

# Neutral Higgs-pair production at 1-loop from a generic 2HDM

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at 1-loop within the general 2HDM*

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- To single out the most favorable regions for the 2H production, and to correlate them with alternative multiparticle Higgs-boson final states
- To quantify the importance of RADCOR's associated to these processes
- To evaluate the impact of the potentially enhanced 3H self-couplings.

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- The Two-Higgs Doublet Model
- Leading-order 2H production revisited

## 2 Quantum corrections to neutral Higgs-pair production

- Overview
- Renormalization of the 2HDM
- Numerical results

## 3 Phenomenological footprints of 3H self-interactions

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Based on the following references:

- DLV, J. Solà arXiv:0908.2898 [hep-ph]
- G. Ferrera, J. Guasch, DLV, J. Solà, *Phys. Lett.* **B659** (2007) 297-307, arXiv:0707.3162 [hep-ph]; PoS RADCOR 2007:043,2007, arXiv:0801.3907 [hep-ph]
- R. N. Hodgkinson, DLV, J. Solà, *Phys. Lett.* **B673** (2009) 47-56, arXiv:0901.2257 [hep-ph]

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# The Two-Higgs Doublet Model: basic settings

- Canonical extension of the SM Higgs sector with a second  $SU_L(2)$  doublet with weak hypercharge  $Y=1$
- The Higgs potential can be written as:

$$\begin{aligned}
 V(\Phi) = & \lambda_1 \left( \Phi_1^\dagger \Phi_1 - \frac{v_1^2}{2} \right)^2 + \lambda_2 \left( \Phi_2^\dagger \Phi_2 - \frac{v_2^2}{2} \right)^2 + \\
 & + \lambda_3 \left( \Phi_1^\dagger \Phi_1 - \frac{v_1^2}{2} + \Phi_2^\dagger \Phi_2 - \frac{v_2^2}{2} \right)^2 + \\
 & + \lambda_4 \left[ (\Phi_1^\dagger \Phi_1)(\Phi_2^\dagger \Phi_2) - (\Phi_1^\dagger \Phi_2)(\Phi_2^\dagger \Phi_1) \right] \\
 & + \lambda_5 \left[ \text{Re}(\Phi_1^\dagger \Phi_2) - \frac{v_1 v_2}{2} \cos \chi \right]^2 + \lambda_6 \left[ \text{Im}(\Phi_1^\dagger \Phi_2) - \frac{v_1 v_2}{2} \sin \chi \right]^2
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# The Two-Higgs Doublet Model: degrees of freedom

- 8 real degrees of freedom:

$$\Phi_1 = \begin{pmatrix} \Phi_1^0 \\ \Phi_1^- \end{pmatrix} = \begin{pmatrix} \frac{v_1 + \phi_1^0 + i\chi_1^0}{\sqrt{2}} \\ \phi_1^- \end{pmatrix}$$

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- 3 Goldstone bosons ( $G^0, G^\pm$ )
- 5 physical Higgs fields: 2  $\mathcal{CP}$ -even Higgs bosons ( $h^0, H^0$ ), 1  $\mathcal{CP}$ -odd Higgs boson  $A^0$  and 2 charged Higgs bosons  $H^\pm$

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# The Higgs sector in the general 2HDM: parameters

- 7 free parameters:
  - 6 couplings in the Higgs potential,  $\lambda_i \quad i = 1 \dots 6$
  - 2 VEV's,  $v_1, v_2$  with one constraint:  $v^2 \equiv v_1^2 + v_2^2 = G_F^{-1}/\sqrt{2}$
- The masses of the physical Higgs particles ( $M_{h^0}, M_{H^0}, M_{A^0}, M_{H^\pm}$ )
- The ratio of the two VEV's,  $\tan \beta \equiv \frac{\langle H_2^0 \rangle}{\langle H_1^0 \rangle} \equiv \frac{v_2}{v_1}$
- The mixing angle  $\alpha$  between the two neutral  $CP$ -even states
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# Phenomenological and Theoretical constraints

- $H^\pm$  contribution to  $\mathcal{B}(b \rightarrow s\gamma)$ :  $M_{H^\pm} > 295$  GeV (for Type-II 2HDM) Misiak et al., 2006.
- Higgs-boson one-loop corrections to  $\rho$ :  $|\delta\rho_{2HDM}| \lesssim 10^{-3}$  Barbieri & Maiani, 1983
- Perturbativity on the Higgs-quark Yukawa couplings:  

$$Y_t \propto \frac{m_t}{v \tan \beta} \quad Y_b \propto \frac{m_b \tan \beta}{v} \Rightarrow$$
  
 $0.3 < \tan \beta \lesssim 60$  El Kaffas, Osland & Greid, 2007
- Vacuum stability Kanemura, Kasai & Okada, 1999
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# $CP$ -allowed 2H channels

$$\begin{array}{lll} e^+e^- & \rightarrow & H^\pm H^\mp \\ e^+e^- & \rightarrow & h^0 A^0 \\ e^+e^- & \rightarrow & H^0 A^0 \end{array} \quad \left. \right\} \text{LO: tree-level diagrams } (\mathcal{O}(\alpha_{ew}^2)), \sigma \sim 0.01 - 0.1 \text{ pb.}$$

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$$C_{\text{2HDM}}(h^0 A^0 Z) = \frac{e \cos(\beta - \alpha)}{2 \sin \theta_W \cos \theta_W}$$

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- ♣ There is no dynamical distinction between the general 2HDM and the MSSM
- ♣ Dedicated studies on radiative corrections in 2H processes are hence mandatory:  
Chankowski, Pokorski, Driesen, Hollik, Rosiek ['96]; Arhrib, Moultaka ['98]; Guasch, Hollik, Kraft ['01]; Heinemeyer et al. ['01]

