

Electroweak corrections to W +jet hadroproduction including leptonic W -boson decays

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in collaboration with

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T. Kasprzik (MPI Munich, Karlsruhe)

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based on Denner, Dittmaier, Kasprzik, AM, JHEP 08 (2009) 075 [arXiv:0906.1656]

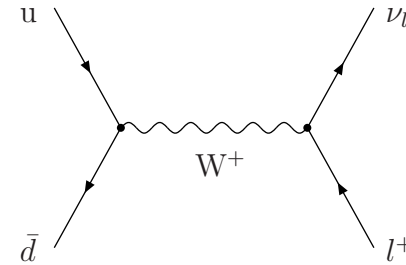
- **W production** at the LHC
- **W+jet** production: $pp \rightarrow W + \text{jet} \rightarrow l\nu_l + \text{jet}$
 - **motivation** and theoretical **status**
 - **Electroweak** and QCD **corrections**
 - Numerical **results** for the LHC
 - towards $\mathcal{O}(\alpha\alpha_s)$ corrections for **inclusive W** prod.
- **Conclusions**

W Production at the LHC

Charged-current Drell-Yan:

$$pp \rightarrow W^\pm \rightarrow l^\pm \nu_l$$

- clean signal: **lepton + missing** p_T
- huge cross section: $\sigma_W = 30 \text{ nb}$ (5 nb after basic cuts)
- very **useful**: M_W , Γ_W , luminosity, PDFs, calibration

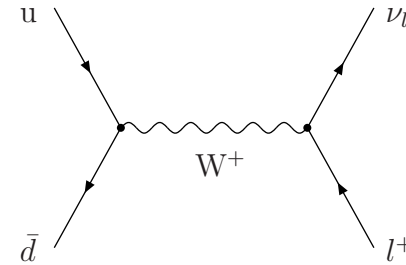


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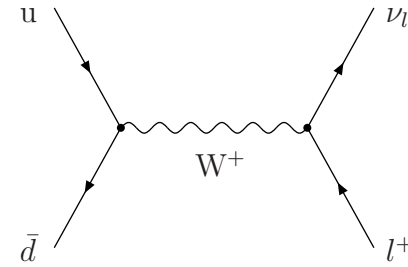
Theory status:

- **QCD**: NNLO, resummation, parton shower matching
- **EW**: NLO, leading higher order contributions

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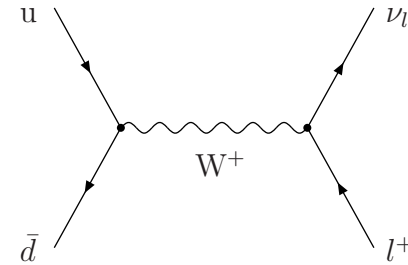
$$d\sigma = d\sigma_{\text{MC@NLO}} + (d\sigma_{\text{EW}}^{\text{HORACE}} - d\sigma_{\text{Born}})_{\text{HERWIG-PS}} \text{ etc.}$$

Balossini et al. [arXiv:0907.0276]

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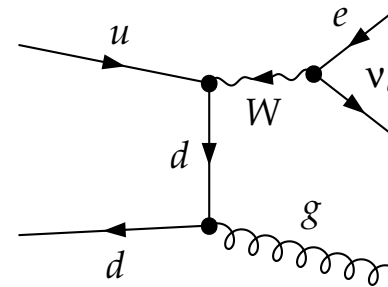
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hard QCD radiation + EW corrections?
 \Rightarrow look at **EW** corrections for **W+jet** production

W+jet production

$$pp \rightarrow l\nu_l + \text{jet}:$$

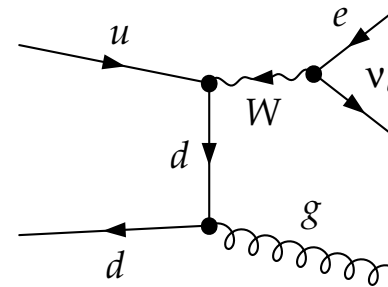
- **large** cross section
($\sim 1\text{nb}$ after basic cuts)
- dominant SM channel for **high p_T leptons**
- precision tests for **jet dynamics**
- W+jet(s) **important background** for many searches
(high p_T lepton, missing energy, jet(s))



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Theoretical status:

- **NLO QCD** corrections known and available

DYRAD: Giele et al. [hep-ph/9302225]

MCFM: Campbell, Ellis [hep-ph/0202176]

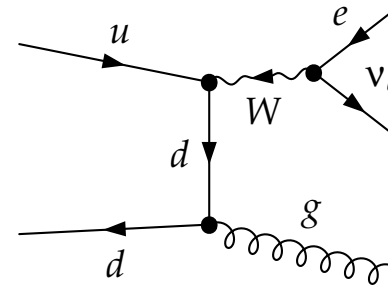
and as part of NNLO single W: Melnikov, Petriello [hep-ph/0609070]

Catani et al. [arXiv:0903.2120]

W+jet production

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Theoretical status:

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- **EW** corrections for **stable (on-shell) W bosons**

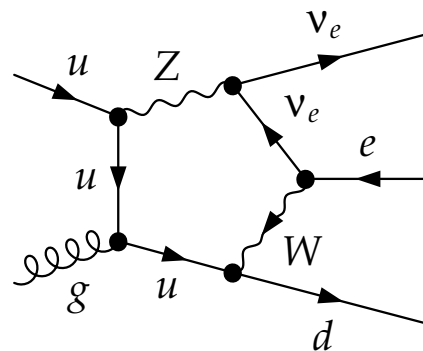
Kühn, Kulesza, Pozzorini, Schulze [hep-ph/0703283], [arXiv:0708.0476]

Hollik, Kasprzik, Kniehl [arXiv:0707.2553]

EW corrections

Complete EW corrections calculated

Denner, Dittmaier, Kasprzik, AM [arXiv:0906.1656]



