

THEORY OF THE SCATTERING CROSS SECTION

for DM direct detection

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based on work with F. Bishara, J. Brod, B. Grinstein, JZ, 1611.00368, 1707.06998;1707.06998;+
J. Brod, A. Gootjes-Dreesbach, M. Tamaro, JZ, 1710.10218
J. Brod, E. Stamou, JZ, 1801.04240

Dark Matter at the Dawn of Discovery?, Heidelberg, Apr 14 2018

MOTIVATION

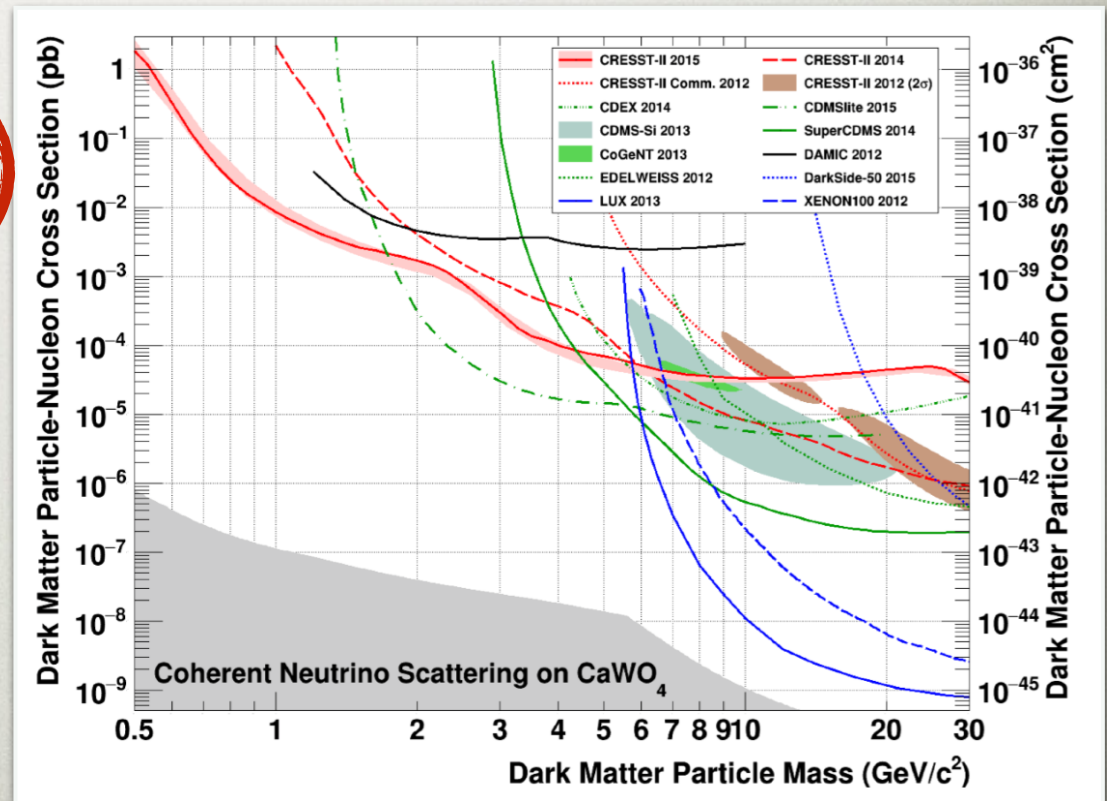
- DM candidate at EW scale in many solutions to the hierarchy problem
 - the dominant interactions with the SM may be unconventional
- can parametrize our ignorance by using EFT for DM interactions

MOTIVATION

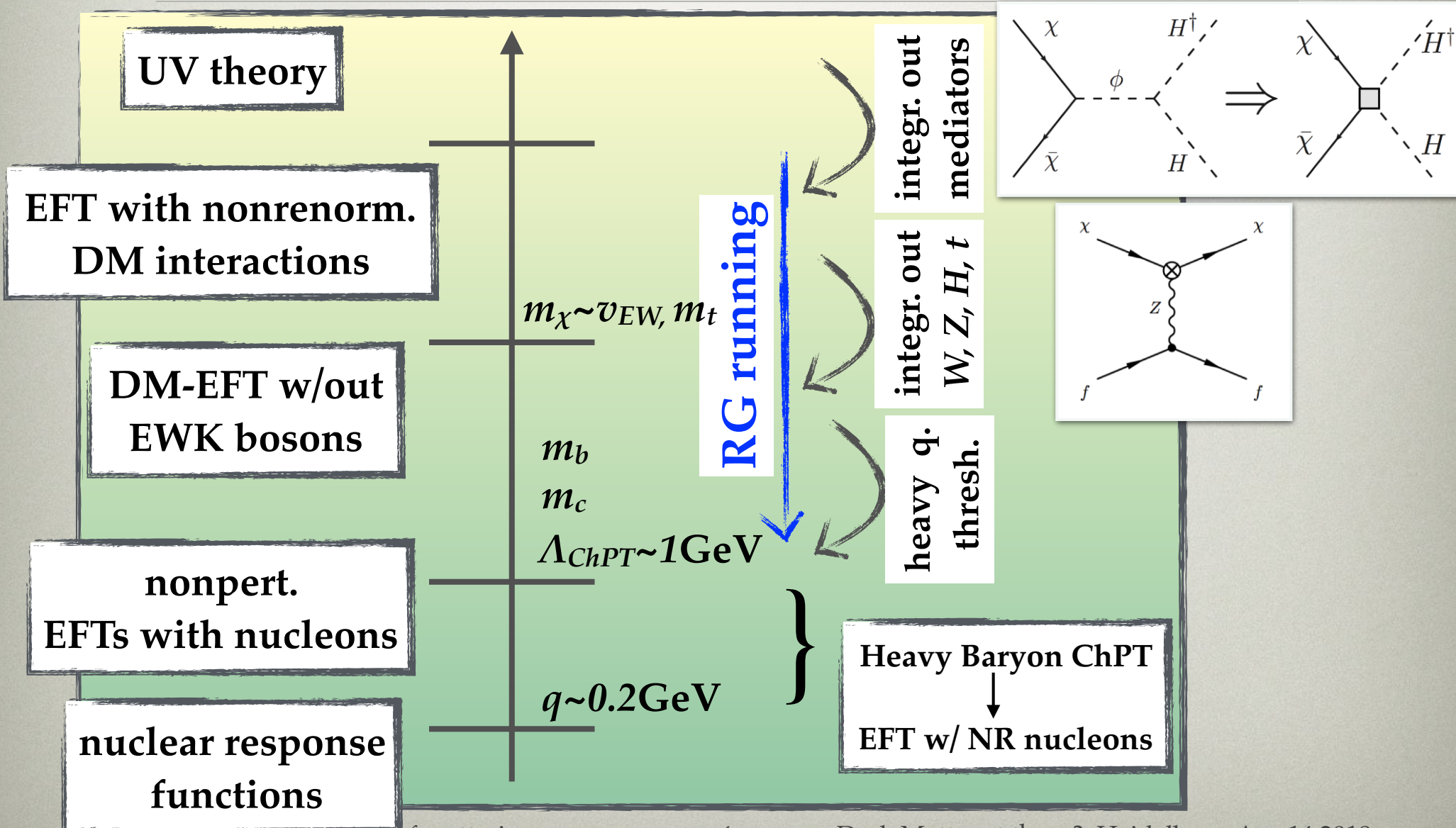
- two immediate questions if signal of DM

- comparing different DM direct detection experiments

- comparing direct detection with LHC and indirect detection



TOWER OF EFTs



EFT EXPANSION

- at which mass dimension to stop?

$$\mathcal{L}_{\text{EW}} = \sum_{a,d} \frac{C_a^{(d)}}{\Lambda^{d-4}} Q_a^{(d)}$$

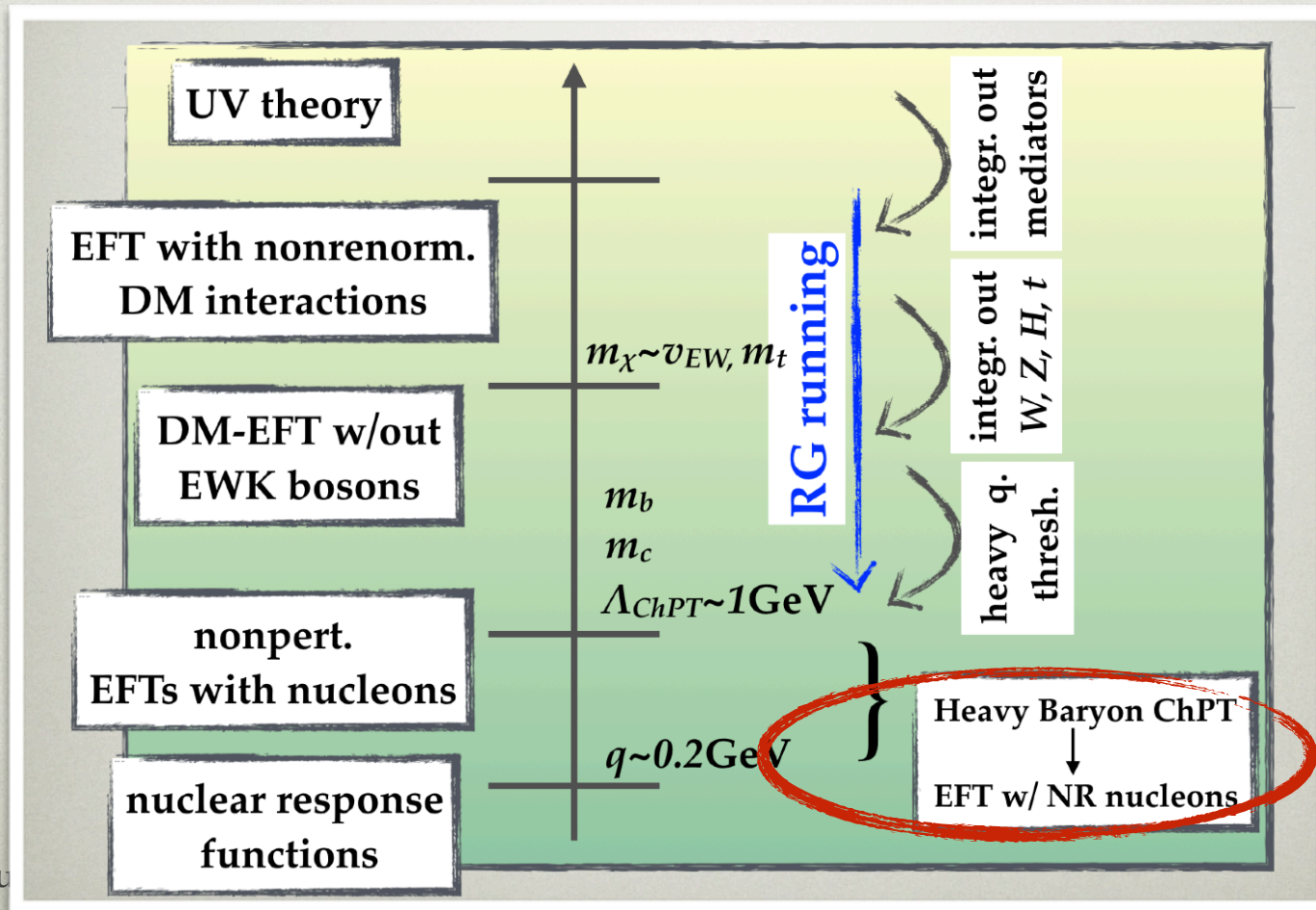
- at dimension 7 all chiral / Lorentz structures without derivatives
 - probably captures leading behaviour in most theories of DM
- already a large set of operators
 - above EW, if Dirac fermion DM in general EW multiplet
 - 8 dim-5 ops., 18 dim-6 ops., 100 dim-7 ops.
 - this not counting flavor multiplicities
 - at $\mu_{str} \sim 2$ GeV smaller set
 - 2 dim-5 ops., 4 dim-6 ops., 22 dim-7 ops.

AIM

- the aim is to be able to
 - take any DM EFT up to dim 7 above EW scale
J. Brod, A. Gootjes-Dreesbach, M. Tamaro, JZ, 1710.10218
 - consistently give the leading expression for cross section
 - includes renormalization group running
 - consistent counting, including ChPT
F. Bishara, J. Brod, B. Grinstein, JZ, 1611.00368, 1707.06998
- part of this already available in a **Mathematica** & **Python** package **DirectDM** F. Bishara, J. Brod, B. Grinstein, JZ, 1708.02678

GOAL FOR TODAY

- matching at $\mu_{str} \sim 2 \text{ GeV}$ from relativistic theory to nuclear physics



$$\mathcal{Q}_1^{(5)} = \frac{e}{8\pi^2} (\bar{\chi} \sigma^{\mu\nu} \chi) F_{\mu\nu},$$

$$\mathcal{Q}_{1,q}^{(6)} = (\bar{\chi} \gamma_\mu \chi) (\bar{q} \gamma^\mu q),$$

$$\mathcal{Q}_{3,q}^{(6)} = (\bar{\chi} \gamma_\mu \chi) (\bar{q} \gamma^\mu \gamma_5 q),$$

$$\mathcal{Q}_1^{(7)} = \frac{\alpha_s}{12\pi} (\bar{\chi} \chi) G^{a\mu\nu} G_{\mu\nu}^a,$$

$$\mathcal{Q}_3^{(7)} = \frac{\alpha_s}{8\pi} (\bar{\chi} \chi) G^{a\mu\nu} \tilde{G}_{\mu\nu}^a,$$

$$\mathcal{Q}_{5,q}^{(7)} = m_q (\bar{\chi} \chi) (\bar{q} q),$$

$$\mathcal{Q}_{7,q}^{(7)} = m_q (\bar{\chi} \chi) (\bar{q} i \gamma_5 q),$$

$$\mathcal{Q}_2^{(5)} = \frac{e}{8\pi^2} (\bar{\chi} \sigma^{\mu\nu} i \gamma_5 \chi) F_{\mu\nu}$$

$$\mathcal{Q}_{2,q}^{(6)} = (\bar{\chi} \gamma_\mu \gamma_5 \chi) (\bar{q} \gamma^\mu q),$$

$$\mathcal{Q}_{4,q}^{(6)} = (\bar{\chi} \gamma_\mu \gamma_5 \chi) (\bar{q} \gamma^\mu \gamma_5 q),$$

$$\mathcal{Q}_2^{(7)} = \frac{\alpha_s}{12\pi} (\bar{\chi} i \gamma_5 \chi) G^{a\mu\nu} G_{\mu\nu}^a,$$

$$\mathcal{Q}_4^{(7)} = \frac{\alpha_s}{8\pi} (\bar{\chi} i \gamma_5 \chi) G^{a\mu\nu} \tilde{G}_{\mu\nu}^a,$$

$$\mathcal{Q}_{6,q}^{(7)} = m_q (\bar{\chi} i \gamma_5 \chi) (\bar{q} q),$$

$$\mathcal{Q}_{8,q}^{(7)} = m_q (\bar{\chi} \gamma_5 \chi) (\bar{q} \gamma_5 q).$$

relativistic
theory with
quarks and gluons

?

