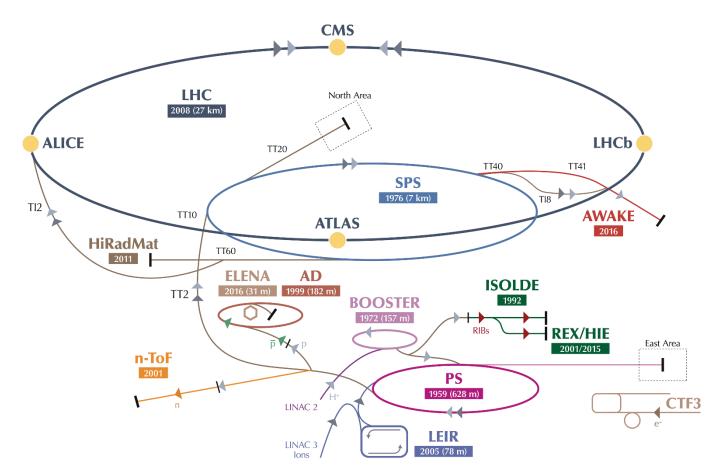




JUAS 2018, Archamps, France

Tutorial on Gas Flow, Conductance, Pressure Profiles

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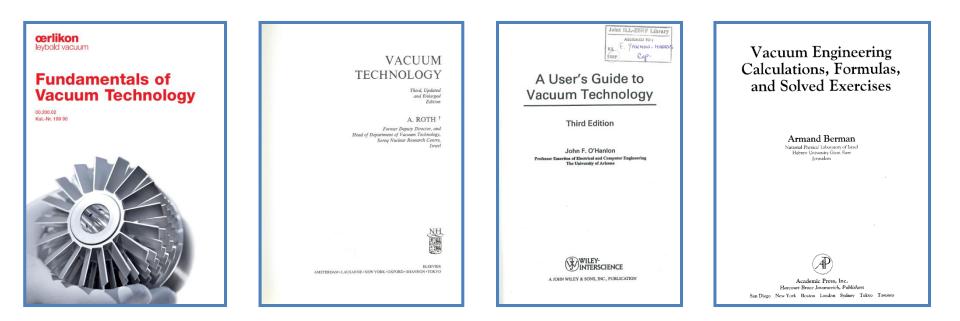


Content:

- •Concepts of gas flow, conductance, pressure profile as relevant to the design of the vacuum system of modern accelerators;
- A quick definition of the terms involved;
- •Some computational models and algorithms: analytical vs numerical;
- Simple exercises (if times allows)
- Summary;

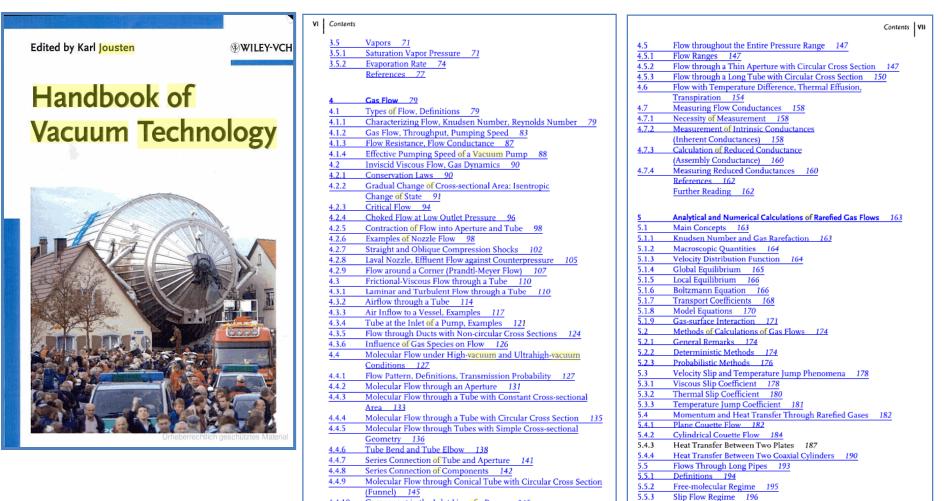
Sources: "[1] Fundamentals of Vacuum Technology", Oerlikon-Leybold (*); [2] "Vacuum Technology, A. Roth, Elsevier; [3] "A User's Guide to Vacuum Technology", J.F. O'Hanlon, Wiley-Interscience; [4] "Vacuum Engineering Calculations, Formulas, and Solved Exercises", A. Berman,

Academic Press;



(*) Not endorsing products of any kind or brand

Sources: [5] "Handbook of Vacuum Technology", K. Jousten ed., Wiley-Vch, 1002 p.

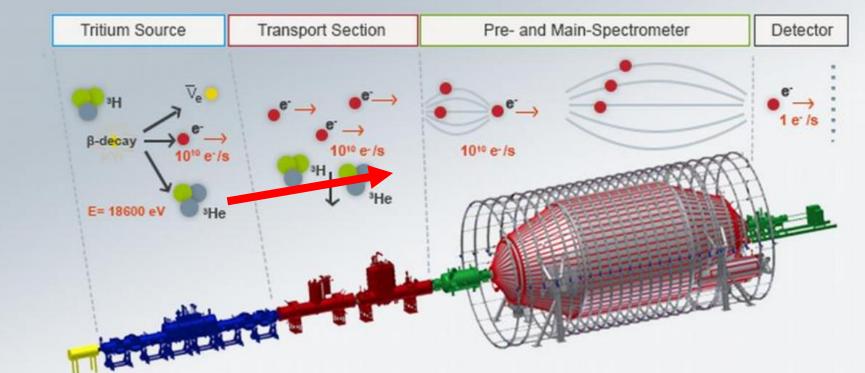


4.4.10 Component in the Inlet Line of a Pump 146

KATRIN neutrino mass experiment: a <u>very sophisticated</u> vacuum system (cryogenic system with eguiding solenoids integrated into the cryostats, plus turbo pumps to decrease the source-todetector transmission probability, and more...); Fully analysed, mand modelled via Test-Particle

Monte Carlo (TPMC) simulations

Deconstruction: KATRIN's odvssev



Tritinium decays, releasing an electron and an antielectron-neutrino. While the neutrino escapes undetected, the eletron starts ist journey to the detector.

Electrons are guided towards the sprectrometer by magnetic fields. Tritium has to be pumped out to provide tritium free spectrometers. The electron energy is analyzed by applying an electrostatic retarding potential. Electrons are only transmitted if their kinetic energy is sufficiently high.

At the end of their journey, the electrons are counted at the detector. Their rate varies with the spectrometer potential and hence gives an integrated β-spectrum.









