

# A Generalized Model for Light Transport in Scintillators

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# Introduction

## Scintillators

### 5 Types of scintillators

5.1 Organic crystals

5.2 Organic liquids

5.3 Plastic scintillators

5.3.1 Bases

5.3.2 Fluors

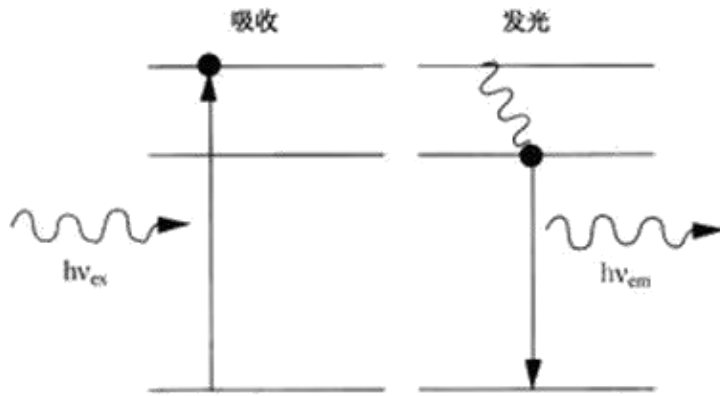
5.4 Inorganic crystals

5.5 Gaseous scintillators

5.6 Glasses



# Introduction



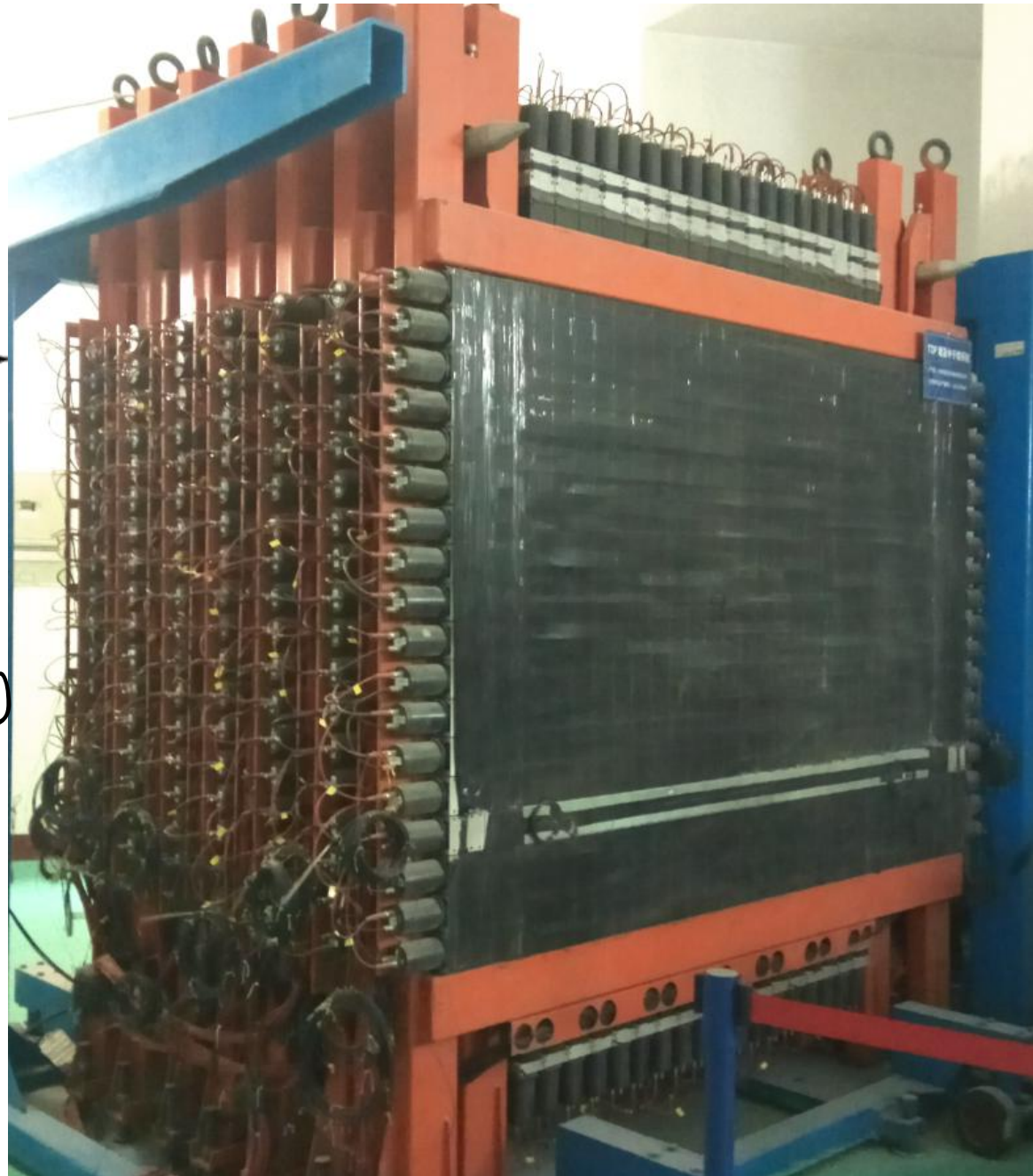
Photomultiplier tube (PMT)