non-relativistic
theory with
nucleons

J. Zupan Theory of s

$$\mathcal{O}_1^N = \mathbb{1}_\chi \mathbb{1}_N,$$

$$\mathcal{O}_3^N = \mathbb{1}_\chi \vec{S}_N \cdot \left(\vec{v}_\perp \times \frac{i\vec{q}}{m_N} \right),$$

$$\mathcal{O}_5^N = \vec{S}_\chi \cdot \left(\vec{v}_\perp \times \frac{i\vec{q}}{m_N} \right) \mathbb{1}_N,$$

$$\mathcal{O}_7^N = \mathbb{1}_\chi (\vec{S}_N \cdot \vec{v}_\perp),$$

$$\mathcal{O}_9^N = \vec{S}_\chi \cdot \left(\frac{i\vec{q}}{m_N} \times \vec{S}_N \right),$$

$$\mathcal{O}_{11}^N = - \left(\vec{S}_\chi \cdot \frac{i\vec{q}}{m_N} \right) \mathbb{1}_N,$$

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$$\mathcal{O}_{10}^N = - \mathbb{1}_\chi \left(\vec{S}_N \cdot \frac{i\vec{q}}{m_N} \right),$$

$$\mathcal{O}_{12}^N = \vec{S}_\chi \cdot \left(\vec{S}_N \times \vec{v}_\perp \right),$$

DIRECT DM DETECTION

KINEMATICS

- WIMPS form DM halo
 - typical velocity $v \sim 10^{-3}$
- scatters on target nuclei $\chi N \rightarrow \chi N$
 - typical energy deposit

$$E_d = 2 \frac{\mu_\chi^2}{M_A} v^2 \sim 2 \text{keV} \left(\frac{120 \text{GeV}}{M_A} \right) \left(\frac{\mu_\chi}{10 \text{GeV}} \right)^2 \left(\frac{v}{10^{-3}} \right)^2$$

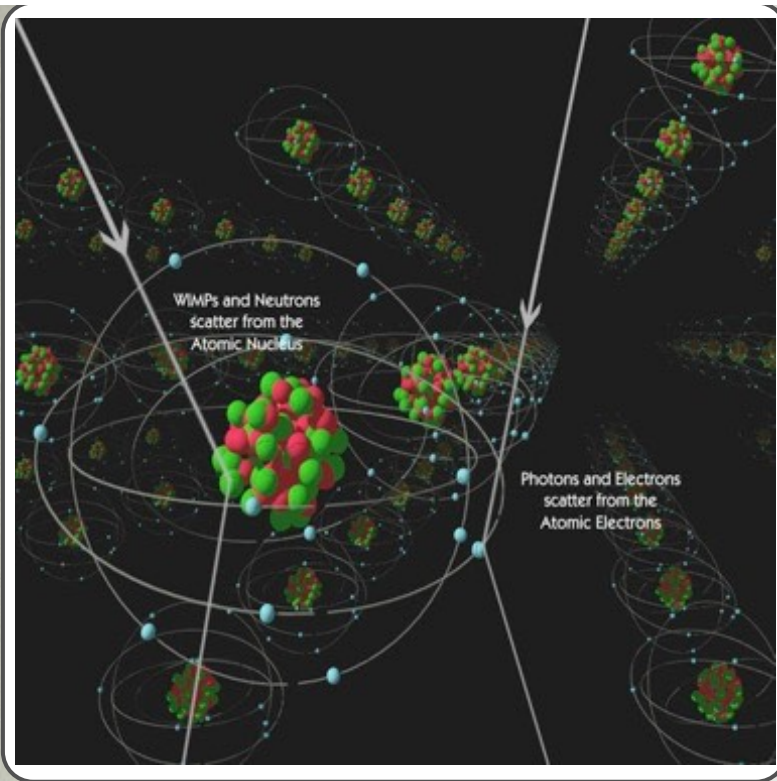
- typical momentum exchange

$$q_{\text{max}} \sim 200 \text{ MeV.}$$

- this allows for treatment with ChPT, expansion in q/Λ_{ChEFT}



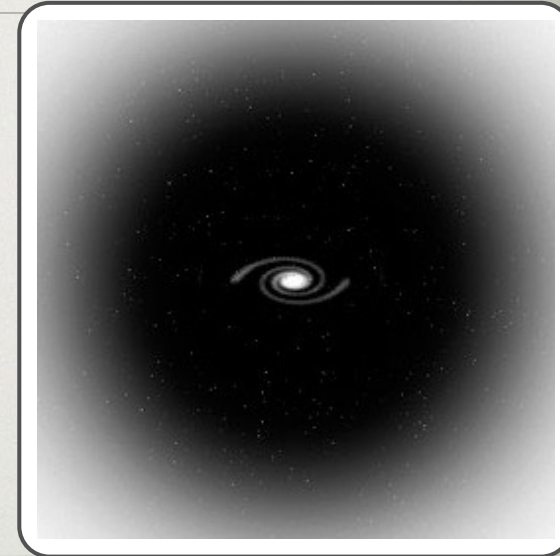
DM DETECTION DYNAMICS



DM halo

$$v \sim 10^{-3}$$

$$\chi N \rightarrow \chi N$$



- typical energy deposit

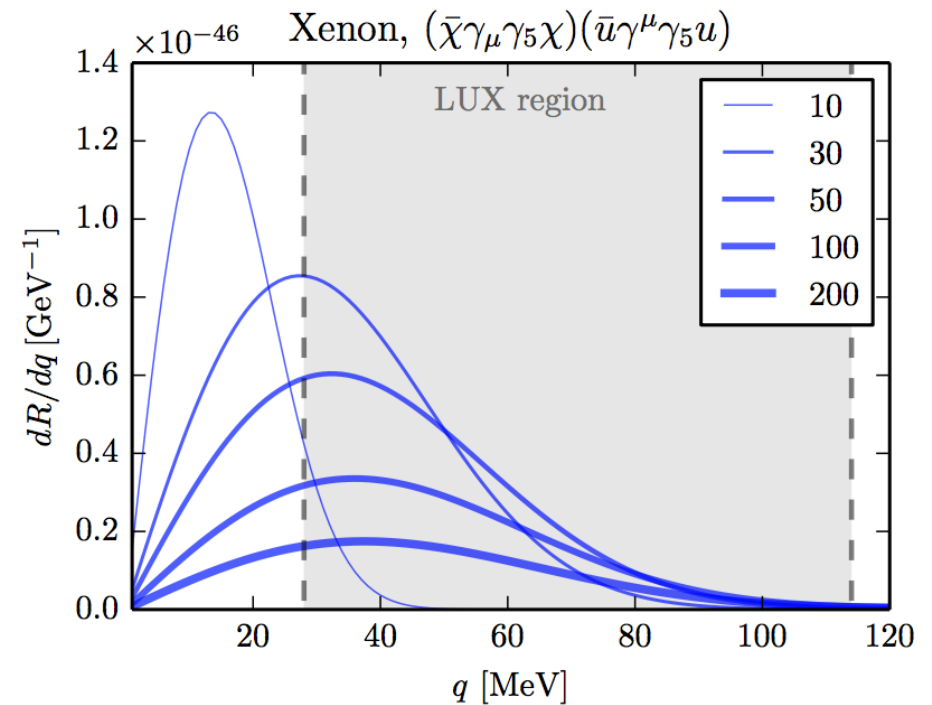
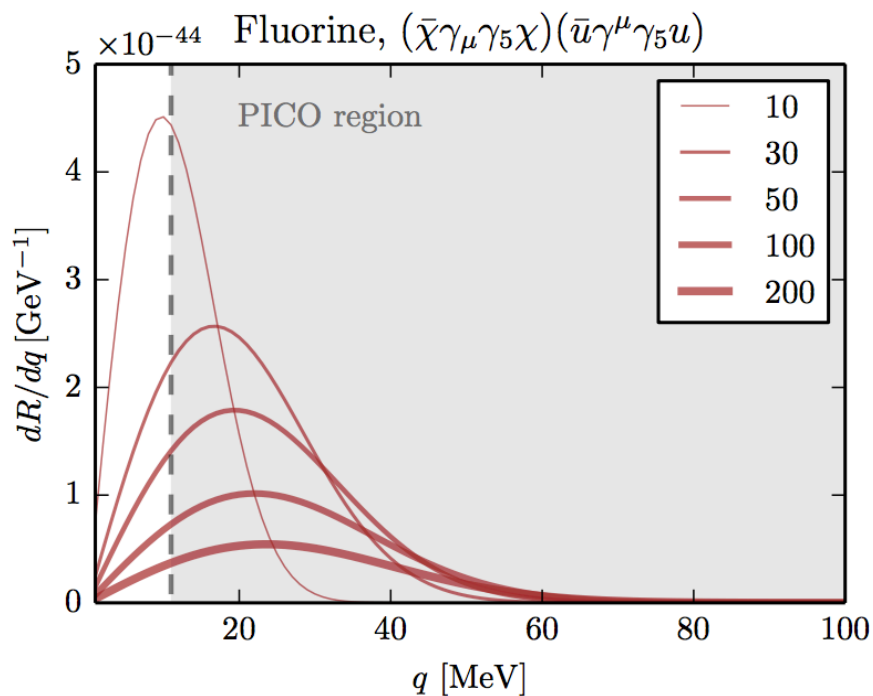
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- typical momentum exchange

$$q_{\text{max}} \sim 200 \text{ MeV.}$$

- this allows for treatment with ChPT, expansion in q/Λ_{ChEFT}

DM DETECTION



$$E_d = 2 \frac{\tilde{v}^2}{M_A} \sim 2\text{keV} \left(\frac{1}{M_A} \right) \left(\frac{1}{10\text{GeV}} \right) \left(\frac{1}{10^{-3}} \right)$$

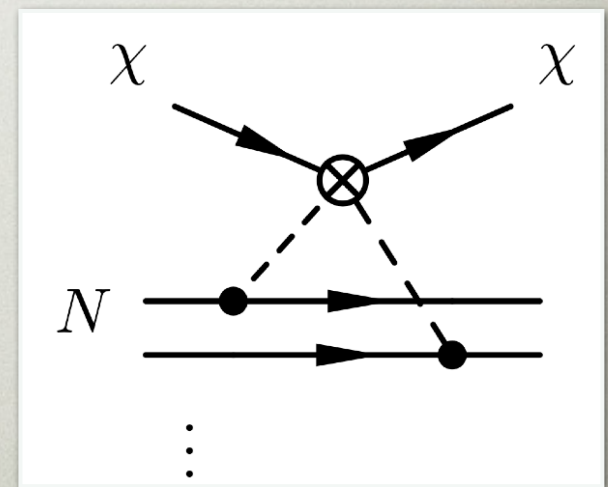
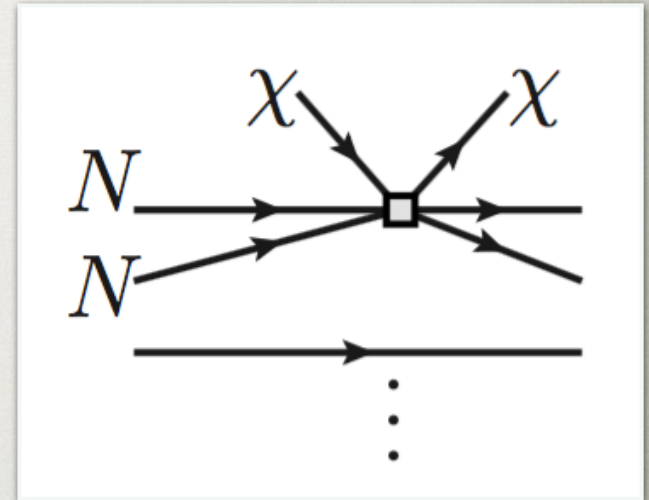
- typical momentum exchange

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GENERAL LESSONS

- chirally leading contributions due to DM scattering on a single nucleon current
 - DM coupling to four-nucleon ops. always $O(q^3)$ suppressed
 - long distance contribs. only $O(q)$ suppr. for scalar couplings
- not all NR ops. generated
- switching on just one NR oper. at a time not justified



ALL OPERATORS?

- do we need all the operators? [F. Bishara, J. Brod, B. Grinstein, JZ, 1611.00368; 1707.06998](#)
 - 15 operators with up to 2 derivatives
 - general dim 5 and 6 EFT above EW scale requires at LO

$$\mathcal{O}_1^N = \mathbb{1}_\chi \mathbb{1}_N,$$

$$\mathcal{O}_3^N = \mathbb{1}_\chi \vec{S}_N \cdot \left(\vec{v}_\perp \times \frac{i\vec{q}}{m_N} \right),$$

$$\mathcal{O}_5^N = \vec{S}_\chi \cdot \left(\vec{v}_\perp \times \frac{i\vec{q}}{m_N} \right) \mathbb{1}_N,$$

$$\mathcal{O}_7^N = \mathbb{1}_\chi (\vec{S}_N \cdot \vec{v}_\perp),$$

$$\mathcal{O}_9^N = \vec{S}_\chi \cdot \left(\frac{i\vec{q}}{m_N} \times \vec{S}_N \right),$$

$$\mathcal{O}_{11}^N = - \left(\vec{S}_\chi \cdot \frac{i\vec{q}}{m_N} \right) \mathbb{1}_N,$$

$$\mathcal{O}_{13}^N = - \left(\vec{S}_\chi \cdot \vec{v}_\perp \right) \left(\vec{S}_N \cdot \frac{i\vec{q}}{m_N} \right),$$

$$\mathcal{O}_2^N = (v_\perp)^2 \mathbb{1}_\chi \mathbb{1}_N,$$

$$\mathcal{O}_4^N = \vec{S}_\chi \cdot \vec{S}_N,$$

$$\mathcal{O}_6^N = \left(\vec{S}_\chi \cdot \frac{\vec{q}}{m_N} \right) \left(\vec{S}_N \cdot \frac{\vec{q}}{m_N} \right),$$

$$\mathcal{O}_8^N = (\vec{S}_\chi \cdot \vec{v}_\perp) \mathbb{1}_N,$$

$$\mathcal{O}_{10}^N = - \mathbb{1}_\chi \left(\vec{S}_N \cdot \frac{i\vec{q}}{m_N} \right),$$

$$\mathcal{O}_{12}^N = \vec{S}_\chi \cdot \left(\vec{S}_N \times \vec{v}_\perp \right),$$

$$\mathcal{O}_{14}^N = - \left(\vec{S}_\chi \cdot \frac{i\vec{q}}{m_N} \right) \left(\vec{S}_N \cdot \vec{v}_\perp \right),$$

$$\mathcal{O}_{2b}^N = (\vec{S}_N \cdot \vec{v}_\perp) (\vec{S}_\chi \cdot \vec{v}_\perp)$$

- do we need the $O(q^2)$ terms? Can we stop at $O(q^2)$?

