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Reverse emittance exchange at MICE

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Wedge absorbers and emittance exchange

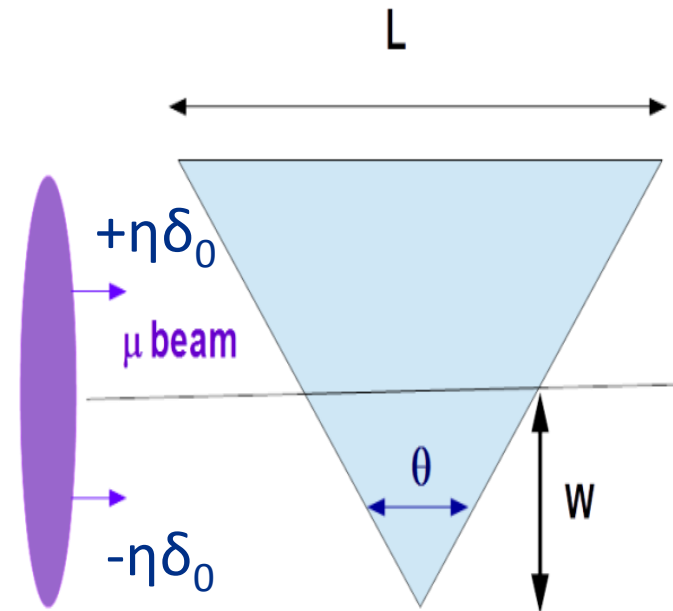
- Matrix formalism:

$$\mathbf{M}_\delta = \begin{bmatrix} 1 & 0 \\ -\delta' & 1 \end{bmatrix} \quad \mathbf{M}_\eta = \begin{bmatrix} 1 & \eta_0 \\ 0 & 1 \end{bmatrix}$$

– wedge is $\delta' = dp/ds \approx 2 \tan[\theta/2]/p$

$$\delta_1 = \delta_0 \left[(1 - \eta_0 \delta')^2 + \frac{\delta'^2 \sigma_0^2}{\delta_0^2} \right]^{1/2}$$

$$- \varepsilon_{L,1} / \varepsilon_{L,0} = \delta_1 / \delta_0; \quad \varepsilon_{t,1} / \varepsilon_{t,0} = \delta_0 / \delta_1$$



Can decrease ε_L and increase ε_t (or reverse)