signal

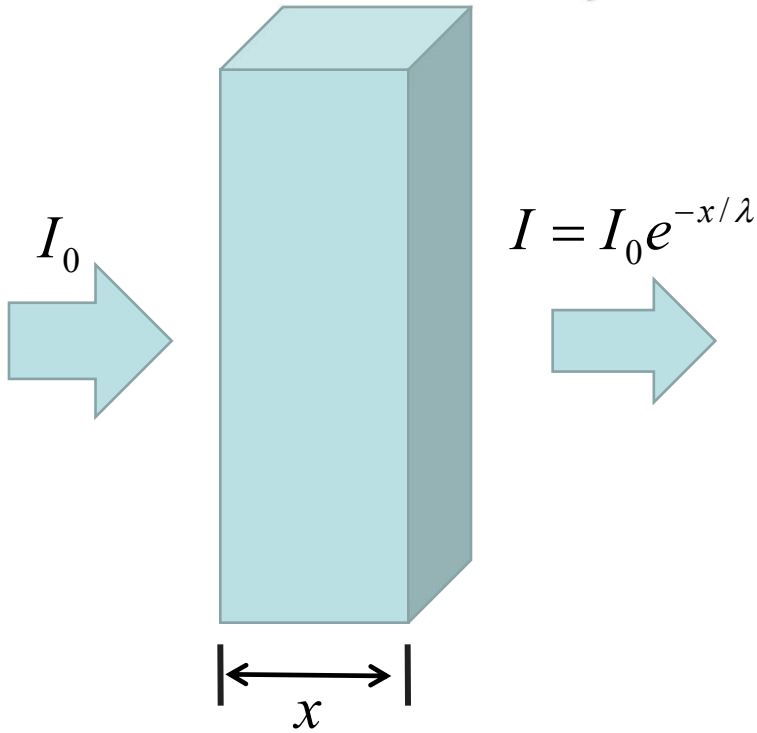


extract: hit position or deposited energy



# Light Transport

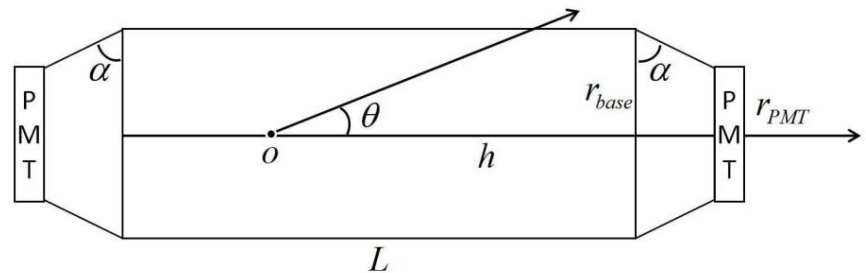
Intensity: decay length,  $\lambda$



$4\pi$  uniform



Section of Right Circular Cylinders

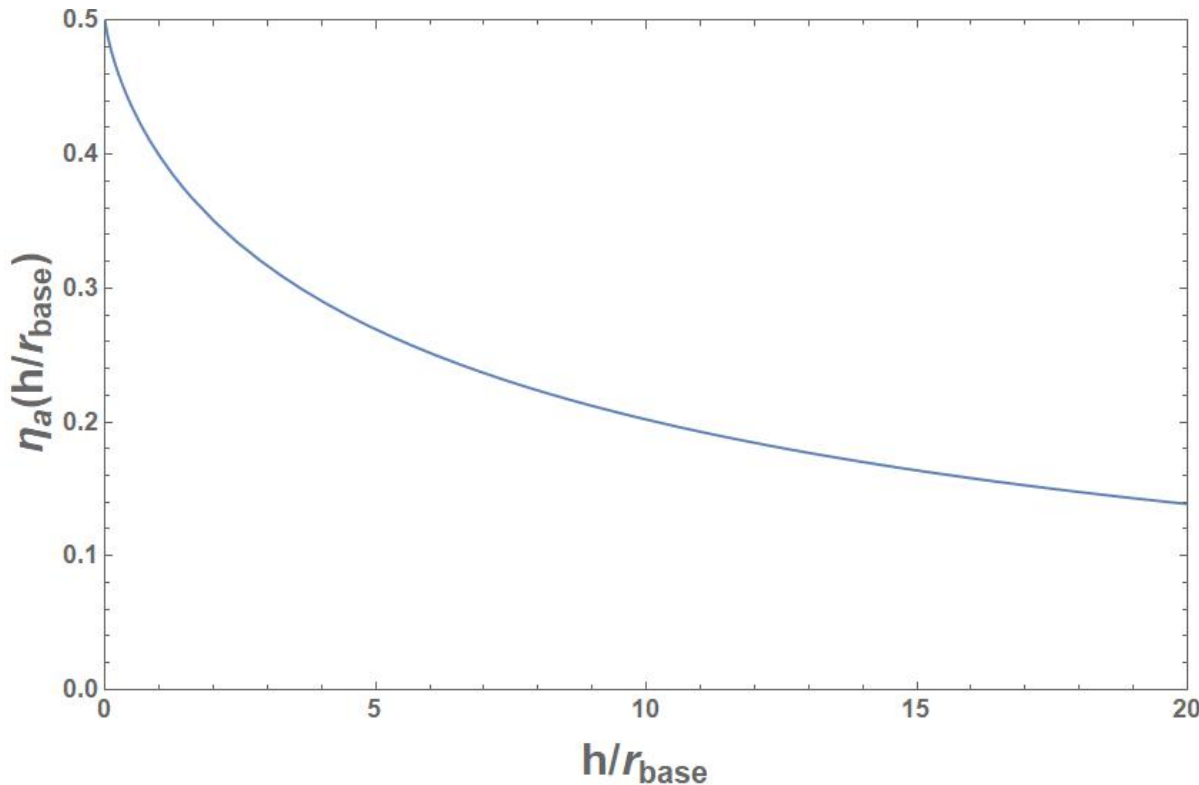


This formula only works in parallel light.  
But the light is radial in Scintillators.

Figure 2: We analyse the geometric shape of scintillator as a right circular cylinders with base radius  $r_{base}$  and height  $L$  and the collection PMT is a right circular cylinders with base radius  $r_{PMT}$  contracted by a right conical frustum with top is scintillator's base and base is PMT's base and the base angle is  $\alpha$ , and the position of emitted light on the axis with height  $h$  and  $\theta$  direction for each light.

# Light Transport

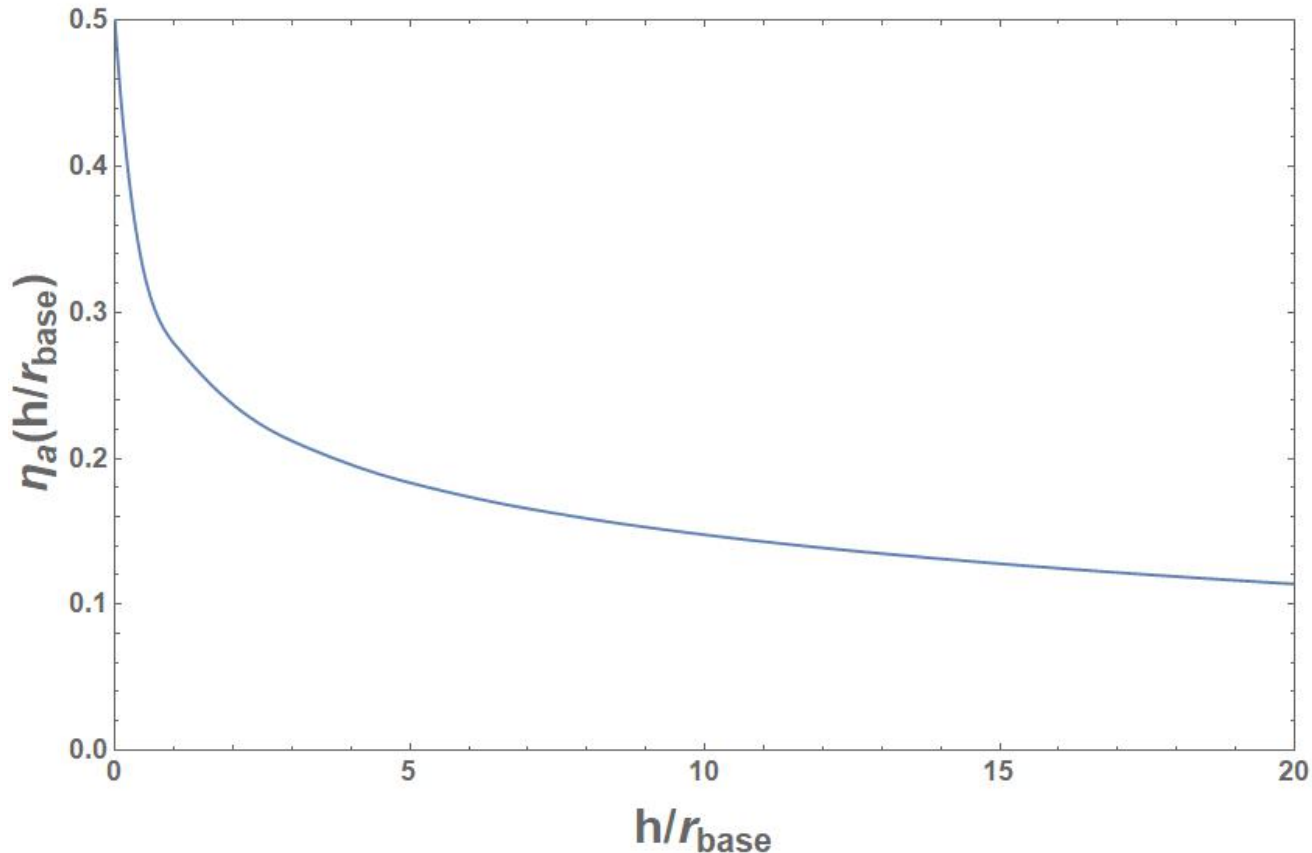
$$I_a(h/r_{base}) = I_0 \frac{2\pi}{4\pi} \int_0^{\pi/2} e^{-\frac{h/r_{base}}{\lambda \cos\theta}} \sin\theta d\theta$$
$$= I_0 \eta_a(h/r_{base}) e^{-\frac{h/r_{base}}{\lambda}},$$



