

Fast Generation of Covariance Matrices for Weak Lensing

[Sgier, Réfrégier, Amara, Nicola 2018 \(1801.05745\)](#)

Raphaël Sgier

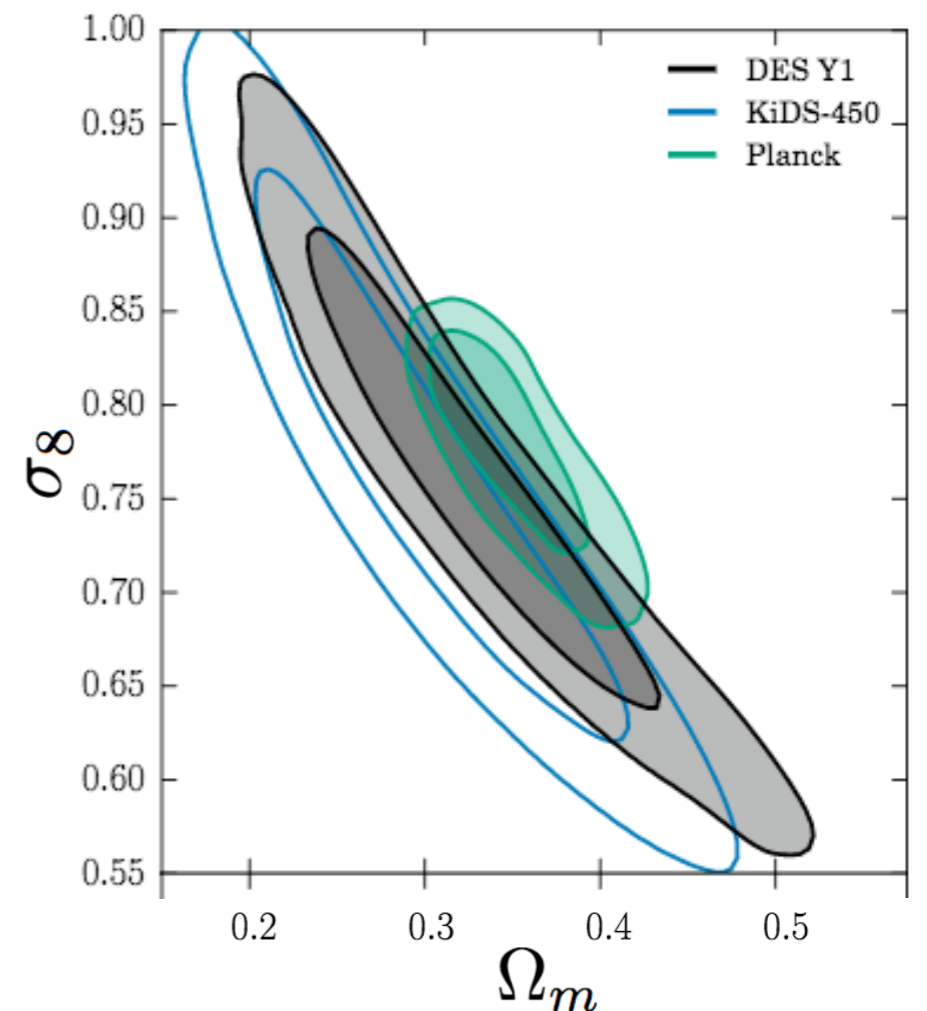
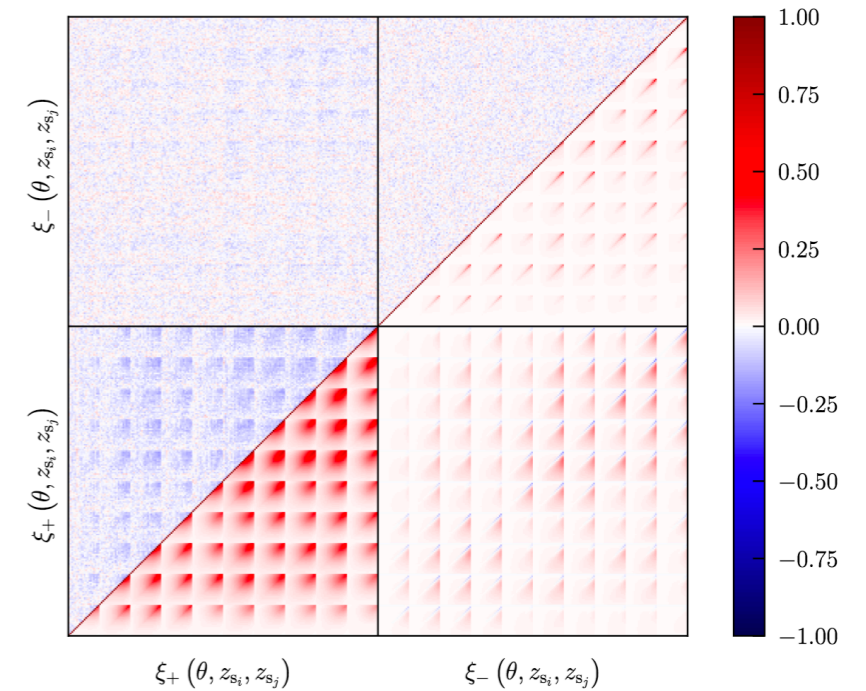
Institute for Particle Physics and Astrophysics

Motivation

- Interpretation of LSS data.

$$\mathcal{L}(D|\theta) \propto e^{-\frac{1}{2}(X^D - X^M)^T \text{cov}^{-1}(X^D - X^M)}$$

- large ensemble of **N-Body simulations** needed for a well-converged covariance matrix.



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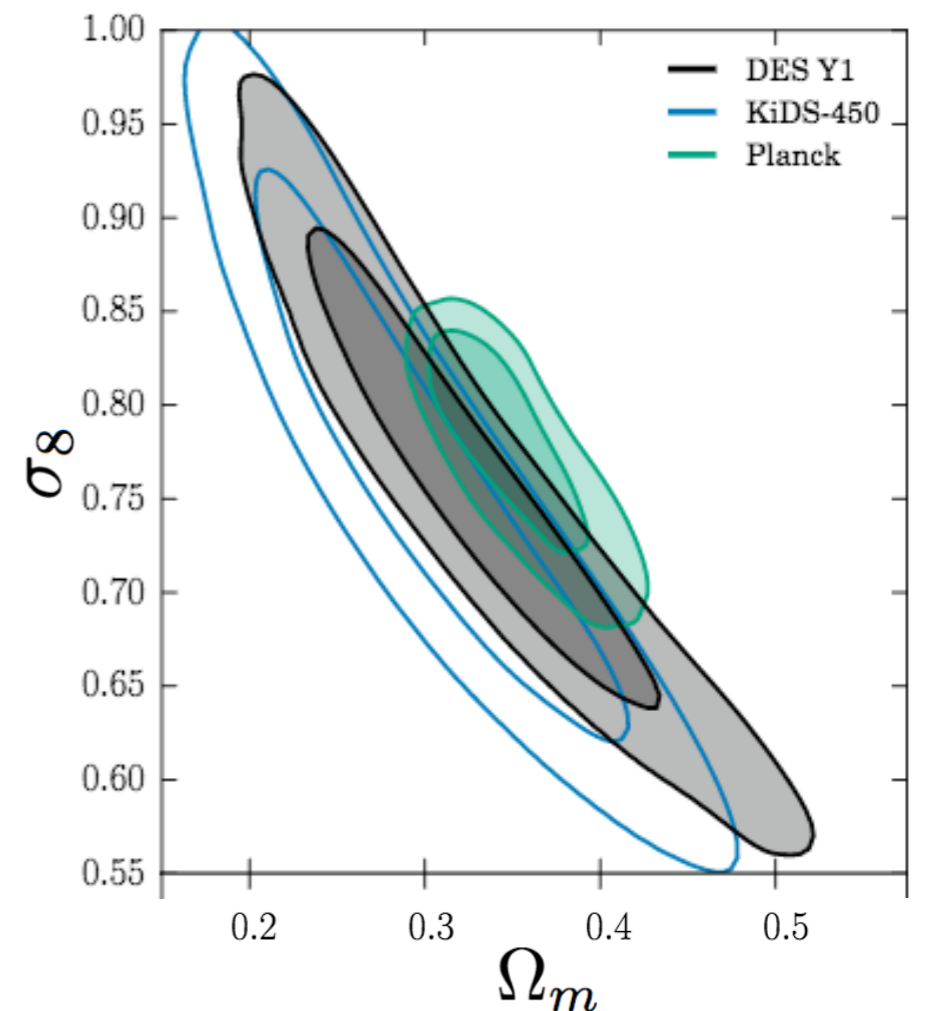
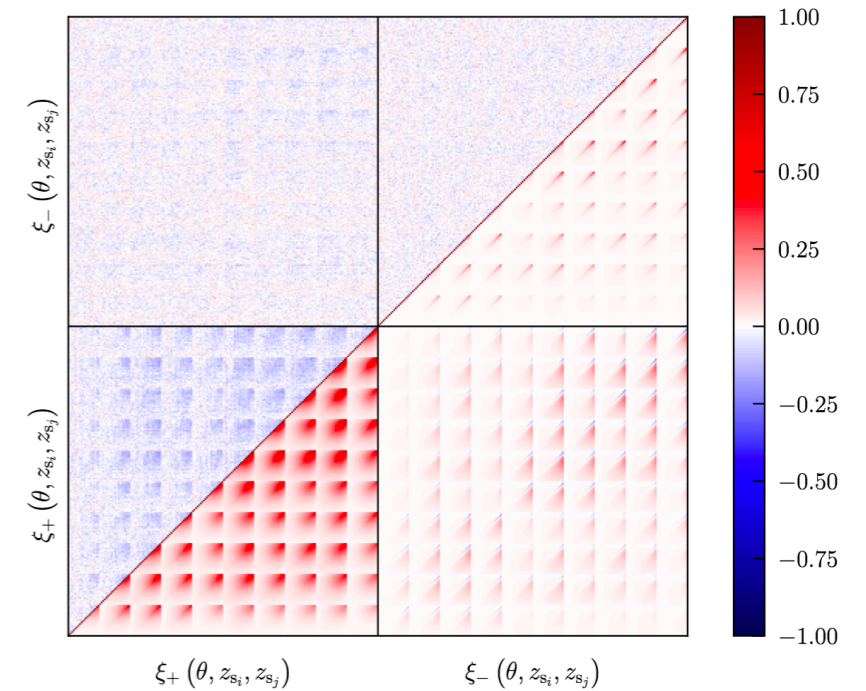
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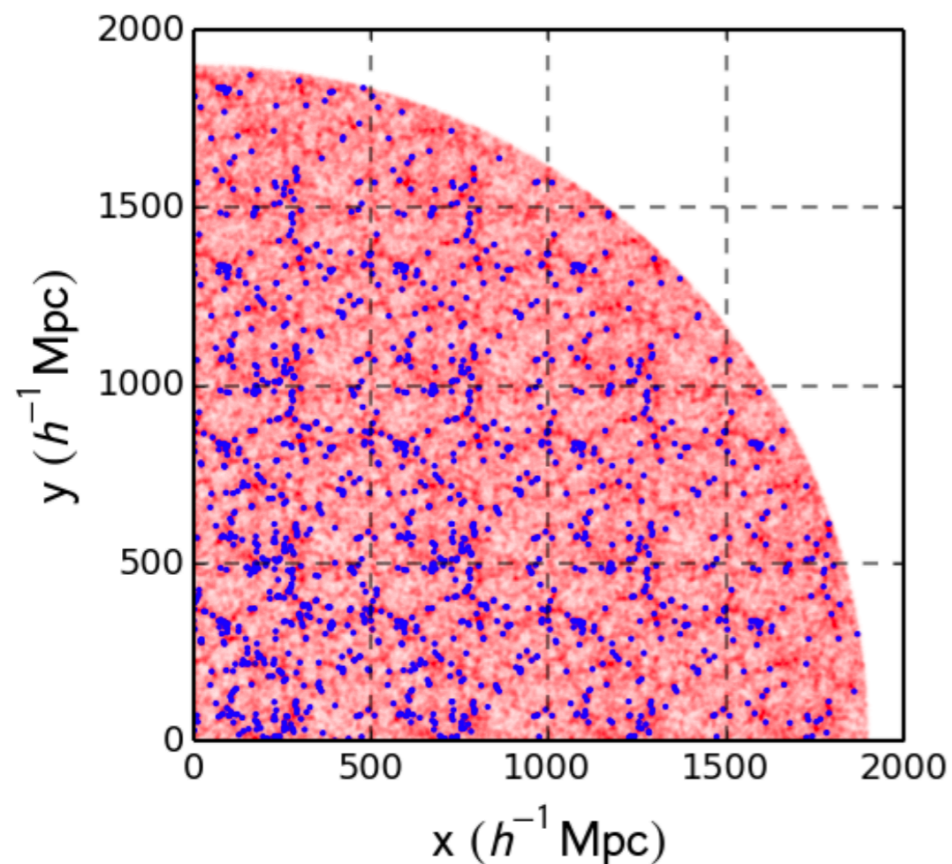