Units and Definitions

Unit	N · m ⁻² , Pa ²⁾	mbar	bar	Torr
1 N · m ^{−2} (= 1 Pa)	1	1 · 10 ⁻²	1 · 10 ^{–5} 1 · 10 ^{–3}	7.5 · 10 ^{−3}
1 mbar	100	1	1 · 10 ⁻³	0.75
1 bar	1 · 10 ⁵	1 · 103	1	750
1 Torr ³⁾	133	1.33	1.33 · 10 ⁻³	1
 The torr is included in statutory units N · m⁻² mercury column (mm atmosphere absolute) 	, mbar and bar. In fu	ture the pressu chnical atmosph	re units torr, mm v ere (at), physicala	water column, mm atmosphere (atm),

Table I: Permissible pressure units including the torr 1) and its conversion

Abbrev.	Gas	$C^* = \lambda \cdot p$ [cm · mbar]
H ₂	Hydrogen	12.00 · 10 ⁻³
He	Helium	18.00 · 10 ⁻³
Ne	Neon	12.30 · 10 ⁻³
Ar	Argon	6.40 · 10 ⁻³
Kr	Krypton	4.80 · 10 ⁻³
Xe	Xenon	3.60 · 10 ⁻³
Hg	Mercury	3.05 · 10 ⁻³
02	Oxygen	6.50 · 10 ⁻³
N ₂	Nitrogen	6.10 · 10 ⁻³
HĈI	Hydrochloric acid	4.35 · 10 ^{−3}
CO_2	Carbon dioxide	3.95 · 10 ⁻³
H₂Ó	Water vapor	3.95 · 10 ⁻³
NH ₃	Ammonia	4.60 · 10 ⁻³
C ₂ H ₅ OH	Ethanol	2.10 · 10 ⁻³
Cĺ ₂	Chlorine	3.05 · 10 ⁻³
Air	Air	6.67 · 10 ⁻³

Table III: Mean free path I

Values of the product c* of the mean free path λ (and pressure p for various gases at 20 °C (see also Fig. 9.1)

1↓=→	mbar	Pa	dyn · cm ⁻²	atm	Torr	inch	Micron	cm	kp · cm ^{−2}	lb · in ^{−2}	lb · ft ^{−2}
		(N/m ³)	(µbar)	(phys.)	(mm Hg)	Hg	(μ)	H₂O	(at tech.)	(psi)	
mbar	1	10 ²	10 ³	9.87 · 10 ⁻⁴	0.75	2.953 · 10 ⁻²	7.5 · 10 ²	1.02	1.02 · 10 ^{−3}	1.45 · 10 ⁻²	2.089
Pa	10 ⁻²	1	10	9.87 · 10 ⁻⁶	7.5 · 10 ^{−3}	2.953 · 10 ⁻⁴	7.5	1.02 · 10 ⁻²	1.02 · 10 ^{−5}	1.45 · 10 ⁻⁴	2.089 · 10 ⁻²
μbar	10 ⁻³	0.1	1	9.87 · 10 ⁻⁷	7.5 · 10 ⁻⁴	2.953 · 10 ⁻⁵	7.5 · 10 ⁻¹	1.02 · 10 ⁻³	1.02 · 10 ⁻⁶	1.45 · 10 ⁻⁵	2.089 · 10 ⁻³
atm	1013	1.01 · 10 ⁵	1.01 · 10 ⁶	1	760	29.92	7.6 · 10 ⁵	1.03 · 10 ³	1.033	14.697	2116.4
Torr	1.33	1.33 · 10 ²	1.33 · 10 ³	1.316 · 10 ⁻³	1	3.937 · 10 ⁻²	10 ³	1.3595	1.36 · 10 ^{−3}	1.934 · 10 ⁻²	2.7847
in Hg	33.86	33.9 · 10 ²	33.9 · 10 ³	3.342 · 10 ⁻²	25.4	1	2.54 · 10 ⁴	34.53	3.453 · 10 ⁻²	0.48115	70.731
μ	1.33 · 10 ⁻³	1.33 · 10 ⁻¹	1.333	1.316 · 10 ⁻⁶	10 ⁻³	3.937 · 10 ⁻⁵	1	1.36 · 10 ⁻³	1.36 · 10 ⁻⁶	1.934 · 10 ⁻⁵	2.785 · 10 ⁻³
cm H ₂ O	0.9807	98.07	980.7	9.678 · 10 ⁻⁴	0.7356	2.896 · 10 ⁻²	7.36 · 10 ²	1	10 ⁻³	1.422 · 10 ⁻²	2.0483
at	9.81 · 10 ²	9.81 · 10 ⁴	9.81 · 10 ⁵	0.968	7.36 · 10 ²	28.96	7.36 · 10 ⁵	103	1	14.22	2048.3
psi	68.95	$68.95 \cdot 10^2$	68.95 · 10 ³	6.804 · 10 ⁻²	51.71	2.036	51.71 · 10 ³	70.31	7.03 · 10 ⁻²	1	1.44 · 10 ²
lb · ft ^{−2}	0.4788	47.88	478.8	4.725 · 10 ⁻⁴	0. 3591	1.414 · 10 ⁻²	359.1	0.488	4.88 · 10 ⁻⁴	6.94 · 10 ⁻³	1

Normal conditions: 0 °C and sea level, i.e. p = 1013 mbar = 760 mm Hg = 760 torr = 1 atm

in Hg = inches of mercury; 1 mtorr (millitorr) = 10^{-3} torr = 1 μ (micron ... μ m Hg column)

Pounds per square inch = lb · in 2 = lb / sqin = psi (psig = psi gauge ... pressure above atmospheric, pressure gauge reading; psia = psi absolute ... absolute pressure)

Pounds per square foot = lb / sqft = lb / ft²; kgf/sqcm² = kg force per square cm = kp / cm² = at; analogously also: lbf / squin = psi

1 dyn · cm⁻² (cgs) = 1 µbar (microbar) = 1 barye; 1 bar = 0.1 Mpa; 1 cm water column (cm water column = g / cm² at 4 °C) = 1 Ger (Geryk)

atm ... physical atmosphere - at ... technical atmosphere; 100 - (x mbar / 10.13) = y % vacuum

Table II: Conversion of pressure units

Units and Definitions [2]

•Without bothering Democritus, Aristoteles, Pascal, Torricelli et al... a <u>modern</u> definition of "vacuum" is the following (American Vacuum Society, 1958):

"... a given space or volume filled with gas at pressures below atmospheric pressure"

•Keeping this in mind, the following curve [2] defines the <u>molecular density</u> vs <u>pressure</u> and the <u>mean free path (MFP)</u>, a very important quantity:

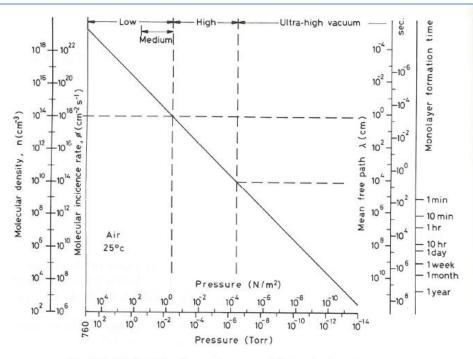
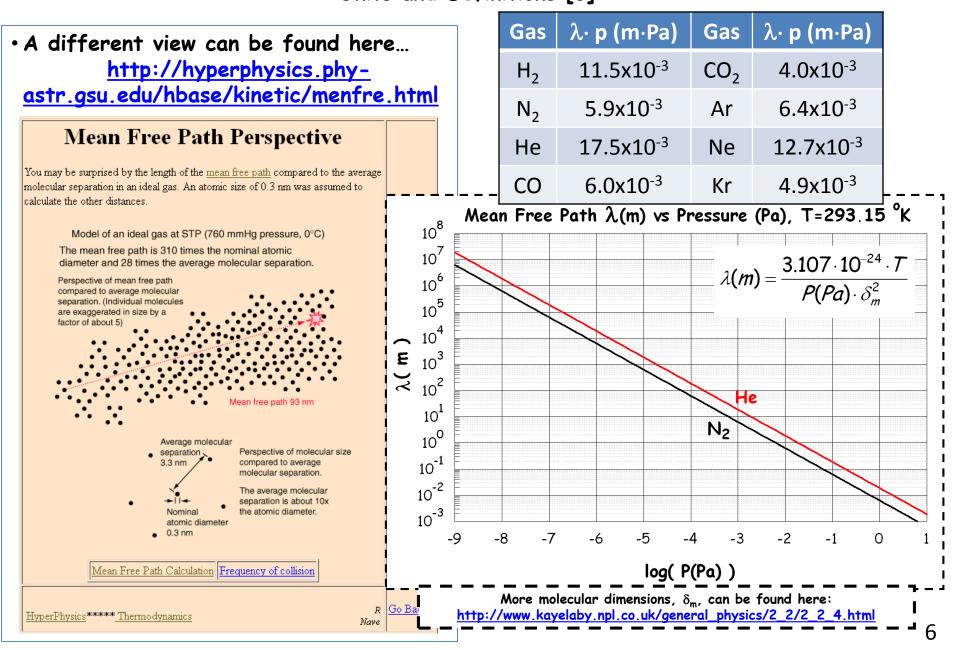


Fig. 1.1 Relationship of several concepts defining the degree of vacuum.

