



中国科学院高能物理研究所

Institute of High Energy Physics Chinese Academy of Sciences

Future Colliders

Lecture-1

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Chinese Academy of Sciences*

**For the First International High Energy Physics School and Workshop in Western China,
Aug 2018, Lanzhou, China**

The Topic

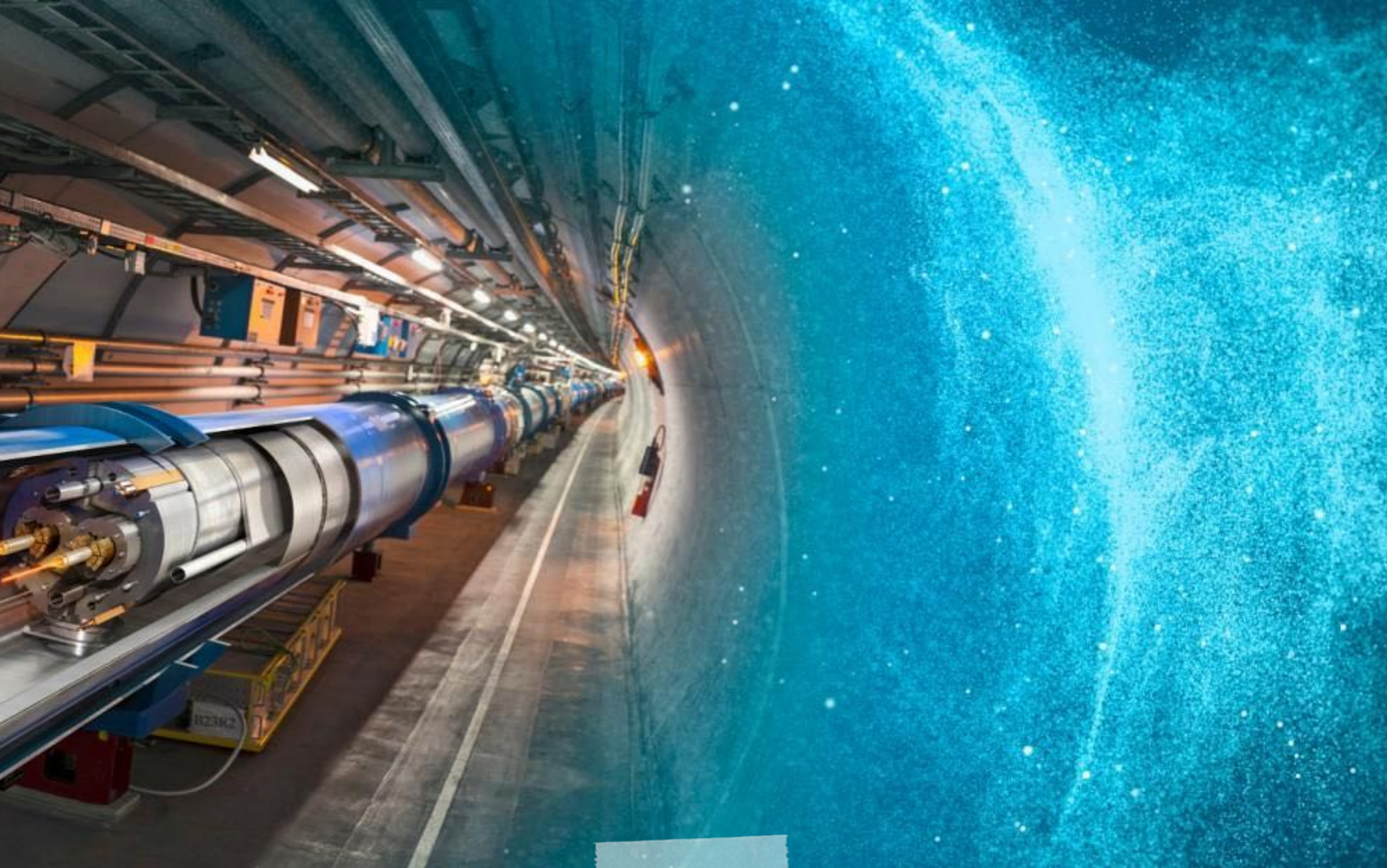
- Some review of the LHC exp (overlap with Prof. Rachid Mazini);
- Some review of the phenomenology at the LHC (overlap with Prof. Joey Huston and Prof. Tao Han);
- Some knowledge of the electroweak standard model, especially the Higgs physics (overlap with Prof. Shinya Kanemura);
- Phenomenology at the future lepton colliders and hadron colliders (overlap with Prof. Tao Han and Prof. Rachid Mazini);
- Search for new physics at future colliders (overlap with Prof. Andrea Romanino and Prof. Michael Ramsey-Musolf);
- ... (more overlaps?)



Outline

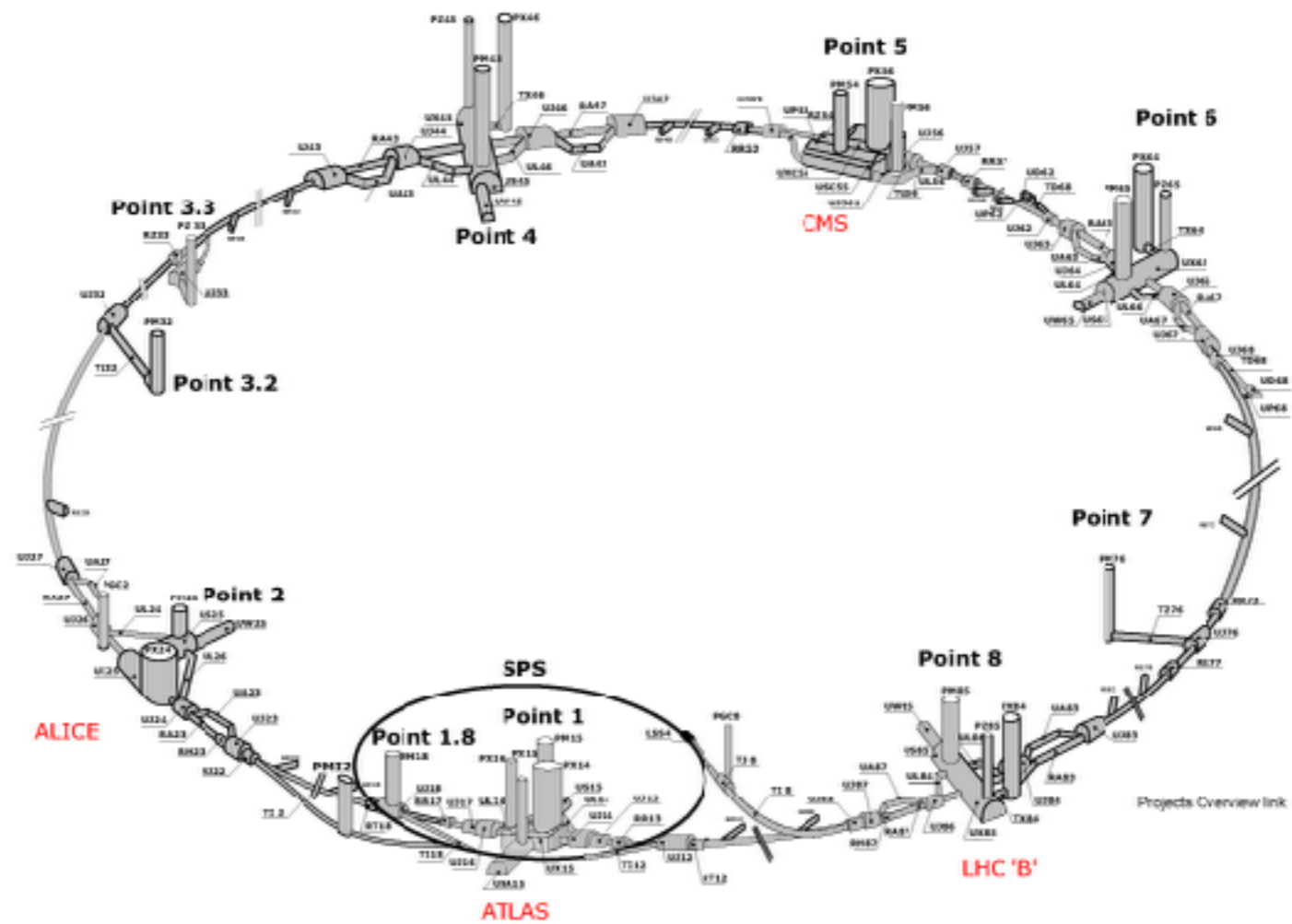
- From the LHC to the future lepton colliders.
- (Higgs) Physics at future lepton colliders.
- Physics at future hadron colliders.
- Summary and outlook.





Lecture 1: From the LHC to the Future Lepton Colliders

A Review of the LHC



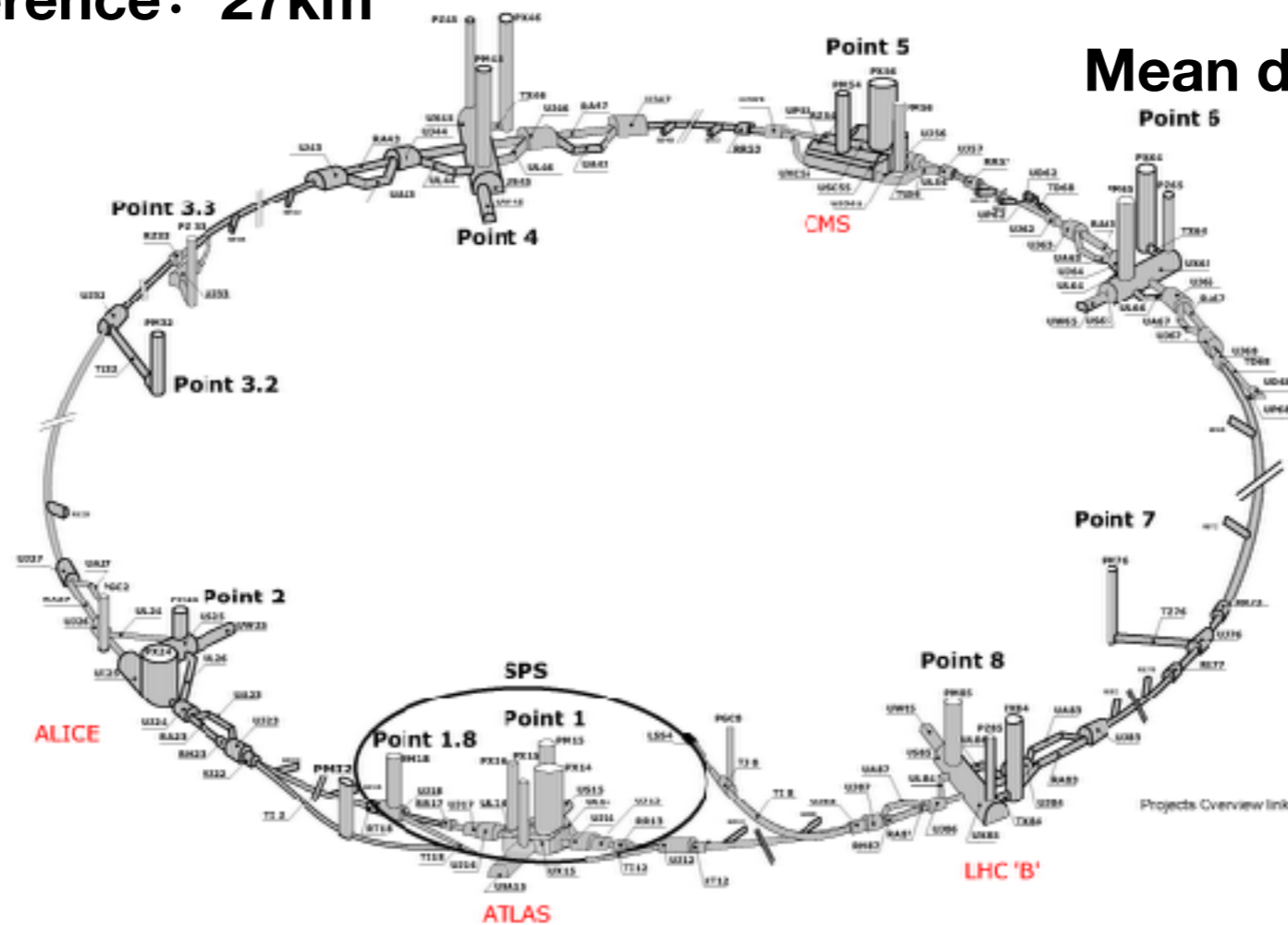
A Review of the LHC

Center of mass energy: $14\text{TeV}=2.2\times 10^{-6}\text{J}$, $v=0.999999991c$

Total cost: ~4 billion \$

Circumference: 27km

Mean depth: 100m



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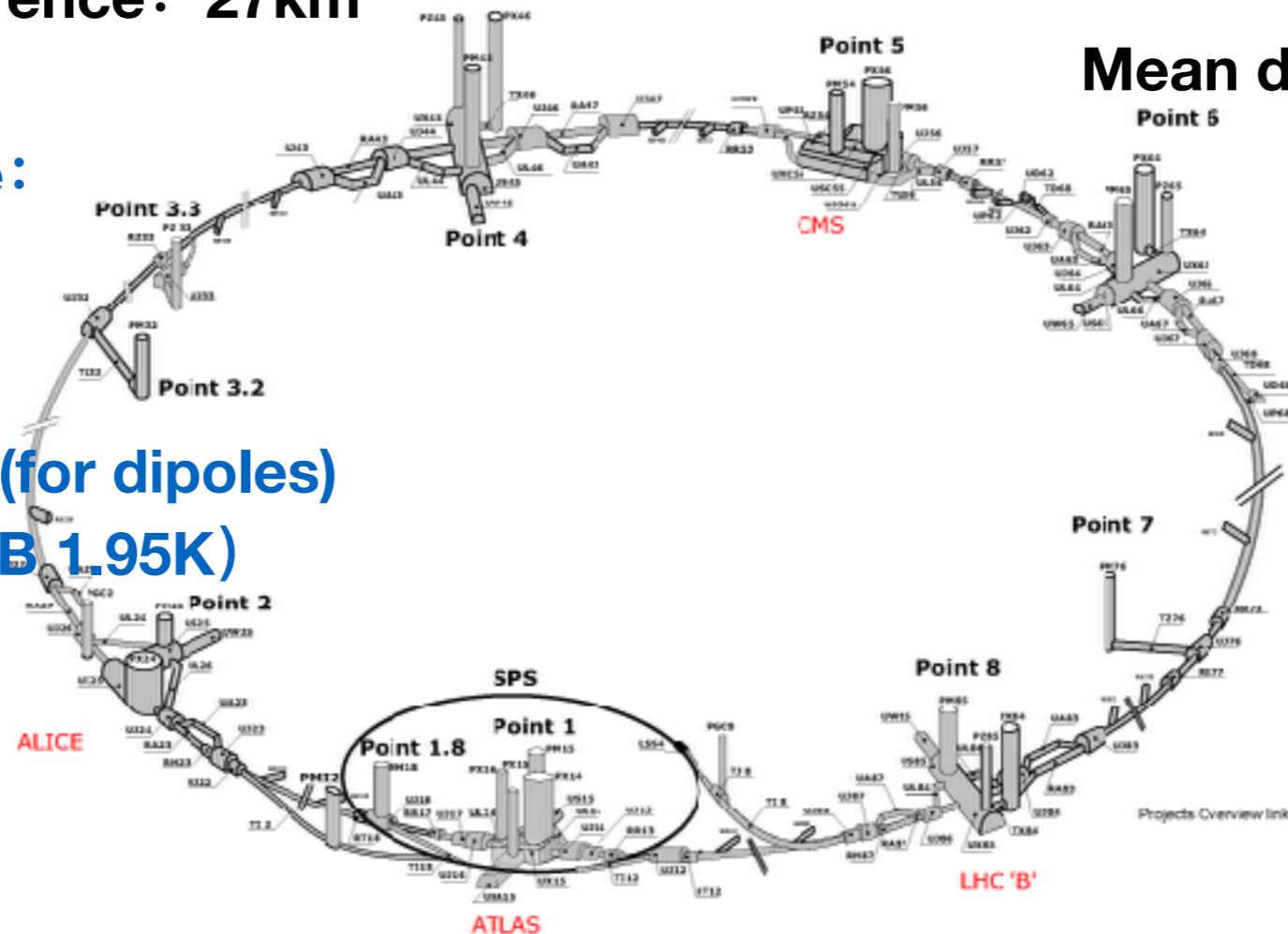
Effect from the (moon) tidal force: 1mm/27km

Circumference: 27km

Mean depth: 100m

Vacuum pressure:
 10^{-13}atm

Temperature: 1.9K (for dipoles)
(CMB 2.71K, CNB 1.95K)



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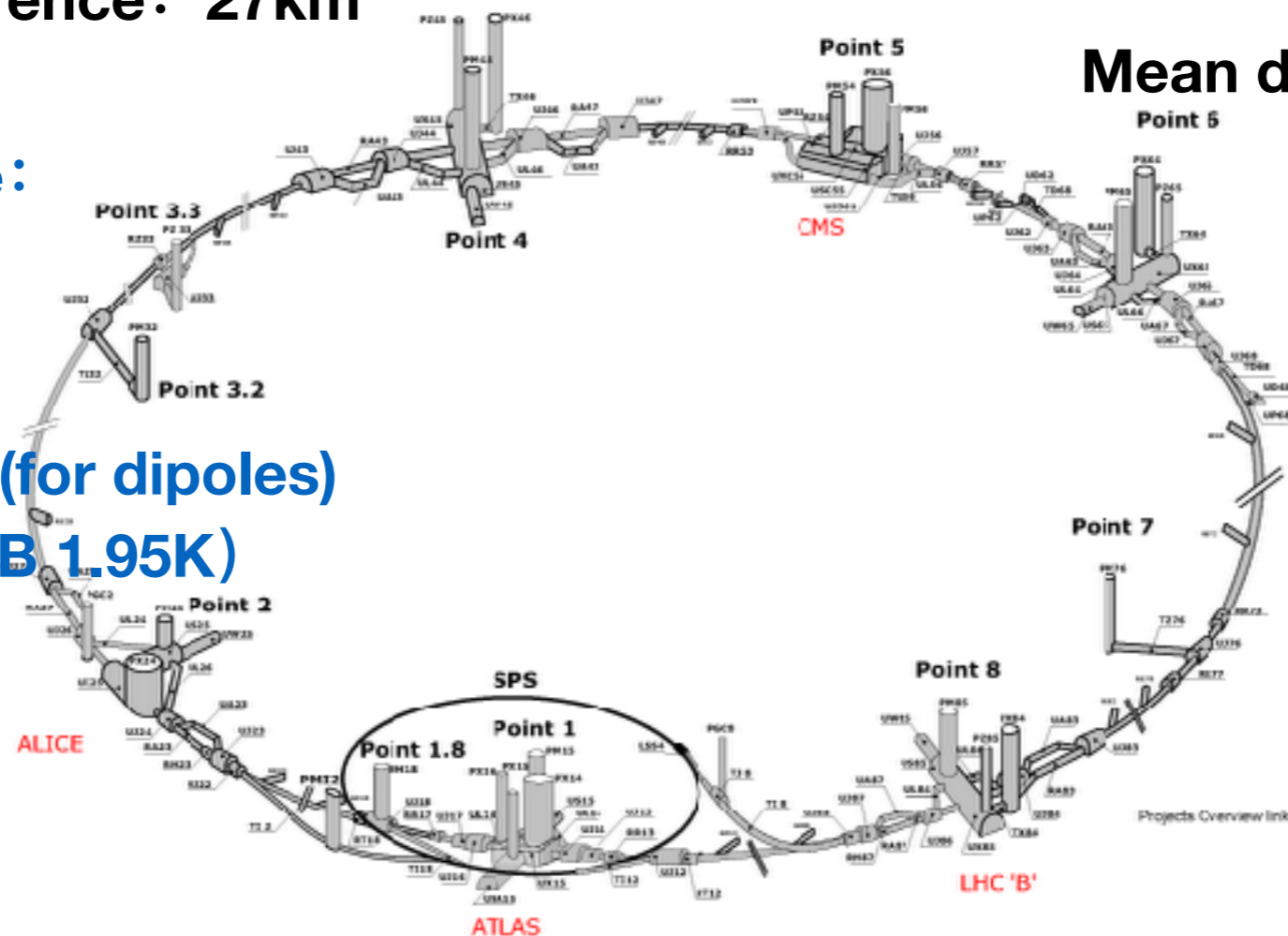
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Temperature: 1.9K (for dipoles)
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9593 magnets

1232 dipoles: 15m, 35t
(1.9K, $I=11850\text{A}$), ~8T



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Mean depth: 100m

Vacuum pressure:
 10^{-13}atm

No. of bunches per
proton beam: 2808

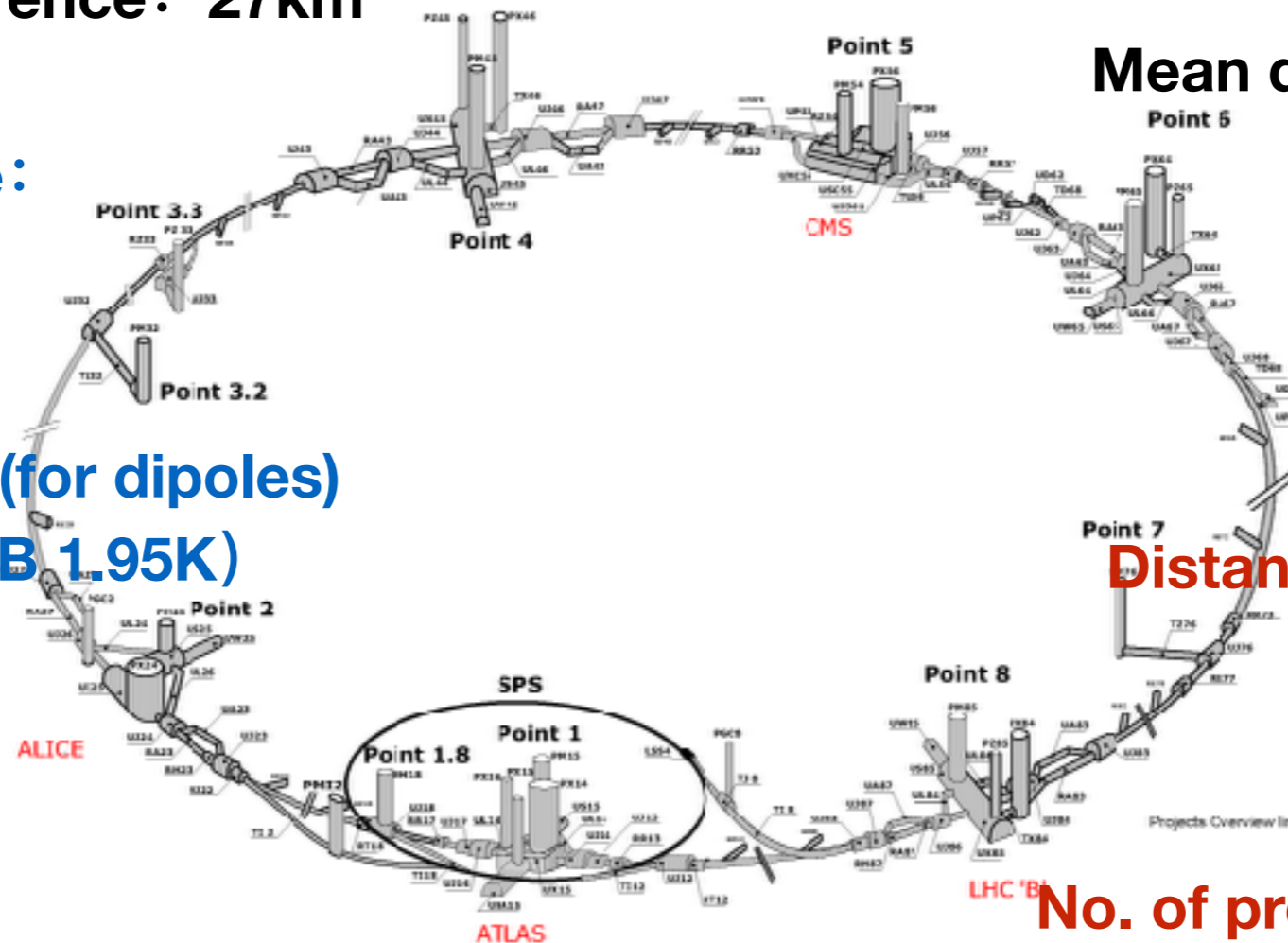
Temperature: 1.9K (for dipoles)
(CMB 2.71K, CNB 1.95K)

