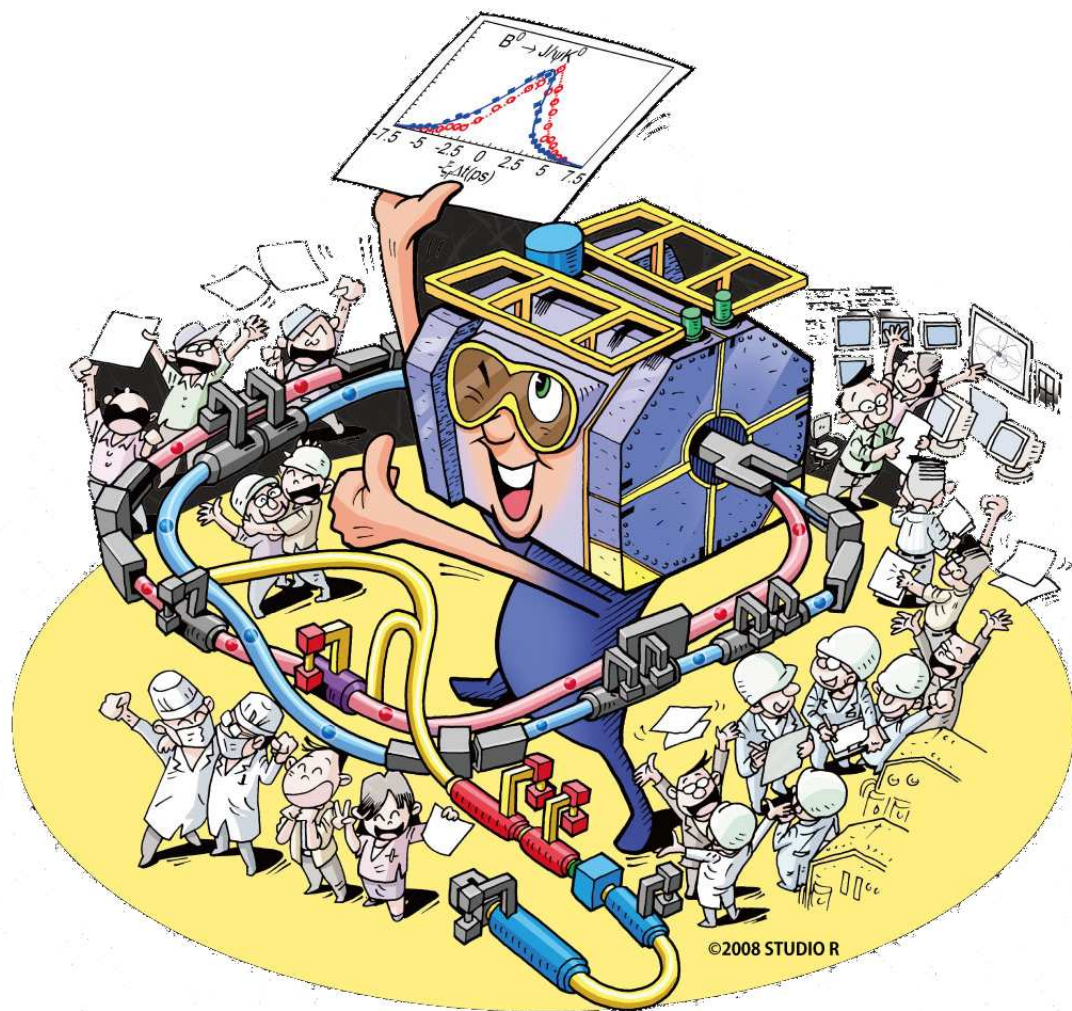


# $A_{CP}(K\pi)$ , $A_{FB}(K^*\ell^+\ell^-)$ and $D^0$ mixing as probe of 4th Generation

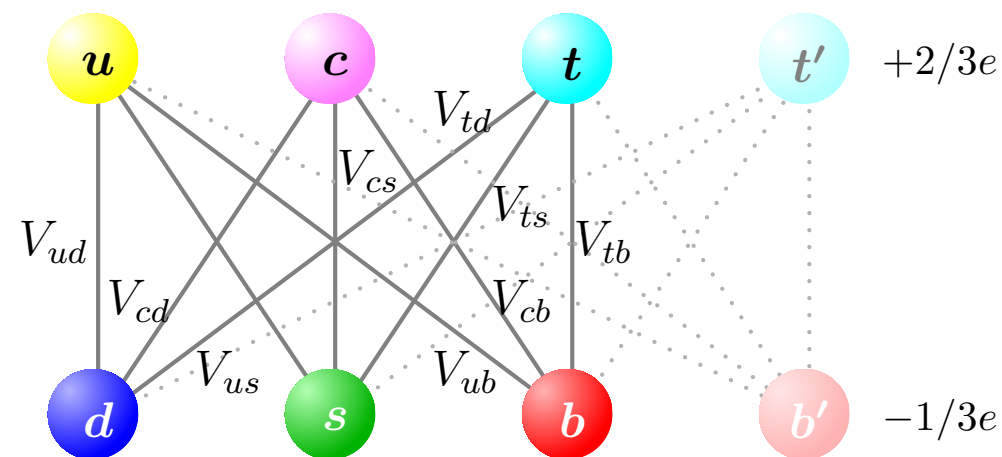
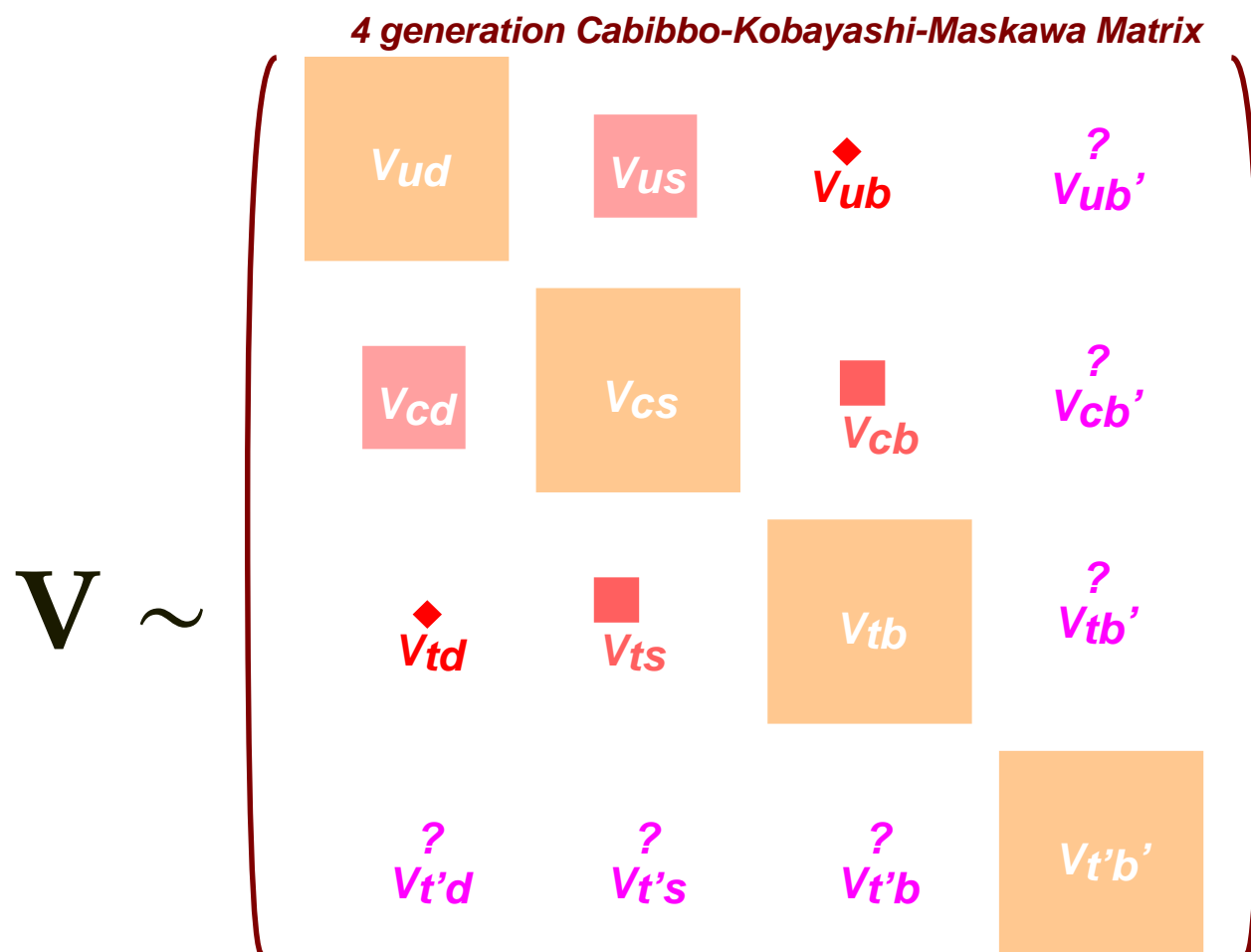


Mikihiro Nakao  
for the Belle collaboration

KEK, IPNS  
mikihiro.nakao@kek.jp

*at the Second Workshop on  
Beyond 3 Generation SM  
2009.1.15, Taipei*

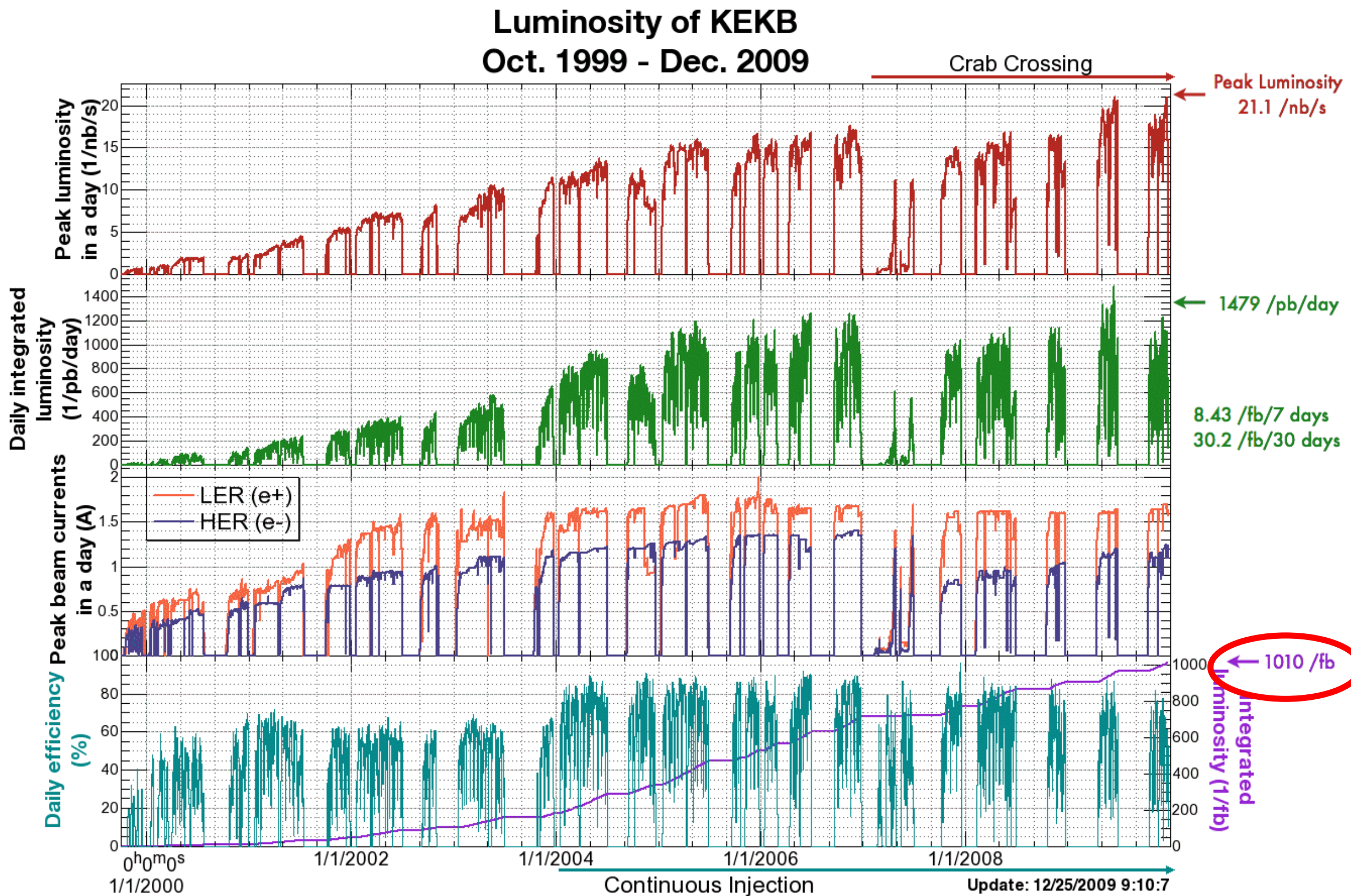
# 4th generation and Belle physics



- Unitarity triangle does not close
- Many effects on loop processes ( $A_{CP}(K\pi)$ ,  $A_{FB}(K^*\ell^+\ell^-)$ , ...)
- Large contributions to charm decays ( $D^0$  mixing, CPV)

