
Results on Diffractive Physics at LHCb



Ronan McNulty (UCD Dublin)
On behalf of the LHCb collaboration



Diffractive and electromagnetic processes at high energies,
WE-Heraeus-Summerschool, Heidelberg, Sept 2-6, 2013

Outline

- Theoretical background and motivation
 - Understanding the vacuum
 - Investigating the pomeron
 - Gluon PDF
 - New phenomena
- Experimental Signatures
- The LHCb experiment
- Analysis and Results
 - Central Exclusive $J/\psi, \psi', \chi_c, \mu\mu$
- Future plans
 - $Y, \Phi, \chi, \eta\eta, X, \text{searches}$

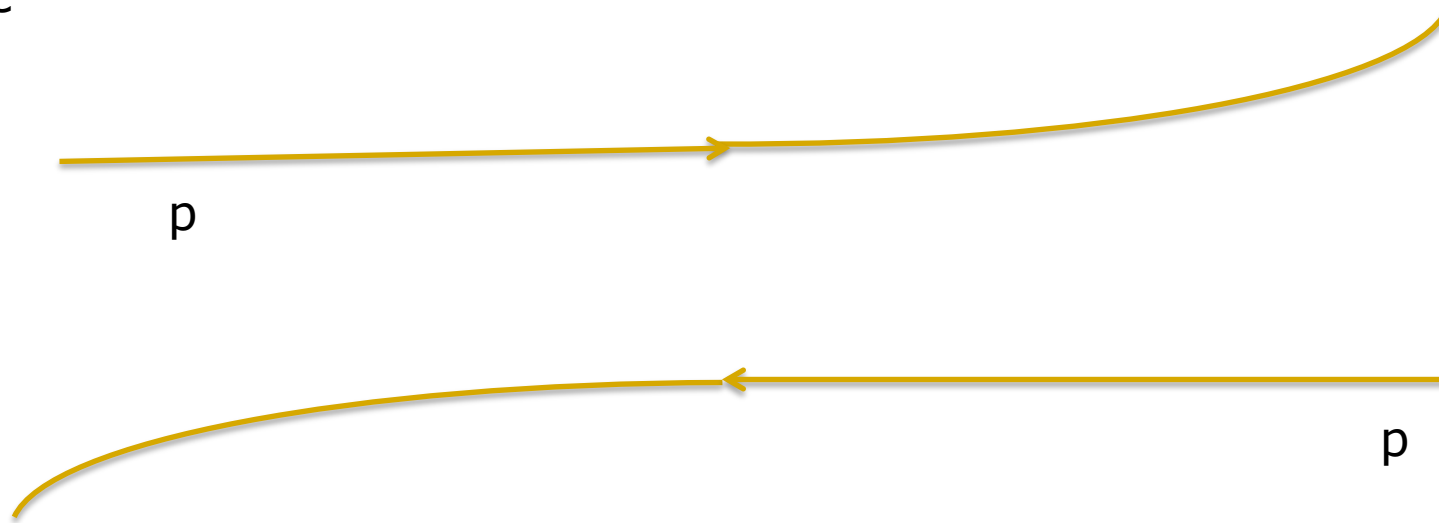
Theoretical background and motivation

Understanding QCD


- At hard scales
 - theory perturbative and thus predictive
 - well tested by experiment
 - non-abelian nature (colour / α_s running) confirmed
- At soft scales
 - difficult (impossible?) to predict
 - yet this is where most physics happens
 - describes bound hadrons and nature of vacuum
 - choose your experimental environment carefully and challenge theory
- Open questions
 - colourless objects (pomeron, reggeon, odderon)
 - glueballs
 - QCD must 'break down' at very soft scales (rise of gluon PDF violates unitarity) – there must be new phenomenology like saturation.

Physics of the Vacuum

Elastic

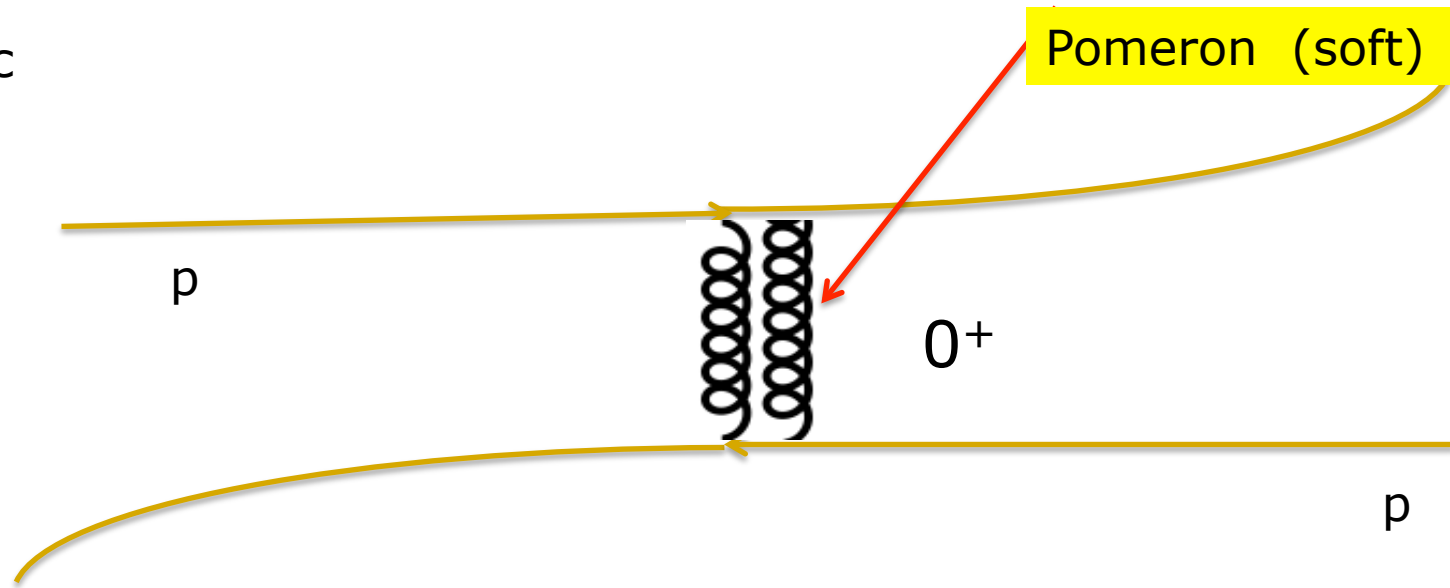


It's QCD – but not as we normally see it. It's colour-free

σ_{elastic}	$\approx 40\text{mb}$	
$\sigma_{\text{diffractive}}$	$\approx 10\text{mb}$	
$\sigma_{\text{inelastic}}$	$\approx 60\text{mb}$	

Physics of the Vacuum

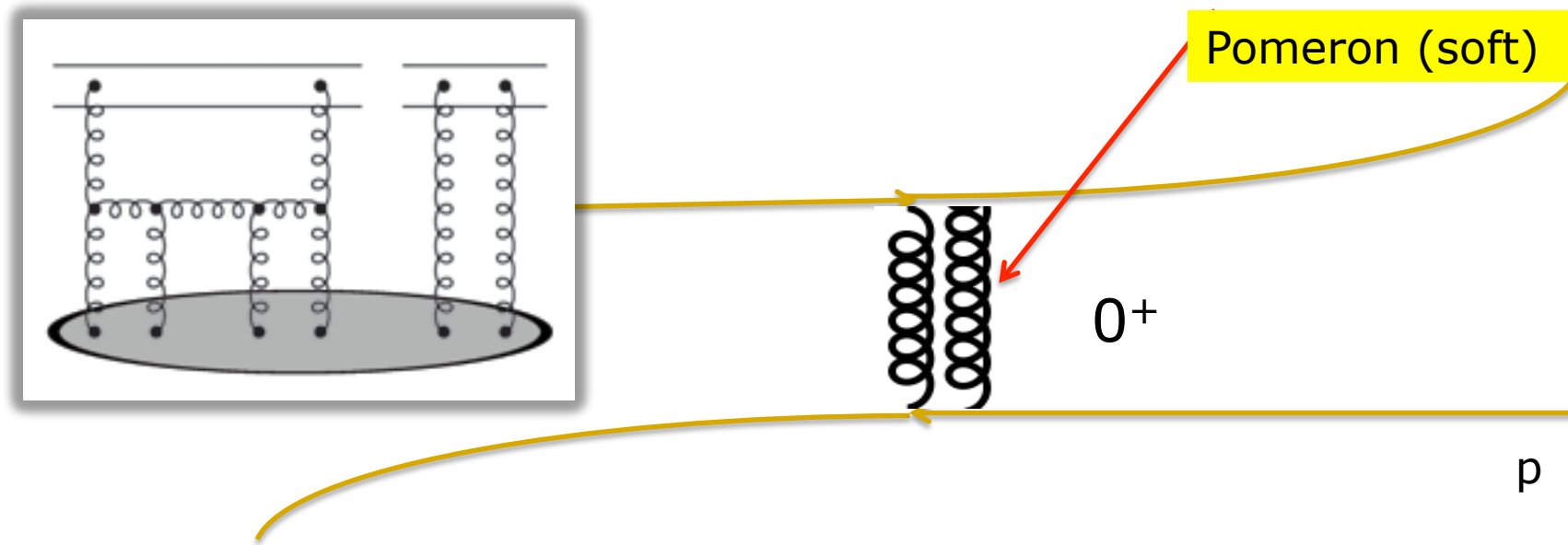
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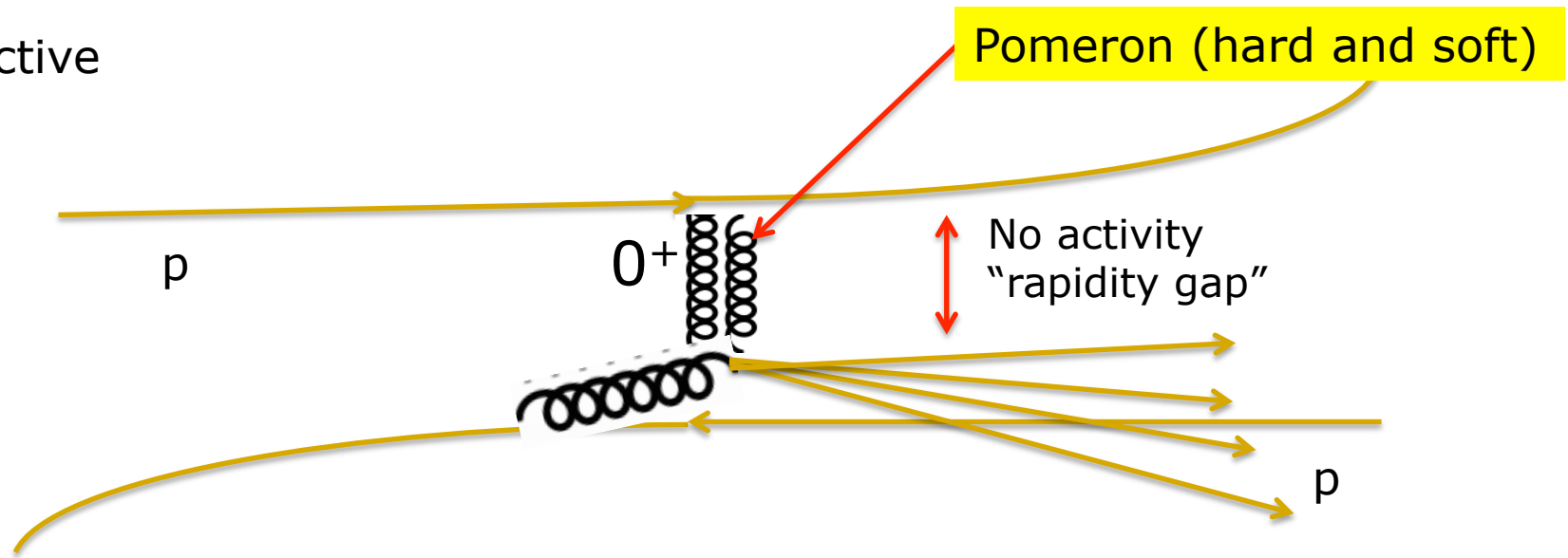


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Physics of the Vacuum

Diffractive

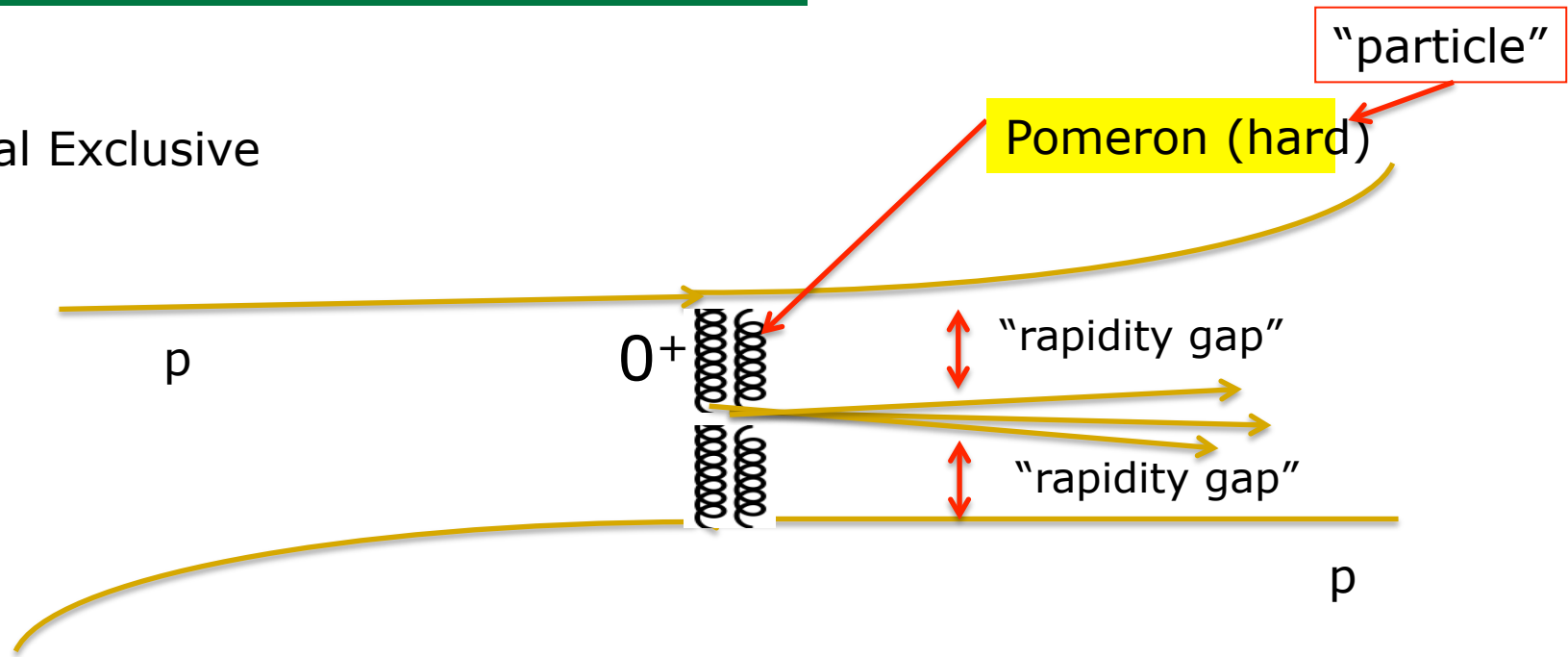


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Physics of the Vacuum

Central Exclusive

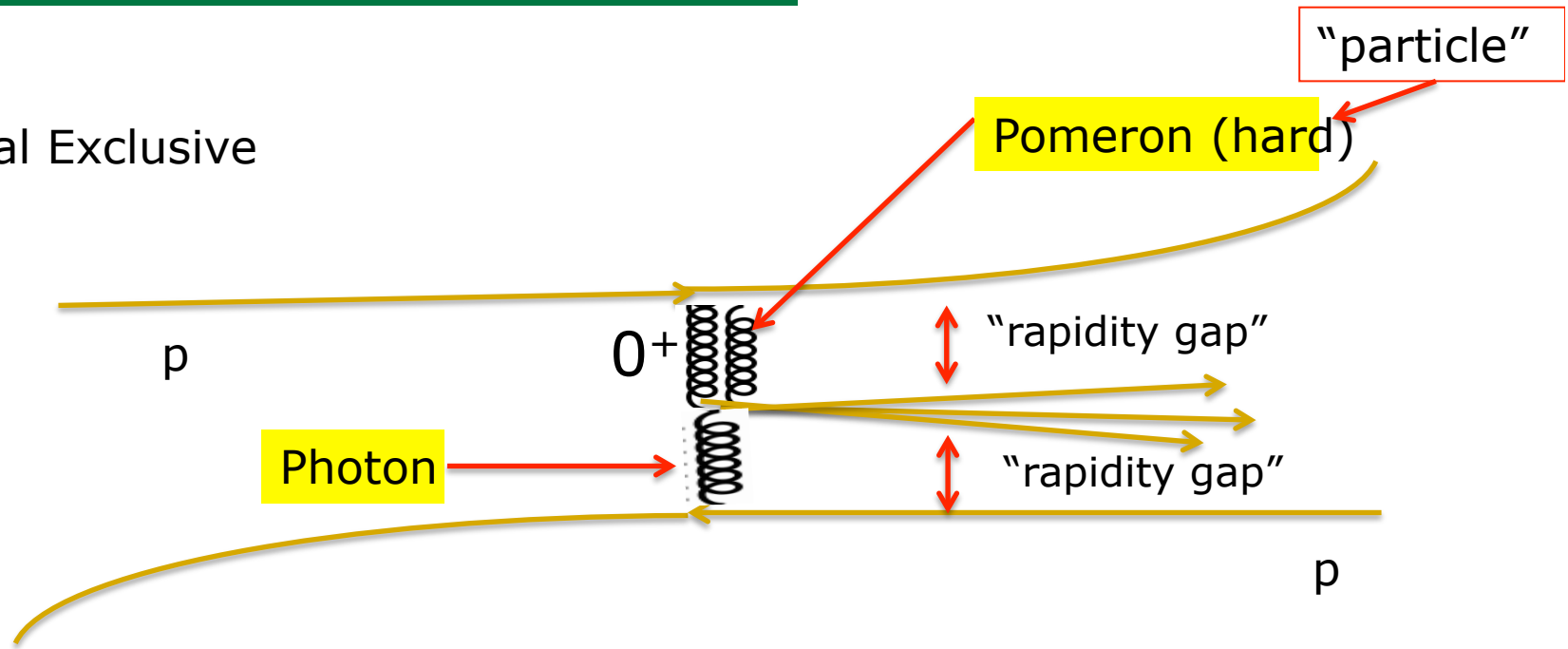


Elastic diffractive: clean environment to study vacuum, and in particular, transition between soft and hard pomeron.

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Physics of the Vacuum

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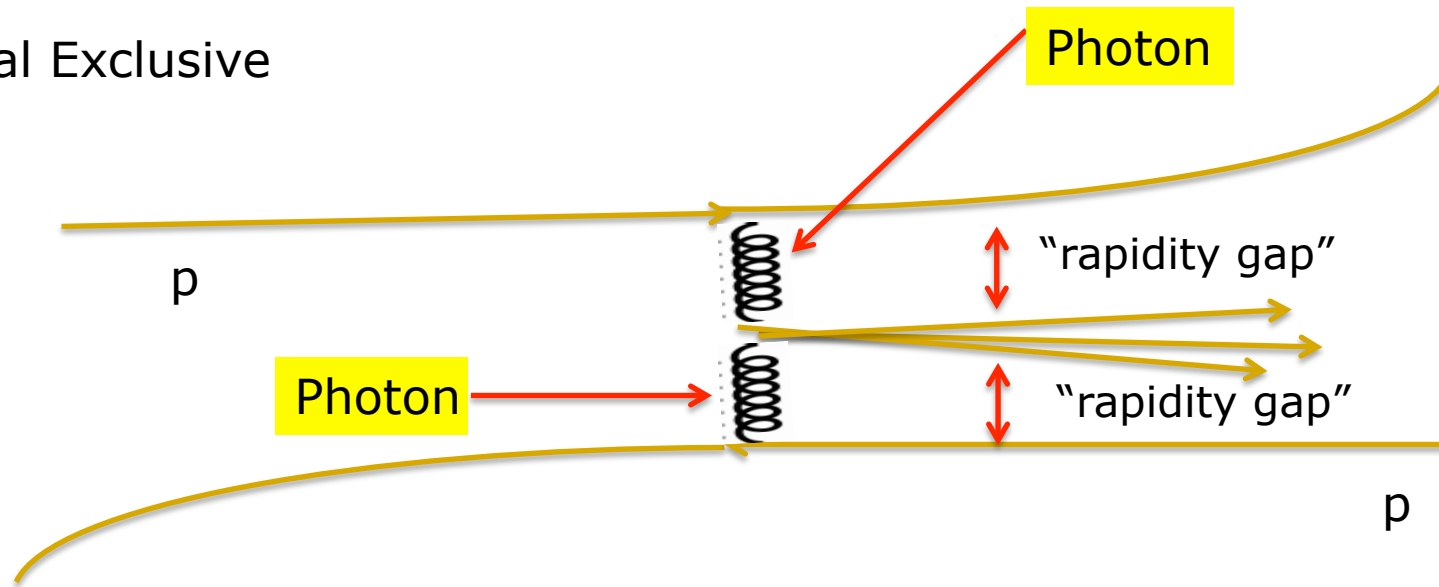


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Physics of the Vacuum

Central Exclusive



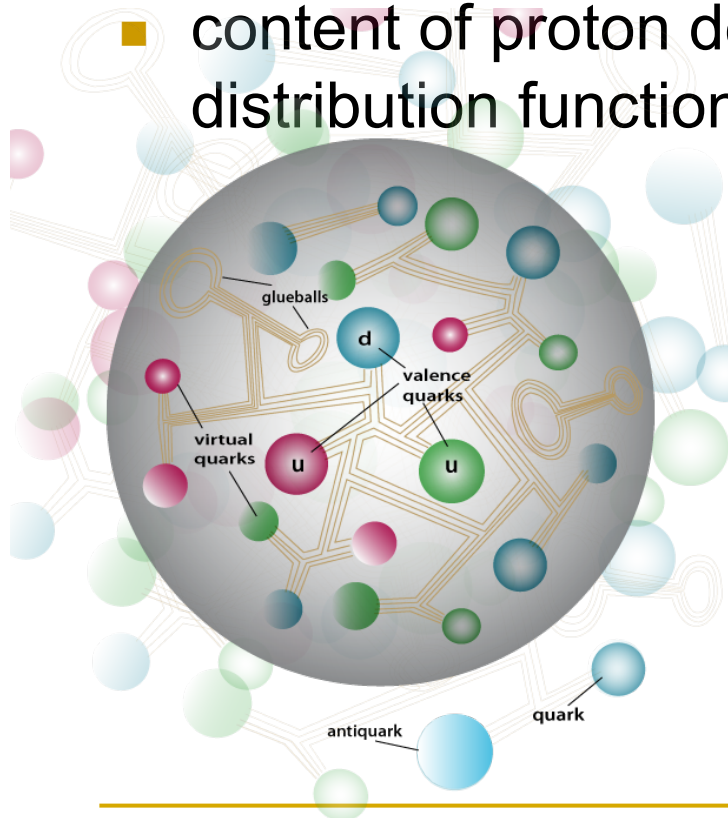
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Pragmatic reasons to understand gluon

- If you want to describe $gg \rightarrow X$, $gg \rightarrow H$
- if you want to describe the underlying event

