

# Pick-Ups for bunched Beams

## Outline:

- **Signal generation → transfer impedance**
- **Capacitive *button* BPM for high frequencies**
- **Capacitive *shoe-box* BPM for low frequencies**
- **Electronics for position evaluation**
- **BPMs for measurement of closed orbit, tune and further lattice functions**
- **Summary**

# Usage of BPMs

A ***Beam Position Monitor*** is an **non-destructive device for bunched beams**

It has a low cut-off frequency i.e. dc-beam behavior can not be monitored

The abbreviation BPM and pick-up PU are synonyms

## 1. It delivers information about the transverse center of the beam

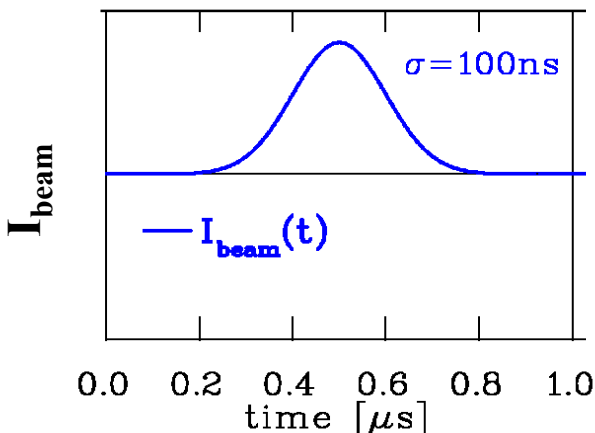
- ***Trajectory***: Position of an individual bunch within a transfer line or synchrotron
- ***Closed orbit***: central orbit averaged over a period much longer than a betatron oscillation
- ***Single bunch position*** → determination of parameters like tune, chromaticity,  $\beta$ -function
- Bunch position on a large time scale: bunch-by-bunch → turn-by-turn → averaged position
- Time evolution of a single bunch can be compared to ‘macro-particle tracking’ calculations
- Feedback: fast bunch-by-bunch damping *or* precise (and slow) closed orbit correction

## 2. Information on longitudinal bunch behavior (see next chapter)

- **Bunch shape and evolution** during storage and acceleration
- For proton LINACs: the beam **velocity** can be determined by two BPMs
- For electron LINACs: **Phase** measurement by Bunch Arrival Monitor
- **Relative** low current measurement down to 10 nA.

# Excuse: Time Domain ↔ Frequency Domain

**Time domain: Recording of a voltage as a function of time:**



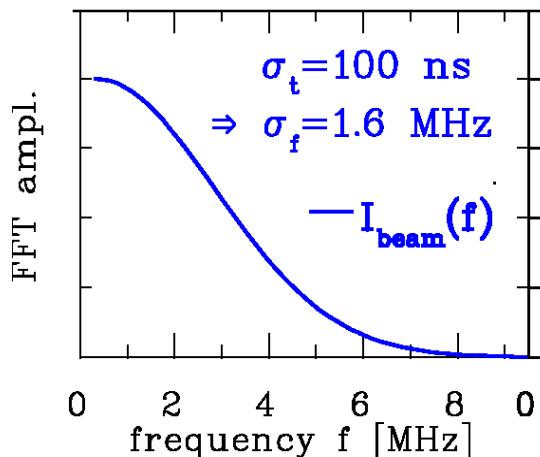
**Instrument:  
Oscilloscope**



**Fourier  
Transformation:**

$$\tilde{f}(\omega) = \int_{-\infty}^{\infty} f(t) e^{-i\omega t} dt$$

**Frequency domain: Displaying of a voltage as a function of frequency:**



**Instrument:  
Spectrum Analyzer**



**Fourier Transformation  
of time domain data**

**Care: Contains amplitude  
and phase**

# Excuse: Properties of Fourier Transformation

**Fourier Transform.:**  $\tilde{f}(\omega) \equiv \int_{-\infty}^{\infty} f(t)e^{-i\omega t} dt$     **Inv. F. T.:**  $f(t) \equiv \frac{1}{2\pi} \int_{-\infty}^{\infty} \tilde{f}(\omega)e^{i\omega t} d\omega$   
 tech.  $DFT(f)$  or  $FFT(f)$     tech.  $IDFT(f)$

⇒ a process can be described either with  $f(t)$  ‘time domain’ or  $\tilde{f}(\omega)$  ‘frequency domain’

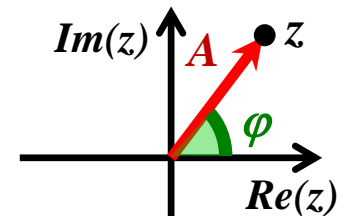
**No loss of information:** If  $\tilde{f}(\omega) = \int f(t)e^{-i\omega t} dt$  exists, then  $f(t) = \frac{1}{2\pi} \int \int f(\tau)e^{i\omega(t-\tau)} d\omega d\tau$

**FT is complex:**  $\tilde{f}(\omega) \in \mathbb{C} \rightarrow$  amplitude  $A(\omega) = |\tilde{f}(\omega)|$  and phase  $\varphi(\omega) = \arctan \frac{Im(\tilde{f})}{Re(\tilde{f})}$

**Similarity Law:** For  $a \neq 0$  it is for  $f(at)$ :  $|1/a| \cdot \tilde{f}(\omega/a) = \int_{-\infty}^{\infty} f(at)e^{-i\omega t} dt$

→ the properties can be scaled to any frequency range;

⇔ ‘shorter time signal has wider FT’



**Differentiation Law:** for  $n^{\text{th}}$  derivative  $f^{(n)}(t)$  it is:  $(i\omega)^n \cdot \tilde{f}(\omega) = \int_{-\infty}^{\infty} f^{(n)}(t)e^{-i\omega t} dt$

→ differentiation in time domain corresponds to multiplication with  $i\omega$  in frequency domain

**Convolution Law:** For  $f(t) = f_1(t) * f_2(t) \equiv \int_{-\infty}^{\infty} f_1(\tau) \cdot f_2(t-\tau) d\tau$

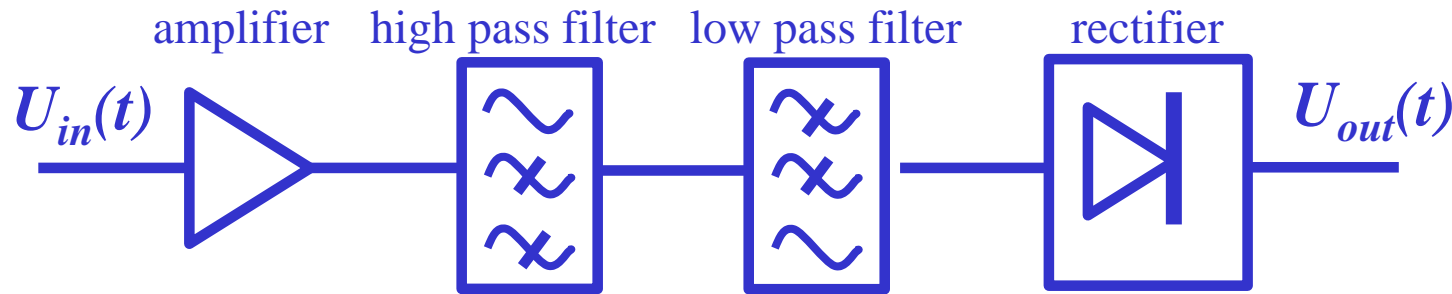
⇒  $\tilde{f}(\omega) = \tilde{f}_1(\omega) \cdot \tilde{f}_2(\omega)$  → convolution be expressed as multiplication of FT

# Excuse: Properties of Fourier Trans. → technical Realization

**Convolution Law:** For  $f(t) = f_1(t) * f_2(t) \equiv \int_{-\infty}^{\infty} f_1(\tau) \cdot f_2(t - \tau) d\tau$   
 $\Rightarrow \tilde{f}(\omega) = \tilde{f}_1(\omega) \cdot \tilde{f}_2(\omega)$

→ convolution in time domain can be expressed as multiplication of FT in frequency domain

**Application:** Chain of electrical elements calculated in frequency domain more easily  
 parameters are more easy in frequency domain (bandwidth,  $f$ -dependent amplification.....)



**Engineering formulation for finite number of discrete samples:**

**Digital Fourier Transformation  $DFT(f)$ :** corresponds to math. FT for finite number of samples

**Fast Fourier Transformation:  $FFT(f)$**  dedicated algorithm for **fast** calc. with  $2^n$  increments

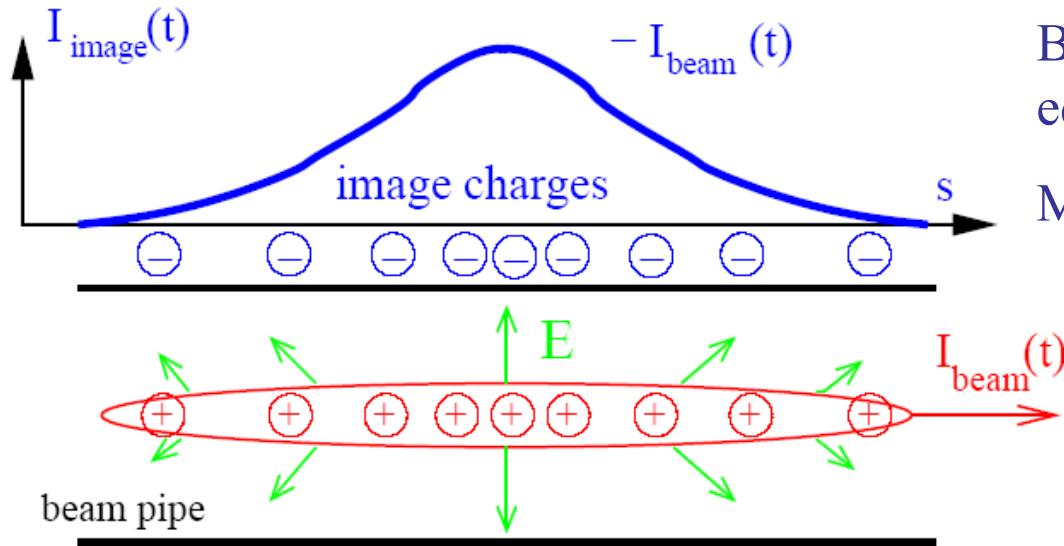
**Transfer function  $H(\omega)$**  and  $h(t)$  are used to describe electrical elements

Calculation with  $H(\omega)$  in frequency domain or

$h(t)$  time domain → ‘Finite Impulse Response’ FIR filter or ‘Infinite Impulse Response’ IIR filter

# Pick-Ups for bunched Beams

The image current at the beam pipe is monitored on a high frequency basis  
i.e. the ac-part given by the bunched beam.



Beam Position Monitor **BPM**  
equals Pick-Up **PU**

Most frequent used instrument!

For relativistic velocities,  
the electric field is transversal:  
$$E_{\perp,lab}(t) = \gamma \cdot E_{\perp,rest}(t')$$

## ➤ Signal treatment for capacitive pick-ups:

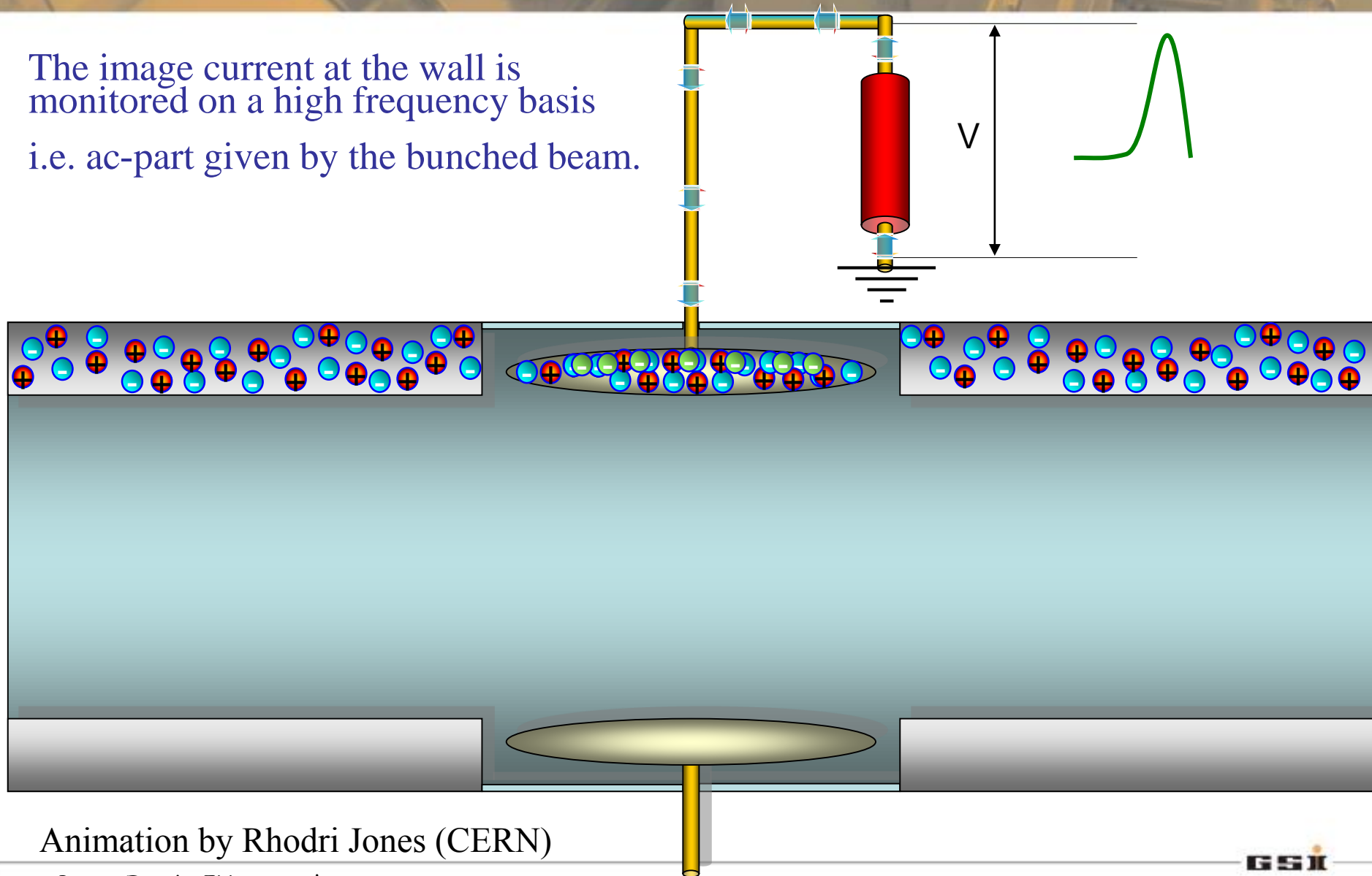
- Longitudinal bunch shape
- Overview of processing electronics for Beam Position Monitor (BPM)

## ➤ Measurements:

- Trajectory and closed orbit determination
- Tune and lattice function measurements (synchrotron only).

# Principle of Signal Generation of capacitive BPMs

The image current at the wall is monitored on a high frequency basis  
i.e. ac-part given by the bunched beam.

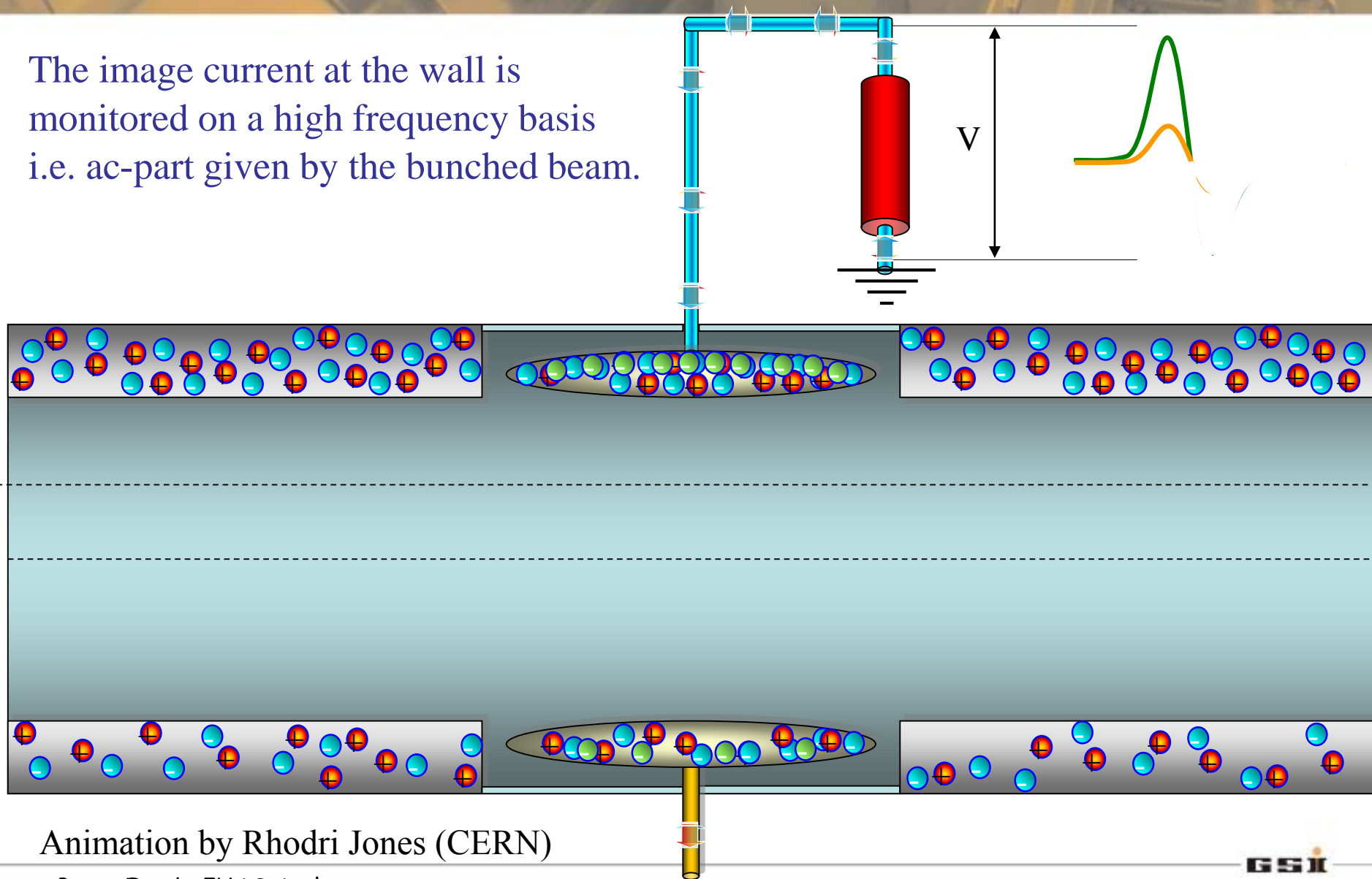


Animation by Rhodri Jones (CERN)

Peter Forck, JUAS Archamps

# Principle of Signal Generation of a BPMs, off-center Beam

The image current at the wall is monitored on a high frequency basis i.e. ac-part given by the bunched beam.



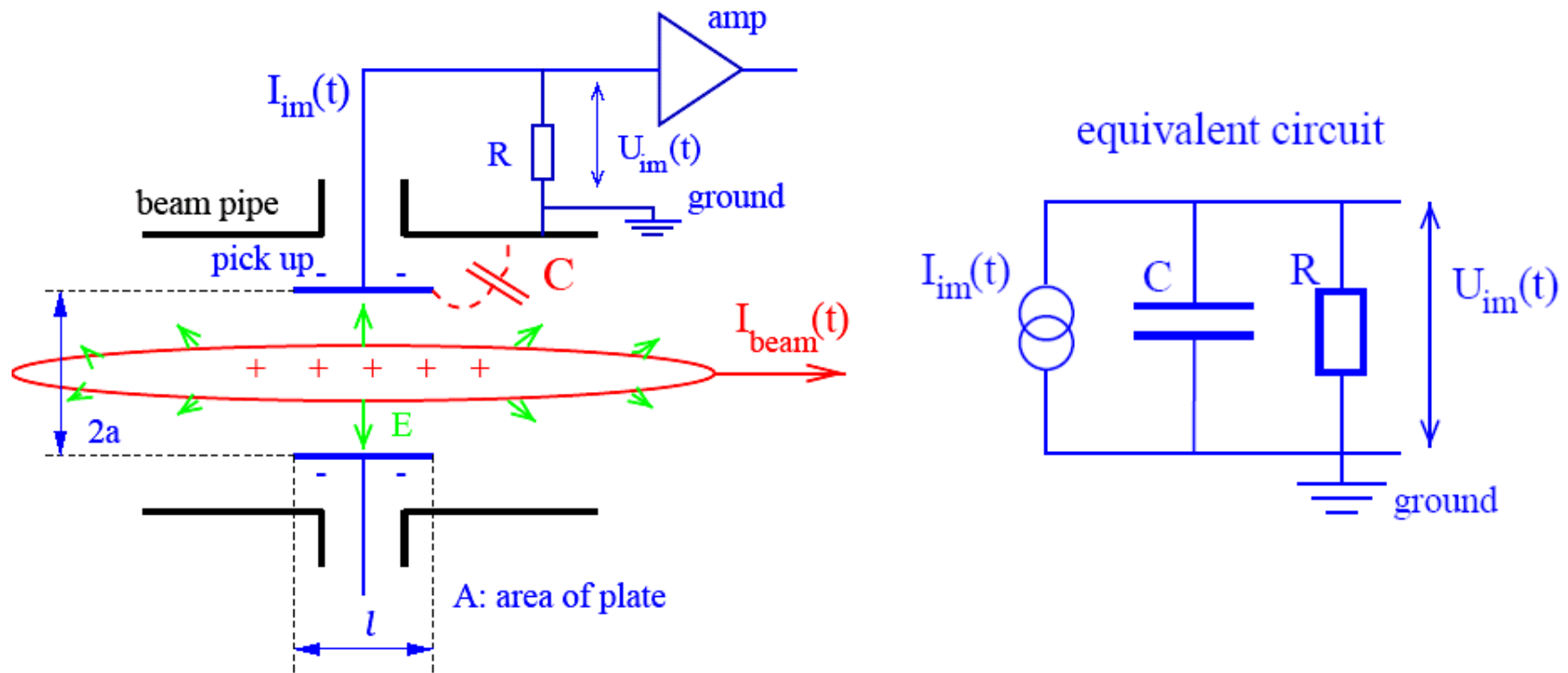
Animation by Rhodri Jones (CERN)

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# Model for Signal Treatment of capacitive BPMs

The wall current is monitored by a plate or ring inserted in the beam pipe:



The image current  $I_{im}$  at the plate is given by the beam current and geometry:

$$I_{im}(t) = -\frac{dQ_{im}(t)}{dt} = \frac{-A}{2\pi a l} \cdot \frac{dQ_{beam}(t)}{dt} = \frac{-A}{2\pi a} \cdot \frac{1}{\beta c} \cdot \frac{dI_{beam}(t)}{dt} = \frac{A}{2\pi a} \cdot \frac{1}{\beta c} \cdot i\omega I_{beam}(\omega)$$

Using a relation for Fourier transformation:  $I_{beam} = I_0 e^{-i\omega t} \Rightarrow dI_{beam}/dt = -i\omega I_{beam}$ .

# Transfer Impedance for a capacitive BPM

At a resistor  $R$  the voltage  $U_{im}$  from the image current is measured.

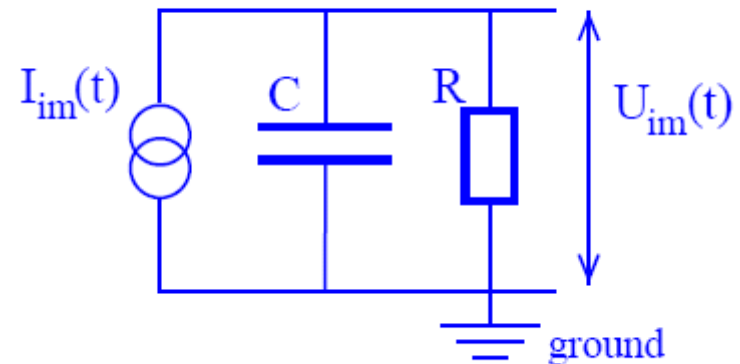
The transfer impedance  $Z_t$  is the ratio between voltage  $U_{im}$  and beam current  $I_{beam}$  in *frequency domain*:  $U_{im}(\omega) = R \cdot I_{im}(\omega) = Z_t(\omega, \beta) \cdot I_{beam}(\omega)$ .