Computational Power ⚡ Resolution



N-Body Simulations

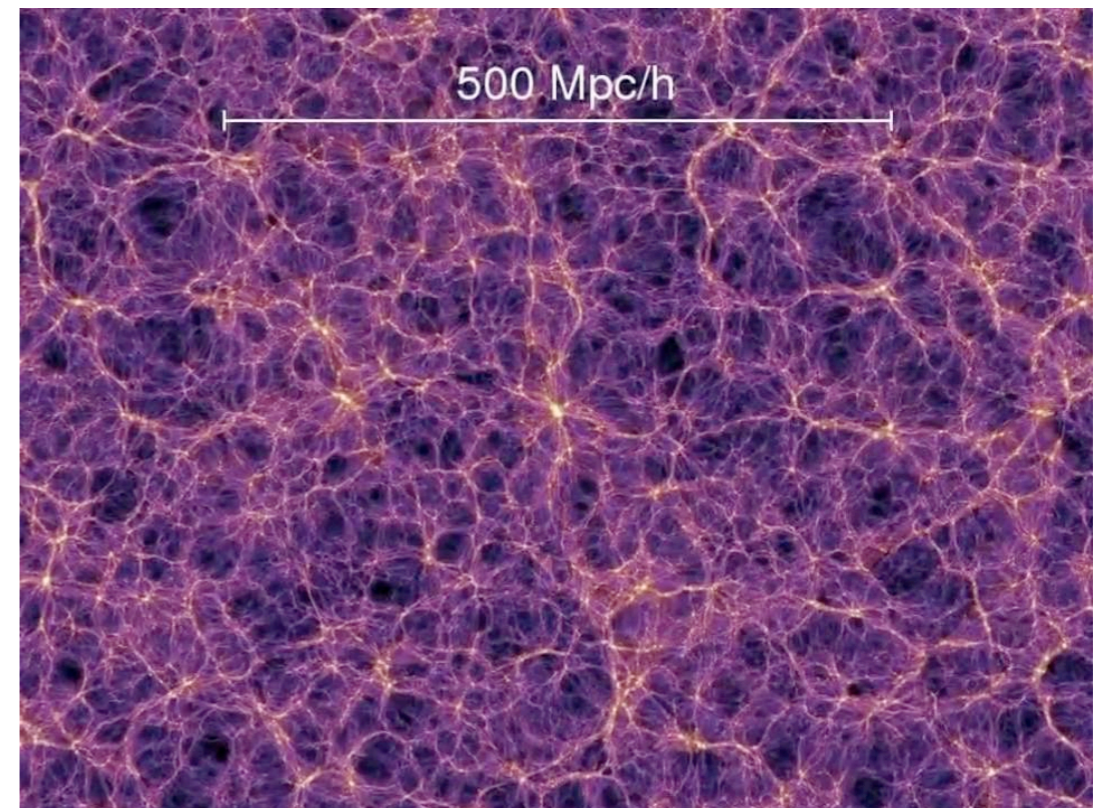
Mass resolution: $m = \frac{V}{N} \cdot \rho_{\text{crit}} \cdot \Omega_{\text{m}}$



L-PICOLA Simulation code

Howlett et al. 2015 (1506.03737)

$$N = 2160^3 \quad V = 500 \text{ Mpc}/h$$

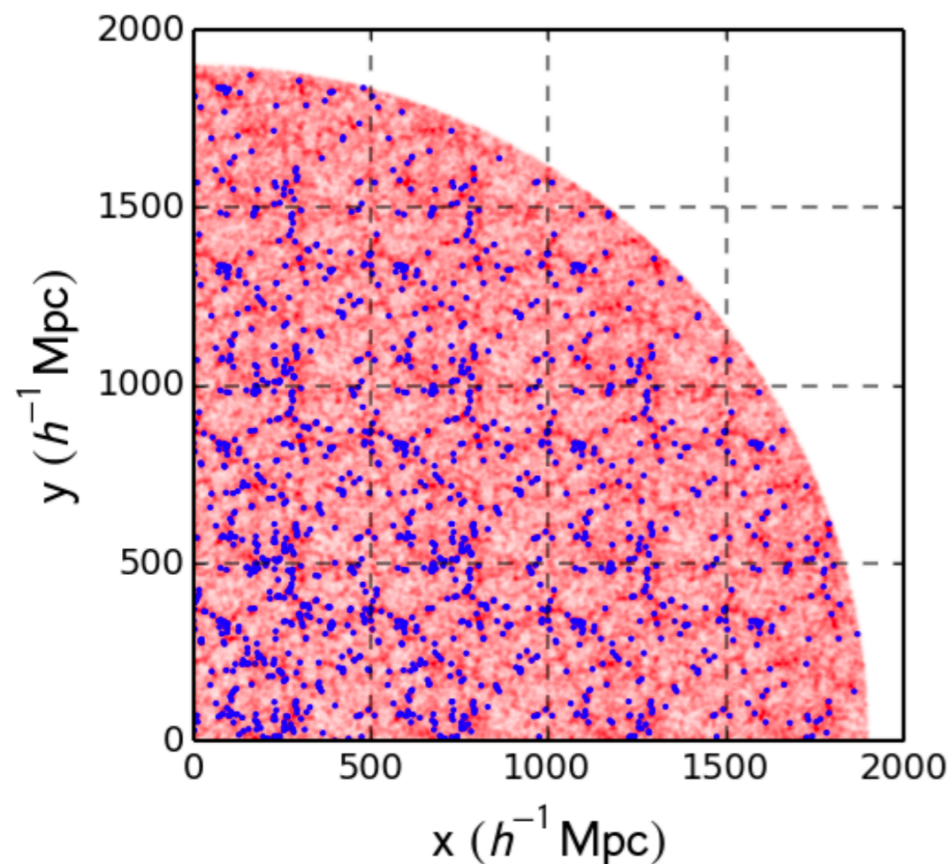


Millennium Simulation (MPA Garching)

