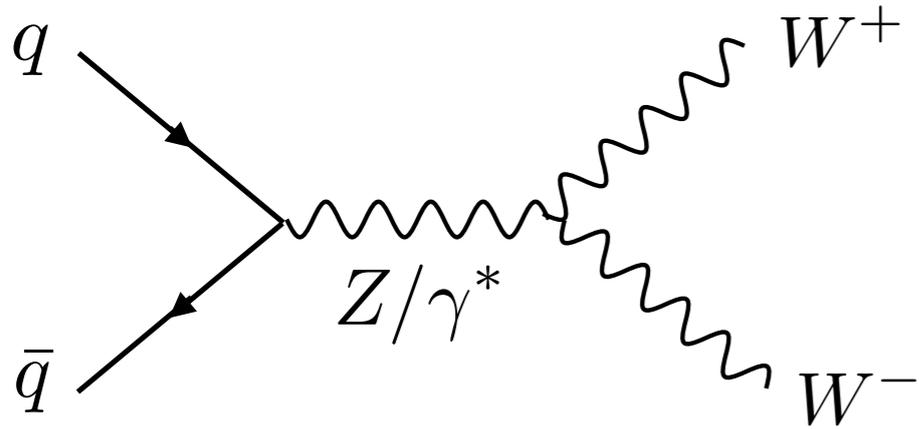
s-channel sensitive to different anomalous trilinear couplings



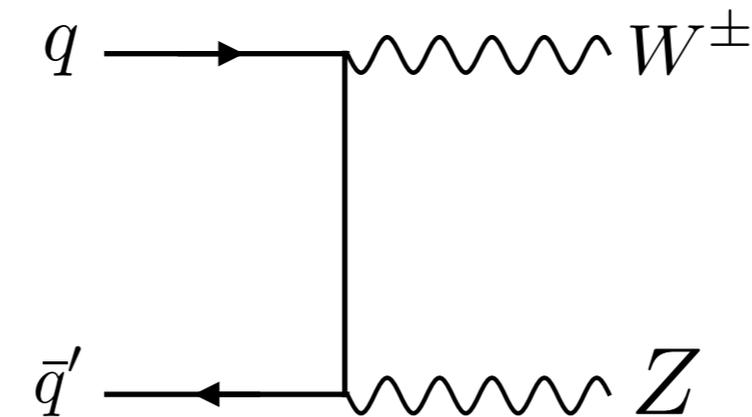
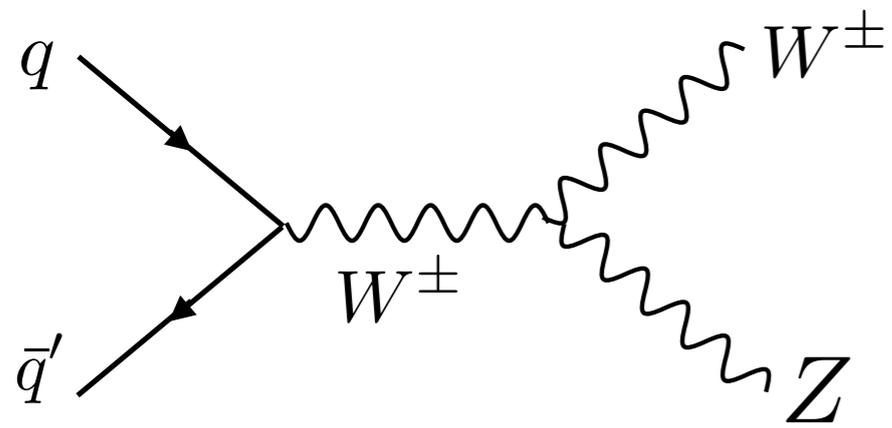
Loop induced  $gg$  contribution to processes with neutral final state  
Formally NNLO but enhanced by gluon luminosity

# Introduction

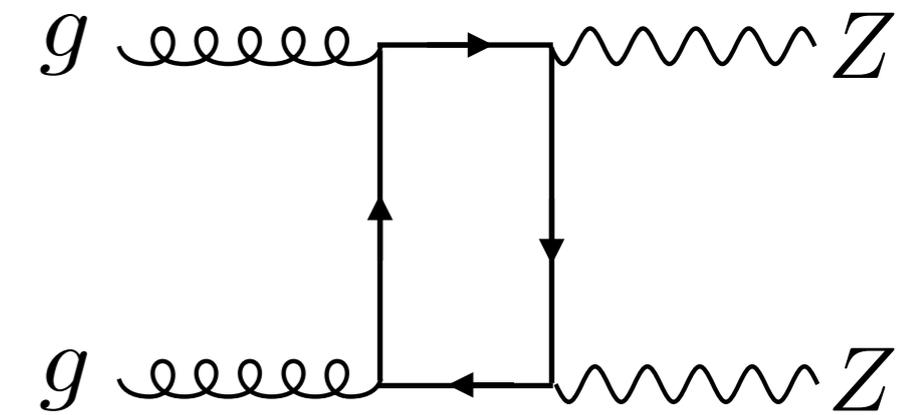
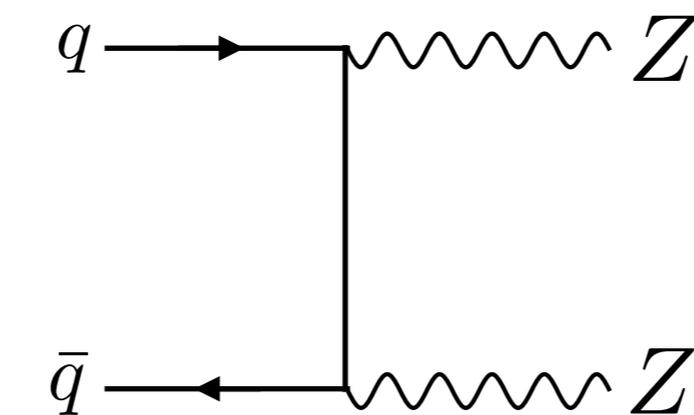
## **WW production**



## **WZ production**

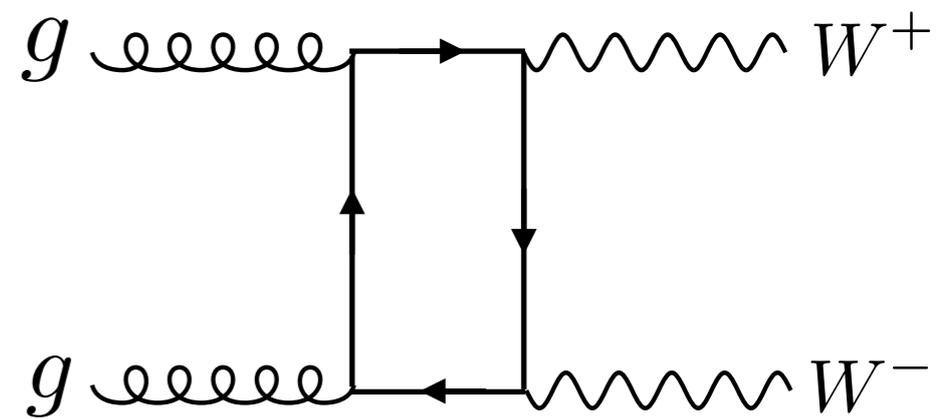
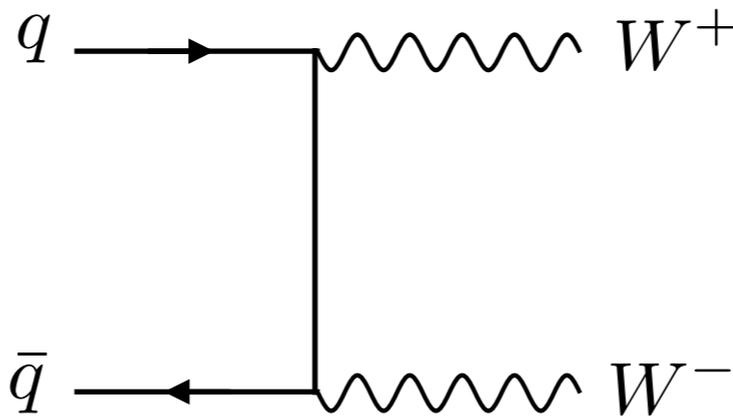
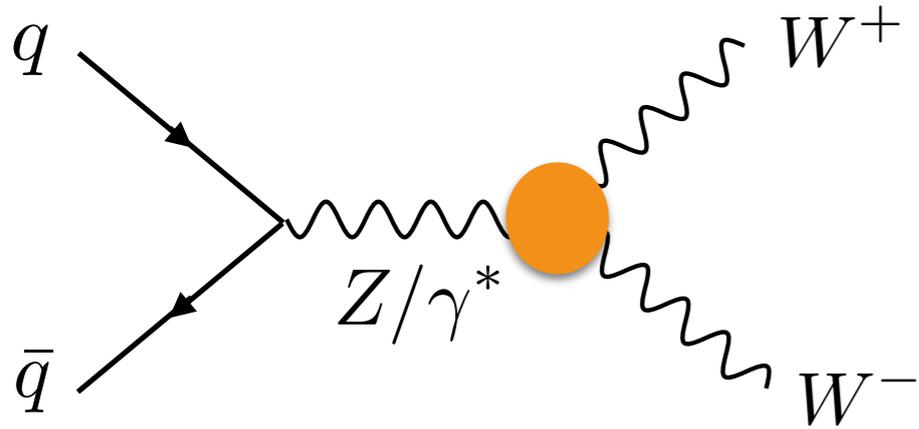


## **ZZ production**

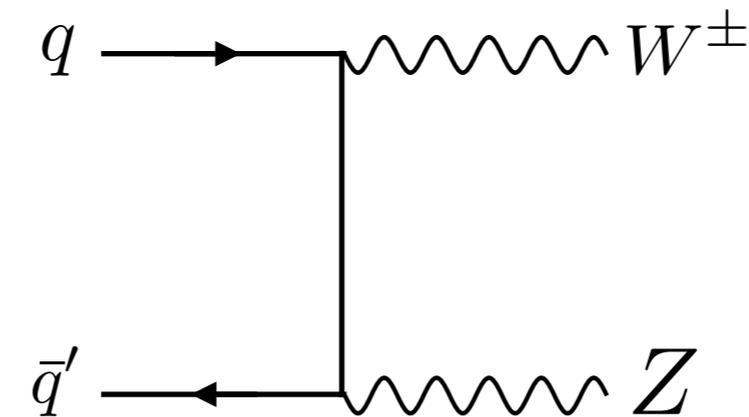
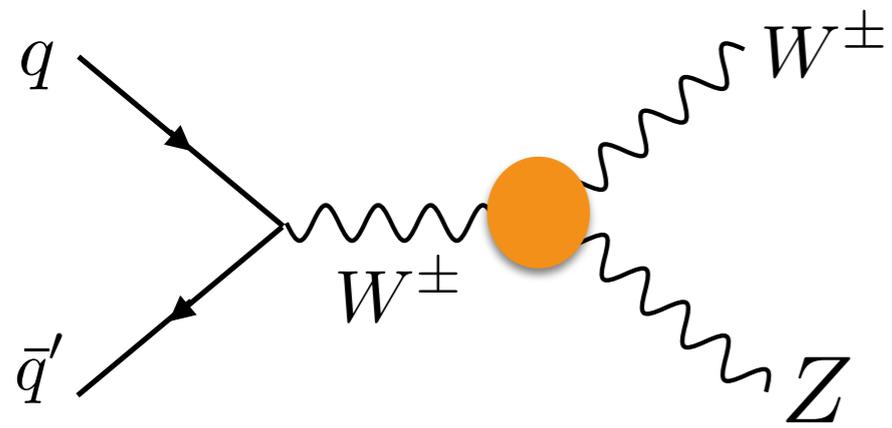


# Introduction

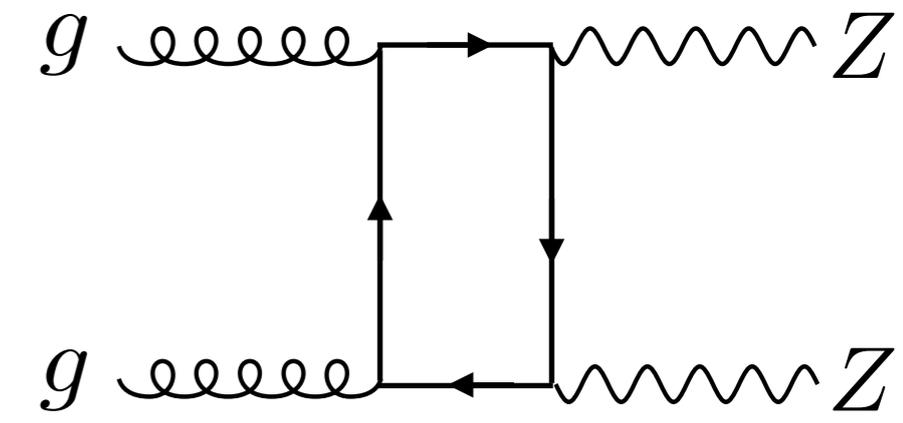
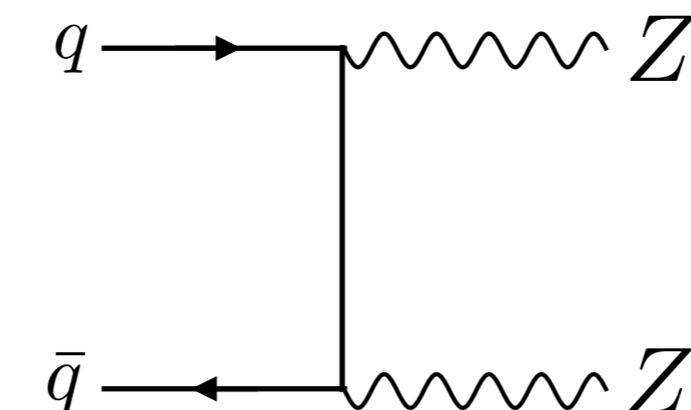
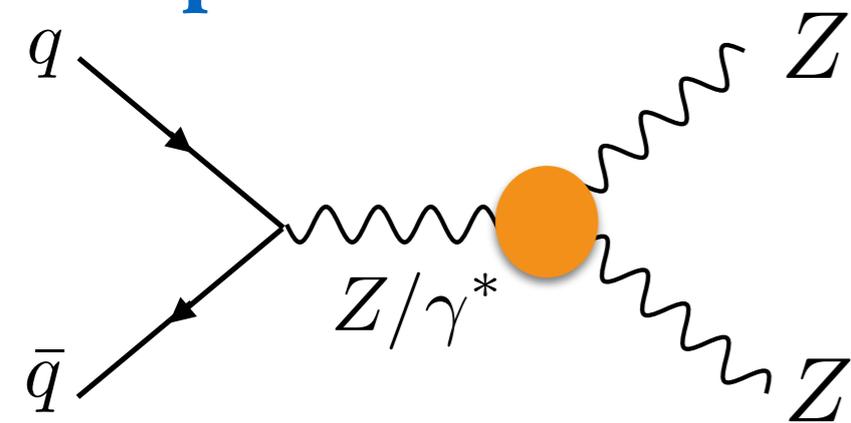
## **WW production**



