Collider Physics — From basic knowledge to new physics searches

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Contents: Lecture I: Basics of Collider physics Lecture II: Physics at an e^+e^- Collider Lecture III: Physics at Hadron Colliders

(plus remarks on new physics searches)

June 3, 2015: Run-II started at $E_{cm} = 6.5 \oplus 6.5 = 13$ TeV. New era in science begun!

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The completion of the Standard Model: With the discovery of the Higgs boson, for the first time ever, we have a consistent relativistic quantum-mechanical theory, weakly coupled, unitary, renormalizable, vacuum (quasi?) stable, valid up to an exponentially high scale! Question: Where IS the next scale? $O(1 \text{ TeV})? M_{GUT}? M_{Planck}?$





Large hierarchy: Electroweak scale $\Leftrightarrow M_{Planck}$? Conceptual.



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Consult with the other excellent lectures.

COLLISION COURSE

Particle physicists around the world are designing colliders that are much larger in size than the Large Hadron Collider at CERN, Europe's particle-physics laboratory.



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- FCC_{hh}/SPPC/VLHC (100 TeV, 3 ab^{-1}) to the energy frontier: 2040?

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$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2}{4E^2 \sin^4 \theta/2} \left(\frac{F_1(x,Q^2)}{m_p} \sin^2 \frac{\theta}{2} + \frac{F_2(x,Q^2)}{E-E'} \cos^2 \frac{\theta}{2} \right)$$

QCD parton model $\Rightarrow 2xF_1(x,Q^2) = F_2(x,Q^2) = \sum_i xf_i(x)e_i^2.$

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Rutherford's legendary method continues to date!

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1. The energy:



$$s \equiv (p_1 + p_2)^2 = \begin{cases} (E_1 + E_2)^2 - (\vec{p}_1 + \vec{p}_2)^2, \\ m_1^2 + m_2^2 + 2(E_1 E_2 - \vec{p}_1 \cdot \vec{p}_2). \end{cases}$$

 $E_{cm} \equiv \sqrt{s} \approx \begin{cases} 2E_1 \approx 2E_2 & \text{in the c.m. frame } \vec{p_1} + \vec{p_2} = 0, \\ \sqrt{2E_1m_2} & \text{in the fixed target frame } \vec{p_2} = 0. \end{cases}$

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(a some beam transverse profile) in units of #particles/cm²/s $\Rightarrow 10^{33} \text{ cm}^{-2}\text{s}^{-1} = 1 \text{ nb}^{-1} \text{ s}^{-1} \approx 10 \text{ fb}^{-1}/\text{year}.$

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Current and future high-energy colliders:

Hadron	\sqrt{s}	\mathcal{L}	$\delta E/E$	f	#/bunch	L
Colliders	(TeV)	$(cm^{-2}s^{-1})$		(MHz)	(10^{10})	(km)
LHC Run (I) II	(7,8) 13	$(10^{32}) \ 10^{33}$	0.01%	40	10.5	26.66
HL-LHC	14	$7 imes 10^{34}$	0.013%	40	22	26.66
FCC_{hh} (SppC)	100	$1.2 imes10^{35}$	0.01%	40	10	100

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	e^+e^-		\sqrt{s}	\mathcal{L}	δ	$\delta E/E$		f	р	olar.	L	L	
	Colliders		(TeV)	$(cm^{-2}s^{-1})$			(N	1Hz)		(k		n)	
	ILC		0.5-1	$2.5 imes 10^{34}$	(D.1%	3		80),60% 14 -		- 33	
	CEPC	EPC 0.25-0.35		2×10^{34}	0	.13%					50-3	100	
	CLIC		3–5	$\sim 10^{35}$	0	.35%	1!	500	80	,60%	33 -	- 53	

(B). e^+e^- Colliders

The collisions between e^- and e^+ have major advantages:

- The system of an electron and a positron has zero charge, zero lepton number etc.,
- \implies it is suitable to create new particles after e^+e^- annihilation.
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- With well-understood beam properties,
- \implies the scattering kinematics is well-constrained.
- Backgrounds low and well-undercontrol:

For $\sigma \approx 10 \text{ pb} \Rightarrow 0.1 \text{ Hz at } 10^{34} \text{ cm}^{-2}\text{s}^{-1}$.

Linear Collider: possible to achieve high degrees of beam polarizations,
⇒ chiral couplings and other asymmetries can be effectively explored.

Disadvantages

• Large synchrotron radiation due to acceleration,

$$\Delta E \sim \frac{1}{R} \left(\frac{E}{m_e}\right)^4.$$

Thus, a multi-hundred GeV e^+e^- collider will have to be made a linear accelerator.

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CEPC/FCC_{ee} Higgs Factory

It has been discussed to build a circular e^+e^- collider $E_{cm} = 245 \text{ GeV}-350 \text{ GeV}$ with multiple interaction points for very high luminosities.

(C). Hadron Colliders LHC: the new high-energy frontier



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• Higher c.m. energy, thus higher energy threshold: $\sqrt{S} = 14 \text{ TeV}: \quad M_{new}^2 \sim s = x_1 x_2 S \Rightarrow M_{new} \sim 0.3 \sqrt{S} \sim 4 \text{ TeV}.$ • Higher luminosity: $10^{34}/\text{cm}^2/\text{s} \Rightarrow 100 \text{ fb}^{-1}/\text{yr}$. Annual yield: 1B W^{\pm} ; 100M $t\bar{t}$; 10M W^+W^- ; 1M H^0 ...

