

# **FCC-hh DESIGN REPORT**

JOHN ADAMS INSTITUTE

Hannah Harrison  
Christopher Arran  
Rob Williamson  
Mehpare Atay  
Alberto Arteche  
Rob Shalloo  
Talitha Bromwich  
Huibo Zhang

# INTRODUCTION

Hannah Harrison

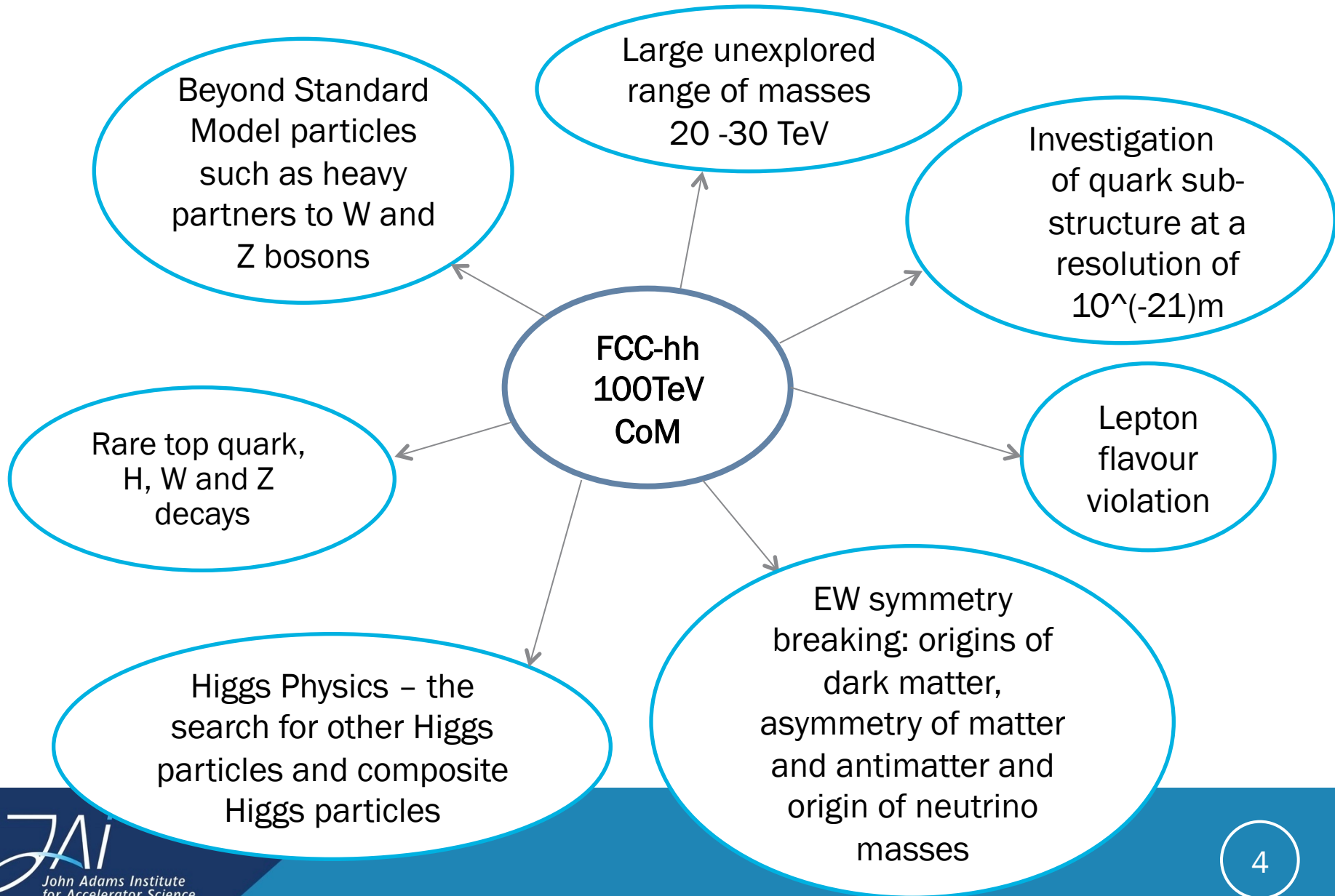
# THE FCC-hh PROPOSAL

- Future Circular Collider – Hadron Hadron
- Ring circumference → 100 km (80 km)
- Magnetic field strength → 16T (Nb<sub>3</sub>Sn superconductor)
- Centre of mass energy → 100 TeV (80 TeV)
- Location currently not decided

Magnetic  
Rigidity

$$B\rho = \frac{p}{e}$$

# THE PHYSICS JUSTIFICATION FOR THE FCC-hh



# THE FCC-ee AND FCC-he

## •FCC-ee

- High Luminosity → precision physics
- Collisions of Z, W, H and t
- CoM range in the region of 240GeV-500GeV
- Detailed studies of electroweak symmetry breaking

## •FCC-he

- Investigate deep inelastic scattering
- Electron-deuteron/electron-ion scattering → investigate nuclear structure
- Quark-Gluon plasma formation
- Heavy ion collisions

# PROJECT BRIEF

- Carry out in-depth studies of various aspects of the FCC-hh
- Look at possible ways of reducing the cost of building such a machine
  - Reducing the Aperture
    - Less superconducting material would be needed
    - Reduction in possible centre-of-mass energy
    - Reduction in luminosity
  - Use different material to construct the dipoles
    - Other superconductors are cheaper than Nb<sub>3</sub>Sn (e.g. NbTi)
    - Cannot support such high magnetic fields
    - Reduction in possible centre-of-mass energy

*Need to examine the trade off between the best possible parameters for the machine to perform physics and the cost of achieving them*

# ASPECTS OF THE FCC-hh DESIGN CONSIDERED

- Lattice Design
- Synchrotron Radiation and Instabilities
- Magnet Design
- RF cavities
- Conclusion – *how will our ideas impact the physics capabilities of FCC –hh?*

# LATTICE DESIGN

Christopher Arran

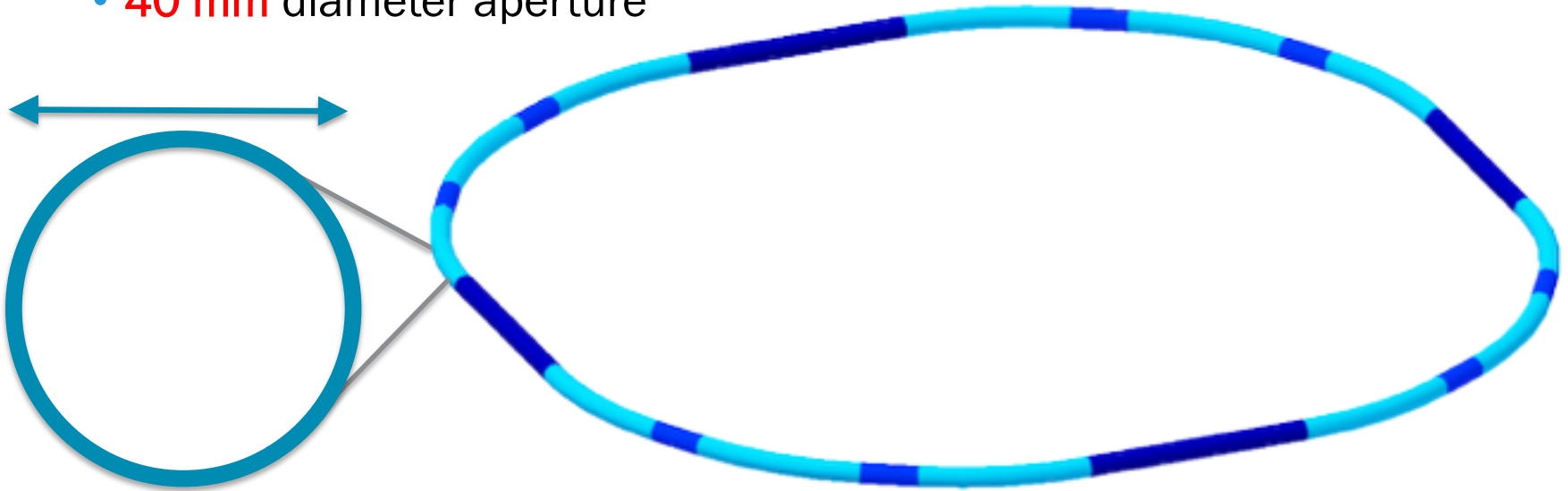
- Possible Cost Reductions
- Effect on Beam Energy



# STARTING POINT

## Reyes Alemany & Bernhard Holzer Design:

- 12 arcs and 12 straights (exaggerated length)
- 4 long straights for Interaction Points, injection etc
- $450 \text{ Tm}^{-1}$  quadrupole field gradient ( $\text{Nb}_3\text{Sn}$ )
- **14.7 T** dipoles ( $\text{Nb}_3\text{Sn}$ )
- **40 mm** diameter aperture



# POSSIBLE COST REDUCTIONS

## Smaller aperture

- Less superconductor material required
- Consider **40mm**, **30mm** and **20mm** apertures

## Cheaper dipole magnets

- Consider NbTi at **10.5T** vs Nb<sub>3</sub>Sn at **16T**

Aperture Diameter	Maximum Twiss Beta
40mm	354.6 m
30mm	199.4 m
20mm	88.6 m

Dipole Strength
14.7 T
10.5 T
16 T

# CONSTRAINTS

## Physical limits on lattice:

- Space for RF, IP, injection and extraction
- Require space between components

Constraint	
Ring circumference	100 km
Long straight length	$\geq 1$ km
Dipole length	$\leq 14.2$ m
Dipole-Dipole spacing	1.3 m
Dipole-Quadrupole spacing	3.6 m

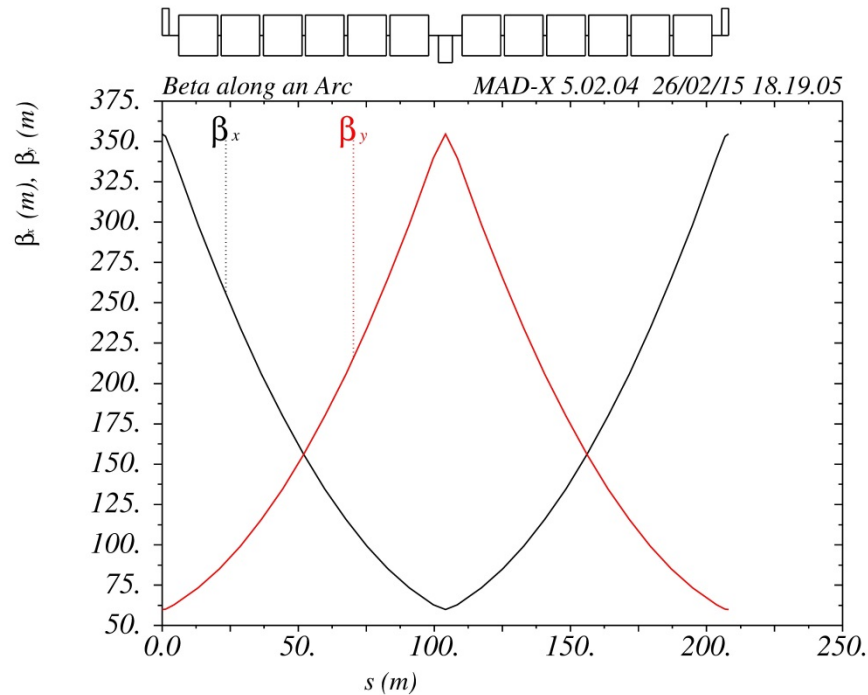
# LATTICE AFFECTS BEAM ENERGY

## Scaling Laws:

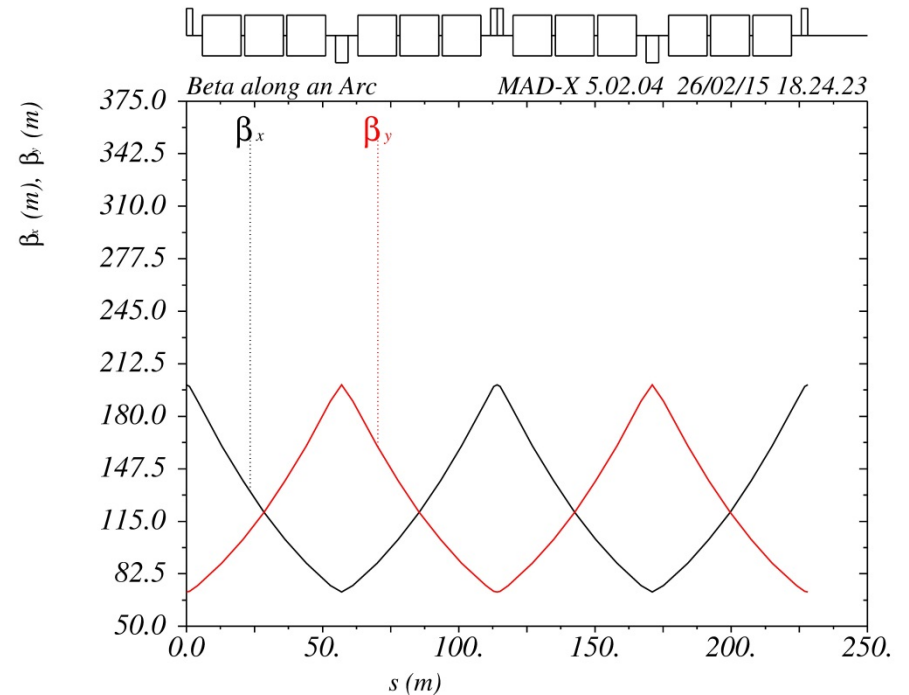
- **Aperture**  $\Rightarrow$  Maximum Twiss beta  
 $\Rightarrow$  FODO cell length  
 $\Rightarrow$  No. dipoles  
 $\Rightarrow$  Beam energy
- **Dipole strength**  $\Rightarrow$  Beam energy