Distance between bunches:
7.5m (25ns)

9593 magnets

1232 dipoles: 15m, 35t
(1.9K, $I=11850\text{A}$), ~8T

No. of collisions per second: ~1 billion



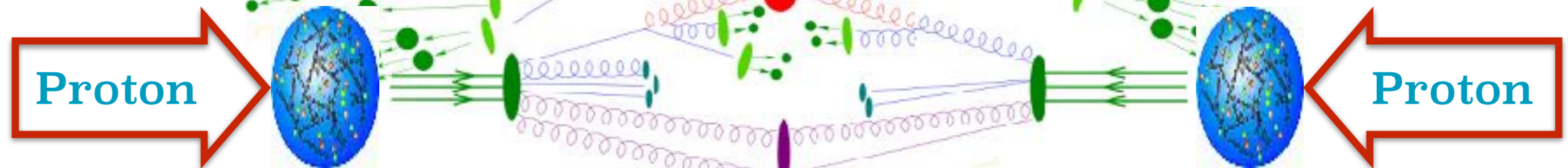
A Review of the LHC

Electromagnetic radiation

Hadronization

Parton Showering

Hard scattering



Proton

Proton

Decay

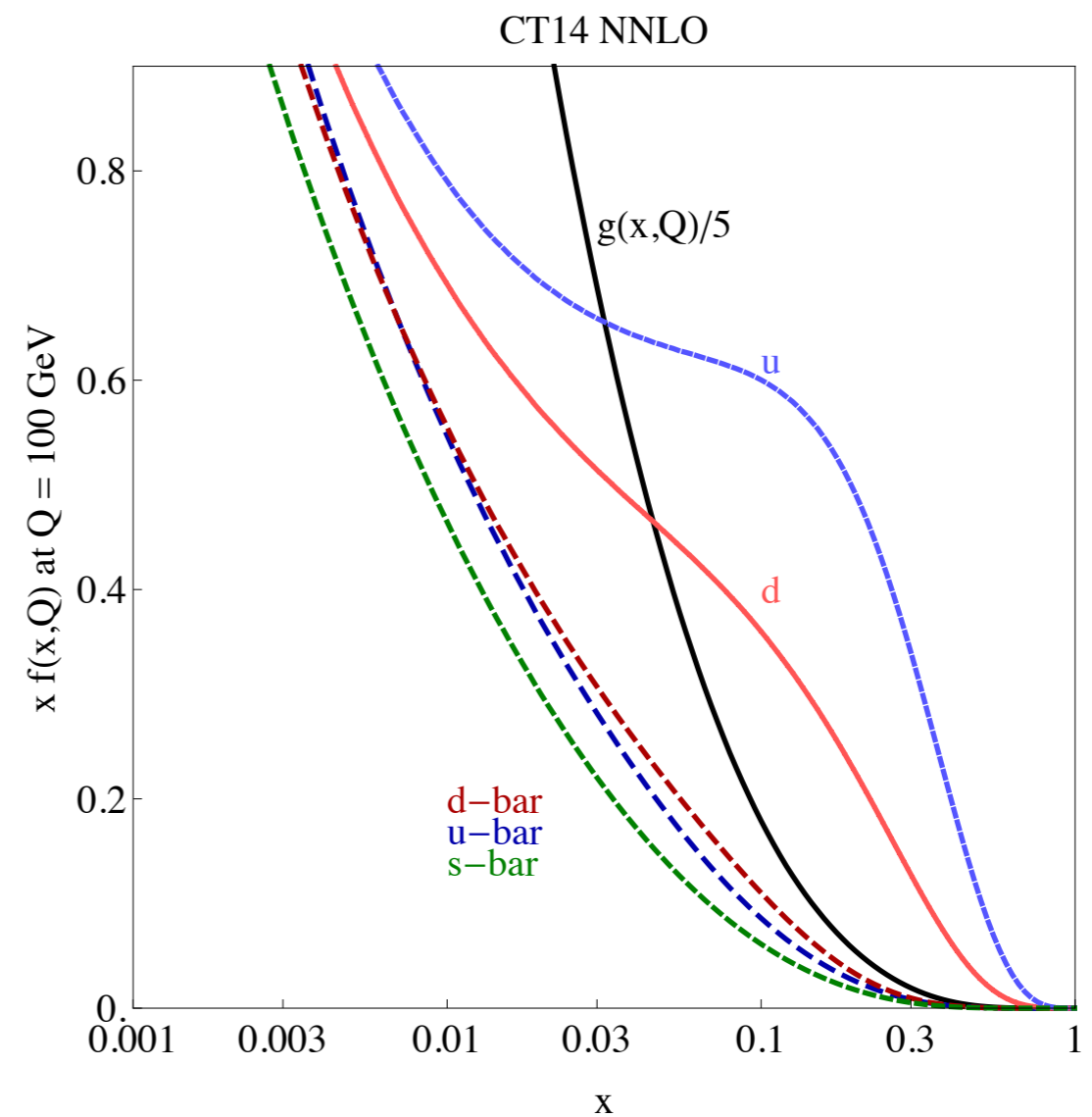
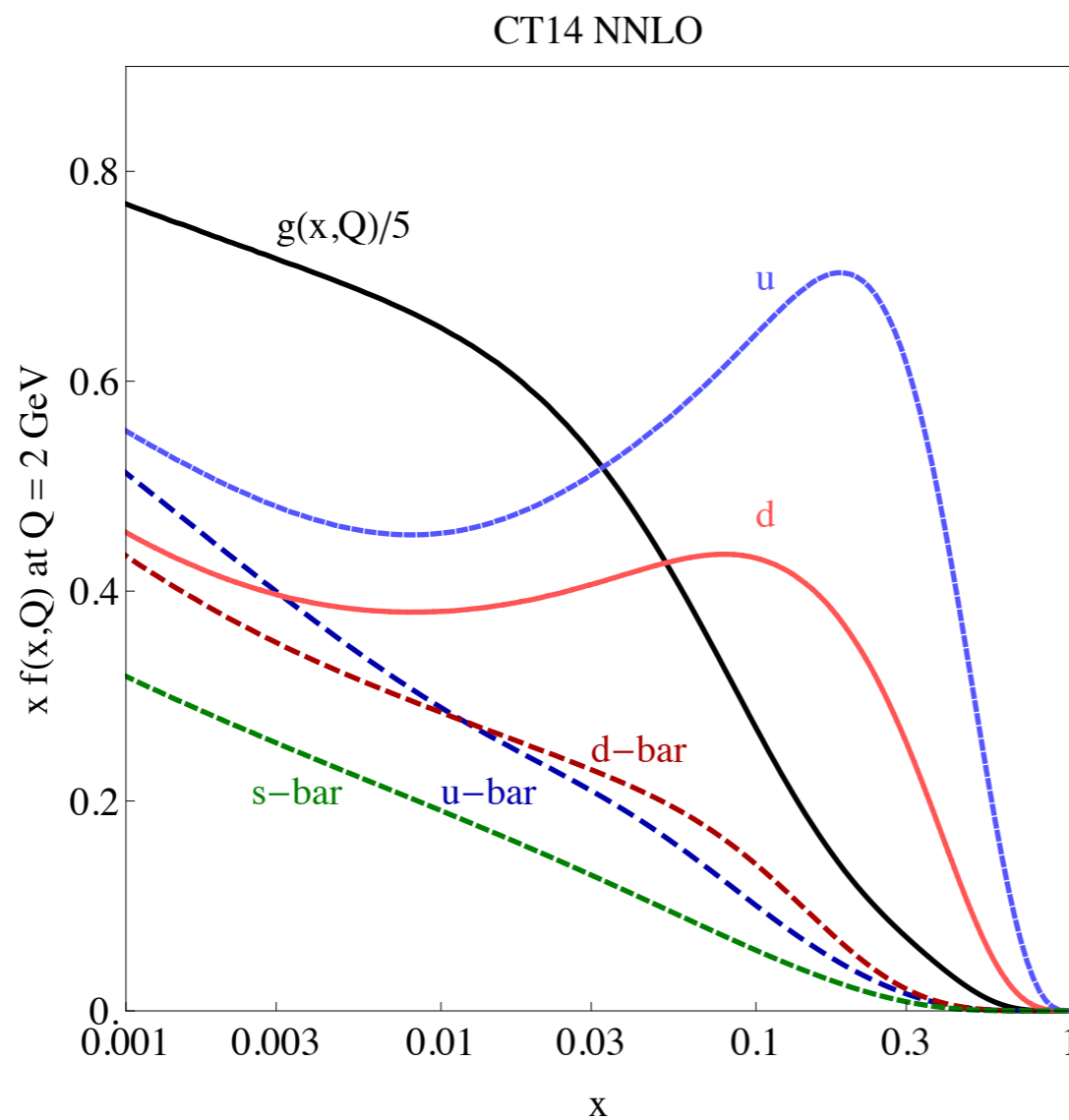
Underlying events



A Review of the LHC

- Parton distribution function (PDF).

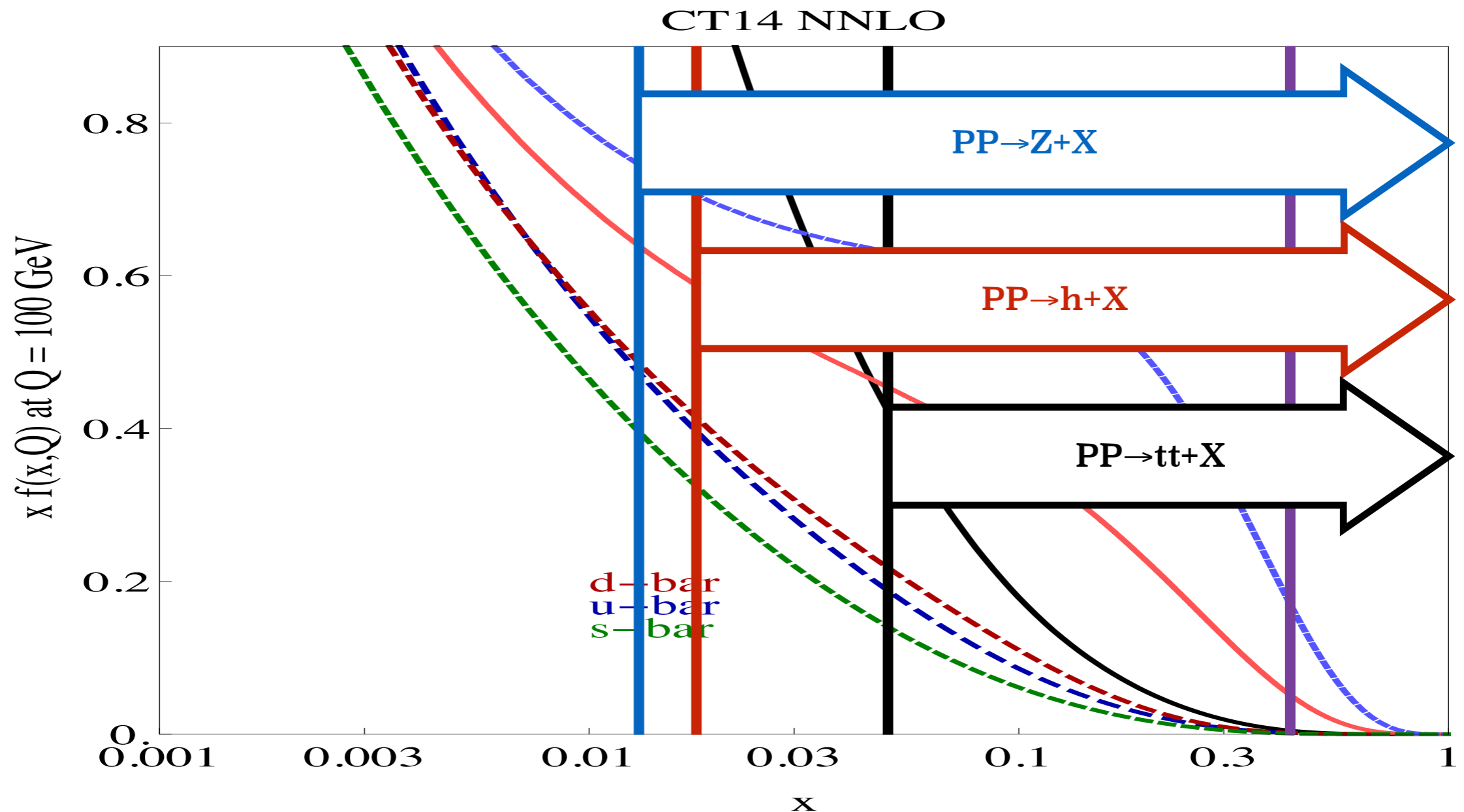
$$N(\sqrt{S}) = \mathcal{L}\sigma(\sqrt{S}) = \mathcal{L} \sum_{a,b} \int dx_1 dx_2 \sigma_H(\sqrt{x_1 x_2 S}) f_{a/P}(x_1) f_{b/P}(x_2)$$



A Review of the LHC

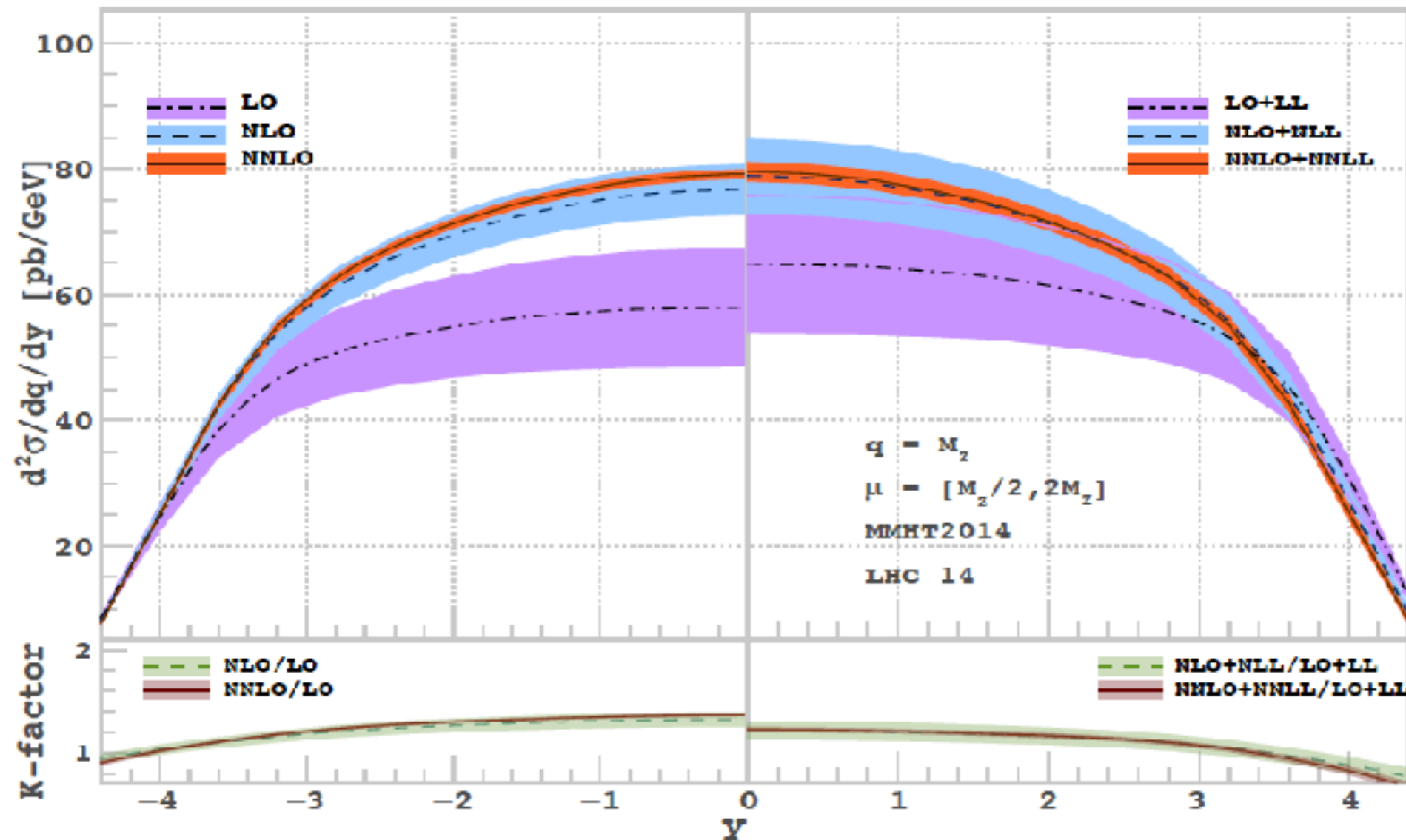
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A Review of the LHC

- Large coupling constant α_s .
- Large higher order corrections from both real and virtual processes.

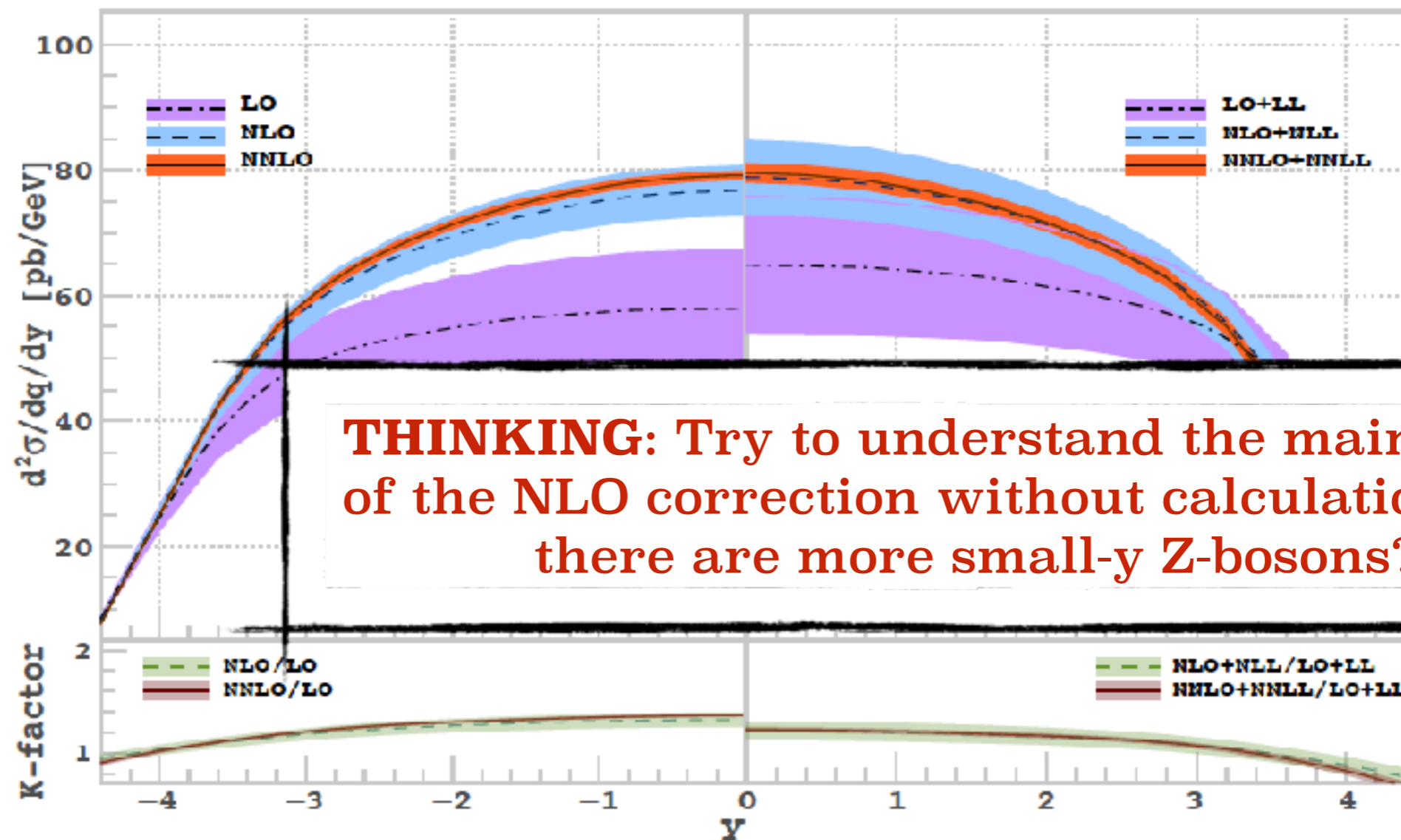


Drell-Yan rapidity distribution for 14 TeV LHC, arXiv:1805.01186



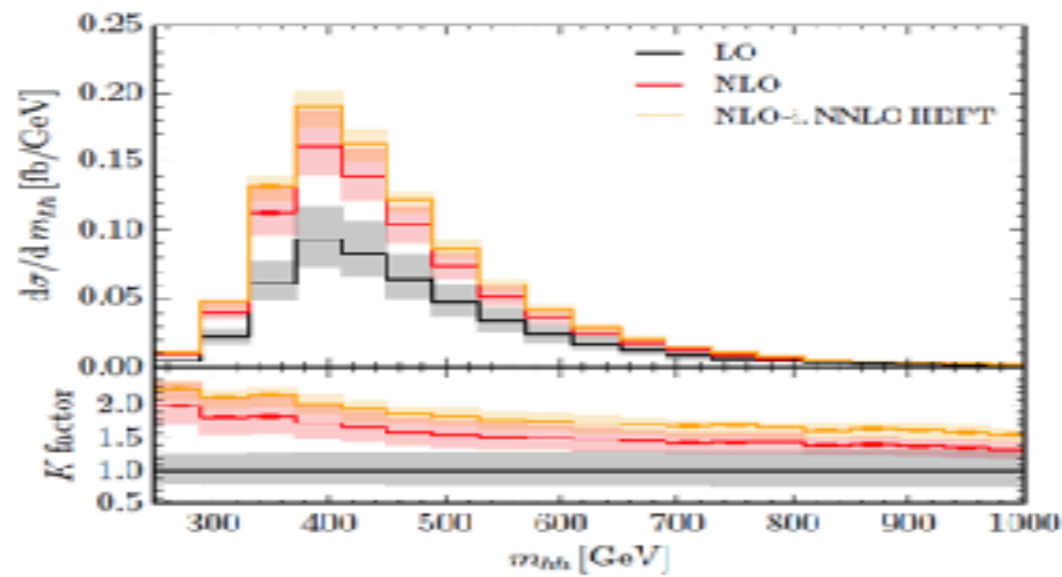
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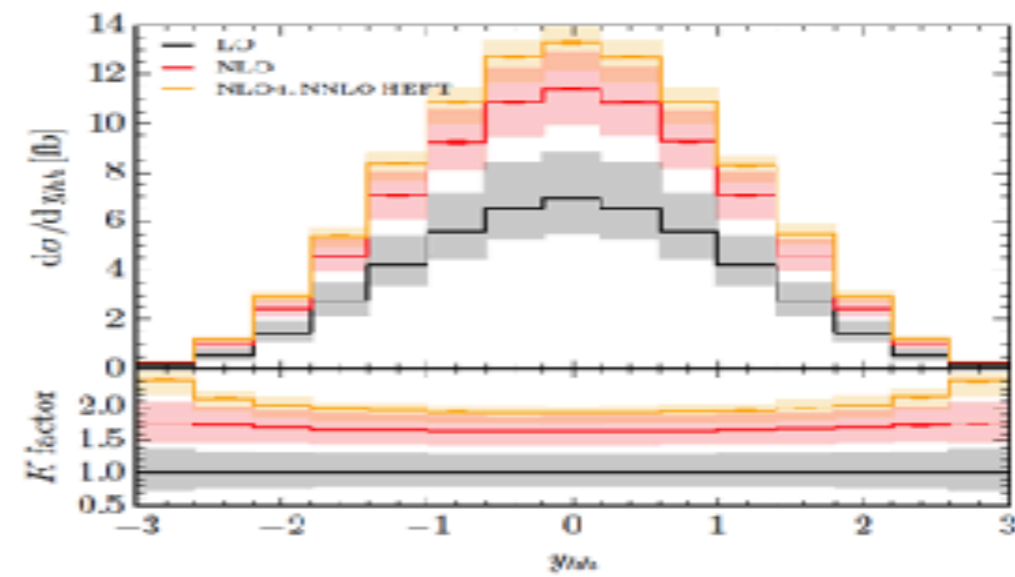