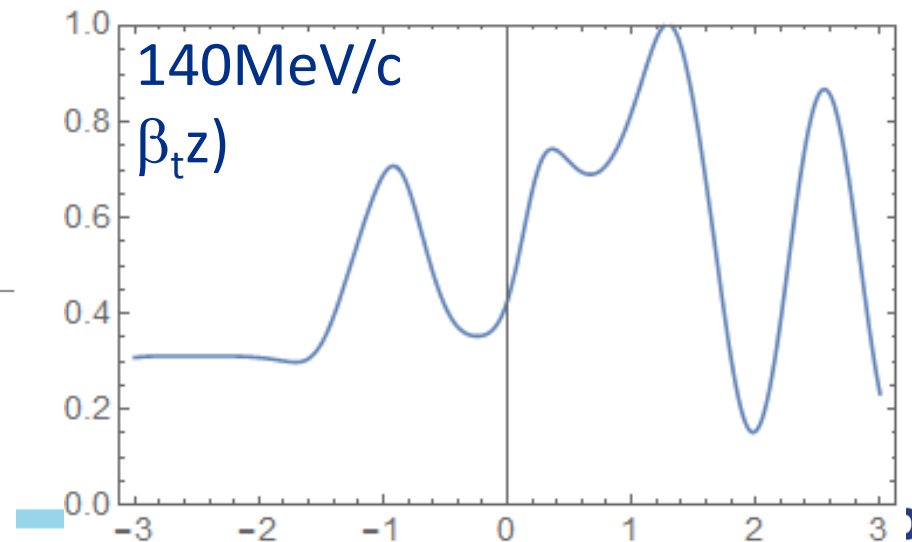
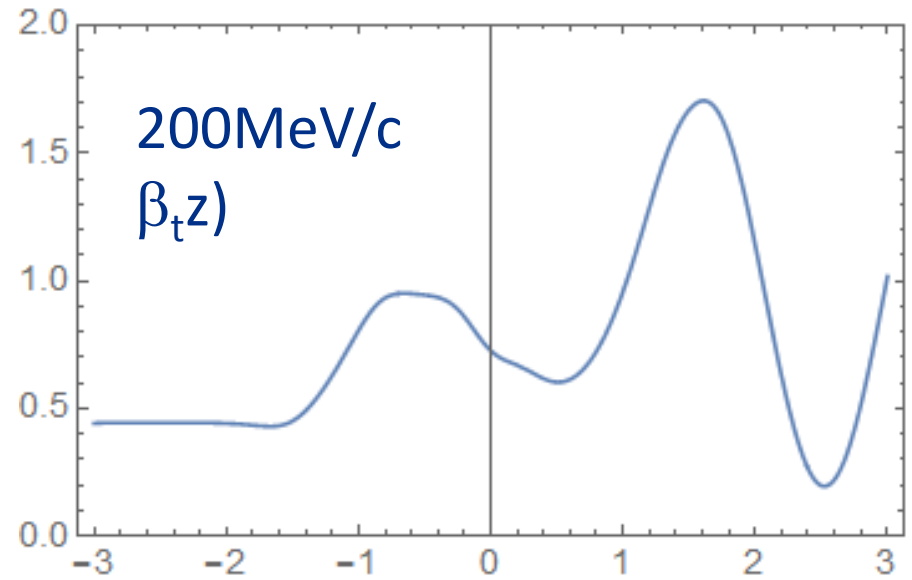
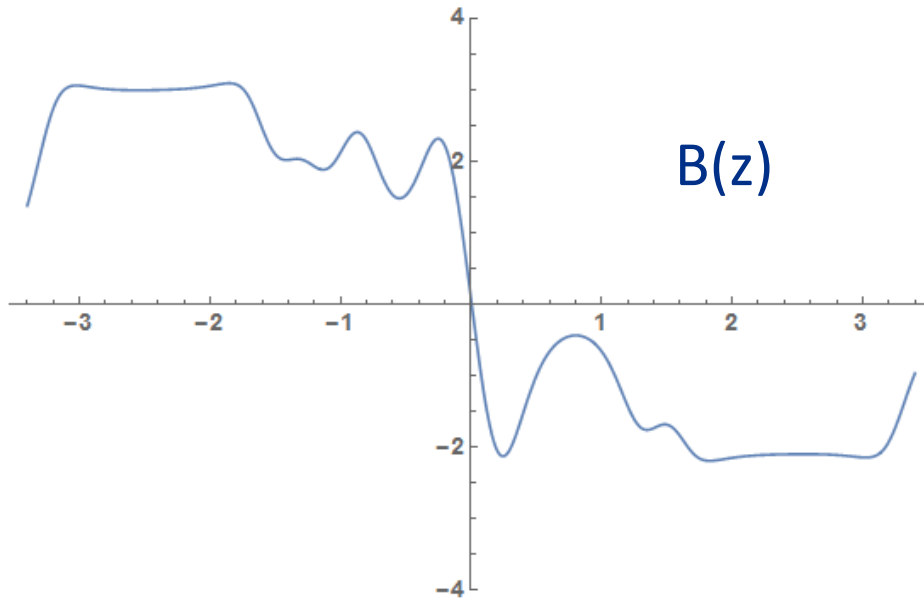
- Reverse emittance exchange (at $\eta=0$):

$$\frac{\varepsilon_{t,1}}{\varepsilon_{t,0}} = \sqrt{\frac{\delta_0^2}{\delta_0^2 + \delta'^2 \sigma_0^2}}$$