# MAD X OUTPUT

40 mm Aperture  
12 dipoles per cell



30 mm Aperture  
6 dipoles per cell



# RESULTS

<i>Energies / TeV</i>	Dipole Field	14.7 T	10.5 T	16 T
Aperture Diameter	40 mm	100	74.6	100
	30 mm	96.4	70.8	100
	20 mm	68.8	53.0	

<i>Dipole Fill Factor</i>	Dipole Field	14.7 T	10.5 T	16 T
Aperture Diameter	40 mm	71%	75%	66%
	30 mm	69%	71%	66%
	20 mm	50%	53%	

# CONCLUSIONS

- 30 mm aperture  $\Rightarrow$  only slightly lower energy
- 20 mm aperture is too small
- 10.5 T  $\Rightarrow$  **70-75 TeV** centre of mass
- 16 T is stronger than necessary

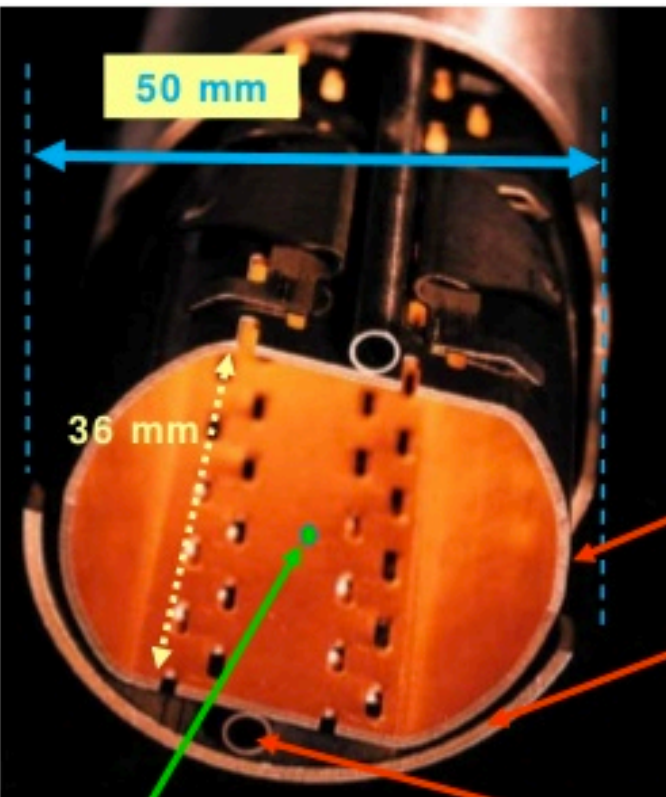
# INSTABILITIES

Rob Williamson

- Resistive Wall
- Aperture Implications
- Coupled Bunch
- TMCI
- Damping Possibilities



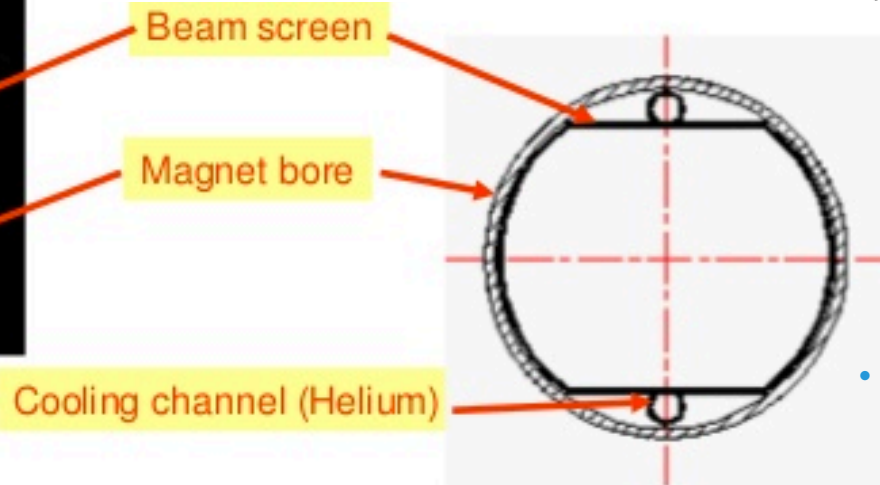
# RESISTIVE WALL IMPEDANCE



LHC Beam Screen

- Beam interacts with its environment through impedances
- Transverse impedance dominated by resistive wall:

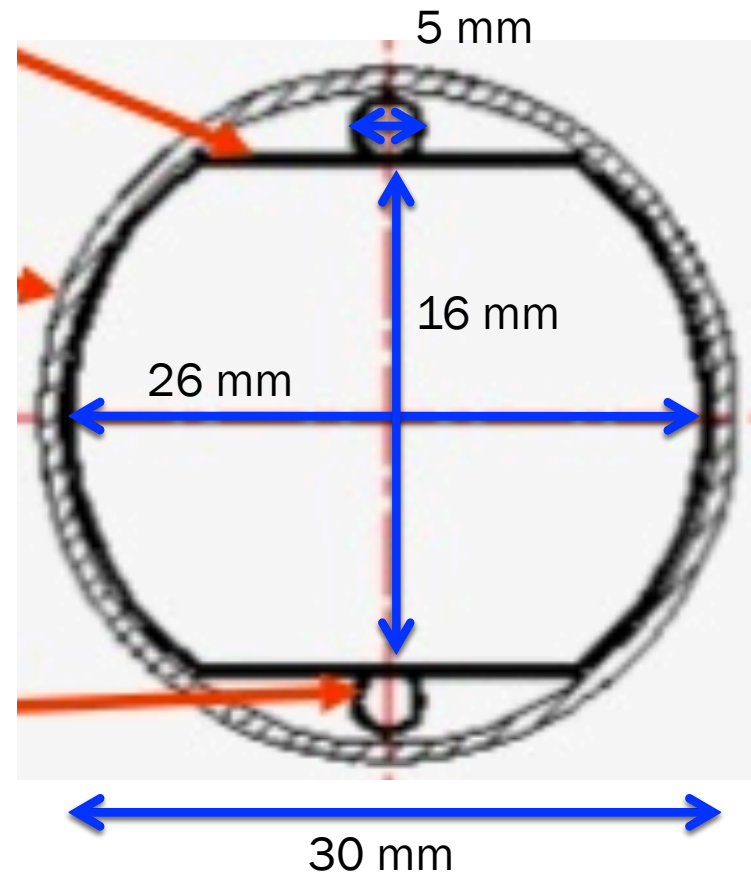
$$Z_{\perp}(\omega) = (\text{sgn}(\omega) - i) \frac{Z_0 R \delta_s}{b^3}$$



- $b$  = beampipe radius
- $\delta_s$  = skin depth

# IMPLICATIONS OF APERTURE REDUCTION

- Assume LHC-style beam screen geometry
- Minimum aperture
  - +/- 8 mm for 30 mm aperture
  - +/- 13 mm for 40 mm aperture
- Impedance proportional to  $b^{-3}$
- Effect on instability growth rates?

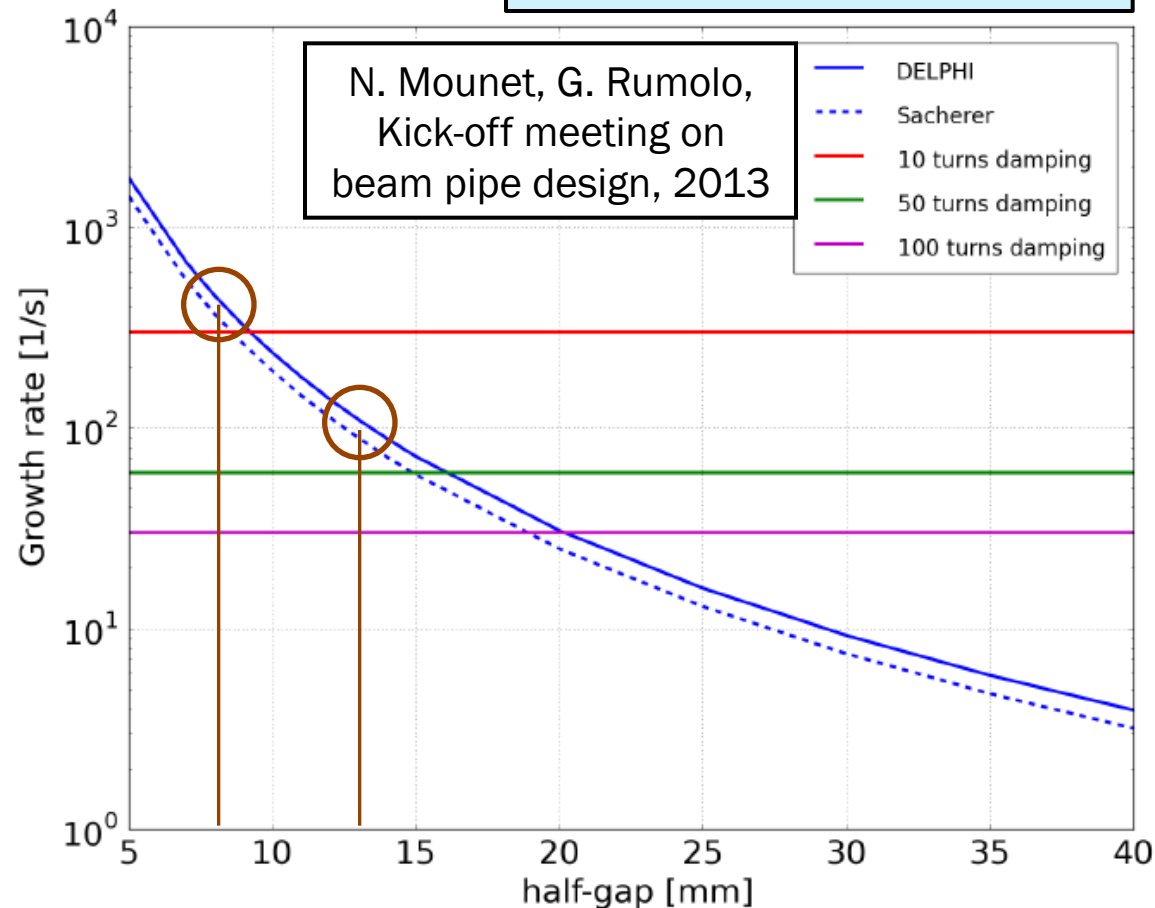


**FCC-30mm**

# COUPLED BUNCH INSTABILITY

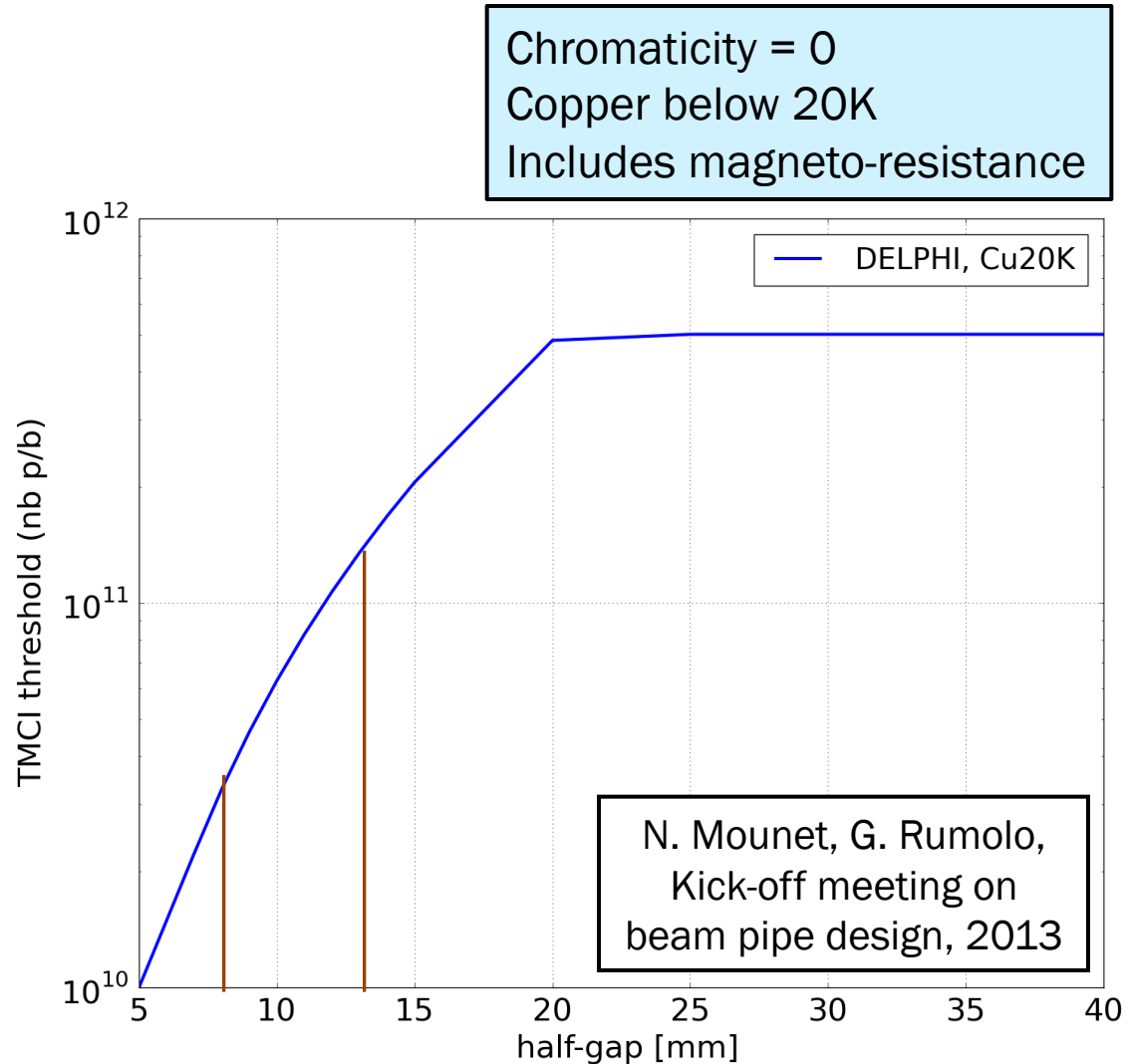
25ns bunch spacing  
 $10^{11}$  protons per bunch  
Chromaticity = 0  
Copper below 20K  
Includes magneto-resistance

