



CP Violation in $b' \rightarrow s$ decays

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Based on:

A.A and W.S. Hou, [arXiv:0908.0901](#); PRD80, 076005 2009

Second Workshop on beyond 3 Generation Standard Model,
14-16 January NTU Taipei

Outline

- Motivations
- Mechanism of CPV
- Relevant CP Invariant Phase
- Numerical Results on CPV in $b' \rightarrow sX$, $X = Z, \gamma, g, H$
- Short report on “CP violation and the fourth generation”
 $b' \rightarrow \{b, s\}X$, $t' \rightarrow \{c, t\}X$ and $t \rightarrow cX$, $X = Z, \gamma, g, H$
by G. Eilam B. Melic and J. Trampetic, PRD'09
- Observability of CPV in $b' \rightarrow sX$
- Conclusions

Motivations:

- In the SM, the amount of CPV in CKM, may be enough to explain the observed size of CPV in B and K meson system.
- However, it is too small to generate the observable **Baryon Asymmetry in the Universe (BAU)**. Therefore, models with extra CP violating phases are welcome [[A.D. Sakharov '67](#)].
- A 4th generation could enhance the invariant CPV measure of Jarlskog parameter by a factor of $10^{13} - 10^{15}$ [[W.-S.Hou'08](#)] [[more detail in Chia-Hsien Shen talk](#)]

Hints

- CPV in $B_s \rightarrow J/\psi\phi$ ($\sin 2\Phi_{B_s}$) (Chien-Yi Ma talk)
- CDF and DØ reported a large and negative value for $\sin 2\Phi_{B_s}$.
[DØ PRL'08]: $2\Phi_{B_s} = -0.57_{-0.30}^{+0.23}(\text{stat})_{-0.02}^{+0.08}(\text{syst})$.
- The SM predicts $2\Phi_{B_s}^{\text{SM}} \simeq 2 \arg(-V_{tb}V_{ts}^*/V_{cb}V_{cs}^*) \simeq -0.04 \pm 0.01$.
While 4th generation SM can predict large and negative $\sin 2\Phi_{B_s}$
W.-S.Hou et al, PRL, PRD '05, A.A and W.-S.Hou'EPJC'03
- The difference in $\Delta A_{K\pi} \equiv A_{B^+ \rightarrow K^+\pi^0} - A_{B^0 \rightarrow K^+\pi^-} \neq 0$ is now established beyond 5σ [Lin, Unno, Hou, Chang Nature'08].
(M. Nakao talk)
- It could be due to hadronic effects, but it could be also **New Physics in the EW penguin** amplitude such as 4th generation [Hou, Nagashima, Soddu PRL'05].

With the start of the LHC,

- If b' and t' have a mass within perturbativity range, due to their strong production, they will be copiously produced at LHC.
- Therefore, the LHC has the capability to produce b' and t' and measure some of their decays, including FCNC decays such as $b' \rightarrow bX, t' \rightarrow tX, \text{Br} \in]10^{-2}, 10^{-4}[, t' \rightarrow cX, b' \rightarrow sX$
A.A and W.S. Hou'2006.
- The LHC has also the capability to establish CPV in top quark and may be also in b' if not too heavy and CPV not too small.
- CPV studies in $b' \rightarrow s$ transitions are complementary with low energies processes $B_s \rightarrow J/\psi\phi, K_L \rightarrow \pi^0\bar{\nu}\nu, D^0$ mixing ...
- CPV in $b' \rightarrow s$ transitions is of Direct CPV type, unlike Direct CPV in B decays, the strong phases in $b' \rightarrow s$ transitions are calculable.

Mechanism of CPV:

Suppose an amplitude \mathcal{M} with two components $\mathcal{M}_{1,2}$:

$$\begin{aligned}\mathcal{M} &= |\mathcal{M}_1| e^{i\delta_1} e^{i\phi_1} + |\mathcal{M}_2| e^{i\delta_2} e^{i\phi_2} , \\ \overline{\mathcal{M}} &= |\mathcal{M}_1| e^{i\delta_1} e^{-i\phi_1} + |\mathcal{M}_2| e^{i\delta_2} e^{-i\phi_2} ,\end{aligned}$$

δ_i absorptive “strong” phases, ϕ_i weak phases. One can easily show:

$$|\mathcal{M}|^2 - |\overline{\mathcal{M}}|^2 = 4|\mathcal{M}_1||\mathcal{M}_2| \sin(\delta_2 - \delta_1) \sin(\phi_2 - \phi_1)$$

The CP asymmetry is then

$$A_{CP} = \frac{|\mathcal{M}|^2 - |\overline{\mathcal{M}}|^2}{|\mathcal{M}|^2 + |\overline{\mathcal{M}}|^2} = \frac{2|\mathcal{M}_1||\mathcal{M}_2| \sin(\delta_2 - \delta_1) \sin(\phi_2 - \phi_1)}{|\mathcal{M}_1|^2 + |\mathcal{M}_2|^2 + 2|\mathcal{M}_1||\mathcal{M}_2| \cos \delta \cos \phi} ,$$

It is clear that A_{CP} vanishes unless both the weak *and* “strong” phase differences $\phi \equiv \phi_2 - \phi_1 \neq 0$ and $\delta \equiv \delta_2 - \delta_1 \neq 0$.

$b' \rightarrow bX$ decays and CP violation

The CKM factors $V_{ub}^* V_{ub'}$ and $V_{cb}^* V_{cb'}$ are rather small, the unitarity relation imply

$$V_{tb}^* V_{tb'} \cong -V_{t'b}^* V_{t'b'}$$

then

$$\mathcal{M}_{b' \rightarrow b} = V_{t'b}^* V_{t'b'} [f(m_{t'}) - f(t)]$$

dominated by single amplitude.

$b' \rightarrow sX, t' \rightarrow \{c, t\}X$ decays and CP violation

- Using the following unitarity relations:

$$\begin{aligned} V_{us}^* V_{ub'} + V_{cs}^* V_{cb'} &= -(V_{ts}^* V_{tb'} + V_{t's}^* V_{t'b'}), \\ V_{cd} V_{t'd}^* + V_{cs} V_{t's}^* + V_{cb} V_{t'b}^* &= -V_{cb'} V_{t'b'}^*, \\ V_{td} V_{t'd}^* + V_{ts} V_{t's}^* + V_{tb} V_{t'b}^* &= -V_{tb'} V_{t'b'}^*. \end{aligned}$$