– large effect, with small δ_0 ; used $\delta p = 2\text{MeV}/c$ for MICE 

Optics for MICE system

- 2017-02-07
 - B(Z)
 - 200 MeV/c
 - 140 MeV/c

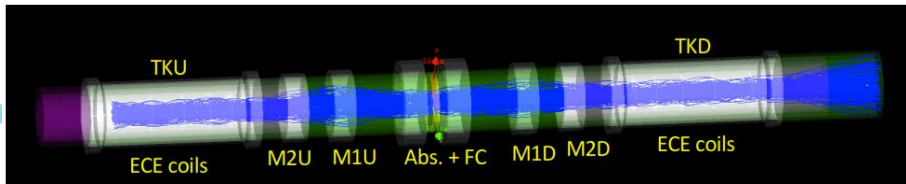
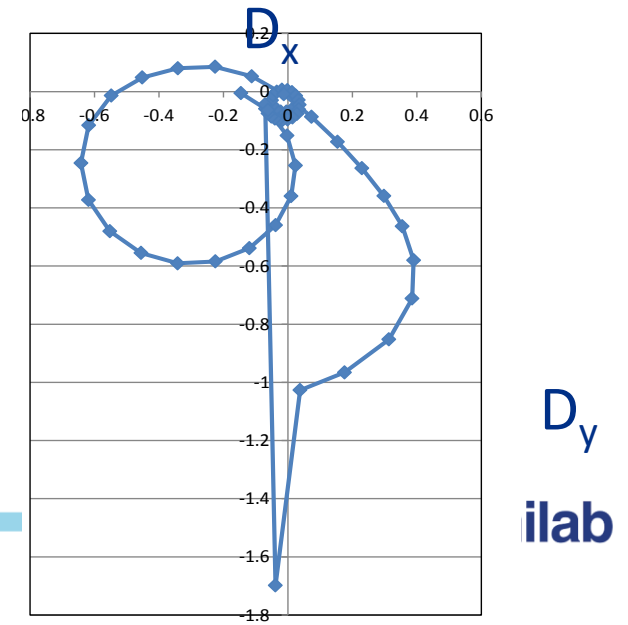
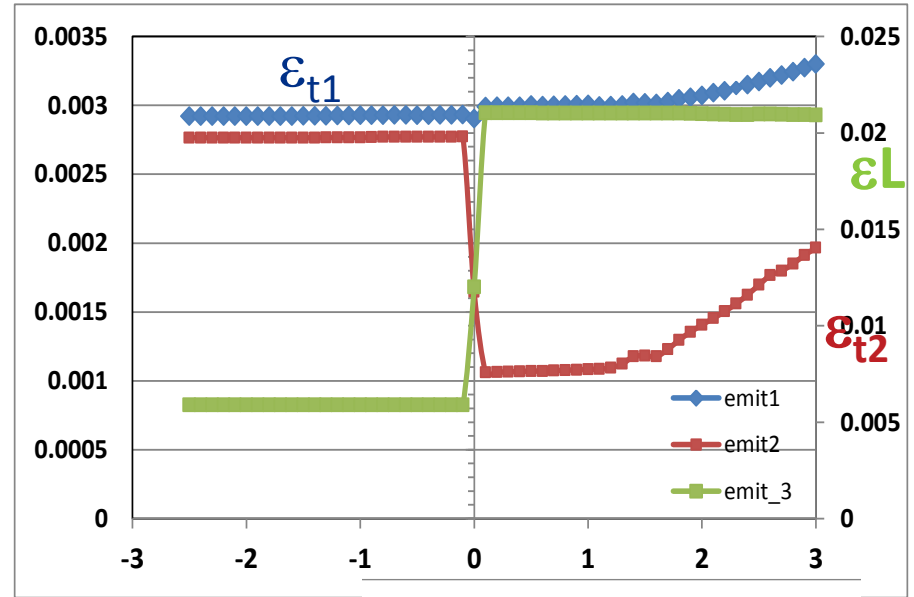


MICE with M2 (2017-02-7 settings)

- 200MeV/c; $\varepsilon_t=3\text{mm}$; $\delta p_0=2\text{ MeV/c}$
- with M2 on (-195 A)
 - 3T \rightarrow 2T in DS
- good behavior
 - less emittance dilution in DS
 - 1.05 \rightarrow 2.0mm
 - 3.0 \rightarrow 3.3mm