<u>Mean-free path</u>: average distance travelled by a molecule before hitting another one (ternary, and higher-order, collisions are negligible) The importance of obtaining low a pressure, in accelerators, is evident: reduce collisions between the particle beams and the residual gas; - increase beam lifetime: - reduce losses: - reduce activation of components; - reduce doses to personnel; - decrease number of injection cycles; improve beam up-time statistics; more.

Tutorial on Gas Flow, Conductance, Pressure Profiles Units and Definitions [3]



Tutorial on Gas Flow, Conductance, Pressure Profiles Units and Definitions [4]

Definition of "flow regime"

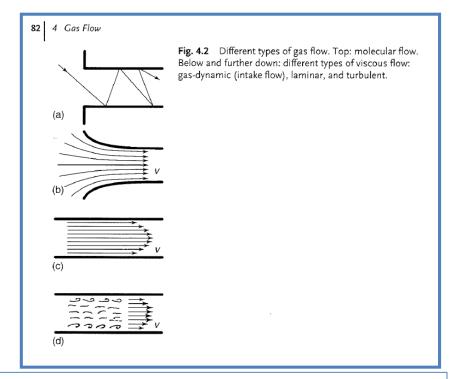
The so-called "Knudsen number" is defined as this:

$$Kn = \frac{\lambda}{D}$$

And the different flow (pressure) regimes are identified as follows:

FREE MOLECULAR FLOW:Kn >1TRANSITIONAL FLOW:0.01CONTINUUM (VISCOUS) FLOW:Kn0.01

Practically all accelerators work in <u>the</u> <u>free-molecular regime</u> i.e. in a condition where the MFP λ is bigger than the "typical" dimension of the vacuum chamber (e.g.its diameter), and therefore molecular collisions can be neglected.



IMPORTANT: in molecular flow regime, the absence of collisions between molecules translates into the fact that high-vacuum pumps DO NOT "SUCK" GASES they simply generate some probability s that once a molecule enters into the pump it is permanently removed from the system. can be identified as the equivalent S

sticking coefficient.

Units and Definitions [5]

Definition of "<u>vacuum ranges</u>"

• Linked to the Knudsen number and the flow regimes, historically defined as in table

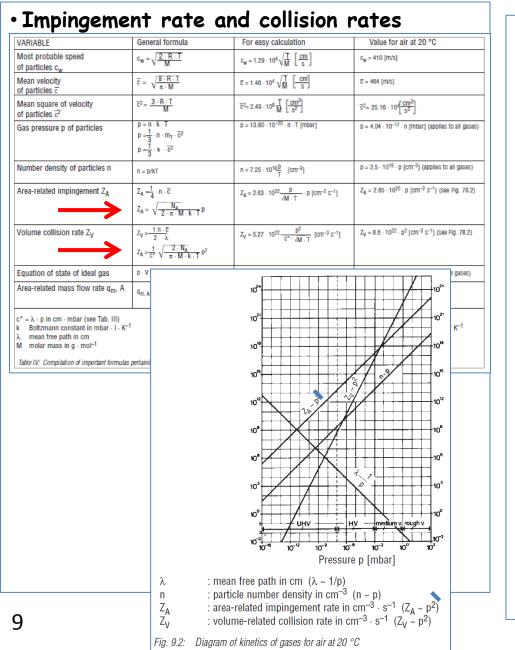
elow [1];			Rough vacuum	Medium vacuum	High vacuum	Ultrahigh vacuum
	Pressure Particle number density Mean free path Impingement rate Volrelated collision rate Monolayer time Type of gas flow	p [mbar] n [cm ⁻³] λ [cm] Z _a [cm ⁻² · s ⁻¹] Z _V [cm ⁻³ · s ⁻¹] τ [s]	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$10^{-3} - 10^{-7}$ $10^{13} - 10^{9}$ $10 - 10^{5}$ $10^{17} - 10^{13}$ $10^{17} - 10^{9}$ $10^{-2} - 100$ Molecular flow	< 10 ⁻⁷ < 10 ⁹ > 10 ⁵ < 10 ¹³ < 10 ⁹ > 100 Molecular flow
	Other special features		Convection dependent on pressure	Significant change in thermal conductivity of a gas	Significant reduction- in volume related collision rate	Particles on the surfaces dominate to a great extend in relation to particles in gaseous space

•With the invention of very low-outgassing materials and treatments (e.g. NEGcoating), "Ultrahigh vacuum" (UHV) is sometimes split up into "UHV" and "XHV" (eXtreme High Vacuum) regimes

	Classification of vacuum ranges [8].							
	Vacuum	Pressure Units						
	Ranges	Pa		mbar				
		min	max	min	max			
	Low (LV)	3.3×10^{3}	1.0×10^{5}	3.3×10	1.0×10^{3}			
1	Medium (MV)	1.0×10^{-1}	3.3×10^{3}	1.0×10^{-3}	3.3×10			
	High (HV)	1.0×10^{-4}	1.0×10^{-1}	1.0×10^{-6}	1.0×10^{-3}			
(Def N) Mensuendt	Very High (VHV)	1.0×10^{-7}	1.0×10^{-4}	1.0×10^{-9}	1.0×10^{-6}			
•(Ref. N. Marquardt, 🔤	Ultra-High (UHV)	1.0×10^{-10}	1.0×10^{-7}	1.0×10^{-12}	1.0×10^{-9}			
CERN CAS 1999)	Extreme	\leq 1.0 $ imes$ 10 ⁻¹⁰		$\leq 1.0 \times 10^{-12}$				
	Ultra-High (XHV)							

8

Tutorial on Gas Flow, Conductance, Pressure Profiles Impingement and Collision rates; Ideal Gas Law



•The <u>ideal gas law</u> states that the pressure P of a diluted gas is given by $PV = \frac{m}{M}RT = n_M RT = n_M N_A k_B T$... where: V = volume, m^3 ; m = mass of gas, kg M = molecular mass, kg/mole T = absolute temperature, °K R = gas constant = 8.31451 J/mol/K n_{M} = number of moles N_A = Avogadro's number = 6.022E+23 molecules/mole $k_{\rm B}$ = Boltzmann's constant = 1.381E-23 J/K

 Deviation from this law are taken care of by introducing higher-order terms, the so called <u>virial expansion</u>,...

 $PV = RT(1 + BP + CP^2 + ...)$... which are not discussed here.

Volumetric Flow Rate – Throughput – Basic Equations – Conductance

How does all this translates into "accelerator vacuum"?