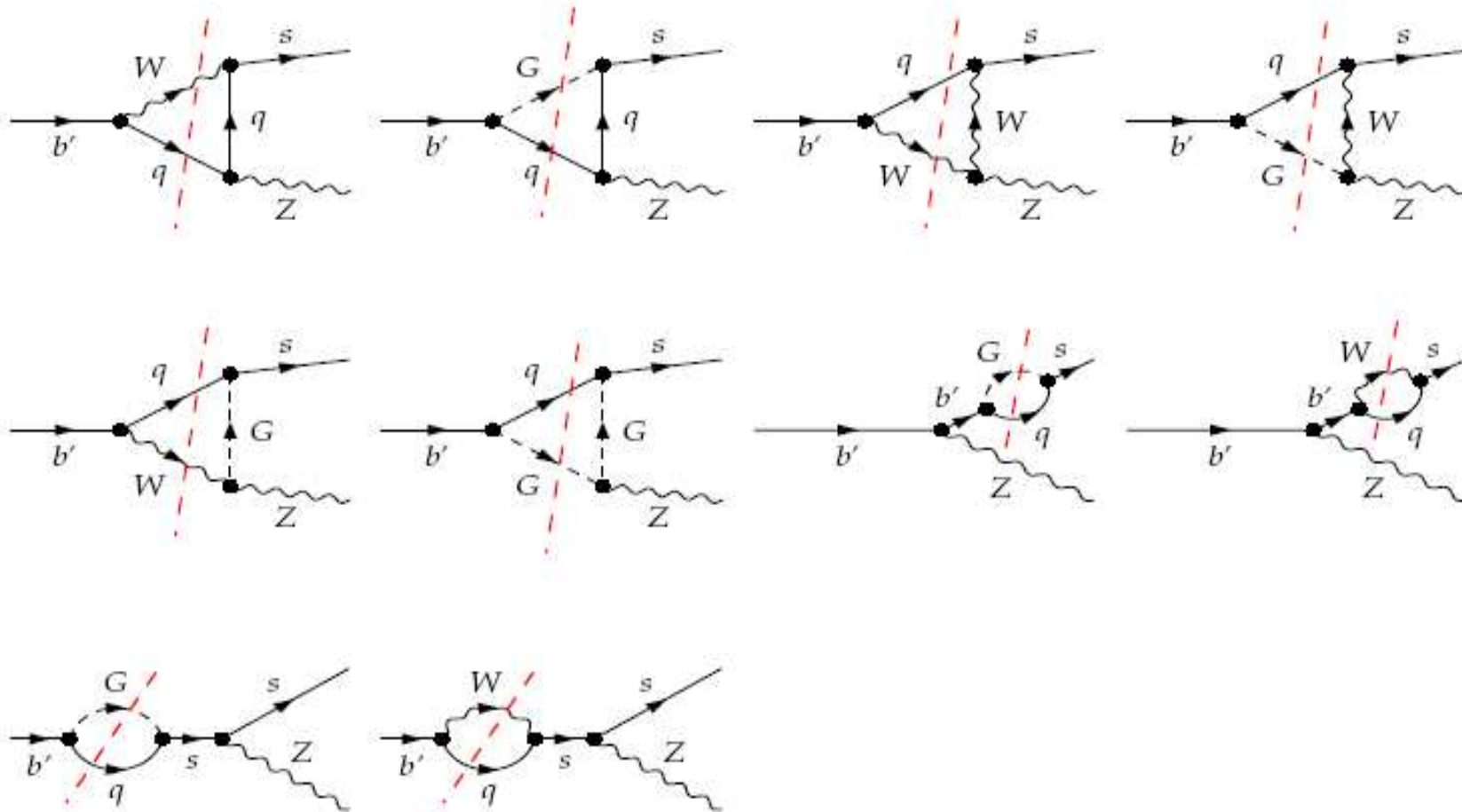
- The loop amplitudes for $b' \rightarrow s$ and $t' \rightarrow \{c, t\}$ transitions are

$$\mathcal{M}_{b' \rightarrow s} \propto V_{ts}^* V_{tb'} [f(m_t) - f(0)] + V_{t's}^* V_{t'b'} [f(m_{t'}) - f(0)],$$

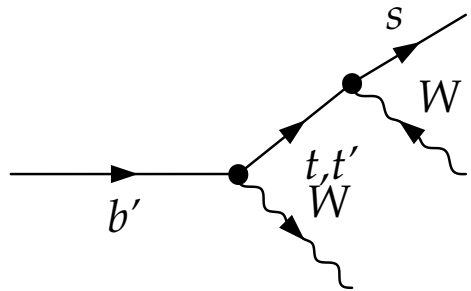
$$\mathcal{M}_{t' \rightarrow c} \propto V_{cb'} V_{t'b'}^* [f(m_{b'}) - f(0)].$$

$$\mathcal{M}_{t' \rightarrow t} \propto V_{tb'} V_{t'b'}^* [f(m_{b'}) - f(0)].$$

- Both $V_{ts}^* V_{tb'}$ and $V_{t's}^* V_{t'b'}$ have CP phases. The phase difference, together with absorptive parts can lead to CPV in $b' \rightarrow s$ transitions.



Unlike B meson decays (with hadronic phases), the absorptive parts in this case are calculable perturbatively, while QCD corrections are also perturbative.



Calculation of Relevant CP Invariant Phase

The general amplitude of $b' \rightarrow sH$ can be written, as

$$\mathcal{M}_{sH} = V_{qs}^* V_{qb'} [H_L(m_q) \bar{u}_s L u_{b'} + H_R(m_q) \bar{u}_s R u_{b'}]$$

$H_{L,R}$ are form factors expressed in terms of Passarino-Veltman functions.

$H_L \propto m_s$ and $H_R \propto m_{b'}$.

$H_{L,R}$ are UV divergent, after GIM subtraction the result is finite.

We denote the subtracted quantities as

$$\Delta_H^{L,R}(Q, 0) = H_{L,R}(Q) - H_{L,R}(m_c) \approx H_{L,R}(Q) - H_{L,R}(0) , \quad Q = m_{t,t'}$$

In the case of $b' \rightarrow sV^0$:

$$\begin{aligned}
M_{sV} = & V_{qs}^* V_{qb'} \{ k_{b'}^\mu [A_L(m_q) \bar{u}_s L u_{b'} + A_R(m_q) \bar{u}_s R u_{b'}] \\
& + k_s^\mu [B_L(m_q) \bar{u}_s L u_{b'} + B_R(m_q) \bar{u}_s R u_{b'}] \\
& + [C_L(m_q) \bar{u}_s L \gamma^\mu u_{b'} + C_R(m_q) \bar{u}_s R \gamma^\mu u_{b'}] \} ,
\end{aligned}$$

$$A_L, B_L, C_L \propto m_s$$

Only $C_{L,R}$ terms are UV divergent. Similar to the Higgs case, the divergent terms cancel after GIM subtraction.

In the case of $b' \rightarrow s\gamma$ and $b' \rightarrow sg$, from electromagnetic or color current conservation, we have:

$$(A_L + B_L)(m_{b'}^2 - m_s^2)/2 + m_{b'} C_L - m_s C_R = 0.$$

$$(A_R + B_R)(m_{b'}^2 - m_s^2)/2 - m_s C_L + m_{b'} C_R = 0.$$

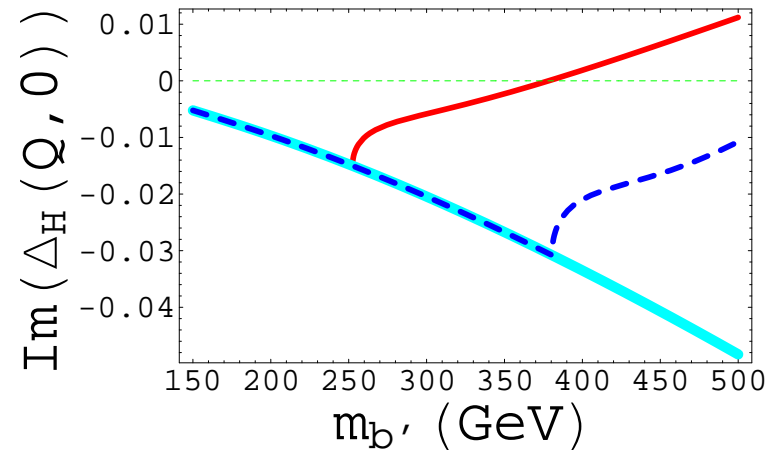
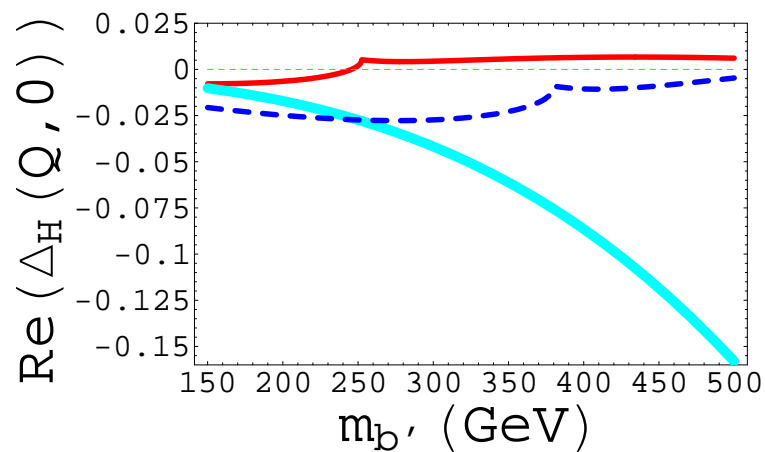
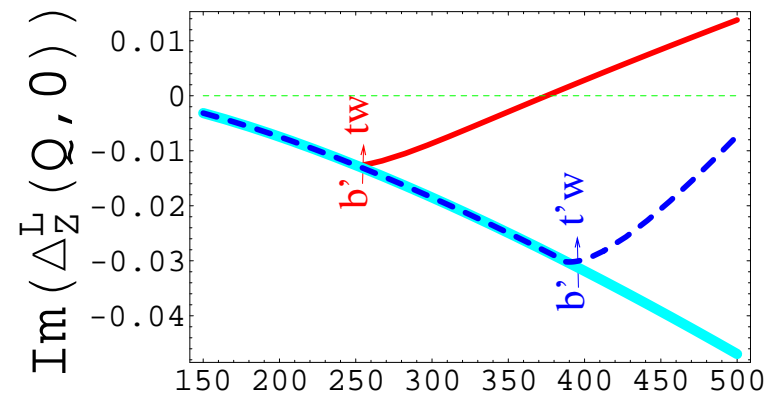
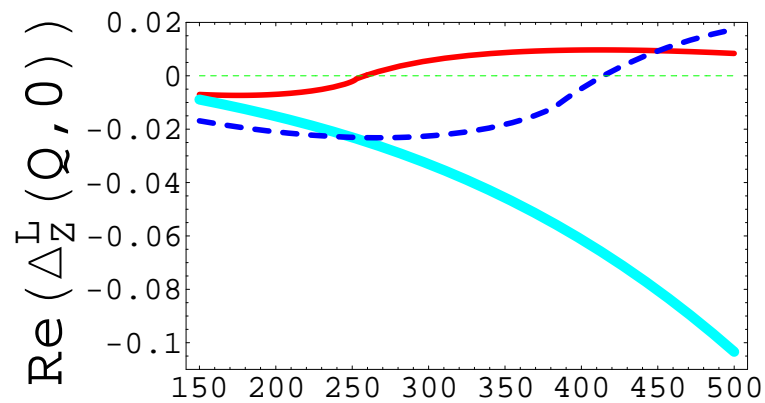


Figure 1: $\Delta_{Z,H}(Q, 0)$, $m_H = 120$ GeV: Solid line is $Q = m_t$, cyan solid $Q = m_{t'} = m_{b'} + 50$ GeV, blue dash $Q = m_{t'} = 300$ GeV

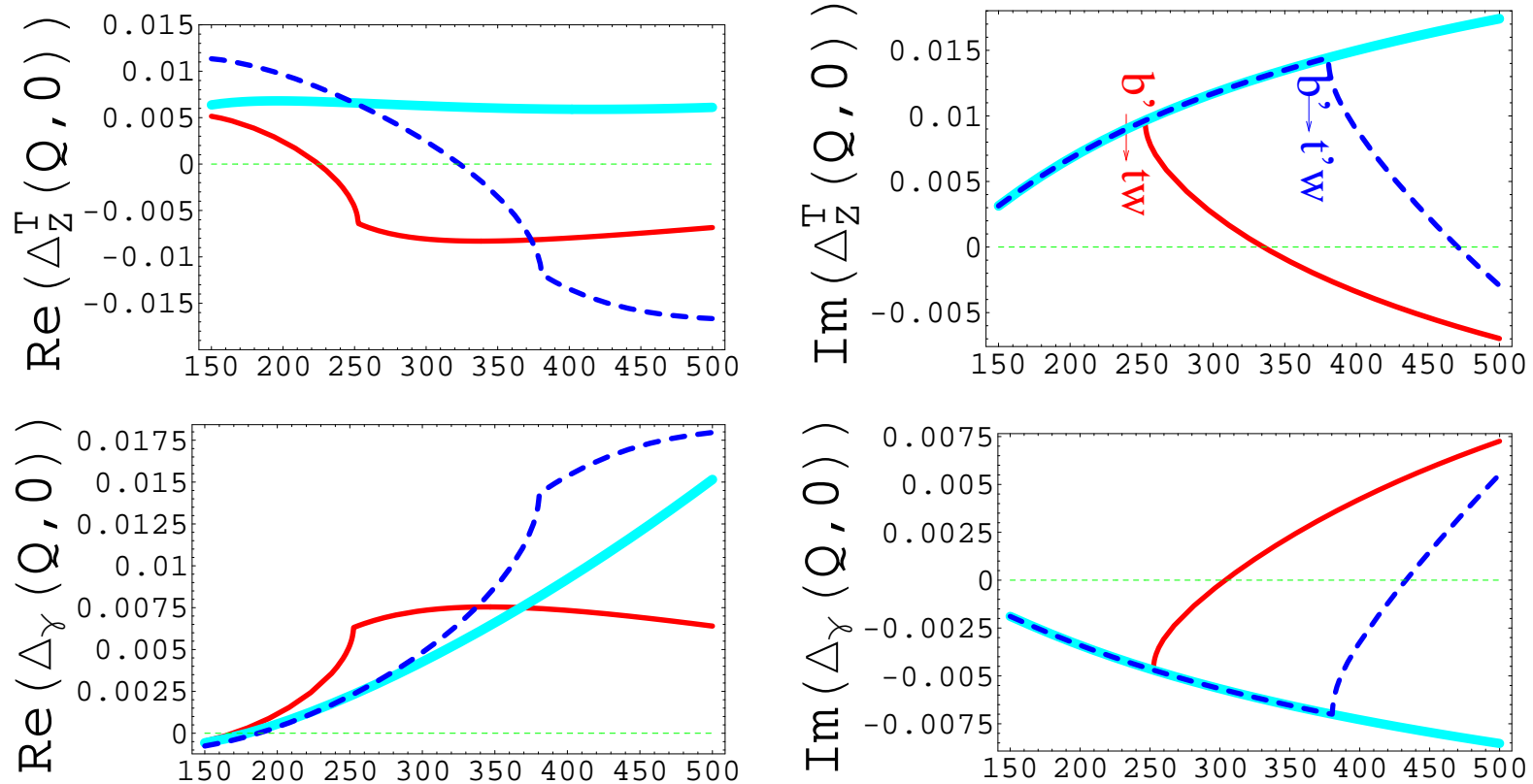


Figure 2: $\Delta_V^R(Q, 0)$, $V = Z, \gamma$, $M_H = 120$ GeV Solid line is $Q = m_t$, cyan solid $Q = m_{t'} = m_{b'} + 50$ GeV, blue dash $Q = m_{t'} = 300$ GeV