LO DIAGRAMS

- quark and gluon currents hadronize as

nucleon currents

$$\begin{aligned} \tilde{J}_{q,\mu}^V &\sim v_B^\mu \bar{N}N + \dots, & \tilde{J}_{q,\mu}^A &\sim S_\mu \bar{N}N + \dots, \\ \tilde{J}_q^S &\sim m_q \bar{N}N + \dots, & \tilde{J}_q^P &\sim m_q \bar{N}N \pi + \dots, \\ \tilde{J}^G &\sim \bar{N}N + \dots, & \tilde{J}^\theta &\sim q^\mu S_\mu \bar{N}N + \dots, \end{aligned}$$

$$\begin{aligned} J_{q,\mu}^V &\sim \pi \partial_\mu \pi + \dots, & J_{q,\mu}^A &\sim \partial_\mu \pi + \dots, \\ J^G &\sim \pi^2, & J_q^S &\sim m_q \pi^2 + \dots, & J_q^P &\sim m_q \pi + \dots, \end{aligned}$$

meson currents

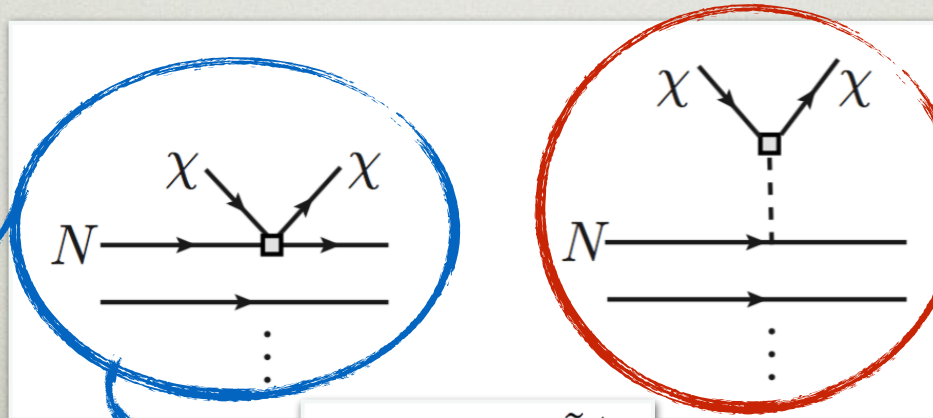
- two types of leading order diagrams

$$\bar{q} \gamma_\mu q \rightarrow \tilde{J}_{q,\mu}^V,$$

$$\bar{q} q \rightarrow \tilde{J}_q^S,$$

$$GG \rightarrow \tilde{J}^G,$$

$$G\tilde{G} \rightarrow \tilde{J}^\theta$$



$$i\bar{q} \gamma_5 q \rightarrow \tilde{J}_q^P,$$

$$\bar{q} \gamma_\mu \gamma_5 q \rightarrow \tilde{J}_{q,\mu}^A,$$

COMPARISON

F. Bishara, J. Brod, B. Grinstein, JZ, 1611.00368; 1707.06998

see also, e.g., Cirelli, Del Nobile, Panci, 1307.5955;
Hill, Solon, 1409.8290;

- what is new?
- for most NR operators the results agree with previous literature

$$\mathcal{O}_1^N = \mathbb{1}_\chi \mathbb{1}_N,$$

$$\mathcal{O}_3^N = \mathbb{1}_\chi \vec{S}_N \cdot \left(\vec{v}_\perp \times \frac{i\vec{q}}{m_N} \right),$$

$$\mathcal{O}_5^N = \vec{S}_\chi \cdot \left(\vec{v}_\perp \times \frac{i\vec{q}}{m_N} \right) \mathbb{1}_N,$$

$$\mathcal{O}_7^N = \mathbb{1}_\chi (\vec{S}_N \cdot \vec{v}_\perp),$$

$$\mathcal{O}_9^N = \vec{S}_\chi \cdot \left(\frac{i\vec{q}}{m_N} \times \vec{S}_N \right),$$

$$\mathcal{O}_{11}^N = - \left(\vec{S}_\chi \cdot \frac{i\vec{q}}{m_N} \right) \mathbb{1}_N,$$

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$$\mathcal{O}_{12}^N = \vec{S}_\chi \cdot \left(\vec{S}_N \times \vec{v}_\perp \right),$$

COMPARISON

see also Hoferichter, Klos, and Schwenk, 1503.04811

- what is new?
- re-amphasing the importance of (pion) pole enhanced contribs.

$$\mathcal{O}_1^N = \mathbb{1}_\chi \mathbb{1}_N,$$

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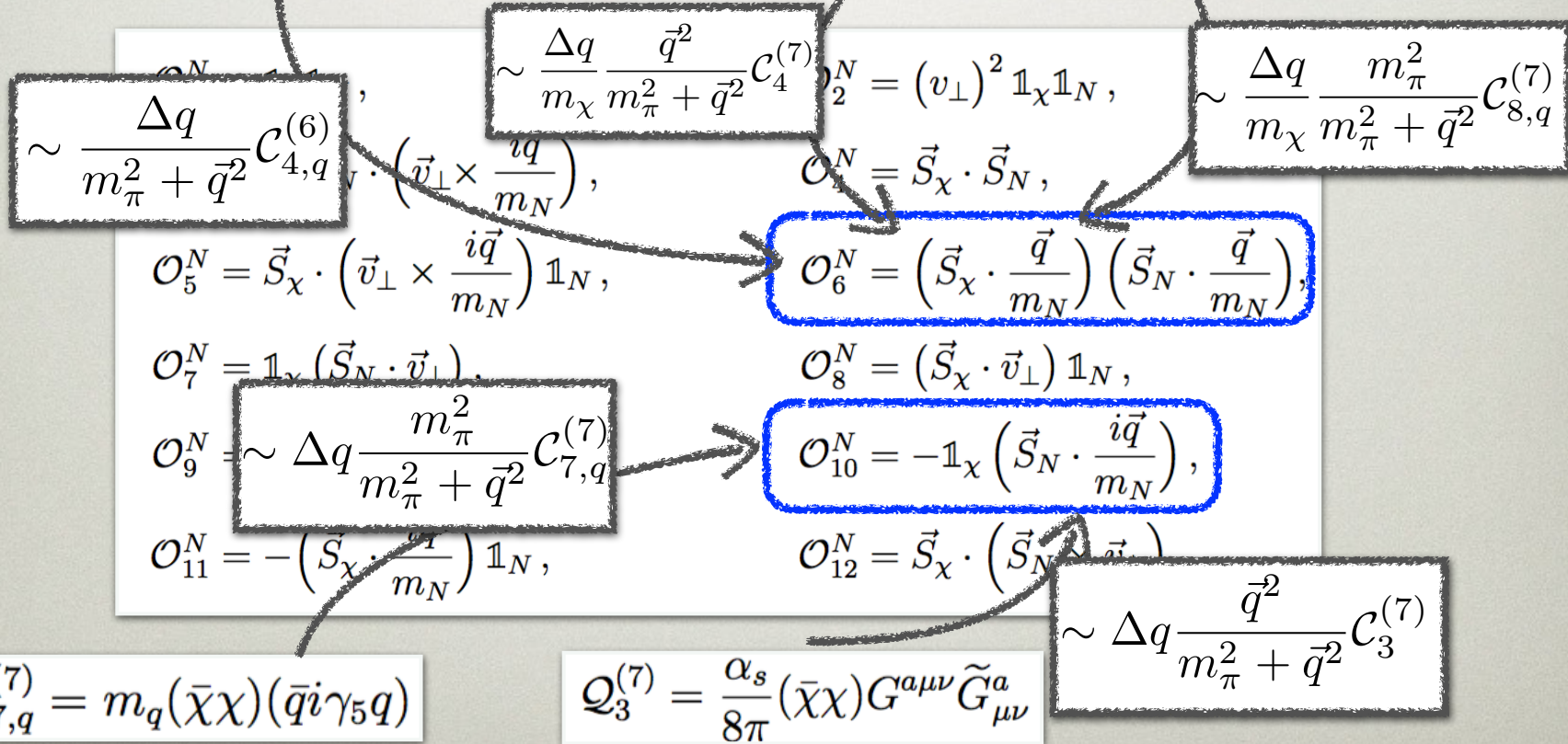
PION POLES

- the pion poles important for

$$Q_{4,q}^{(6)} = (\bar{\chi}\gamma_\mu\gamma_5\chi)(\bar{q}\gamma^\mu\gamma_5q)$$

$$Q_4^{(7)} = \frac{\alpha_s}{8\pi}(\bar{\chi}i\gamma_5\chi)G^{a\mu\nu}\tilde{G}_{\mu\nu}^a$$

$$Q_{8,q}^{(7)} = m_q(\bar{\chi}\gamma_5\chi)(\bar{q}\gamma_5q)$$



COMPARISON

- what is new?
 - consistent chiral counting
 - for instance: $Ax A$ operator

$$Q_{4,q}^{(6)} = (\bar{\chi} \gamma_\mu \gamma_5 \chi) (\bar{q} \gamma^\mu \gamma_5 q)$$

$$\sim \Delta q C_{4,q}^{(6)}$$

$$= (v_\perp)^2 \mathbb{1}_x \mathbb{1}_N,$$

$$\sim \frac{\Delta q}{m_\pi^2 + \bar{q}^2} C_{4,q}^{(6)}$$

$$\mathcal{O}_1^N = \mathbb{1}_x \mathbb{1}_N,$$

$$\mathcal{O}_3^N = \mathbb{1}_x \vec{S}_N \cdot \left(\vec{v}_\perp \times \frac{i\vec{q}}{m_N} \right),$$

$$\mathcal{O}_5^N = \vec{S}_x \cdot \left(\vec{v}_\perp \times \frac{i\vec{q}}{m_N} \right) \mathbb{1}_N,$$

$$\mathcal{O}_7^N = \mathbb{1}_x (\vec{S}_N \cdot \vec{v}_\perp),$$

$$\mathcal{O}_9^N = \vec{S}_x \cdot \left(\frac{i\vec{q}}{m_N} \times \vec{S}_N \right),$$

$$\mathcal{O}_{11}^N = - \left(\vec{S}_x \cdot \frac{i\vec{q}}{m_N} \right) \mathbb{1}_N,$$

$$\mathcal{O}_4^N = \vec{S}_x \cdot \vec{S}_N,$$

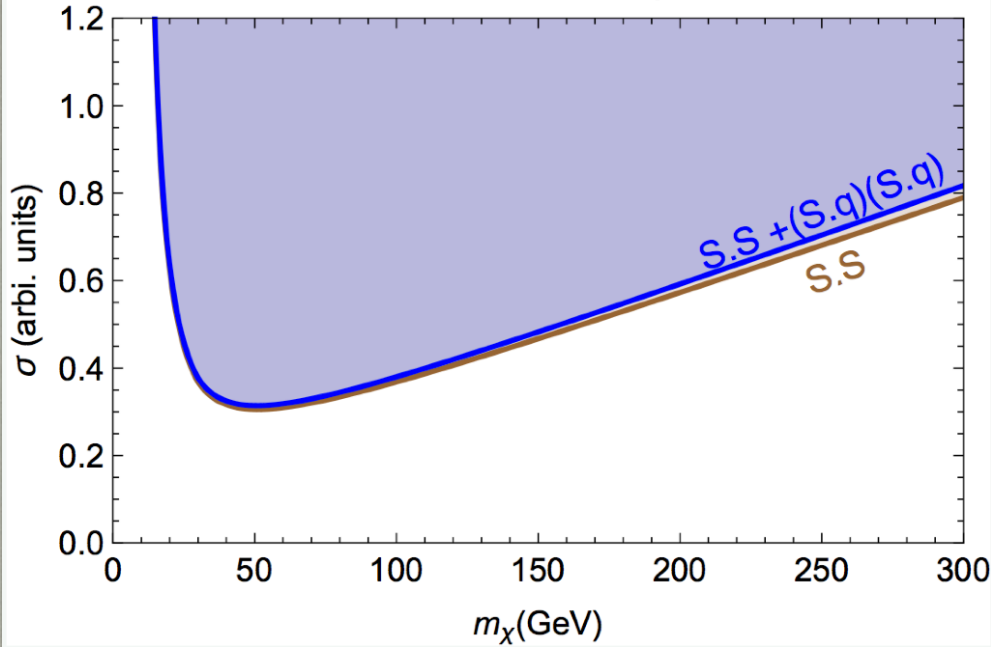
$$\mathcal{O}_6^N = \left(\vec{S}_x \cdot \frac{q}{m_N} \right) \left(\vec{S}_N \cdot \frac{q}{m_N} \right),$$

$$\mathcal{O}_8^N = (\vec{S}_x \cdot \vec{v}_\perp) \mathbb{1}_N,$$

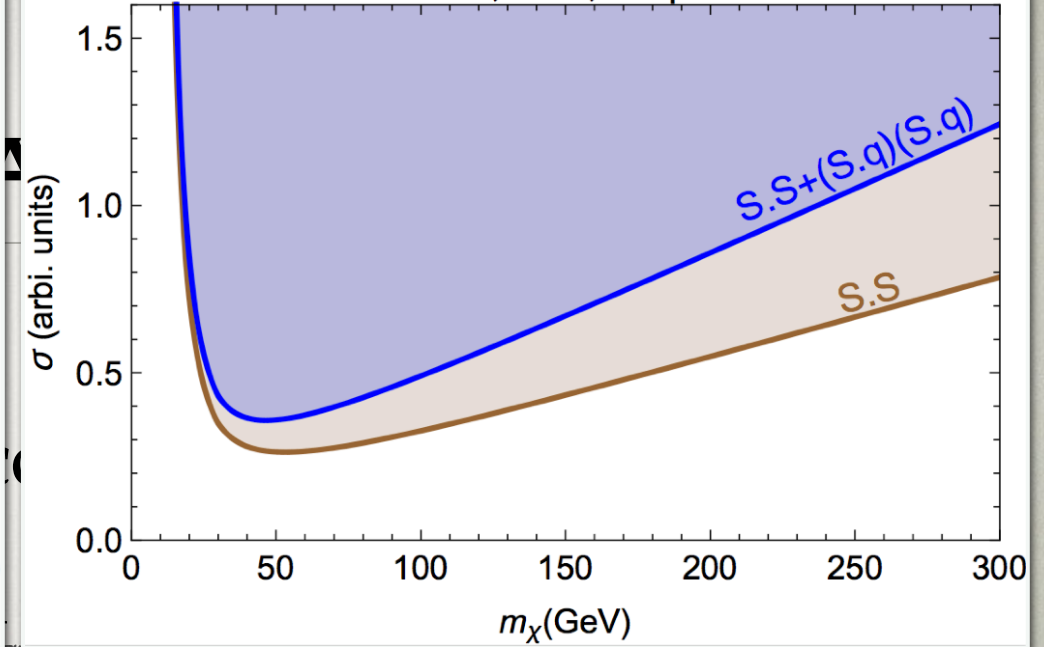
$$\mathcal{O}_{10}^N = - \mathbb{1}_x \left(\vec{S}_N \cdot \frac{i\vec{q}}{m_N} \right),$$

$$\mathcal{O}_{12}^N = \vec{S}_x \cdot \left(\vec{S}_N \times \vec{v}_\perp \right),$$