- content of proton described in terms of parton distribution functions

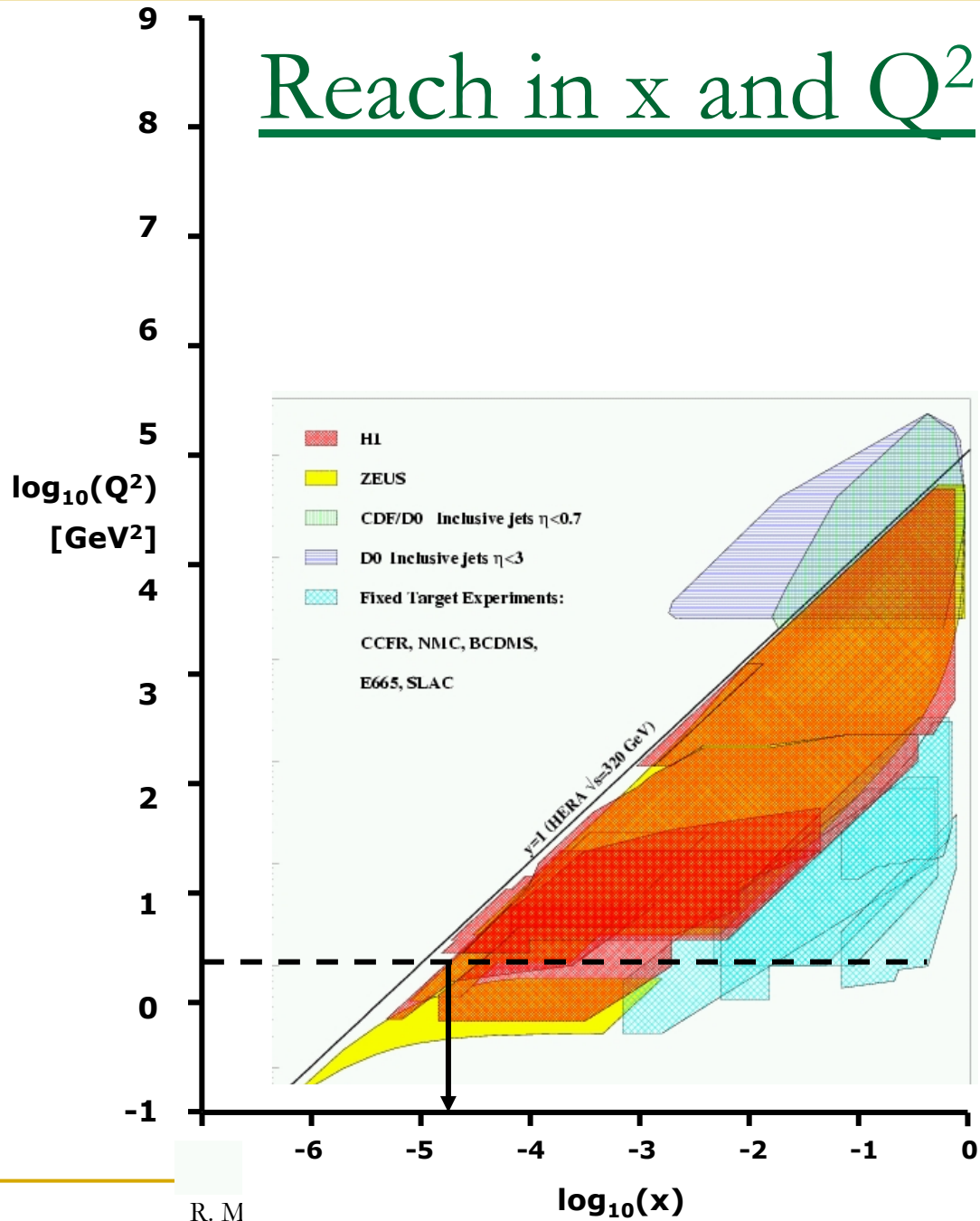


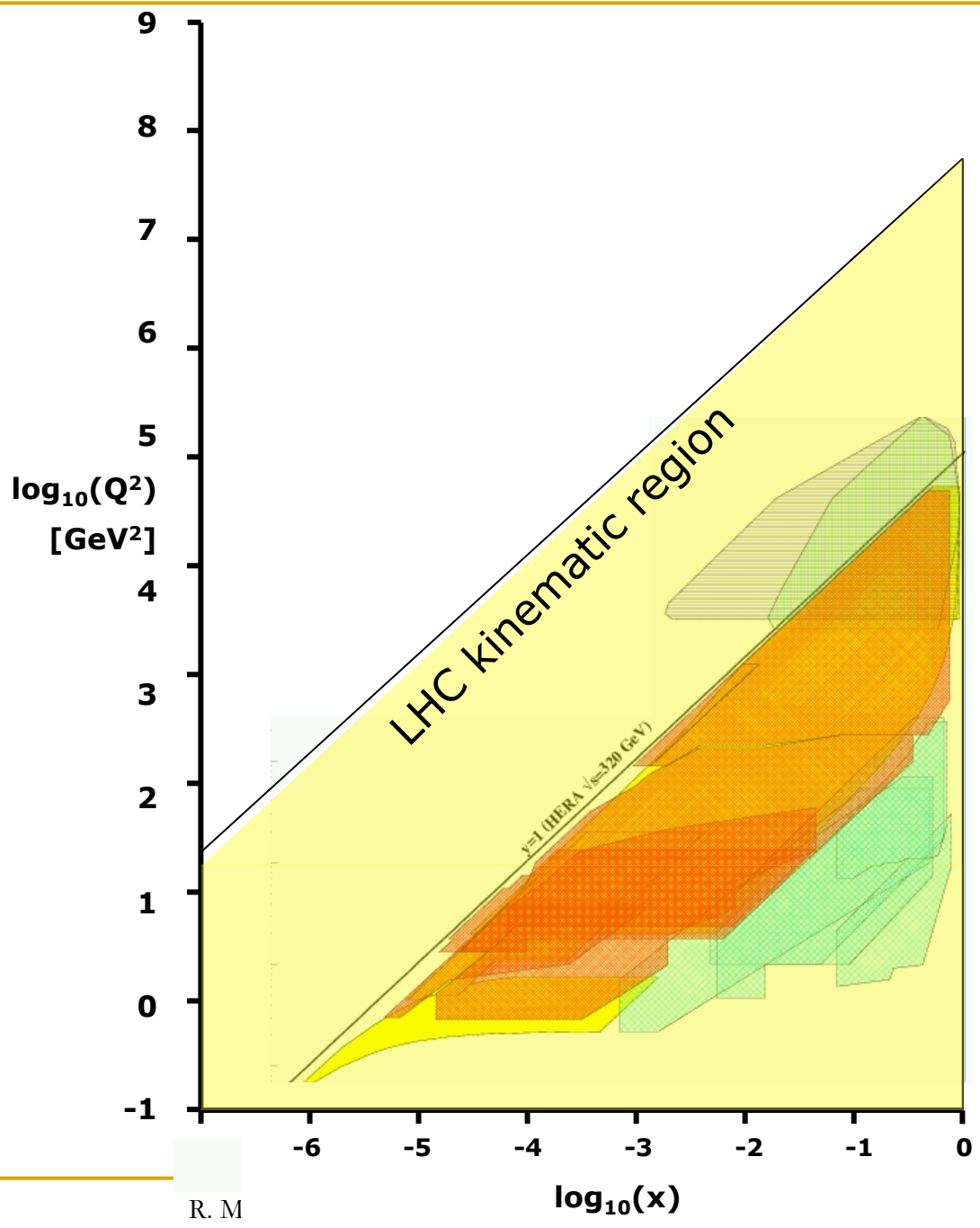
$$f_q(x, Q^2)$$

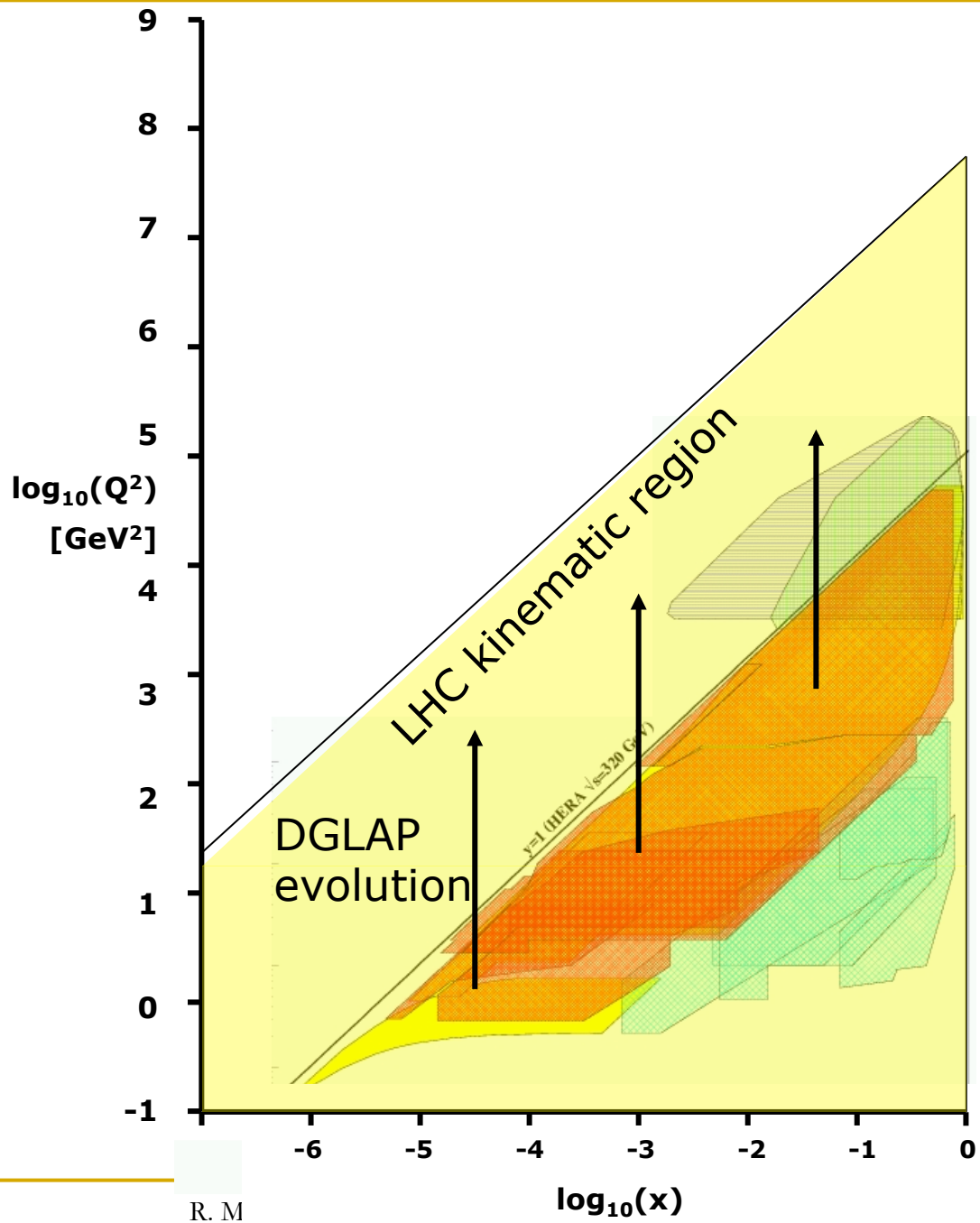
Probability that proton contains this parton
with this momentum fraction

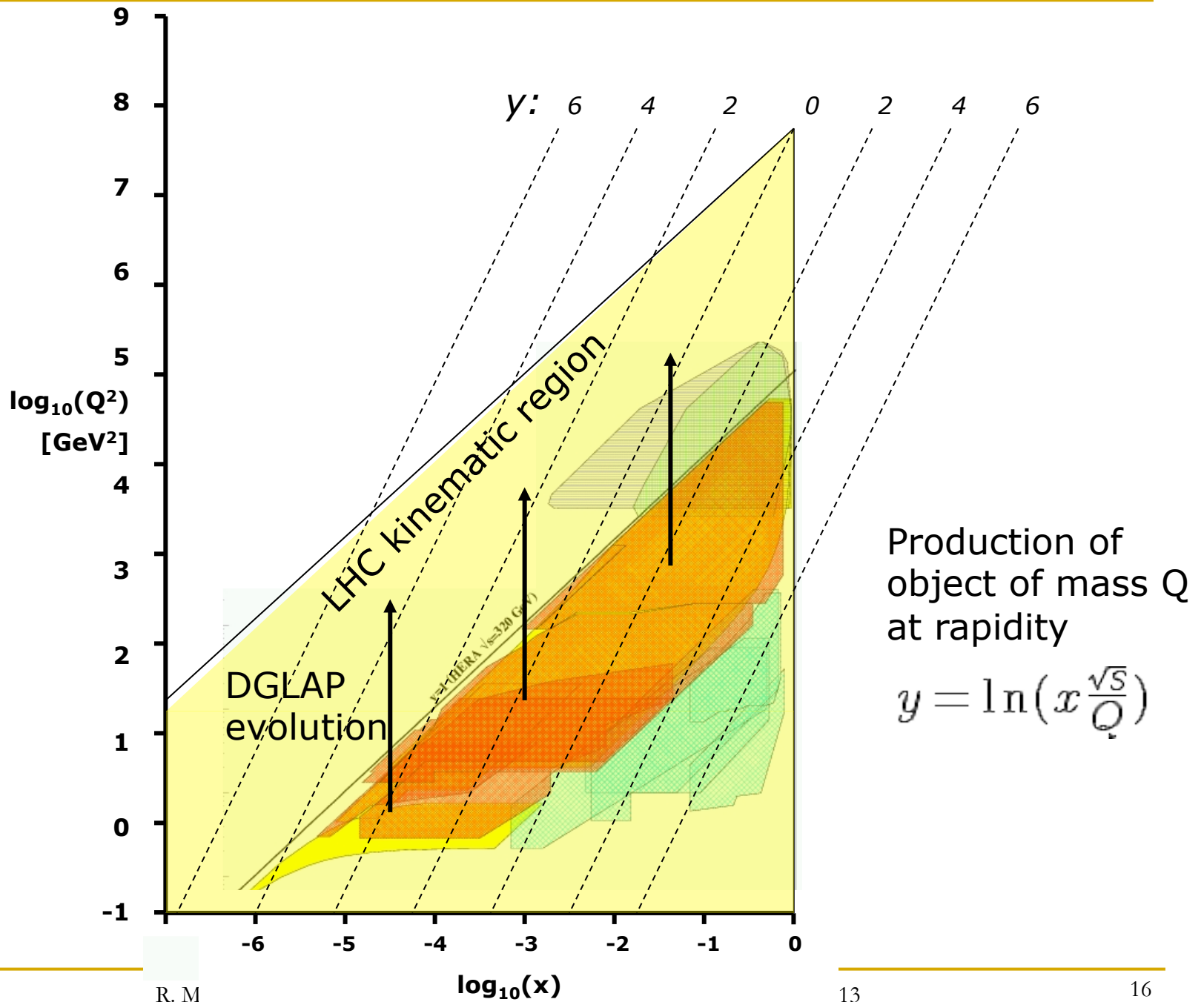
Q = Invariant mass of parton interaction
 $x = Qe^{\pm y}/\sqrt{s}$ [y is rapidity, \sqrt{s} c.o.m]

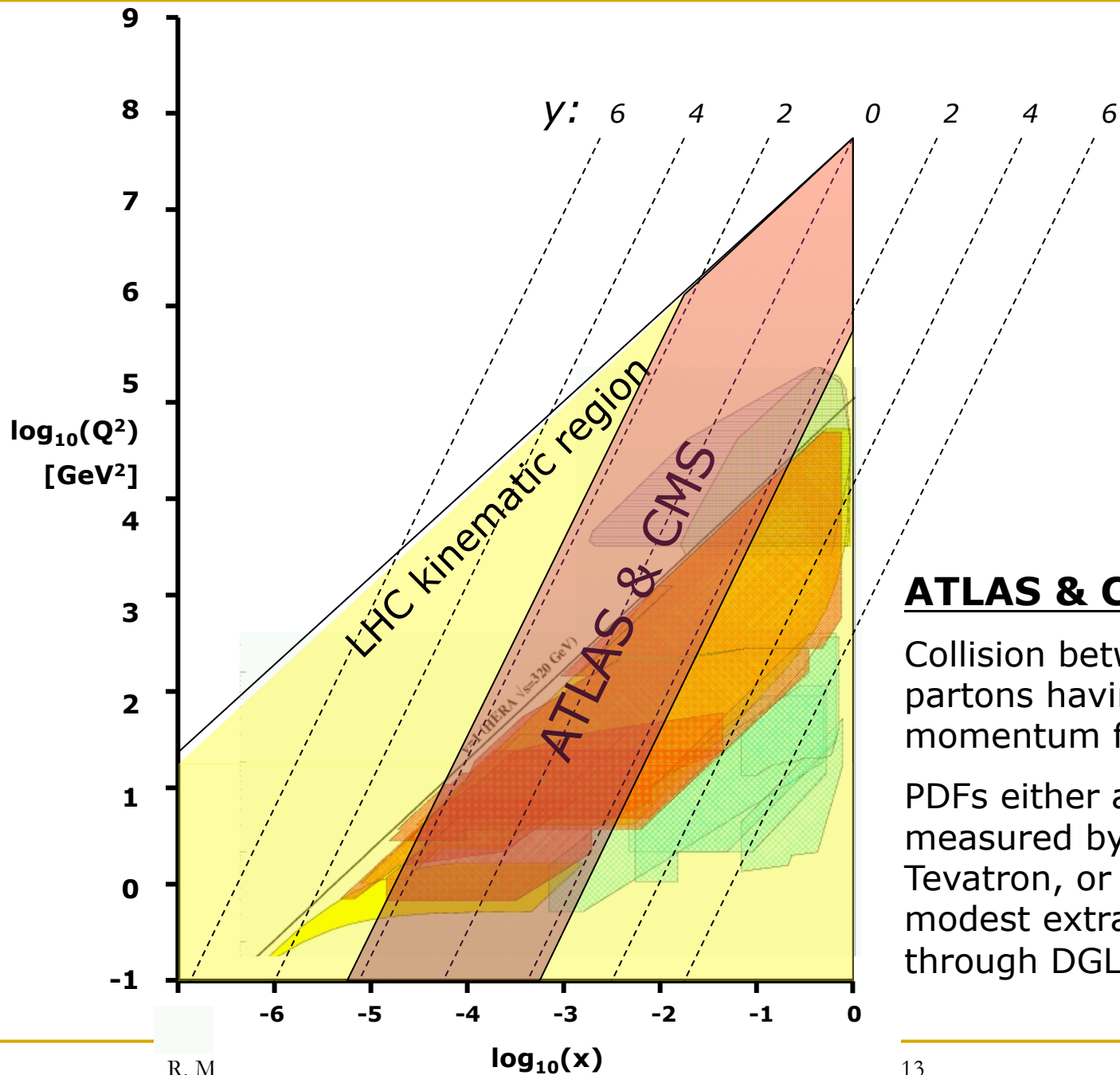
Reach in x and Q^2







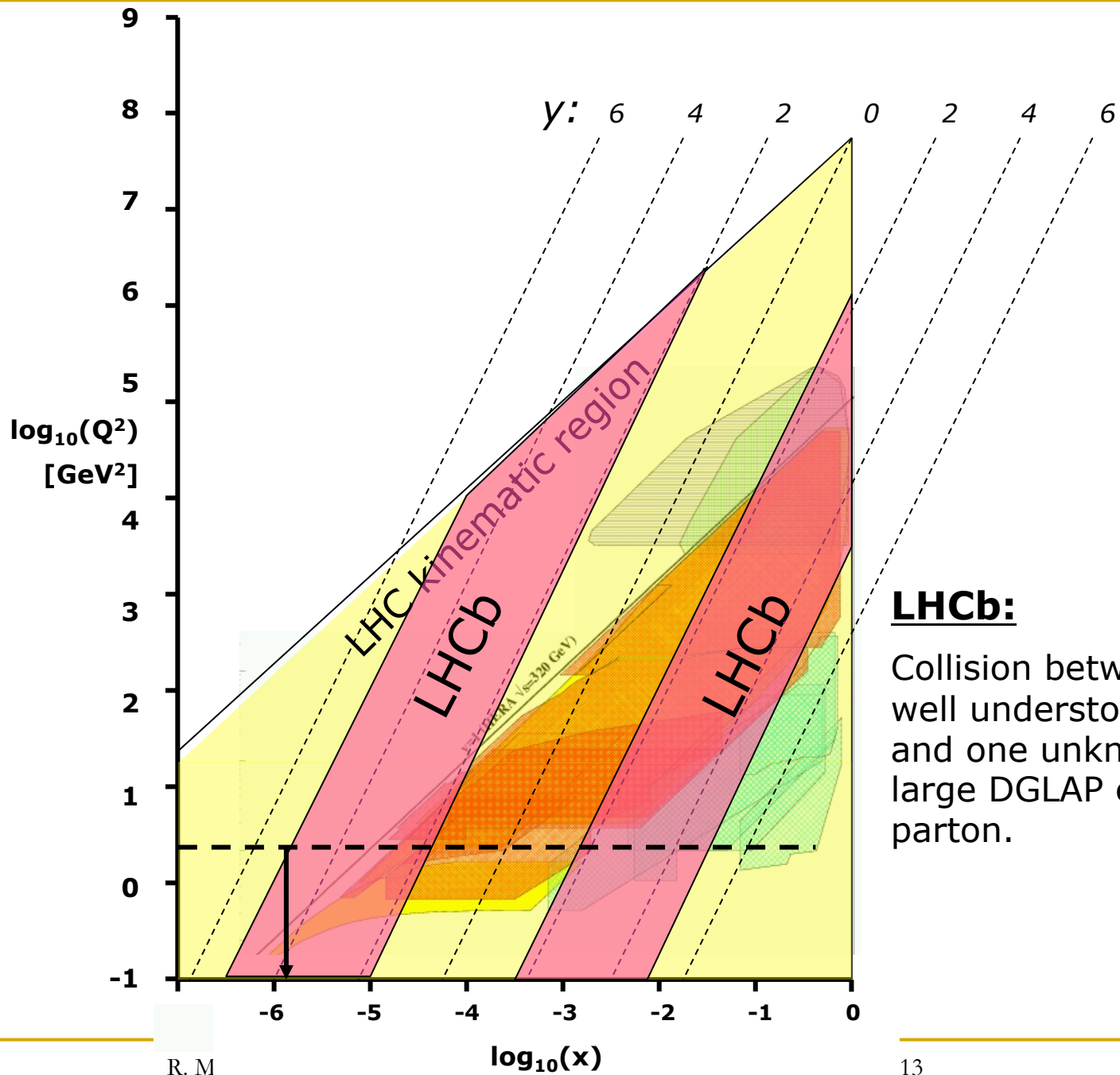




ATLAS & CMS:

Collision between two partons having similar momentum fractions.

PDFs either already measured by HERA or Tevatron, or requiring modest extrapolation through DGLAP.

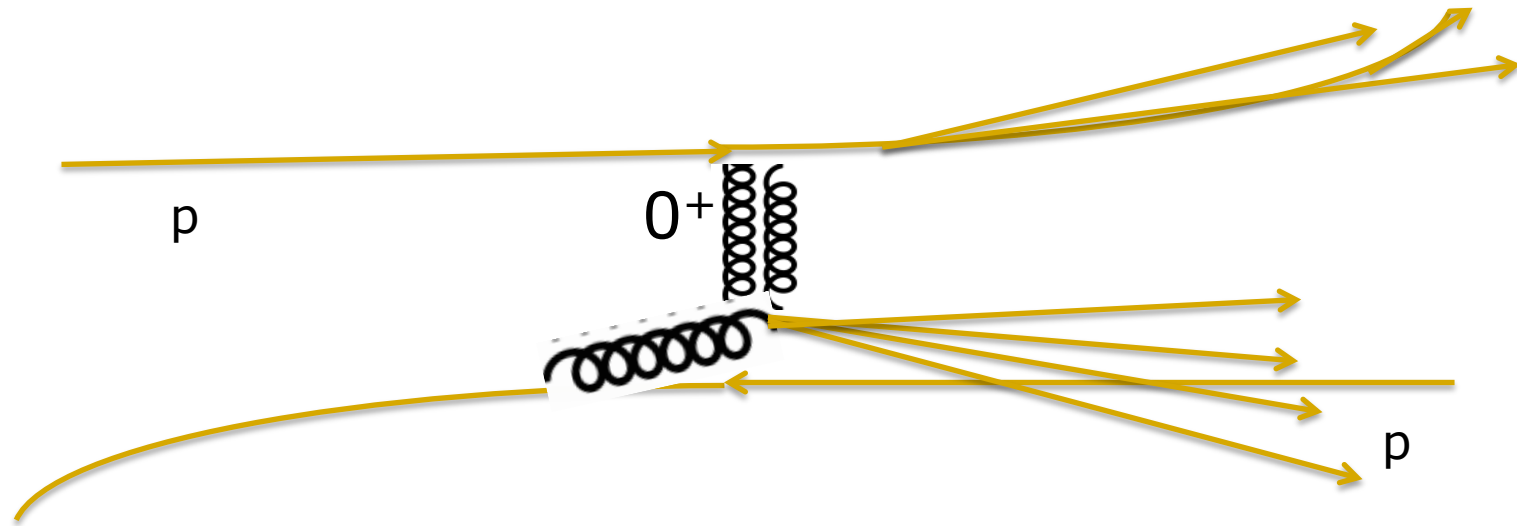


LHCb:

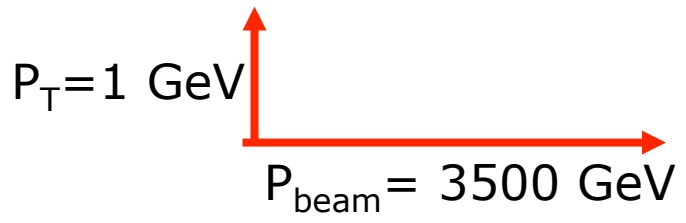
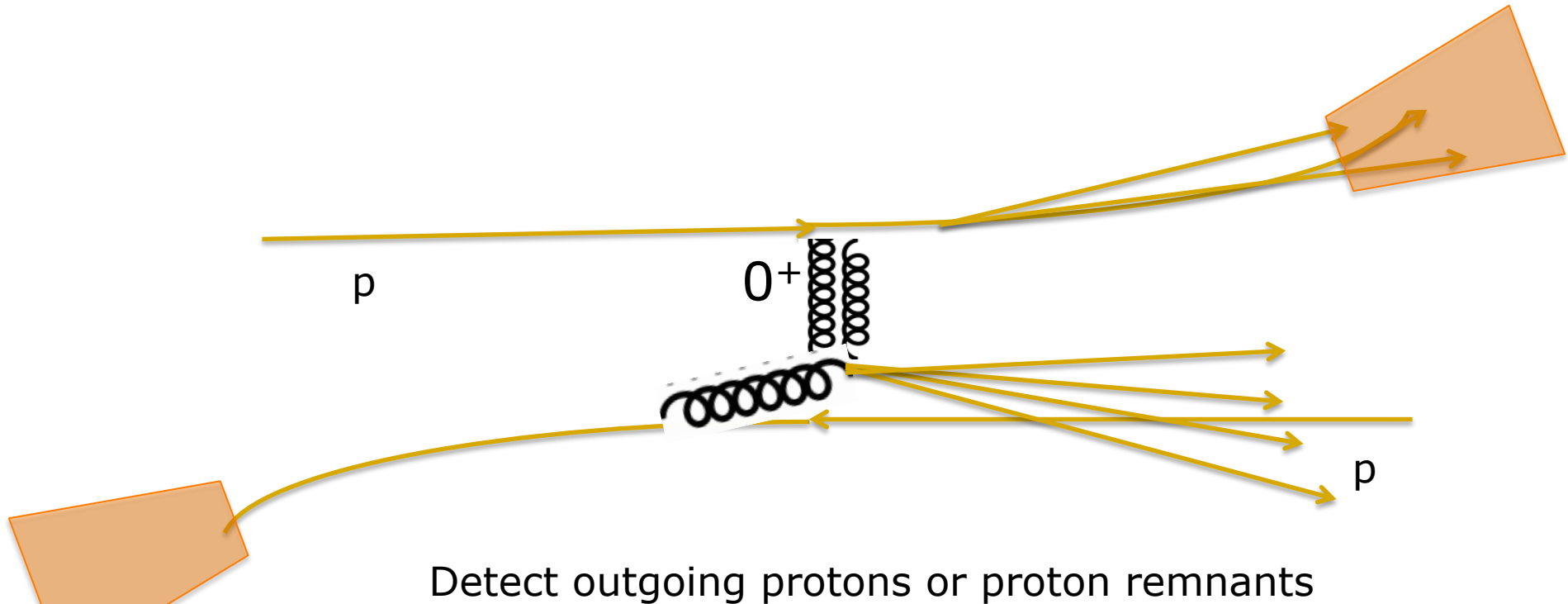
Collision between one well understood parton and one unknown or large DGLAP evolved parton.

