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**ENERGY**

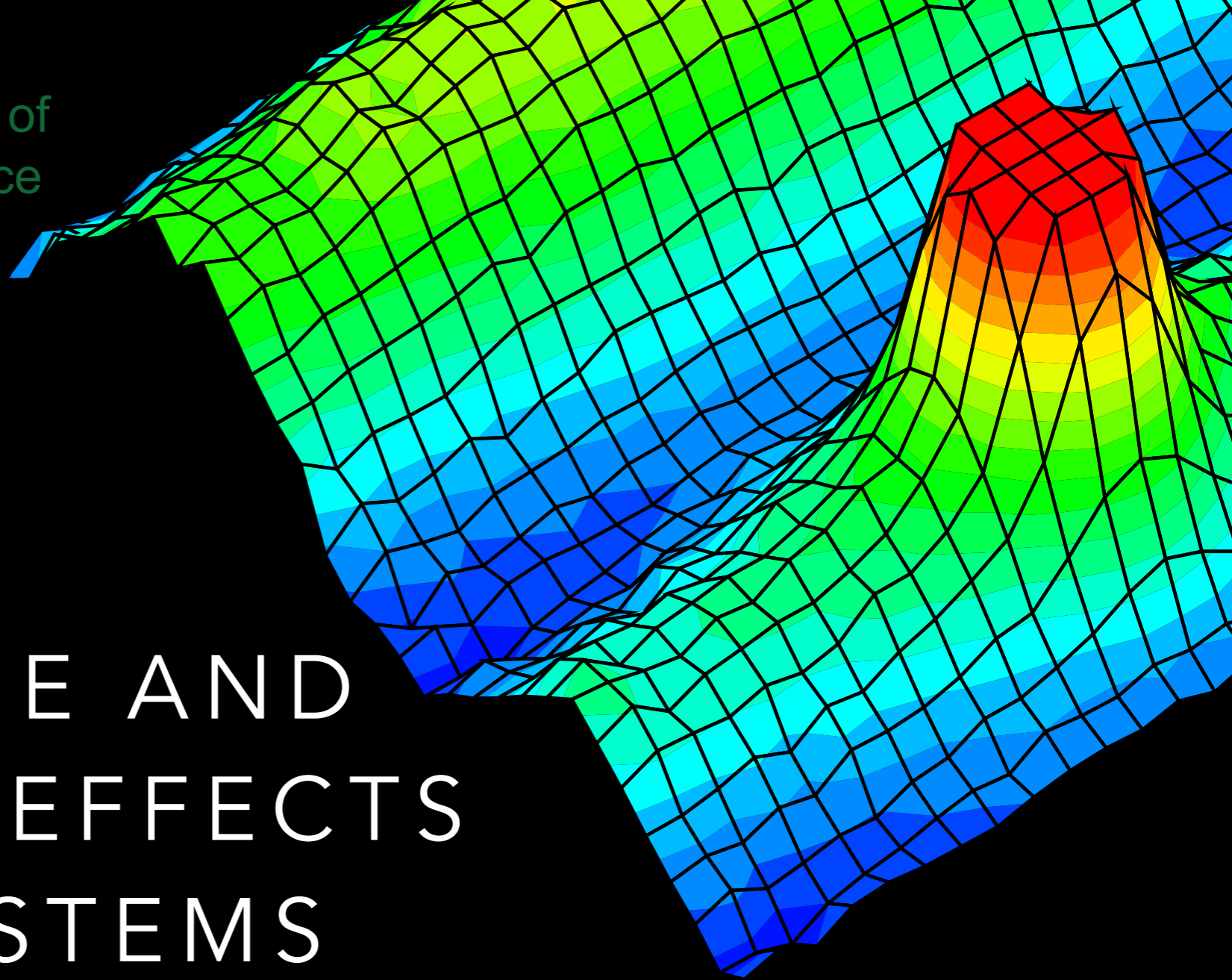
Office of  
Science

# INITIAL STAGE AND COLLECTIVE EFFECTS IN SMALL SYSTEMS

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Brookhaven National Laboratory

June 6, 2018  
LHCP 2018  
Bologna, Italy

**BROOKHAVEN**  
NATIONAL LABORATORY

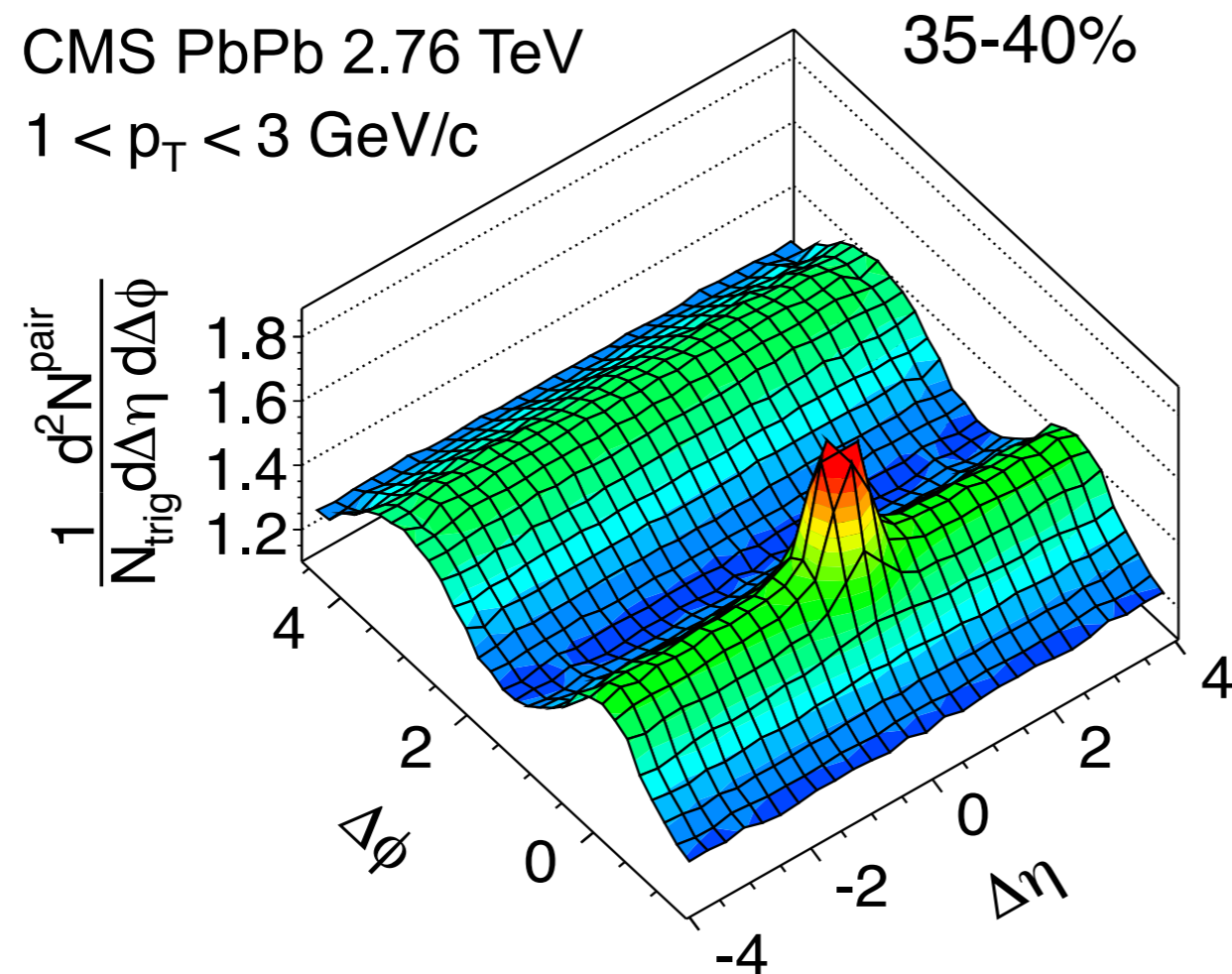


# TWO-PARTICLE CORRELATIONS

2-particle correlation as a function of  $\Delta\eta$  and  $\Delta\phi$

$\Delta\eta$ : DIFFERENCE IN PSEUDO-RAPIDITY

$\Delta\phi$ : DIFFERENCE IN AZIMUTHAL ANGLE



**Ridge:**

Structure that is long range in  $\Delta\eta$  and generally shows two bumps in  $\Delta\phi$   
"double-ridge"

# RIDGE IN HEAVY ION COLLISIONS

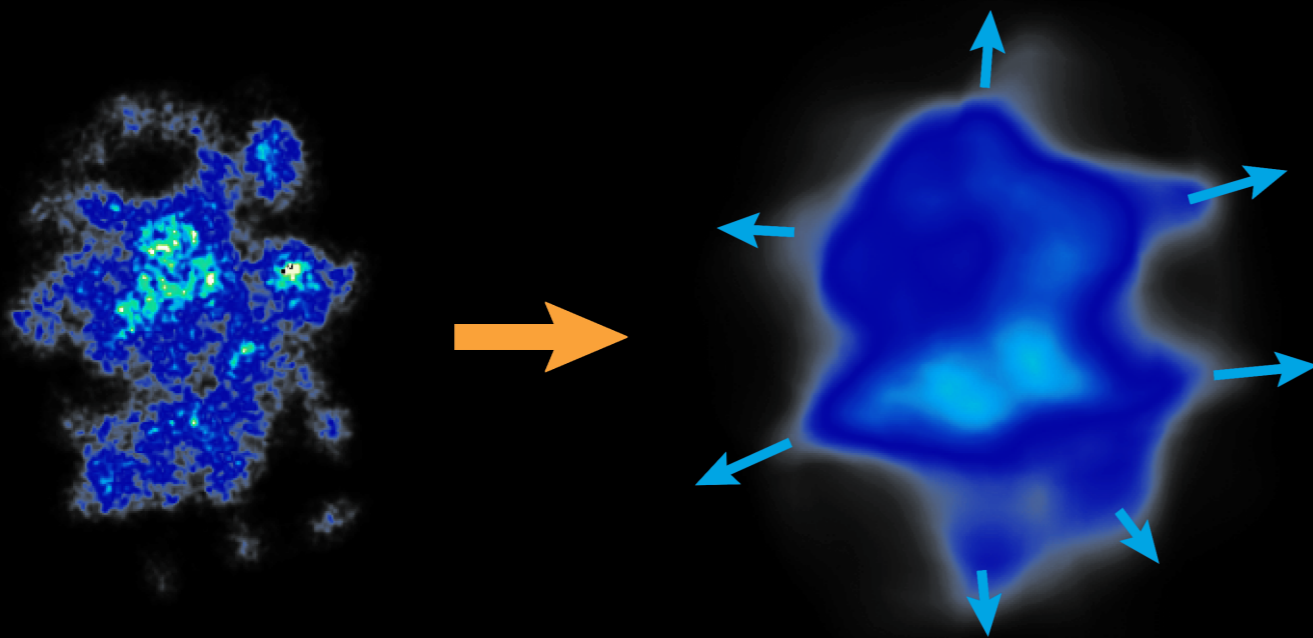
First seen in heavy ion collisions at RHIC

STAR COLLABORATION, PHYS. REV. C80 (2009) 064912

PHOBOS COLLABORATION, PHYS. REV. LETT. 104 (2010) 062301

Interpretation in heavy ion collision:

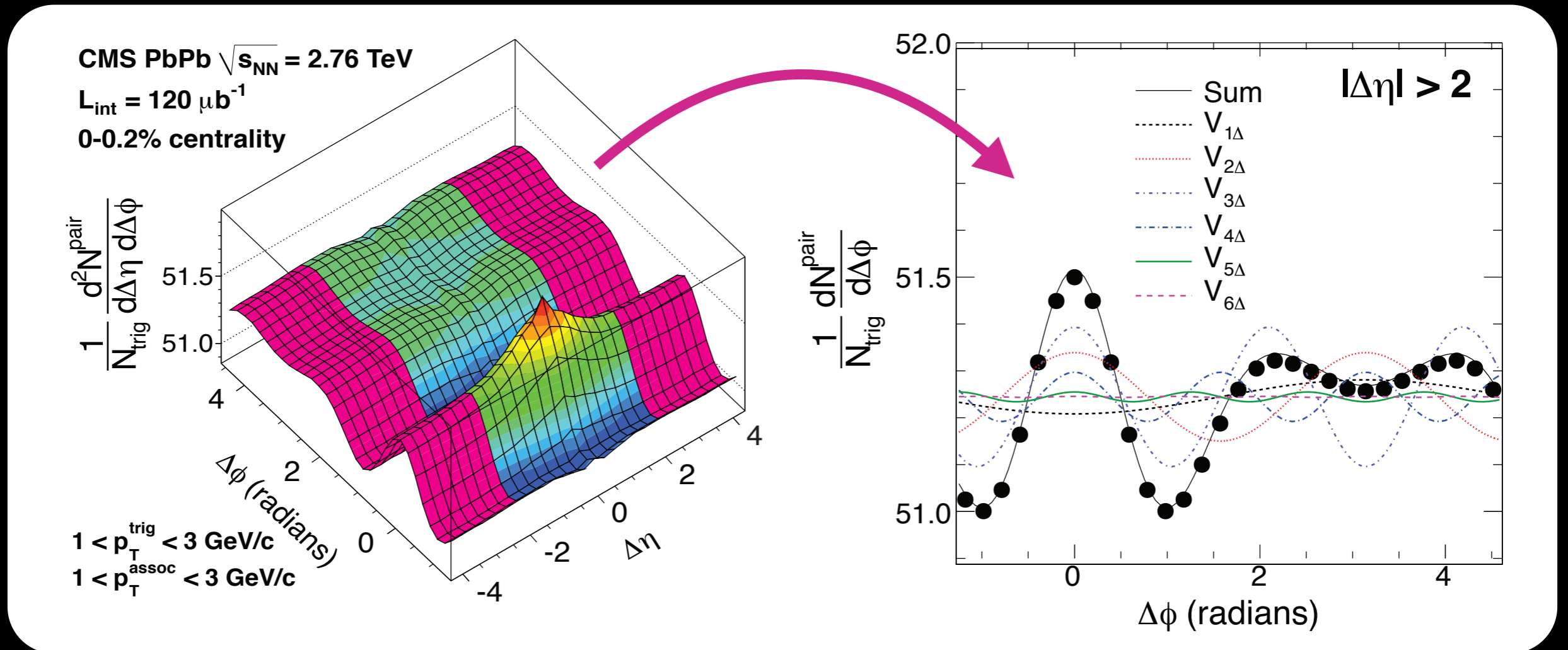
- Long range correlations emerging from early times (causality)
- Azimuthal structure formed by the medium response to the initial transverse geometry (well described by hydrodynamics)



2 ridges come from dominant  $\cos(2\Delta\Phi)$  contribution due to the mostly elliptic shape