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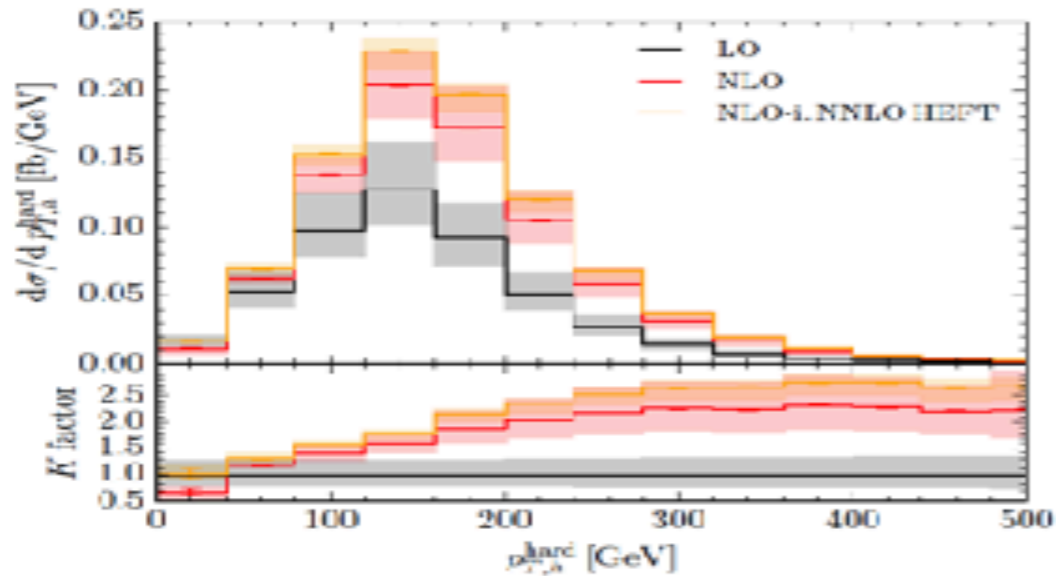
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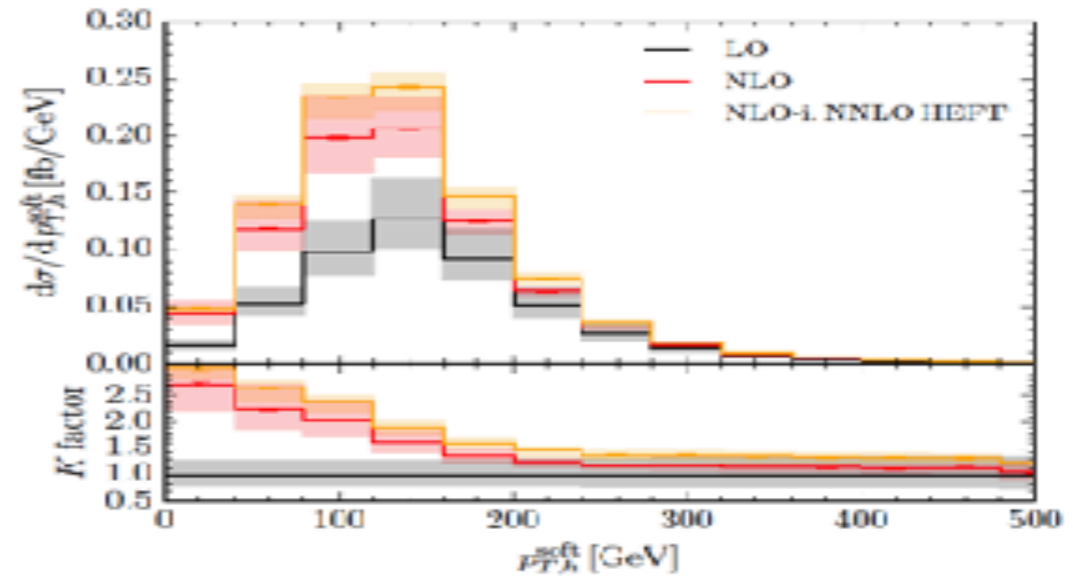
(a) 14 TeV, m_{hh} .



(b) 14 TeV, y_{hh} .



(c) 14 TeV, leading p_T .

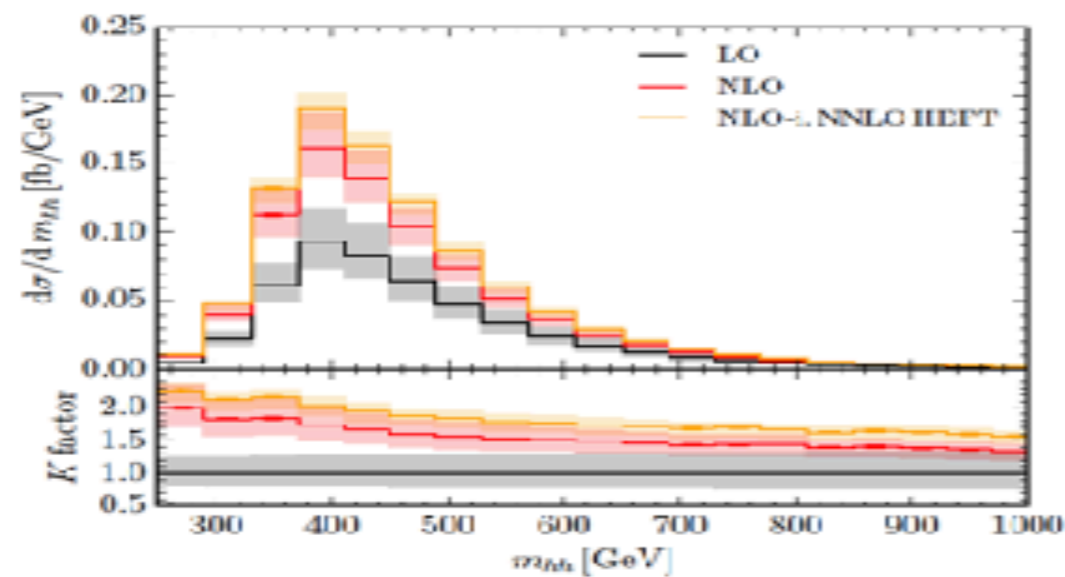


(d) 14 TeV, subleading p_T .

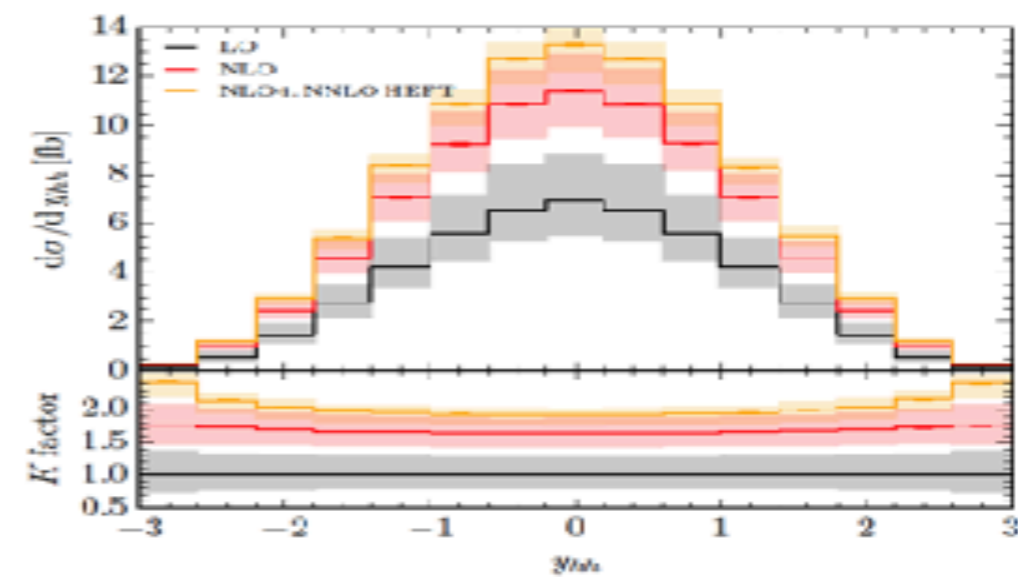


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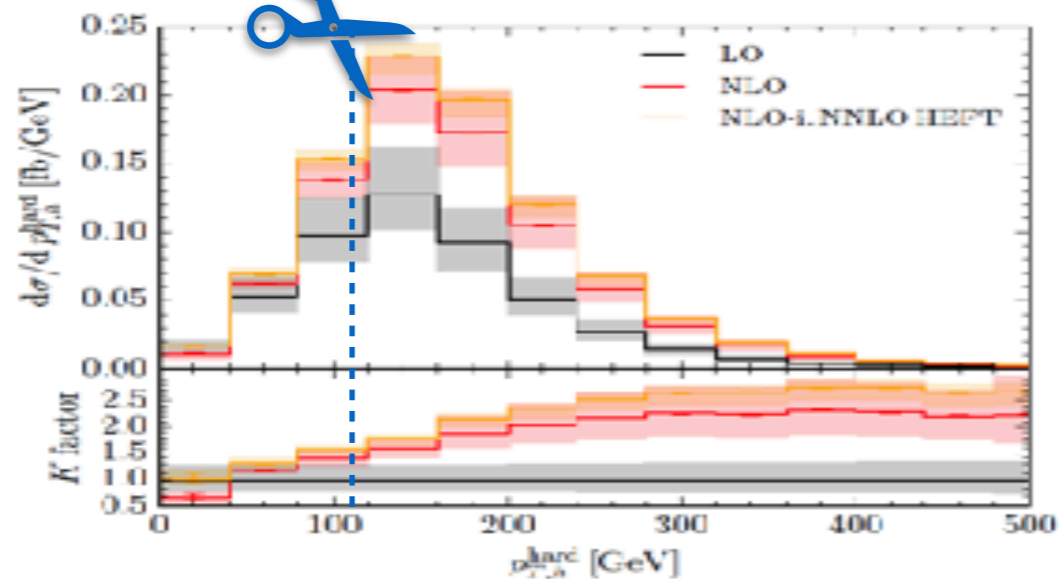
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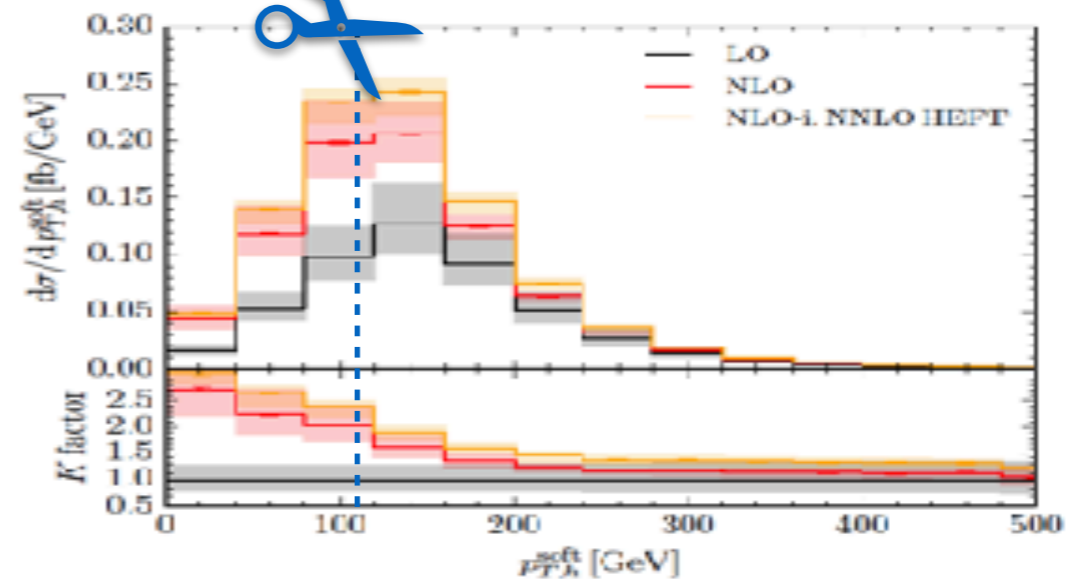
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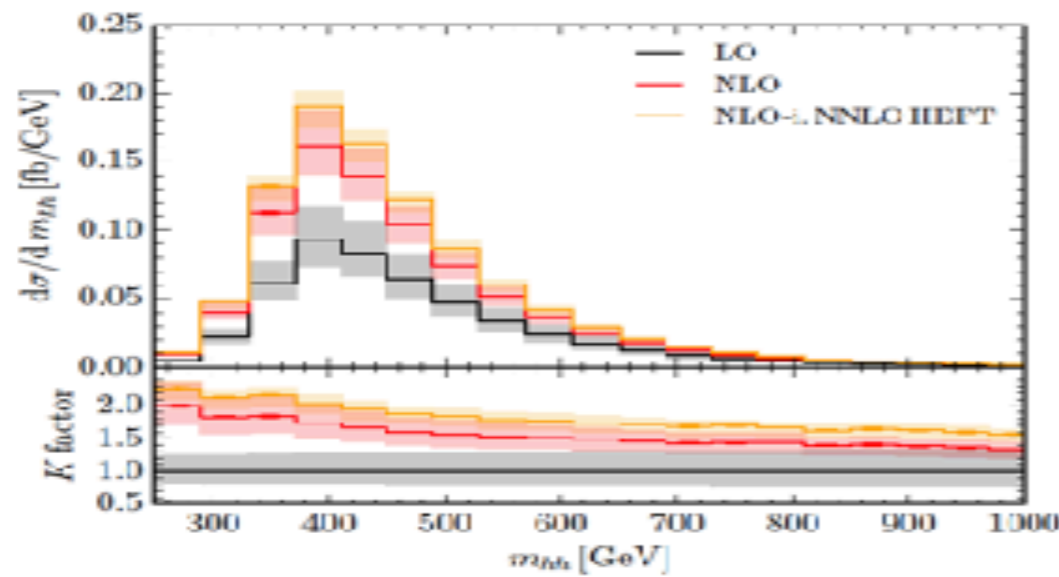


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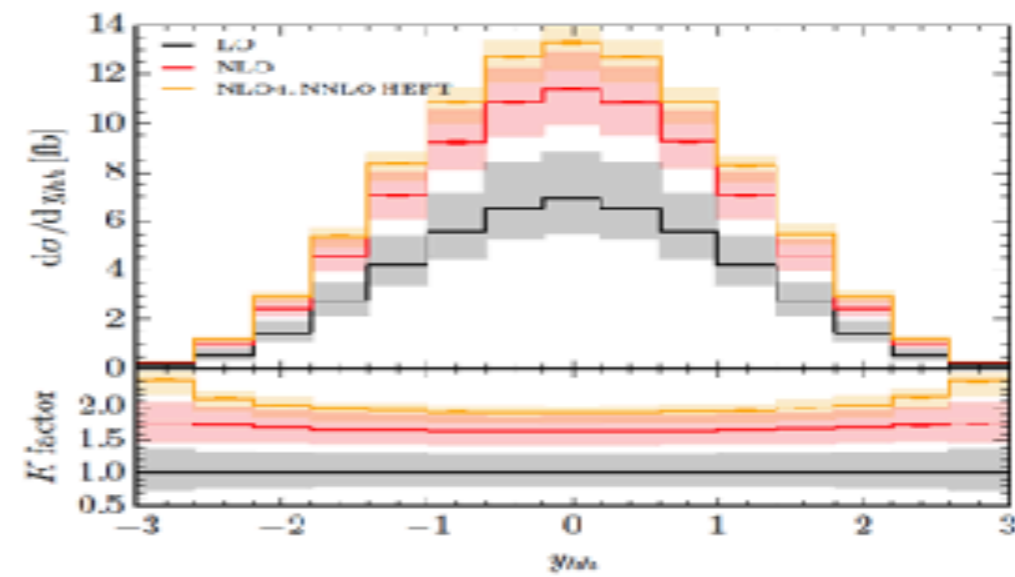


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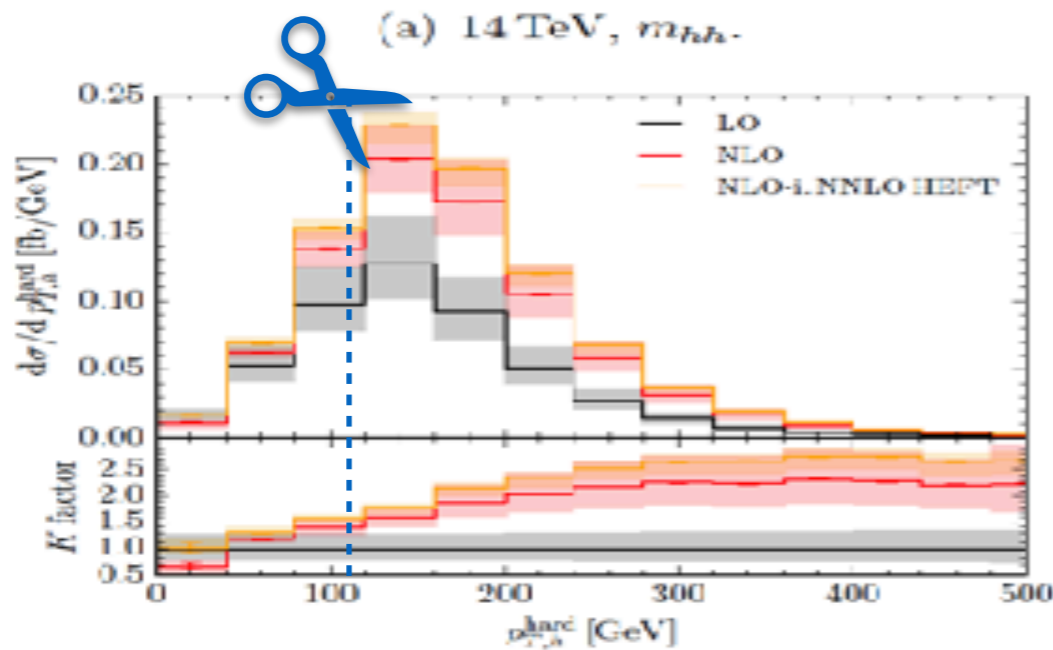
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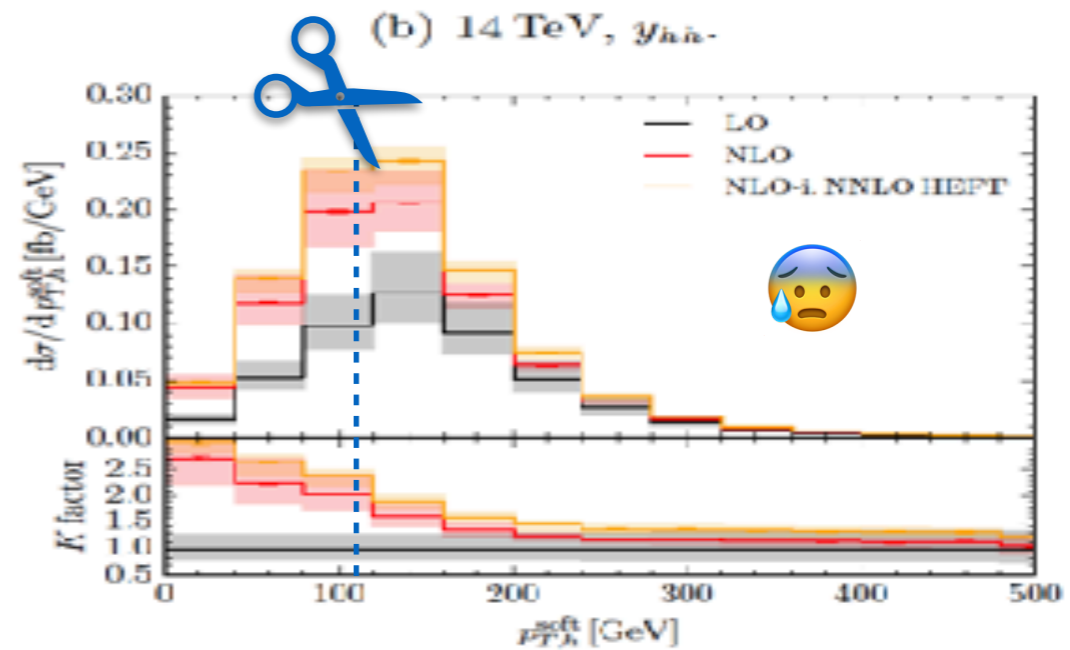
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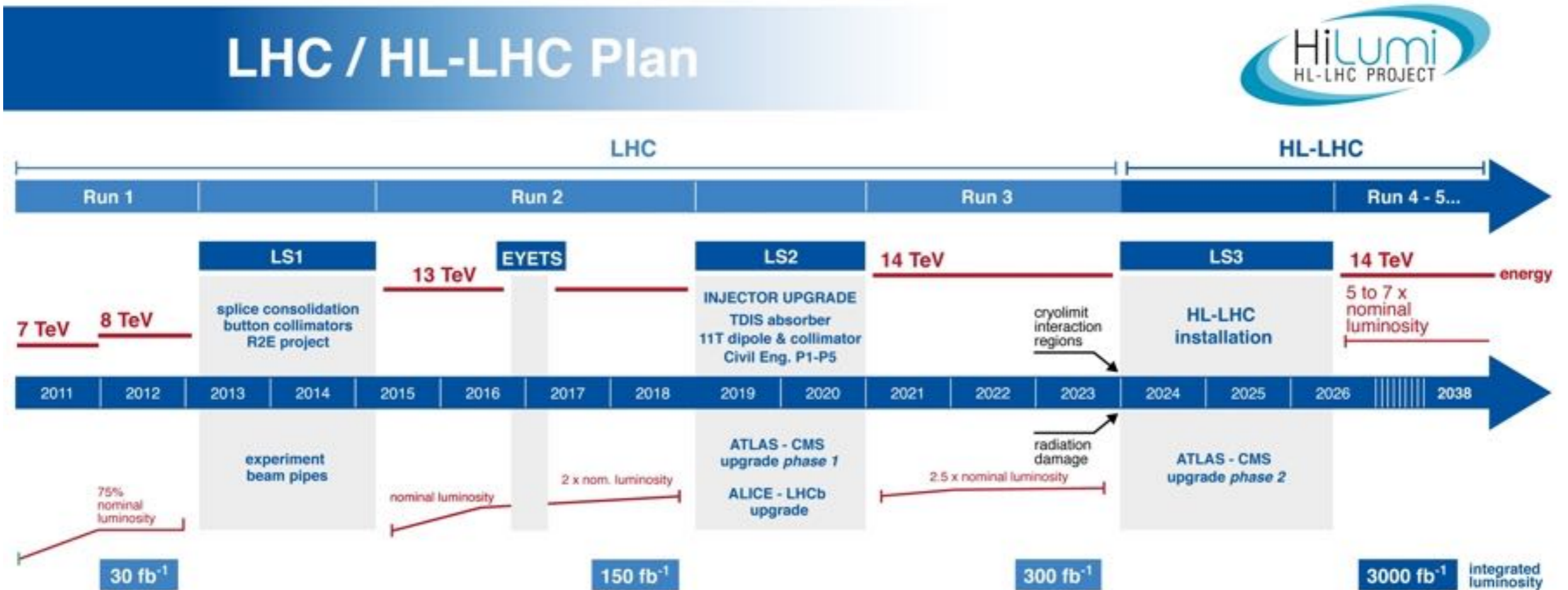