- Growth rate for coupled-bunch instability is proportional to the transverse impedance
- Scales as  $1/\gamma$
- Plot at 3 TeV
- Factor of 4.3 larger growth rate
- < 10 turns damping



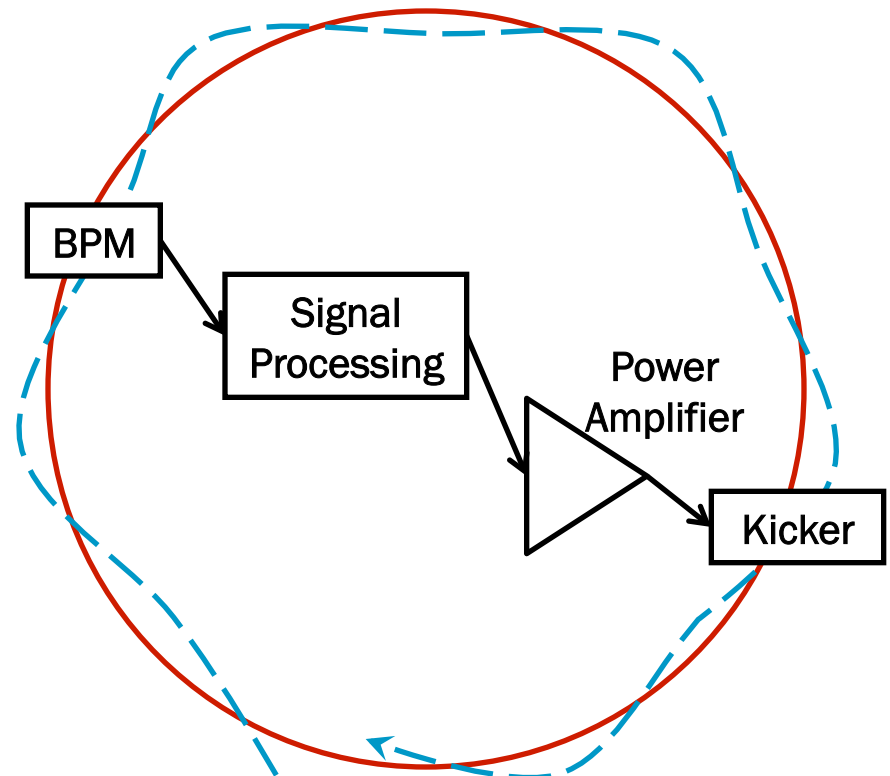
# TRANSVERSE MODE COUPLING INSTABILITY

- Headtail instability driven by resistive wall impedance
- Threshold increases with beam energy
  - Plot at 3 TeV
- Maximum intensity
  - $\sim 3 \times 10^{10}$  ppb
  - $\sim 1.5 \times 10^{11}$  ppb
- Nominal =  $1 \times 10^{11}$  ppb



# DAMPING SYSTEMS

- Landau octupoles
- Transverse damper system
- LHC system
  - < 40 turns (3.6 ms)
  - Equates to 11 turns FCC
  - < 10 turns hard limit
- FCC system (30 mm aperture)
  - < 7 turns => multiple kickers
  - Good noise control on BPMs
  - Power available
  - GHz system for TMCI



# CONCLUSIONS

- **Reducing the aperture**
  - Increases growth rate for coupled bunch instability by factor 4
  - Damping in  $<7$  turns
  - Reduces threshold to TMCI to  $3 \times 10^{10}$  ppb
  - Reduces luminosity by factor of 10 from design
- **Transverse damping system**
  - Faster damping than LHC
  - GHz intra-bunch system for TMCI

# SYNCHROTRON RADIATION

Mehpare Atay

## Alternative Considerations for Synchrotron Radiation

# SYNCHROTRON RADIATION IN FCC-hh

<i>Machine</i>	<i>Bending radius(m)</i>	<i>Beam energy(GeV)</i>	$\gamma$	<i>Beam current(mA)</i>	<i>Critical photon energy(eV)</i>	<i>Total SR power radiated(W)</i>
<b>LHC</b>	<b>2803.95</b>	<b>6500</b>	<b>6928</b>	<b>490</b>	<b>35.1</b>	<b>2431</b>
<b>FCC-hh 15T</b>	<b>11146.32</b>	<b>50000</b>	<b>53306</b>	<b>500</b>	<b>4016</b>	<b>2.18E+06</b>
<b>LEP-2</b>	<b>3096.2</b>	<b>104</b>	<b>203521</b>	<b>4.5</b>	<b>8.06E+05</b>	<b>1.51E+07</b>
<b>ESRF</b>	<b>23.366</b>	<b>6</b>	<b>11742</b>	<b>200</b>	<b>20504</b>	<b>9.81E+05</b>

- The critical energy is in the X-ray region.
- FCC generates 170 times of SR power of the LHC.



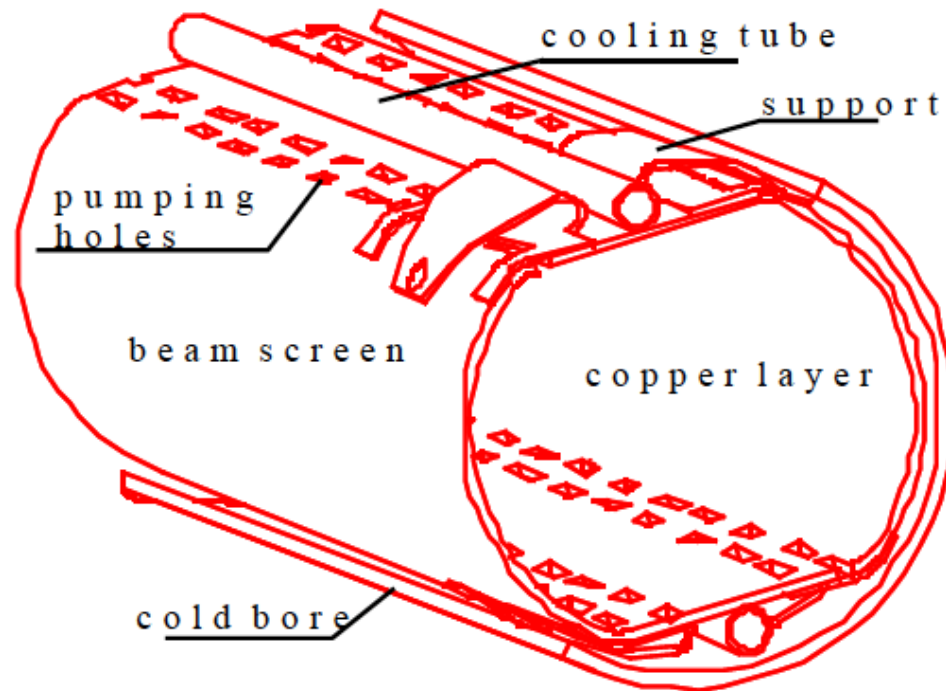
# CHALLENGES DUE TO SYNCHROTRON RADIATION

Power radiated per mrad	0.35	kW
SR line power density	31.18	W/m
Photon flux	1.54E+17	ph/s/m
Critical angle for SR emission	1.88E-05	rad
SR energy loss	4.67	MeV/turn

- High temperature of the beam pipe; *due to the SR power density*
  - Large gas load; *due to the large photon flux*
- ➡ SR needs to be absorbed by the designed beam pipe.

# LHC BEAM SCREEN DESIGN

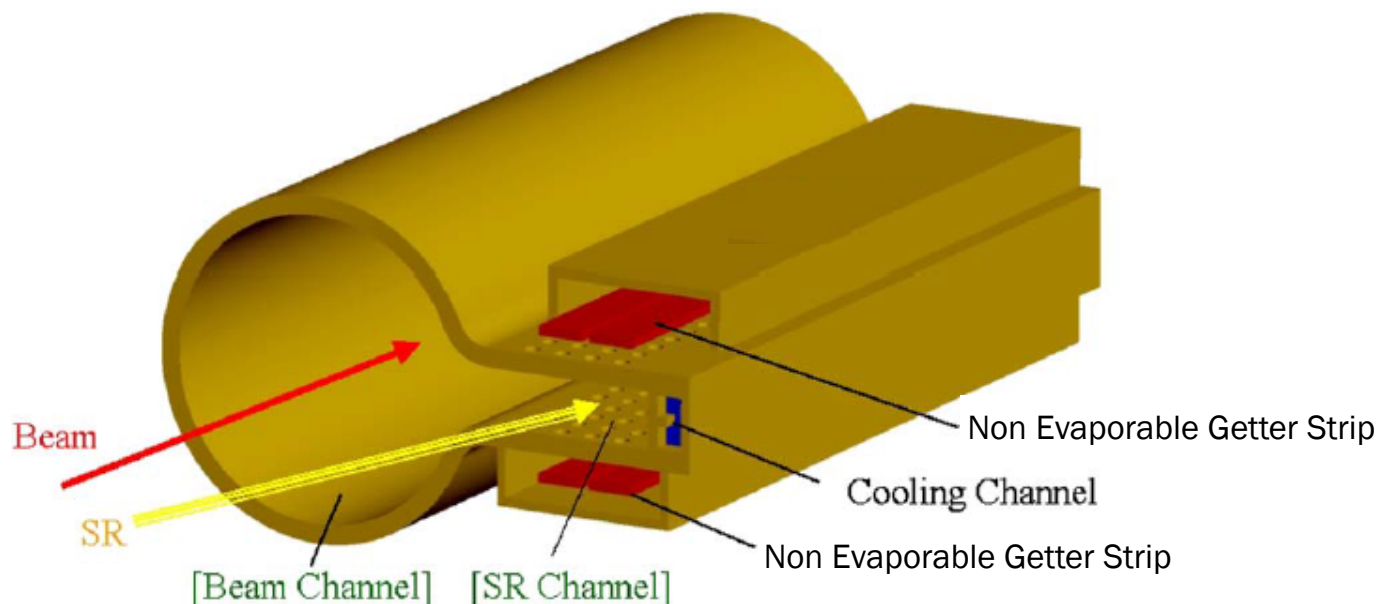
- Why is the beam screen effective in absorption?
- Impedance of the beam pipe; *exciting strong beam instabilities*