# RIDGE IN HEAVY ION COLLISIONS

Azimuthal structure quantified using Fourier expansion

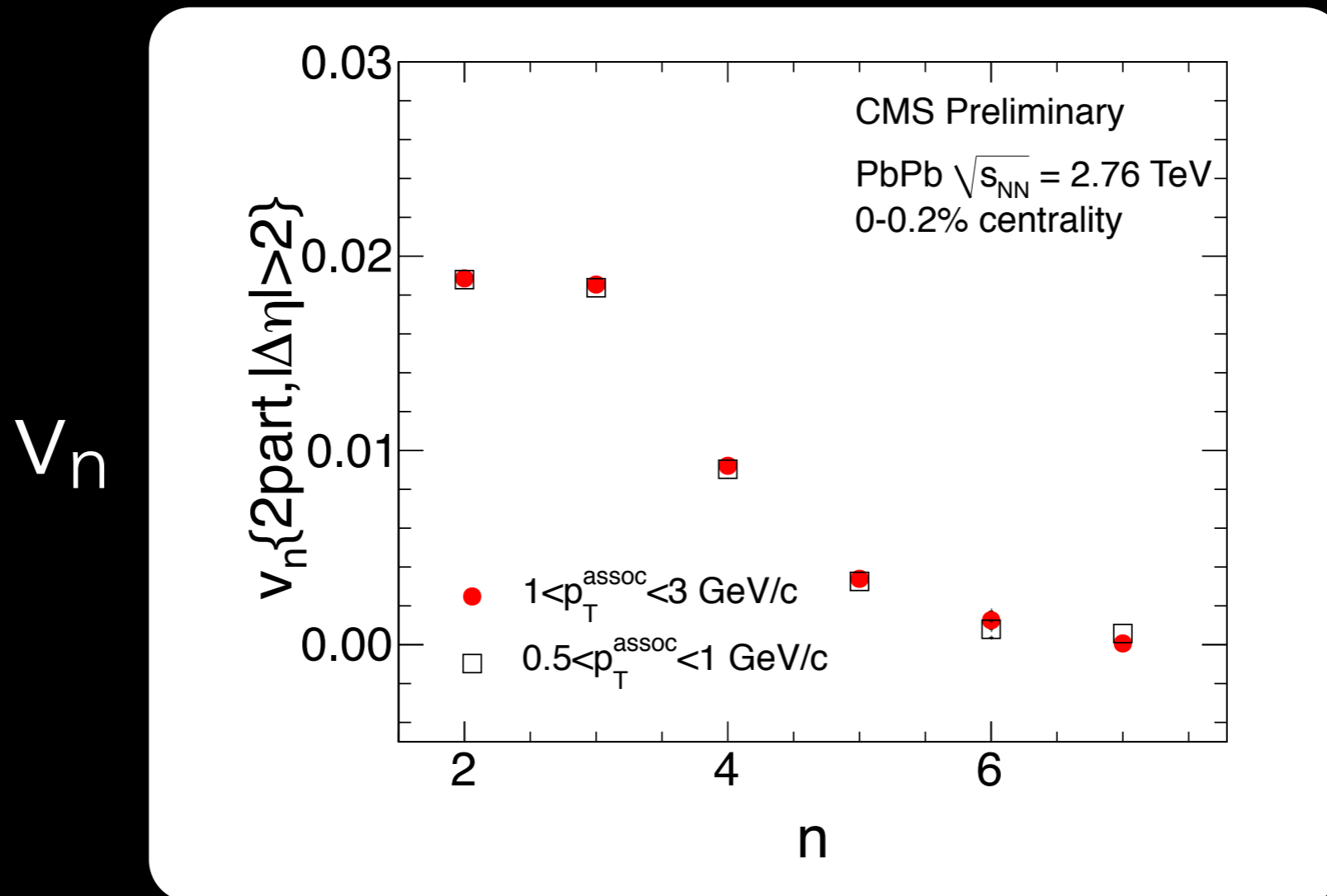


$$\frac{1}{N_{\text{trig}}} \frac{dN^{\text{pair}}}{d\Delta\phi} \sim 1 + 2 \sum_{n=1}^{n=\infty} V_{n\Delta}(p_T^{\text{trig}}, p_T^{\text{assoc}}) \cos(n\Delta\phi) \quad v_n = \sqrt{V_{n\Delta}}$$



# RIDGE IN HEAVY ION COLLISIONS

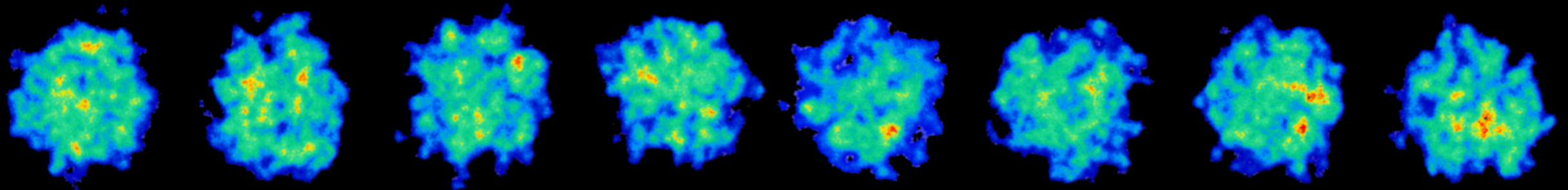
Azimuthal structure quantified using Fourier expansion



$$\frac{1}{N_{\text{trig}}} \frac{dN^{\text{pair}}}{d\Delta\phi} \sim 1 + 2 \sum_{n=1}^{n=\infty} V_{n\Delta}(p_T^{\text{trig}}, p_T^{\text{assoc}}) \cos(n\Delta\phi) \quad v_n = \sqrt{V_{n\Delta}}$$

# THEORETICAL DESCRIPTION IN HEAVY IONS

Fluctuating nucleon positions and color charges →  
Fluctuating deposited energy



High energy: Initial energy density can be computed in the color glass condensate framework (effective theory of QCD)

One realization is the IP-Glasma model

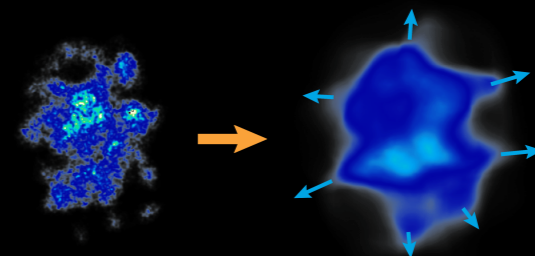
Includes gluon saturation at high densities

(small  $x$  and small transverse momentum  $p_T \approx Q_s$ )

B.SCHENKE, P.TRIBEDY, R.VENUGOPALAN, PRL108, 252301 (2012), PRC86, 034908 (2012)

Pressure gradients drive the evolution

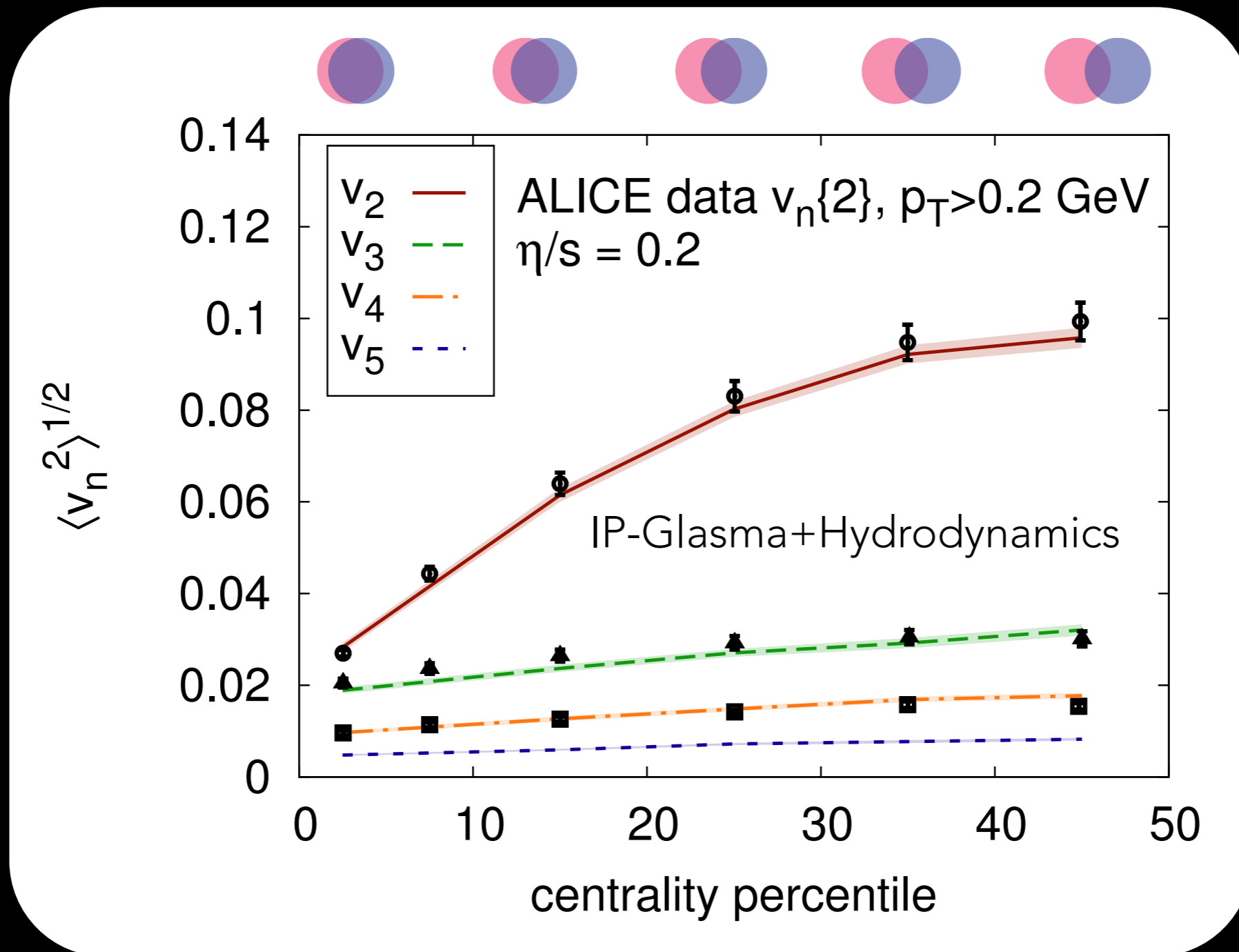
Described by hydrodynamics



C.GALE, S.JEON, B.SCHENKE, P.TRIBEDY, R.VENUGOPALAN, PRL110, 012302 (2013)

# COMPARISON OF THEORY TO EXPERIMENT

C. GALE, S. JEON, B.SCHENKE, P.TRIBEDY, R.VENUGOPALAN, PRL110, 012302 (2013)



Quantitative description of the experimental data!

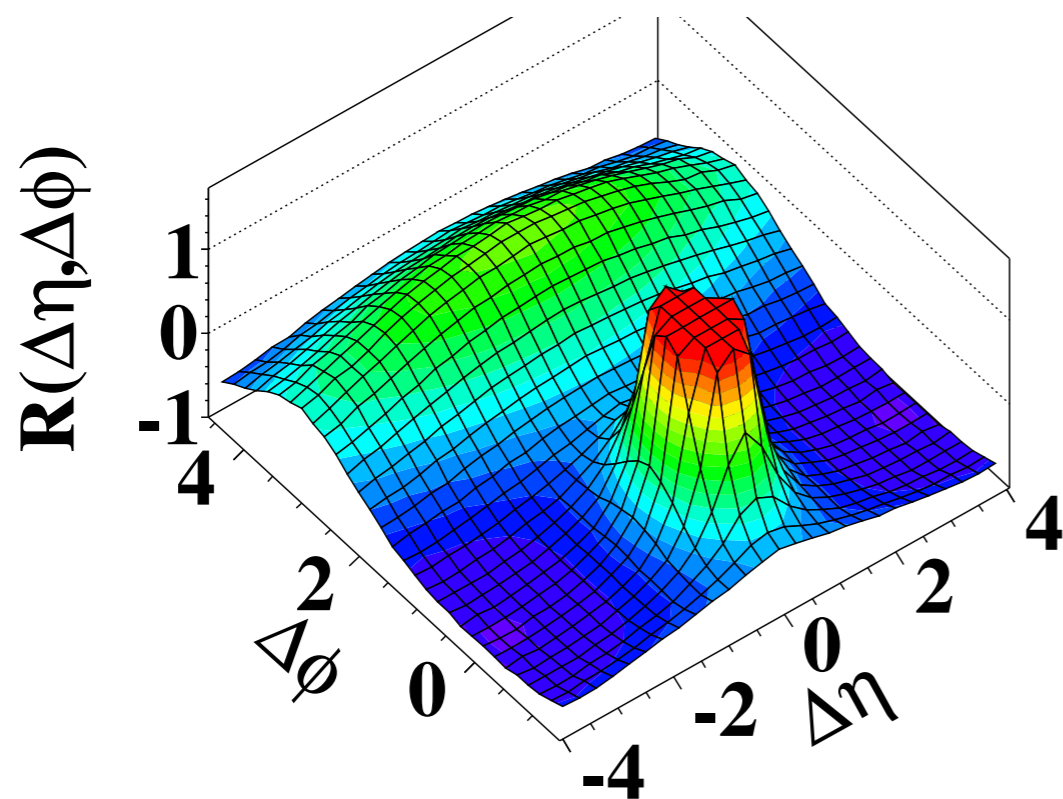
ALICE COLLABORATION, PHYS. REV. LETT. 107, 032301 (2011)

# RIDGE IN SMALL COLLISION SYSTEMS

minimum bias p+p

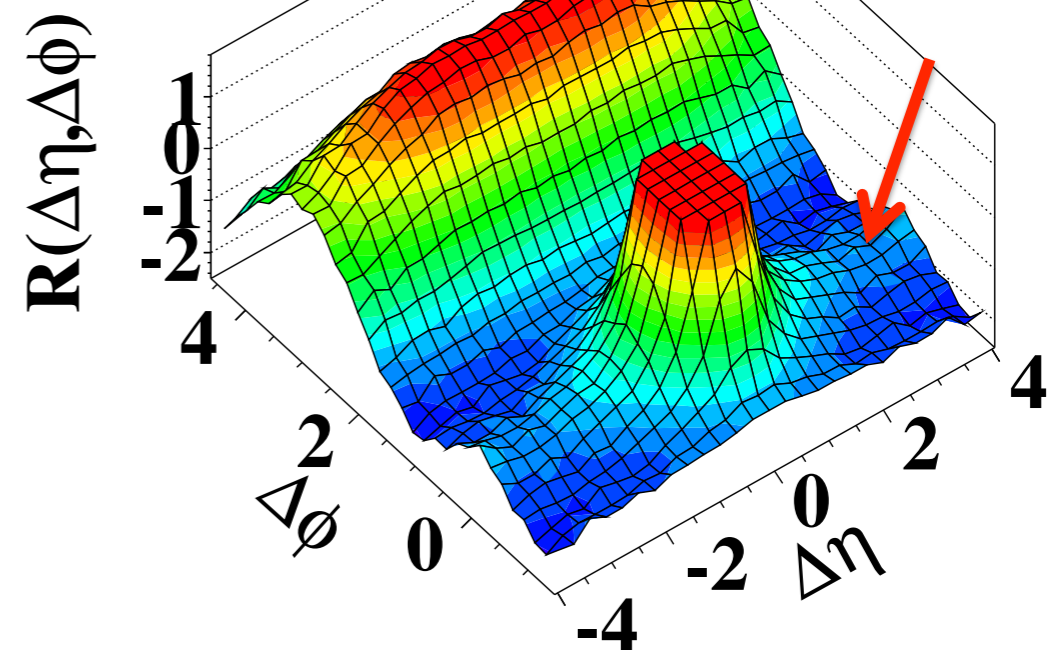
high multiplicity p+p

CMS MinBias,  $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



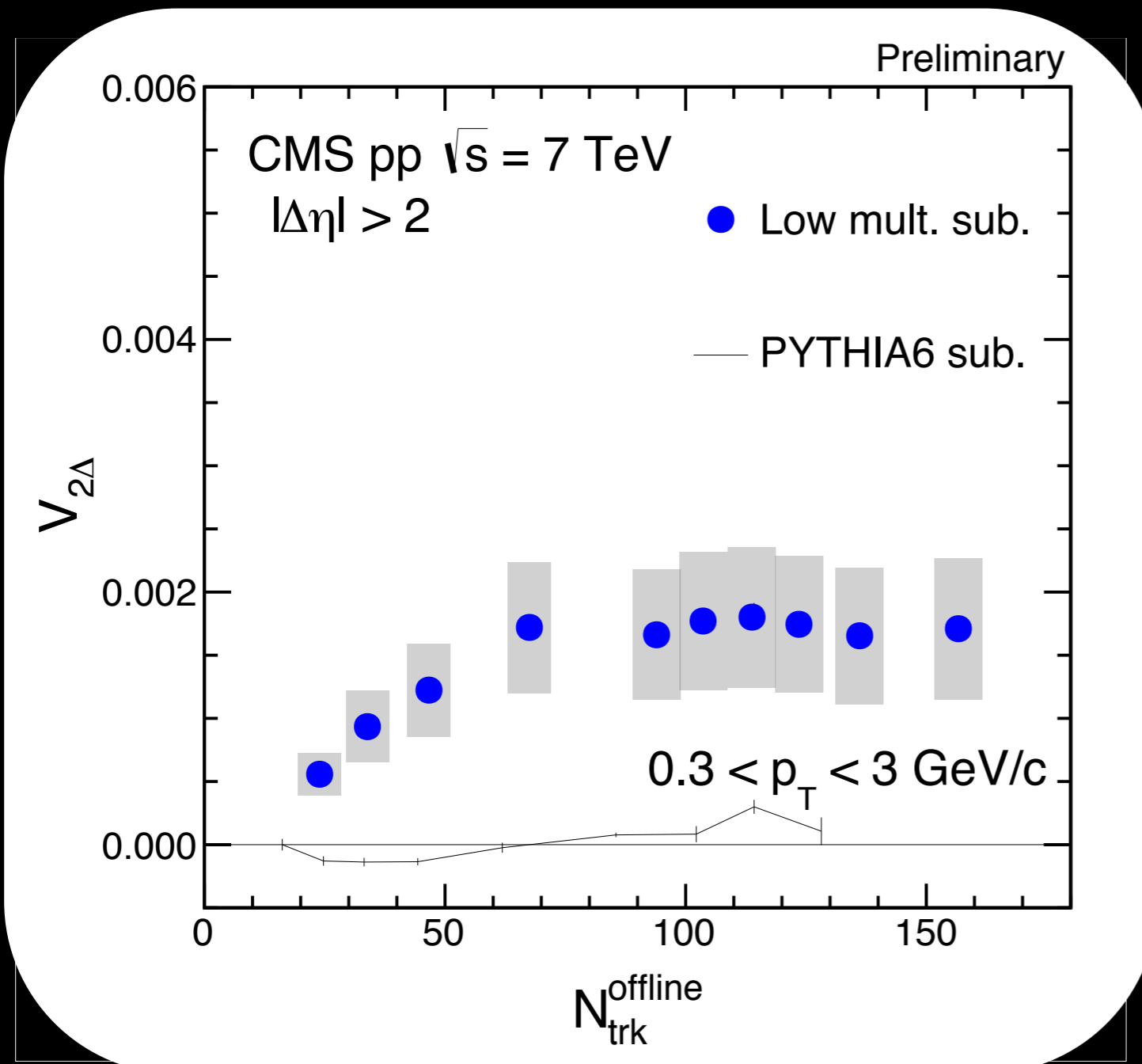
CMS pp 7 TeV,  $N_{\text{trk}} > 110$

$1 < p_T < 3 \text{ GeV}/c$



# $V_{2\Delta}$ IN p+p COLLISIONS

Result after correcting for back-to-back jet correlations estimated from low multiplicity events



