

SO(10) × S₄ Grand Unified Theory of flavour and Leptogenesis

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Motivation

Flavour problem

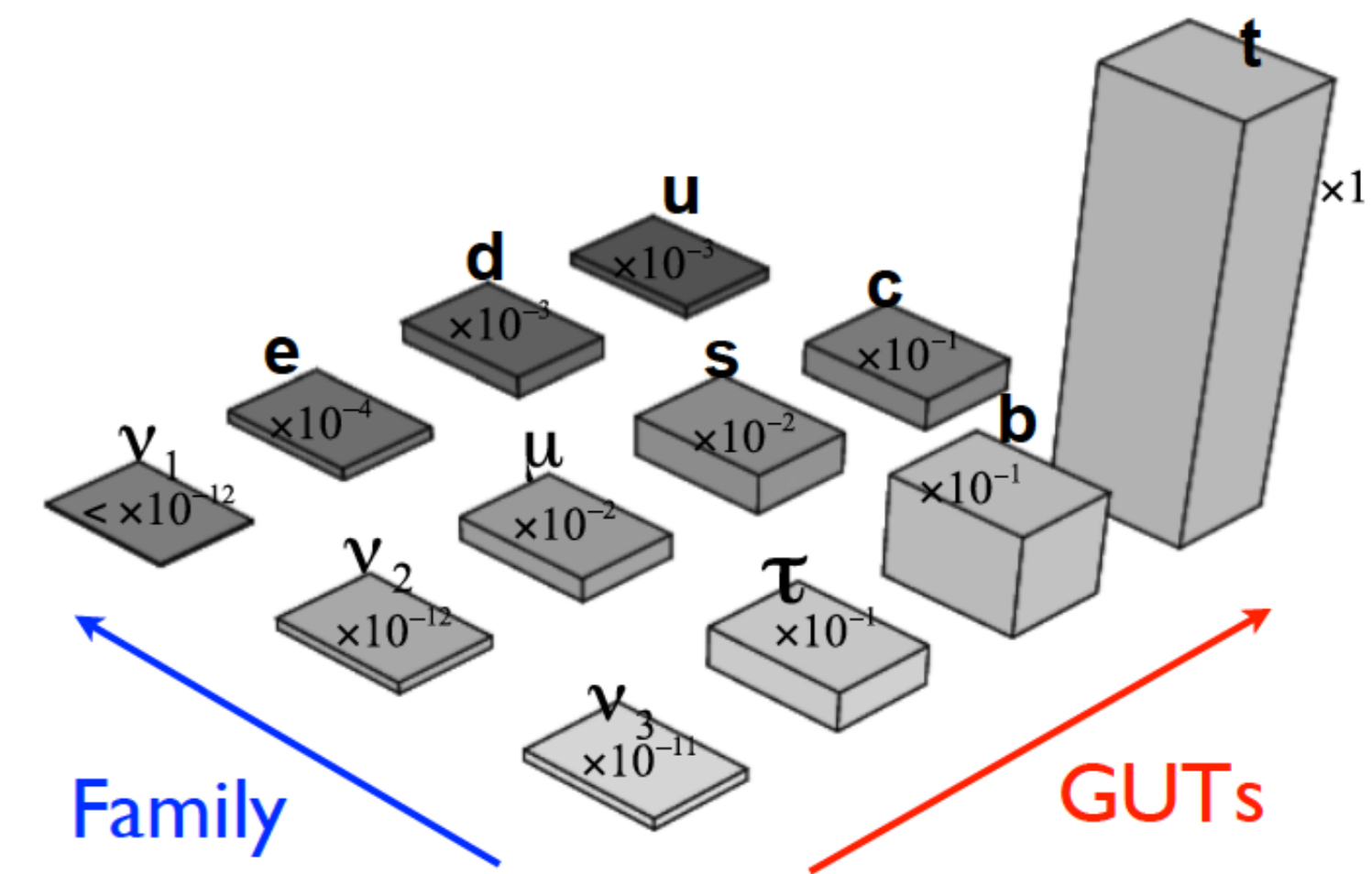
Origin of the three families of quarks and leptons. Very hierarchical charged fermion masses, small and hierarchical quark mixing, small neutrino masses and large lepton mixing.

Family symmetry

A non-Abelian discrete symmetry imposes constraints on the Yukawa couplings and reproduces precise predictions for masses and mixing. S₄ enforces CSD(2).

Grand Unified Theory

Unifies fermions within each family and reproduces an universal mass matrix structure, predicting relationships between quark and lepton Yukawa matrices.



Unified model of flavour

- We present a model with quarks and leptons unified in a single ψ representation of SO(10) × S₄.
- The essential superfields are given in the table below. We only allow small Higgs representations **10**, **16** and **45**.

Field	Representation			
	S ₄	SO(10)	Z ₄ ^R	
ψ	3'	16	1	Quarks and leptons
$H_{10}^{u,d}$	1	10	0	Break electroweak symmetry
$H_{16,16}^{\bar{16}}$	1	$\bar{16}$	0	Break SO(10) and give RH Majorana masses
$H_{45}^{X,Y,W,Z}$	1	45	0	Separate quarks and lepton masses
H_{45}^{B-L}	1	45	2	Gives DT splitting via DW mechanism
ϕ_i	3'	1	0	Acquire CSD(2) vacuum alignments

- The discrete symmetry Z₄^R is broken at the GUT scale by the H₄₅^{B-L} VEV to Z₂^R, the usual R parity in the MSSM.