## Capacitive BPM:

- The pick-up capacitance  $C$ :  
plate ↔ vacuum-pipe and cable.
- The amplifier with input resistor  $R$ .
- The beam is a high-impedance current source:

$$\begin{aligned}
 U_{im} &= \frac{R}{1 + i\omega RC} \cdot I_{im} \\
 &= \frac{A}{2\pi a} \cdot \frac{1}{\beta c} \cdot \frac{1}{C} \cdot \frac{i\omega RC}{1 + i\omega RC} \cdot I_{beam} \\
 &\equiv Z_t(\omega, \beta) \cdot I_{beam}
 \end{aligned}$$

equivalent circuit



$$\frac{1}{Z} = \frac{1}{R} + i\omega C \Leftrightarrow Z = \frac{R}{1 + i\omega RC}$$

This is a high-pass characteristic with  $\omega_{cut} = 1/RC$ :

**Amplitude:**  $|Z_t(\omega)| = \frac{A}{2\pi a} \cdot \frac{1}{\beta c} \cdot \frac{1}{C} \cdot \frac{\omega / \omega_{cut}}{\sqrt{1 + \omega^2 / \omega_{cut}^2}}$  **Phase:**  $\varphi(\omega) = \arctan(\omega_{cut} / \omega)$

# Example of Transfer Impedance for Proton Synchrotron

The high-pass characteristic for typical synchrotron BPM:

$$U_{im}(\omega) = Z_t(\omega) \cdot I_{beam}(\omega)$$

$$|Z_t| = \frac{A}{2\pi a} \cdot \frac{1}{\beta c} \cdot \frac{1}{C} \cdot \frac{\omega / \omega_{cut}}{\sqrt{1 + \omega^2 / \omega_{cut}^2}}$$

$$\varphi = \arctan(\omega_{cut} / \omega)$$

Parameter for shoe-box BPM:

$$C=100\text{pF}, l=10\text{cm}, \beta=50\%$$

$$f_{cut} = \omega / 2\pi = (2\pi RC)^{-1}$$

$$\text{for } R=50 \Omega \Rightarrow f_{cut} = 32 \text{ MHz}$$

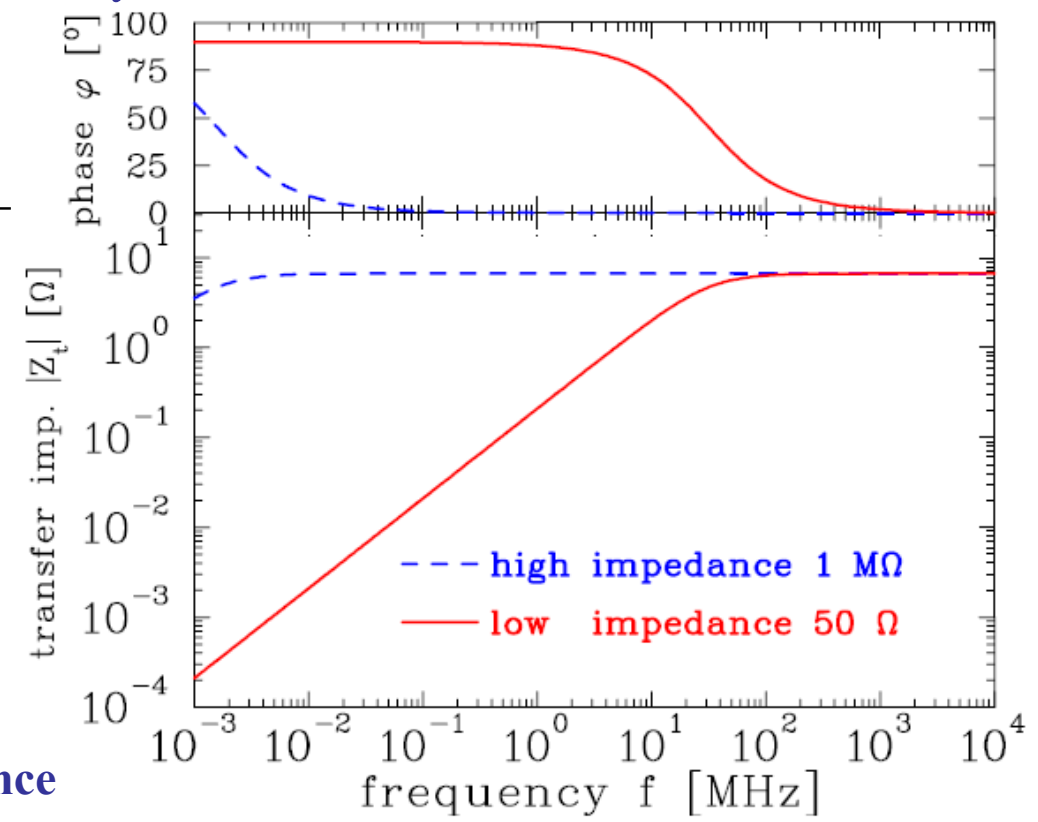
$$\text{for } R=1 \text{ M}\Omega \Rightarrow f_{cut} = 1.6 \text{ kHz}$$

Large signal strength → **high impedance**

Smooth signal transmission → **50 Ω**

**Remark:** For  $\omega \rightarrow 0$  it is  $Z_t \rightarrow 0$  i.e. **no** signal is transferred from dc-beams e.g.

- de-bunched beam inside a synchrotron
- for slow extraction through a transfer line



# Signal Shape for capacitive BPMs: differentiated $\leftrightarrow$ proportional

Depending on the frequency range *and* termination the signal looks different:

➤ *High frequency range*  $\omega \gg \omega_{cut}$ :

$$Z_t \propto \frac{i\omega / \omega_{cut}}{1 + i\omega / \omega_{cut}} \rightarrow 1 \Rightarrow U_{im}(t) = \frac{1}{C} \cdot \frac{1}{\beta c} \cdot \frac{A}{2\pi a} \cdot I_{beam}(t)$$

⇒ **direct image** of the bunch. Signal strength  $Z_t \propto A/C$  i.e. nearly independent on length

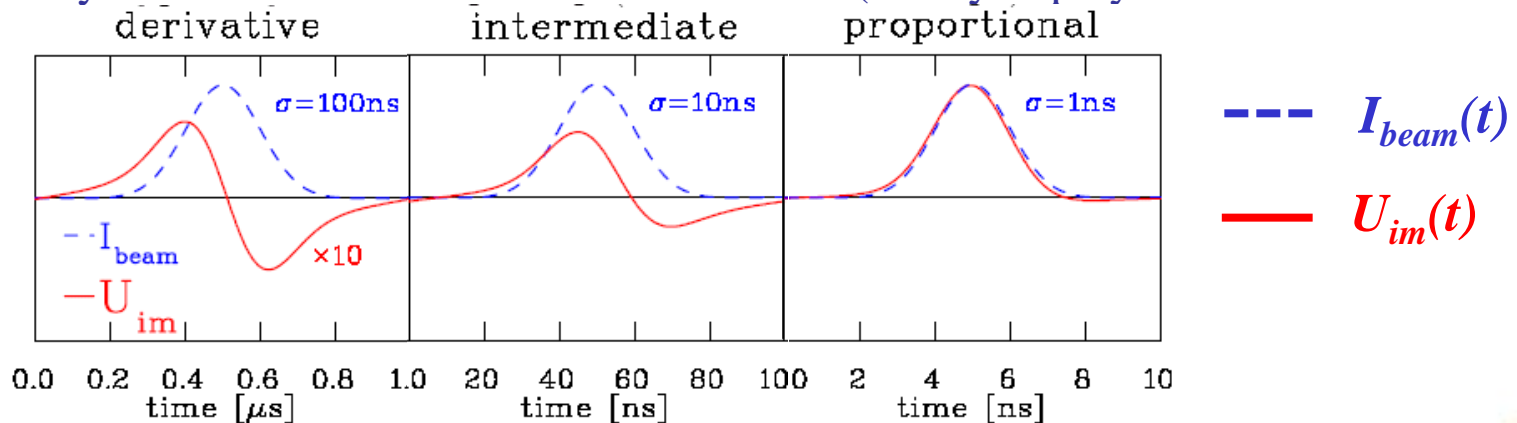
➤ *Low frequency range*  $\omega \ll \omega_{cut}$ :

$$Z_t \propto \frac{i\omega / \omega_{cut}}{1 + i\omega / \omega_{cut}} \rightarrow i \frac{\omega}{\omega_{cut}} \Rightarrow U_{im}(t) = R \cdot \frac{A}{\beta c \cdot 2\pi a} \cdot i\omega I_{beam}(t) = R \cdot \frac{A}{\beta c \cdot 2\pi a} \cdot \frac{dI_{beam}}{dt}$$

⇒ **derivative** of bunch, single strength  $Z_t \propto A$ , i.e. (nearly) independent on  $C$

➤ *Intermediate frequency range*  $\omega \approx \omega_{cut}$ : Calculation using Fourier transformation

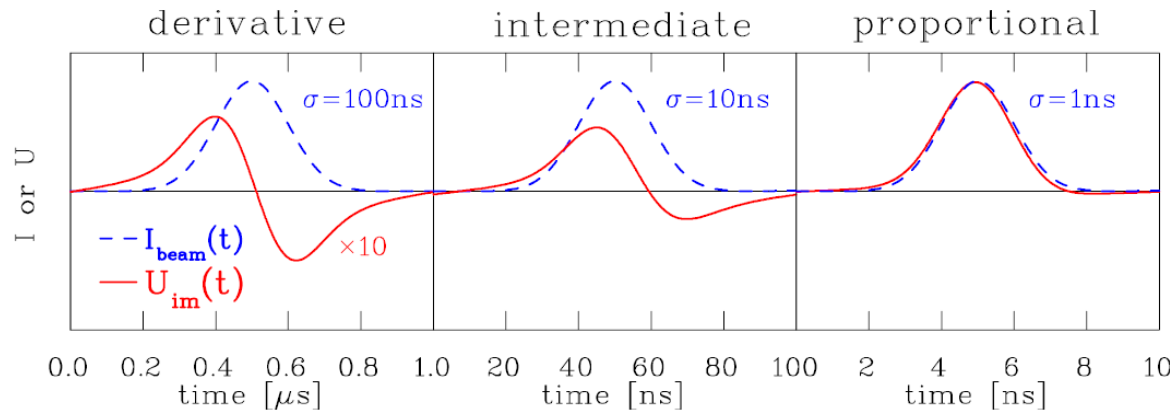
Example from synchrotron BPM with  $50 \Omega$  termination (reality at p-synchrotron :  $\sigma \gg 1$  ns):



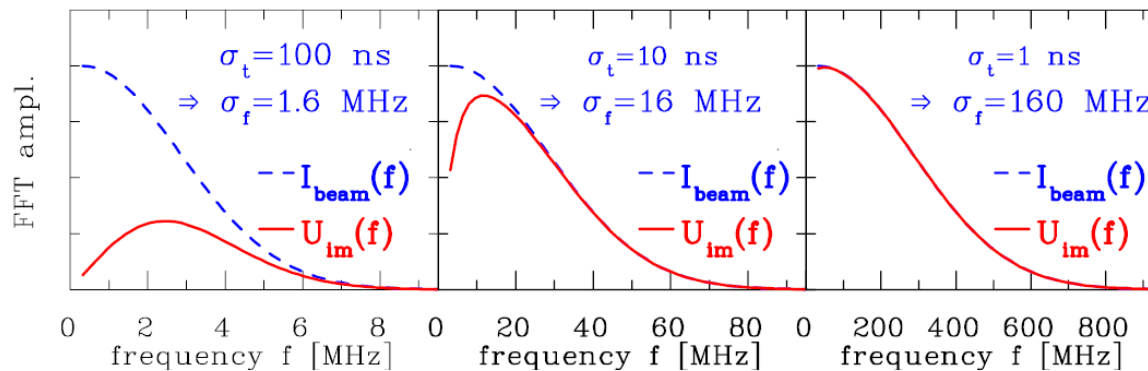
# Calculation of Signal Shape (here single bunch)

The transfer impedance is used in frequency domain! The following is performed:

**1. Start:** Time domain Gaussian function  $I_{beam}(t)$  having a width of  $\sigma_t$



**2. FFT** of  $I_{beam}(t)$  leads to the frequency domain Gaussian  $I_{beam}(f)$  with  $\sigma_f = (2\pi\sigma_t)^{-1}$



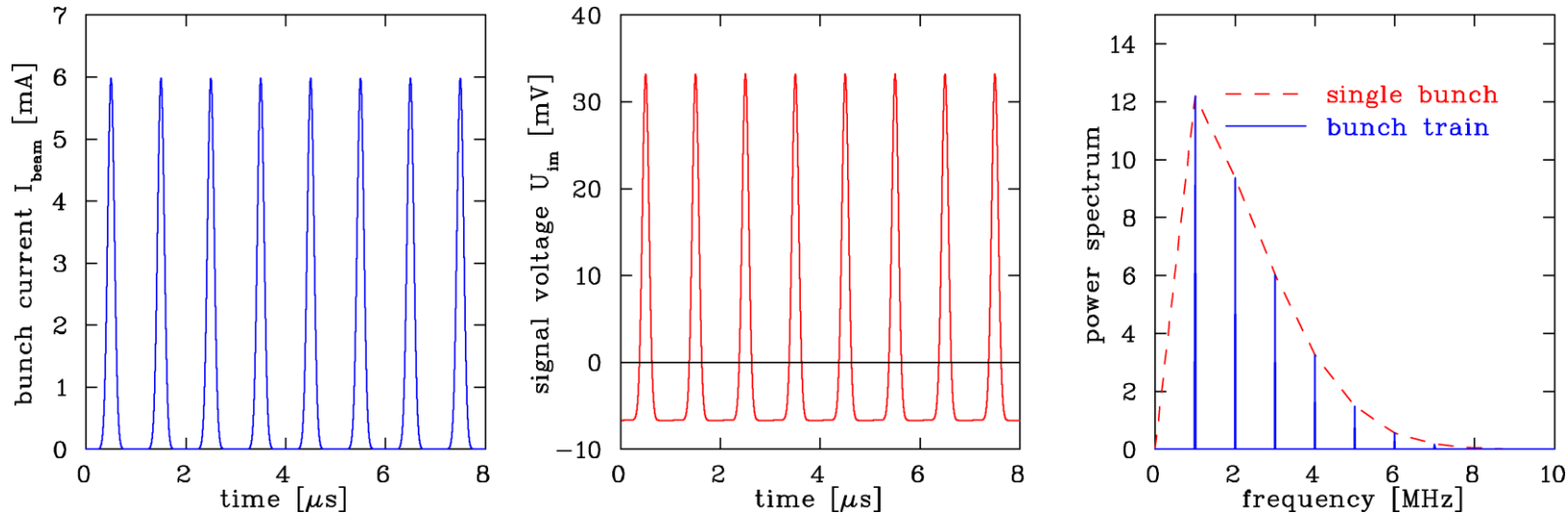
**3. Multiplication** with  $Z_t(f)$  with  $f_{cut} = 32\text{ MHz}$  leads to  $U_{im}(f) = Z_t(f) \cdot I_{beam}(f)$

**4. Inverse FFT** leads to  $U_{im}(t)$

# Calculation of Signal Shape: repetitive Bunch in a Synchrotron

Synchrotron filled with 8 bunches accelerated with  $f_{acc}=1$  MHz

BPM terminated with  $R=1$  M $\Omega \Rightarrow f_{acc} \gg f_{cut}$ :



**Parameter:**  $R=1$  M $\Omega \Rightarrow f_{cut}=2$  kHz,  $Z_t=5$   $\Omega$ , all buckets filled

$C=100$  pF,  $l=10$  cm,  $\beta=50\%$ ,  $\sigma_t=100$  ns  $\Rightarrow \sigma_l=15$  m

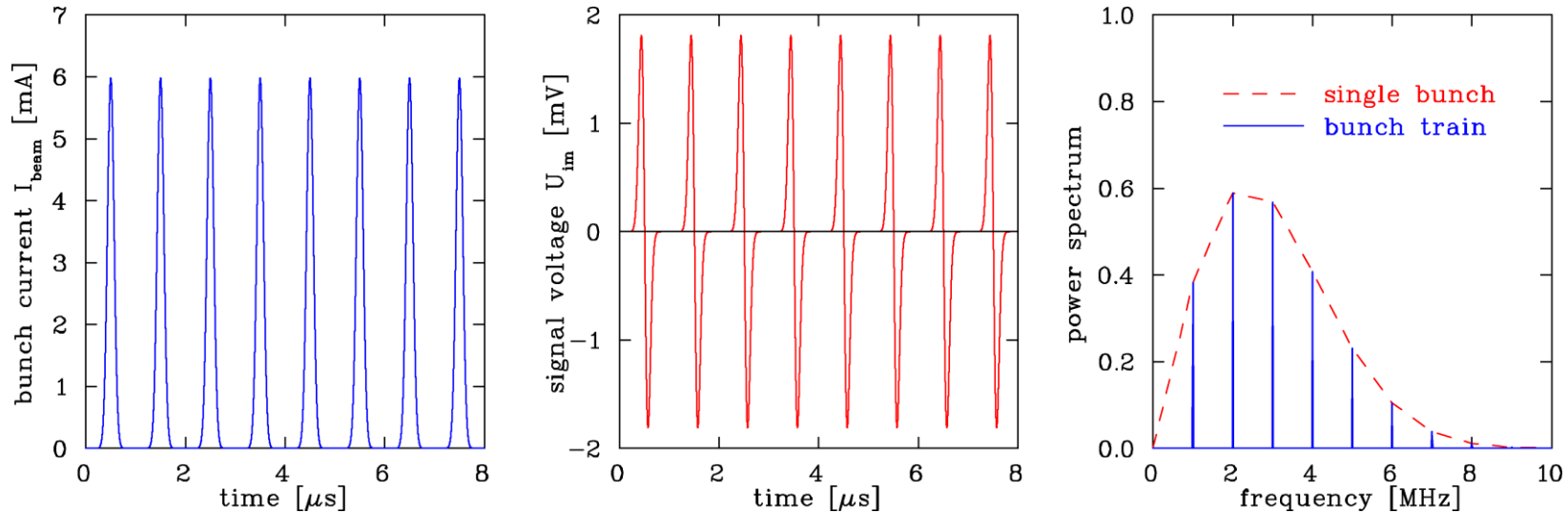
- Fourier spectrum is composed of lines separated by acceleration  $f_{rf}$
- Envelope given by single bunch Fourier transformation
- Baseline shift due to ac-coupling

**Remark:**  $1$  MHz  $< f_{rf} < 10$  MHz  $\Rightarrow$  Bandwidth  $\approx 100$  MHz  $= 10 \cdot f_{rf}$  for broadband observation

# Calculation of Signal Shape: repetitive Bunch in a Synchrotron

Synchrotron filled with 8 bunches accelerated with  $f_{acc}=1$  MHz

BPM terminated with  $R=50 \Omega \Rightarrow f_{acc} \ll f_{cut}$ :



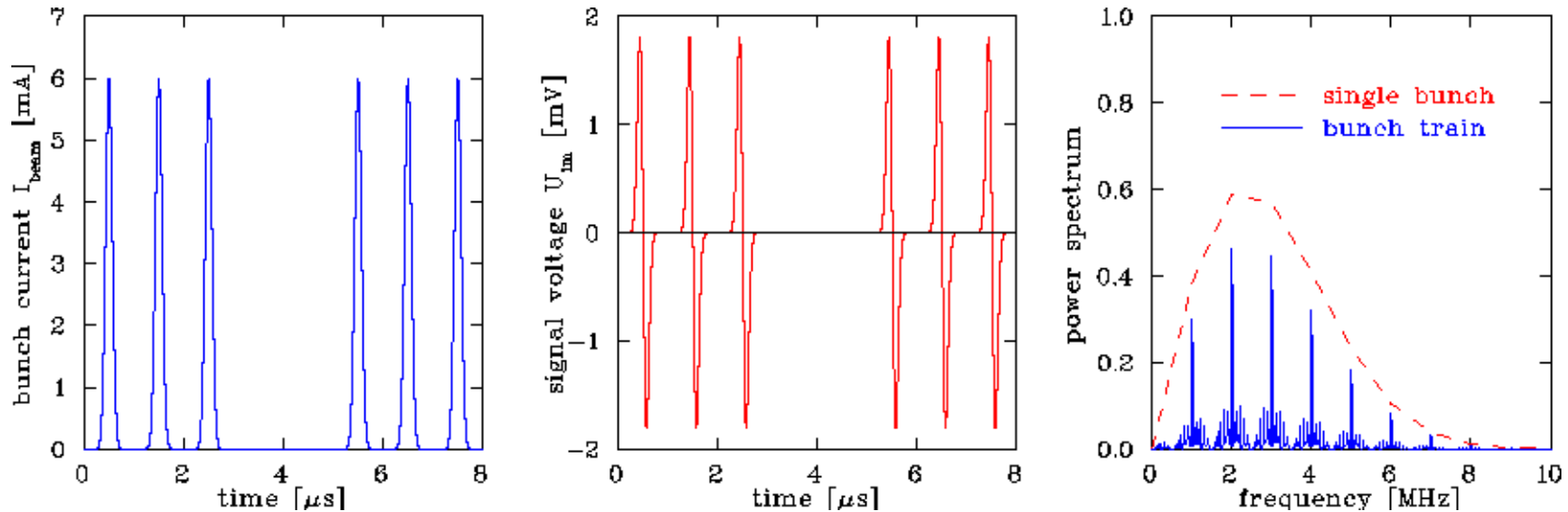
**Parameter:  $R=50 \Omega \Rightarrow f_{cut}=32$  MHz, all buckets filled**

$C=100$  pF,  $l=10$  cm,  $\beta=50\%$ ,  $\sigma_t=100$  ns  $\Rightarrow \sigma_l=15$  m

- Fourier spectrum is concentrated at acceleration harmonics with single bunch spectrum as an envelope.
- Bandwidth up to typically  $10 \cdot f_{acc}$

# Calculation of Signal Shape: Bunch Train with empty Buckets

Synchrotron during filling: Empty buckets,  $R=50 \Omega$ :



Parameter:  $R=50 \Omega \Rightarrow f_{\text{cut}}=32 \text{ MHz}$ , 2 empty buckets

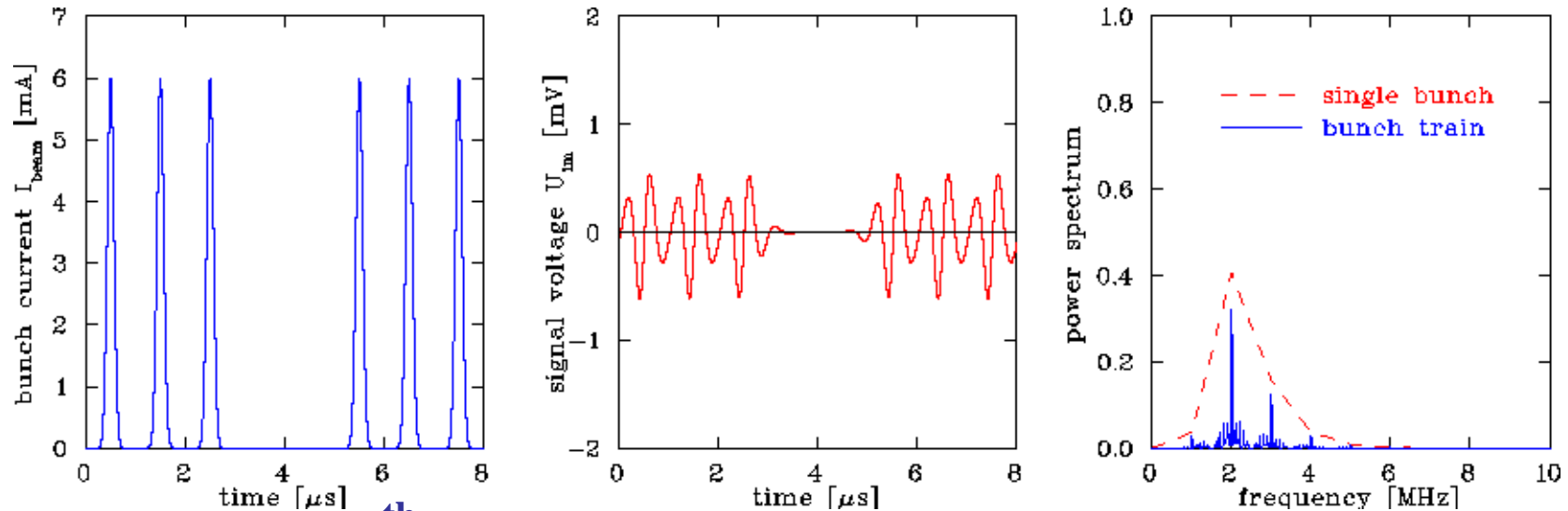
$C=100\text{pF}$ ,  $l=10\text{cm}$ ,  $\beta=50\%$ ,  $\sigma_t=100 \text{ ns} \Rightarrow \sigma_l=15\text{m}$