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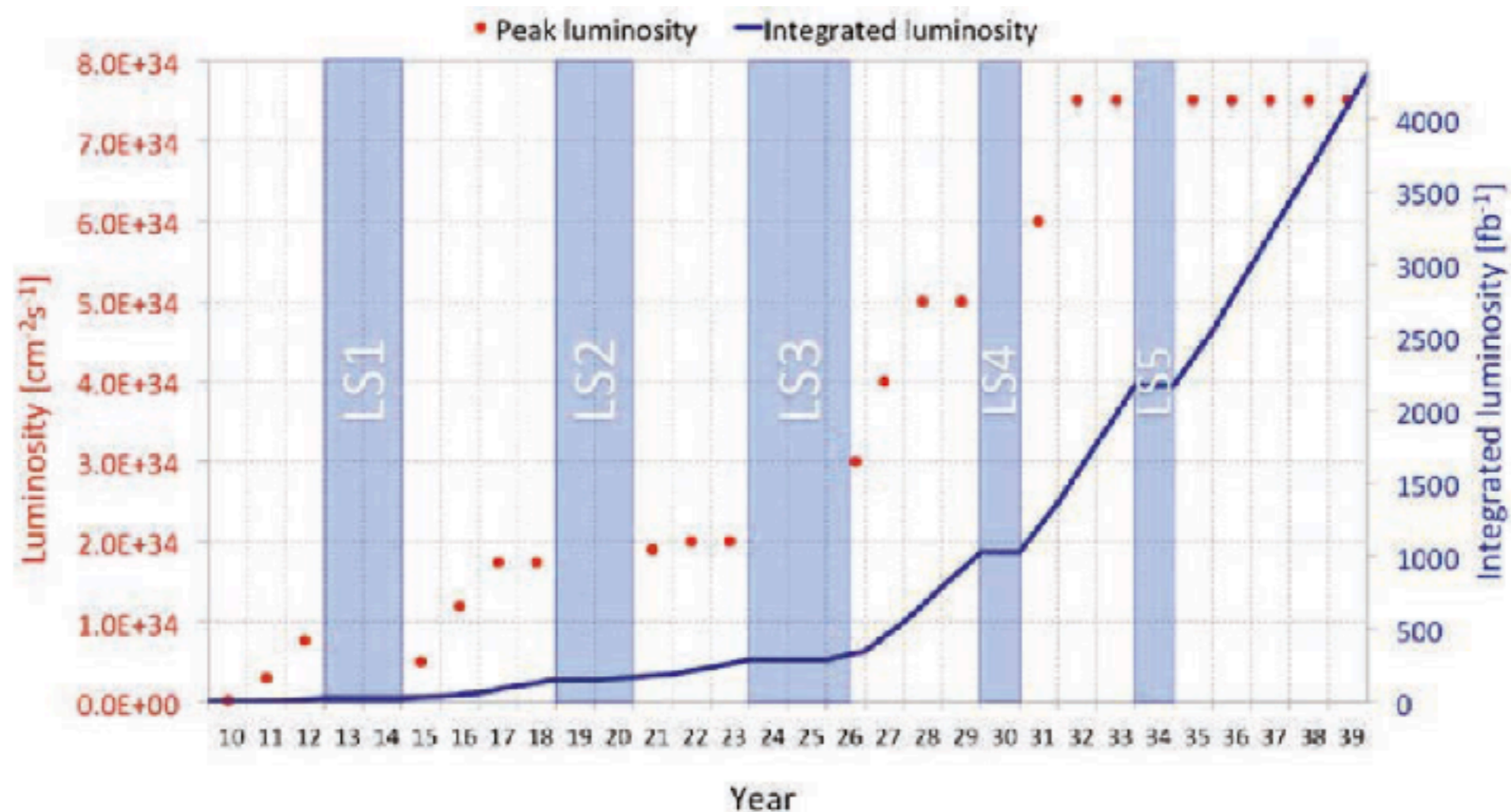
A Review of the LHC



- Quasi-future collider: High Luminosity LHC (HL-LHC).
- More data, lower statistic error.
- More data can probably help us reduce the systematic error.
- High luminosity, high pile-up...



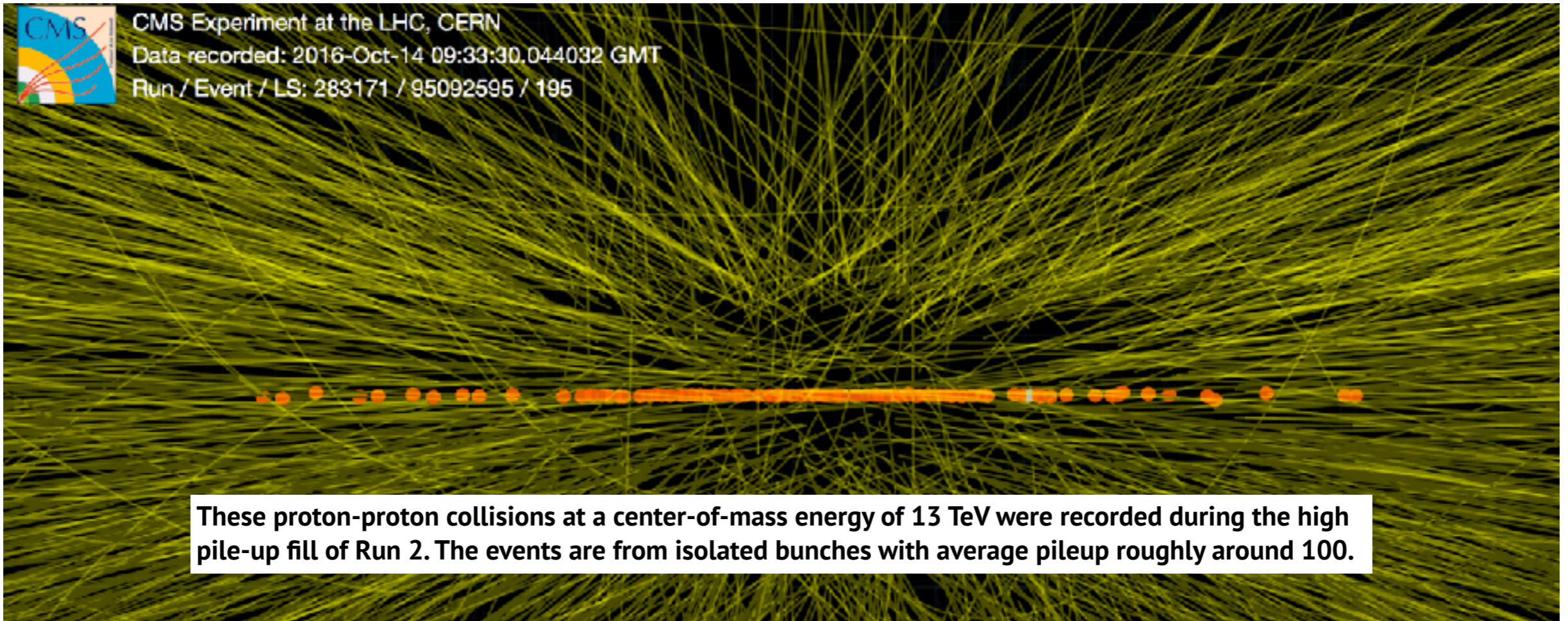
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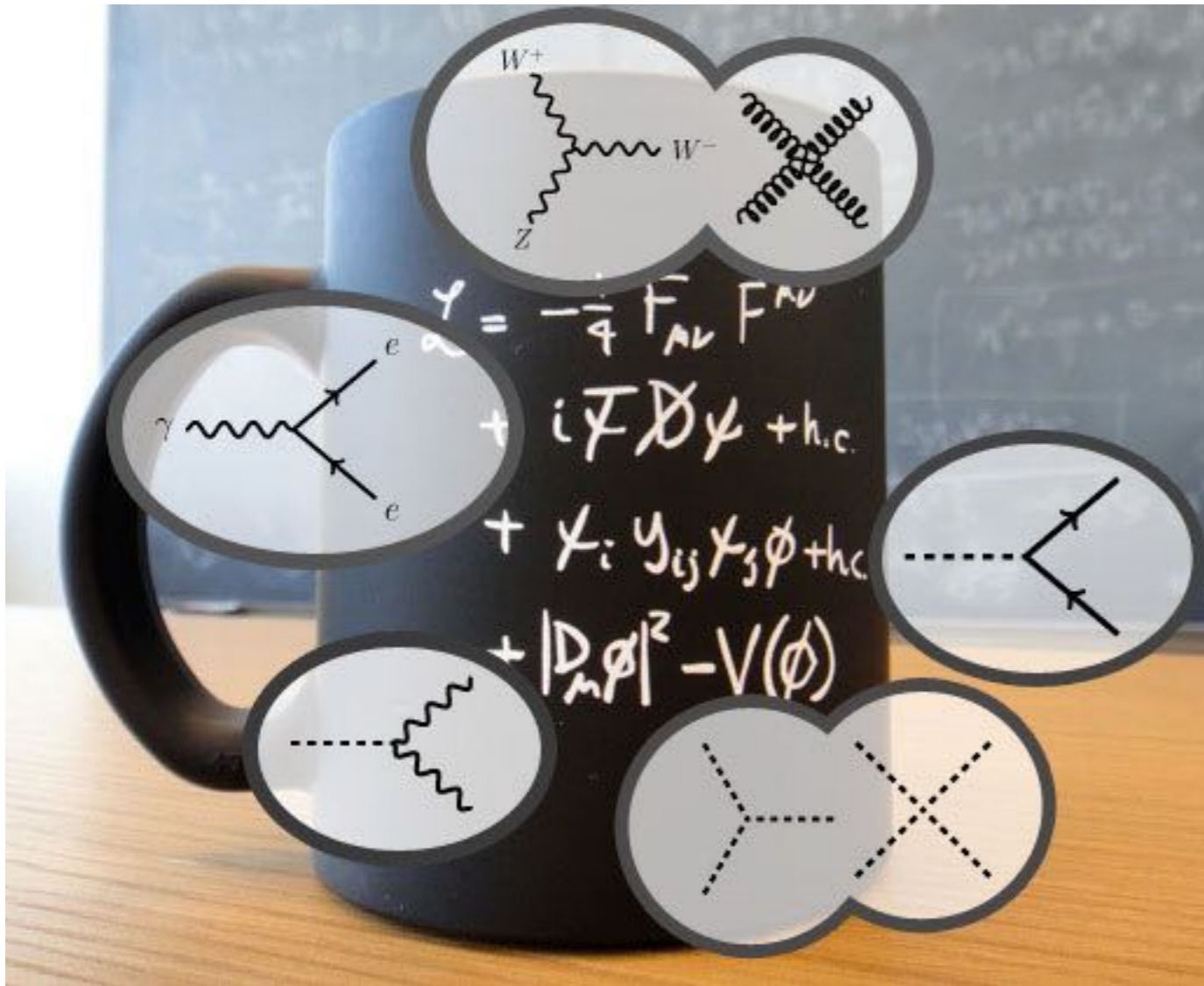
A Review of the LHC

- The LHC is a very powerful hadron collider.
- Advantages:
 - High energy;
 - High luminosity;
 - ...
- Disadvantages:
 - The effective c.m. energy is \sim TeV;
 - Large theoretical uncertainty, large SM backgrounds, large pile-up;
 - ...
- It is designed for discovering physics at high energy scale, but not precisely measurements.
- Is TeV enough?



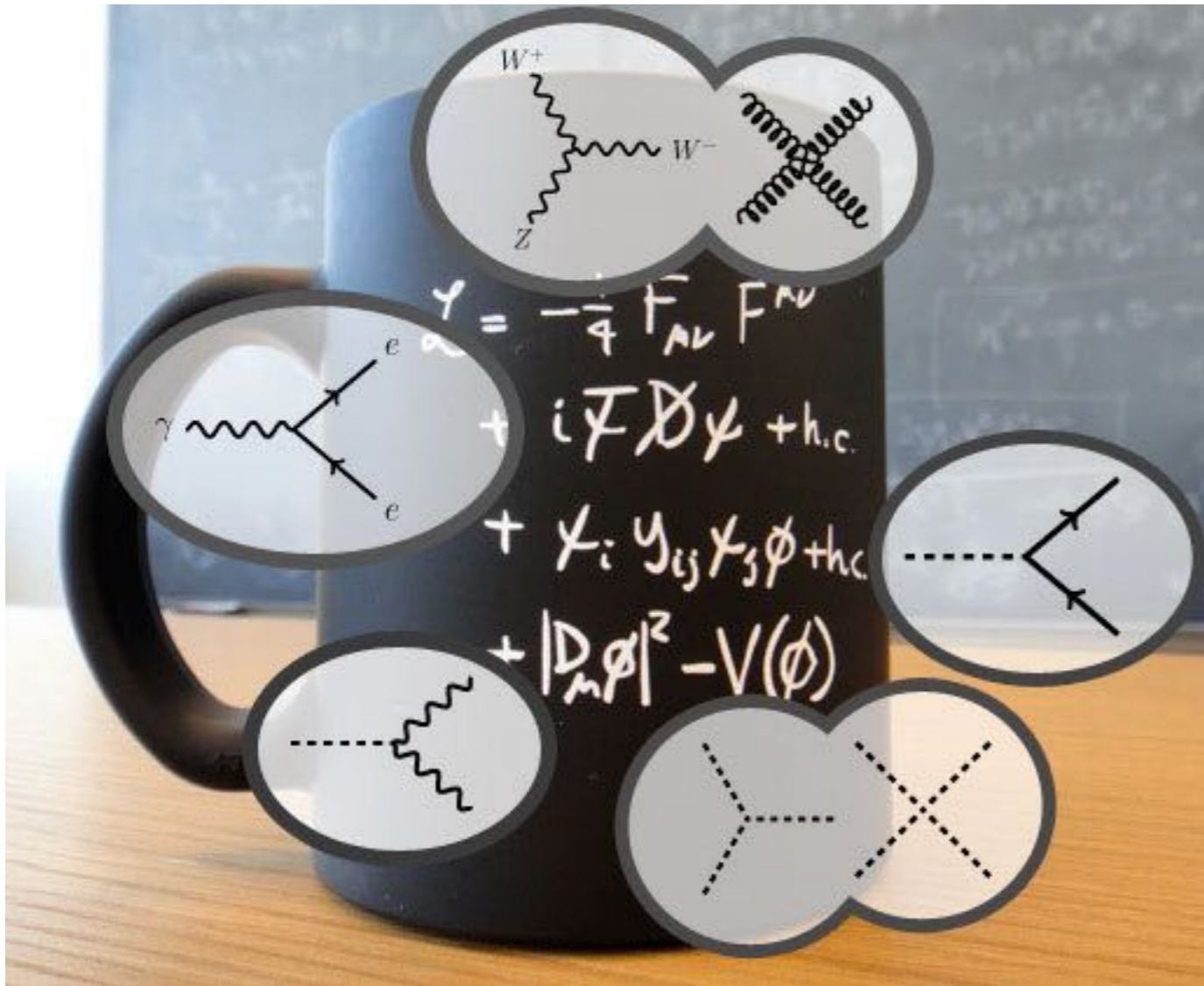
Some Challenges

- Do we really understand the SM well?



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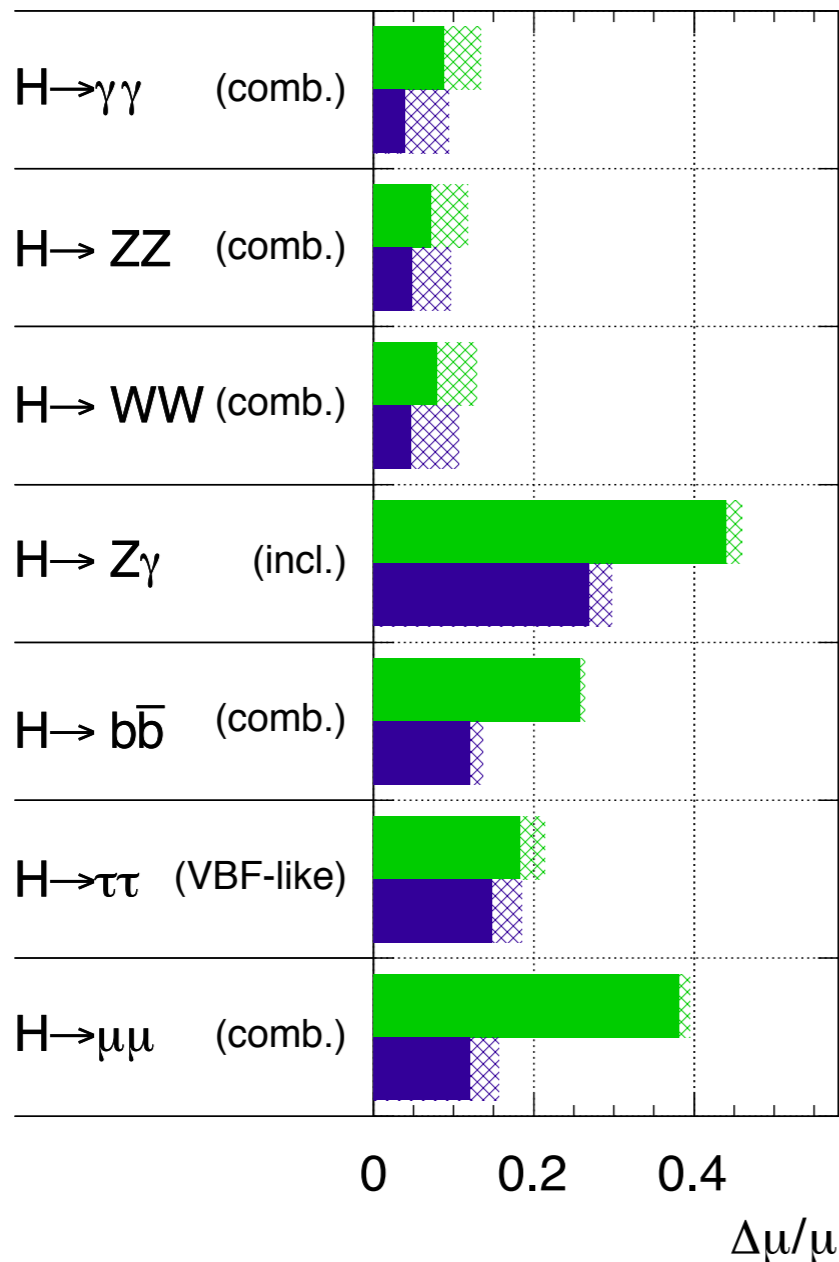
$$\begin{aligned}
 & -\frac{1}{2}\partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\nu^a g_\mu^b g_\nu^c - \frac{1}{4}g_s^2 f^{abc} f^{cde} g_\mu^a g_\nu^b g_\mu^c g_\nu^d + \\
 & \frac{1}{2}ig_s^2 (\bar{q}_i^\mu \gamma^\mu q_j^\nu) g_\mu^a + G^a \partial^2 G^a + g_s f^{abc} \partial_\mu G^a G^b g_\mu^c - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- - \\
 & M^2 W_\mu^+ W_\mu^- - \frac{1}{2}\partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2}M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2}\partial_\nu A_\nu \partial_\nu A_\nu - \frac{1}{2}\partial_\nu H \partial_\nu H - \\
 & \frac{1}{2}m_h^2 H^2 - \partial_\mu \phi^I \partial_\mu \phi^I - M^2 \phi^I \phi^I - \frac{1}{2}\partial_\mu \phi^0 \partial_\mu \phi^0 - \frac{1}{2}M\phi^I \phi^0 - \beta_h \left[\frac{2M^2}{g^2} + \right. \\
 & \left. \frac{2M}{g} H + \frac{1}{2}(H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-) \right] + \frac{2M^2}{g^2} \alpha_h - ig_{cW} [\partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - \\
 & W_\mu^- W_\nu^+) - Z_\mu^0 (W_\mu^+ \partial_\nu W_\nu^- - W_\mu^- \partial_\nu W_\nu^+) + Z_\mu^0 (W_\mu^+ \partial_\nu W_\nu^- - \\
 & W_\mu^- \partial_\nu W_\nu^+)] - ig_{sW} [\partial_\nu A_\mu (W_\mu^+ W_\nu^- - W_\mu^- W_\nu^+) - A_\nu (W_\mu^+ \partial_\nu W_\mu^- - \\
 & W_\mu^- \partial_\nu W_\mu^+) - A_\mu (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+)] - \frac{1}{2}g^2 W_\mu^+ W_\mu^- W_\nu^+ W_\nu^- - \\
 & \frac{1}{2}g^2 W_\mu^+ W_\nu^- W_\mu^- W_\nu^+ + g^2 e_w^2 (Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- - Z_\mu^0 Z_\nu^0 W_\mu^+ W_\nu^-) - \\
 & g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\nu W_\mu^+ W_\nu^-) + g^2 e_w e_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - \\
 & W_\mu^- W_\nu^+) - 2A_\nu Z_\mu^0 W_\mu^+ W_\nu^-] - g\alpha [H^3 + H\phi^0 \phi^0 + 2H\phi^+ \phi^-] - \\
 & \frac{1}{8}g^2 \alpha_h [H^4 + (\phi^0)^4 + 4(\phi^+ \phi^-)^2 + 4(\phi^I)^2 \phi^I \phi^I + 4H^2 \phi^I \phi^I + 2(\phi^0)^2 H^2] - \\
 & gM W_\mu^+ W_\mu^- H - \frac{1}{2}g \frac{M}{c_w} Z_\mu^0 Z_\mu^0 H - \frac{1}{2}ig [W_\mu^+ (\phi^I \partial_\mu \phi^I - \phi^I \partial_\mu \phi^I) - \\
 & W_\mu^- (\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0)] + \frac{1}{2}g [W_\mu^+ (H \partial_\mu \phi^- - \phi^- \partial_\mu H) - W_\mu^- (H \partial_\mu \phi^+ - \\
 & \phi^+ \partial_\mu H)] + \frac{1}{2}g \frac{1}{c_w} (Z_\mu^0 (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) - ig \frac{M}{c_w} Z_\mu^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+)) + \\
 & ig_{sW} M A_\mu (W_\mu^+ \phi^- - W_\mu^- \phi^+) - ig \frac{1}{2c_w} Z_\mu^0 (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + \\
 & ig_{sW} A_\nu (\phi^+ \partial_\nu \phi^- - \phi^- \partial_\nu \phi^+) - \frac{1}{4}g^2 W_\mu^+ W_\mu^- H^2 + (\phi^0)^2 + 2\phi^+ \phi^- - \\
 & \frac{1}{2}g^2 \frac{1}{c_w} Z_\mu^0 Z_\mu^0 H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2 \phi^+ \phi^- - \frac{1}{2}g^2 \frac{e_w^2}{c_w} Z_\mu^0 \phi^0 (W_\mu^- \phi^- + \\
 & W_\mu^+ \phi^+) - \frac{1}{2}ig^2 \frac{M}{c_w} Z_\mu^0 H (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0 (W_\mu^+ \phi^- + \\
 & W_\mu^- \phi^+) + \frac{1}{2}ig^2 s_w A_\mu H (W_\mu^+ \phi^- - W_\mu^- \phi^+) - g^2 \frac{e_w}{c_w} (2c_w^2 - 1) Z_\mu^0 A_\mu \phi^+ \phi^- - \\
 & g^1 s_w^2 A_\mu A_\mu \phi^+ \phi^- - \bar{e}^\lambda (\gamma^\mu + m_e^1) e^\lambda - \bar{\nu}^\lambda \gamma^\mu \nu^\lambda - \bar{u}_j^\lambda (\gamma^\mu + m_u^1) u_j^\lambda - \\
 & \bar{d}_j^\lambda (\gamma^\mu - m_d^1) d_j^\lambda + ig_{sW} A_\mu [-(\bar{e}^\lambda \gamma^\mu e^\lambda) + \frac{2}{3}(\bar{u}_j^\lambda \gamma^\mu u_j^\lambda) - \frac{1}{3}(\bar{d}_j^\lambda \gamma^\mu d_j^\lambda)] + \\
 & \frac{ig}{c_w} Z_\mu^0 (\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{e}^\lambda \gamma^\mu (4s_w^2 - 1 - \gamma^5) e^\lambda) + (\bar{u}_j^\lambda \gamma^\mu (\frac{4}{3}s_w^2 - \\
 & 1 - \gamma^5) u_j^\lambda) + (\bar{d}_j^\lambda \gamma^\mu (1 - \frac{2}{3}s_w^2 - \gamma^5) d_j^\lambda) + \frac{ig}{2\sqrt{2}} W_\mu^+ (\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) - \\
 & (\bar{u}_j^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda\kappa} d_j^\lambda) + \frac{ig}{2\sqrt{2}} W_\mu^- (\bar{e}^\lambda \gamma^\mu (1 + \gamma^5) e^\lambda) - (\bar{u}_j^\lambda C_{\lambda\kappa}^\dagger \gamma^\mu (1 + \\
 & \gamma^5) u_j^\lambda) + \frac{ig}{2\sqrt{2}} \frac{m_\lambda^1}{2d} [-\phi^+ (\bar{\nu}^\lambda (1 - \gamma^5) e^\lambda) + \phi^- (\bar{e}^\lambda (1 + \gamma^5) \nu^\lambda)] - \\
 & \frac{g}{2} \frac{m_\lambda^1}{M} [H (\bar{e}^\lambda e^\lambda) + i\phi^0 (\bar{e}^\lambda \gamma^5 e^\lambda)] + \frac{ig}{2M\sqrt{2}} \phi^- [-m_\lambda^1 (\bar{u}_j^\lambda C_{\lambda\kappa} (1 - \gamma^5) d_j^\lambda) + \\
 & m_\lambda^1 (\bar{u}_j^\lambda C_{\lambda\kappa} (1 - \gamma^5) d_j^\lambda) + \frac{ig}{2M\sqrt{2}} \phi^- [m_\lambda^1 (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 + \gamma^5) u_j^\lambda) - m_\lambda^1 (\bar{u}_j^\lambda C_{\lambda\kappa}^\dagger (1 - \\
 & \gamma^5) u_j^\lambda) - \frac{g}{2} \frac{m_\lambda^1}{M} H (\bar{u}_j^\lambda u_j^\lambda) - \frac{g}{2} \frac{m_\lambda^1}{M} H (\bar{d}_j^\lambda d_j^\lambda) + \frac{g}{2} \frac{m_\lambda^1}{M} \phi^0 (\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \\
 & \frac{ig}{2} \frac{m_\lambda^1}{M} \phi^0 (\bar{d}_j^\lambda \gamma^5 d_j^\lambda) - \bar{X}^+ (\partial^2 - M^2) X^+ + \bar{X}^- (\partial^2 - M^2) X^- + \bar{X}^0 (\partial^2 - \\
 & \frac{M^2}{c_w}) X^0 + \bar{Y} \partial^2 Y + ig_{cW} W_\mu^+ (\partial_\mu \bar{X}^0 X^- - \partial_\mu \bar{X}^- X^0) + ig_{sW} W_\mu^+ (\partial_\mu \bar{Y} X^- - \\
 & \partial_\mu \bar{X}^+ Y) + ig_{cW} W_\mu^- (\partial_\mu \bar{X}^- X^0 - \partial_\mu \bar{X}^0 X^-) + ig_{sW} W_\mu^- (\partial_\mu \bar{X}^- Y - \\
 & \partial_\mu \bar{Y} X^+) + ig_{cW} Z_\mu^0 (\partial_\mu \bar{X}^+ X^- - \partial_\mu \bar{X}^- X^+) - ig_{sW} A_\mu (\partial_\mu \bar{X}^+ X^- - \\
 & \partial_\mu \bar{X}^- X^+) - \frac{1}{2}gM [\bar{X}^+ X^+ H + \bar{X}^- X^- H + \frac{1}{c_w} \bar{X}^0 X^0 H] + \\
 & \frac{1}{2} \frac{2e_w^2}{c_w} igM [\bar{X}^- X^0 \phi^+ - \bar{X}^- X^0 \phi^-] + \frac{1}{2} igM [\bar{X}^+ X^- \phi^+ - \bar{X}^+ X^- \phi^-] + \\
 & igM e_w [\bar{X}^+ X^+ \phi^I - X^+ X^+ \phi^I] + \frac{1}{2} igM [\bar{X}^+ X^+ \phi^I - X^+ X^+ \phi^I]
 \end{aligned}$$