CSD(2) flavon vacuum alignments

The Yukawa parameters are given a dynamical origin

$$\mathcal{L} \sim \frac{1}{\lambda} \phi H \bar{\psi} \psi \rightarrow \frac{\langle \phi \rangle}{\lambda} H \bar{\psi} \psi \rightarrow y H \bar{\psi} \psi,$$

where the flavon fields break S₄ with the CSD(2) vacuum alignment [1]

$$\langle \phi_1 \rangle = v_1 \begin{pmatrix} 1 \\ 0 \\ 2 \end{pmatrix}, \quad \langle \phi_2 \rangle = v_2 \begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix}, \quad \langle \phi_3 \rangle = v_3 \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix}.$$

VEVs driven to scales with the hierarchy $v_1 \ll v_2 \ll v_3 \sim M_{\text{GUT}}$.

Yukawa matrices

- Up-type quarks and neutrinos couple to one Higgs H₁₀^u, leading to Yukawa matrices $Y_{ij} \sim \langle \phi_i \rangle \langle \phi_j \rangle^T$ with an universal structure

$$Y^{u,v} = y_1^{u,v} \begin{pmatrix} 1 & 2 & 0 \\ 2 & 4 & 0 \\ 0 & 0 & 0 \end{pmatrix} + y_2^{u,v} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 1 & 1 \end{pmatrix} + y_3^{u,v} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}.$$

Natural understanding of the hierarchical Yukawa couplings

$$y_u \sim v_1^2 / M_{\text{GUT}}^2, \quad y_c \sim v_2^2 / M_{\text{GUT}}^2, \quad y_t \sim v_3^2 / M_{\text{GUT}}^2.$$

- Down-type quarks and charged leptons couple to a second Higgs H₁₀^d, with a new mixed term involving $Y_{12} \sim \langle \phi_1 \rangle \langle \phi_2 \rangle^T$

$$Y^{d,e} = y_{12}^{d,e} \begin{pmatrix} 0 & 1 & 1 \\ 1 & 4 & 2 \\ 1 & 2 & 0 \end{pmatrix} + y_2^{d,e} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 1 & 1 \end{pmatrix} + y_3^{d,e} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix} + y^p \begin{pmatrix} 0 & 0 & 1 \\ 0 & 2 & 0 \\ 1 & 0 & 0 \end{pmatrix}.$$

This new term enforces a zero in the (1,1) element of Y^d, giving the GST relation [2] for the Cabbibo angle, i.e. $\vartheta_{12}^q \approx \sqrt{y_d/y_s}$. It also leads to a milder hierarchy in the down and charged lepton sectors.

Seesaw mechanism

The right-handed neutrino (RHN) mass M^R has the same structure as Y^V . The light neutrino mass matrix is obtained by the **type-I seesaw mechanism** [3, 4] and will also have the CSD(2) structure

$$m^V = \mu_1^V \begin{pmatrix} 1 & 2 & 0 \\ 2 & 4 & 0 \\ 0 & 0 & 0 \end{pmatrix} + \mu_2^V \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 1 & 1 \end{pmatrix} + \mu_3^V \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}.$$

The parameters μ_i are given in terms of the parameters y_i^V and M_i^R simply by

$$\mu_i = v_u^2 \frac{(y_i^V)^2}{M_i^R}$$

The flavons yield a light neutrino mass matrix m^V , where the normal hierarchy $m_1 \ll m_2 \ll m_3$ after seesaw is due to the very hierarchical RHN masses.

Numerical fit

The model accurately fits all available quark and lepton data, with 15 input parameters to fit 19 data points and a reduced $\chi^2 \approx 3$. It predicts **normal neutrino hierarchy** and a CP phase δ^l

$$\delta^l \sim 200^\circ$$

The neutrino masses are also predicted

$$m_1 \approx 10.94 \text{ meV}, \quad m_2 \approx 13.95 \text{ meV}, \quad m_3 \approx 51.42 \text{ meV}.$$

The model predicts significant deviation from both zero and maximal CP violation.

N₂ Leptogenesis

- Baryon Asymmetry of the Universe (BAU)

$$\eta_B \equiv \frac{n_B - n_{\bar{B}}}{n_\gamma} = (6.1 \pm 0.1) \times 10^{-10}$$

- Asymmetry generated through CP breaking decays of heavy RHNs into leptons, then converted into baryons through sphalerons [5].
- Leptogenesis generated mainly by the decays of the second RHN “N₂ leptogenesis”.
- Using the parameters from the fit, the correct BAU is generated when

$$M_2 \simeq 1.9 \times 10^{11} \text{ GeV},$$

natural expected value for the second RHN mass.

Conclusion

Simple	Natural	Complete
Minimal field content	No tuning of $\mathcal{O}(1)$ parameters	Renormalisable
Low-dimensional representations	Predictions	Reduces to MSSM μ term of $\mathcal{O}(TeV)$
CSD(2) from S ₄	Neutrino masses	DT splitting
	Normal Hierarchy	Proton decay suppressed
	$\delta^l \sim 200^\circ$	

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[3] P. Minkowski Phys. Lett. B 67 (1977) 421

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