## **WZ production**



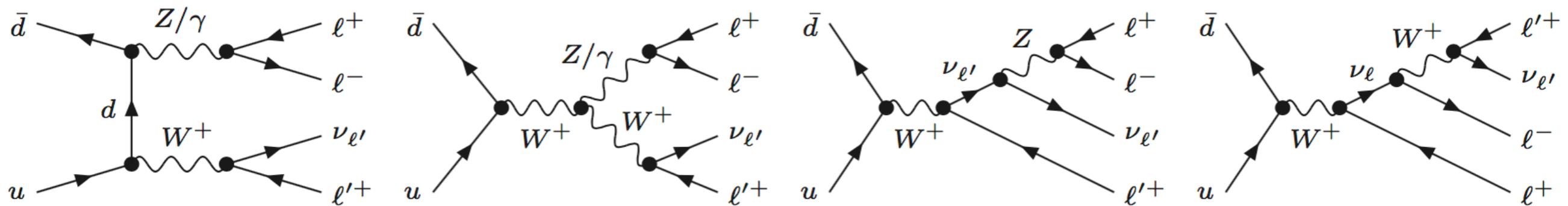
## **ZZ production**



# Off-shell and interference effects

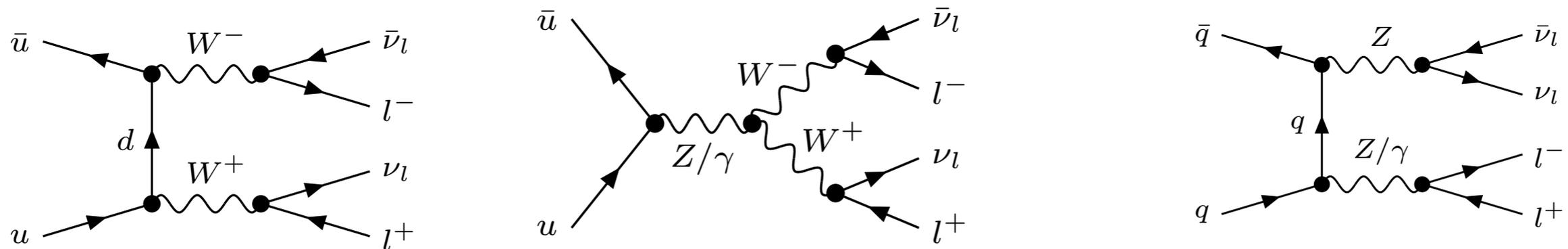
When we talk about  $VV'$  production we refer to the full calculation including resonant and non resonant diagrams with off-shell and interference effects

eg:  $W^+Z \rightarrow l^+l^-l'^+\nu_{l'}$



In some cases more than one  $VV'$  topology may contribute

eg:  $W^+W^- (ZZ) \rightarrow l^+l^- \bar{\nu}_l \nu_l$



# Vector boson pair production

$W\gamma, Z\gamma, WW, WZ, ZZ$  production known in NLO QCD since quite some time

J.Ohnemus (1993); U.Baur, T.Han, J.Ohnemus (1998)

B.Mele, P.Nason, G.Ridolfi (1991)

Also including leptonic decay

S.Frixione, P.Nason, G.Ridolfi (1992); S.Frixione (1993)

L.Dixon, Z.Kunszt, A.Signer (1999); J.Campbell, K.Ellis (1999)

D. de Florian, A.Signer (2000)

The gluon fusion loop contribution (part of NNLO) to  $Z\gamma, ZZ$  and  $WW$  is known since some time (often assumed to provide the dominant NNLO contribution)

T.Binoth et al. (2005,2008)

M.Duhrssen et al. (2005)

L.Amettler et al. (1985)

J. van der Bij, N.Glover (1988)

K. Adamson, D. de Florian, A.Signer (2000)

NLO EW corrections have also been studied

W.Hollik, C.Meier (2004)

E.Accomando, A.Denner, C.Meier (2005)

A.Bierweiler, T.Kasprzik, J.Kuhn, S.Uccirati (2012)

M.Billoni, S.Dittmaier, B.Jager, C.Speckner (2013)

A.Denner, S. Dittmaier, M. Hecht, C. Pasold (2014)

B. Biedermann et al (2016,2017)

S.Kallweit et al. (2017)

All two-loop helicity amplitudes for  $V\gamma, WW, WZ$  and  $ZZ$  production recently evaluated

T.Gehrmann, L.Tancredi (2012)

F.Caola, J.Henn, K.Melnikov, A.Smirnov, V.Smirnov (2014)

T.Gehrmann, A. von Manteuffel, L.Tancredi (2014,2015)

➔ **NNLO calculation possible**

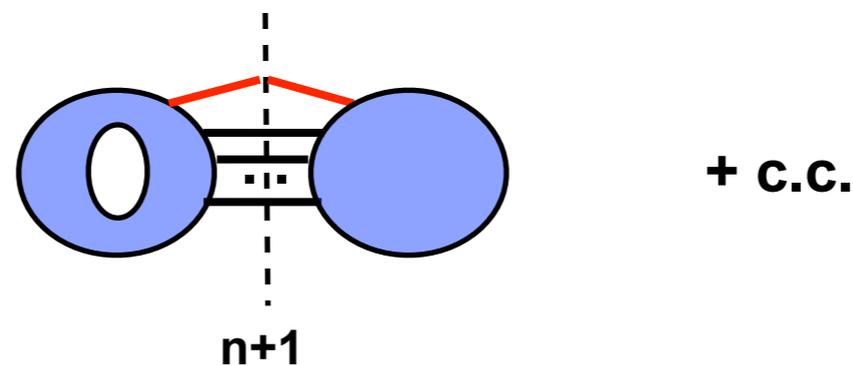
# Ingredients of NNLO calculations

Assume that the process involves  $n$  partons at LO ( $n=2$  in our case)  $\rightarrow$  we need:

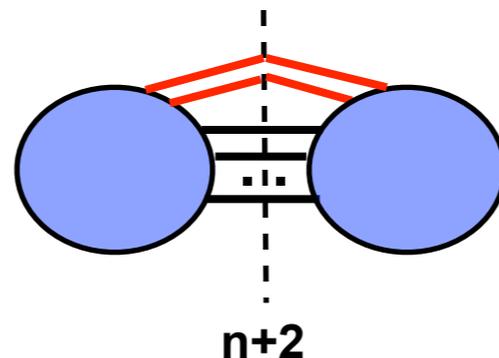
- Double virtual contribution with  $n$  resolved partons



- Real-virtual contribution with 1 unresolved parton



- Double-real contribution with 2 unresolved partons



All the three contributions are divergent: how can we handle IR singularities ?

# NNLO methods

Broadly speaking there are two approaches that we can follow:

- Organise the calculation from scratch so as to cancel all the singularities
  - sector decomposition T. Binoth, G.Heinrich (2000,2004)  
C.Anastasiou, K.Melnikov, F.Petriello (2004)
  - antenna subtraction A. & T. Gehrmann, N. Glover (2005)
  - “colourful” subtraction G, Somogyi, Z. Trocsanyi,  
V. Del Duca (2005, 2007)
  - joint use of subtraction and sector decomposition M.Czakon (2010,2011)  
R.Boughezal, K.Melnikov, F.Petriello (2011)
- Start from an inclusive NNLO calculation (sometimes obtained through resummation) and combine it with an NLO calculation for  $n+1$  parton process
  - $q_T$  subtraction S.Catani, MG (2007)
  - “N-jettiness” method R.Boughezal, C.Focke,X.Liu, F.Petriello (2015)  
F.Tackmann et al. (2015)
  - recently introduced “Born projection” method for VBF M.Cacciari, F.Dreyer, A.Karlberg, G.Salam,G.Zanderighi (2015)

# The $q_T$ subtraction method

S. Catani, MG (2007)

The  $q_T$  subtraction method allows us to write the cross section to produce an **arbitrary system  $F$  of non coloured particles** in hadronic collisions as

$$d\sigma_{(N)NLO}^F = \mathcal{H}_{(N)NLO}^F \otimes d\sigma_{LO}^F + \left[ d\sigma_{(N)LO}^{F+jets} - d\sigma_{(N)LO}^{CT} \right]$$

**this difference is computed with a cut  $r_{cut}$  on  $q_T/Q$**

**process dependent hard-collinear function**

**NLO  $F$ +jets cross section computed with dipole subtraction**

**universal counterterm**

The hard-collinear function  $\mathcal{H}^F$  has been explicitly computed up to NNLO for vector and Higgs boson production

S. Catani, MG (2010)

S. Catani, L.Cieri, D. de Florian, G.Ferrera, MG (2013)

Its general form in terms of the relevant virtual amplitudes for an arbitrary colour singlet  $F$  has been provided up to NNLO

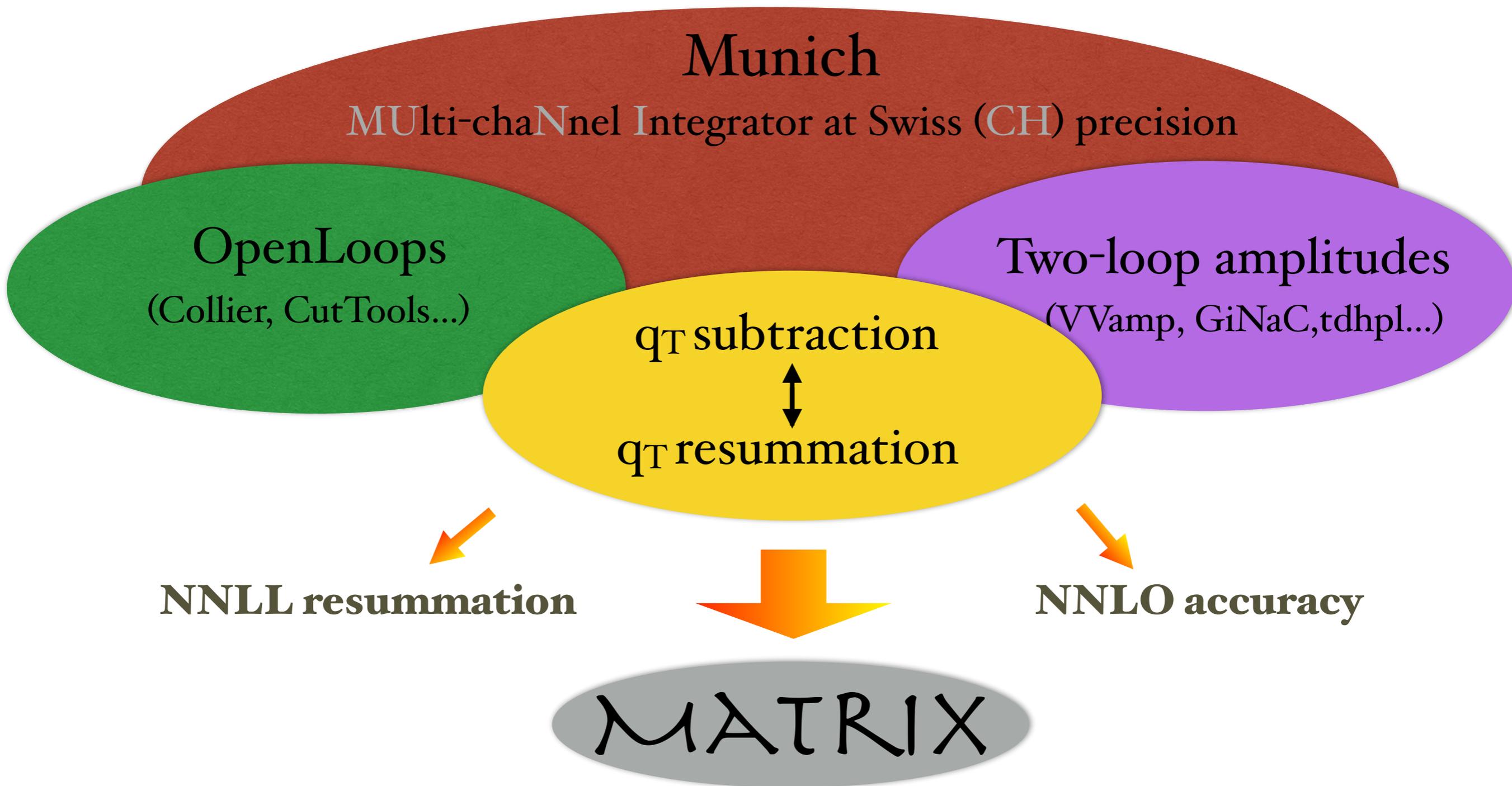
S. Catani, L.Cieri, D. de Florian, G.Ferrera, MG (2013)

T. Gehrmann, T.Lubbert, L. Yang (2014)

→ the method can be applied to the production of arbitrary colour singlets once the relevant amplitudes are available

# The MATRIX project

S. Kallweit, D. Rathlev, M. Wiesemann, MG



Munich Automates  $q_T$  subtraction and Resummation to Integrate X-sections

# Status

- $pp \rightarrow Z/\gamma^* (\rightarrow l+l')$  ✓
- $pp \rightarrow W (\rightarrow l\nu)$  ✓
- $pp \rightarrow H$  ✓
- $pp \rightarrow \gamma\gamma$  ✓
- $pp \rightarrow W\gamma \rightarrow l\nu\gamma$  ✓
- $pp \rightarrow Z\gamma \rightarrow l+l' (\nu\nu)\gamma$  ✓
- $pp \rightarrow ZZ (\rightarrow 4l)$  ✓
- $pp \rightarrow WW \rightarrow (l\nu l'\nu')$  ✓
- $pp \rightarrow ZZ/WW \rightarrow ll\nu\nu$  ✓
- $pp \rightarrow WZ \rightarrow l\nu ll$  ✓
- $pp \rightarrow HH$  (✓) not in public release

First public release out  
in November 2017

S.Kallweit, M.Wiesemann, MG (2017)

now also in MCFM

see also G.Heinrich et al. 2018 for on shell Z bosons

# Results

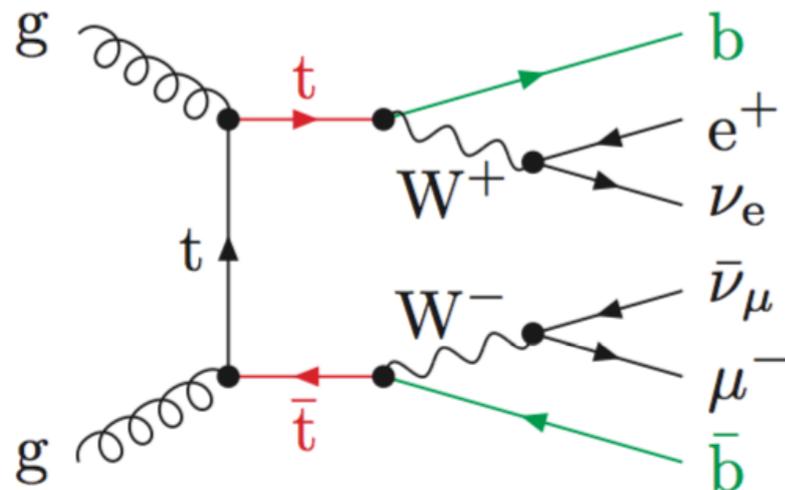
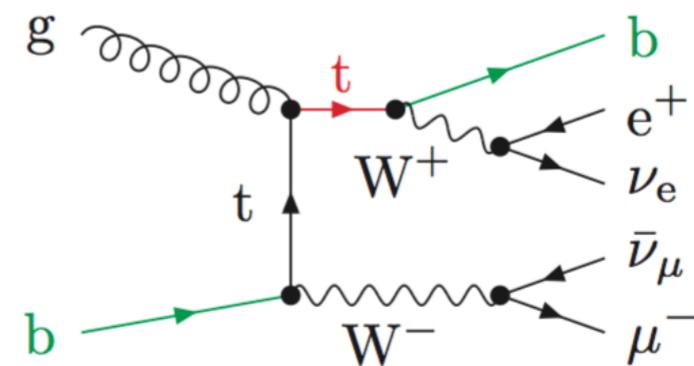
# $pp \rightarrow WW + X$ at NNLO

T. Gehrmann, S. Kallweit, P. Maierhofer, A. von Manteuffel,  
S. Pozzorini, D. Rathlev, L. Tancredi, MG (2014)

The  $WW$  cross section cannot be naively defined in QCD perturbation theory

In the 5-flavor scheme diagrams with real b-quarks are crucial to cancel collinear singularities from  $g \rightarrow b\bar{b}$  splitting