N-Body Simulations

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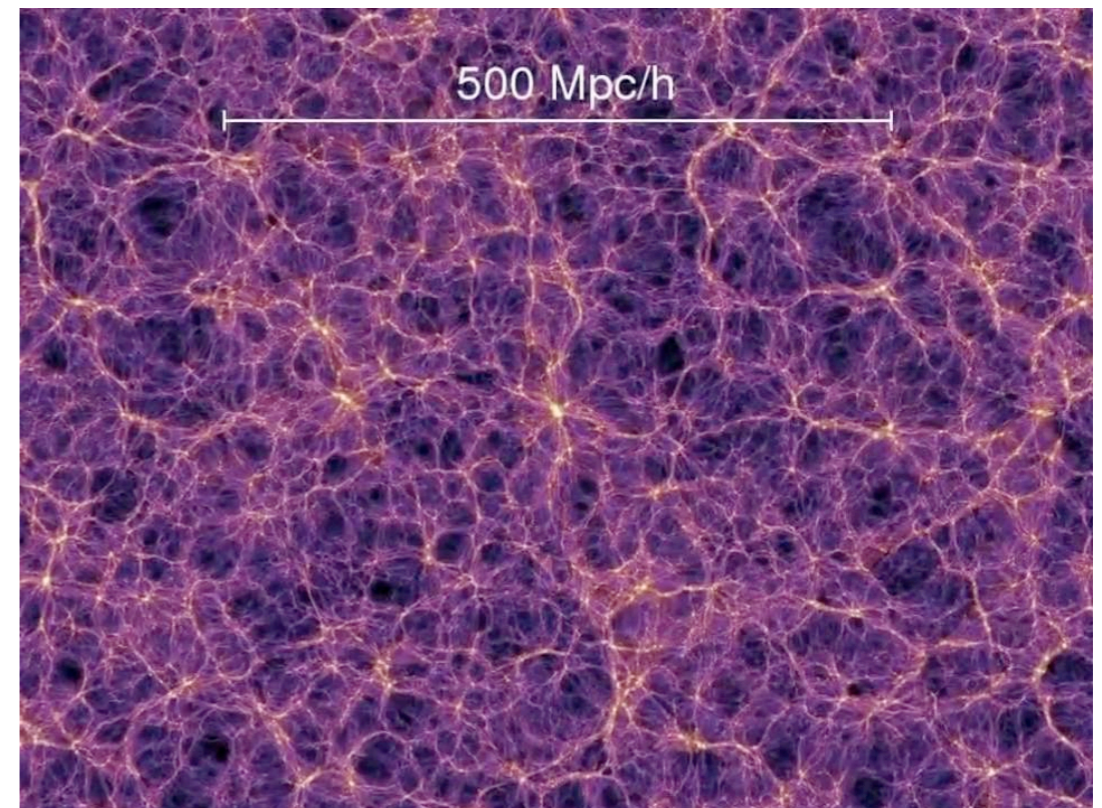
→ we use large V to avoid replications and avoid dealing with SSC.



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Millennium Simulation (MPA Garching)

L-PICOLA

N-Body code

- ⊕ recovers non-linear regime
- ⊖ computationally expensive

Lagrangian Perturbation Theory

- ⊕ exact results on large scales
- ⊖ PT breaks down at k_{NL}

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COLA

Tassev, Zaldarriaga,
Eisenstein 2013 (1301.0322)

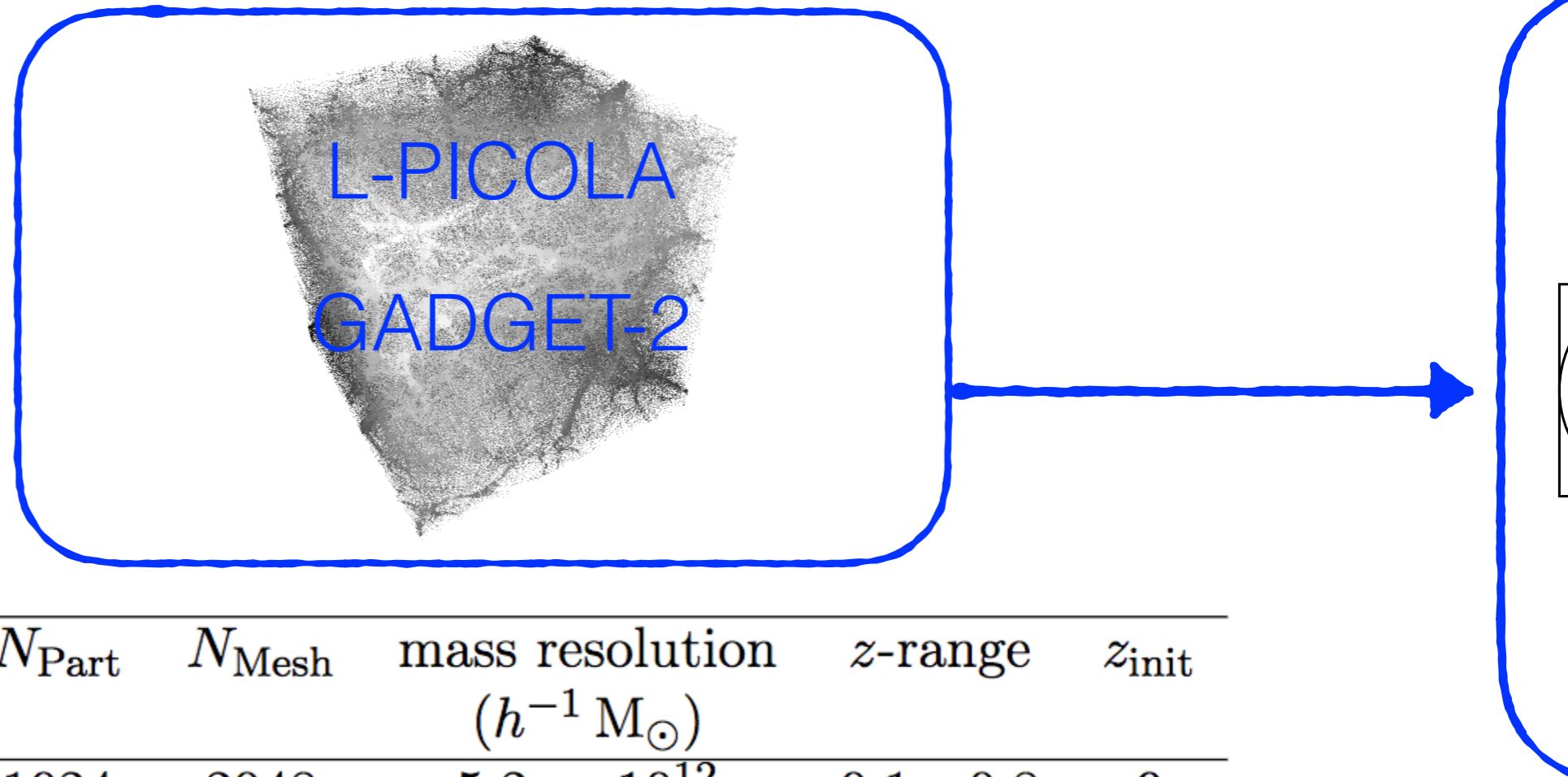
calculate large scales exactly with 2LPT
PM-code solves small scales

L-PICOLA

Howlett et al. 2015 (1506.03737)

Can we use L-PICOLA to
efficiently and *accurately*
generate covariance matrices
for weak lensing?

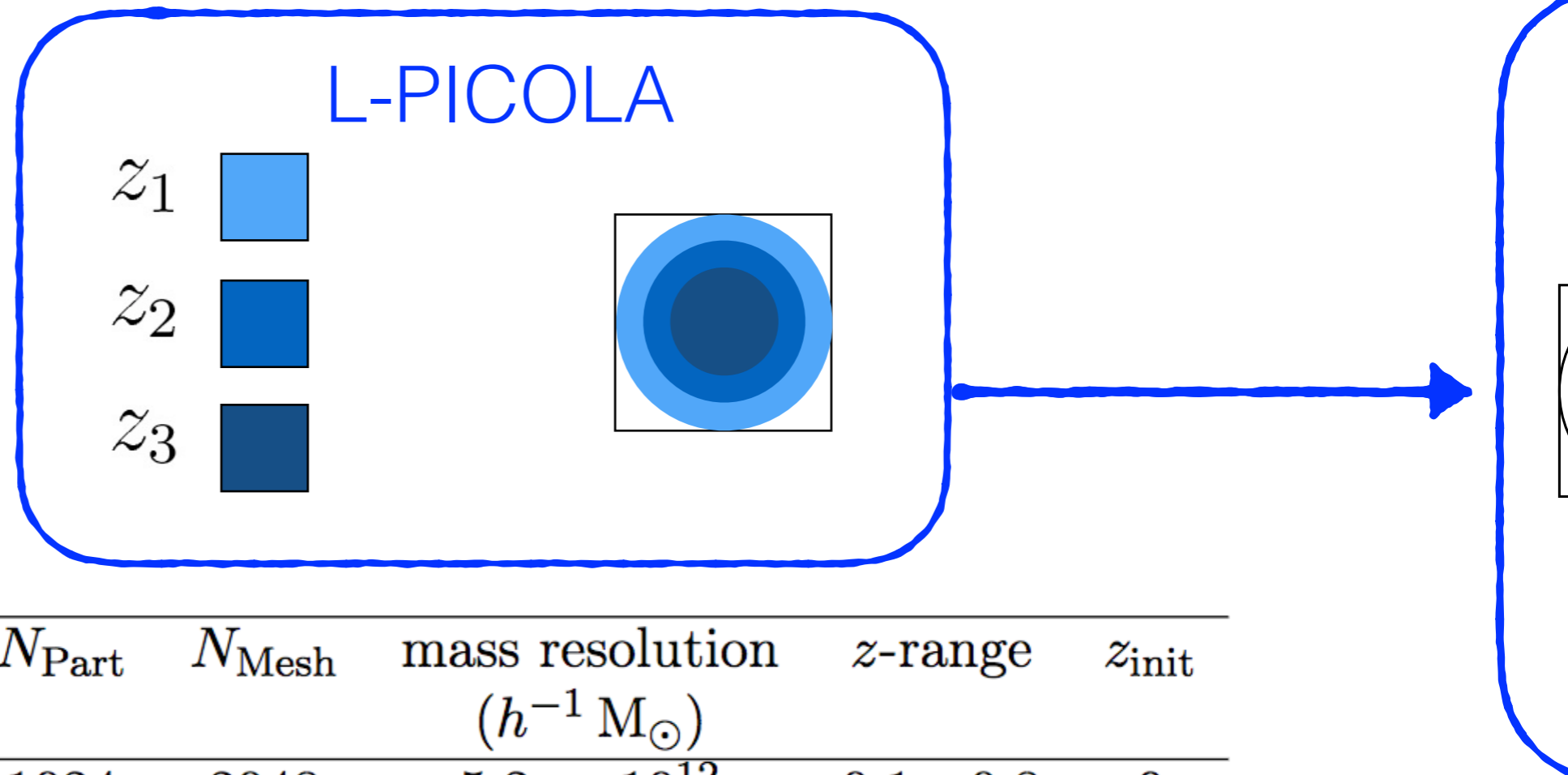
Simulations and Lightcone



L_{Box} (h^{-1} Mpc)	N_{Part}	N_{Mesh}	mass resolution ($h^{-1} M_{\odot}$)	z -range	z_{init}
4200	1024	2048	5.2×10^{12}	0.1 - 0.8	9
6300	1024	2048	1.8×10^{13}	0.8 - 1.5	9

$$h = 0.7, \Omega_{\text{m}} = 0.276, \Omega_{\text{b}} = 0.045, n_s = 0.961, \sigma_8 = 0.811$$