Fluorine, AxA, u-quark



Xenon, AxA, u-quark



$$\mathcal{O}_1^N = \mathbb{1}_\chi \mathbb{1}_N,$$

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$$\mathcal{O}_5^N = \vec{S}_\chi \cdot \left(\vec{v}_\perp \times \frac{i\vec{q}}{m_N} \right) \mathbb{1}_N,$$

$$\mathcal{O}_7^N = \mathbb{1}_\chi (\vec{S}_N \cdot \vec{v}_\perp),$$

$$\mathcal{O}_9^N = \vec{S}_\chi \cdot \left(\frac{i\vec{q}}{m_N} \times \vec{S}_N \right),$$

$$\mathcal{O}_{11}^N = - \left(\vec{S}_\chi \cdot \frac{i\vec{q}}{m_N} \right) \mathbb{1}_N,$$

$$\sim \Delta q \mathcal{C}_{4,q}^{(6)}$$

$$= (v_\perp)^2 \mathbb{1}_\chi \mathbb{1}_N,$$

$$\sim \frac{\Delta q}{m_\pi^2 + \vec{q}^2} \mathcal{C}_{4,q}^{(6)}$$

$$\mathcal{O}_4^N = \vec{S}_\chi \cdot \vec{S}_N,$$

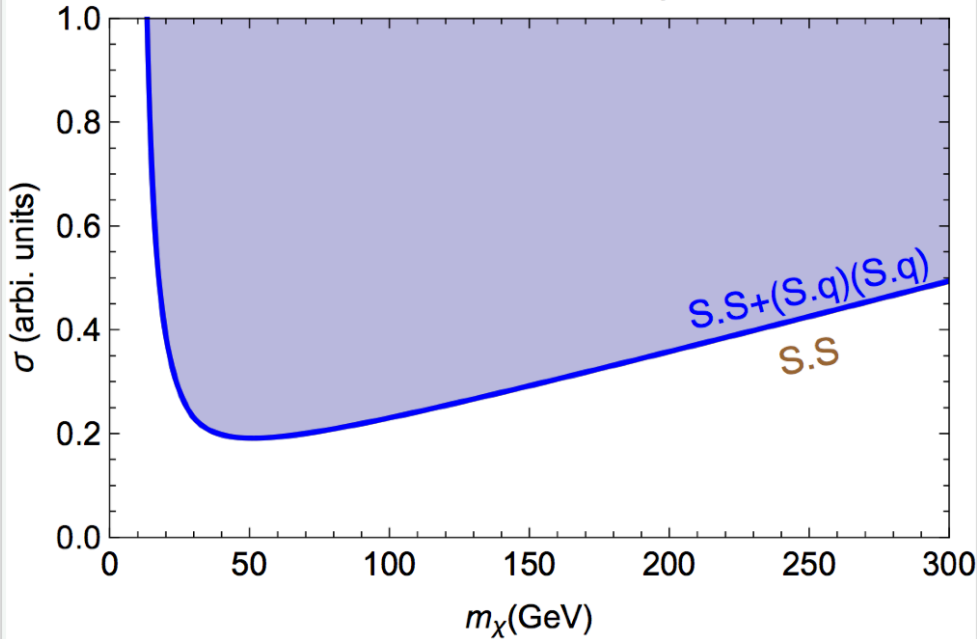
$$\mathcal{O}_6^N = \left(\vec{S}_\chi \cdot \frac{\vec{q}}{m_N} \right) \left(\vec{S}_N \cdot \frac{\vec{q}}{m_N} \right),$$

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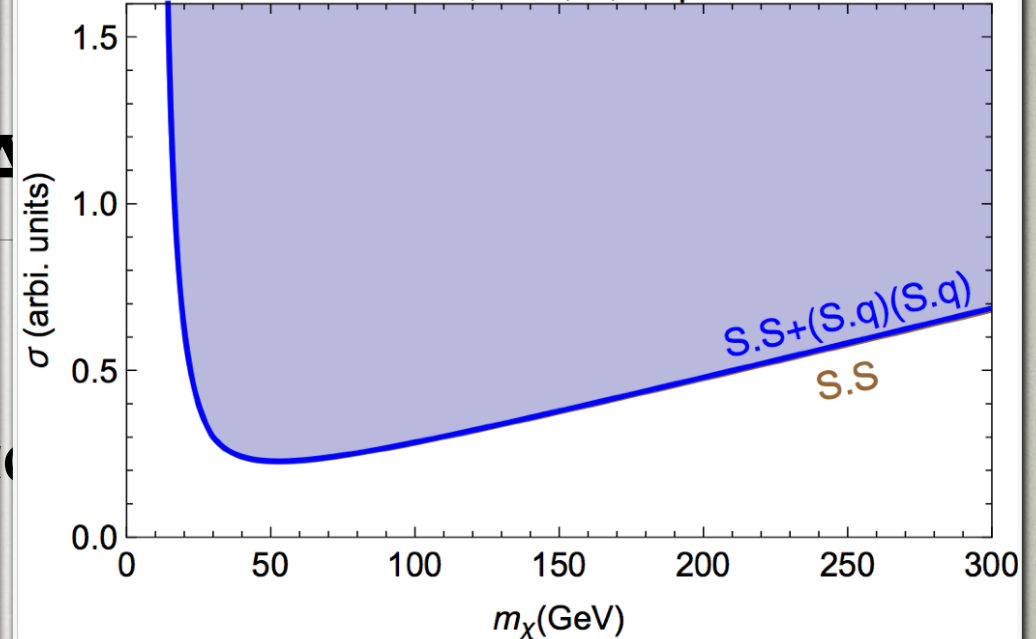
$$\mathcal{O}_{10}^N = -\mathbb{1}_\chi \left(\vec{S}_N \cdot \frac{i\vec{q}}{m_N} \right),$$

$$\mathcal{O}_{12}^N = \vec{S}_\chi \cdot (\vec{S}_N \times \vec{v}_\perp),$$

Fluorine, AxA, u,d-quark



Xenon, AxA, u,d-quark



$$\mathcal{O}_1^N = \mathbb{1}_\chi \mathbb{1}_N,$$

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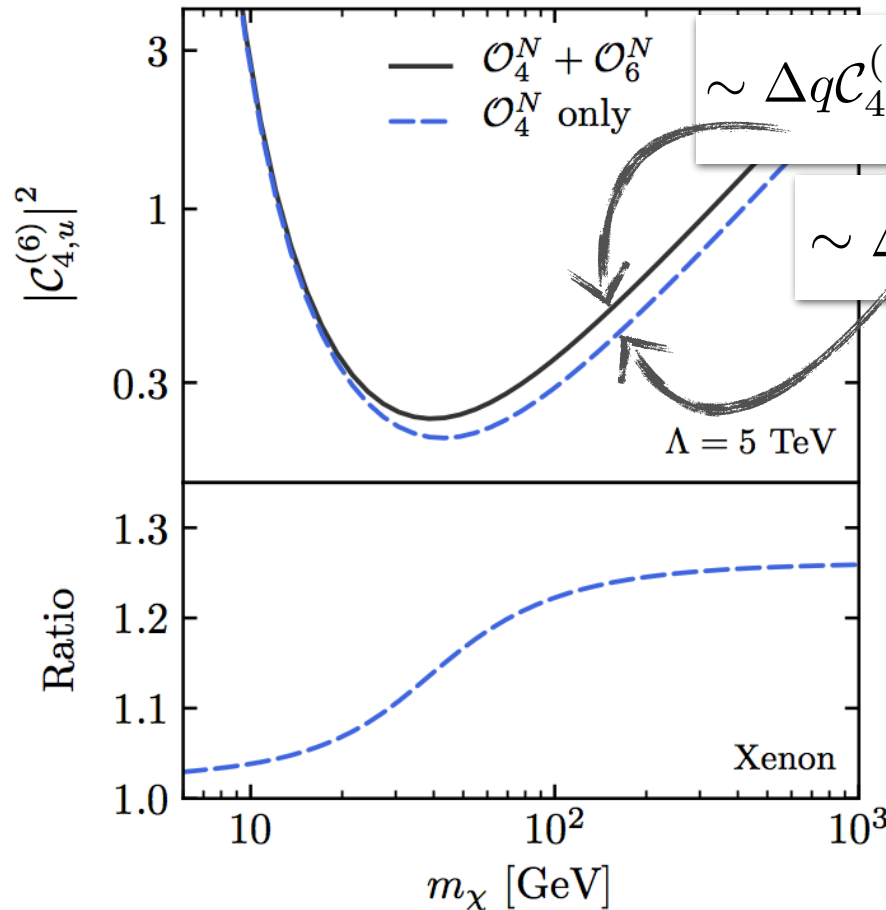
$$\mathcal{O}_{12}^N = \vec{S}_\chi \cdot (\vec{S}_N \times \vec{v}_\perp),$$

AXIAL-AXIAL

- some further examples

$$\mathcal{Q}_{4,q}^{(6)} = (\bar{\chi}\gamma_\mu\gamma_5\chi)(\bar{q}\gamma^\mu\gamma_5q)$$

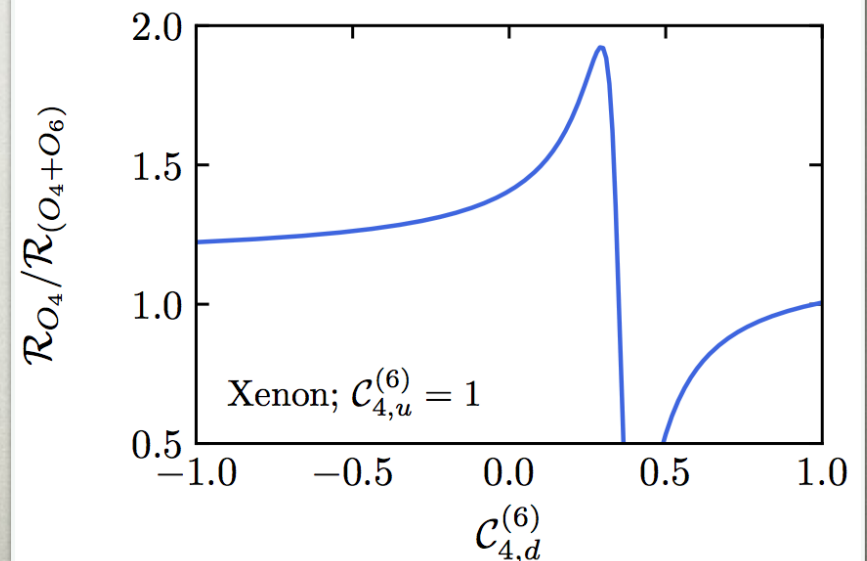
- axial-axial interaction: $C_{4u} = -C_{4d}$



$$\sim \Delta q C_{4,q}^{(6)} (\vec{S}_\chi \cdot \vec{S}_N) + \frac{\Delta q}{m_\pi^2 + \vec{q}^2} C_{4,6}^{(6)} (\vec{S}_\chi \cdot \vec{q}) (\vec{S}_N \cdot \vec{q})$$

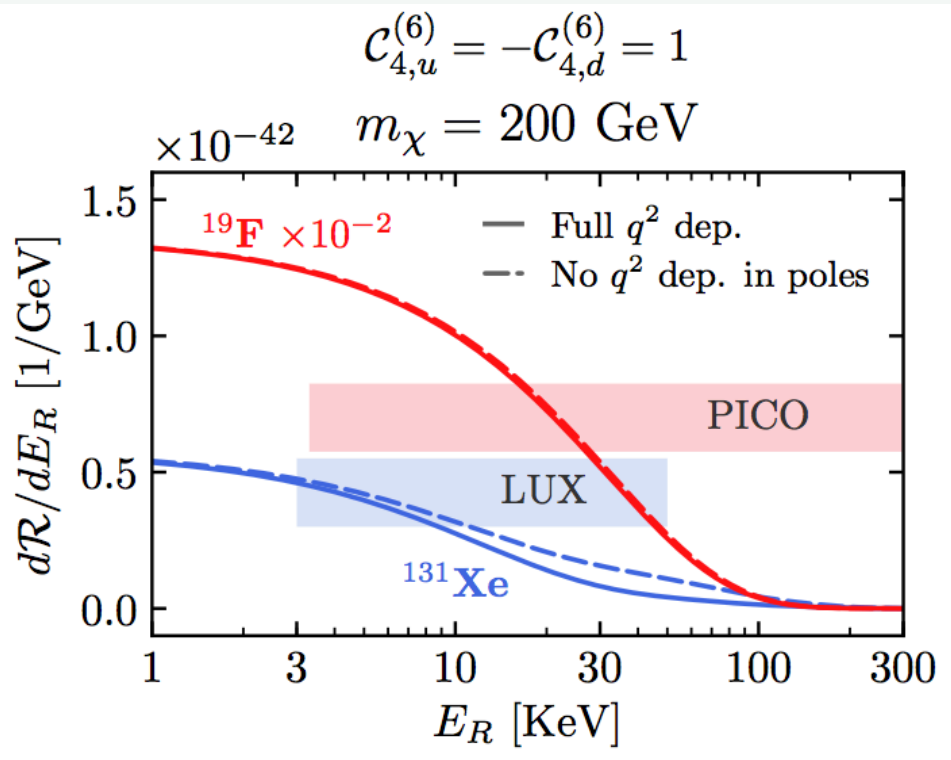
$$\sim \Delta q C_{4,q}^{(6)} (\vec{S}_\chi \cdot \vec{S}_N)$$