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- Multiple (strong, electroweak) channels:

 $q\bar{q}', gg, qg, b\bar{b} \rightarrow \text{colored}; Q = 0, \pm 1; J = 0, 1, 2 \text{ states};$ WW, WZ, ZZ, $\gamma\gamma \rightarrow I_W = 0, 1, 2; Q = 0, \pm 1, \pm 2; J = 0, 1, 2 \text{ states}.$

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• Initial state unknown:

colliding partons unknown on event-by-event basis; parton c.m. energy unknown: $E_{cm}^2 \equiv s = x_1 x_2 S$; parton c.m. frame unknown.

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Our primary job !

(D). Particle Detection:

The detector complex:

Utilize the strong and electromagnetic interactions between detector materials and produced particles.



For a relativistic particle, the travel distance:

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- short-lived not "directly seen", but "reconstructable": $\pi^0, \rho^{0,\pm}, \dots, Z, W^{\pm}, t, H...$
- missing particles are weakly-interacting and neutral:

 $\nu, \ \tilde{\chi}^0, G_{KK}...$

† For stable and quasi-stable particles of a life-time $\tau \ge 10^{-10} - 10^{-12}$ s, they show up as







Theorists should know:

For charged tracks : $\Delta p/p \propto p$, typical resolution : $\sim p/(10^4 \text{ GeV})$. For calorimetry : $\Delta E/E \propto \frac{1}{\sqrt{E}}$, typical resolution : $\sim (10\%_{ecal}, 50\%_{hcal})/\sqrt{E/\text{GeV}}$

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Typical resolution: $d_0 \sim 30 - 50 \ \mu m$ or so

 \Rightarrow Better have two (non-collinear) charged tracks for a secondary vertex;

Or use the "impact parameter" w.r.t. the primary vertex.

For theorists: just multiply a "tagging efficiency":

 $\epsilon_b \sim 70\%; \quad \epsilon_c \sim 40\%; \quad \epsilon_\tau \sim 40\%.$

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But in hadron collisions, the longitudinal momenta unknown, thus transverse direction only:

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often called "missing p_T " (p_T) or (conventionally) "missing E_T " (E_T).

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Note: "missing E_T " (MET) is *conceptually* ill-defined! It is only sensible for massless particles: $\not\!\!\!E_T = \sqrt{\vec{p}_{miss}^2 + m^2}$. What we "see" for the SM particles: no universality!

What we "see" for the SM particles: no universality! How to search for new particles?



I-B. Basic Techniques

and Tools for Collider Physics

(A). Scattering cross section

For a $2 \rightarrow n$ scattering process:

$$\sigma(ab \to 1 + 2 + ...n) = \frac{1}{2s} \overline{\sum} |\mathcal{M}|^2 dPS_n,$$

$$dPS_n \equiv (2\pi)^4 \,\delta^4 \left(P - \sum_{i=1}^n p_i \right) \prod_{i=1}^n \frac{1}{(2\pi)^3} \frac{d^3 \vec{p_i}}{2E_i},$$

$$s = (p_a + p_b)^2 \equiv P^2 = \left(\sum_{i=1}^n p_i\right)^2,$$

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where $\overline{\sum}|\mathcal{M}|^2$: dynamics (dimension 4 - 2n); dPS_n : kinematics (Lorentz invariant, dimension 2n - 4.) For a $1 \rightarrow n$ decay process, the partial width in the rest frame:

$$\Gamma(a \to 1 + 2 + \dots n) = \frac{1}{2M_a} \overline{\sum} |\mathcal{M}|^2 dPS_n.$$

$$\tau = \Gamma_{tot}^{-1} = (\sum_f \Gamma_f)^{-1}.$$

(B). Phase space and kinematics * One-particle Final State $a + b \rightarrow 1$:

$$dPS_1 \equiv (2\pi) \frac{d^3 \vec{p_1}}{2E_1} \delta^4 (P - p_1)$$

$$\doteq \pi |\vec{p_1}| d\Omega_1 \delta^3 (\vec{P} - \vec{p_1})$$

$$\doteq 2\pi \ \delta(s - m_1^2).$$

where the first and second equal signs made use of the identities:

$$|\vec{p}|d|\vec{p}| = EdE, \quad \frac{d^3\vec{p}}{2E} = \int d^4p \ \delta(p^2 - m^2).$$

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The "dimensinless phase-space volume" is $s(dPS_1) = 2\pi$.

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Two-particle Final State $a + b \rightarrow 1 + 2$:

$$dPS_{2} \equiv \frac{1}{(2\pi)^{2}} \delta^{4} (P - p_{1} - p_{2}) \frac{d^{3}\vec{p}_{1}}{2E_{1}} \frac{d^{3}\vec{p}_{2}}{2E_{2}}$$

$$\doteq \frac{1}{(4\pi)^{2}} \frac{|\vec{p}_{1}^{cm}|}{\sqrt{s}} d\Omega_{1} = \frac{1}{(4\pi)^{2}} \frac{|\vec{p}_{1}^{cm}|}{\sqrt{s}} d\cos\theta_{1} d\phi_{1}$$

$$= \frac{1}{4\pi} \frac{1}{2} \lambda^{1/2} \left(1, \frac{m_{1}^{2}}{s}, \frac{m_{2}^{2}}{s}\right) dx_{1} dx_{2},$$

$$d\cos\theta_{1} = 2dx_{1}, \quad d\phi_{1} = 2\pi dx_{2}, \quad 0 \le x_{1,2} \le 1,$$

Two-particle Final State $a + b \rightarrow 1 + 2$:

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The magnitudes of the energy-momentum of the two particles are fully determined by the four-momentum conservation:

$$|\vec{p}_1^{cm}| = |\vec{p}_2^{cm}| = \frac{\lambda^{1/2}(s, m_1^2, m_2^2)}{2\sqrt{s}}, \ E_1^{cm} = \frac{s + m_1^2 - m_2^2}{2\sqrt{s}}, \ E_2^{cm} = \frac{s + m_2^2 - m_1^2}{2\sqrt{s}},$$
$$\lambda(x, y, z) = (x - y - z)^2 - 4yz = x^2 + y^2 + z^2 - 2xy - 2xz - 2yz.$$

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The phase-space volume of the two-body is scaled down with respect to that of the one-particle by a factor

$$\frac{dPS_2}{s \ dPS_1} \approx \frac{1}{(4\pi)^2}.$$

just like a "loop factor".