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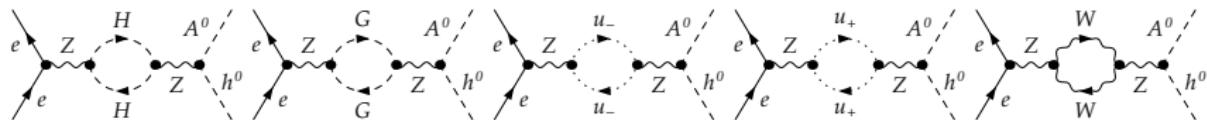
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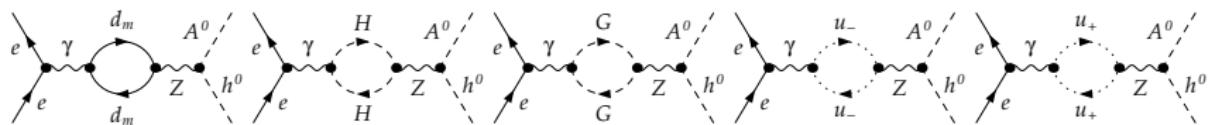
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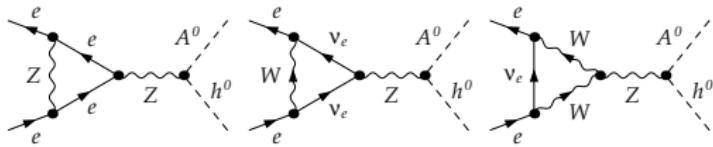
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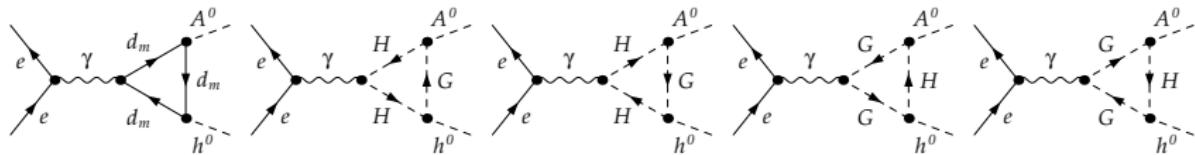
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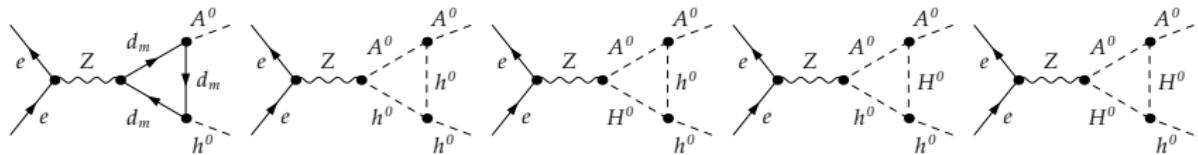
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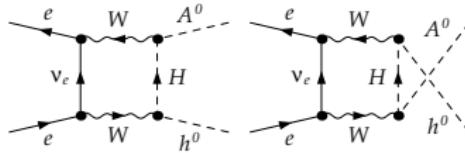
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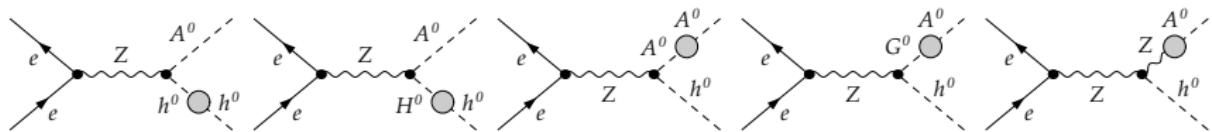
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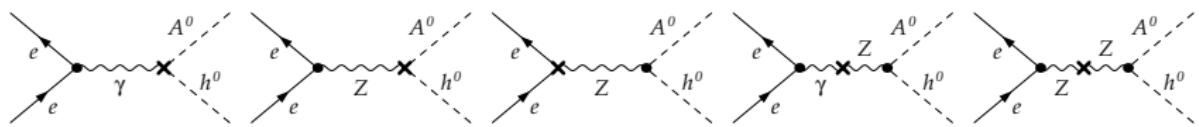
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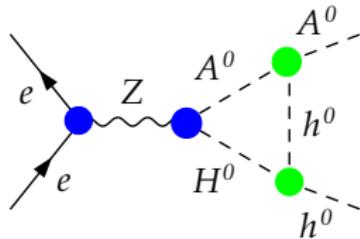
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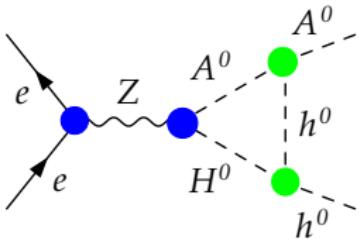
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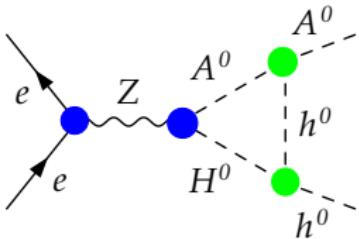
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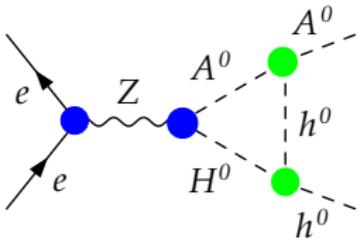
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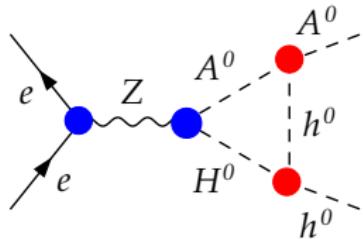