# Belle/KEKB history — $1 \text{ ab}^{-1}$ 😊

$A_{CP}(K\pi)$ ,  $A_{FB}(K^* \ell^+ \ell^-)$  and  $D^0$  mixing as probe of 4th Generation — Mikihiko Nakao — p.3



772M  $B\bar{B}$  for  $B$  physics, all  $1000 \text{ fb}^{-1}$  for  $D$  mixing, grand reprocess in progress



# $A_{CP}(K\pi)$ and $K\pi$ puzzle

(Belle S-W Lin *et al.*,  
Nature 452, 332 (2008) 535 MB $\bar{B}$ )

$$A_{CP} = \frac{N(\bar{B} \rightarrow \bar{f}) - N(B \rightarrow f)}{N(\bar{B} \rightarrow \bar{f}) + N(B \rightarrow f)}$$

$$A_{CP}(K^+\pi^-) = -0.094 \pm 0.018 \pm 0.008$$

$$A_{CP}(K^+\pi^0) = +0.07 \pm 0.03 \pm 0.01$$

Differences:

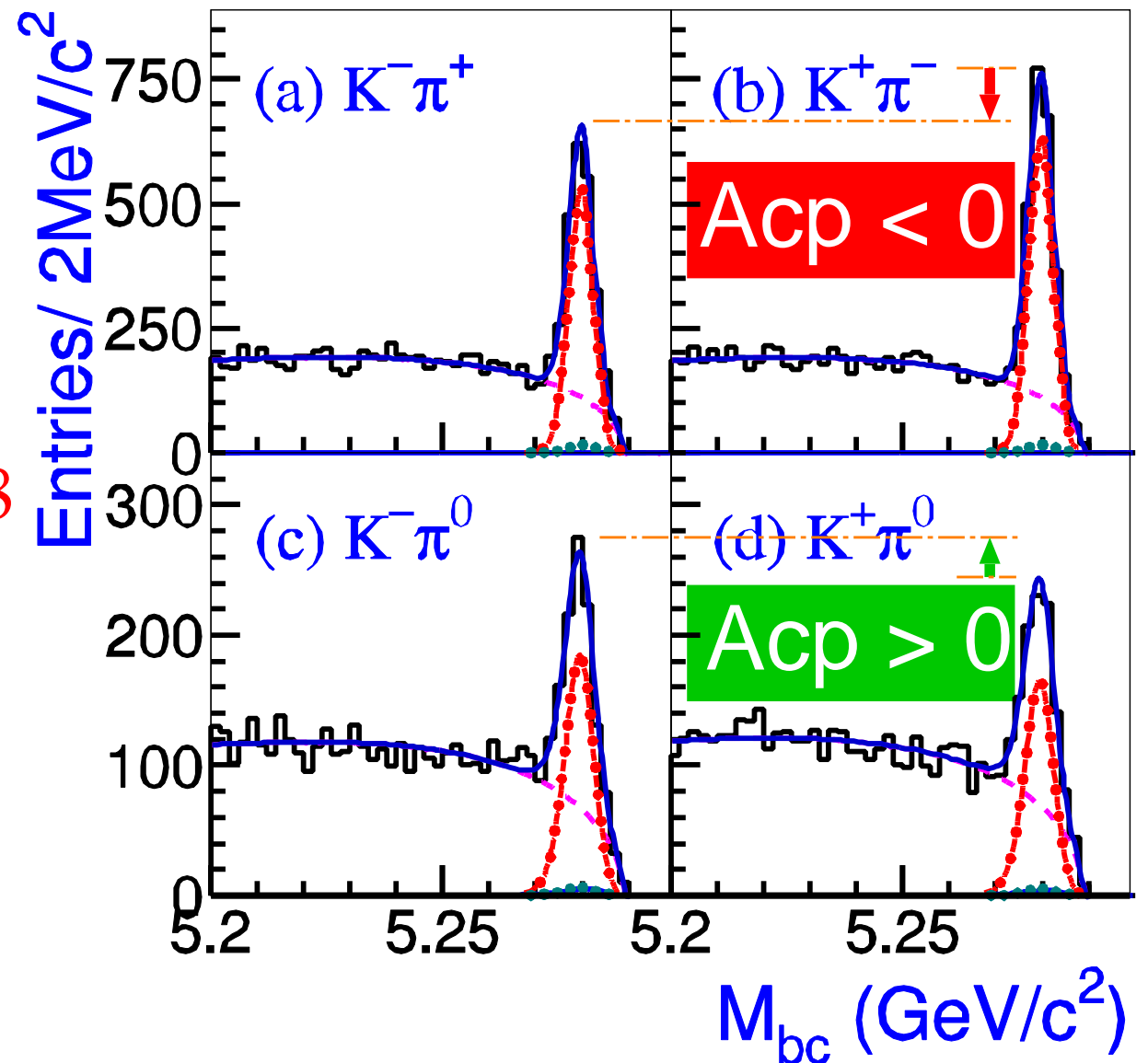
- Color suppressed diagram
- EW penguin diagram

Both are small in SM,  
the latter could be large in NP

Sum rule

$$\delta_{K\pi} =$$

$$A_{CP} \times \Gamma(K^+\pi^-) + A_{CP} \times \Gamma(K^0\pi^+) - 2A_{CP} \times \Gamma(K^+\pi^0) - 2A_{CP} \times \Gamma(K^0\pi^0)$$



# Branching fractions and $A_{CP}(B \rightarrow K^0 \pi^0)$

## Branching fraction measurements

(Belle PRL99,121601(2007) and  
Belle PRL98,181804(2007) 535MB $\bar{B}$ )

$$A_{CP}(K^0 \pi^+) = +0.03 \pm 0.03 \pm 0.01$$

$$\mathcal{B}(K^0 \pi^+) = (8.7 \pm 0.5 \pm 0.6) \times 10^{-6}$$

$$\mathcal{B}(K^+ \pi^-) = (19.9 \pm 0.4 \pm 0.8) \times 10^{-6}$$

$$\mathcal{B}(K^+ \pi^0) = (12.4 \pm 0.5 \pm 0.6) \times 10^{-6}$$

## $K^0 \pi^0$ mode requires time-dependent measurement

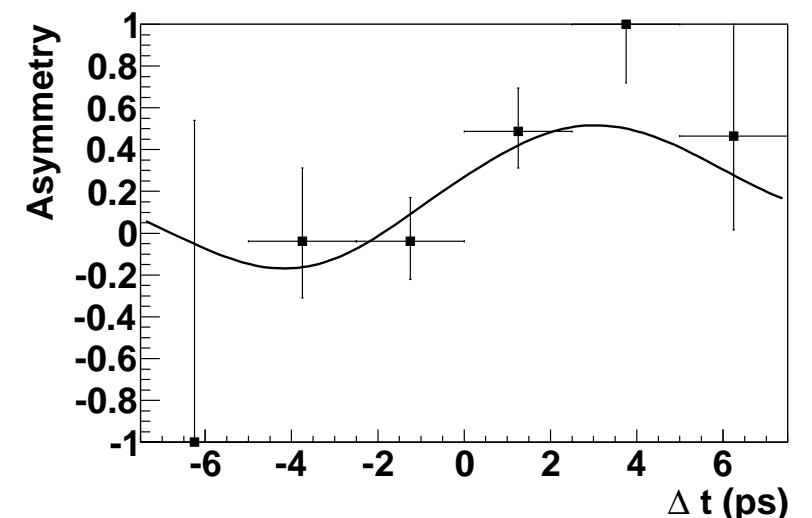
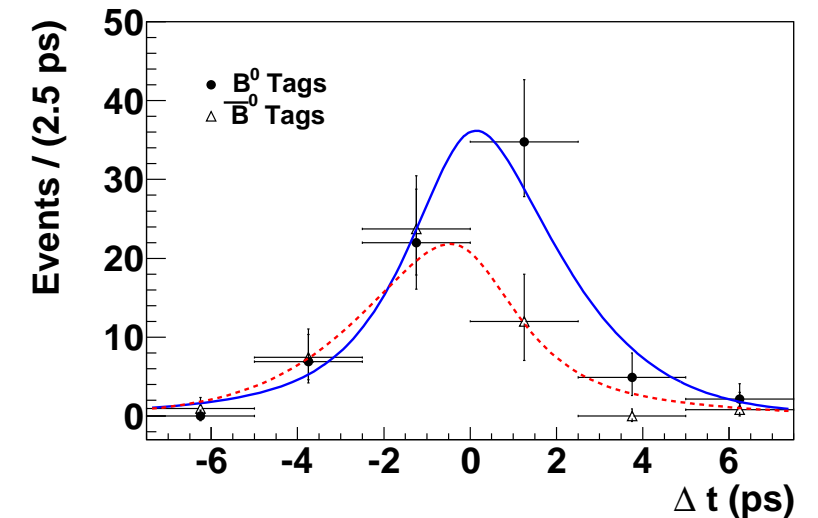
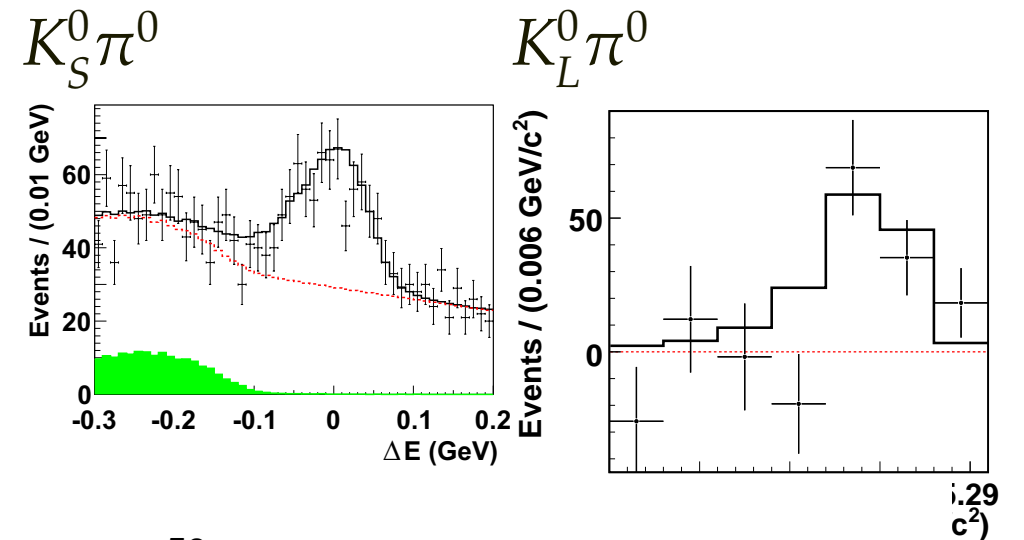
(Belle arxiv0809.4366(to appear in PRD), 657MB $\bar{B}$ )

$$A_{CP}(K^0 \pi^0) = +0.14 \pm 0.13 \pm 0.06$$

$$\mathcal{B}(K^0 \pi^0) = (8.7 \pm 0.5 \pm 0.6) \times 10^{-6}$$

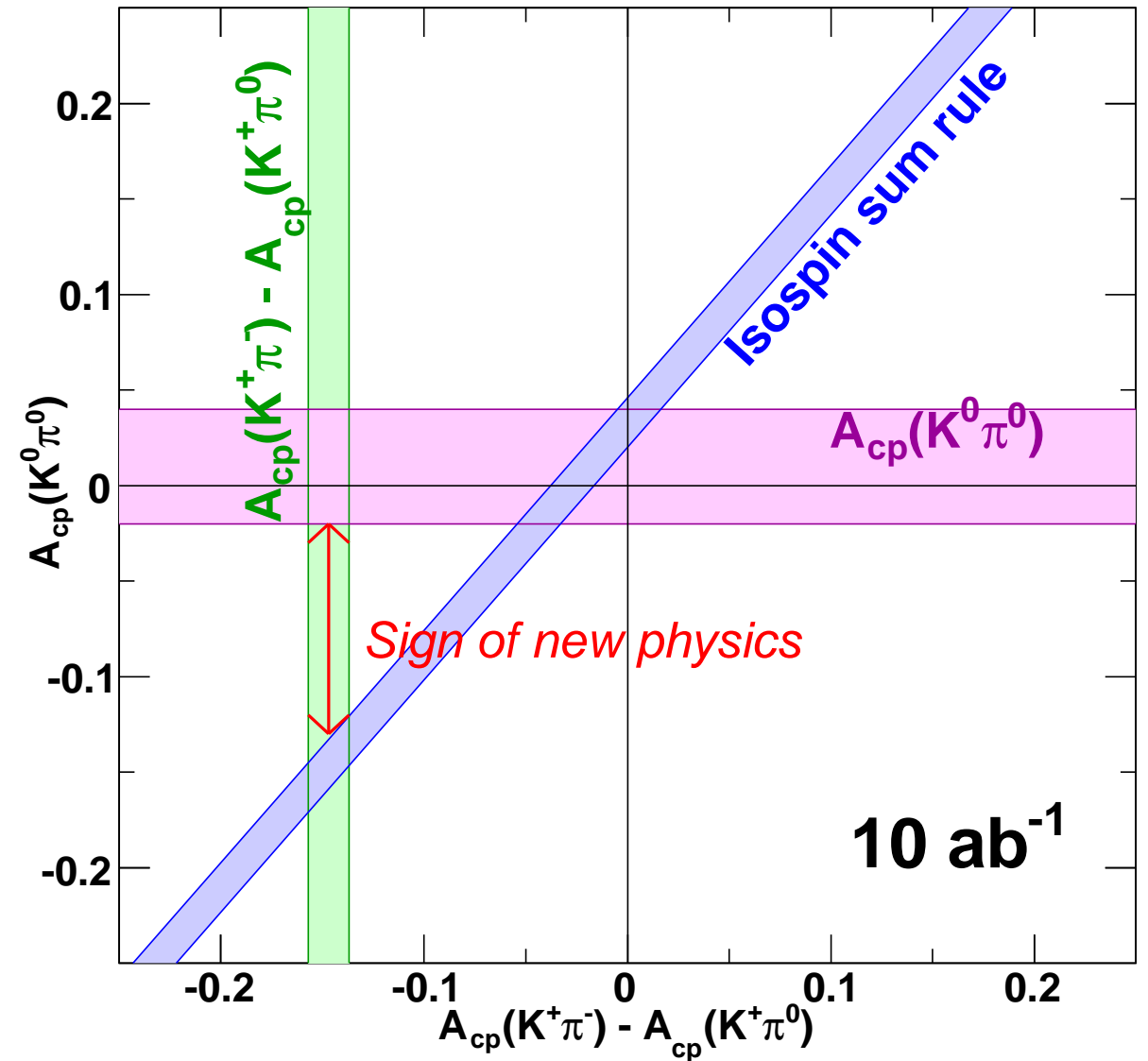
$$S(K^0 \pi^0) = +0.67 \pm 0.31 \pm 0.08$$