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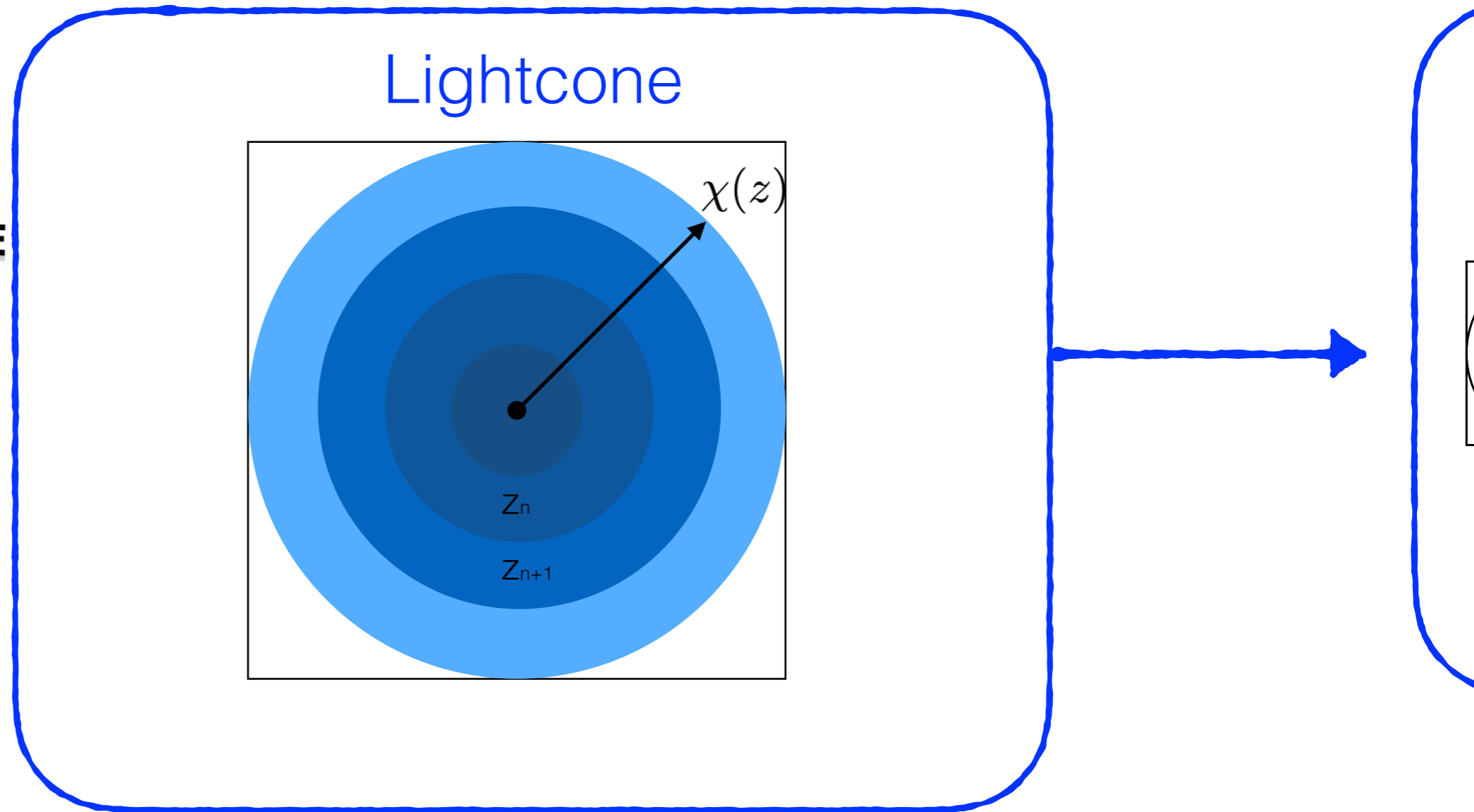
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- 1 [GADGET-2](#) and [L-PICOLA](#) sims in snapshot mode
- 150 [L-PICOLA](#) sims in lightcone mode

