

Extracting the Odderon from pp and $p\bar{p}$ scattering data

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Content

- Introduction
- The generalized Phillips-Barger (PB) model
- Fitting the model to data
- Results: the Pomeron and the Odderon
- Conclusions

Introduction

The basic idea: The pp and $p\bar{p}$ elastic scattering amplitude can be well described as a function of “even” and “odd” parts with Pomeron (P), Odderon (O) and secondary Reggeons (f , ω):

$$A(s, t)_{pp}^{\bar{p}p} = A_P(s, t) + A_f(s, t) \pm [A_\omega(s, t) + A_O(s, t)]$$

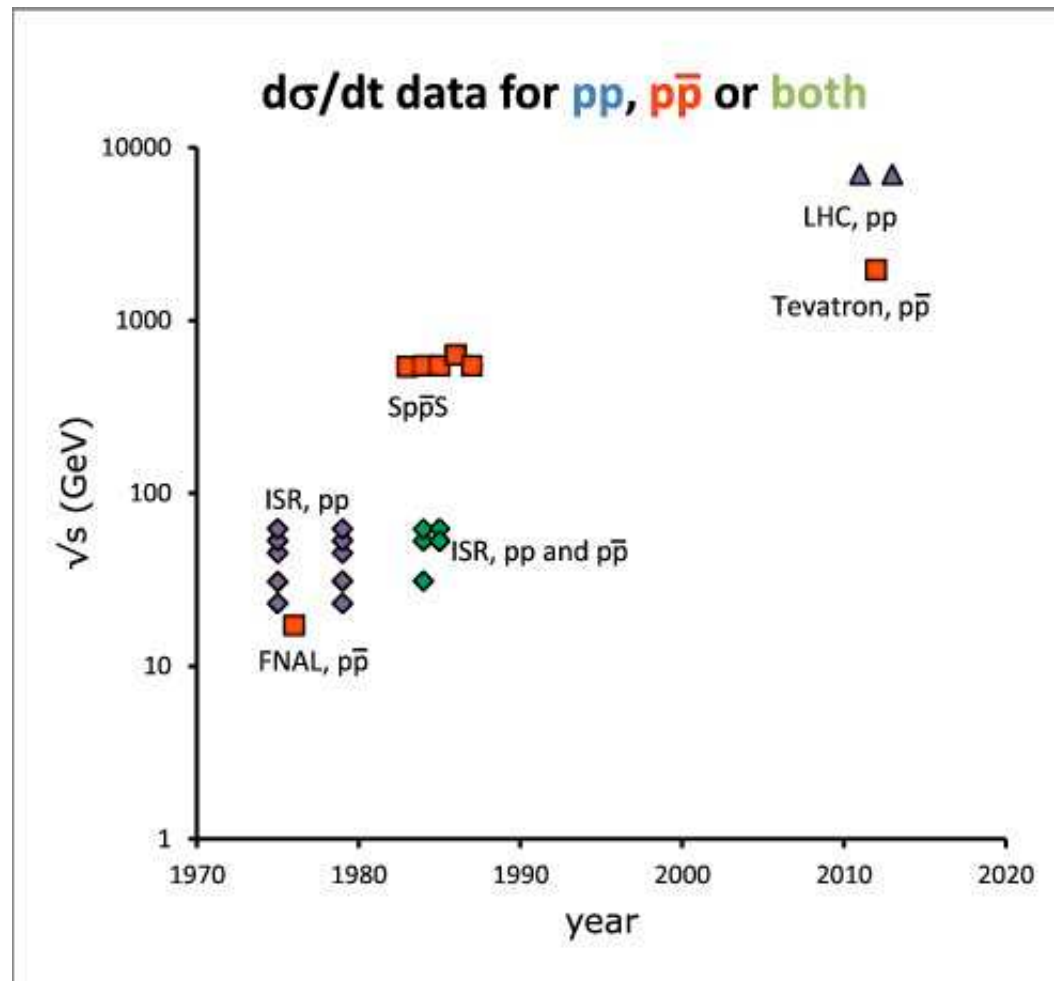
$$\mathcal{A}_{pp}^{\bar{p}p} = \mathcal{A}_{even} \pm \mathcal{A}_{odd}$$

At higher energies (LHC) secondary Reggeons are negligible:

$$\mathcal{A}^{\bar{p}p} - \mathcal{A}^{pp} = \mathcal{A}_{Odd}$$

Introduction

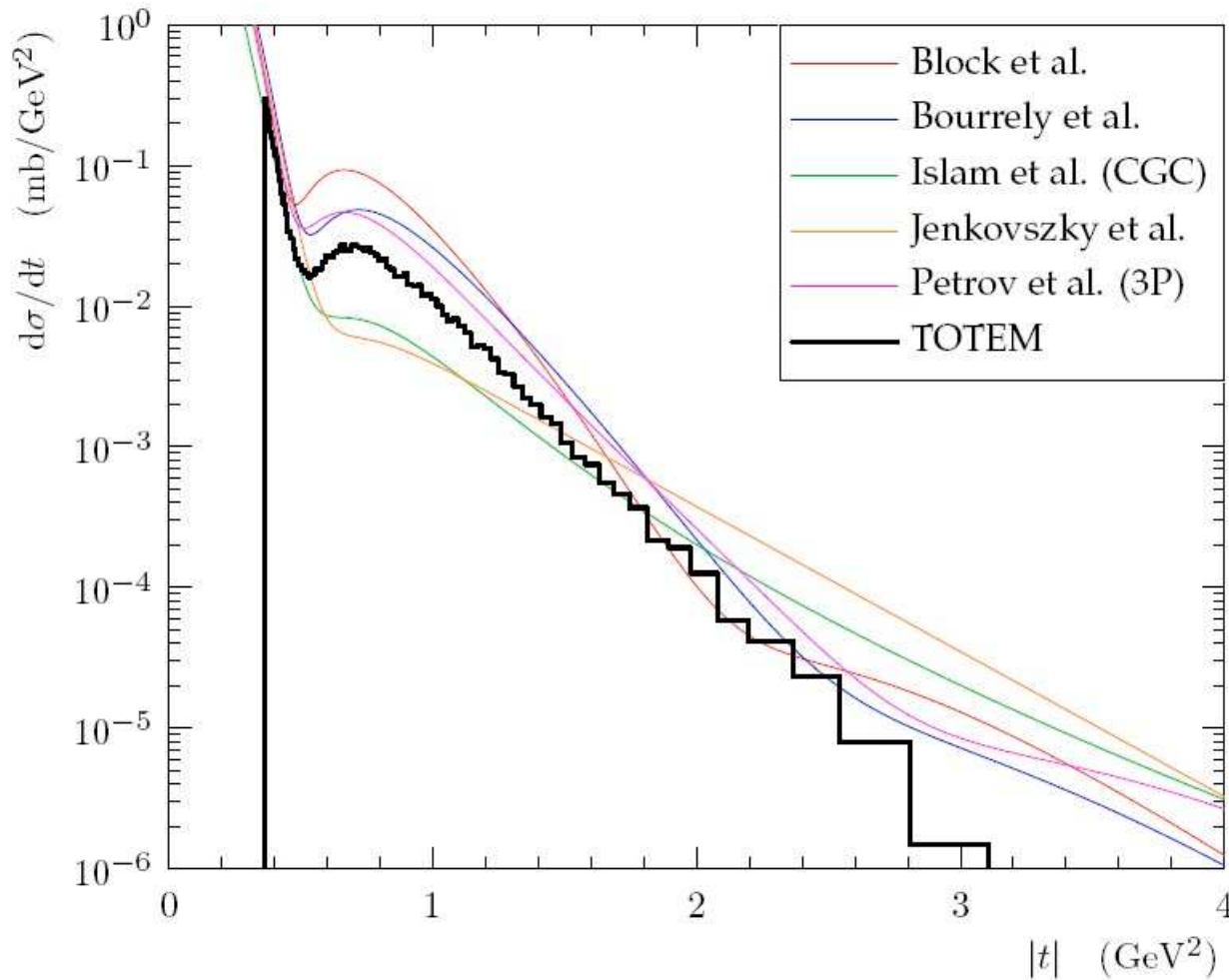
Problem: available elastic $p\bar{p}$ and pp data do not match in energy