CP conserving phase: $\sin \delta = \sin(\arg[\Delta(m_t)] - \arg[\Delta(m_{t'})])$

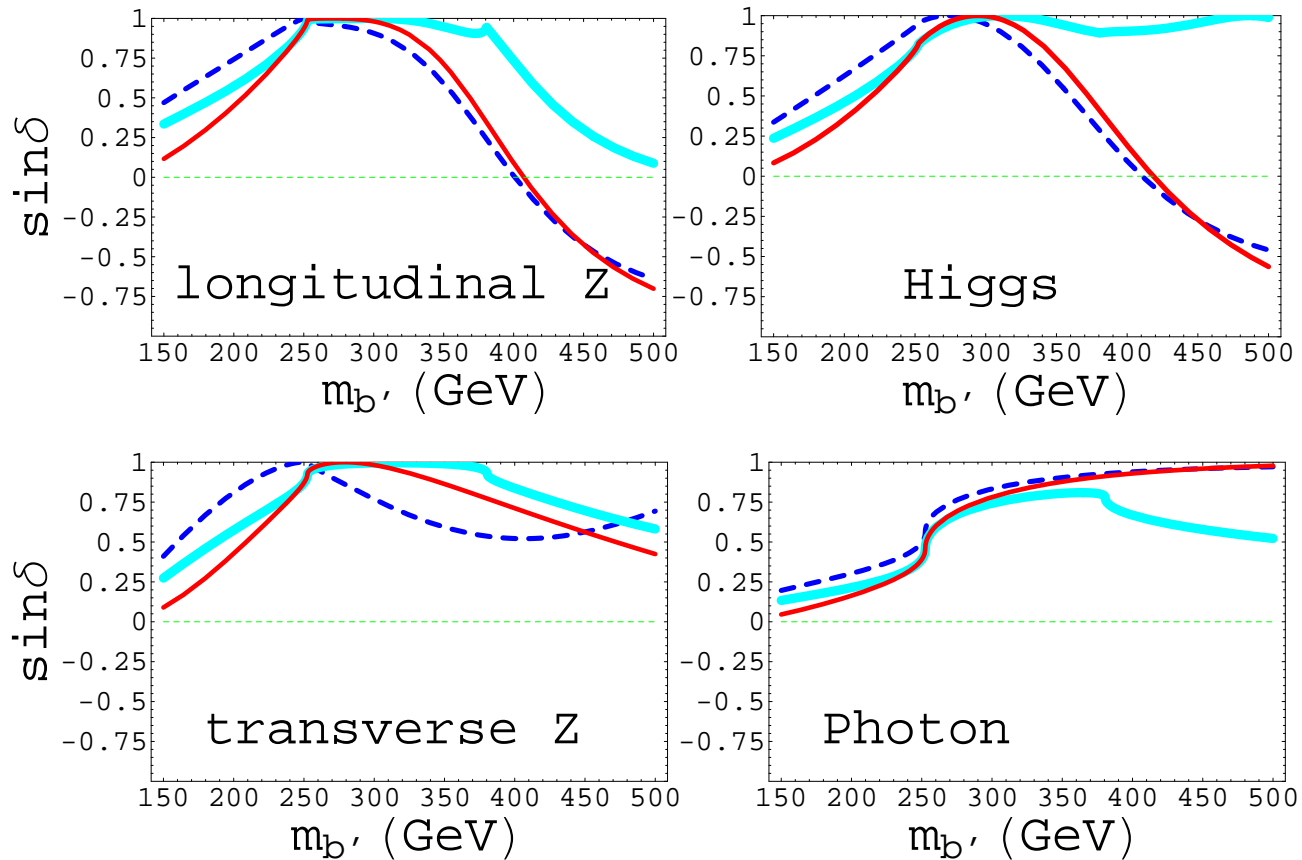


Figure 3: $M_H = 120$ GeV, Solid line is for $m_{t'} = m_{b'} + 50$ GeV
cyan solid is for $m_{t'} = 300$ GeV, blue dash is for $Q = m_{t'} = 500$ GeV

Numerical results

The rate CP asymmetry A_{CP} is defined as:

$$\begin{aligned} \mathcal{A}_{CP}(b' \rightarrow sX) &= \frac{\Gamma(b' \rightarrow sX) - \Gamma(\bar{b}' \rightarrow \bar{s}X)}{\Gamma(b' \rightarrow sX) + \Gamma(\bar{b}' \rightarrow \bar{s}X)} \\ &\propto 2|\mathcal{M}_1||\mathcal{M}_2| \sin(\delta_2 - \delta_1) \sin(\phi_2 - \phi_1) \end{aligned}$$

$V_{ts}^* V_{tb'}$ and $V_{t's}^* V_{t'b'}$ would have **different CP violating phase**:

$$\sin(\phi_2 - \phi_1) \neq 0$$

$\sin(\delta_2 - \delta_1)$ could be maximal.

HNS scenario

Motivated by CP violation problem in $B \rightarrow K^+ \pi^-$ vs $K^+ \pi^0$ modes, and taking into account other B physics observables, [Hou, Nagashima, Soddu \(HNS scenario\)'05](#), with $m_{t'} \approx 300$ GeV, concluded that

$$\begin{pmatrix} 0.9745 & 0.2225 & 0.0038 e^{-i 60^\circ} & 0.0281 e^{i 61^\circ} \\ -0.2241 & 0.9667 & 0.0415 & 0.1164 e^{i 66^\circ} \\ 0.0073 e^{-i 25^\circ} & -0.0555 e^{-i 25^\circ} & 0.9746 & 0.2168 e^{-i 1^\circ} \\ -0.0044 e^{-i 10^\circ} & -0.1136 e^{-i 70^\circ} & -0.2200 & 0.9688 \end{pmatrix}$$

$$V_{t's} = 0.1136 e^{-i 70^\circ}, \quad V_{ts} \approx -0.055 e^{-i 25^\circ}, \quad V_{t'b} \approx 0.217 e^{-i 1^\circ}, \\ V_{cb'} \approx 0.0415, \quad V_{ub'} \approx 0.0281 e^{i 61^\circ}, \quad V_{t'b'} \approx 0.97,$$

HNS scenario for $\Delta\mathcal{A}_{K\pi}$

$$\begin{aligned}
 V_{t's} &\approx -0.114e^{-i70^\circ} \quad , \quad V_{ts} \approx -0.055e^{-i25^\circ} \quad , \quad V_{t'b} \approx 0.22e^{-i1^\circ} \quad , \\
 V_{cb'} &\approx 0.042 \quad , \quad V_{ub'} \approx 0.028e^{i61^\circ} \quad , \quad V_{t'b'} \approx 0.97 \quad , \\
 |V_{ts}^* V_{tb'}| &= 0.012 \quad , \quad |V_{t's}^* V_{t'b'}| = 0.11
 \end{aligned}$$