Already at NLO there are contributions with final state b-quarks coming from  $Wt$  production (+30-60%)



At NNLO it is even worse with doubly resonant  $t\bar{t}$  diagrams which enhance the cross section at 7(14) TeV by a factor 4(8)

→ We use the 4-flavor scheme: the bottom quarks are massive and we can omit diagrams with b-quark emissions and obtain a consistent  $WW$  cross section at NNLO

# WW: fully differential

S. Kallweit, S.Pozzorini, D. Rathlev, M.Wiesemann, MG (2016)

Consider for simplicity only the different flavour channel

Focus in particular on  $pp \rightarrow W^+W^- + X \rightarrow e^- \mu^+ \bar{\nu}_e \nu_\mu + X$

WW cuts:

- $p_{T1} > 25 \text{ GeV}$      $p_{T2} > 20 \text{ GeV}$   
 $\Delta R(l,l) > 0.1$      $|\eta_\mu| < 2.4$      $|\eta_e| < 1.37$  or  $1.52 < |\eta_e| < 2.47$
- $\begin{cases} p_{T^{\text{rel}}} = p_{T^{\text{miss}}} & \Delta\phi > \pi/2 \\ p_{T^{\text{rel}}} = p_{T^{\text{miss}}} \sin\Delta\phi & \Delta\phi < \pi/2 \end{cases}$      $\Delta\phi = \text{azimuthal separation between } p_{T^{\text{miss}}} \text{ and the closest lepton}$
- $m_{ll} > 10 \text{ GeV}$      $p_{T^{\text{miss}}} > 20 \text{ GeV}$      $p_{T^{\text{rel}}} > 15 \text{ GeV}$
- **Jet veto:** no jets with  $p_T > 25 \text{ GeV}$ ,  $|\eta| < 4.5$

Jets: anti-kt  
with  $R=0.4$

Use NNPDF3.0 with  $\mu_F = \mu_R = m_W$  as central scale

Work in the 4FNS but always compare with subtracted 5FNS result

# WW: fully differential

S. Kallweit, S.Pozzorini, D. Rathlev, M.Wiesemann, MG (2016)

Corresponding fiducial cross sections and acceptances:

$\sqrt{s}$	$\sigma_{\text{fiducial}}(W^+W^-\text{-cuts})$ [fb]		$\sigma/\sigma_{\text{NLO}} - 1$	
	8 TeV	13 TeV	8 TeV	13 TeV
LO	147.23 (2) $^{+3.4\%}_{-4.4\%}$	233.04(2) $^{+6.6\%}_{-7.6\%}$	-3.8%	- 1.3%
NLO	153.07 (2) $^{+1.9\%}_{-1.6\%}$	236.19(2) $^{+2.8\%}_{-2.4\%}$	0	0
NLO'	156.71 (3) $^{+1.8\%}_{-1.4\%}$	243.82(4) $^{+2.6\%}_{-2.2\%}$	+2.4%	+ 3.2%
NLO'+gg	166.41 (3) $^{+1.3\%}_{-1.3\%}$	267.31(4) $^{+1.5\%}_{-2.1\%}$	+8.7%	+13.2%
NNLO	164.16(13) $^{+1.3\%}_{-0.8\%}$	261.5(2) $^{+1.9\%}_{-1.2\%}$	+7.2%	+10.7%

Impact of radiative corrections strongly reduced by the jet veto

$\sqrt{s}$	$\epsilon = \sigma_{\text{fiducial}}(W^+W^-\text{-cuts})/\sigma_{\text{inclusive}}$		$\epsilon/\epsilon_{\text{NLO}} - 1$	
	8 TeV	13 TeV	8 TeV	13 TeV
LO	0.34608(7) $^{+0.6\%}_{-0.7\%}$	0.29915(6) $^{+0.8\%}_{-1.0\%}$	+41.0%	+52.6%
NLO	0.24552(5) $^{+4.4\%}_{-4.7\%}$	0.19599(4) $^{+4.4\%}_{-4.7\%}$	0	0
NLO'+gg	0.25374(7) $^{+3.5\%}_{-3.7\%}$	0.20773(5) $^{+3.2\%}_{-3.1\%}$	+ 3.3%	+ 6.0%
NNLO	0.2378(4) $^{+1.3\%}_{-0.9\%}$	0.1907(3) $^{+1.2\%}_{-0.9\%}$	- 3.2%	- 2.7%

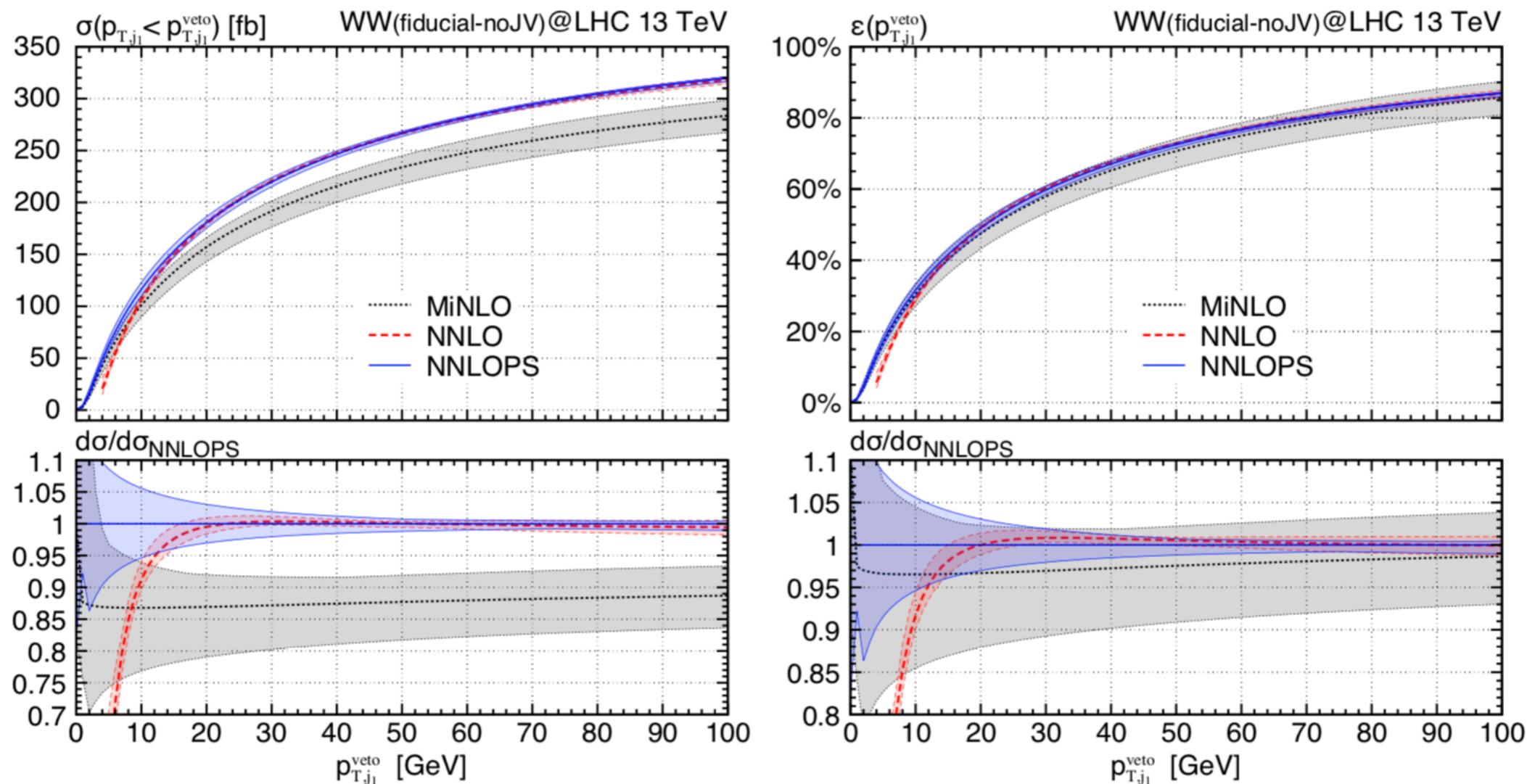
Consequently NLO+gg provides good approximation of the fiducial cross sections (but not of the acceptance)

# NNLOPS for WW

E.Re, M.Wiesemann, G.Zanderighi (2018)

NNLO predictions can be matched to parton showers by using the NNLOPS method

K. Hamilton, P. Nason, E. Re and G. Zanderighi (2013)



NNLO works well down to  $p_{T,j_1}^{\text{veto}}$  of about 15 GeV

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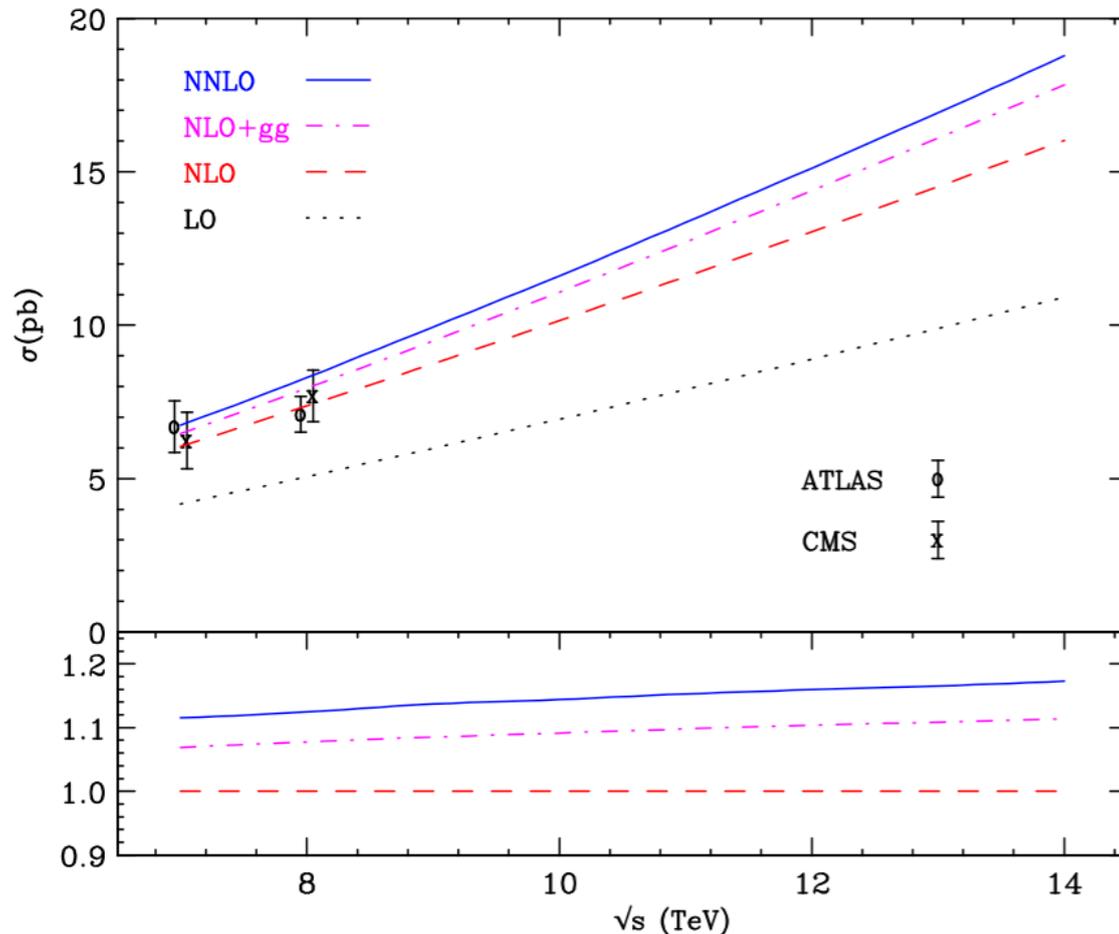
K. Hamilton, P. Nason, E. Re and G. Zanderighi (2013)

$q\bar{q}$ (no loop <sup>2</sup> $gg$ )	$\sigma_{\text{incl}}(pp \rightarrow W^+W^-)$ [pb]	$\sigma_{\text{fid}}(pp \rightarrow e^\mp \nu_e \mu^\pm \nu_\mu)$ [fb]	$A = \sigma_{\text{fid}}/\sigma_{\text{incl}}$ [%]
LO	$70.66(1)^{+5.1\%}_{-6.2\%}$	$440.5(0)^{+6.0\%}_{-7.1\%}$	0.623
NLO	$99.96(3)^{+3.5\%}_{-2.8\%}$	$411.8(1)^{+2.7\%}_{-2.3\%}$	0.412
NNLO	$110.0(1)^{+1.6\%}_{-1.6\%}$	$413.1(2)^{+1.0\%}_{-0.7\%}$	0.376
MINLO	$96.05(1)^{+7.1\%}_{-4.9\%}$	$359.6(1)^{+5.4\%}_{-8.3\%}$	0.374
NNLOPS	$110.2(2)^{+1.7\%}_{-1.6\%}$	$413.0(2)^{+2.2\%}_{-2.3\%}$	0.375
ATLAS- $gg$ [9]	$124.7 \pm 5$ (stat) $\pm 13$ (syst) $\pm 3$ (lumi)	$473 \pm 20$ (stat) $\pm 50$ (syst) $\pm 11$ (lumi)	0.379
CMS- $gg$ [10]	$108.5 \pm 5.8$ (stat) $\pm 5.7$ (exp. syst) $\pm 6.4$ (theo. syst) $\pm 3.6$ (lumi)	—	—

NNLOPS impact more visible in soft-gluon sensitive observables

# $pp \rightarrow ZZ + X$ at NNLO

F.Cascioli, T.Gehrmann, S.Kallweit, P.Maierhoefer, A. von Manteuffel,  
S.Pozzorini, D.Rathlev, L.Tancredi, E.Weih, MG (2014)



Inclusive cross sections for on shell ZZ pairs

NNLO effect ranges from **12 to 17 %**  
when  $\sqrt{s}$  varies from 7 to 14 TeV

Loop induced gg contribution **58-62%** of  
the full NNLO effect

We choose  $\mu_F = \mu_R = m_Z$  as central scale

Scale uncertainties of order  $\pm 3\%$  at NLO and  
at NNLO

$\sqrt{s}$ (TeV)	$\sigma_{LO}$ (pb)	$\sigma_{NLO}$ (pb)	$\sigma_{NNLO}$ (pb)
7	$4.167^{+0.7\%}_{-1.6\%}$	$6.044^{+2.8\%}_{-2.2\%}$	$6.735^{+2.9\%}_{-2.3\%}$
8	$5.060^{+1.6\%}_{-2.7\%}$	$7.369^{+2.8\%}_{-2.3\%}$	$8.284^{+3.0\%}_{-2.3\%}$
9	$5.981^{+2.4\%}_{-3.5\%}$	$8.735^{+2.9\%}_{-2.3\%}$	$9.931^{+3.1\%}_{-2.4\%}$
10	$6.927^{+3.1\%}_{-4.3\%}$	$10.14^{+2.9\%}_{-2.3\%}$	$11.60^{+3.2\%}_{-2.4\%}$
11	$7.895^{+3.8\%}_{-5.0\%}$	$11.57^{+3.0\%}_{-2.4\%}$	$13.34^{+3.2\%}_{-2.4\%}$
12	$8.882^{+4.3\%}_{-5.6\%}$	$13.03^{+3.0\%}_{-2.4\%}$	$15.10^{+3.2\%}_{-2.4\%}$
13	$9.887^{+4.9\%}_{-6.1\%}$	$14.51^{+3.0\%}_{-2.4\%}$	$16.91^{+3.2\%}_{-2.4\%}$
14	$10.91^{+5.4\%}_{-6.7\%}$	$16.01^{+3.0\%}_{-2.4\%}$	$18.77^{+3.2\%}_{-2.4\%}$

# $pp \rightarrow ZZ + X$ at NNLO: lepton decays and off-shell effects

S. Kallweit, D. Rathlev, MG (2015)

Consider  $pp \rightarrow ZZ \rightarrow 4$  leptons at 8 TeV

Use ATLAS cuts to define fiducial region:

$$p_{T1} > 7 \text{ GeV} \quad |\eta_1| < 2.7 \quad \Delta R(1,1) > 0.2$$

$$66 \text{ GeV} < m_{Z1}, m_{Z2} < 116 \text{ GeV}$$

crucial for IR safety!