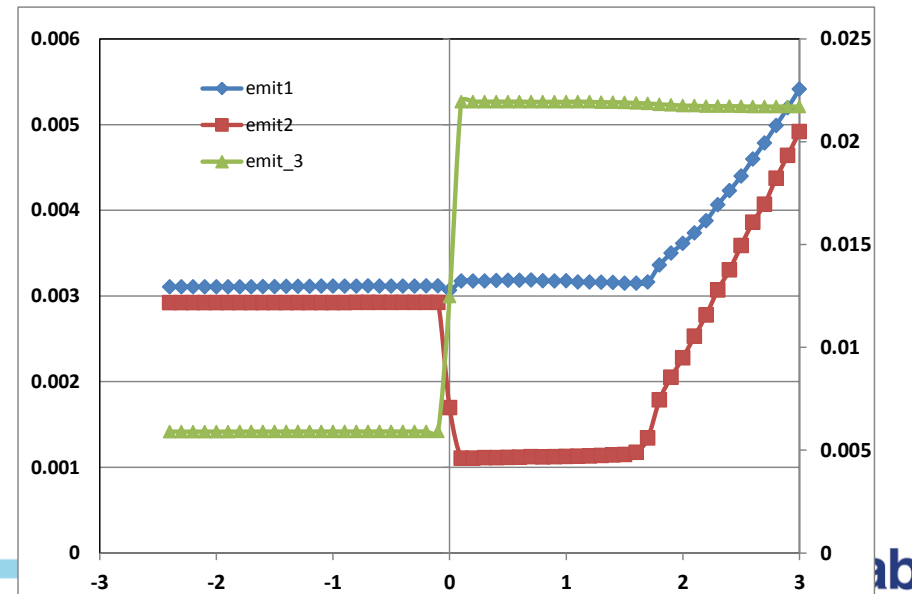
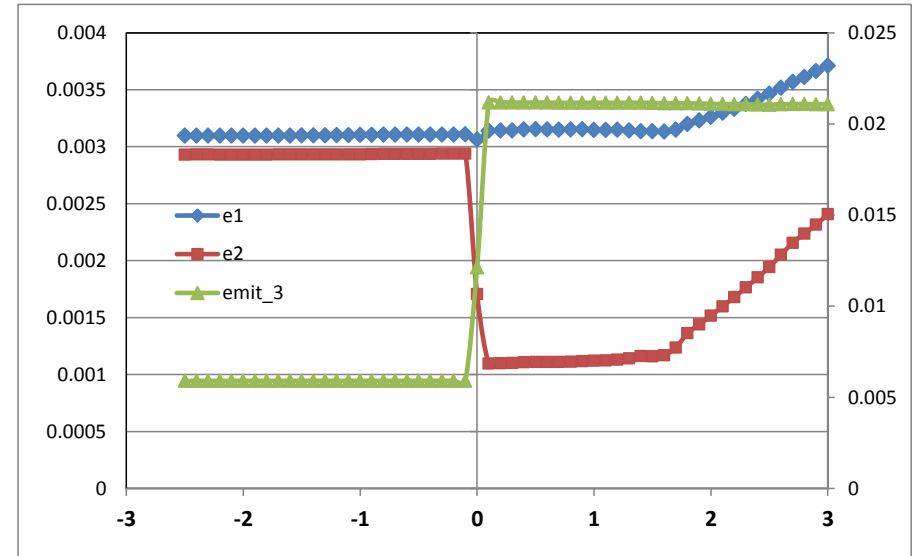
Dispersion in DS is well behaved

200 MeV/c-3mm is a good beam setting to include in the experiment



Other cases

- M2D reduced to -110
 - reverse emittance exchange about as good as 2017-02-7
- M2D off (2016-05-1)
 - not as good
 - nonlinear emittance growth in DS much larger
 - effect still visible at DS entrance



12/7/2017

Summary

- **Wedge emittance exchange is an important part of beam cooling**
- Experiment at MICE could demonstrate the principle
 - in both “direct “ and “reverse” exchange
- **Large effect in reverse exchange could be measured**