P. Cruikshank et al. / Mechanical Design Aspects of the LHC Beam Screen

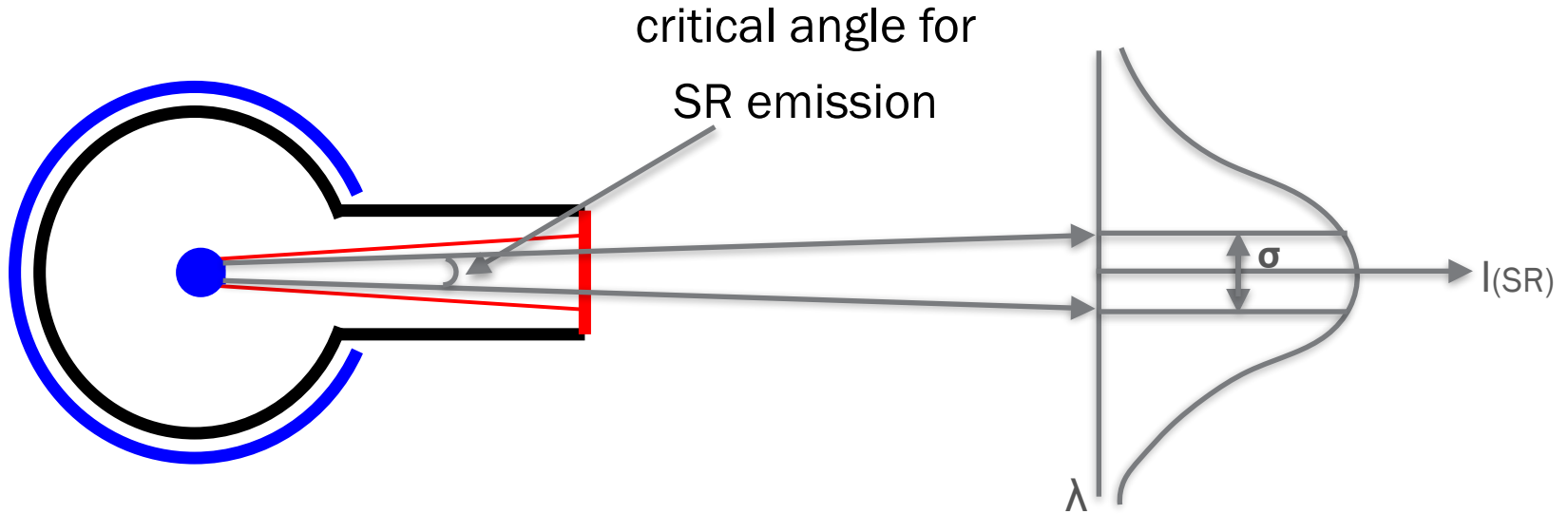
# ANTECHAMBER

- It can reduce the power density of the SR on the walls of the beam pipe:
  - ➔ SR is diluted due to its vertical spread; *the chamber has a wider outer half-aperture*
  - ➔ The horizontal spread contributes to reduce the maximum power density; *SR from bending magnet hits the outside of the magnet*



Y. Suetsugu et al. / Nuclear Instruments and Methods in Physics Research A 538 (2005) 206-217

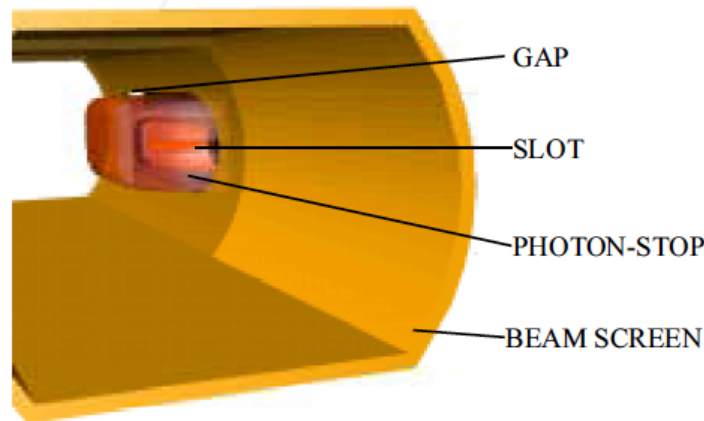
# ANTECHAMBER PARAMETERS



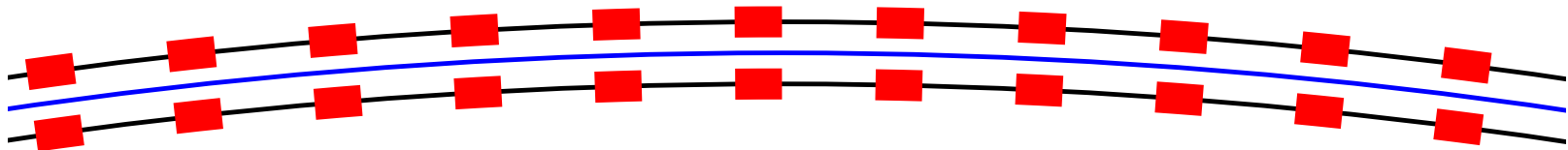
- Small beam impedance:
  - ➔ The effect of the pumping slots on the beam is decreased.
- Reduced photoelectron density in the beam channel; *diminishes the electron cloud effect*

# PHOTON STOP

- Absorbs the SR power at the room temperature with water cooling
- Commonly used in synchrotron light sources



- Inserted in the beam tube at the end of each magnet



*T. K. Kroc/Synchrotron Radiation in the VLHC*

# CONCLUSIONS

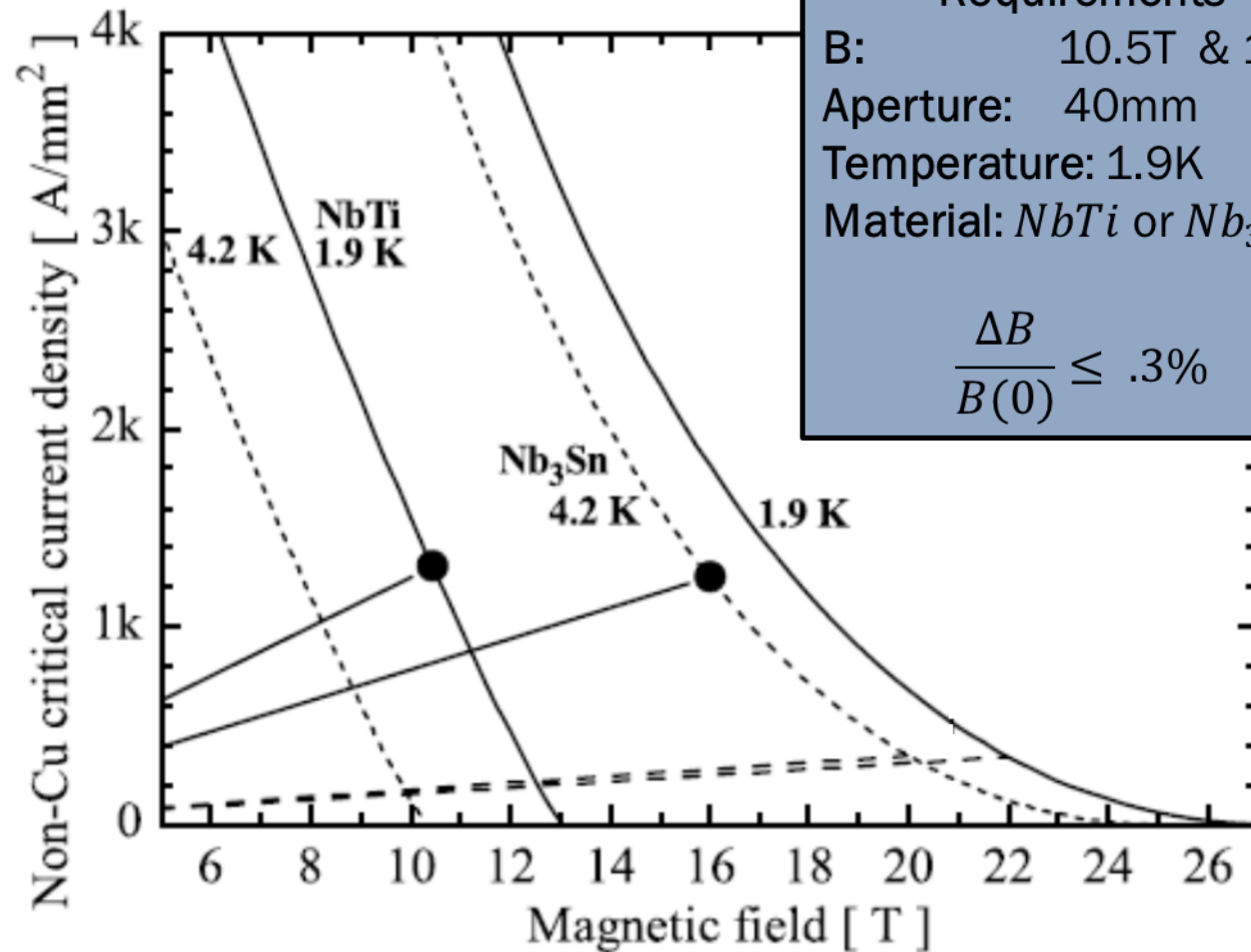
- FCC-hh makes a powerful source of SR with total radiated SR power of 2.18 MW.
- Antechamber and photon stop solutions have been considered for the high SR problem in FCC-hh.
- However, the geometry of the beam pipe also needs to be optimized to minimize the cost of the superconductive magnets.

# MAGNET DESIGN

Alberto Arteche & Rob Shalloo



# DESIGN BRIEF



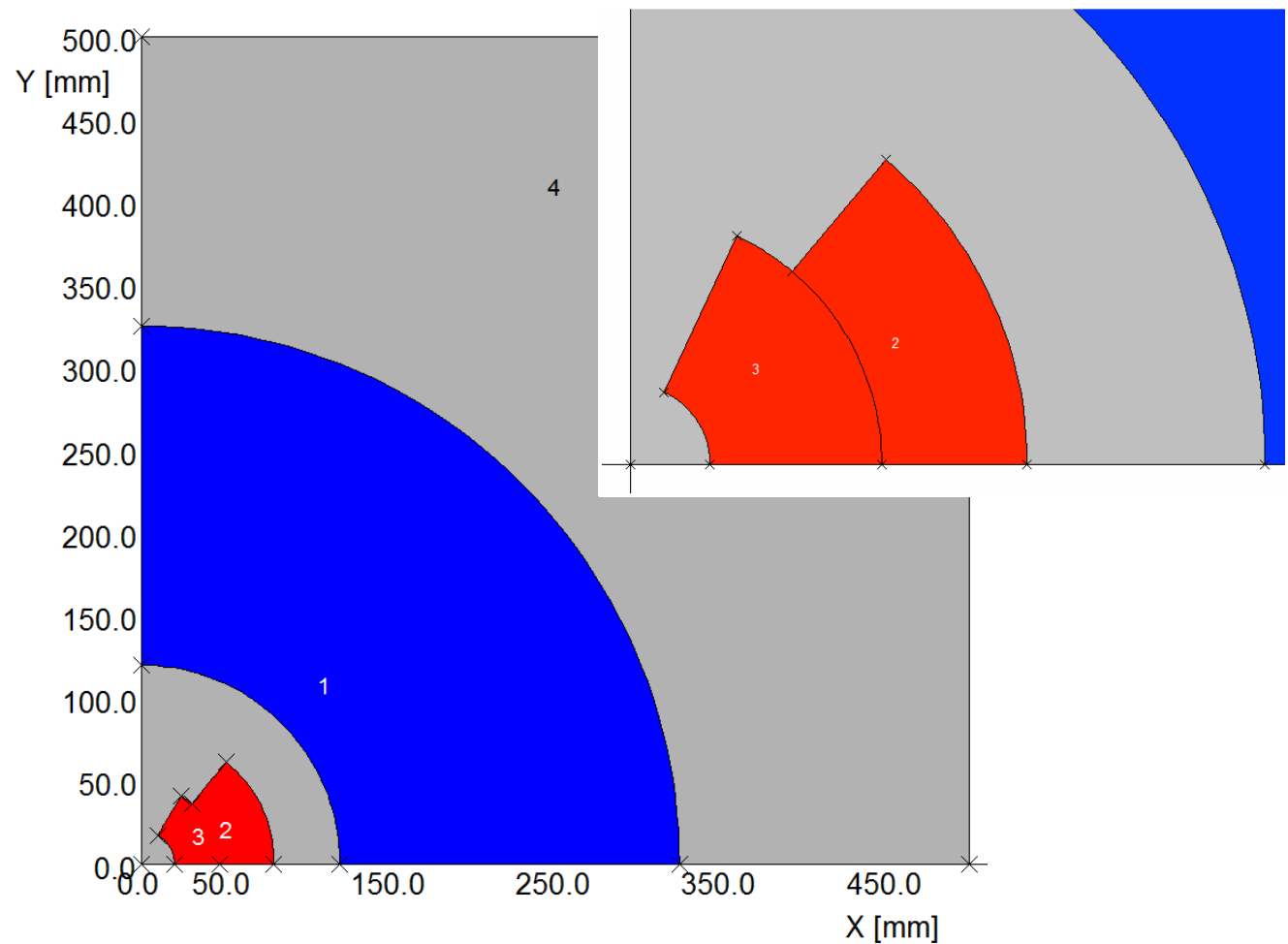
Requirements

B: 10.5T & 16T  
Aperture: 40mm  
Temperature: 1.9K  
Material: *NbTi* or *Nb<sub>3</sub>Sn*