Experimental Signatures

Experimental Signatures: How to distinguish diffractive events



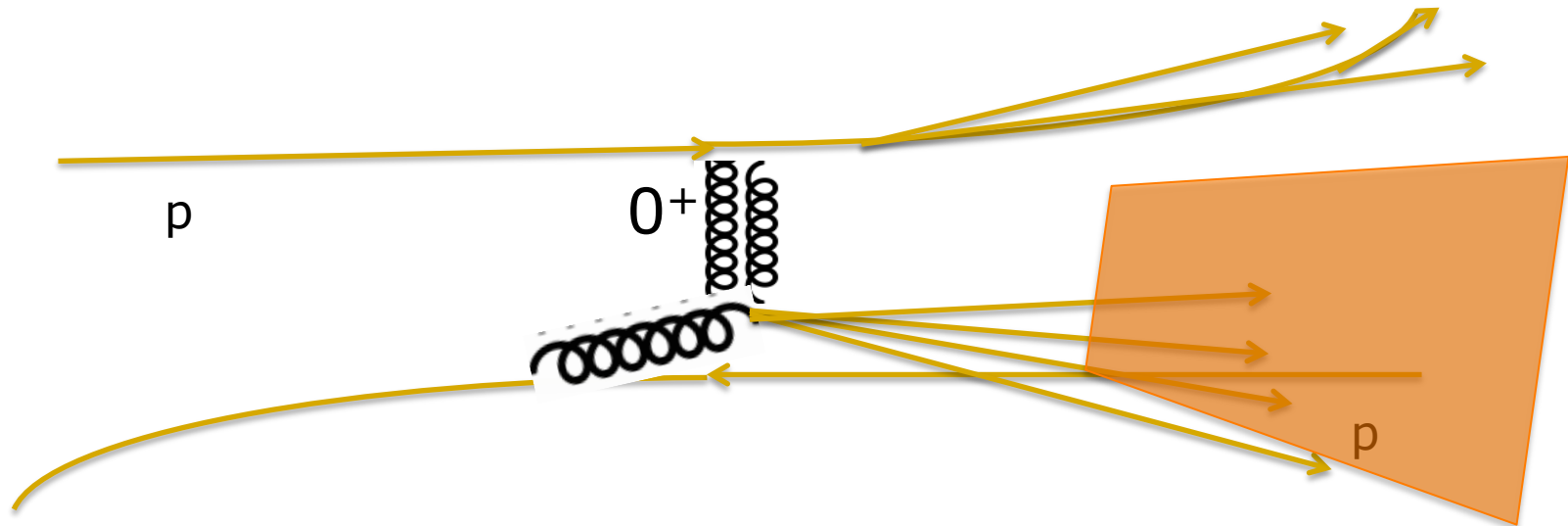
How to distinguish diffractive events



$$y \sim \eta = -\log(\tan(\theta/2)) = 9$$

Requires detector that approaches the beamline

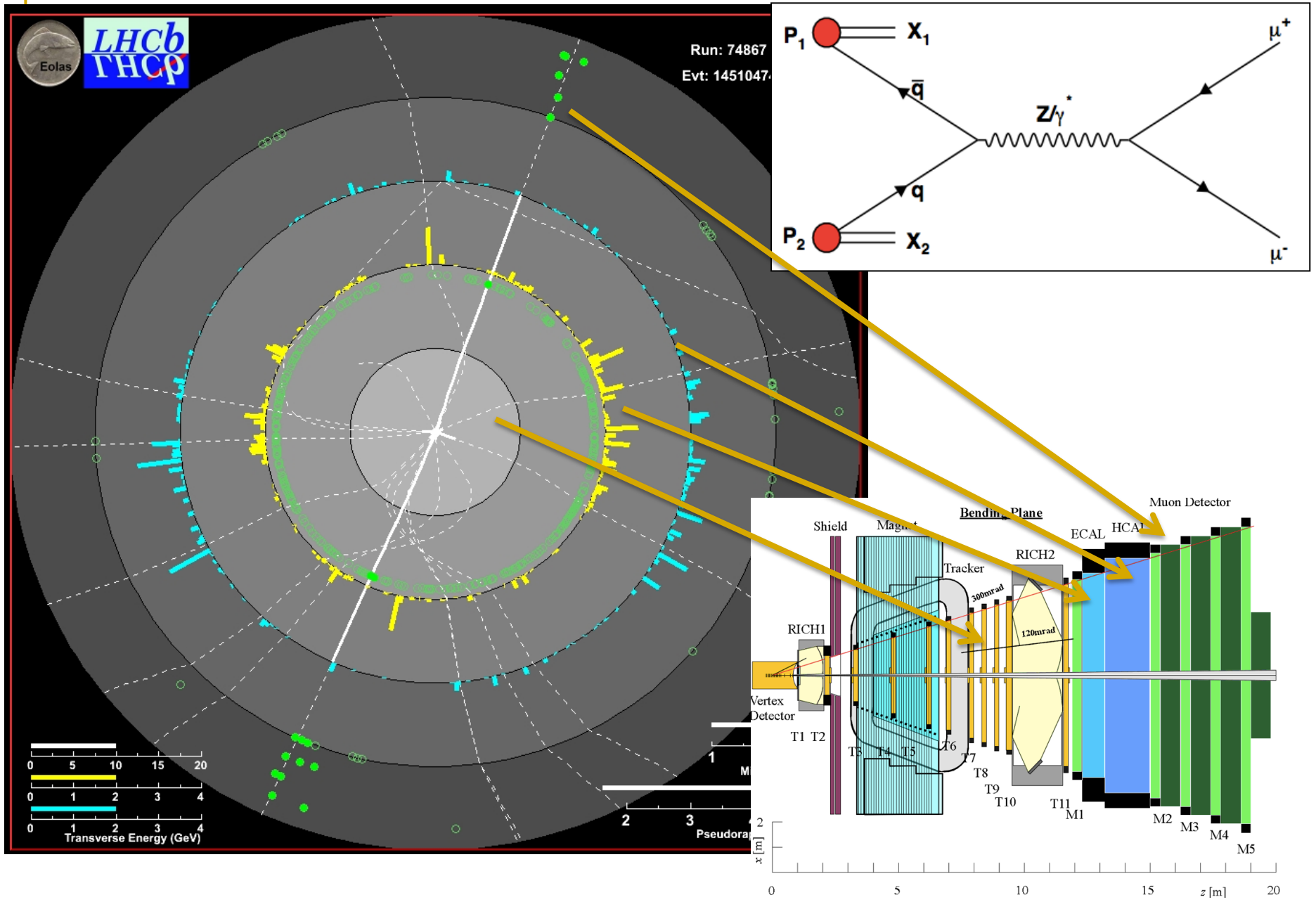
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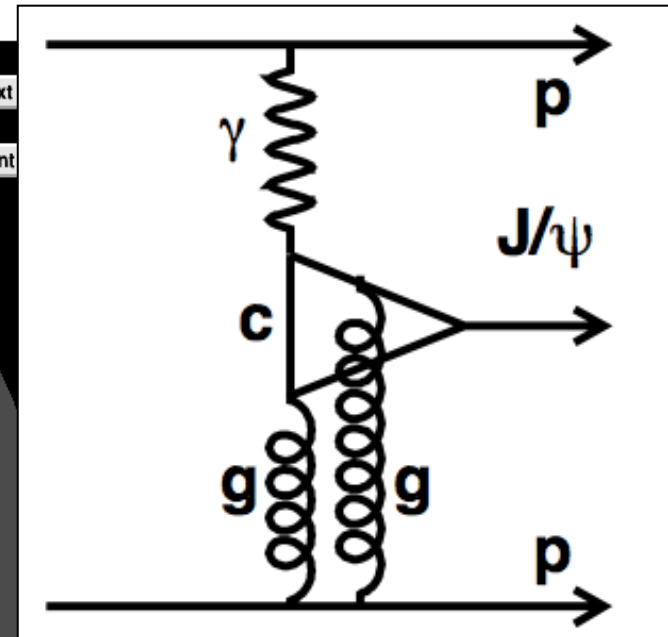
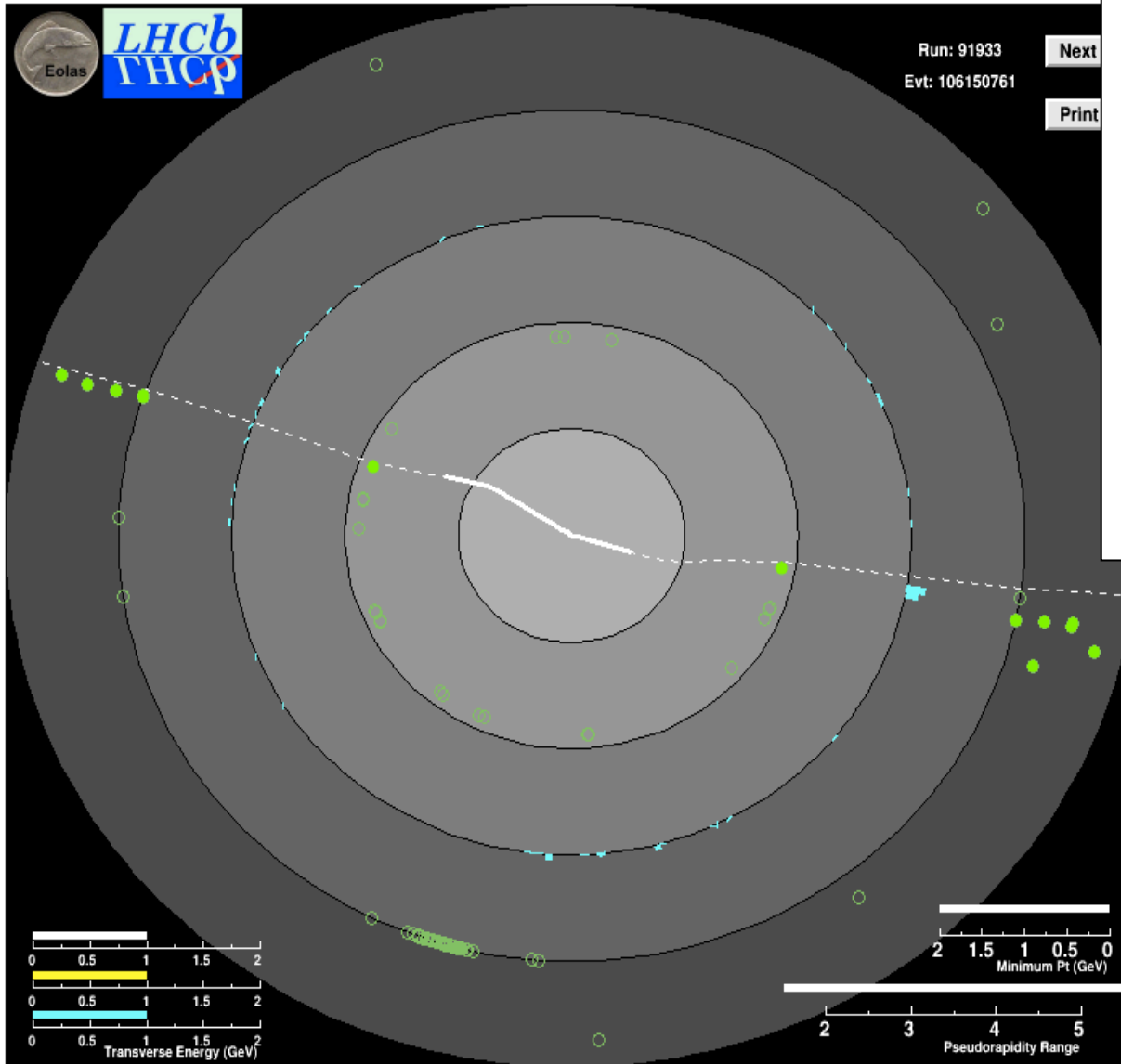


Detect 'central' system including presence of **rapidity gap**

All diffractive events will have a large rapidity gap (from the system down to the beam line) due to the colourless exchange

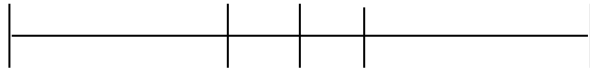
Most pp interactions distribute particles throughout 4π (collimated in jets but also with activity between jets)



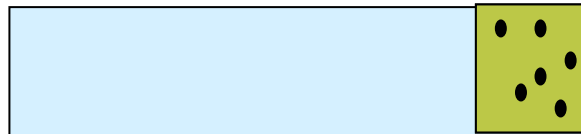


Graphical Representation

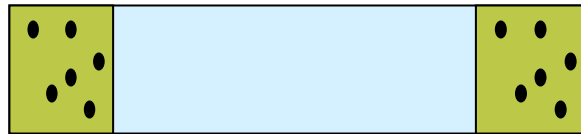
$y=-10$ $y=-2$ $y=0$ $y=2$ $y=10$



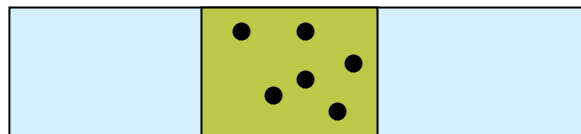
Elastic Scattering



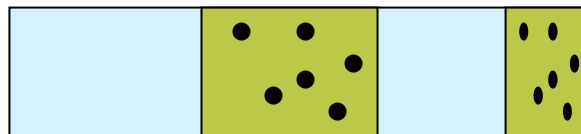
Single Diffraction



Double Diffraction



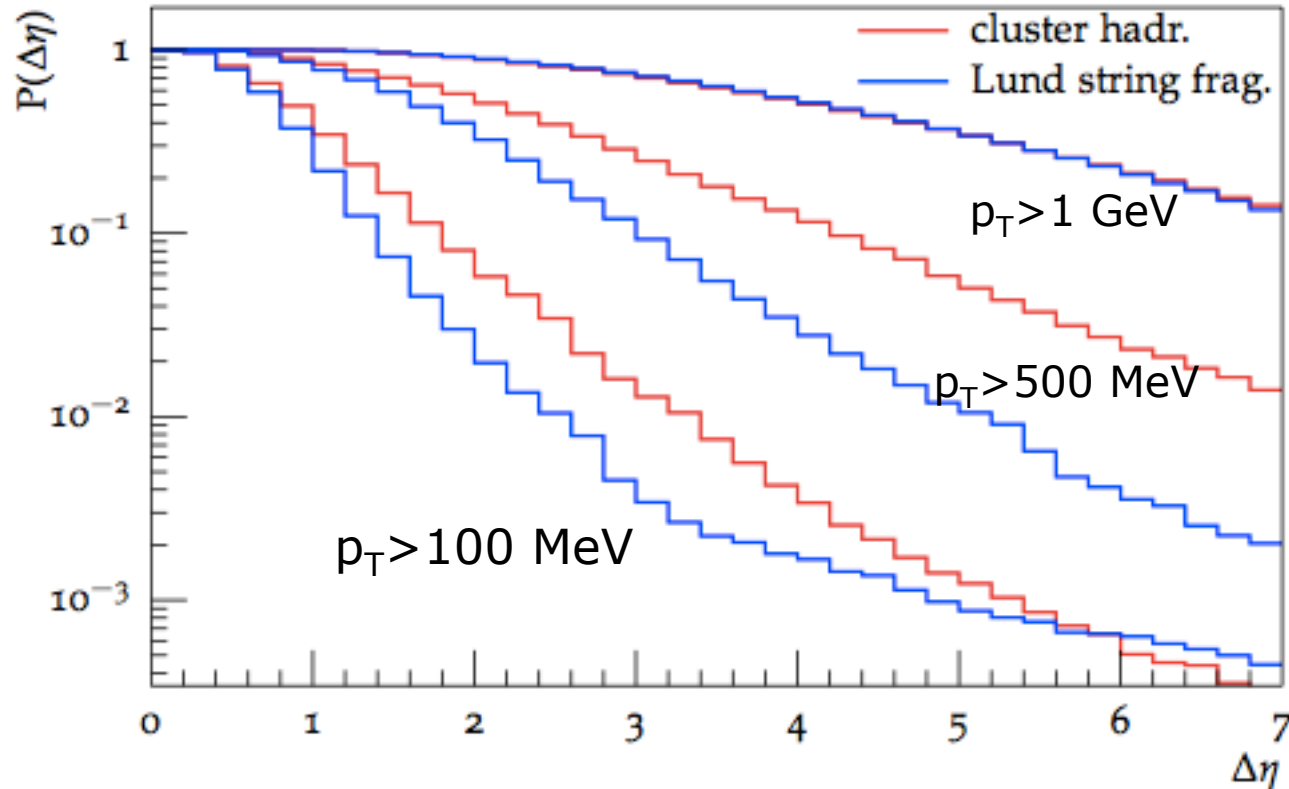
Central Exclusive Production (elastic)



Central Exclusive Production (inelastic)

What's a large gap?

Probability for finding a
rapidity gap $> \Delta\eta$
in inclusive QCD events



- Khoze, Kraus, Martin, Ryskin, Zapp, “Diffraction and correlations at the LHC: definitions and observables”, arXiv:1005.4839v2
- Probability for inclusively produced J/psi to give two muons and nothing else inside LHCb is < 0.000005

Effect of beam pile-up

Detect empty event except for some isolated activity.

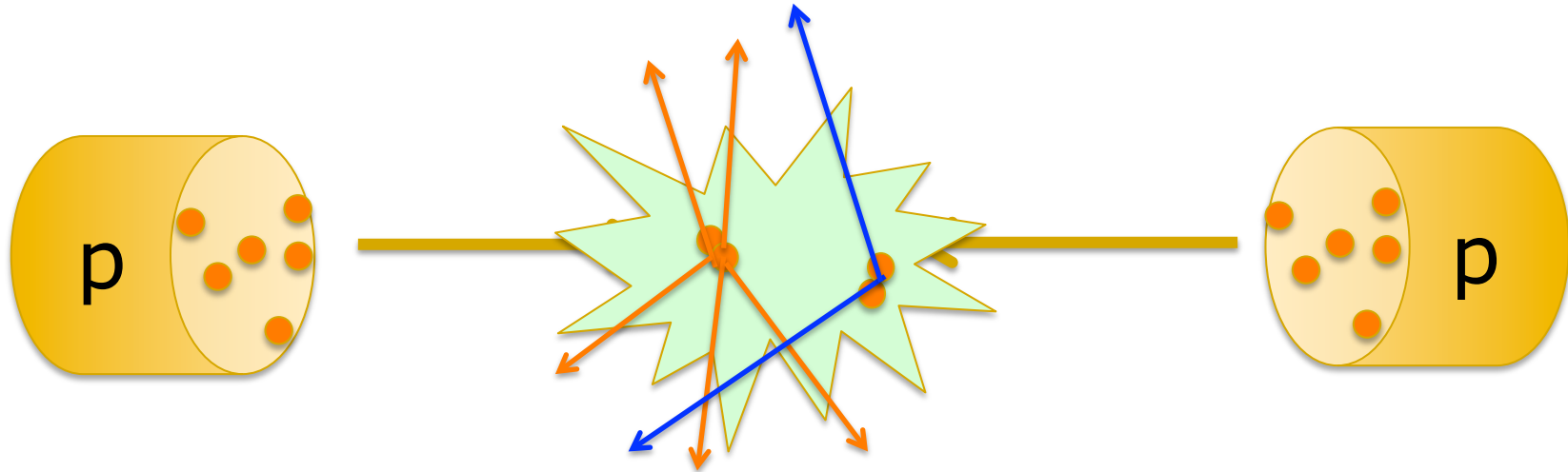


$N_x = \sigma_x L$ with L luminosity (number of protons per unit area)

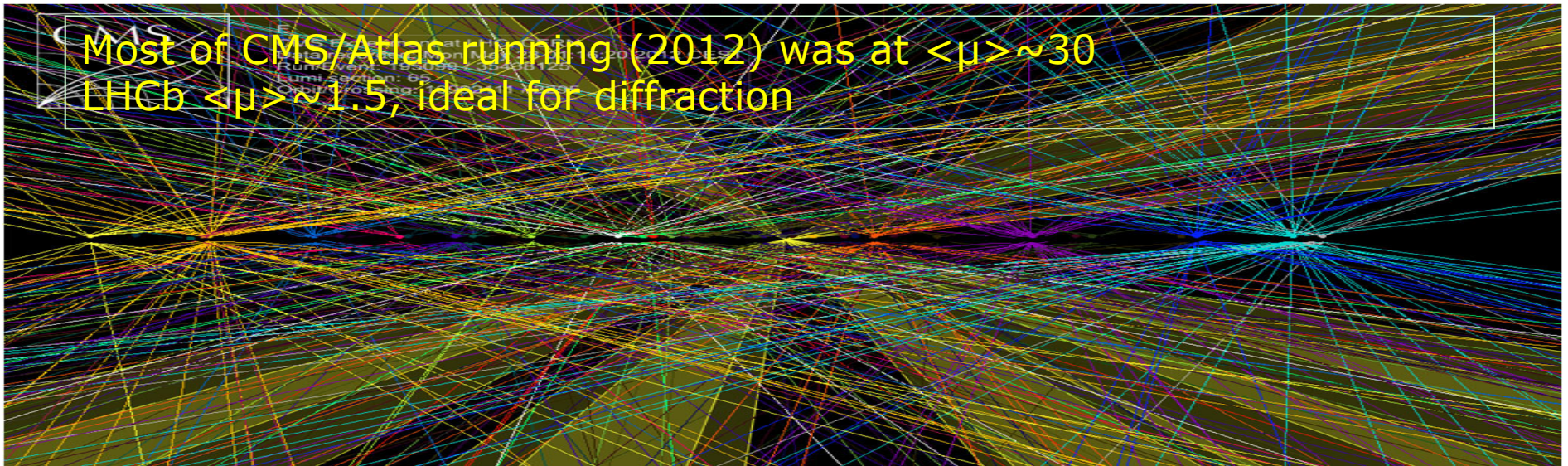
High luminosity to increase probability for producing rare processes like Higgs (or SUSY)

Increases number of interactions $\langle \mu \rangle$.

Detect empty event except for some isolated activity.



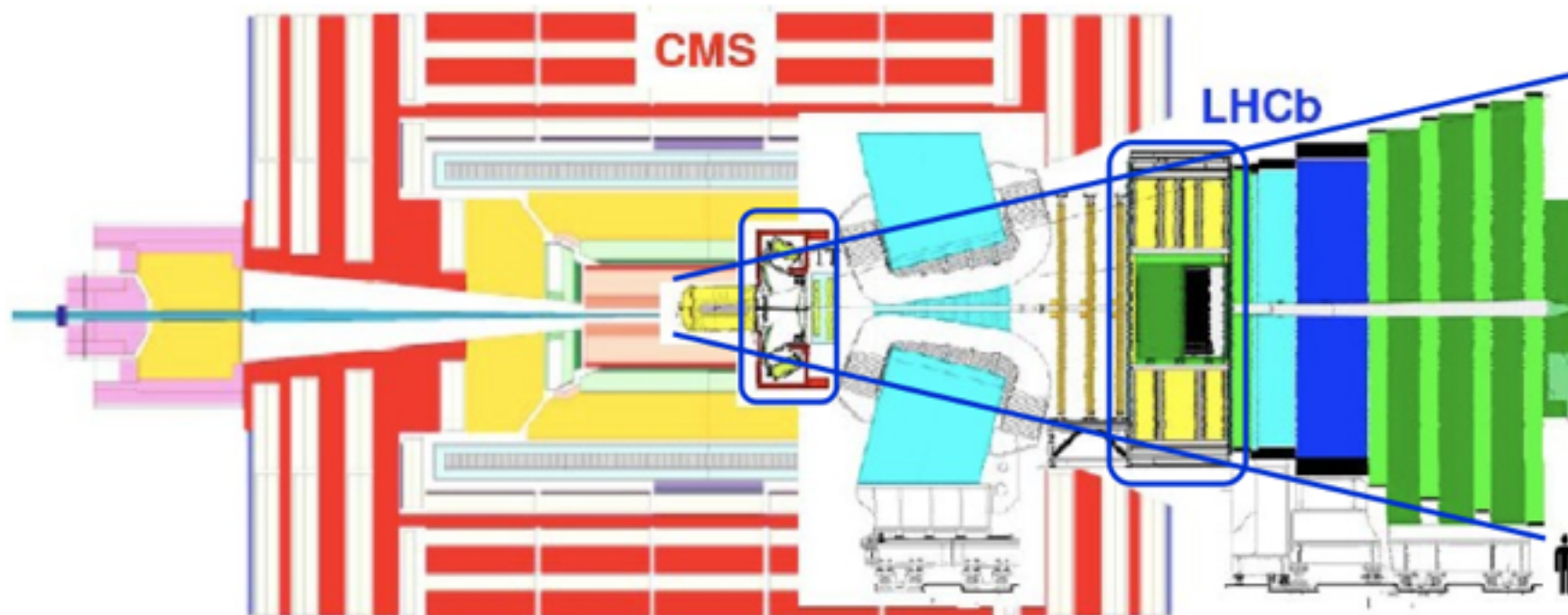
Most of CMS/Atlas running (2012) was at $\langle\mu\rangle\sim 30$
LHCb $\langle\mu\rangle\sim 1.5$, ideal for diffraction



The LHCb experiment

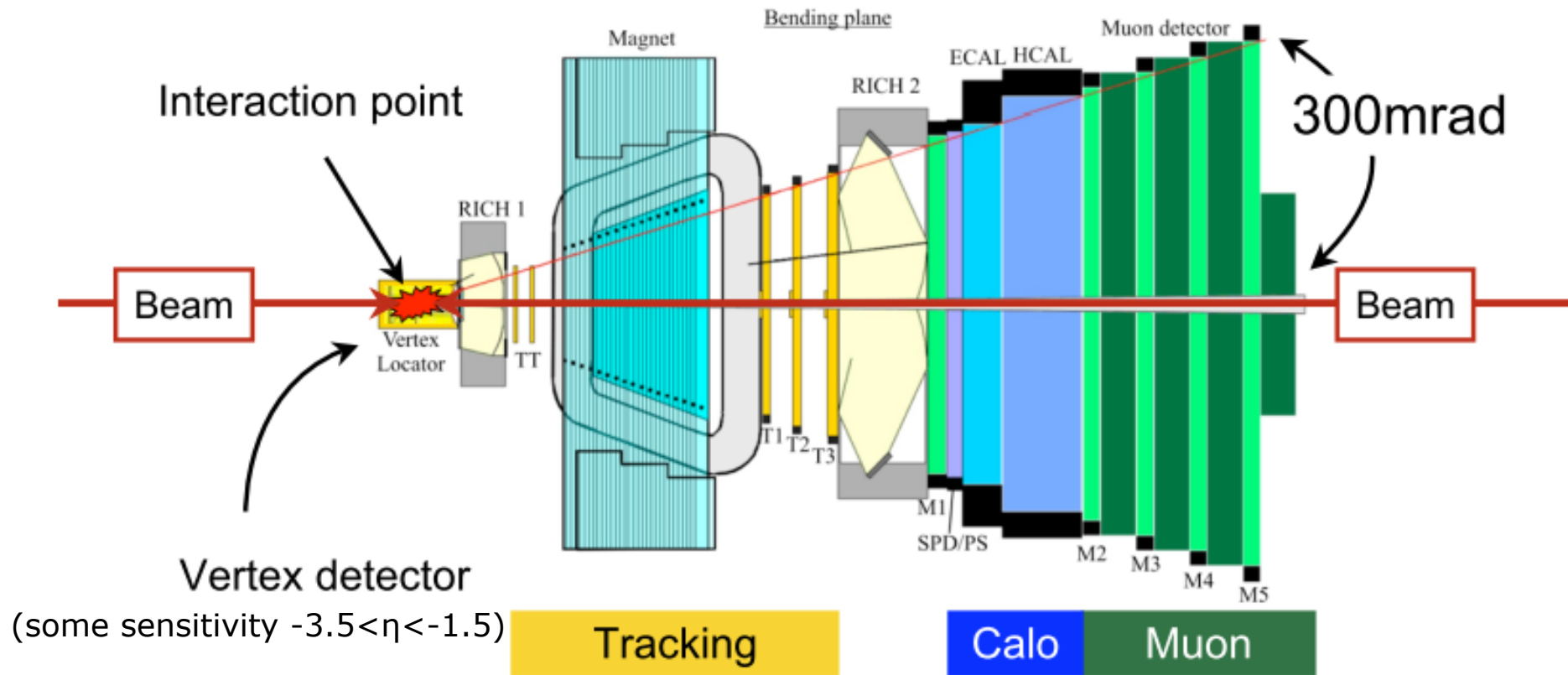


LHCb: A forward detector



Fully instrumented in region: $2 < \eta < 5$
Some detection: $-3.5 > \eta > -1.5$
Large enough acceptance to look for gaps
Can trigger on low transverse momentum objects