Possible solution:
interpolation of scattering
amplitudes in energy

Introduction

Model describing the elastic pp and pp scattering data is needed:

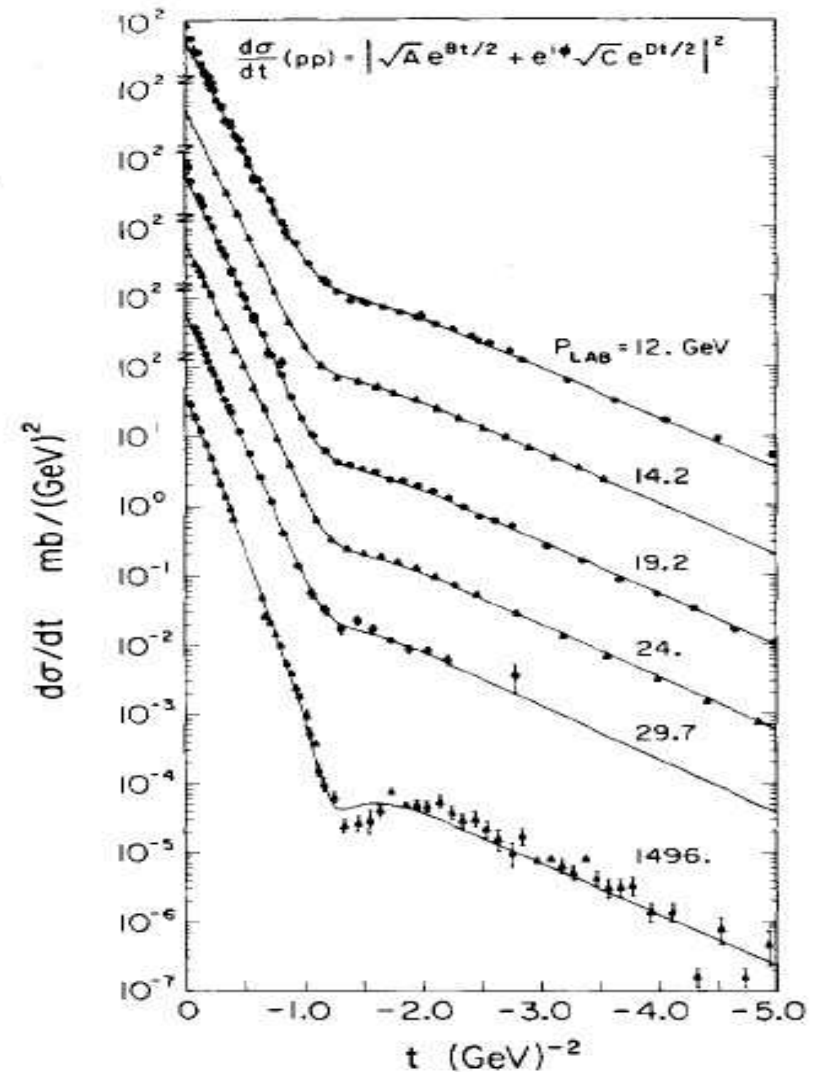


(Plot taken from earlier TOTEM presentations)

Introduction

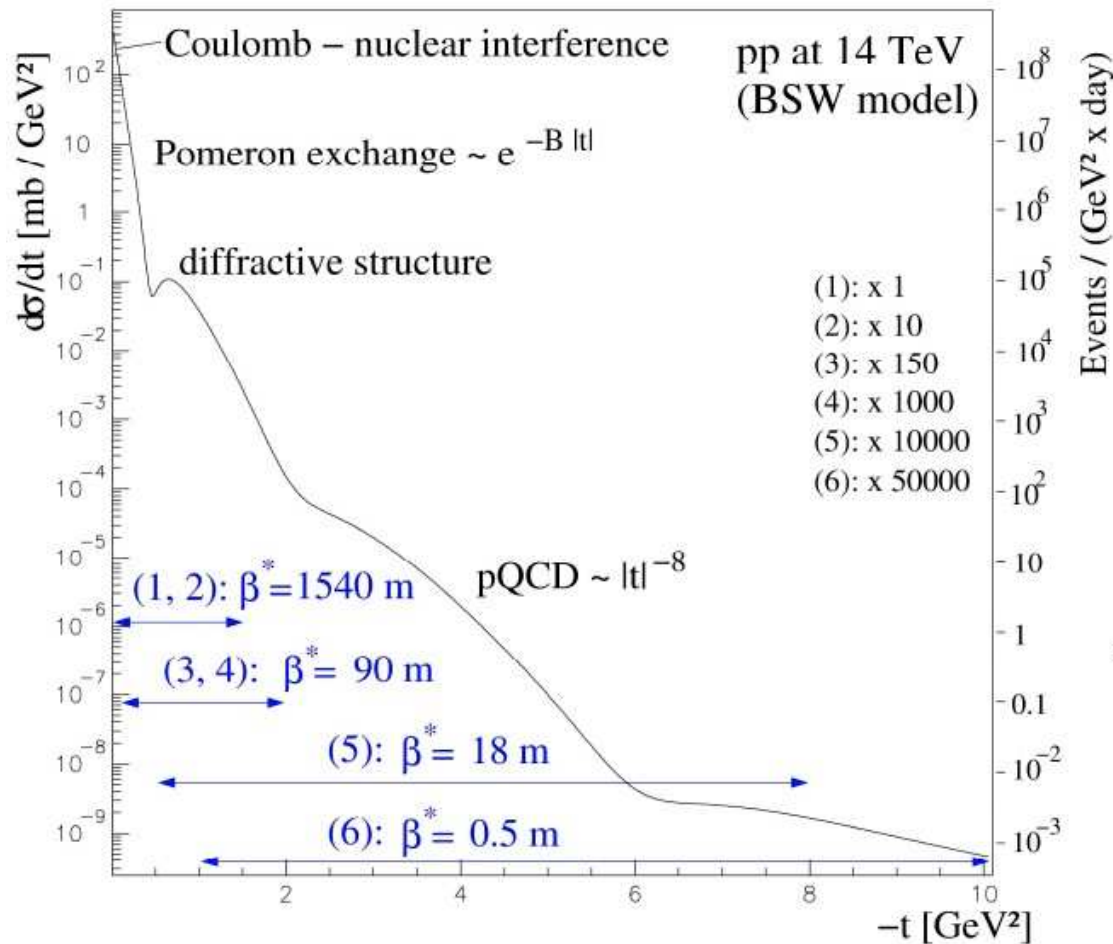
A simple and quasi-successful parametrization is an empirical one of Phillips and Barger for elastic pp scattering with two exponentials:

R. J. N. Phillips and V. D. Barger, Phys. Lett. 46B, 412 (1973)



Introduction

The applicable range in t for the PB ansatz is limited:



Possible solution for low $-t$:
improving parametrization



Fagundes et al., Phys. Rev. D 88,
094019 (2013)

(Plot taken from Risto
Orava's presentations)

The generalized PB Model

Keep the original PB ansatz introducing s dependence of the model parameters in the elastic scattering amplitude:

$$\mathcal{A}(s, t) = i[\sqrt{A} \exp(Bt/2) + \exp(i\phi(s))\sqrt{C} \exp(Dt/2)]$$