Correction fraction:  
describes the  
properties of the  
Scintillators

# Light Transport

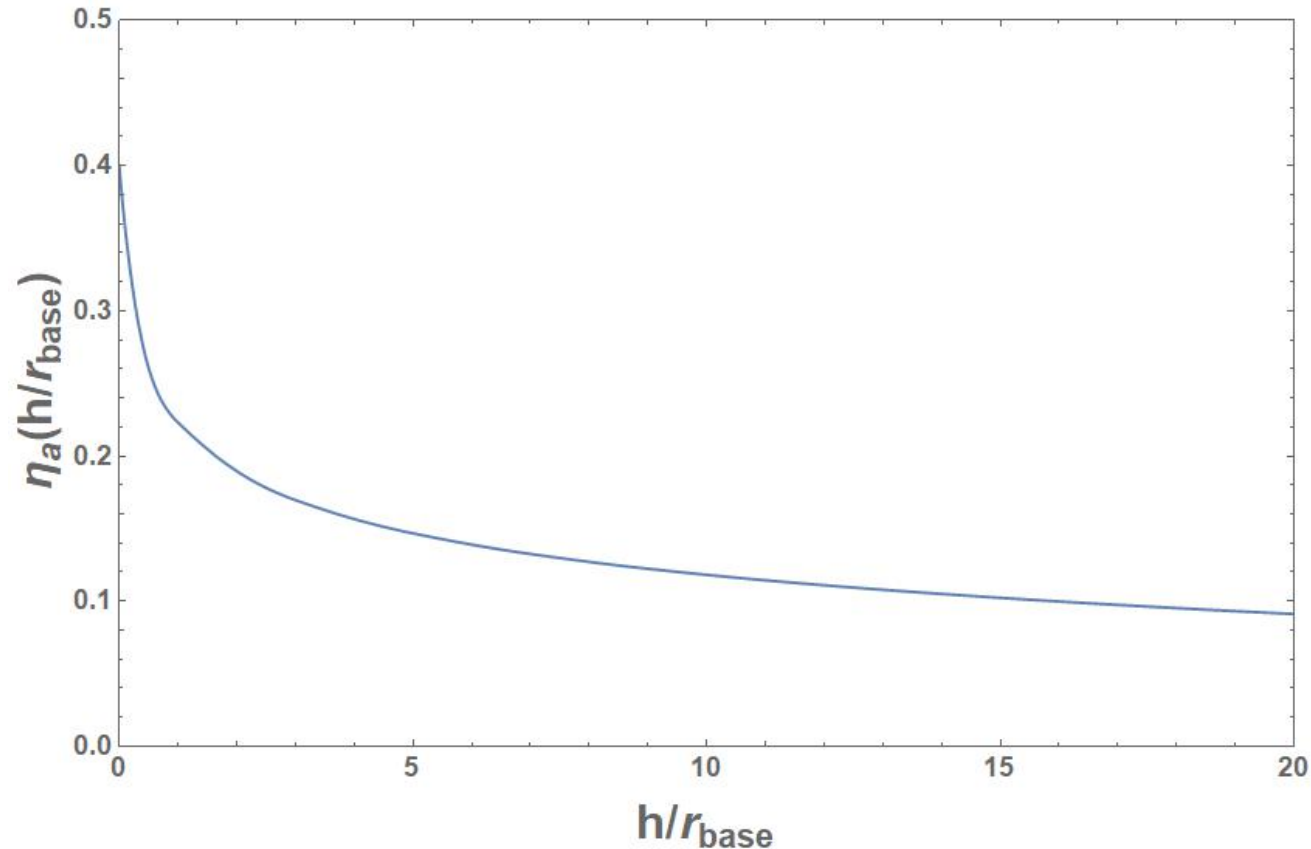
$$I_a(h/r_{base}) = I_0 \frac{2\pi}{4\pi} \int_0^{\pi/2} e^{-\frac{h/r_{base}}{\lambda \cos\theta}} \left( \frac{\sin(\pi/2 - \theta)}{\sin\theta_c} \right)^{\left\lfloor \frac{h/r_{base} + \tan(\pi/2 - \theta)}{2 \tan(\pi/2 - \theta)} \right\rfloor} \sin\theta d\theta$$
$$= I_0 \eta_a(h/r_{base}) e^{-\frac{h/r_{base}}{\lambda}},$$



# Light Transport

$$I_a(h/r_{base}) = I_0 \frac{2\pi}{4\pi} \int_0^{\pi/2} e^{-\frac{h/r_{base}}{\lambda \cos\theta}} \left( \frac{\sin(\pi/2 - \theta)}{\sin\theta_c} \right)^{\lfloor \frac{h/r_{base} + \tan(\pi/2 - \theta)}{2 \tan(\pi/2 - \theta)} \rfloor} R_a \sin\theta d\theta$$