The LHCb detector

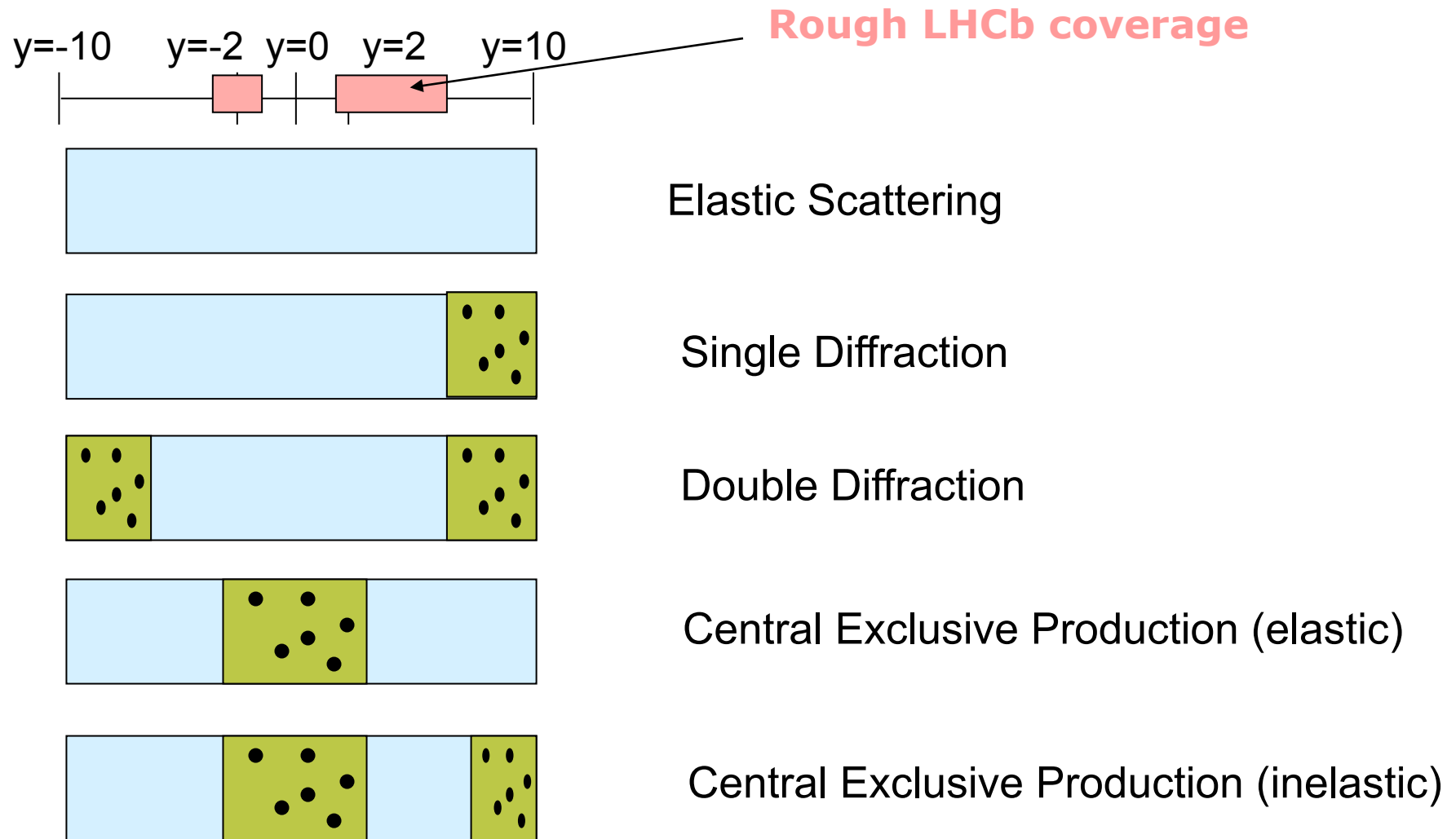


Fully instrumented within $2 < \eta < 5$

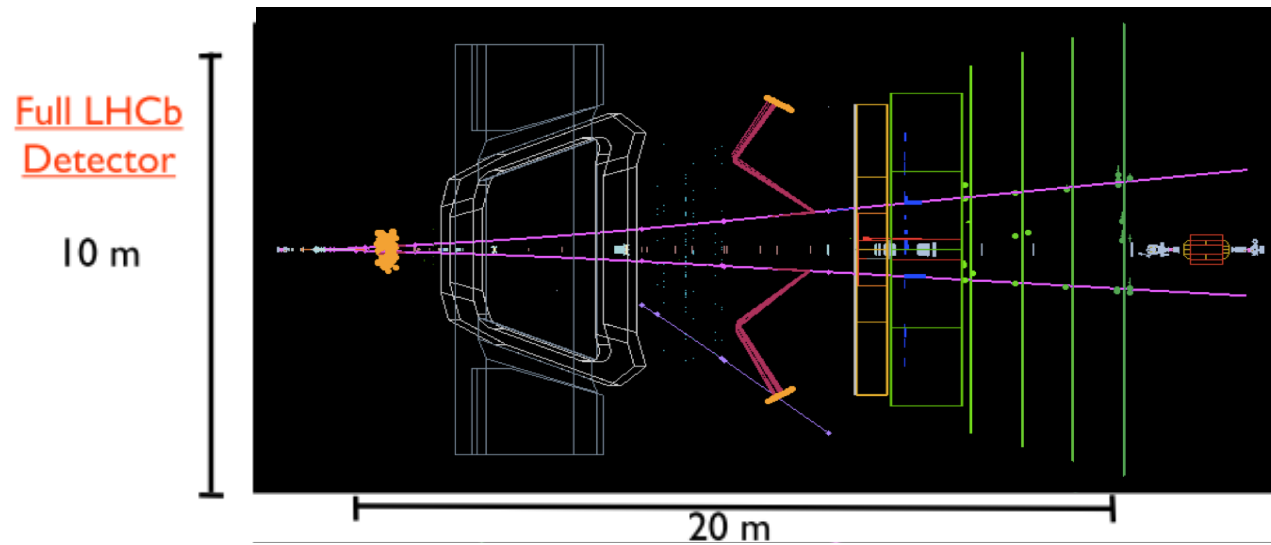
Trigger: $p_{\mu} > 3 \text{ GeV}$, $pt_{\mu} > 0.4 \text{ GeV}$, $m_{\mu\mu} > 2.5 \text{ GeV}$

Low multiplicity required. Restricts to single-interaction collisions

Graphical Representation



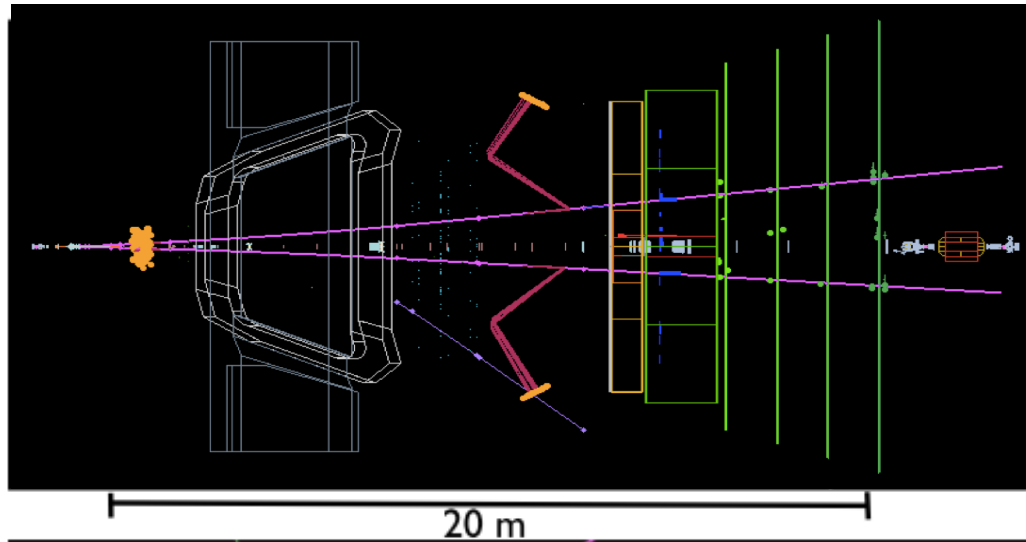
Use of backwards tracks



Use of backwards tracks

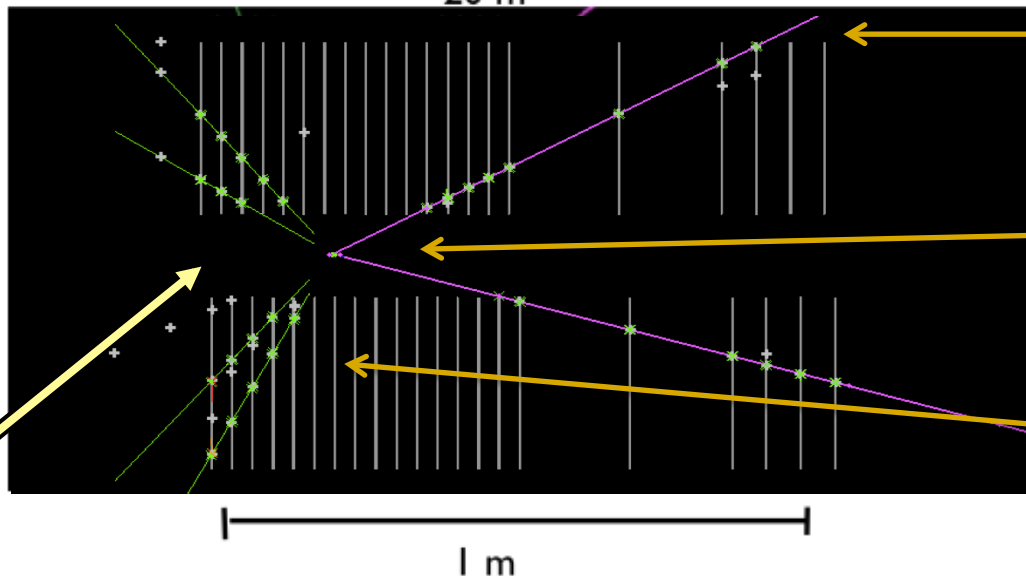
Full LHCb Detector

10 m



VELO Close Up

8.4 cm

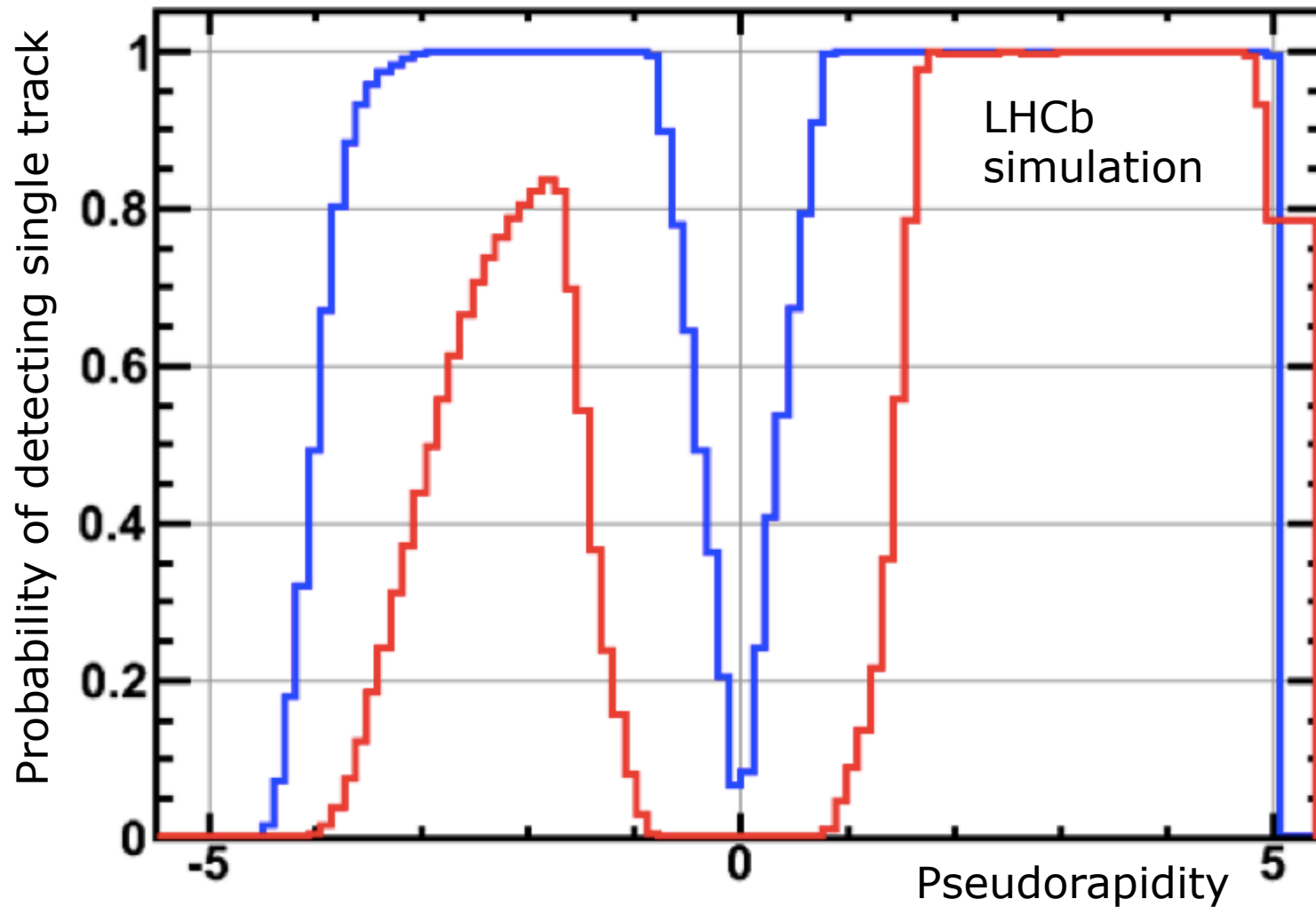


Muon

Primary Vertex

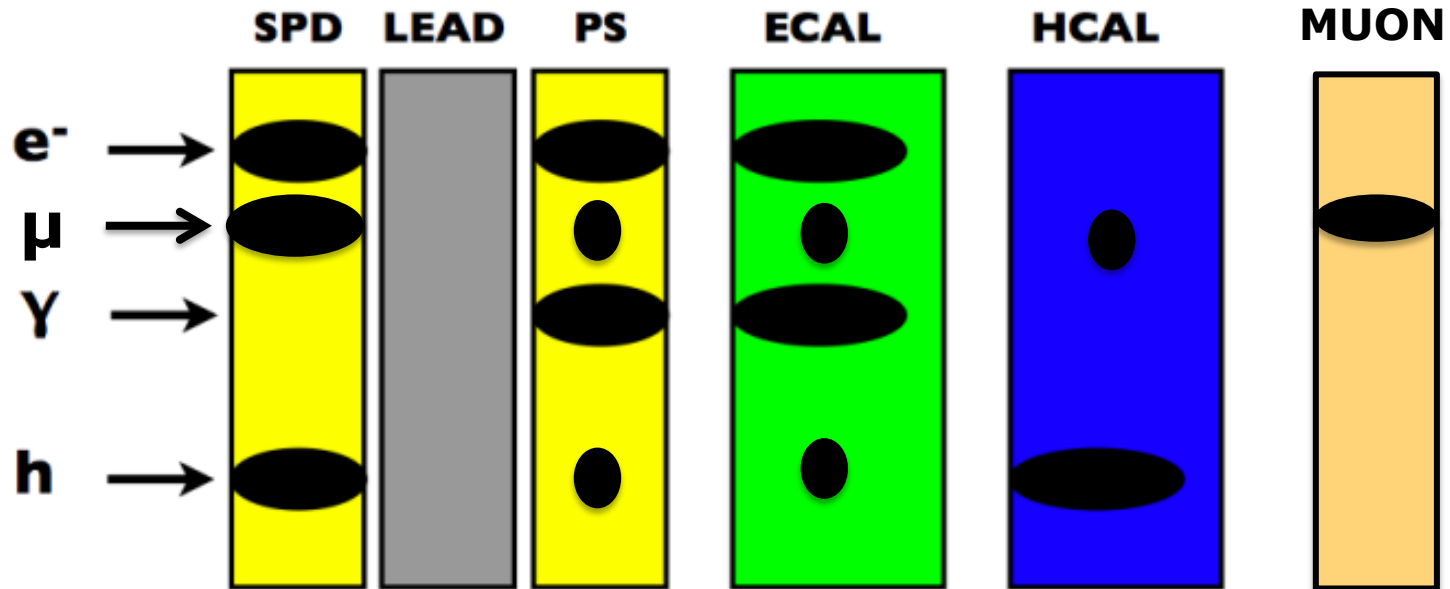
Backward Tracks

Clearly not exclusive



All results I show imply red region void, except for signal.

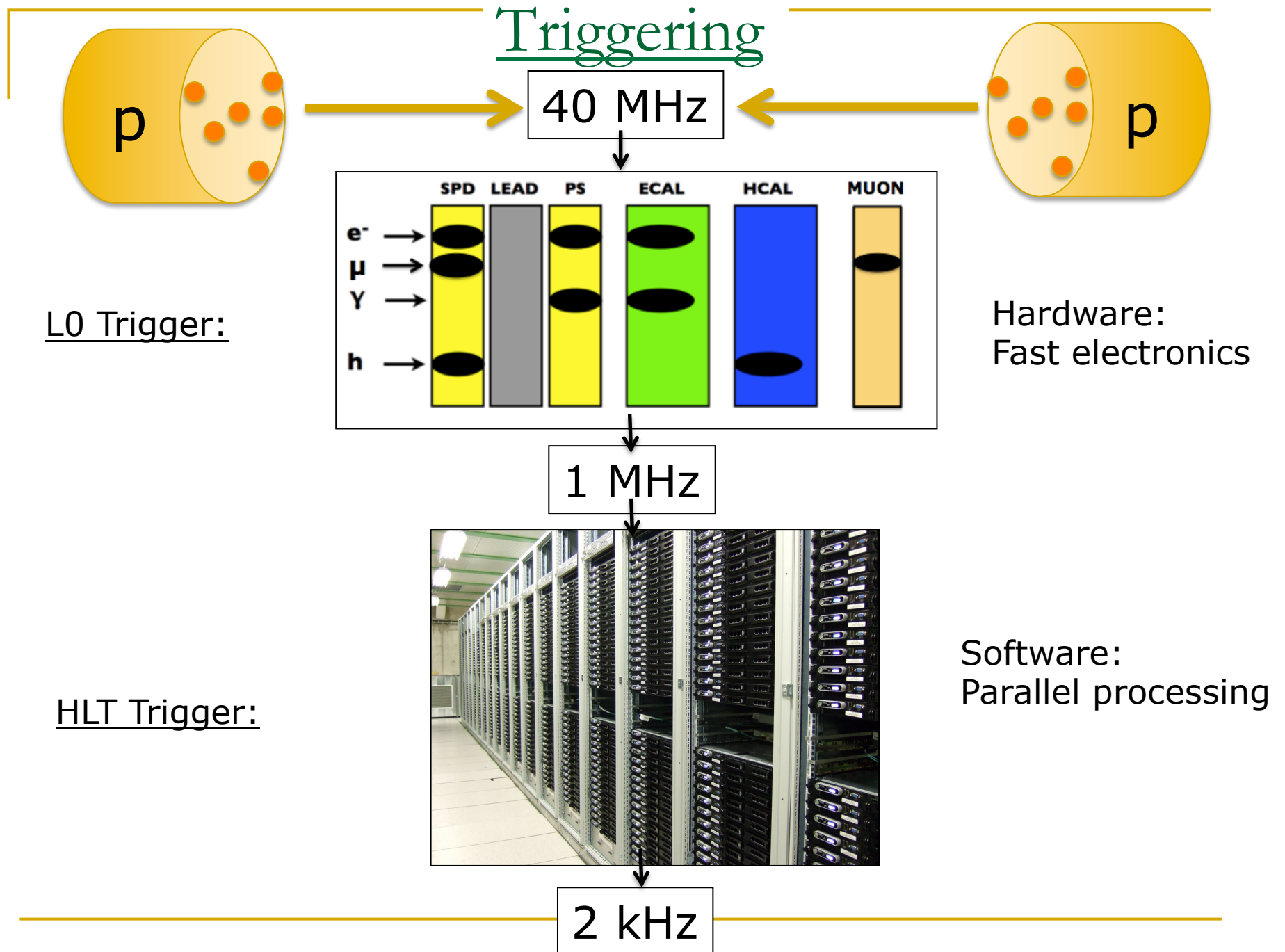
Calorimeter System in LHCb



Scintillation Pad Detector.

If a charged particle goes through, we get a signal.
Rough count of number of charged particles.

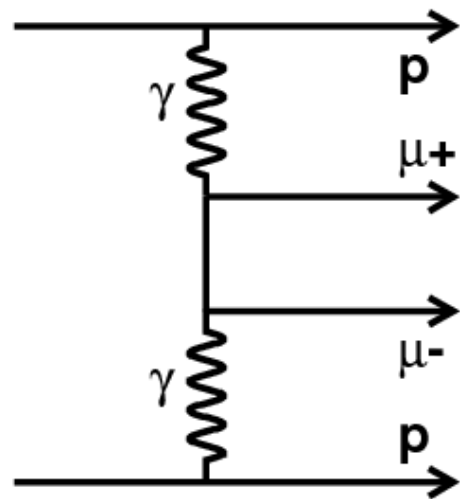
Use in trigger to select **low multiplicity** events for CEP. $>0, <20$ hits



Diffraction Physics with muons

Central Exclusive Production with Dimuon final states

Related phenomena where the colourless object creates a particle



QED

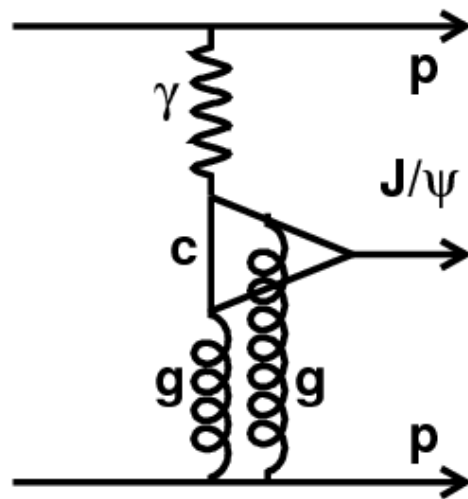
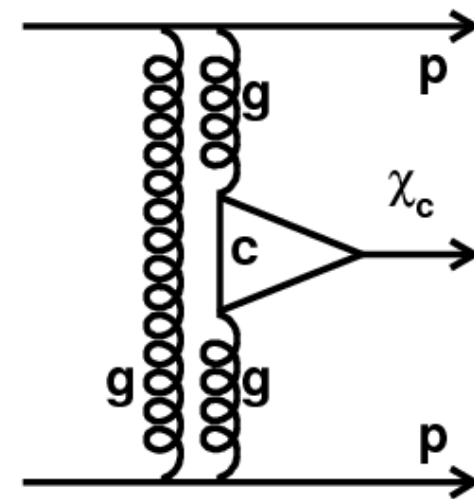


Photo production



Double pomeron exchange

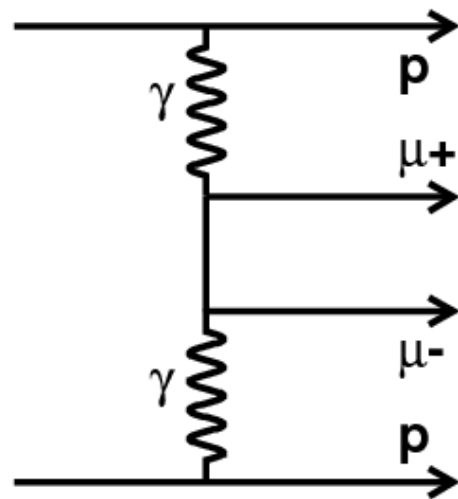
(Note: $J/\psi \rightarrow \mu\mu$ and $\chi_c \rightarrow J/\psi\gamma$)

Requiring dimuons significantly reduces inclusive QCD backgrounds

Motivation

Usually proton collisions produce very many final state particles because the gluon is a coloured object.

But if a **colourless** object is exchanged.....



QED

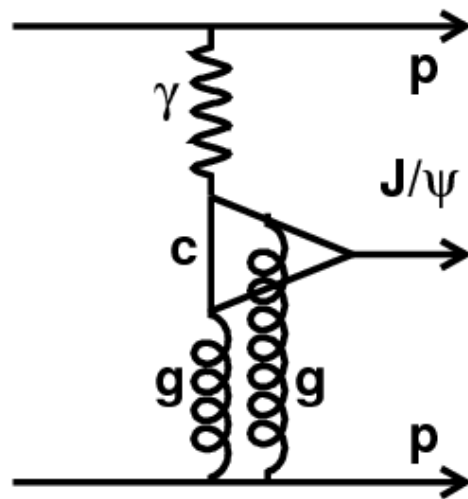
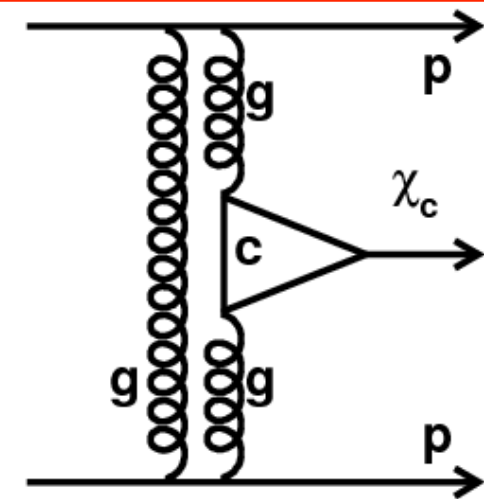


Photo production



Double pomeron exchange

Unambiguous evidence for pomeron

Constrain diffractive PDF at very low x (10^{-6})

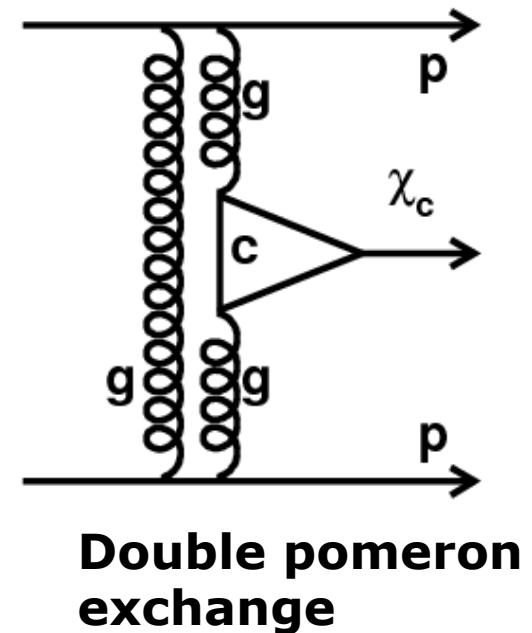
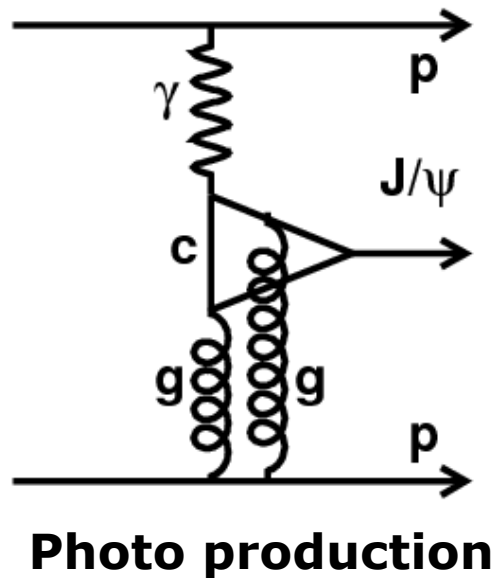
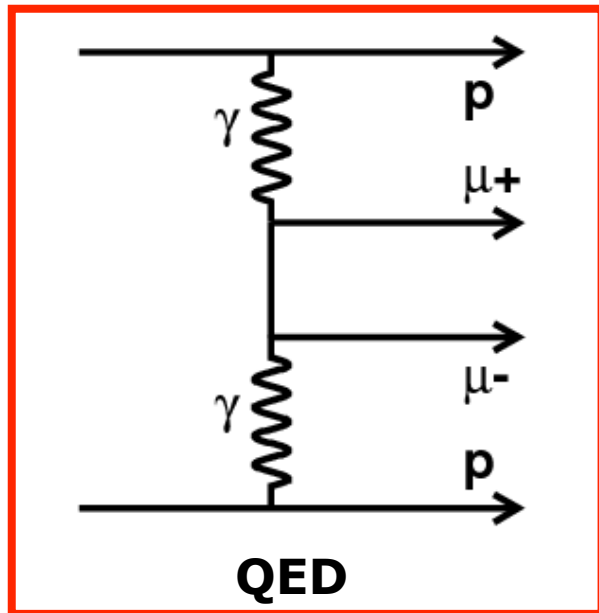
Sensitive to **saturation** effects

'Standard Candle' for other DPE processes, in particular, Higgs.