The observables:

$$\frac{d\sigma}{dt} = \pi |\mathcal{A}(t)|^2 = \pi [Ae^{Bt} + Ce^{Dt} + 2\sqrt{A}\sqrt{C}e^{(B+D)t/2} \cos \phi]$$

$$\sigma_{tot} = 4\pi \Im A(t=0) = 4\pi [\sqrt{A} + \sqrt{C} \cos \phi]$$

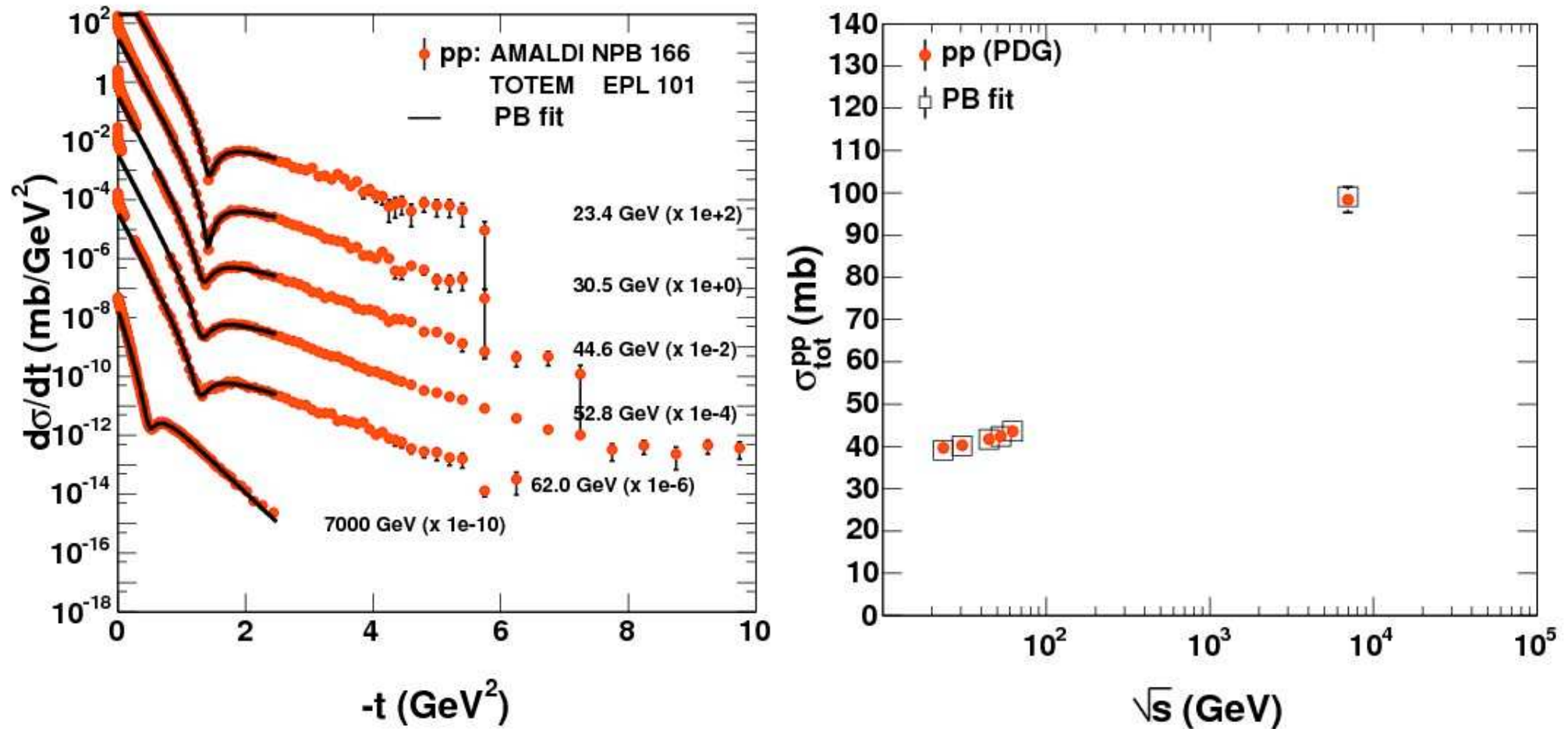
Fitting the model to data

Imposed quality fit criterias:

- Simultaneous fits to elastic and σ_{tot} data for each energy
- Only fits with good χ^2 are accepted
- Setting the fitted $-t$ range from 0.35 GeV^2 to 2.5 GeV^2
- Reconstructing σ_{tot} in the whole available energy range

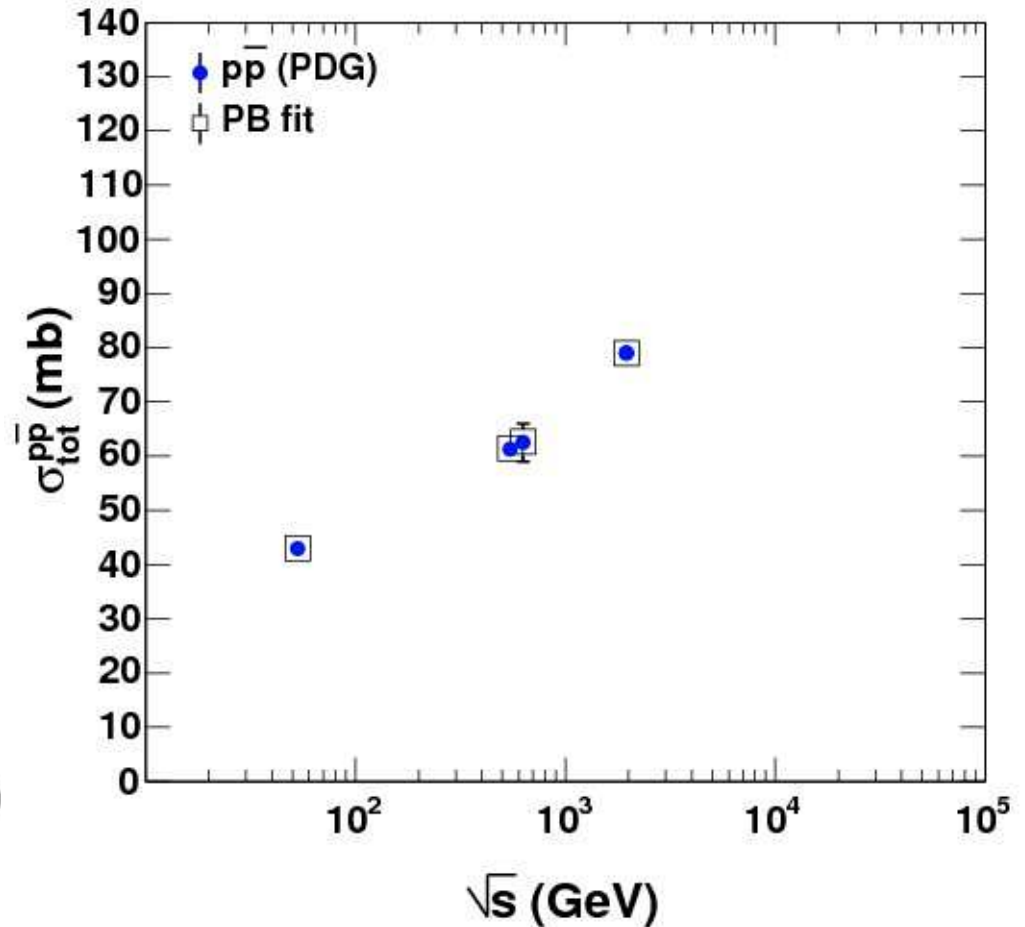
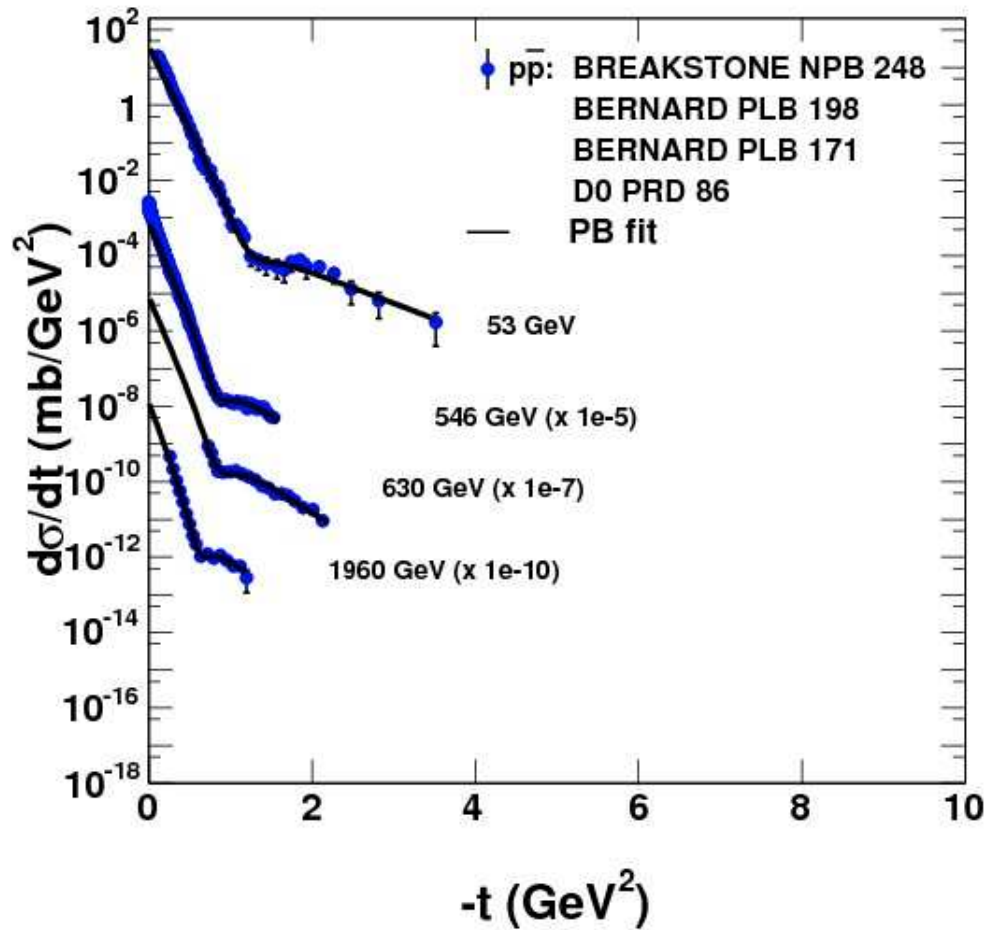
Fitting the model to data