$A_{CP}(K^0 \pi^0)$  violates the sum rule by  $1.9 \sigma$   
(but BaBar's result is in a opposite direction...)



# $B \rightarrow K\pi$ prospects

- BF measurements are already systematics dominated
- $A_{CP}$  measurements will be systematics dominated with  $\sim 10 \text{ ab}^{-1}$



# $b \rightarrow s\ell^+\ell^-$

$\mathcal{B}(B \rightarrow X_s\gamma)$ ,  $A_{FB}(B \rightarrow K^*\ell^+\ell^-)$  and  $\mathcal{B}(B \rightarrow X_s\ell^+\ell^-)$  are direct probes of Wilson coefficients  $C_7$ ,  $C_9$  and  $C_{10}$  as functions of  $\hat{s}(= q^2/m_b^2)$

$$\mathcal{B}(B \rightarrow X_s\gamma) \propto |C_7|^2$$

$$A_{FB}(B \rightarrow K^*\ell^+\ell^-; \hat{s}) = -C_{10}\xi(\hat{s}) \left[ \text{Re}(C_9)F_1 + \frac{1}{\hat{s}}C_7F_2 \right]$$

$$\frac{d\Gamma(B \rightarrow X_s\ell^+\ell^-)}{d\hat{s}} = \left(\frac{\alpha_{\text{em}}}{4\pi}\right)^2 \frac{G_F^2 m_b^5 |V_{ts}^* V_{tb}|^2}{48\pi^3} (1 - \hat{s})^2 \times \left[ (1 + 2\hat{s}) (|C_9|^2 + |C_{10}|^2) + 4 \left(1 + \frac{2}{\hat{s}}\right) |C_7|^2 + 12\text{Re}(C_7C_9) \right] + \text{corr.}$$

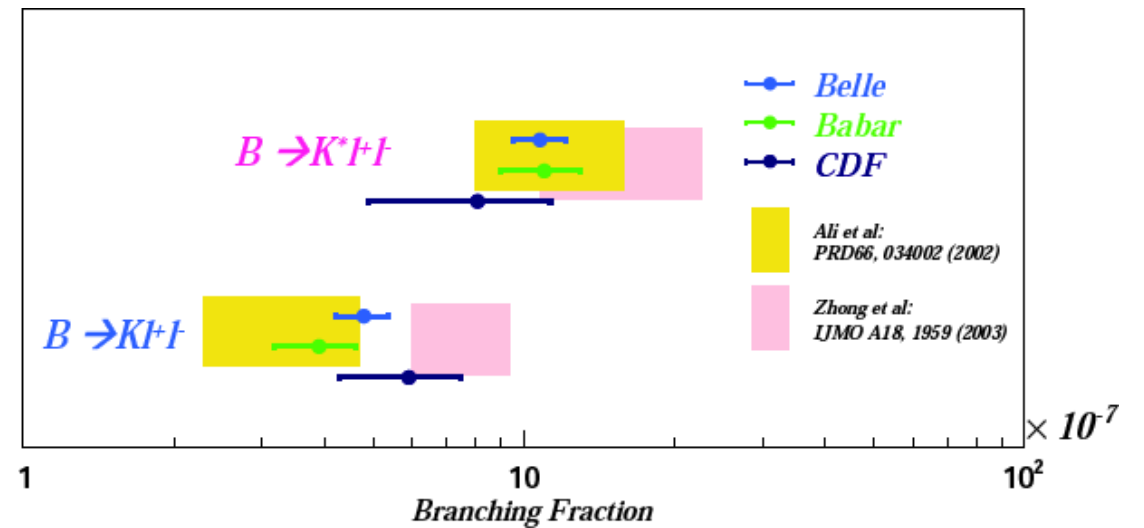
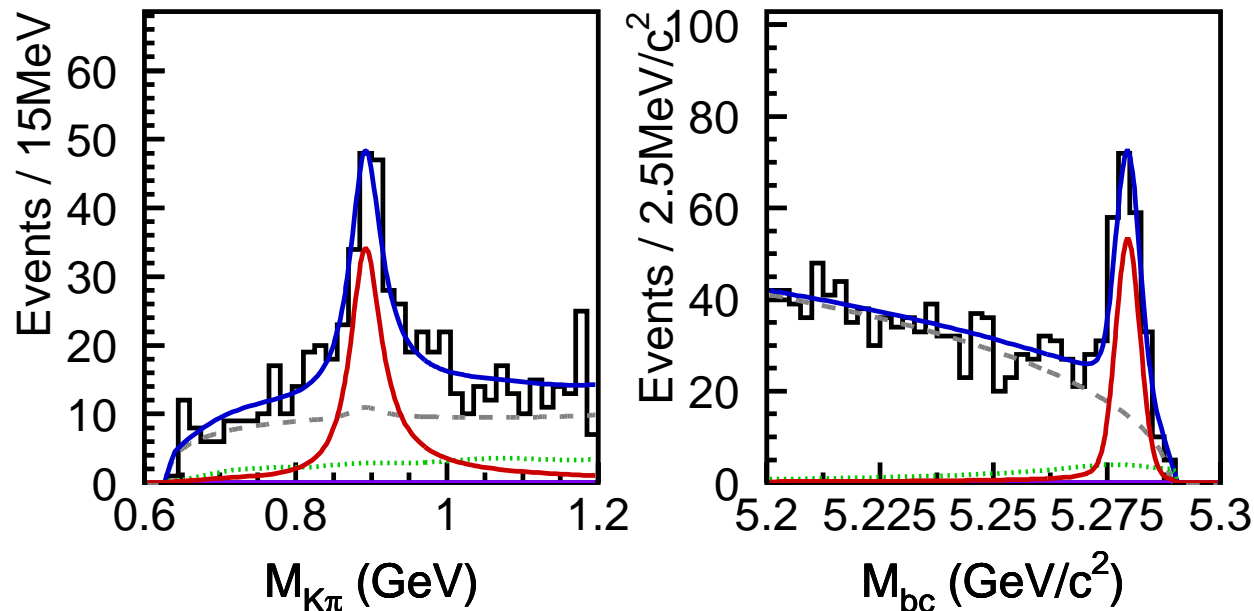
## Key features:

- Size of  $C_7$  from  $\mathcal{B}(B \rightarrow X_s\gamma)$
- Zero crossing of  $A_{FB}(B \rightarrow K^*\ell^+\ell^-)$
- $C_7C_9$  term in  $\mathcal{B}(B \rightarrow X_s\ell^+\ell^-)$

# $B \rightarrow K^* \ell^+ \ell^-$

(Belle J-T Wei *et al.*, PRL 103, 171801 (2009), 657M  $B\bar{B}$ )

- Very small branching fraction  $\sim 10^{-6}$  or less  
But branching fraction is not very predictive



(SM suffers from form factor uncertainties)

- Various ratios (Forward-backward asymmetry,  $F_L$ , CPV, isospin, lepton flavor, etc)

- Three-body decay:

➔ Observables as functions of  $q^2$  ( $q^2 = m_{\ell^+ \ell^-}^2$ )



# $A_{FB}(B \rightarrow K^* \ell^+ \ell^-)$

## Angular distributions to extract FB asymmetries

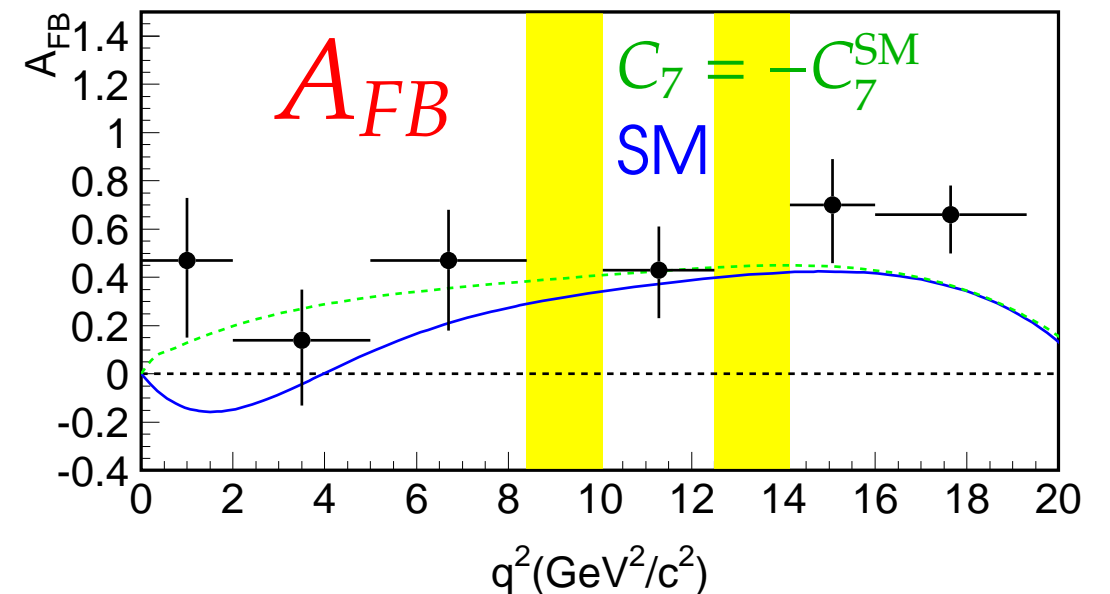
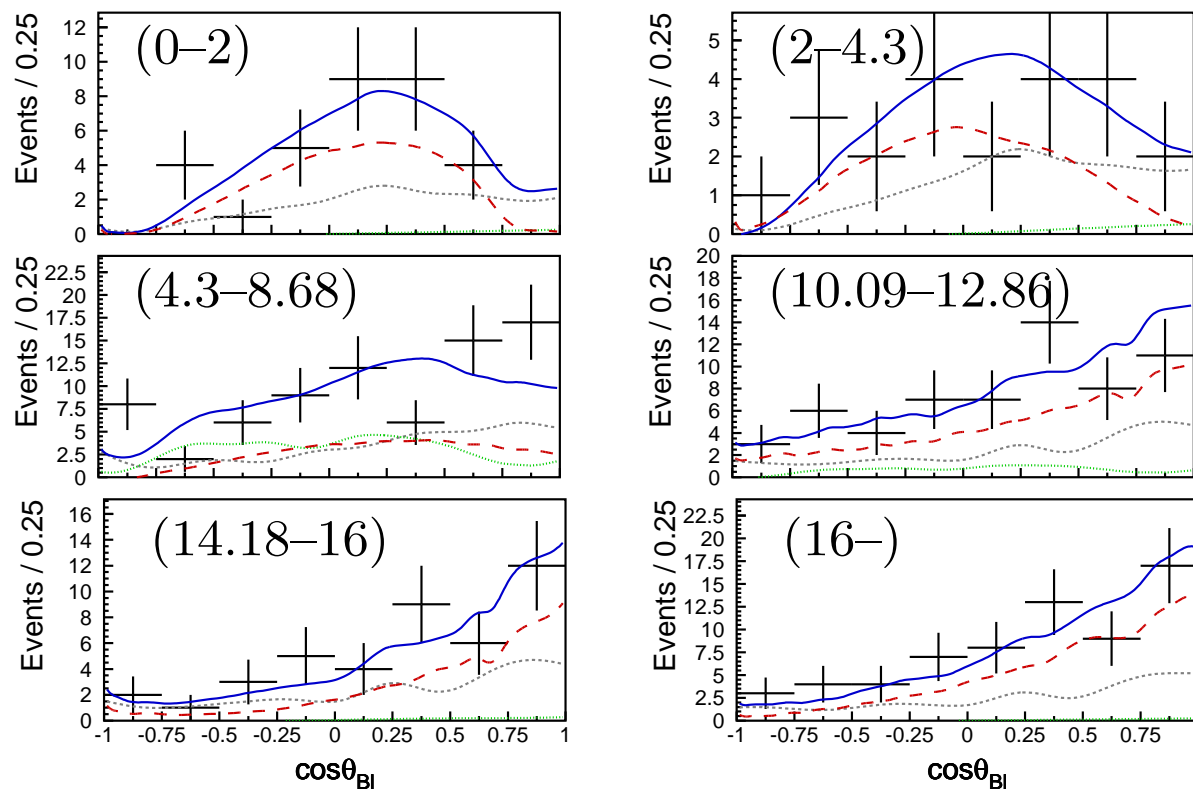
$K^*$  longitudinal polarization  $F_L$  from kaon angle  $\theta_K$

$$\frac{3}{2}F_L \cos^2 \theta_K + \frac{3}{4}(1 - F_L)(1 - \cos^2 \theta_K)$$

Forward-backward asymmetry  $A_{FB}$  from lepton angle  $\theta_\ell$

$$\frac{3}{4}F_L(1 - \cos^2 \theta_\ell) + \frac{3}{8}(1 - F_L)(1 + \cos^2 \theta_\ell) + A_{FB} \cos \theta_\ell$$