•Let's imagine the simplest vacuum sistem, a straight tube with constant cross-section <u>connecting two large</u> <u>volumes</u>, P₁>P₂

 $Q = P \cdot dV/dt$

Q, which in the SI has the units of

 $[Pa \cdot m^3/s] \rightarrow [N \cdot m /s] = [J/s] = [W]$

... is called the <u>throughput</u>. Therefore the throughput is <u>the power carried by</u> <u>a gas flowing out (or in) of the volume V</u> <u>at a rate of dV/dt and pressure P.</u>

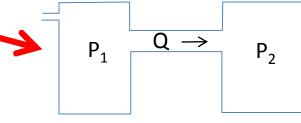
dV/dt is also called "<u>volumetric</u> <u>flow rate</u>", and when applied to the inlet of a pump, it is called "<u>pumping</u> <u>speed</u>".

Therefore, we can also write a first basic equation of vacuum technology

 $Q = P \cdot S$

• Having defined the throughput, we move now to the concept of <u>conductance</u>, C:

Suppose we have two volumes V_1 and V_2 , at pressures $P_1 > P_2$ respectively, connected via a tube



...we can define a second <u>basic</u> <u>equation</u> of vacuum technology

 $Q = C \cdot (P_1 - P_2) = C \cdot \Delta P$

... which, making an electrical analogy...

I= V / R

... gives an obvious interpretation of C as the reciprocal of a resistance to flow.

The higher the conductance the
more "current" (throughput) runs
through the system.10

Kinetic Theory of Gases

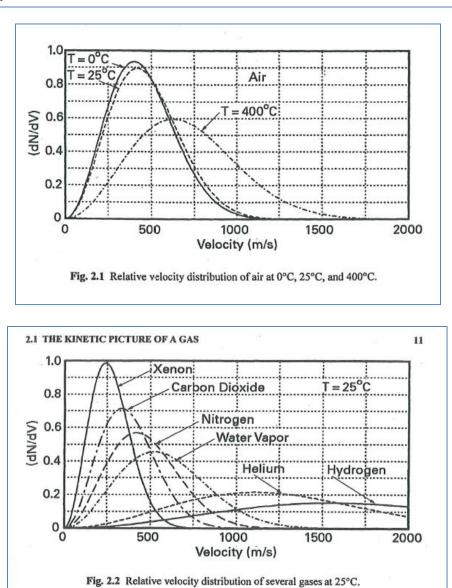
How can conductances be calculated? How does the dimension, shape, length, etc... of a vacuum component define its conductance?

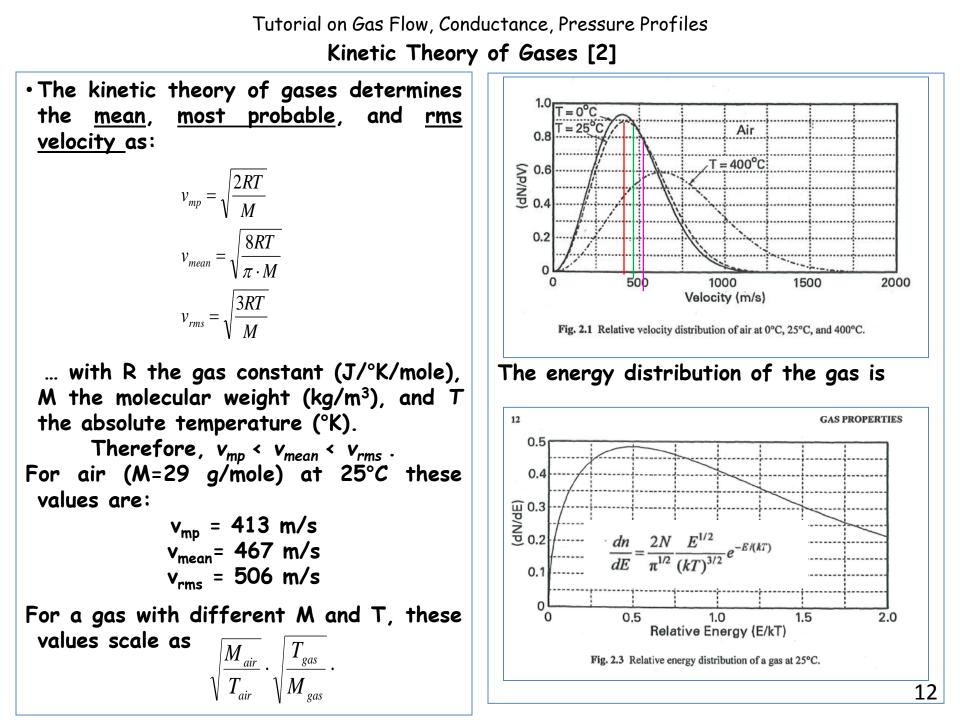
- •We need to recall some concepts of kinetic theory of gases:
- The Maxwell-Boltzmann velocity distribution defines an ensemble of N molecules of given mass m and temperature T as

$$\frac{dn}{dv} = \frac{2N}{\pi^{1/2}} \left(\frac{m}{2kT}\right)^{3/2} v^2 e^{-m \cdot v^2 / (2 \cdot k_B \cdot T)}$$

... with n the molecular density, and k_b as before.

• The shape of this distribution for air at different temperatures, and for different gases at 25°C are shown on the right:





Transmission probability

•Within the kinetic theory of gases, it can be shown that the volumetric flow rate passing through an infinitely thin hole of surface area A between two volumes is given by $q = A \cdot \frac{v_{mean}}{r} \Delta P$

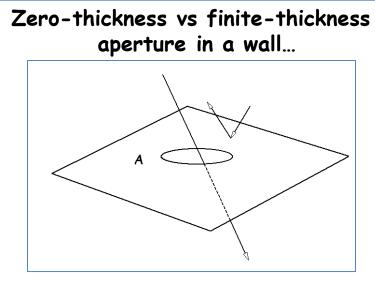
... and by the analogy with the second basic equation we get that the <u>conductance c</u> of this thin hole is

For holes which are not of zerothickness, a "reduction" factor k, 0 < k < 1, can be defined. K is called <u>transmission probability</u>, and can be visualized as the effect of the "side wall" generated by the thickness.

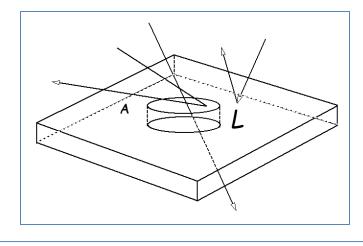
It depends in a complicated way from the shape of the hole.

So, in general, for a hole of area A across a wall of thickness L

$$c(A,L) = A \cdot \frac{v_{mean}}{4} \cdot k(A,L)$$



... the transmission probability decreases as L increases...