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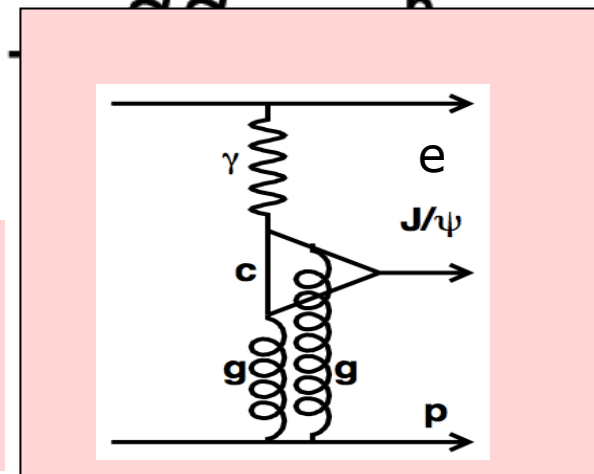
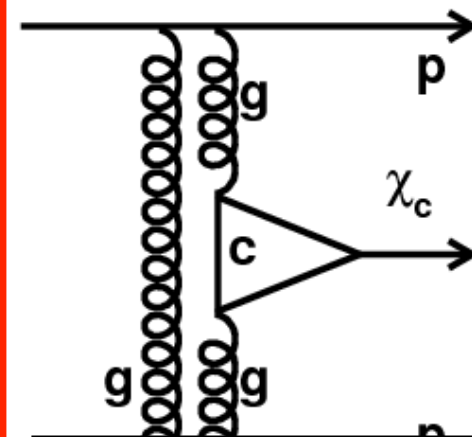
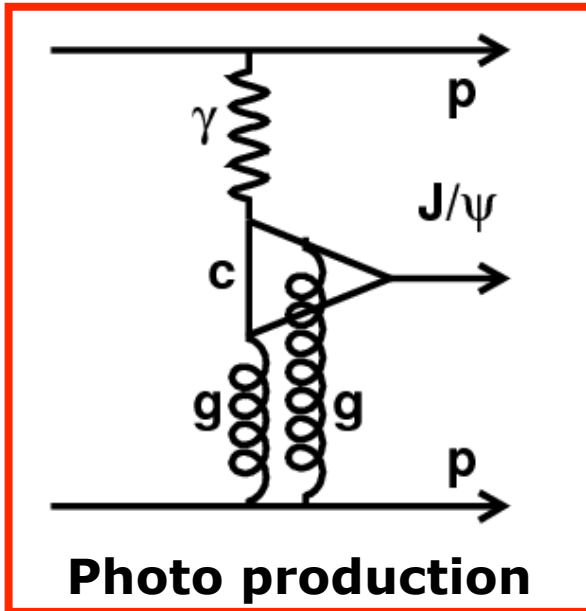
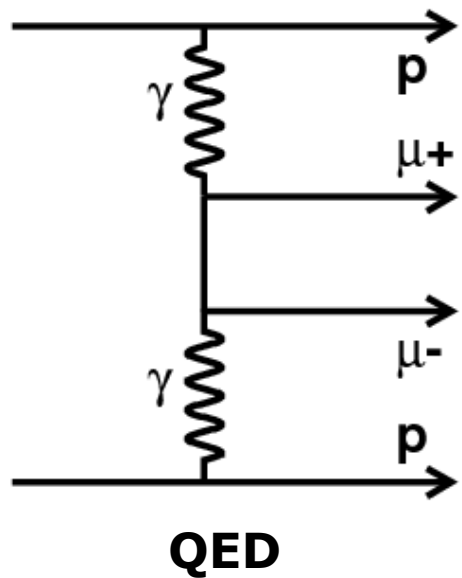


QED process. Can be predicted with high accuracy ($<1\%$)
Candidate process for very precise luminosity determination at LHC

Motivation

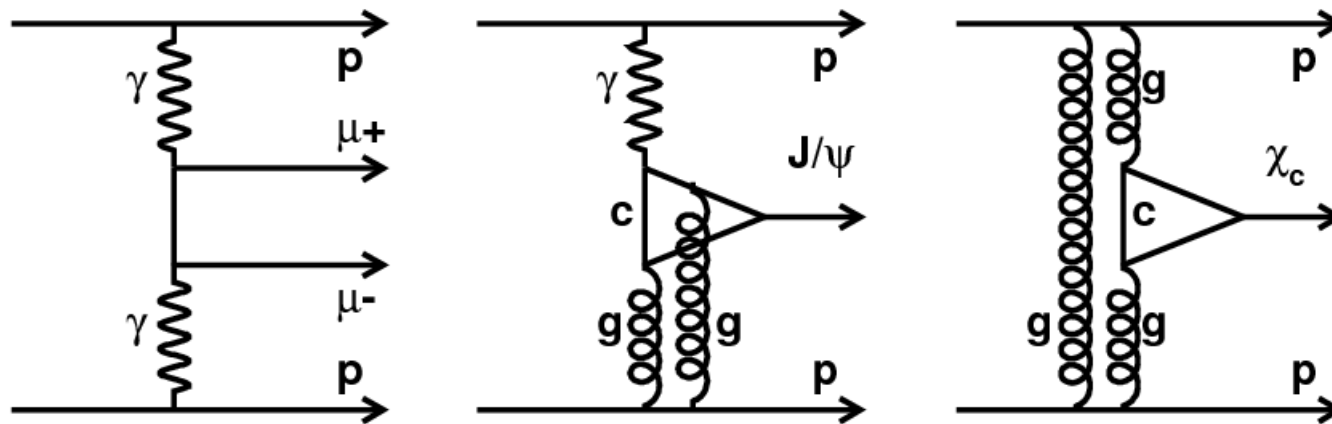
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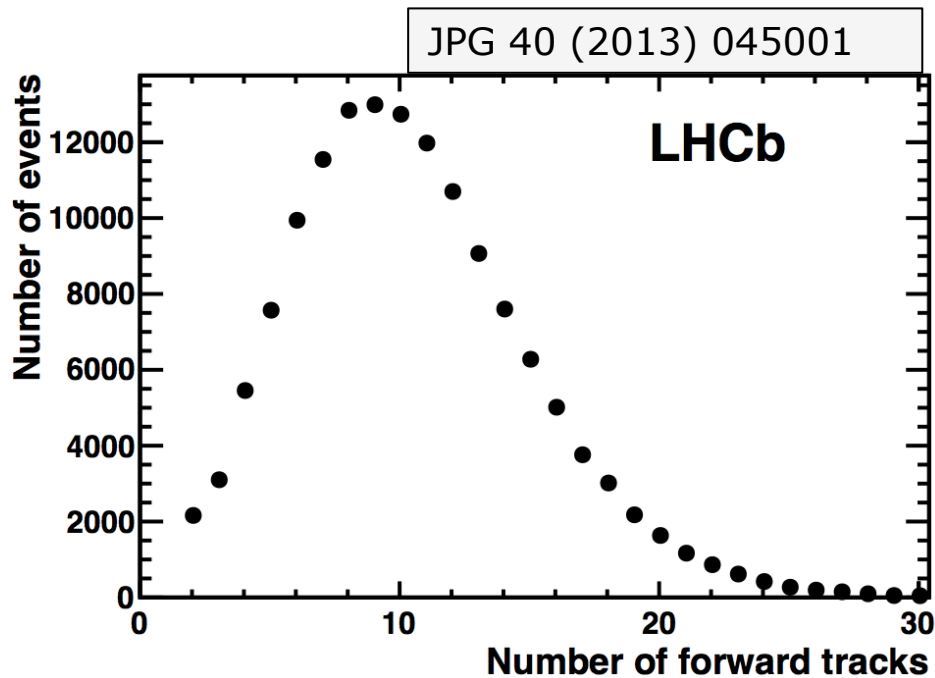
Test of QCD and pomeron in clean environment
 Measured at HERA/Tevatron but at different W
 Sensitive to diffractive PDF at very low x (10^{-6})
 Search for the odderon

Simple Selection Criteria

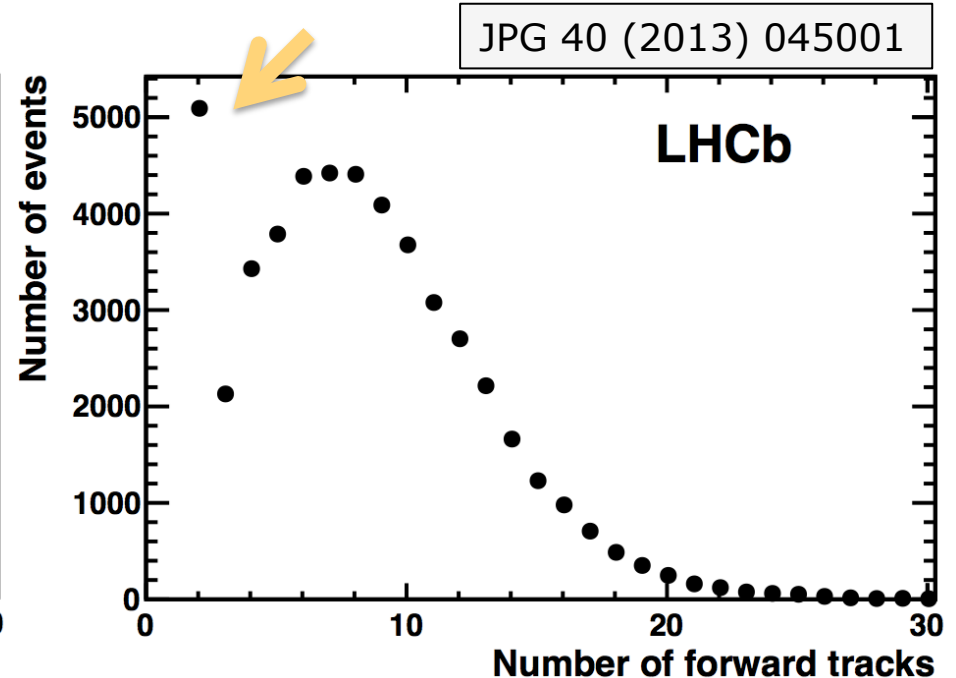


- **No backward tracks (2 gaps that sum to 3.5 units of rapidity)**
- **Precisely two forward muons**
- No photons (for J/ψ and diphoton process)
- One photon (for χ_c analysis)
- p_T of dimuon < 900 MeV (< 100 MeV for $p_{\mu\mu}$).

Effect of rapidity gap requirement on low multiplicity muon triggered events



All triggered events



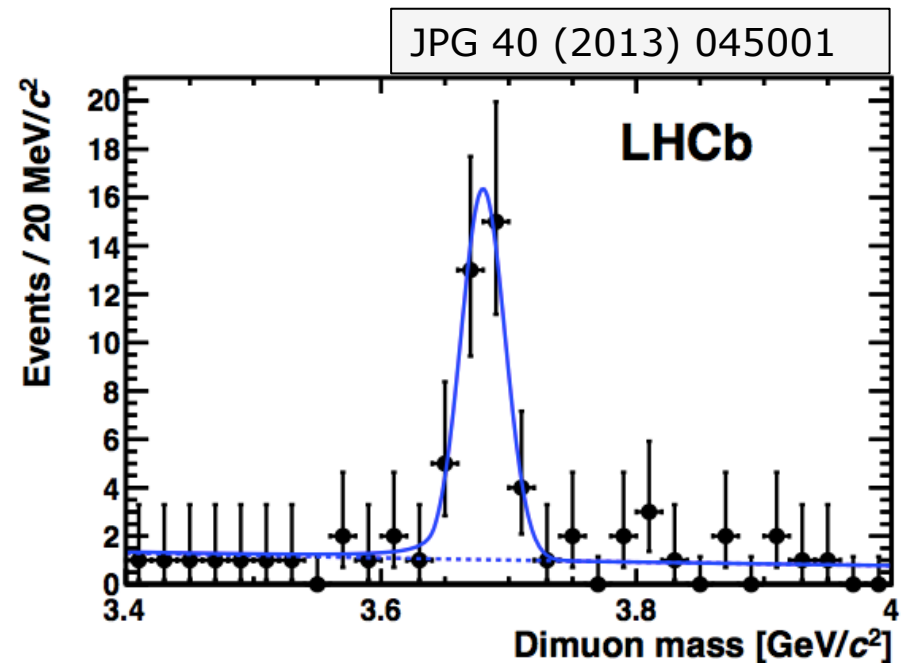
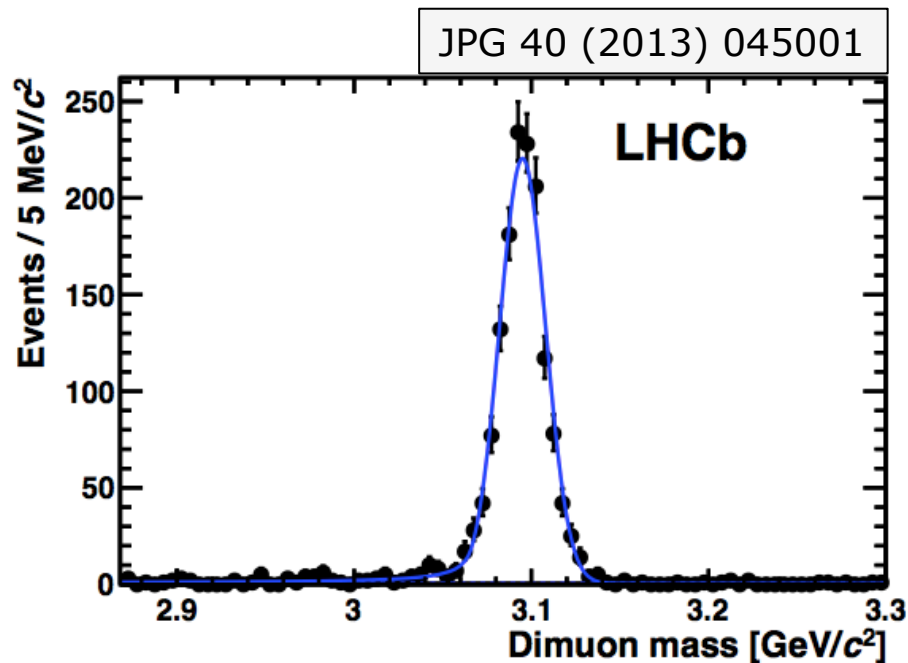
With veto on backward tracks

J/ψ and ψ'

- Results published in JPG 40 (2013) 045001
- Based on 37pb^{-1} (Full 2010 dataset)

- No backward tracks
- Precisely two forward muons
- No photons

Non-resonant background very small



Distributions are not background-subtracted.
37pb-1 of data: 1492 J/ψ and 40 ψ(2s)

Cross-section measurement

Purity:

1. non-resonant bkg (1%)
2. Chi_c feeddown (9%)
3. Psi' feeddown (2%)
4. Inelastic Jpsi production (30%)

Number of events observed

$$\sigma = \frac{pN}{\epsilon L}$$

Luminosity

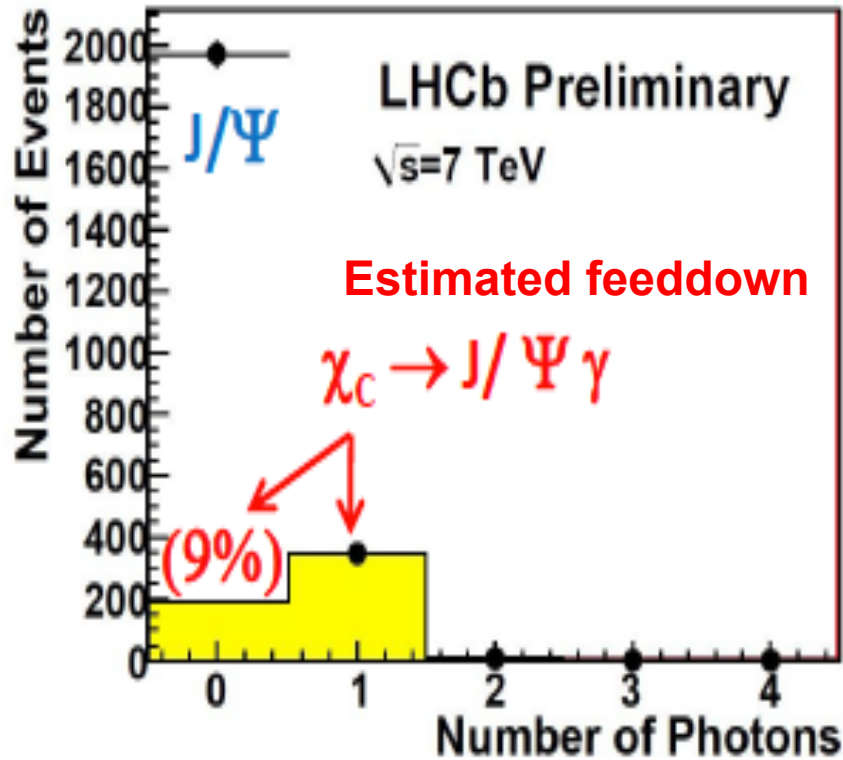
Efficiency:

1. Trigger
2. Tracking & muon id.
3. Single interaction beam-crossing

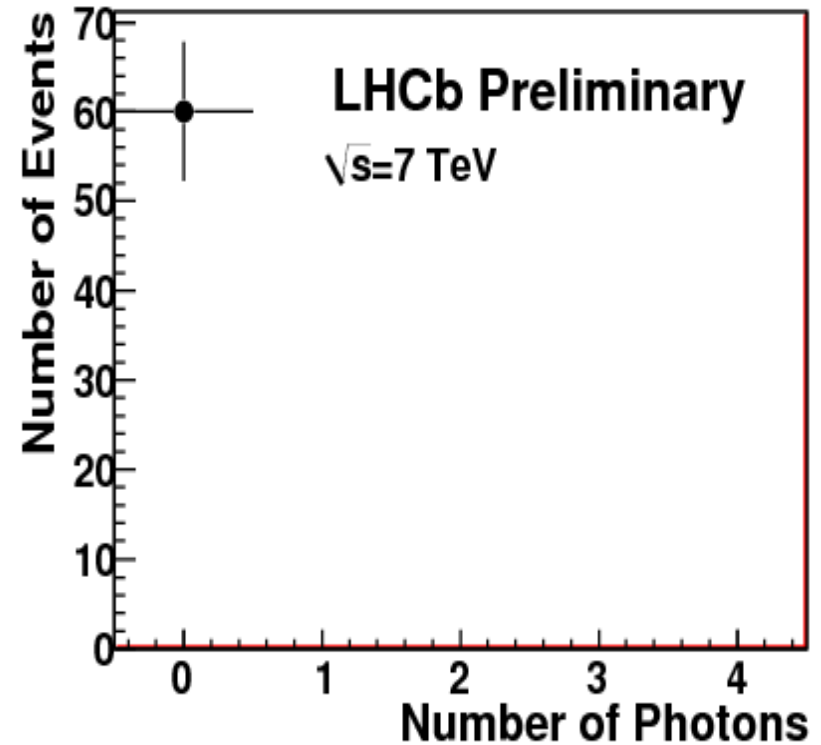
$$P(n) = \frac{\mu^n e^{-\mu}}{n!}$$

Feed-down background

J/ψ

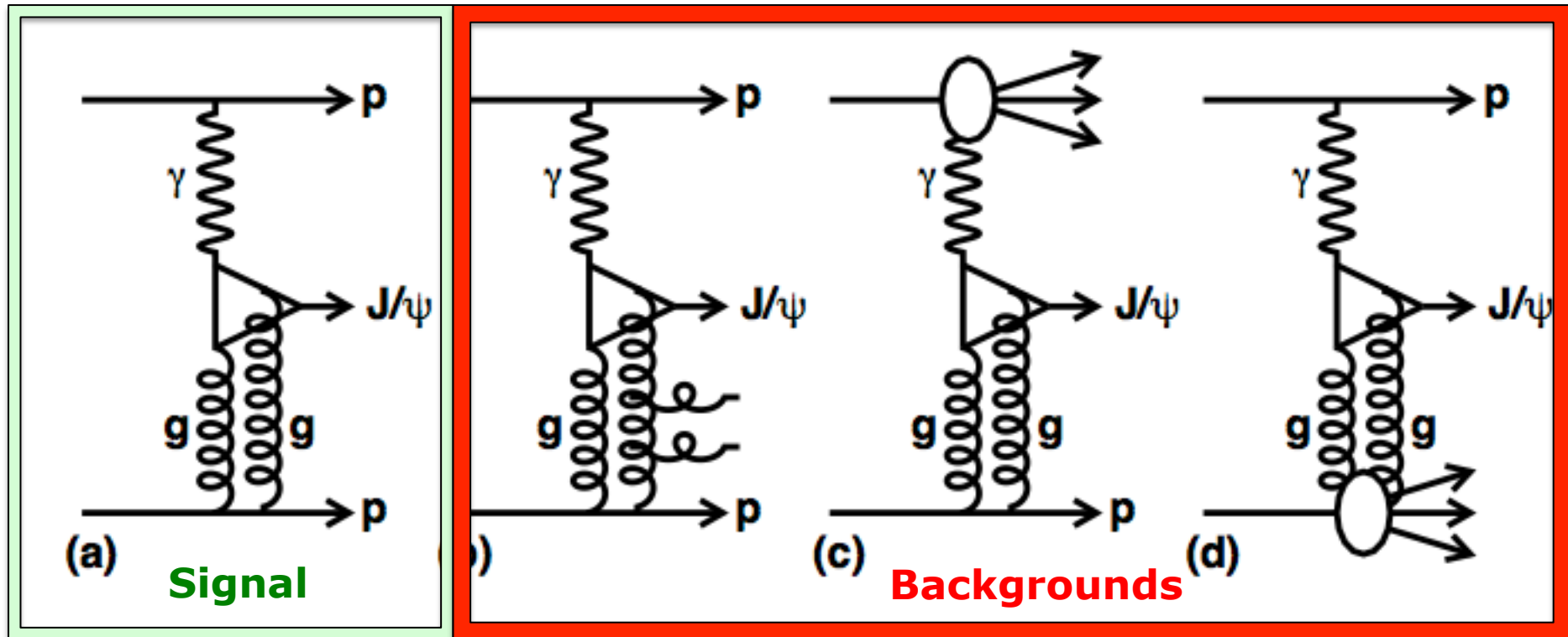


ψ'



(Note: $J/\psi \rightarrow \mu\mu$ and $\chi_c \rightarrow J/\psi\gamma$)

Inelastic background



Characterise p_T spectrum of background using shapes with 3-8 tracks and extrapolate to 2 track case.

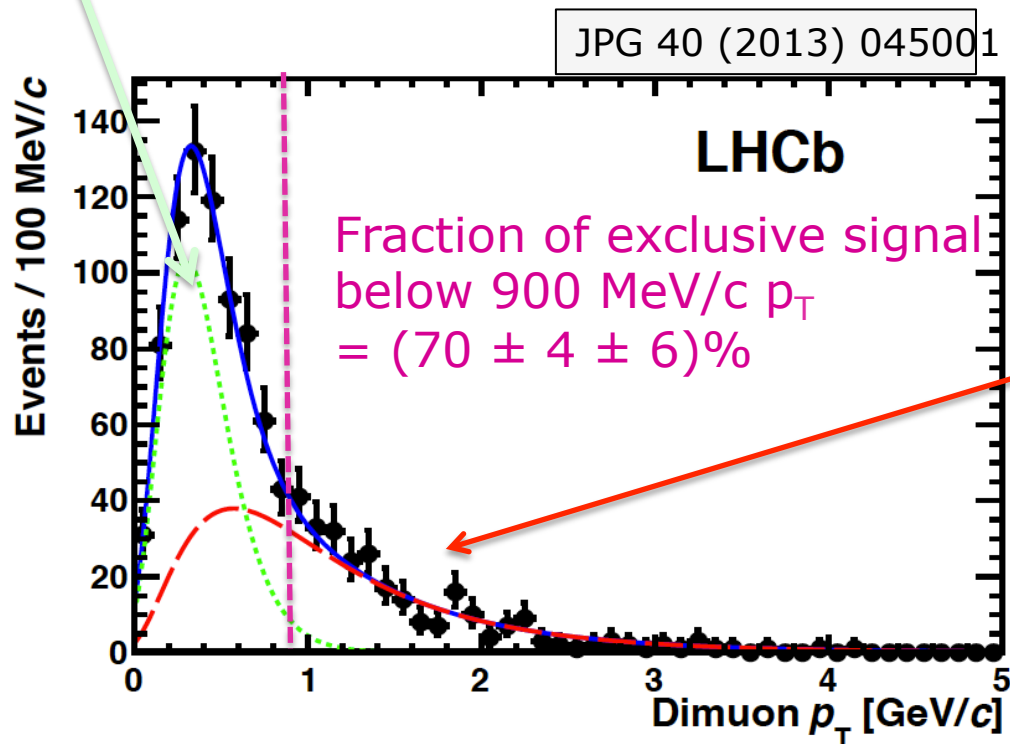
Inelastic background

Signal shape

Estimated from Superchic using $\exp(-b p_T^2)$ (arXiv: 0909.4748)

Take b from HERA. Extrapolate to LHCb energy to get $b = 6.1 \pm 0.3 \text{ GeV}^{-2}$

Crosscheck: Fit to spectrum below with b free gives $b = 5.8 \pm 1 \text{ GeV}^{-2}$



Inelastic background shape

Estimated from data.
Characterise shape for 3-8 tracks
and extrapolate to 2 tracks.

LHCb compared to theory & experiment

Results (in pb) are for VM with two muons with $2 < \eta < 4.5$

Predictions	$\sigma_{pp \rightarrow J/\psi (\rightarrow \mu^+ \mu^-)}$	$\sigma_{pp \rightarrow \psi(2S) (\rightarrow \mu^+ \mu^-)}$
Gonçaves and Machado	275	
STARLIGHT	292	6.1
Motyka and Watt	334	
SUPERCHIC ^a	396	
Schäfer and Szczurek	710	17
LHCb measured value	$307 \pm 21 \pm 36$	$7.8 \pm 1.3 \pm 1.0$

^a SUPERCHIC simulation does not include a gap survival factor.

All predictions (bar Schaefer&Szcaurek) have similar approach and give similar results and are consistent with our data.