$m_\chi = 100$ GeV



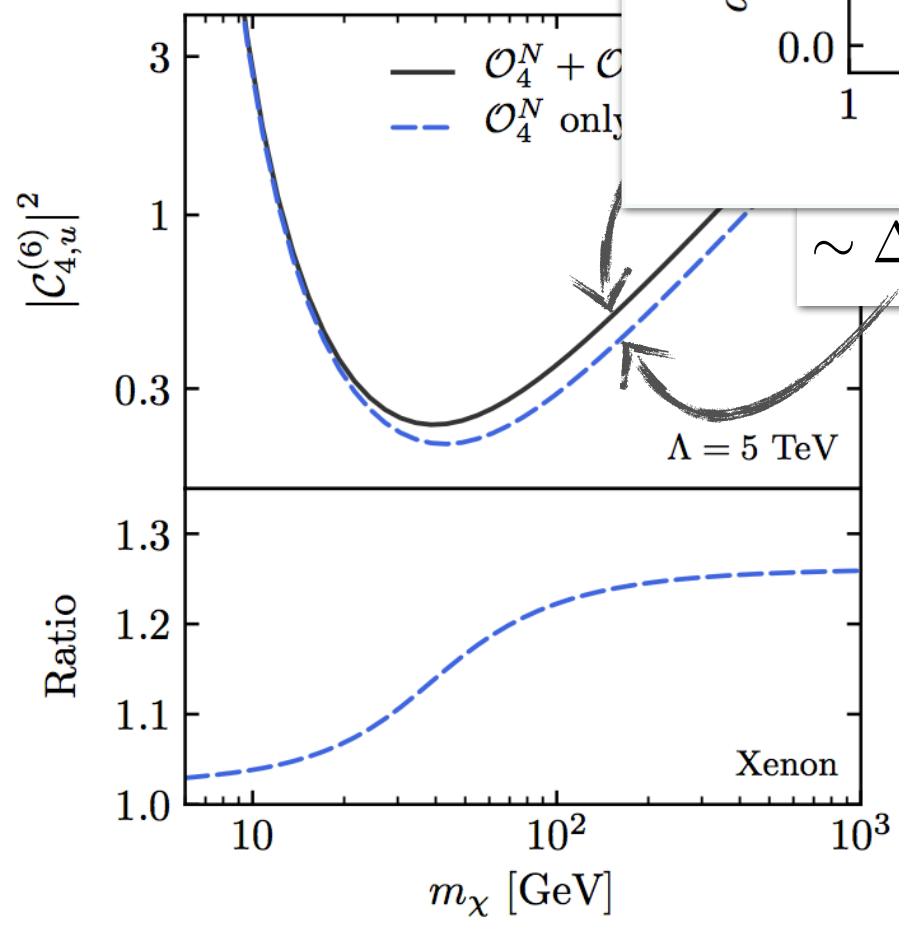
AX

- some further ex
- axial-axial int

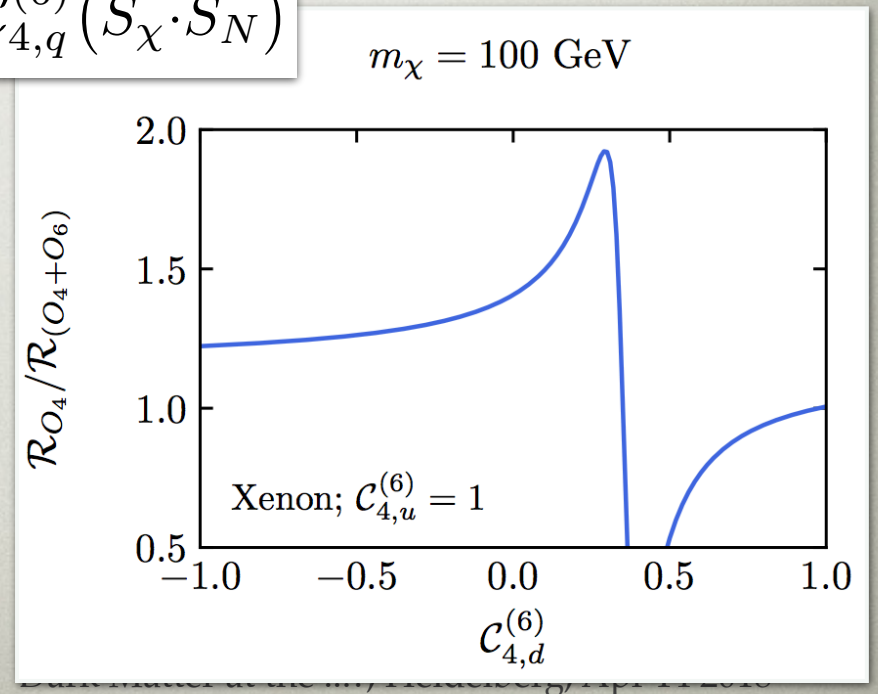


$(\vec{S}_N \cdot \vec{q})$

$(\vec{S}_N \cdot \vec{q})$



$\sim \Delta q C_{4,q}^{(6)} (\vec{S}_\chi \cdot \vec{S}_N)$

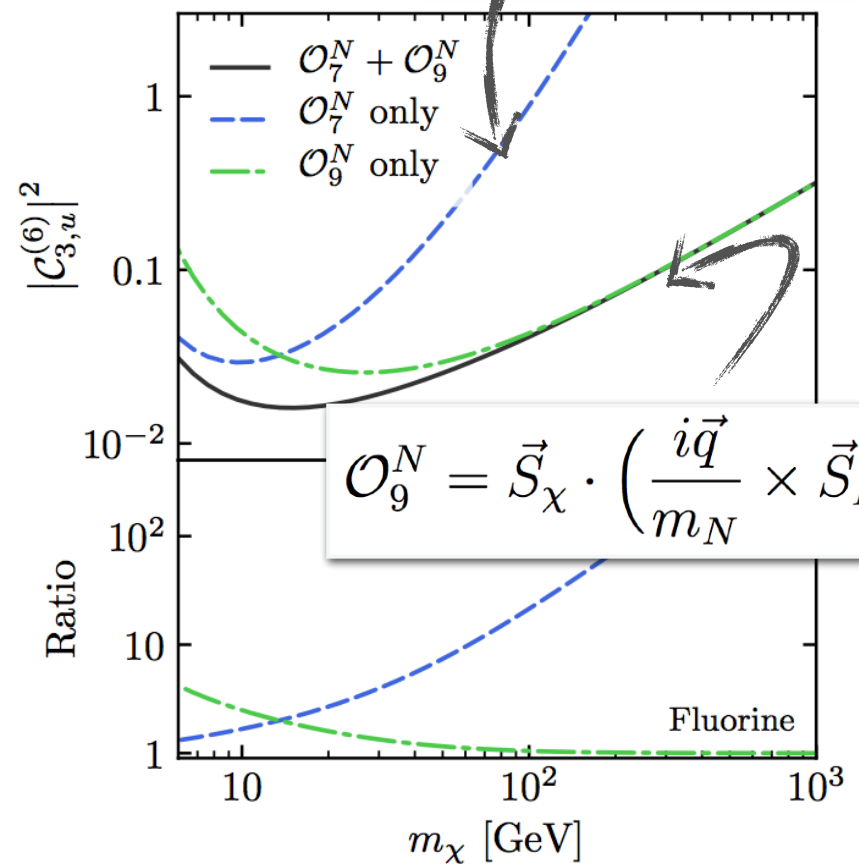
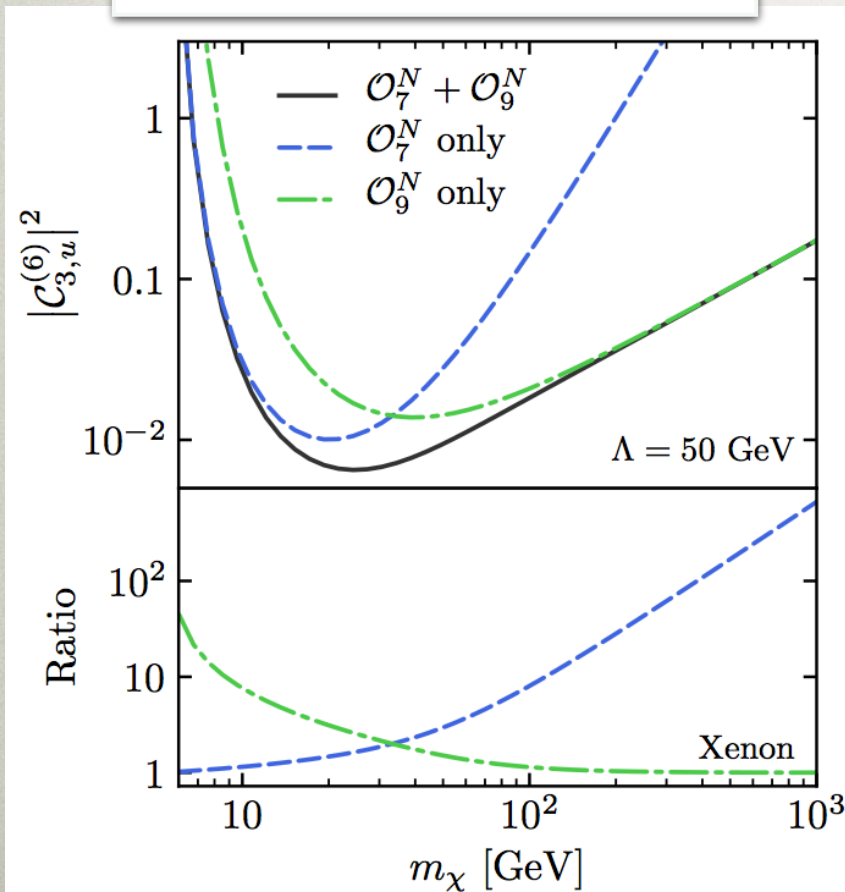


VECTOR-AXIAL

- vector-axial interaction: $C_{3u}=C_{3d}=C_{3s}=1$

$$Q_{3,q}^{(6)} = (\bar{\chi}\gamma_\mu\chi)(\bar{q}\gamma^\mu\gamma_5q)$$

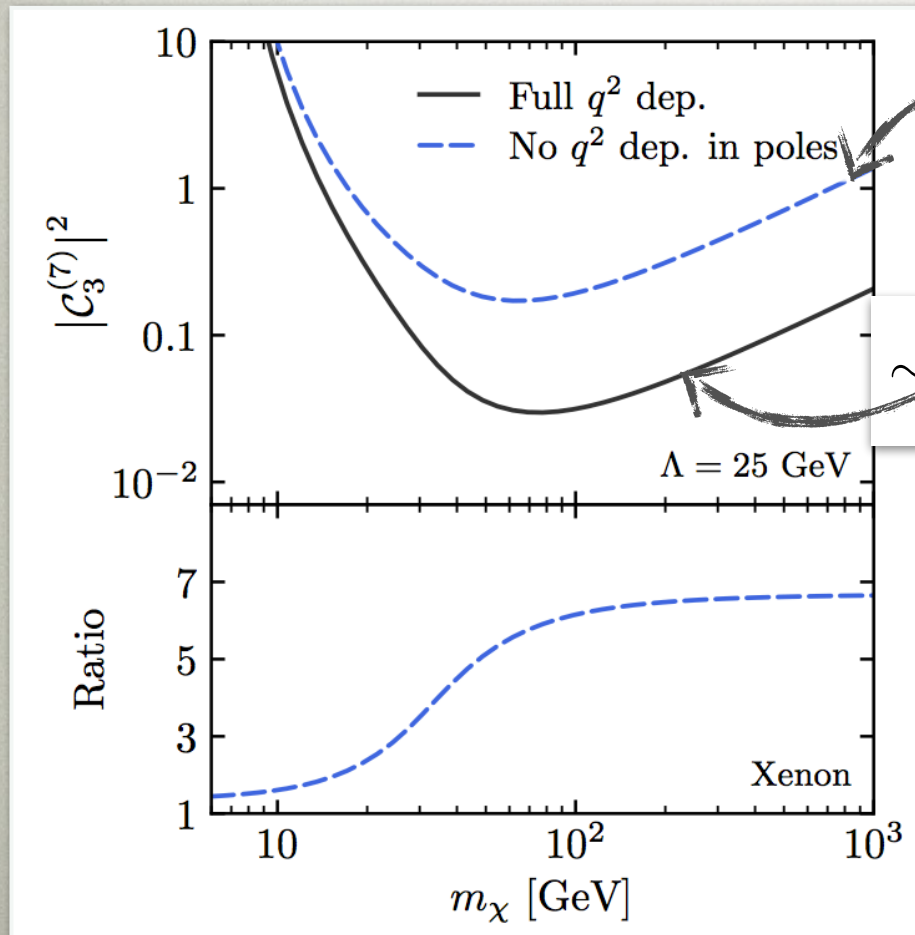
$$\mathcal{O}_7^N = \mathbb{1}_\chi (\vec{S}_N \cdot \vec{v}_\perp)$$



CP-ODD GLUONIC OPERATOR

- SxCP-odd gluonic operator
 - compare with $q \rightarrow 0$ limit

$$Q_3^{(7)} = \frac{\alpha_s}{8\pi} (\bar{\chi}\chi) G^{a\mu\nu} \tilde{G}_{\mu\nu}^a$$



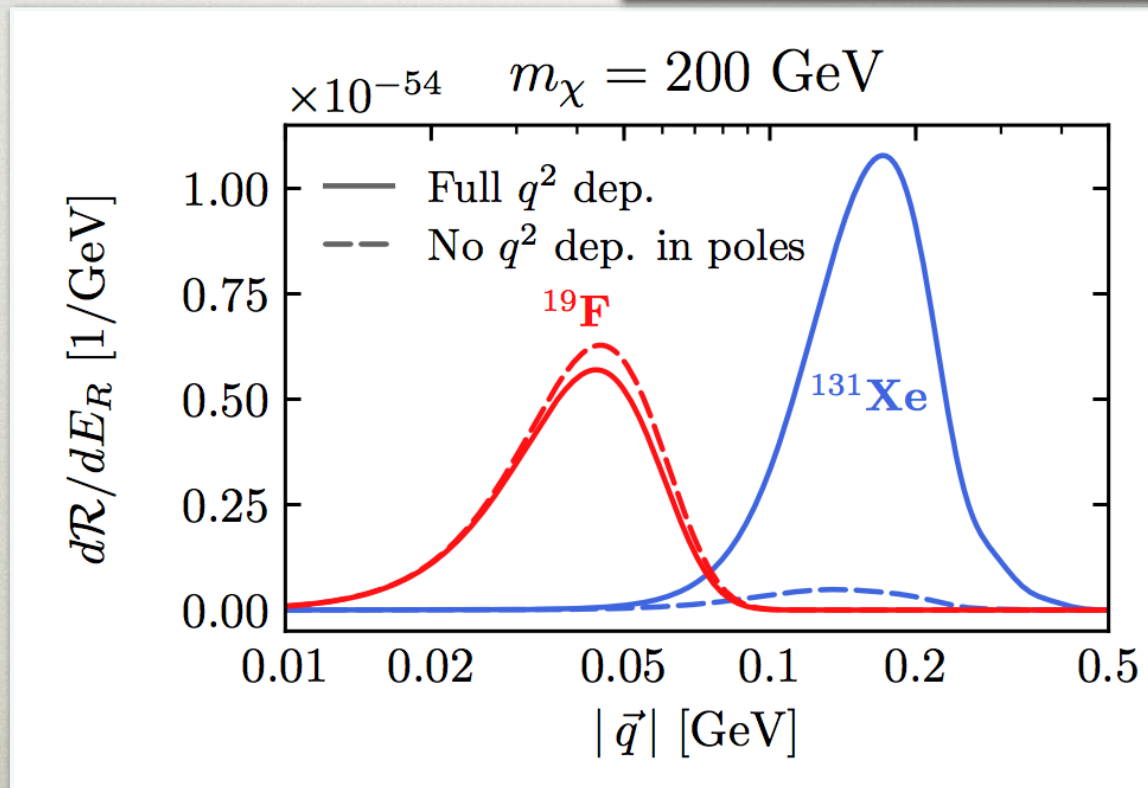
$$\sim \frac{\Delta q}{m_q} (\vec{S}_N \cdot \vec{q})$$

$$\sim \left(\frac{\Delta q}{m_q} + \left(\frac{1}{m_u} - \frac{1}{m_d} \right) \frac{(\Delta u - \Delta d) \vec{q}^2}{m_\pi^2 + \vec{q}^2} \right) (\vec{S}_N \cdot \vec{q})$$