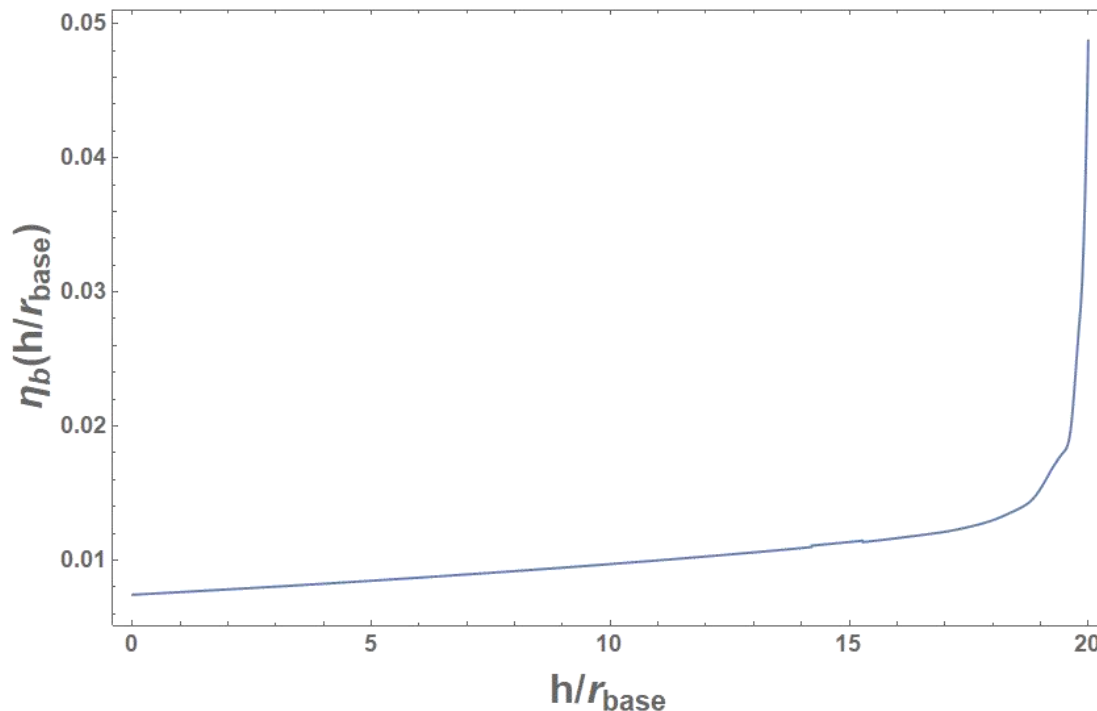
$$= I_0 \eta_a(h/r_{base}) e^{-\frac{h/r_{base}}{\lambda}},$$



# Light Transport

Integrate from  $\pi/2$  to  $\pi$ .

$$I_b(h/r_{base}) = I_0 \frac{2\pi}{4\pi} \int_{\pi/2}^{\pi} \dots \sin\theta d\theta$$
$$= I_0 \eta_b(h/r_{base}) e^{-\frac{(2L-h)/r_{base}}{\lambda}},$$



Correction fraction:  
describes the  
properties of the  
Scintillators



# Light Transport

$$I(x) = I_0 \left( \eta_a(x) e^{-x/\lambda} + \eta_b(x) e^{-(2L-x)/\lambda} \right).$$

$$\eta_a(x) = e^{\frac{c_1}{c_2+x}} \quad \eta_b(x) = \frac{c_3}{1-x/c_4}$$

Where the parameter :

$c_1$  and  $c_2$  are in the same order of  $r_{base}$

$c_3$  is in the order of  $r_{base}/L$ ,

$c_4$  is in the order of  $L$ .

$\eta_a(x) \rightarrow 1$  under  $x \gg c_1$ , and  $\eta_b(x) \rightarrow 0$  under  $x \ll L$ .

Section of Right Circular Cylinders

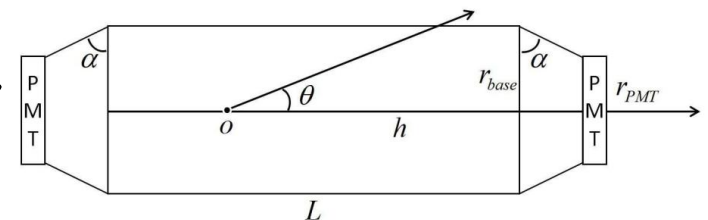


Figure 2: We analyse the geometric shape of scintillator as a right circular cylinders with base radius  $r_{base}$  and height  $L$  and the collection PMT is a right circular cylinders with base radius  $r_{PMT}$  and height  $h$ . The PMT is a right circular frustum with top is scintillator's base and base is PMT's base and the base angle is  $\alpha$ , and the position of emitted light on the axis with height  $h$  and  $\theta$  direction for each light.

# Result

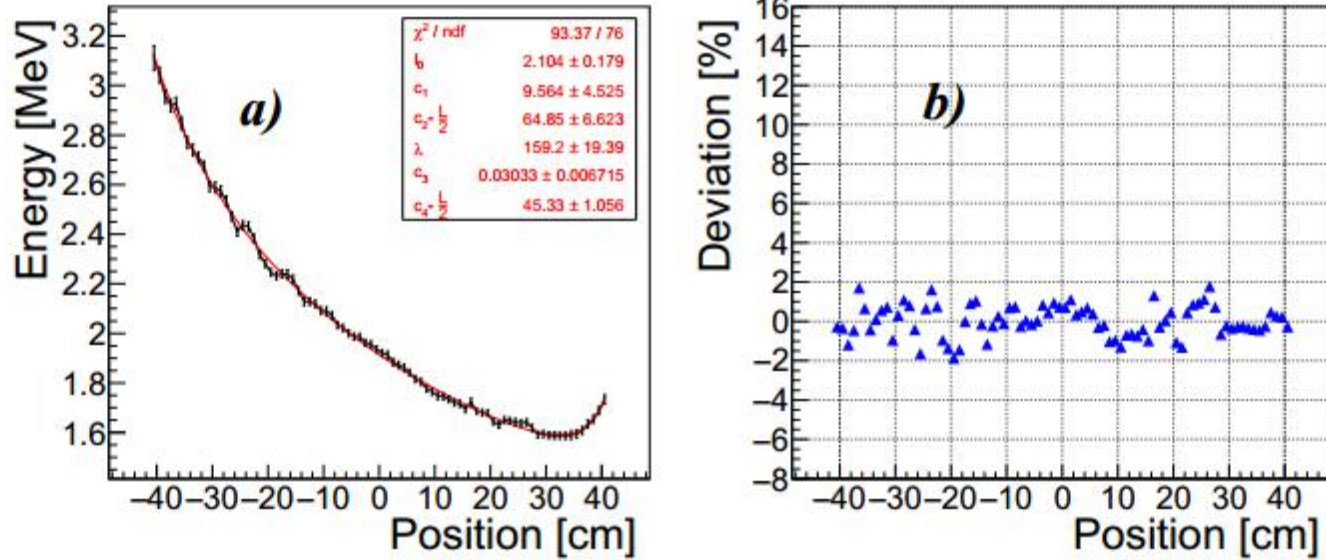
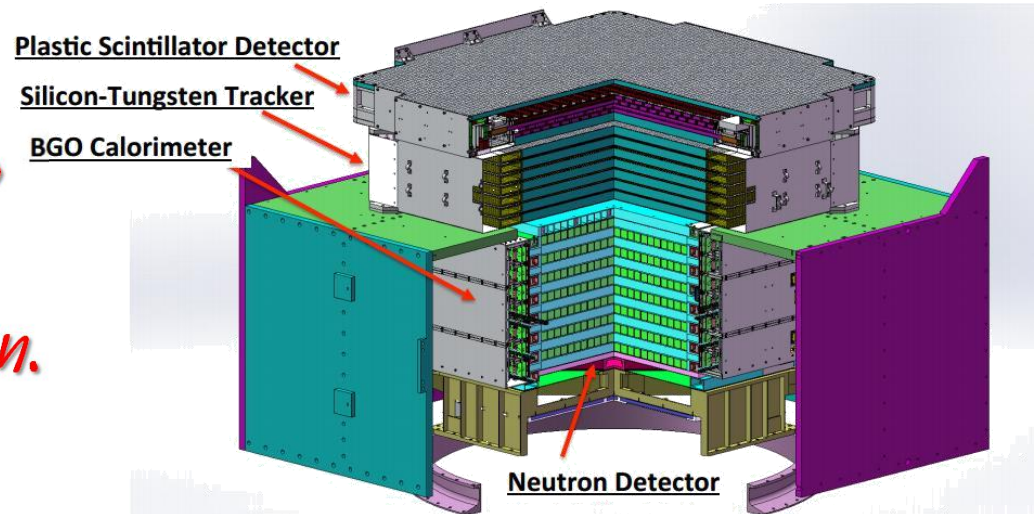