Some Challenges

- Example: precisely Higgs physics.

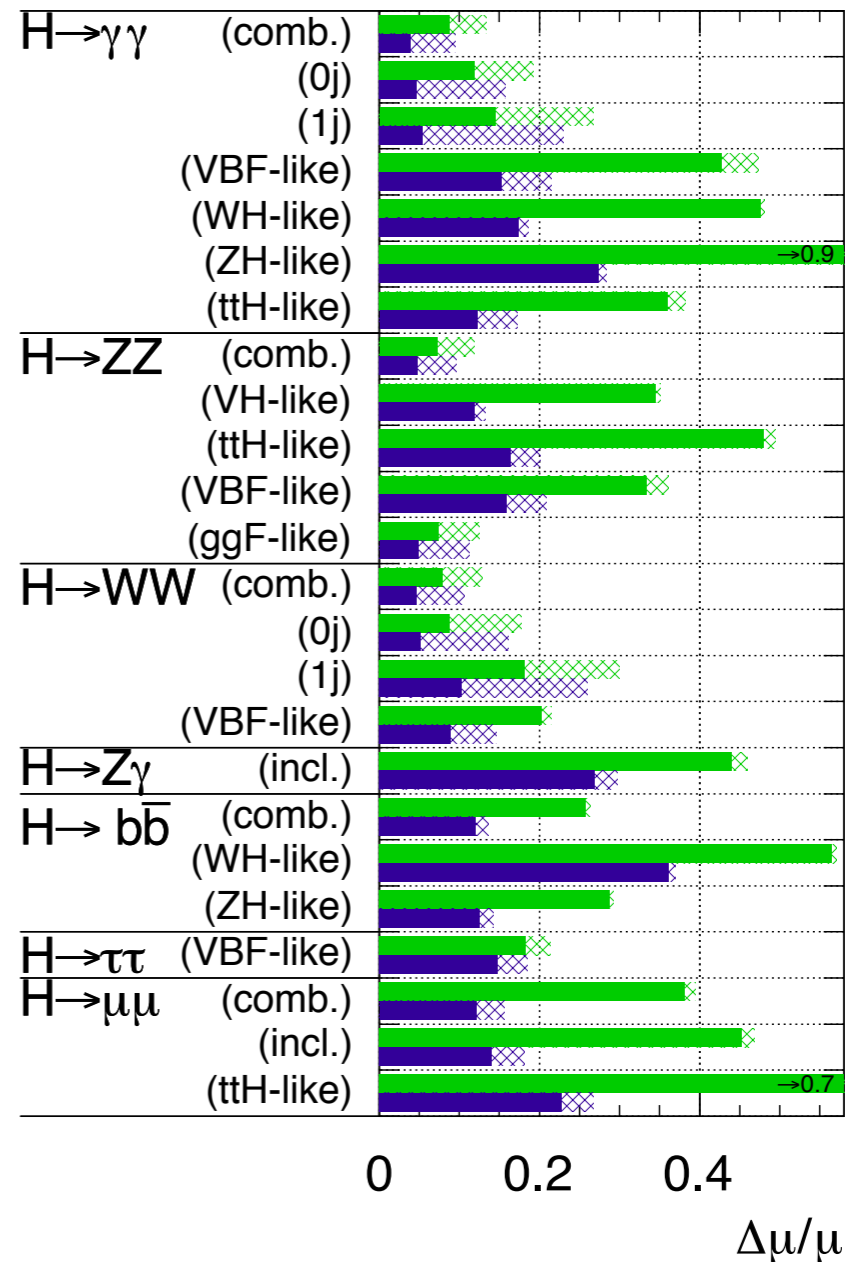
ATLAS Simulation Preliminary

$\sqrt{s} = 14$ TeV: $\int L dt = 300 \text{ fb}^{-1}$; $\int L dt = 3000 \text{ fb}^{-1}$



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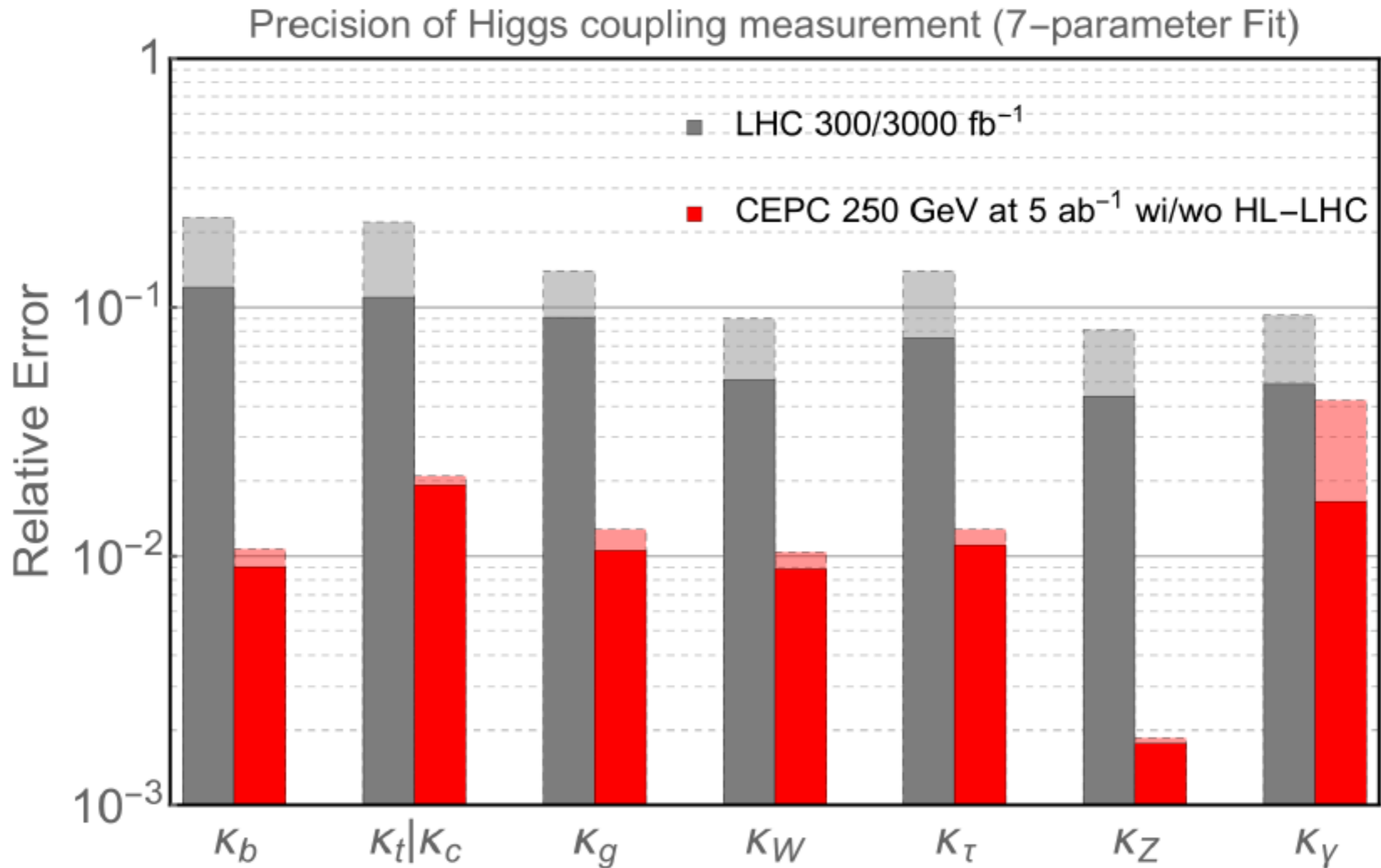
- Example: precisely Higgs physics.

$\Delta\mu/\mu$	300 fb ⁻¹		3000 fb ⁻¹	
	All unc.	No theory unc.	All unc.	No theory unc.
$H \rightarrow \gamma\gamma$ (comb.)	0.13	0.09	0.09	0.04
(0j)	0.19	0.12	0.16	0.05
(1j)	0.27	0.14	0.23	0.05
(VBF-like)	0.47	0.43	0.22	0.15
(WH-like)	0.48	0.48	0.19	0.17
(ZH-like)	0.85	0.85	0.28	0.27
(ttH-like)	0.38	0.36	0.17	0.12
$H \rightarrow ZZ$ (comb.)	0.11	0.07	0.09	0.04
(VH-like)	0.35	0.34	0.13	0.12
(ttH-like)	0.49	0.48	0.20	0.16
(VBF-like)	0.36	0.33	0.21	0.16
(ggF-like)	0.12	0.07	0.11	0.04
$H \rightarrow WW$ (comb.)	0.13	0.08	0.11	0.05
(0j)	0.18	0.09	0.16	0.05
(1j)	0.30	0.18	0.26	0.10
(VBF-like)	0.21	0.20	0.15	0.09
$H \rightarrow Z\gamma$ (incl.)	0.46	0.44	0.30	0.27
$H \rightarrow b\bar{b}$ (comb.)	0.26	0.26	0.14	0.12
(WH-like)	0.57	0.56	0.37	0.36
(ZH-like)	0.29	0.29	0.14	0.13
$H \rightarrow \tau\tau$ (VBF-like)	0.21	0.18	0.19	0.15
$H \rightarrow \mu\mu$ (comb.)	0.39	0.38	0.16	0.12
(incl.)	0.47	0.45	0.18	0.14
(ttH-like)	0.74	0.72	0.27	0.23



Some Challenges

- Example: precisely Higgs physics.



Some Challenges

- Example: precisely Higgs physics.



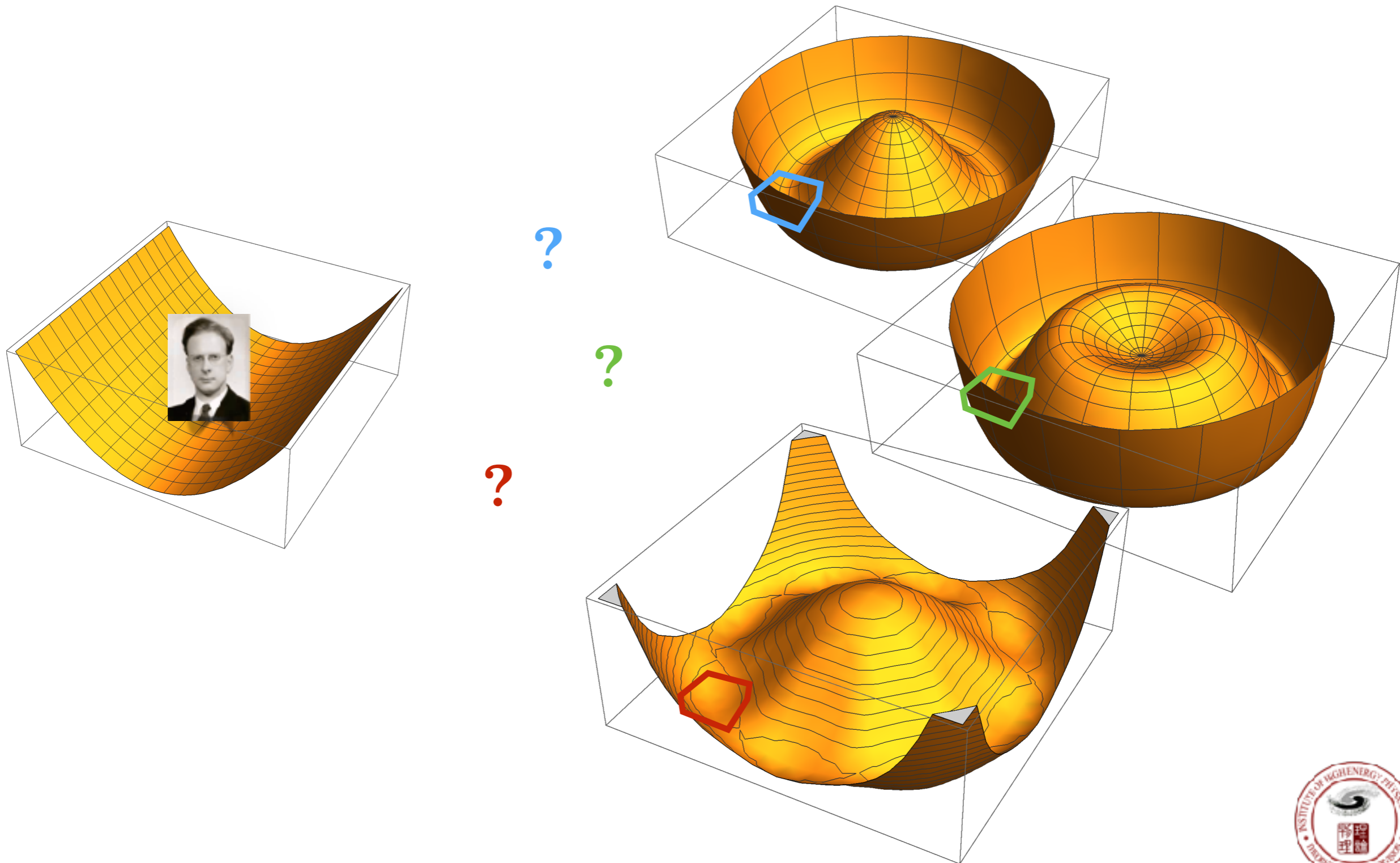
Some Challenges

- Example: precisely Higgs physics.



Some Challenges

- Example: understand the EWSB.



Some Challenges

- Example: understand the EWSB.

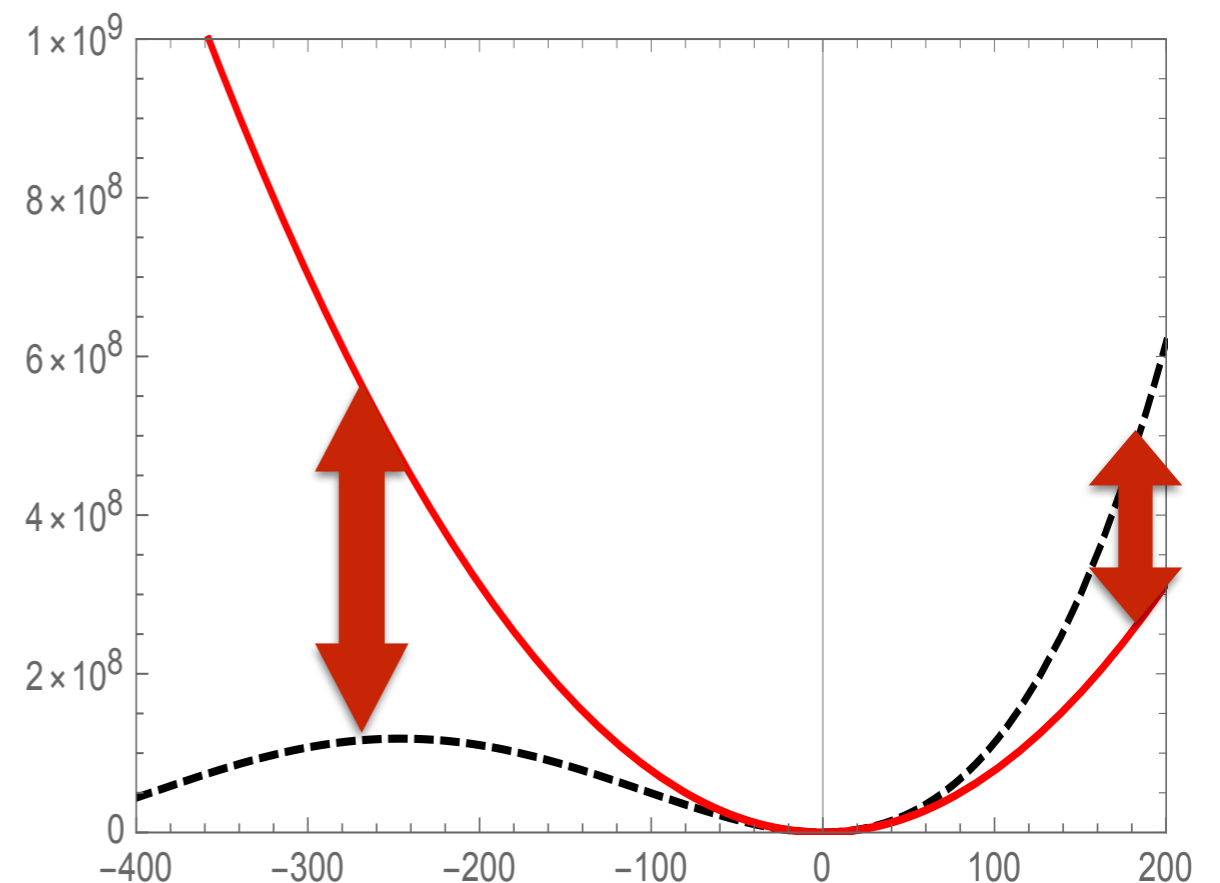
$$V(\Phi)_{SM} = \lambda (\Phi^\dagger \Phi - v^2)^2$$

$$\Phi(x) \sim \exp \left[ig' \alpha(x) + ig \sum_{j=1}^3 \sigma^j \alpha_j(x) \right] \left(v + \frac{h(x)}{\sqrt{2}} \right)$$

$$V(\Phi)_{SM} = \frac{1}{2} (4\lambda v^2) h^2 + \sqrt{2} \lambda v h^3 + \frac{\lambda}{4} h^4$$