In our numerics we use:

- i) $V_{t's}^* V_{t'b'}$ as free parameter in the range $|V_{t's}^* V_{t'b'}| < 0.12$,
- ii) the CP phase is also free, if not its fixed to $\arg(-V_{t's}^* V_{t'b'}) = 70^\circ$,
- iii) $V_{ts} = -0.1 e^{-i10^\circ}$ and $V_{tb'} = 0.1$

The result is not very sensitive to $\arg(V_{ts})$, but may affect the zero of A_{CP}

$V_{cb'}$ is fixed by:

$$V_{us}^* V_{ub'} + V_{cs}^* V_{cb'} \approx -(V_{ts}^* V_{tb'} + V_{t's}^* V_{t'b'})$$

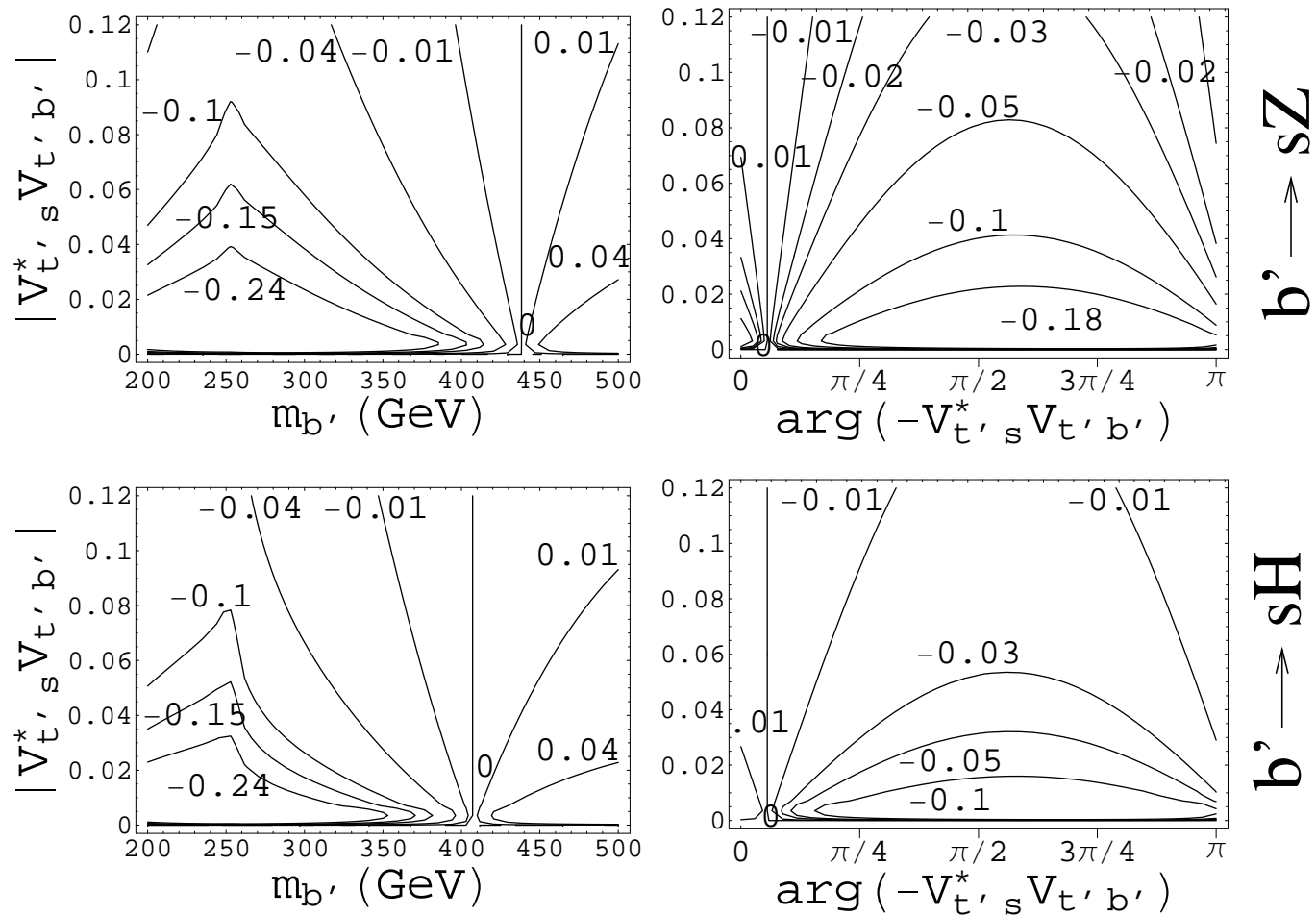


Figure 4: $m_{t'} = m_{b'} + 50$ GeV, $m_{b'} = 340$ GeV and $m_H = 120$ GeV, $V_{ts}V_{tb'} = -0.01 e^{-i10^\circ}$ and $\arg(-V_{t's}^* V_{t'b'}) = 70^\circ$