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$$\Gamma_{A^0 h^0 Z^0}^{eff} \sim \Gamma_{A^0 h^0 Z^0}^0 \frac{\lambda_{3H}^2}{16\pi^2 s} f(M_{h^0}^2/s, M_{A^0}^2/s)$$

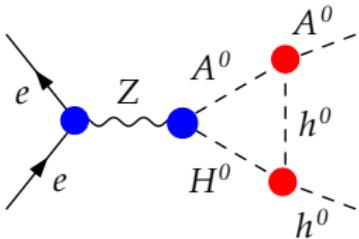
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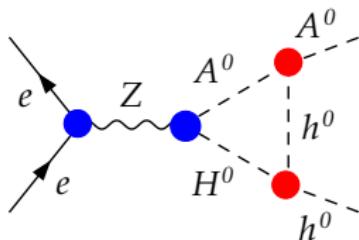
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SUSY invariance enforces the 3H couplings to be gauge-like, thus  
**no enhancement is present**

# Renormalization of the Higgs sector

- ♣ Higgs fields: 1 WF constant per  $SU_L(2)$  doublet

$$\begin{pmatrix} \Phi_1^+ \\ \Phi_1^0 \end{pmatrix} \rightarrow Z_{\Phi_1}^{1/2} \begin{pmatrix} \Phi_1^+ \\ \Phi_1^0 \end{pmatrix}, \quad \begin{pmatrix} \Phi_2^+ \\ \Phi_2^0 \end{pmatrix} \rightarrow Z_{\Phi_2}^{1/2} \begin{pmatrix} \Phi_2^+ \\ \Phi_2^0 \end{pmatrix},$$

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Higgs fields (OS scheme) **Dabelstein ['94], Chankowski et al ['95]**

$$\text{Re } \hat{\Sigma}'_{A^0 A^0}(k^2) \Big|_{k^2=M_{A^0}^2} = 0 \quad , \quad \text{Re } \hat{\Sigma}_{A^0 Z^0}(k^2) \Big|_{k^2=M_{A^0}^2} = 0$$

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**Physical content of the OS conditions:**

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- Likewise, the absence of  $A^0 - G^0$  mixing is guaranteed by the Slavnov-Taylor identity:

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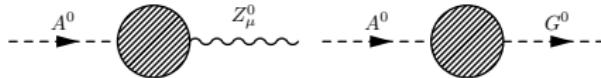
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## Higgs masses (OS scheme)

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- ♠ The same condition ensures that the  $CP$ -even Higgs final state is on-shell, as the *physical* masses must fulfill

$$\left(p^2 - M_{H^0}^2 + \hat{\Sigma}_{H^0 H^0}\right) \left(p^2 - M_{h^0}^2 + \hat{\Sigma}_{h^0 h^0}\right) - \hat{\Sigma}_{h^0 H^0}^2 = 0.$$

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$$\delta_r = \frac{\sigma^{(0+1)-\sigma^{(0)}}}{\sigma^{(0)}} \left\{ \begin{array}{l} \sqrt{s} = 0.5 \text{ TeV} : 50\% \\ \sqrt{s} = 1.0 \text{ TeV} : -50\% \end{array} \right.$$