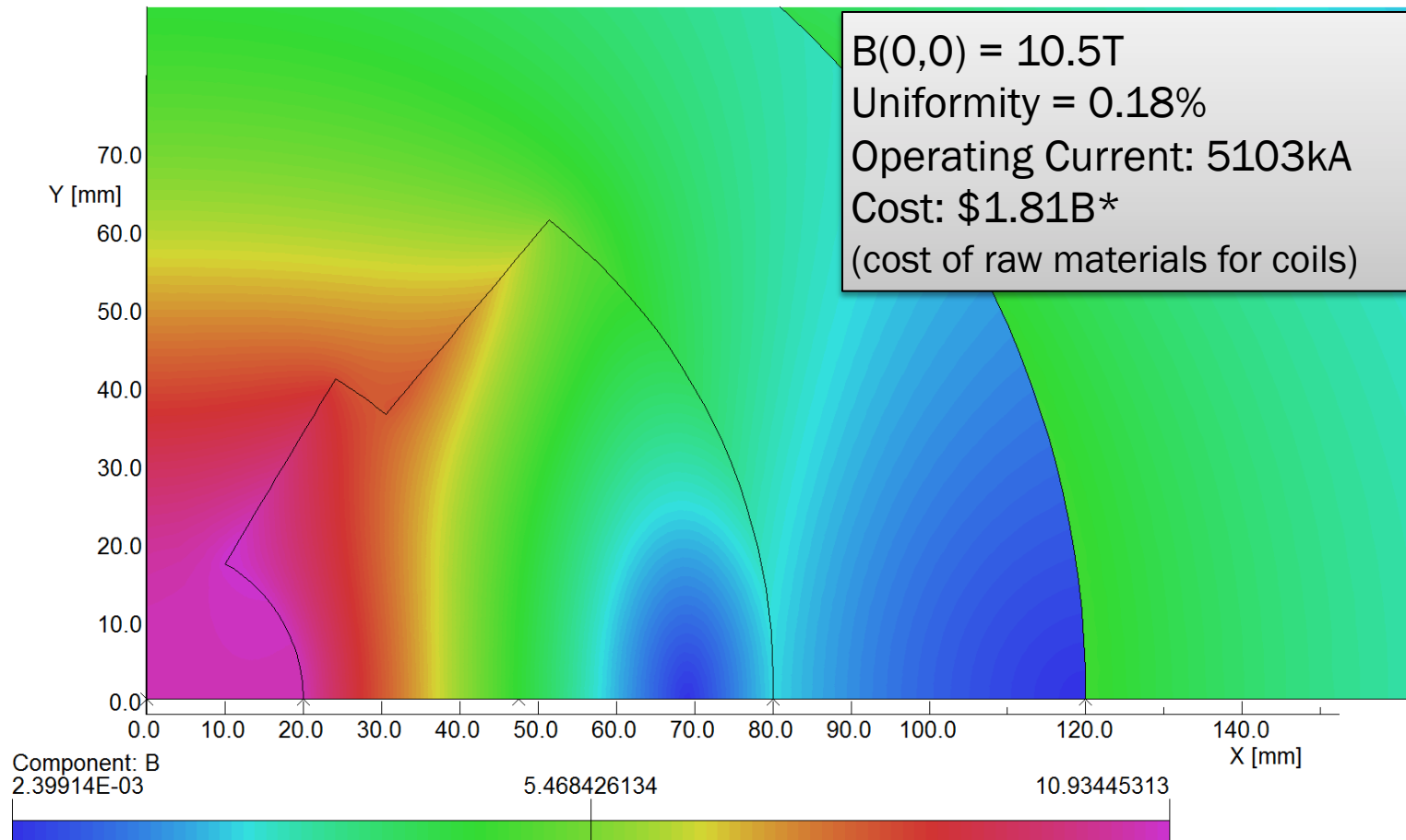
$$\frac{\Delta B}{B(0)} \leq .3\%$$



# SUPERCONDUCTING MAGNETS

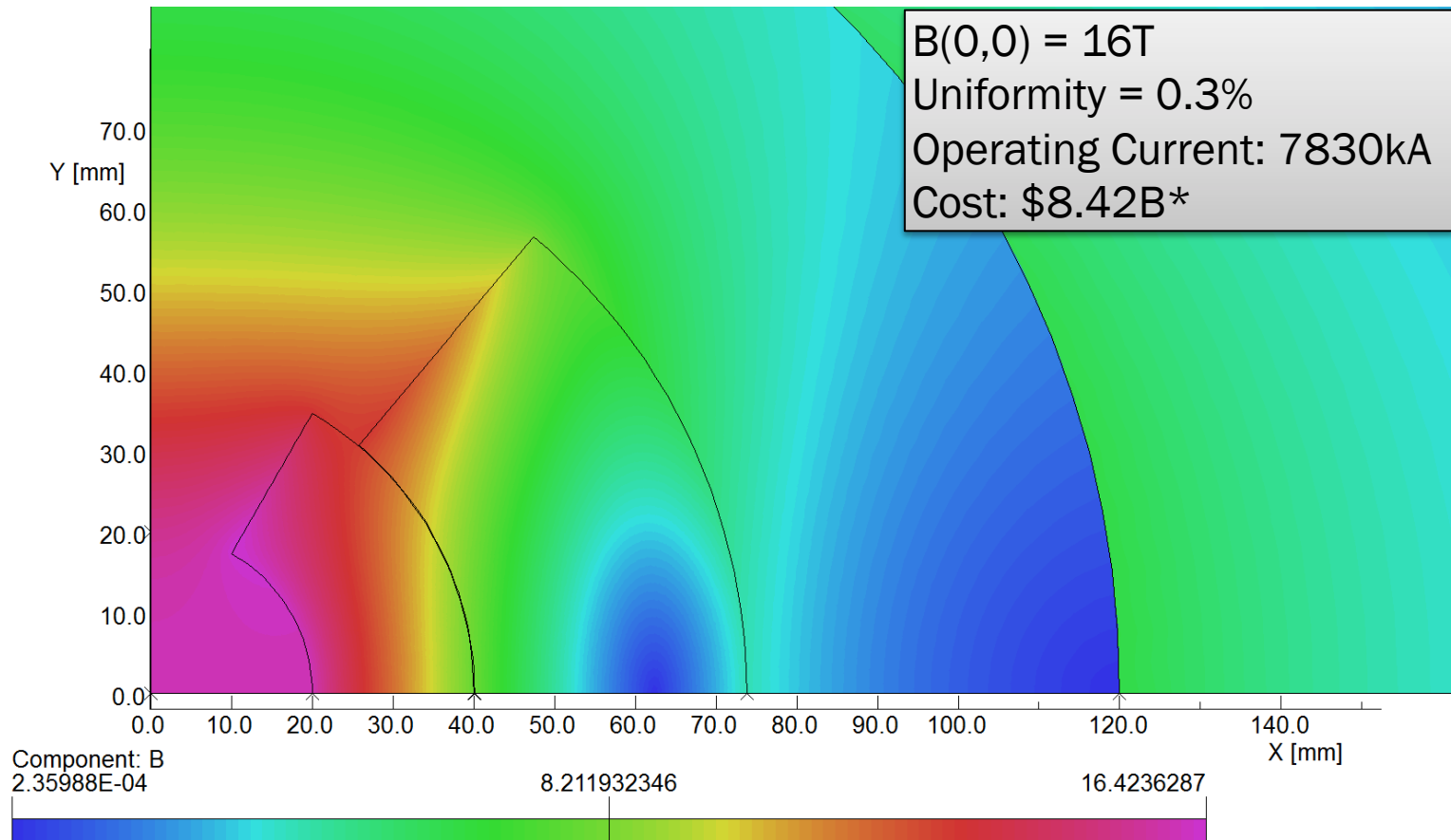


# 10.5T NIOBIUM **TITANIUM**



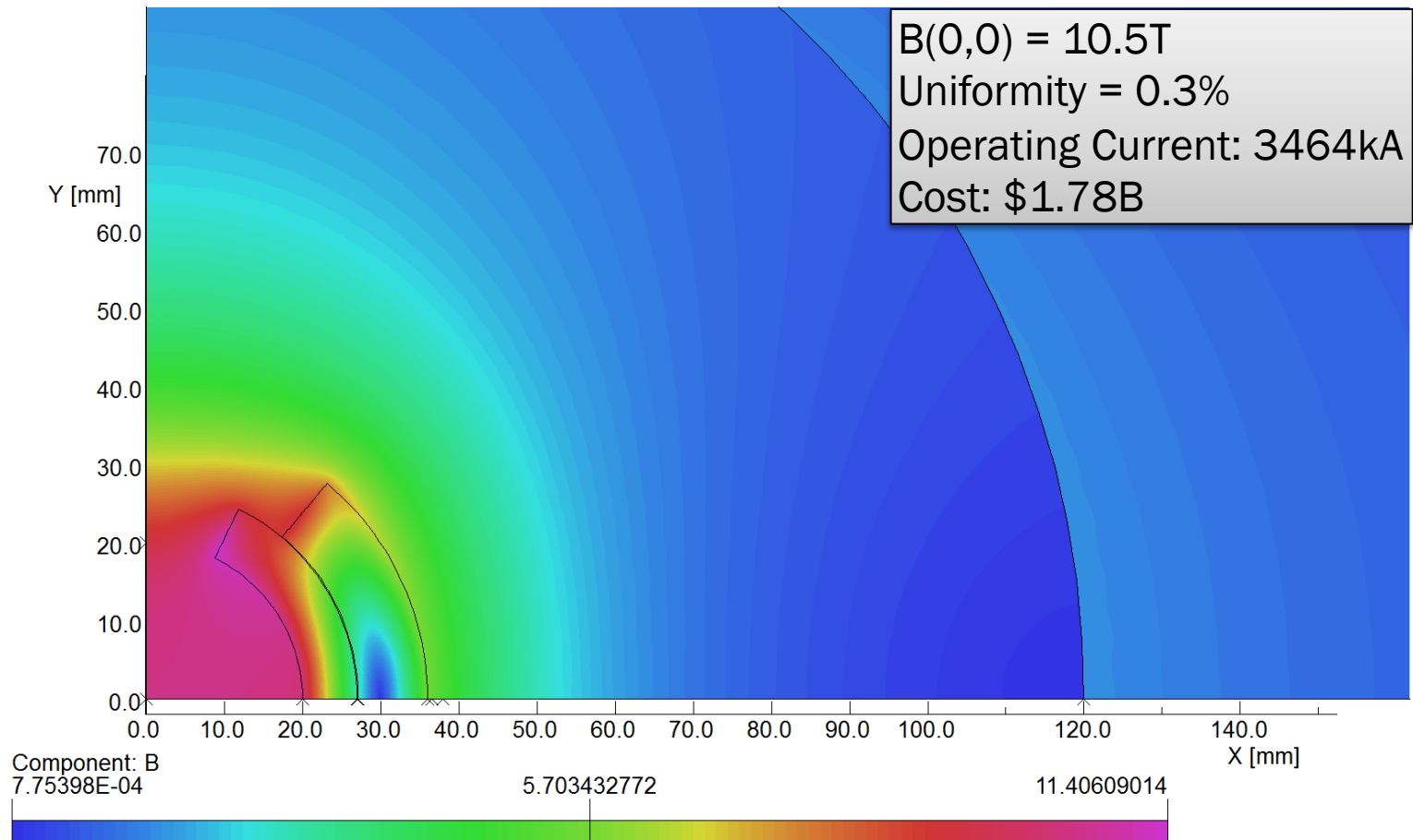
\*L. Rossi and E. Todesco. Conceptual design of 20 T dipoles for high-energy LHC. 2011.

# 16T NIOBIUM **TIN**

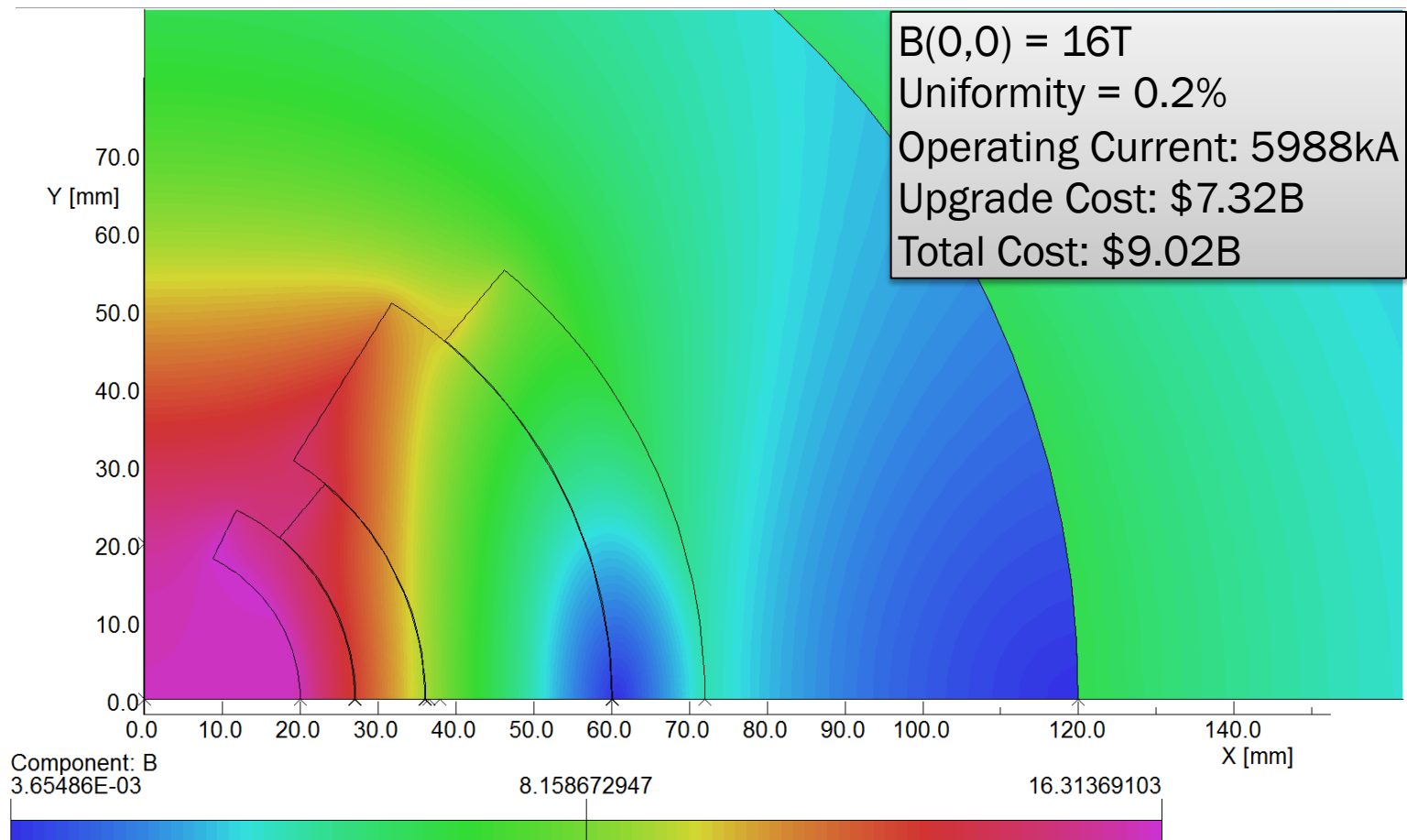


\*L. Rossi and E. Todesco. Conceptual design of 20 T dipoles for high-energy LHC. 2011.