$\cos \theta_\ell$



- Opposite sign  $C_7$  is favored
- $2.7 \sigma$  deviation from the SM

# $B \rightarrow X_s \ell^+ \ell^-$ (Belle 657M $B\bar{B}$ , preliminary)

- Sum-of-exclusive analysis

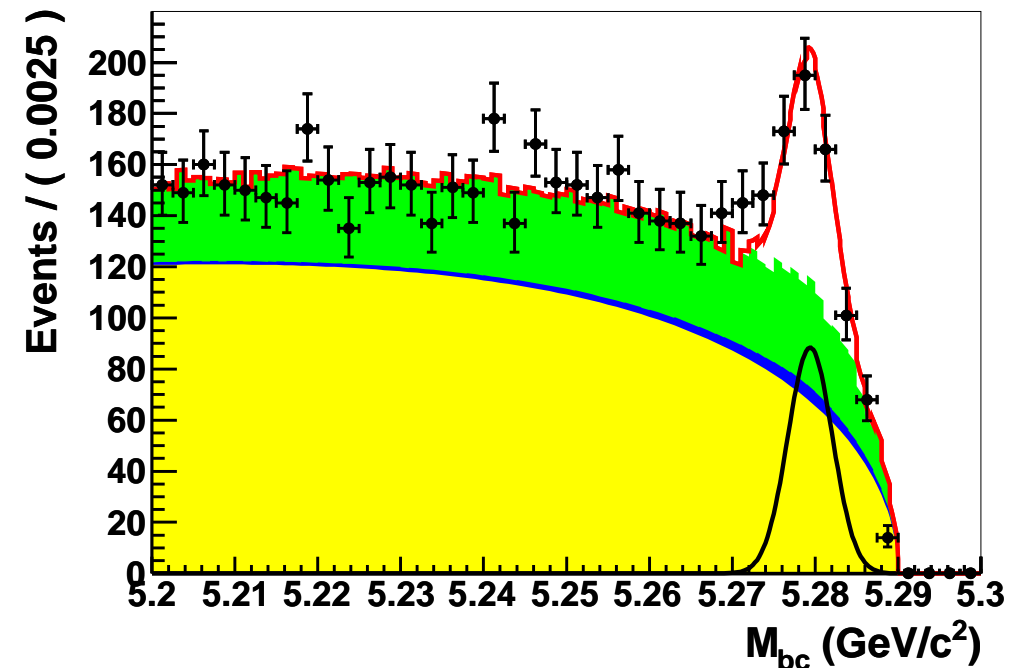
$$X_s = K + n\pi \quad (n = 0..4)$$

(sum of  $K\ell^+\ell^-$ ,  $K^*\ell^+\ell^-$ , high-mass  $X_s\ell^+\ell^-$ )

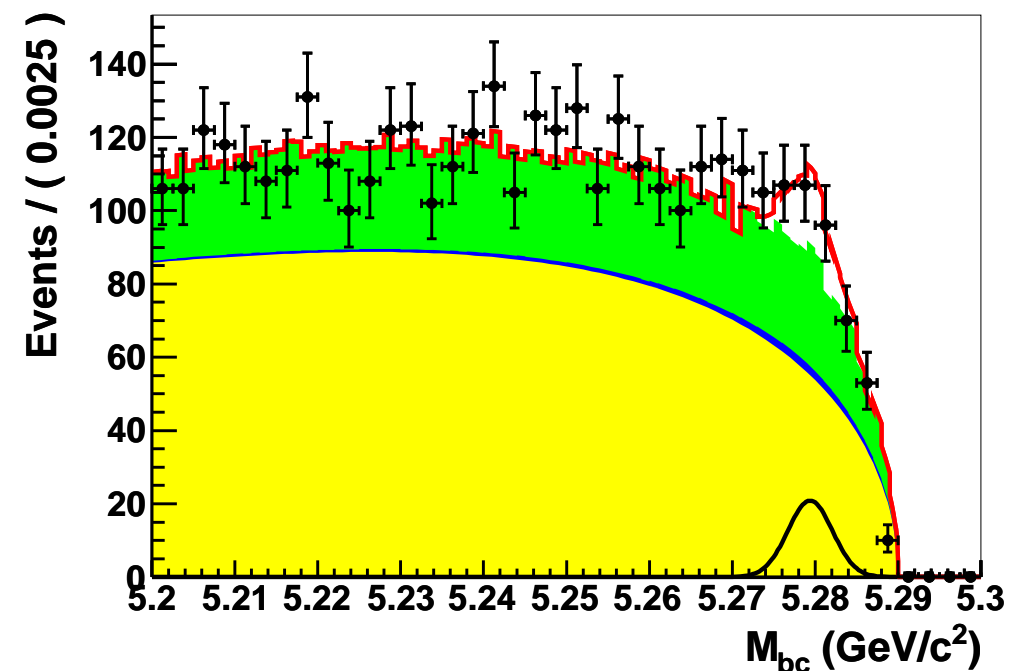
Updated with 4.5 times data  
and analysis improvements

- Backgrounds

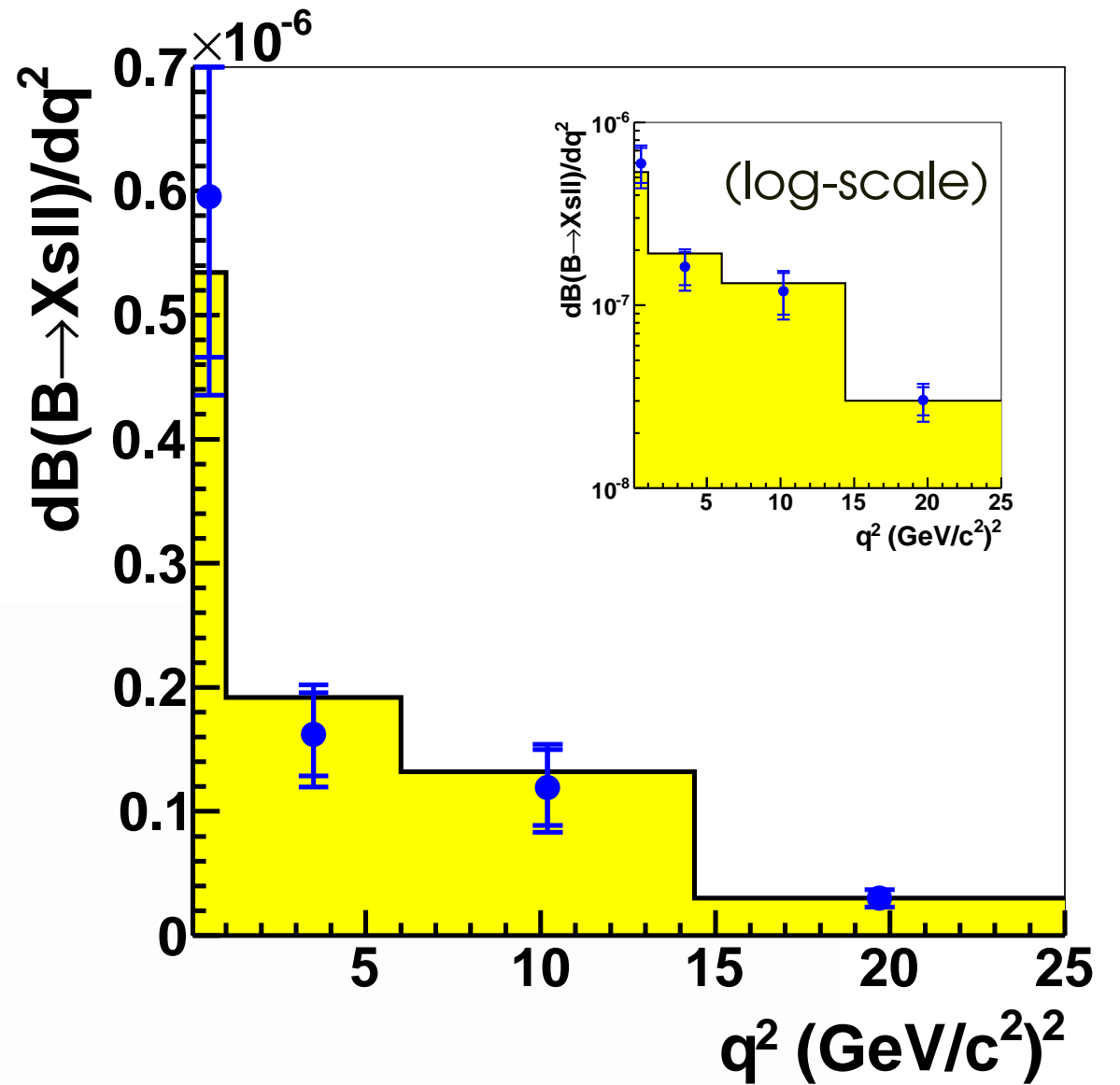
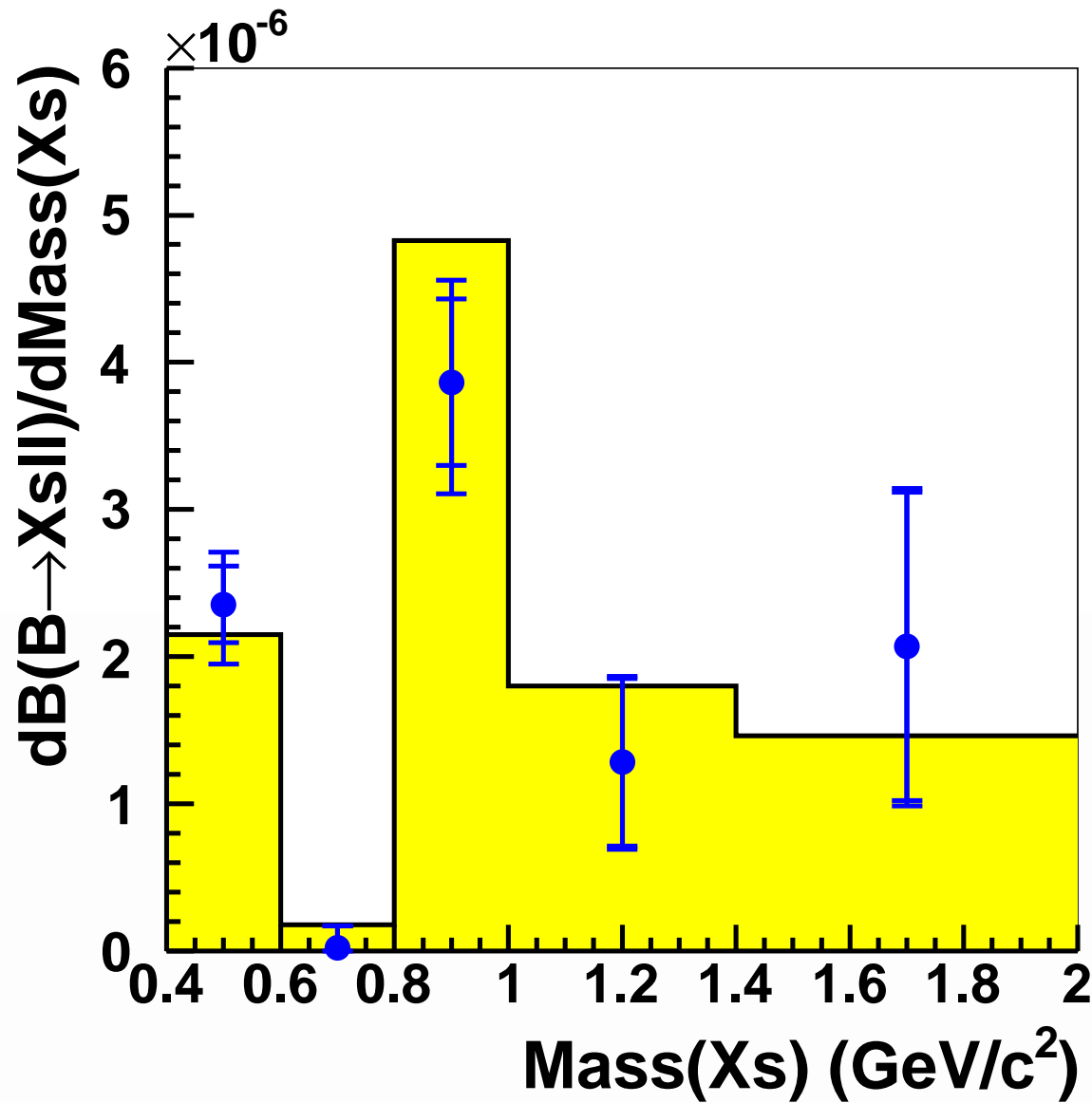
- Semileptonic  $B$  decays, continuum  $q\bar{q}$
- Leakage from  $J/\psi$  and  $\psi'$  veto
- $B \rightarrow X_s \pi^+ \pi^-$  (double mis-id)
- $\psi(3770)$ ,  $\psi(4040)$ ,  $\psi(4160) \rightarrow \ell^+ \ell^-$
- $B \rightarrow X_c(l\nu) \rightarrow X_s \ell \nu$  (single mis-id + random slow  $\pi$  replacing  $\nu$ )