In the identical flavour case there is an ambiguity in choosing the Z candidates: solved by choosing the pairs for which the sum of the distances from  $m_Z$  is minimum

Channel	$\sigma_{\text{LO}}$ (fb)	$\sigma_{\text{NLO}}$ (fb)	$\sigma_{\text{NNLO}}$ (fb)	$\sigma_{\text{exp}}$ (fb)
$e^+e^-e^+e^-$	$3.547(1)^{+2.9\%}_{-3.9\%}$	$5.047(1)^{+2.8\%}_{-2.3\%}$	$5.79(2)^{+3.4\%}_{-2.6\%}$	$4.6^{+0.8}_{-0.7}(\text{stat})^{+0.4}_{-0.4}(\text{syst.})^{+0.1}_{-0.1}(\text{lumi.})$
$\mu^+\mu^-\mu^+\mu^-$				$5.0^{+0.6}_{-0.5}(\text{stat})^{+0.2}_{-0.2}(\text{syst.})^{+0.2}_{-0.2}(\text{lumi.})$
$e^+e^-\mu^+\mu^-$	$6.950(1)^{+2.9\%}_{-3.9\%}$	$9.864(2)^{+2.8\%}_{-2.3\%}$	$11.31(2)^{+3.2\%}_{-2.5\%}$	$11.1^{+1.0}_{-0.9}(\text{stat})^{+0.5}_{-0.5}(\text{syst.})^{+0.3}_{-0.3}(\text{lumi.})$

NNLO corrections improve agreement with ATLAS data in the  $2e2\mu$  channel but make the agreement worse in the other channels (but experimental uncertainties still large)

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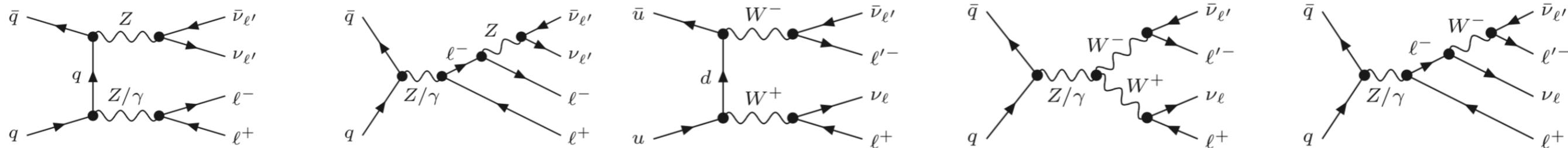
+15% (60% comes from gg fusion)

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**NEW:**

# $pp \rightarrow 2l2\nu + X$ at NNLO

S. Kallweit, M. Wiesemann (to appear)



$e^+e^- \nu\nu$  and  $\mu^+\mu^- \nu\nu$  final states can originate from both  $ZZ$  and  $WW$  production

First NNLO calculation where two different doubly resonant topologies are accounted for

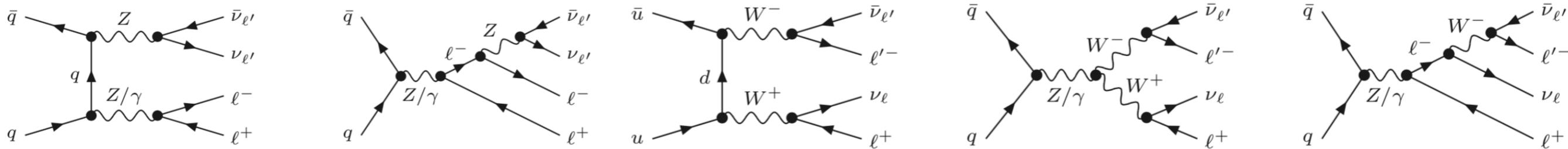
➔ Follow experimental strategy and isolate the  $ZZ$  signal by subtracting the different-flavour contribution which includes resonant  $WW$  and  $t\bar{t}$  production

Their interference with the  $ZZ$  signal is instead kept

**NEW:**

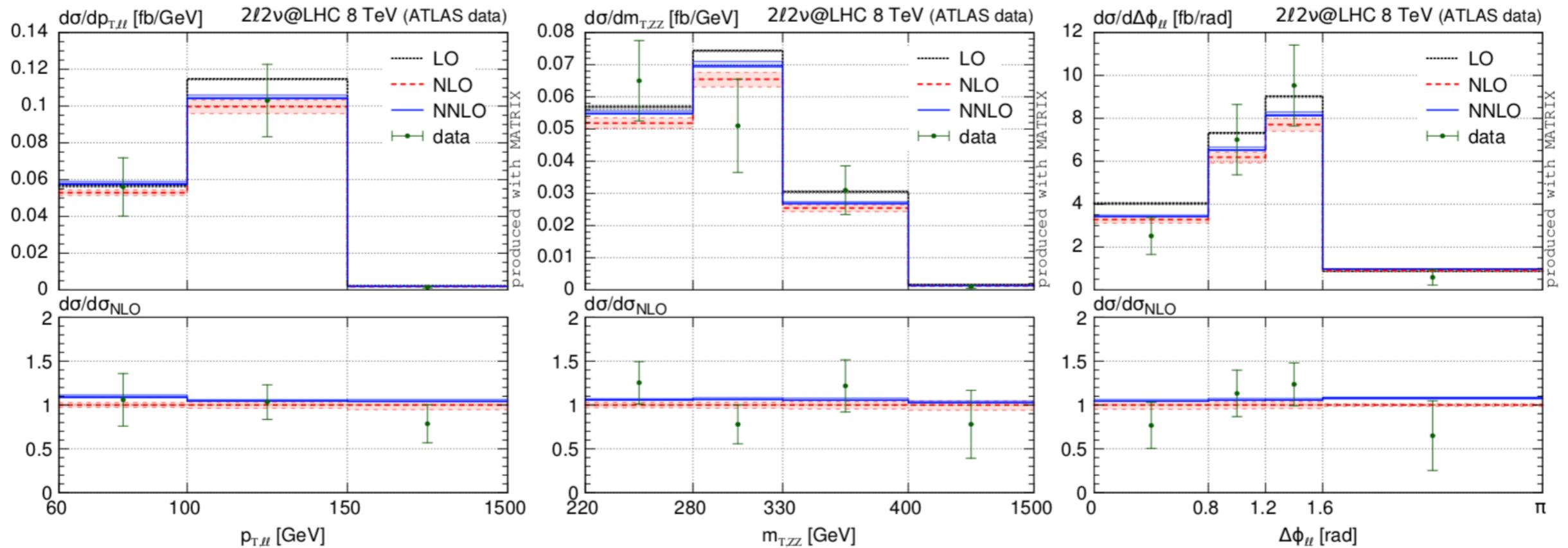
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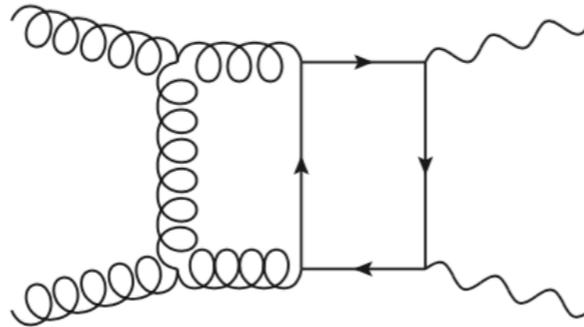
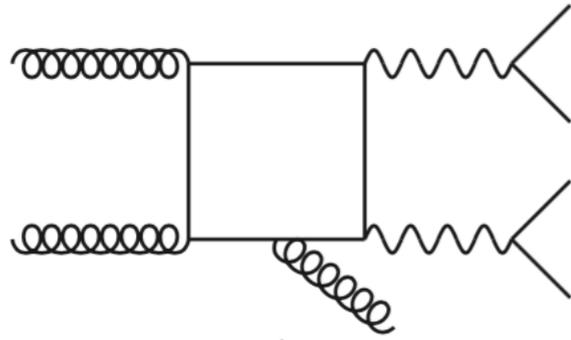
$2l2\nu_1$  final states can originate from both ZZ and WW production

**PRELIMINARY**



Improved agreement between data and theoretical predictions

# $gg \rightarrow WW/ZZ + X$ at NLO



NLO corrections to  $gg \rightarrow WW/ZZ$  are formally  $N^3LO$  but important given the large gluon luminosity

Two-loop amplitude available

F. Caola, J. M. Henn, K. Melnikov, A. V. Smirnov and V. A. Smirnov (2015)  
A. von Manteuffel and L. Tancredi (2015)

Computation completed (no fermionic channels)

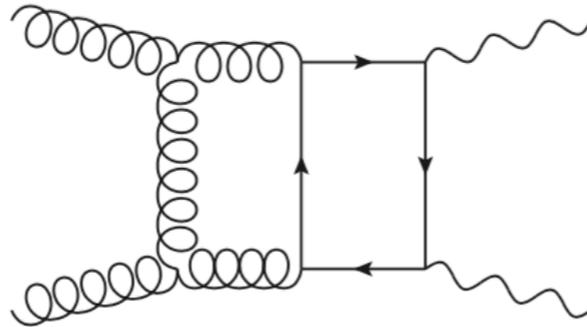
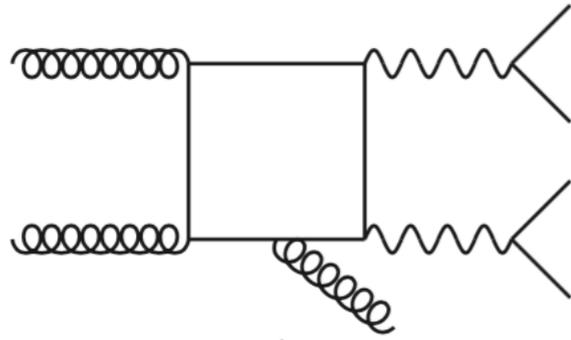
F. Caola, K. Melnikov, R. Röntsch, L. Tancredi (2015)

Impact particularly relevant for  $ZZ$

Recently matched to parton shower in the POWHEG framework

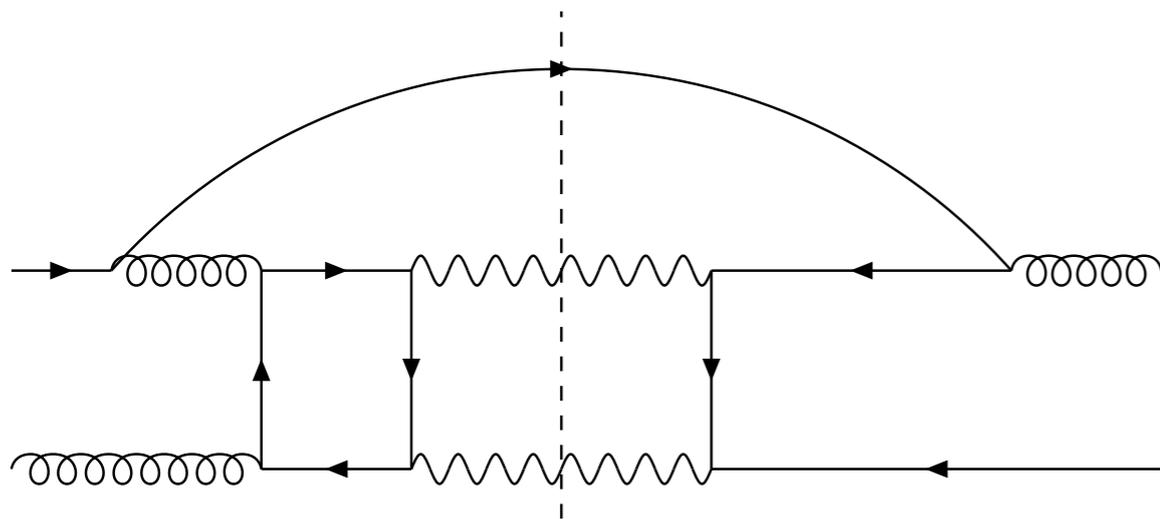
S. Alioli, F. Caola, G. Luisoni, R. Röntsch (2016)

# $gg \rightarrow WW/ZZ+X$ at NLO



Experimental analyses combine NNLO in qqbar and NLO in gg as if they were independent processes

But this is only an approximation !



Already at NNLO the two production channels mix

It would be useful to include the two calculations in a single generator

**NEW:**

# $gg \rightarrow ZZ + X$ at NLO

JY Yook, S. Kallweit, M. Wiesemann, MG (in progress)

We have included the NLO calculation within the MATRIX framework

Use ATLAS cuts at 13 TeV and consider  $gg \rightarrow ZZ \rightarrow 2e2\mu$

$p_{T,\ell} > 7 \text{ GeV}$ , one electron with  $|\eta_e| < 4.9$ , the others  $|\eta_e| < 2.5$ ,  $|\eta_\mu| < 2.7$

$\Delta R_{\ell\ell} > 0.2$ ,  $\Delta R_{\ell\ell'} > 0.2$ ,  $66 \text{ GeV} \leq m_{Z_{a/b}^{\text{rec}}} \leq 116 \text{ GeV}$ ,

anti- $k_T$  jets with  $R = 0.4$ ,  $p_{T,j} > 25 \text{ GeV}$ ,  $|\eta_j| < 4.5$