# 10.5T NIOBIUM **TIN**



# (10.5+5.5)T NIOBIUM **TIN**



# CONCLUSION

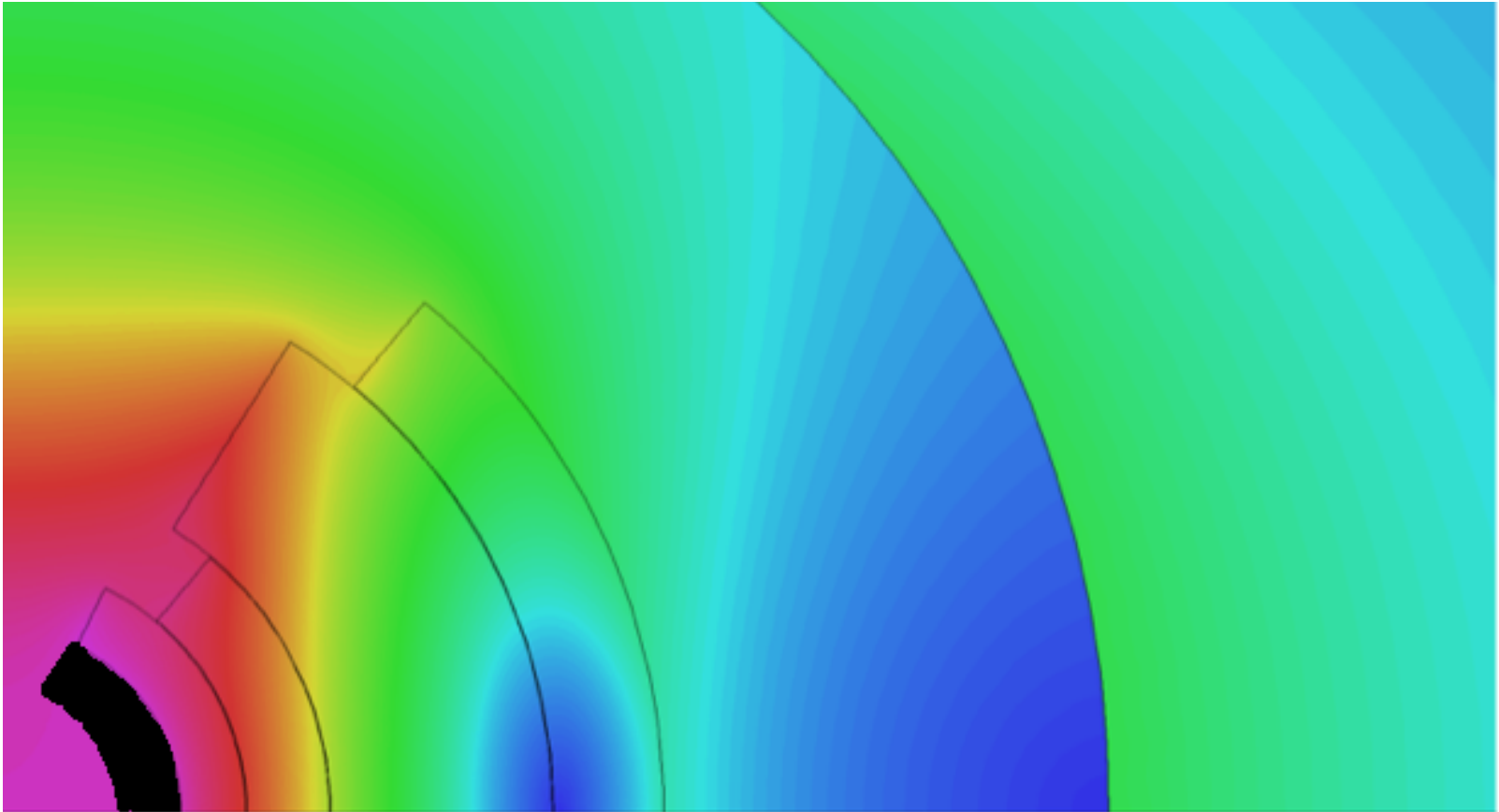
Design	Current (kA)	Amount Required (Tonnes)	Years to Acquire* **	Cost	C.O.M Energy (TeV)
10.5T NbTi	5103	9026	5	\$1.81B	75
16T Nb3Sn	7830	7322	73	\$8.42	100
10.5Nb3Sn	3464	1546	15	\$1.78	75
(10.5+5.5)T Nb3Sn	5988	1546+6363 =7909	15+63 = 78	\$(1.78+7.32)B	100

\* G. Donnier-Valentin – NEEL Institut

\*\* C. Sborchia - ITER Magnet Design

# WHAT IF?

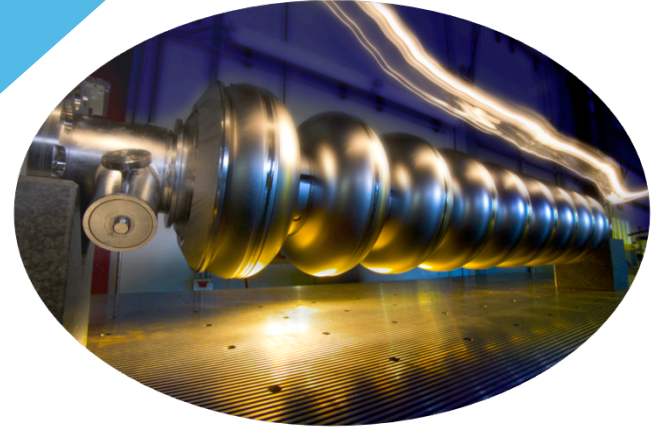
20+T Machine with 30mm Aperture?



# RF CAVITIES

Talitha Bromwich & Huibo Zhang

Superconducting RF cavity  
© Fermilab



## Design of the RF structures for particle acceleration

- Accelerating voltage required per turn
- Optimisation of cavity geometry
- Cavity models in 2D and 3D



# SUPERCONDUCTING ELLIPTICAL RF CAVITY

Calculating total RF voltage per turn required to meet accelerator design parameters

Ring circumference	100 km
Max KE (per beam)	50 TeV
Max field strength	16 T
Max injection energy	3.3 TeV
Magnetic field ramp time	25 minutes
Phase	70 degrees
Accelerating gradient	20 MV/m
Accelerating frequency	400.8 MHz
Accelerating voltage	29.8 MV/turn
SR energy loss	4.67 MeV/turn
Total voltage	34.2 MV/turn



*Nine-cell Niobium superconducting cavity © ILC*

- ← Match LHC timing
- ← SC cavity frontier
- ← Match LHC RF system

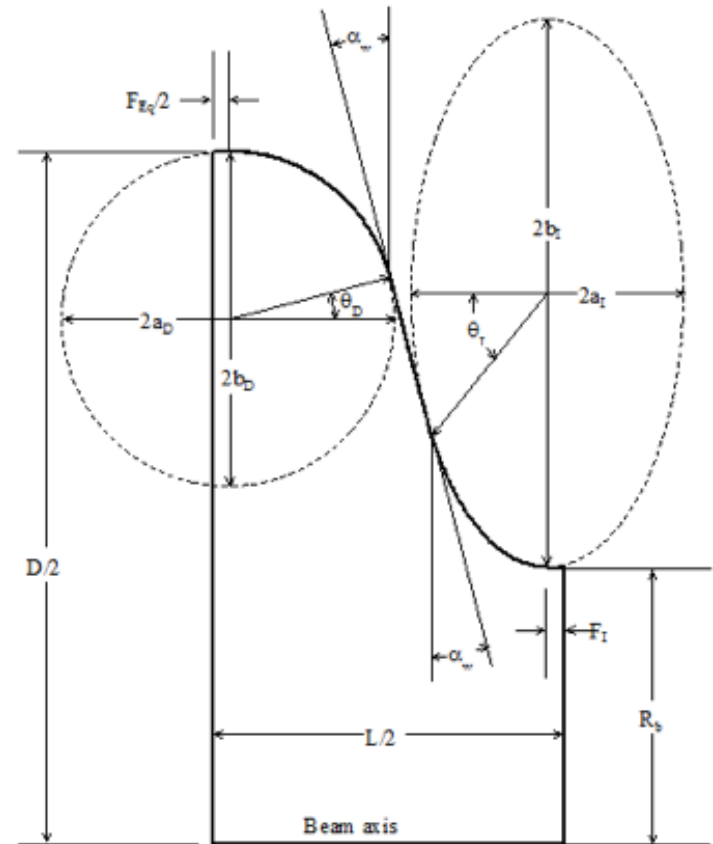
# CAVITY GEOMETRY OPTIMISATION

## FACTORS TO CONSIDER:

- **Electric field on cavity surface** - high fields might cause electric breakdown or field emission – *minimise and avoid peaks*
- **Magnetic field on cavity surface** - high field peaks might cause quenching or thermal breakdown – *minimise and avoid peaks*
- **Quality factor  $Q$**  – ratio of the stored energy in the cavity to energy dissipated along the walls - *maximise*
- **$E_{\max}/E_0$**  – *minimise*

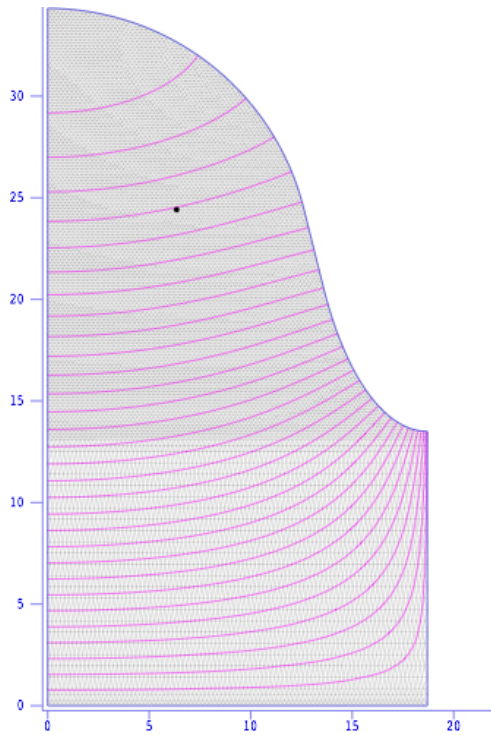
## TRY ALTERING:

- **Iris ratio  $a/b$**
- **Dome ratio  $a/b$  and dome height**

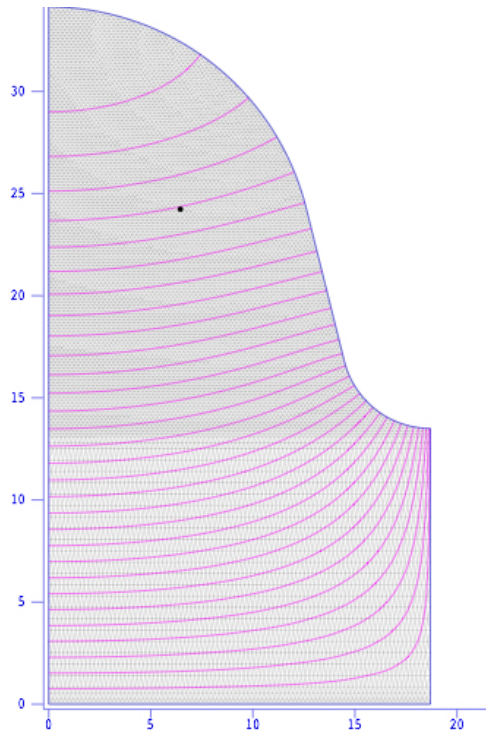


# IRIS SHAPE OPTIMISATION

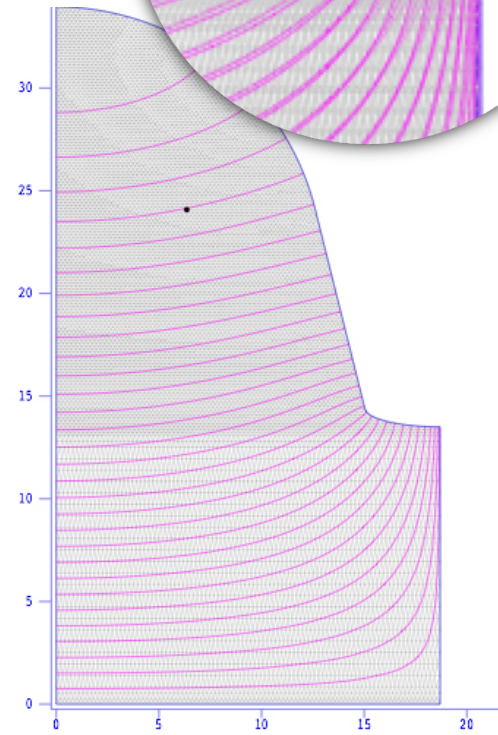
Examples of varying iris a/b ratio to change cavity geometry