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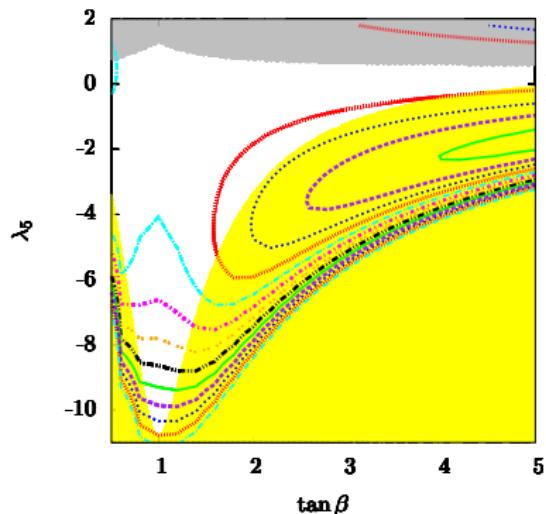
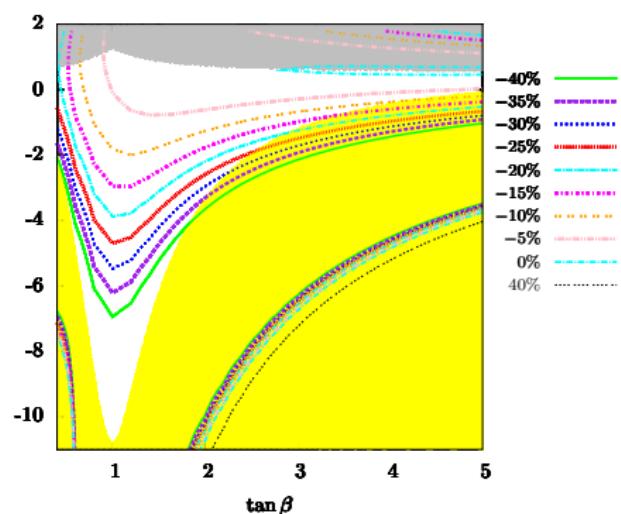
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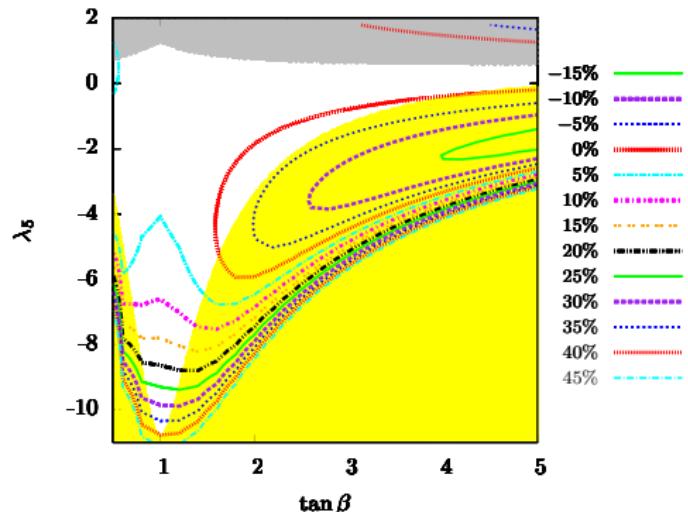
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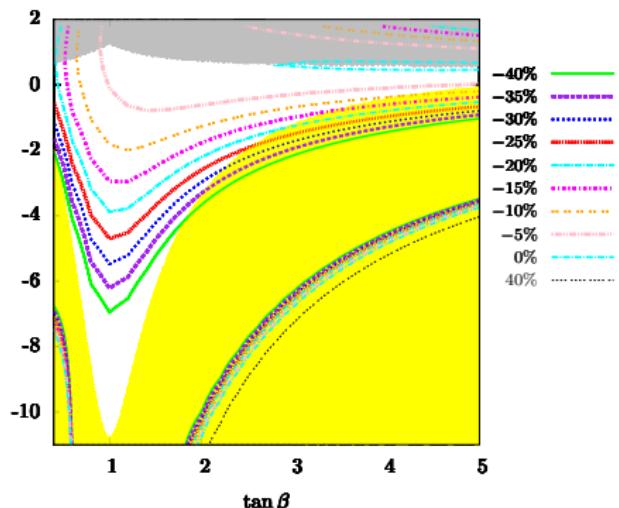
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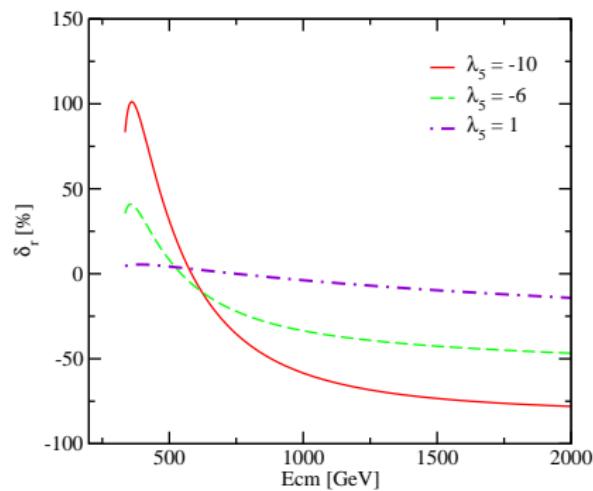
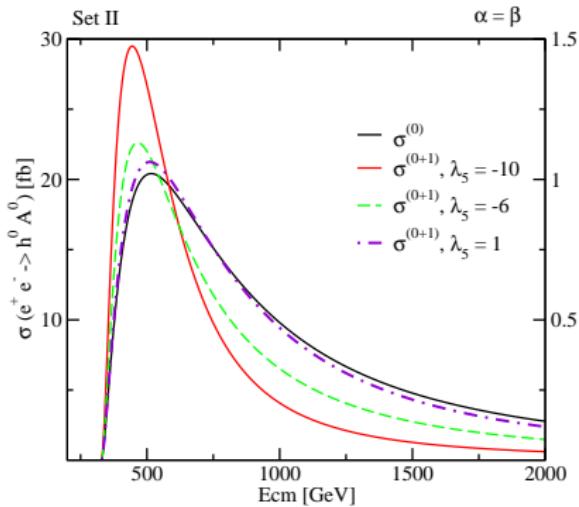
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$$\sim 2 \times 10^4 \text{ events per } 500 \text{ fb}^{-1}$$

# $e^+ e^- \rightarrow A^0 h^0$ phenomenology in a nutshell

$\tan \beta$	$\alpha$	$M_{h^0}$ [ GeV ]	$M_{H^0}$ [ GeV ]	$M_{A^0}$ [ GeV ]	$M_{H^\pm}$ [ GeV ]
1	$\beta$	130	150	200	160



# $e^+ e^- \rightarrow A^0 h^0$ phenomenology in a nutshell

♠  $\sqrt{s} = 500$  GeV

		$\alpha = \beta$	$\alpha = \beta - \pi/3$	$\alpha = \beta - \pi/6$	$\alpha = \pi/2$
Set II	$\sigma_{max}$ [fb]	26.71	7.34	20.05	13.10
	$\delta_r$ [%]	31.32	44.43	31.42	28.81
Set III	$\sigma_{max}$ [fb]	11.63	3.60	9.08	6.36
	$\delta_r$ [%]	35.17	67.59	40.68	47.86
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Set II	130	150	200	160	Type I
Set III	150	200	260	300	Type II
Set IV	95	205	200	215	Type I

# $e^+ e^- \rightarrow A^0 h^0$ phenomenology in a nutshell

♠  $\sqrt{s} = 1 \text{ TeV}$

		$\alpha = \beta$	$\alpha = \beta - \pi/3$	$\alpha = \beta - \pi/6$	$\alpha = \pi/2$
Set II	$\sigma_{max} [\text{fb}]$	4.08	0.85	2.70	1.56
	$\delta_r [\%]$	-58.42	-65.14	-63.28	-68.11
Set III	$\sigma_{max} [\text{fb}]$	6.11	1.39	4.22	2.86
	$\delta_r [\%]$	-30.16	-36.36	-35.62	-34.58
Set IV	$\sigma_{max} [\text{fb}]$	5.99	1.19	2.65	1.67
	$\delta_r [\%]$	-40.53	-52.78	-64.96	-66.81