Consider a 2 \rightarrow 2 scattering process $p_a + p_b \rightarrow p_1 + p_2$,



the (Lorentz invariant) Mandelstam variables are defined as

$$s = (p_a + p_b)^2 = (p_1 + p_2)^2 = E_{cm}^2,$$

$$t = (p_a - p_1)^2 = (p_b - p_2)^2 = m_a^2 + m_1^2 - 2(E_a E_1 - p_a p_1 \cos \theta_{a1}),$$

$$u = (p_a - p_2)^2 = (p_b - p_1)^2 = m_a^2 + m_2^2 - 2(E_a E_2 - p_a p_2 \cos \theta_{a2}),$$

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$$s + t + u = m_a^2 + m_b^2 + m_1^2 + m_2^2.$$

The two-body phase space can be thus written as

$$dPS_2 = \frac{1}{(4\pi)^2} \frac{dt \ d\phi_1}{s \ \lambda^{1/2} \left(1, m_a^2/s, m_b^2/s\right)}.$$

Three-particle Final State $a + b \rightarrow 1 + 2 + 3$:

$$dPS_3 \equiv \frac{1}{(2\pi)^5} \,\delta^4 \,(P - p_1 - p_2 - p_3) \frac{d^3 \vec{p}_1}{2E_1} \frac{d^3 \vec{p}_2}{2E_2} \frac{d^3 \vec{p}_3}{2E_3}$$

$$\doteq \frac{|\vec{p}_1|^2 \, d|\vec{p}_1| \, d\Omega_1}{(2\pi)^3 \, 2E_1} \, \frac{1}{(4\pi)^2} \, \frac{|\vec{p}_2^{(23)}|}{m_{23}} \, d\Omega_2$$

$$= \frac{1}{(4\pi)^3} \,\lambda^{1/2} \left(1, \frac{m_2^2}{m_{23}^2}, \frac{m_3^2}{m_{23}^2}\right) \, 2|\vec{p}_1| \, dE_1 \, dx_2 dx_3 dx_4 dx_5.$$

$$d\cos\theta_{1,2} = 2dx_{2,4}, \quad d\phi_{1,2} = 2\pi dx_{3,5}, \quad 0 \le x_{2,3,4,5} \le 1, \\ |\vec{p}_1^{cm}|^2 = |\vec{p}_2^{cm} + \vec{p}_3^{cm}|^2 = (E_1^{cm})^2 - m_1^2, \\ m_{23}^2 = s - 2\sqrt{s}E_1^{cm} + m_1^2, \quad |\vec{p}_2^{23}| = |\vec{p}_3^{23}| = \frac{\lambda^{1/2}(m_{23}^2, m_2^2, m_3^2)}{2m_{23}},$$

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$$= \frac{1}{(4\pi)^{3}} \lambda^{1/2} \left(1, \frac{m_{2}^{2}}{m_{23}^{2}}, \frac{m_{3}^{2}}{m_{23}^{2}}\right) 2|\vec{p}_{1}| dE_{1} dx_{2} dx_{3} dx_{4} dx_{5}.$$

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The particle energy spectrum is not monochromatic. The maximum value (the end-point) for particle 1 in c.m. frame is

$$E_1^{max} = \frac{s + m_1^2 - (m_2 + m_3)^2}{2\sqrt{s}}, \quad m_1 \le E_1 \le E_1^{max},$$
$$|\vec{p}_1^{max}| = \frac{\lambda^{1/2}(s, m_1^2, (m_2 + m_3)^2)}{2\sqrt{s}}, \quad 0 \le p_1 \le p_1^{max}.$$

With $m_i = 10, 20, 30, \sqrt{s} = 100 \text{ GeV}.$



More intuitive to work out the end-point for the kinetic energy, – recall the direct neutrino mass bound in β -decay:

$$K_1^{max} = E_1^{max} - m_1 = \frac{(\sqrt{s} - m_1 - m_2 - m_3)(\sqrt{s} - m_1 + m_2 + m_3)}{2\sqrt{s}}.$$

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For $n \to p^+ e^- \overline{\nu}_e$,

$$K_e^{max} \approx (m_n - m_p - m_e) - m_{\nu}.$$

In general, the 3-body phase space boundaries are non-trivial. That leads to the "Dalitz Plots".

One practically useful formula is: A particle of mass M decays to 3 particles $M \rightarrow abc$.