Simultaneous fits to elastic and σ_{tot} **pp** data for each energy:



Fitting the model to data

Simultaneous fits to elastic and σ_{tot} $p\bar{p}$ data for each energy:



Fitting the model to data

Model parameter fit results

Energy (GeV)	\sqrt{A}	B	\sqrt{C}	D	$\cos(\phi)$	χ^2/NDF
23.4	$3.13 \pm 0.6\%$	$8.66 \pm 0.4\%$	$0.019 \pm 8.3\%$	$1.54 \pm 5.1\%$	$-0.97 \pm 0.3\%$	1.6
30.5	$3.21 \pm 0.2\%$	$8.95 \pm 0.3\%$	$0.014 \pm 7.4\%$	$1.28 \pm 5.6\%$	$-0.98 \pm 0.2\%$	1.1
44.6	$3.33 \pm 0.7\%$	$9.32 \pm 0.5\%$	$0.017 \pm 8.0\%$	$1.45 \pm 5.3\%$	$-0.93 \pm 0.8\%$	1.7
52.8	$3.38 \pm 0.3\%$	$9.44 \pm 0.6\%$	$0.017 \pm 7.6\%$	$1.43 \pm 5.0\%$	$-0.92 \pm 0.9\%$	1.1
62.0	$3.49 \pm 0.5\%$	$9.66 \pm 0.6\%$	$0.018 \pm 9.9\%$	$1.53 \pm 6.3\%$	$-0.92 \pm 1.6\%$	1.5
7000.0	$8.51 \pm 1.6\%$	$15.05 \pm 0.8\%$	$0.670 \pm 2.3\%$	$4.71 \pm 0.8\%$	$-0.93 \pm 0.3\%$	1.4

Energy (GeV)	\sqrt{A}	B	\sqrt{C}	D	$\cos(\phi)$	χ^2/NDF
63	$3.43 \pm 1.1\%$	$10.07 \pm 1.3\%$	$0.022 \pm 30.8\%$	$1.90 \pm 14.8\%$	$-0.60 \pm 22.7\%$	0.7
546	$5.06 \pm 1.2\%$	$11.25 \pm 1.3\%$	$0.204 \pm 21.0\%$	$3.55 \pm 8.6\%$	$-0.86 \pm 2.7\%$	0.6
630	$5.13 \pm 3.9\%$	$11.26 \pm 3.7\%$	$0.176 \pm 26.6\%$	$3.23 \pm 9.6\%$	$-0.81 \pm 7.9\%$	0.5
1960	$6.85 \pm 3.7\%$	$12.46 \pm 3.3\%$	$0.629 \pm 41.6\%$	$4.69 \pm 15.4\%$	$-0.90 \pm 3.6\%$	0.4

Fitting the model to data

Specifying (Regge type) s dependent model parameters:

$$\sqrt{A} \rightarrow \sqrt{A(s)} = a_1 s^{-\epsilon_{a1}} + a_2 s^{\epsilon_{a2}}, \quad \sqrt{C} \rightarrow \sqrt{C(s)} = c s^{\epsilon_c}$$

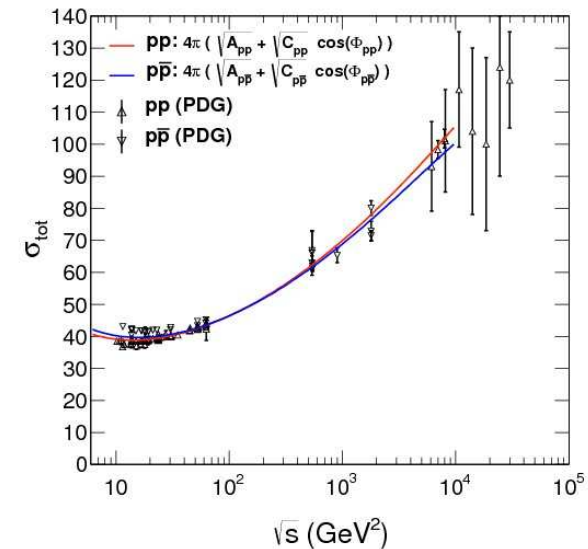
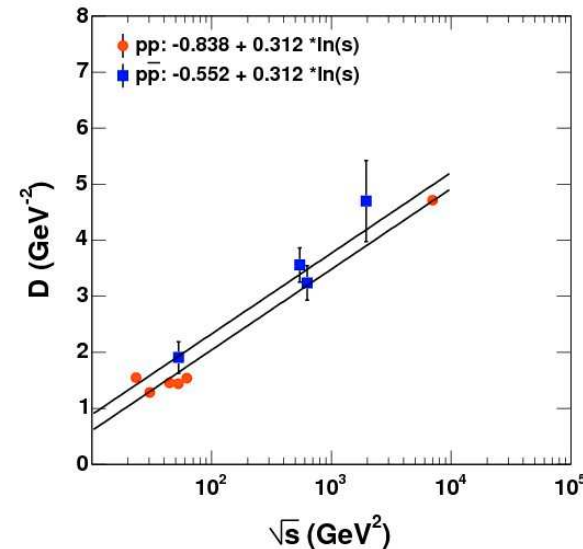
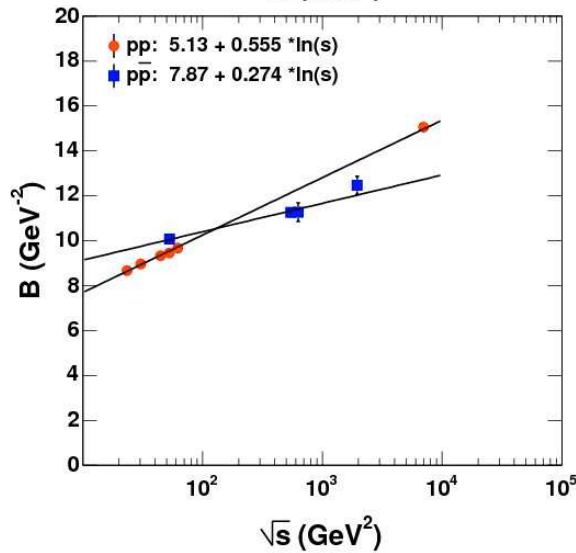
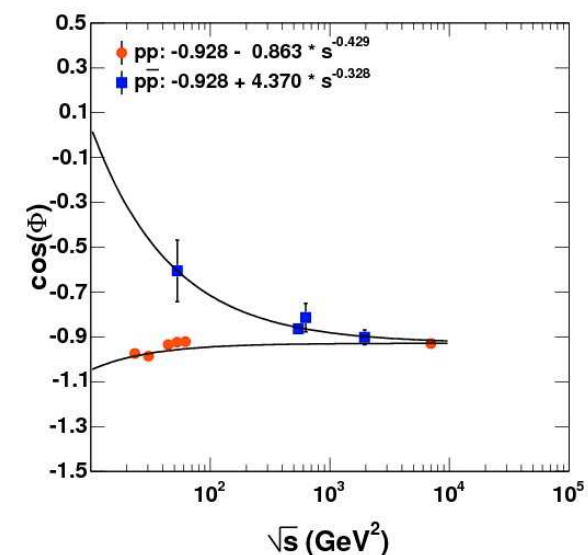
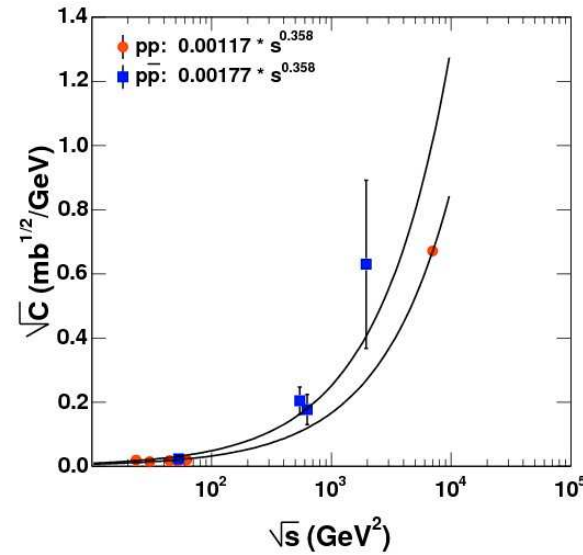
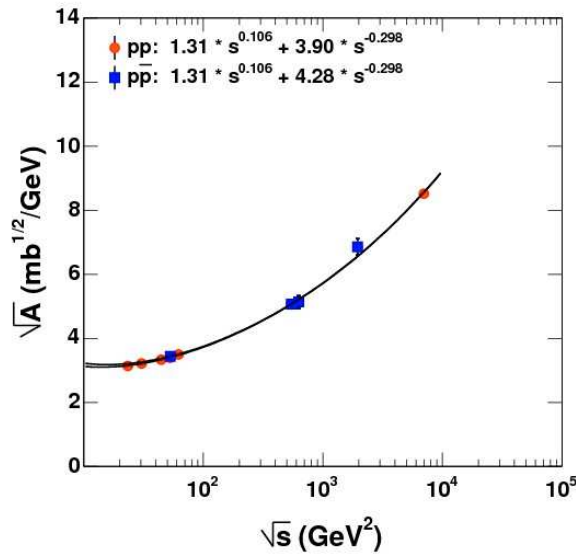
$$B \rightarrow B(s) = b_0 + b_1 \ln(s/s_0), \quad D \rightarrow D(s) = d_0 + d_1 \ln(s/s_0)$$