Figure 4: (Color online) a) The curve fitted with the samples from PSD at DAMPE by our model under converting length coordinates to position coordinates. b) The deviation between our new model fitting function and the samples.

*Our model is used to do calibration/alignment by DAMPE Collaboration.*

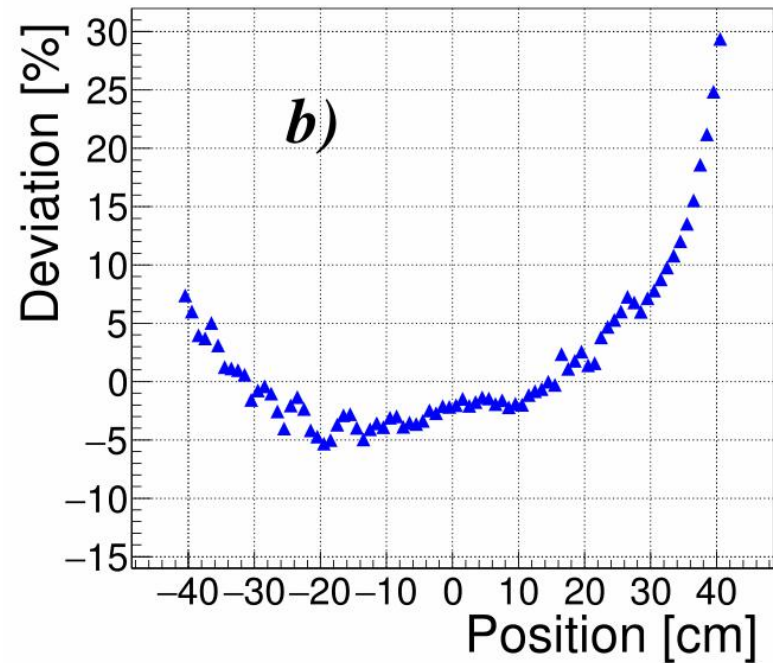
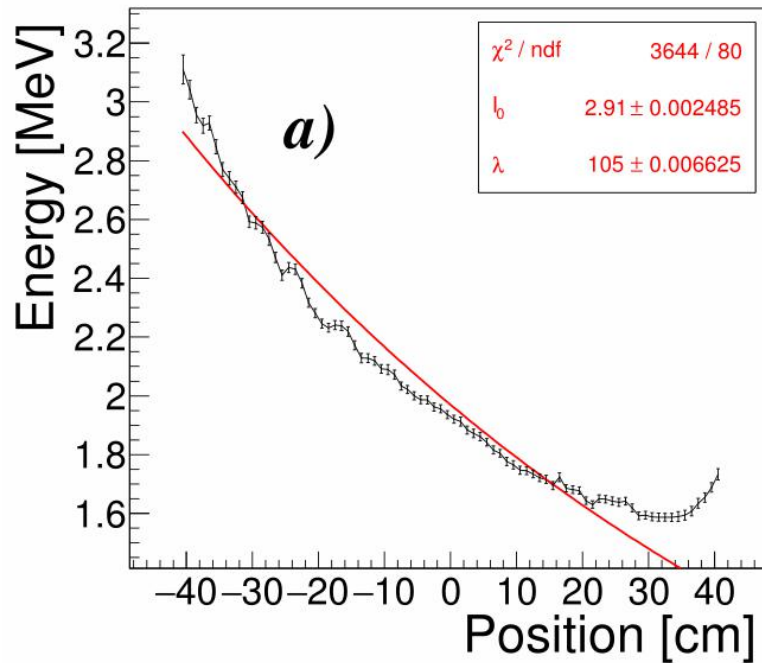