Simulations and Lightcone

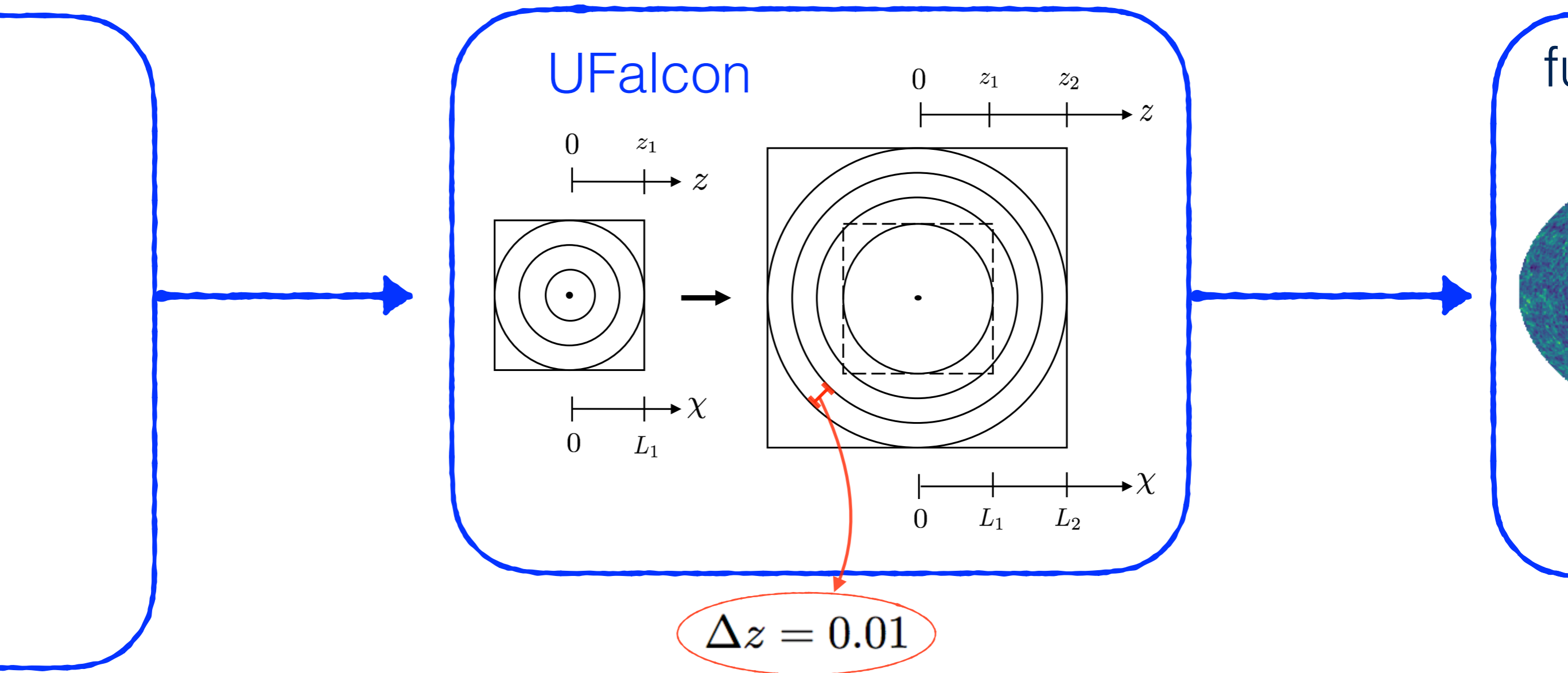


MICE Simulation
based on GADGET-2



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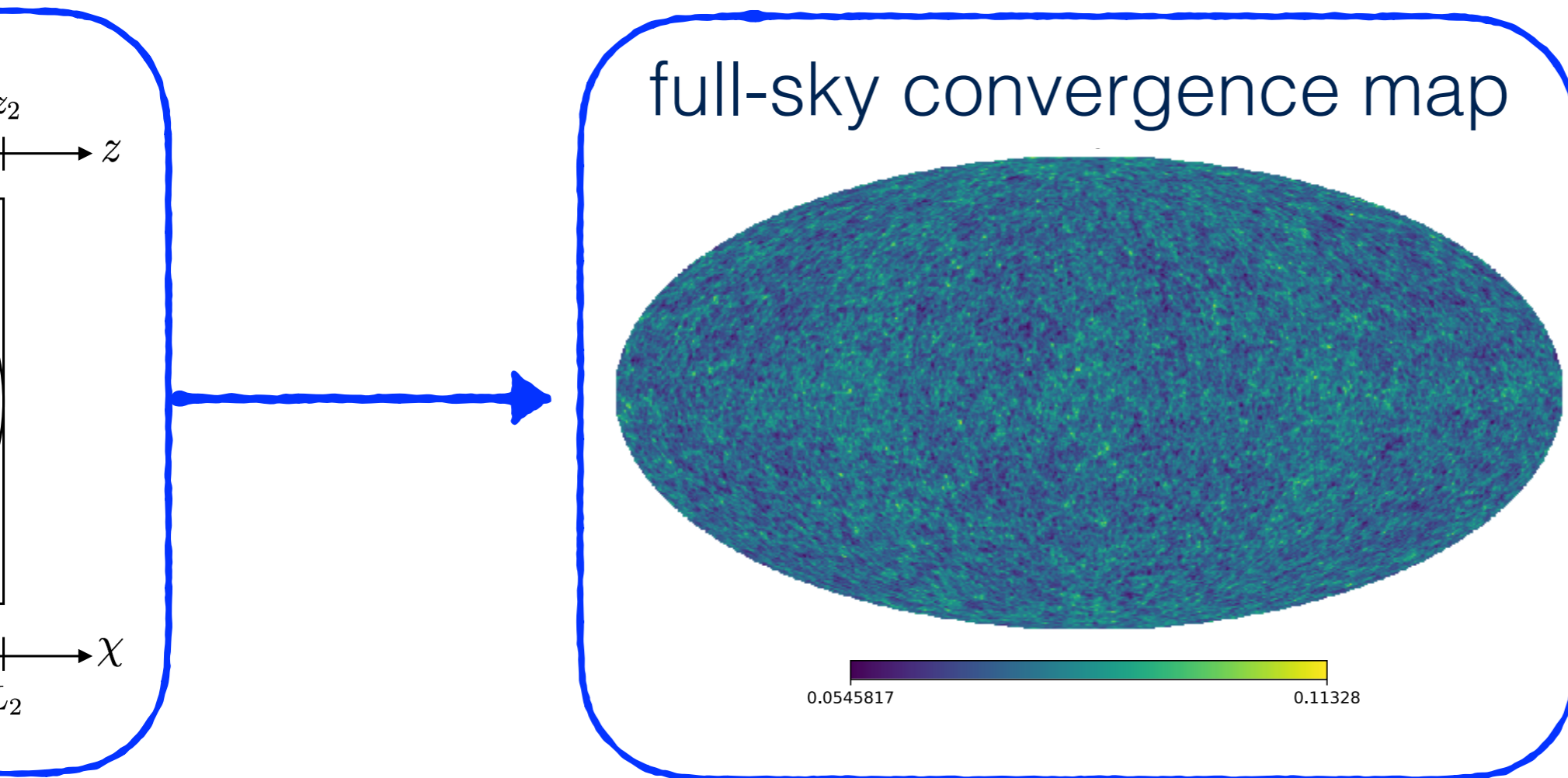
Simulations and Lightcone



- Use Born-Approximation for the convergence map:

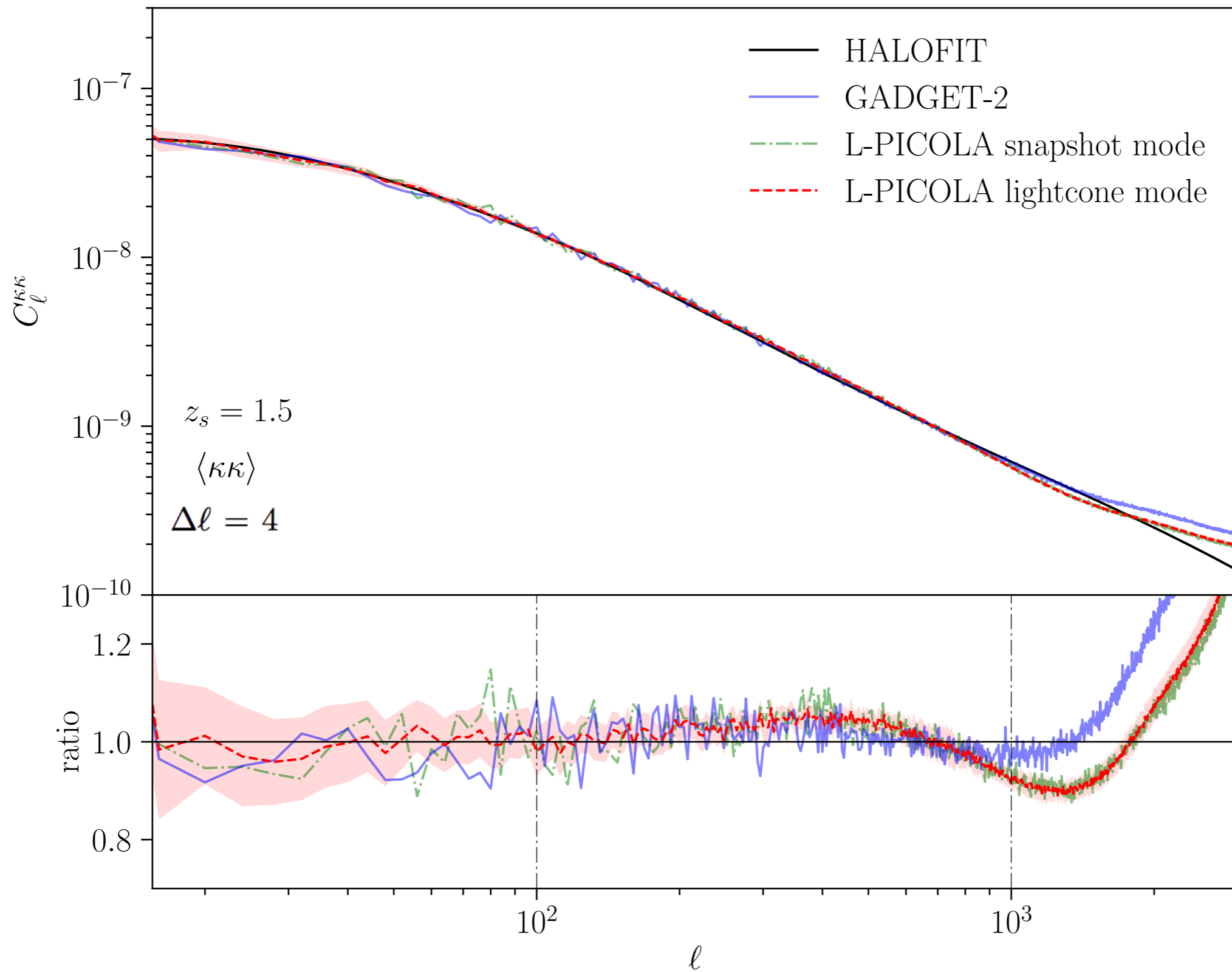
$$\kappa(\theta_{\text{pix}}) \approx \frac{3}{2} \Omega_m \sum_b W_b \frac{H_0}{c} \left[\frac{N_{\text{pix}}}{4\pi} \frac{V_{\text{sim}}}{N_{\text{part}}^{\text{sim}}} \left(\frac{H_0}{c} \right)^2 \frac{n_p(\theta_{\text{pix}}, \Delta\chi_b)}{\mathcal{D}^2(z_b)} - \left(\frac{c}{H_0} \Delta\mathcal{D}_b \right) \right]$$

Simulations and Lightcone

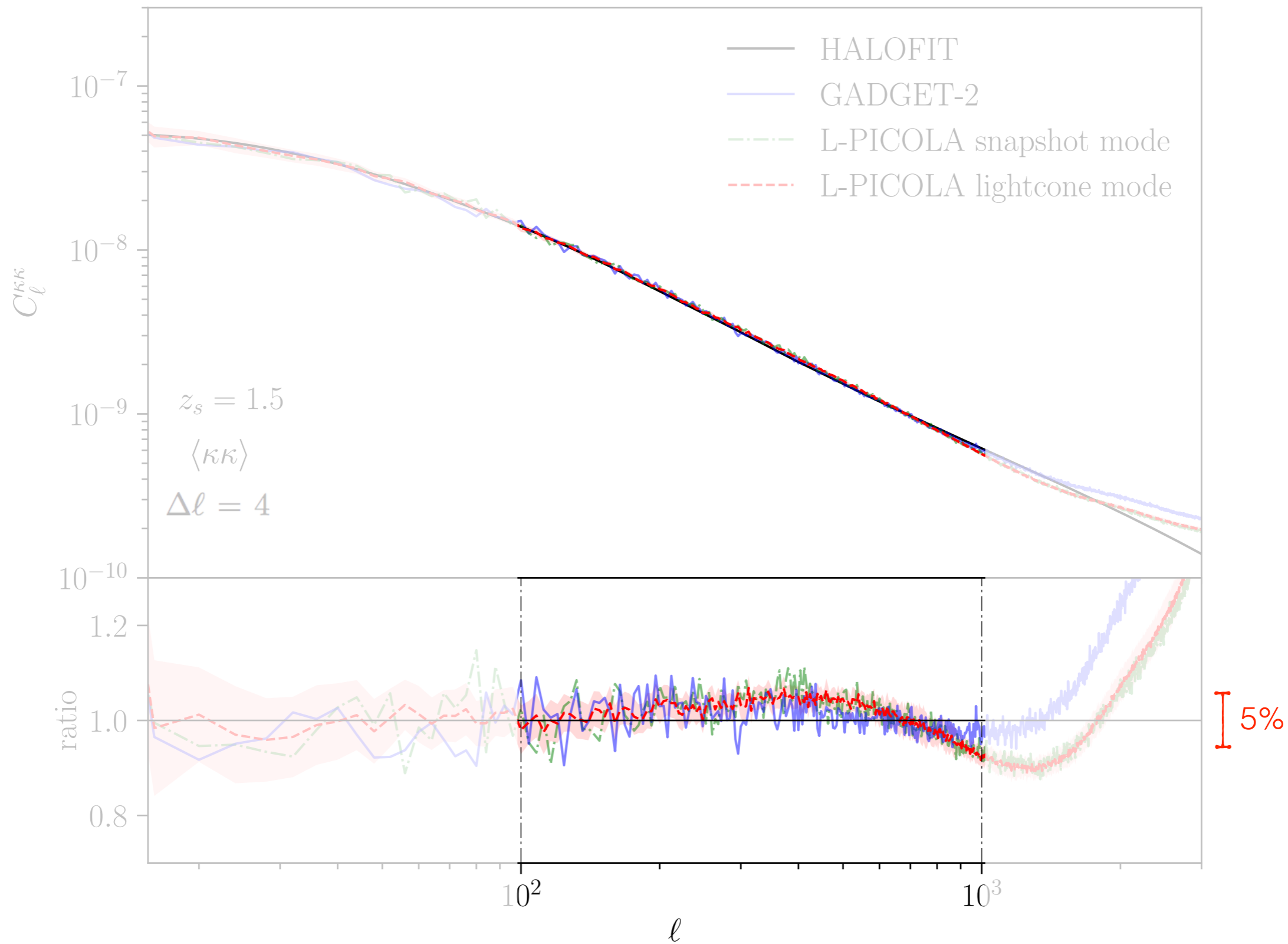


- Waltime: ~ 2 h for simulation + ~ 1 h for lightcone
- both parts parallelized on Cluster