No ridge in PYTHIA

CMS PAS HIN-15-009

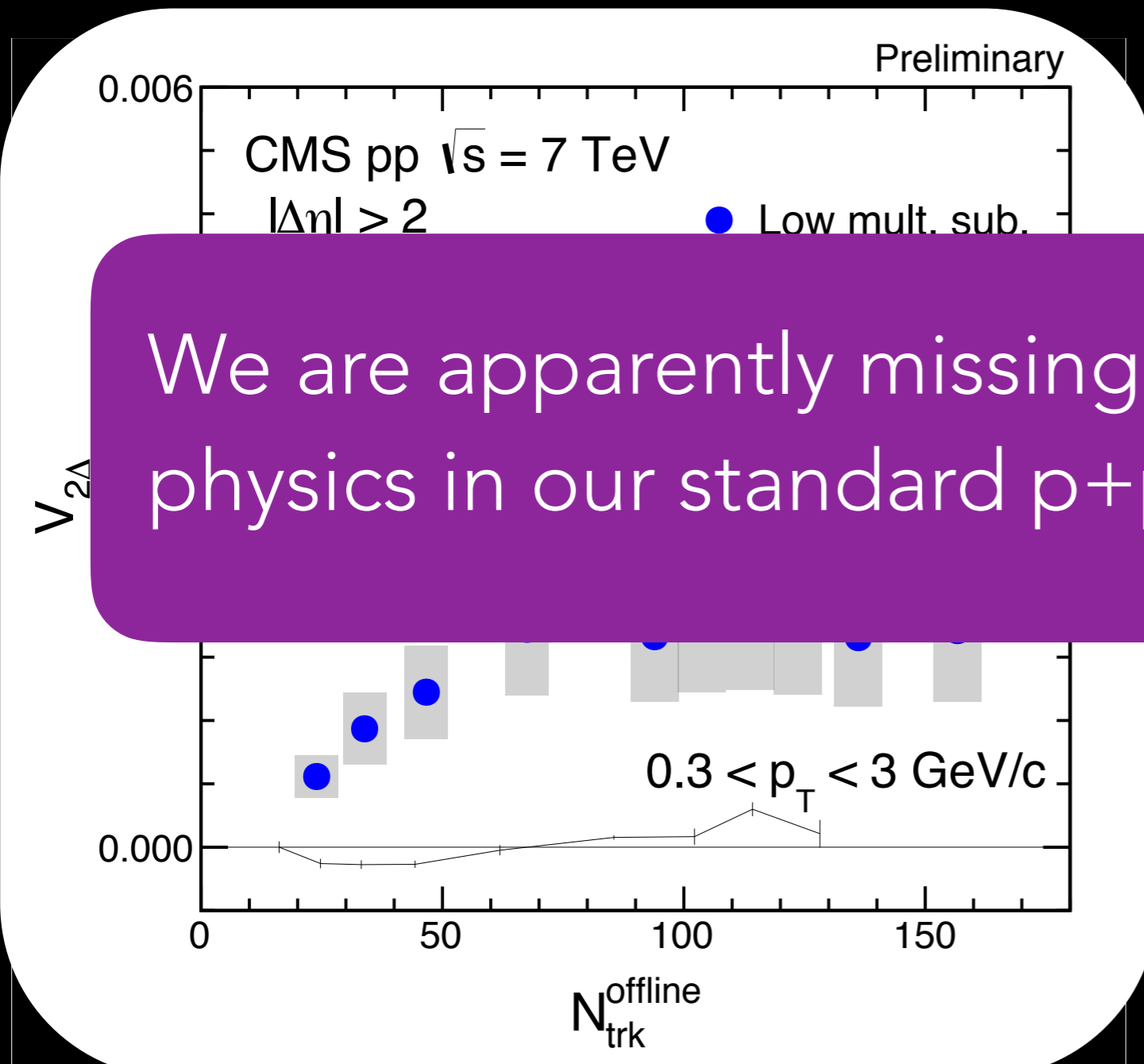
But progress including  
*final* state effects via  
'string shoving'

In Pythia8 v.8.235; Bierlich, Gustafson,  
Lönnblad: PLB779 (2018) 58-63  
Bierlich, arXiv:1606.09456 [hep-ph]  
Bierlich, Gustafson, Lönnblad, Tarasov  
JHEP 1503 (2015) 148



# $V_{2\Delta}$ IN p+p COLLISIONS

Result after correcting for back-to-back jet correlations estimated from low multiplicity events



No ridge in PYTHIA

We are apparently missing important physics in our standard p+p event generators!

'string shoving'

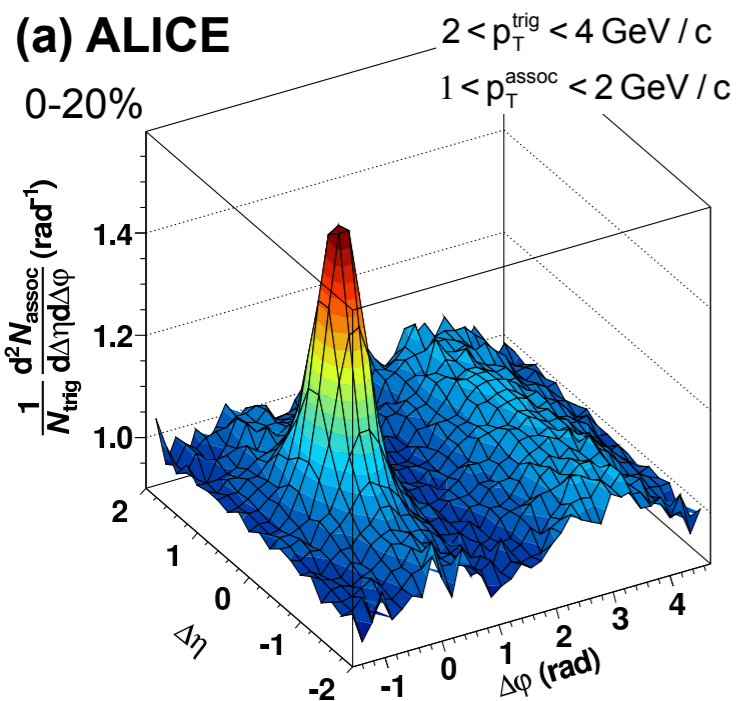
In Pythia8 v.8.235; Bierlich, Gustafson, Lönnblad: PLB779 (2018) 58-63  
Bierlich, arXiv:1606.09456 [hep-ph]  
Bierlich, Gustafson, Lönnblad, Tarasov  
JHEP 1503 (2015) 148

# RIDGE IN p+Pb COLLISIONS

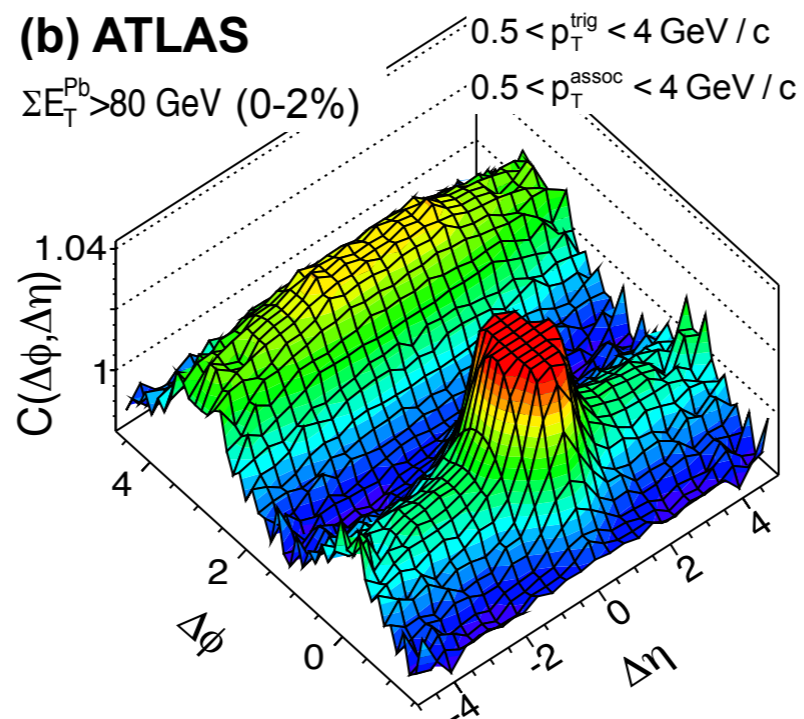
high multiplicity p+Pb

pPb  $\sqrt{s_{NN}} = 5.02$  TeV at the LHC

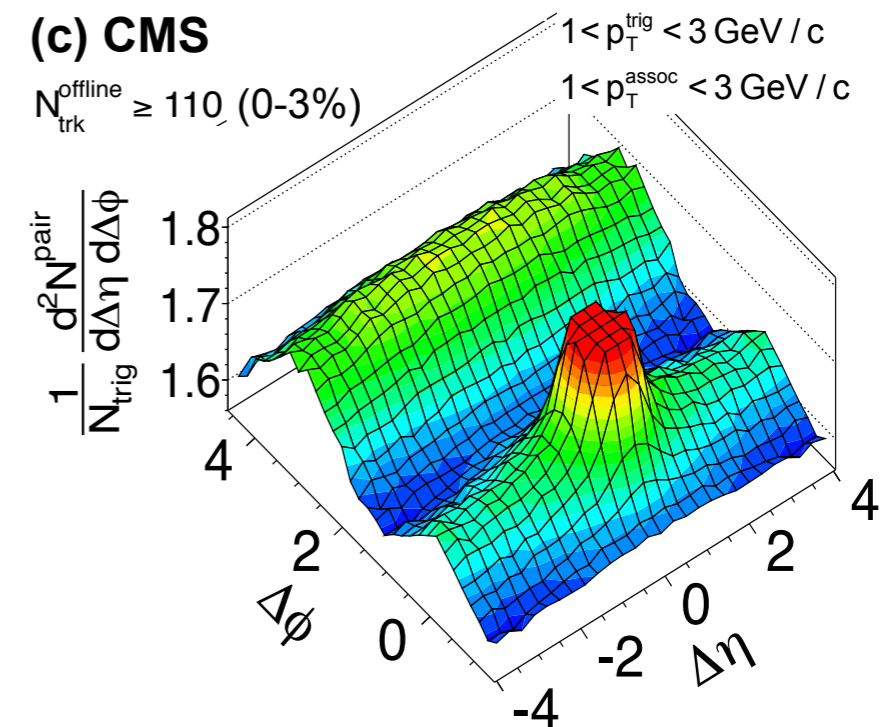
(a) ALICE



(b) ATLAS



(c) CMS

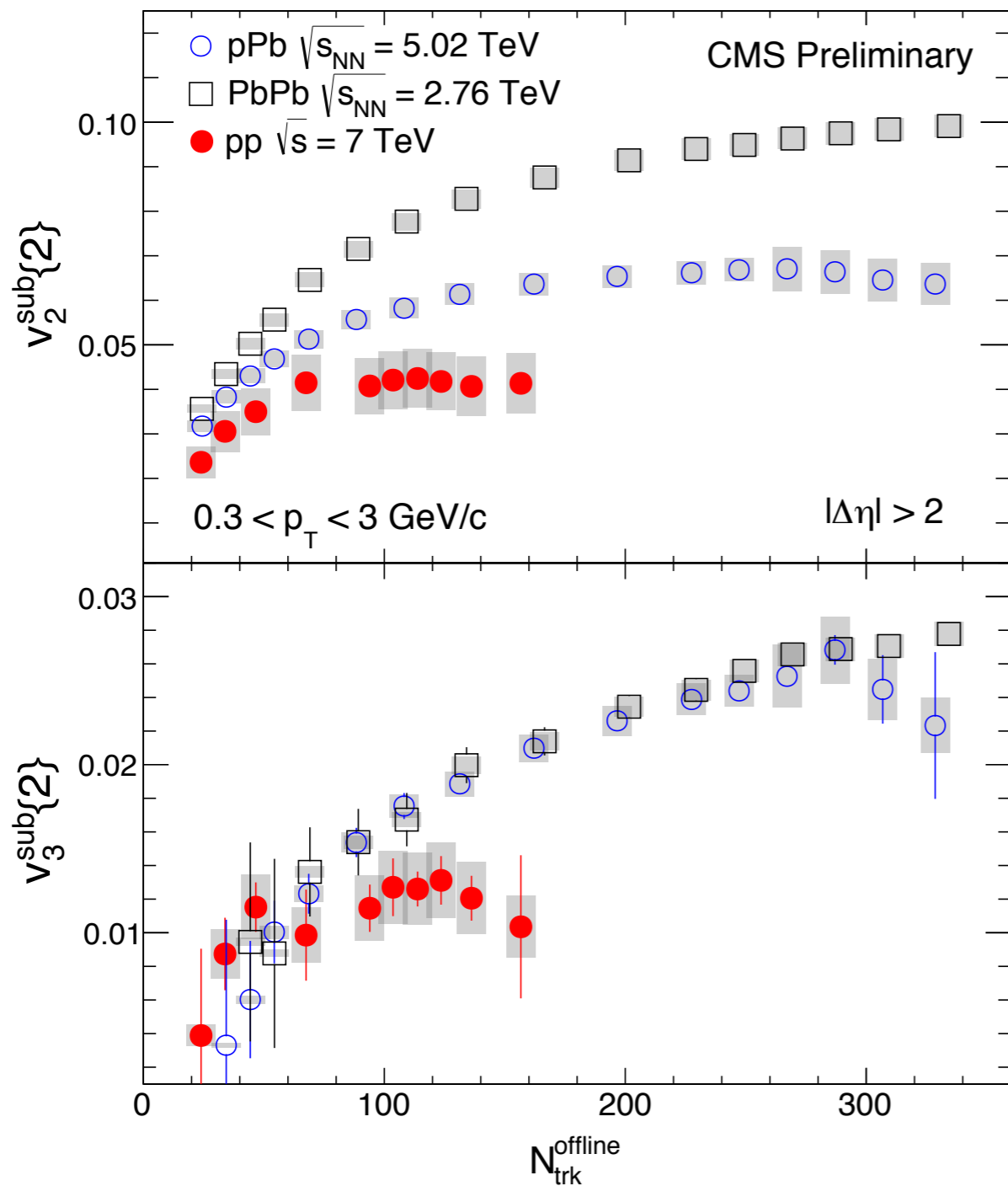


ALICE COLLABORATION, PHYS. LETT. B 719 (2013) 29

ATLAS COLLABORATION, PHYS. REV. LETT. 110 (2013) 182302

CMS COLLABORATION, PHYS. LETT. B 718 (2013) 795

# $v_2$ IN p+p, p+Pb, Pb+Pb COLLISIONS



SEE ALSO:

ALICE COLLABORATION  
 PHYS. LETT. B719 (2013) 29-41;  
 PHYS. REV. C 90, 054901

ATLAS COLLABORATION  
 PHYS. REV. LETT. 110, 182302  
 (2013); PHYS. REV. C 90.044906  
 (2014)

CMS COLLABORATION  
 PHYS.REV.LETT. 115, 012301 (2015)