➤ Fourier spectrum is more complex, harmonics are broader due to sidebands



# Calculation of Signal Shape: Filtering of Harmonics

Effect of filters, here bandpass:



Parameter:  $R=50 \Omega$ , 4<sup>th</sup> order Butterworth filter at  $f_{cut}=2 \text{ MHz}$

$C=100\text{pF}$ ,  $l=10\text{cm}$ ,  $\beta=50\%$ ,  $\sigma=100 \text{ ns}$

- Ringing due to sharp cutoff
- Other filter types more appropriate

$$\begin{aligned}
 & n^{\text{th}} \text{ order Butterworth filter, math. simple, but } \mathbf{not} \text{ well suited:} \\
 & |H_{low}| = \frac{1}{\sqrt{1 + (\omega / \omega_{cut})^{2n}}} \quad \text{and} \quad |H_{high}| = \frac{(\omega / \omega_{cut})^n}{\sqrt{1 + (\omega / \omega_{cut})^{2n}}} \\
 & H_{filter} = H_{high} \cdot H_{low}
 \end{aligned}$$

Generally:  $Z_{tot}(\omega) = H_{cable}(\omega) \cdot H_{filter}(\omega) \cdot H_{amp}(\omega) \cdot \dots \cdot Z_t(\omega)$

Remark: For numerical calculations, time domain filters (FIR and IIR) are more appropriate

# Examples for differentiated & proportional Shape

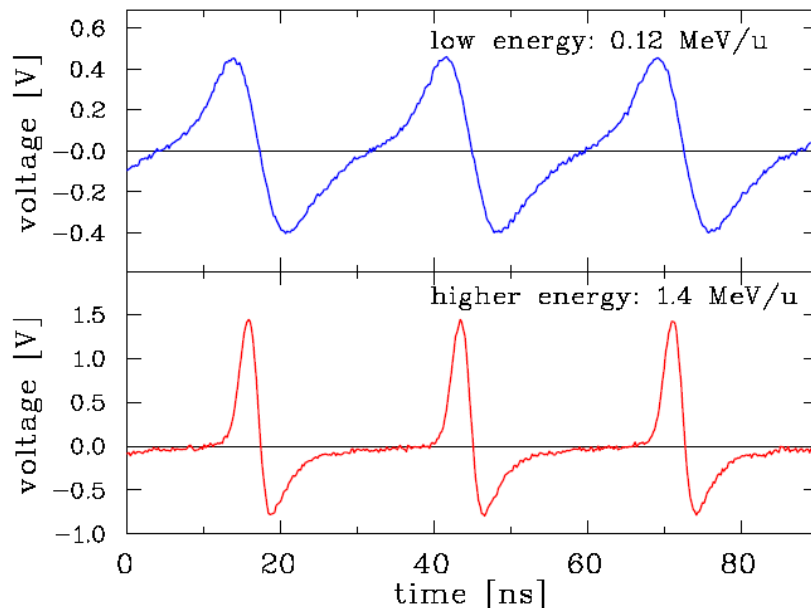
## Proton LINAC, e<sup>-</sup>-LINAC & synchrotron:

100 MHz <  $f_{rf}$  < 1 GHz typically

$R=50 \Omega$  processing to reach bandwidth

$C \approx 5 \text{ pF} \Rightarrow f_{cut} = 1/(2\pi RC) \approx 700 \text{ MHz}$

**Example:** 36 MHz GSI ion LINAC



## Proton synchrotron:

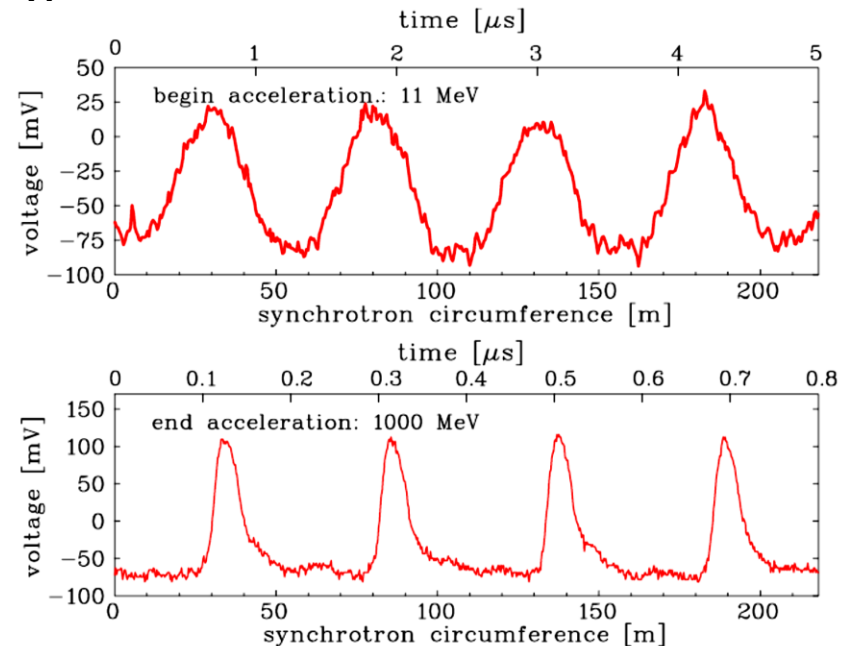
1 MHz <  $f_{rf}$  < 30 MHz typically

$R=1 \text{ M}\Omega$  for large signal i.e. large  $Z_t$

$C \approx 100 \text{ pF} \Rightarrow f_{cut} = 1/(2\pi RC) \approx 10 \text{ kHz}$

**Example:** non-relativistic GSI synchrotron

$f_{rf} : 0.8 \text{ MHz} \rightarrow 5 \text{ MHz}$



**Remark:** During acceleration the bunching-factor is increased: ‘adiabatic damping’.

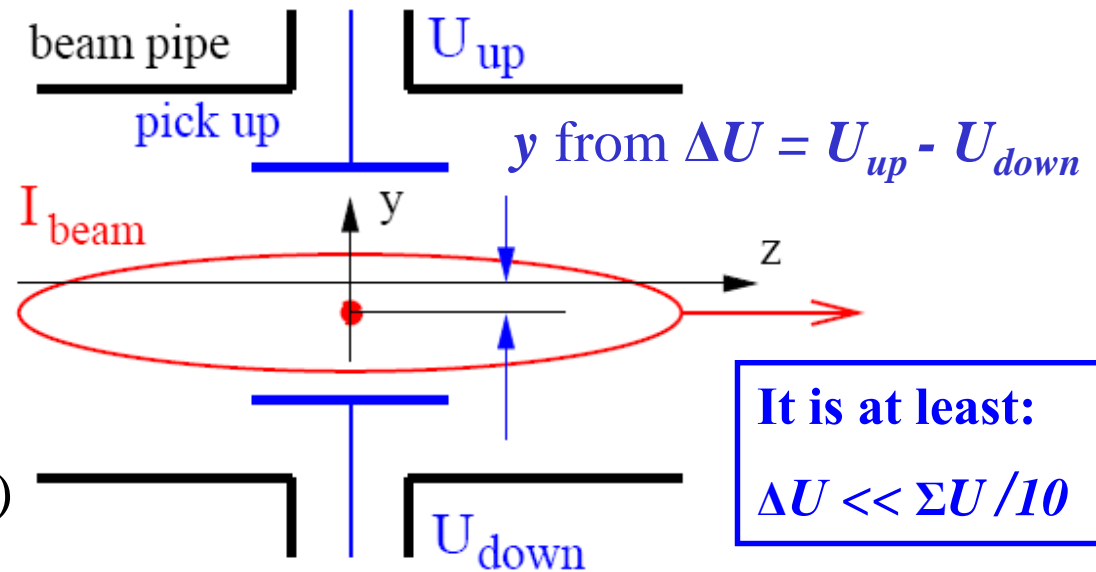
# Principle of Position Determination by a BPM

The difference voltage between plates gives the beam's center-of-mass  
 → **most frequent application**

‘Proximity’ effect leads to different voltages at the plates:

$$y = \frac{1}{S_y(\omega)} \cdot \frac{U_{up} - U_{down}}{U_{up} + U_{down}} + \delta_y(\omega)$$

$$\equiv \frac{1}{S_y} \cdot \frac{\Delta U_y}{\Sigma U_y} + \delta_y$$



Correspondingly:

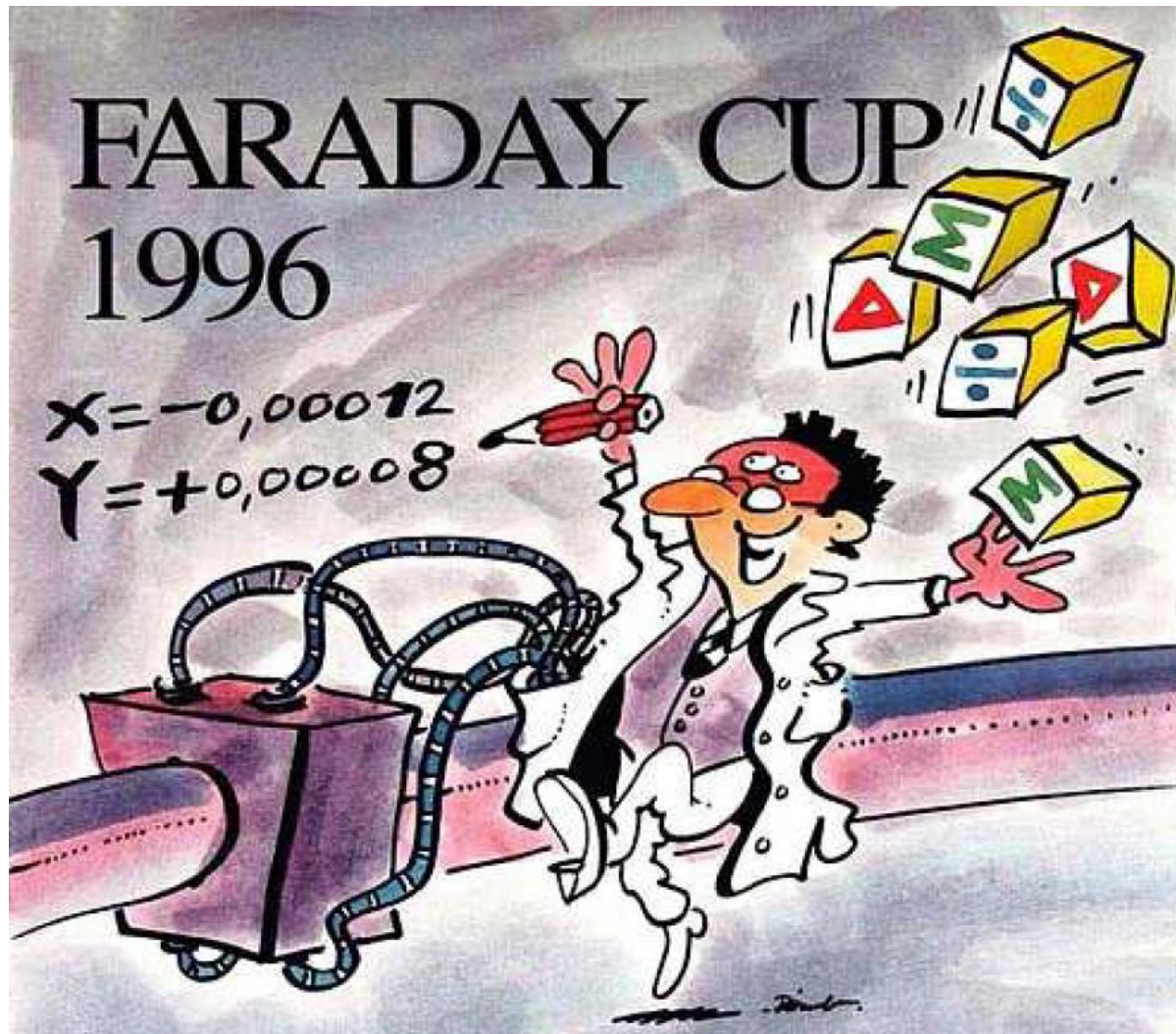
$$x = \frac{1}{S_x(\omega)} \cdot \frac{U_{right} - U_{left}}{U_{right} + U_{left}} + \delta_x(\omega)$$

$S(\omega, x)$  is called **position sensitivity**, sometimes the inverse is used  $k(\omega, x) = 1/S(\omega, x)$

$S$  is a geometry dependent, non-linear function, which have to be optimized

Units:  $S = [\%/mm]$  and sometimes  $S = [dB/mm]$  or  $k = [mm]$ .

# The Artist View of a BPM



## Outline:

- Signal generation → transfer **impedance**
- Capacitive button BPM for high frequencies  
used at most proton LINACs and electron accelerators
- Capacitive *shoe-box* BPM for low frequencies
- Electronics for position evaluation
- BPMs for measurement of closed orbit, tune and further lattice functions
- Summary

## 2-dim Model for a Button BPM

**‘Proximity effect’**: larger signal for closer plate

**Ideal 2-dim model**: Cylindrical pipe  $\rightarrow$  image current density via ‘image charge method’ for ‘pensile’ beam:

$$j_{im}(\phi) = \frac{I_{beam}}{2\pi a} \cdot \left( \frac{a^2 - r^2}{a^2 + r^2 - 2ar \cdot \cos(\phi - \theta)} \right)$$

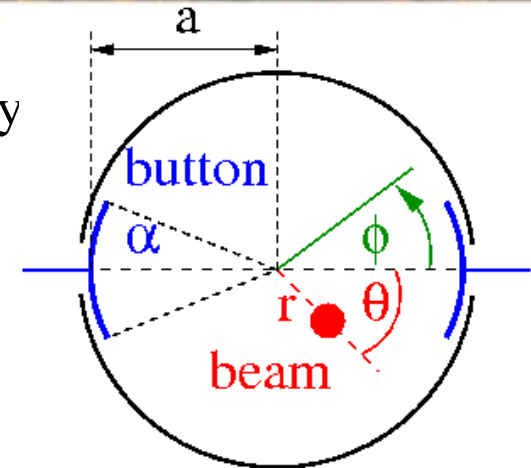
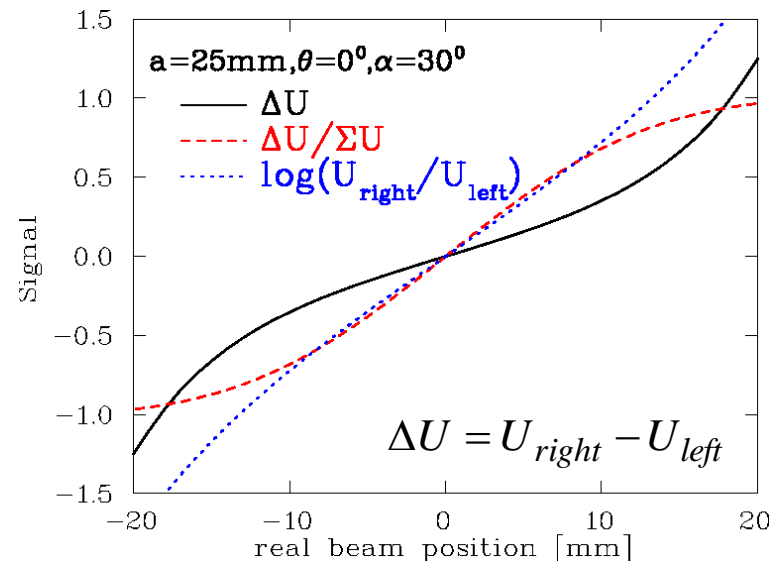
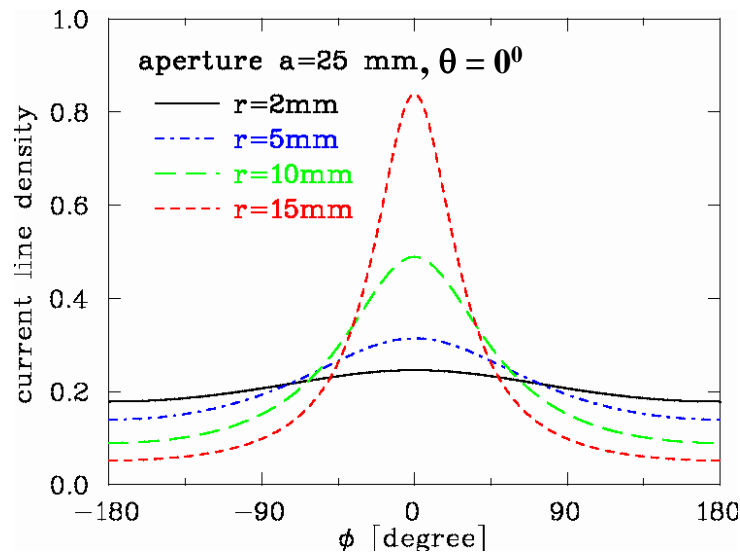


Image current: Integration of finite BPM size:  $I_{im} = a \cdot \int_{-\alpha/2}^{\alpha/2} j_{im}(\phi) d\phi$



## 2-dim Model for a Button BPM

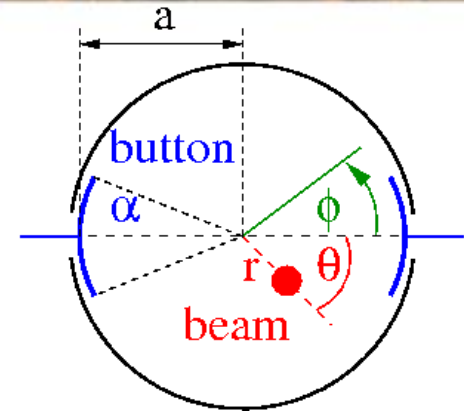
**Ideal 2-dim model:** Non-linear behavior and hor-vert coupling:

Sensitivity  $S$  is converts signal to position  $x = \frac{1}{S} \cdot \frac{\Delta U}{\Sigma U}$

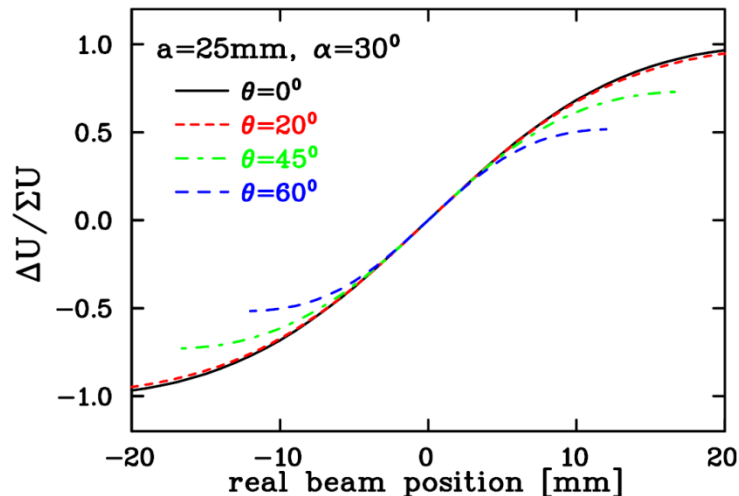
with  $S$  [%/mm] or [dB/mm]

i.e.  $S$  is the derivative of the curve  $S_x = \frac{\partial(\frac{\Delta U}{\Sigma U})}{\partial x}$ , here  $S_x = S_x(x, y)$  i.e. non-linear.

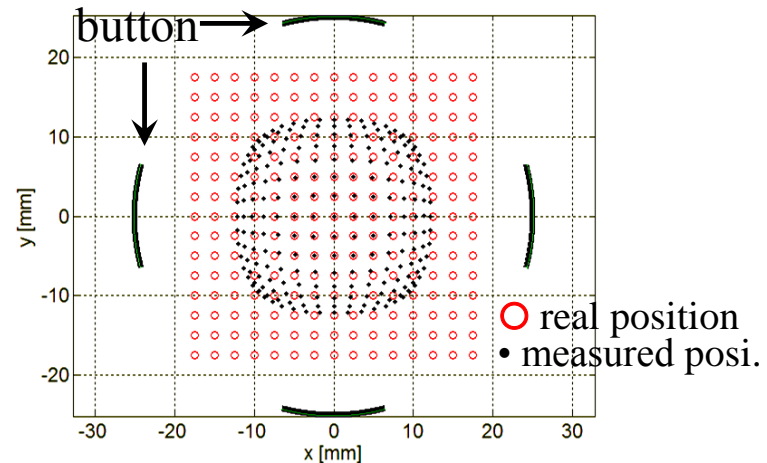
For this example: center part  $S=7.4\%/mm \Leftrightarrow k=1/S=14mm$



*Horizontal plane:*



*'Position Map':*

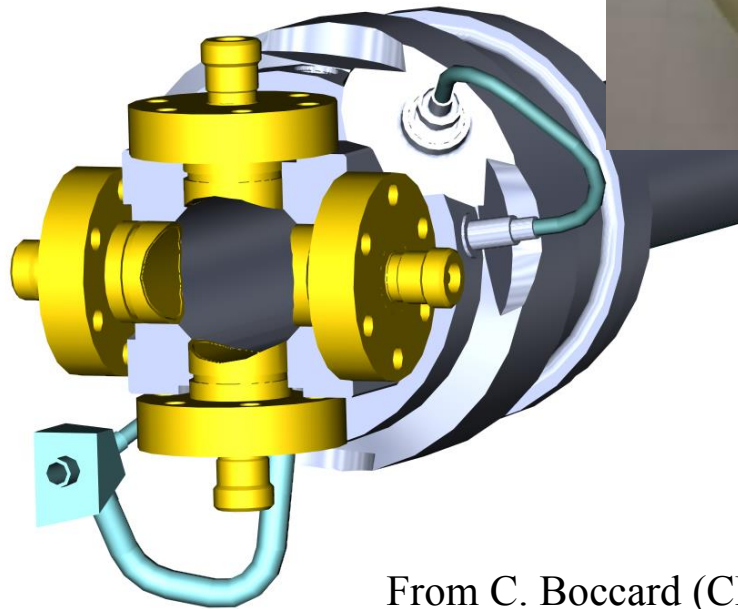


# Button BPM Realization

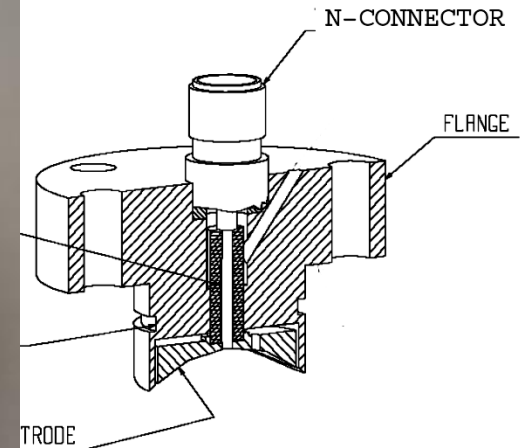
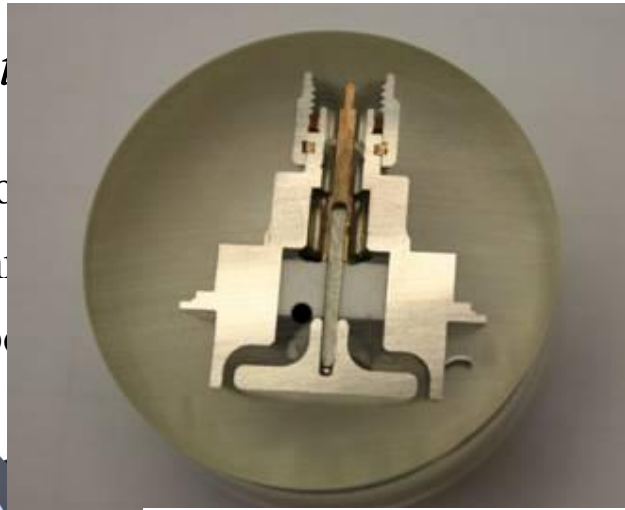
LINACs, e-synchrotrons:  $100 \text{ MHz} < f_{rf} < 3 \text{ GHz} \rightarrow$  bunch length  $\approx$  BPM length  
 $\rightarrow 50 \Omega$  signal path to prevent reflections

Button BPM with  $50 \Omega \Rightarrow U_{im}(t)$

Example: LHC-type inside cryo  
 $\varnothing 24 \text{ mm}$ , half aperture  $a=25 \text{ mm}$   
 $\Rightarrow f_{cut}=400 \text{ MHz}$ ,  $Z_t = 1.3 \Omega$  ab



From C. Boccard (CERN)