$\mu_F = \mu_R = m_{ZZ}/2$

**PRELIMINARY:**

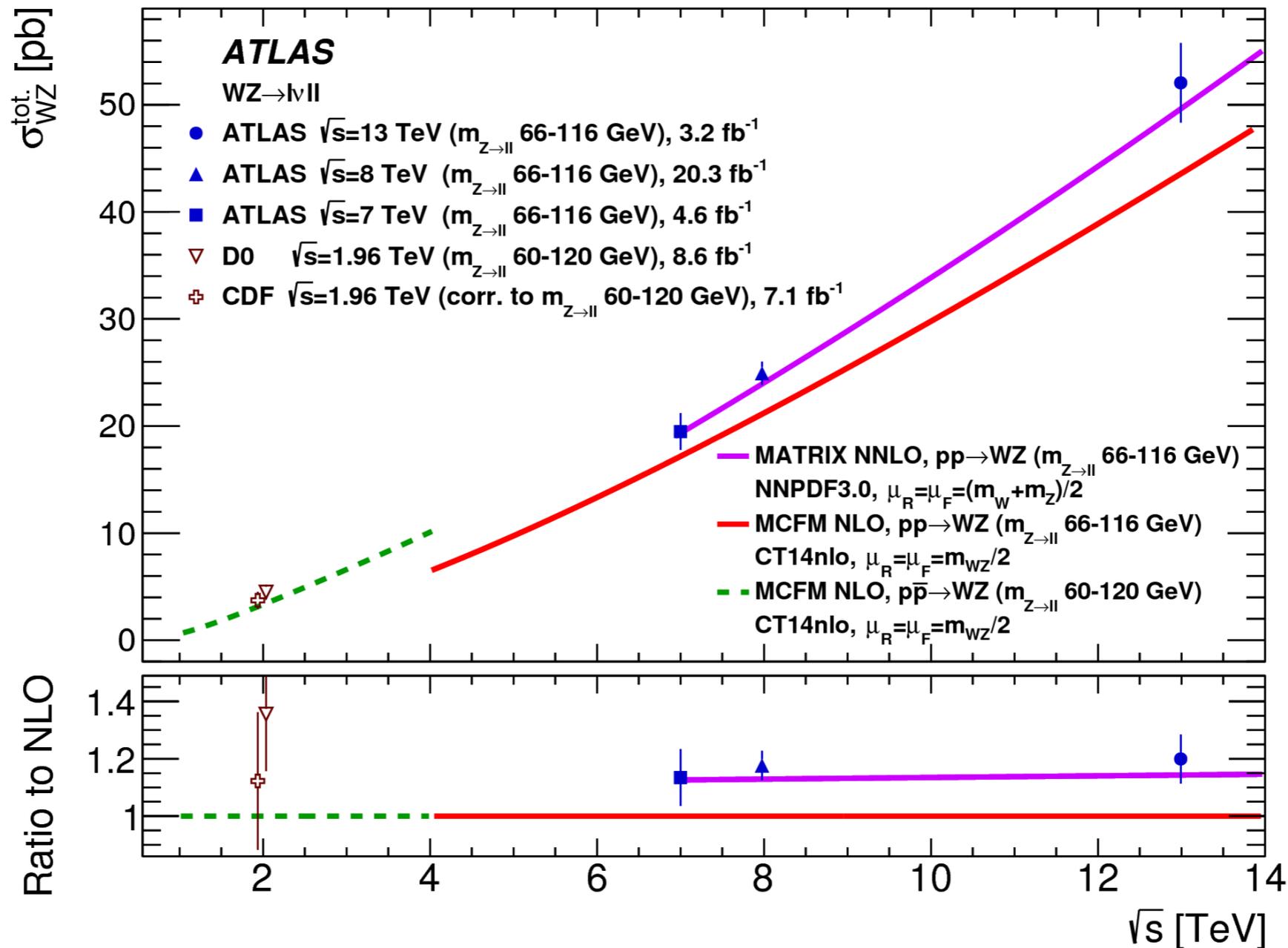
	NLO	NNLO	LO <sub>gg</sub>	NLO <sub>gg</sub> (gg only)	NLO <sub>gg</sub>	N <sup>3</sup> LO approx
$\sigma(\text{fb})$	19.82(6) <sup>+2.5%</sup> <sub>-2.0%</sub>	23.57(2) <sup>+3.2%</sup> <sub>-2.6%</sub>	2.002(4) <sup>+23.5%</sup> <sub>-17.9%</sub>	3.62(2) <sup>+15.2%</sup> <sub>-12.7%</sub>	3.41(2) <sup>+13.8%</sup> <sub>-12.0%</sub>	24.98(4) <sup>+3.0%</sup> <sub>-2.7%</sub>

↑  
**+19% wrt  
NLO**

↑  
**+6% wrt  
NNLO**

# WZ: inclusive cross section

S. Kallweit, D. Rathlev, M. Wiesemann, MG (2016)



NNLO corrections nicely improve the agreement with the data (with the exception of CMS at 13 TeV where, however, the uncertainties are still large)

# EW corrections

When precision is concerned EW corrections should also be considered: automatic NLO (QCD+)EW generators now exist that can complement the progress on the NNLO side

Recola2 → **talk by Jean-Nicolas Lang**

Setup	LO [fb]	NLO QCD [fb]	NLO EW [fb]
$W^-Z$ ATLAS	$12.6455(9)^{+5.5\%}_{-6.8\%}$	$23.780(4)^{+5.5\%}_{-4.6\%}$	$11.891(4)^{+5.6\%}_{-6.9\%}$
$W^-Z$ CMS	$9.3251(8)^{+5.3\%}_{-6.7\%}$	$17.215(4)^{+5.4\%}_{-4.3\%}$	$8.870(2)^{+5.5\%}_{-6.7\%}$
$W^+Z$ ATLAS	$18.875(1)^{+5.2\%}_{-6.4\%}$	$34.253(6)^{+5.3\%}_{-4.3\%}$	$17.748(8)^{+5.3\%}_{-6.5\%}$
$W^+Z$ CMS	$14.307(1)^{+5.0\%}_{-6.2\%}$	$26.357(6)^{+5.4\%}_{-4.3\%}$	$13.600(4)^{+5.1\%}_{-6.3\%}$

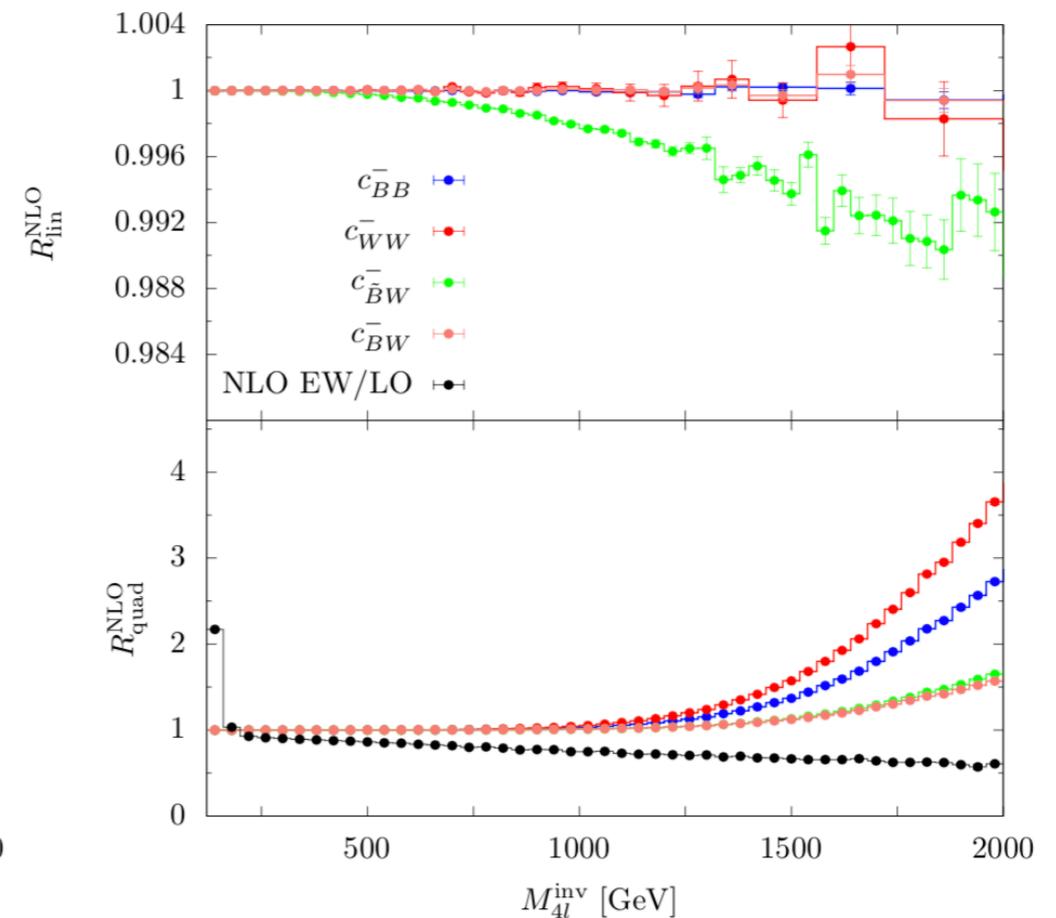
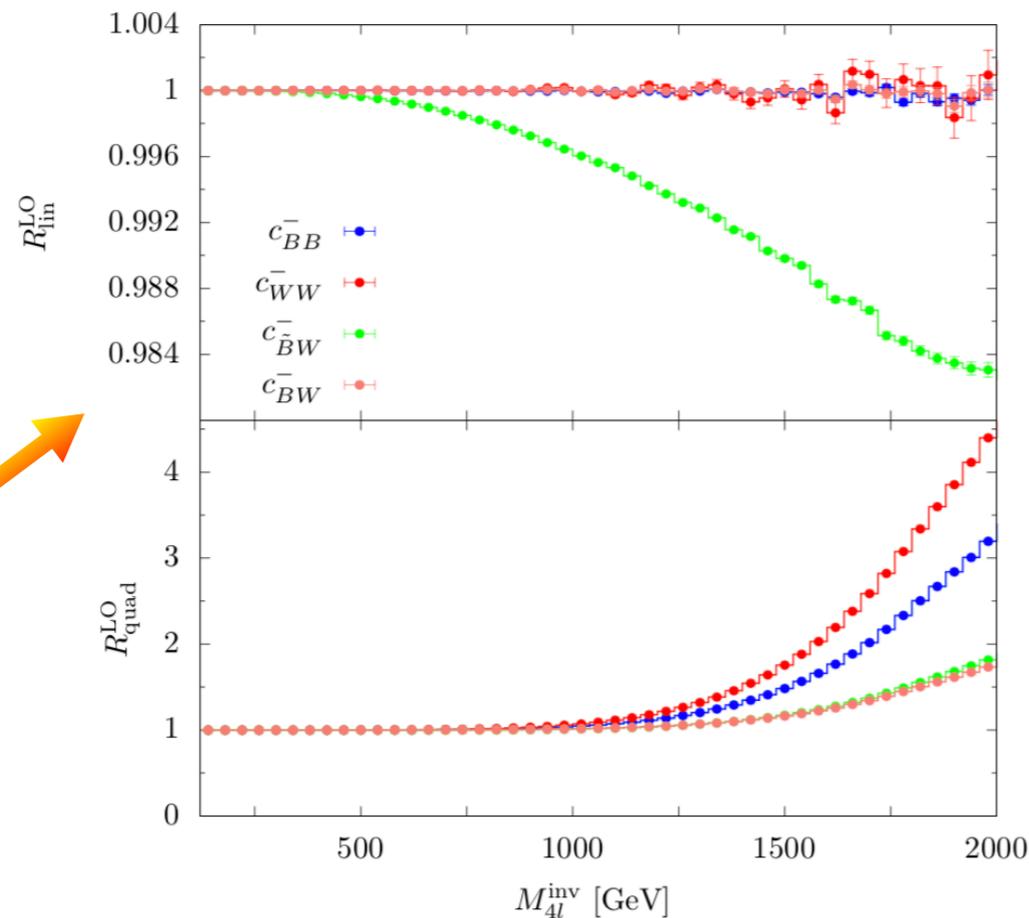
# EW corrections

When precision is concerned EW corrections should also be considered: automatic NLO (QCD+)EW generators now exist that can complement the progress on the NNLO side

Recola2 → **talk by Jean-Nicolas Lang**

Inclusion of Dimension 6 and Dimension 8 operators !  $pp \rightarrow e^+e^-\mu^+\mu^-$

**Relative impact of anomalous coupling in the linear and quadratic approximation**



# EW corrections

When precision is concerned EW corrections should also be considered: automatic NLO (QCD+)EW generators now exist that can complement the progress on the NNLO side

See also:

- Munich/Sherpa+Openloops S. Kallweit, J.M. Lindert, S. Pozzorini, M. Schönherr (2017)
- MadGraph5 aMC@NLO R. Frederix, S. Frixione, V. Hirschi, D. Pagani, H.-S. Shao, M. Zaro (2018)
- Gosam M.Chiesa, N.Greiner, F.Tramontano (2015)

# Summary & Outlook

- Vector boson pair production is an essential process at hadron colliders: it is a background for Higgs and new physics searches and it may provide first evidence of new physics signatures
- The computation of the two-loop helicity amplitudes made possible the exact fully exclusive NNLO calculations of  $ZZ$ ,  $WW$  and  $WZ$  including leptonic decays
- The NNLO parton level generator *MATRIX* implements all these calculations in a unique framework and includes all the vector-boson pair production processes
- The program combines the *MUNICH* Monte Carlo framework with amplitudes from *Openloops* and  $q_T$  subtraction and is able to compute inclusive and differential cross sections for vector boson pair production including off-shell and interference effects

# Summary & Outlook

- The impact of NNLO corrections is significant and generally depends on the applied cuts
- Other groups are working on diboson production at NNLO and produced results in the last period
- In the case of  $WW$  production the NNLO calculation has been matched to the Parton Shower with the NNLOPS method
- I have presented preliminary results for  $ZZ$  production with the inclusion of a class of  $N_3LO$  contributions originating from the NLO corrections to the loop-induced  $gg$  contribution
- When precision is concerned EW corrections should also be considered: automatic NLO QCD+EW generators now exist including also anomalous couplings



It would be great to have a single generator with all these features

Backup

# Stability of the subtraction procedure

$$d\sigma_{(N)NLO}^F = \mathcal{H}_{(N)NLO}^F \otimes d\sigma_{LO}^F + \left[ d\sigma_{(N)LO}^{F+jets} - d\sigma_{(N)LO}^{CT} \right]$$

The  $q_T$  subtraction counterterm is non-local  $\rightarrow$  the difference in the square bracket is evaluated with a cut-off  $r_{cut}$  on the ratio  $r = q_T/Q$