Show that the phase space element can be expressed as

$$dPS_{3} = \frac{1}{2^{7}\pi^{3}} M^{2} dx_{a} dx_{b}.$$
$$x_{i} = \frac{2E_{i}}{M}, \ (i = a, b, c, \ \sum_{i} x_{i} = 2).$$

where the integration limits for $m_a = m_b = m_c = 0$ are

$$0 \le x_a \le 1, \quad 1 - x_a \le x_b \le 1.$$

Recursion relation $P \rightarrow 1 + 2 + 3... + n$:



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$$dPS_n(P; p_1, ..., p_n) = dPS_{n-1}(P; p_1, ..., p_{n-1,n})$$
$$dPS_2(p_{n-1,n}; p_{n-1}, p_n) \frac{dm_{n-1,n}^2}{2\pi}.$$

For instance,

$$dPS_3 = dPS_2(i) \frac{dm_{prop}^2}{2\pi} dPS_2(f).$$

This is generically true, but particularly useful when the diagram has an *s*-channel particle propagation.
Breit-Wigner Resonance, the Narrow Width Approximation

An unstable particle of mass M and total width Γ_V , the propagator is

$$R(s) = \frac{1}{(s - M_V^2)^2 + \Gamma_V^2 M_V^2}.$$

the Narrow Width Approximation

$$\frac{1}{(m_*^2 - M_V^2)^2 + \Gamma_V^2 M_V^2} \approx \frac{\pi}{\Gamma_V M_V} \ \delta(m_*^2 - M_V^2).$$

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Consider a three-body decay of a top quark,

 $t \rightarrow bW^* \rightarrow b \ e\nu$. Making use of the phase space recursion relation and the narrow width approximation for the intermediate W boson, show that the partial decay width of the top quark can be expressed as (ignore spin correlations)

$$\Gamma(t \to bW^* \to b \ e\nu) \approx \Gamma(t \to bW) \cdot BR(W \to e\nu).$$

"Proof": Consider an intermediate state V^*

 $a \rightarrow bV^* \rightarrow b \ p_1p_2.$

By the reduction formula, the resonant integral reads

$$\int_{(m_*^{min})^2 = (m_a - m_b)^2}^{(m_*^{max})^2 = (m_a - m_b)^2} dm_*^2 dm_*^2$$

Variable change

$$\tan\theta = \frac{m_*^2 - M_V^2}{\Gamma_V M_V},$$

resulting in a flat integrand over $\boldsymbol{\theta}$

$$\int_{(m_*^{min})^2}^{(m_*^{max})^2} \frac{dm_*^2}{(m_*^2 - M_V^2)^2 + \Gamma_V^2 M_V^2} = \int_{\theta^{min}}^{\theta^{max}} \frac{d\theta}{\Gamma_V M_V}.$$

In the limit

$$(m_{1} + m_{2}) + \Gamma_{V} \ll M_{V} \ll m_{a} - m_{b} - \Gamma_{V},$$

$$\theta^{min} = \tan^{-1} \frac{(m_{1} + m_{2})^{2} - M_{V}^{2}}{\Gamma_{V} M_{V}} \to -\pi,$$

$$\theta^{max} = \tan^{-1} \frac{(m_{a} - m_{b})^{2} - M_{V}^{2}}{\Gamma_{V} M_{V}} \to 0,$$

then the Narrow Width Approximation

$$\frac{1}{(m_*^2 - M_V^2)^2 + \Gamma_V^2 M_V^2} \approx \frac{\pi}{\Gamma_V M_V} \,\,\delta(m_*^2 - M_V^2).$$

Properties of scattering amplitudes T(s, t, u)

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• Unitarity:

S-matrix unitarity leads to :

 $-i(T-T^{\dagger}) = TT^{\dagger}$

$$\mathcal{M}(s,t) = 16\pi \sum_{J=M}^{\infty} (2J+1)a_J(s)d_{\mu\mu'}^J(\cos\theta)$$
$$a_J(s) = \frac{1}{32\pi} \int_{-1}^1 \mathcal{M}(s,t) \ d_{\mu\mu'}^J(\cos\theta)d\cos\theta.$$

where $\mu = s_a - s_b$, $\mu' = s_1 - s_2$, $M = \max(|\mu|, |\mu'|)$.

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By Optical Theorem: $\sigma = \frac{1}{s} \text{Im} \mathcal{M}(\theta = 0) = \frac{16\pi}{s} \sum_{J=M}^{\infty} (2J+1) |a_J(s)|^2$.

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(a). partial wave unitarity: $\text{Im}(a_J) \ge |a_J|^2$, or $|\text{Re}(a_J)| \le 1/2$,



Argand diagram for partial wave unitarity

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(D). Calculational Tools



II. Physics at an e^+e^- Collider

(A.) Simple Formalism

Event rate of a reaction:

$$R(s) = \sigma(s)\mathcal{L}, \text{ for constant } \mathcal{L}$$
$$= \mathcal{L} \int d\tau \frac{dL(s,\tau)}{d\tau} \sigma(\hat{s}), \quad \tau = \frac{\hat{s}}{s}.$$

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As for the differential production cross section of two-particle a, b,

$$\frac{d\sigma(e^+e^- \to ab)}{d\cos\theta} = \frac{\beta}{32\pi s} \overline{\sum} |\mathcal{M}|^2$$

where

• $\beta = \lambda^{1/2}(1, m_a^2/s, m_b^2/s)$, is the speed factor for the out-going particles in the c.m. frame, and $p_{cm} = \beta \sqrt{s/2}$,

• $\sum |\mathcal{M}|^2$ the squared matrix element, summed and averaged over quantum numbers (like color and spins etc.)

unpolarized beams so that the azimuthal angle trivially integrated out,

Total cross sections and event rates for SM processes:



(B). Resonant production: Breit-Wigner formula

$$\frac{1}{(s - M_V^2)^2 + \Gamma_V^2 M_V^2}$$

If the energy spread $\delta\sqrt{s}\ll \Gamma_V$, the line-shape mapped out:

$$\sigma(e^+e^- \to V^* \to X) = \frac{4\pi(2j+1)\Gamma(V \to e^+e^-)\Gamma(V \to X)}{(s - M_V^2)^2 + \Gamma_V^2 M_V^2} \frac{s}{M_V^2}.$$

(physical examples?)

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(physical examples?)