ENERGY DEPENDENCE

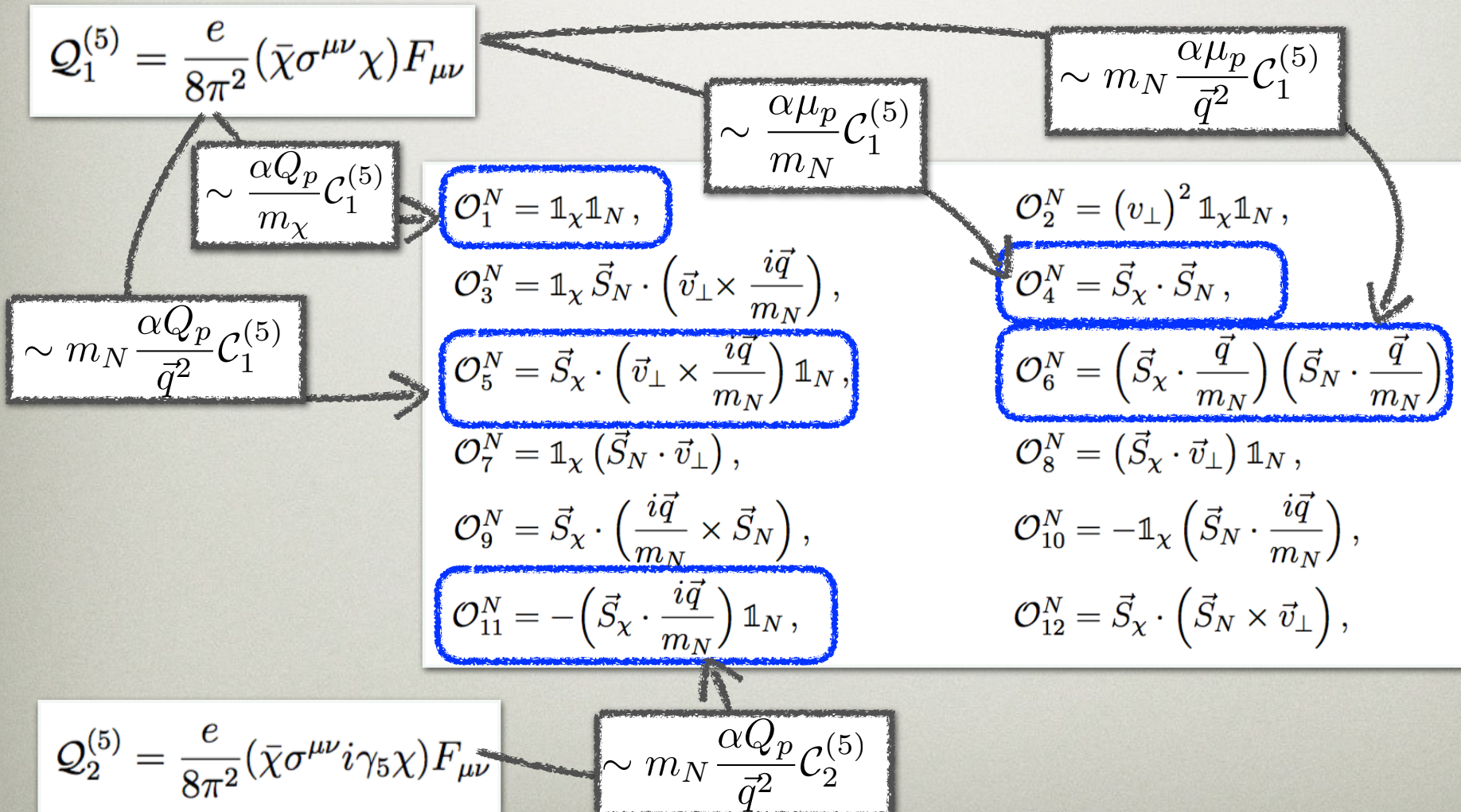
- The differential event rate as a function of the momentum transfer as an example: $Q_4^{(7)}$

$$Q_4^{(7)} = \frac{\alpha_s}{8\pi} (\bar{\chi} i \gamma_5 \chi) G^{a\mu\nu} \tilde{G}_{\mu\nu}^a$$



PHOTON POLES

- due to photon poles also need $O(q^2)$ ops

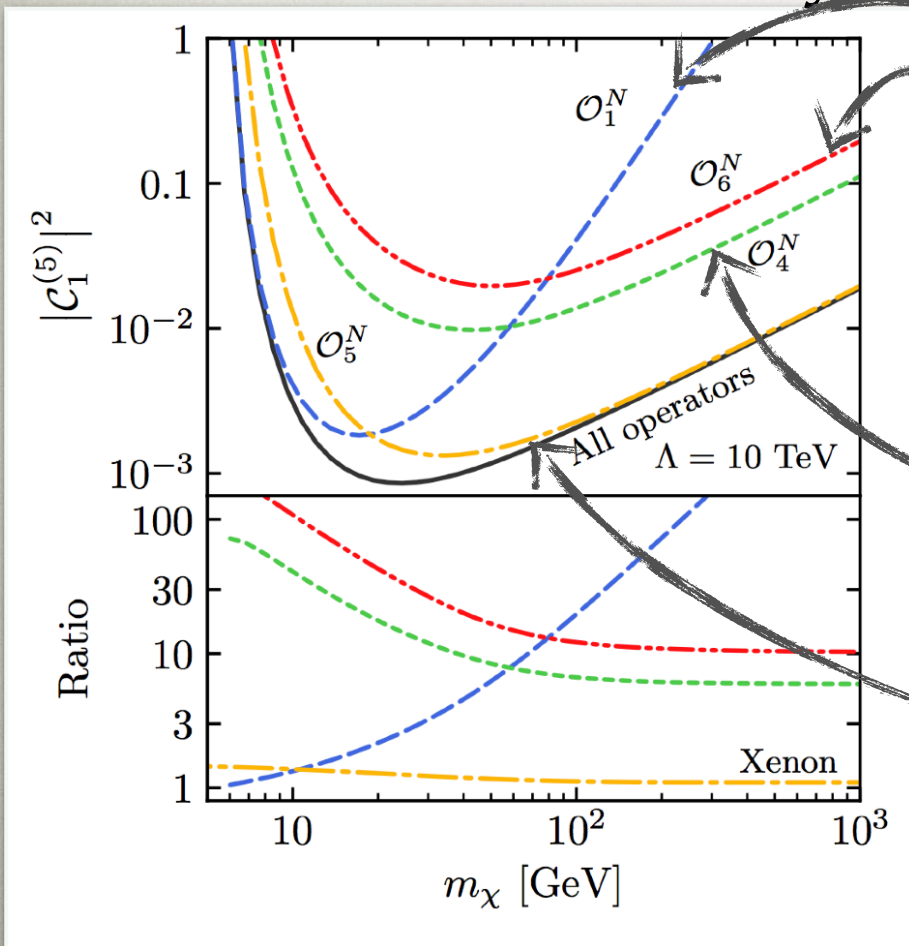


PHOTON POLES - XENON

- for magnetic dipole interaction

$$Q_1^{(5)} = \frac{e}{8\pi^2} (\bar{\chi} \sigma^{\mu\nu} \chi) F_{\mu\nu}$$

- two coherently enhanced operators



$$-\frac{\alpha Q_p}{2\pi m_\chi} \hat{C}_1^{(5)} \quad \mathcal{O}_1^N = \mathbb{1}_\chi \mathbb{1}_N$$

$$\frac{2\alpha \mu_N m_N}{\pi \vec{q}^2} \hat{C}_1^{(5)} \quad \mathcal{O}_6^N = \left(\vec{S}_\chi \cdot \frac{\vec{q}}{m_N} \right) \left(\vec{S}_N \cdot \frac{\vec{q}}{m_N} \right)$$

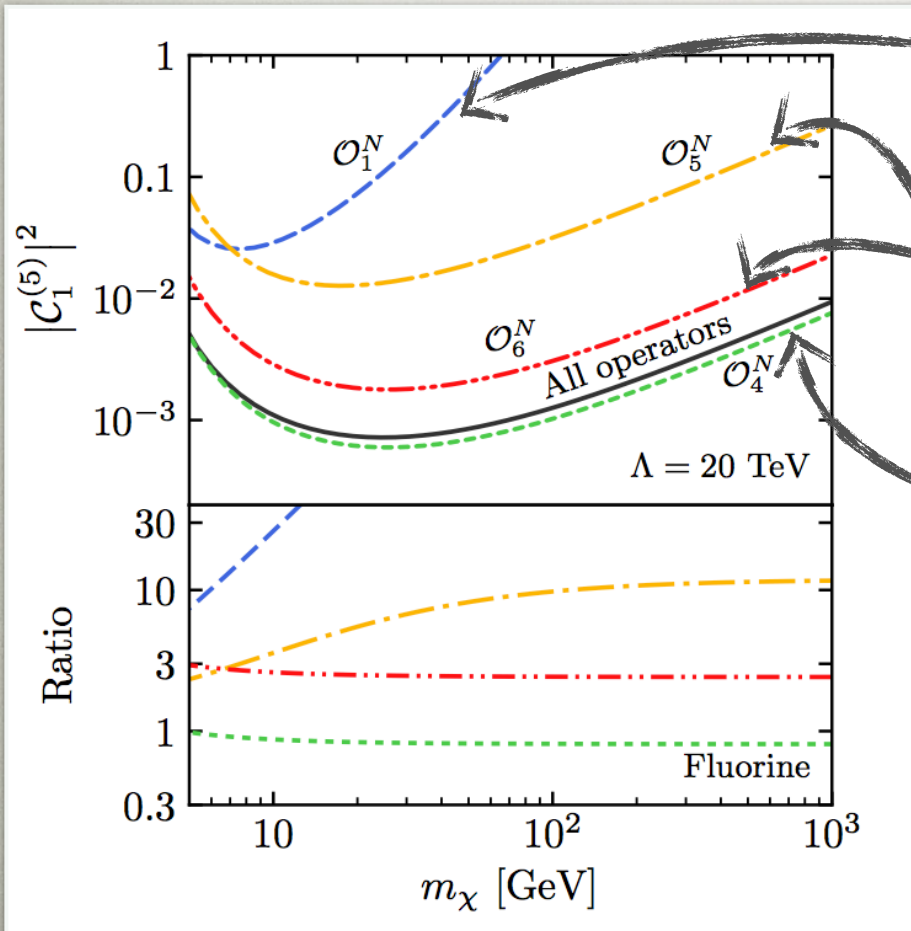
$$-\frac{2\alpha \mu_N}{\pi m_N} \hat{C}_1^{(5)} \quad \mathcal{O}_4^N = \vec{S}_\chi \cdot \vec{S}_N$$

$$\frac{2\alpha Q_p m_N}{\pi \vec{q}^2} \hat{C}_1^{(5)} \quad \mathcal{O}_5^N = \vec{S}_\chi \cdot \left(\vec{v}_\perp \times \frac{i\vec{q}}{m_N} \right) \mathbb{1}_N$$

PHOTON POLES - FLUORINE

- magnetic dipole interaction
- both SD operators important

$$Q_1^{(5)} = \frac{e}{8\pi^2} (\bar{\chi} \sigma^{\mu\nu} \chi) F_{\mu\nu}$$



$$-\frac{\alpha Q_p}{2\pi m_\chi} \hat{C}_1^{(5)}$$

$$\mathcal{O}_1^N = \mathbb{1}_\chi \mathbb{1}_N$$

$$\frac{2\alpha \mu_N m_N}{\pi} \frac{\hat{C}_1^{(5)}}{\vec{q}^2}$$

$$\mathcal{O}_6^N = \left(\vec{S}_\chi \cdot \frac{\vec{q}}{m_N} \right) \left(\vec{S}_N \cdot \frac{\vec{q}}{m_N} \right)$$

$$-\frac{2\alpha \mu_N}{\pi m_N} \hat{C}_1^{(5)}$$

$$\mathcal{O}_4^N = \vec{S}_\chi \cdot \vec{S}_N$$

$$\frac{2\alpha Q_p m_N}{\pi \vec{q}^2} \hat{C}_1^{(5)}$$

$$\mathcal{O}_5^N = \vec{S}_\chi \cdot \left(\vec{v}_\perp \times \frac{i\vec{q}}{m_N} \right) \mathbb{1}_N$$

NLO - SINGLE CURRENTS

F. Bishara, J. Brod, B. Grinstein, JZ, 1611.00368; 1707.06998

- for many operators two-nucleon currents highly suppressed
- are $O(q^2)$ corrections to single currents ever important?
 - part of it captured by form factors for LO operators
 - but also new operators generated
- example: tensor-tensor operator

$$Q_{9,q}^{(7)} = m_q (\bar{\chi} \sigma^{\mu\nu} \chi) (\bar{q} \sigma_{\mu\nu} q) \sim \frac{\Delta q}{m_q} (\vec{S}_\chi \cdot \vec{S}_N) + \frac{\vec{q}^2}{m_N m_\chi} \mathbb{1}_\chi \mathbb{1}_N$$

LO spin-dep. NLO spin-indep. coherently enhanced $\sim A^2$

- numerical factors make it small, though

SCALAR DARK MATTER

- analysis for scalar DM easier
- no DM spin \Rightarrow no cancellations in products of $J_\chi \times$ (leading chiral J_q)
- for P_q and A_q currents the contriBs. are enhanced by pion poles

$$\begin{aligned}
 Q_{1,q}^{(6)} &= (\varphi^* i \overleftrightarrow{\partial}_\mu \varphi) (\bar{q} \gamma^\mu q), & Q_{2,q}^{(6)} &= (\varphi^* i \overleftrightarrow{\partial}_\mu \varphi) (\bar{q} \gamma^\mu \gamma_5 q), \\
 Q_{3,q}^{(6)} &= m_q (\varphi^* \varphi) (\bar{q} q), & Q_{4,q}^{(6)} &= m_q (\varphi^* \varphi) (\bar{q} i \gamma_5 q), \\
 Q_5^{(6)} &= \frac{\alpha_s}{12\pi} (\varphi^* \varphi) G^{a\mu\nu} G_{\mu\nu}^a, & Q_6^{(6)} &= \frac{\alpha_s}{8\pi} (\varphi^* \varphi) G^{a\mu\nu} \tilde{G}_{\mu\nu}^a. \\
 Q_7^{(6)} &= i \frac{e}{8\pi^2} (\partial_\mu \varphi^* \partial_\nu \varphi) F^{\mu\nu},
 \end{aligned}$$

relativistic
theory with
quarks and gluons

non-relativistic
theory with
nucleons

$$\begin{aligned}
 Q_{1,p}^{(0)} &= (\varphi_v^* \varphi_v) (\bar{p}_v p_v), \\
 Q_{1,p}^{(1)} &= (\varphi_v^* \varphi_v) (\bar{p}_v i q \cdot S_N p_v), \\
 Q_{2,p}^{(1)} &= m_N (\varphi_v^* \varphi_v) (\bar{p}_v v_\perp \cdot S_N p_v),
 \end{aligned}$$

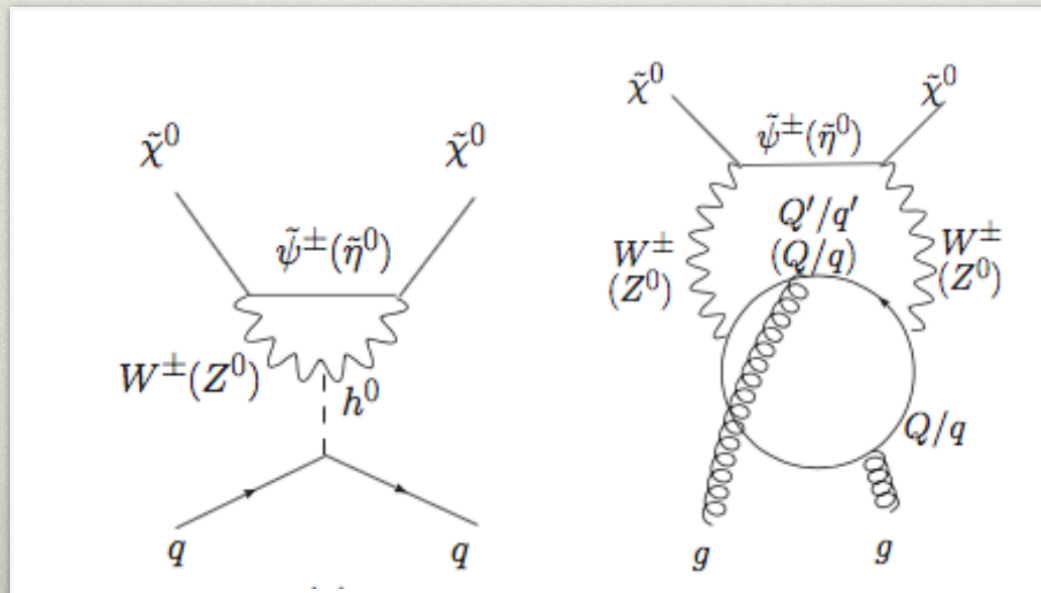
CONCLUSIONS

- presented LO + partial NLO matching from DM interacting with gluons and quarks to nuclear physics
- not always consistent to take single NR operators
- one should use EFT with gluons and quarks to consistently compare direct detection experiments