 $c = A \cdot \frac{v_{mean}}{\Delta}$

Transmission probability [2]

- •Only for few simple cross-sections of the hole, an analytic expression of k(A,L) exists.
- For arbitrary shapes, numerical integration of an integro-differential equation must be carried out, and no analytical solution exists:

7. Clausing's investigation of the transmission probability of a tube

Clausing 25-34 calculated the probability W for a tube of circular cross-section

$$W = \int_{0}^{L} W_{SR}(x) \cdot w(x) dx + W_{ss}(L)$$
(27)

where w(x) is given by an integral equation

$$w(x) = \int_{0}^{L} W_{RR}(\xi - x) d\xi . w(\xi) + W_{RS}(L - x)$$
(28)

down w(x) in the case of a circular tube:

$$w(x) = \frac{1}{4R} \int_{0}^{L} \left\{ 2 + \frac{(\xi - x)^{3}}{[(\xi - x)^{2} + 4R^{2}]^{\frac{1}{2}}} - \frac{3(\xi - x)}{[(\xi - x)^{2} + 4R^{2}]^{\frac{1}{2}}} \right\}$$

$$w(\xi) d\xi + \frac{1}{4R} \left\{ [(\overline{L - x)^{2} + 4R^{2}}]^{\frac{1}{2}} + \frac{(L - x)^{2}}{[(L - x)^{2} + 4R^{2}]^{\frac{1}{2}}} - 2(L - x) \right\}$$
(29)

(ref. W. Steckelmacher, Vacuum 16 (1966) p561-584)

Where W_{SR} , W_{SS} , W_{RR} and W_{RS} are appropriate functions of R and relate to probabilities of the molecular passage and emittance of molecules (assuming a cosine law of emission) from different parts of the tube wall. Clausing also showed that the function w(x) was related to the impact density g(x) for molecules impinging on the walls of the tube, where x is measured along the tube length. Defining the relative impact

density
$$h(x) = \frac{g(x)}{N_0}$$
 he proved the identity

$$h(x) \equiv w(L-x) \tag{30}$$

This proof depends on the principle of detailed balancing according to which for each direction and velocity the number of emitted molecules is equal to the number adsorbed (see also Clausing²⁷).

In trying to solve the integral equation Clausing³²⁻³⁴ assumes that for $\frac{R}{r}$ large (≥ 1) a good solution is given by

$$v(x) = \alpha + \frac{1 - 2\alpha}{L} \cdot x \tag{31}$$

with α =const. Substitution of this in the integral actually gave an expression for α which may be written in the form:

$$\alpha = \frac{\left[u(u^{2}+1)^{\frac{1}{2}} - u^{2}\right] - \left[v(v^{2}+1)^{\frac{1}{2}} - v^{2}\right]}{\frac{u(2v^{2}+1) - v}{(v^{2}+1)^{\frac{1}{2}}} - \frac{v(2u^{2}+1) - u}{(u^{2}+1)^{\frac{1}{2}}} = \alpha \left(\frac{R}{L}, \frac{x}{L}\right)$$
(32)

where
$$u = (L-x)/2R$$
 and $v = x/2R$, ie $u = (L/R) - v$ (34)

He then selected α such that $W = \frac{\sigma R}{3L}$ for long tubes, is assuming the Knudsen formula for long tubes. He showed that a good approximation was obtained for short tubes when $L \leq 4R$ by taking

$$\alpha = \frac{\sqrt{L^2 + 4R^2 - L}}{4R^2}$$
(35), and when $L > 4R$, $\alpha = \alpha \left(\frac{R}{L}, \frac{x}{L}\right)$ (35)
$$2R + \frac{4R^2}{\sqrt{L^2 + 4R^2}}$$
given by the above formula for $\alpha \left(\frac{R}{L}, \frac{x}{L}\right)$ but with

given by the above formula for $\alpha\left(\frac{R}{L},\frac{\alpha}{L}\right)$ but with

$$x/L = 2R\sqrt{7}/(3L + 2R\sqrt{7})$$
 ie $u = \frac{L\sqrt{7}}{3L + 2R\sqrt{7}}$ (36)

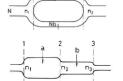
With this choice (he points out, it is one of many), for very small R/L

$$\alpha \rightarrow \frac{4R}{3L}$$
 so that $W \rightarrow \frac{8R}{3L}$.

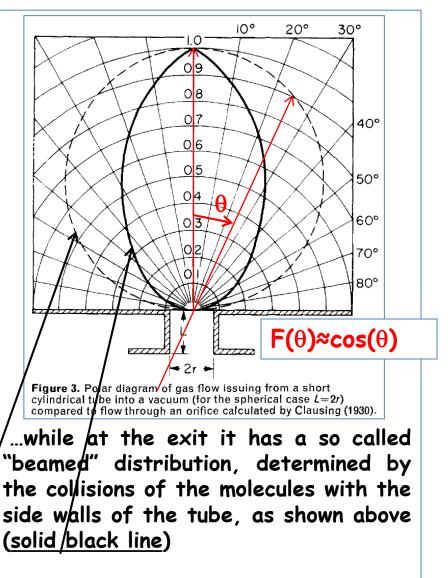
With these approximations Clausing then calculated W for a range of values of L/R, which he tabulated, and these Clausing probability factors formed the basis for flow calculations in tubes for more than 20 years.

Sum of Conductances

- Keeping in mind the interpretation of the <u>conductance as the reciprocal of a</u> <u>resistance</u> in an electric circuit, we may be tempted to use "summation rules" similar to those used for series and parallel connection of two resistors.
 It turns out that these rules are not so
- far off, they give meaningful results provided some "correction factors" are introduced
- $C = C_1 + C_2 \text{ parallel}$ $\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} \text{ series} =$



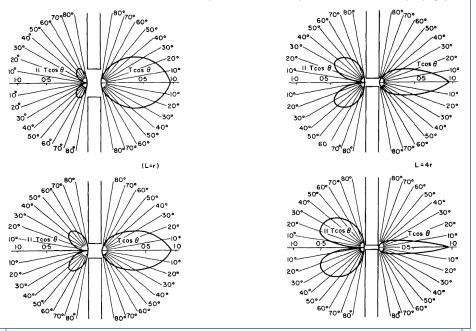
- and they can be extended to more elements by adding them up.
- The correction factor takes into account also the fact that the flow of the gas as it enters the tube "develops" a varying angular distribution as it moves along it, even for a constant section.
- At the entrance, the gas crosses the aperture with a "cosine distribution"



• As the length of the tube increases...

Molecular Beaming Effect

... so does the beaming, and the forward- and backward-emitted molecules become more and more skewed, as shown here...



W Steckelmacher : The molecular flow conductance for systems of tubes and components and measurement of pumping speed

- The transmission probability of <u>any</u> shape can be calculated with arbitrary precision by using the <u>Test-Particle</u> <u>Montecarlo method (TPMC)</u>.
- The TPMC generates "random" molecules according to the cosine distribution...

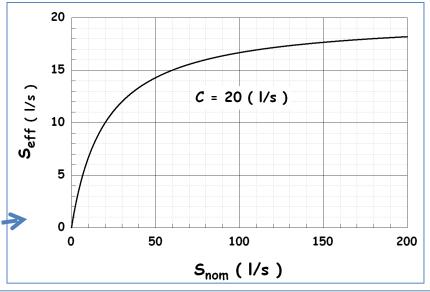
- ... at the entrance of the tube, and then follows their traces until they reach the exit of the tube.
- Time is not a factor, and residence time on the walls is therefore not an issue (although they can be taken into account).
- Each collision with the walls is followed by a random emission following, again, the cosine distribution...
- ... this is repeated a very large number of times, in order to reduce the statistical scattering and apply the large number theorem.
- The same method can be applied not only to tubes but also to threedimensional, arbitrarily-shaped components, i.e. "models" of any vacuum system.
- In this case, pumps are simulated by assigning "<u>sticking coefficients</u>" to the surfaces representing their inlet flange.
- The sticking coefficient is nothing else than the probability that a molecule... 16

- ... hitting that surface gets pumped, i.e. removed from the system.
- The <u>equivalent sticking coefficient</u> s of a pump of pumping speed S [l/s] represented by an opening of A [cm²] is given by
 - $s = \frac{S}{A \cdot \frac{v_{mean}}{4}}$

... i.e. it is the ratio between the given pumping speed and the conductance of the zero-thickness hole having the same surface area of the opening A.