Power Spectrum



Power Spectrum



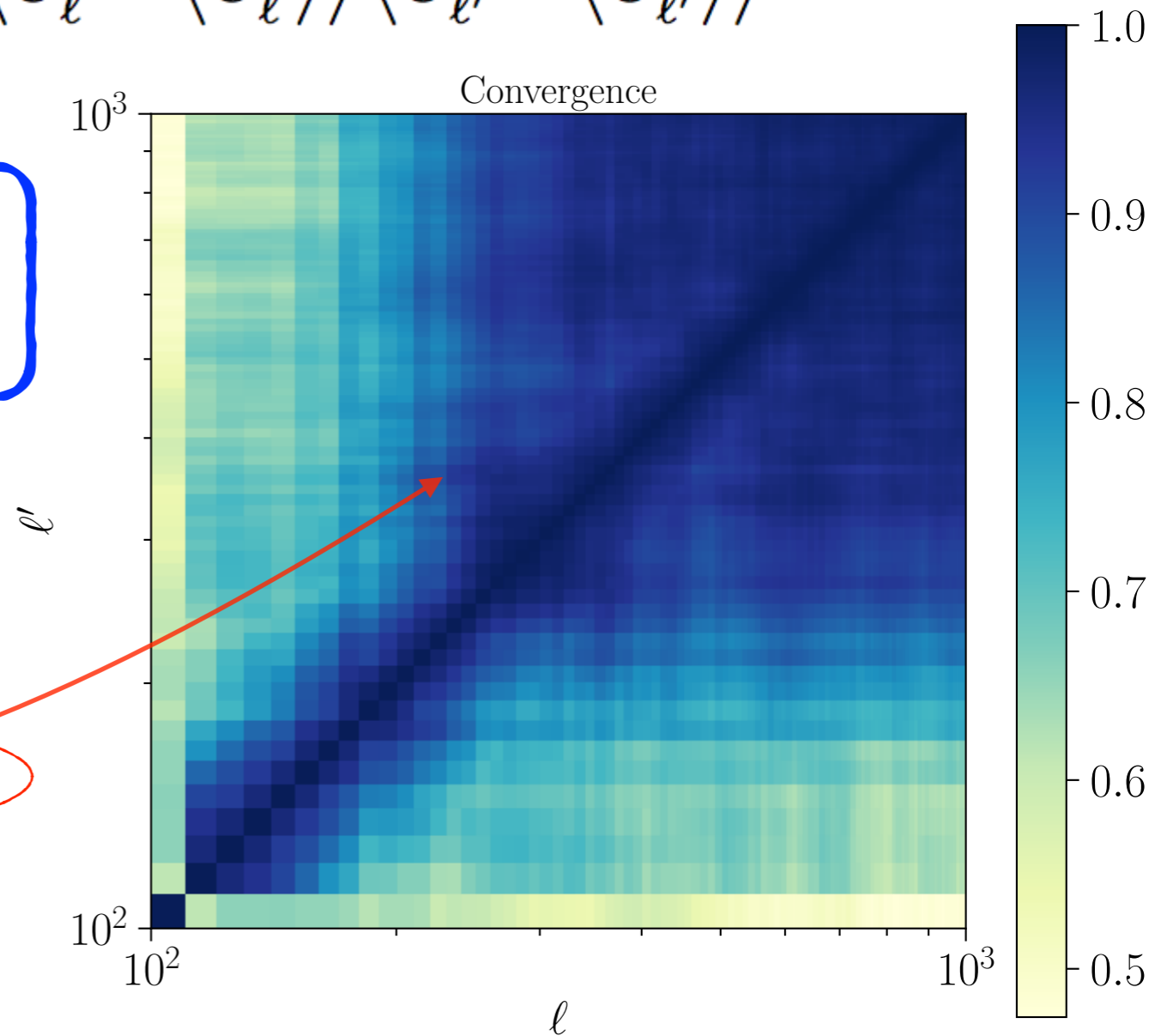
Covariance Matrix

Covariance matrix for scales $10^2 < \ell < 10^3$ using 150

UFalcon maps: $\text{cov}(\ell, \ell') = \langle C_\ell^q - \langle C_\ell^q \rangle \rangle \langle C_{\ell'}^q - \langle C_{\ell'}^q \rangle \rangle$

$$\text{corr}(\ell, \ell') = \frac{\text{cov}(\ell, \ell')}{\sqrt{\text{cov}(\ell, \ell) \text{cov}(\ell', \ell')}}$$

stronger mode-coupling



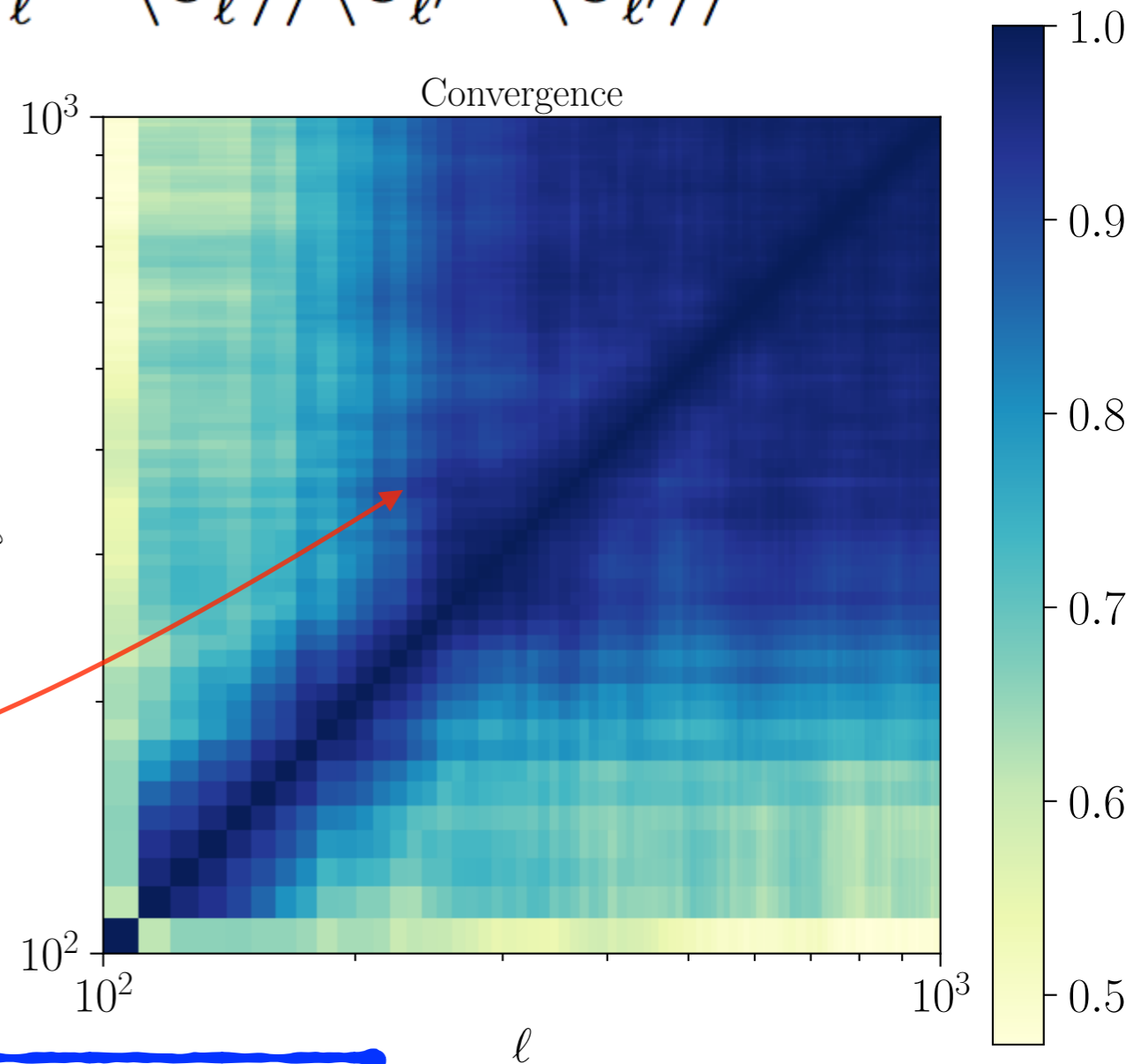
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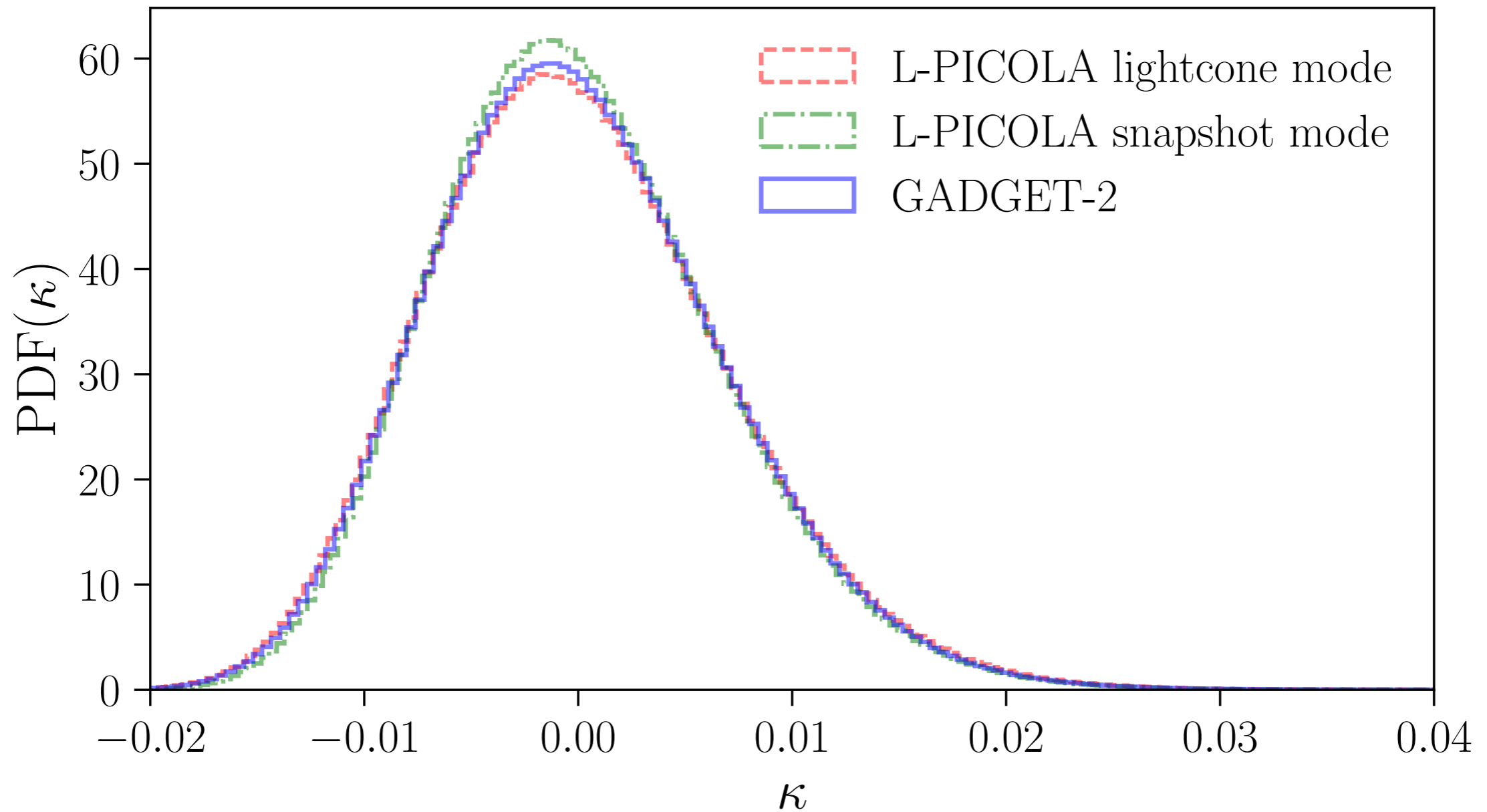
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→ accurate enough for weak lensing?