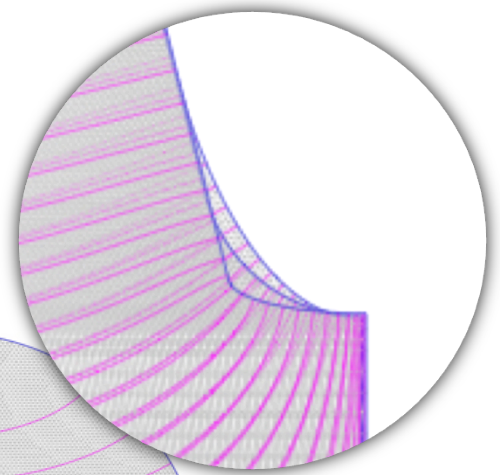
0.4



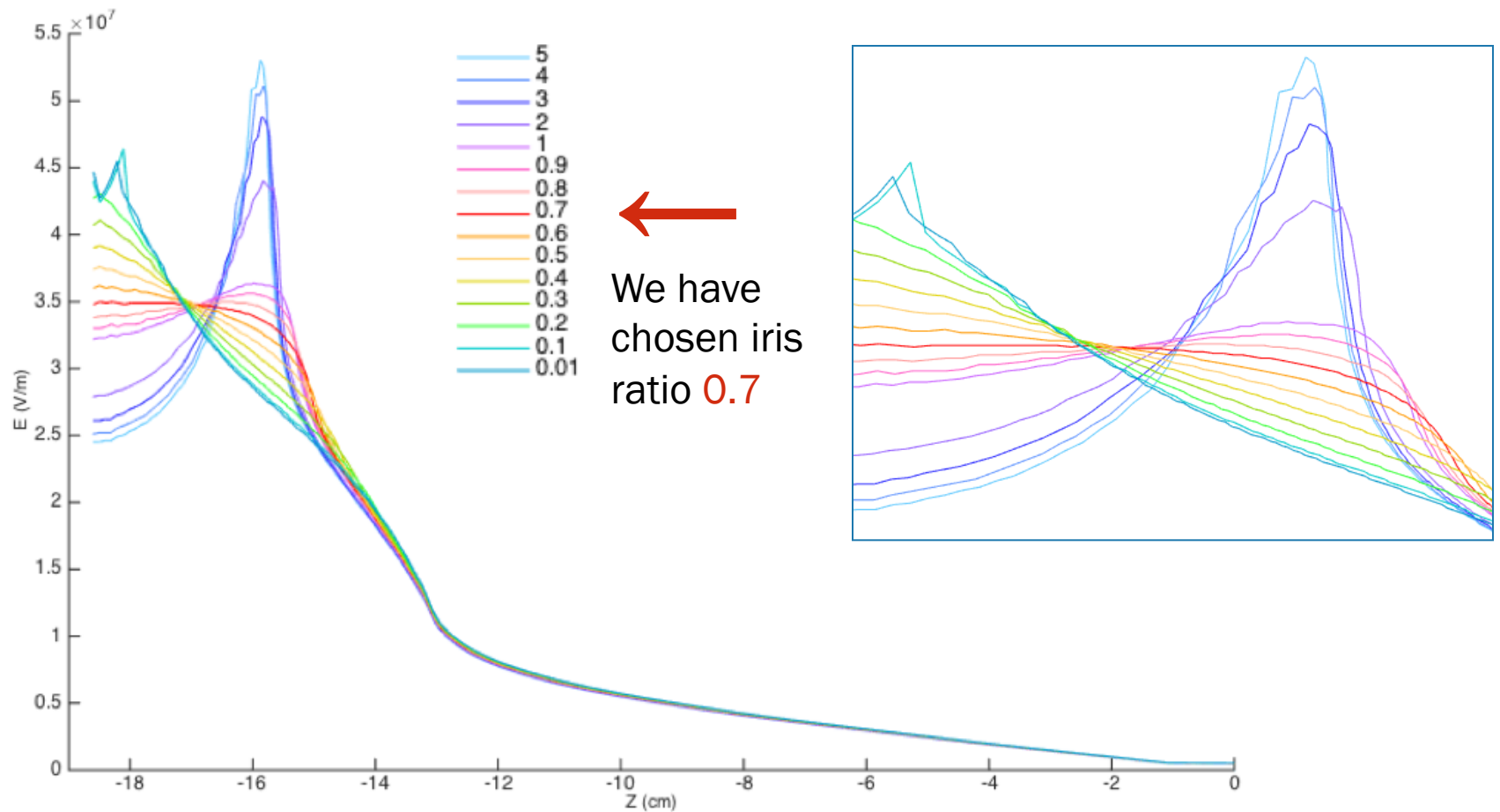
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4

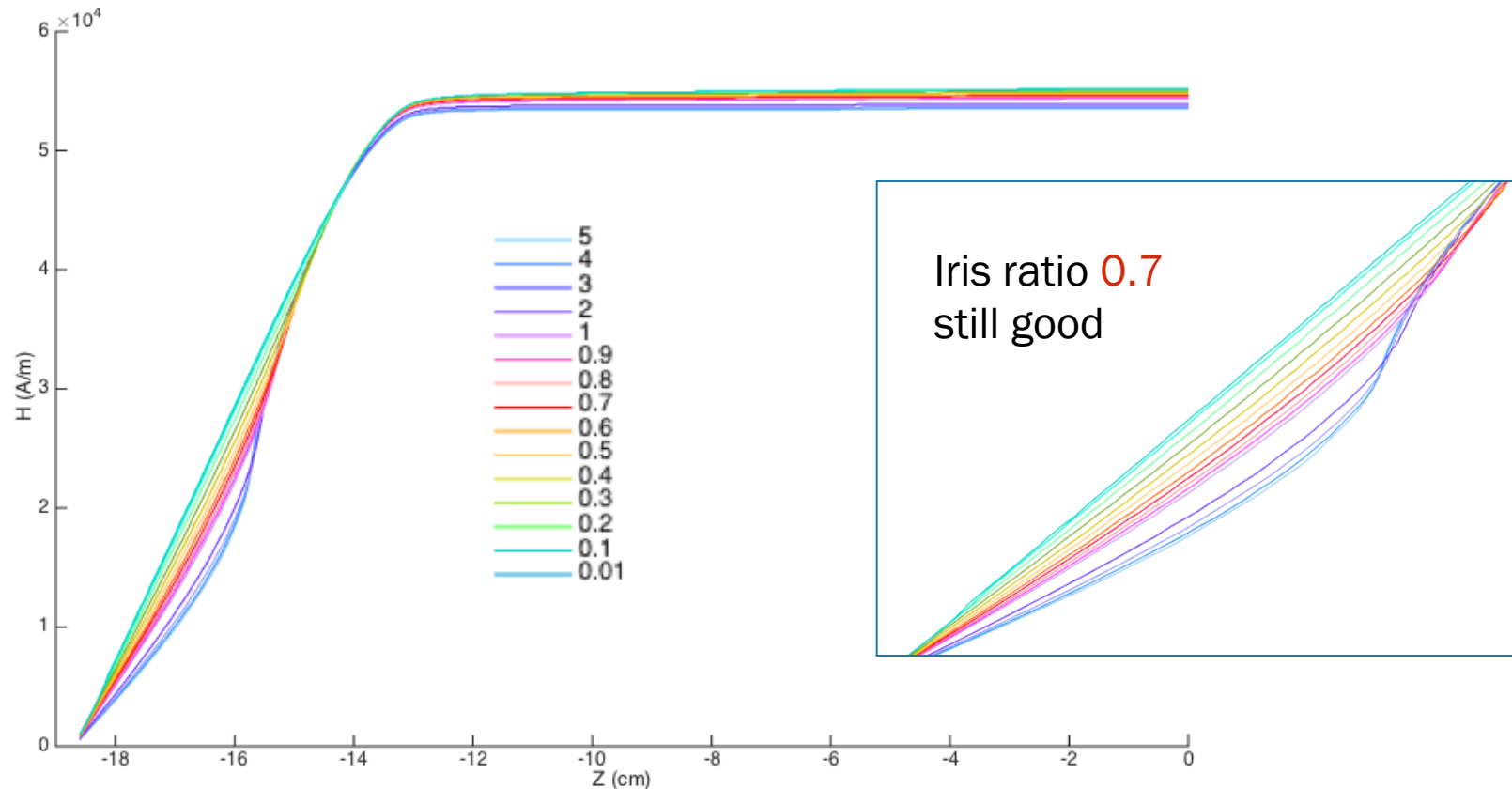


# IRIS OPTIMISATION: E FIELD ON SURFACE

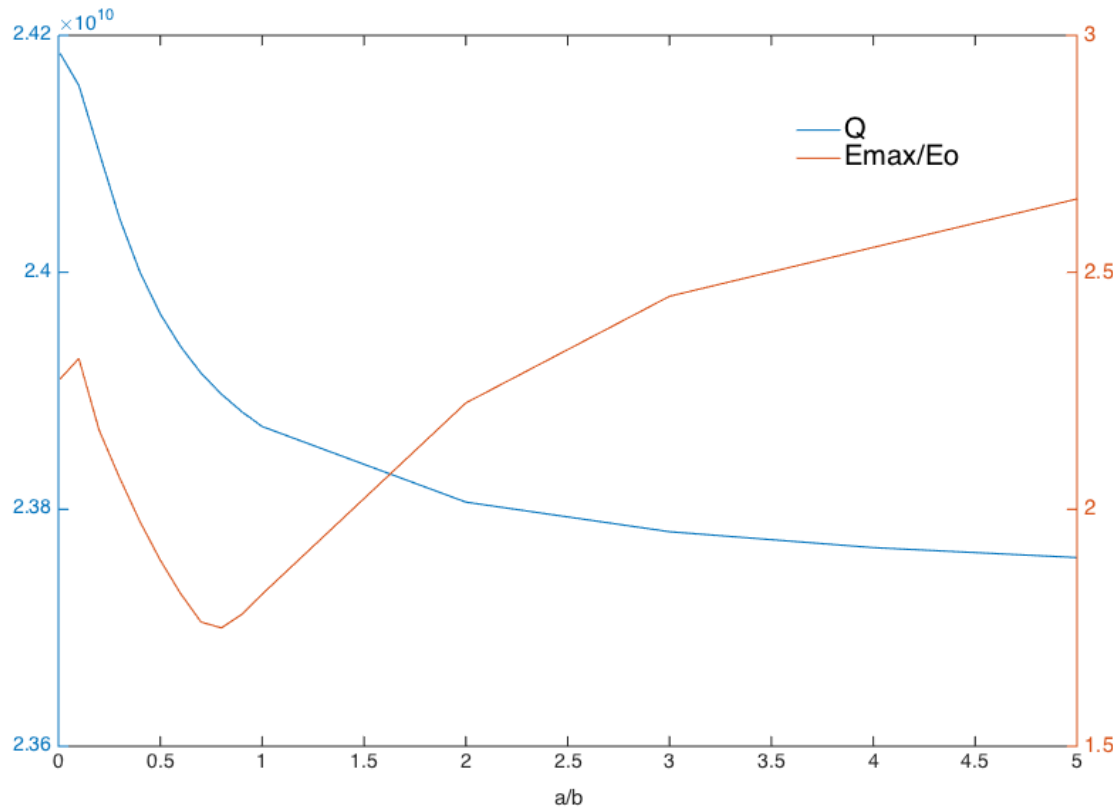


# IRIS OPTIMISATION: MAG FIELD ON SURFACE

All values acceptable - the surface magnetic field does not seem to vary significantly very much with changing iris dimensions