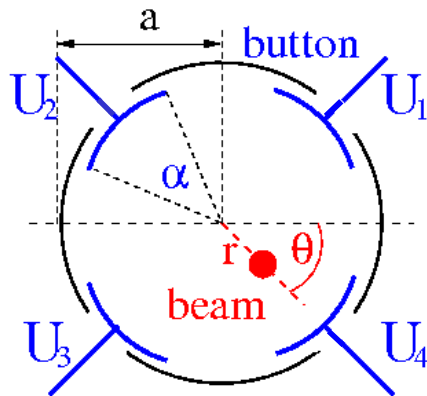




# Button BPM at Synchrotron Light Sources

The button BPM can be rotated by  $45^\circ$  to avoid exposure by synchrotron light:

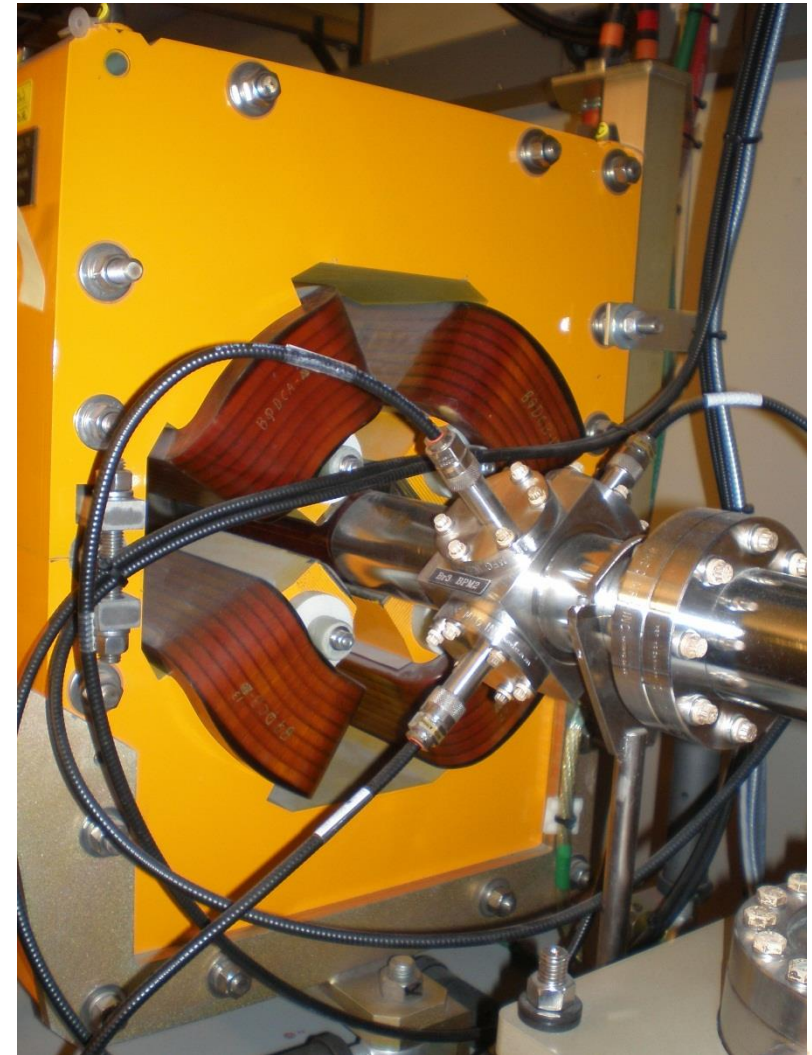
Frequently used at boosters for light sources



$$\text{horizontal} : x = \frac{1}{S} \cdot \frac{(U_1 + U_4) - (U_2 + U_3)}{U_1 + U_2 + U_3 + U_4}$$

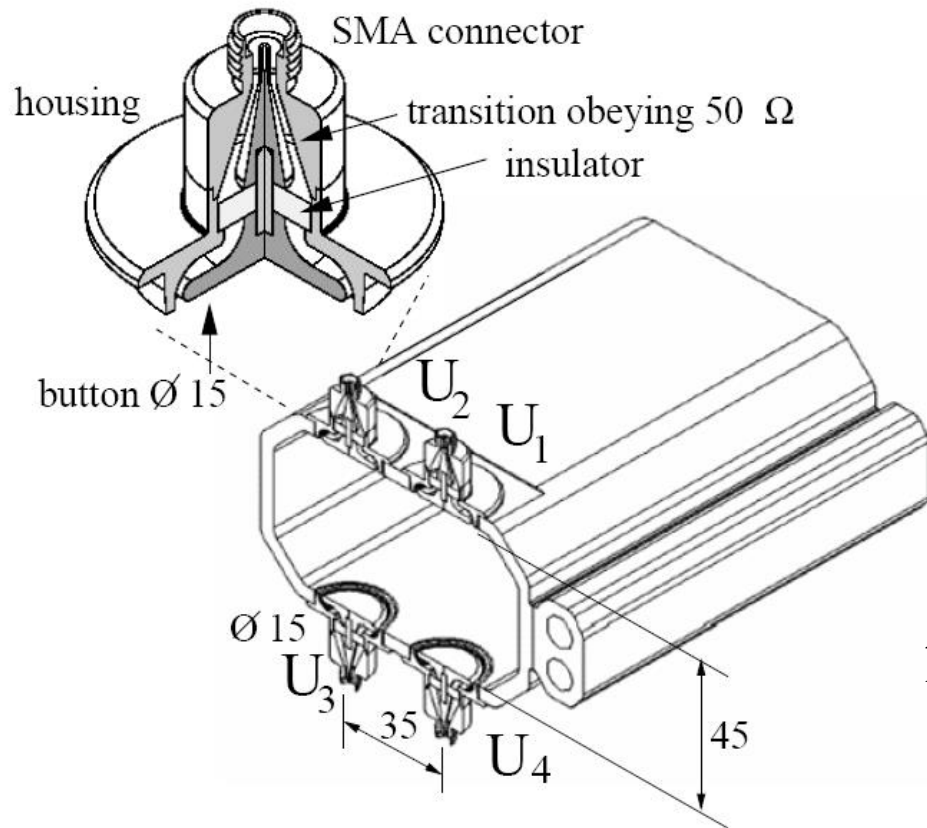
$$\text{vertical} : y = \frac{1}{S} \cdot \frac{(U_1 + U_2) - (U_3 + U_4)}{U_1 + U_2 + U_3 + U_4}$$

*Example:* Booster of ALS, Berkeley

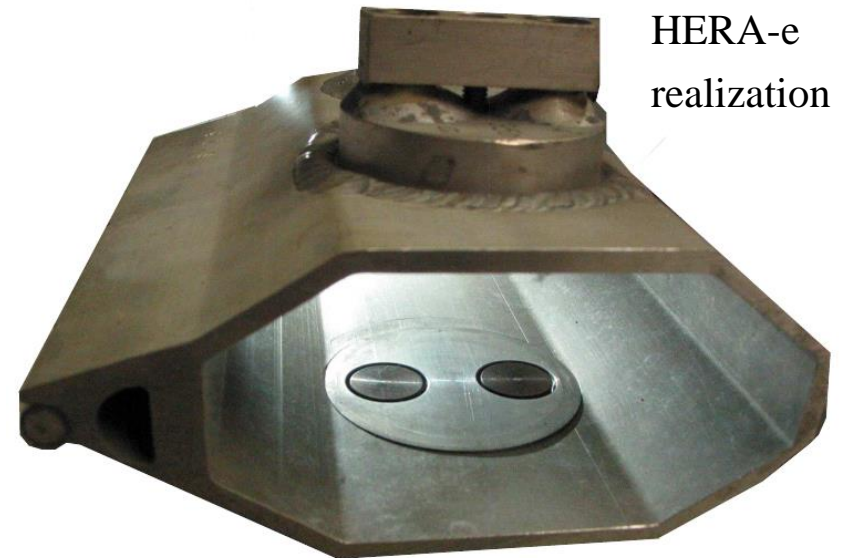


# Button BPM at Synchrotron Light Sources

Due to synchrotron radiation, the button insulation might be destroyed  
 ⇒ buttons only in vertical plane possible ⇒ increased non-linearity



PEP-realization



HERA-e realization

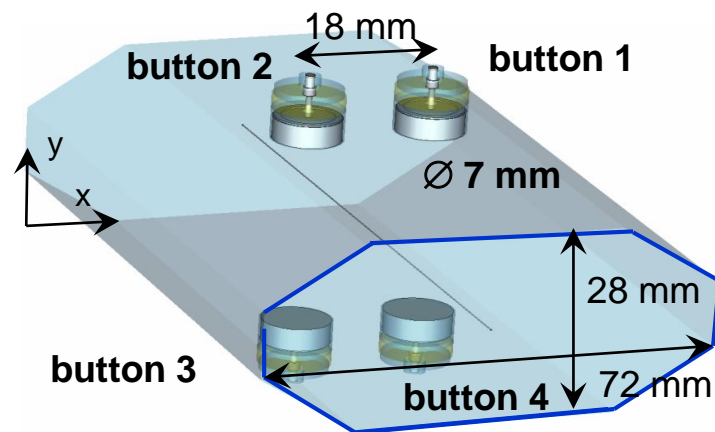
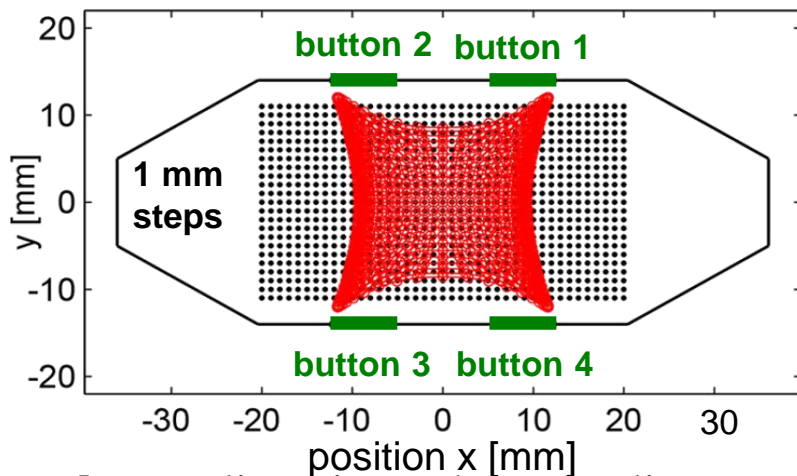
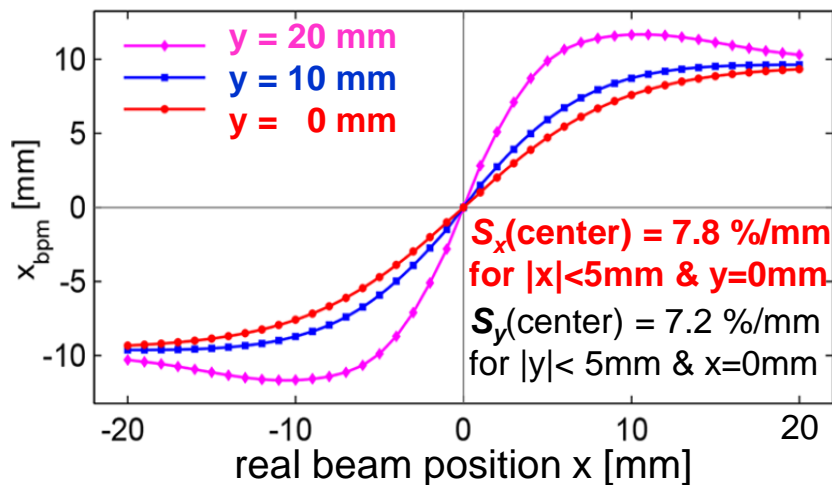
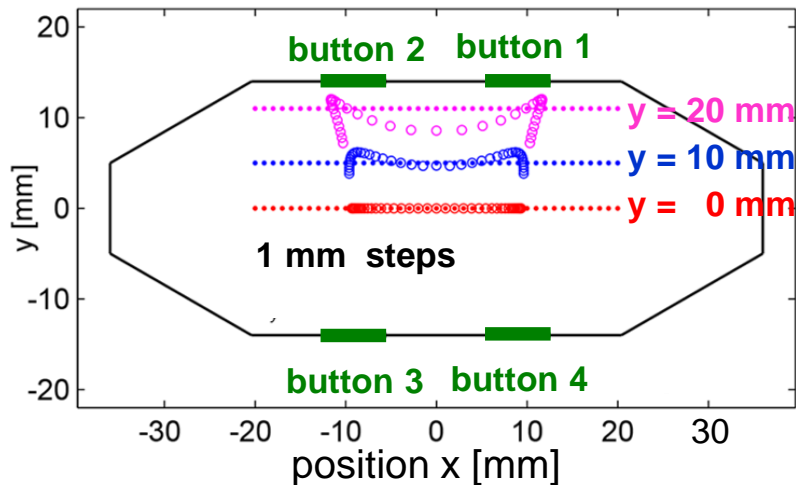
$$\text{horizontal: } x = \frac{1}{S_x} \cdot \frac{(U_1 + U_4) - (U_2 + U_3)}{U_1 + U_2 + U_3 + U_4}$$

$$\text{vertical: } y = \frac{1}{S_y} \cdot \frac{(U_1 + U_2) - (U_3 + U_4)}{U_1 + U_2 + U_3 + U_4}$$

# Simulations for Button BPM at Synchrotron Light Sources

Example: Simulation for ALBA light source for 72 x 28 mm<sup>2</sup> chamber

**Optimization:** horizontal distance and size of buttons



**Result:** non-linearity and *xy*-coupling occur in dependence of button size and position

## Outline:

- Signal generation → transfer impedance
- Capacitive *button* BPM for high frequencies  
used at most proton LINACs and electron accelerators
- Capacitive shoe-box BPM for low frequencies  
used at most proton synchrotrons due to linear position reading
- Electronics for position evaluation
- BPMs for measurement of closed orbit, tune and further lattice functions
- Summary

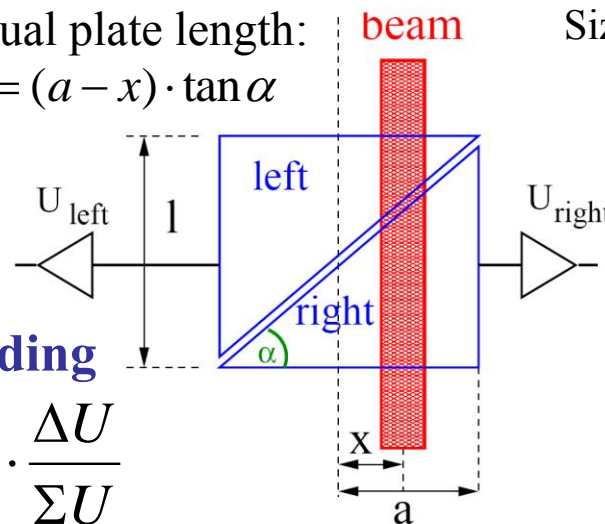
# Shoe-box BPM for Proton Synchrotrons

Frequency range:  $1 \text{ MHz} < f_{rf} < 10 \text{ MHz} \Rightarrow \text{bunch-length} \gg \text{BPM length}$ .

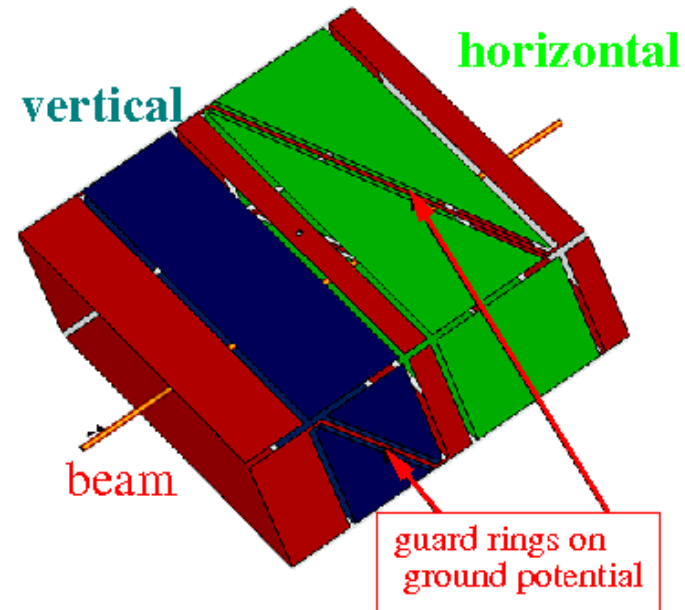
Signal is proportional to actual plate length:

$$l_{\text{right}} = (a + x) \cdot \tan \alpha, \quad l_{\text{left}} = (a - x) \cdot \tan \alpha$$

$$\Rightarrow x = a \cdot \frac{l_{\text{right}} - l_{\text{left}}}{l_{\text{right}} + l_{\text{left}}}$$

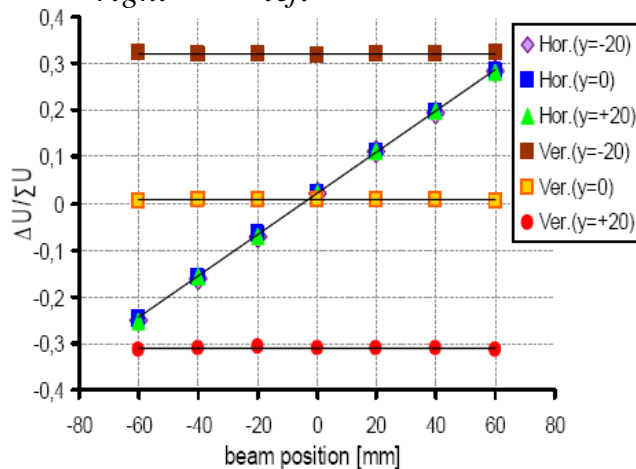


Size: 200x70 mm<sup>2</sup>



**In ideal case: linear reading**

$$x = a \cdot \frac{U_{\text{right}} - U_{\text{left}}}{U_{\text{right}} + U_{\text{left}}} \equiv a \cdot \frac{\Delta U}{\Sigma U}$$



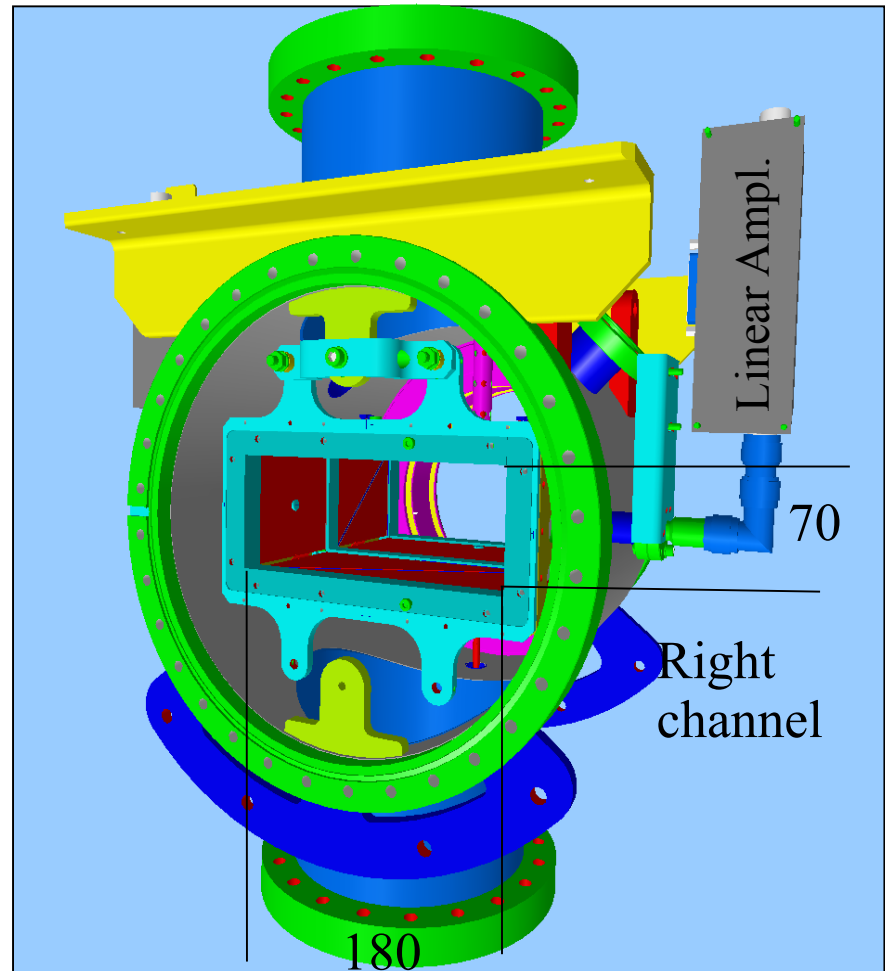
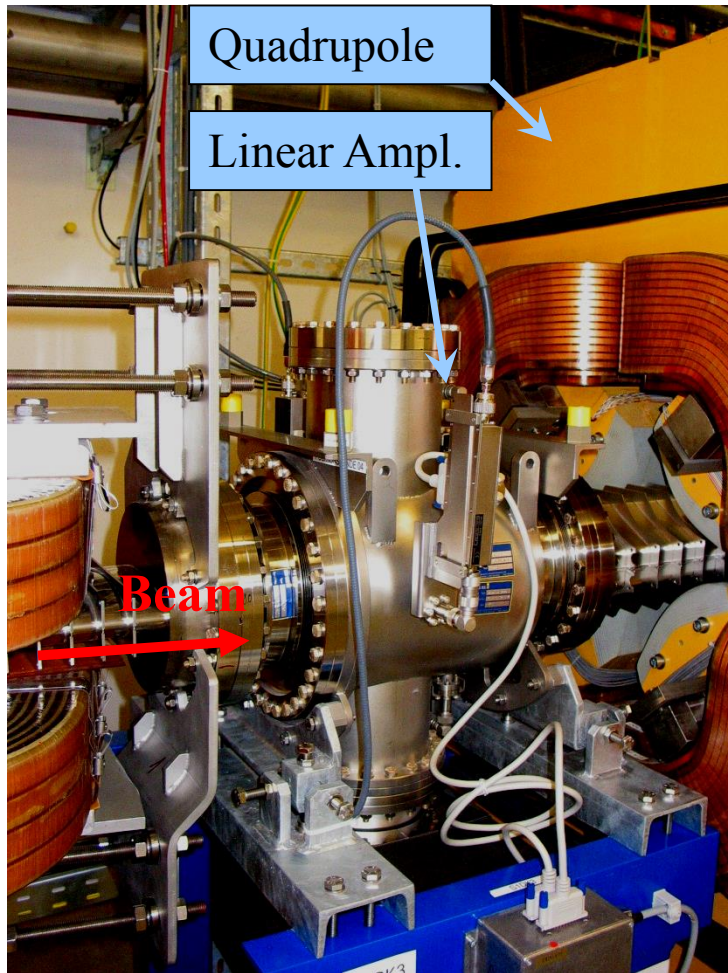
**Shoe-box BPM:**

**Advantage:** Very linear, low frequency dependence  
i.e. position sensitivity  $S$  is constant

**Disadvantage:** Large size, complex mechanics  
high capacitance

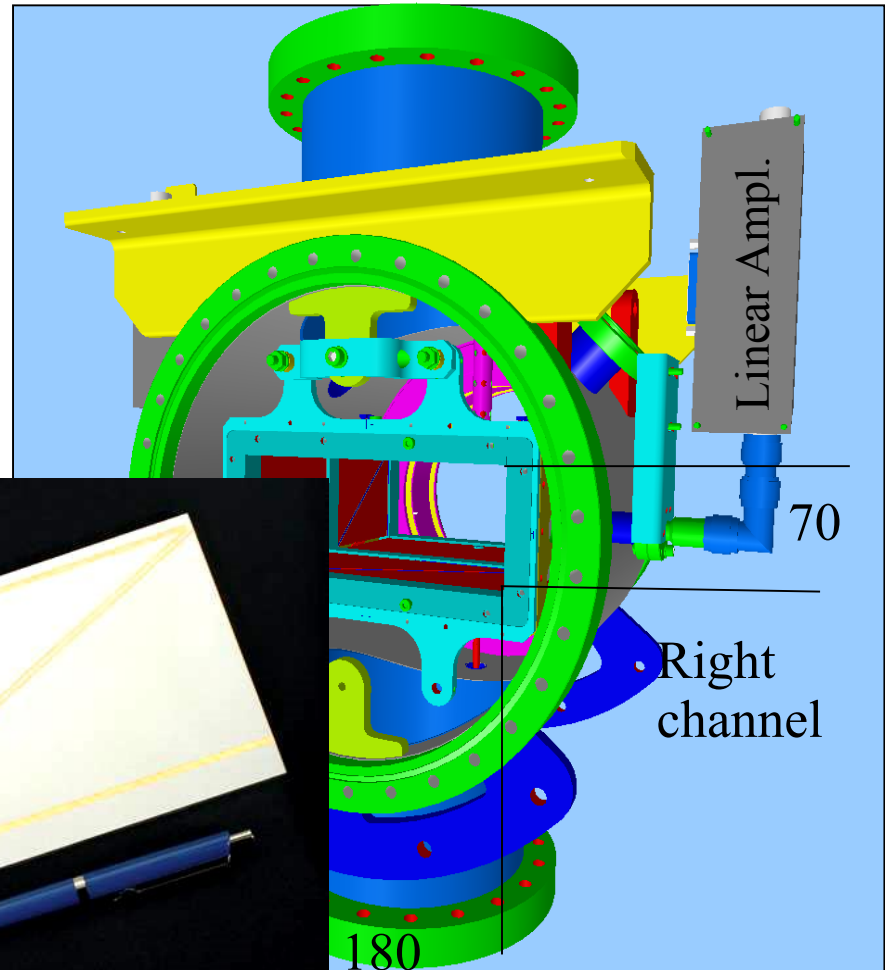
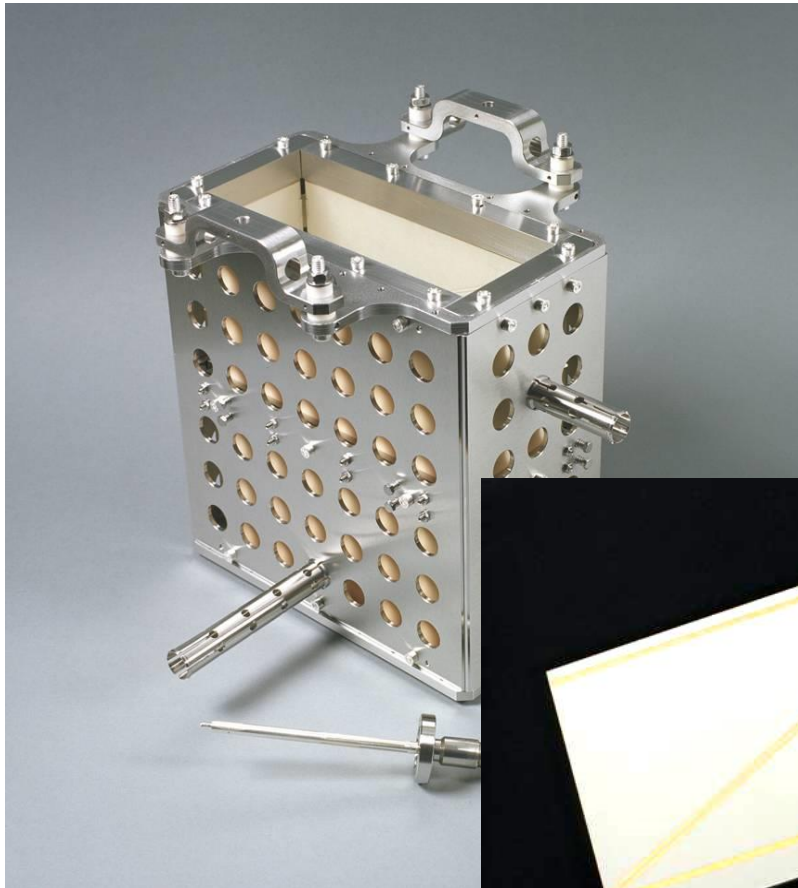
# Technical Realization of a Shoe-Box BPM

Technical realization at HIT synchrotron of 46 m length for 7 MeV/u → 440 MeV/u  
 BPM clearance: 180x70 mm<sup>2</sup>, standard beam pipe diameter: 200 mm.