+
 $\mathcal{O}(100)$ diagrams
per partonic channel

- physical final state
- all off-shell effects included
- part of the $\mathcal{O}(\alpha\alpha_s)$ corrections for incl. W production

EW corrections

Complete EW corrections calculated

Denner, Dittmaier, Kasprzik, AM [arXiv:0906.1656]

- **stable reduction** scheme for tensor integrals

Denner, Dittmaier [hep-ph/0509141]

- avoid inverse Gram determinants for pentagon reduction
- expand around vanishing determinants in critical phase-space regions

Complete EW corrections calculated

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- **stable reduction** scheme for tensor integrals

Denner, Dittmaier [hep-ph/0509141]

- **complex mass scheme** for resonances

Denner, Dittmaier, Roth, Wieders [hep-ph/0505042]

- use complex W and Z masses everywhere by means of complex renormalization:

$$M_{W,0}^2 = \mu_W^2 + \delta\mu_W^2$$

with: $M_{W,0}^2 =$ bare mass

$\mu_W^2 =$ ren. complex mass

$\delta\mu_W^2 =$ complex counterterm

- \Rightarrow complex $s_W^2 = 1 - \mu_W^2/\mu_Z^2$

- loop-integrals for complex masses needed

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- **dipole subtraction** for infrared divergencies

Catani, Seymour [hep-ph/9605323]

Dittmaier [hep-ph/9904440]

- subtraction formalism also for **non-collinear safe** observables
e.g. for **bare muons** (without lepton–photon recombination)

⇒ muon-mass logarithms extracted analytically

Dittmaier, Kabelschacht, Kasprzik [arXiv:0802.1405]

- phase-space slicing used as a check

non collinear-safe subtract.

- usual subtraction procedure:

$$\int d\Phi_{n+1} |\mathcal{M}|^2 = \int d\Phi_{n+1} (|\mathcal{M}|^2 - |\mathcal{M}_{\text{Sub}}|^2) + \int d\Phi_n \int dk_\gamma |\mathcal{M}_{\text{Sub}}|^2$$

- clever choice of $|\mathcal{M}_{\text{Sub}}|^2$

$\Rightarrow (|\mathcal{M}|^2 - |\mathcal{M}_{\text{Sub}}|^2)$ is integrable

$\Rightarrow \int dk_\gamma |\mathcal{M}_{\text{Sub}}|^2$ can be done analytically

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- $\mathcal{M}_{\text{Sub}} = \sum_f \mathcal{M}_{\text{Sub}}(p_{\text{jet}}, z_f)$ where $z_f \rightarrow p_f^0 / (p_f^0 + p_\gamma^0)$, $p_{\text{jet}} \rightarrow p_f^0 + p_\gamma^0$
for collinear events
- only cuts on p_{jet} , **no cuts on $p_f \Rightarrow$ cuts independent of z_f**
 $\Rightarrow z_f$ integration can be done analytically

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- **non-collinear safe** implementation:

- no recombination: **cuts on p_f** allowed
- cut on z_f in \mathcal{M}_{Sub} to ensure cancellation of singularities
- **integrate over z_f in dk_γ numerically**

(soft divergence treated via Plus-distribution
in analogy to treatment of initial-state emitters/spectators)

photon–jet recombination

Treat **photon** like another **parton**?

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The problem: **W+jet** \Leftrightarrow **W+photon**

- do not distinguish (also calculate $W+\gamma$ and its NLO QCD corr.)
- or **cut on photon energy** fraction z_γ inside a jet

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The problem: **W+jet** \Leftrightarrow **W+photon**

- do not distinguish (also calculate $W+\gamma$ and its NLO QCD corr.)
- or **cut on photon energy** fraction z_γ inside a jet
 \Rightarrow this is what we want

But: **not infrared safe**

photon–jet recombination

What does z_γ cut imply?

- sensitivity to $q \rightarrow q\gamma$ splitting
- **non-perturbative** corrections to be included

photon–jet recombination

What does z_γ cut imply?

- sensitivity to $q \rightarrow q\gamma$ splitting
- **non-perturbative** corrections to be included
- introduce **quark-to-photon fragmentation function** $D_{q \rightarrow \gamma}(z_\gamma, \mu_F)$
 - measured in hadronic Z decays at LEP ($Z \rightarrow q\bar{q} \rightarrow q\bar{q}\gamma$)
 - using ALEPH fit:

$$D_{q \rightarrow \gamma}(z_\gamma, \mu_F) = \frac{\alpha Q_q^2}{2\pi} P_{q \rightarrow \gamma}(z_\gamma) \left(\ln \frac{m_q^2}{\mu_F^2} + 2 \ln z_\gamma + 1 \right) + D_{q \rightarrow \gamma}^{\text{ALEPH}}(z_\gamma, \mu_F),$$

where

$$D_{q \rightarrow \gamma}^{\text{ALEPH}}(z_\gamma, \mu_F) = \frac{\alpha Q_q^2}{2\pi} \left(P_{q \rightarrow \gamma}(z_\gamma) \ln \frac{\mu_F^2}{(1 - z_\gamma)^2 \mu_0^2} + C \right)$$

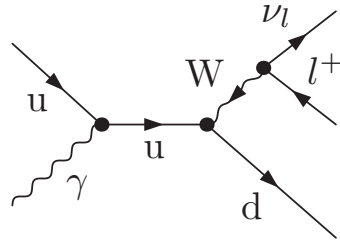
$$P_{q \rightarrow \gamma}(z_\gamma) = \frac{1 + (1 - z_\gamma)^2}{z_\gamma}$$

up to $\mathcal{O}(\alpha^3 \alpha_s)$

- also **full NLO QCD** corrections
 - **variable** (phase-space dependent) **scale** supported