See J. Figiel presentation at this school

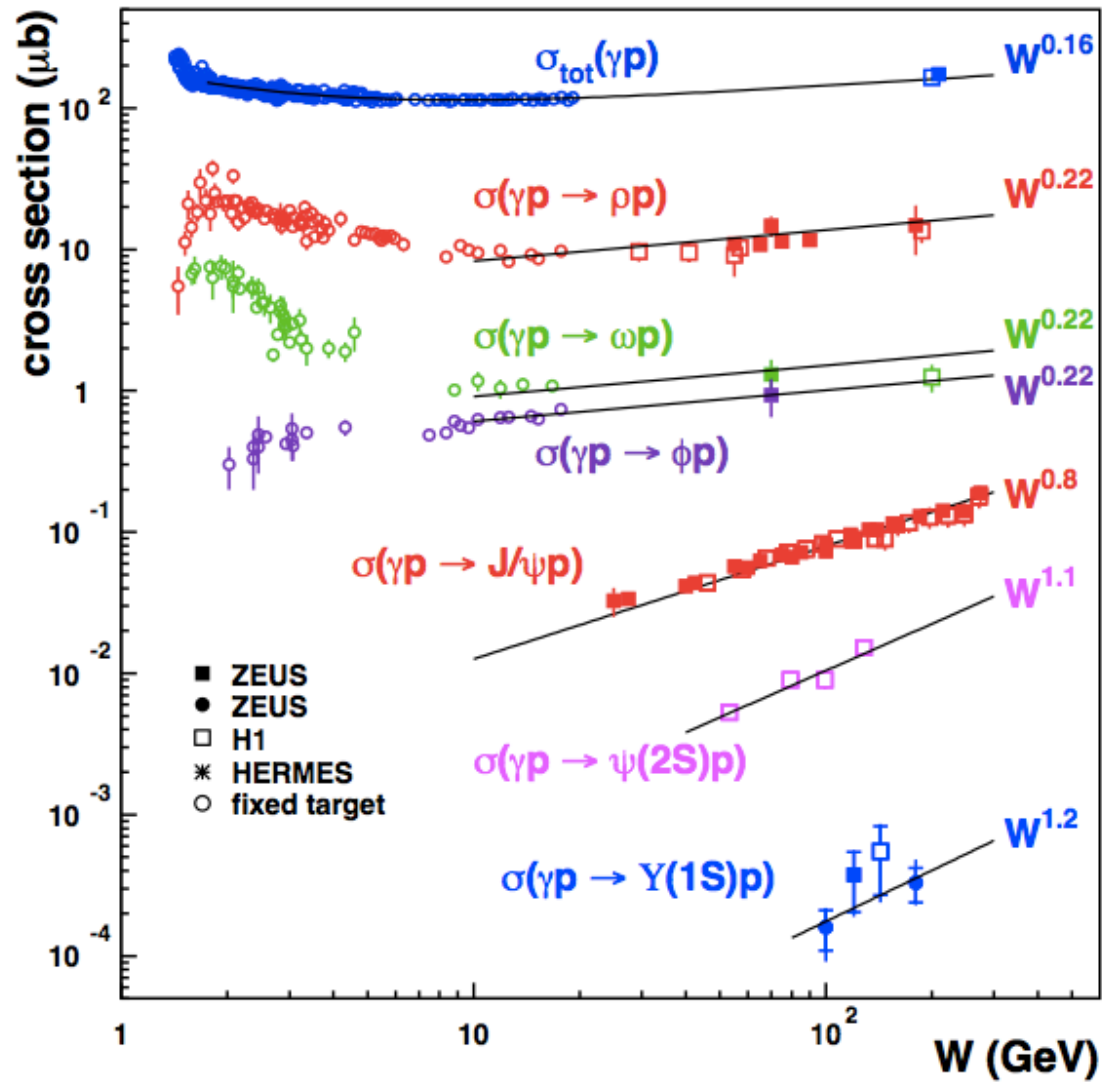
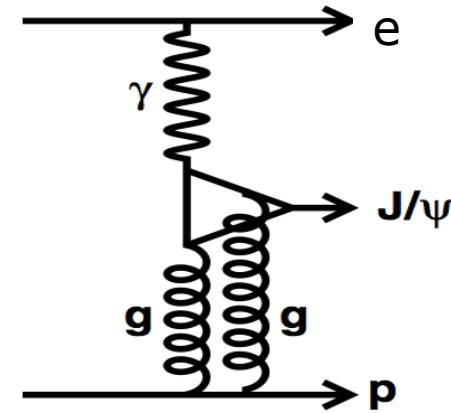


Photo-production cross-section



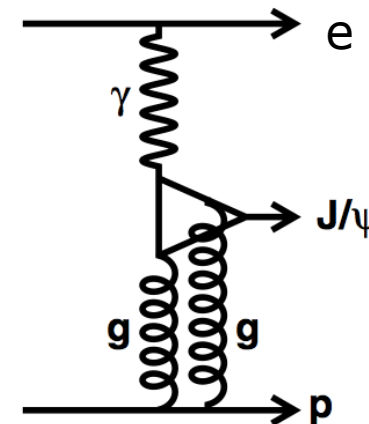
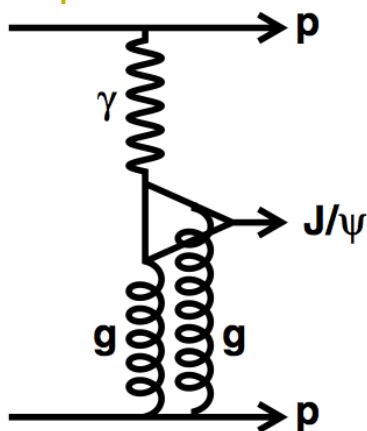
$$\frac{d\sigma}{dt} (\gamma^* p \rightarrow J/\psi p) \Big|_{t=0} = \frac{\Gamma_{ee} M_{J/\psi}^3 \pi^3}{48\alpha} \left[\frac{\alpha_s(\bar{Q}^2)}{\bar{Q}^4} xg(x, \bar{Q}^2) \right]^2 \left(1 + \frac{Q^2}{M_{J/\psi}^2} \right)$$

$$\bar{Q}^2 = (Q^2 + M_{J/\psi}^2)/4, \quad x = (Q^2 + M_{J/\psi}^2)/(W^2 + M_{J/\psi}^2).$$

Cross-section proportional to gluon² $\sigma \sim (xg)^2$ and so $\sigma \sim x^\lambda$

- [1] Martin A D, Nockles C, Ryskin M and Teubner T 2008 Small x gluon from exclusive J/ψ production *Phys. Lett. B* **662** 252 (arXiv:0709.4406)
- [2] Ryskin M G 1993 J/ψ electroproduction in LLA QCD *Z. Phys. C* **57** 89
- [3] Ryskin M G, Roberts R G, Martin A D and Levin E M 1997 Diffractive J/ψ photoproduction as a probe of the gluon density *Z. Phys. C* **76** 231 (arXiv:hep-ph/9511228)

LHCb compared to HERA



$$W^2 \equiv (q + p_2)^2 = x_\gamma s - Q^2,$$

Twofold ambiguity \rightarrow

$$x_\gamma = \frac{M_{\psi_\perp}}{\sqrt{s}} e^{y_\psi},$$

$$x = \frac{M_{\psi_\perp}}{\sqrt{s}} e^{-y_\psi},$$

LHCb c/s is HERA c/s + photon spectrum + gap survival factor ($r \sim 0.8$)

$$\frac{d\sigma}{dy}_{pp \rightarrow pVp} = r(y) \left[k_+ \frac{dn}{dk_+} \sigma_{\gamma p \rightarrow Vp}(W_+) + k_- \frac{dn}{dk_-} \sigma_{\gamma p \rightarrow Vp}(W_-) \right],$$

$$k_\pm \approx (m_V/2) \exp(\pm|y|),$$

LHCb differential data fitted assuming power law dependence $\sigma(W) = aW^\delta$

$$a = 0.8_{-0.5}^{+1.2} nb$$

$$\delta = 0.92 \pm 0.15$$

LHCb

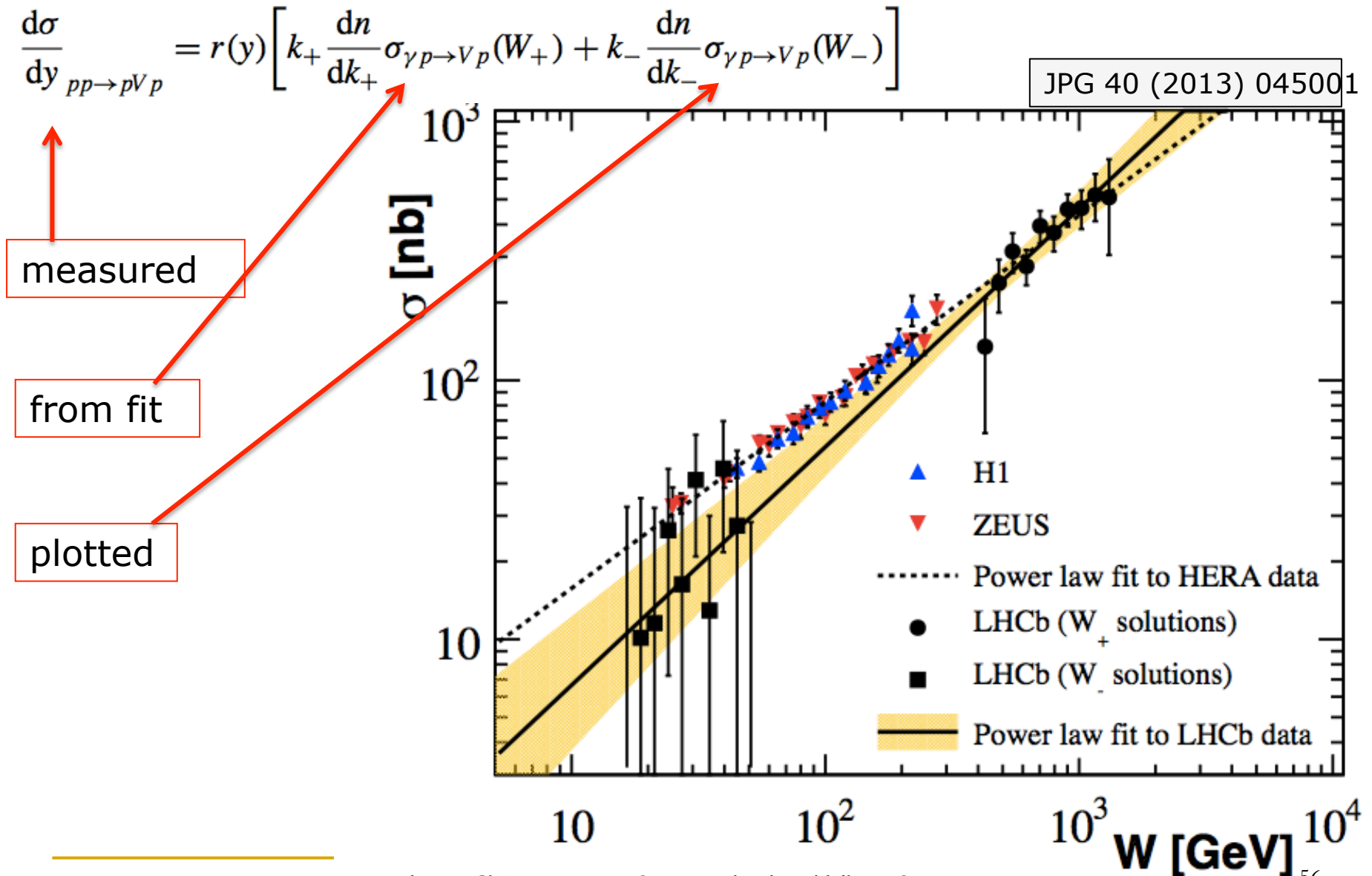
Power law results

$$a = 3nb$$

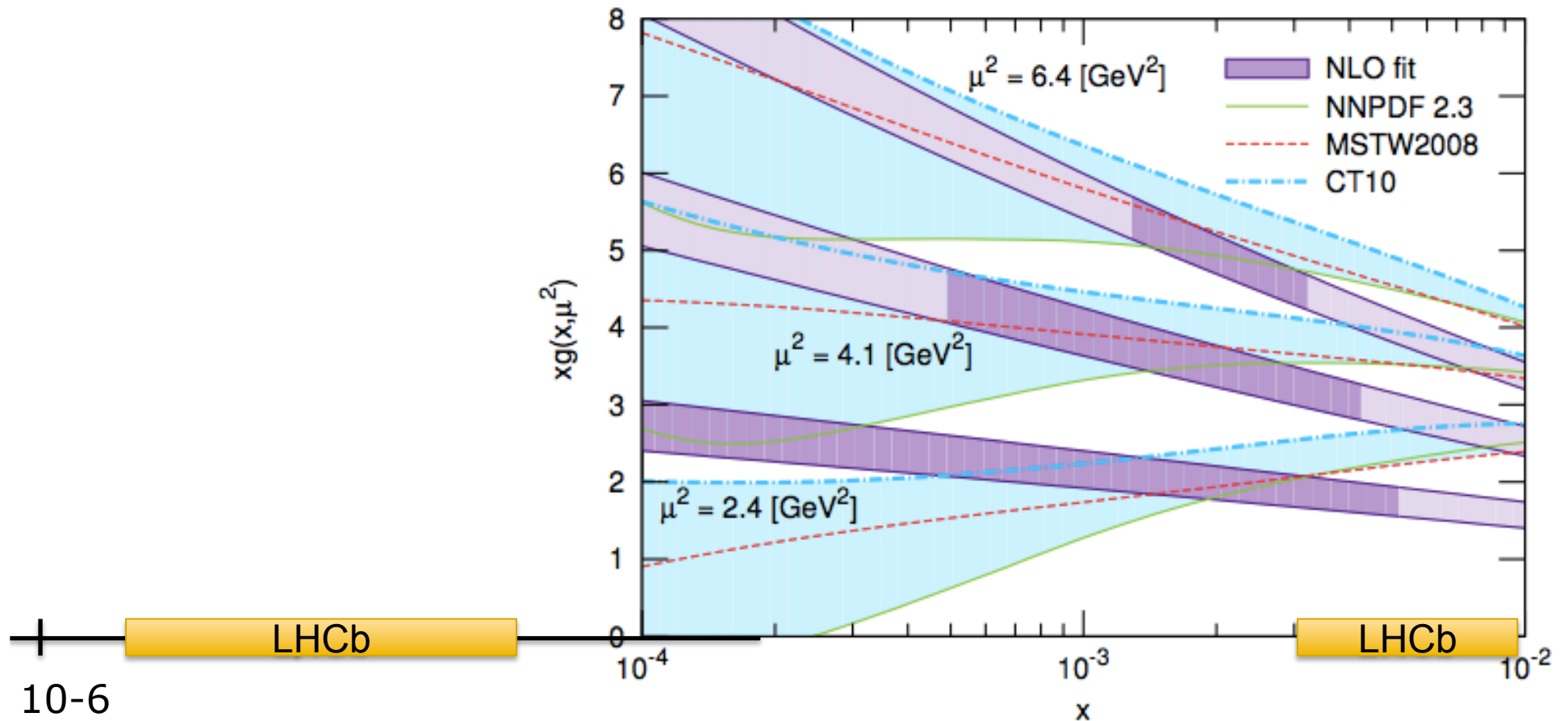
$$\delta = 0.72$$

HERA

LHCb compared to theory & experiment

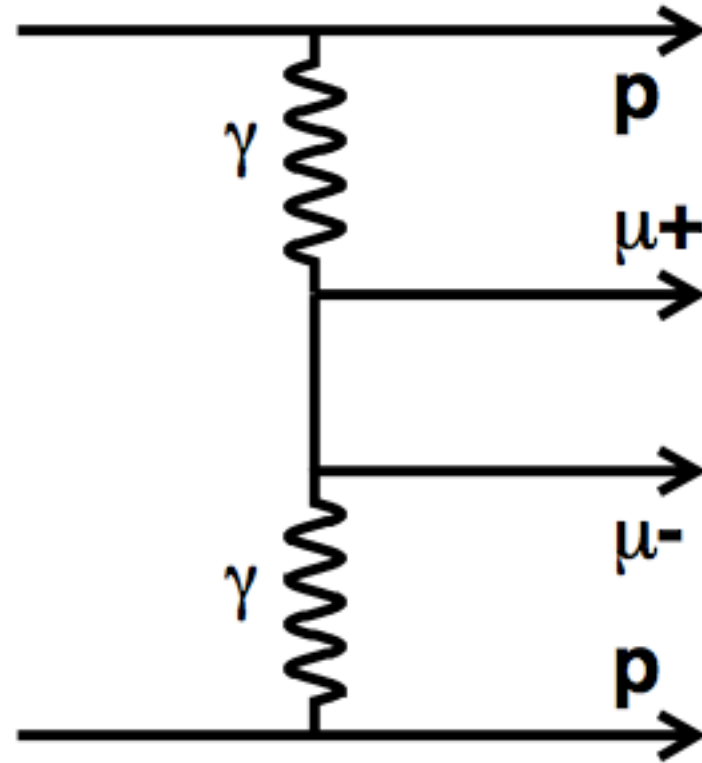


Sensitivity to gluon pdf (arXiv: 1307.7099)



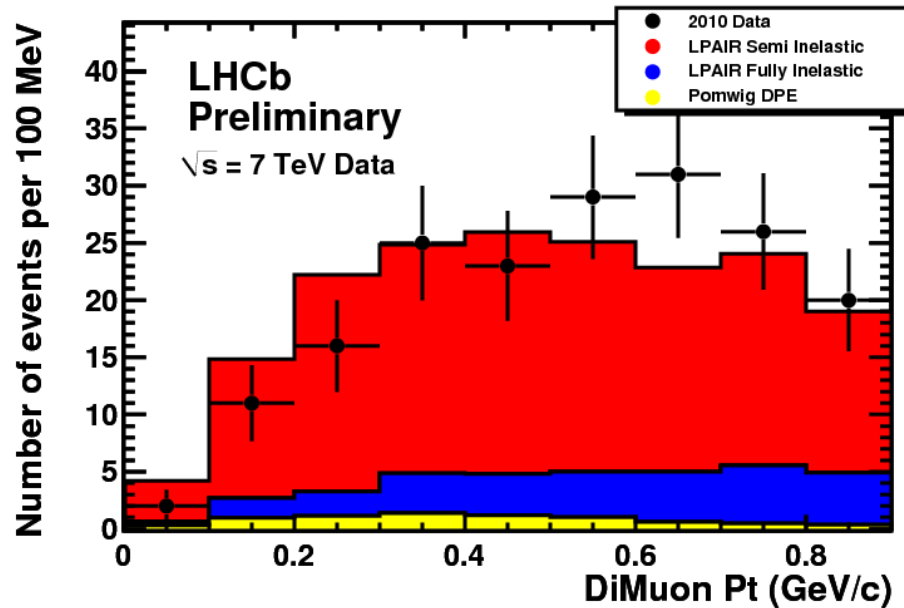
pp->pμμp

LHCb-CONF-2011-022



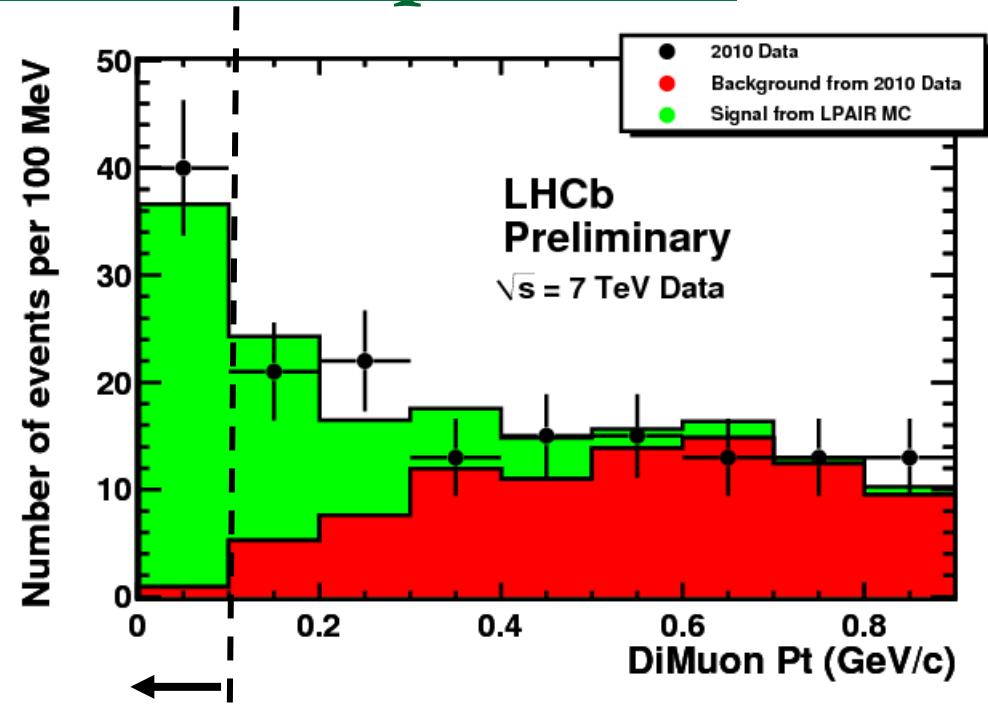
- No backward tracks
- Precisely two forward muons. $m_{\mu\mu} > 2.5 \text{ GeV}$
- No photons

Fit elastic and inelastic components



Shape for inelastic events

Note: this time we have simulation that predicts the shape for the three contributions.



Fit to signal events

Background shape from data
 Signal shape from simulation.

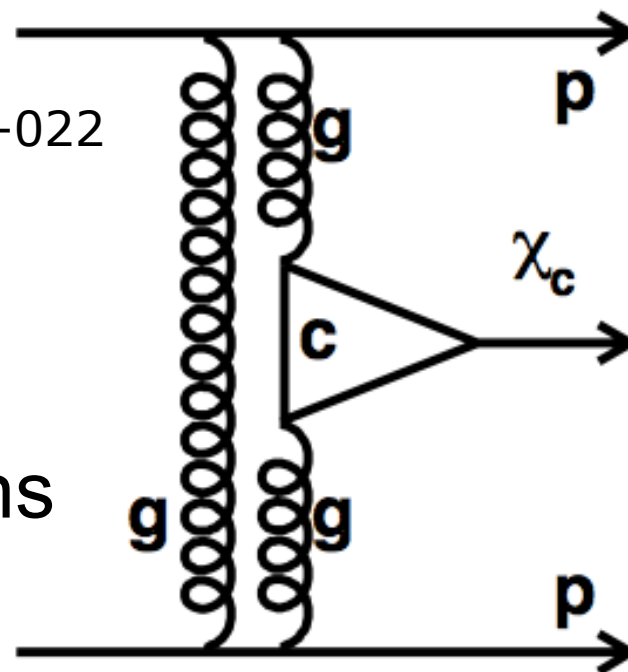
Measured cross-section $p\mu\mu p$: 67 ± 19 pb

LPAIR (J. Vermaseren) 42 pb

$\chi_{c0,c1,c2}$

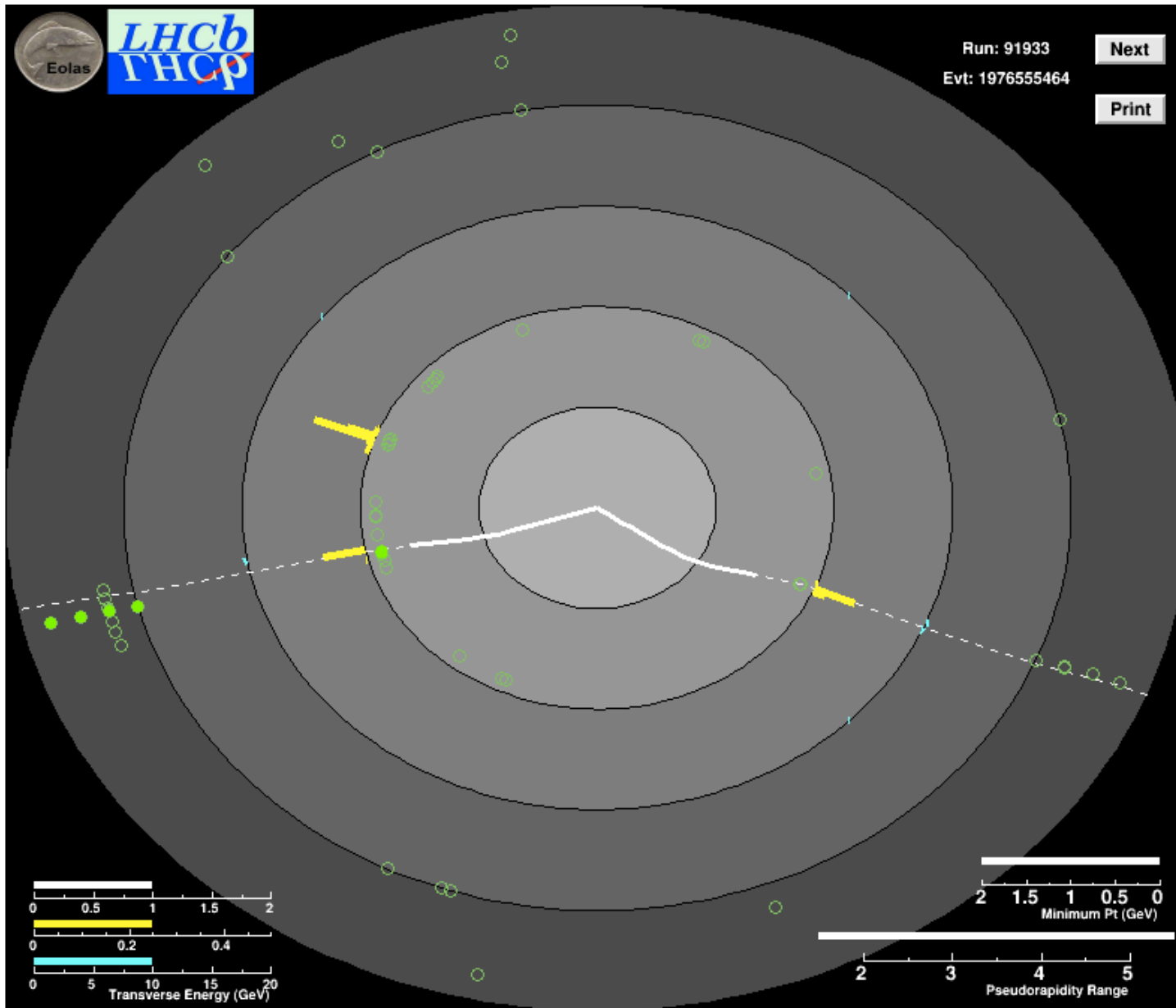
LHCb-CONF-2011-022

- No backward tracks
- Precisely two forward muons
- Precisely one photon

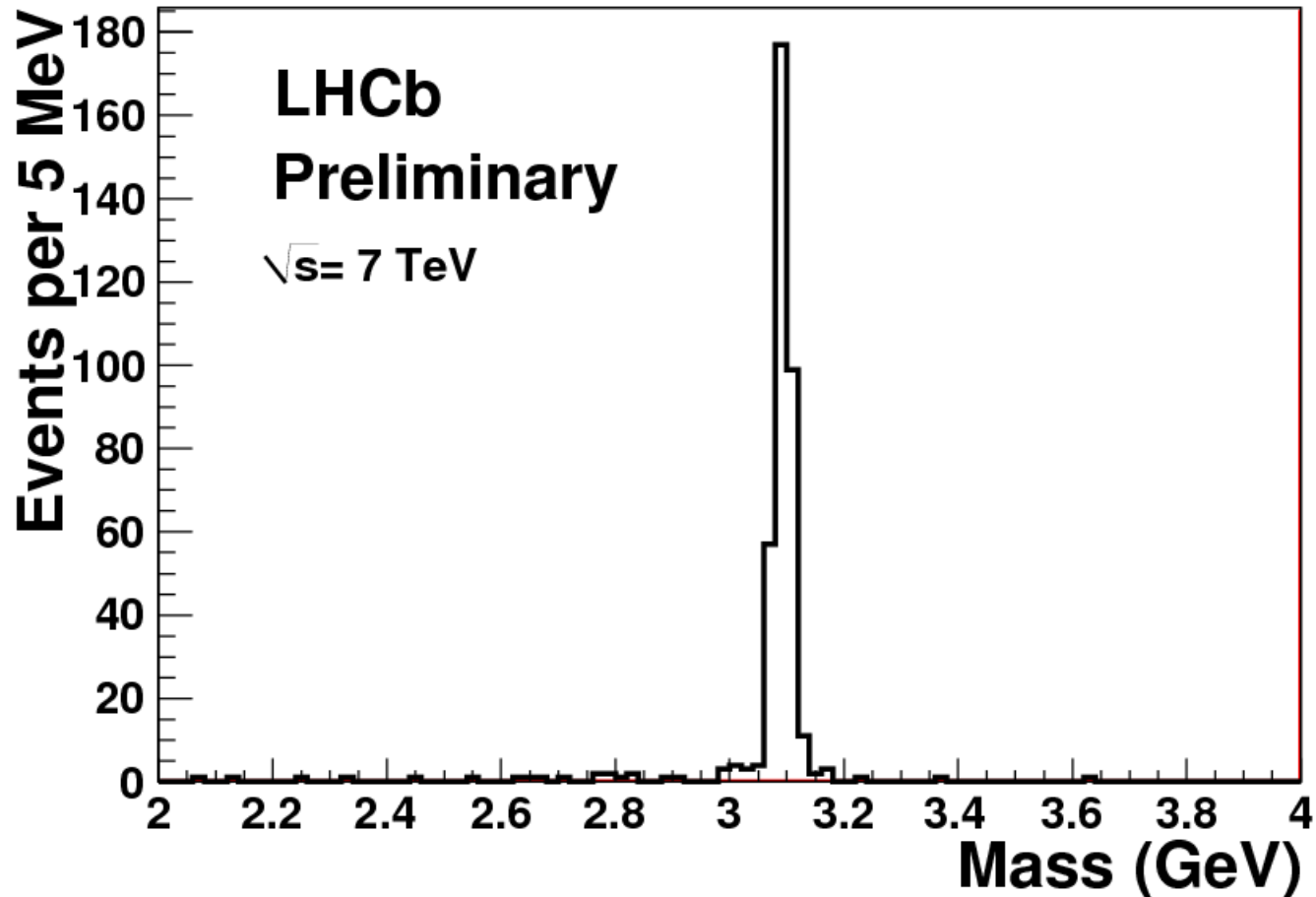


(Note: $\chi_c \rightarrow J/\psi \gamma$) and $J/\psi \rightarrow \mu\mu$

- Expect
 - χ_{c1} suppressed due to Landau-Yang theorem
 - χ_{c2} suppressed: can't have a bound state with $J=2, J_z=0$
 - χ_{c0} dominant (for small p_T)
 - This is different from inclusive chi production.