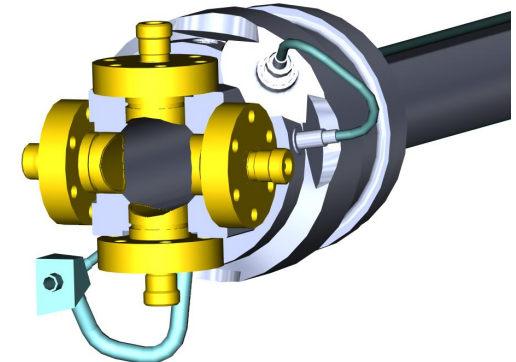
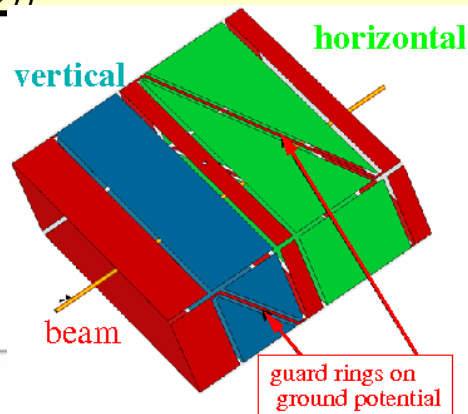
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# Comparison Shoe-Box and Button BPM

	Shoe-Box BPM	Button BPM
<b>Precaution</b>	Bunches longer than BPM	Bunch length comparable to BPM
<b>BPM length (typical)</b>	10 to 20 cm length per plane	∅1 to 5 cm per button
<b>Shape</b>	Rectangular or cut cylinder	Orthogonal or planar orientation
<b>Bandwidth (typical)</b>	0.1 to 100 MHz	100 MHz to 5 GHz
<b>Coupling</b>	1 MΩ or ≈1 kΩ (transformer)	50 Ω
<b>Cutoff frequency (typical)</b>	0.01... 10 MHz (C=30...100pF)	0.3... 1 GHz (C=2...10pF)
<b>Linearity</b>	Very good, no x-y coupling	Non-linear, x-y coupling
<b>Sensitivity</b>	Good, care: plate cross talk	Good, care: signal matching
<b>Usage</b>	At proton synchrotrons, $f_{rf} < 10$ MHz	All electron acc., proton Linacs, $f_{rf} > 100$ MHz





## Outline:

- **Signal generation → transfer impedance**
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used at most proton LINACs and electron accelerators
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used at most proton synchrotrons due to linear **position reading**
- **Electronics for position evaluation**  
analog signal conditioning to achieve small signal processing
- **BPMs for measurement of closed orbit, tune and further lattice functions**
- **Summary**

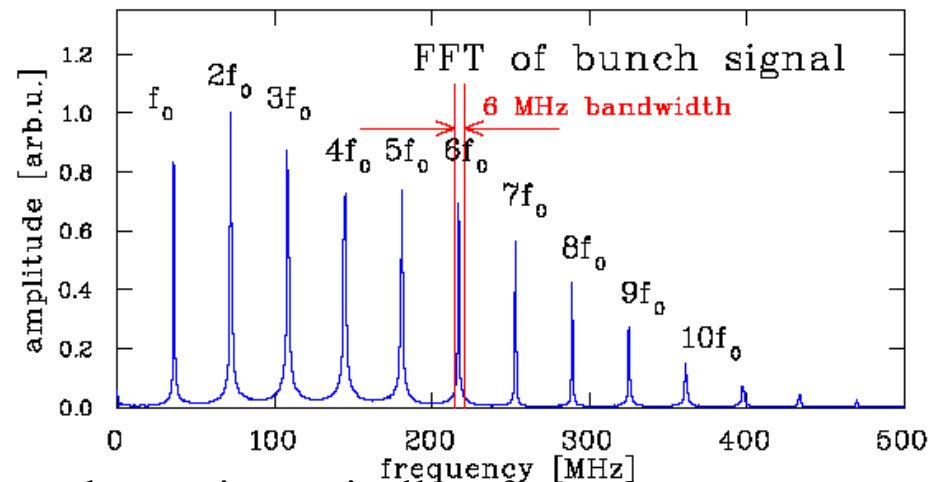
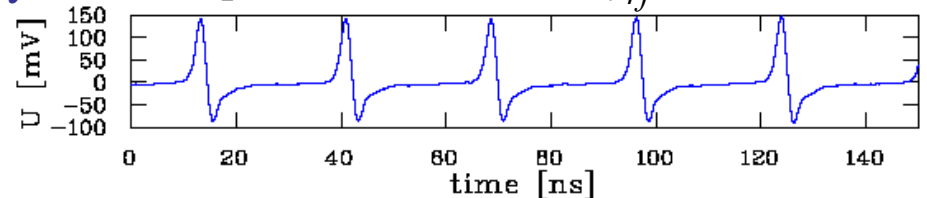
# General: Noise Consideration

1. Signal voltage given by:  $U_{im}(f) = Z_t(f) \cdot I_{beam}(f)$
2. Position information from voltage difference:  $x = 1/S \cdot \Delta U / \Sigma U$
3. Thermal noise voltage given by:  $U_{eff}(R, \Delta f) = \sqrt{4k_B \cdot T \cdot R \cdot \Delta f}$

⇒ Signal-to-noise  $\Delta U_{im}/U_{eff}$  is influenced by:

- Input signal amplitude
  - large or matched  $Z_t$
- Thermal noise at  $R=50 \Omega$  for  $T=300 \text{ K}$ 
  - (for shoe box  $R = 1 \text{ k}\Omega \dots 1 \text{ M}\Omega$ )
- Bandwidth  $\Delta f$ 
  - ⇒ Restriction of frequency width because the power is concentrated on the harmonics of  $f_{rf}$

*Example:* GSI-LINAC with  $f_{rf}=36 \text{ MHz}$

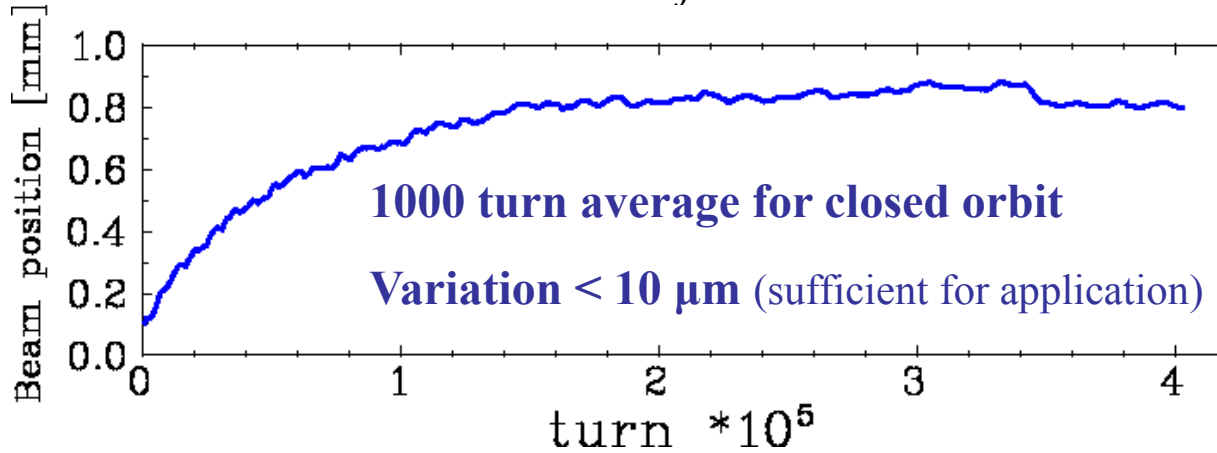


**Remark:** Additional contribution by non-perfect electronics typically a factor 2

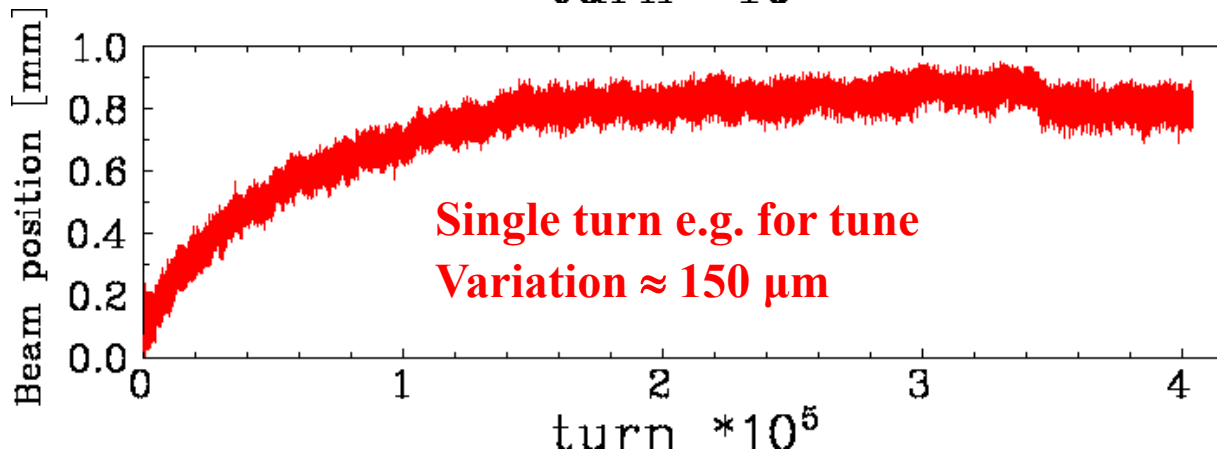
Moreover, pick-up by electro-magnetic interference can contribute ⇒ good shielding required

# Comparison: Filtered Signal ↔ Single Turn

*Example:* GSI Synchr.:  $U^{73+}$ ,  $E_{inj}=11.5$  MeV/u → 250 MeV/u within 0.5 s,  $10^9$  ions



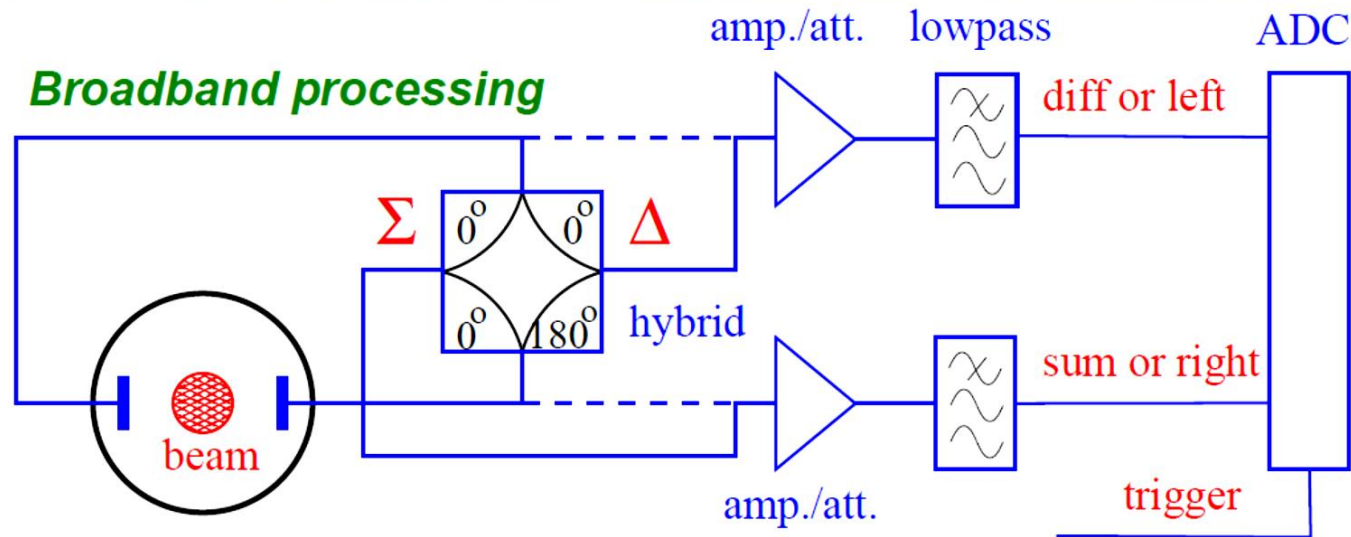
- Position resolution < 30  $\mu\text{m}$  (BPM half aperture  $a=90$  mm)
- average over 1000 turns corresponding to  $\approx 1$  ms or  $\approx 1$  kHz bandwidth



- Turn-by-turn data have much larger variation

**However:** not only noise contributes but additionally **beam movement** by betatron oscillation  
 $\Rightarrow$  broadband processing i.e. turn-by-turn readout for tune determination.

# Broadband Signal Processing

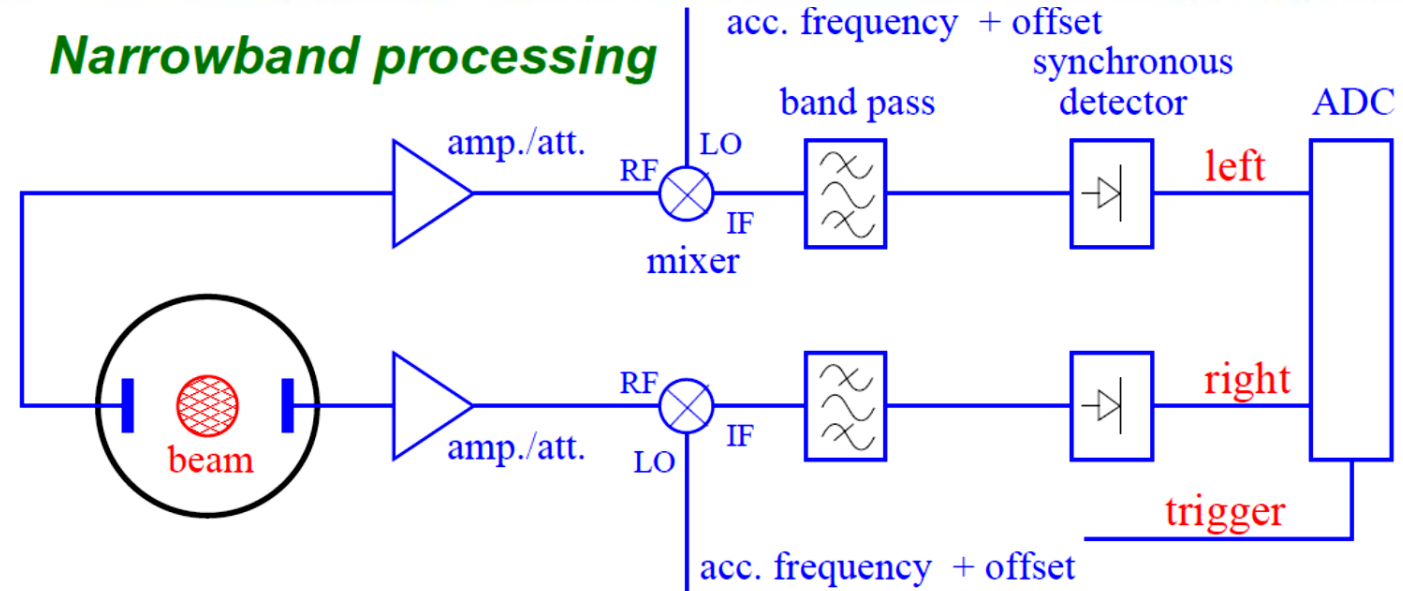


- Hybrid or transformer close to beam pipe for analog  $\Delta U$  &  $\Sigma U$  generation or  $U_{left}$  &  $U_{right}$
- Attenuator/amplifier
- Filter to get the wanted harmonics and to suppress stray signals
- ADC: digitalization  $\rightarrow$  followed by calculation of  $\Delta U / \Sigma U$

**Advantage:** Bunch-by-bunch possible, versatile post-processing possible

**Disadvantage:** Resolution down to  $\approx 100 \mu\text{m}$  for shoe box type, i.e.  $\approx 0.1\%$  of aperture, resolution is worse than narrowband processing

# Narrowband Processing for improved Signal-to-Noise



Narrowband processing equals heterodyne receiver (e.g. AM-radio or spectrum analyzer)

- Attenuator/amplifier
- Mixing with accelerating frequency  $f_{rf} \Rightarrow$  signal with sum and difference frequency
- Bandpass filter of the mixed signal (e.g at 10.7 MHz)
- Rectifier: synchronous detector
- ADC: digitalization  $\rightarrow$  followed calculation of  $\Delta U/\Sigma U$

**Advantage:** spatial resolution about 100 time better than broadband processing

**Disadvantage:** No turn-by-turn diagnosis, due to mixing = 'long averaging time'

For non-relativistic p-synchrotron:  $\rightarrow$  variable  $f_{rf}$  leads via mixing to constant intermediate freq.

# Mixer and Synchronous Detector

**Mixer:** A passive rf device with

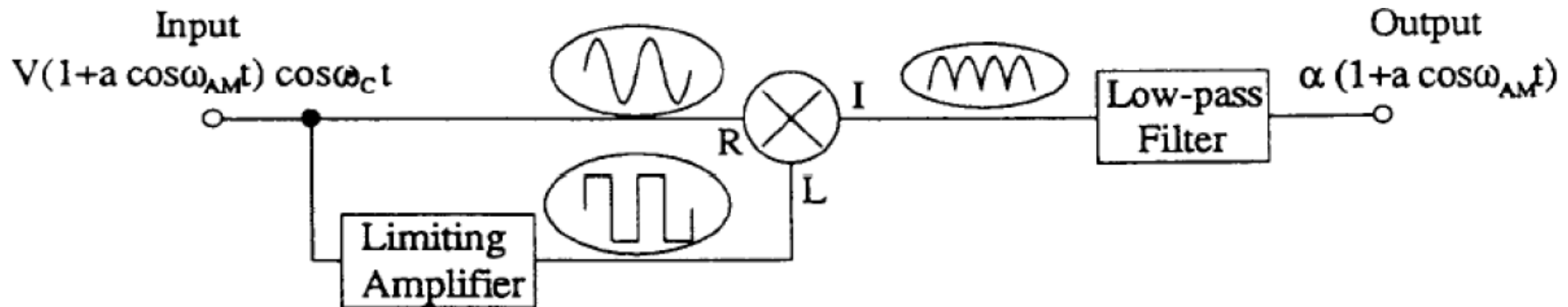
- Input RF (radio frequency): Signal of investigation  $A_{RF}(t) = A_{RF} \cos \omega_{RF} t$
- Input LO (local oscillator): Fixed frequency  $A_{LO}(t) = A_{LO} \cos \omega_{LO} t$
- Output IF (intermediate frequency)

$$A_{IF}(t) = A_{RF} \cdot A_{LO} \cos \omega_{RF} t \cdot \cos \omega_{LO} t$$

$$= A_{RF} \cdot A_{LO} [\cos(\omega_{RF} - \omega_{LO})t + \cos(\omega_{RF} + \omega_{LO})t]$$

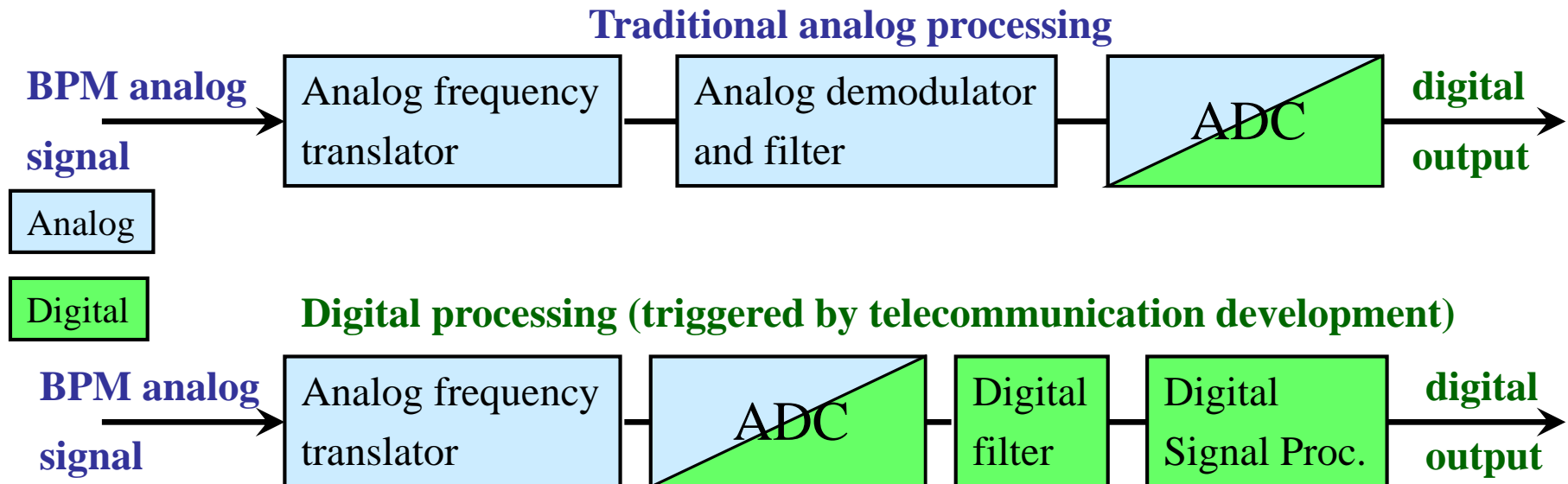
⇒ Multiplication of both input signals, containing the sum and difference frequency.

**Synchronous detector:** A phase sensitive rectifier



# Analog versus Digital Signal Processing

Modern instrumentation uses **digital** techniques with extended functionality.