$$\cos(\phi(s)) = k_0 + k_1 s^{-\epsilon_{cos}}$$

The s dependent differential cross section:

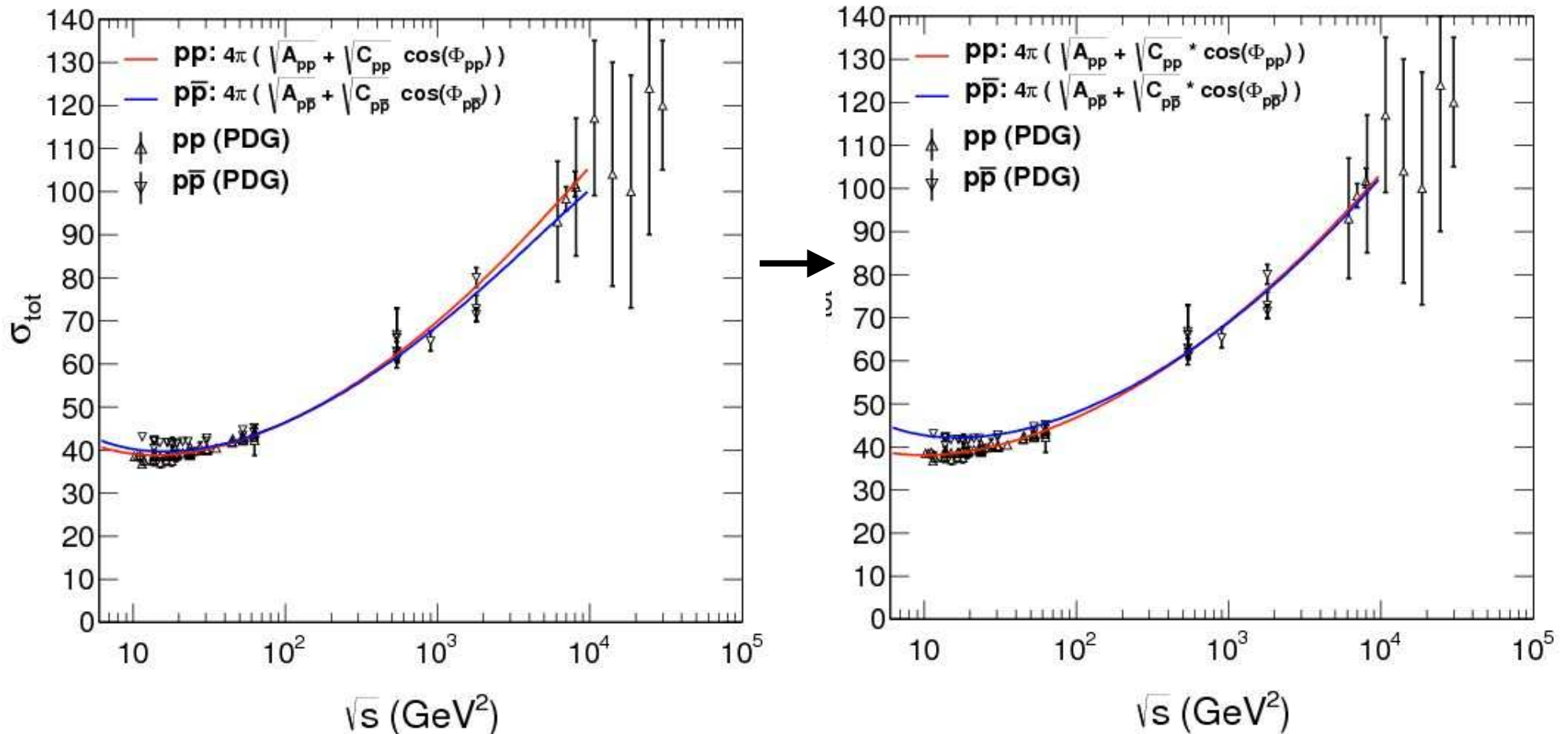
$$\frac{d\sigma}{dt} = \pi |\mathcal{A}(t)|^2 = \pi [A e^{Bt} + C e^{Dt} + 2\sqrt{A}\sqrt{C} e^{(B+D)t/2} \cos \phi]$$