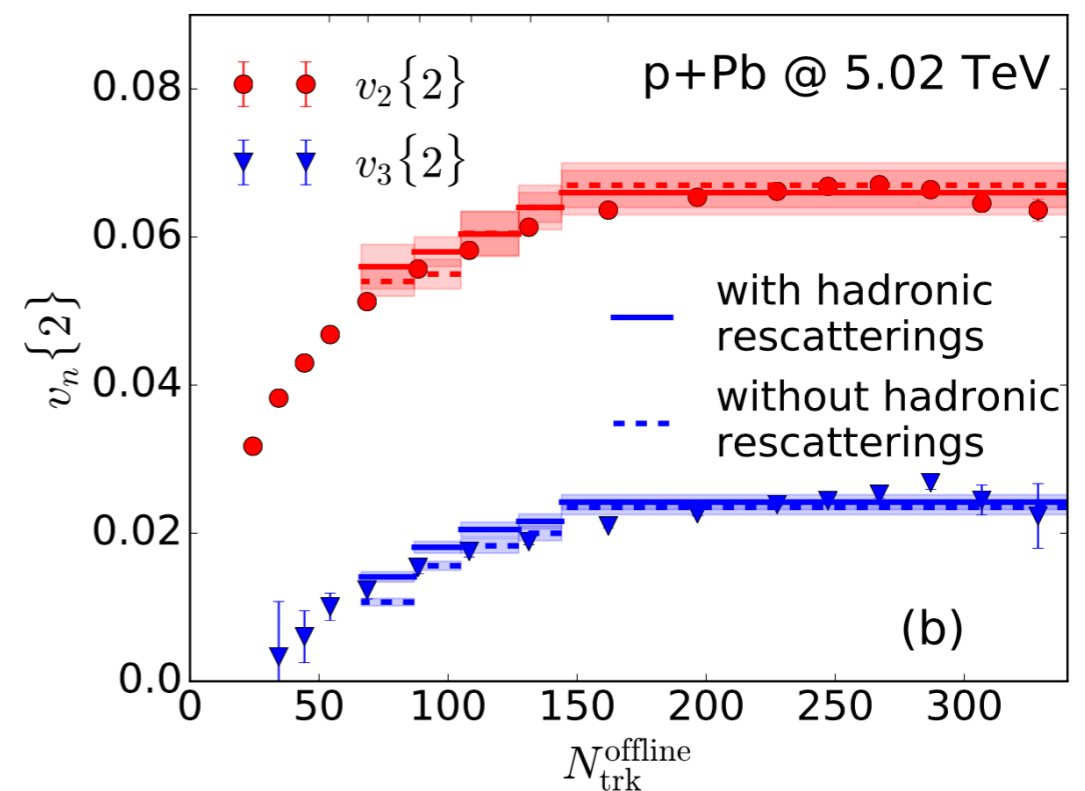
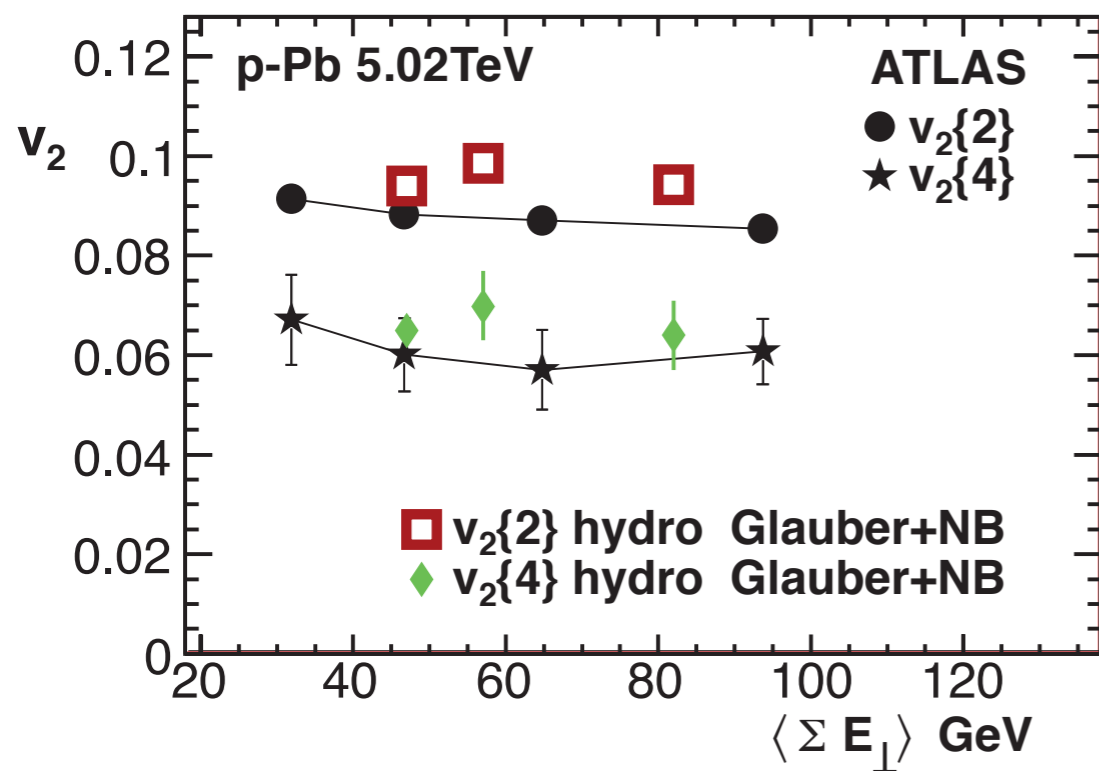


# HYDRO IN SMALL SYSTEMS

MC-Glauber initial state + viscous hydrodynamics works

ATLAS Coll. PLB725 (2013) 60-78

CMS Coll. PLB724, 213–240 (2013)



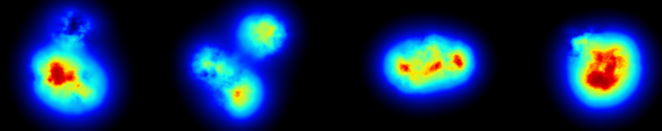
Bozek, Broniowski, PRC88 (2013) 014903

Shen, Paquet, Denicol, Jeon, Gale, PRC95 (2017) 014906

Also see: Kozlov, Luzum, Denicol, Jeon, Gale; Werner, Beicher, Guiot, Karpenko, Pierog; Romatschke; Kalaydzhyan, Shuryak, Zahed; Ghosh, Muhuri, Nayak, Varma; Qin, Mueller; Bozek, Broniowski, Torrieri; Habich, Miller, Romatschke, Xiang; T. Hirano, K. Kawaguchi, K. Murase; ...

# IP-Glasma + hydro + fluctuating proton geometry

H. Mäntysaari, B. Schenke, C. Shen, P. Tribedy, *Phys. Lett. B* 772, 681–686 (2017)

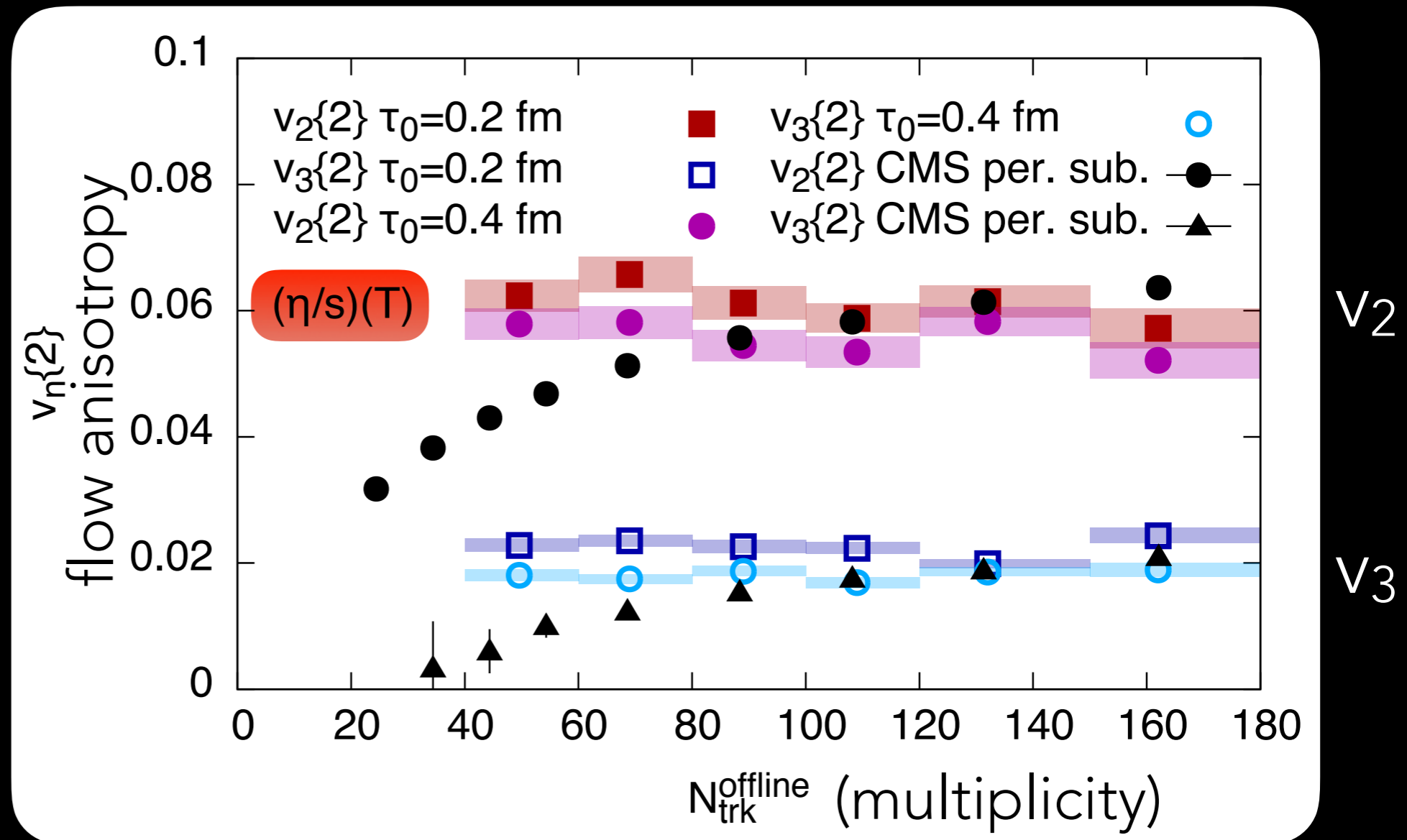


Constrain that fluctuating geometry by HERA diffractive  $J/\Psi$  prod.

H. Mäntysaari, B. Schenke, *Phys. Rev. Lett.* 117 (2016) 052301; *Phys. Rev. D* 94 (2016) 034042

Round proton  
would produce  
much smaller  $v_n$

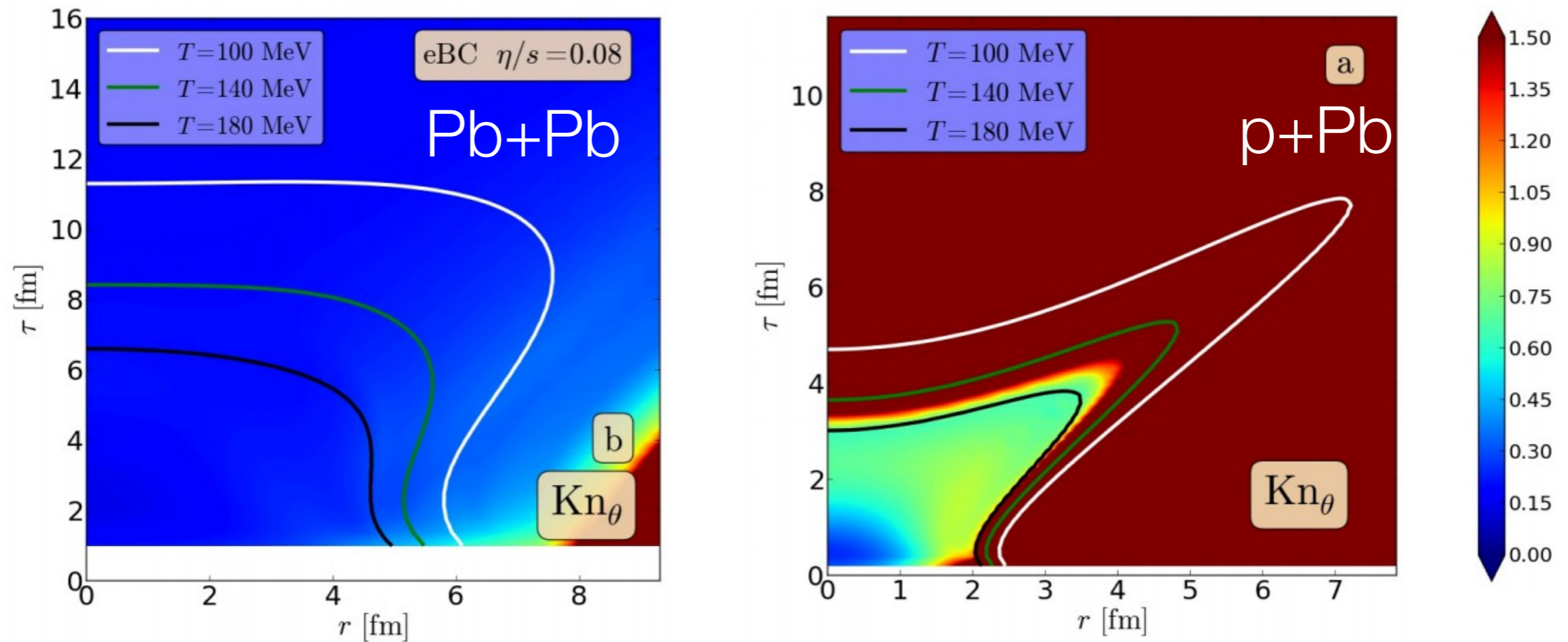
Would not  
describe the  
data





# CAN WE TRUST HYDRODYNAMICS?

Knudsen number: ratio of a microscopic over macroscopic scale  
Small Knudsen number means hydrodynamics is valid



H. NIEMI, G.S. DENICOL, E-PRINT: ARXIV:1404.7327

see review [W. Florkowski, M. P. Heller, M. Spalinski, Rept.Prog.Phys. 81 \(2018\) 046001](#) on recent progress in understanding the validity of relativistic hydrodynamics in systems with large gradients

SEE TALK BY S. FLOERCHINGER ON TUESDAY

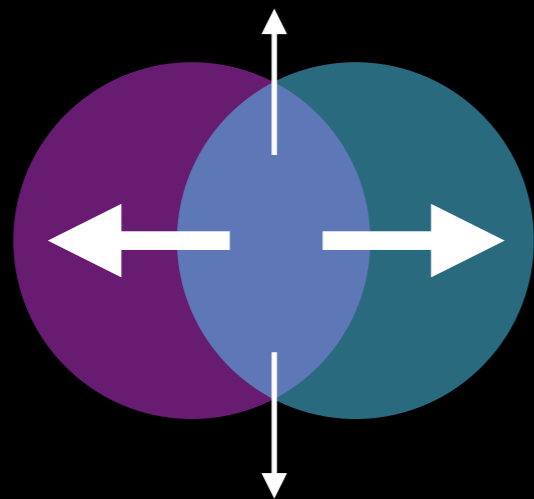
# KINETIC THEORY "ANISOTROPIC ESCAPE"

A. Bzdak, G.-L. Ma, PRL113 (2014) 252301; G.-L. Ma, A. Bzdak, PLB739 (2014) 209-213;

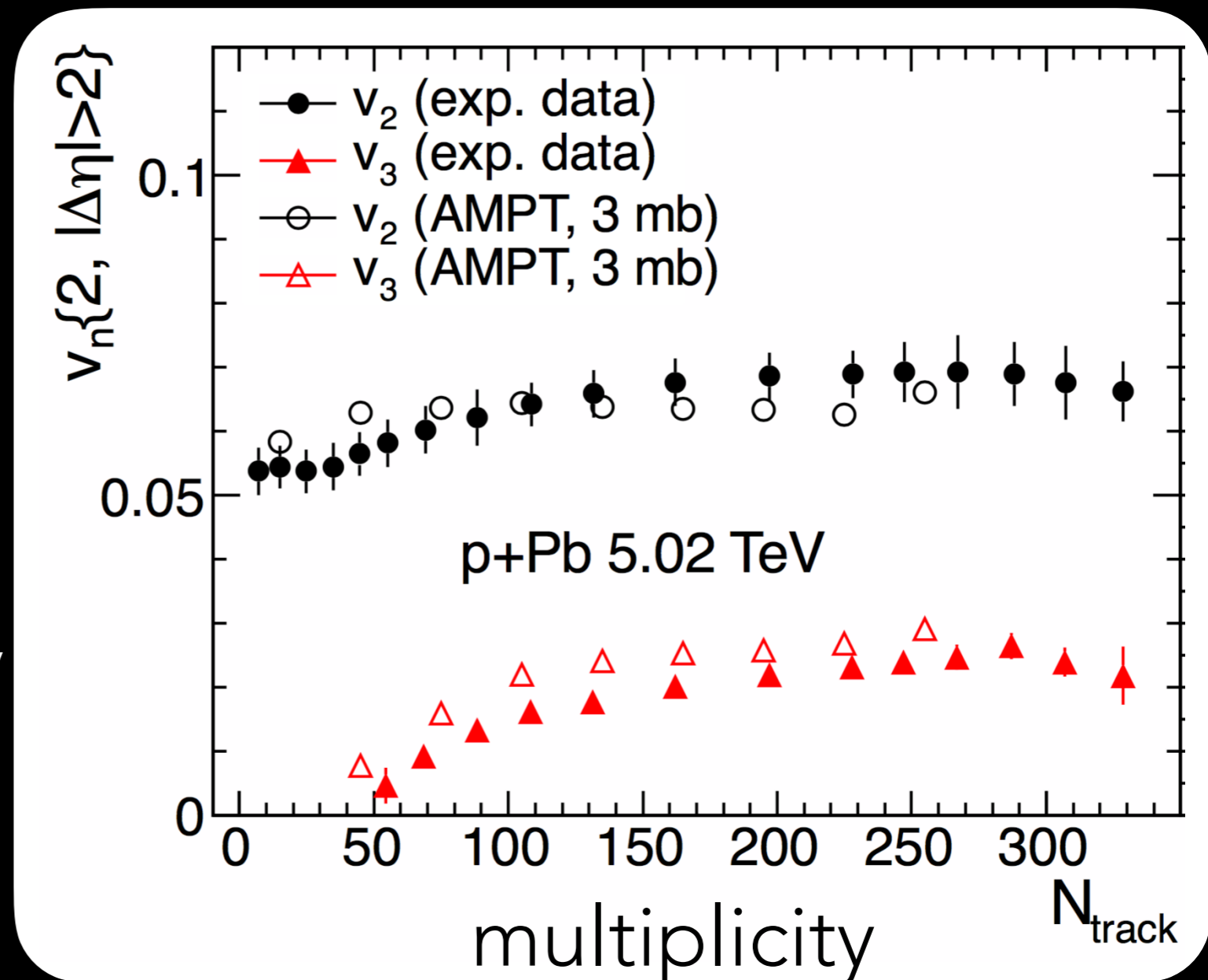
J.D. Orjuela Koop, A. Adare, D. McGlinchey, J.L. Nagle, PRC92 (2015) 054903; P. Bozek, A. Bzdak, G.-L. Ma, PLB748 (2015) 301-305; L. He, T. Edmonds, Z.-W. Lin, F. Liu, D. Molnar, F. Wang, PLB753 (2016)

Final state effect, but weakly interacting (3 mb x-sect.)