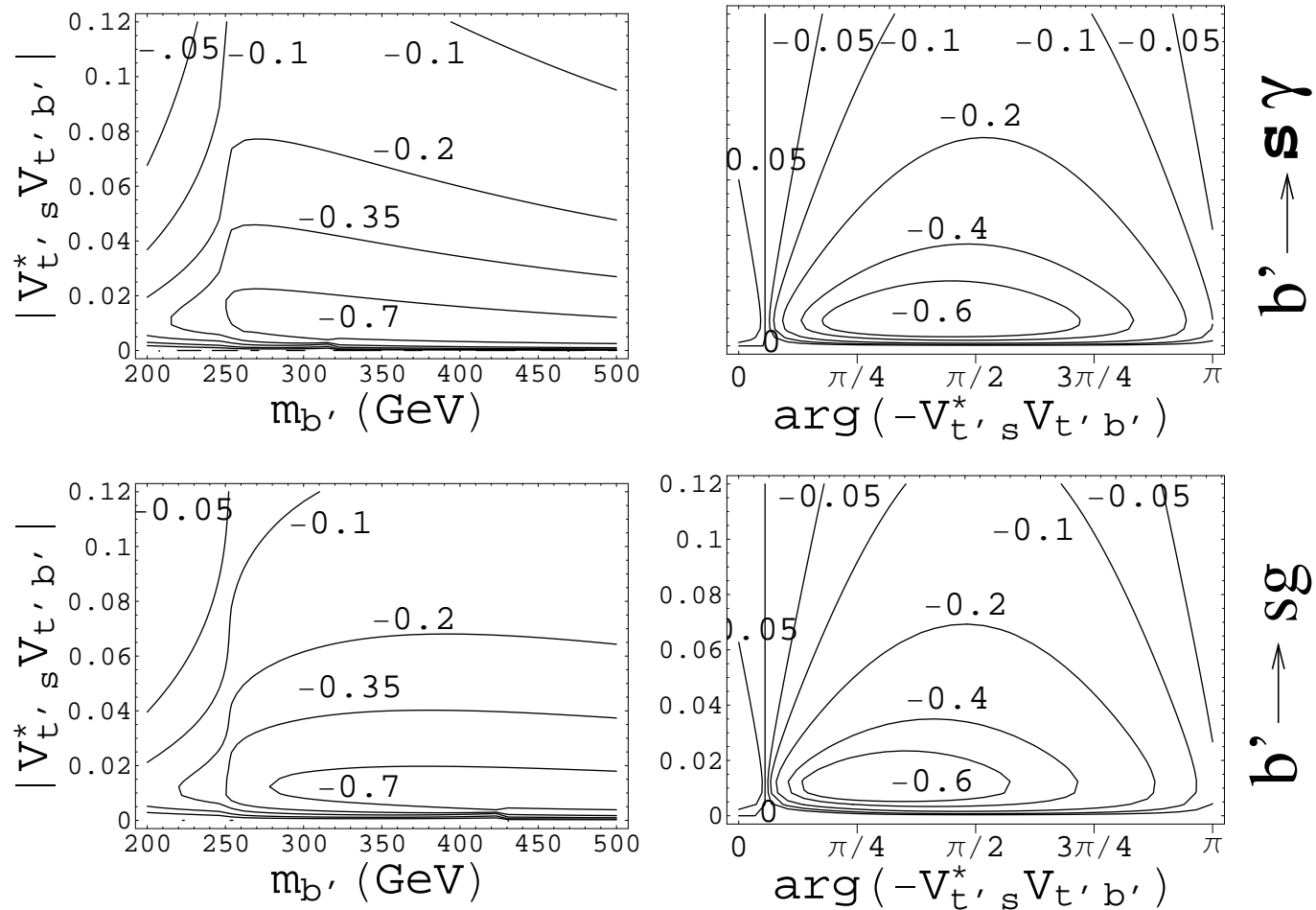


Figure 5: $m_{t'} = m_{b'} + 50$ GeV, $m_{b'} = 340$ GeV, $V_{t's}^* V_{t'b'} = -0.01 e^{i 10^\circ}$ and $\arg(-V_{t's}^* V_{t'b'}) = 70^\circ$

Short report on “CP violation and the fourth generation” by G. Eilam, B. Melic and J. Trampetic, PRD’09

- CPV in FCNC processes $t \rightarrow c X$, $b' \rightarrow s X$, $b' \rightarrow b X$, $t' \rightarrow c X$, and $t' \rightarrow t X$, with $X = H, Z, \gamma, g$ is done, by constructing and employing global, unique fit for the 4th generation mass mixing matrix CKM4 at $300 \leq m_{t'} \leq 700$ GeV.
- The fit procedure includes (similar [Bobrowski’09](#) , [Lenz talk](#)):
 - 1) Check of the unitarity of the CKM3 matrix in SM3
 - 2) $K^0 - \bar{K}^0$, $D^0 - \bar{D}^0$, $B_{d,s}^0 - \bar{B}_{d,s}^0$ mixings
 - 3) $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ and $B \rightarrow X_s \gamma$ processes
 - 4) $\sin 2\beta$ from $B \rightarrow J/\psi K$
 - 5) EW precision data constraint from [Chanowitz’09](#) which restrict the mixing between 3th and 4th generation to be of the order Cabibbo angle.

$$V_{\text{CKM4}} = R_{34} \cdot R_{24} \cdot R_{14} \cdot V_{\text{CKM3}} ; \quad R_{34} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & c_{34} & s_{34} \\ 0 & 0 & -s_{34} & c_{34} \end{pmatrix}$$

$$R_{24} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & c_{24} & 0 & s_{24}e^{-i\phi_2} \\ 0 & 0 & 1 & 0 \\ 0 & -s_{24}e^{i\phi_2} & 0 & c_{24} \end{pmatrix}, \quad R_{14} =$$

$$\begin{pmatrix} c_{14} & 0 & 0 & s_{14}e^{-i\phi_3} \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ -s_{14}e^{i\phi_3} & 0 & 0 & c_{14} \end{pmatrix}$$

$s_{14,24,34}$ and $\phi_{2,3}$ need to be fitted.

$m_{t'} (\text{GeV})$	$ \sin \theta_{34} $	$\chi_{\text{min}}^2/d.o.f$
300	0.25 ± 0.04	0.85
350	0.13 ± 0.03	0.98
400	0.10 ± 0.02	0.84
500	0.10 ± 0.04	0.80
600	0.11 ± 0.03	0.93
700	0.11 ± 0.02	1.17
800	0.11 ± 0.02	1.45
1000	0.11 ± 0.02	2.07

Table 1: Results of our fit on the mixing between the third and the fourth generation obtained including the EW constraints from Chanowitz'09.

V_{CKM4} for $m_{t'} = 300$ and 400 GeV respectively

$$\begin{pmatrix} 0.9742 & 0.2257 & 0.0035e^{-68.9^\circ i} & 0.0018e^{-12.4^\circ i} \\ -0.2255 & 0.9732 & 0.0414 & 0.0102e^{29.8^\circ i} \\ 0.0086e^{-24.1^\circ i} & -0.0416e^{0.7^\circ i} & 0.9649 & 0.2589 \\ -0.0019e^{18.9^\circ i} & 0.0052e^{69.3^\circ i} & -0.2591 & 0.9658 \end{pmatrix},$$

$$\begin{pmatrix} 0.9740 & 0.2256 & 0.0036e^{-68.9^\circ i} & 0.0164e^{-87.4^\circ i} \\ -0.2259 & 0.9728 & 0.0414 & 0.0290e^{-76.1^\circ i} \\ 0.0092e^{-27.7^\circ i} & -0.0414 & 0.9932 & 0.1079 \\ -0.0091e^{89.9^\circ i} & 0.0310e^{-94.6^\circ i} & -0.1082 & 0.9935 \end{pmatrix},$$