10 $\sigma$  signal for entire  $M(X_s)$



3.0 $\sigma$  signal for  $M(X_s) > 1.0$  GeV



$$\mathcal{B}(B \rightarrow X_s \ell^+ \ell^-) = (3.33 \pm 0.80^{+0.19}_{-0.24}) \times 10^{-6}$$

$[q^2 > 0.2 \text{ GeV}^2/c^2, \text{ extrapolated for } J/\psi, \psi', \text{ and } M(X_s) > 2.0 \text{ GeV}]$

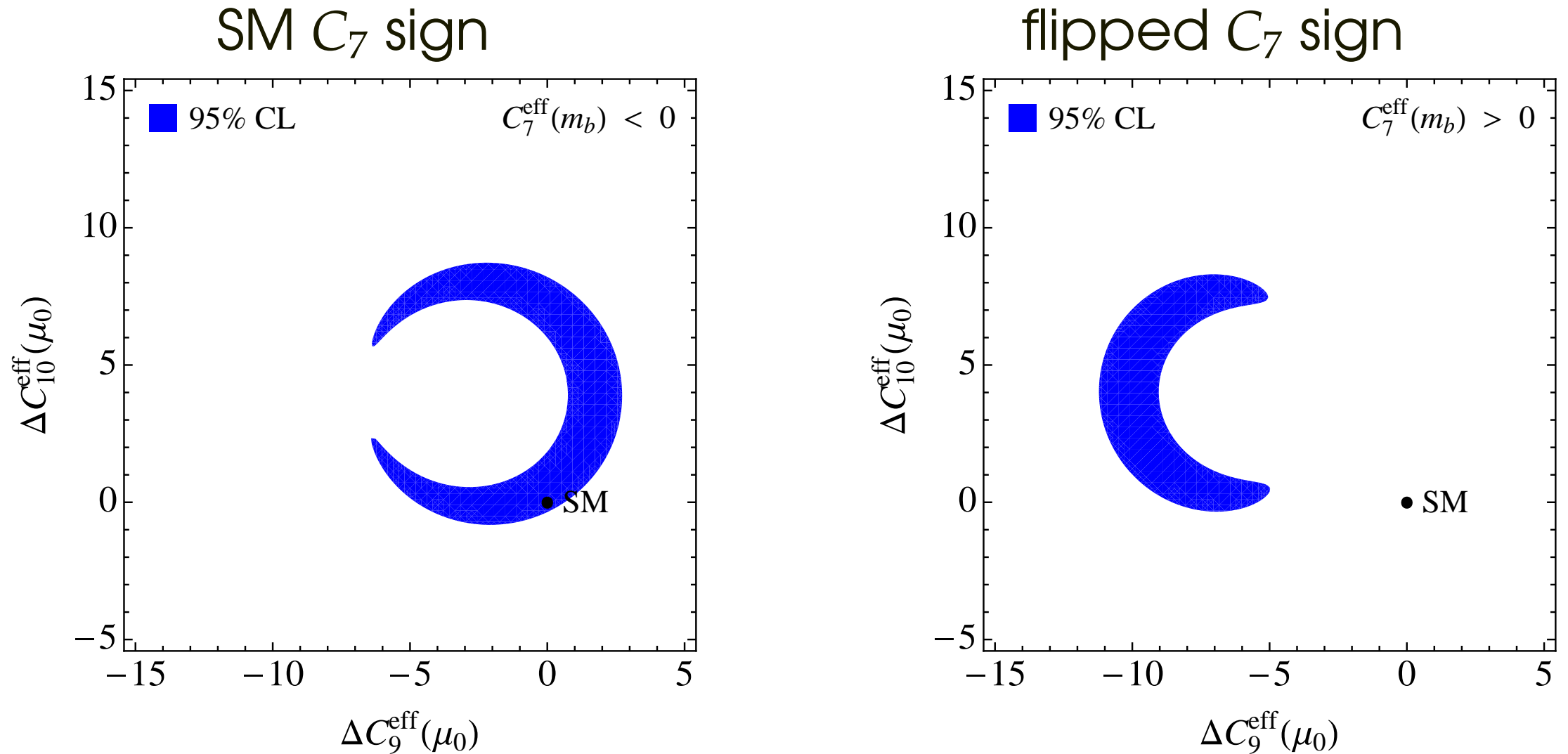
HFAG average:  $\mathcal{B} = (3.66^{+0.76}_{-0.77}) \times 10^{-6}$

SM (Ali et al):  $\mathcal{B}_{\text{SM}} = (4.2 \pm 0.7) \times 10^{-6}$

$C_7$  sign-flip (Gambino et al):  $\mathcal{B}_{C_7 > 0} = (8.8 \pm 1.0) \times 10^{-6}$

➔ Flipped-sign  $C_7$  is disfavored...

# $b \rightarrow s\ell^+\ell^-$ puzzle?



by U. Haisch for new HFAG results, based on PRL94,061803(2005)

- $B \rightarrow X_s\ell^+\ell^-$  results prefers SM-like signs ( $C_7C_9 < 0$ )
- $A_{FB}(B \rightarrow K^*\ell^+\ell^-)$  prefers opposite signs? ( $C_7C_9 > 0$ )



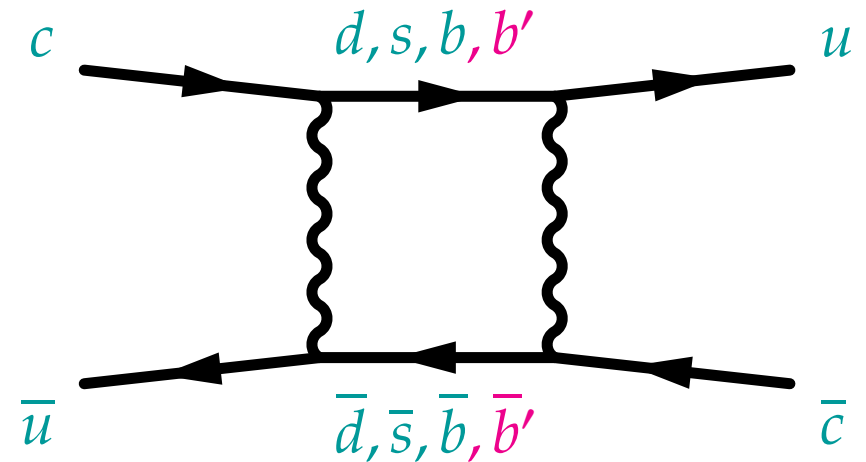
# $D^0$ mixing and CPV

Mixing ( $D^0 \Leftrightarrow \bar{D}^0$ ) occurs if  $x \neq 0$  or  $y \neq 0$

$$\left[ x = \frac{m_1 - m_2}{\Gamma}, y = \frac{\Gamma_1 - \Gamma_2}{2\Gamma}, \Gamma = \frac{\Gamma_1 + \Gamma_2}{2}, m = \frac{m_1 + m_2}{2} \right]$$

mass eigenstate  $\neq$  flavor eigenstate

$$D_{1,2} = pD^0 \pm q\bar{D}^0 \neq D^0(c\bar{u}), \bar{D}^0(\bar{c}u)$$



- SM short distance —  $x, y$  are extremely small ( $O(10^{-5})$ )
- SM long distance — could be  $O(10^{-2})$
- Non SM effects — could be  $O(10^{-2})$

CPV — both in mixing and decay

- SM Mixing —  $A_M \leq O(\arg(V_{cd}^* V_{ud})) \sim O(10^{-3})$
- SM Decay —  $A_D \leq O(\arg(V_{cs}^* V_{us})) \sim O(10^{-3})$  (in e.g.  $D^0 \rightarrow K^+ K^-$ )
- Interference between mixing and decay —  $\phi$

# $D^0$ mixing methods

Observable are combinations of  $x$ ,  $y$ ,  $A_M$ ,  $A_D$  and  $\phi$

- Decays to CP eigenstate (e.g.  $K^+K^-$ ) 😊

$$\text{Lifetime: } y_{CP} = \frac{\tau(D^0 \rightarrow K^- \pi^+)}{\tau(D^0 \rightarrow K^- K^+)} - 1 = y \cos \phi - \frac{A_M}{2} x \sin \phi$$

- Wrong sign semileptonic decays

$$\text{Any mixing, sensitive to } R_M = \frac{P(D^0 \rightarrow K^{(*)+} \ell^- \bar{\nu})}{P(D^0 \rightarrow K^{(*)-} \ell^+ \nu)} = \frac{x^2 + y^2}{2}$$

- Wrong sign hadronic decays ( $D^0 \rightarrow K^+ \pi^-$ )

Complication due to doubly Cabibbo-suppressed decays,  
Sensitive to  $x'^2 = (x \cos \delta + y \sin \delta)^2$  and  $y' = y \cos \delta - x \sin \delta$

- Time-dependent Dalitz analysis 😊

$D \rightarrow K_S^0 \pi^+ \pi^-$  — many involved modes  $K^{*\pm} \pi^\mp$ ,  $K_S^0 \rho^0$ , ...

Direct extraction of  $x$ ,  $y$  (and  $p/q$ )

# $D^0$ mixing — $y_{CP}$

(Belle PRL98,211803(2007) 540 fb<sup>-1</sup>)

Lifetime measured in  $D^0 \rightarrow K^-\pi^+, K^+K^-, \pi^+\pi^-$

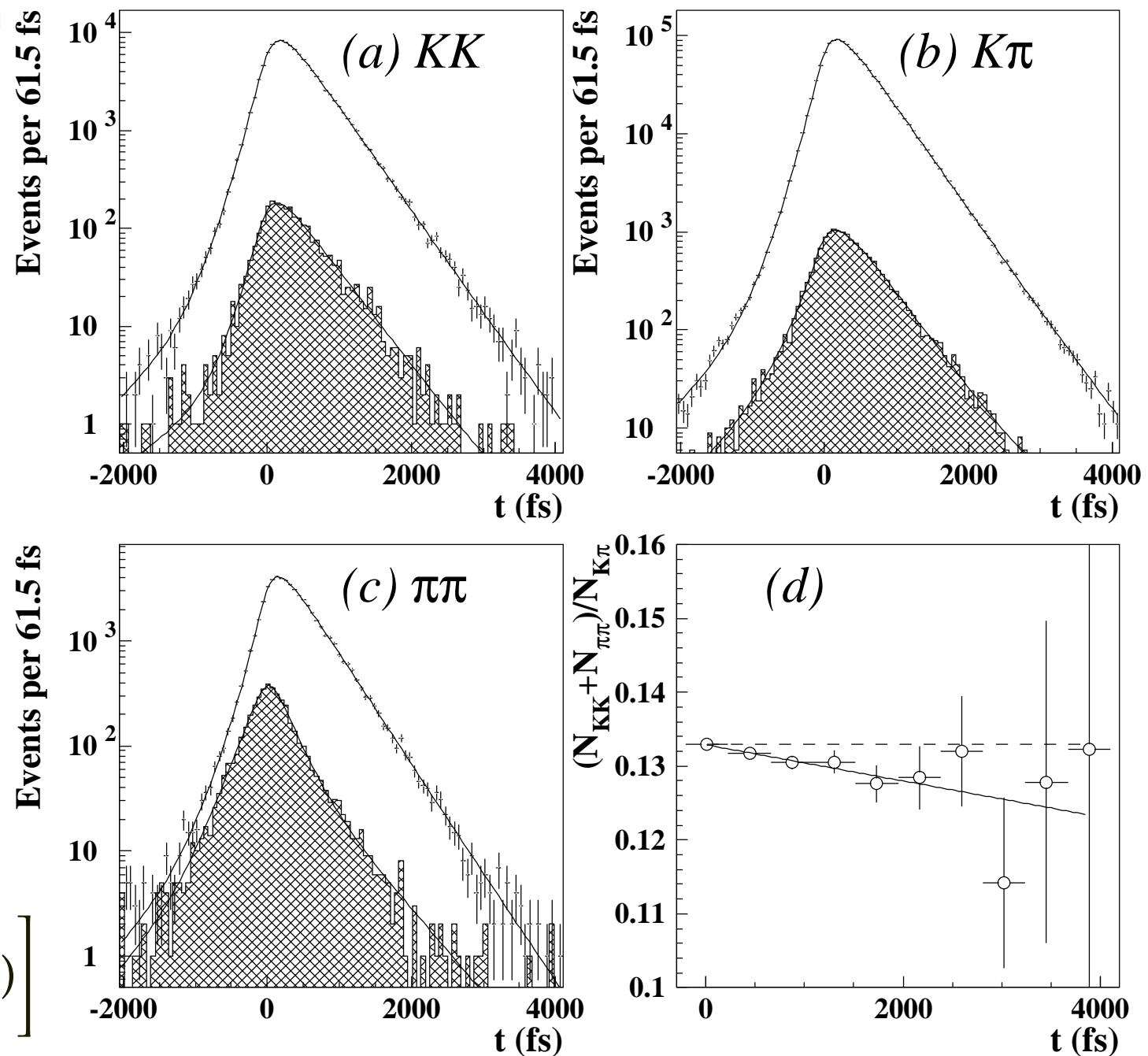
$$y_{CP} = (1.31 \pm 0.32 \pm 0.25)\%$$

Lifetime difference:

Tag  $D^0/\bar{D}^0$  from  $D^{*\pm} \rightarrow D\pi_s^\pm$

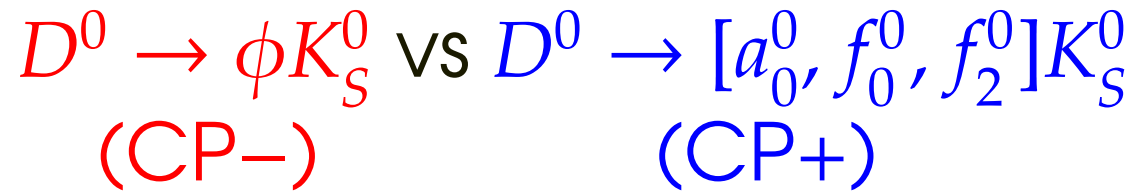
$$A_\Gamma = (0.01 \pm 0.30 \pm 0.15)\%$$

$$\begin{aligned}
 A_\Gamma &= \frac{\tau(\bar{D}^0 \rightarrow K^+K^-) - \tau(D^0 \rightarrow K^+K^-)}{\tau(\bar{D}^0 \rightarrow K^+K^-) + \tau(D^0 \rightarrow K^+K^-)} \\
 &= \frac{1}{2} \left[ \left( \left| \frac{p}{q} \right| - \left| \frac{q}{p} \right| \right) y \cos \phi - \left( \left| \frac{p}{q} \right| + \left| \frac{q}{p} \right| \right) x \sin \phi \right]
 \end{aligned}$$



# $D^0$ mixing $y_{CP}$ in $K^+K^-K_S^0$

Lifetime difference:

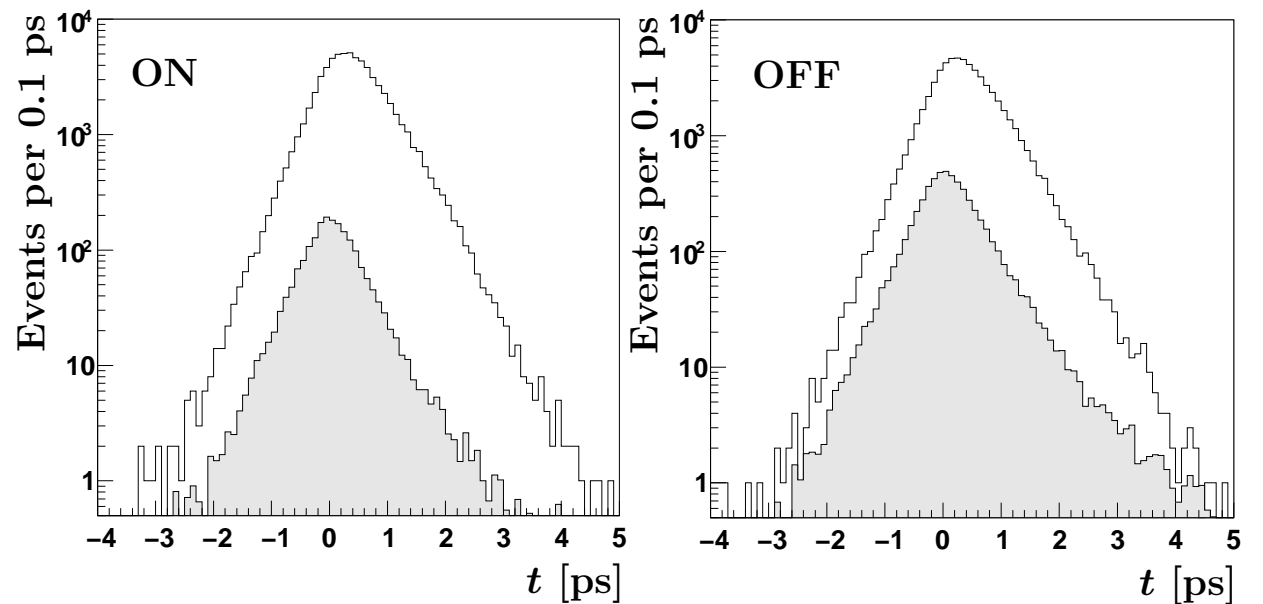
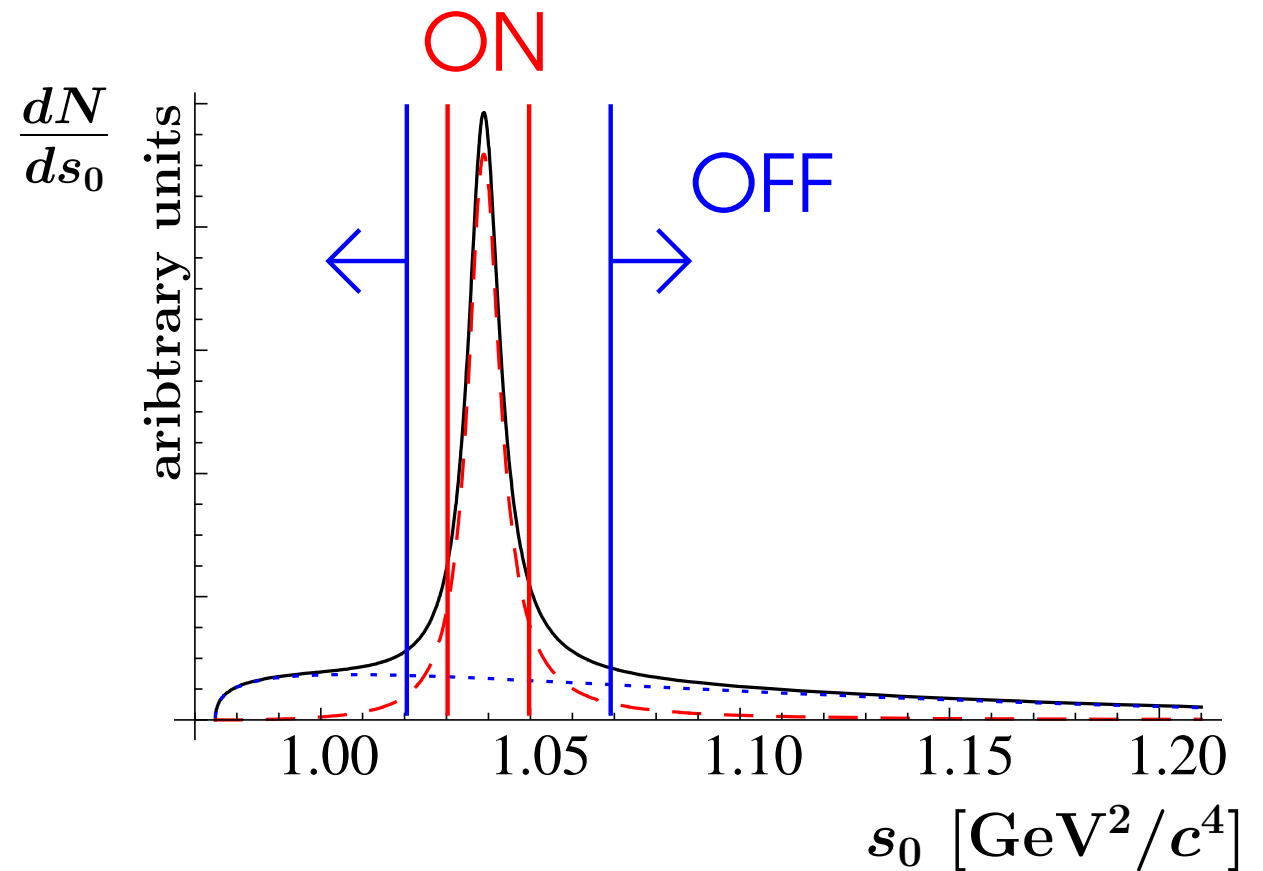


(Belle PRD80,052006(2009) 673 fb<sup>-1</sup>)

Dalitz analysis of  $K^+K^-K_S^0$   
 (with flavor specific  $[a_0^+, f_0^+, f_2^+]K^-$ )

$$y_{CP} = \frac{1}{f_{ON} - f_{OFF}} \left( \frac{\tau_{OFF} - \tau_{ON}}{\tau_{OFF} + \tau_{ON}} \right)$$

$$= (0.11 \pm 0.61 \pm 0.52)\%$$





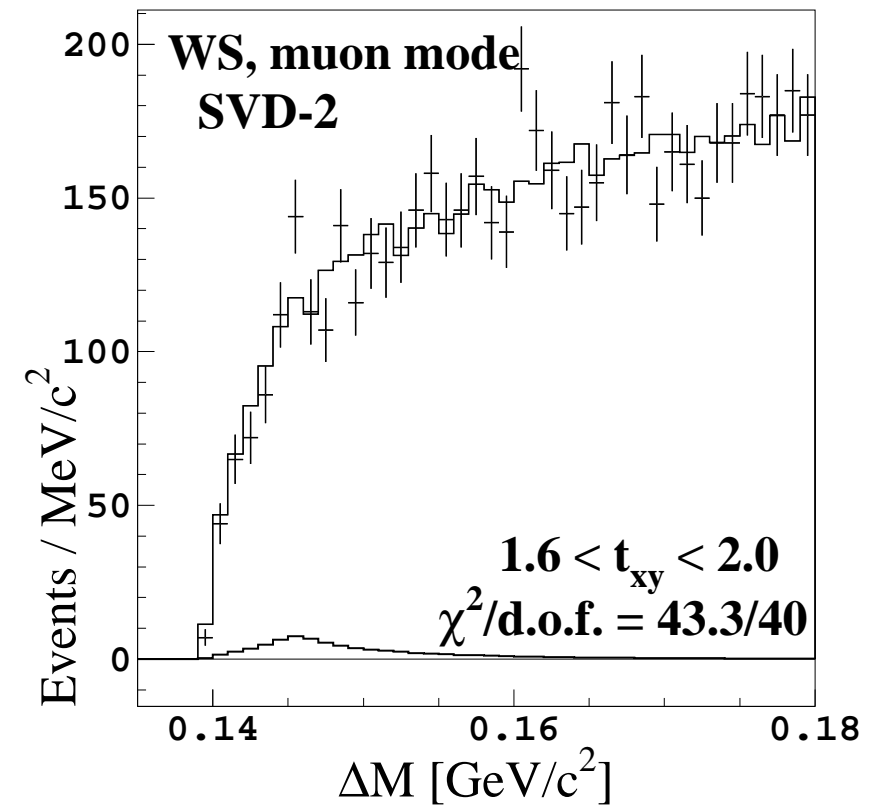
# Wrong sign measurements

## Leptonic ( $D^0 \rightarrow K^+ \ell^- \bar{\nu}$ )

(Belle PRD77,112003(2008) 492 fb<sup>-1</sup>)