Described in AMPT

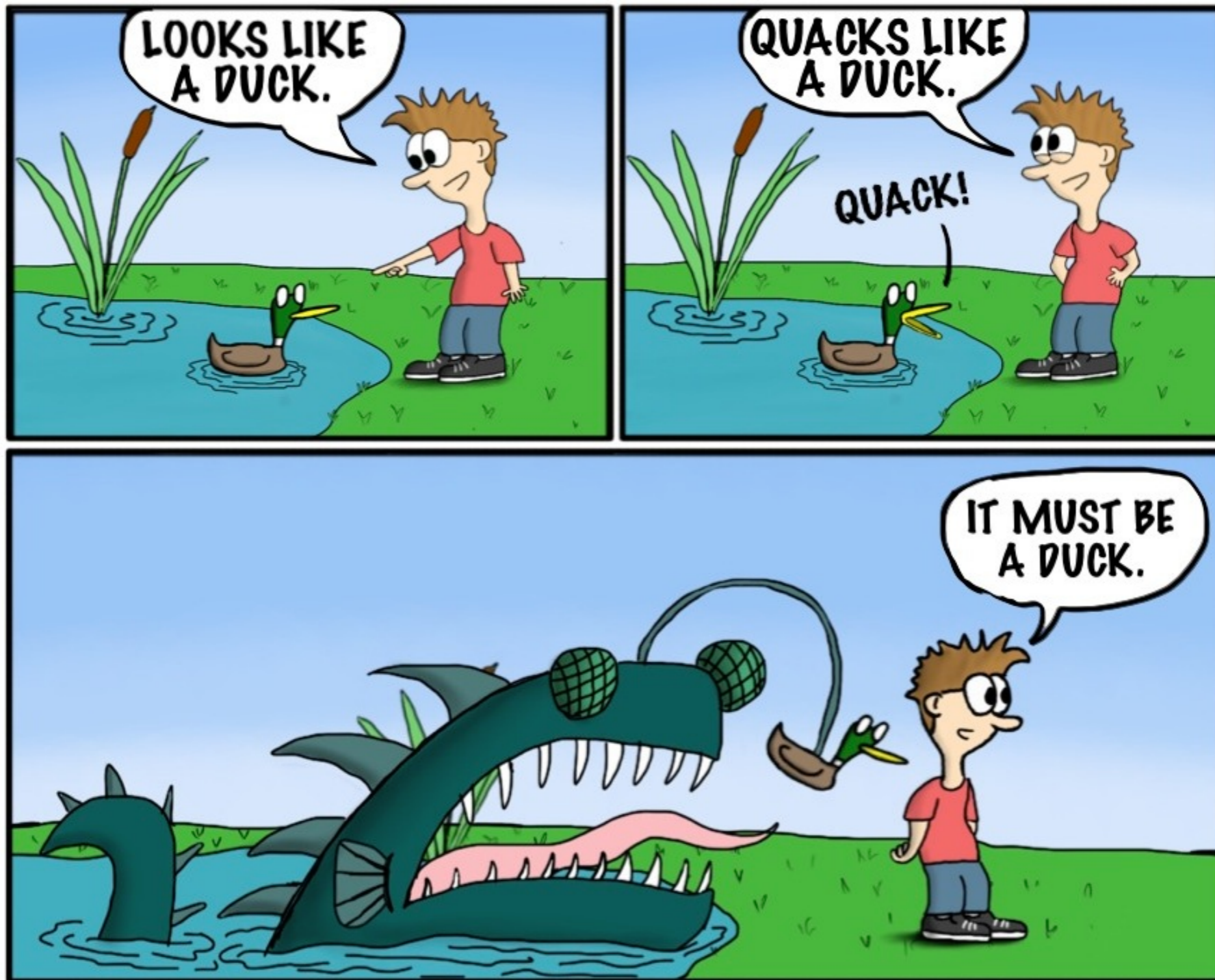


Partons are more likely to escape in the short direction  $\rightarrow v_n$



also see Kurkela, Wiedemann, Wu, arXiv:1803.02072

# INITIAL STATE MOMENTUM CORRELATIONS



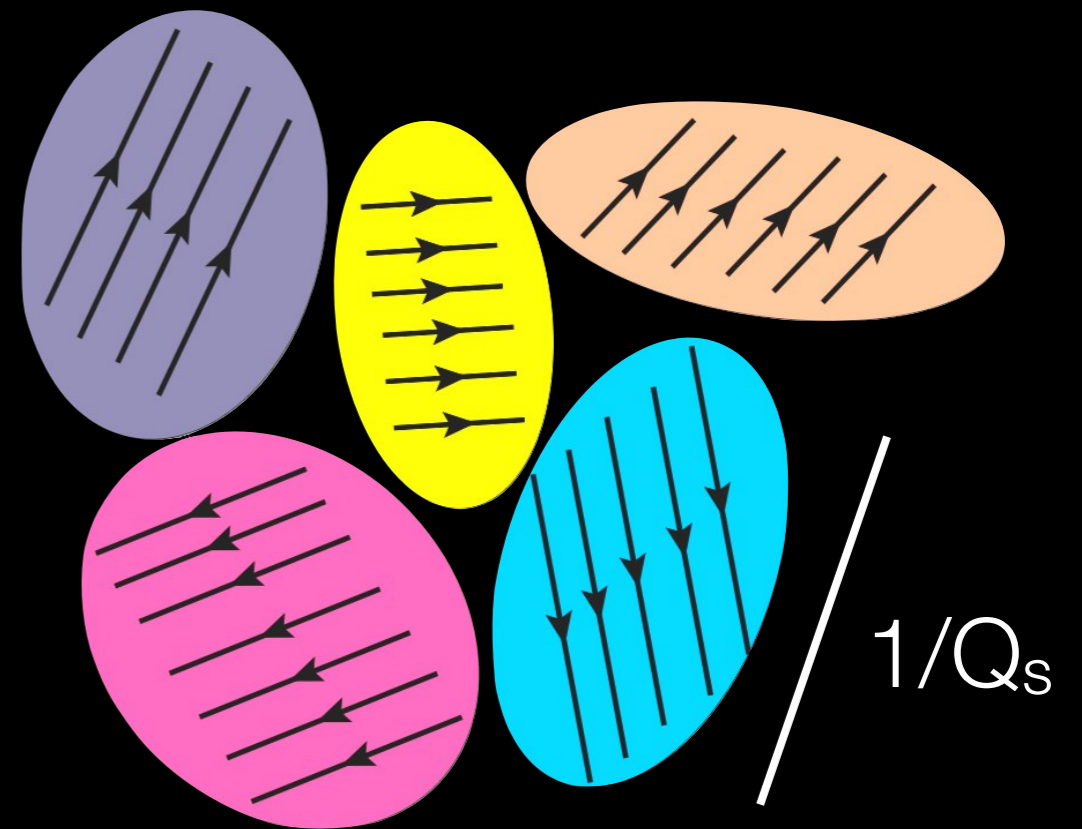


# INITIAL STATE PICTURE

## Intuitive picture:

Quarks or gluons are produced from color field domains in the Pb or p target

Particles that come from the same domain are correlated

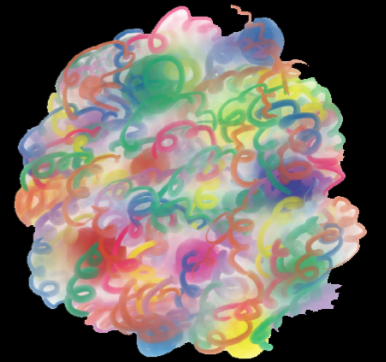


Effect is suppressed by the number of colors and the number of domains (it is small for heavy ions)

FIGURE: T. LAPPI, B. SCHENKE, S. SCHLICHTING, R. VENUGOPALAN  
JHEP 1601 (2016) 061; SEE ALSO: A. DUMITRU, A.V. GIANNINI, NUCL.PHYS.A933 (2014)  
212; A. DUMITRU, V. SKOKOV, PHYS.REV.D91 (2015) 074006; A. DUMITRU  
L. MCLERRAN, V. SKOKOV, PHYS.LETT.B743 (2015), 134;  
V. SKOKOV. PHYS.REV.D91 (2015) 054014

# INITIAL STATE PICTURE

High-multiplicity events are rare configurations of nuclear wave-function with large number of small-x gluons



Situation described by the **Color Glass Condensate** an effective theory of QCD at high energy.

Particle production is governed by the **Yang Mills equations**

$$[D_\mu, F^{\mu\nu}] = J^\nu$$

$J^\nu$ : Combination of incoming target and projectile color currents

**This is it.**

Different approximations and assumptions on the market



# APPROXIMATIONS

- **Glasma graph approximation:** two gluon exchange (not more) and Gaussian statistics of color charges (MV model)

Gelis, Lappi Venugopalan PRD 78 054020 (2008), PRD 79 094017 (2009); Dumitru, Gelis, McLerran, Venugopalan NPA810, 91 (2008); Dumitru, Jalilian-Marian PRD 81 094015 (2010); Dusling, Venugopalan PRD 87 (2013), ...

- **Non-linear Gaussian approximation:**

Resums multi-gluon exchanges - still Gaussian statistics

McLerran, Venugopalan, PRD 59 (1999) 094002; Dominguez, Marquet, Wu, NPA 823 (2009) 99; Lappi, Schenke, Schlichting, Venugopalan, JHEP 1601 (2016) 061; ...

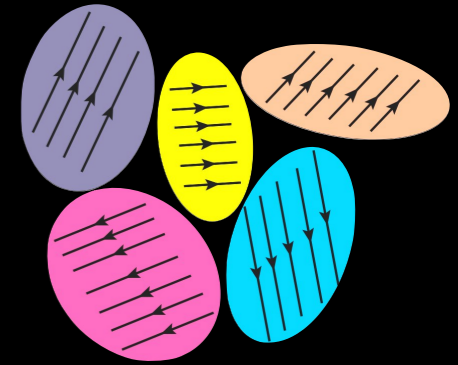
- **Numerical solution:** Solves the Yang-Mills equations exactly for any initial color source statistics and spatial configuration, includes multiple-gluon exchange, "rescattering"

Krasnitz, Venugopalan, NPB 557 (1999) 237; Krasnitz, Nara, Venugopalan, NPA 717 (2003) 268; Lappi, PRC 67 (2003) 054903; Schenke, Tribedy, Venugopalan, PRL 108 (2012) 252301; Schenke, Schlichting, Venugopalan, PLB 747, 76-82 (2015), ...

- One can add **JIMWLK** evolution which will introduce leading quantum correction and (some) non-Gaussian correlations

J. Jalilian-Marian, A. Kovner, A. Leonidov, and H. Weigert, NPB504, 415 (1997), PRD59, 014014 (1999)  
E. Iancu, A. Leonidov, and L. D. McLerran, NPA692, 583 (2001); A. H. Mueller, PLB523, 243 (2001)  
Lappi, PLB 744 (2015) 315-319, ...

# INITIAL STATE PICTURE GENERATES ANISOTROPY



Gelis, Lappi Venugopalan PRD 78 054020 (2008), PRD 79 094017 (2009)

Dumitru, Gelis, McLerran, Venugopalan NPA810, 91 (2008); Dumitru, Jalilian-Marian PRD 81 094015 (2010);

A. Dumitru, K. Dusling, F. Gelis, J. Jalilian-Marian, T. Lappi, R. Venugopalan, PLB697 (2011) 21-25

Dusling, Venugopalan PRD 87 (2013) 5, 051502; PRD 87 (2013) 5, 054014; PRD 87 (2013) 9, 094034

## CAN WE DISTINGUISH INITIAL FROM FINAL STATE EFFECTS?

Many possibilities. Different observables.

I will focus on studying

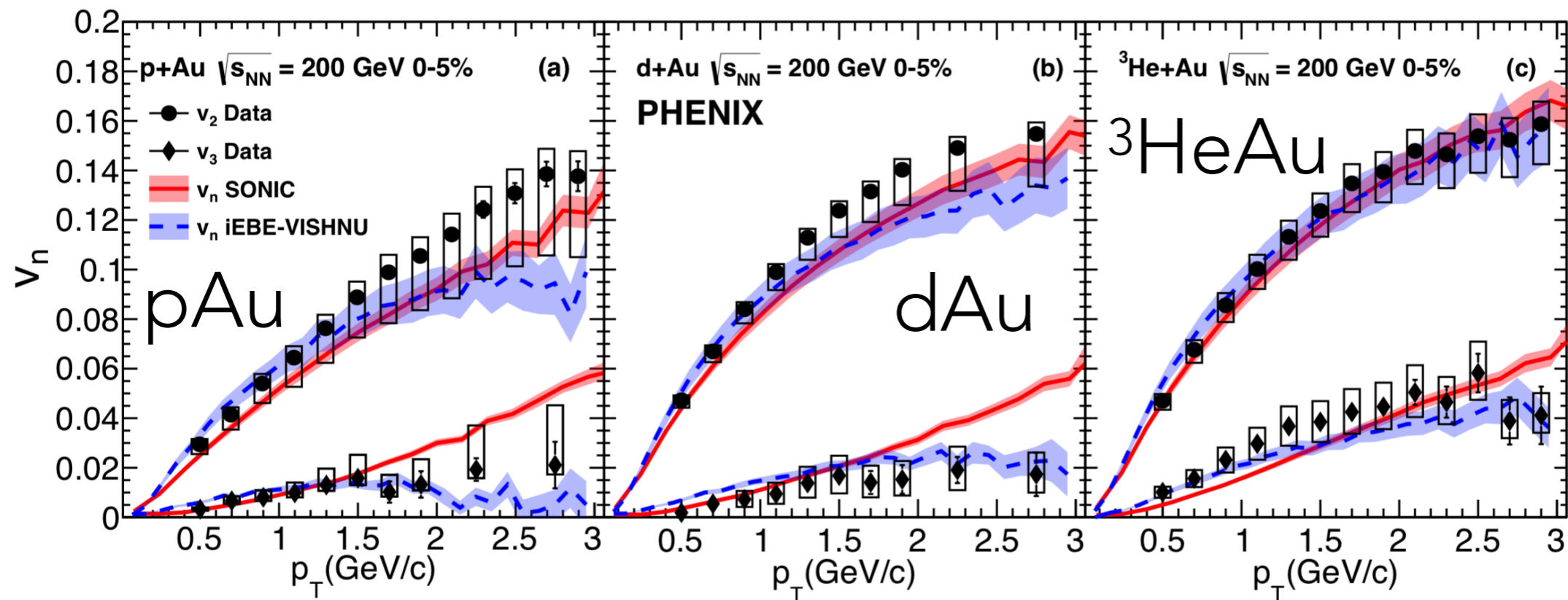
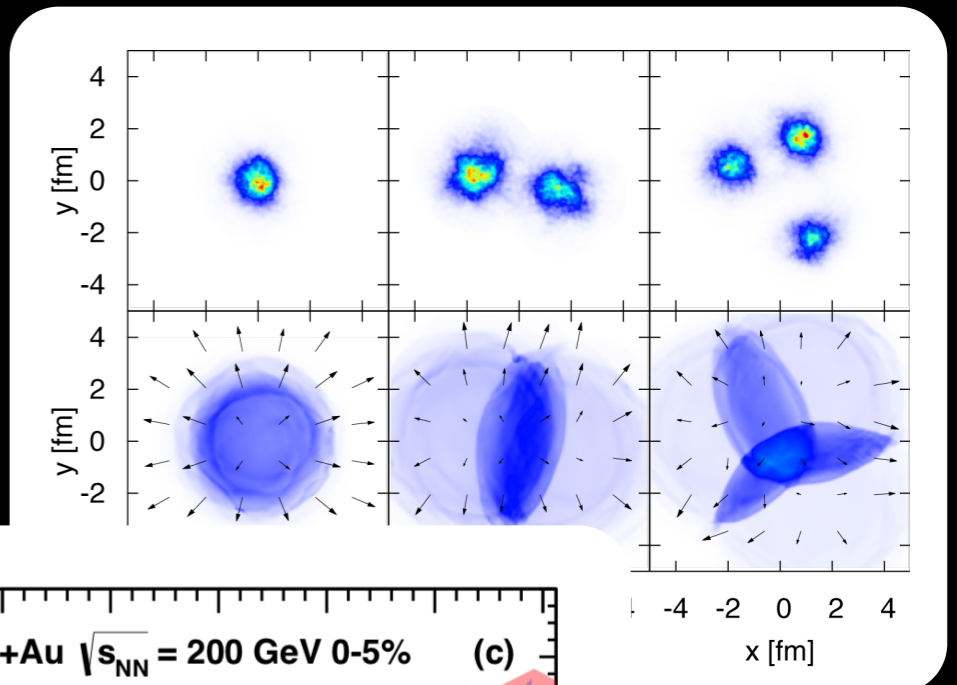
**Different collision systems: Allow to control initial geometry**