1-Point Distribution

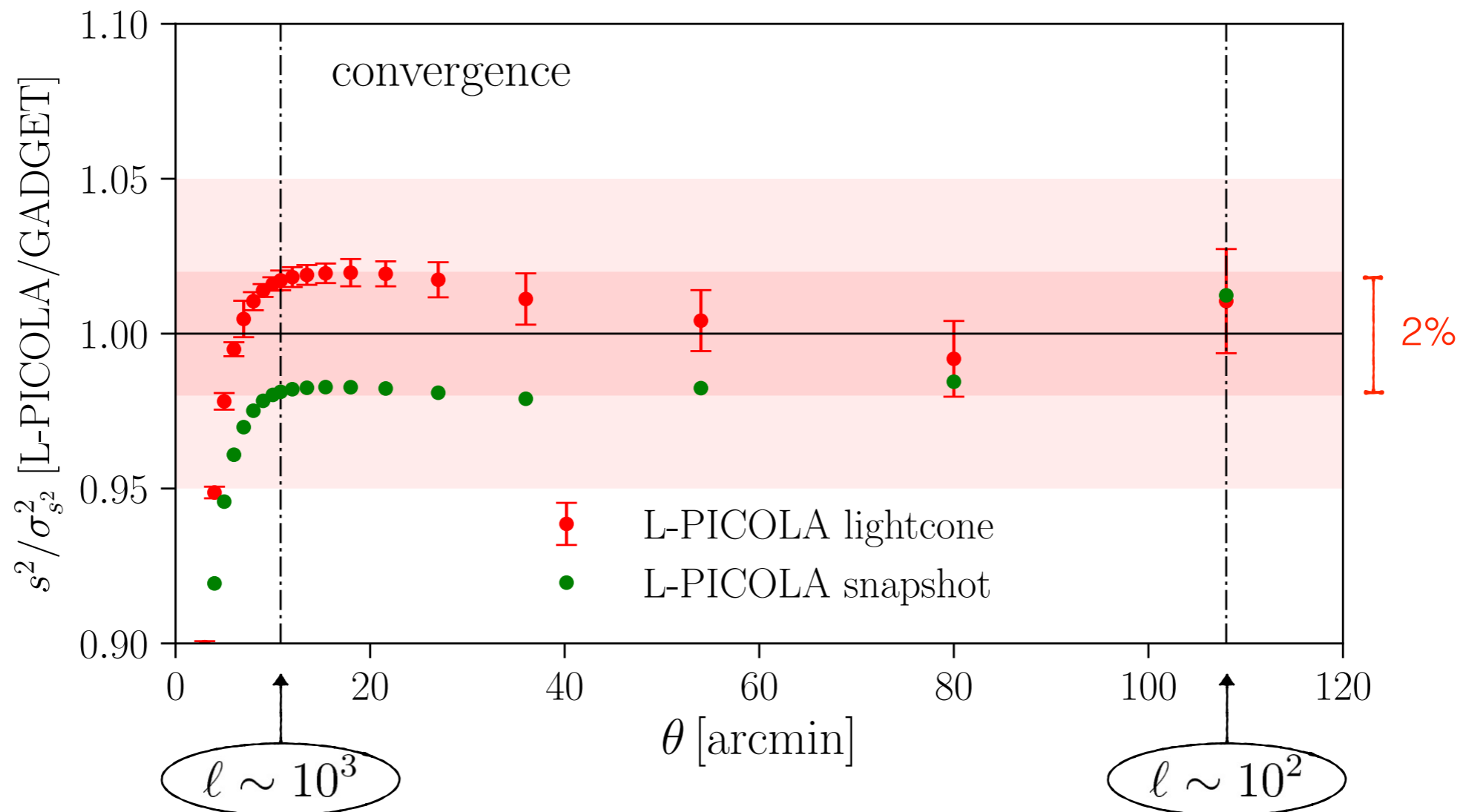


1-Point Distribution

Variance of sample variance as a measure of non-Gaussianity.

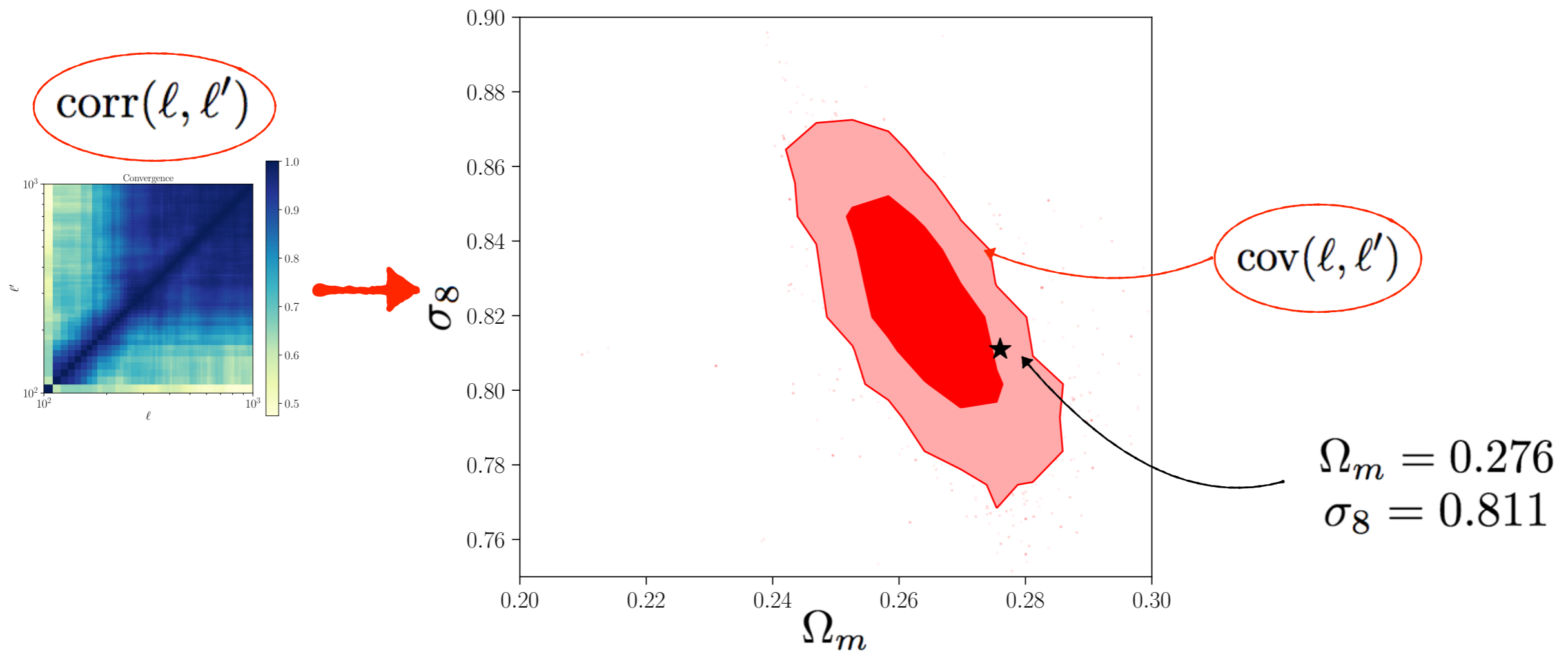
$$s^2 = \frac{1}{N} \sum_{i=1}^N (q_i - \bar{q})^2, \quad \sigma_{s^2}^2 = \frac{(N-1)^2}{N^3} \mu_4 - \frac{(N-1)(N-3)}{N^3} \mu_2^2 \sim \frac{1}{N} (\mu_4 - \mu_2^2)$$