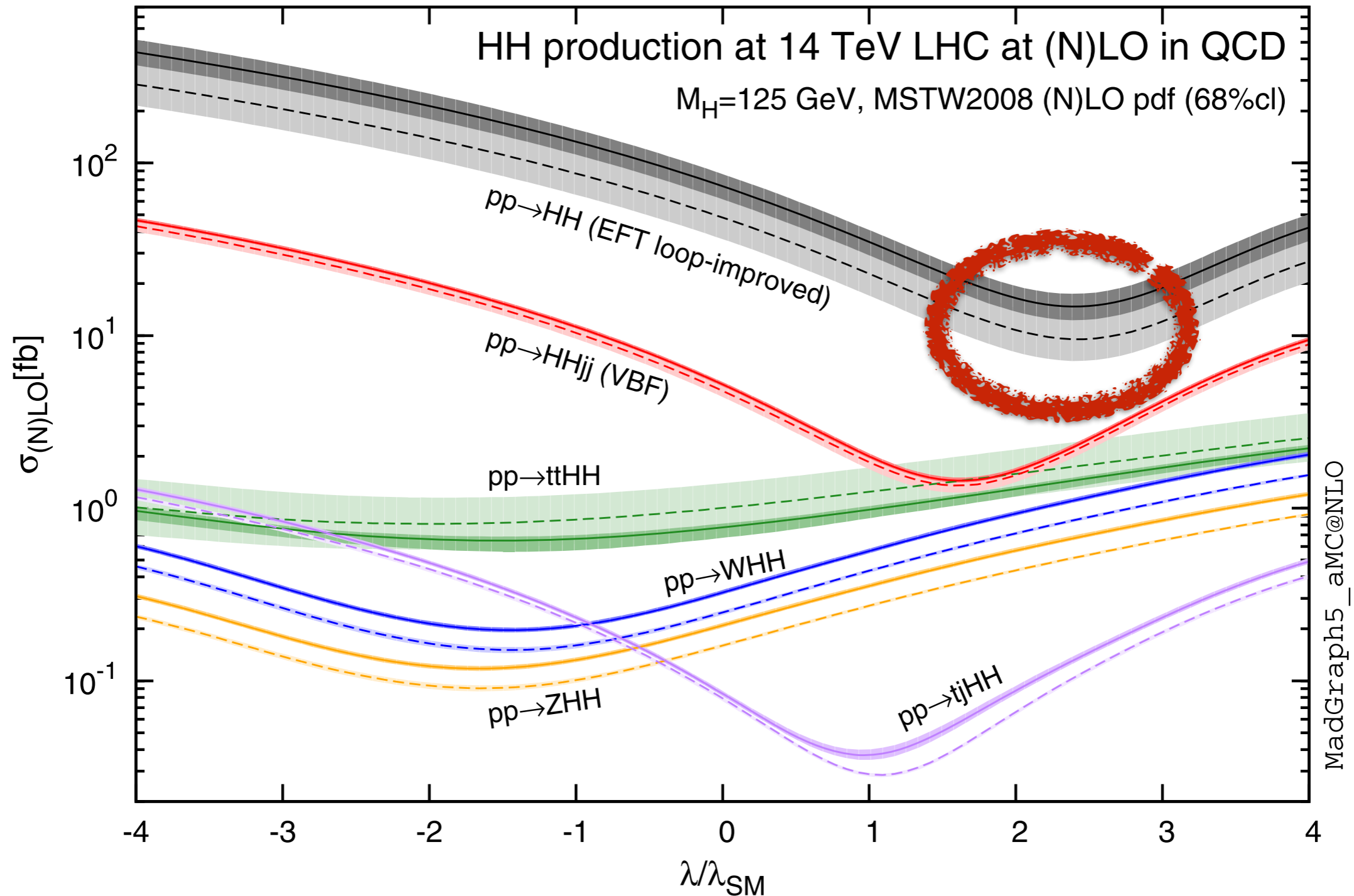
**Zero temperature,
tree level!**

$$\lambda_{SM} = \frac{m_h^2}{4v^2} \sim 0.13$$



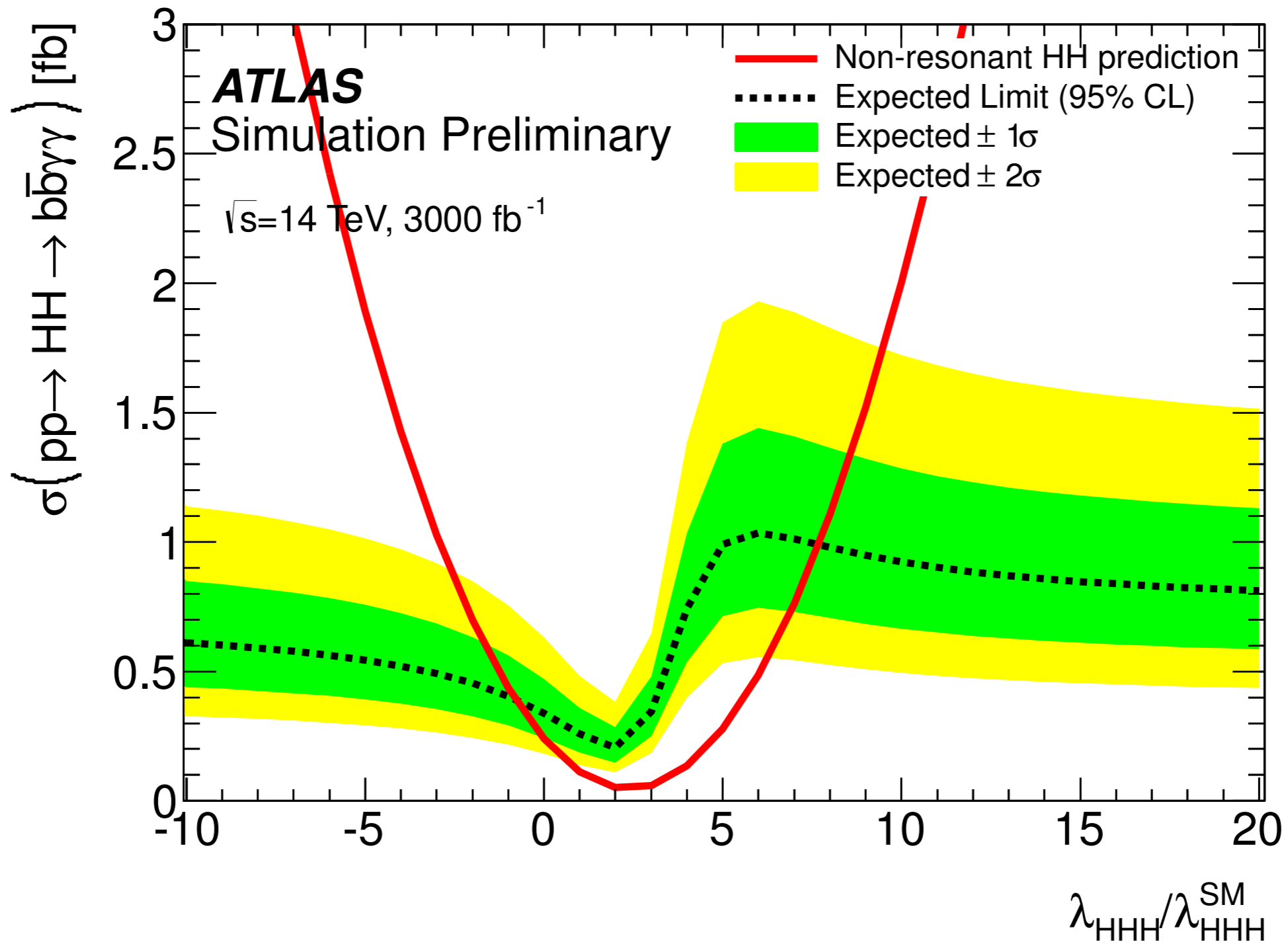
Some Challenges

- Example: understand the EWSB.



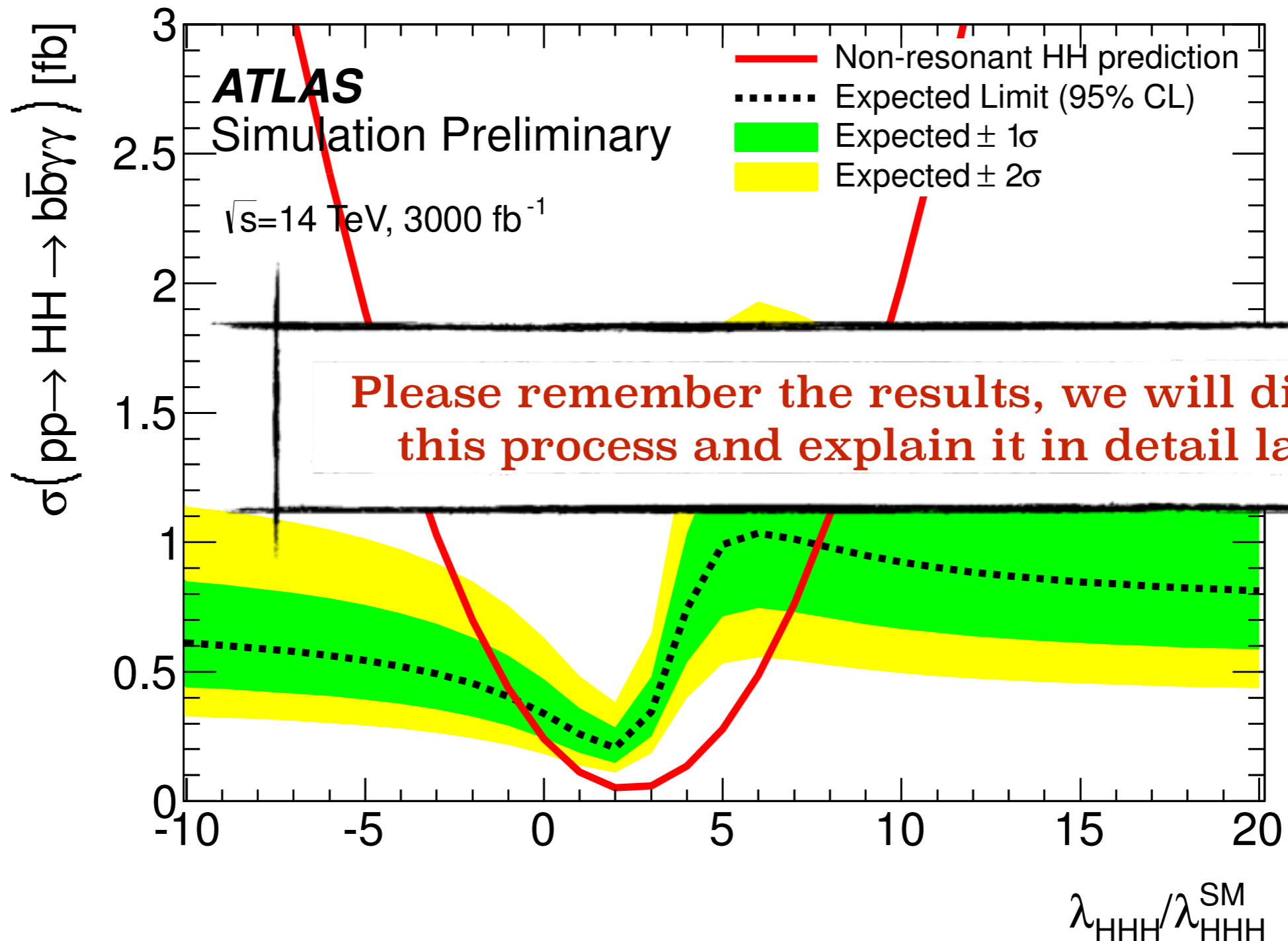
Some Challenges

- Example: understand the EWSB.



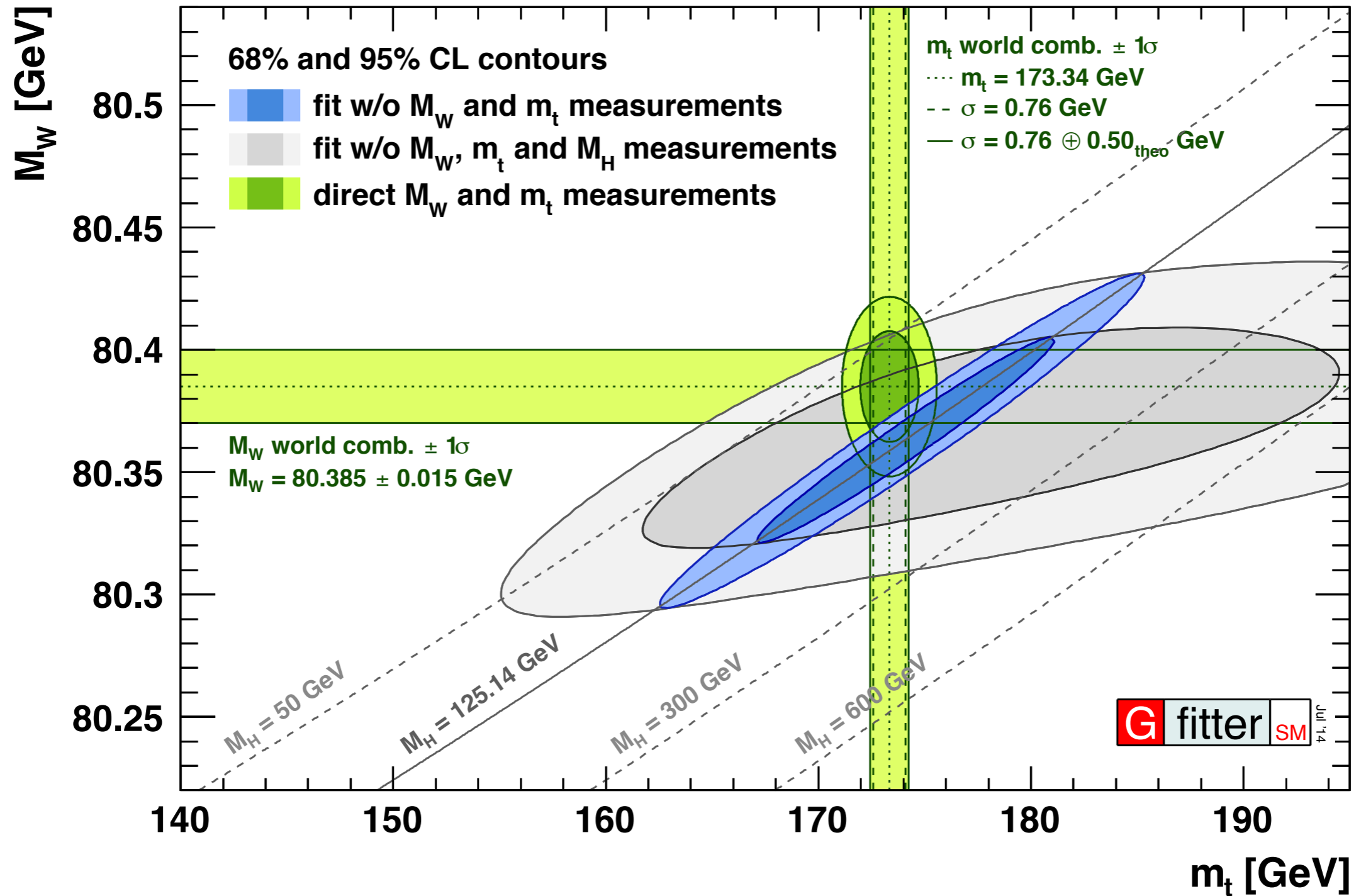
Some Challenges

- Example: understand the EWSB.



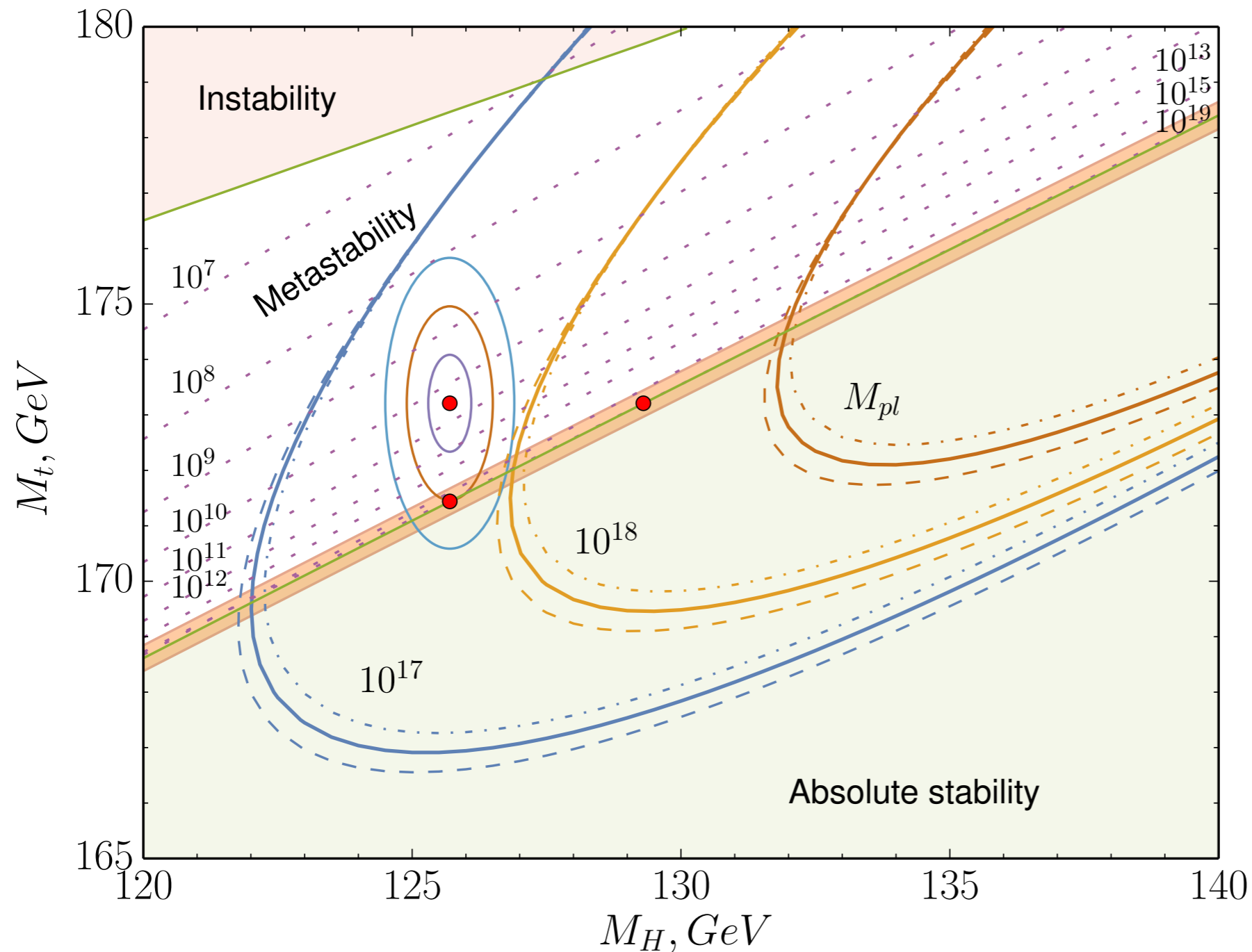
Some Challenges

- Example: top quark “mass”.



Some Challenges

- Example: top quark “mass”.



The diagram shows a top quark self-energy loop. It consists of a solid line forming a square loop, with dashed lines extending from the four vertices. Below the diagram is the equation for the beta function β_λ :

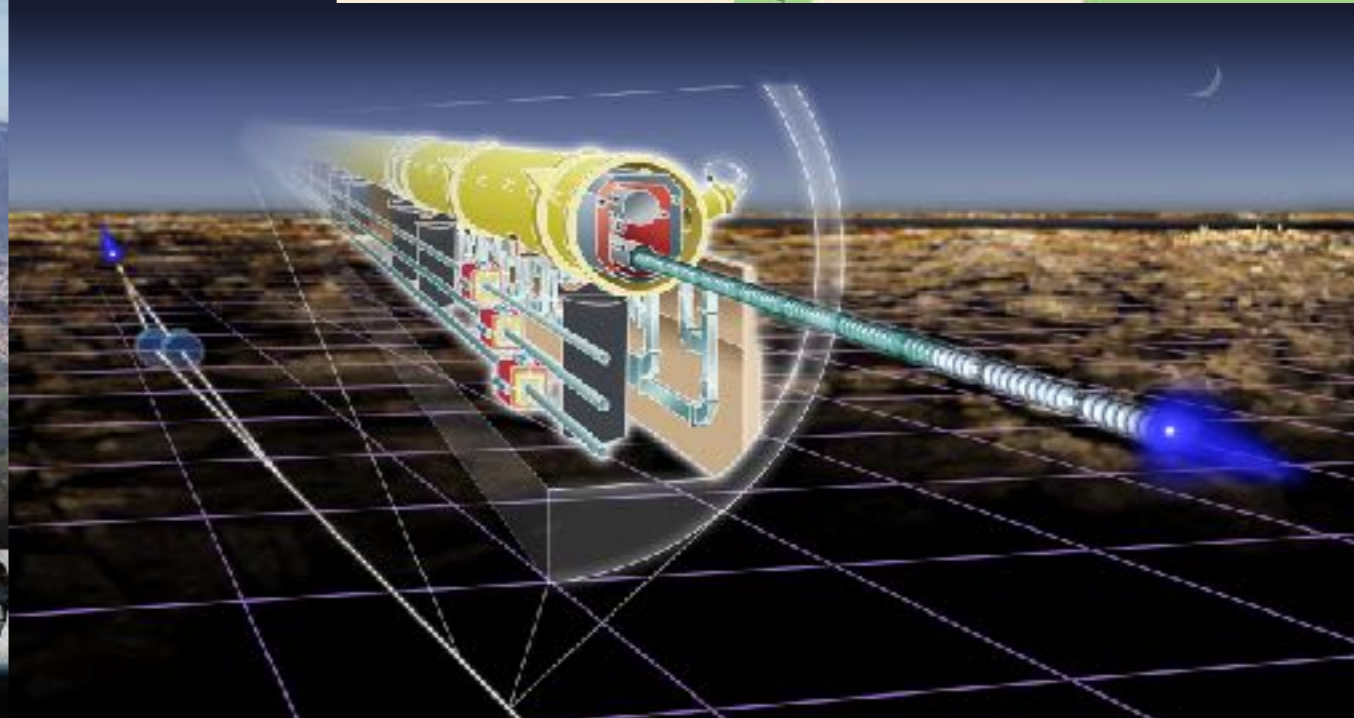
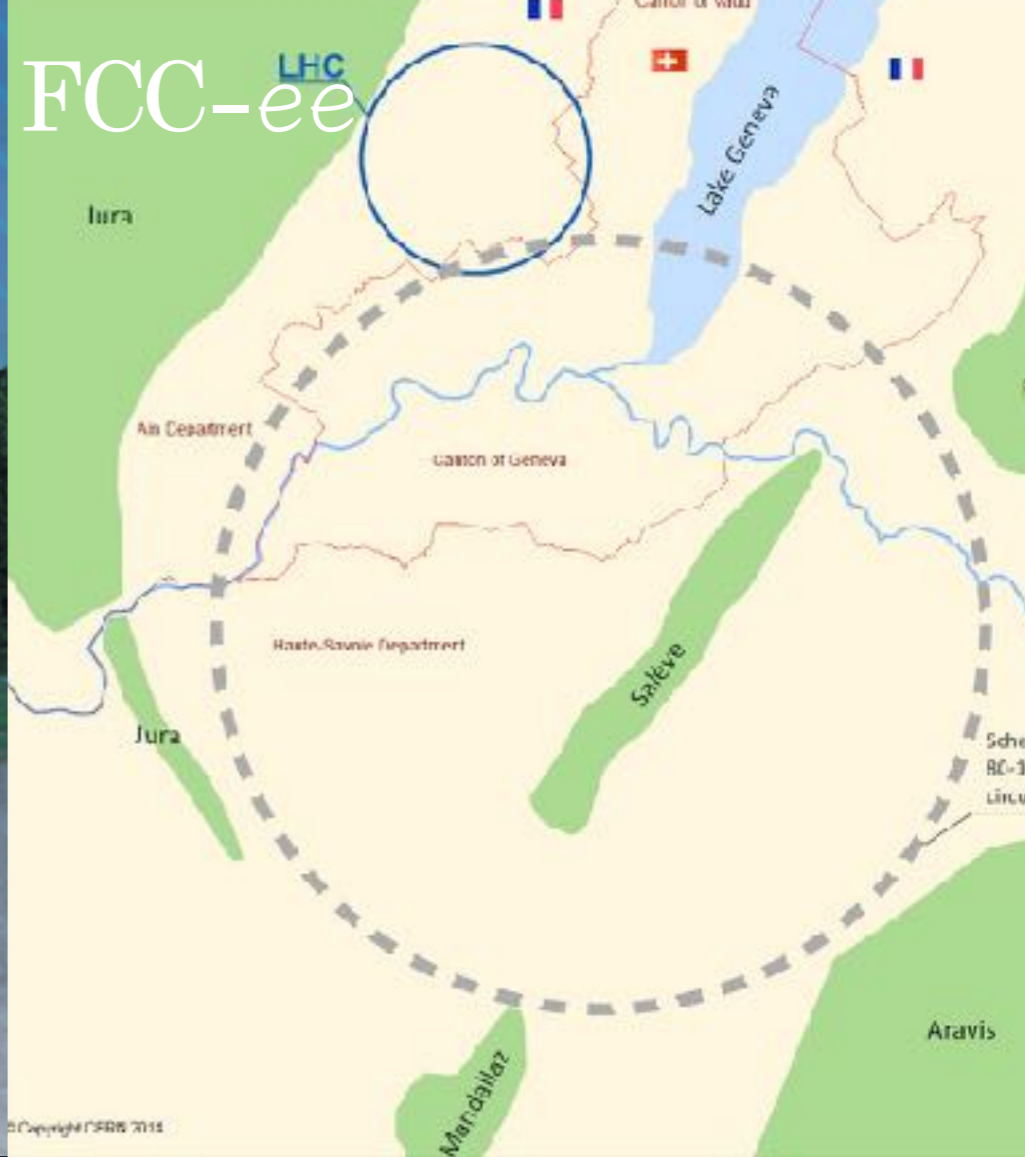
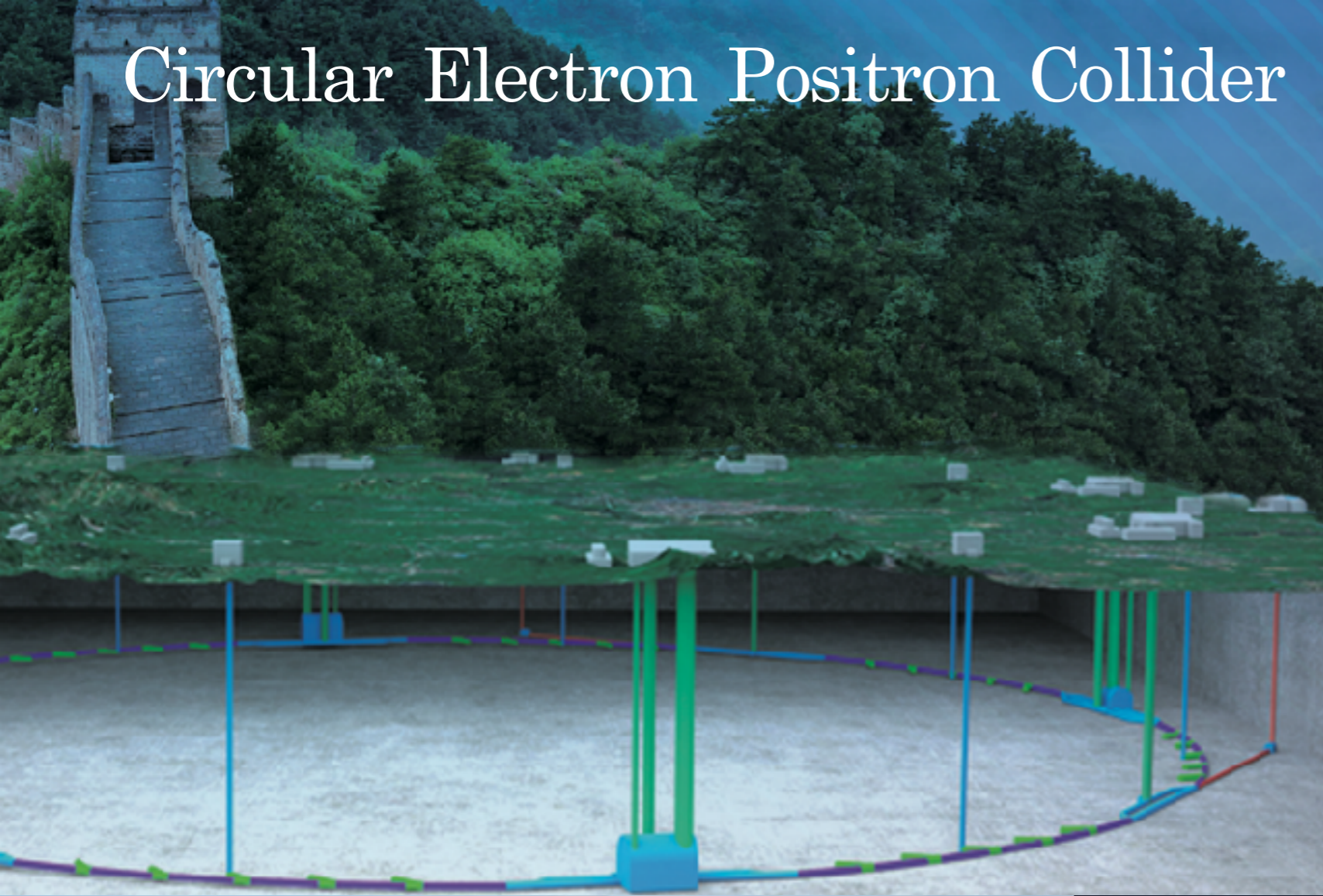
$$\beta_\lambda \ni - \frac{(M_t^{\overline{MS}})^4}{16\pi^2 v_0^4}$$