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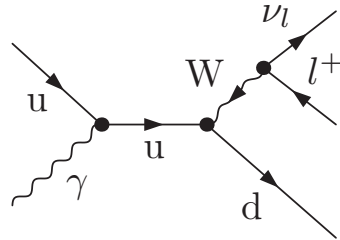
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 - **variable** (phase-space dependent) **scale** supported
- **photon-induced** processes



at **NLO QCD**
(phenomenologically irrelevant)

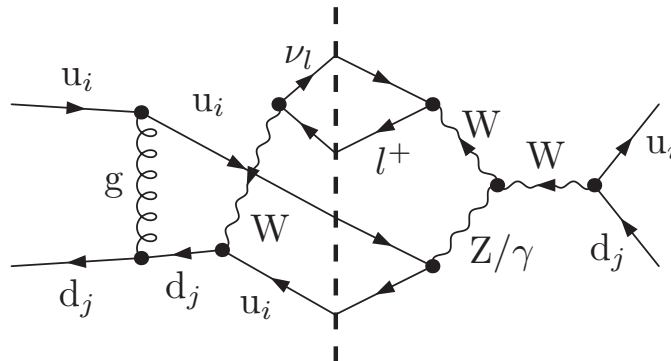
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at **NLO QCD**
(phenomenologically irrelevant)

- QCD-EW **interference terms** in 4-quark processes



(phenomenologically irrelevant)

Monte-Carlo programs

two completely **independent calculations**

- in mutual **agreement**

- MPI: FeynArts 1.0 [Böhm, Denner, Küblbeck]

in-house Mathematica Routines

loop integral library: DD [Dittmaier]

Vegas integration

- PSI: FeynArts 3.2, FormCalc 3.1 [Hahn]

loop integral library: Coli [Denner]

Pole [Meier, AM]

- using Weyl-van der Waerden formalism

Dittmaier [hep-ph/9805445]

- automatic generation of subtraction/slicing terms

- automatic multi-channeling using Lusifer

Dittmaier, Roth [hep-ph/0206070]

basic cuts

- $p_{T,l/miss/jet} > 25 \text{ GeV}$
- $|y_{l/jet}| < 2.5$
- lepton isolation: $R_{l,jet} > 0.5$
- photon-energy fraction inside jets: $z_\gamma < 0.7$

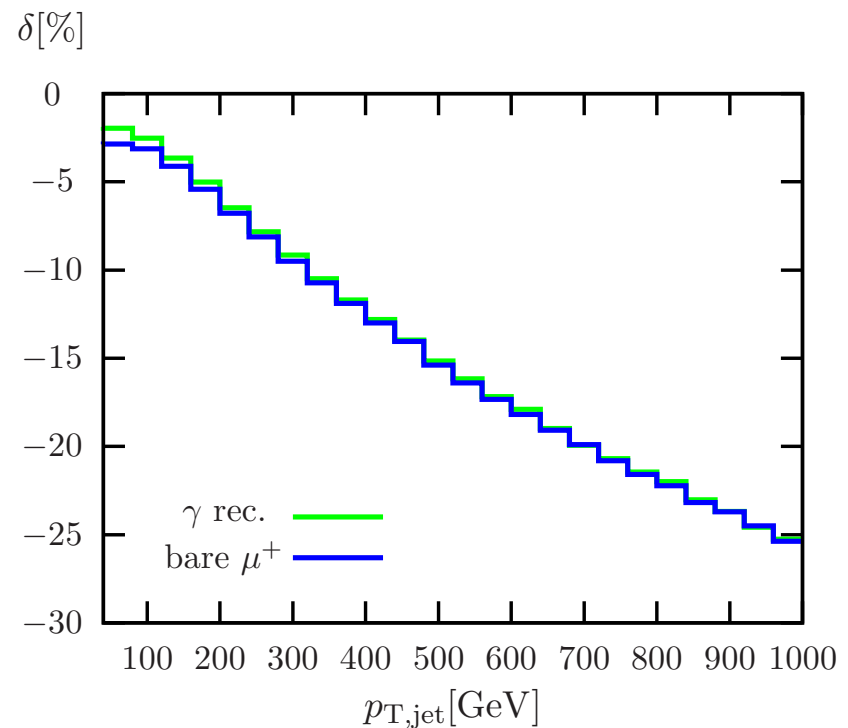
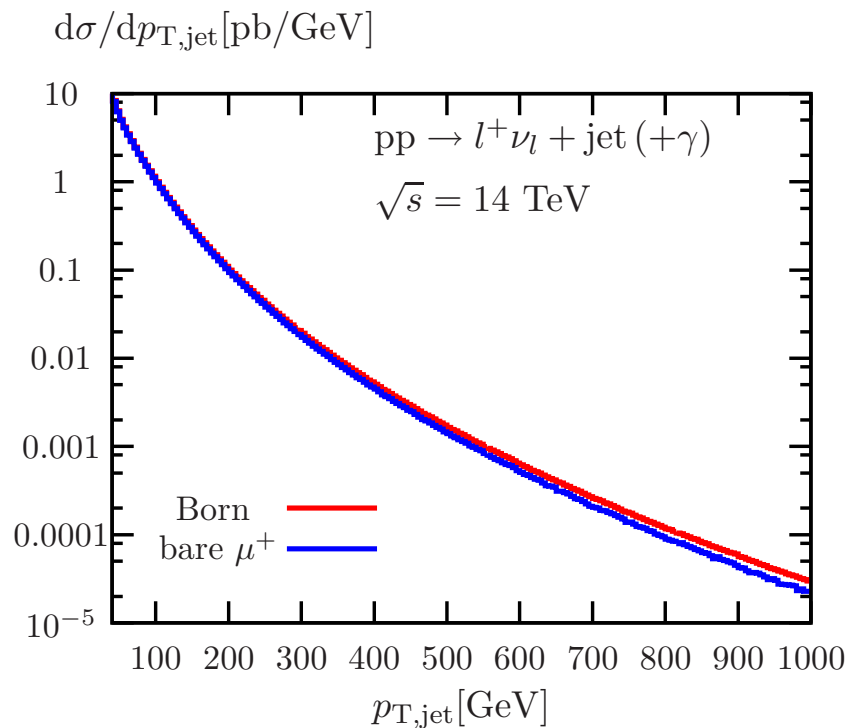
recombination