$$q_i = \kappa_i$$



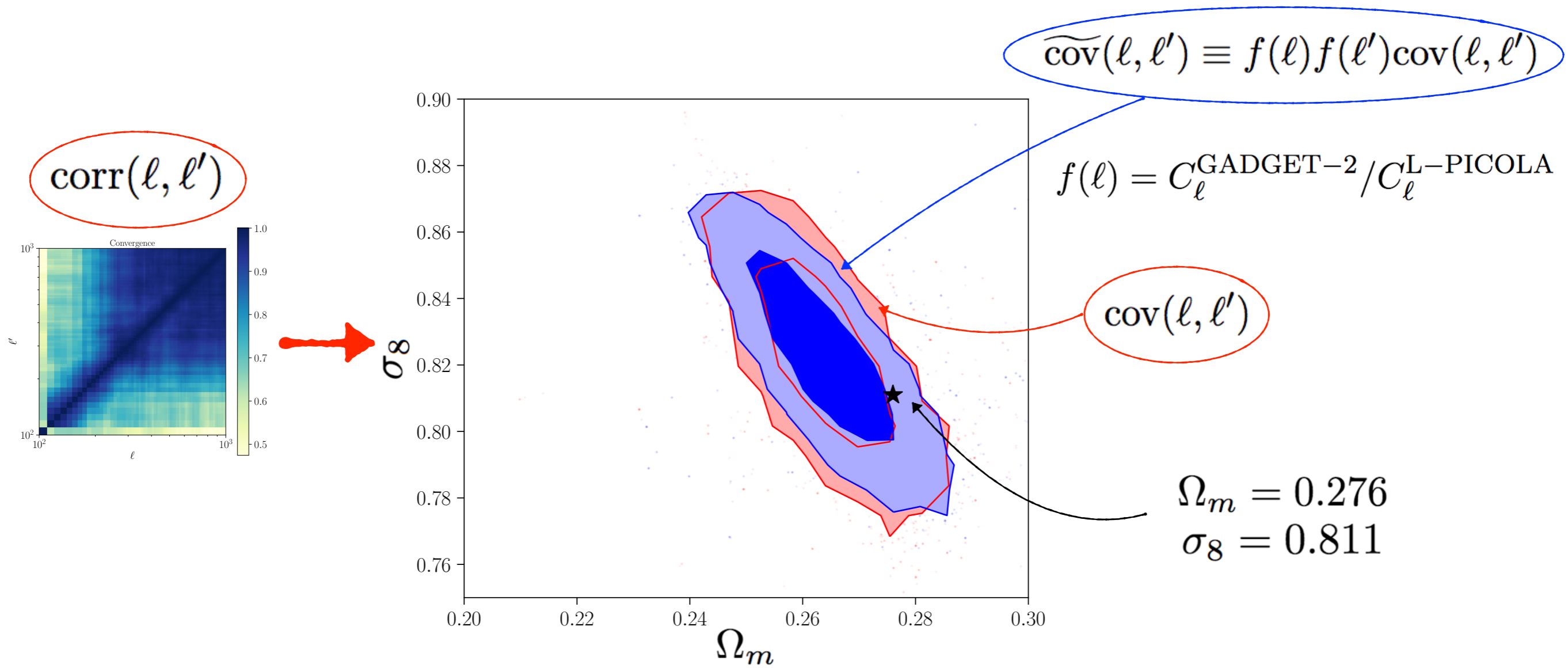
Parameter Constraints

- Sample Ω_m and σ_8 with a Monte Carlo Markov Chain (MCMC) on scales $10^2 < \ell < 10^3$.
- Flat priors: $0.05 < \Omega_m < 0.9$, $0.2 < \sigma_8 < 1.6$



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Conclusion

Summary:

- UFalcon applied to [L-PICOLA](#): Fast way to generate full-sky weak lensing maps up to $z_s = 1.5$ (**2-3h walltime**).
- 5% agreement between [L-PICOLA](#) and [GADGET-2](#) power spectra.
- 2% agreement between $s^2/\sigma_{s^2}^2$ based on [L-PICOLA](#) and [GADGET-2](#) maps.
- Obtained constraints in the $\Omega_m - \sigma_8$ plane are robust to changes on percent level for optimistic survey configuration.
- Survey specific masks applicable.

Outlook:

- UFalcon: include further probes.
- Application of pipeline to models beyond Λ CDM.

Thank you!

Backup Slides

Simulations and Lightcone

N-Body code

Lagrangian Perturbation Theory

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- ⊕ exact results on large scales
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COLA

calculate large scales exactly with 2LPT
N-Body code (PM) solves small scales
several orders of magnitude faster than GADGET-2

$$\partial_t^2 \mathbf{x}_{\text{res}} = -\nabla\Phi - \partial_t^2 \mathbf{x}_{\text{LPT}} \quad \text{with} \quad \mathbf{x}_{\text{res}} = \mathbf{x} - \mathbf{x}_{\text{LPT}}$$

discretize in PM-code

use exact 2LPT expression

Checks Performed

- 1) Compare maps using **L-PICOLA** to **GADGET-2**:
 - spherical harmonic power spectrum C_l^{KK}
 - probability distribution function (PDF)
 - higher order moments
- 2) Compute covariance matrix using 150 **L-PICOLA** maps.
- 3) Infer cosmological parameter constraints in the $\Omega_m - \sigma_8$ - plane.

Mass Maps

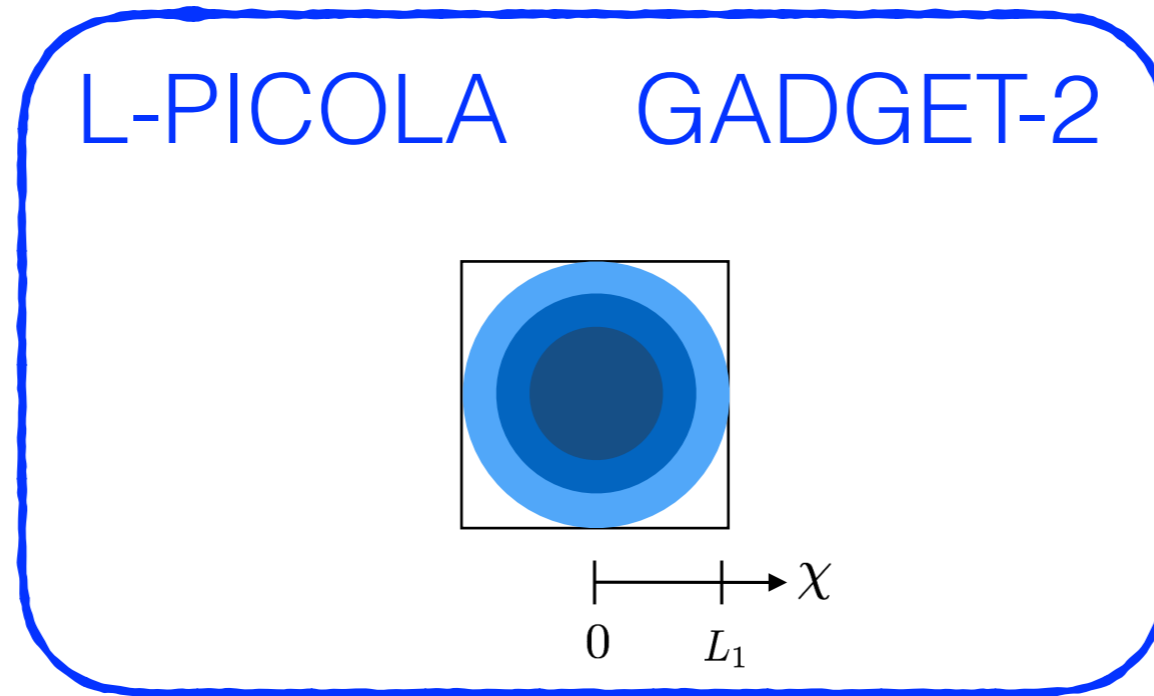
$$\delta(\theta_{\text{pix}}) \approx \sum_b \left[\frac{N_{\text{pix}}}{4\pi} \frac{V_{\text{sim}}}{N_{\text{part}}^{\text{sim}}} \left(\frac{H_0}{c} \right)^2 \frac{n_p(\theta_{\text{pix}}, \Delta\chi_b)}{\mathcal{D}^2(z_b)} - \left(\frac{c}{H_0} \Delta\mathcal{D}_b \right) \right] / \sum_b \left(\frac{c}{H_0} \Delta\mathcal{D}_b \right)$$

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