Fitting the model to data

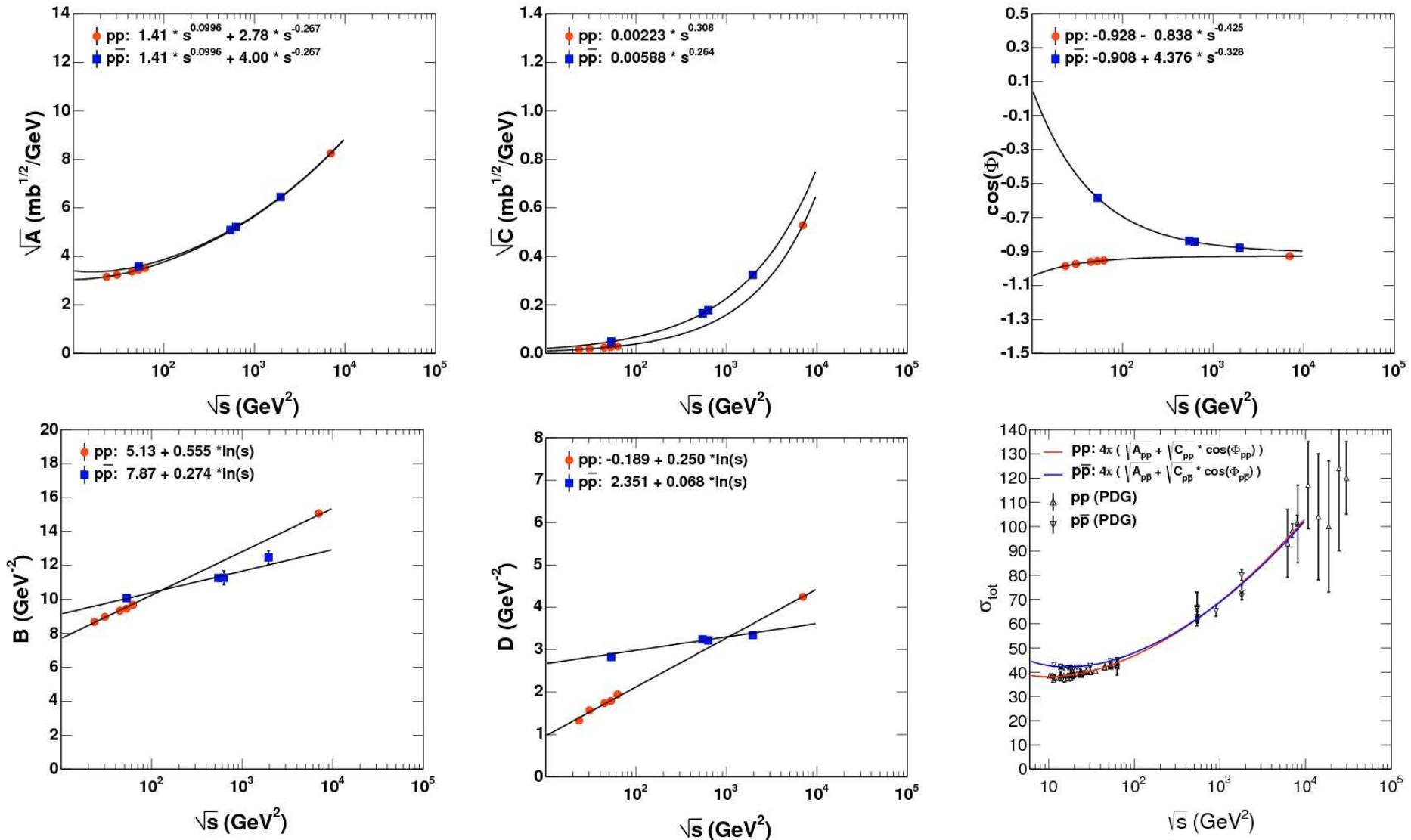


Fitting the model to data

Second step: tuning model parameters to fit σ_{tot} data for the whole energy range with data:



Fitting the model to data



Fitting the model to data

The final extracted s dependent model parameters:

$$\sqrt{A_{pp}(s)} = 1.41s^{0.0966} + 2.78s^{-0.267},$$

$$\sqrt{A_{p\bar{p}}(s)} = 1.41s^{0.0996} + 4.00s^{-0.267},$$

$$\sqrt{C_{pp}(s)} = 0.00223s^{0.308},$$

$$\sqrt{C_{p\bar{p}}(s)} = 0.00588s^{0.264},$$

$$B_{pp}(s) = 4.86 + 0.586 \ln s,$$

$$B_{p\bar{p}}(s) = 6.55 + 0.398 \ln s,$$

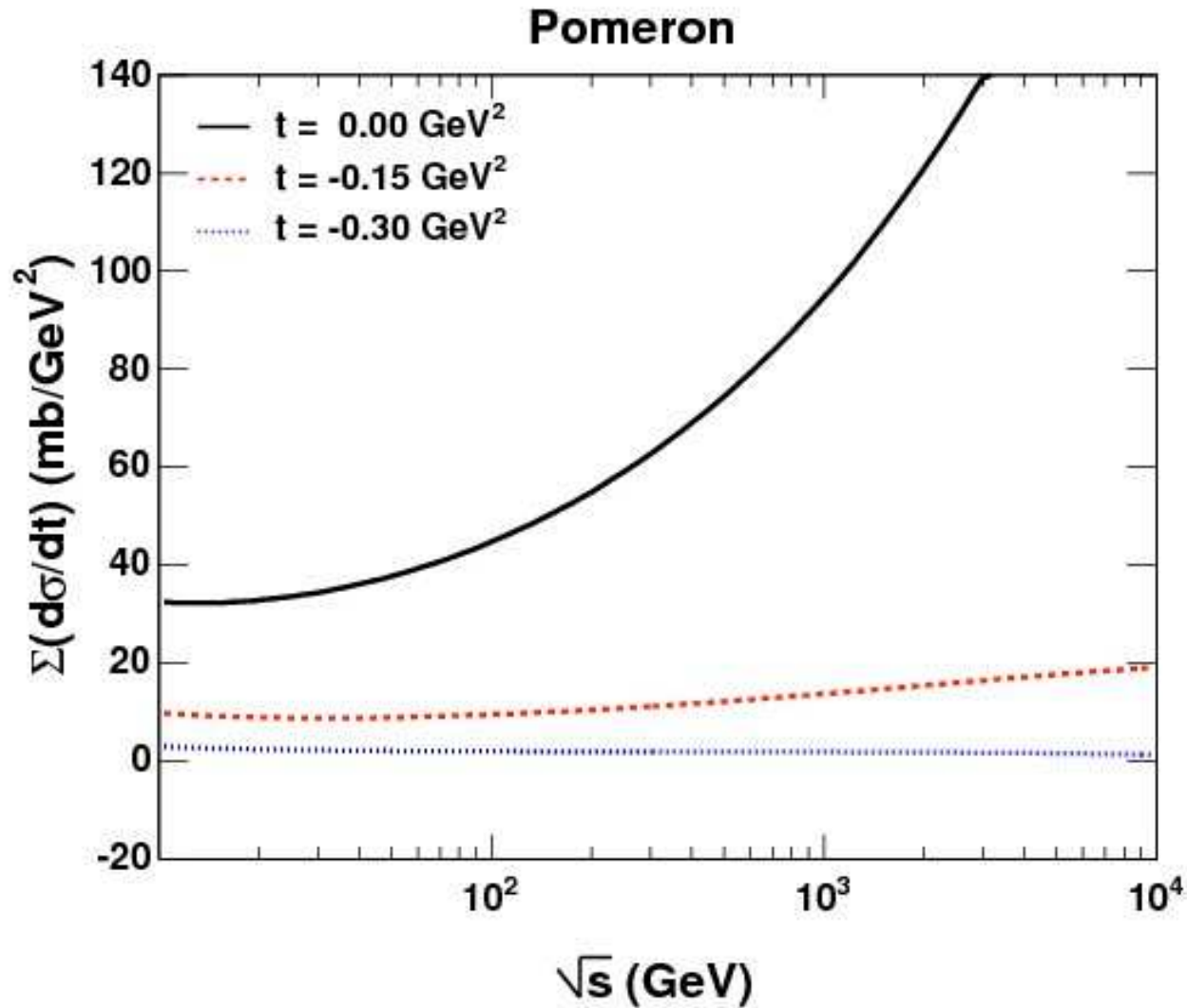
$$D_{pp}(s) = -0.189 + 0.250 \ln s.$$

$$D_{p\bar{p}}(s) = 2.351 + 0.068 \ln s,$$

$$\cos(\phi_{pp}(s)) = -0.928 - 0.838s^{-0.425}.$$

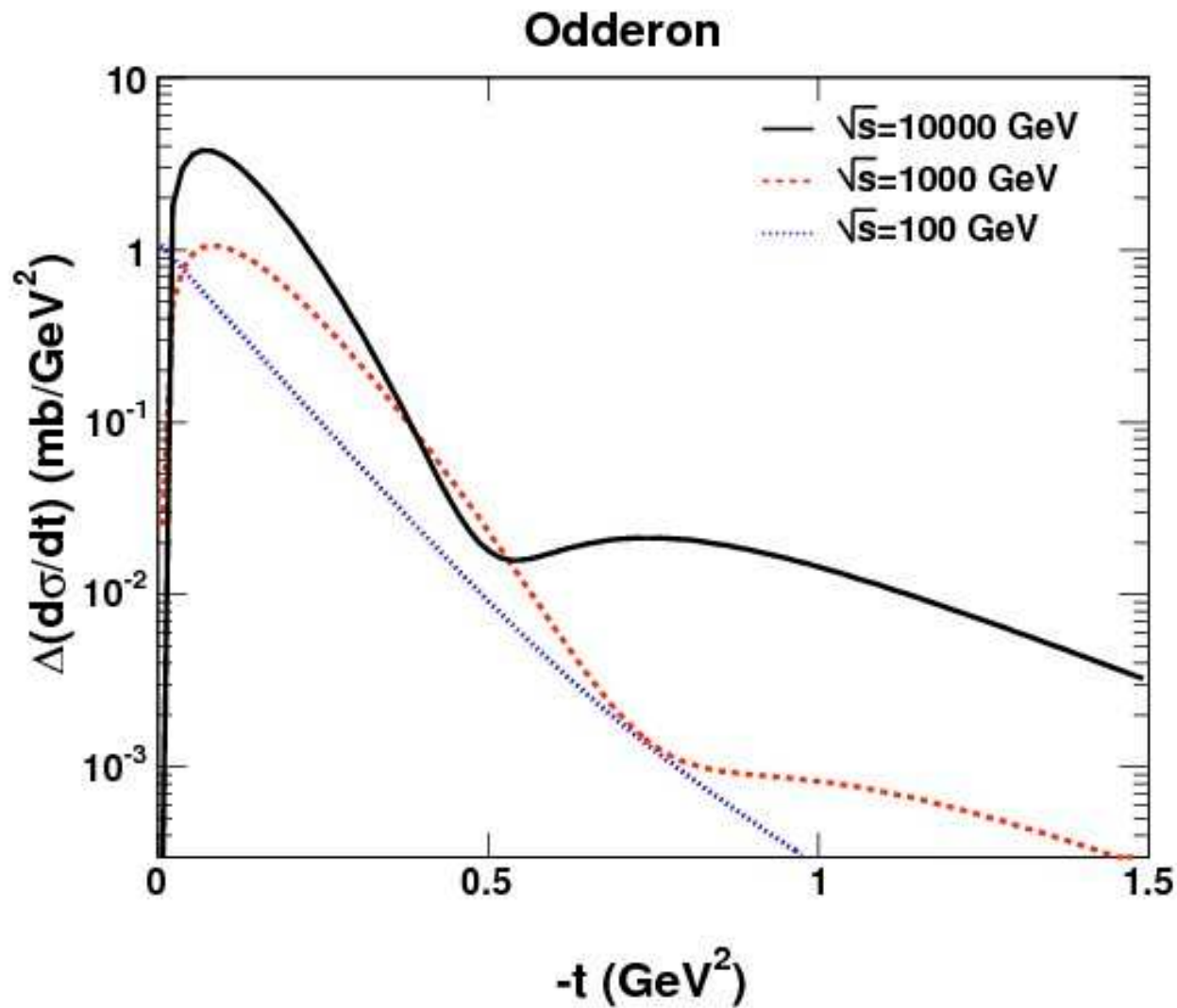
$$\cos(\phi_{p\bar{p}}(s)) = -0.908 + 4.376s^{-0.328}.$$

Results: the Pomeron and the Odderon



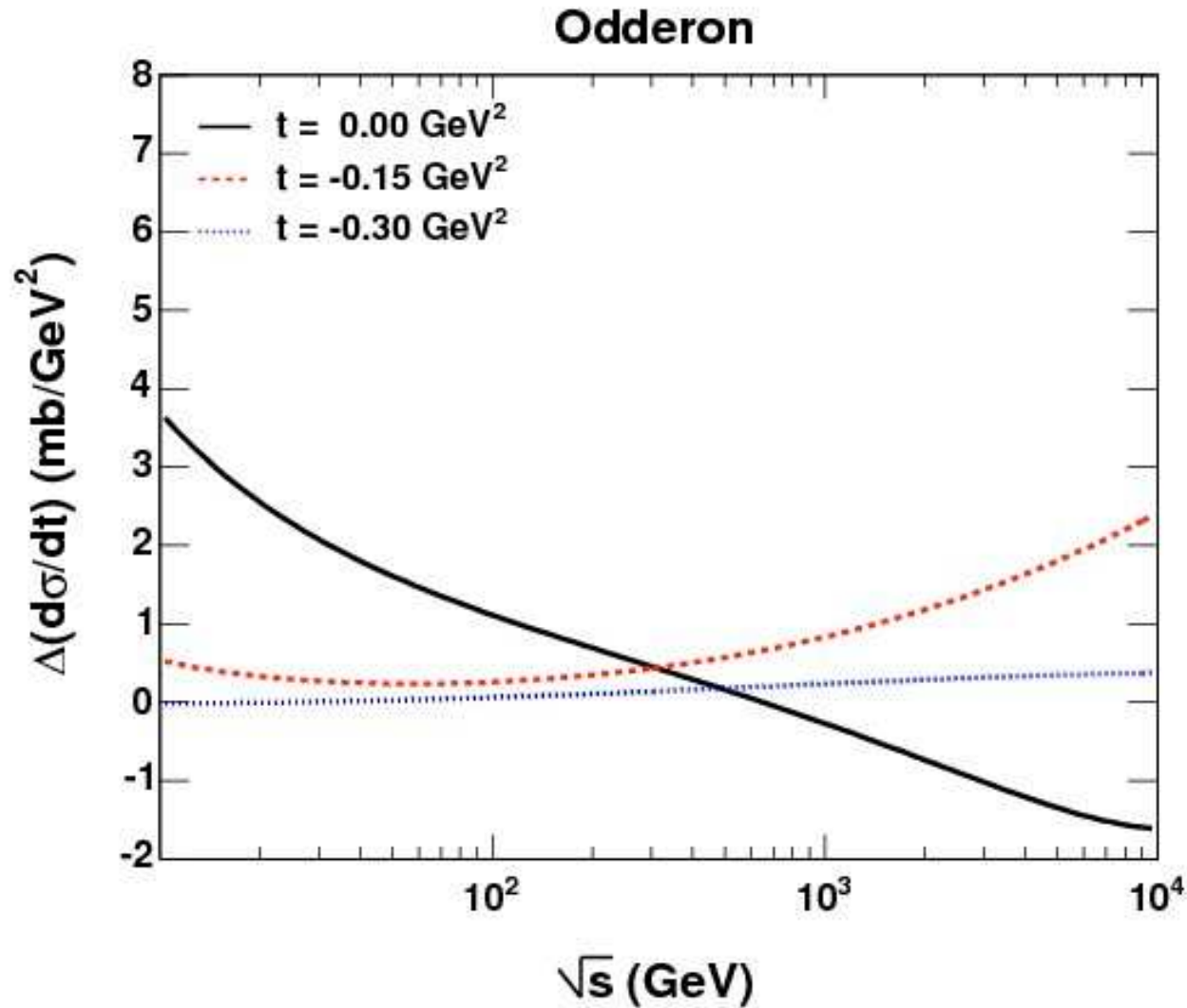
$$|\mathcal{A}|_{\bar{p}p}^2 + |\mathcal{A}|_{pp}^2 = \Sigma_{Pom}$$