If $\delta\sqrt{s} \gg \Gamma_V$, the narrow-width approximation:

$$\frac{1}{(s-M_V^2)^2 + \Gamma_V^2 M_V^2} \rightarrow \frac{\pi}{M_V \Gamma_V} \,\delta(s-M_V^2),$$

$$\sigma(e^+e^- \rightarrow V^* \rightarrow X) = \frac{2\pi^2(2j+1)\Gamma(V \rightarrow e^+e^-)BF(V \rightarrow X)}{M_V^2} \frac{dL(\hat{s}=M_V^2)}{d\sqrt{\hat{s}}}$$

(physical examples?)

Away from resonance

For an *s*-channel or a finite-angle scattering:

$$\sigma \sim \frac{1}{s}.$$

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For an *s*-channel or a finite-angle scattering:

$$\sigma \sim \frac{1}{s}.$$

For forward (co-linear) scattering:

$$\sigma \sim \frac{1}{M_V^2} \ln^2 \frac{s}{M_V^2}.$$

• The simplest reaction

$$\sigma(e^+e^- \to \gamma^* \to \mu^+\mu^-) \equiv \sigma_{pt} = \frac{4\pi\alpha^2}{3s}.$$

In fact, $\sigma_{pt} \approx 100 \text{ fb}/(\sqrt{s}/\text{TeV})^2$ has become standard units to measure the size of cross sections.

(C). Gauge boson radiation:

A qualitatively different process is initiated from gauge boson radiation, typically off fermions:



The simplest case is the photon radiation off an electron, like:

$$e^+e^- \rightarrow e^+, \ \gamma^*e^- \rightarrow e^+e^-.$$

The dominant features are due to the result of a t-channel singularity, induced by the collinear photon splitting:

$$\sigma(e^-a \to e^-X) \approx \int dx \ P_{\gamma/e}(x) \ \sigma(\gamma a \to X).$$

The so called the effective photon approximation.

For an electron of energy E, the probability of finding a collinear photon of energy xE is given by

$$P_{\gamma/e}(x) = \frac{\alpha}{2\pi} \frac{1 + (1 - x)^2}{x} \ln \frac{E^2}{m_e^2},$$

known as the Weizsäcker-Williams spectrum.

Exercise 3.3: Try to derive this splitting function.

We see that:

- m_e enters the log to regularize the collinear singularity;
- 1/x leads to the infrared behavior of the photon;
- This picture of the photon probability distribution is also valid for other photon spectrum:

Based on the back-scattering laser technique, it has been proposed to produce much harder photon spectrum, to construct a "photon collider"...

A similar picture may be envisioned for the electroweak massive gauge bosons, $V = W^{\pm}, Z$.

Consider a fermion f of energy E, the probability of finding a (nearly) collinear gauge boson V of energy xE and transverse momentum p_T (with respect to \vec{p}_f) is approximated by

$$P_{V/f}^{T}(x, p_{T}^{2}) = \frac{g_{V}^{2} + g_{A}^{2}}{8\pi^{2}} \frac{1 + (1 - x)^{2}}{x} \frac{p_{T}^{2}}{(p_{T}^{2} + (1 - x)M_{V}^{2})^{2}},$$

$$P_{V/f}^{L}(x, p_{T}^{2}) = \frac{g_{V}^{2} + g_{A}^{2}}{4\pi^{2}} \frac{1 - x}{x} \frac{(1 - x)M_{V}^{2}}{(p_{T}^{2} + (1 - x)M_{V}^{2})^{2}}.$$

Although the collinear scattering would not be a good approximation until reaching very high energies $\sqrt{s} \gg M_V$, it is instructive to consider the qualitative features.

One of the most important techniques, that distinguishes an e^+e^- collisions from hadronic collisions.

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Consider a process:

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Then:

$$p_{e^+} + p_{e^-} = p_V + p_X, \ (p_{e^+} + p_{e^-} - p_V)^2 = p_X^2, M_X^2 = (p_{e^+} + p_{e^-} - p_V)^2 = s + M_V^2 - 2\sqrt{s}E_V.$$

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One thus obtain the "model-independent" inclusive measurements

- a. mass of X by the recoil mass peak
- b. coupling of X by simple event-count at the peak



At peak cross section ≈ 200 fb with 5 ab⁻¹ $\Rightarrow 1M h^{0}!$

The key point for a Higgs factory:

Model-independent measurements on the ZZh coupling in a clean experimental environment.





III. Hadron Collider Physics

(A). New HEP frontier: the LHC The Higgs discovery and more excitements ahead ...



ATLAS (90m underground)

CMS



LHC Event rates for various SM processes:



 $\begin{array}{l} 10^{34}/\mathrm{cm}^2/\mathrm{s} \Rightarrow 100 \ \mathrm{fb}^{-1}/\mathrm{yr}.\\ & \text{Annual yield } \# \ \mathrm{of \ events} = \sigma \times L_{int}:\\ 10B \ W^{\pm}; \ 100M \ t\overline{t}; \ 10M \ W^+W^-; \ 1M \ H^0...\\ & \text{Discovery of the Higgs boson opened a new chapter of HEP!} \end{array}$

Theoretical challenges: Unprecedented energy frontier Theoretical challenges: Unprecedented energy frontier

(a) Total hadronic cross section: Non-perturbative. The order of magnitude estimate:

 $\sigma_{pp} = \pi r_{eff}^2 \approx \pi/m_\pi^2 \sim 120 \ \mathrm{mb}.$
Theoretical challenges: Unprecedented energy frontier

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Energy-dependence?