They are (were?) the most promising tool

# SYSTEM DEPENDENCE OF ANISOTROPIES

Hydrodynamics converts initial shape to momentum anisotropy.

At RHIC different systems with different average shapes were studied.



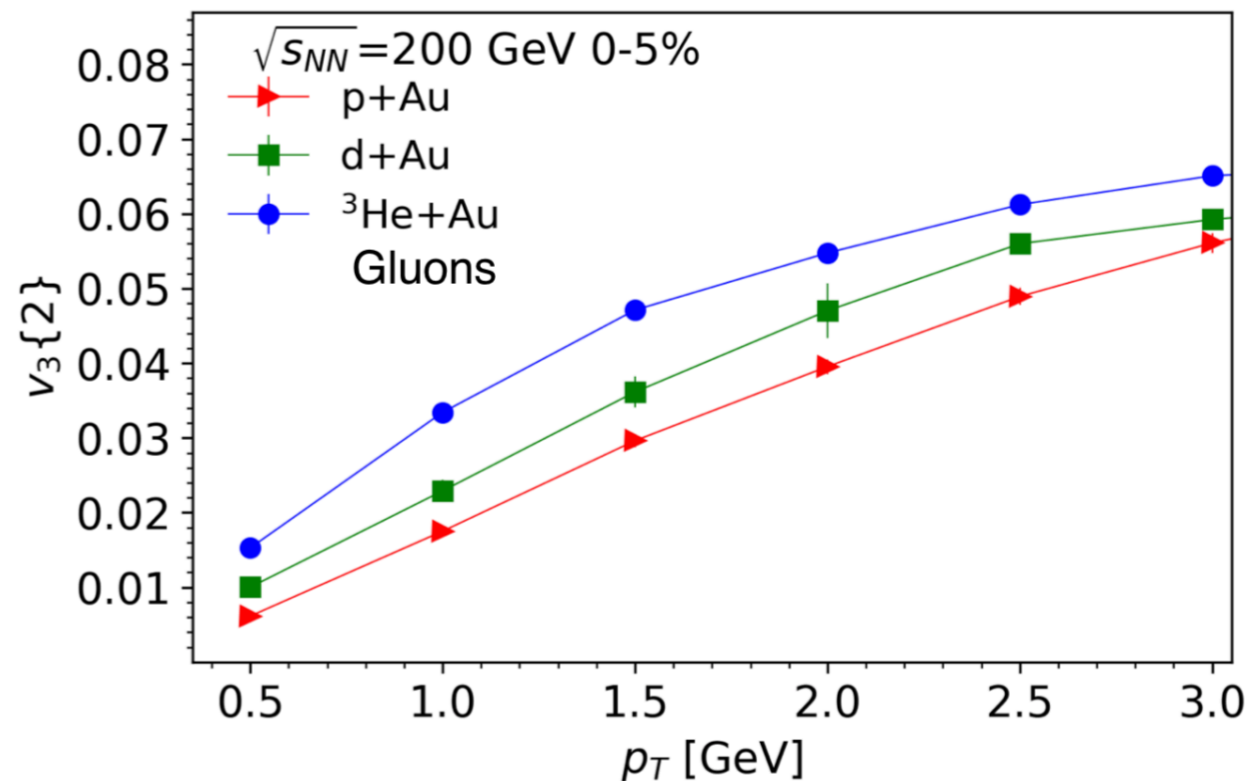
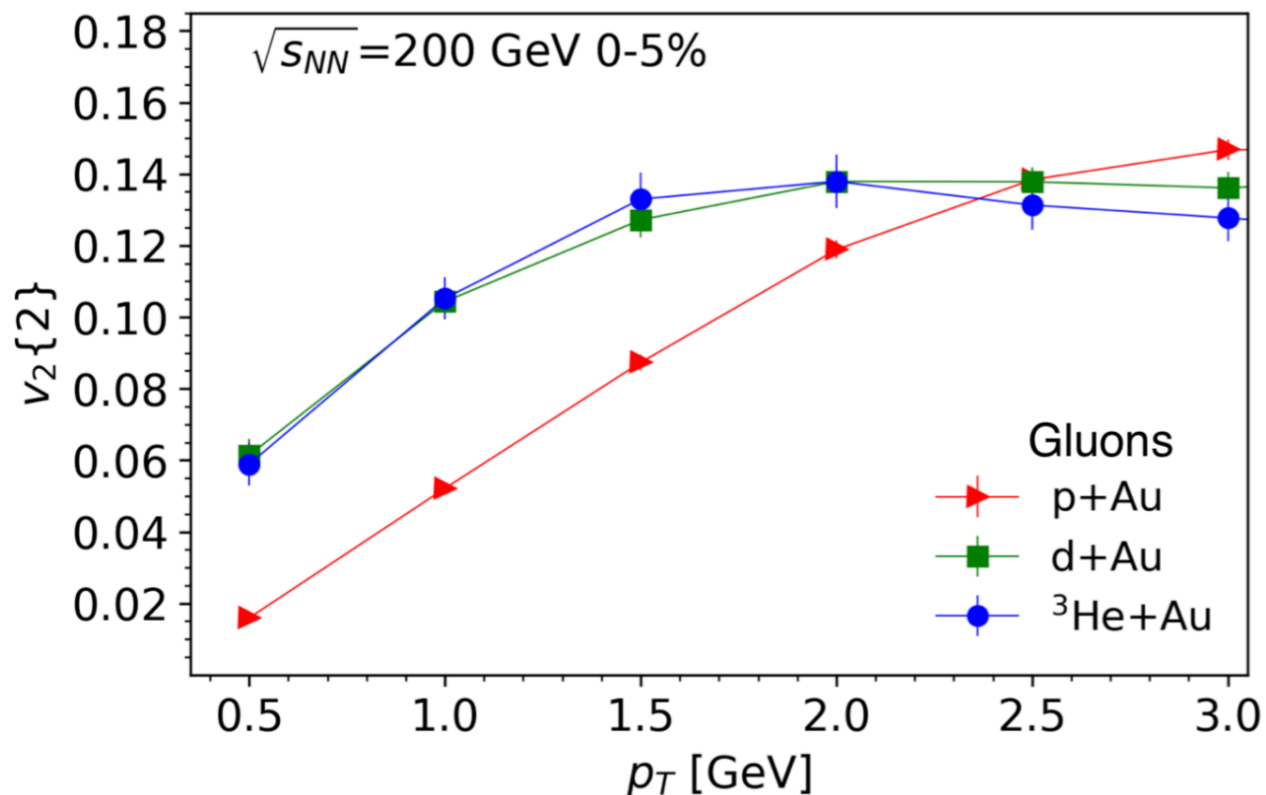
PHENIX, arXiv:1805.02973

Hydrodynamics correctly describes anisotropies in different systems

OTHER CALCULATIONS: BOZEK, BRONIEWSKI, PLB739 (2014) 308; NAGLE ET AL, PRL113 (2014); BOZEK, BRONIEWSKI, PLB747 (2015) 135; SCHENKE, VENUGOPALAN, NPA931 (2014) 1039; ROMATSCHKE, EUR. PHYS. J. C75 (2015) 305

# SYSTEM DEPENDENCE OF ANISOTROPIES

Recent results from **initial state** momentum correlations:



Mark Mace, Vladimir V. Skokov, Prithwish Tribedy, Raju Venugopalan, arXiv:1805.09342

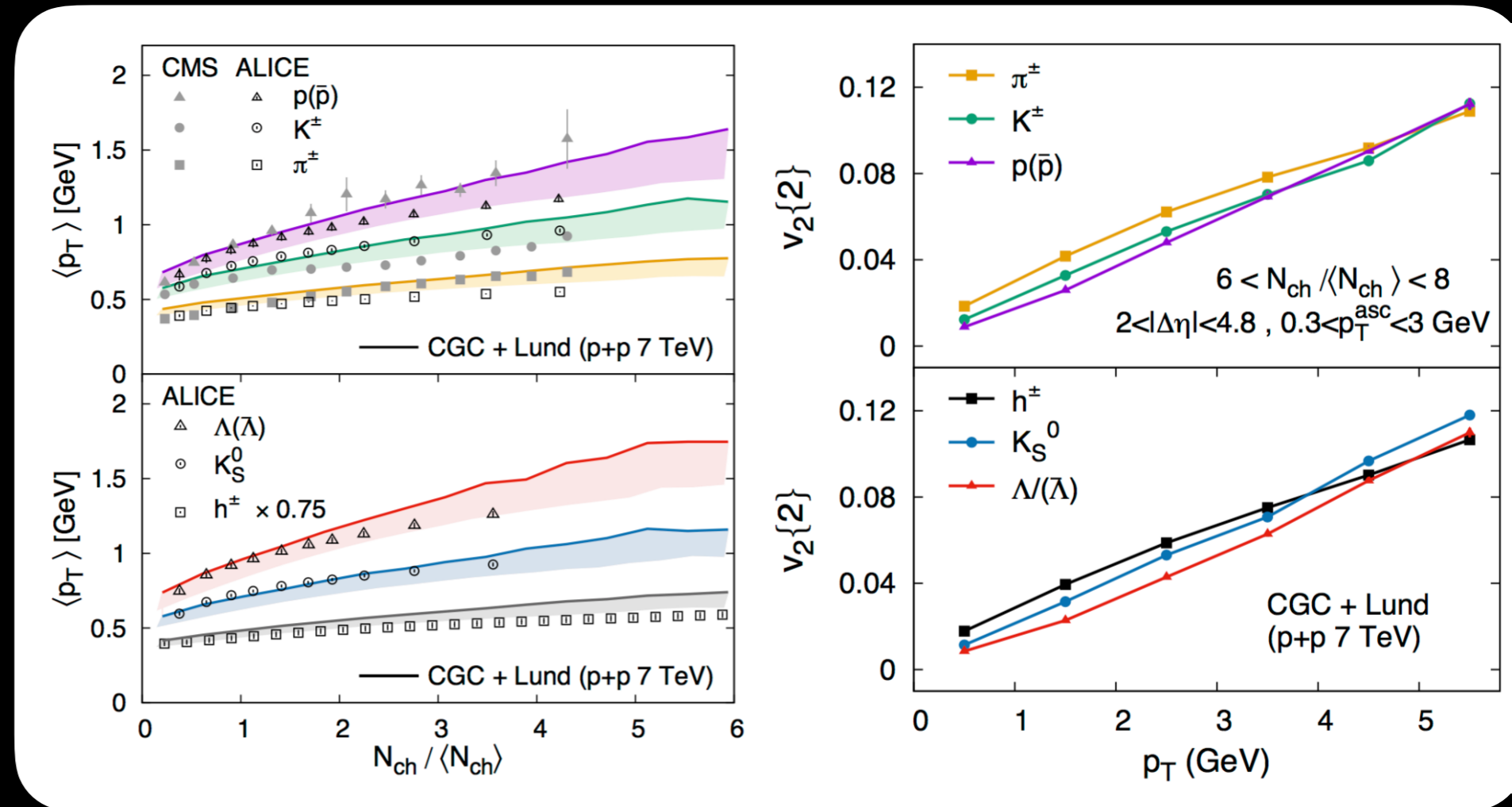
System dependence present when selecting 0-5% central events (which have different multiplicities in different systems)

# IP-GLASMA + ~~HYDRO~~ + LUND

B. Schenke, S. Schlichting, P. Tribedy, R. Venugopalan, Phys. Rev. Lett. 117, 162301 (2016)

First step towards an event generator with dense initial gluon fields and Lund fragmentation

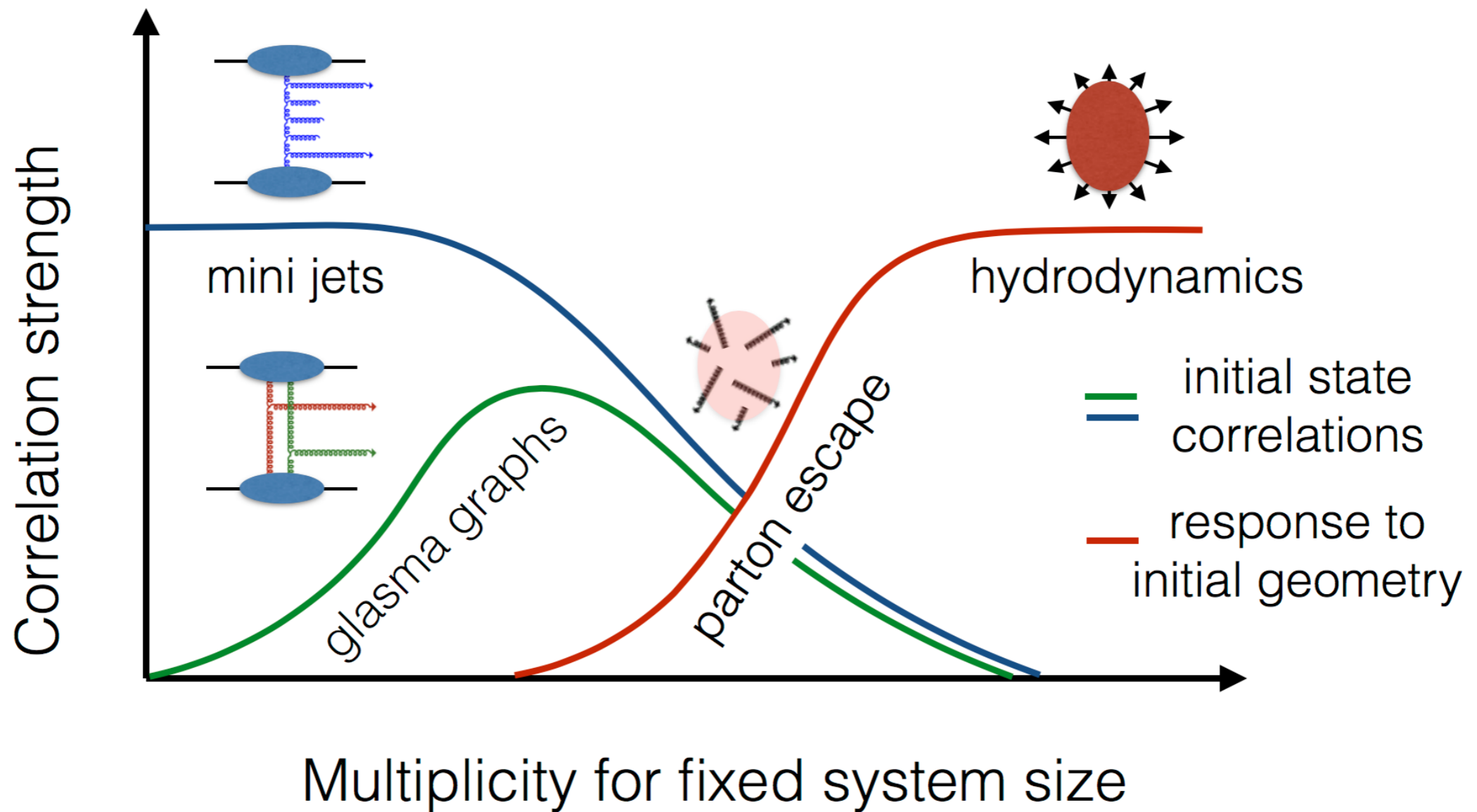
Sample gluons and connect with Lund strings  
Arrange similar to what color reconnection would do