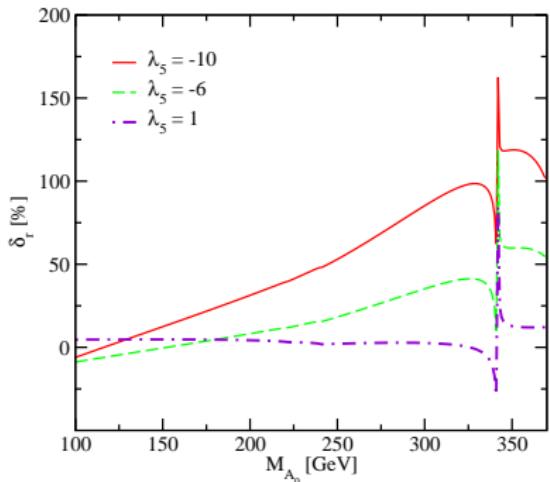
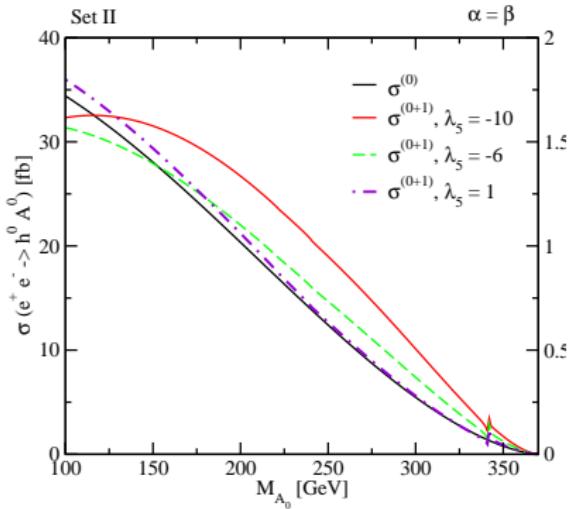
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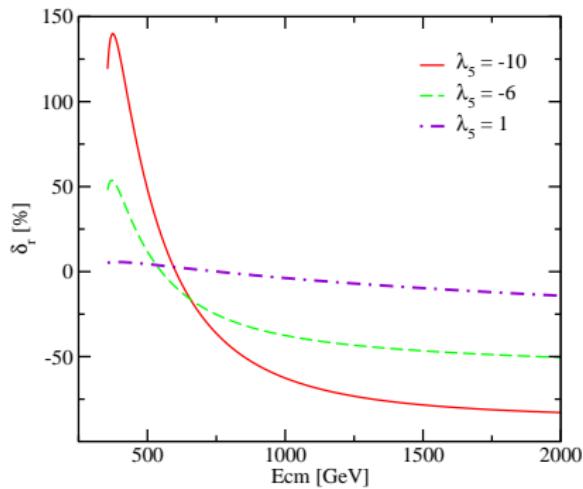
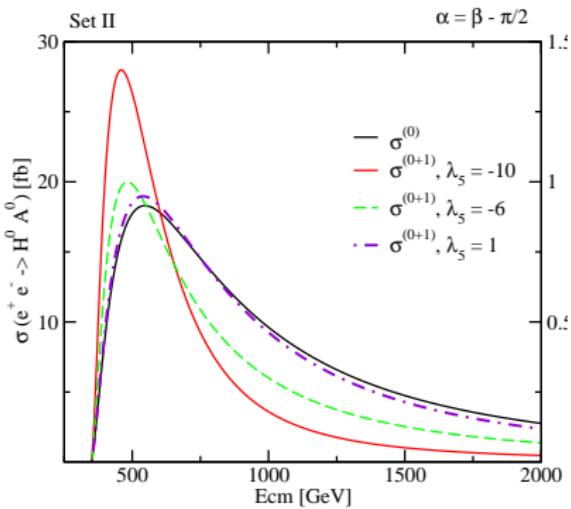


♠ Distinctive signature from the MSSM – wherein  $\cos(\beta - \alpha)$  becomes suppressed with growing  $M_{A^0}$ .

# $e^+e^- \rightarrow A^0H^0$ phenomenology in a nutshell

♣ The basic phenomenological trends are recovered for the  $H^0A^0$  channel.

$\tan\beta$	$\alpha$	$M_{h^0}$ [ GeV ]	$M_{H^0}$ [ GeV ]	$M_{A^0}$ [ GeV ]	$M_{H^\pm}$ [ GeV ]
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# Outline