## Digital receiver as modern successor of super heterodyne receiver

- Basic functionality is preserved but implementation is very different
- Digital transition just after the amplifier & filter or mixing unit
- Signal conditioning (filter, decimation, averaging) on digital electronics e.g. FPGA

**Advantage of DSP:** Versatile operation, flexible adoption without hardware modification

**Disadvantage of DSP:** non, good engineering skill requires for development, expensive

# Comparison of BPM Readout Electronics (simplified)

Type	Usage	Precaution	Advantage	Disadvantage
<b>Broadband</b>	p-sychr.	Long bunches	Bunch structure signal Post-processing possible Required for fast feedback	Resolution limited by noise
<b>Narrowband</b>	all synchr.	Stable beams >100 rf-periods	High resolution	No turn-by-turn Complex electronics
<b>Digital Signal Processing</b>	all	Several bunches ADC 125 MS/s	Very flexible High resolution <b>Trendsetting technology for future demands</b>	Limited time resolution by ADC → undersampling complex and expensive



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used at most proton synchrotrons due to linear position reading
- Electronics for position evaluation  
analog signal conditioning to achieve small signal processing
- **BPMs for measurement of closed orbit, tune and further lattice functions**  
**frequent application of BPMs**
- **Summary**

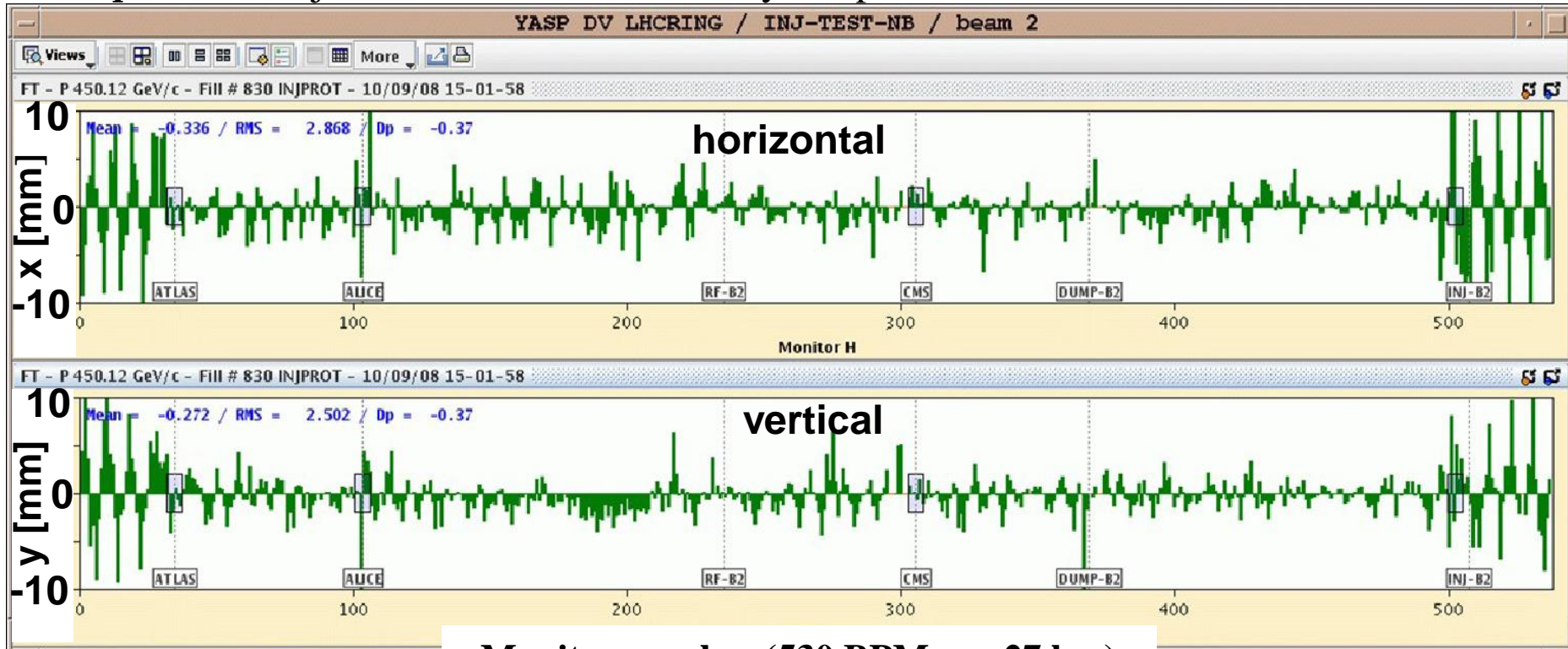
# Trajectory Measurement with BPMs

## Trajectory:

The position delivered by an **individual bunch** within a transfer line or a synchrotron.

Main task: Control of matching (center and angle), first-turn diagnostics

*Example:* LHC injection 10/09/08 i.e. first day of operation !



Monitor number (530 BPMs on 27 km)

Tune values:  $Q_h = 64.3$ ,  $Q_v = 59.3$

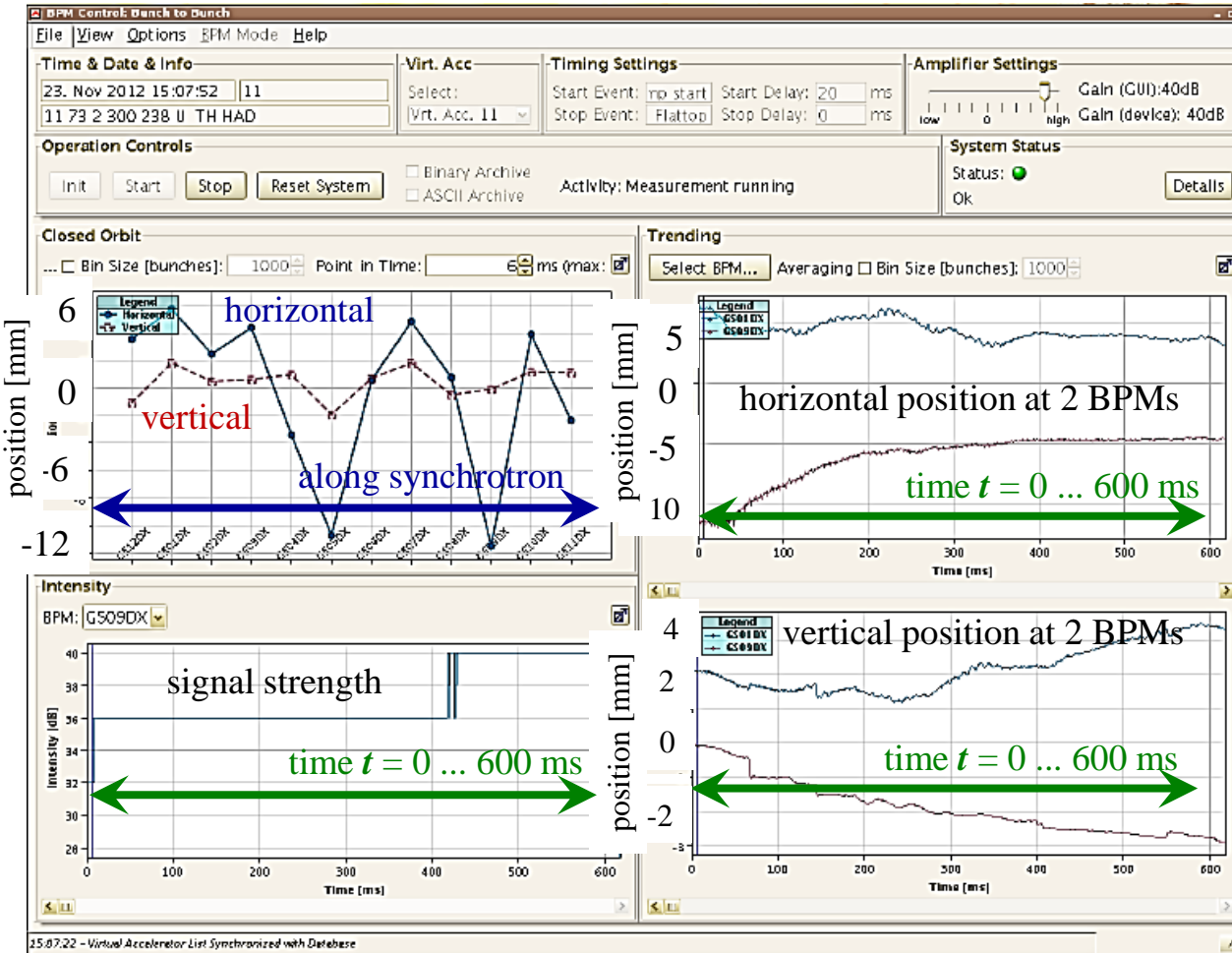
From R. Jones (CERN)

# Close Orbit Measurement with BPMs

Single bunch position averaged over 1000 bunches → closed orbit with ms time steps.

It differs from ideal orbit by misalignments of the beam or components.

*Example: GSI-synchrotron at two BPM locations, 1000 turn average during acceleration:*



## Closed orbit:

Beam position averaged over many turns (i.e. betatron oscillations). The result is the basic tool for alignment & stabilization

## Remark as a role of thumb:

Number of BPMs within a synchrotron:  $N_{BPM} \approx 4 \cdot Q$   
 Relation BPMs ↔ tune due to close orbit stabilization feedback (justification outside of the scope of this lecture)

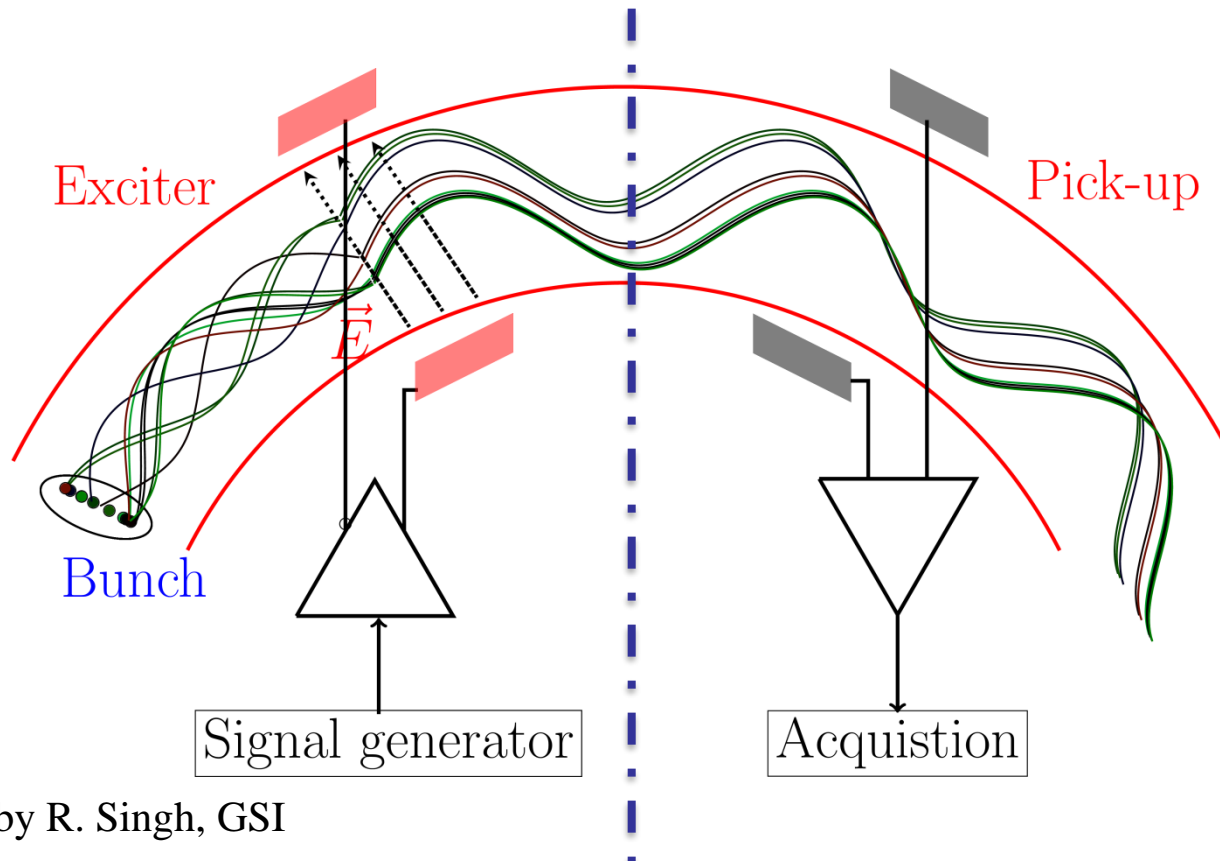
# Tune Measurement: General Considerations

Coherent excitations are required for the detection by a BPM

Beam particle's *in-coherent* motion  $\Rightarrow$  center-of-mass stays constant

Excitation of **all** particles by rf  $\Rightarrow$  *coherent* motion

$\Rightarrow$  center-of-mass variation turn-by-turn



Graphics by R. Singh, GSI

# Tune Measurement: General Considerations

The tune  $Q$  is the number of betatron oscillations per turn.

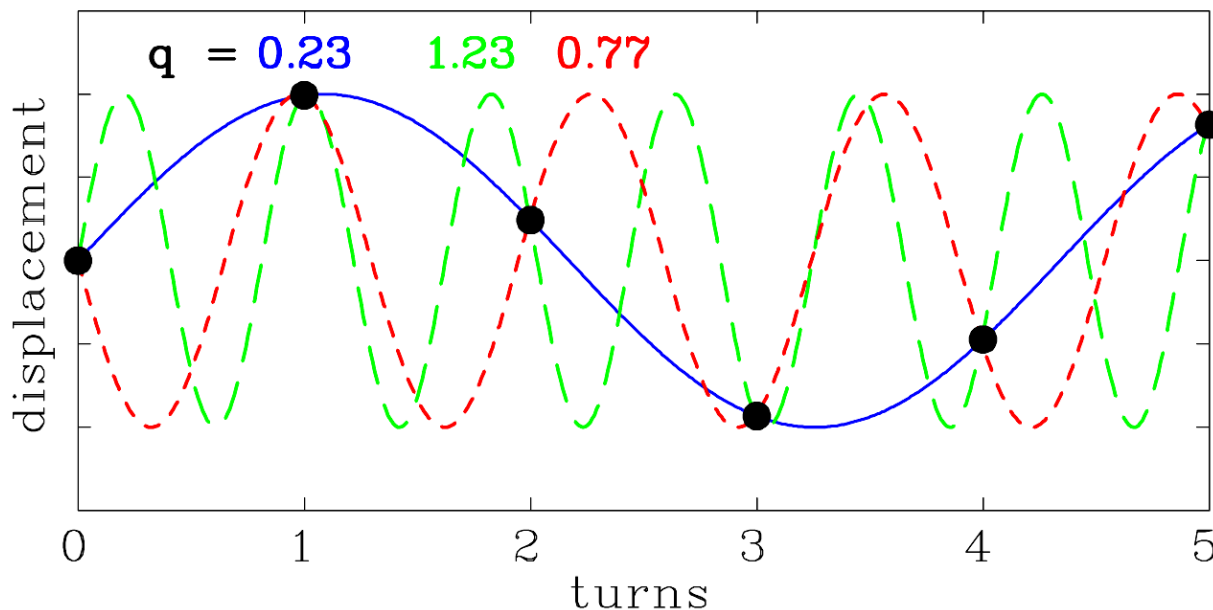
The betatron frequency is  $f_\beta = Q \cdot f_0$ .

**Measurement:** excitation of *coherent* betatron oscillations + position from one BPM.

From a measurement one gets only the non-integer part  $q$  of  $Q$  with  $Q = n \pm q$ .

Moreover, only  $0 < q < 0.5$  is the unique result.

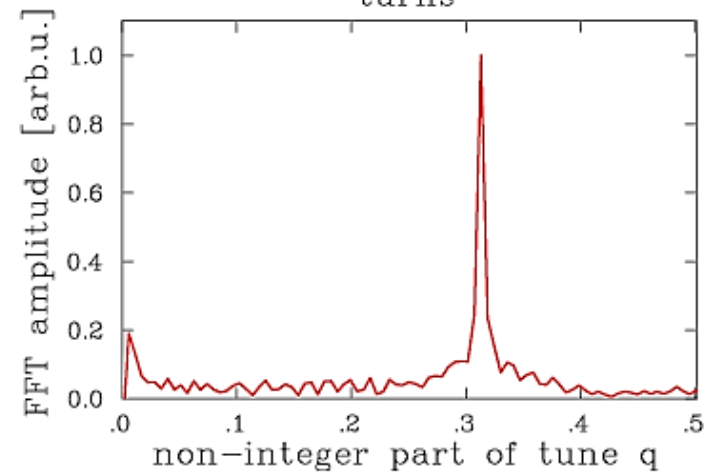
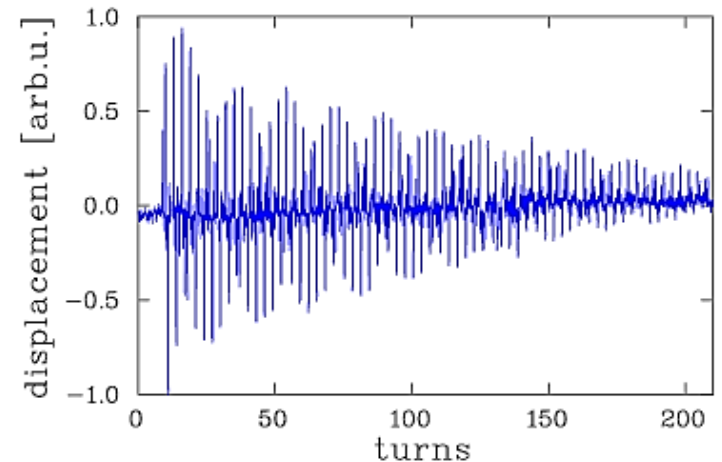
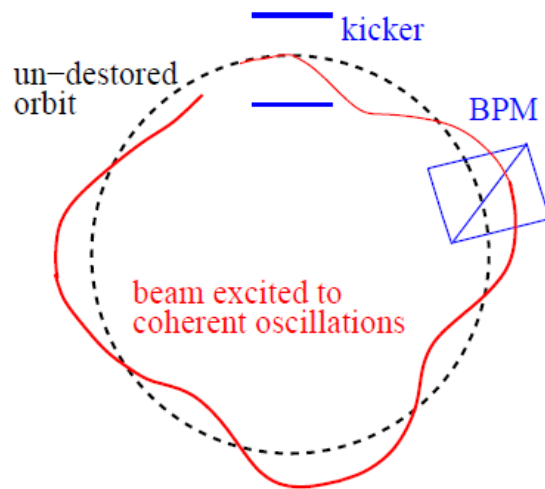
**Example:** Tune measurement for six turns with the three lowest frequency fits:



To distinguish  
for  $q < 0.5$  or  $q > 0.5$ :  
Changing the tune slightly,  
the direction of  $q$  shift differs.

# Tune Measurement: The Kick-Method in Time Domain

The beam is excited to coherent betatron oscillation  
 → the beam position measured each revolution ('turn-by-turn')  
 → Fourier Trans. gives the non-integer tune  $q$ .  
 Short kick compared to revolution.



The de-coherence time limits the **resolution**:

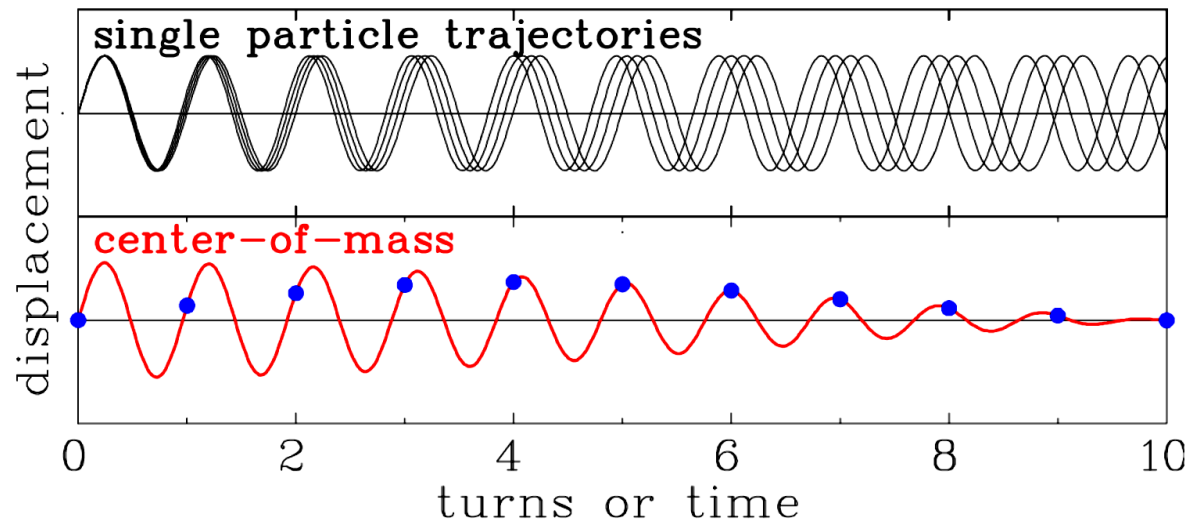
$N$  non-zero samples

⇒ General limit of discrete FFT:  $\Delta q > \frac{1}{2N}$

$N = 200$  turn ⇒  $\Delta q > 0.003$  as resolution  
 (tune spreads are typically  $\Delta q \approx 0.001!$ )

## Tune Measurement: De-Coherence Time

The particles are excited to betatron oscillations, but due to the spread in the betatron frequency, they getting out of phase ('Landau damping'):



Scheme of the individual trajectories of four particles after a kick (top) and the resulting *coherent* signal as measured by a pick-up (bottom).

⇒ Kick excitation leads to limited resolution

Remark: The tune spread is much lower for a real machine.

# Tune Measurement: Beam Transfer Function in Frequency Domain

Instead of one kick, the beam can be excited by a sweep of a sine wave, called ‘chirp’

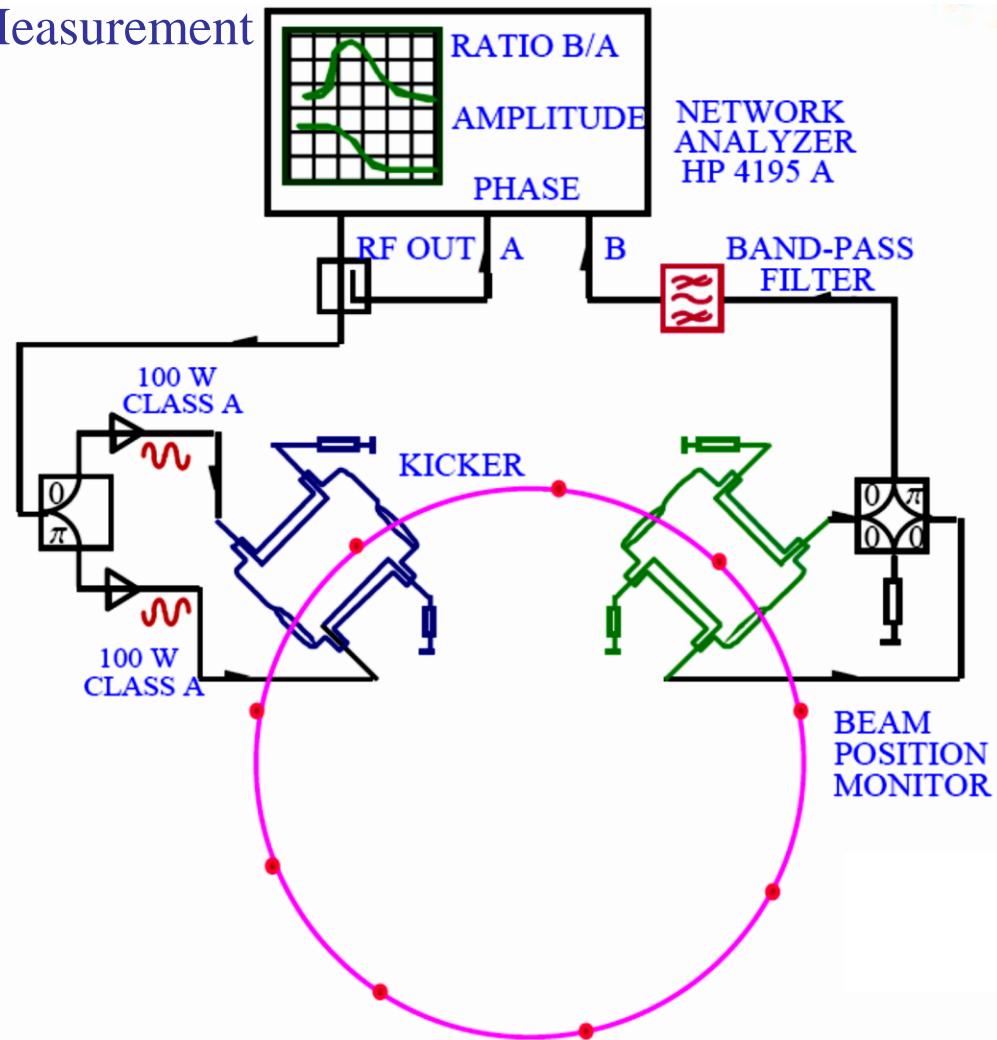
→ **Beam Transfer Function (BTF) Measurement**  
as the velocity response to a kick

## Principle:

**Beam acts like a driven oscillator!**

Using a network analyzer:

- RF OUT is feed to the beam by a kicker (reversed powered as a BPM)
- The position is measured at one BPM
- Network analyzer: amplitude and phase of the response
- Sweep time up to seconds due to de-coherence time per band
- resolution in tune: up to  $10^{-4}$



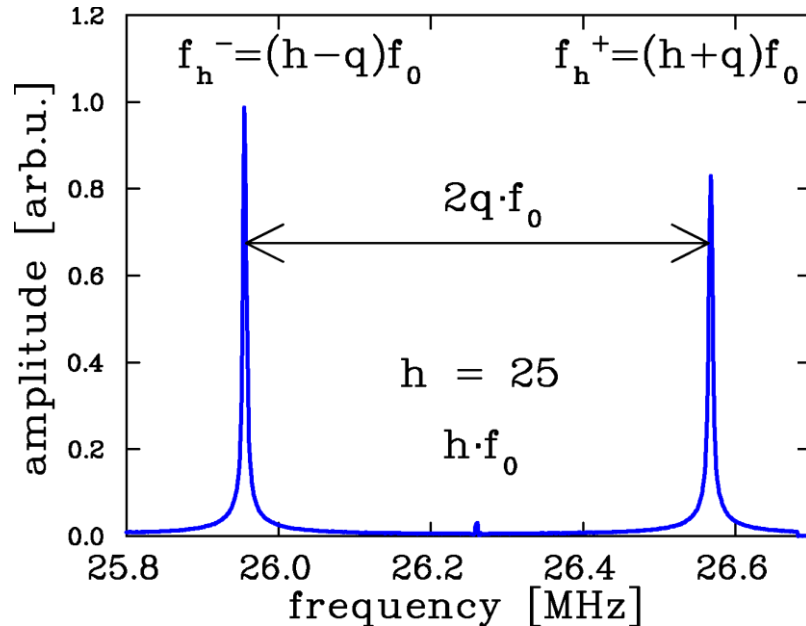


# Tune Measurement: Result for BTF Measurement

BTF measurement at the GSI synchrotron, recorded at the 25th harmonics.