Emission from common boosted source: mass splitting



# STUDY RELATIVE STRENGTH OF INITIAL AND FINAL STATE CORRELATIONS IN THEORY



S. Schlichting, Quark Matter 2015

**Calculate** the relative contribution of "glasma graphs" and final state effects

# IP-Glasma + parton cascade

M. Greif, C. Greiner, B. Schenke, S. Schlichting, Z. Xu, arXiv:1708.02076, Phys. Rev. D96, 091509(R)

To study how final state interactions affect the initial state correlations, we use a microscopic final state model, the parton cascade BAMPS

Z.Xu, C. Greiner, PRC71, 064901 (2005)



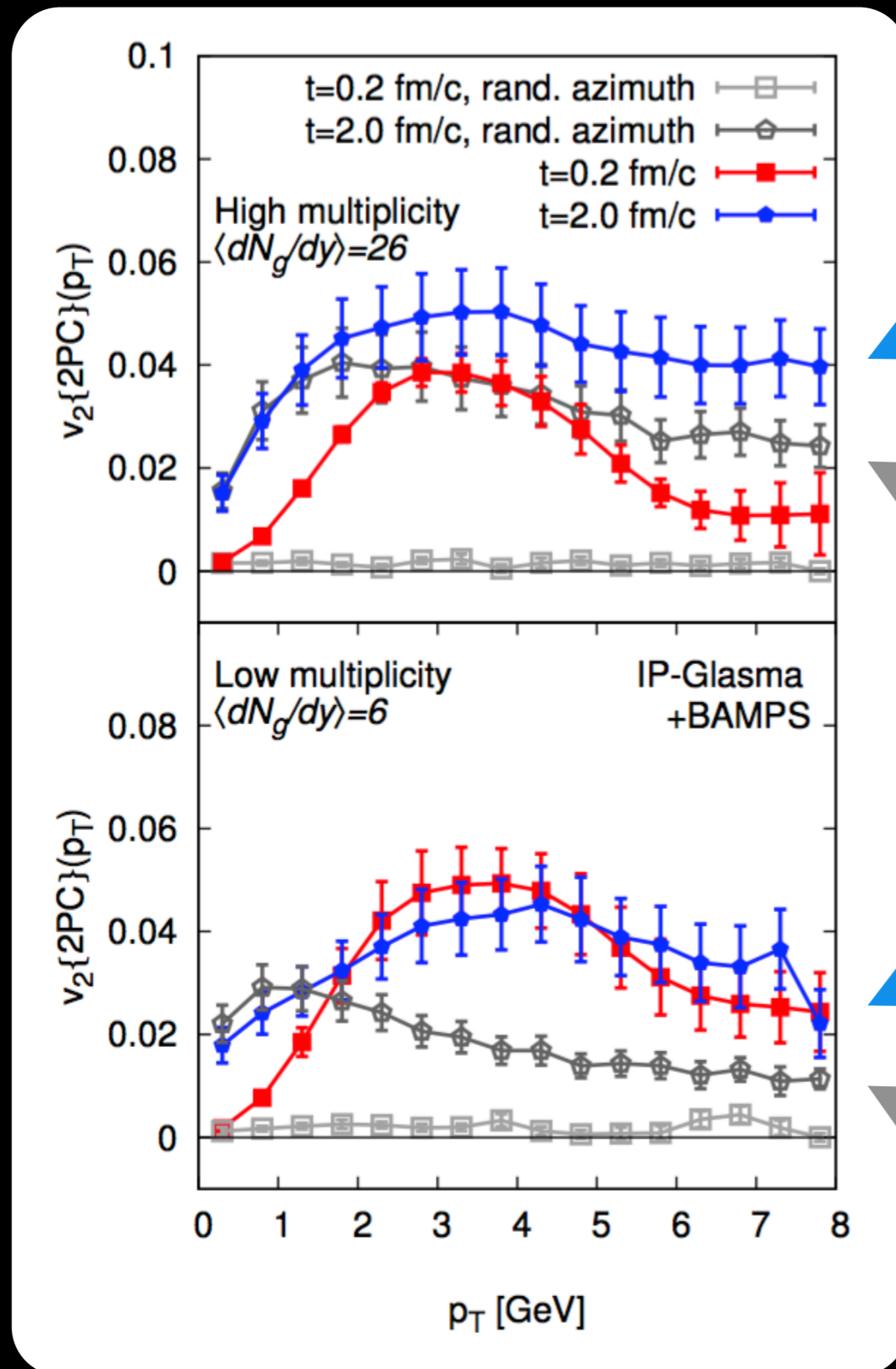
smear → Husimi Distribution

➔ study momentum anisotropy as function of time

# Effect of initial correlations on final $v_2$

M. Greif, C. Greiner, B. Schenke, S. Schlichting, Z. Xu, arXiv:1708.02076, Phys. Rev. D96, 091509(R)

high  
multiplicity  
low  
multiplicity



with initial corr.

without initial corr.

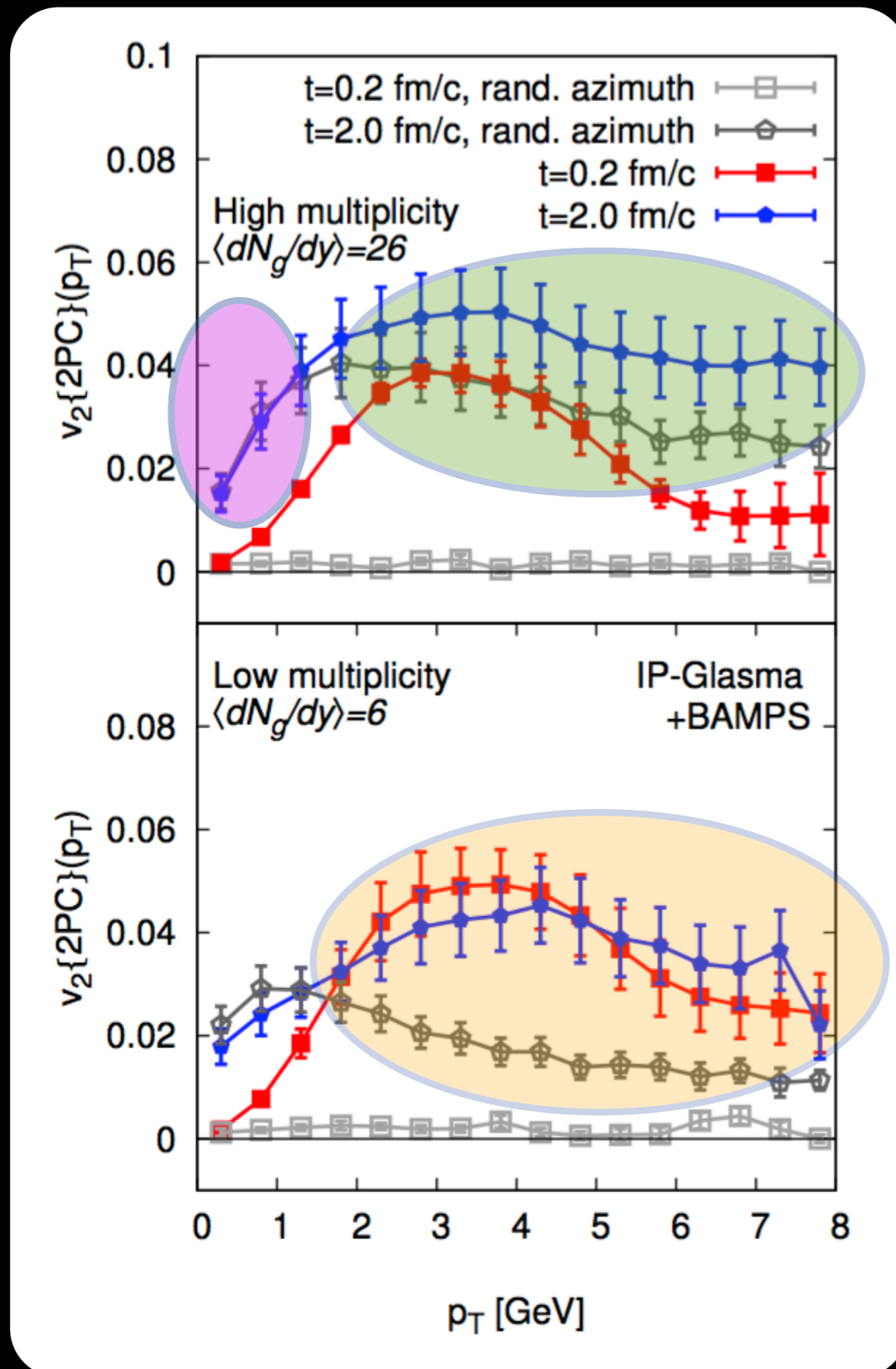
with initial corr.

without initial corr.

# Effect of initial correlations on final $v_2$

M. Greif, C. Greiner, B. Schenke, S. Schlichting, Z. Xu, arXiv:1708.02076, Phys. Rev. D96, 091509(R)

high  
multiplicity  
low  
multiplicity



- negligible effect at small  $p_T$  and high multiplicity
- significant effect at  $p_T > 2$  GeV and low multiplicity
- visible effect at  $p_T > 3$  GeV and high multiplicity

# CONCLUSIONS & OUTLOOK

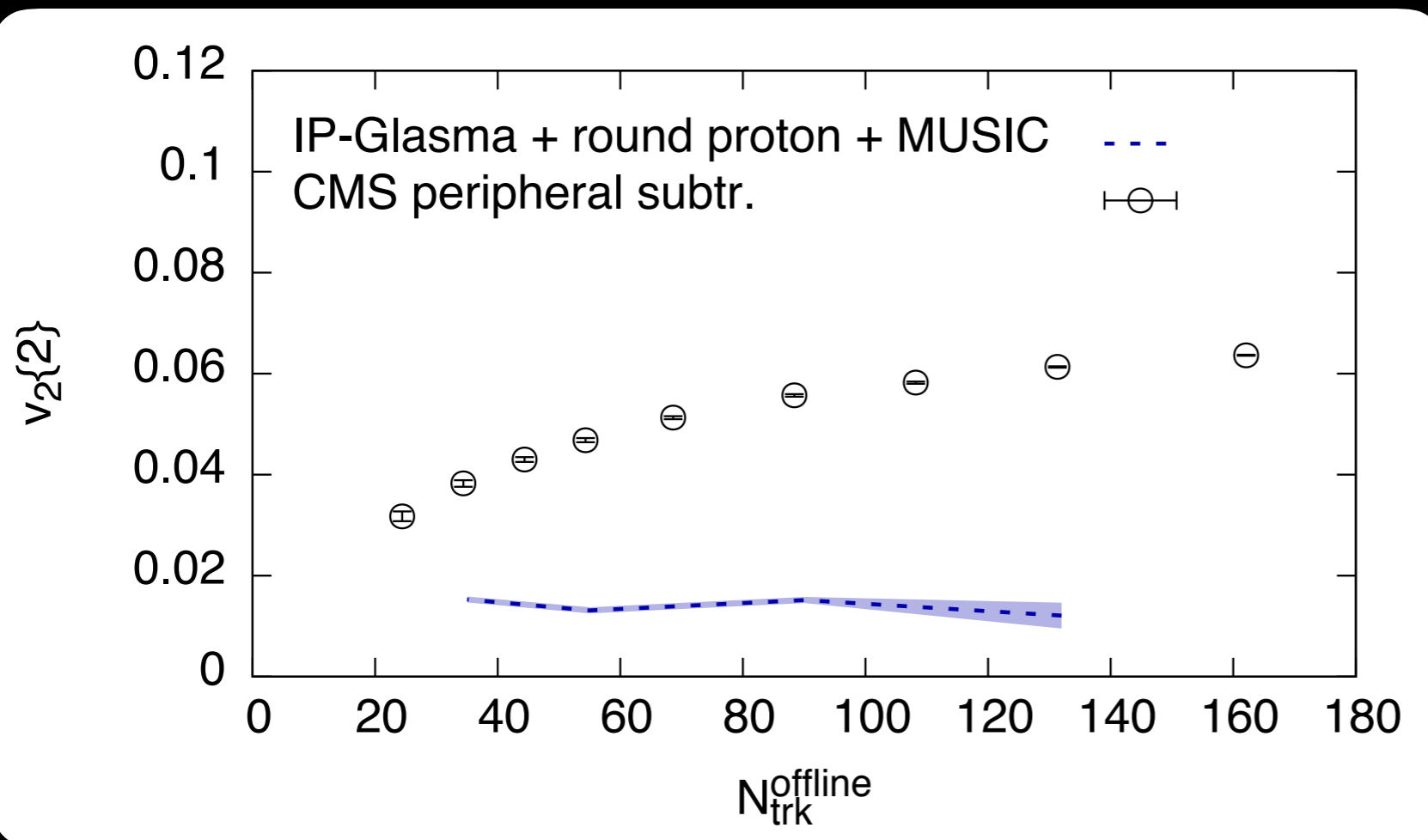
- Multi-particle correlation measurements in small systems ( $p+p$ ,  $p/d/He+A$ ) have revealed interesting structures
- There are contributions from initial momentum anisotropies in the QCD particle production
- With increasing multiplicity, final state effects become important: similar to  $A+A$  collisions - QGP in  $p+p$ ?
- Our standard event generators apparently miss this important physics. Work in progress for PYTHIA final state effects. What about the production process in high multiplicity events?



# BACKUP

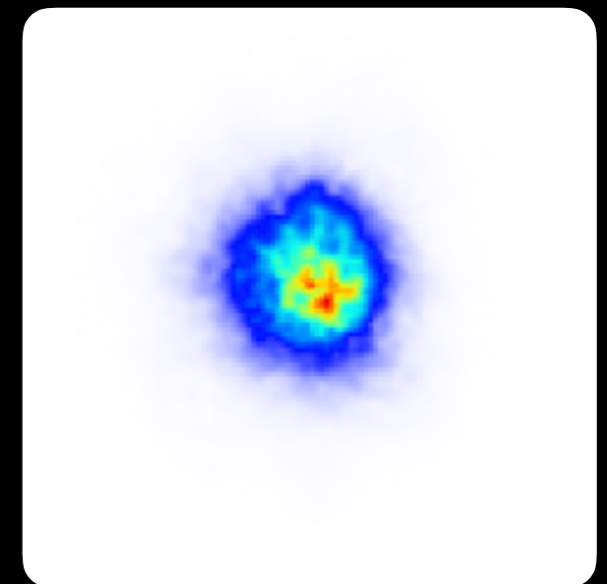
# p + Pb $v_2$ from IP-GLASMA + Hydro

Model worked well in A+A. In p+A it did not.  
Not because hydro does not work.  
But because initial state was missing physics.