## 1 Theoretical setup

- The Two-Higgs Doublet Model
- Leading-order 2H production revisited

## 2 Quantum corrections to neutral Higgs-pair production

- Overview
- Renormalization of the 2HDM
- Numerical results

## 3 Phenomenological footprints of 3H self-interactions

## 4 Conclusions

# Probing the 3H self-couplings at Linear Colliders

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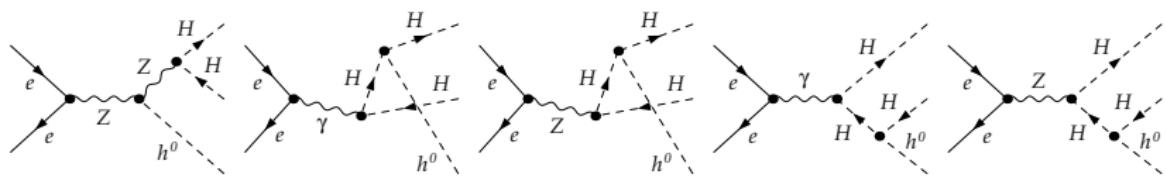
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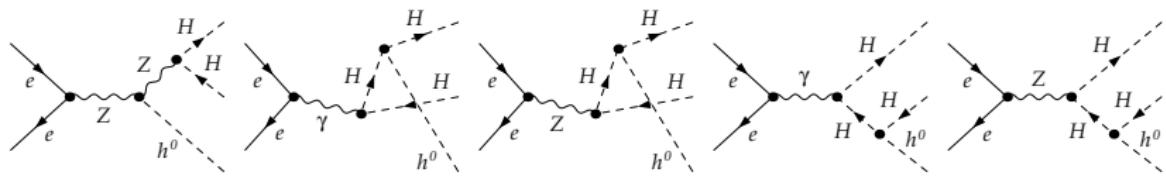
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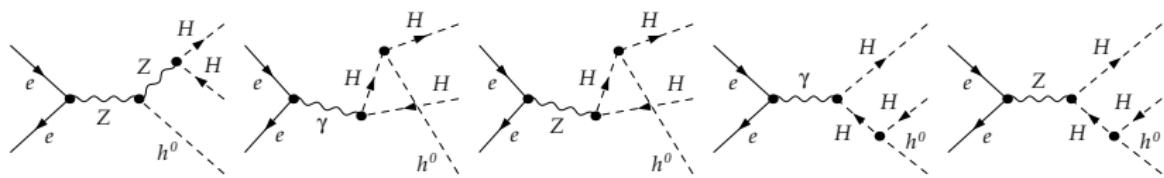
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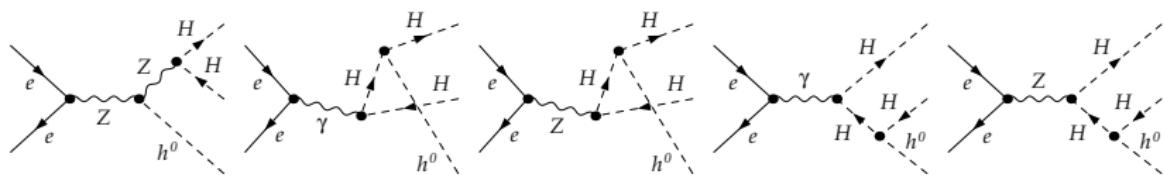
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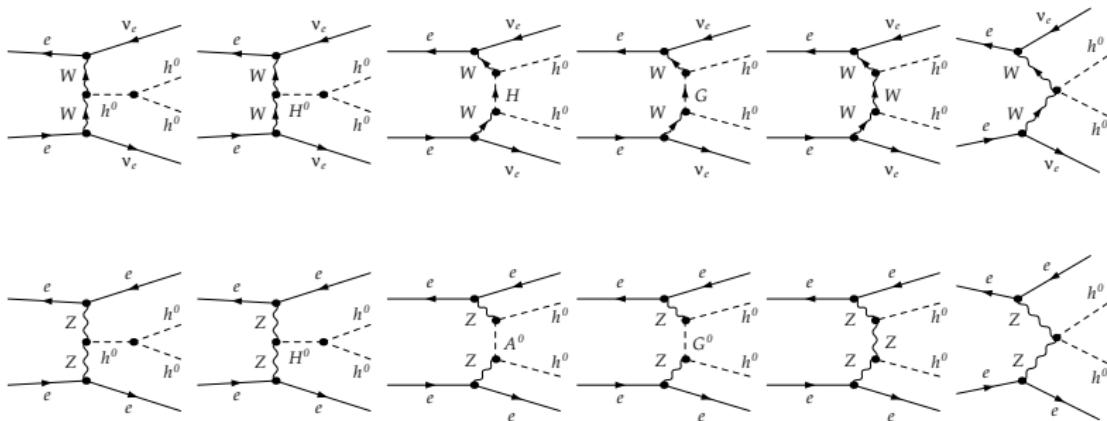
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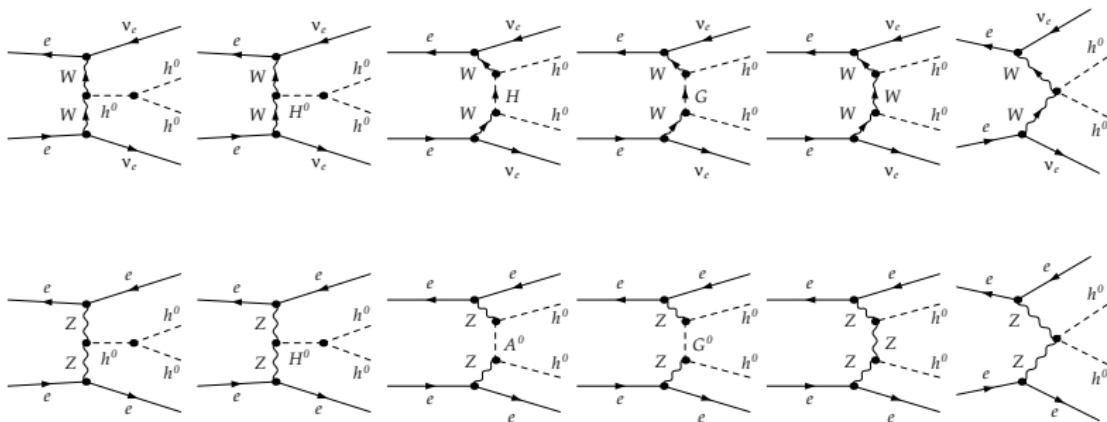
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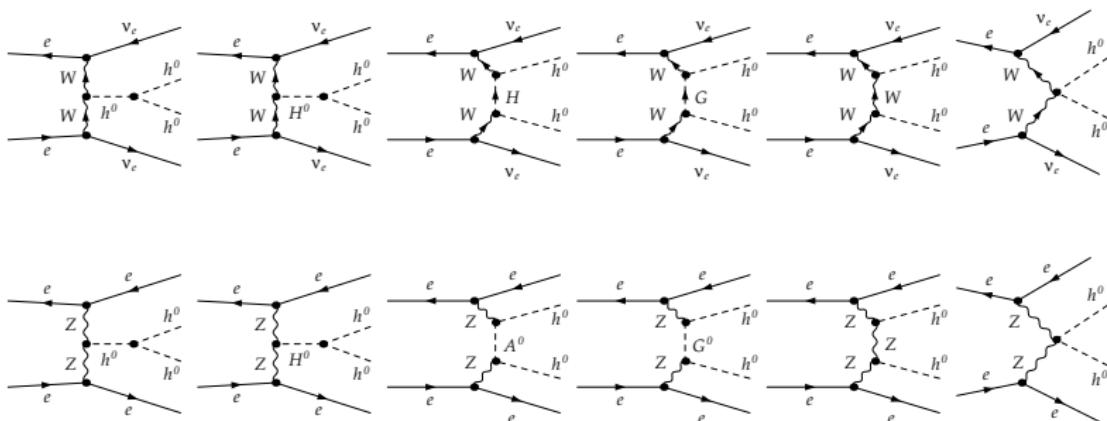
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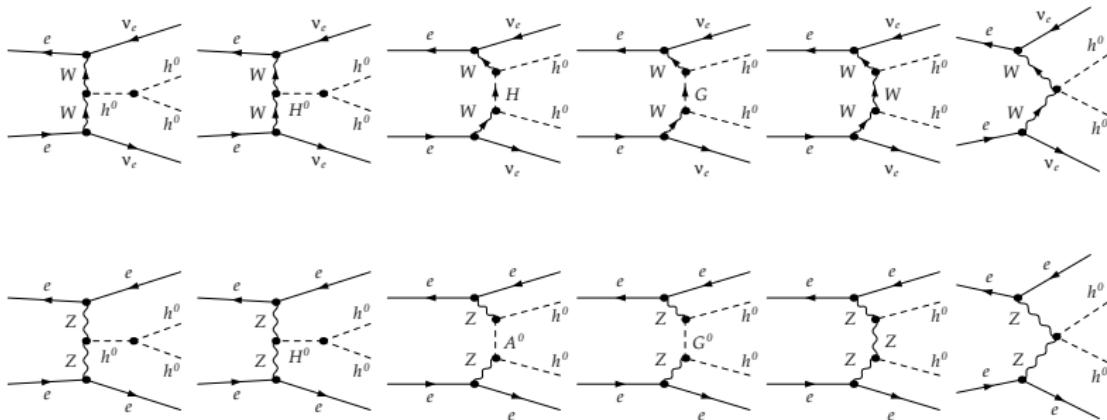
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**Hodgkinson, DLV, Solà [’09].**