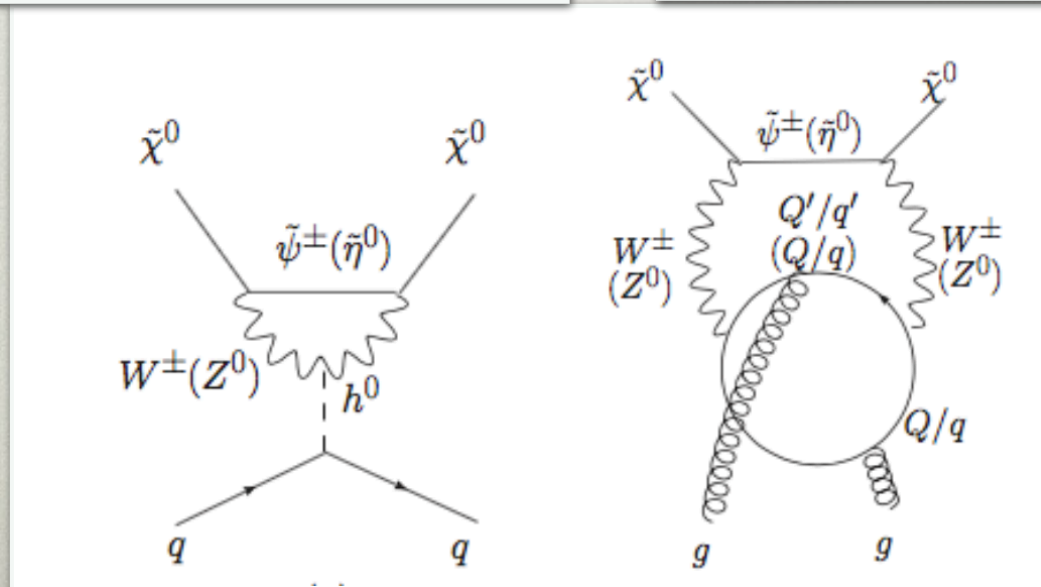
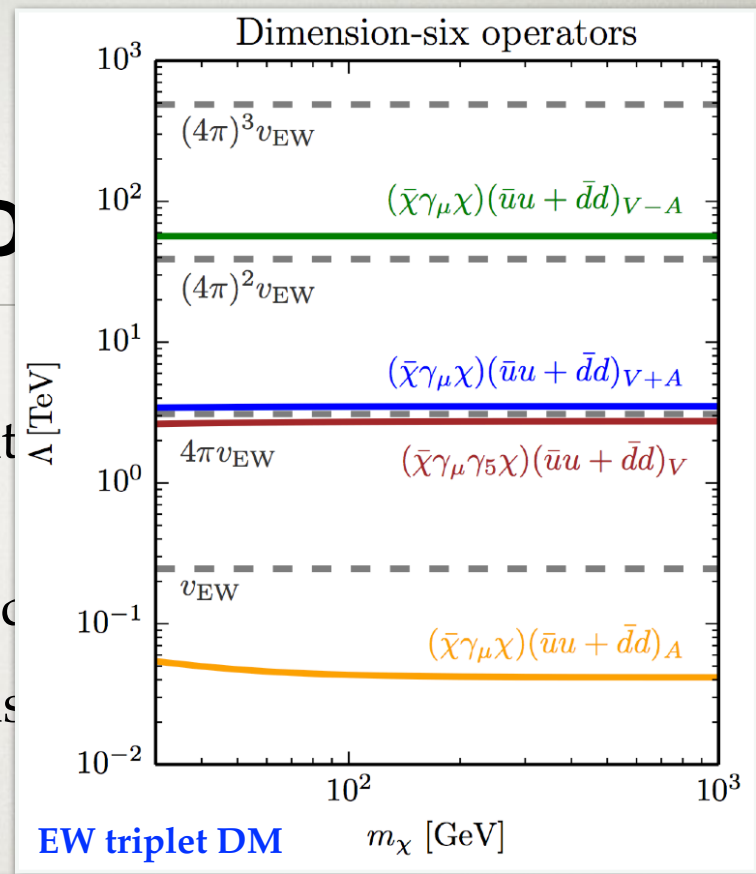
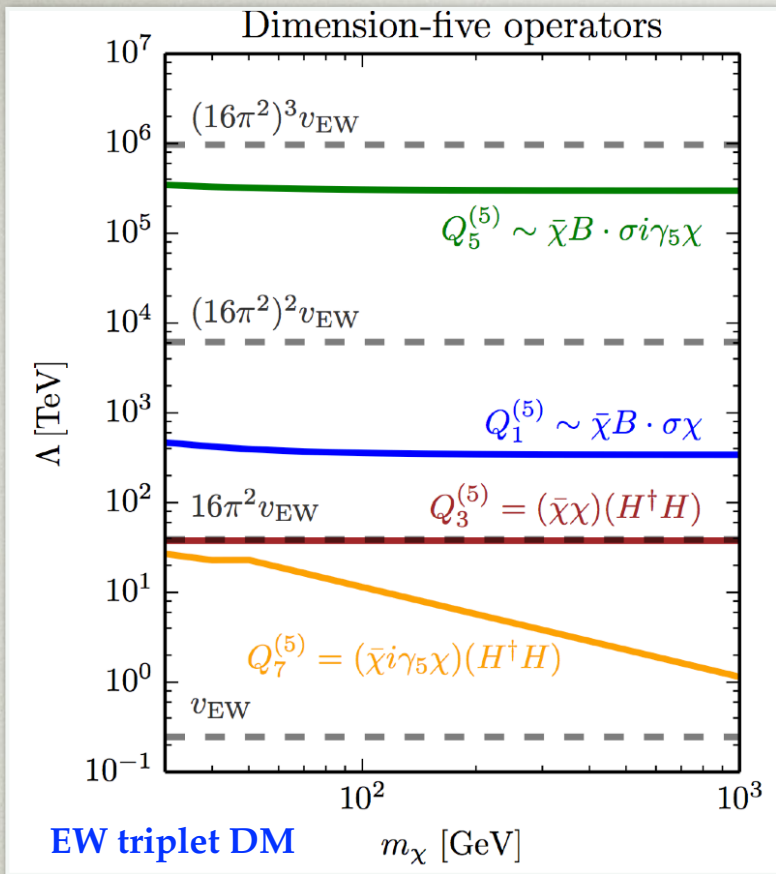
BACKUP SLIDES

HIGHER DIM OPS?

- 0-th order question:
 - since renormalizable EW interactions, do we care about higher dim ops?
- if tree level Z exchange allowed, ruled out by direct detection
- this leaves 1-loop and 2-loop as leading
- higher dim ops can dominate



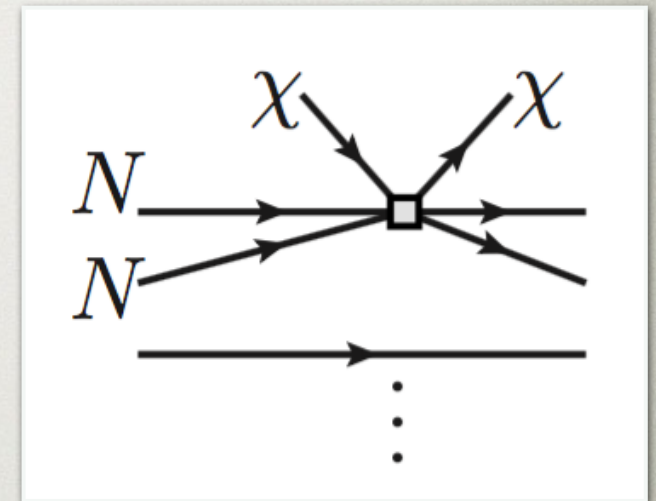
Hisano et al, 1104.0228, 1007.2601



Hisano et al, 1104.0228, 1007.2601

Heavy Baryon ChPT

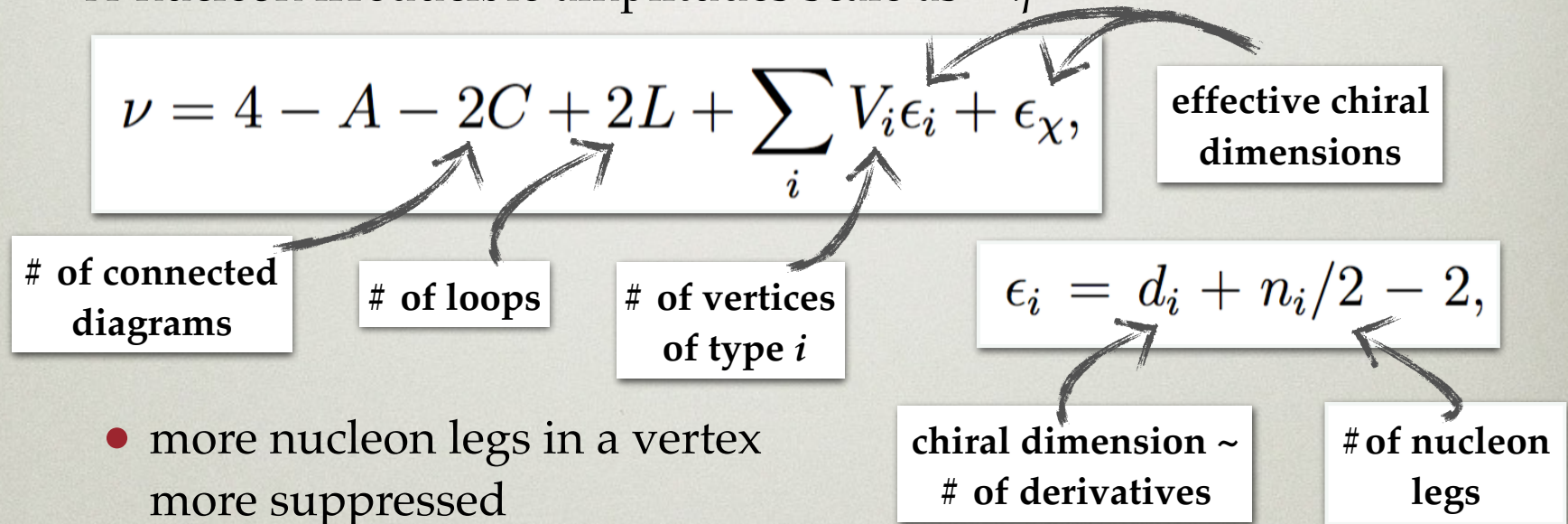
- assumption in the formalism for nuclear response functions
 - DM scatters on single nucleon
- how justified is this assumption?
 - how large are contributions from DM coupling to four-nucleon operators
- can be addressed using
 - Heavy Baryon Chiral Perturbation Theory (HBChPT)
 - ChEFT of nuclear forces
 - proton and neutron treated as heavy, $m_{p,n} \gg q \sim 200 \text{ MeV}$



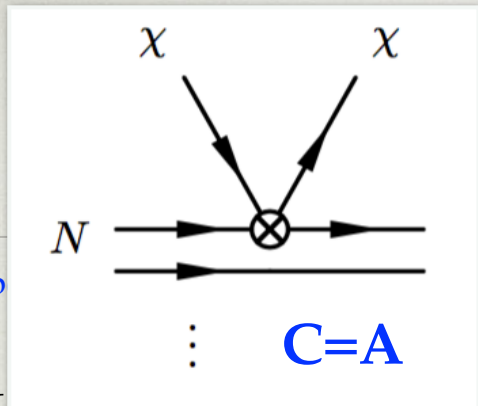
HBChPT counting

Weinberg, NPB363, 3 (1991); Kaplan, Savage, Wise, nucl-th/9605002; Cirigliano, Graesser, Ovanesyan, 1205.2695

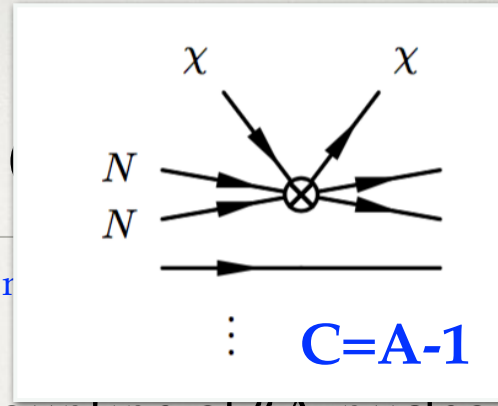
- HBChPT allows for consistent counting of “A-nucleon potentials”
 - expansion in $q/\Lambda_{\text{ChEFT}} \sim q/m_{p,n} \sim 0.3$
- A-nucleon irreducible amplitudes scale as $\sim q^\nu$



- more nucleon legs in a vertex more suppressed
- gives scaling for LO and NLO potentials



hPT



Weinb

, Savage, Wise, r

essner, Ovanesyan, 1205.2695

- FIDELITY allows for consistent counting of “A-nucleon potentials”
 - expansion in $q/\Lambda_{\text{ChEFT}} \sim q/m_{p,n} \sim 0.3$
- A-nucleon irreducible amplitudes scale as $\sim q^\nu$

$$\nu = 4 - A - 2C + 2L + \sum_i V_i \epsilon_i + \epsilon_\chi,$$

effective chiral dimensions

of connected diagrams

of loops

of vertices of type i

$$\epsilon_i = d_i + n_i/2 - 2,$$

chiral dimension ~ # of derivatives

of nucleon legs

- more nucleon legs in a vertex more suppressed
- gives scaling for LO and NLO potentials

A COMPLICATION

- the external currents are due to nonrelativistic fermions (WIMPs)
- need to match on Heavy DM Effective Theory (HDMET)
 - expansion in $1/m_\chi$
 - similar to HQET for heavy quarks
 - matching trivial if one works to tree level
- after contracting with hadronic currents leading terms in chiral counting vanish for $J_\chi^V \cdot \tilde{J}_q^A, J_\chi^V \cdot \tilde{J}_q^A$
- the J_χ^P starts at $1/m_\chi$

$$J_\chi^V \cdot \tilde{J}_q^V \sim J_\chi^S \tilde{J}^G \sim (\bar{\chi}_v \chi_v) (\bar{N} N),$$

$$J_\chi^A \cdot \tilde{J}_q^A \sim (\bar{\chi}_v S_\chi \chi_v) \cdot (\bar{N} S_N N),$$

$$J_\chi^A \cdot \tilde{J}_q^V \sim J_\chi^P \tilde{J}^G \sim (\bar{\chi}_v \partial \cdot S_\chi \chi_v) (\bar{N} N),$$

$$J_\chi^V \cdot \tilde{J}_q^A \sim J_\chi^S \tilde{J}^\theta \sim (\bar{\chi}_v \chi_v) (\bar{N} \partial \cdot S_N N),$$

$$J_\chi^S \tilde{J}_q^S \sim m_q (\bar{\chi}_v \chi_v) (\bar{N} N), \quad J_\chi^S \tilde{J}_q^P \sim m_q (\bar{\chi}_v \chi_v) (\bar{N} N) \pi, \quad J_\chi^P \tilde{J}^\theta \sim (\bar{\chi}_v \partial \cdot S_\chi \chi_v) (\bar{N} \partial \cdot S_N N),$$

$$J_\chi^P \tilde{J}_q^S \sim (\bar{\chi}_v \partial \cdot S_\chi \chi_v) m_q (\bar{N} N),$$

$$J_\chi^P \tilde{J}_q^P \sim (\bar{\chi}_v \partial \cdot S_\chi \chi_v) m_q (\bar{N} N) \pi,$$