- do not recombine photons and muons (bare μ^+)
- photons and electrons: $R_{\gamma,l} < 0.1$ (γ rec.)
- photons and partons: $R_{\gamma,jet} < 0.5$

renormalization and factorization scale

- fixed scale ($\mu = M_W$)
- variable scale: $\mu = \sqrt{M_W^2 + p_T^{\text{had}}}$ (our default choice)

$p_{T,\text{jet}}$ distribution for the LHC:



large corrections at large energies (Sudakov logs)
(on-shell W good approximation)

QCD corrections

$p_{T,\text{jet}}$ distribution for the LHC:

huge NLO QCD corrections:

new kinematical configuration:

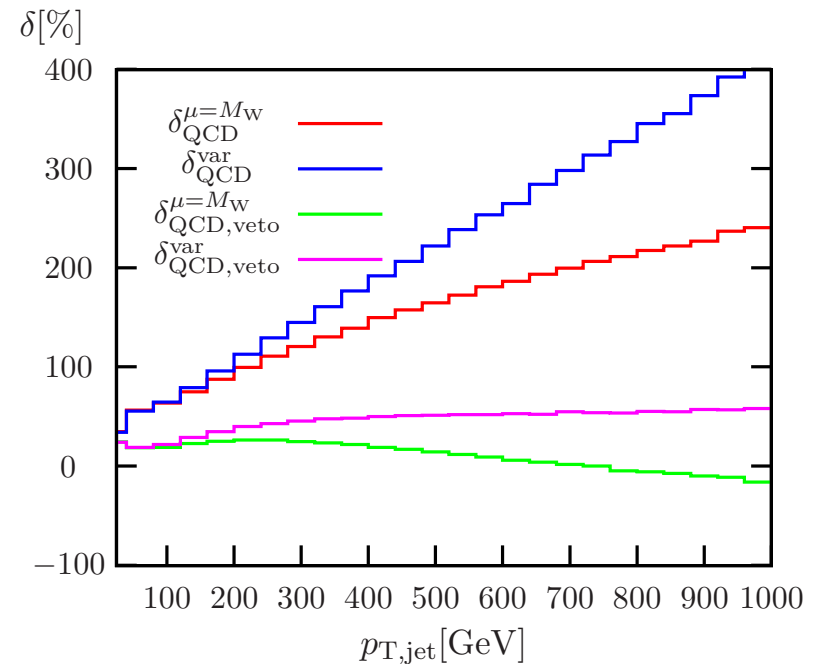
back-to-back jets balance p_T

⇒ 2 jet events with W emission

⇒ no genuine QCD correction for W+jet

use simple jet veto:

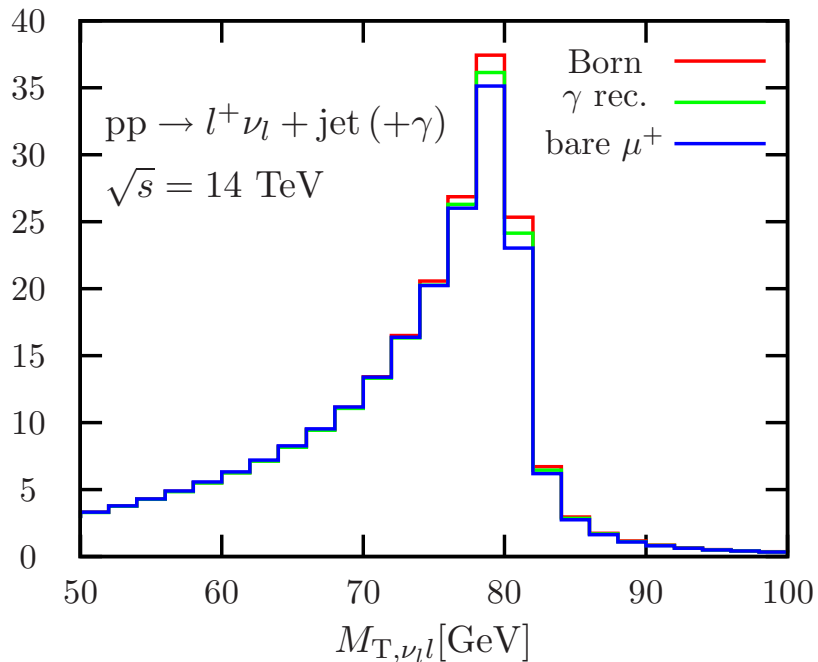
veto second jet with $p_T > \frac{1}{2} p_T^{\text{lead}}$.