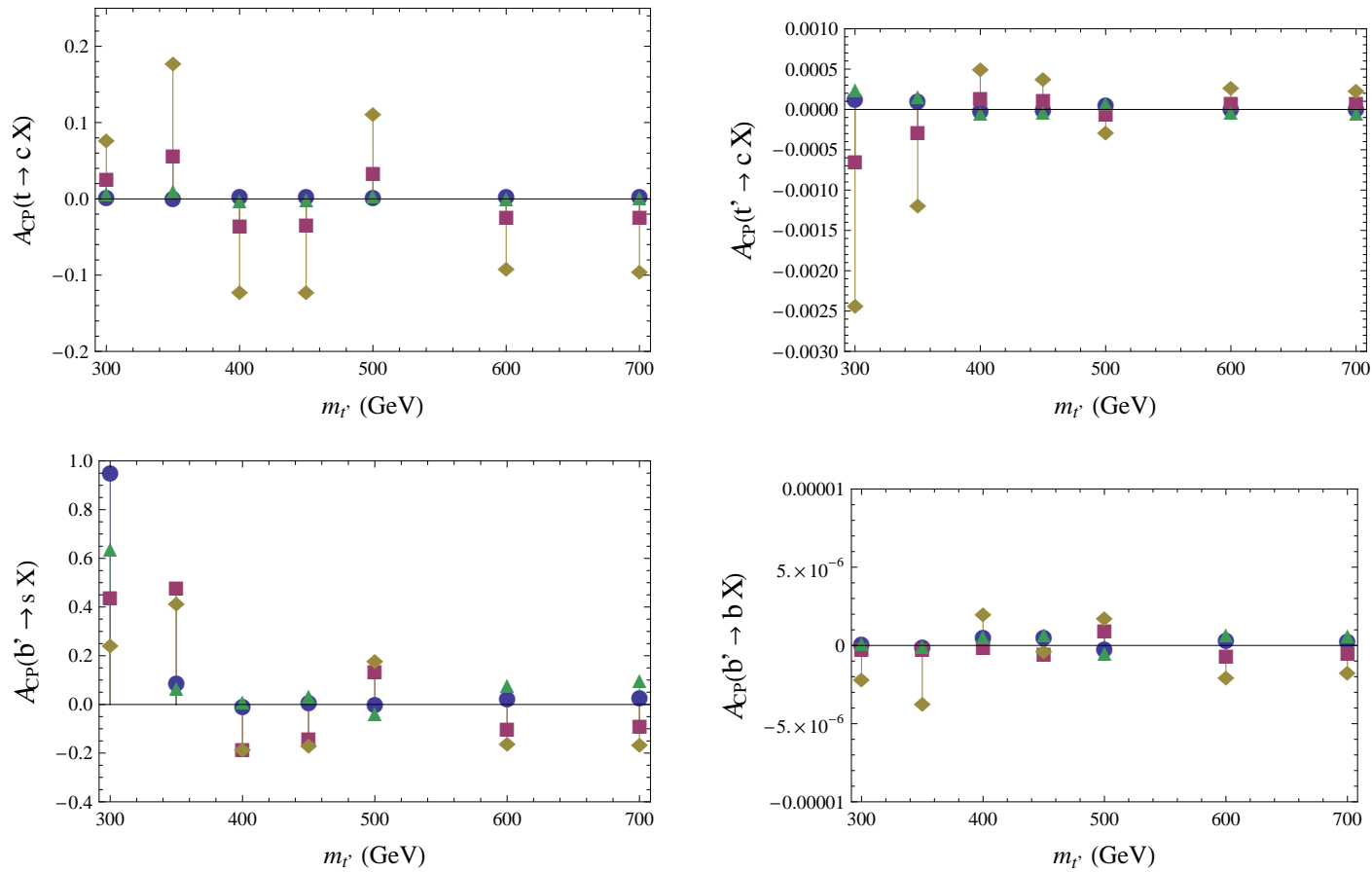


Figure 6: X denotes possible decays to $X = H(\bullet)$, $Z(\blacktriangle)$, $\gamma(\blacksquare)$, $g(\blacklozenge)$

Is it possible to observe CPV in b' at LHC , ILC?

Br for $b' \rightarrow sX$

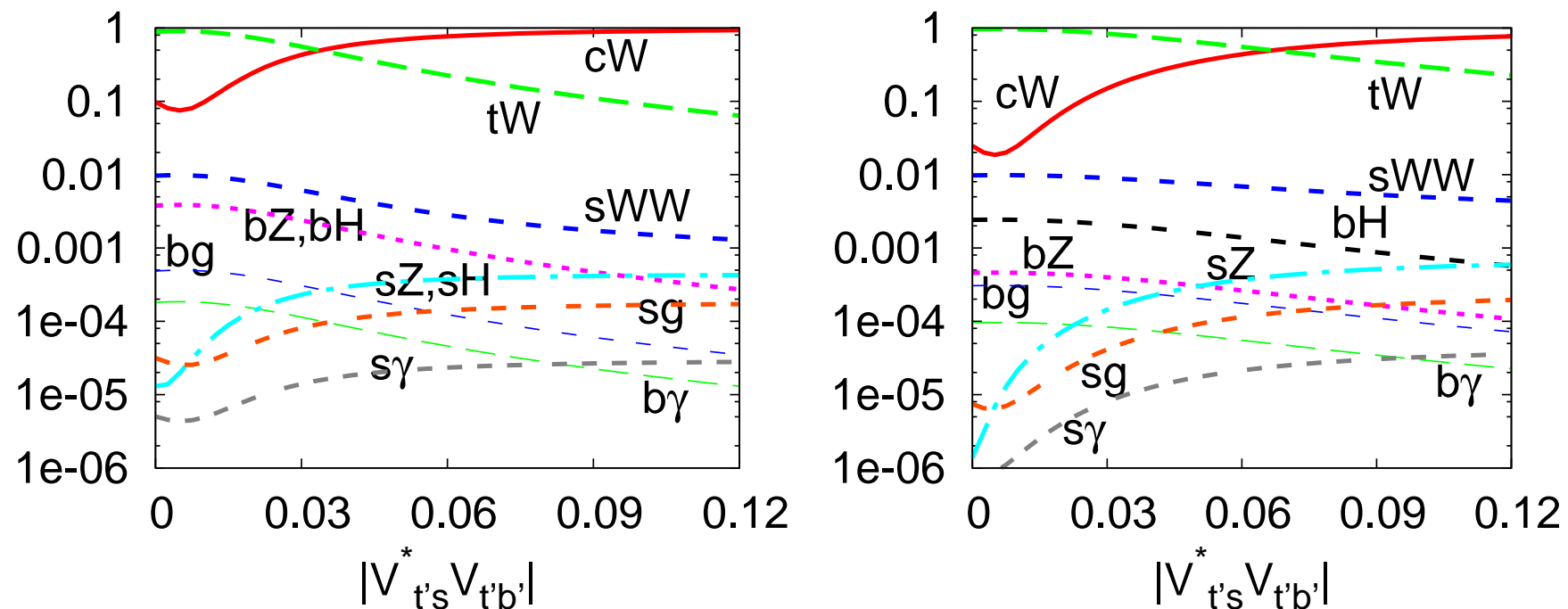
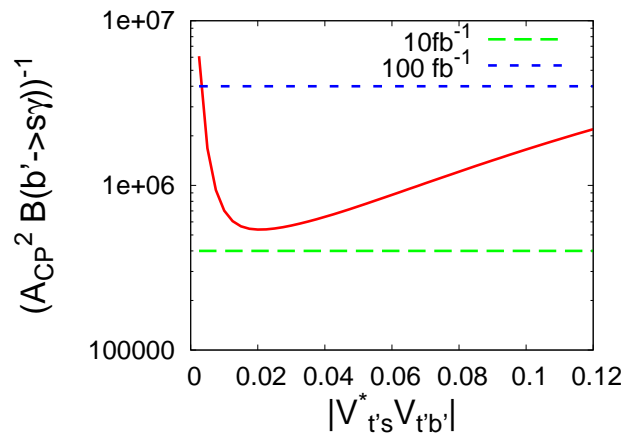
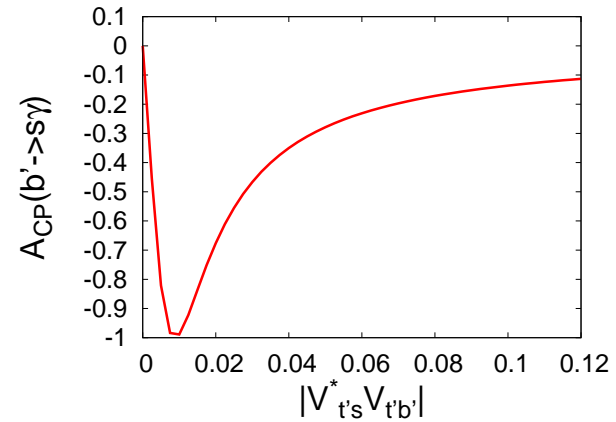
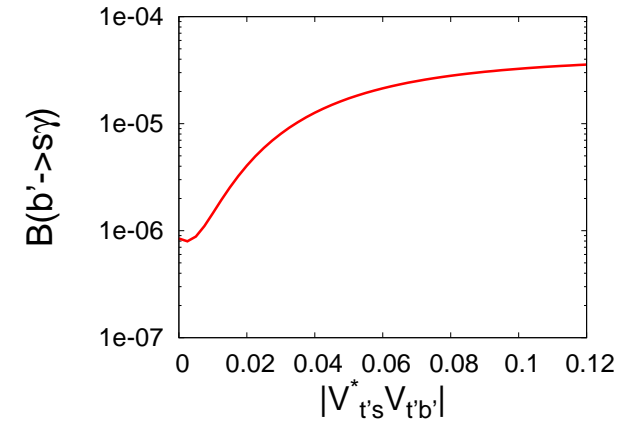