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# Compared predictions for 2H and 3H events

$\tan \beta$	$\alpha$	$\lambda_5$	$M_{h^0}$ [ GeV ]	$M_{H^0}$ [ GeV ]	$M_{A^0}$ [ GeV ]	$M_{H^\pm}$ [ GeV ]
1	$\beta$	-10	130	150	200	160

Process	$\sigma(\sqrt{s} = 0.5 \text{ TeV})[\text{fb}]$	$\sigma(\sqrt{s} = 1.0 \text{ TeV})[\text{fb}]$	$\sigma(\sqrt{s} = 1.5 \text{ TeV})[\text{fb}]$
$h^0 A^0$	26.71	4.07	1.27
$h^0 H^0 A^0$	0.02	5.03	3.55
$H^0 H^+ H^-$	0.17	11.93	8.39
$h^0 h^0 + X$	1.47	17.36	38.01

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# Outline

## 1 Theoretical setup

- The Two-Higgs Doublet Model
- Leading-order 2H production revisited

## 2 Quantum corrections to neutral Higgs-pair production

- Overview
- Renormalization of the 2HDM
- Numerical results

## 3 Phenomenological footprints of 3H self-interactions

## 4 Conclusions

# Conclusions

- We have presented a complete  $\mathcal{O}(\alpha_{ew}^3)$  calculation of the pairwise production of neutral Higgs bosons ( $A^0 h^0 \{H^0\}$ ) at Linear Colliders within the general 2HDM.
- Our analysis identifies sizable quantum effects:
  - up to 50%
  - in regions with  $\tan\beta \sim 1$  and  $|\lambda_5| \sim 5 - 10$  ( $\lambda_5 < 0$ )
  - either positive ( $\sqrt{s} = 0.5$  TeV) and negative ( $\sqrt{s} = 1.0$  TeV)
  - sourced by the Higgs-mediated vertex corrections at one-loop, which are sensitive to the potentially enhanced 3H self-couplings
- The production rates at  $\sqrt{s} = 0.5$  TeV may amount up to **a few thousands** of 2H events per  $500\text{ fb}^{-1}$ .
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THANK YOU !