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Theoretical challenges: Unprecedented energy frontier

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- Accurate (higher orders) partonic cross sections $\hat{\sigma}_{parton}(s)$.
- Parton distribution functions to the extreme (density):

 $Q^2 \sim (a \ few \ TeV)^2, \ x \sim 10^{-3} - 10^{-6}.$

Experimental challenges:

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 ≈ 25 overlapping events/bunch crossing:



Triggering thresholds:

	ATLAS	
Objects	η	$p_T~({\sf GeV})$
μ inclusive	2.4	6 (20)
e/photon inclusive	2.5	17 (26)
Two e 's or two photons	2.5	12 (15)
1-jet inclusive	3.2	180 (290)
3 jets	3.2	75 (130)
4 jets	3.2	55 (90)
au/hadrons	2.5	43 (65)
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Jets+ $ ot\!\!\!/ E_T$	3.2, 4.9	50,50 (100,100)

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With optimal triggering and kinematical selections:

(B). Special kinematics for hadron colliders

Hadron momenta: $P_A = (E_A, 0, 0, p_A), \quad P_B = (E_A, 0, 0, -p_A),$ The parton momenta: $p_1 = x_1 P_A, \quad p_2 = x_2 P_B.$

Then the parton c.m. frame moves randomly, even by event:

$$\beta_{cm} = \frac{x_1 - x_2}{x_1 + x_2}, \text{ or :}$$

$$y_{cm} = \frac{1}{2} \ln \frac{1 + \beta_{cm}}{1 - \beta_{cm}} = \frac{1}{2} \ln \frac{x_1}{x_2}, \quad (-\infty < y_{cm} < \infty).$$

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The four-momentum vector transforms as

$$\begin{pmatrix} E'\\ p'_z \end{pmatrix} = \begin{pmatrix} \gamma & -\gamma & \beta_{cm} \\ -\gamma & \beta_{cm} & \gamma \end{pmatrix} \begin{pmatrix} E\\ p_z \end{pmatrix}$$
$$= \begin{pmatrix} \cosh y_{cm} & -\sinh y_{cm} \\ -\sinh y_{cm} & \cosh y_{cm} \end{pmatrix} \begin{pmatrix} E\\ p_z \end{pmatrix}.$$

This is often called the "boost".

One wishes to design final-state kinematics invariant under the boost: For a four-momentum $p \equiv p^{\mu} = (E, \vec{p})$,

$$E_T = \sqrt{p_T^2 + m^2}, \quad y = \frac{1}{2} \ln \frac{E + p_z}{E - p_z},$$

$$p^{\mu} = (E_T \cosh y, \ p_T \sin \phi, \ p_T \cos \phi, \ E_T \sinh y),$$

$$\frac{d^3 \vec{p}}{E} = p_T dp_T d\phi \ dy = E_T dE_T d\phi \ dy.$$

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In the massless limit, rapidity \rightarrow pseudo-rapidity:

$$y \to \eta = \frac{1}{2} \ln \frac{1 + \cos \theta}{1 - \cos \theta} = \ln \cot \frac{\theta}{2}.$$

The "Lego" plot:



A CDF di-jet event on a lego plot in the $\eta - \phi$ plane.

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 $\phi, \Delta y = y_2 - y_1$ is boost-invariant. Thus the "separation" between two particles in an event $\Delta R = \sqrt{\Delta \phi^2 + \Delta y^2}$ is boost-invariant, and lead to the "cone definition" of a jet. (C). Characteristic observables: Crucial for uncovering new dynamics.

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Energy momentum observables \implies mass parameters Angular observables \implies nature of couplings; Production rates, decay branchings/lifetimes \implies interaction strengths.

(D). Kinematical features:

(a). *s*-channel singularity: bump search we do best.

• invariant mass of two-body $R \rightarrow ab$: $m_{ab}^2 = (p_a + p_b)^2 = M_R^2$. combined with the two-body Jacobian peak in transverse momentum:

$$\frac{d\hat{\sigma}}{dm_{ee}^2 \ dp_{eT}^2} \propto \frac{\Gamma_Z M_Z}{(m_{ee}^2 - M_Z^2)^2 + \Gamma_Z^2 M_Z^2} \ \frac{1}{m_{ee}^2 \sqrt{1 - 4p_{eT}^2/m_{ee}^2}}$$

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• "transverse" mass of two-body $W^- \rightarrow e^- \overline{\nu}_e$:

$$m_{e\nu T}^{2} = (E_{eT} + E_{\nu T})^{2} - (\vec{p}_{eT} + \vec{p}_{\nu T})^{2}$$

= $2E_{eT}E_{T}^{miss}(1 - \cos\phi) \le m_{e\nu}^{2}$.



If $p_T(W) = 0$, then $m_{e\nu} T = 2E_{eT} = 2E_T^{miss}$.

• $H^0 \to W^+ W^- \to j_1 j_2 \ e^- \bar{\nu}_e$: cluster transverse mass (I): $m_{WW\ T}^2 = (E_{W_1T} + E_{W_2T})^2 - (\vec{p}_{jjT} + \vec{p}_{eT} + \vec{p}_T^{\ miss})^2$ $= (\sqrt{p_{jjT}^2 + M_W^2} + \sqrt{p_{e\nu T}^2 + M_W^2})^2 - (\vec{p}_{jjT} + \vec{p}_{eT} + \vec{p}_T^{\ miss})^2 \le M_H^2.$ where $\vec{p}_T^{\ miss} \equiv \vec{p}_T = -\sum_{obs} \ \vec{p}_T^{\ obs}.$

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 $m_{WW C} \approx \sqrt{p_{T,\ell\ell}^2 + M_{\ell\ell}^2 + p_T}$



 M_{WW} invariant mass (WW fully reconstructable): ----- $M_{WW, T}$ transverse mass (one missing particle ν): ----- $M_{eff, T}$ effetive trans. mass (two missing particles): ----- $M_{WW, C}$ cluster trans. mass (two missing particles): -----



YOU design an optimal variable/observable for the search.