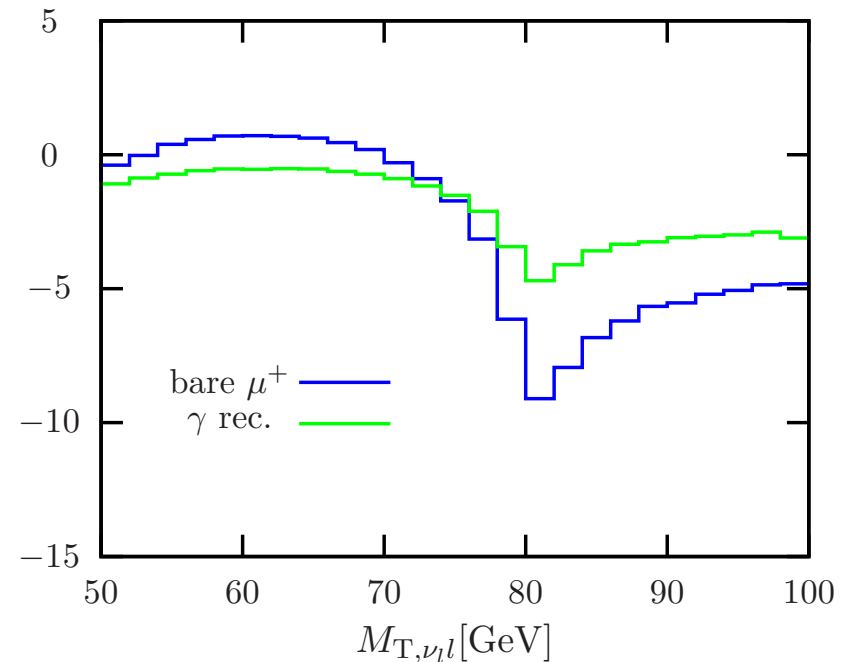
M_T distribution for the LHC:
(similar results for the Tevatron)