• The "interchangeability" of the concept of conductance and pumping speed, both customarily defined by the units of [l/s] (or [m³/s], or [m³/h]), suggests that if a pump of nominal speed S_{nom} [l/s] is connected to a volume V via a tube of conductance C, the <u>effective pumping</u> <u>speed</u> of the pump will be given by the relationship $\frac{1}{S_{eff}} = \frac{1}{S_{nom}} + \frac{1}{C}$ • From this simple equation it is clear that it doesn't pay to increase the installed pumping speed much more than the conductance *C*, which therefore sets a limit to the <u>achievable effective pumping speed</u>.

• This has <u>severe implications</u> for accelerators, as they typically have vacuum chambers with a tubular shape: they are "<u>conductance-</u> <u>limited systems</u>", and as such need a specific strategy to deal with them



Tutorial on Gas Flow, Conductance, Pressure Profiles Transmission Probability and Analytical Formulae

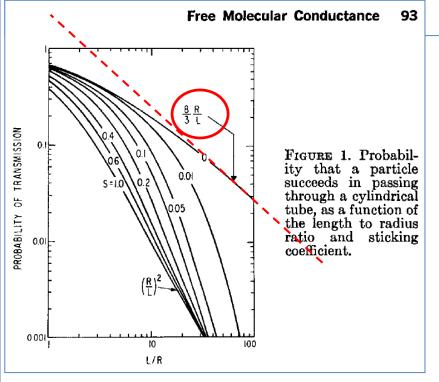
• The transmission probability of tubes has been calculated many times. This paper (J.Vac.Sci.Technol. 3(3) 1965 p92-95)...

Free Molecular Conductance of a Cylindrical Tube with Wall Sorption

Craig G. Smith and Gerhard Lewin

Plasma Physics Laboratory, Princeton University, Princeton, New Jersey (Received 26 October 1965)

A Monte Carlo method was used to calculate the probability that a molecule passes through a cylindrical tube with wall sorption. This probability is presented as a function of the ratio of length to radius and the sticking coefficient s of the wall. For s = 0, the results confirm those of Clausing for the conductance of a tube of finite length. For $s \neq 0$, wall pumping can greatly roduce the flow of measurement of the values of s. The backettering statel has ratio about the second se



... gives us a way to calculate the conductance of a cylindrical tube of any length to radius ratio L/R >0.001:

 $C_{transm}(l/s) = A_{inlet}(cm^2) \cdot 11.77(l/s/cm^2) \cdot P_{transm}$

... where P_{transm} is the transmission probability of the tube, as read on the graph and 11.77 is the "usual" kinetic factor of a mass 28 gas at 20°C.

• Other authors have given approximate equations for the calculation of C_{transm} , namely <u>Dushman</u> (1922), prior to the advent of modern digital computers

$$C_{transm}(l/s) = 12.4 \frac{D^3/L}{1+4 \cdot \frac{D}{3 \cdot L}}$$

... with D and L in m.

•We can derive this equation by considering a tube as two conductances in series: C_A , the aperture of the tube followed by the tube itself, C_B .

18

• By using the summation rule for....

Dushman's Formula for Tubes

• This fundamental conductance limitation ... 2 conductances in series... $\frac{1}{C} = \frac{1}{C_A} + \frac{1}{C_B}$... we obtain: has *profound effects* on the design of the pumping system of accelerators: the location, number and size of the pumps must be decided on the merit of minimizing the average pressure seen by $C_{A} = 9.3 \cdot D^{3}$ and $C_{B} = 12.4 \cdot D^{3}/L$ the beam(s), and reducing local bumps. ... with D and L in cm. Substituting •The process is carried out in several above... steps: first a "back of the envelope" $C = \frac{C_A \cdot C_B}{C_A + C_B} = \frac{12.4 \cdot D^3 / L}{1 + 4 \cdot D / (3 \cdot L)}$ calculation with evenly spaced pumps, followed by a number of iterations where the position of the pumps and Beware: the error can be large! eventually their individual size (speed) are customized • Exercise: 1) estimate the conductance of a tube of D=10 [cm] and L=50 [cm] • Step 1 resembles to this: a crossby using the transmission probability section common to all magnetic elements concept and compare it to the one is chosen, i.e. one which fits inside all obtained using Dushman's formula. magnets (dipoles, quadrupoles, sextupoles, etc...): this determines a 2) Repeat for a tube with L=500 [cm]. <u>specific conductance</u> for the vacuum 3) Calculate the relative error. chamber c_{spec} (I·m/s), by means of, for instance, the <u>transmission probability</u> 19 method.

Tutorial on Gas Flow, Conductance, Pressure Profiles Pressure Profiles and Conductance

•We then consider a chamber of uniform cross-section, of specific surface A [cm²/m], specific outgassing rate of q [mbar·l/s/cm²], with equal pumps (pumping speed S [l/s] each) evenly spaced at a distance L. The following equations can be written:

$$Q(x) = -c \frac{dP(x)}{dx}$$
$$\frac{dQ(x)}{dx} = Aq$$

...which can be combined into

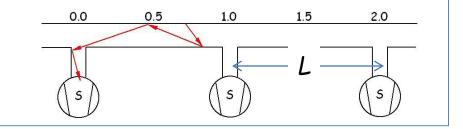
$$c\frac{d^2P}{dx^2} = -Ac$$

... with boundary conditions

$$\frac{dP}{dx}(x = L/2) = 0$$
$$P(x = 0) = AqL/S$$

... to obtain the final result

$$P(x) = \frac{Aq}{2c} \left(Lx - x^2 \right) + \frac{AqL}{S}$$



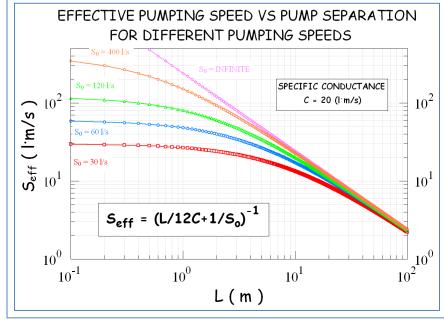
Tutorial on Gas Flow, Conductance, Pressure Profiles Pressure Profiles and Conductance [2]

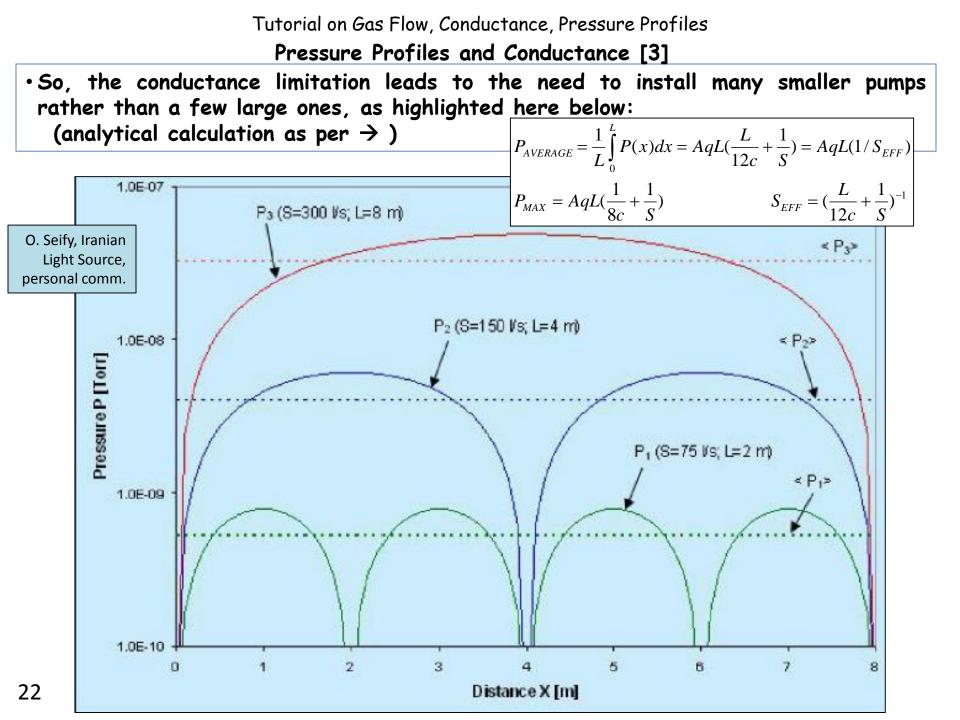
•From this equation for the pressure profile, we derive three interesting quantities: the <u>average pressure</u>, the <u>peak pressure</u>, and the <u>effective</u> <u>pumping speed</u> as:

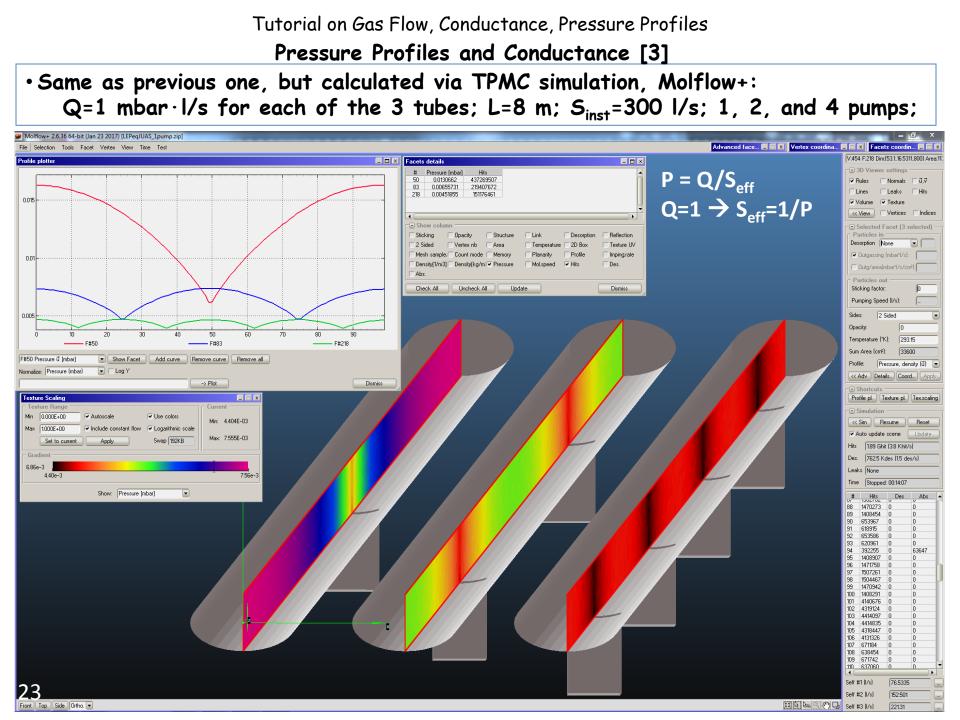
$$P_{AVERAGE} = \frac{1}{L} \int_{0}^{L} P(x) dx = AqL(\frac{L}{12c} + \frac{1}{S}) = AqL(1/S_{EFF})$$
$$P_{MAX} = AqL(\frac{1}{8c} + \frac{1}{S}); \quad AqL = Q_{tot}; \quad S_{EFF} = (\frac{L}{12c} + \frac{1}{S})^{-1}$$

- From the 1st and 3rd ones we see that once the specific conductance is chosen (determined by the size of the magnets, and the optics of the machine), how low the average pressure seen by the beam can be is limited by the effective pumping speed, which in turn depends strongly on c.
- The following graph shows an example of this: for c=20 $[l \cdot m/s]$ and different nominal pumping speeds for the pumps, the graphs show how S_{eff} would change.

- This, in turn, determines the average... <u>pump spacing</u>, and ultimately the <u>number of pumps</u>.
- Summarizing: in one simple step, with a simple model, one can get an estimate of the size of the vacuum chamber, the number and type of pumps, and from this, roughly, a first estimate of the capital costs for the vacuum system of the machine. Not bad! ⁽²⁾







Tutorial on Gas Flow, Conductance, Pressure Profiles **Pressure Profiles and Distributed Pumping**

• From the previous analysis it is clear that there may be cases when either because of the size of the machine or the dimensions of (some of its) vacuum chambers, the number of pumps which would be necessary in order to obtain a sufficiently low pressure could be too large, i.e. impose <u>technical and cost</u> <u>issues</u>. One example of this was the LEP accelerator, which was 27 kmlong, and would have needed thousands of pumps, based on the analysis we've carried out so far.

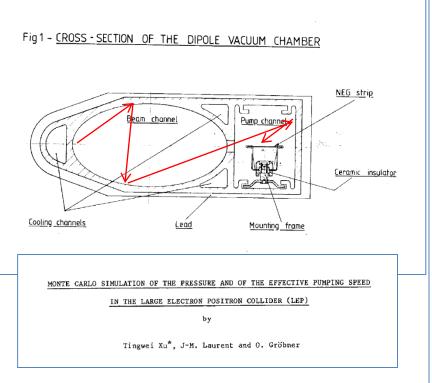
- So, what to do in this case? Change many small pumps into one more or less continuous pump, i.e. implement <u>distributed pumping</u>.
- In this case if S_{dist} is the distributed pumping speed, its units are [l/s/m], the equations above become:

$$P_{AVG} = Aq / S_{EFF};$$

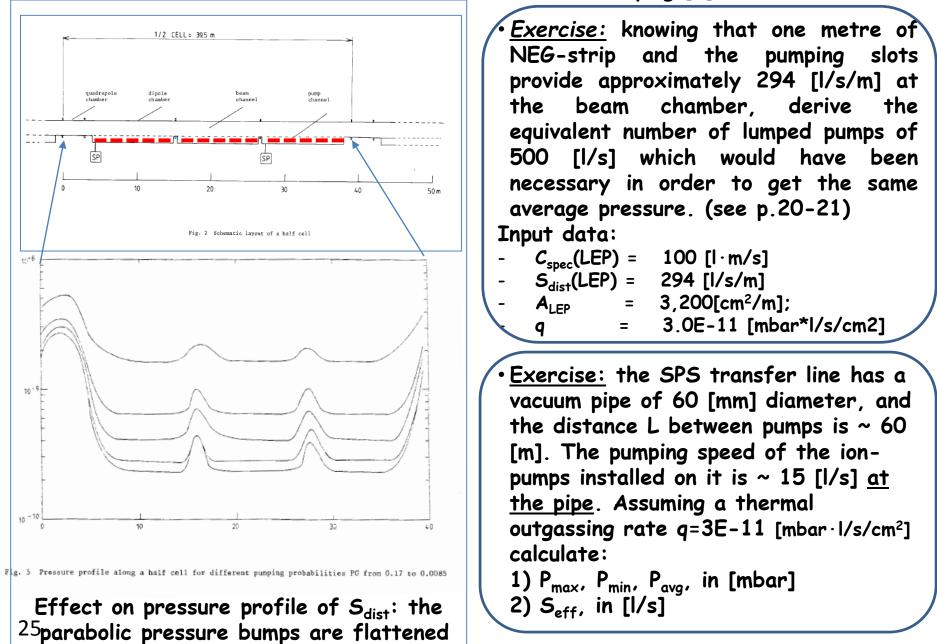
$$P_{MAX} = P_{AVG};$$

$$S_{EFF} = S_{dist} \cdot L$$

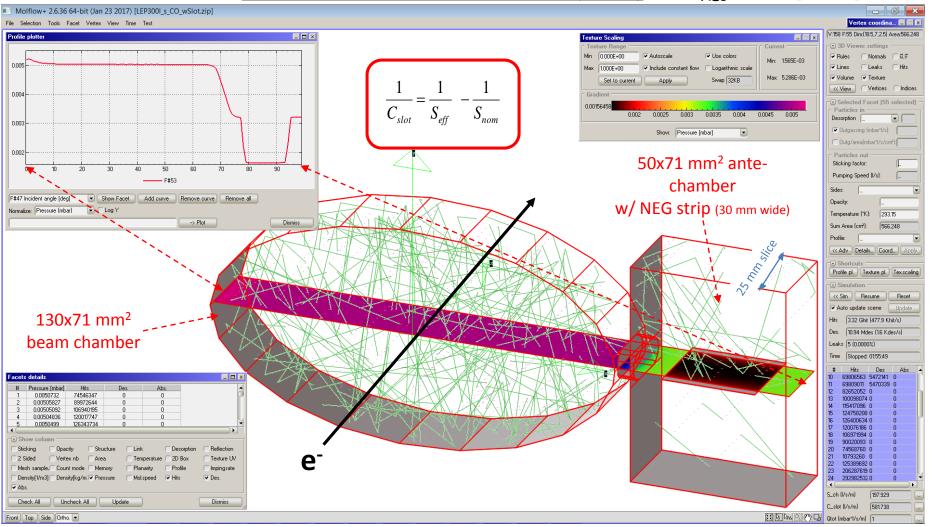
- •We obtain a flat, <u>constant</u>, pressure profile.
- The distributed pressure profile in LEP had been obtained by inserting a NEG-strip along an <u>ante-chamber</u>, running parallel to the beam chamber, and connected by small oval slots:



Tutorial on Gas Flow, Conductance, Pressure Profiles **Pressure Profiles and Distributed Pumping** [2]

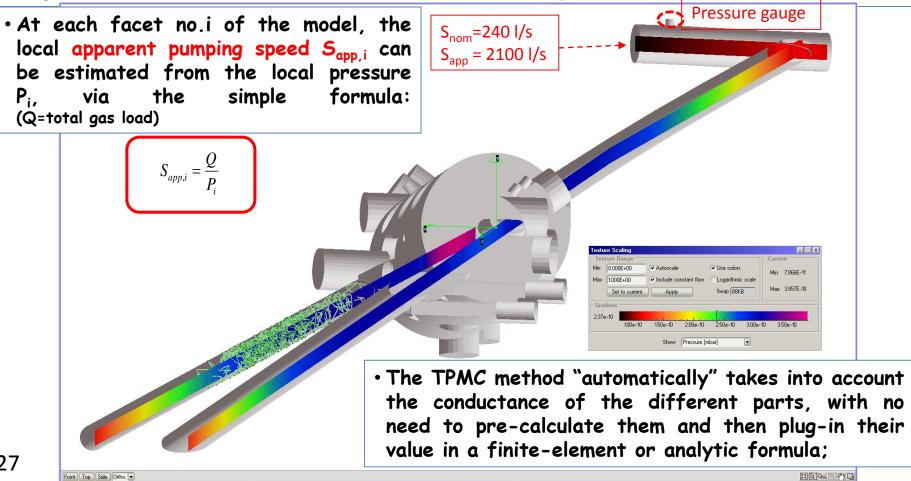


• A modern way to calculate the effective pumping speed of the 20×9 mm² racetrack pumping slots in LEP is via the <u>Test-Particle Montecarlo method (TPMC)</u>: S_{NEG}= 300 [l/s/m]



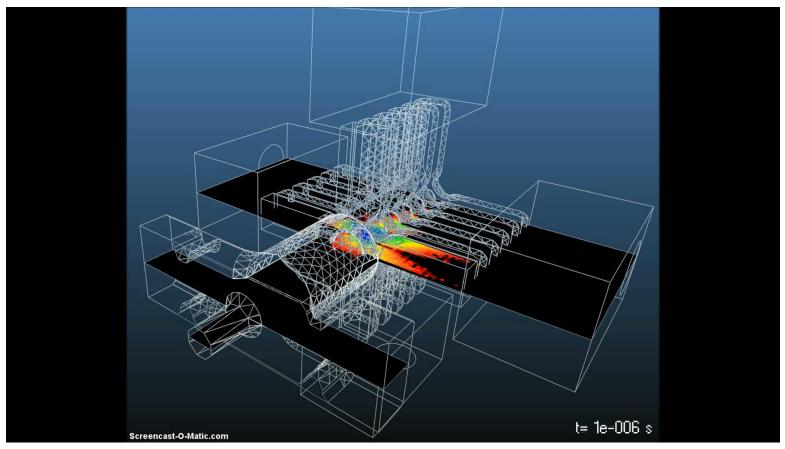
A virtual "test facet" is laid across the chamber's cross-section and the pressure profile is calculated by recording all the rays crossing it; It is then possible to calculate S_{eff}(l/s/m) and from this C_{elot} [l/s/m] by using the formula shown here above.
 The goal is to maximize C_{slot} and therefore S_{eff} without affecting too much the beam; 26

- Vacuum chamber geometries of arbitrary complexity can also be designed and analysed via the TPMC method:
- In this case a model can be made with a CAD software, exported in STL format to the TPMC code Molflow+, and then the vacuum properties can be assigned to the different facets, such as outgassing rate, sticking coefficient (equivalent pumping speed), opacity (ratio of void-to-solid, to simulate fine grids, for instance), and more...;
- This example shows the recent analysis of a potential new design of an injection septum magnet for the PS accelerator at CERN (model courtesy of J. Hansen, CERN-TE-VSC);



One example of a time-dependent Test-Particle Monte Carlo simulation

Propagation of the **pressure wave following an RF breakdown** in a cell of the CLIC linear accelerator:



Ref.: M. Ady's PhD thesis CERN-EPFL, 2016;

Summary:

- During this short tutorial we have reviewed some important concepts and equations related to the field of vacuum for particle accelerators.
- •We have seen that one limiting factor of accelerators is the fact that they always have long tubular chambers, which are inherently <u>conductance limited</u>.
- We have also seen some basic equations of vacuum, namely the P=Q/S which allows a very first glimpse at the level of pumping speed S which will be necessary to implement on the accelerator in order to get rid of the outgassing Q, with the latter depending qualitatively and quantitatively on the type of accelerator (see V. Baglin's lessons on outgassing and synchrotron radiation, this school).
- Links between the thermodynamic properties of gases and the technical specification of pumps (their pumping speed) as been given: the link is via the <u>equivalent sticking</u> <u>coefficient</u> which can be attributed to the inlet of the pump.
- One simple model of accelerator vacuum system, having uniform desorption, evenly spaced pumps of equal speed has allowed us to derive some preliminary but useful equations relating the *pressure* to the *conductance* to the <u>effective pumping speed</u>, and ultimately giving us a ballpark estimate about the number of pumps which will be needed in our accelerator.
- An example of a real, now dismantled, accelerator has been discussed (LEP), and the advantages of <u>distributed pumping</u> vs <u>lumped pumping</u> detailed.
- Two examples of a more modern way of calculating conductances and pressure profiles (TPMC) have been shown: it should be the preferred method for the serious vacuum scientist;

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