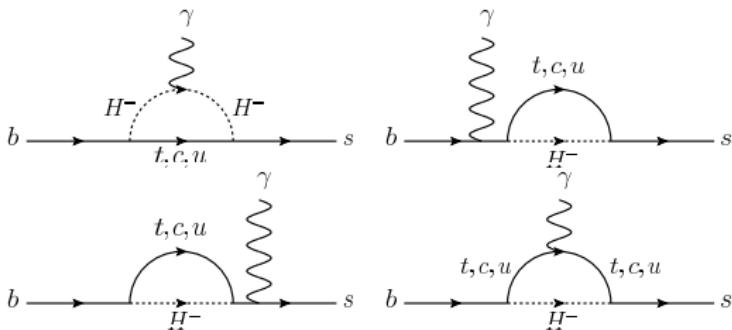


BACKUP !

# Restrictions: $\mathcal{B}(b \rightarrow s\gamma)$

- We have strong constraints coming from flavor physics  
 $\mathcal{B}(\bar{B} \rightarrow X_s \gamma) \sim (3.55 \pm 0.25) \cdot 10^{-4}$  from BaBar and Belle  
 $\mathcal{B}(\bar{B} \rightarrow X_s \gamma) \sim (3.15 \pm 0.23) \cdot 10^{-4}$  SM NNLO prediction
- The good agreement between the SM prediction and the experimental result puts severe constraints on the flavor structure of NP models.

New charged-particles contribute to this rare decay.



Leading-order contributions due to the charged Higgs  $H^\pm$

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The charged Higgs bosons contribution:

- positive
- increases when  $M_{H^\pm}$  decreases

Type-I 2HDM:      Couplings  $H^\pm qq' \propto 1/\tan\beta$

Couplings highly suppressed for  $\tan\beta > 1$

Type-II 2HDM:      Couplings  $H^\pm qq' \propto \tan\beta$

Couplings enhanced for  $\tan\beta > 1$

Restriction     $M_{H^\pm} > 295$  GeV

Misiak et al., 2006

# Restrictions: $\delta\rho$

- rho-parameter:  $\rho = \rho_0 + \delta\rho$

$$\rho = \frac{M_W^2}{M_Z^2 \cos^2 \theta_W} = 1$$

One-loop corrections induced by Higgs bosons      Barbieri & Maiani, 1983

$$\begin{aligned} \delta\rho_{2HDM} = & \frac{G_F}{8\sqrt{2}\pi^2} \left\{ M_{H^\pm}^2 \left[ 1 - \frac{M_{A^0}^2}{M_{H^\pm}^2 - M_{A^0}^2} \ln \frac{M_{H^\pm}^2}{M_{A^0}^2} \right] \right. \\ & + \cos^2(\beta - \alpha) M_{h^0}^2 \left[ \frac{M_{A^0}^2}{M_{A^0}^2 - M_{h^0}^2} \ln \frac{M_{A^0}^2}{M_{h^0}^2} - \frac{M_{H^\pm}^2}{M_{H^\pm}^2 - M_{h^0}^2} \ln \frac{M_{H^\pm}^2}{M_{h^0}^2} \right] \\ & \left. + \sin^2(\beta - \alpha) M_{H^0}^2 \left[ \frac{M_{A^0}^2}{M_{A^0}^2 - M_{H^0}^2} \ln \frac{M_{A^0}^2}{M_{H^0}^2} - \frac{M_{H^\pm}^2}{M_{H^\pm}^2 - M_{H^0}^2} \ln \frac{M_{H^\pm}^2}{M_{H^0}^2} \right] \right\} \end{aligned}$$

Experimental measurements:  $|\delta\rho_{2HDM}| \lesssim 10^{-3}$   
 $\delta\rho_{2HDM}$  vanish for  $M_A \rightarrow M_{H^\pm}$

We will demand       $M_A \sim M_{H^\pm}$

# Restrictions: Perturbativity and Vacuum Stability

## Perturbativity on the Higgs-quark Yukawa couplings

$$H^\pm: Y_t \propto \frac{m_t}{v \tan \beta} \quad Y_b \propto \frac{m_b \tan \beta}{v} \Rightarrow \\ 0.3 < \tan \beta \lesssim 60$$

El Kaffas, Osland & Greid, 2007

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## Vacuum stability

We assume that the quartic interaction terms in the potential do not give negative contribution for all directions of scalar fields at each energy scale up to  $\Lambda$

Require a Higgs potential bounded from below

$$\lambda_1 + \lambda_3 > 0 \quad \lambda_2 + \lambda_3 > 0$$

$$2\sqrt{(\lambda_1 + \lambda_3)(\lambda_2 + \lambda_3)} + 2\lambda_3 + \lambda_4 + \frac{1}{2} \text{Min}\left(0, \lambda_5 + \lambda_6 - 2\lambda_4 - |\lambda_5 - \lambda_6|\right) > 0$$

Kanemura, Kasai & Okada, 1999

# Unitarity bounds

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Numerous extended analyses for the 2HDM

Higgs and Goldstone boson  $2 \rightarrow 2$  S-matrix elements,  $S_{ij} \Rightarrow$  Unitarity condition over its eigenvalues  $|\alpha_i| < 1/2 \forall i$ .

e.g.

$$a_{\pm} = \frac{1}{16\pi} \left\{ 3(\lambda_1 + \lambda_2 + 2\lambda_3) \pm \left( \sqrt{9(\lambda_1 - \lambda_2)^2 + (4\lambda_3 + \lambda_4 + \frac{\lambda_5}{2} + \frac{\lambda_6}{2})^2} \right) \right\}$$

Kanemura, Kubota & Takasugi, 1993; Akeroyd, Arhrib & Naimi, 2000;  
 Horejsi & Kladiva, 2006

# $e^+ e^- \rightarrow A^0 h^0$ phenomenology in a nutshell

♠  $\sigma(e^+ e^- \rightarrow A^0 h^0)$  and quantum effects as a function of  $M_{h^0}$

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