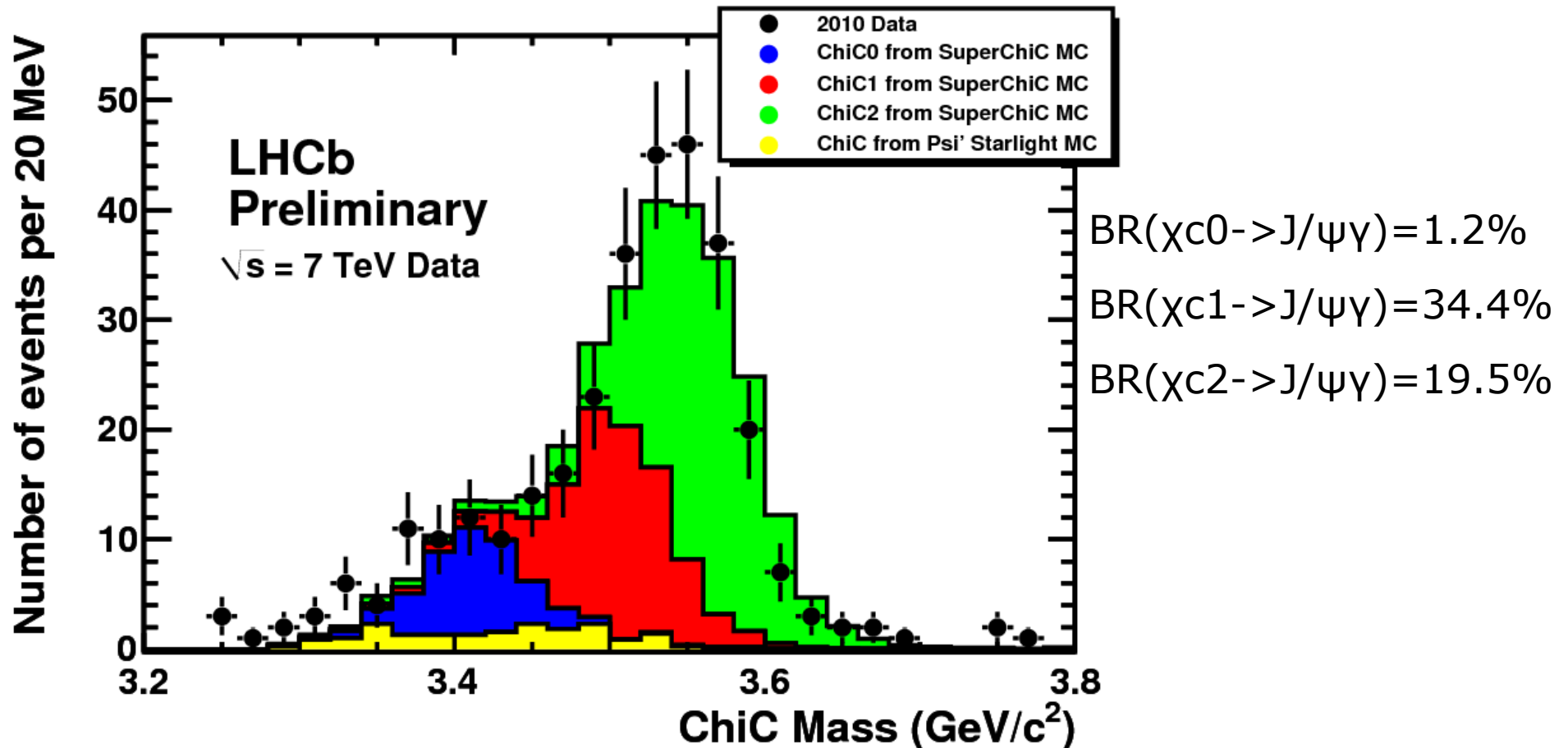


χ_c : DiMuon Invariant Mass



About half the background that was observed in the exclusive J/ψ analysis (since no continuum process).

χ_c : DiMuon+Photon Invariant Mass



Inelastic contribution appears to be much larger than for J/ψ .
In a first approximation it should be square of bkg in J/ψ process.

Theory v experiment

$$\begin{aligned}\sigma_{\chi_{c0} \rightarrow \mu+\mu-\gamma} &= 9.3 \pm 2.2 \pm 3.5 \pm 1.8 \text{ pb} \\ \sigma_{\chi_{c1} \rightarrow \mu+\mu-\gamma} &= 16.4 \pm 5.3 \pm 5.8 \pm 3.2 \text{ pb} \\ \sigma_{\chi_{c2} \rightarrow \mu+\mu-\gamma} &= 28.0 \pm 5.4 \pm 9.7 \pm 5.4 \text{ pb}\end{aligned}$$

LHCb preliminary results with 2010 data

$$\chi_0: 9.3 \pm 4.5 \text{ pb} \quad \chi_1: 16.4 \pm 7.1 \text{ pb} \quad \chi_2: 28.0 \pm 12.3 \text{ pb}$$

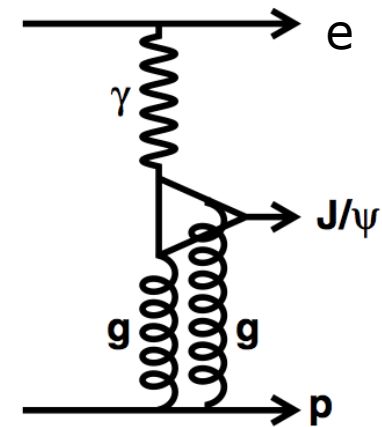
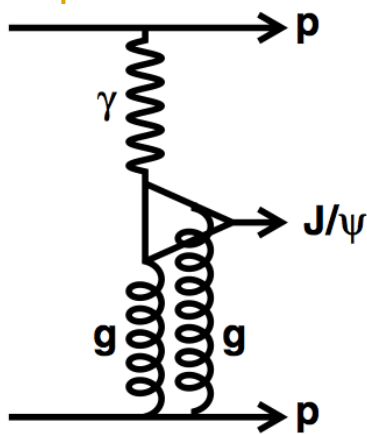
SuperChic: 14 pb 10 pb 3 pb

Large contribution due to χ_{c0} is confirmed.

χ_{c2} larger than expected but note that non-elastic background has been assumed same for each resonance. More precise data required.

Future Prospects

LHCb compared to HERA

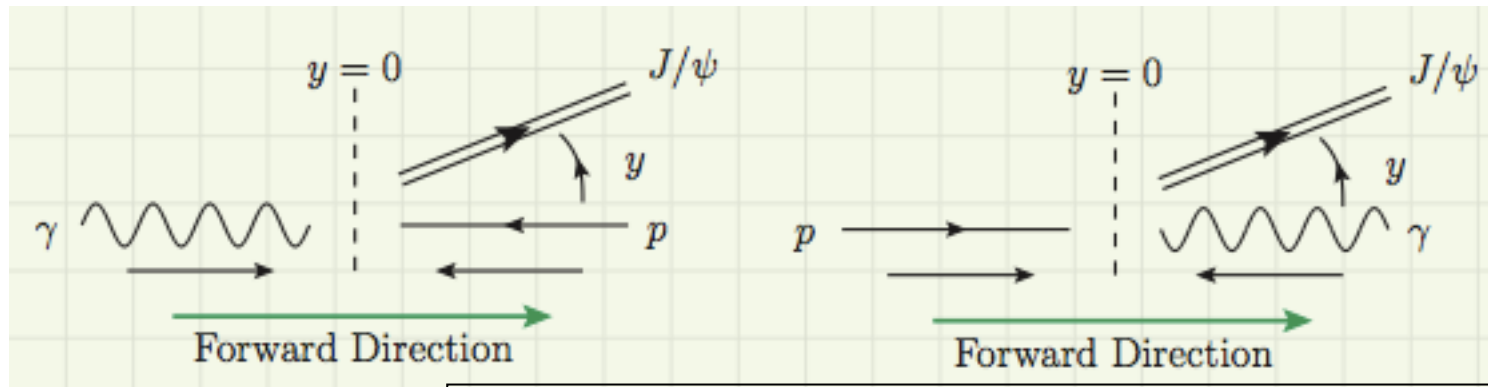


$$W^2 \equiv (q + p_2)^2 = x_\gamma s - Q^2,$$

Twofold ambiguity

$$x_\gamma = \frac{M_{\psi_\perp}}{\sqrt{s}} e^{y_\psi},$$

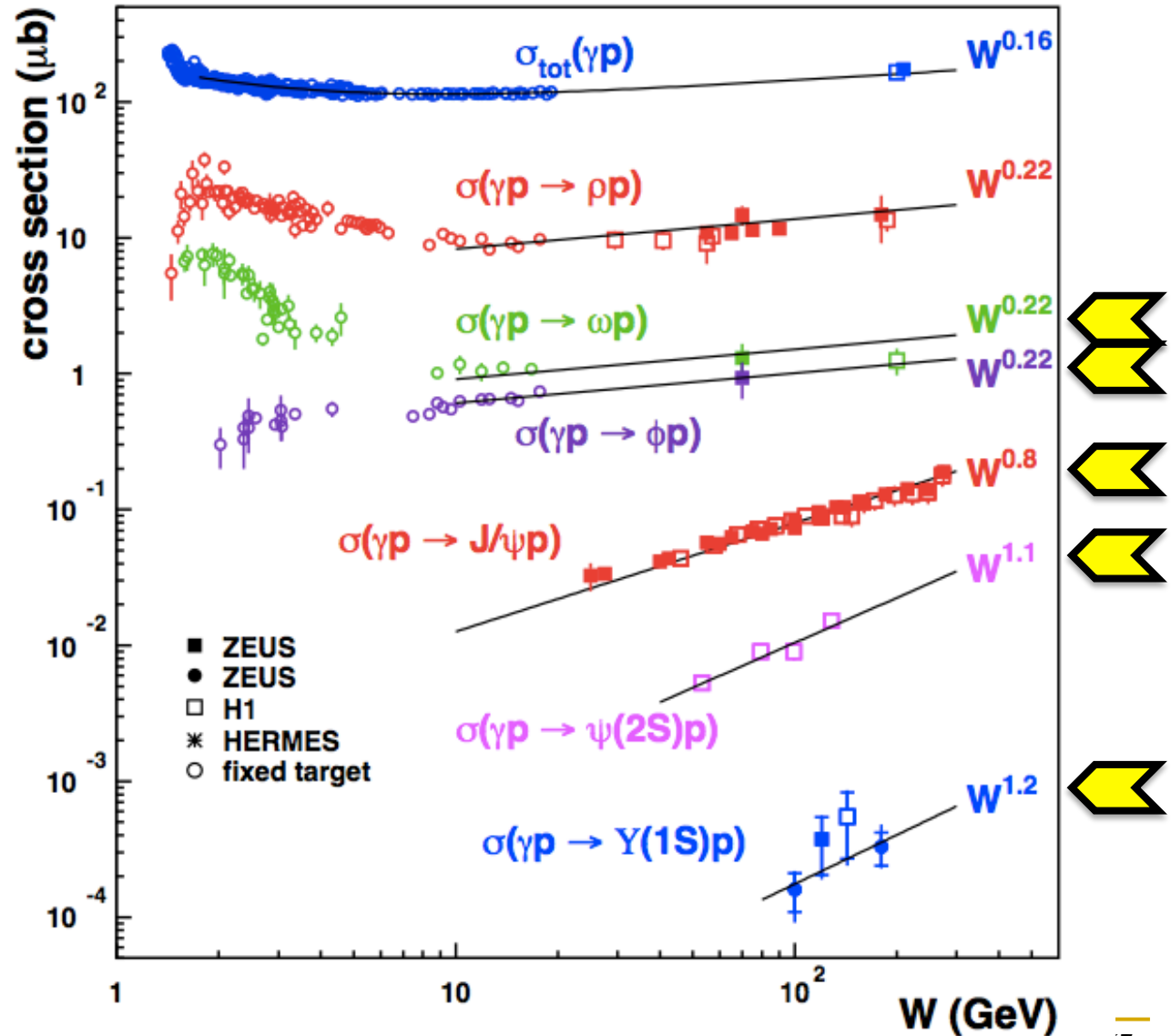
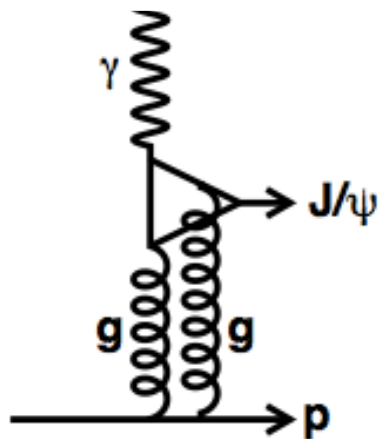
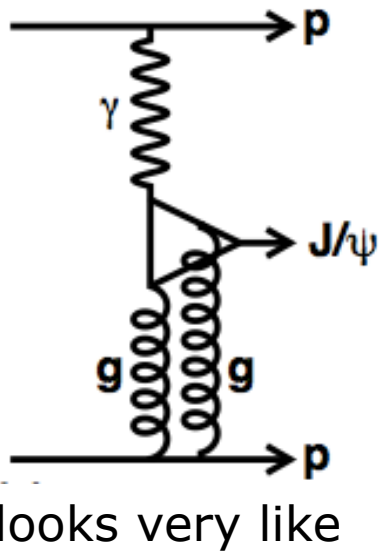
$$x = \frac{M_{\psi_\perp}}{\sqrt{s}} e^{-y_\psi},$$



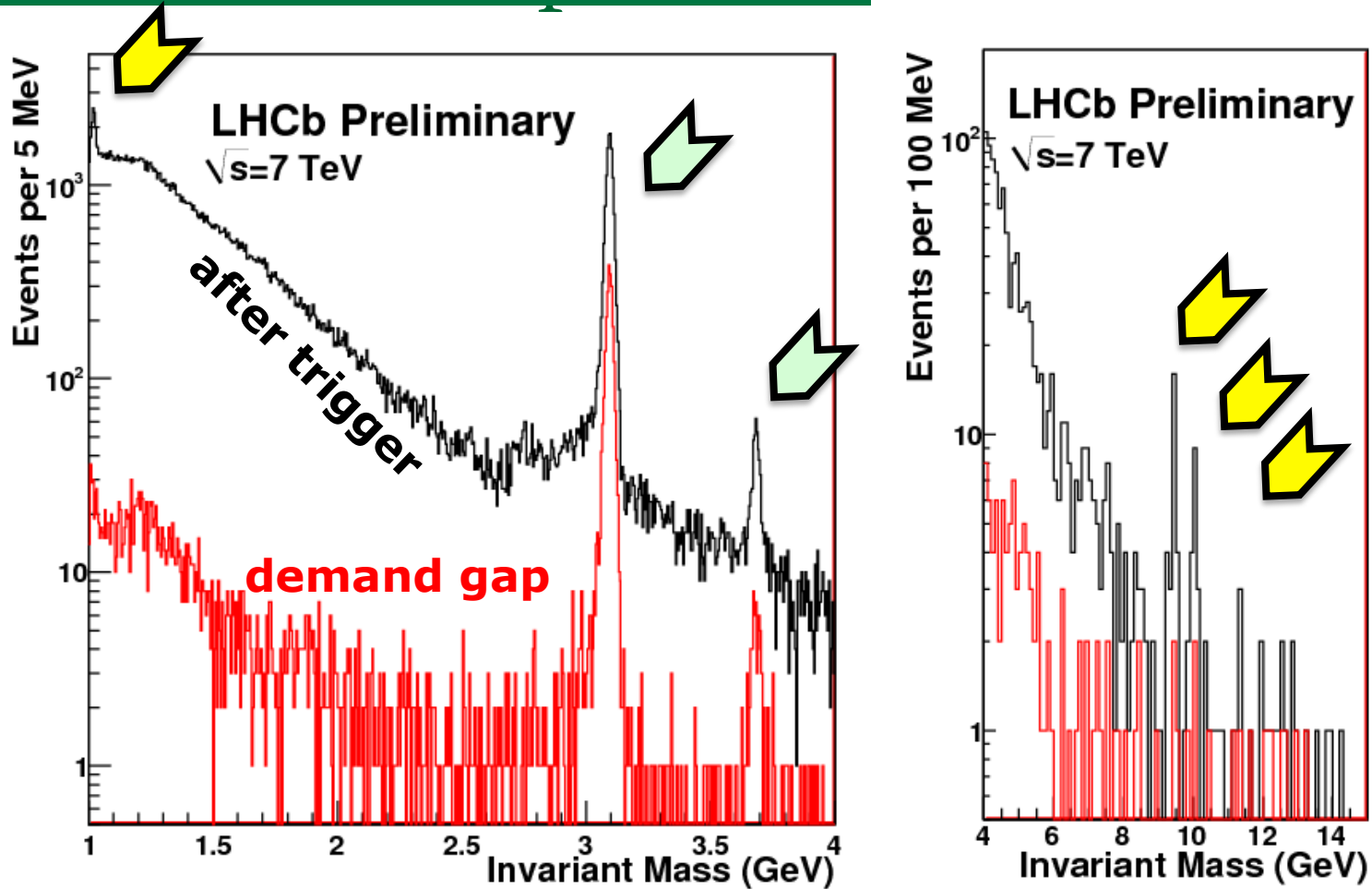
S. Jones, LHC Forward Physics WG , 27.8.2013

Repeat measurement with proton-lead collision data.
 Photon nearly always comes from the lead nucleus (Z^2)
 (J.Nystrand EPS2013, Stockholm)

LHCb compared to HERA



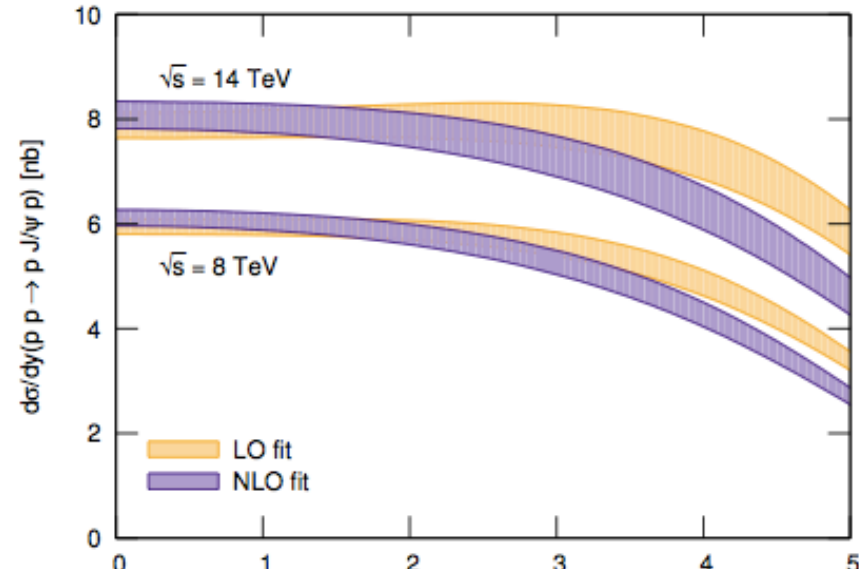
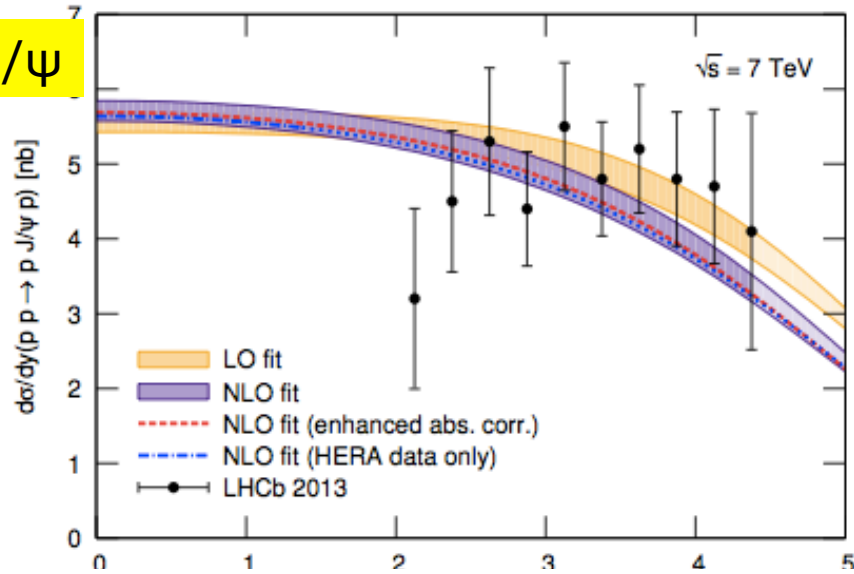
Dimuon Mass Spectrum



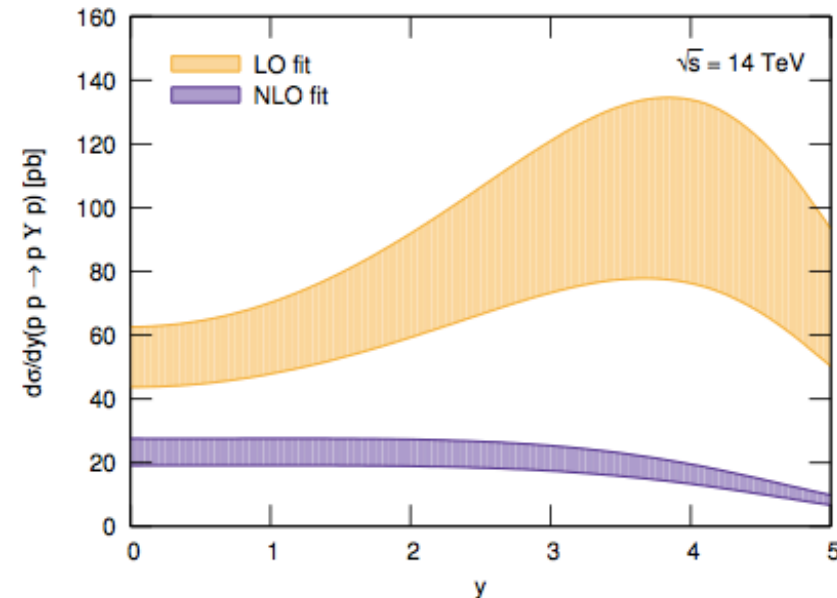
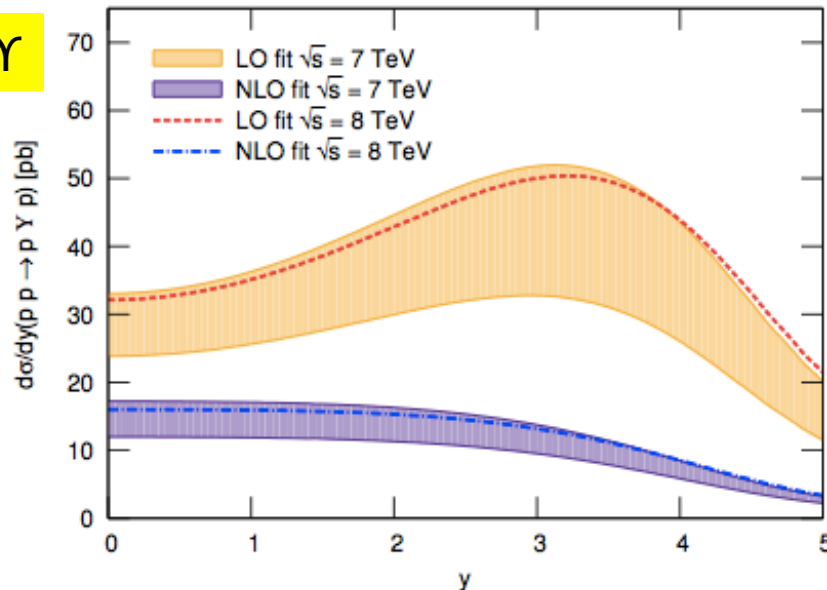
Factor \sim *100 data now available with 2011+2012 ($\sim 3\text{fb}^{-1}$)

Predictions (arXiv: 1307.7099)