• cluster transverse mass (III):

$$H^0 \to \tau^+ \tau^- \to \mu^+ \ \bar{\nu}_\tau \ \nu_\mu, \quad \rho^- \ \nu_\tau$$

A lot more complicated with (many) more $\nu's$?



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 $\tau^+\tau^-$ ultra-relativistic, the final states from a τ decay highly collimated:

$$heta pprox \gamma_{ au}^{-1} = m_{ au}/E_{ au} = 2m_{ au}/m_{H} pprox 1.5^{\circ} \quad (m_{H} = 120 \,\, {
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We can thus take

$$\vec{p}_{\tau^+} = \vec{p}_{\mu^+} + \vec{p}_{+}^{\nu's}, \quad \vec{p}_{+}^{\nu's} \approx c_+ \vec{p}_{\mu^+}.$$

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where c_{\pm} are proportionality constants, to be determined. This is applicable to any decays of fast-moving particles, like

$$T \to Wb \to \ell \nu, \ b.$$

Experimental measurements: $p_{\rho^-}, p_{\mu^+}, p_T$:

$$c_{+}(p_{\mu^{+}})_{x} + c_{-}(p_{\rho^{-}})_{x} = (\not p_{T})_{x}, c_{+}(p_{\mu^{+}})_{y} + c_{-}(p_{\rho^{-}})_{y} = (\not p_{T})_{y}.$$

Unique solutions for c_{\pm} exist if

$$(p_{\mu^+})_x/(p_{\mu^+})_y \neq (p_{\rho^-})_x/(p_{\rho^-})_y.$$

Physically, the τ^+ and τ^- should form a finite angle, or the Higgs should have a non-zero transverse momentum. Experimental measurements: $p_{\rho^-}, p_{\mu^+}, p_T$:

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(b). Two-body versus three-body kinematics

• Energy end-point and mass edges:

utilizing the "two-body kinematics" Consider a simple case:

 $e^+e^- \to \tilde{\mu}_R^+ \ \tilde{\mu}_R^$ with two – body decays : $\tilde{\mu}_R^+ \to \mu^+ \tilde{\chi}_0, \quad \tilde{\mu}_R^- \to \mu^- \tilde{\chi}_0.$ In the $\tilde{\mu}_R^+$ -rest frame: $E_{\mu}^0 = \frac{M_{\tilde{\mu}_R}^2 - m_{\chi}^2}{2M_{\tilde{\mu}_R}}$.

In the Lab-frame:

$$\begin{aligned} (1-\beta)\gamma E^0_\mu &\leq E^{lab}_\mu \leq (1+\beta)\gamma E^0_\mu \\ \text{with } \beta &= \left(1-4M^2_{\tilde{\mu}_R}/s\right)^{1/2}, \ \gamma &= (1-\beta)^{-1/2}. \\ \text{Energy end-point: } E^{lab}_\mu \Rightarrow M^2_{\tilde{\mu}_R} - m^2_\chi. \\ \text{Mass edge: } m^{max}_{\mu^+\mu^-} &= \sqrt{s} - 2m_\chi. \end{aligned}$$

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Same idea can be applied to hadron colliders ...

Consider a squark cascade decay:



1st edge: $M^{max}(\ell \ell) = M_{\chi_2^0} - M_{\chi_1^0};$ 2nd edge: $M^{max}(\ell \ell j) = M_{\tilde{q}} - M_{\chi_1^0}.$



(c). *t*-channel singularity: splitting.

• Gauge boson radiation off a fermion:

The familiar Weizsäcker-Williams approximation



$$\sigma(fa \to f'X) \approx \int dx \ dp_T^2 \ P_{\gamma/f}(x, p_T^2) \ \sigma(\gamma a \to X),$$
$$P_{\gamma/e}(x, p_T^2) = \frac{\alpha}{2\pi} \frac{1 + (1-x)^2}{x} \left(\frac{1}{p_T^2}\right)|_{m_e}^E.$$

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† The kernel is the same as $q \rightarrow qg^* \Rightarrow$ generic for parton splitting; † The form $dp_T^2/p_T^2 \rightarrow \ln(E^2/m_e^2)$ reflects the collinear behavior.
• Generalize to massive gauge bosons:

$$P_{V/f}^{T}(x, p_{T}^{2}) = \frac{g_{V}^{2} + g_{A}^{2}}{8\pi^{2}} \frac{1 + (1 - x)^{2}}{x} \frac{p_{T}^{2}}{(p_{T}^{2} + (1 - x)M_{V}^{2})^{2}},$$

$$P_{V/f}^{L}(x, p_{T}^{2}) = \frac{g_{V}^{2} + g_{A}^{2}}{4\pi^{2}} \frac{1 - x}{x} \frac{(1 - x)M_{V}^{2}}{(p_{T}^{2} + (1 - x)M_{V}^{2})^{2}}.$$

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Special kinematics for massive gauge boson fusion processes: For the accompanying jets,

At low- p_{jT} ,

$$\begin{array}{c} p_{jT}^2 \approx (1-x)M_V^2 \\ E_j \sim (1-x)E_q \end{array} \right\} forward \ jet \ tagging \end{array}$$

At high- p_{jT} ,

$$\frac{\frac{d\sigma(V_T)}{dp_{jT}^2} \propto 1/p_{jT}^2}{\frac{d\sigma(V_L)}{dp_{jT}^2} \propto 1/p_{jT}^4} \begin{cases} central \ jet \ vetoing \end{cases}$$

has become important tools for Higgs searches, single-top signal etc.