# Result: Case-I

$$I(x) = I_0 e^{-x/\lambda}.$$

*exponential decay*

*Not good !!*

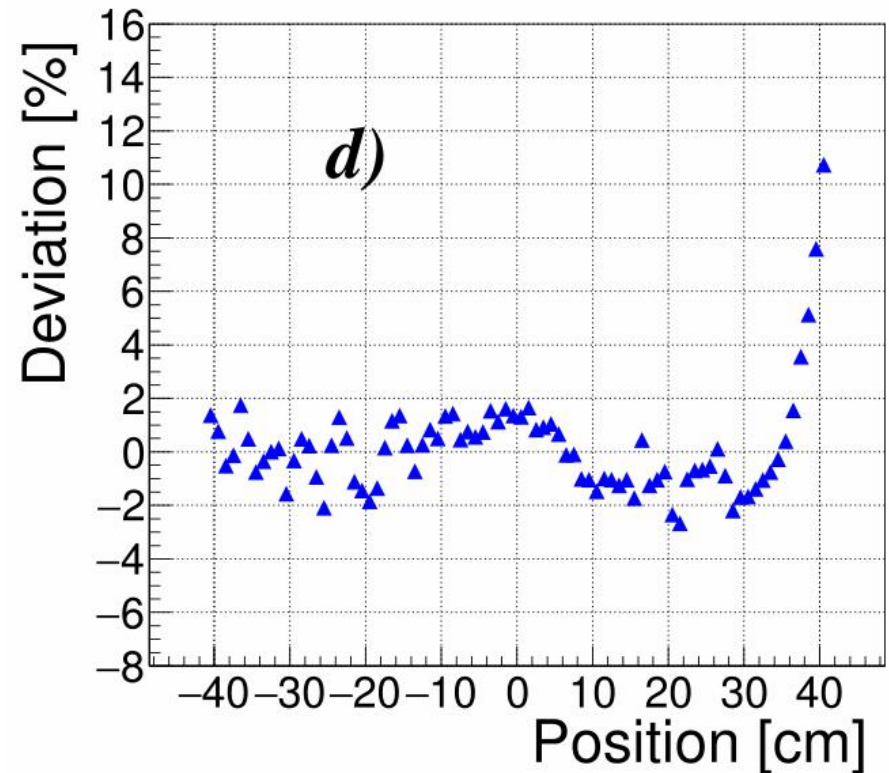
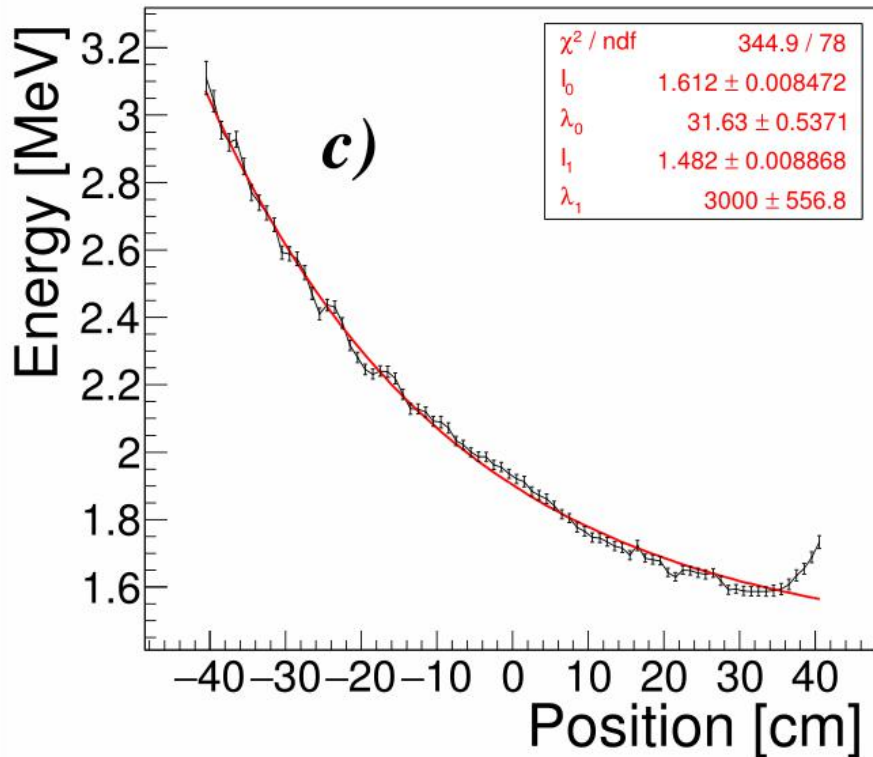


# Result: Case-II

*Still not so good !!*

$$I(x) = I_1 e^{-x/\lambda_1} + I_2 e^{-x/\lambda_2},$$

Ref: IEEE Transactions on Nuclear Science. Publication Year: 1964,  
Page(s):29- 37

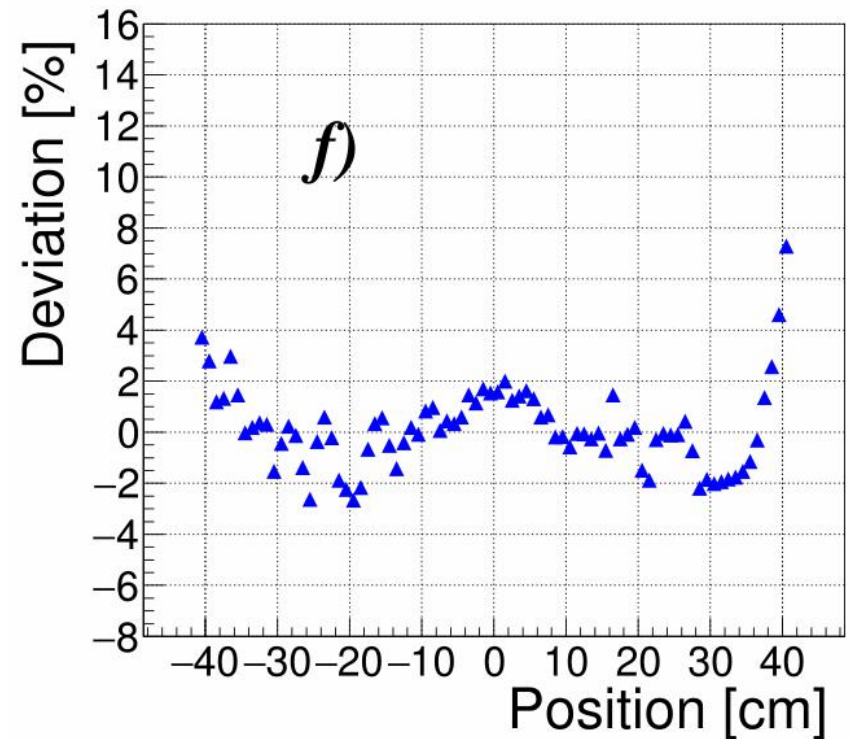
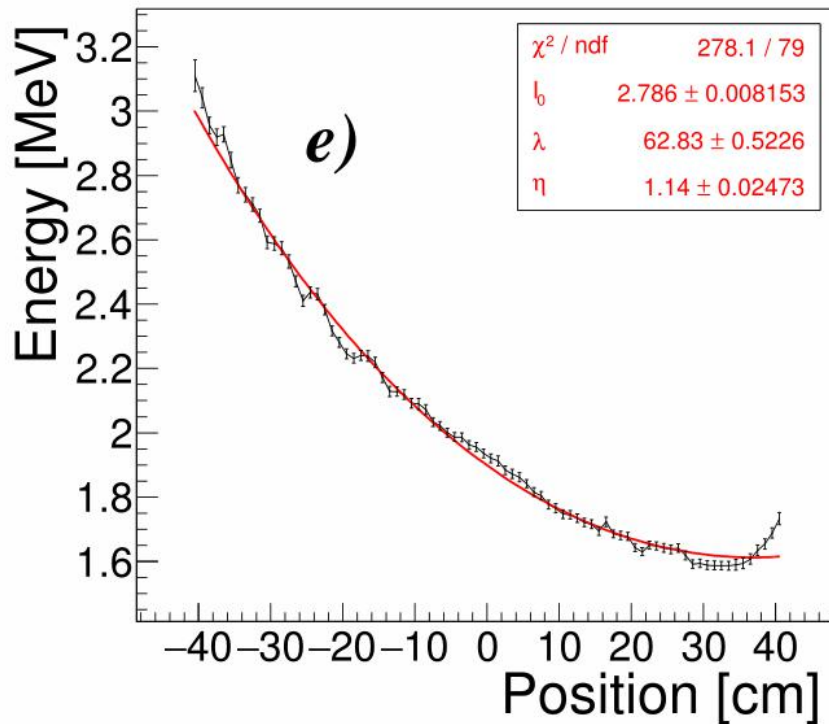