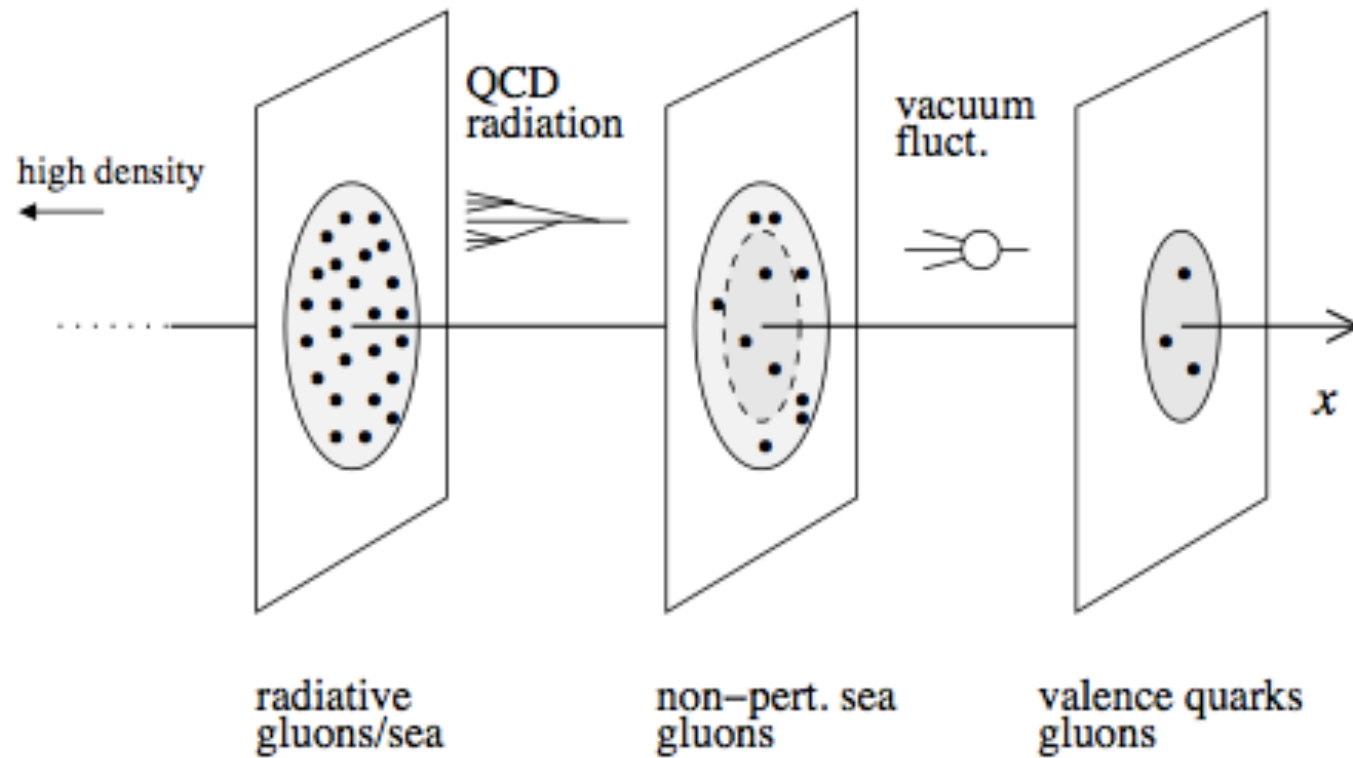
J/ψ



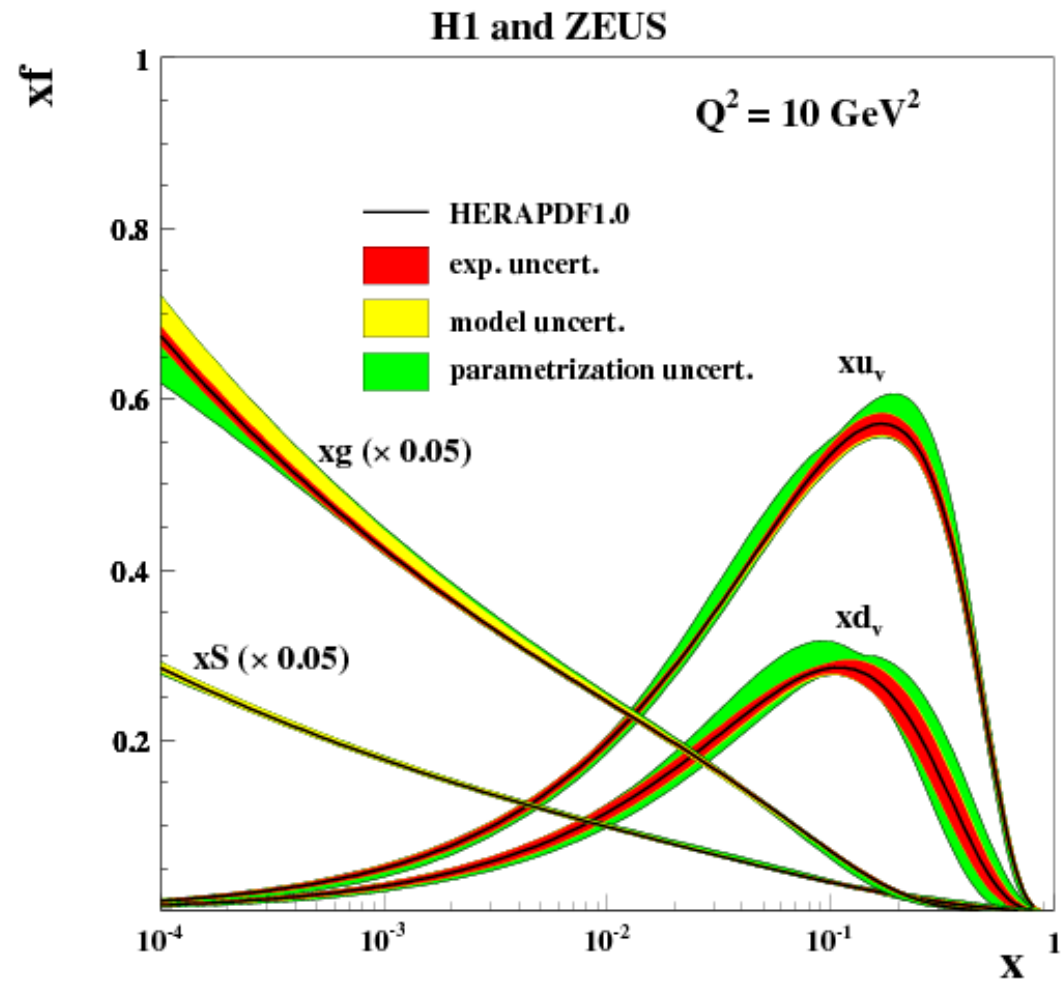
Υ



Sensitivity to saturation effects



Sensitivity to saturation effects

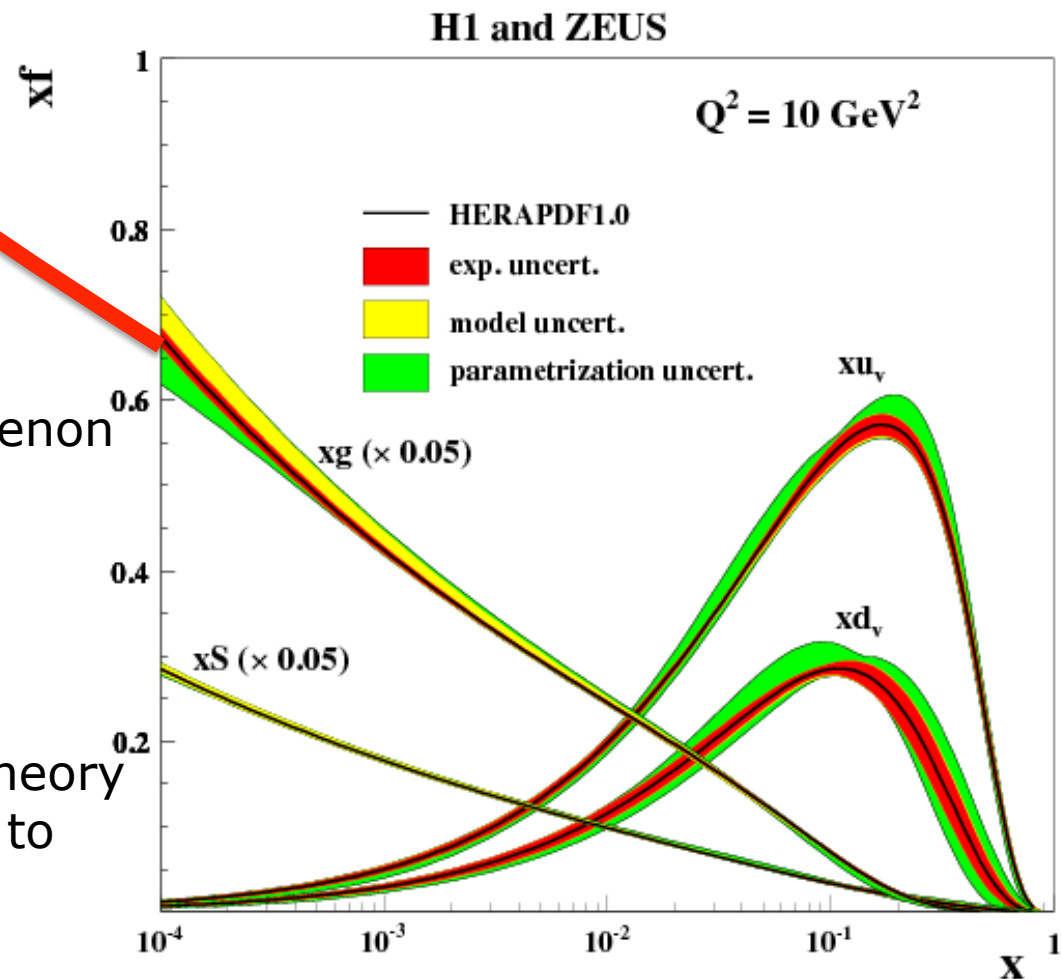


Sensitivity to saturation effects

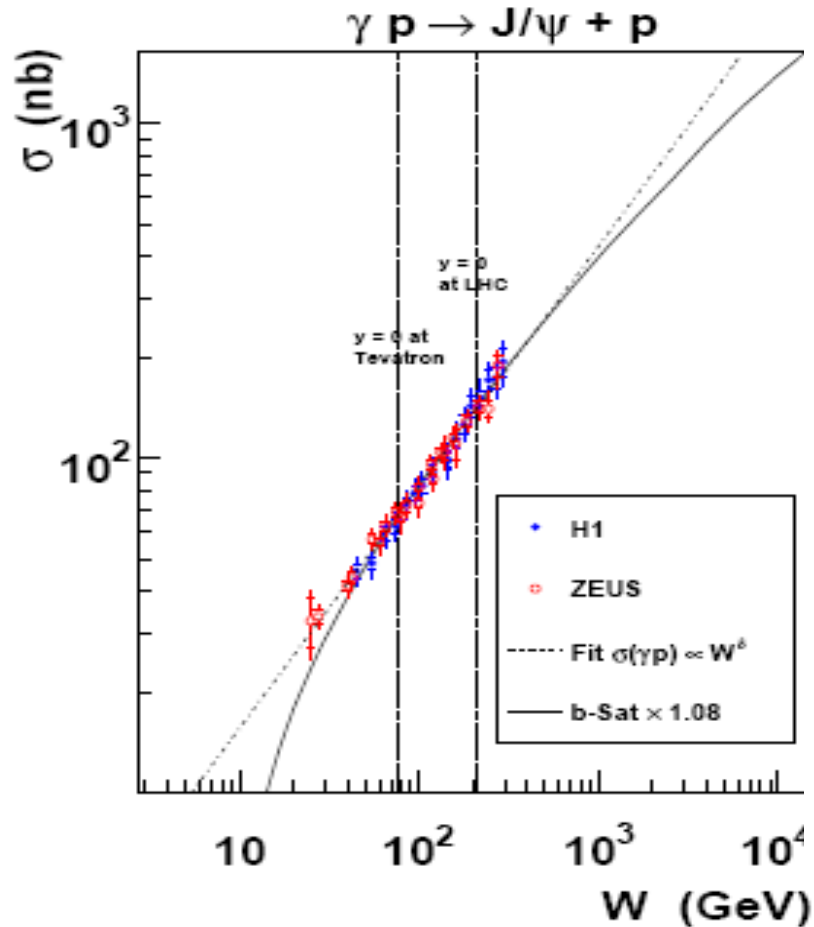
At some point a new phenomenon must come into play.

- perhaps a 'detail' of QCD
- perhaps a new particle

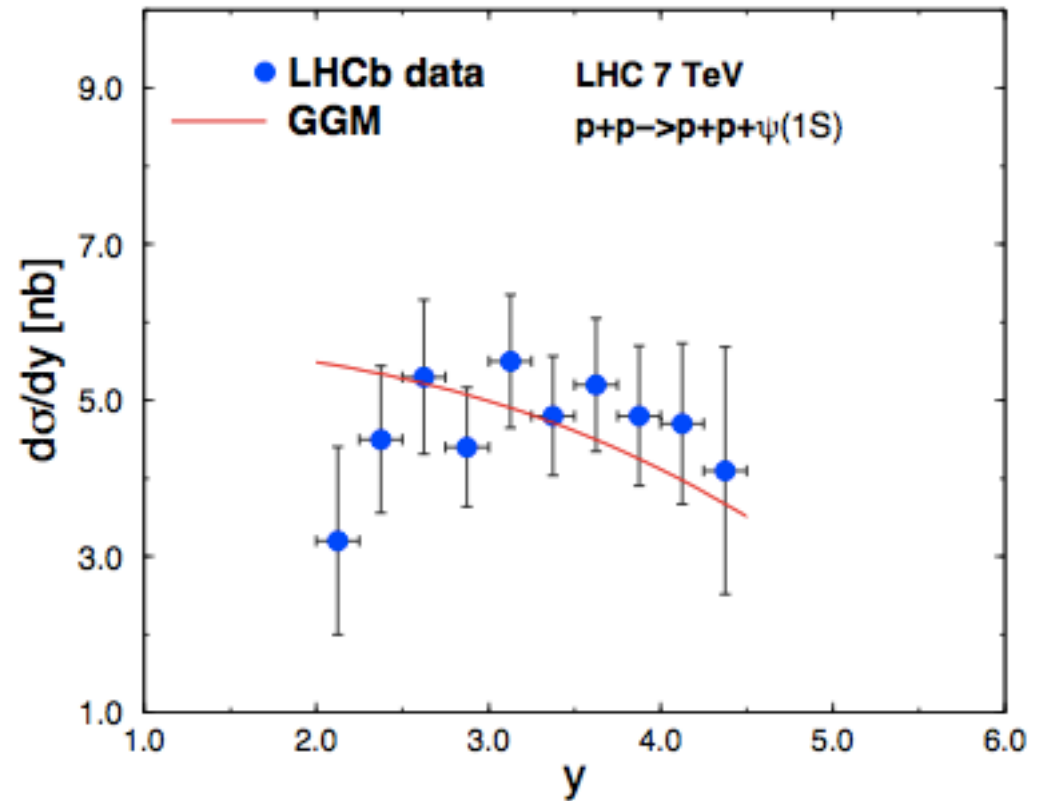
A region in which you know theory breaks down, is a good place to perform experiments.



Sensitivity to saturation effects



Motyka, Watt:
PRD 78, 014023 (2008)

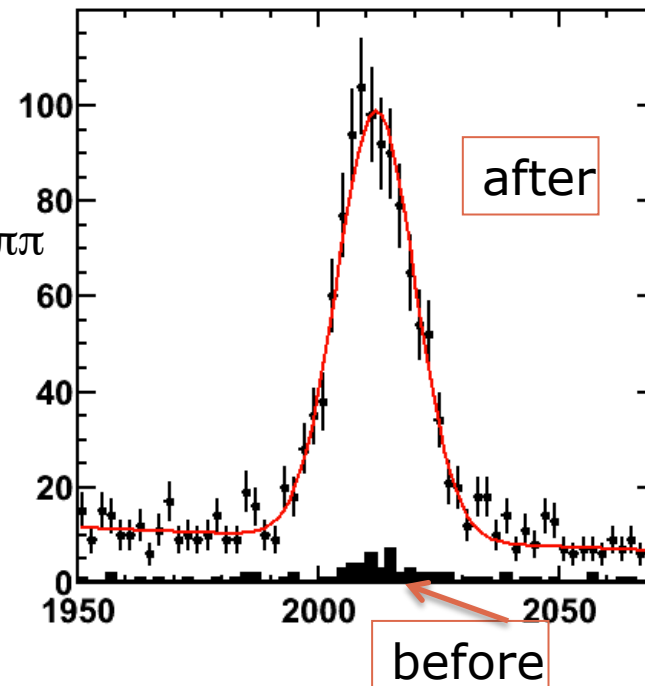


Gay Ducati et al., arXiv: 1305.4611

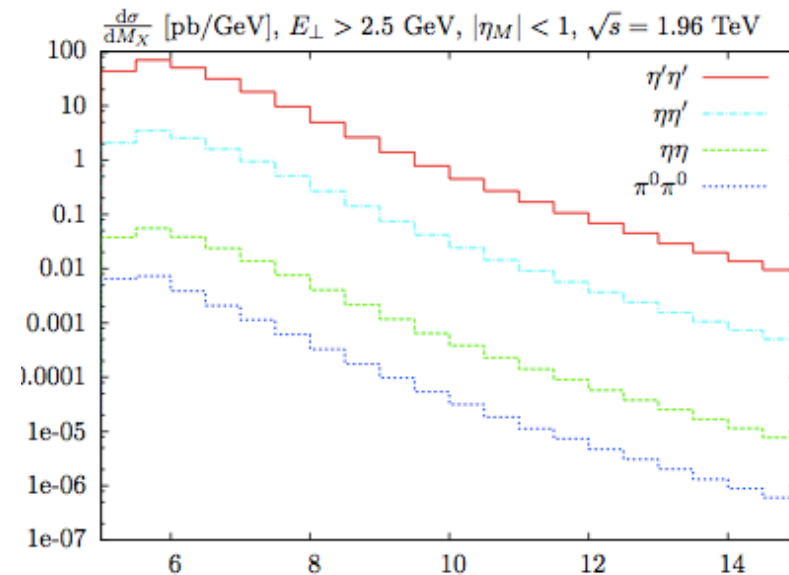
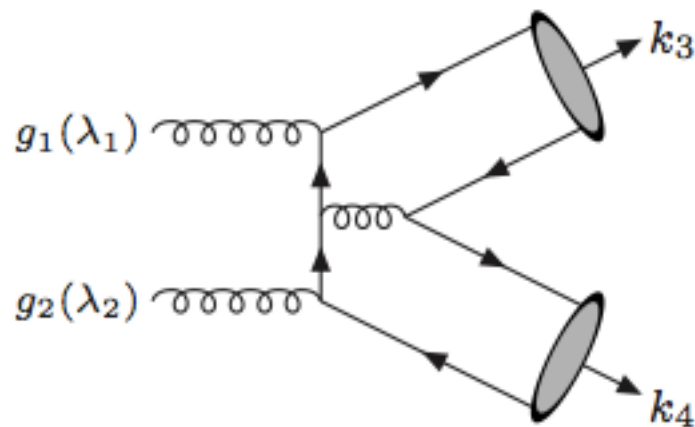
χ_c meson

- To see χ_{c0} , choose more favourable decay:
 - $\chi_{c0} \rightarrow \pi\pi\pi$ or KK $\sim 1\%$ while $\chi_{c2} \rightarrow \pi\pi$ or KK $\sim 0.1\%$
 - Backgrounds? (Harland-Lang et al. arXiv: 1105.1626)
 - LHCb: RICH detectors + real-time analysis

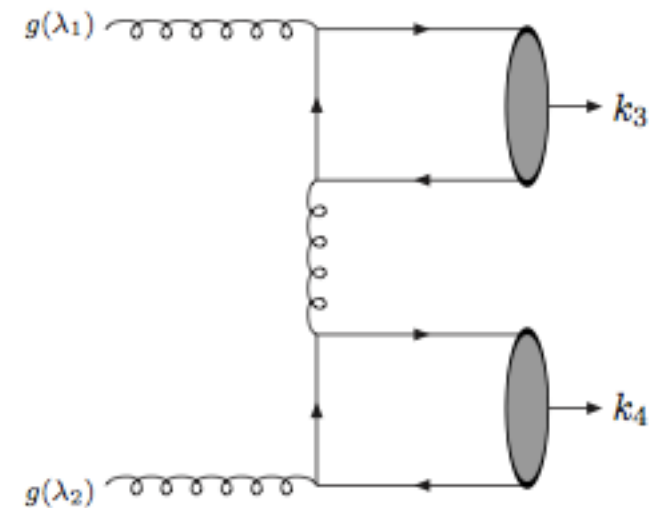
Example of $D^* \rightarrow K\pi\pi$
reconstruction
in low multiplicity
events



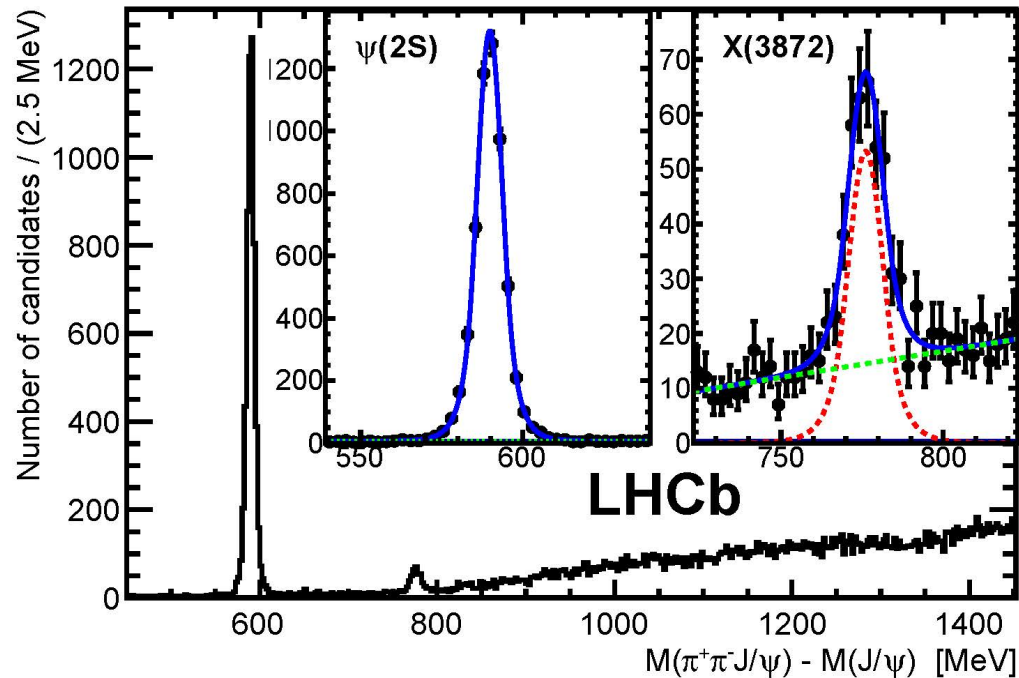
CEP meson-meson production arXiv:1105.1626



- Vanishing cs when gluons in $J_z=0$
- Flavour non-singlet mesons suppressed (thus $\pi\pi$ / KK small)
- Flavour singlet (e.g. $\eta'\eta'$ production) can proceed via



Relevance for X(3872)



← X(3872) observed inclusively. (arXiv:1112.5310) Could it be produced exclusively?

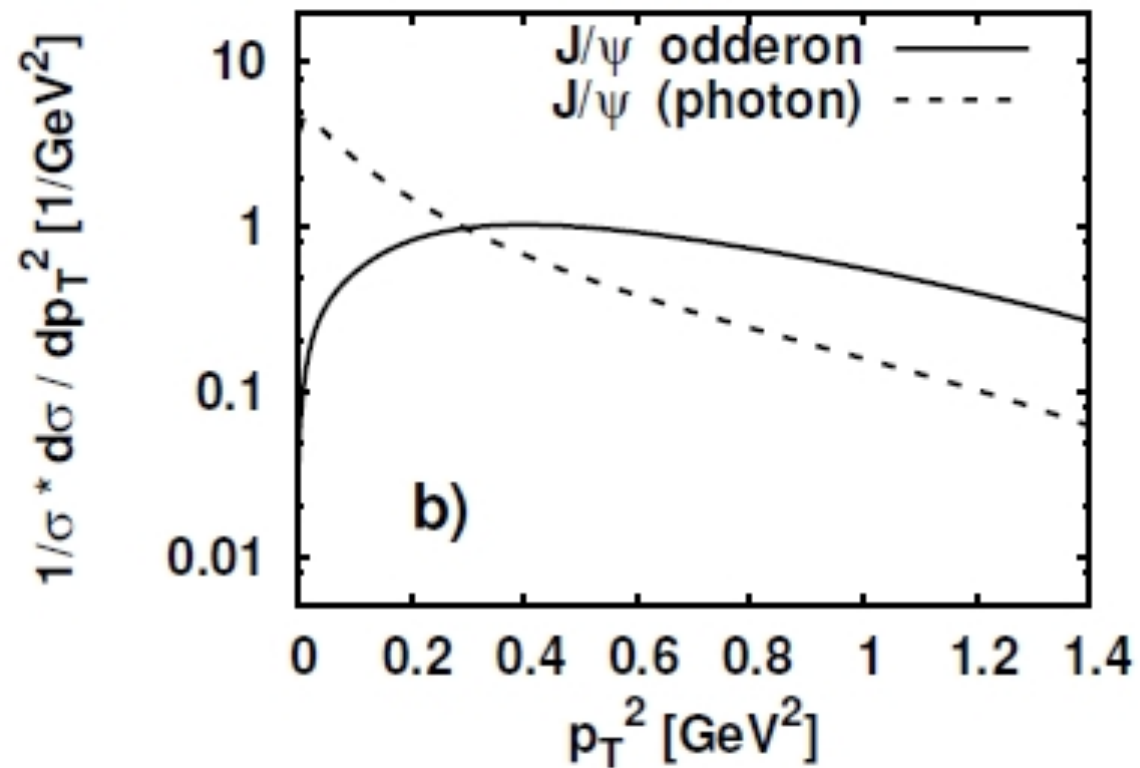
- J^{PC} of X(3872) shown by LHCb to be 1^{++} (arXiv:1302.6269)
- $\chi_{c(1^{++})}$ has been observed exclusively.
- If X(3872) is a bound cc state, might expect to observe it in central exclusive production – it decays in similar way as $\psi(2S)$ and χ_c

Exotics

- CEP is rich in colour-neutral gluons
- Excellent laboratory to find two predicted QCD objects: **odderons** and **glueballs**
- Backgrounds from normal (colourful) QCD heavily suppressed.

Search for odderon

- Motyka, DIS 2008.



Glueballs

Machado & daSilva, arXiv: 1111.608

Meson	LHC ($\sqrt{s} = 5.5$ TeV)				ALICE ($\sqrt{s} = 2.76$ TeV)	
	$\Gamma_{\gamma\gamma}$ [eV]	Γ_{gg} [MeV]	$\sigma_{\gamma\gamma}$ [μb]	σ_{PP} [mb]	$\sigma_{\gamma\gamma}$ [μb]	σ_{PP} [mb]
$f_0(1500)$	0.77	69.8	1.30	1.07	0.78	0.99
$f_0(1710)$	7.03	70.2	8.60	0.68	4.10	0.64
$X(1835)$	0.02	70.3	0.02	0.54	0.01	0.50

- Glueball candidates may be copiously produced at LHC but obscured by coloured combinatoric background.
- Different sensitivities in pp and pA running.
- In DPE only resonances are produced and decay_mode + spin-parity analysis + bkg estimates may allow their observation.

Summary

- First Observation of CEP at LHC
- First separation of χ_c spin states in CEP
- Good agreement with theory predictions
- Consistency with HERA and CDF results for J/ψ and QED produced dimuons.

- Excellent testing ground for QCD and behaviour of gluon at low x .

- Potential to discover glueballs, saturation and other exotic phenomena

$J/\psi, \psi(2s), \Upsilon$

Data

Zeus collaboration, hep-ex/9704013

Zeus collaboration, hep-ex/0201043

H1 collaboration, hep-ex/0205107

H1 collaboration, arXiv:0510.016

CDF collaboration, arXiv:0902.1271

Zeus collaboration, arXiv:0903.4205

LHCb collaboration, arXiv:1301.7084

H1 collaboration, arXiv:1304.5162

Theory:

Ryskin, Z.Phys. C57 (1993) 89.

Ryskin, Roberts, Martin, Levin, hep-ph/9511228

Martin, Nockles, Ryskin, Teubner, hep-ph/0709.4406

Jones, Martin, Ryskin, Teubner, arXiv: 1307.7099

Khoze Martin Ryskin, hep-ph/0201301

Khoze, Martin, Ryskin, Stirling, hep-ph/0410020v2

Motyka, Watt: PRD 78, 014023 (2008)

Schaefer, Szczurek: PRD 76, 094014 (2007)

Klein, Nystrand, PRL92, 142003 (2004); PRD60 014903 (1999).

Goncalves, Machado, PRD77, 014037 (2008), arXiv:1305.4611.

Further references

■ Odderon:

- Leszek, Motyka, DIS2008
- Bzdak, Motyka, Szymanowski, Cudell, PRD 75, 094023 (2007)
- Khoze, Martin, Ryskin, hep-ph/0201301v2
- Stein, Schafer, PLB 300 (1993) 400.
- Schaefer, Mankiewicz, Nachtman, PLB272 (1991) 419.
- Ewerz, hep-ph/0306137

■ Chi_c:

- Harland-Lang, Khoze, Ryskin, Stirling, arXiv:0909.4748, arXiv:1304.4262
- Khoze, Martin, Ryskin, Stirling, Eur. Phys. J. C35 (2004) 211.
- Pasechnik, Szczurek, hep-ph/0901.4187v2
- Pasechnik, Szczurek, Teryaev, hep-ph/0909.4498v1

■ Di photon production

- J. Vermaseren, Nucl. Phys. B229 (1983) 347.
- Boonekamp et al., hep-ph/1102.2531v1