- $\Delta M = M(D^0 \pi_{\text{slow}}^+) - M(D^0)$
- Missing neutrino — kinematic constraints  $p_{\text{miss}}, M_{\text{miss}}, M_{D^0}$

$$R_M(\sim \frac{x^2+y^2}{2}) < 6.1 \times 10^{-4}$$

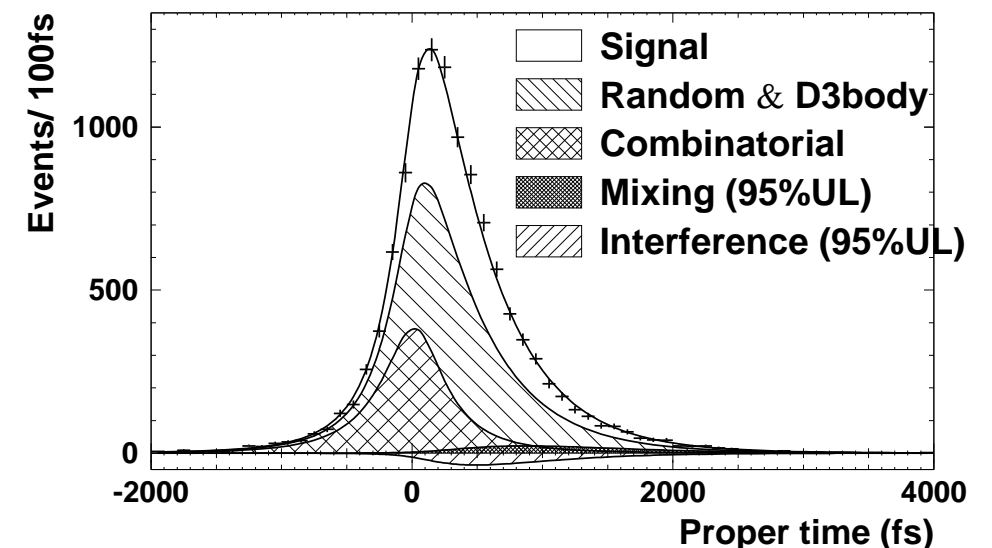


## Hadronic ( $D^0 \rightarrow K^+ \pi^-$ )

(Belle PRL96,151801(2006) 400 fb<sup>-1</sup>)

- Large DCS component, precision time measurement

$$x'^2 < 7.2 \times 10^{-4}, y' \in [-9.9, 6.8] \times 10^{-3}$$



Belle sees no  $D$  mixing in  $D^0 \rightarrow K^+ \pi^-$  although BaBar saw  $3.9\sigma$  evidence

# $D^0$ mixing — time-dependent Dalitz

(Belle PRL99,131803(2007) 540 fb<sup>-1</sup>)

$$\begin{aligned} \mathcal{M}(m_-^2, m_+^2, t) &= \frac{1}{2} \mathcal{A}(m_-^2, m_+^2) [e^{-i\lambda_1 t} + e^{-i\lambda_2 t}] \\ &+ \frac{1}{2} \frac{q}{p} \overline{\mathcal{A}}(m_-^2, m_+^2) [e^{-i\lambda_1 t} - e^{-i\lambda_2 t}] \end{aligned}$$

$$(\lambda_{1,2} = m_{1,2} - i\Gamma_{1,2}/2)$$

$\mathcal{A} = \sum (5 \times \text{CF}, 8 \times \text{CP}, 5 \times \text{DCS}, \text{NR})$

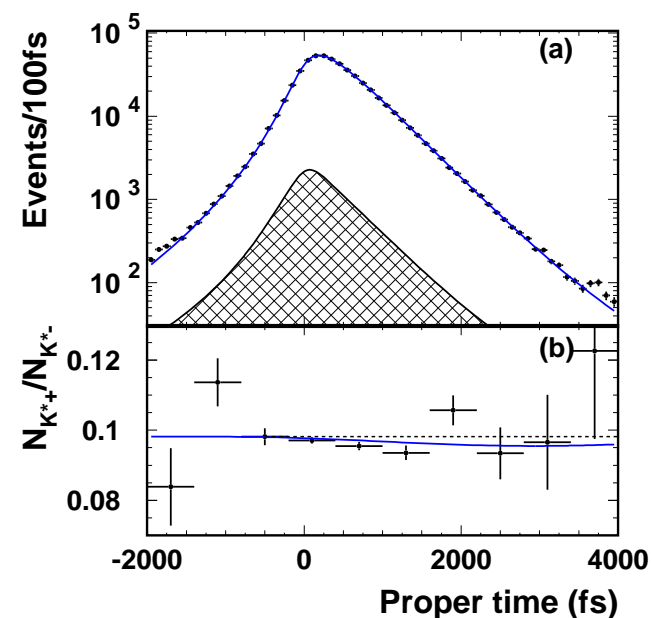
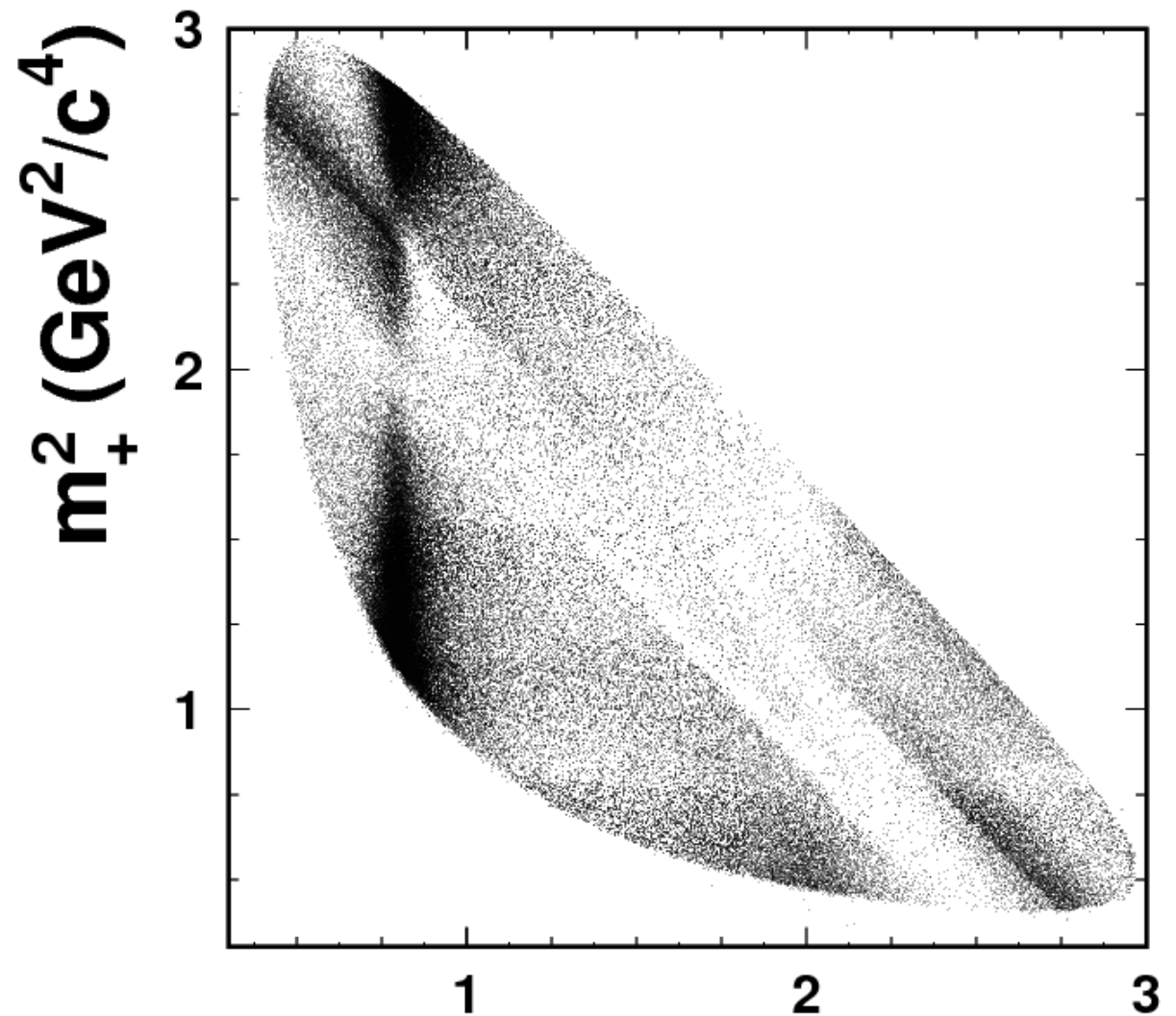
Fit  $|\mathcal{M}|^2$  and  $|\overline{\mathcal{M}}|^2$  with  $m_-^2, m_+^2, t$

$$x = (0.80 \pm 0.29^{+0.13}_{-0.16})\%$$

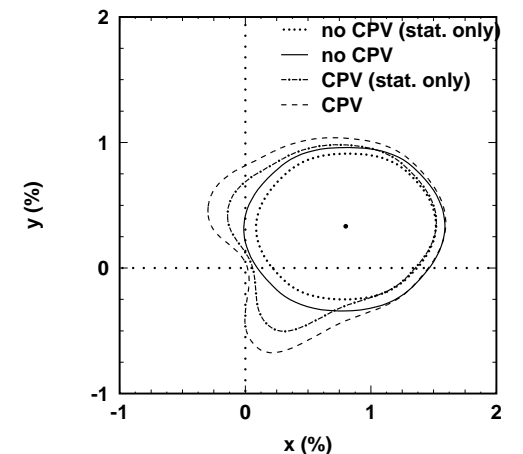
$$y = (0.33 \pm 0.24^{+0.10}_{-0.14})\%$$

$$|p/q| = 1 + \frac{A_M}{2} = 0.86^{+0.30}_{-0.29} {}^{+0.10}_{-0.09}$$

$$\phi = (-0.24^{+0.28}_{-0.30} \pm 0.09) \text{ rad}$$



$m_-^2$  (GeV<sup>2</sup>/c<sup>4</sup>)





# D mixing/CPV status and prospects

B. Golob at FPCP09

expected sensitivity  
only  $KK/\pi\pi$ ,  $K\pi$  and  
 $K_S\pi\pi$  projected  
sensitivities included

HFAG  $\chi^2$  fit  
50  $ab^{-1}$

$$x = (0.793 \pm 0.087)\%$$

$$y = (0.798 \pm 0.062)\%$$

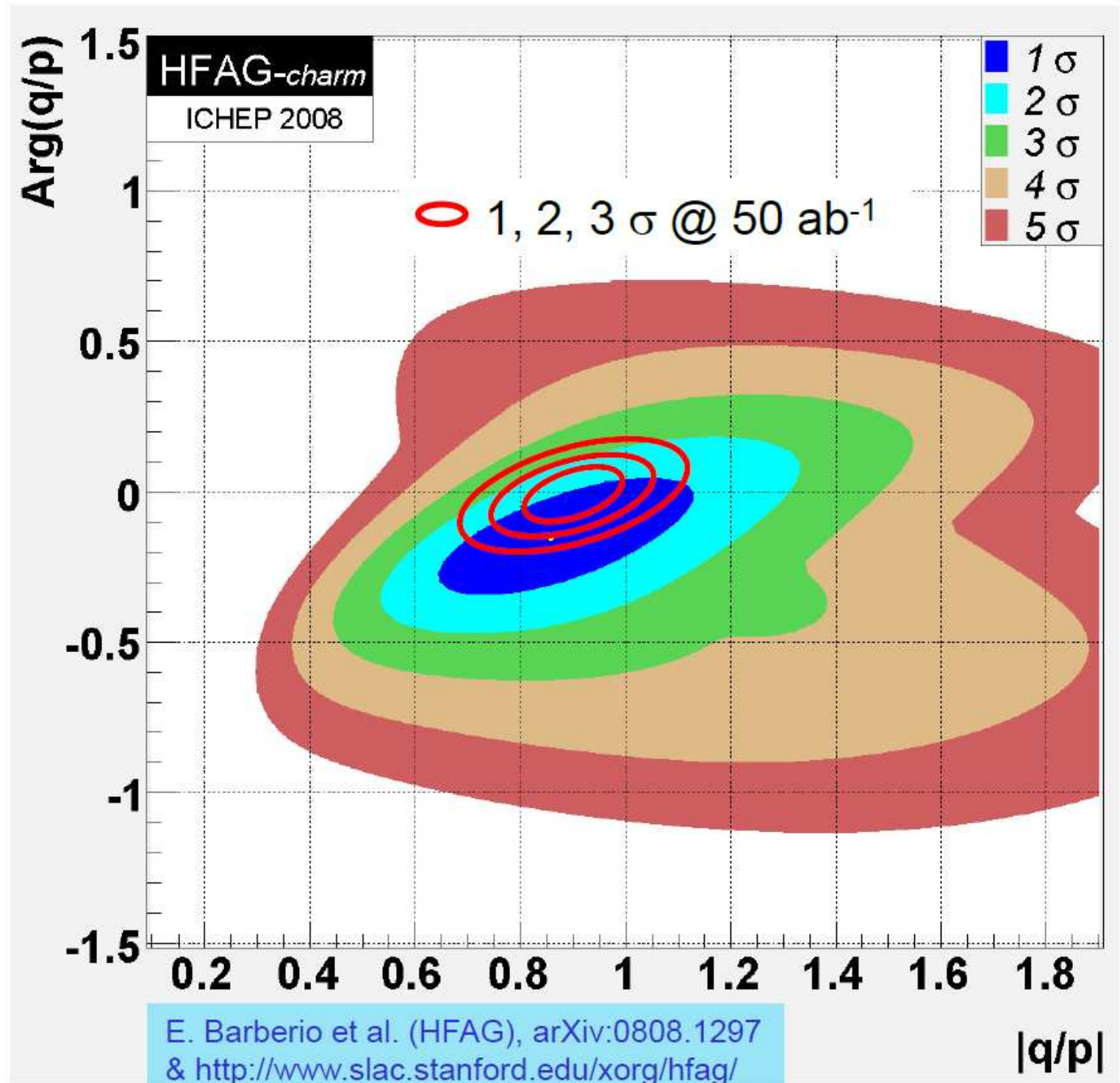
$$\delta_{K\pi} = 24.5^\circ \pm 4.6^\circ$$

$$R_D = (0.336 \pm 0.001)\%$$

$$\frac{|q|}{|p|} = 0.919 \pm 0.055$$

$$\varphi = -0.01 \pm 0.049 \text{ rad}$$

$$A_D = (-0.1 \pm 0.3)\%$$



# Summary

- Many intriguing results from Belle, hopefully useful hints for new physics, including 4th generation quarks
- Still some more data to be analyzed by Belle
- Belle II future seems to be bright 😊