# Result : Case -III

Not so bad !!

$$I(x) = I_0(e^{-x/\lambda} + \eta e^{-(2L-x)/\lambda}).$$

Ref: Nuclear Instruments and Methods in Physics A 370(1996)429-434



# Result: Comparison

$$\delta(x) = \frac{I_{\text{experimental data}}(x) - I_{\text{fitting}}(x)}{I_{\text{fitting}}(x)}.$$

Table 1: Compare The Deviation With Other Models

	ED model	DE model	RB model	our model
$\delta_{max}$	29%	11%	7%	<2%
$\chi^2/ndf$	3644/80	344.9/78	278.1/79	93.4/76

Case -I

Case -II

Case -III

# Result: our model

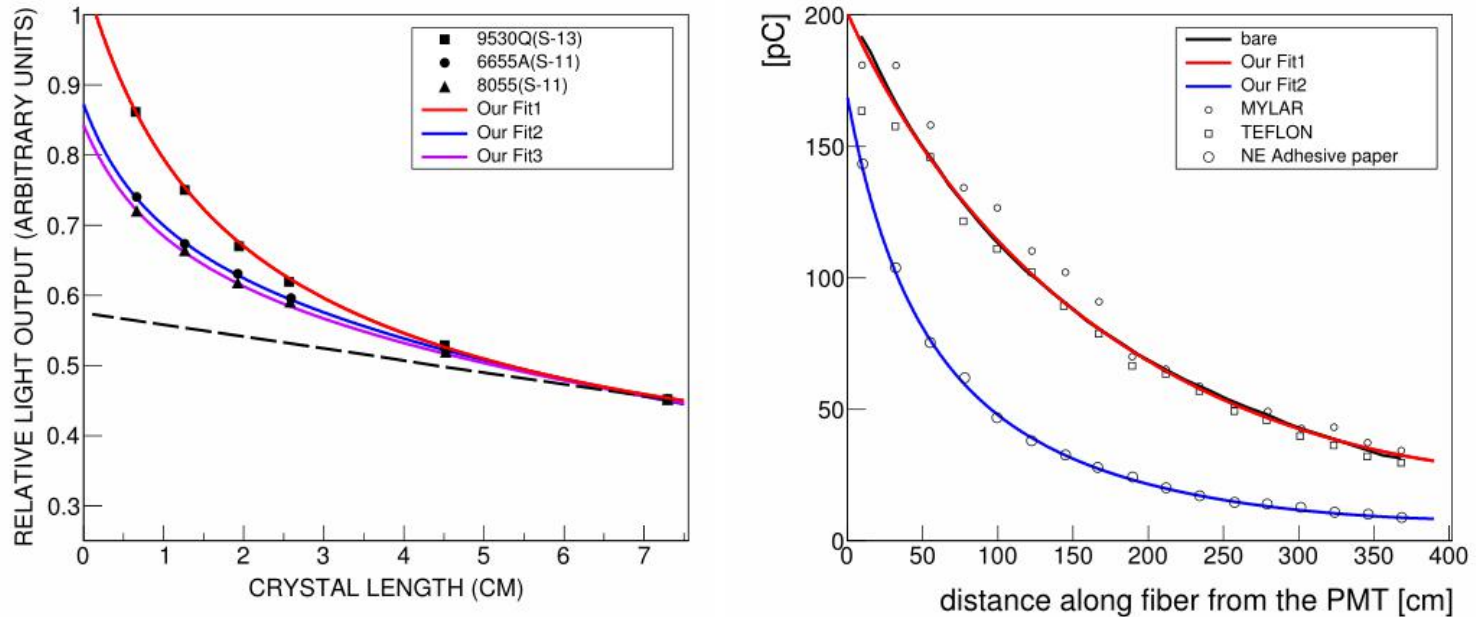


Figure 5: (Color online) left) All the data are from Kaiser's experiment data about light output with length[8], and the three thick lines are our model fitting result. right) All the data are from Taiuti's experiment data about light output with length[9], and the two thick lines are our model fit result.

[8] *IEEE Transactions on Nuclear Science*. Publication Year: 1964,  
Page(s):29- 37