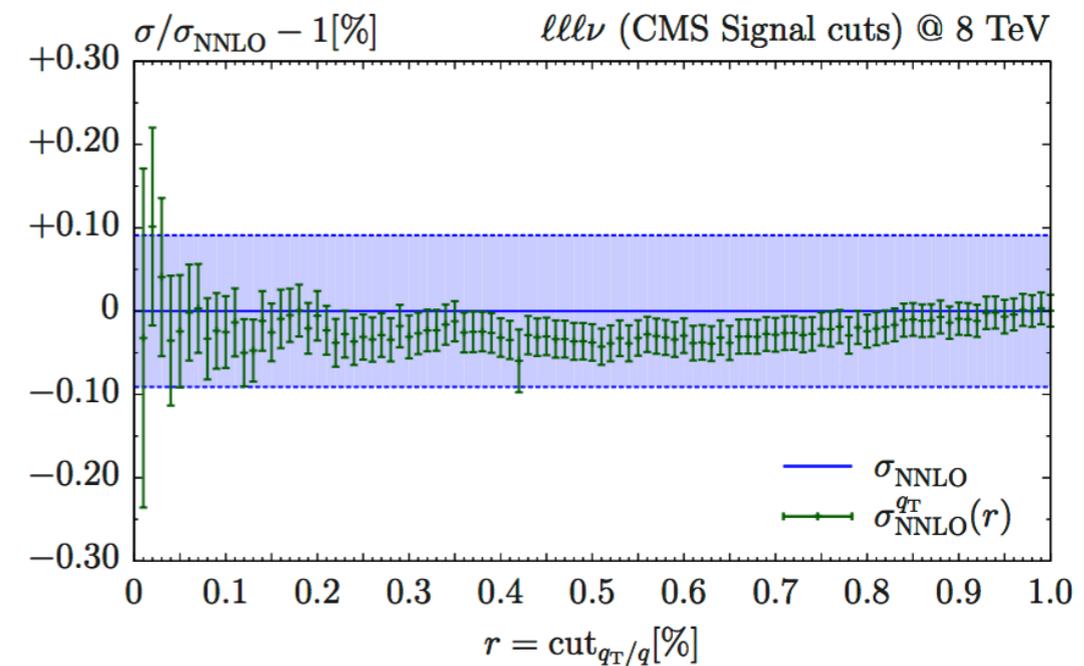
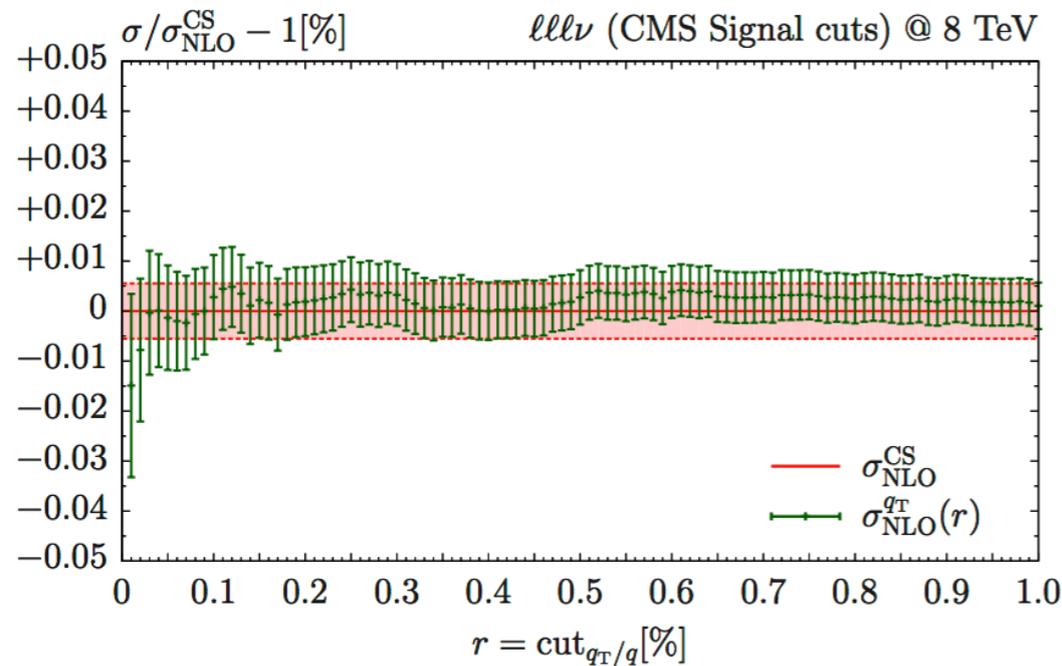
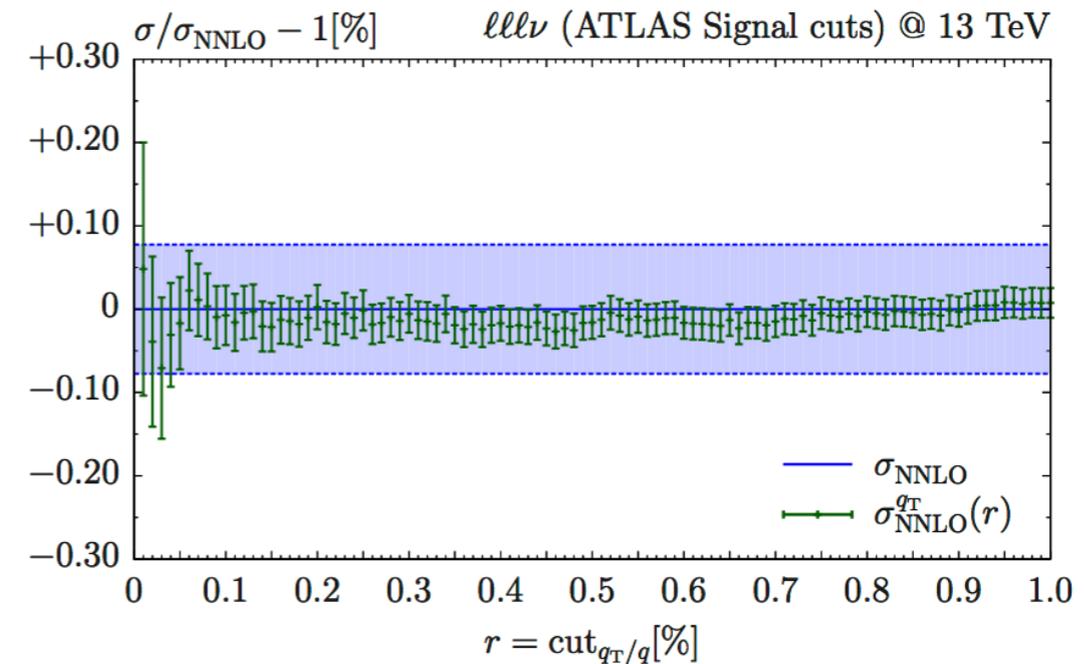
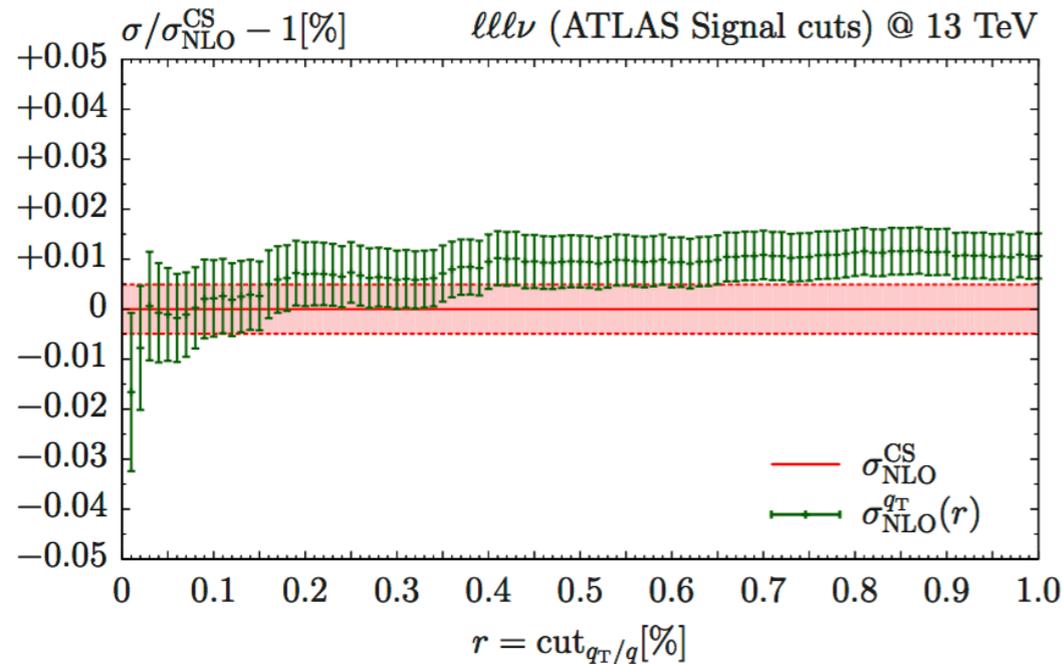
In our implementation  $q_T$  subtraction indeed works as a slicing method

It is important to monitor the dependence of our results on  $r_{cut}$

MATRIX allows for a simultaneous evaluation of the NNLO cross section for different values of  $r_{cut}$

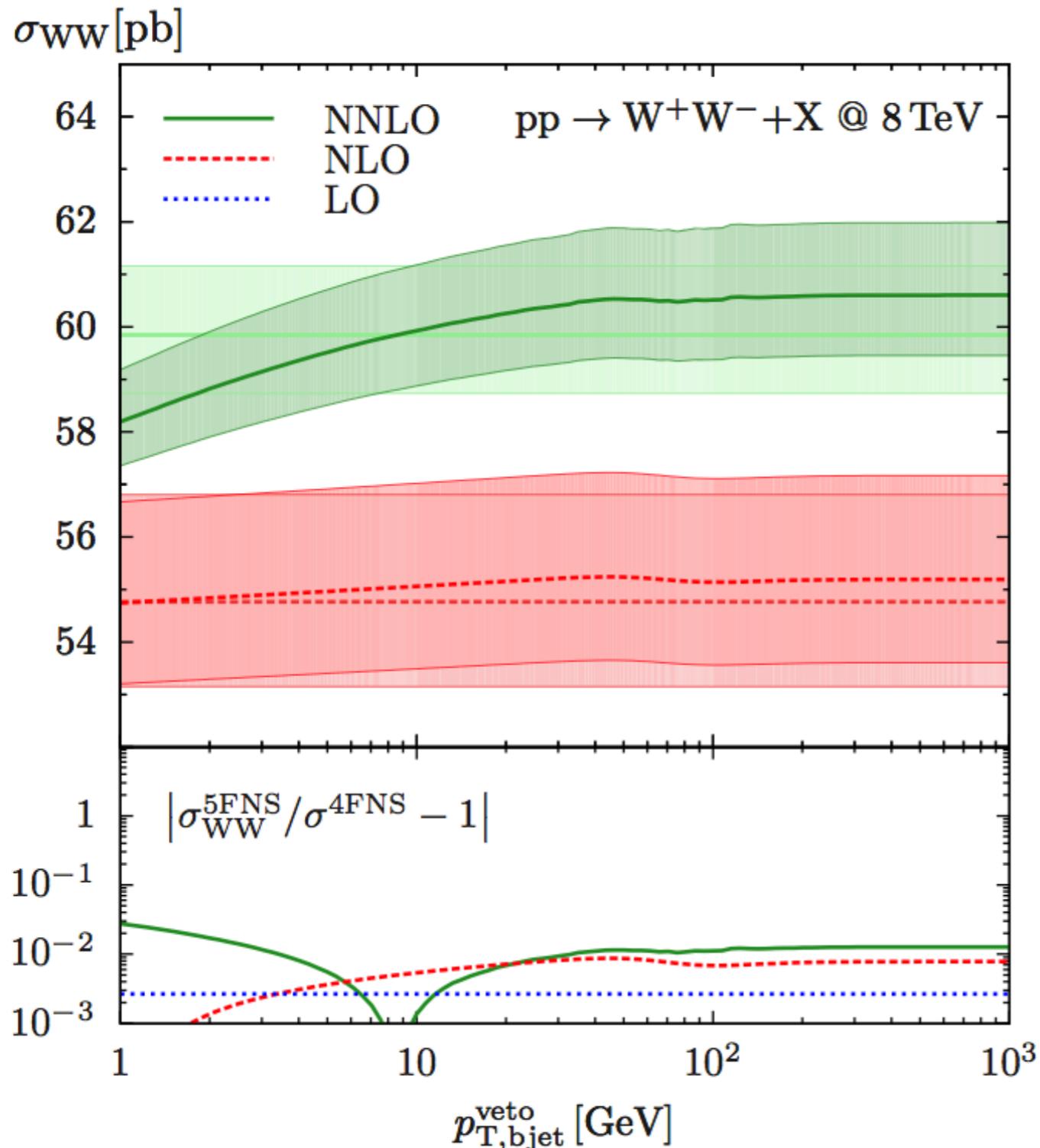
The dependence on  $r_{cut}$  is used by the code to provide an estimate of the systematic uncertainty in any NNLO run

# Stability of the subtraction procedure



For all processes we consider (except those involving photons) the NNLO uncertainties are typically at the 0.1% level or smaller

# The $WW$ cross section in the 5FNS



A better definition of the 5FNS cross section can be obtained by exploiting the different scaling behaviour with  $1/\Gamma_t$

Doubly (singly) resonant diagrams scale quadratically (linearly) with  $1/\Gamma_t$

A.Denner, S.Dittmaier, S.Kallweit, S.Pozzorini (2012)  
F.Cascioli, P.Maierhofer, S.Kallweit, S.Pozzorini (2013)

$t\bar{t}$  and  $Wt$  component subtracted by exploiting this different behaviour

As  $p_{T,bjet}^{veto} \rightarrow 0$  the logarithmic singularity is still present but for  $p_{T,bjet}^{veto} \gtrsim 10$  GeV the 5FNS result is approximately independent on the veto

➔ The agreement with the 4FNS result is at the 1(2)% level for 8(14) TeV

# $pp \rightarrow V\gamma + X$ at NNLO

S.Kallweit, D.Rathlev, A.Torre, MG (2013)

S.Kallweit, D.Rathlev, MG (2015)

We present results of a complete calculation of  $pp \rightarrow V\gamma + X$  up to NNLO

We compute NNLO corrections to  $pp \rightarrow l+l^- \gamma + X$  and  $pp \rightarrow lv\gamma + X$  by consistently including the final state photon radiation from the leptons and the non resonant diagrams

The calculation allows us to apply arbitrary kinematical cuts on the final state lepton(s), the photon and the QCD radiation

→ We can compute fiducial cross sections and distributions !

We consider pp collisions at 7 TeV and we use MMHT2014 PDFs with  $\alpha_s$  evaluated at each corresponding order

We set the central values of the scales to  $\mu_0 = \sqrt{m_V^2 + (p_T^\gamma)^2}$

Scale uncertainties computed by varying  $\mu_F$  and  $\mu_R$  simultaneously and independently with  $1/2 \mu_0 < \mu_F, \mu_R < 2 \mu_0$  with no constraint on their ratio

# $pp \rightarrow Z\gamma + X$ at NNLO

S.Kallweit, D.Rathlev, MG (2015)

see also J.Campbell, T.Neumann, C.Williams (2017)

ATLAS cuts (arXiv:1302.1283)