## New Physics CP Violation in $b \rightarrow s$ & $b_s \leftrightarrow s_b$ Transitions

George W.S. Hou (侯維恕)  
National Taiwan University

September 5, 2008, Beyond 3SM @ CERN



## Outline

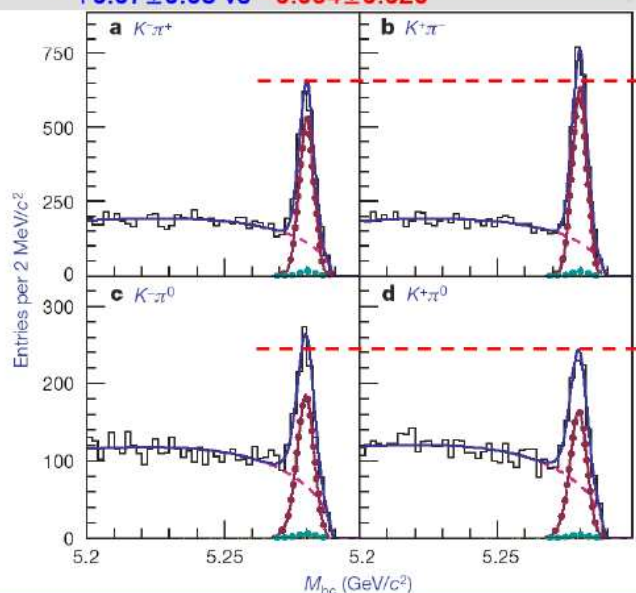
- I.  $\Delta A_{K\pi} = A_{B \rightarrow K^+\pi^0} - A_{B \rightarrow K^+\pi^-} \neq 0$
- II. Consistence and 4 x 4 CKM
- III.  $\sin 2\Phi_s < 0$  and Large
- IV.  $A_{FB}(B \rightarrow K^*\ell^+\ell^-)$  and Other Predictions
- V. Conclusion

CERN
NTU

### Belle 2008 Nature: Simple Bean Count

$\Delta A = A_{K^+\pi^0} - A_{K^+\pi^-} = +0.164 \pm 0.037 \quad 4.4\sigma$   
 $+0.07 \pm 0.03$  vs  $-0.094 \pm 0.020$

LETTERS      NATURE | Vol 452 | 20 March 2008



CERN
NTU

$$\Delta A_{K\pi} = A_{B \rightarrow K^+\pi^0}^{+0.050 \pm 0.025} - A_{B \rightarrow K^+\pi^-}^{-0.097 \pm 0.012} \neq 0$$

World Experiment is Firm

$$= +0.147 \pm 0.028 > 5\sigma$$

Why a Puzzle ?

$\Delta A_{K\pi} \sim 0$  expected

$M(B^0 \rightarrow K^+\pi^-) \propto (T + P) = re^{i\phi_3} + e^{i\delta}$

$\sqrt{2}M_{K^+\pi^0} - M_{K^+\pi^-} \propto (P_{EW} + C) ?$

Large C ?

Large EWPenguin ?

A lot of (hadronic) finesse

Baek, London, PLB653, 249 (2007)

Need NP CPV Phase

P<sub>EW</sub> has practically no weak phase in SM

4th Gen. in EWP Natural

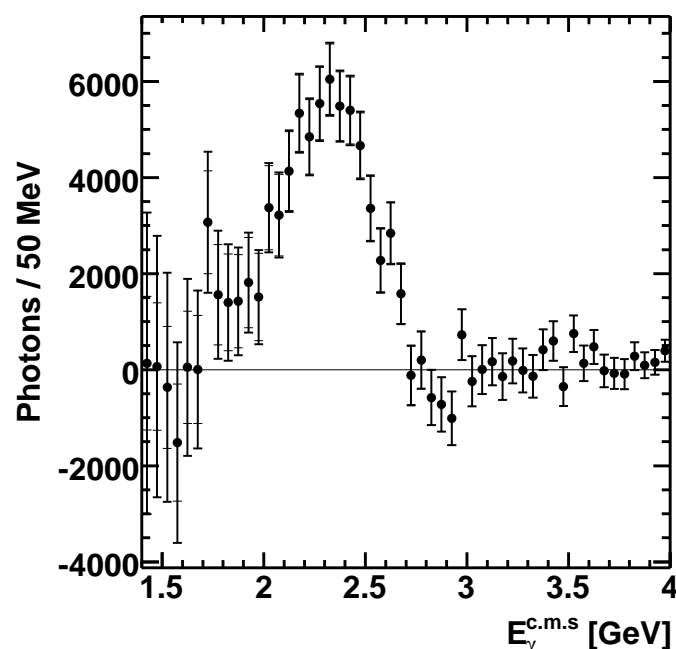
nondecouplin

$B^- (b, \bar{u}) \rightarrow K^- (s, \bar{u}) + \pi^0 (d, \bar{d})$  via  $Z$  penguin with  $t, t'$  loop.

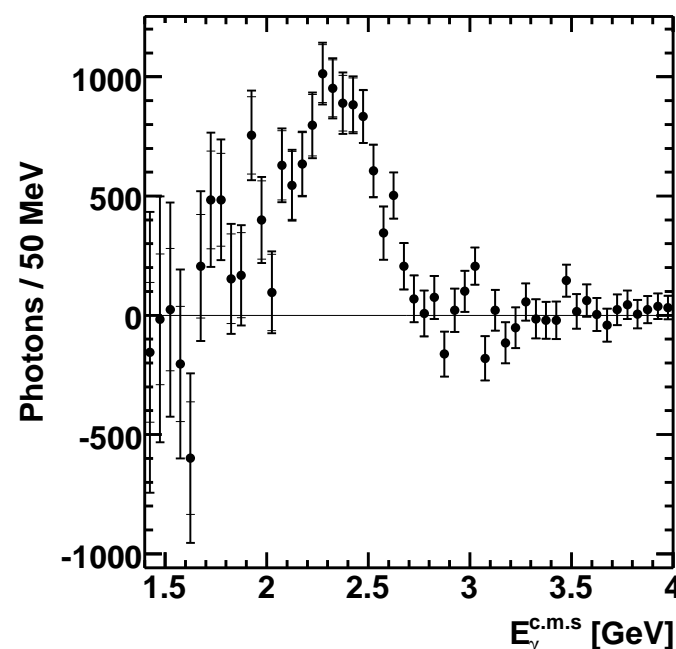
# $\mathcal{B}(B \rightarrow X_s \gamma)$

Background subtracted

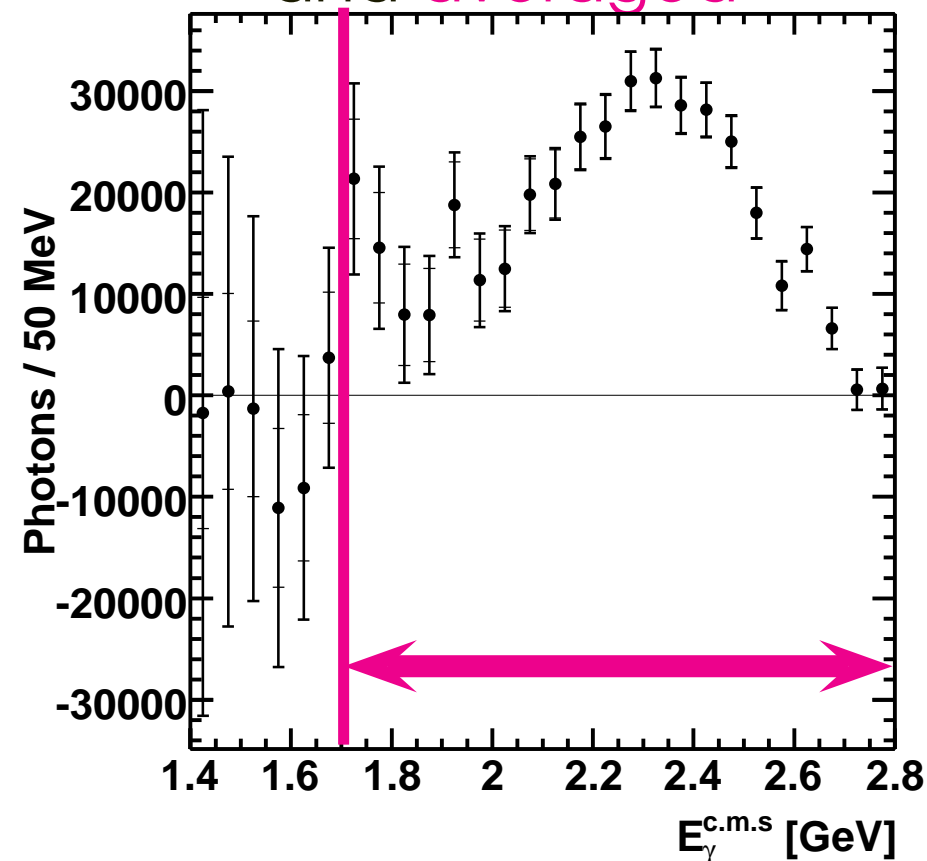
untagged sample



lepton-tag



Efficiency corrected  
and averaged



(Belle PRL 103,241801(2009) 657M  $B\bar{B}$ )

$$\mathcal{B}(B \rightarrow X_s \gamma) = (3.45 \pm 0.15 \pm 0.40) \times 10^{-4} \quad (\text{for } E_\gamma > 1.7 \text{ GeV})$$

- The most precise  $B \rightarrow X_s \gamma$  measurement
- HFAG:  $(3.57 \pm 0.24) \times 10^{-4}$  vs SM  $(3.15 \pm 0.23) \times 10^{-4}$  ( $E_\gamma > 1.6$  GeV)
- Systematic error is dominated by **off-resonance subtraction** and  **$B$  backgrounds other than  $B \rightarrow \pi^0/\eta$**  (syst  $\approx$  stat for  $E_\gamma > 2$  GeV)

# $B \rightarrow X_s \ell^+ \ell^-$ by Belle — table

bin	$N_{\text{sig}}$	eff.(%)	$\mathcal{B} (10^{-7})$
$M(X_s) (\text{GeV}/c^2)$			
(0.4, 0.6)	$104.4 \pm 11.5 \pm 1.8$	$8.44^{+0.86}_{-1.09}$	$4.7 \pm 0.5^{+0.5}_{-0.6}$
(0.6, 0.8)	$0.4 \pm 3.0 \pm 0.2$	$3.86^{+0.39}_{-0.50}$	$0.0 \pm 0.3^{+0.6}_{-0.0}$
(0.8, 1.0)	$79.0 \pm 11.6 \pm 0.5$	$3.89^{+0.40}_{-0.50}$	$7.7 \pm 1.1^{+0.8}_{-1.0}$
(1.0, 1.4)	$23.7 \pm 10.5 \pm 0.3$	$1.68^{+0.17}_{-0.22}$	$5.4 \pm 2.4^{+0.6}_{-0.7}$
(1.4, 2.0)	$32.5 \pm 16.5 \pm 0.9$	$0.99^{+0.10}_{-0.13}$	$12.5 \pm 6.3^{+1.3}_{-1.7}$
Sum (0.4, 2.0) for $X_s \ell^+ \ell^-$			$30.3 \pm 6.9^{+1.7}_{-2.1}$
(Sum (0.4, 2.0) for $X_s e^+ e^-$ )			$40.4 \pm 9.8^{+2.8}_{-3.4}$
(Sum (0.4, 2.0) for $X_s \mu^+ \mu^-$ )			$18.4 \pm 8.8^{+1.5}_{-1.7}$
$q^2 (\text{GeV}^2/c^2)$			
(0.04, 1.0)	$36.1 \pm 7.8 \pm 0.1$	$2.40^{+0.33}_{-0.38}$	$5.7 \pm 1.2^{+0.8}_{-0.9}$
(1.0, 6.0)	$74.0 \pm 15.3 \pm 0.4$	$3.48^{+0.47}_{-0.55}$	$8.1 \pm 1.7^{+1.1}_{-1.3}$
(6.0, 14.4)	$64.9 \pm 16.6 \pm 0.3$	$2.20^{+0.30}_{-0.35}$	$11.2 \pm 2.9^{+1.5}_{-1.8}$
(14.4, 25.0)	$62.8 \pm 11.0 \pm 2.3$	$7.44^{+1.01}_{-1.17}$	$3.2 \pm 0.6 \pm 0.5$

sum up