Figure 7: $m_{b'} = 260, 340$ GeV, $m_{t'} = m_{b'} + 50$ GeV,
 $V_{ts}V_{tb'} = -0.01 e^{-i10^\circ}$ and $\arg(-V_{t's}^* V_{t'b'}) = 70^\circ$

Is it possible to observe CPV in b' at LHC , ILC?



$$\sigma(e^+e^- \rightarrow b'\bar{b}') \times 1000 \text{ fb}^{-1} = 65000 \text{ events}$$

Figure 8: $m_{b'} = 340 \text{ GeV}$, $m_{t'} = m_{b'} + 50 \text{ GeV}$, $V_{ts} V_{tb'} = -0.01 e^{-i 10^\circ}$ and $\arg(-V_{t's}^* V_{t'b'}) = 70^\circ$

Conclusions

- the LHC has the capability to produce b' and t' and measure some of their decays, including FCNC decays such as $b' \rightarrow bX$ and $t' \rightarrow tX$.
- the LHC has also the capability to probe CPV in top quark and also in $b' \rightarrow s$ transitions
- the best mode to probe CPV in b' decays is $b' \rightarrow s\gamma$ due to the presence of high energy single photon in the final state
- once CPA is measured, the CPV phase could be extracted with little theoretical uncertainty.

The longitudinal part of $b' \rightarrow sZ$ is:

$$\begin{aligned} Z_L^L &= A_L(m_{b'}^2 + m_Z^2)/2 + B_L(m_{b'}^2 - m_s^2 - m_Z^2)/2 - m_s C_R + m_{b'} C_L, \\ Z_L^R &= A_R(m_{b'}^2 + m_Z^2)/2 + B_R(m_{b'}^2 - m_s^2 - m_Z^2)/2 + m_{b'} C_R - m_s C_L, \end{aligned}$$

$$\Delta_V^L(Q, 0) = Z_L^R(Q) - Z_L^R(m_c) \approx Z_L^R(Q) - Z_L^R(0),$$

$$\Delta_V^T(Q, 0) = C_R(Q) - C_R(m_c) \approx C_{L,R}(Q) - C_{L,R}(0),$$

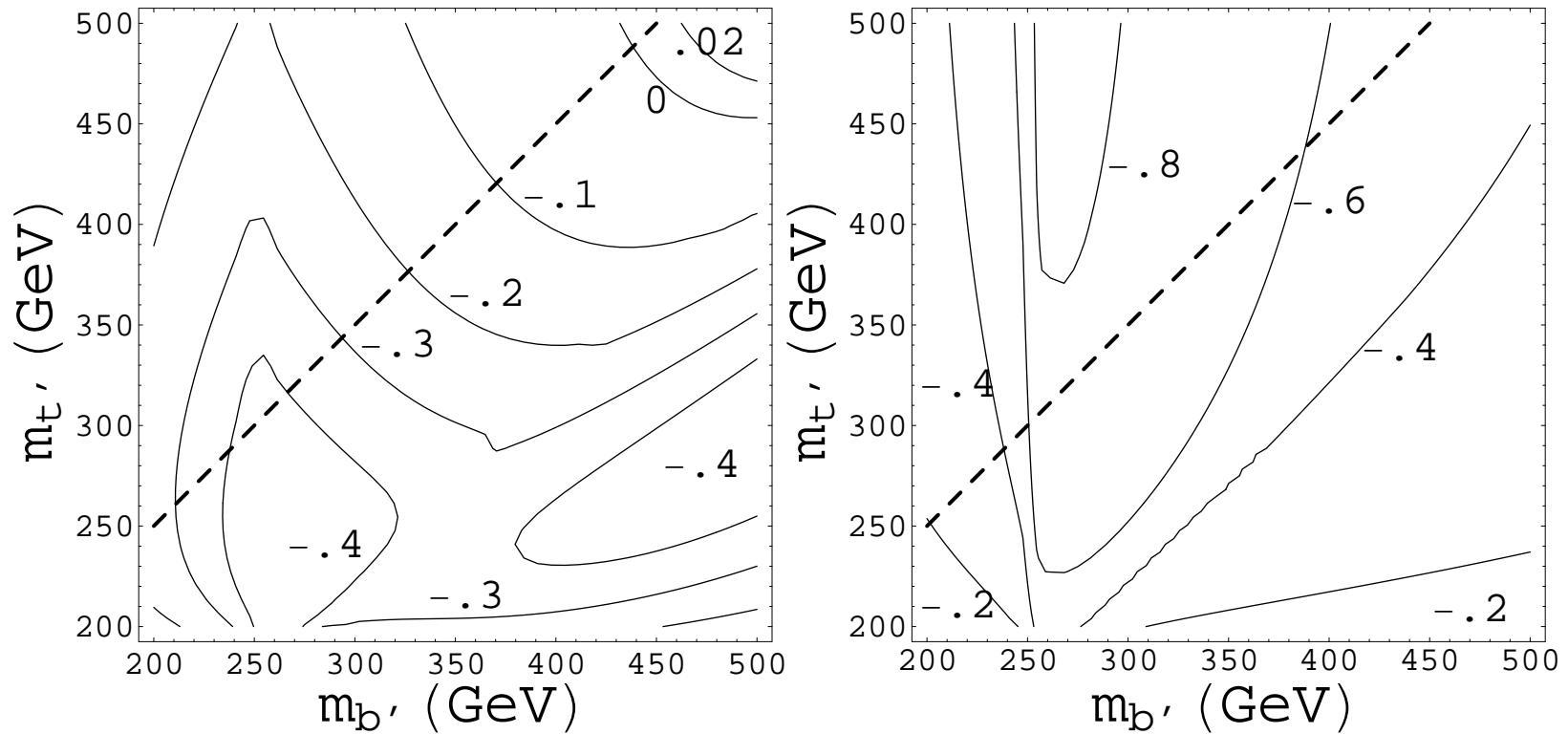


Figure 9: $V_{ts}^* V_{tb'} = -0.01e^{i10^\circ}$ and $\arg(-V_{t's}^* V_{t'b'}) = -0.02e^{i70^\circ}$. The dashed line is for $m_{t'} = m_{b'} + 50 \text{ GeV}$