photon isolation:  $\epsilon = 0.5$   
smooth cone  $R = 0.4$

$p_T^\gamma > 15$  GeV     $p_T^l > 25$  GeV     $\Delta R(l, \gamma) > 0.3$

$|\eta^\gamma| < 2.37$      $|\eta^l| < 2.47$      $\Delta R(l, \gamma) > 0.7$

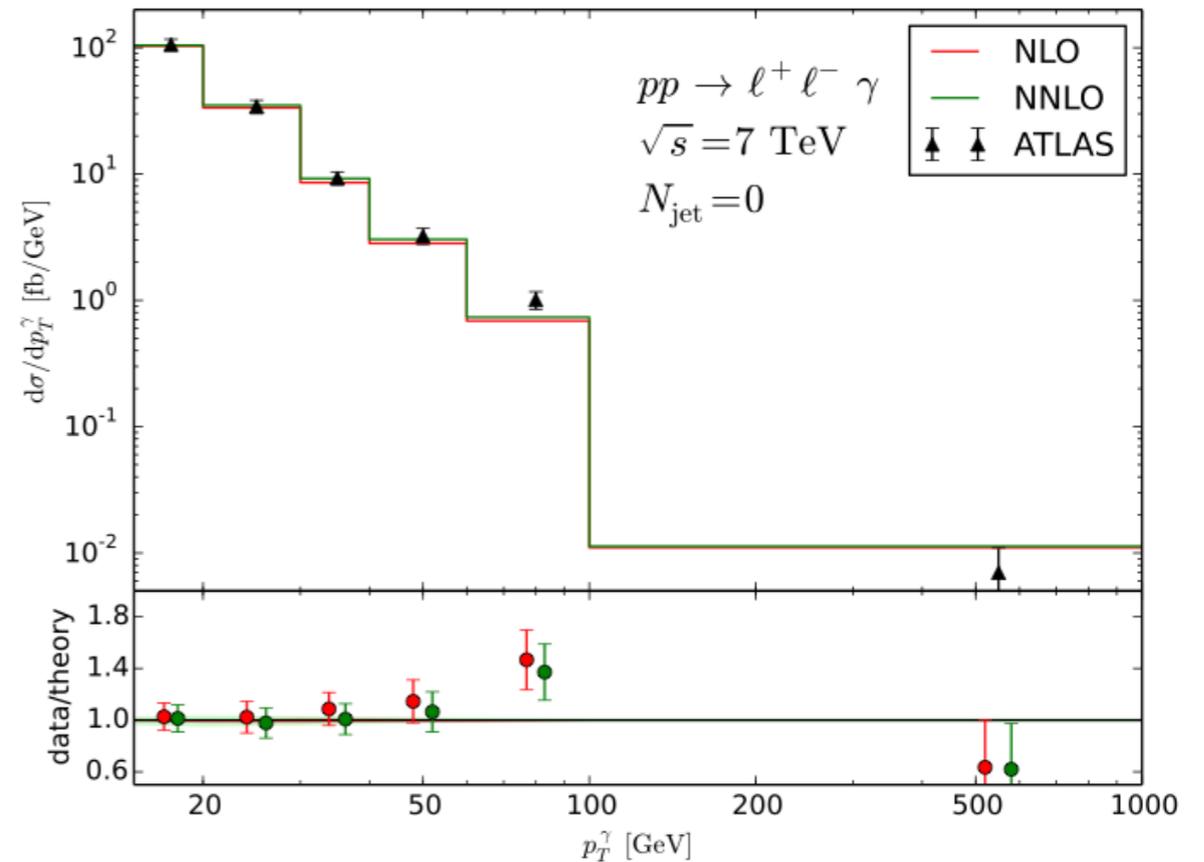
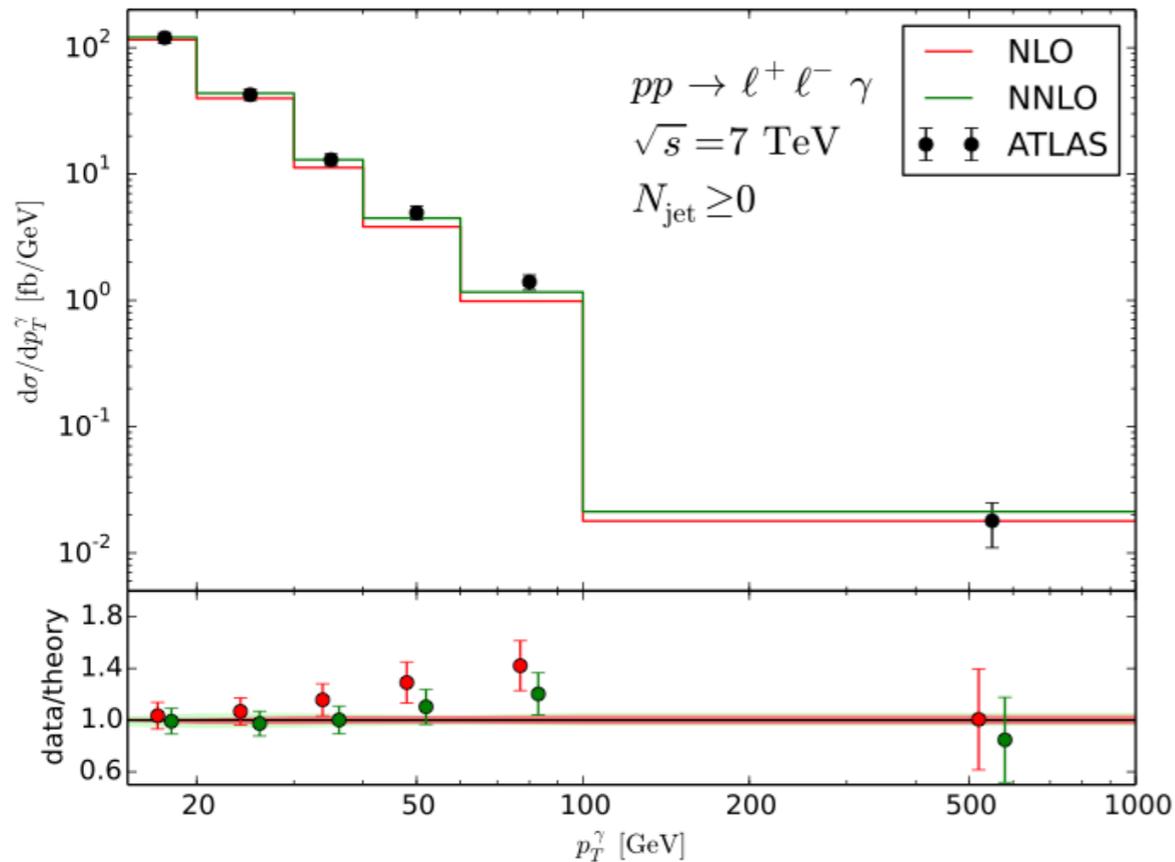
$m_{ll} > 40$  GeV    jets: anti-kt with  $D=0.4$   
 $p_T^{\text{jet}} > 15$  GeV     $|\eta^{\text{jet}}| < 2.47$

$N_{\text{jet}} \geq 0$

$N_{\text{jet}} = 0$

$\sigma_{\text{NLO}}$ [pb]	$\sigma_{\text{NNLO}}$ [pb]	$\sigma_{\text{ATLAS}}$ [pb]
$1.222^{+4.2\%}_{-5.3\%}$	$1.320^{+1.3\%}_{-2.3\%}$	$1.31 \pm 0.02$ (stat) $\pm 0.11$ (syst) $\pm 0.05$ (lumi)
$1.031^{+2.7\%}_{-4.3\%}$	$1.059^{+0.7\%}_{-1.4\%}$	$1.05 \pm 0.02$ (stat) $\pm 0.10$ (syst) $\pm 0.04$ (lumi)

+8%



# pp → Wγ at NNLO

S.Kallweit, D.Rathlev, MG (2015)

ATLAS cuts (arXiv:1302.1283)

photon isolation:  $\epsilon = 0.5$   
smooth cone  $R = 0.4$

$p_T^\gamma > 15 \text{ GeV}$     $p_T^l > 25 \text{ GeV}$     $\Delta R(l, \gamma) > 0.3$

$|\eta^\gamma| < 2.37$     $|\eta^l| < 2.47$     $\Delta R(l, \gamma) > 0.7$

$p_T^{\text{miss}} > 35 \text{ GeV}$    jets: anti-kt with  $D=0.4$

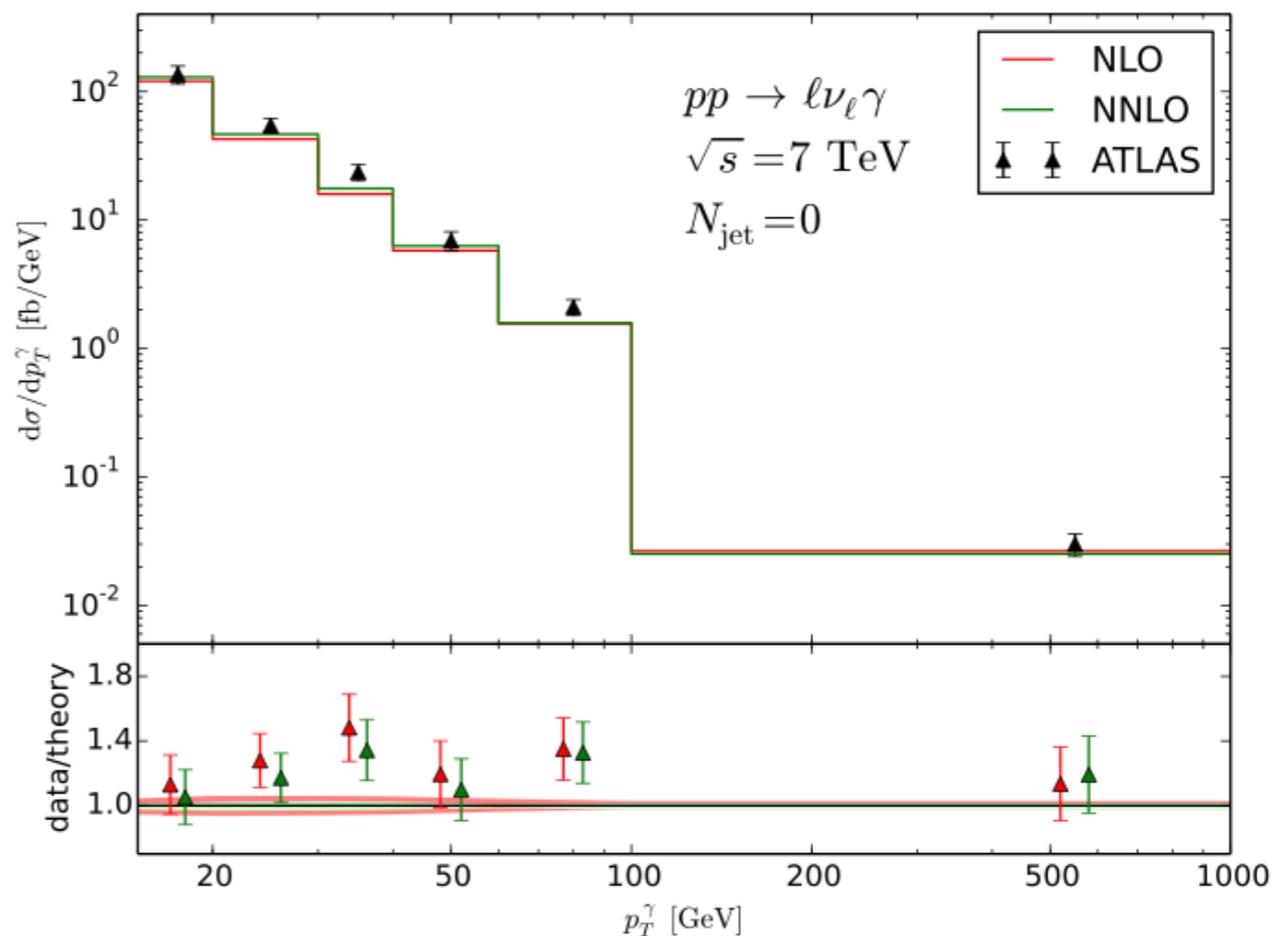
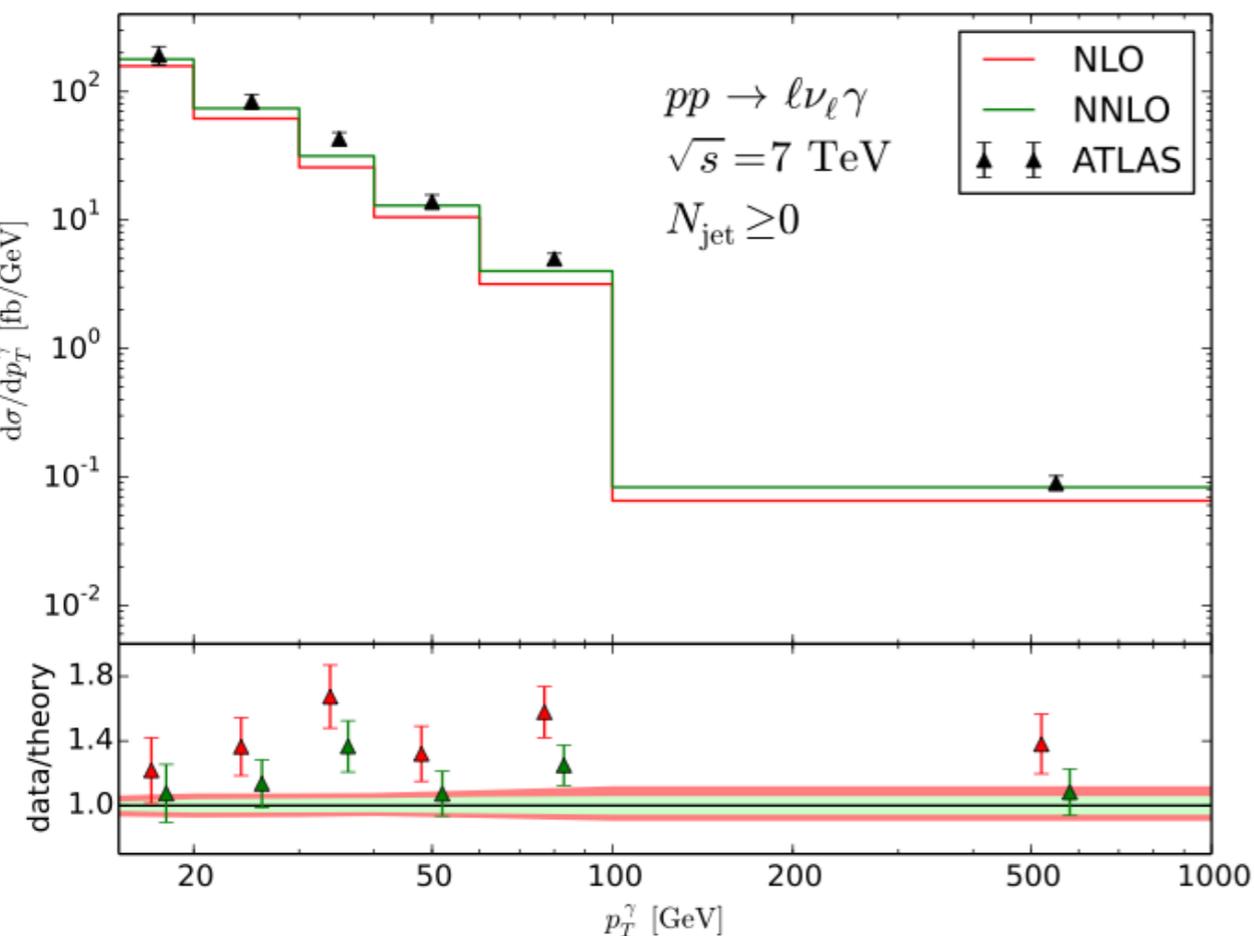
$p_T^{\text{jet}} > 15 \text{ GeV}$     $|\eta^{\text{jet}}| < 2.47$

$N_{\text{jet}} \geq 0$

$N_{\text{jet}} = 0$

+19%

$\sigma_{\text{NLO}}$ [pb]	$\sigma_{\text{NNLO}}$ [pb]	$\sigma_{\text{ATLAS}}$ [pb]
$2.058^{+6.8\%}_{-6.8\%}$	$2.453^{+4.1\%}_{-4.1\%}$	$2.77 \pm 0.03 \text{ (stat)}$ $\pm 0.33 \text{ (syst)}$ $\pm 0.14 \text{ (lumi)}$
$1.395^{+5.2\%}_{-5.8\%}$	$1.493^{+1.7\%}_{-2.7\%}$	$1.76 \pm 0.03 \text{ (stat)}$ $\pm 0.21 \text{ (syst)}$ $\pm 0.08 \text{ (lumi)}$



# WZ: fully differential

S. Kallweit, D. Rathlev, M. Wiesemann, MG (2017)

Setup: NNPDF3.0

central scale choice:  $\mu_F = \mu_R = 1/2 (m_Z + m_W)$

$pp \rightarrow l' \nu_{l'} l l'$

ATLAS fiducial region: requires identification of the leptons coming from the W and the Z boson (non trivial in the case of identical flavours)

Pair with highest P is assigned to the Z boson

$$P = \left| \frac{1}{m_{\ell\ell}^2 - m_Z^2 + i\Gamma_Z m_Z} \right|^2 \cdot \left| \frac{1}{m_{\ell'\nu_{\ell'}}^2 - m_W^2 + i\Gamma_W m_W} \right|^2$$