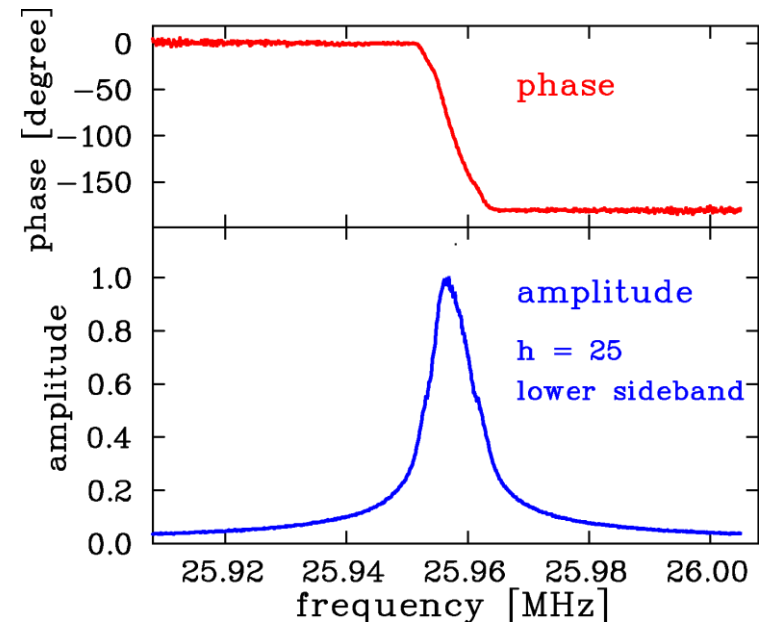
*A wide scan with both sidebands at*

*$h=25^{\text{th}}$ -harmonics:*



*A detailed scan for the lower sideband*

*→ beam acts like a driven oscillator:*



From the position of the sidebands  $q = 0.306$  is determined. From the width

$$\Delta f/f \approx 5 \cdot 10^{-4} \text{ the tune spread can be calculated via } \Delta f_h^- = \eta \frac{\Delta p}{p} \cdot h f_0 \left( h - q + \frac{\xi}{\eta} Q \right)$$

**Advantage:** High resolution for tune and tune spread (also for de-bunched beams)

**Disadvantage:** Long sweep time (up to several seconds).

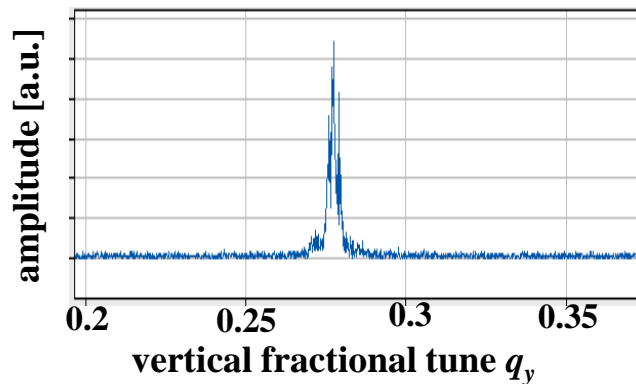
# Tune Measurement: Gentle Excitation with Wideband Noise

Instead of a sine wave, noise with adequate bandwidth can be applied

→ beam picks out its resonance frequency: *Example:* Vertical tune within 4096 turn duration  $\approx 15$  ms at GSI synchrotron 11 → 300 MeV/u in 0.7 s

- broadband excitation with white noise of  $\approx 10$  kHz bandwidth
- turn-by-turn position measurement by fast ADC
- Fourier transformation of the recorded data
- ⇒ Continues monitoring with low disturbance

vertical tune at fixed time  $\approx 15$ ms

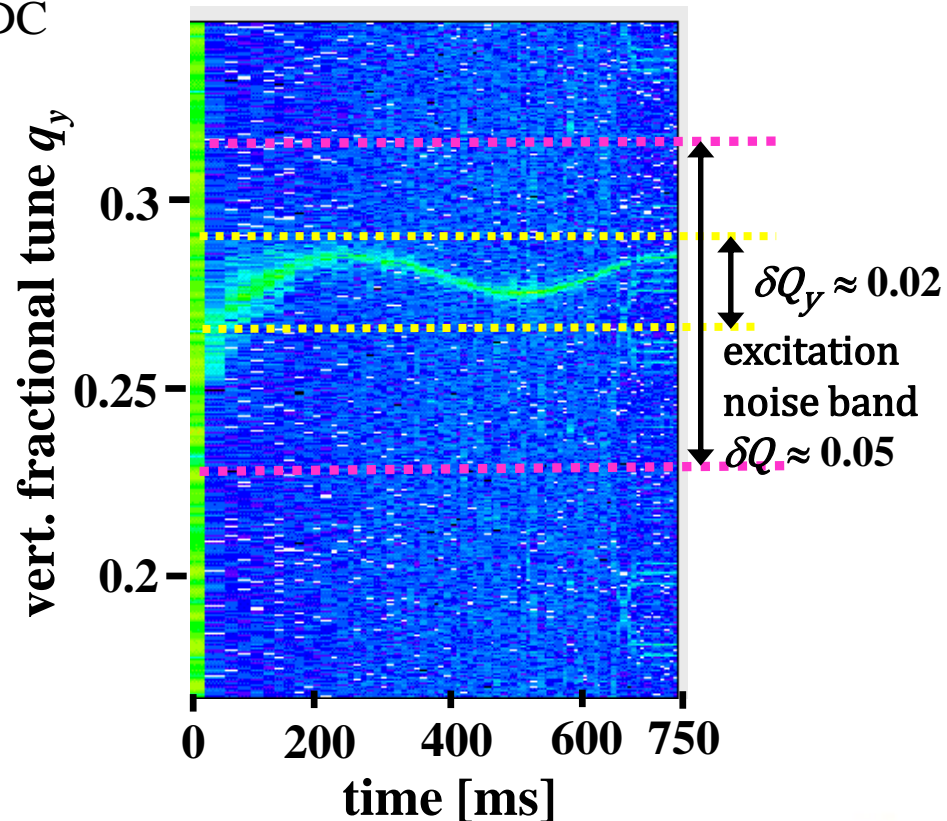


## Advantage:

Fast scan with good time resolution

**Disadvantage:** Lower precision

vertical tune versus time



# Excuse: Example of Lattice Functions

The position of dipoles and quadrupoles

- give the linear lattice functions
- at injection point  $D = 0$  is favored
- chromatic correction with sextupoles,

Definition of dispersion  $D(s)$ :

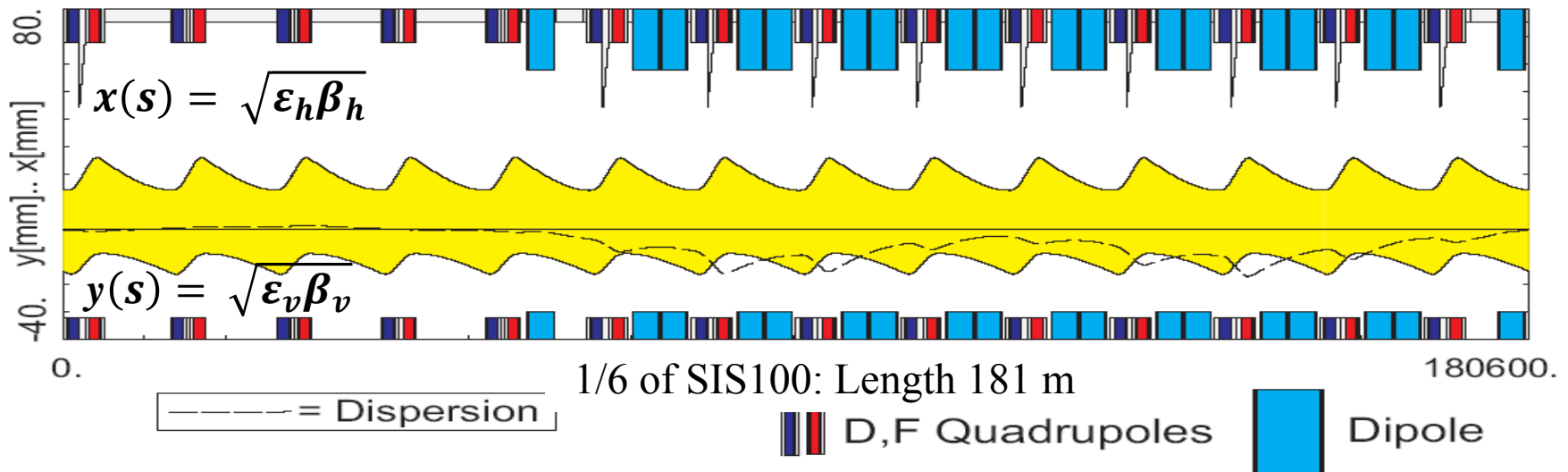
$$x_D(s) = D(s) \cdot \Delta p/p_0$$

Definition of chromaticity  $\xi$  per turn:

$$\Delta Q/Q_0 = \xi \cdot \Delta p/p_0$$

Example: GSI SIS100 ion synchrotron

Length $C$ [m]		1086
Energy $E_{kin}$ [GeV/u]		0.2 → 2
Tune $Q_{h/v}$	h/v	18.84 / 18.73
Max. dispersion $ D $ [m]		1.73
Max. $\beta$ -function $\beta_{h/v}$ [m]	h/v	19.6 / 19.6
Natural chromaticity $\xi_{h/v}$	h/v	-1.19 / -1.20
Injected emittance $\varepsilon_{h/v}$ [mm mrad]	h/v	35 / 15
Injected mom. spread $\Delta p/p_0$ [%]		0.05



# $\beta$ -Function Measurement from Bunch-by-Bunch BPM Data

Excitation of **coherent** betatron oscillations: From the position deviation  $x_{ik}$  at the BPM  $i$  and turn  $k$  the  $\beta$ -function  $\beta(s_i)$  can be evaluated.

The position reading is: ( $\hat{x}_i$  amplitude,  $\mu_i$  phase at  $i$ ,  $Q$  tune,  $s_0$  reference location)

$$x_{ik} = \hat{x}_i \cdot \cos(2\pi Qk + \mu_i) = \hat{x}_0 \cdot \sqrt{\beta(s_i) / \beta(s_0)} \cdot \cos(2\pi Qk + \mu_i)$$

→ a turn-by-turn position reading at many location (4 per unit of tune) is required.

The ratio of  $\beta$ -functions at different location:

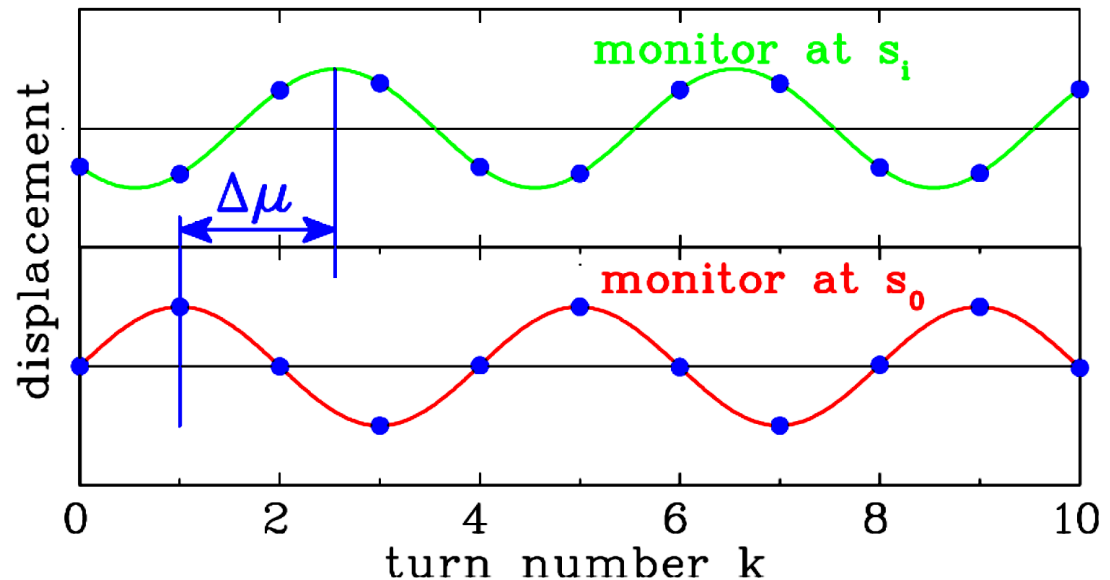
$$\frac{\beta(s_i)}{\beta(s_0)} = \left( \frac{\hat{x}_i}{\hat{x}_0} \right)^2$$

The phase advance is:

$$\Delta\mu = \mu_i - \mu_0$$

Without absolute calibration,  $\beta$ -function is more precise:

$$\Delta\mu = \int_{s_0}^{s_i} \frac{ds}{\beta(s)}$$

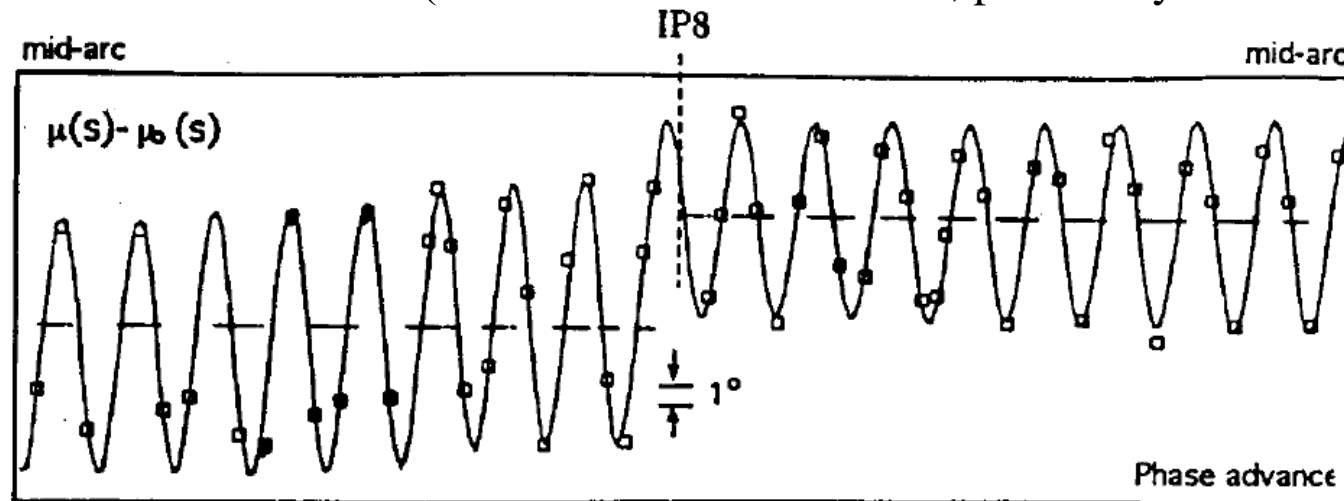


# Phase Measurement from Bunch-by-Bunch BPM Data

Excitation of **coherent** betatron oscillations: From the position deviation  $x_{ik}$  at the BPM  $i$  and turn  $k$  the betatron phase is measured.

$$\Delta\mu(s_i) = \int_{s_0}^{s_i} \frac{ds}{\beta(s)}$$

*Example:* Phase advance  $\mu(s)$  compared to the expected  $\mu_0(s)$  by optics calculation e.g. MADX at each BPM at CERN's at LEP ( $e^+ - e^-$  collider with 27 km, previously in LHC tunnel)



## Result:

From J. Borer et al, EPAC'92

- Model does not describes the reality completely, corrections required
- At interaction point IP (detector location) an additional phase shift is originated
- Alignment by correction dipoles (steerer), quadrupoles or sextupoles.

# Phase Measurement from Bunch-by-Bunch BPM Data

Excitation of **coherent** betatron oscillations: From the position deviation

$x_{ik}$  at the BPM  $i$  and turn  $k$  the beta-function can be determined. 
$$\Delta\mu(s_i) = \int_{s_0}^{s_i} \frac{ds}{\beta(s)}$$

*Example: Measured  $\beta(s)$  compared to the expected  $\beta_0(s)$  and normalized for each BPM at BNL for RHIC (proton-proton or ions circular collider with 3.8 km length)*

## Result:

- Model does not describes the reality completely
- Corrections executed
- Increase of the luminosity

## Remark:

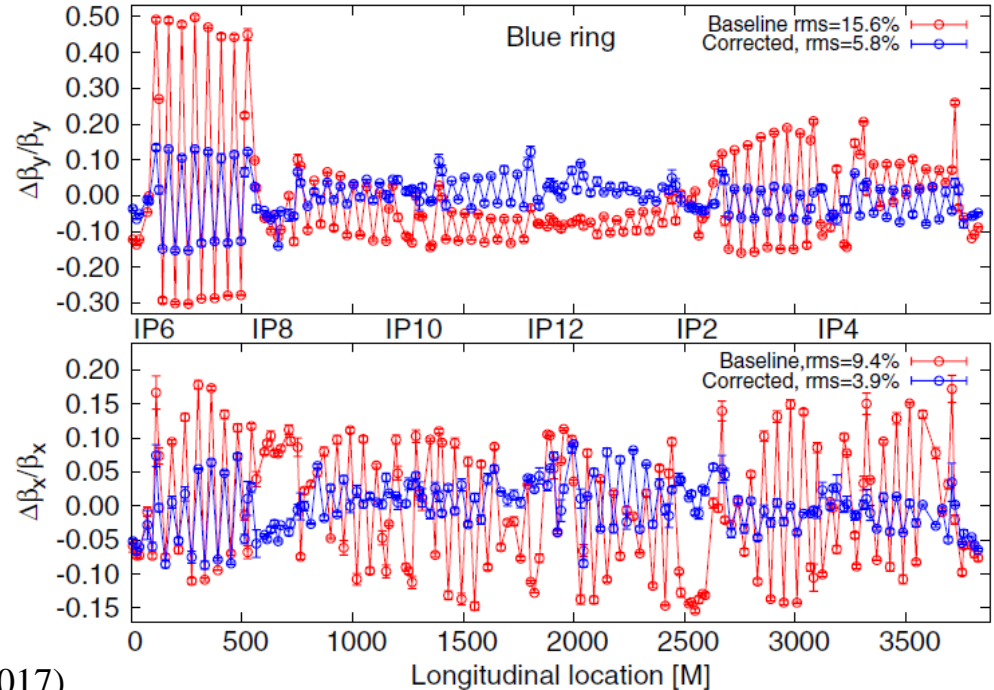
Measurement accuracy depends on

- BPM accuracy
- Numerical evaluation method

See e.g.:

R. Tomas et al., Phys. Rev. Acc. Beams **20**, 054801 (2017)

A. Wegscheider et al., Phys. Rev. Acc. Beams **20**, 111002 (2017)



From X. Shen et al.,  
Phys. Rev. Acc. Beams **16**, 111001 (2013)

# Dispersion and Chromaticity Measurement

**Dispersion  $D(s_i)$ :** Excitation of coherent betatron oscillations and change of momentum  $p$  by detuned rf-cavity:

→ Position reading at one location:  $x_i = D(s_i) \cdot \frac{\Delta p}{p}$

→ Result from plot of  $x_i$  as a function of  $\Delta p/p \Rightarrow$  slope is local dispersion  $D(s_i)$ .

**Chromaticity  $\xi$ :** Excitation of coherent betatron oscillations and change of momentum  $p$  by detuned rf-cavity:

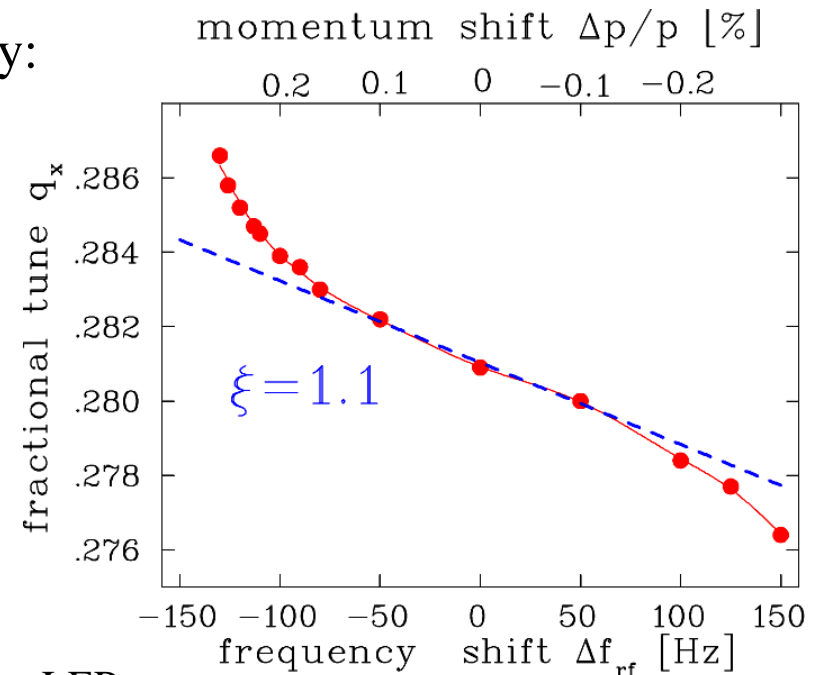
→ Tune measurement

(kick-method, BTF, noise excitation):

$$\frac{\Delta Q}{Q} = \xi \cdot \frac{\Delta p}{p}$$

Plot of  $\Delta Q/Q$  as a function of  $\Delta p/p$

$\Rightarrow$  slope is dispersion  $\xi$ .