Future Collider Plans

- Future lepton collider plans (in alphabetical order):
 - Circular Electron Positron Collider (CEPC)
 - Compact Linear Collider (CLIC)
 - Future Circular Collider - e^+e^- (FCC-ee, TLEP)
 - International Linear Collider (ILC)
- Future hadron collider plans:
 - Future Circular Collider - hadron-hadron (FCC-hh)
 - Super Proton Proton Collider (SPPC)
- Other plans:
 - Future Circular Collider - eh (FCC- eh)
 - Muon Collider?
 - Gamma-Gamma Collider?
 - ...



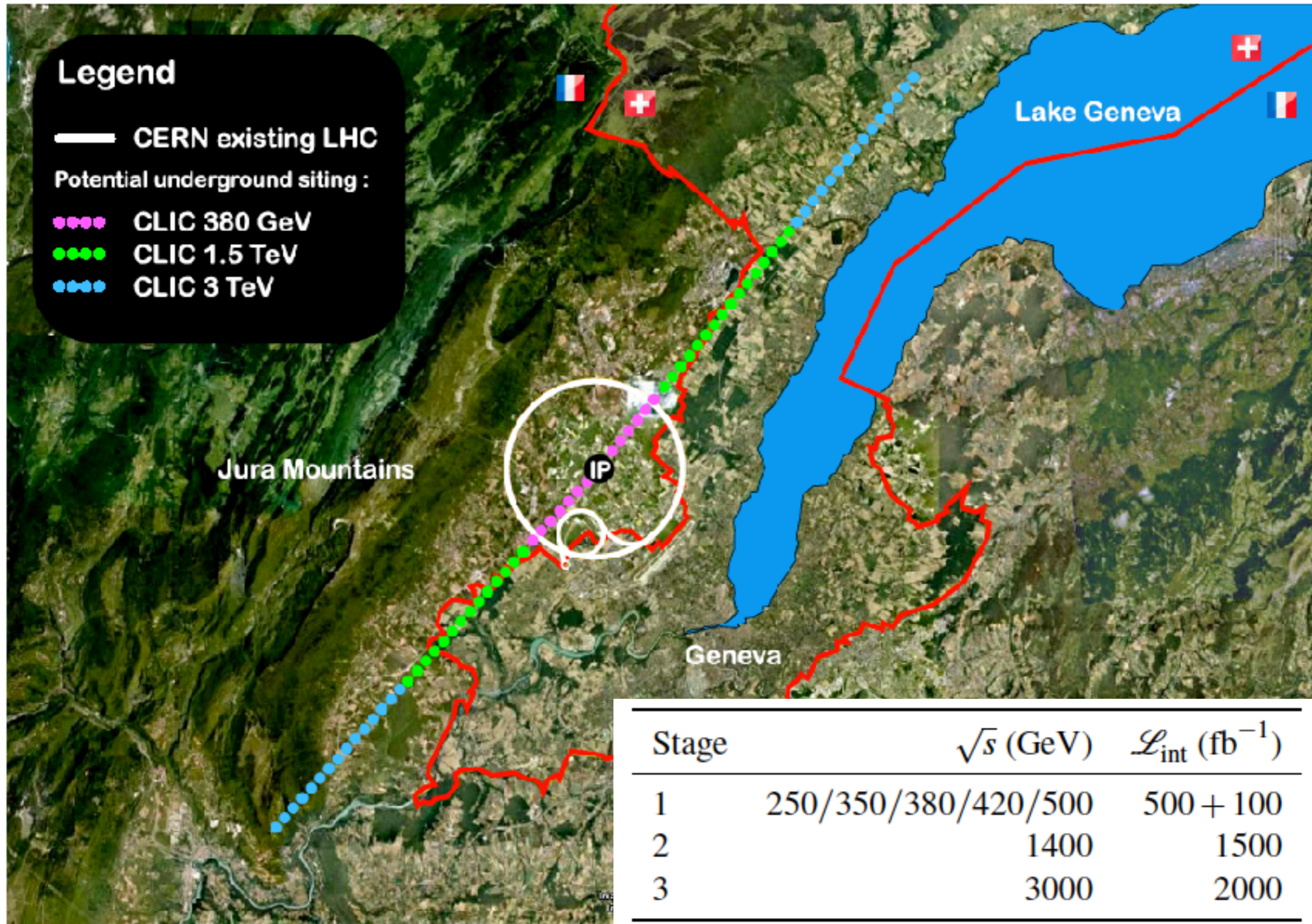
Circular Electron Positron Collider



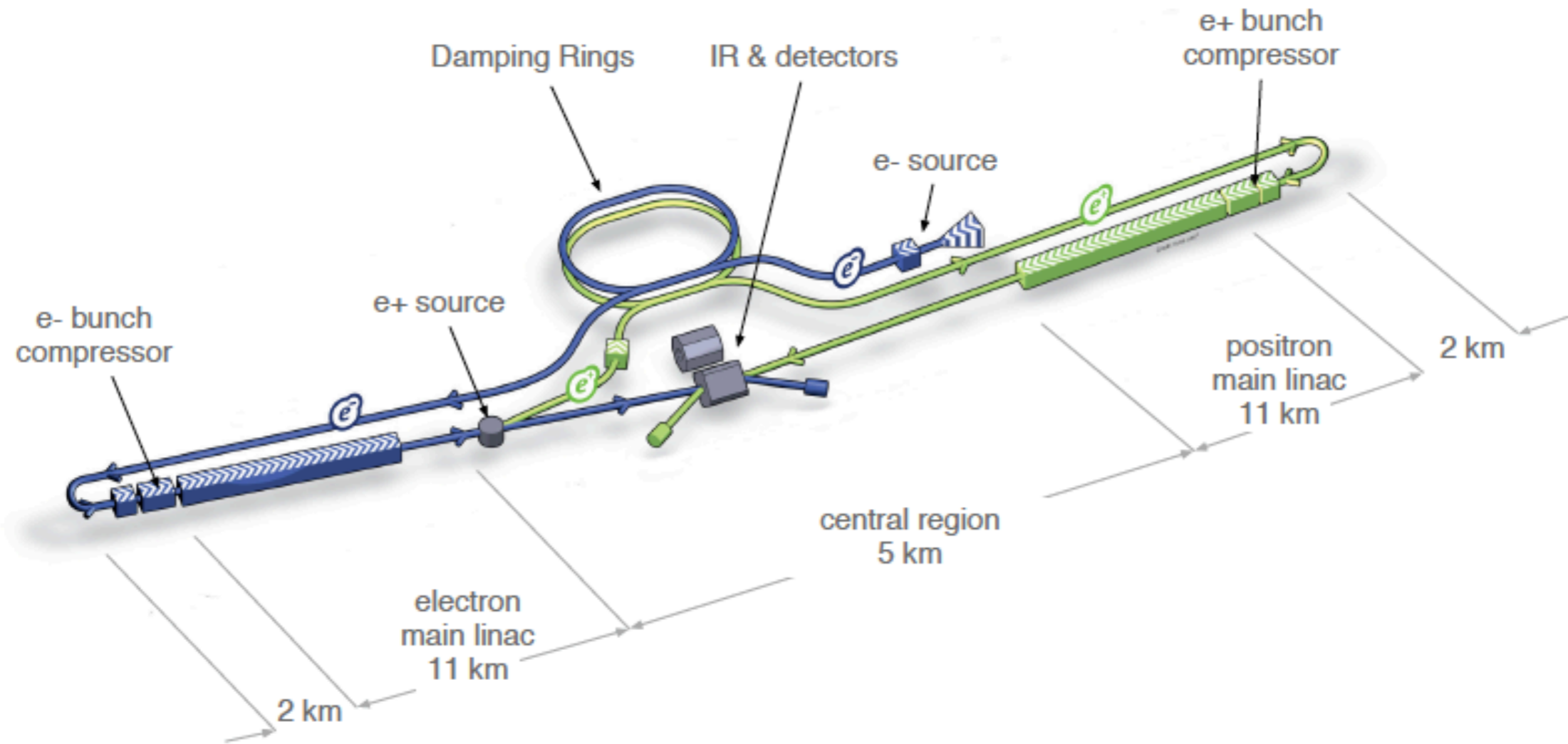
 Compact Linear Collider

International Linear Collider

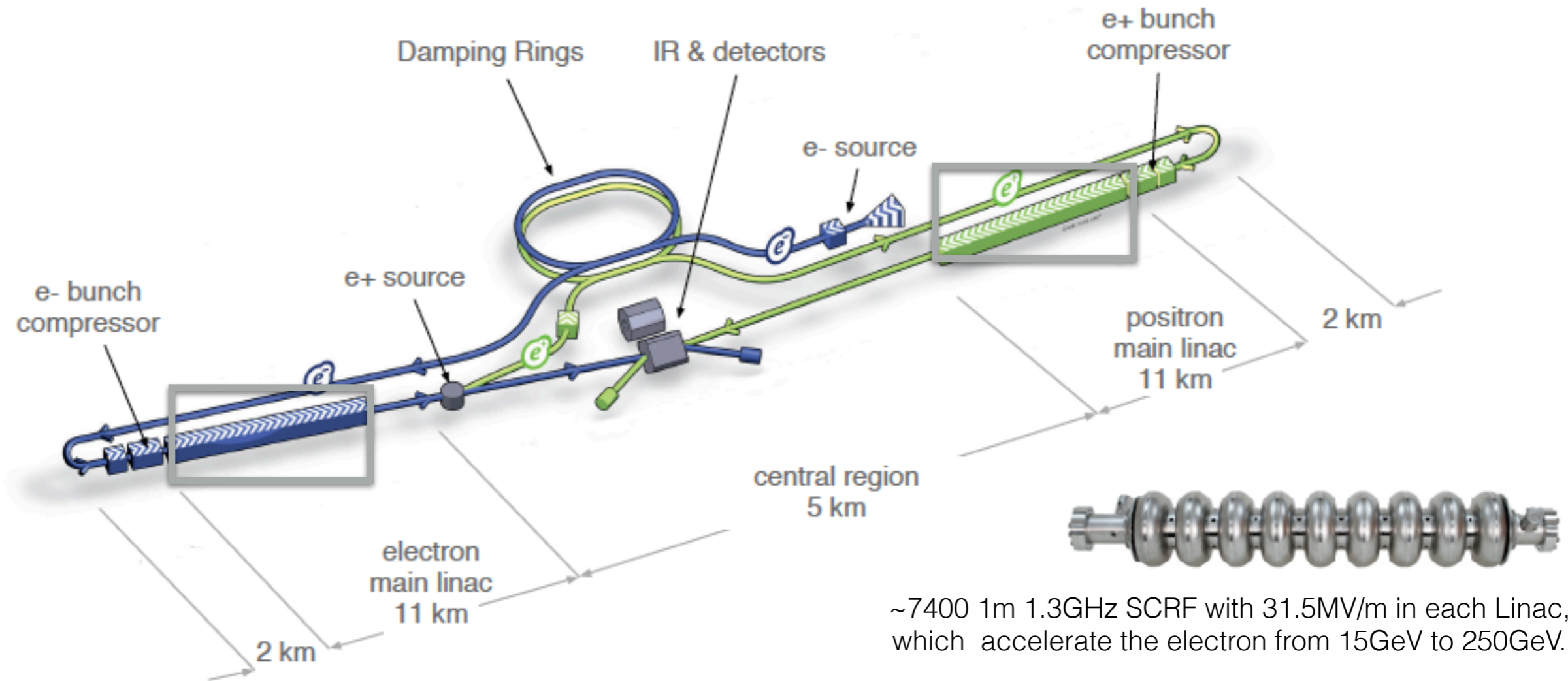
The Linear Colliders



The Linear Colliders

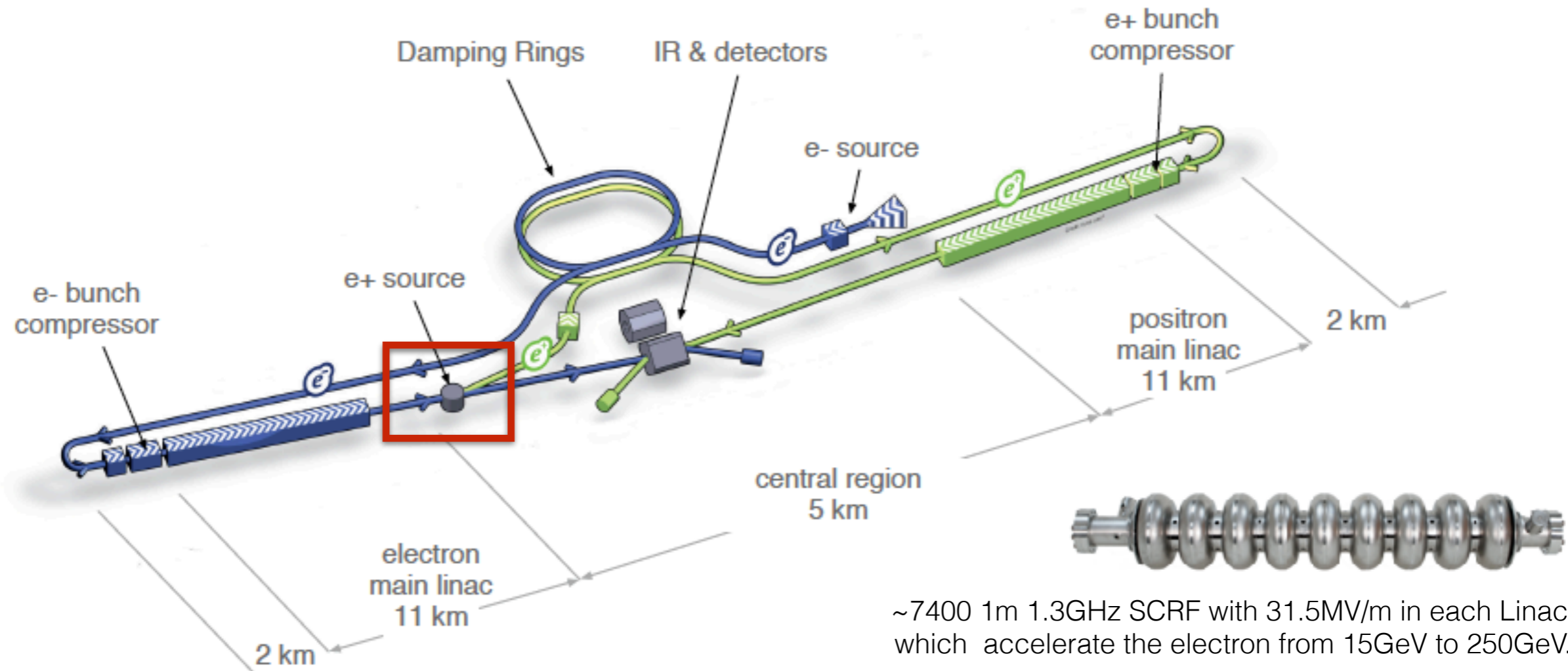


The Linear Colliders

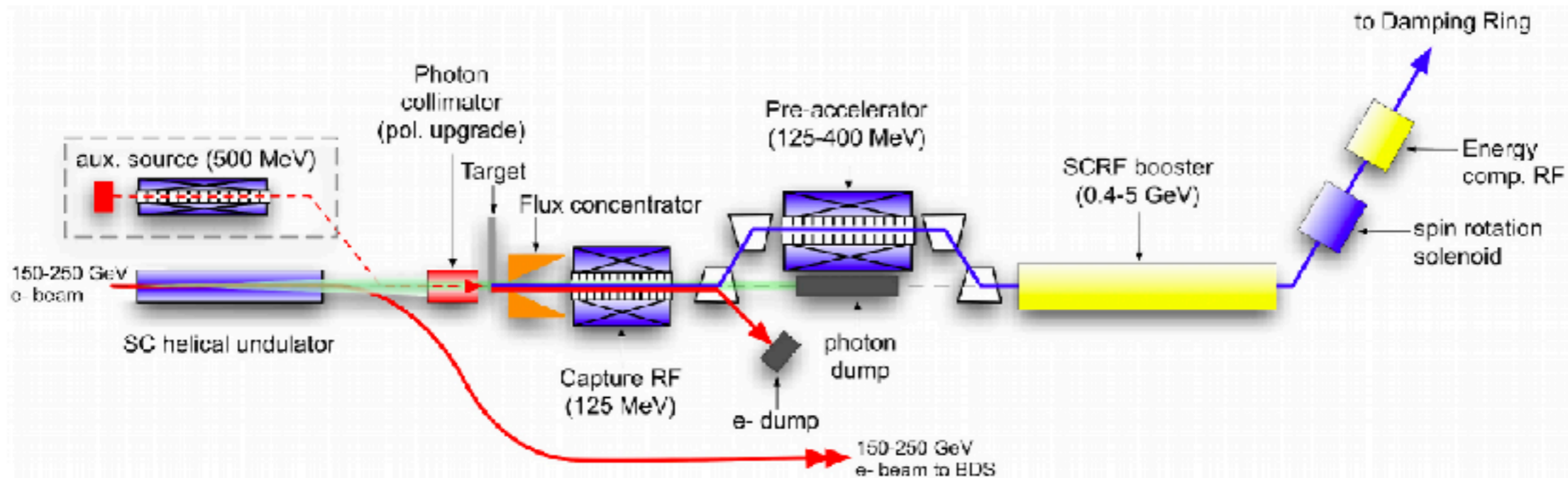


~7400 1m 1.3GHz SCRF with 31.5MV/m in each Linac, which accelerate the electron from 15GeV to 250GeV.