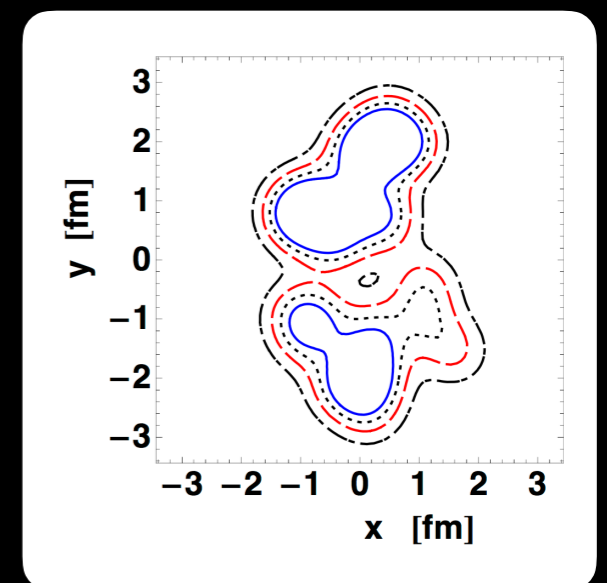


B. Schenke, R. Venugopalan, *Phys. Rev. Lett.* **113**, 102301 (2014)  
Experimental data: CMS Collaboration, *Phys.Lett.* **B724**, 213 (2013)

## IP-Glasma



## MC-Glauber

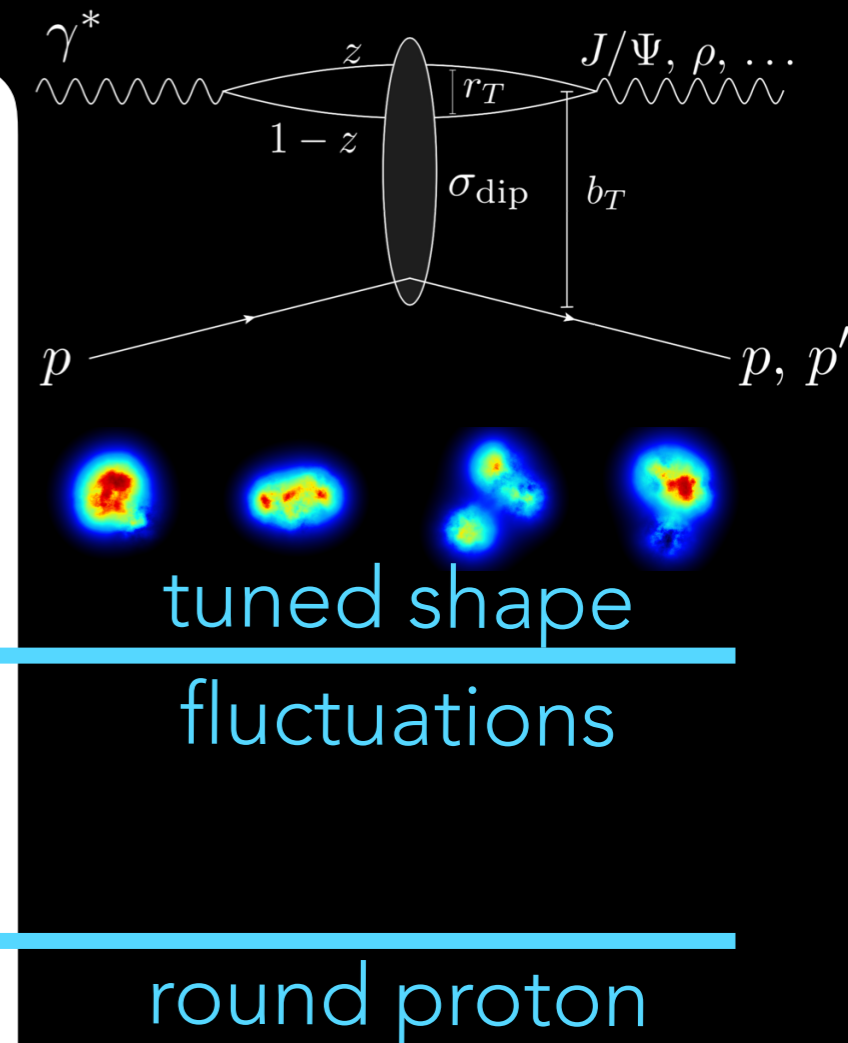
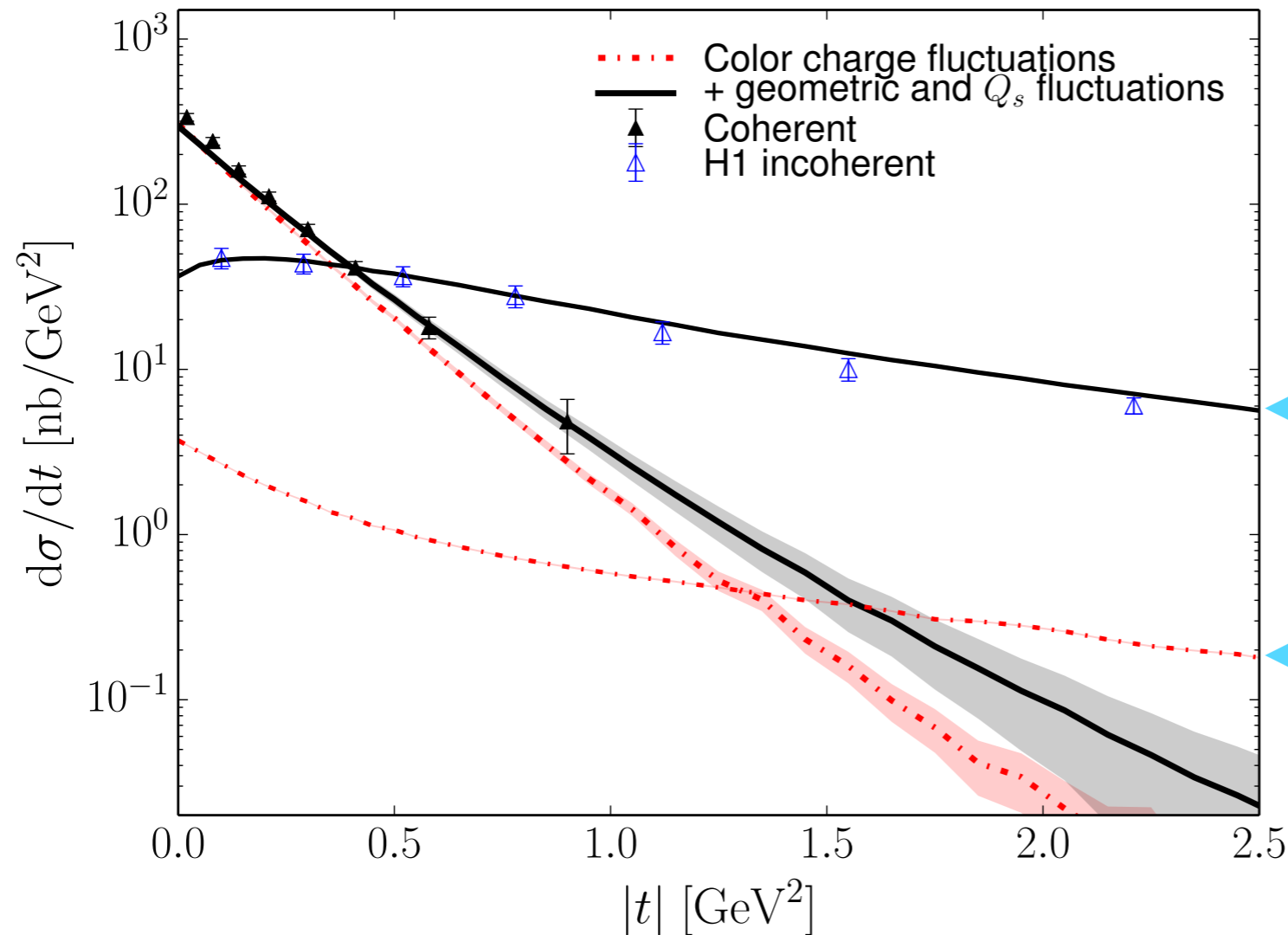


P. Bozek, *Phys.Rev.* **C85** (2012) 014911

# NEED PROTON SHAPE FLUCTUATIONS!

H. Mäntysaari, B. Schenke, Phys. Rev. Lett. 117 (2016) 052301; Phys.Rev. D94 (2016) 034042

e+p (HERA) Exclusive diffractive  $J/\Psi$  production:  
Incoherent x-sec sensitive to fluctuations



# MULTI-PARTICLE CUMULANTS

Hydrodynamics produces  $\sim$ equal  $v_2\{2m\}$  for all  $m \geq 4$

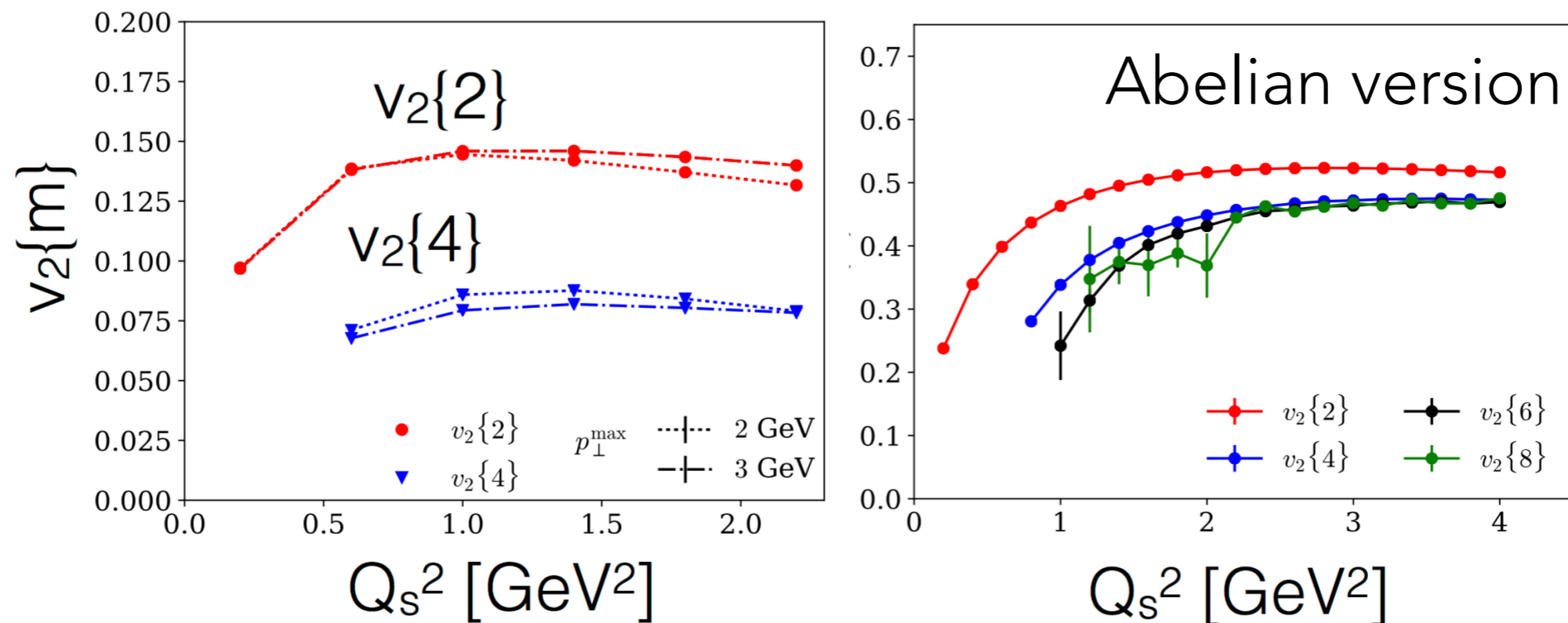
All particles correlated with a common event plane

see e.g. L. Yan, J.-Y. Ollitrault, Phys. Rev. Lett. 112, 082301 (2014)

$v_2\{4\}$  imaginary in 2-gluon exchange approximation

V. Skokov, Phys.Rev. D91 (2015) 054014

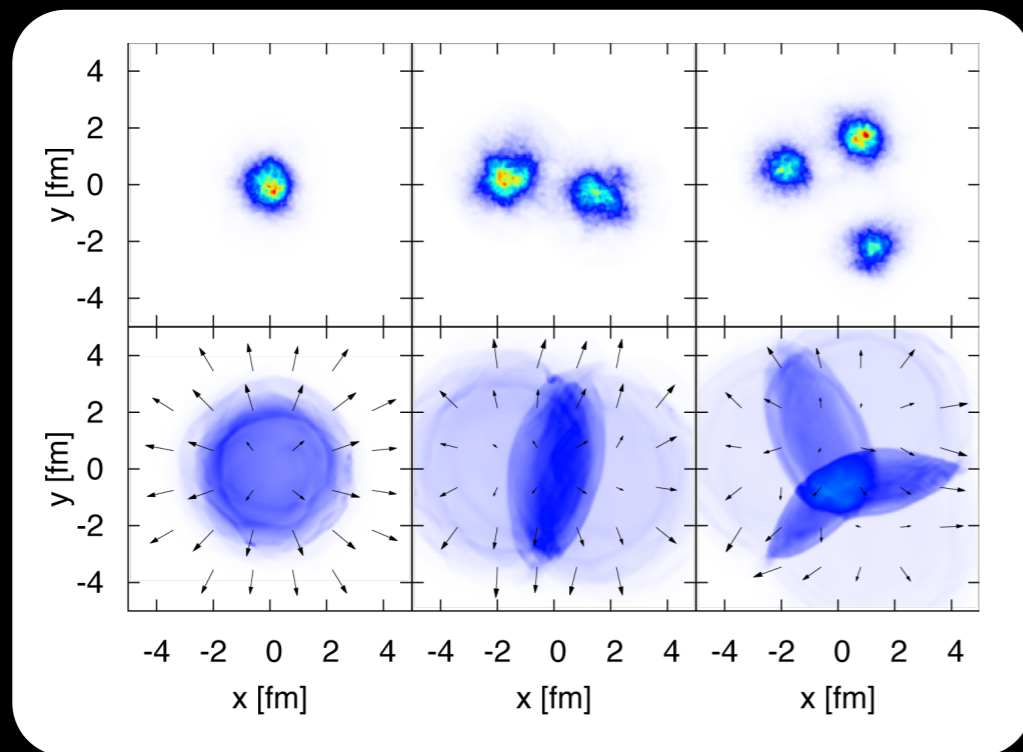
Including multiple interactions will make it real



K. Dusling, M. Mace, R. Venugopalan, Phys.Rev.Lett. 120 (2018) 042002

# HOW TO DISTINGUISH "FLOW" FROM AN "INITIAL STATE" SCENARIO

- **$^3\text{He}+\text{Au}$ ,  $\text{d}+\text{Au}$ :** Systematics of flow in different systems Explained by hydrodynamics. Initial state: no calculation



MEASUREMENT:

PHENIX COLLABORATION, PRL115,

CALCULATIONS:

BOZEK, BRONIOWSKI, PLB739 (2014) 308

NAGLE ET AL, PRL113 (2014)

BOZEK, BRONIOWSKI, PLB747 (2015) 135

SCHENKE, VENUGOPALAN, NPA931 (2014) 1039

ROMATSCHKE, EUR. PHYS. J. C75 (2015) 305

- Higher order cumulants: Data shows that

$$v_2\{4\} \approx v_2\{6\} \approx v_2\{8\} \dots$$

Natural in hydrodynamics but not a unique feature



# HOW TO DISTINGUISH "FLOW" FROM AN "INITIAL STATE" SCENARIO

- **Mass splitting of mean  $p_T$  and  $v_n$ :**  
Natural in any situation where particles are produced from a common boosted source: e.g. fluid cell, strings
- **$c_2\{4\}$  turning positive** as multiplicity increases  
could mean collectivity sets in but also alternative explanations  
[DUMITRU, MCLERRAN, SKOKOV, PHYS.LETT. B743 \(2015\) 134-137](#)
- **HBT:** Relative radii in p+p, p+Pb and Pb+Pb: Data favors description that yields similar radii in p+p and p+Pb  
[ALICE COLLABORATION, PHYS. LETT. B 739 \(2014\) 139-151](#)

# APPROXIMATIONS

- **Glasma graph approximation:** two gluon exchange (not more) and Gaussian statistics of color charges (MV model)

Gelis, Lappi Venugopalan PRD 78 054020 (2008), PRD 79 094017 (2009); Dumitru, Gelis, McLerran, Venugopalan NPA810, 91 (2008); Dumitru, Jalilian-Marian PRD 81 094015 (2010); Dusling, Venugopalan PRD 87 (2013), ...

- **Non-linear Gaussian approximation:**

Resums multi-gluon exchanges - still Gaussian statistics

McLerran, Venugopalan, PRD 59 (1999) 094002; Dominguez, Marquet, Wu, NPA 823 (2009) 99; Lappi, Schenke, Schlichting, Venugopalan, JHEP 1601 (2016) 061; ...

- **Numerical solution:** Solves the Yang-Mills equations exactly for any initial color source statistics and spatial configuration, includes multiple-gluon exchange, "rescattering"

Krasnitz, Venugopalan, NPB 557 (1999) 237; Krasnitz, Nara, Venugopalan, NPA 717 (2003) 268; Lappi, PRC 67 (2003) 054903; Schenke, Tribedy, Venugopalan, PRL 108 (2012) 252301; Schenke, Schlichting, Venugopalan, PLB 747, 76-82 (2015), ...

- One can add **JIMWLK** evolution which will introduce (some) non-Gaussian correlations

J. Jalilian-Marian, A. Kovner, A. Leonidov, and H. Weigert, NPB504, 415 (1997), PRD59, 014014 (1999)

E. Iancu, A. Leonidov, and L. D. McLerran, NPA692, 583 (2001); A. H. Mueller, PLB523, 243 (2001)

Lappi, PLB 744 (2015) 315-319, ...