Measurement at LEP

# Closed Orbit Feedback: Typical Noise Sources

## Beam movement:

### Short term (min to 10 ms):

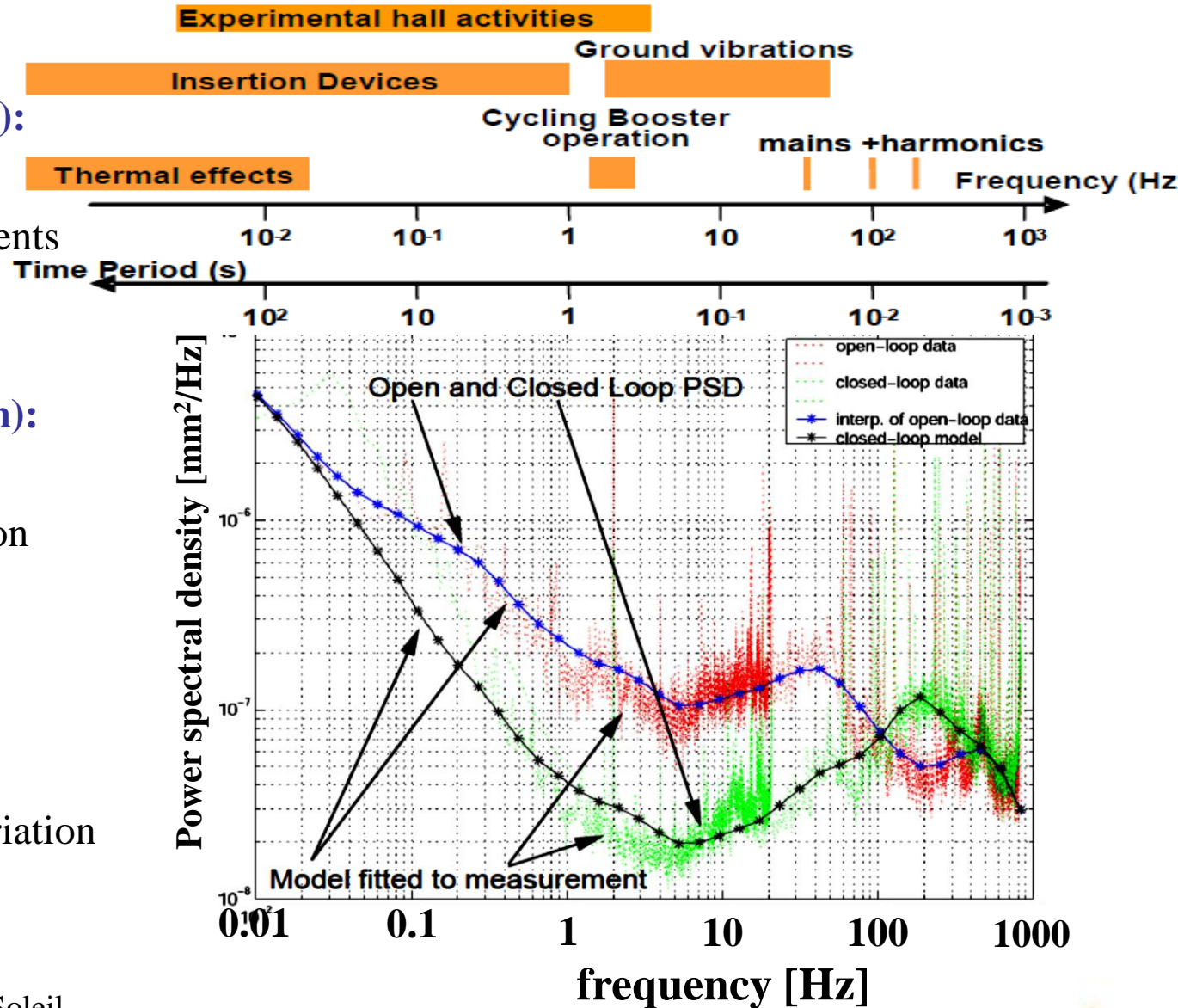
- Traffic
- Machine (crane) movements
- Water & vacuum pumps
- 50 Hz main power net

### Medium term (day to min):

- Movement of chambers due to heating by radiation
- Day-night variation
- tide, moon cycle

### Lang term (> days):

- Ground settlement
- Seasons, temperature variation

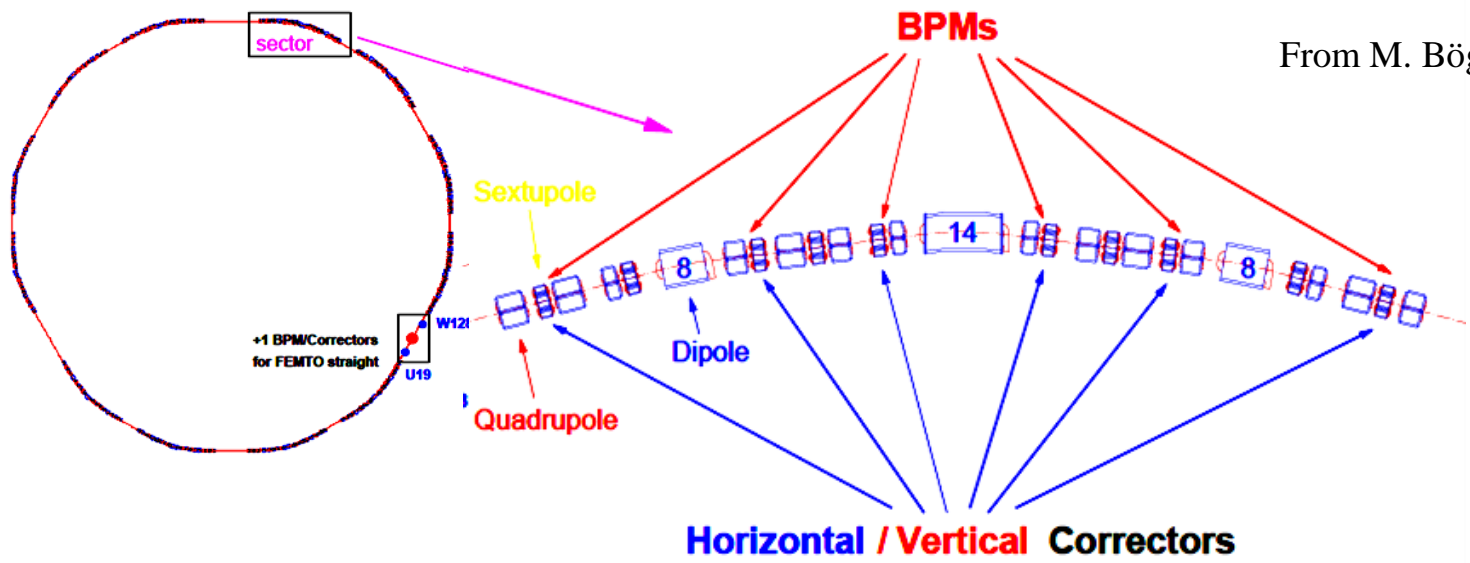




# Close Orbit Feedback: BPMs and magnetic Corrector Hardware

Orbit feedback: Synchrotron light source → spatial stability of light beam

Example from SLS-Synchrotron at Villigen, Swiss:

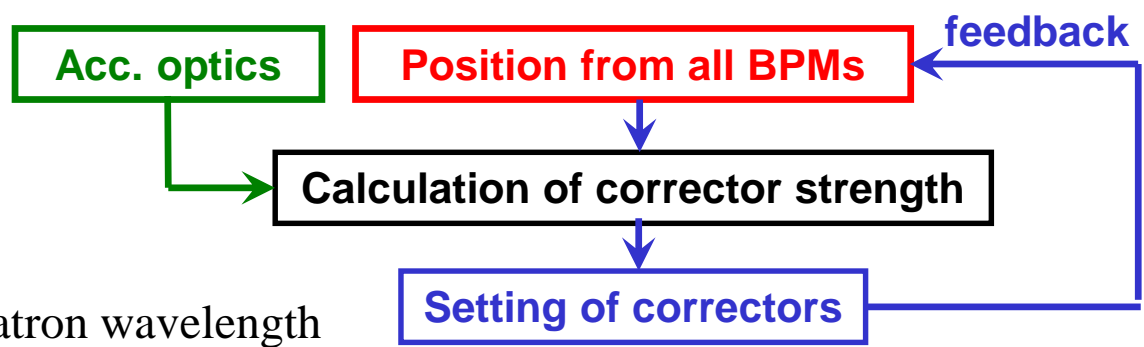


From M. Böge, PSI

## Procedure:

1. Position from all BPMs
2. Calculation of correction setting
3. Digital feedback loop

⇒ regulation time down to 10 ms  
 ⇒ Role of thumb:  $\approx 4$  BPMs per betatron wavelength

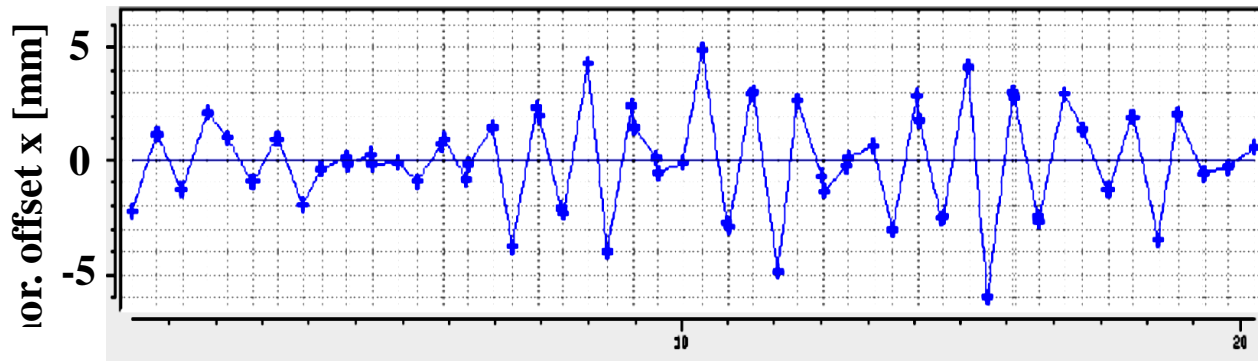


# Closed Orbit Feedback: Results

Orbit feedback: Compensating variations of different kind, goal:  $\Delta x \approx 0.1 \cdot \sigma_x$

Synchrotron light source  $\rightarrow$  spatial stability of light beam

*Example from SLS-Synchrotron at Villigen, Swiss:*

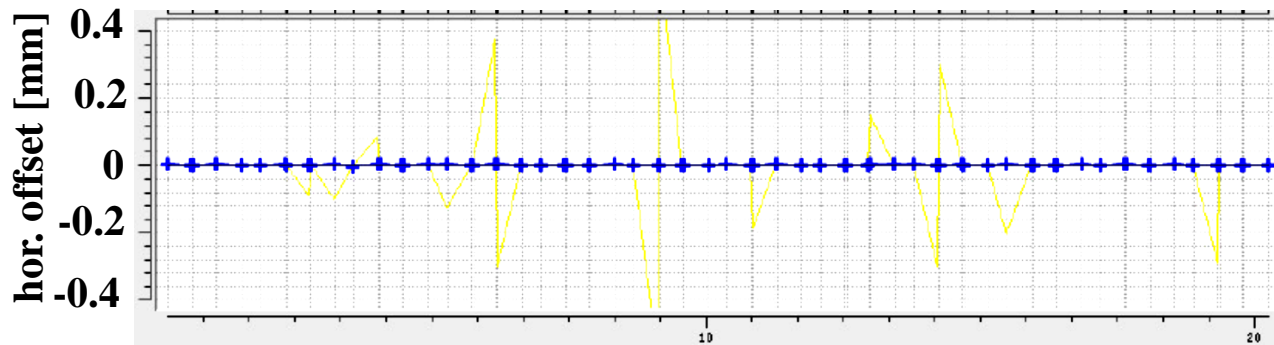


path along synchrotron [betatron phase]

**Uncorrected orbit:**

Beam offset and oscillation

here  $\langle x^2 \rangle_{rms} = 2.3 \text{ mm}$



path along synchrotron [betatron-phase]

**Corrected orbit:**

Beam dynamically corrected

here  $\langle x^2 \rangle_{rms} = 1 \mu\text{m} !$

From M. Böge, PSI

## Summary Pick-Ups for bunched Beams

The electric field is monitored for bunched beams using rf-technologies ('frequency domain'). Beside transformers they are the most often used instruments!

**Differentiated or proportional signal:** rf-bandwidth  $\leftrightarrow$  beam parameters

**Proton synchrotron:** 1 to 100 MHz, mostly 1 M $\Omega$   $\rightarrow$  proportional shape

**LINAC, e--synchrotron:** 0.1 to 3 GHz, 50  $\Omega$   $\rightarrow$  differentiated shape

**Important quantity:** transfer impedance  $Z_t(\omega, \beta)$ .

### Types of capacitive pick-ups:

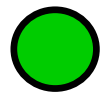
Shoe-box (p-synch.), button (p-LINAC, e--LINAC and synch.)

*Remark:* Stripline BPM as traveling wave devices are frequently used

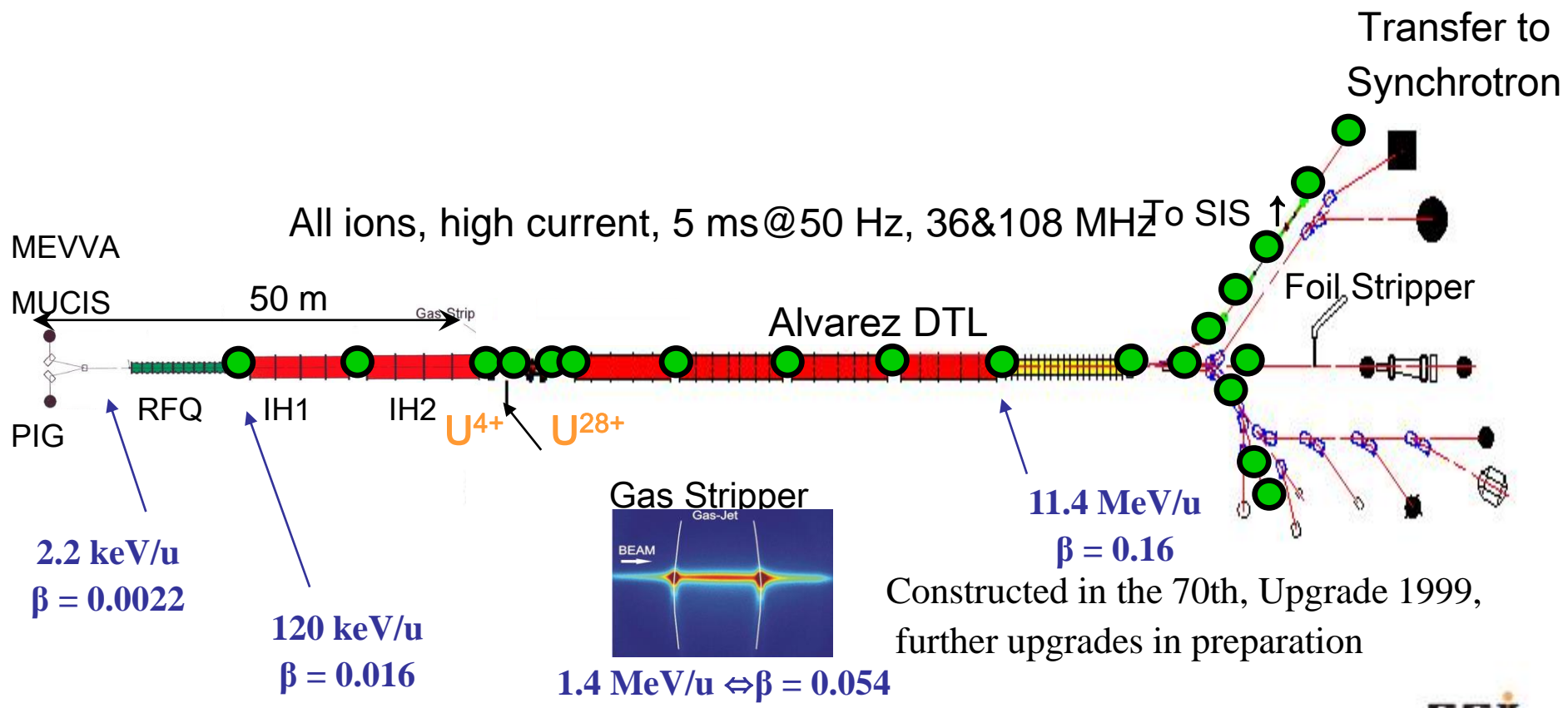
**Position reading:** difference signal of four pick-up plates (BPM):

- **Non-intercepting** reading of center-of-mass  $\rightarrow$  online measurement and control
  - slow reading*  $\rightarrow$  closed orbit, *fast bunch-by-bunch*  $\rightarrow$  trajectory
- Excitation of *coherent betatron oscillations* and response measurement
  - excitation by short kick, white noise or sine-wave (BTF)
  - $\rightarrow$  tune  $q$ , chromaticity  $\xi$ , dispersion  $D$  etc.

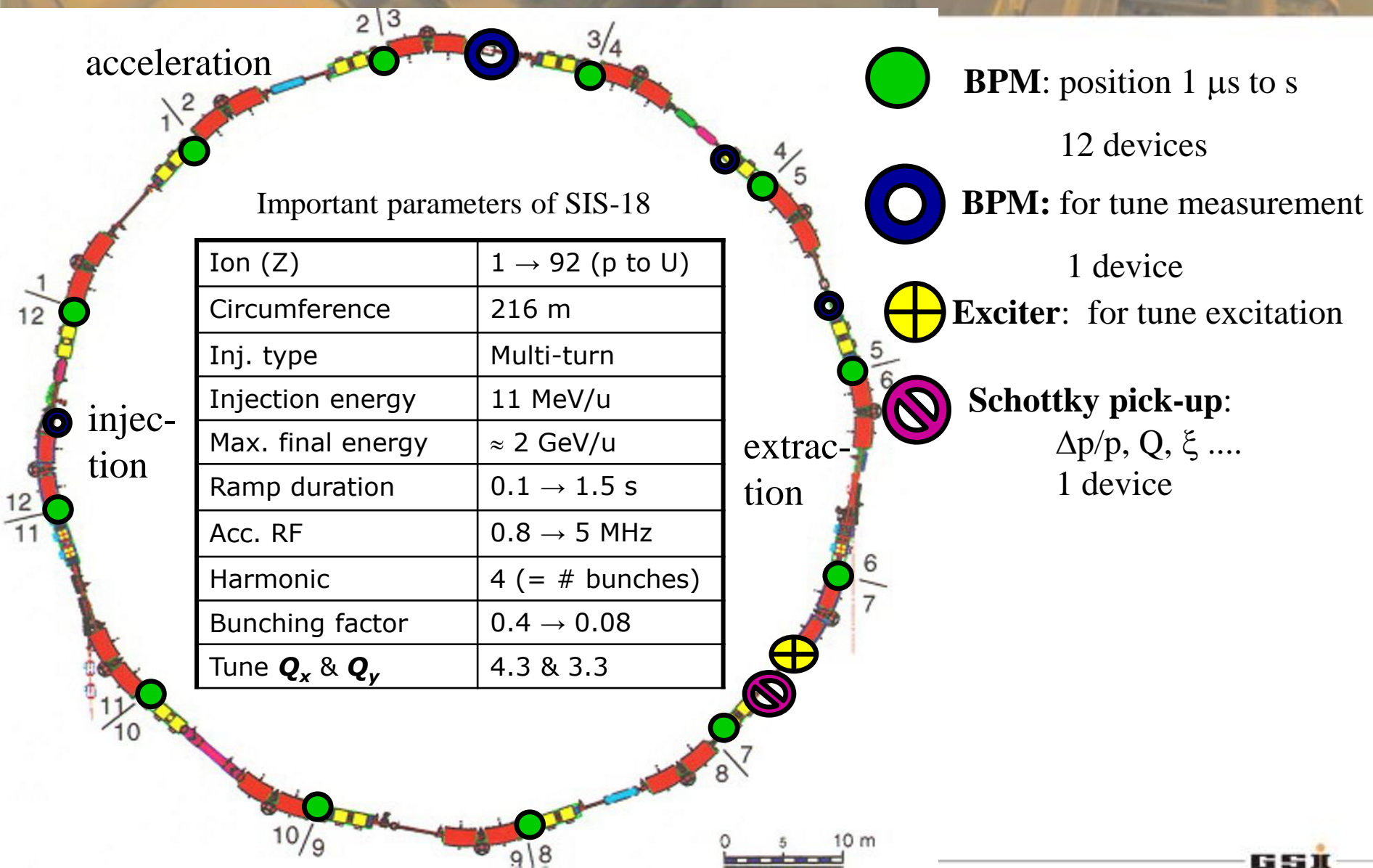
# Appendix GSI Ion LINAC: Position and mean beam energy Meas.



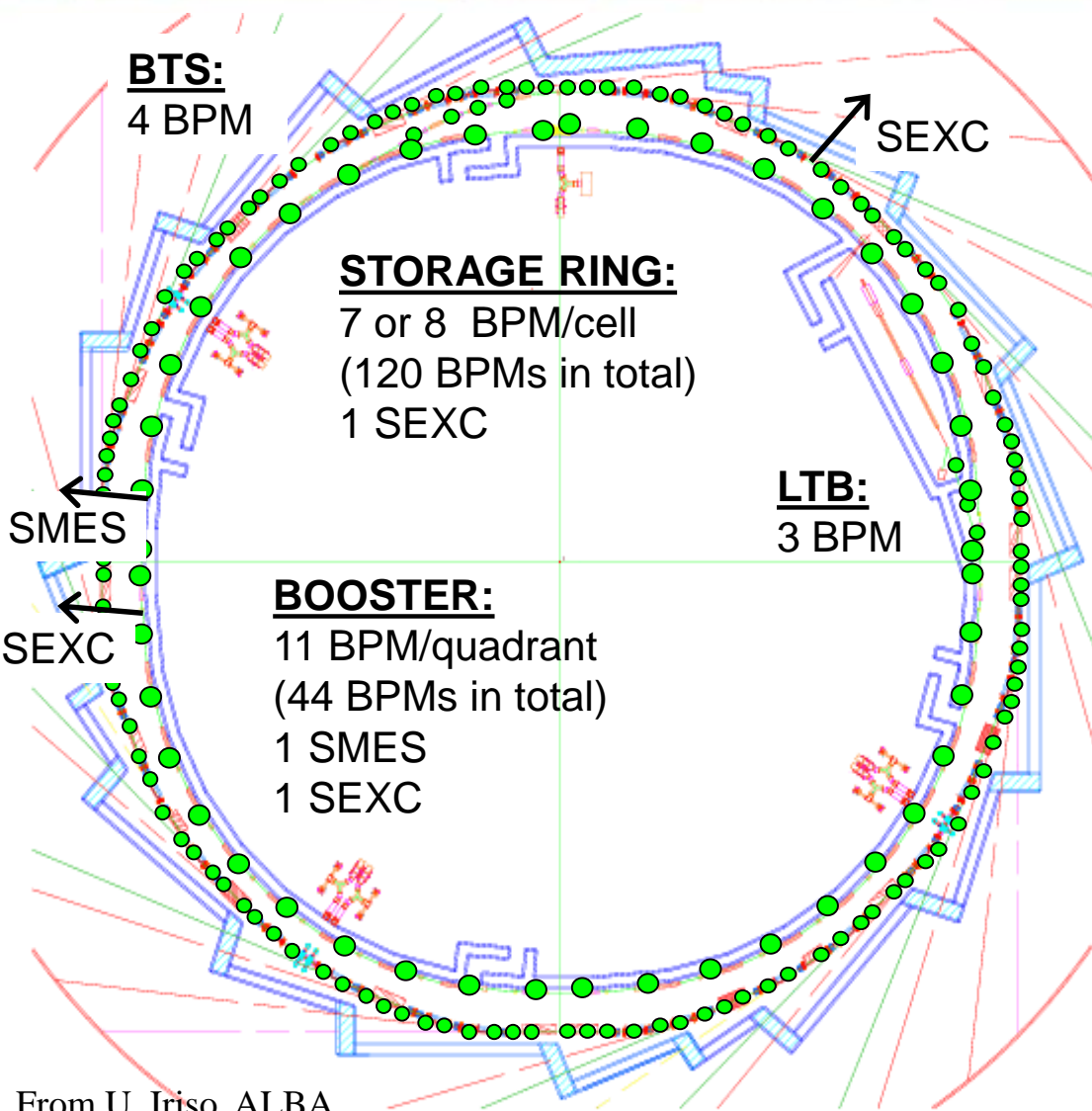
**BPM:** Capacitive type, for position and time-of-flight  
total 25 device



# Appendix GSI Ion Synchrotron: Position, tune ect. Measurement



# Appendix: Synchrotron Light F.ALBA: 'Position, tune ect. Meas.



## Beam position:

Center of mass

- Many locations!
- Frequent operating tool
- For position stabilization  
i.e. closed orbit feedback

## Abbreviation:

Meas. Stripline → SMES ↑

Exc. Stripline → SEXC

Button BPMs → BPM ●

From U. Iriso, ALBA