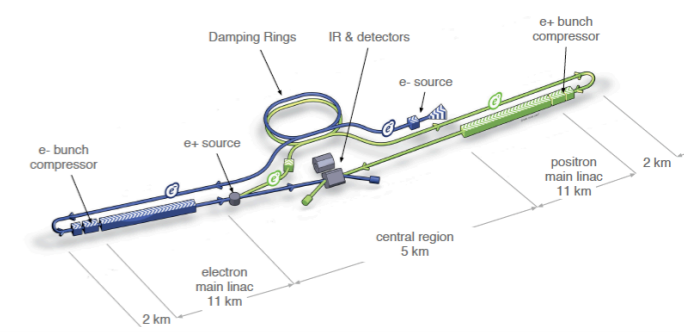
The Linear Colliders



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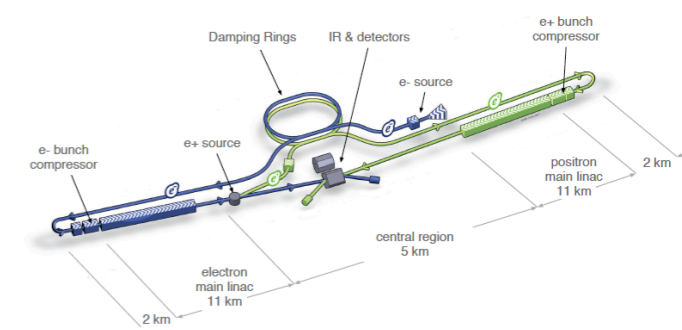
The Linear Colliders



			Baseline 500 GeV Machine			1st Stage	L Upgrade	E_{CM} Upgrade	
			250	350	500	250	500	A	B
Centre-of-mass energy	E_{CM}	GeV	250	350	500	250	500	1000	1000
Collision rate	f_{rep}	Hz	5	5	5	5	5	4	4
Electron linac rate	f_{linac}	Hz	10	5	5	10	5	4	4
Number of bunches	n_b		1312	1312	1312	1312	2625	2450	2450
Bunch population	N	$\times 10^{10}$	2.0	2.0	2.0	2.0	2.0	1.74	1.74
Bunch separation	Δt_b	ns	554	554	554	554	366	366	366
Pulse current	I_{beam}	mA	5.8	5.8	5.8	5.8	8.8	7.6	7.6
Main linac average gradient	G_a	MV m ⁻¹	14.7	21.4	31.5	31.5	31.5	38.2	39.2
Average total beam power	P_{beam}	MW	5.9	7.3	10.5	5.9	21.0	27.2	27.2
Estimated AC power	P_{AC}	MW	122	121	163	129	204	300	300
RMS bunch length	σ_z	mm	0.3	0.3	0.3	0.3	0.3	0.250	0.225
Electron RMS energy spread	$\Delta p/p$	%	0.190	0.158	0.124	0.190	0.124	0.083	0.085
Positron RMS energy spread	$\Delta p/p$	%	0.152	0.100	0.070	0.152	0.070	0.043	0.047
Electron polarisation	P_-	%	80	80	80	80	80	80	80
Positron polarisation	P_+	%	30	30	30	30	30	20	20
Horizontal emittance	$\gamma\epsilon_x$	μm	10	10	10	10	10	10	10
Vertical emittance	$\gamma\epsilon_y$	nm	35	35	35	35	35	30	30
IP horizontal beta function	β_x^*	mm	13.0	16.0	11.0	13.0	11.0	22.6	11.0
IP vertical beta function	β_y^*	mm	0.41	0.34	0.48	0.41	0.48	0.25	0.23
IP RMS horizontal beam size	σ_x^*	nm	729.0	683.5	474	729	474	481	335
IP RMS vertical beam size	σ_y^*	nm	7.7	5.9	5.9	7.7	5.9	2.8	2.7
Luminosity	L	$\times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$	0.75	1.0	1.8	0.75	3.6	3.6	4.9
Fraction of luminosity in top 1%	$L_{0.01}/L$		87.1%	77.4%	58.3%	87.1%	58.3%	59.2%	44.5%
Average energy loss	δ_{BS}		0.97%	1.9%	4.5%	0.97%	4.5%	5.6%	10.5%
Number of pairs per bunch crossing	N_{pairs}	$\times 10^3$	62.4	93.6	139.0	62.4	139.0	200.5	382.6
Total pair energy per bunch crossing	E_{pairs}	TeV	46.5	115.0	344.1	46.5	344.1	1338.0	3441.0



The Linear Colliders

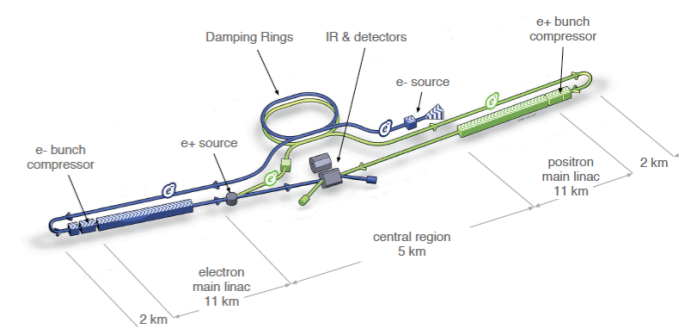


C.M energy: 250GeV, 350GeV, 500GeV, 1TeV

Centre-of-mass energy	E_{CM}	GeV	Baseline 500 GeV Machine			1st Stage	L Upgrade	E_{CM} Upgrade	
			250	350	500	250	500	A 1000	B 1000
Collision rate								4	4
Electron linac rate								4	4
Number of bunches								2450	2450
Bunch population	N_b	$\times 10^8$	2.0	2.0	2.0	2.0	2.0	1.74	1.74
Bunch separation	Δt_b	ns	554	554	554	554	366	366	366
Pulse current	I_{beam}	mA	5.8	5.8	5.8	5.8	8.8	7.6	7.6
Main linac average gradient	G_a	MV m ⁻¹	14.7	21.4	31.5	31.5	31.5	38.2	39.2
Average total beam power	P_{beam}	MW	5.9	7.3	10.5	5.9	21.0	27.2	27.2
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RMS bunch length	σ_z	mm	0.3	0.3	0.3	0.3	0.3	0.250	0.225
Electron RMS energy spread	$\Delta p/p$	%	0.190	0.158	0.124	0.190	0.124	0.083	0.085
Positron RMS energy spread	$\Delta p/p$	%	0.152	0.100	0.070	0.152	0.070	0.043	0.047
Electron polarisation	P_-	%	80	80	80	80	80	80	80
Positron polarisation	P_+	%	30	30	30	30	30	20	20
Horizontal emittance	$\gamma\epsilon_x$	μm	10	10	10	10	10	10	10
Vertical emittance	$\gamma\epsilon_y$	nm	35	35	35	35	35	30	30
IP horizontal beta function	β_x^*	mm	13.0	16.0	11.0	13.0	11.0	22.6	11.0
IP vertical beta function	β_y^*	mm	0.41	0.34	0.48	0.41	0.48	0.25	0.23
IP RMS horizontal beam size	σ_x^*	nm	729.0	683.5	474	729	474	481	335
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Number of pairs per bunch crossing	N_{pairs}	$\times 10^3$	62.4	93.6	139.0	62.4	139.0	200.5	382.6
Total pair energy per bunch crossing	E_{pairs}	TeV	46.5	115.0	344.1	46.5	344.1	1338.0	3441.0



The Linear Colliders



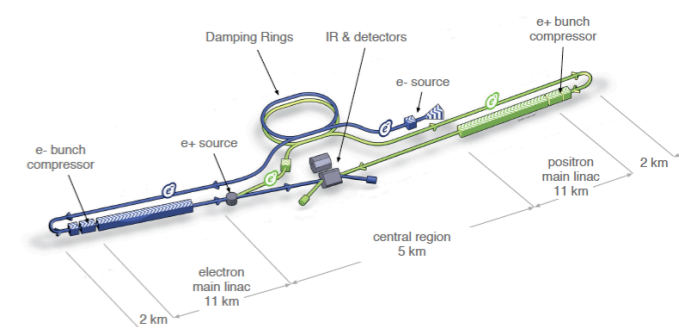
C.M energy: 250GeV, 350GeV, 500GeV, 1TeV

Electron polarization: 80%
Positron polarization: 30%

Centre-of-mass energy	E_{CM}	GeV	Baseline 500 GeV Machine			1st Stage	L Upgrade	E_{CM} Upgrade	
			250	350	500	250	500	A	B
Collision rate								4	4
Electron linac rate								4	4
Number of bunches								2450	2450
Bunch population	N_b	$\times 10^9$	2.0	2.0	2.0	2.0	2.0	1.74	1.74
Bunch separation	Δt_b	ns	554	554	554	554	366	366	366
Pulse current	I_{beam}	mA	5.8	5.8	5.8	5.8	8.8	7.6	7.6
Main linac average gradient	G_a	MV m ⁻¹	14.7	21.4	31.5	31.5	31.5	38.2	39.2
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Electron RMS energy spread	$\Delta p/p$	%	0.190	0.158					
Positron RMS energy spread	$\Delta p/p$	%	0.152	0.100					
Electron polarisation	P_-	%	80	80					
Positron polarisation	P_+	%	30	30					
Horizontal emittance	$\gamma\epsilon_x$	μm	10	10	10	10	10	10	10
Vertical emittance	$\gamma\epsilon_y$	nm	35	35	35	35	35	30	30
IP horizontal beta function	β_x^*	mm	13.0	16.0	11.0	13.0	11.0	22.6	11.0
IP vertical beta function	β_y^*	mm	0.41	0.34	0.48	0.41	0.48	0.25	0.23
IP RMS horizontal beam size	σ_x^*	nm	729.0	683.5	474	729	474	481	335
IP RMS vertical beam size	σ_y^*	nm	7.7	5.9	5.9	7.7	5.9	2.8	2.7
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Total pair energy per bunch crossing	E_{pairs}	TeV	46.5	115.0	344.1	46.5	344.1	1338.0	3441.0



The Linear Colliders



C.M energy: 250GeV, 350GeV, 500GeV, 1TeV

Electron polarization: 80%
Positron polarization: 30%

Luminosity:
 $0.75 \times 10^{34} \text{cm}^{-2}\text{s}^{-1}$ at 250GeV;
 $1.0 \times 10^{34} \text{cm}^{-2}\text{s}^{-1}$ at 350GeV;
 $1.8 \times 10^{34} \text{cm}^{-2}\text{s}^{-1}$ at 500GeV;

	E_{CM}	GeV	Baseline 500 GeV Machine			1st Stage	L Upgrade	E_{CM} Upgrade	
			250	350	500	250	500	A	B
Centre-of-mass energy			250	350	500	250	500	1000	1000
Collision rate								4	4
Electron linac rate								4	4
Number of bunches								2450	2450
Bunch population	N_b	$\times 10^9$	2.0	2.0	2.0	2.0	2.0	1.74	1.74
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RMS bunch length	σ_z	mm	0.3	0.3					
Electron RMS energy spread	$\Delta p/p$	%	0.190	0.158					
Positron RMS energy spread	$\Delta p/p$	%	0.152	0.100					
Electron polarisation	P_-	%	80	80					
Positron polarisation	P_+	%	30	30					
H ₀			10	10	10	10	10	10	10
V ₀			35	35	35	35	35	30	30
IP ₀			13.0	16.0	11.0	13.0	11.0	22.6	11.0
IP ₁			0.41	0.34	0.48	0.41	0.48	0.25	0.23
IP ₂			729.0	683.5	474	729	474	481	335
IP ₃			7.7	5.9	5.9	7.7	5.9	2.8	2.7
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Total pair energy per bunch crossing	E_{pairs}	TeV	46.5	115.0	344.1	46.5	344.1	1338.0	3441.0

$$10^{34} \text{cm}^{-2}\text{s}^{-1} = 10^{34} \times \frac{10^{-39} \text{cm}^2}{1 \text{fb}} \times \frac{365.25 \times 24 \times 60 \times 60 \text{s}}{1 \text{y}} = 315.6 \text{fb}^{-1} \text{y}^{-1}$$



The Linear Colliders

- The C.M. energy can be large.
- The luminosity increases when the C.M. energy increases.
 - The undulator-based positron source must have an electron-beam energy of at least 150 GeV to produce the requisite positron intensity;
 - The beam divergence at the interaction point is constrained by the allowable synchrotron radiation fan generated by the final doublet.
- The initial state electron and positron can be polarized.
- Typical energy is from 250GeV to several TeV.

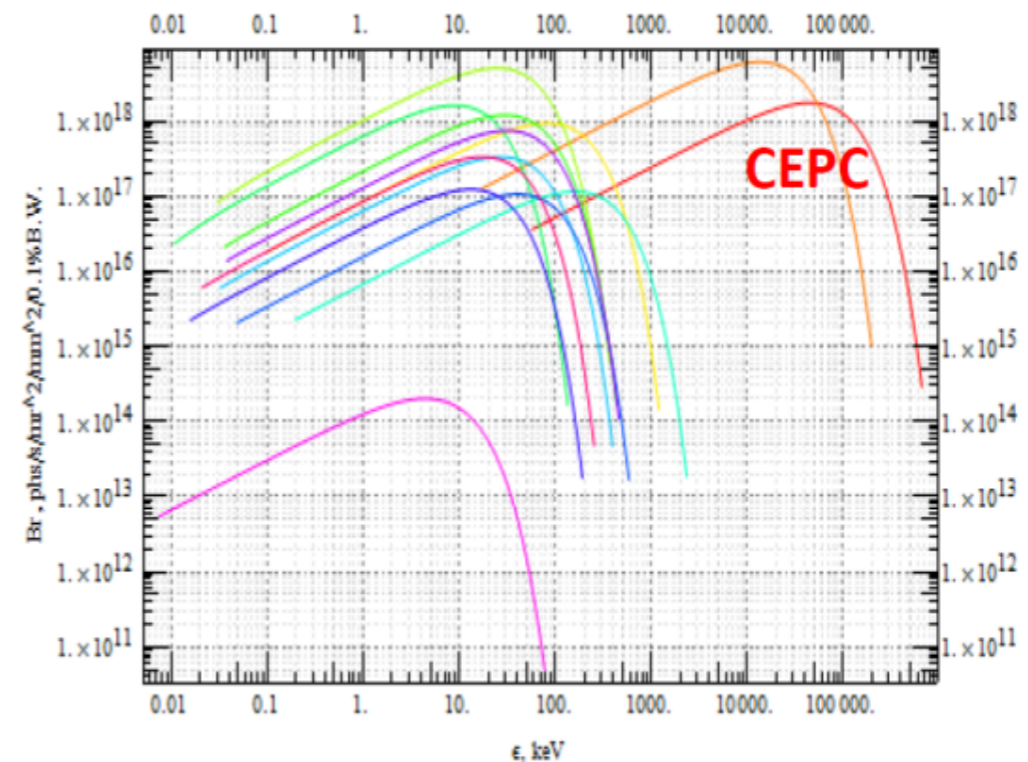
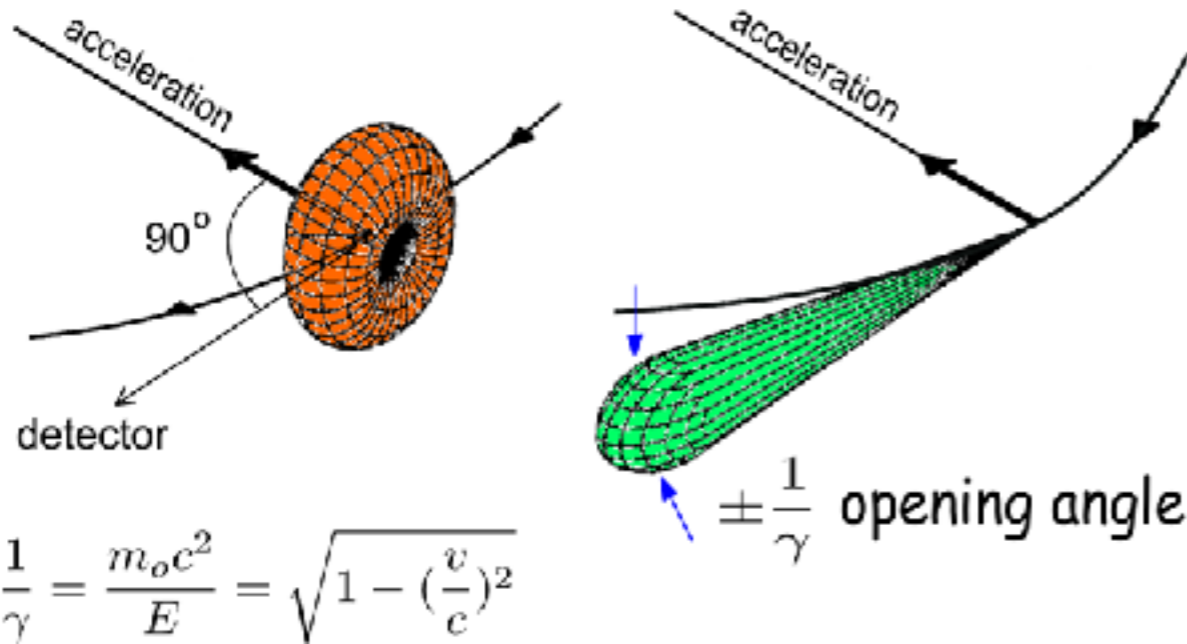


The Circular Colliders

- Classical electrodynamics: synchrotron radiation.

$$P = \frac{e^2 c \beta^4 \gamma^4}{6\pi\epsilon_0 \rho^2}$$

$$= \frac{\pi e^2 c E_{c.m.}^4}{24\epsilon_0 m^4 L^2} = \frac{e^4 E_{c.m.}^2 B^2}{24\pi\epsilon_0 c^5 m^4}$$



The Circular Colliders

- Classical electrodynamics: synchrotron radiation.

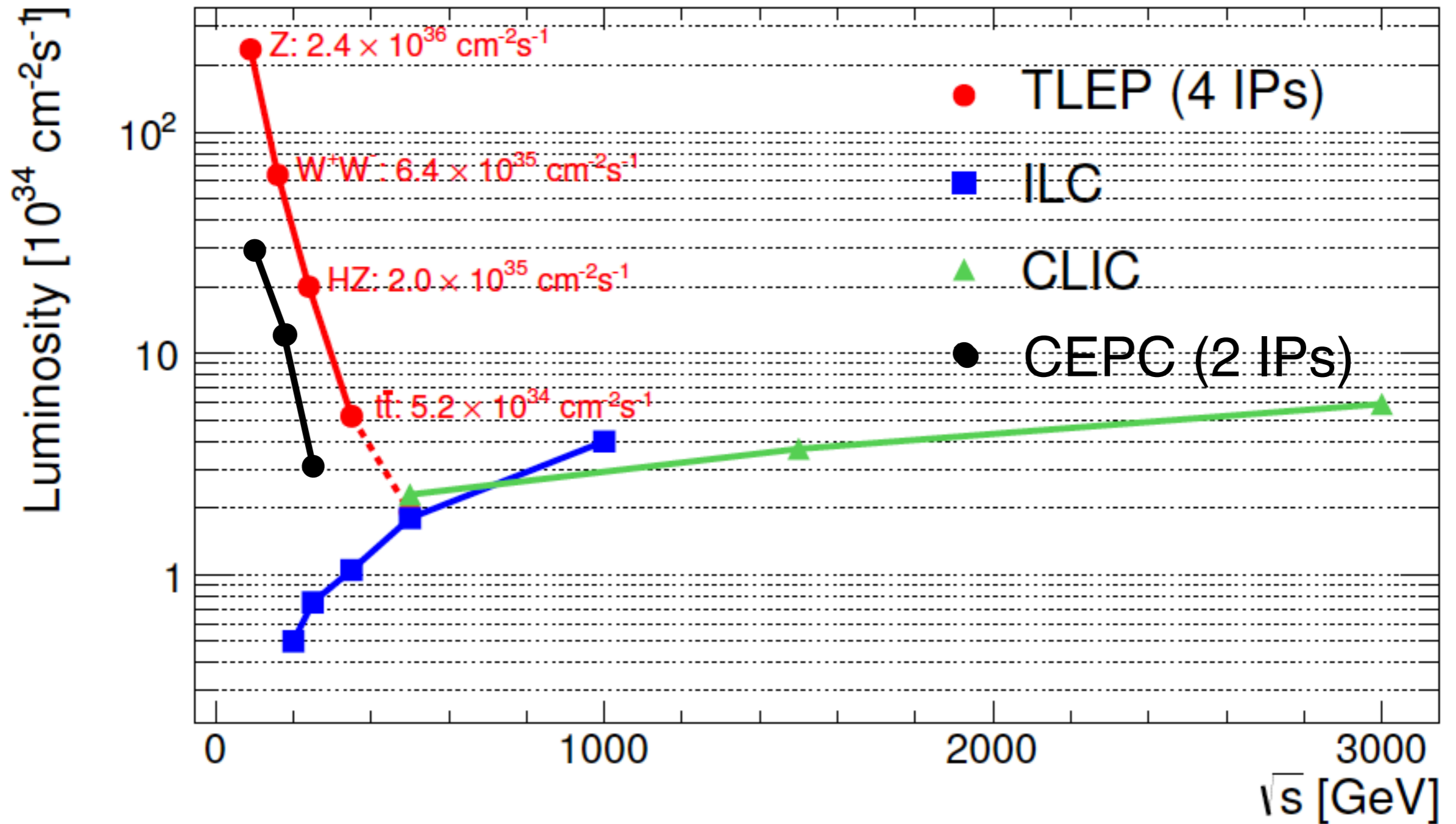
$$\begin{aligned} P &= \frac{e^2 c}{6\pi\epsilon_0} \frac{\beta^4 \gamma^4}{\rho^2} \\ &= \frac{\pi e^2 c}{24\epsilon_0} \frac{E_{c.m.}^4}{m^4 L^2} = \frac{e^4}{24\pi\epsilon_0 c^5} \frac{E_{c.m.}^2 B^2}{m^4} \end{aligned}$$

- For lower E_{cm} , the RadioFrequency cavities' power can use to accelerate much more electron and positron.

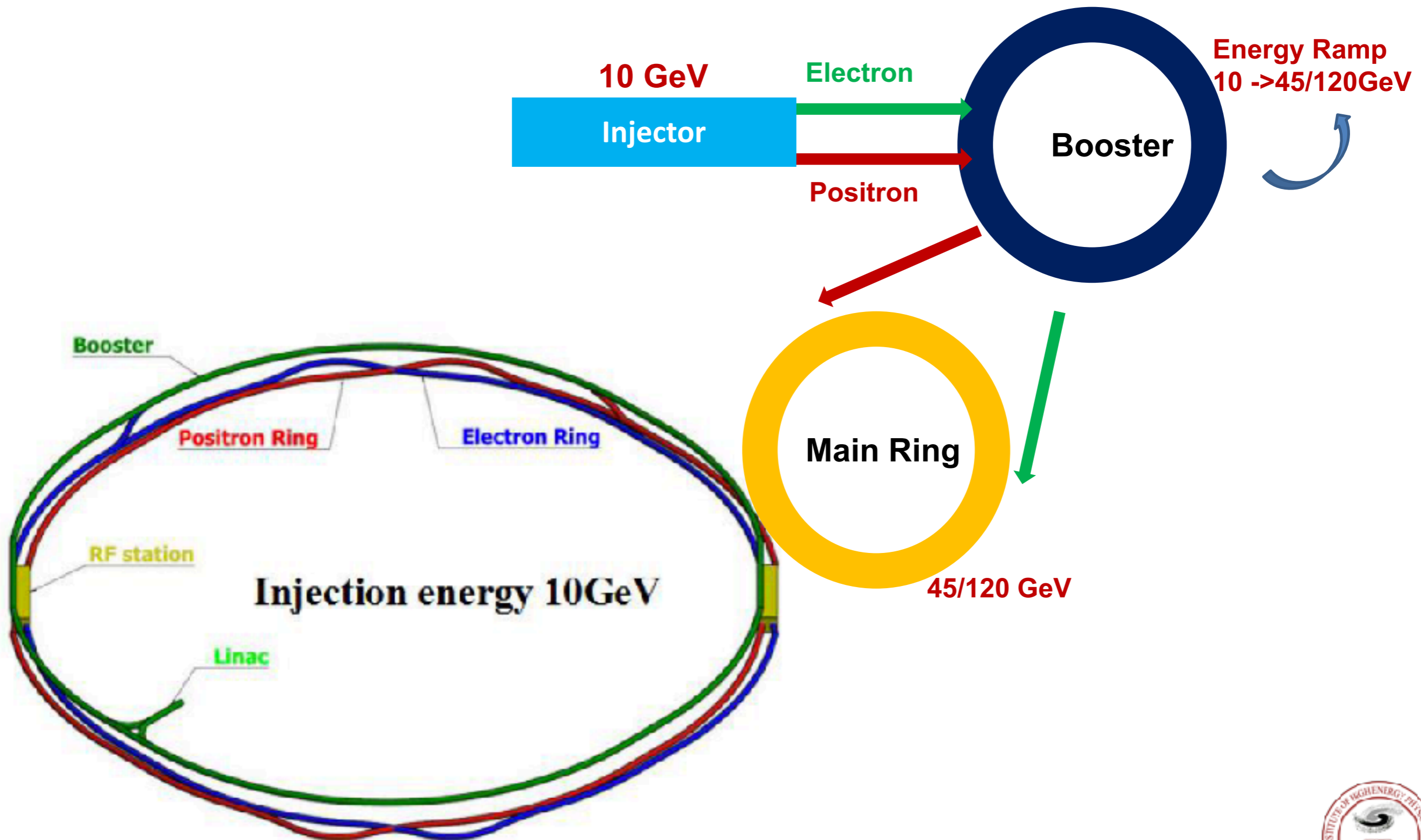
$$\mathcal{L} \sim \frac{1}{E_{c.m.}^3}$$



The Circular Colliders



The Circular Colliders



Next Lecture

- A review of the SM Higgs physics.
- Higgs physics at future lepton colliders and the phenomenology.