NUCLEAR RESPONSE

- for nuclear response we use the formalism of Anand, Fitzpatrick, Haxton
- match onto ops. with NR nucleons
- only this subset of NR operators is generated
- xsec prop. to

$$\mathcal{O}_1^N = \mathbb{1}_\chi \mathbb{1}_N,$$

$$\mathcal{O}_3^N = \mathbb{1}_\chi \vec{S}_N \cdot \left(\vec{v}_\perp \times \frac{i\vec{q}}{m_N} \right),$$

$$\mathcal{O}_5^N = \vec{S}_\chi \cdot \left(\vec{v}_\perp \times \frac{i\vec{q}}{m_N} \right) \mathbb{1}_N,$$

$$\mathcal{O}_7^N = \mathbb{1}_\chi (\vec{S}_N \cdot \vec{v}_\perp),$$

$$\mathcal{O}_9^N = \vec{S}_\chi \cdot \left(\frac{i\vec{q}}{m_N} \times \vec{S}_N \right),$$

$$\mathcal{O}_{11}^N = - \left(\vec{S}_\chi \cdot \frac{i\vec{q}}{m_N} \right) \mathbb{1}_N,$$

$$\mathcal{O}_2^N = (v_\perp)^2 \mathbb{1}_\chi \mathbb{1}_N,$$

$$\mathcal{O}_4^N = \vec{S}_\chi \cdot \vec{S}_N,$$

$$\mathcal{O}_6^N = \left(\vec{S}_\chi \cdot \frac{\vec{q}}{m_N} \right) \left(\vec{S}_N \cdot \frac{\vec{q}}{m_N} \right),$$

$$\mathcal{O}_8^N = (\vec{S}_\chi \cdot \vec{v}_\perp) \mathbb{1}_N,$$

$$\mathcal{O}_{10}^N = -\mathbb{1}_\chi \left(\vec{S}_N \cdot \frac{i\vec{q}}{m_N} \right),$$

$$\mathcal{O}_{12}^N = \vec{S}_\chi \cdot \left(\vec{S}_N \times \vec{v}_\perp \right),$$

Wilson coeffs. in R_i

$$\vec{v}_T^\perp = \vec{v} - \vec{q}/(2\mu_{\chi A}),$$

$$\frac{1}{2J_\chi + 1} \frac{1}{2J_A + 1} \sum_{\text{spins}} |\mathcal{M}|_{\text{nucleus, NR}}^2 = \frac{|\mathcal{M}|^2}{(4m_\chi m_A)^2} =$$

$$\frac{4\pi}{2J_A + 1} \sum_{\tau=0,1} \sum_{\tau'=0,1} \left\{ \left[R_M^{\tau\tau'} W_M^{\tau\tau'}(y) + R_{\Sigma''}^{\tau\tau'} W_{\Sigma''}^{\tau\tau'}(y) + R_{\Sigma'}^{\tau\tau'} W_{\Sigma'}^{\tau\tau'}(y) \right] \right.$$

W_i are nuclear response functions

$$R_M^{\tau\tau'} = (4m_\chi m_N)^2 \left[c_{\text{NR},1}^\tau c_{\text{NR},1}^{\tau'} + \frac{1}{4} \left(\frac{\vec{q}^2}{m_N^2} \vec{v}_T^{\perp 2} c_{\text{NR},5}^\tau c_{\text{NR},5}^{\tau'} \right. \right.$$

$$\left. \left. + \vec{v}_T^{\perp 2} c_{\text{NR},8}^\tau c_{\text{NR},8}^{\tau'} + \frac{\vec{q}^2}{m_N^2} c_{\text{NR},11}^\tau c_{\text{NR},11}^{\tau'} \right) \right],$$

$$+ \frac{\vec{q}^2}{m_N^2} \left[R_\Delta^{\tau\tau'} W_\Delta^{\tau\tau'}(y) + R_{\Delta\Sigma'}^{\tau\tau'} W_{\Delta\Sigma'}^{\tau\tau'}(y) \right] \left. \right\},$$

NUCLEAR RESPONSE FUNCTIONS

- $W_M(q)$: from vector operator
 - in $q \rightarrow 0$ limit counts nucleons \Rightarrow spin-indep. (coherent) scattering

- $W_{\Sigma''}$ and $W_{\Sigma'}$: longit. and transverse axial ops.

- related to conventional spin form factors

$$S_{00,11} = \frac{1}{4\pi} \sum_{\text{spins}} |\langle \vec{S}_p \pm \vec{S}_n \rangle|^2,$$

$$W_{\Sigma'}^{\tau\tau'} + W_{\Sigma''}^{\tau\tau'} = S_{\tau\tau'}, \quad \tau, \tau' = 0, 1.$$

$$S_{01} = \frac{1}{2\pi} \sum_{\text{spins}} (|\langle \vec{S}_p \rangle|^2 - |\langle \vec{S}_n \rangle|^2),$$

- measure the nucleon spin content of the nucleus
- W_{Δ} : vector transverse magnetic operators
 - nucleon angular momentum content of the nucleus

- (very) rough scaling:

$$W_M \sim \mathcal{O}(A^2), \quad W_{\Sigma'}, W_{\Sigma''}, W_{\Delta}, W_{\Delta\Sigma'} \sim \mathcal{O}(1)$$

- in general three more response functions

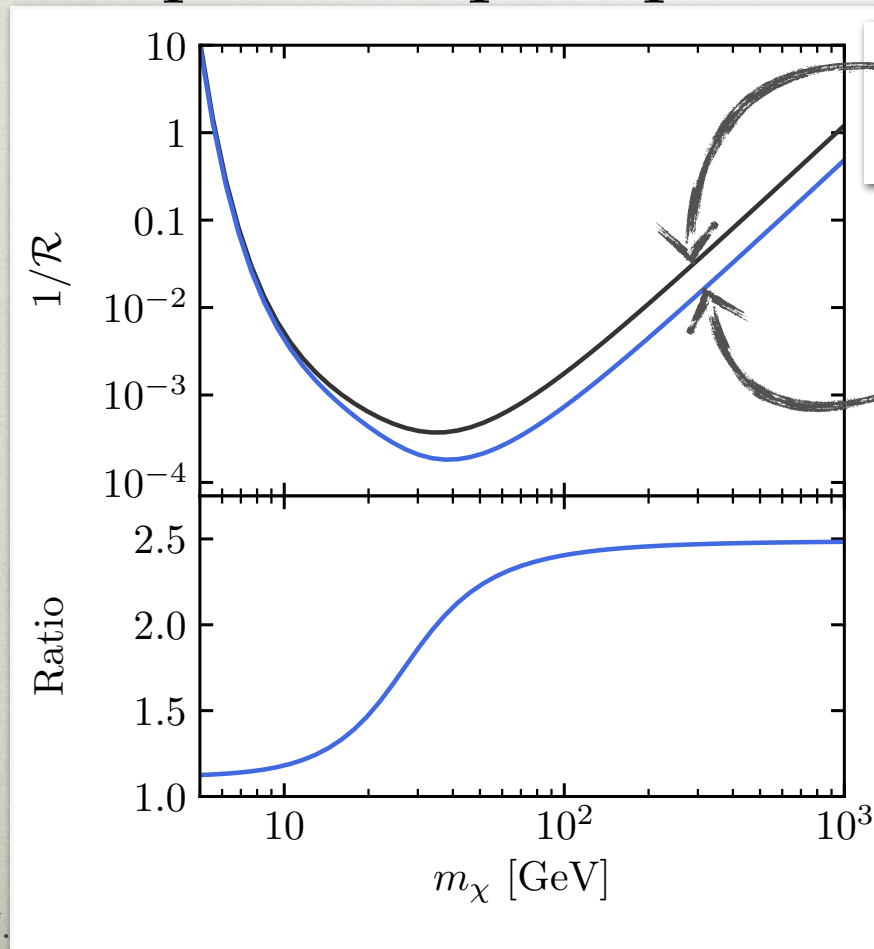
- these not generated to the order we work

PSEUDOSCALAR- PSEUDOSCALAR

- PS-PS operator $C_{8u} = -C_{8d} = -C_{8s}$

$$Q_{8,q}^{(7)} = m_q (\bar{\chi} \gamma_5 \chi) (\bar{q} \gamma_5 q)$$

- compare full pion pole with $q \rightarrow 0$ limit



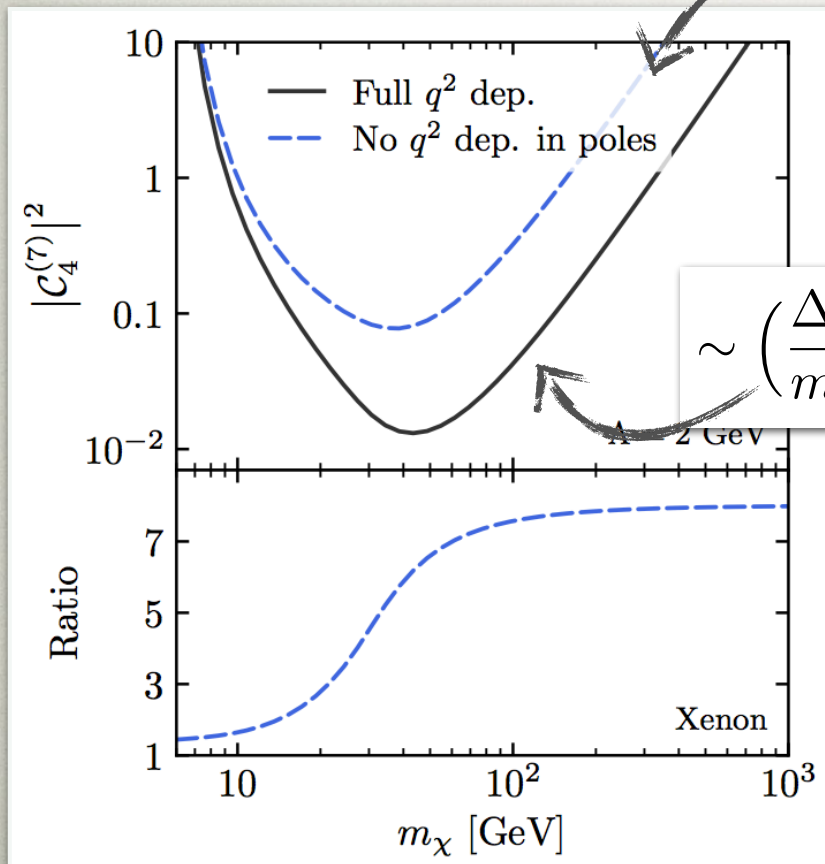
$$\sim \frac{\Delta q}{m_\chi} C_{8,q}^{(7)} \frac{m_\pi^2}{m_\pi^2 + \vec{q}^2} (\vec{S}_\chi \cdot \vec{q}) (\vec{S}_N \cdot \vec{q})$$

$$\sim \frac{\Delta q}{m_\chi} C_{8,q}^{(7)} (\vec{S}_\chi \cdot \vec{q}) (\vec{S}_N \cdot \vec{q})$$

CP-ODD GLUONIC OPERATOR

- PSxCP-odd gluonic operator
- compare with $q \rightarrow 0$ limit

$$Q_4^{(7)} = \frac{\alpha_s}{8\pi} (\bar{\chi} i \gamma_5 \chi) G^{a\mu\nu} \tilde{G}_{\mu\nu}^a$$



$$\sim \frac{\Delta q}{m_q} (\vec{S}_N \cdot \vec{q}) (\vec{S}_\chi \cdot \vec{q})$$

$$\sim \left(\frac{\Delta q}{m_q} + \left(\frac{1}{m_u} - \frac{1}{m_d} \right) \frac{(\Delta u - \Delta d) \vec{q}^2}{m_\pi^2 + \vec{q}^2} \right) (\vec{S}_N \cdot \vec{q}) (\vec{S}_\chi \cdot \vec{q})$$

ALL OPERATORS?

- do we need all the operators?
 - general dim 5 and 6 EFT require for LO description:

$$\mathcal{O}_1^N = \mathbb{1}_\chi \mathbb{1}_N,$$

$$\mathcal{O}_3^N = \mathbb{1}_\chi \vec{S}_N \cdot \left(\vec{v}_\perp \times \frac{i\vec{q}}{m_N} \right),$$

$$\mathcal{O}_5^N = \vec{S}_\chi \cdot \left(\vec{v}_\perp \times \frac{i\vec{q}}{m_N} \right) \mathbb{1}_N,$$

$$\mathcal{O}_7^N = \mathbb{1}_\chi (\vec{S}_N \cdot \vec{v}_\perp),$$

$$\mathcal{O}_9^N = \vec{S}_\chi \cdot \left(\frac{i\vec{q}}{m_N} \times \vec{S}_N \right),$$

$$\mathcal{O}_{11}^N = - \left(\vec{S}_\chi \cdot \frac{i\vec{q}}{m_N} \right) \mathbb{1}_N,$$

$$\mathcal{O}_2^N = (v_\perp)^2 \mathbb{1}_\chi \mathbb{1}_N,$$

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$$\mathcal{O}_8^N = (\vec{S}_\chi \cdot \vec{v}_\perp) \mathbb{1}_N,$$

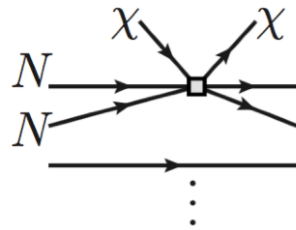
$$\mathcal{O}_{10}^N = -\mathbb{1}_\chi \left(\vec{S}_N \cdot \frac{i\vec{q}}{m_N} \right),$$

$$\mathcal{O}_{12}^N = \vec{S}_\chi \cdot \left(\vec{S}_N \times \vec{v}_\perp \right),$$

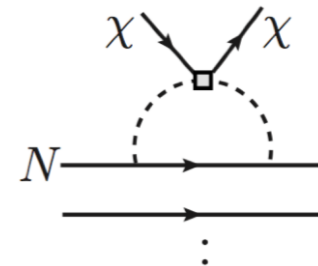
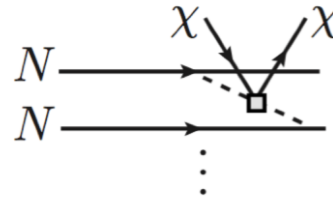
- using the rough scalings $A \sim 100$, $q/m_N \sim 0.1$, $v_T \sim 10^{-3}$
- allow for fine-tuning to get VxA, AxV structures
 - then 2 derivative ops. can be LO
- due to pion poles 2 derivative ops. can be of LO size

NLO CORRECTIONS

short distance corr.



long distance corr.



loop correct.

sample higher
order corrections

- SD always scales as $\sim q^{\nu_{\text{LO}}+3}$
- only for $J_{\chi}^A \cdot \tilde{J}_q^V$, $J_{\chi}^S \tilde{J}_q^S$, $J_{\chi}^P \tilde{J}_q^S$ and $J_{\chi}^V \cdot \tilde{J}_q^A$ LD parametrically larger,
 - $\sim q^{\nu_{\text{LO}}+1}$
 - $\sim q^{\nu_{\text{LO}}+2}$
- we work to LO, results have relative $O(q/\Lambda_{\text{ChEFT}}) \sim 30\%$ accuracy
 - at this order: DM couples only to single nucleon currents
- at $O(q)$ LD DM interaction with two nucleons, e.g., for $\bar{q}q$
 - calculable using HBChPT, expected size $\sim (q/\Lambda_{\text{ChEFT}}) \sim 30\%$
- short distance DM-2nucleon interaction at $O(q^3)$ (size: $\sim \text{few}\%$)