$$M_{T,l\nu_l} = \sqrt{2 p_{T,l} p_T^{\text{miss}} (1 - \cos \phi_{\nu_l l})}$$

$d\sigma/dM_{T,\nu_l l} [\text{pb}/\text{GeV}]$



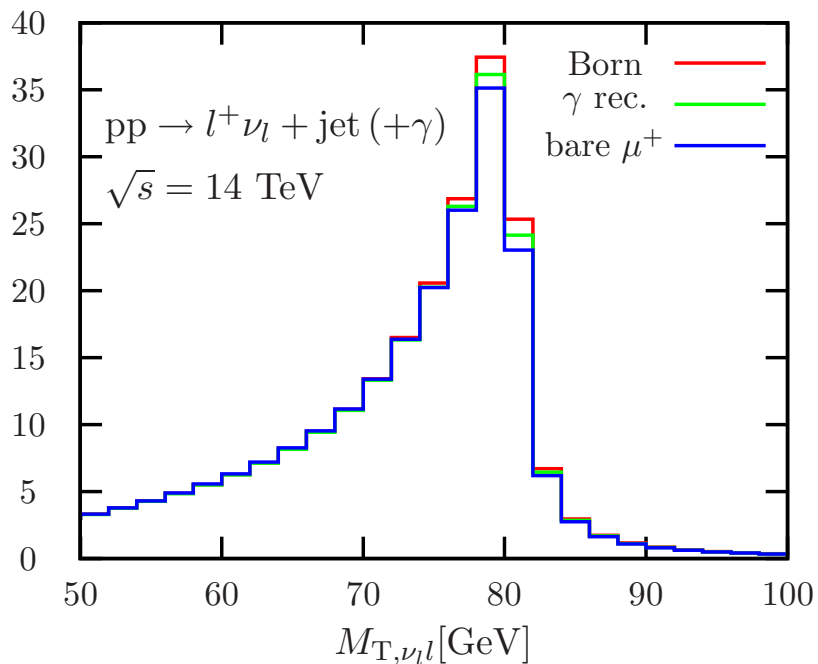
$\delta [\%]$



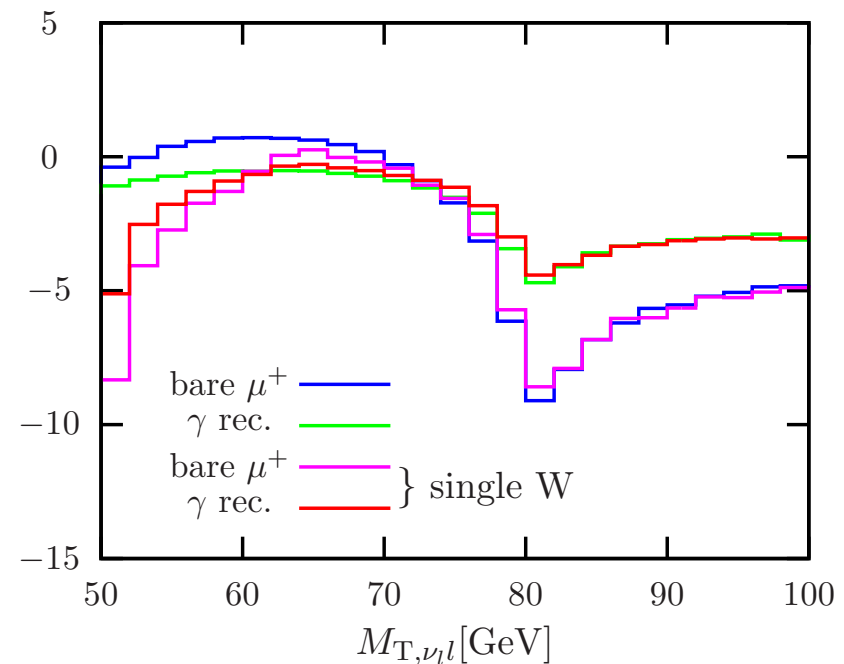
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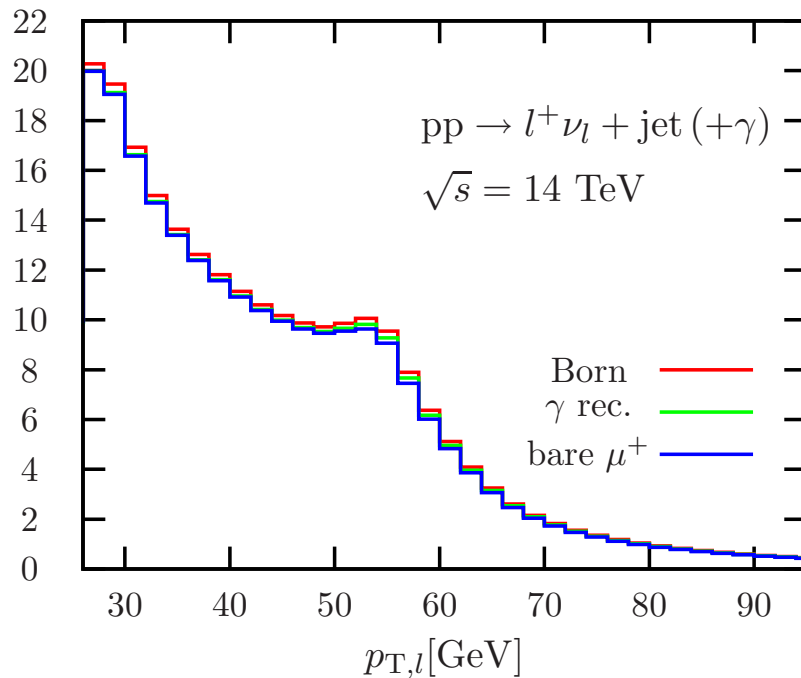
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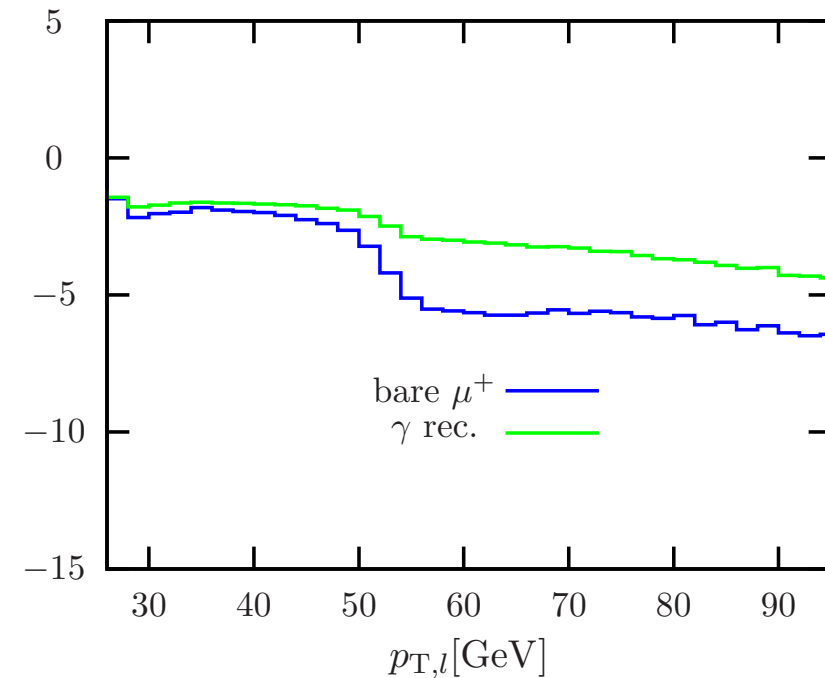
corrections very similar to single W production

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$d\sigma/dp_{T,l}[\text{pb/GeV}]$