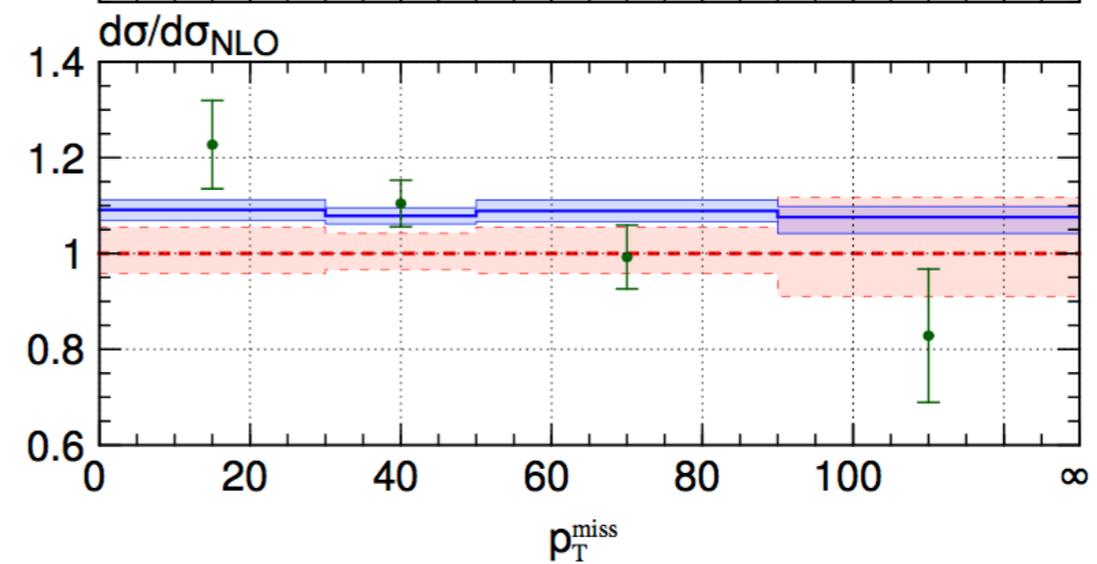
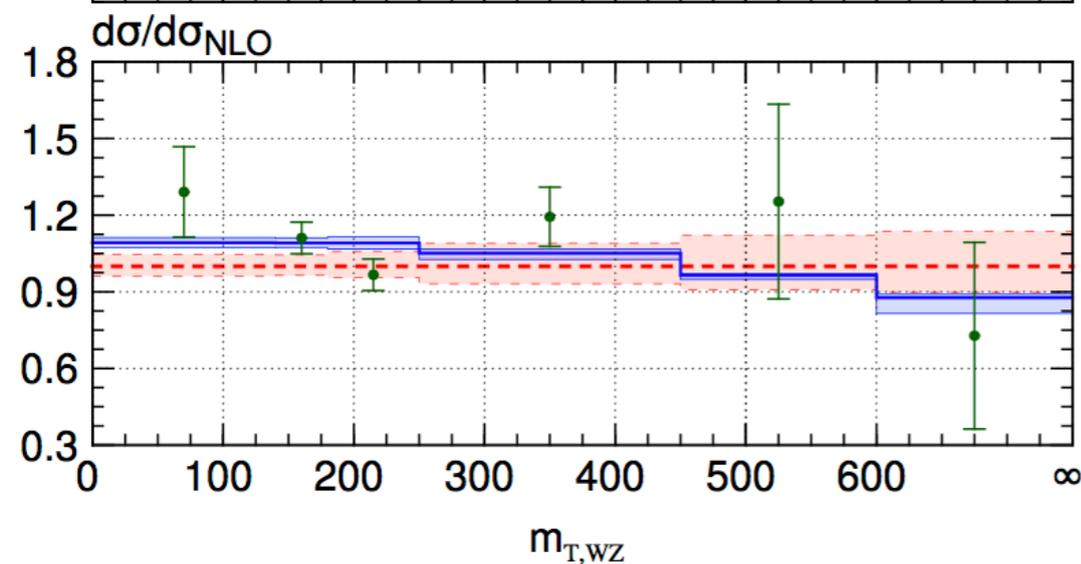
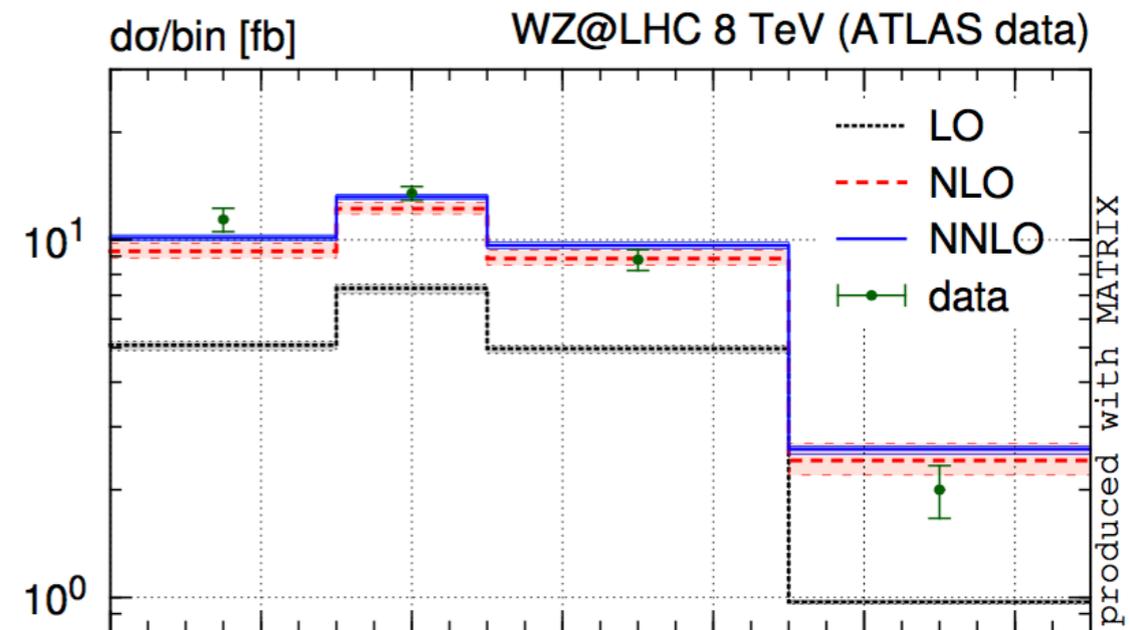
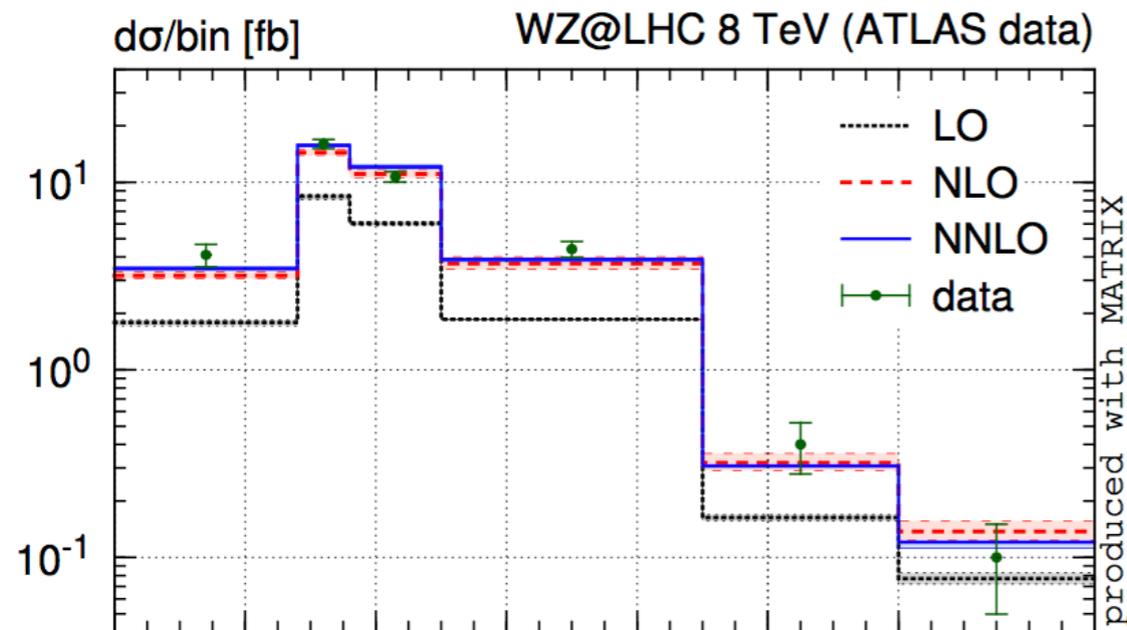
Fiducial cuts:

$$p_{T1} > 15 \text{ GeV} \quad |\eta_1| < 2.5 \quad p_{T1'} > 20 \text{ GeV} \quad |\eta_{1'}| < 2.5$$

$$|m_{11} - m_Z| < 10 \text{ GeV} \quad m_{TW} > 30 \text{ GeV} \quad \Delta R_{11} > 0.2 \quad \Delta R_{11'} > 0.3$$

# WZ: fully differential

S. Kallweit, D. Rathlev, M. Wiesemann, MG (2017)



- NNLO effects on the relevant distributions improve the agreement with ATLAS data mostly due to the improved normalisation
- Slightly different shape for  $p_{T\text{miss}}$  distribution which is driven by W-Z

# WZ: fully differential: NP searches

S. Kallweit, D. Rathlev, M. Wiesemann, MG (2017)

Three lepton+MET signature relevant for many NP searches

We follow the CMS analysis of CMS-PAS-SUS-16 024

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definition of the selection cuts for  $pp \rightarrow \ell'^{\pm} \nu_{\ell'} \ell^+ \ell^- + X$ ,  $\ell, \ell' \in \{e, \mu\}$

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Selection cuts:

$p_{T,\ell_1} > 25(20) \text{ GeV}$  if  $\ell_1 = e(\mu)$ ,  $p_{T,\ell_1} > 25 \text{ GeV}$  if  $\ell_1 = \mu$  and  $\ell_{\geq 2} \neq \mu$

$p_{T,\ell_{\geq 2}} > 15(10) \text{ GeV}$  if  $\ell_{\geq 2} = e(\mu)$ ,  $|\eta_e| < 2.5$ ,  $|\eta_{\mu}| < 2.4$ ,

$|m_{3\ell} - m_Z| > 15 \text{ GeV}$ ,  $m_{\ell^+\ell^-} > 12 \text{ GeV}$

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Four categories are considered:

Category I: no additional cut

Category II:  $p_T^{\text{miss}} > 200 \text{ GeV}$

Category III:  $m_{T,W} > 120 \text{ GeV}$

Category IV:  $m_{ll} > 105 \text{ GeV}$

Dynamic scale more appropriate here

$$\mu_R = \mu_F = \mu_0 \equiv \frac{1}{2} \left( \sqrt{m_Z^2 + p_{T,\ell_z \ell_z}^2} + \sqrt{m_W^2 + p_{T,\ell_w \nu_{\ell_w}}^2} \right)$$

# WZ: fully differential: NP searches

channel	$\sigma_{\text{LO}}$ [fb]	$\sigma_{\text{NLO}}$ [fb]	$\sigma_{\text{NNLO}}$ [fb]	$\sigma_{\text{NLO}}/\sigma_{\text{LO}} - 1$	$\sigma_{\text{NNLO}}/\sigma_{\text{NLO}} - 1$
Category I					
$\ell'^+\ell^+\ell^-$	49.45(0) <sup>+4.9%</sup> <sub>-5.8%</sub>	94.12(2) <sup>+4.8%</sup> <sub>-3.9%</sub>	105.9(1) <sup>+2.3%</sup> <sub>-2.2%</sub>	90.3%	12.6%
$\ell^+\ell^+\ell^-$	48.97(0) <sup>+4.8%</sup> <sub>-5.8%</sub>	93.13(2) <sup>+4.8%</sup> <sub>-3.9%</sub>	104.7(1) <sup>+2.2%</sup> <sub>-2.1%</sub>	90.2%	12.4%
$\ell'^-\ell^+\ell^-$	32.04(0) <sup>+5.3%</sup> <sub>-6.3%</sub>	63.68(3) <sup>+5.0%</sup> <sub>-4.1%</sub>	71.89(4) <sup>+2.3%</sup> <sub>-2.2%</sub>	98.7%	12.9%
$\ell^-\ell^+\ell^-$	31.74(0) <sup>+5.3%</sup> <sub>-6.3%</sub>	63.00(2) <sup>+5.0%</sup> <sub>-4.1%</sub>	71.13(4) <sup>+2.2%</sup> <sub>-2.2%</sub>	98.5%	12.9%
combined	162.2(0) <sup>+5.0%</sup> <sub>-6.0%</sub>	313.9(1) <sup>+4.9%</sup> <sub>-4.0%</sub>	353.7(3) <sup>+2.2%</sup> <sub>-2.2%</sub>	93.5%	12.7%
Category II					
$\ell'^+\ell^+\ell^-$	0.3482(0) <sup>+2.8%</sup> <sub>-2.8%</sub>	1.456(0) <sup>+13%</sup> <sub>-11%</sub>	1.799(1) <sup>+5.2%</sup> <sub>-5.4%</sub>	318%	23.6%
$\ell^+\ell^+\ell^-$	0.3486(0) <sup>+2.8%</sup> <sub>-2.8%</sub>	1.452(0) <sup>+13%</sup> <sub>-11%</sub>	1.789(1) <sup>+5.1%</sup> <sub>-5.4%</sub>	316%	23.2%
$\ell'^-\ell^+\ell^-$	0.1644(0) <sup>+2.6%</sup> <sub>-2.7%</sub>	0.5546(1) <sup>+12%</sup> <sub>-9.9%</sub>	0.6631(4) <sup>+4.3%</sup> <sub>-4.8%</sub>	237%	19.6%
$\ell^-\ell^+\ell^-$	0.1645(0) <sup>+2.6%</sup> <sub>-2.7%</sub>	0.5535(1) <sup>+12%</sup> <sub>-9.9%</sub>	0.6600(3) <sup>+4.2%</sup> <sub>-4.7%</sub>	237%	19.2%
combined	1.026(0) <sup>+2.7%</sup> <sub>-2.8%</sub>	4.015(1) <sup>+13%</sup> <sub>-10%</sub>	4.911(3) <sup>+4.9%</sup> <sub>-5.2%</sub>	292%	22.3%
Category III					
$\ell'^+\ell^+\ell^-$	0.3642(0) <sup>+1.5%</sup> <sub>-2.2%</sub>	0.5909(1) <sup>+4.3%</sup> <sub>-3.3%</sub>	0.6373(16) <sup>+1.6%</sup> <sub>-1.6%</sub>	62.3%	7.86%
$\ell^+\ell^+\ell^-$	1.090(0) <sup>+1.7%</sup> <sub>-2.4%</sub>	1.904(0) <sup>+4.8%</sup> <sub>-3.8%</sub>	2.071(2) <sup>+1.9%</sup> <sub>-1.9%</sub>	74.7%	8.79%
$\ell'^-\ell^+\ell^-$	0.2055(0) <sup>+2.0%</sup> <sub>-2.8%</sub>	0.3447(1) <sup>+4.5%</sup> <sub>-3.4%</sub>	0.3731(9) <sup>+1.6%</sup> <sub>-1.7%</sub>	67.8%	8.22%
$\ell^-\ell^+\ell^-$	0.6463(1) <sup>+2.1%</sup> <sub>-2.9%</sub>	1.136(0) <sup>+4.8%</sup> <sub>-3.7%</sub>	1.232(1) <sup>+1.7%</sup> <sub>-1.7%</sub>	75.8%	8.42%
combined	2.306(0) <sup>+1.8%</sup> <sub>-2.5%</sub>	3.976(1) <sup>+4.7%</sup> <sub>-3.7%</sub>	4.313(6) <sup>+1.8%</sup> <sub>-1.8%</sub>	72.4%	8.50%
Category IV					
$\ell'^+\ell^+\ell^-$	2.500(0) <sup>+3.1%</sup> <sub>-3.9%</sub>	4.299(1) <sup>+4.1%</sup> <sub>-3.4%</sub>	4.682(2) <sup>+1.7%</sup> <sub>-1.6%</sub>	72.0%	8.92%
$\ell^+\ell^+\ell^-$	2.063(0) <sup>+3.4%</sup> <sub>-4.2%</sub>	3.740(1) <sup>+4.5%</sup> <sub>-3.6%</sub>	4.160(2) <sup>+2.2%</sup> <sub>-2.0%</sub>	81.3%	11.2%
$\ell'^-\ell^+\ell^-$	1.603(0) <sup>+3.4%</sup> <sub>-4.4%</sub>	2.805(1) <sup>+4.2%</sup> <sub>-3.5%</sub>	3.058(1) <sup>+1.7%</sup> <sub>-1.6%</sub>	75.0%	9.01%
$\ell^-\ell^+\ell^-$	1.373(0) <sup>+3.8%</sup> <sub>-4.7%</sub>	2.591(1) <sup>+4.7%</sup> <sub>-3.9%</sub>	2.904(1) <sup>+2.2%</sup> <sub>-2.1%</sub>	88.7%	12.1%
combined	7.540(1) <sup>+3.4%</sup> <sub>-4.2%</sub>	13.44(0) <sup>+4.4%</sup> <sub>-3.6%</sub>	14.80(1) <sup>+1.9%</sup> <sub>-1.8%</sub>	78.2%	10.2%

Very large corrections especially in Category II where NNLO effects can reach O(20%)

Different impact of radiative corrections on  $W^+Z$  and  $W^-Z$  due to the different partonic channels that contribute at LO