Results: the Pomeron and the Odderon



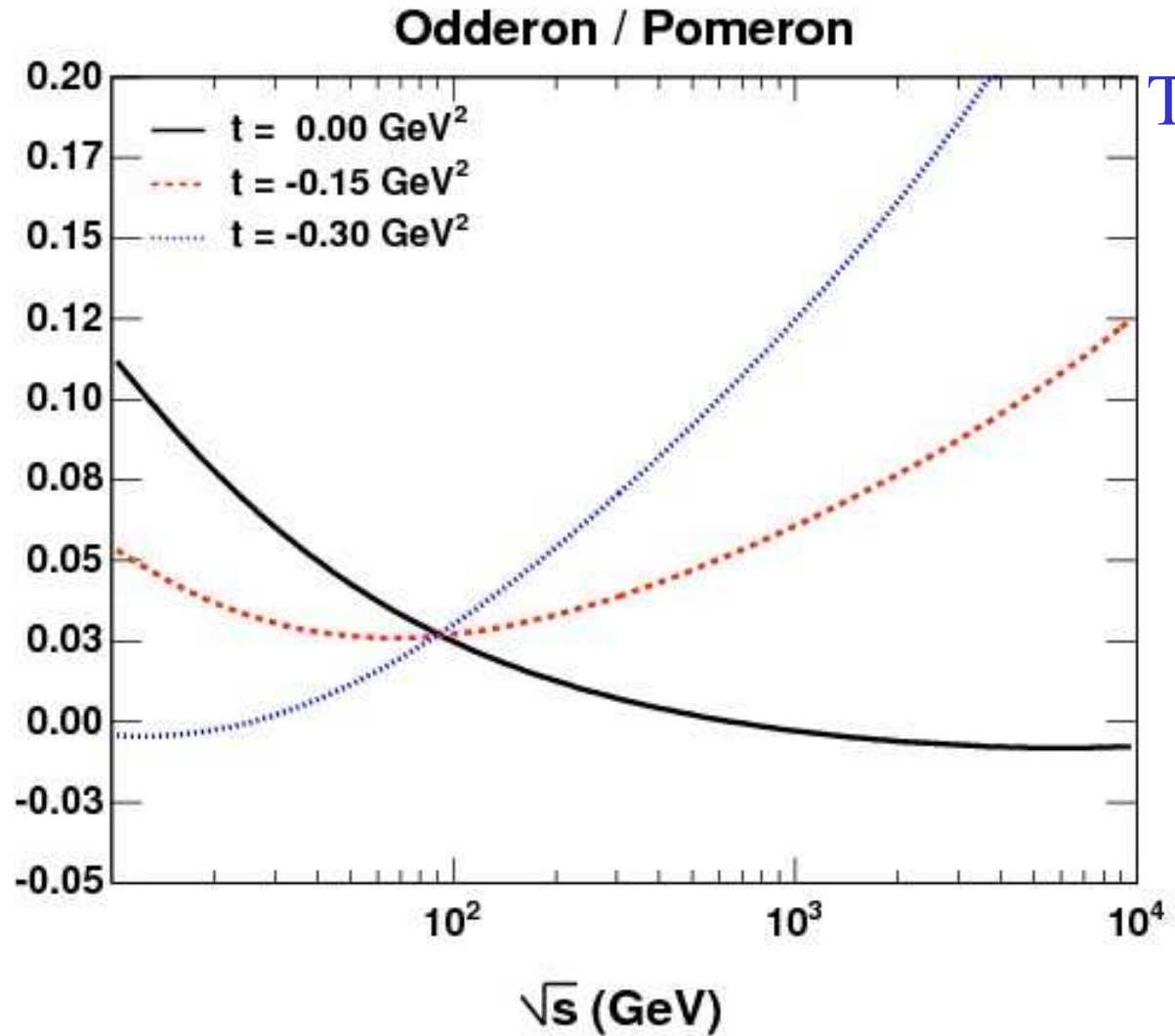
$$|\mathcal{A}|_{\bar{p}p}^2 - |\mathcal{A}|_{pp}^2 = \Delta_{Odd}$$

Results: the Pomeron and the Odderon



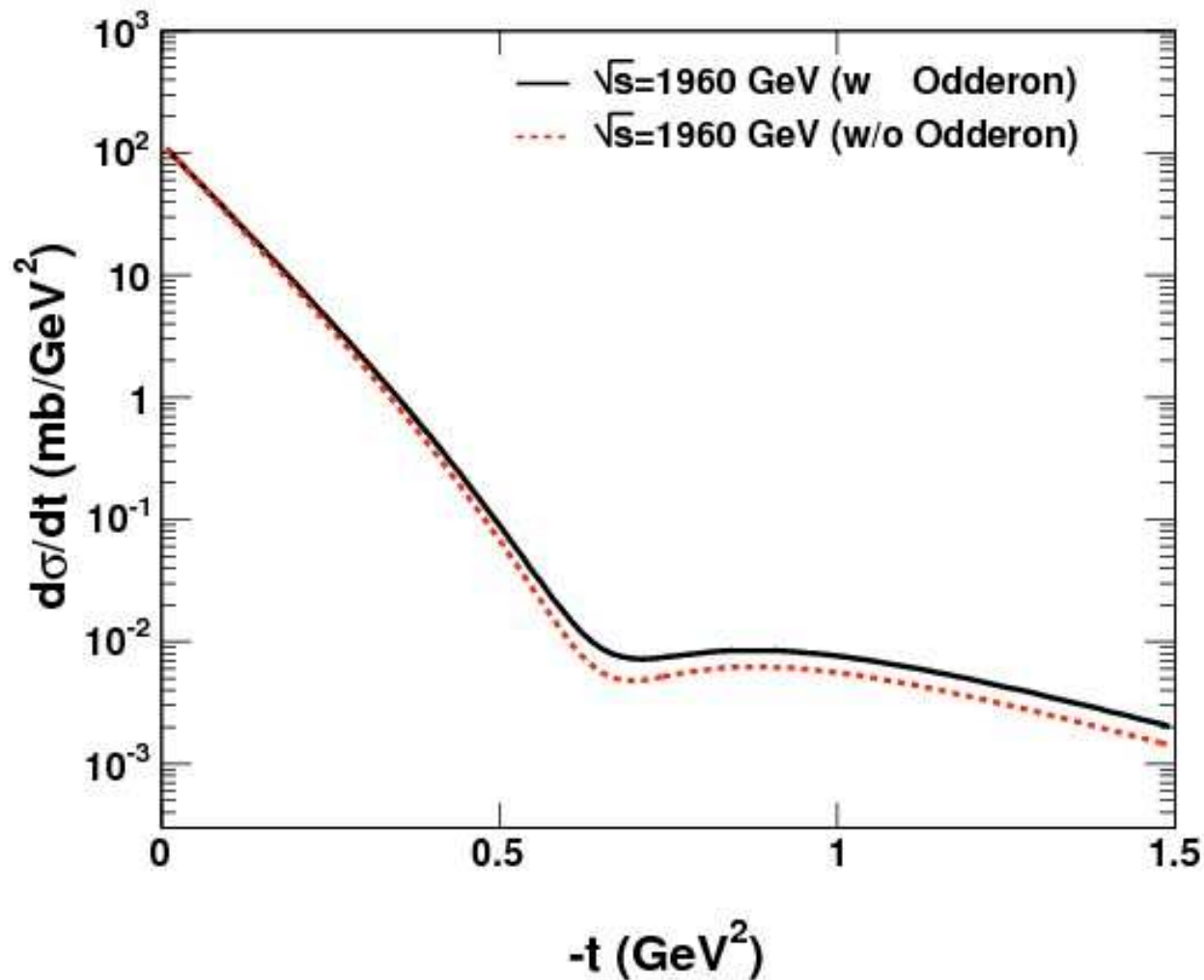
$$|\mathcal{A}|_{\bar{p}p}^2 - |\mathcal{A}|_{pp}^2 = \Delta_{Odd}$$

Results: the Pomeron and the Odderon



The Odderon/Pomeron ratio

Results: the Pomeron and the Odderon



Reflections on earlier remarks:

Differential cross sections with and without Odderon are plotted (left side)



The dip-bump region is not coupled to Odderon exclusively

Outlook

Next steps:

- Include low and high $|t|$ data in the fits (its a collaboration with Fagundes et al.) by improving the model.
- The phase (ϕ) parameter is expected to be t dependant.
- Estimate better the contributions of secondary Reggeons.
-

Conclusions

pp and pp elastic and σ_{tot} data were successfully fitted by a model based on the empirical Phillips-Barger expression.

The (s, t) functional form of the Pomerons and the Odderons were extracted.

The Odderons and Pomerons were studied, plotted and compared in function of the collision and transferred energies.