(E). Charge forward-backward asymmetry A_{FB} :

The coupling vertex of a vector boson V_{μ} to an arbitrary fermion pair f

 $i \sum_{\tau}^{L,R} g_{\tau}^{f} \gamma^{\mu} P_{\tau} \longrightarrow$ crucial to probe chiral structures.

The parton-level forward-backward asymmetry is defined as

$$A_{FB}^{i,f} \equiv \frac{N_F - N_B}{N_F + N_B} = \frac{3}{4} \mathcal{A}_i \mathcal{A}_f,$$
$$\mathcal{A}_f = \frac{(g_L^f)^2 - (g_R^f)^2}{(g_L^f)^2 + (g_R^f)^2}.$$

where $N_F(N_B)$ is the number of events in the forward (backward) direction defined in the parton c.m. frame relative to the initial-state fermion $\vec{p_i}$.

At hadronic level:

$$A_{FB}^{\mathsf{LHC}} = \frac{\int dx_1 \sum_q A_{FB}^{q,f} \left(P_q(x_1) P_{\overline{q}}(x_2) - P_{\overline{q}}(x_1) P_q(x_2) \right) \operatorname{sign}(x_1 - x_2)}{\int dx_1 \sum_q \left(P_q(x_1) P_{\overline{q}}(x_2) + P_{\overline{q}}(x_1) P_q(x_2) \right)}.$$

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In $p\bar{p}$ collisions, \vec{p}_{proton} is the direction of \vec{p}_{quark} .

In pp collisions, however, what is the direction of \vec{p}_{quark} ?

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In $p\bar{p}$ collisions, \vec{p}_{proton} is the direction of \vec{p}_{quark} .

In *pp* collisions, however, what is the direction of \vec{p}_{quark} ? It is the boost-direction of $\ell^+\ell^-$.

How about $W^{\pm}/W'^{\pm}(\ell^{\pm}\nu)$ -type?

In $p\bar{p}$ collisions, \vec{p}_{proton} is the direction of \vec{p}_{quark} , AND ℓ^+ (ℓ^-) along the direction with \bar{q} (q) \Rightarrow OK at the Tevatron,

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In $p\bar{p}$ collisions: (1). a reconstructable system (2). with spin correlation \rightarrow only tops $W' \rightarrow t\bar{b} \rightarrow \ell^{\pm}\nu \ \bar{b}$:



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Definition: A_{CP} vanishes if CP-violation interactions do not exist (for the relevant particles involved).

This is meant to be in contrast to an observable: that'd be *modified* by the presence of CP-violation, but is *not zero* when CP-violation is absent.

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Two ways:

a). Compare the rates between a process and its CP-conjugate process:

$$\frac{R(i \to f) - R(\overline{i} \to \overline{f})}{R(i \to f) + R(\overline{i} \to \overline{f})}, \quad \text{e.g.} \quad \frac{\Gamma(t \to W^+ q) - \Gamma(\overline{t} \to W^- \overline{q})}{\Gamma(t \to W^+ q) + \Gamma(\overline{t} \to W^- \overline{q})}.$$

b). Construct a CP-odd kinematical variable for an initially CP-eigenstate:

$$\mathcal{M} \sim M_1 + M_2 \sin \theta,$$

$$A_{CP} = \sigma^F - \sigma^B = \int_0^1 \frac{d\sigma}{d\cos\theta} d\cos\theta - \int_{-1}^0 \frac{d\sigma}{d\cos\theta} d\cos\theta$$

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E.g. 1: $H \to Z(p_1)Z^*(p_2) \to e^+(q_1)e^-(q_2), \ \mu^+\mu^-$



 $\Gamma^{\mu\nu}(p_1, p_2) = i \frac{2}{v} h[a \ M_Z^2 g^{\mu\nu} + b \ (p_1^{\mu} p_2^{\nu} - p_1 \cdot p_2 g^{\mu\nu}) + \tilde{b} \ \epsilon^{\mu\nu\rho\sigma} p_{1\rho} p_{2\sigma}]$ $a = 1, \ b = \tilde{b} = 0 \text{ for SM.}$ In general, $a, \ b, \ \tilde{b}$ complex form factors, describing new physics at a higher scale. For $H \to Z(p_1)Z^*(p_2) \to e^+(q_1)e^-(q_2), \ \mu^+\mu^-$, define:

$$O_{CP} \sim (\vec{p}_1 - \vec{p}_2) \cdot (\vec{q}_1 \times \vec{q}_2),$$

or $\cos \theta = \frac{(\vec{p}_1 - \vec{p}_2) \cdot (\vec{q}_1 \times \vec{q}_2)}{|\vec{p}_1 - \vec{p}_2| |\vec{q}_1 \times \vec{q}_2)|}.$

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E.g. 2:
$$H \to t(p_t)\bar{t}(p_{\bar{t}}) \to e^+(q_1)\nu_1 b_1, \ e^-(q_2)\nu_2 b_2.$$

$$-\frac{m_t}{v}\bar{t}(a+b\gamma^5)t \ H$$
$$O_{CP} \sim (\vec{p_t} - \vec{p_t}) \cdot (\vec{p_{e^+}} \times \vec{p_{e^-}}).$$

thus define an asymmetry angle.

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A general phenomenological Approach: (mine)

From a theory to experimental predictions

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• Display the key structure of the theory:

(new particle spectrum, interactions, basic parameters \mathcal{L}) EWSB $\Rightarrow m_H$ and $W_L W_L$ interactions. full interaction Lagrangian • Identify the most characteristic state for signal observation: $EWSB \Rightarrow Higgs \text{ or } W_L W_L \text{ interactions.}$ $SUSY \Rightarrow LSP, \tilde{g}, \tilde{t}, \tilde{\chi}...$ Little Higgs \Rightarrow heavy T, and W_H, Z_H .

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