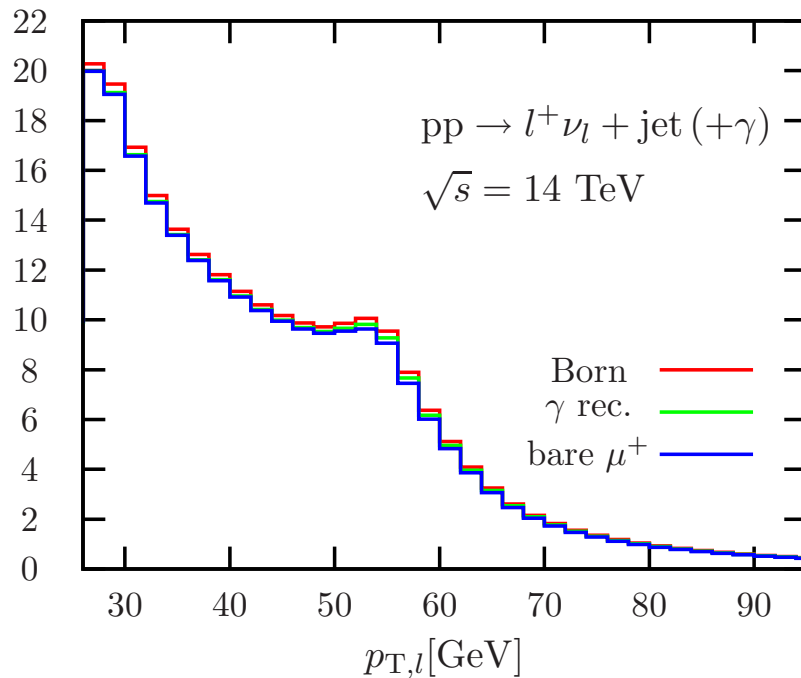


$\delta[\%]$

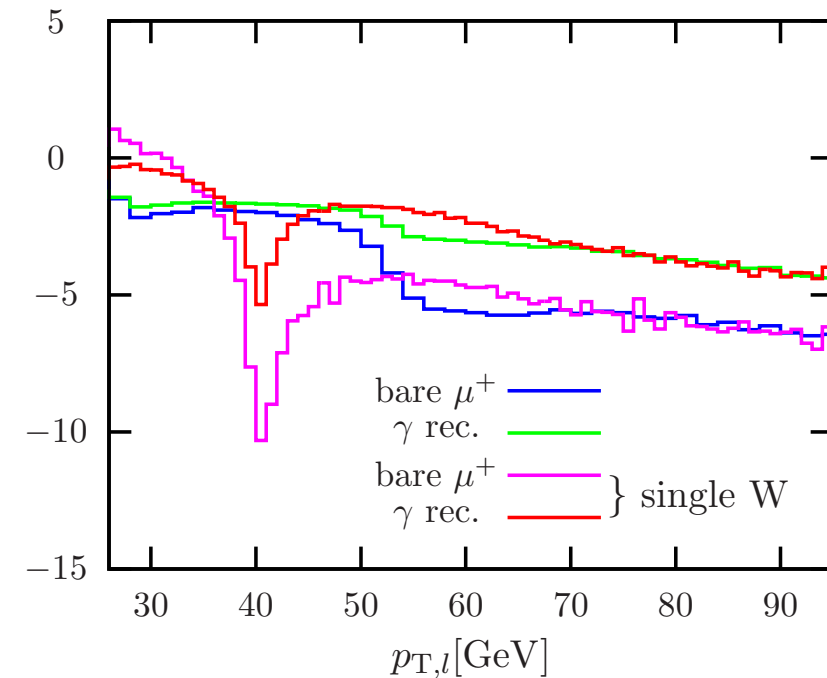


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$d\sigma/dp_{T,l}[\text{pb/GeV}]$



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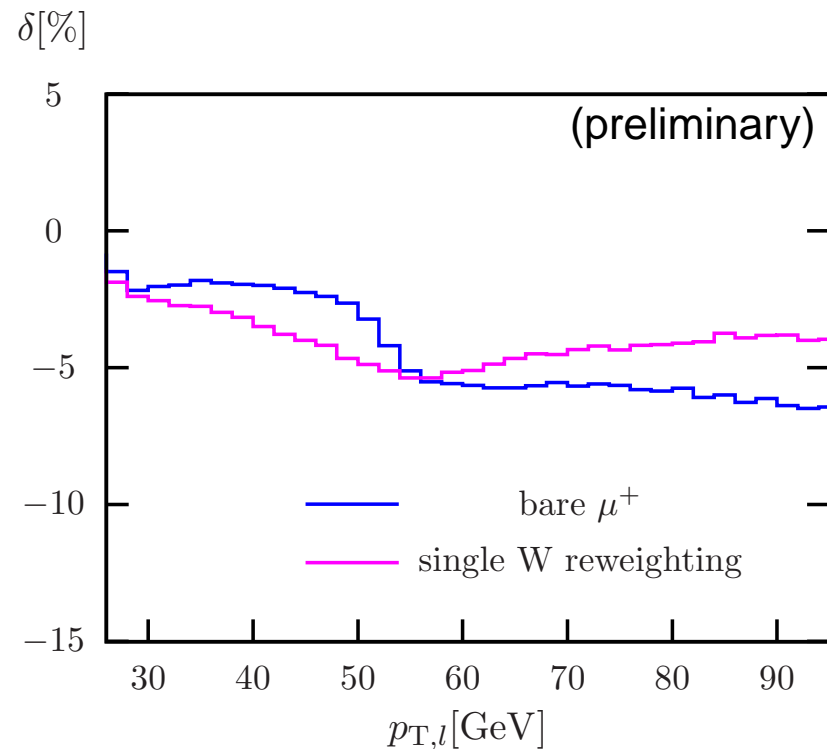
no similarity to single W production

single W vs. W+jet

p_T distribution for the LHC:

single W reweighting:

- **boost** W+jet event to W-boson **rest frame**
- **reweight** event **with EW correction for single W** in rest-frame $p_{T,l}$ bin

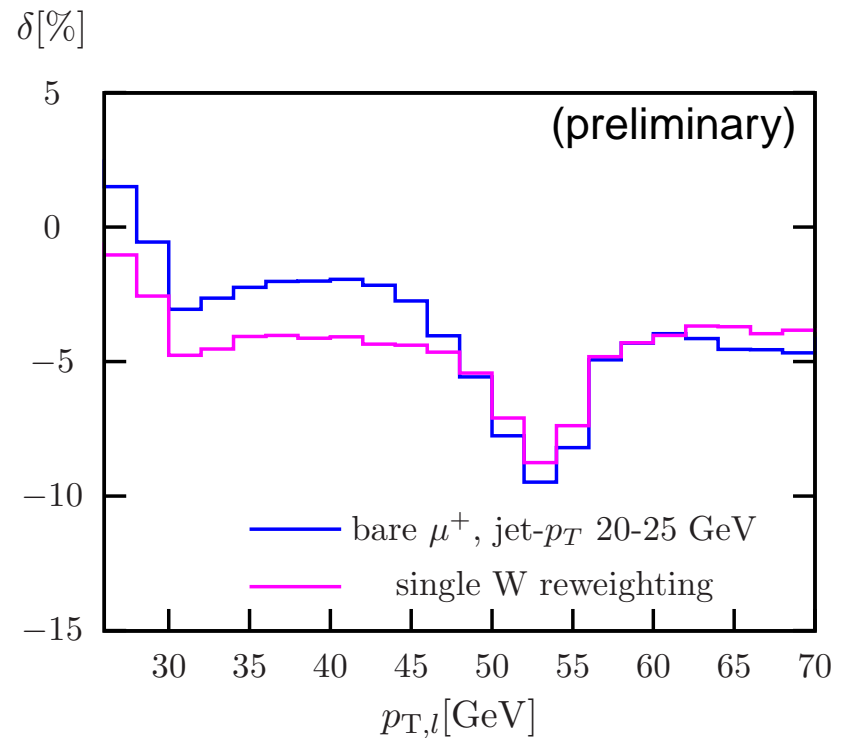


still big differences due to high- p_T jets

single W vs. W+jet

p_T distribution for the LHC:

- only look at jets with
 $p_{T,jet} = 20 - 25 \text{ GeV}$

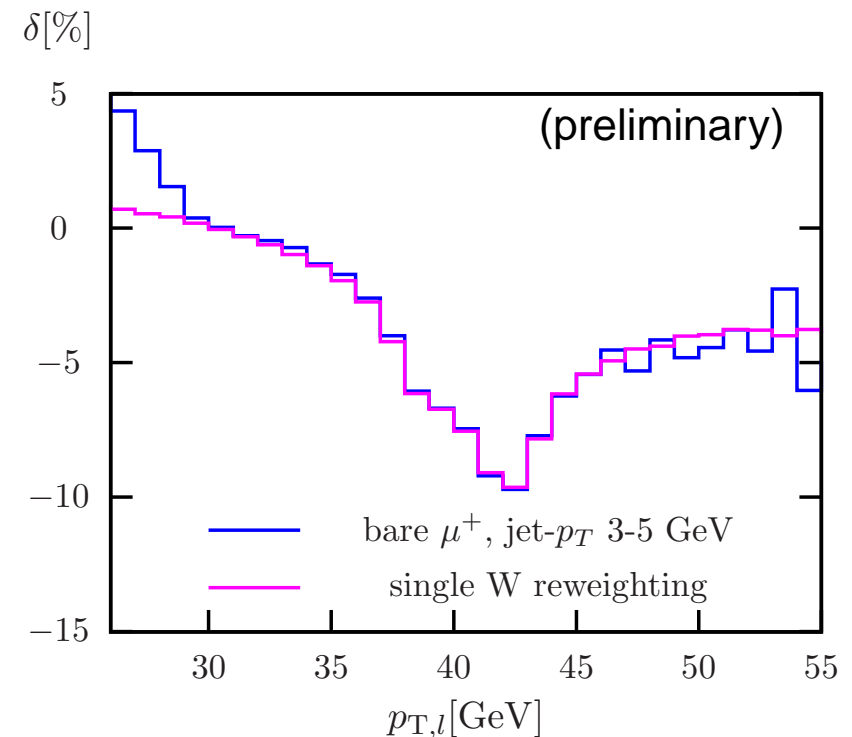


good but not perfect agreement

single W vs. W+jet

p_T distribution for the LHC:

- only look at jets with $p_{T,\text{jet}} = 3 - 5 \text{ GeV}$
- cross-section not reliably predicted in this region
- one can still estimate the EW corrections for the limited kinematical region



very good agreement

RWTH Summary

- **W+jet** is a SM **benchmark** process
- our calculation
 - **flexible** Monte Carlo program
 - recalculation of NLO QCD corrections
 - complete **EW** corrections
 - **physical final state** (all off-shell effects included)
- EW corrections
 - typically at the **percent level**
 - **larger** corrections in some **distributions**
 - **growing** with **energy** ($\sim -25\%$ at $p_{T,\text{jet}} = 1 \text{ TeV}$)
 - a step towards $\mathcal{O}(\alpha\alpha_s)$ for **inclusive W** production
- outlook
 - more on **W+jet vs. inclusive W** production
 - **Z+jet** production

Back-up slides

EW corrections: single W

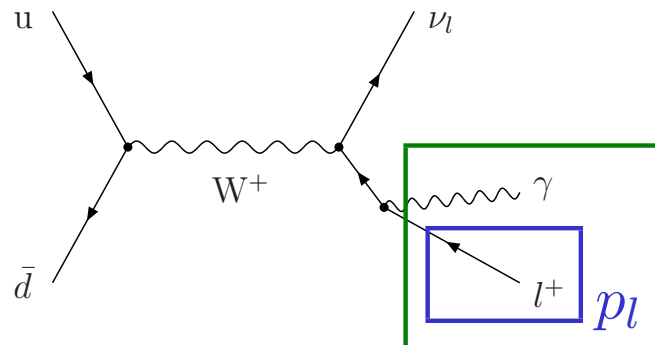
EW corrections **distort shapes**:

- in particular due to **final state photon radiation**
- also for M_T distribution
- strong dependence on lepton-photon **recombination**

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$$p_l = p_l + p_\gamma$$

(for collinear photons)

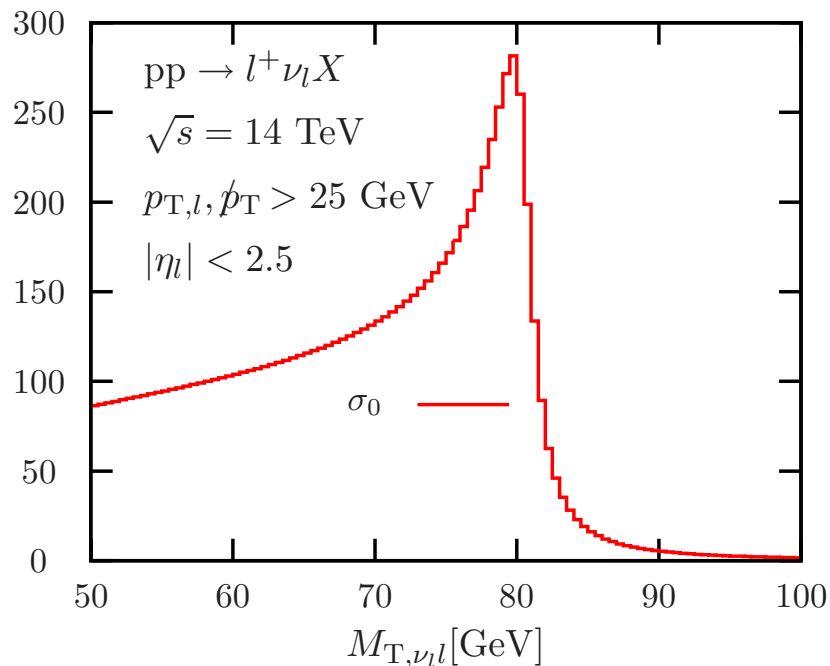
exclusive (bare) leptons (muons): $\propto \log(M_W^2/M_l^2)$ corrections
 inclusive leptons (electrons): **no large logs** (KLN theorem)

EW corrections: single W

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$d\sigma/dM_{T,\nu_l}[\text{pb/GeV}]$



Breusung, Dittmaier, Krämer, AM [arXiv:0710.3309]