[9] *Nuclear Instruments and Methods in Physics A* 370(1996)429-434

# Result: our model

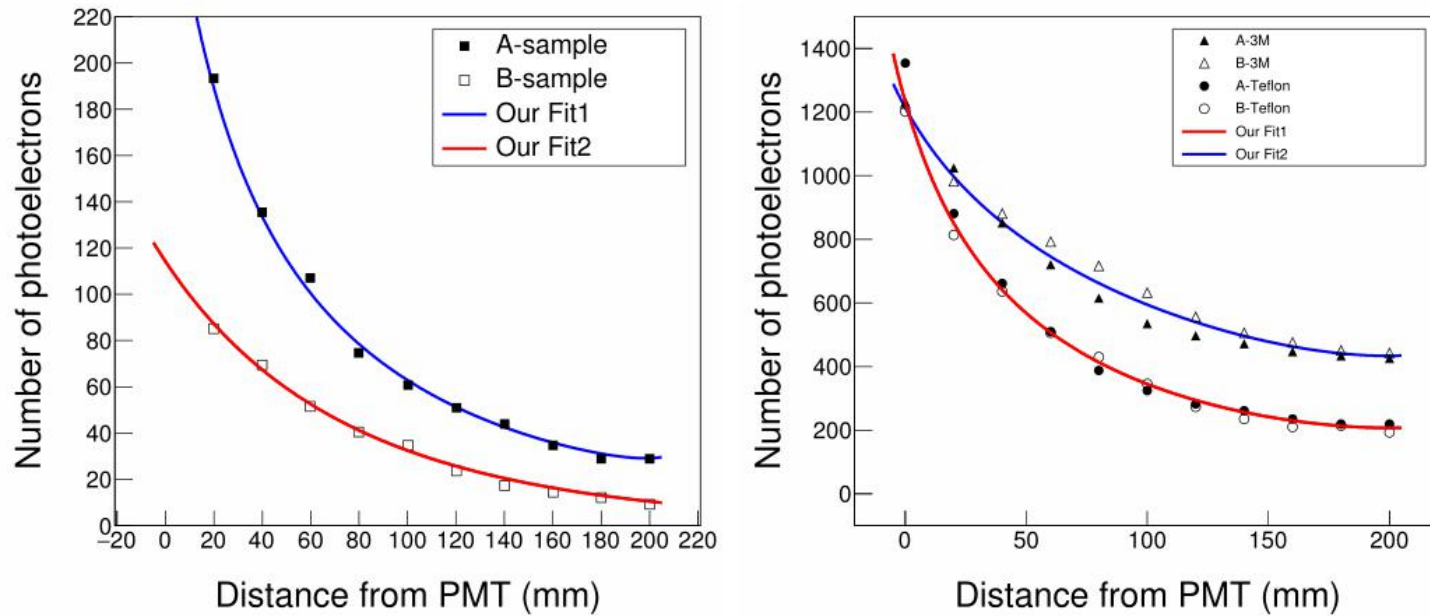


Figure 6: (Color online) All the data are from Gierlik's experiment data about light output with length[10], and the all thick lines are our model fitting result.

[10] *Nuclear Instruments and Methods in Physics Research A* 593 (2008) 426-430



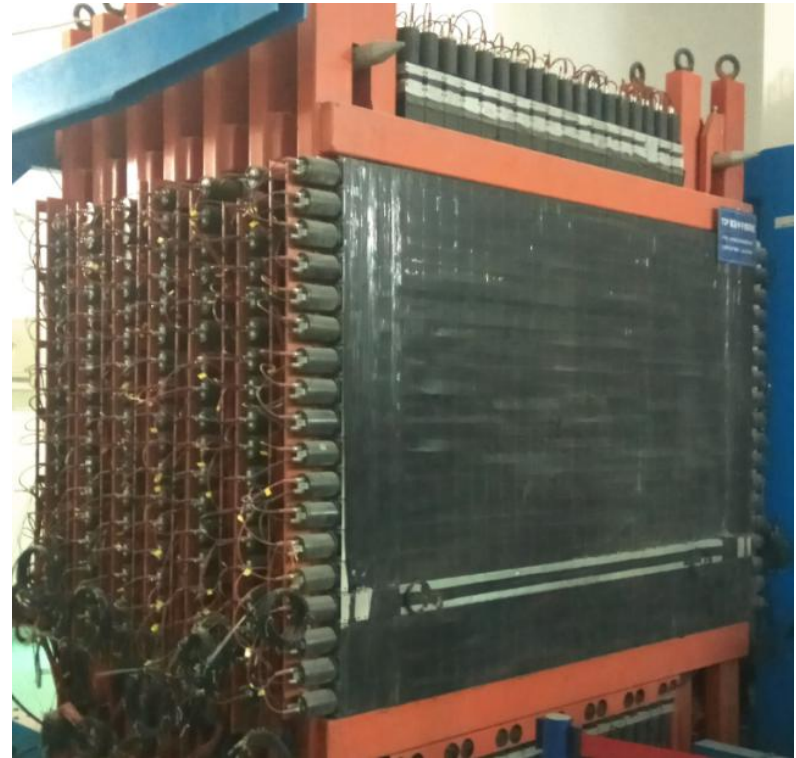
Light Transport: How to get the energy of the particle ?

$$I(x) = I_0 \left( \eta_a(x) e^{-x/\lambda} + \eta_b(x) e^{-(2L-x)/\lambda} \right).$$

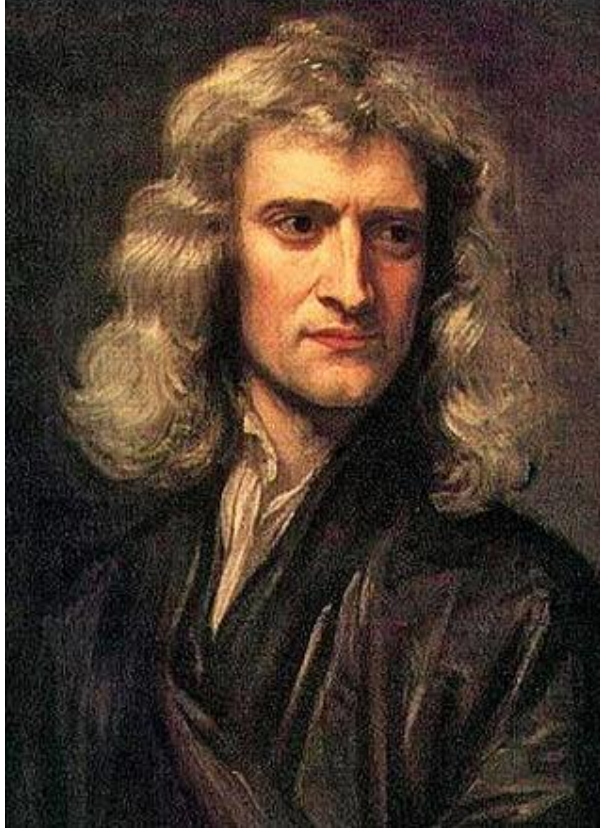
Extract the particle  
Energy:

$$E_{cor} = \frac{E_{adc}}{I(x)}$$

*It can work in half number  
of PMT, and saves cost.*

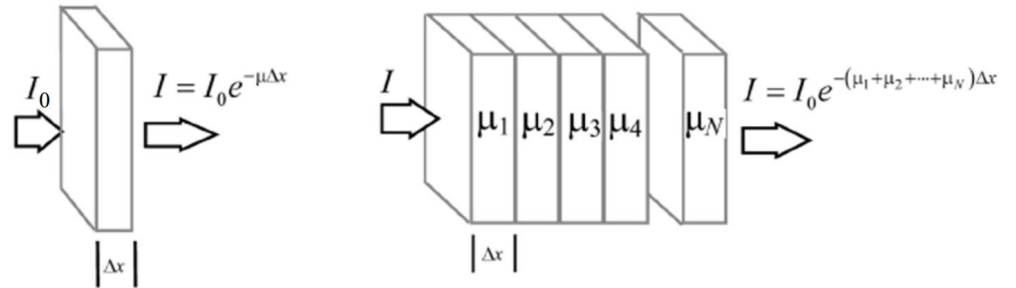


By the way--->>>



Isaac Newton

LHC Collaboration considers small cell one by one for light transport in scintillators, as follows:



$$I = I_0 e^{-\mu \Delta x} \quad I = I_0 e^{-\mu_1 \Delta x} e^{-\mu_2 \Delta x} e^{-\mu_3 \Delta x} \dots e^{-\mu_N \Delta x} = I_0 e^{-\sum_{n=1}^N \mu_n \Delta x}$$

This model likes *calculus* and needs a lot calculation. But it is very powerful.

Anyway, our model is simple without a lot calculation.

*Thank you for your attention,  
please question.*