# IRIS OPTIMISATION: CAVITY Q AND $E_{\text{MAX}}/E_0$



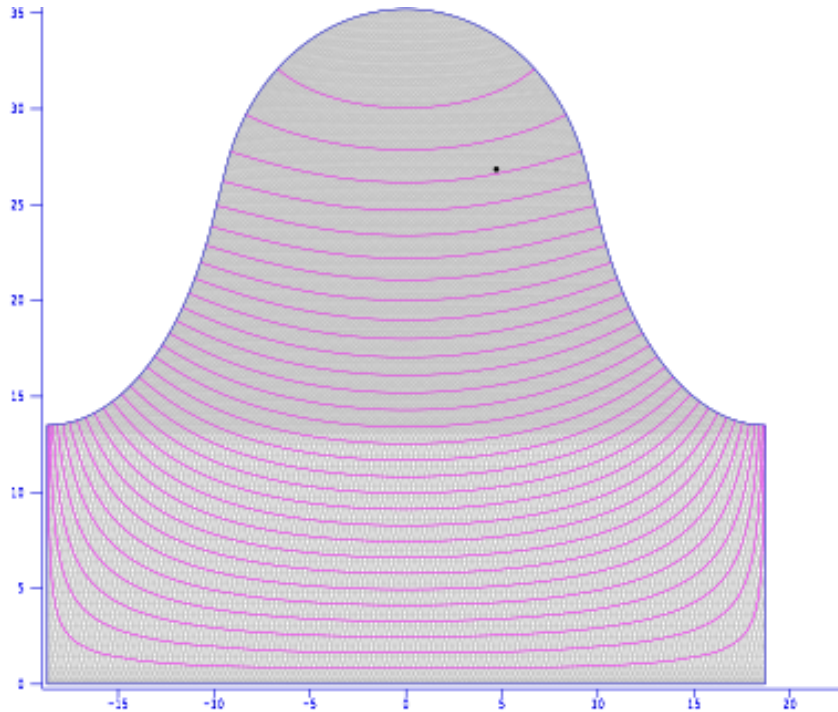
**0.7** is a good compromise between maximising Q and minimising  $E_{\text{MAX}}/E_0$

**IRIS RATIO: 0.7**

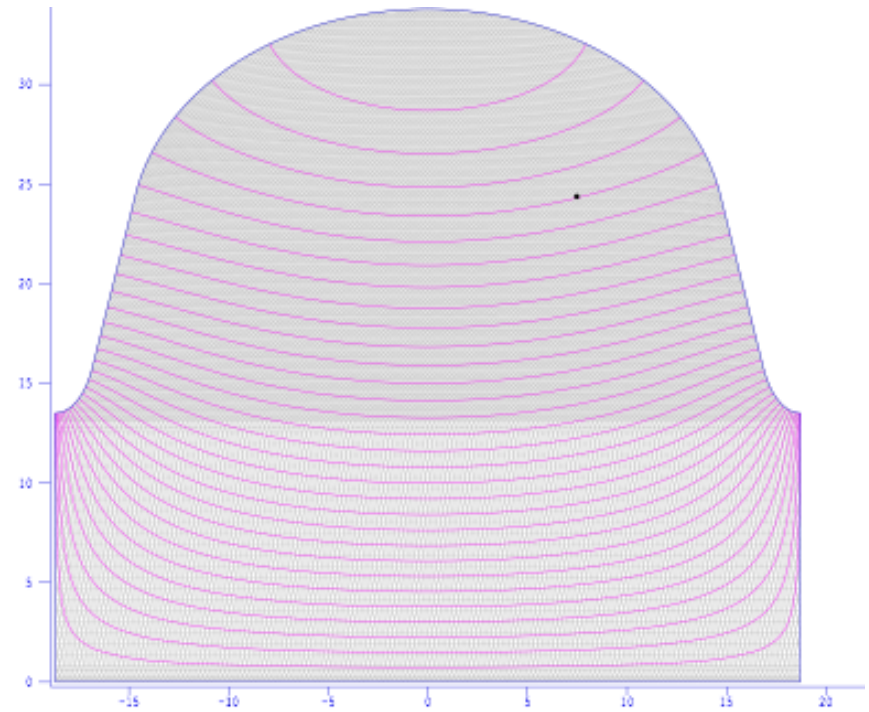


# DOME SHAPE OPTIMISATION

Examples of varying dome a/b ratio and changes to the cavity geometry



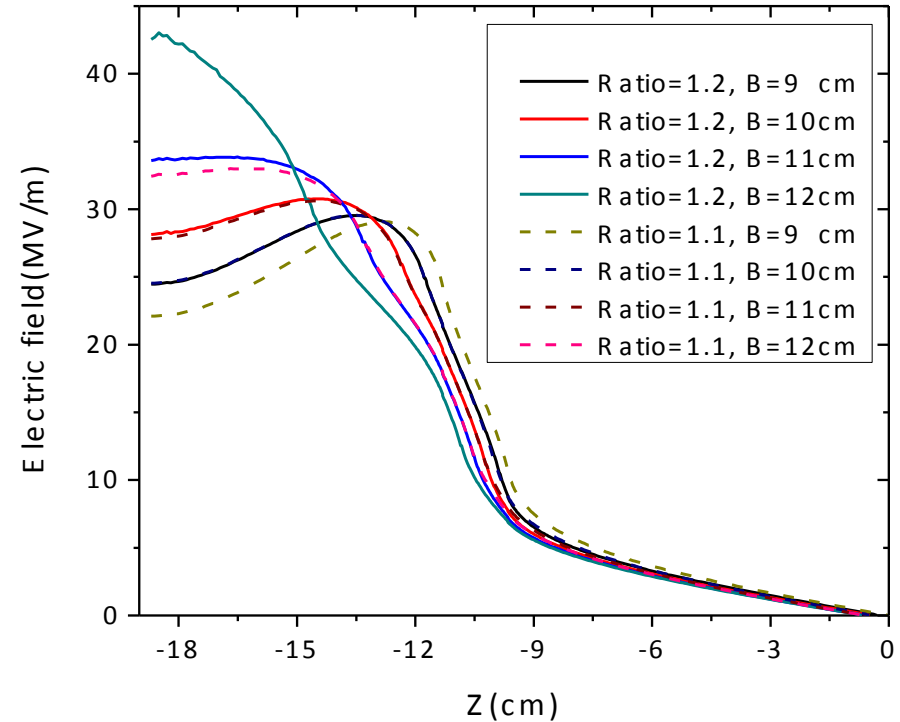
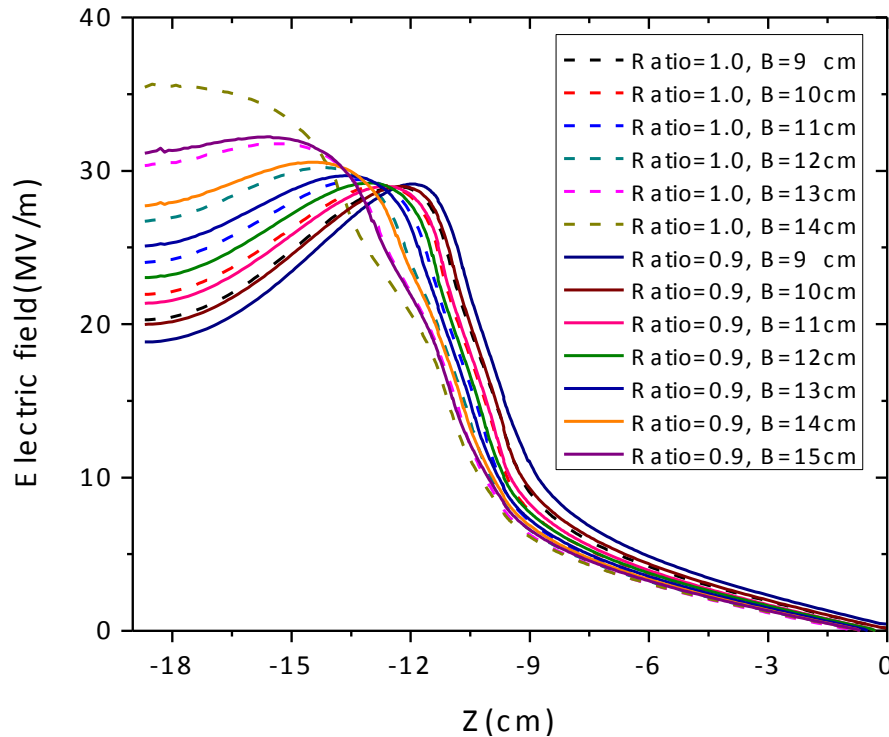
Dome  $a/b = 0.85$



Dome  $a/b = 1.3$

# DOME OPTIMISATION: E FIELD ON SURFACE

Dome ratio varied 0.9 to 1.2, dome height 9 cm to 15 cm, iris ratio fixed at 0.7



Fixed dome ratio: maximum electric field increases with the increasing of dome height

Fixed dome height: the maximum electric field increases with the increasing of dome ratio



# DOME OPTIMISATION

Optimal dome geometry combinations to avoid electric field peaks on the surface

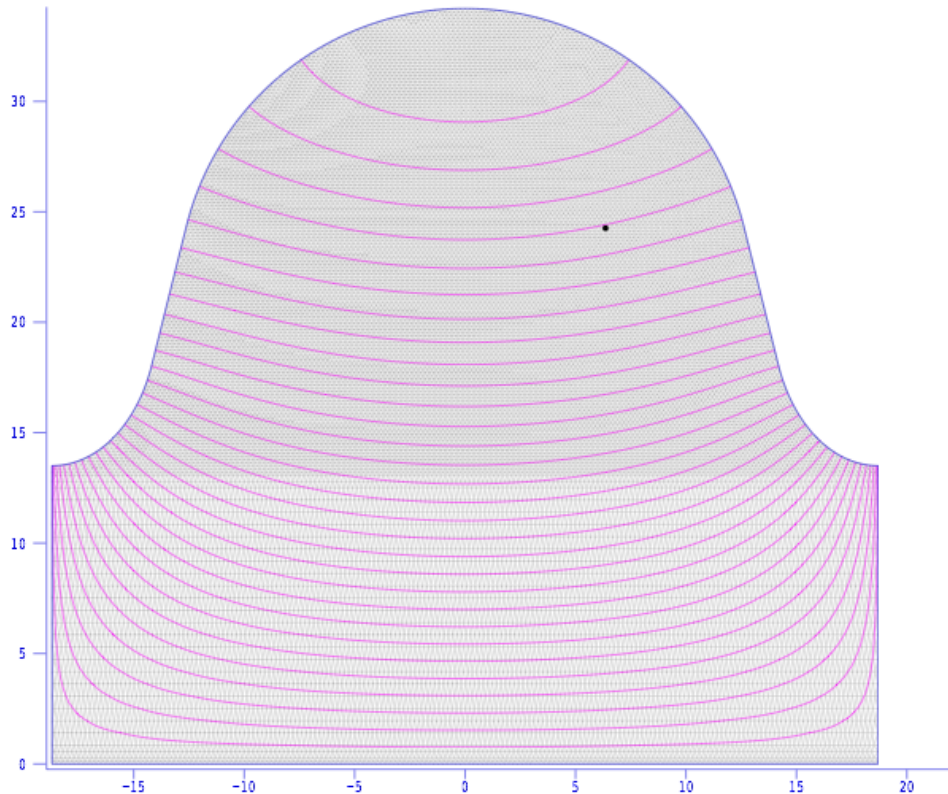
	$E_{\max}$	$Q$ (E+11)	$E_{\max}/E_0$
dome ratio=0.9, dome height=15cm	32.415	0.2336	1.621
dome ratio=1.0, dome height=13cm	31.98	0.2323	1.599
dome ratio=1.1, dome height=12cm	33.208	0.236	1.6615
dome ratio=1.2, dome height=11cm	34.153	0.2377	1.7072

Weighting of geometric parameters is complex: concentrate on reducing electric field on the surface, maximising  $Q$  and minimising  $E_{\max}/E_0$

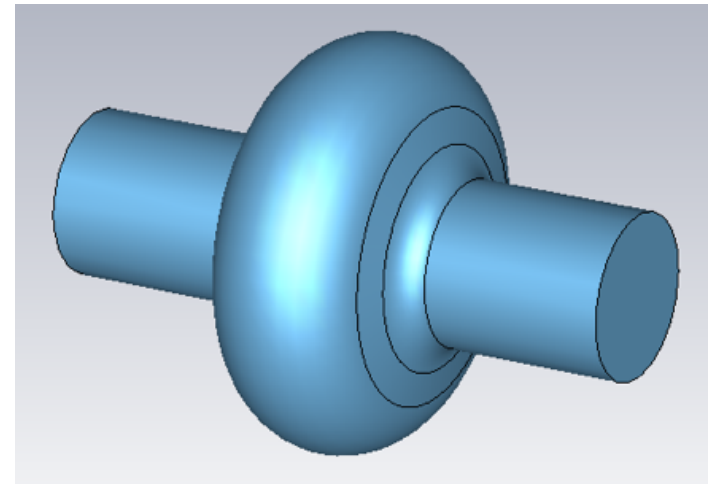
**DOME RATIO 1.0, DOME HEIGHT 13 CM**

# CAVITY DESIGN

Single-cell elliptical cavity modelled in 2D  
Superfish and 3D in CST Studio



Diameter	68.415 cm
Length	37.399 cm
Iris ratio $a/b$	0.7
Iris horiz half axis $a$	4.79 cm
Iris vert half axis $b$	6.85 cm
Dome vert half axis $a$	13 cm
Dome $a/b$	1.0



# CAVITY DESIGN PARAMETERS

	<i>Our cavity</i>	<i>TESLA cavity</i>
Accelerating structure	Standing wave	Standing wave
Accelerating mode	TM <sub>010</sub> , Pi mode	TM <sub>010</sub> , Pi mode
Fundamental frequency	400.8 MHz	1300 MHz
Accelerating gradient	20 MV/m	25 MV/m
Quality factor	$2.323 \times 10^{10}$	$> 5 \times 10^9$
Active length	2.618 m	1.038 m
Geometry factor	269.440 Ohm	270 Ohm
R/Q	48.256 Ohm	518 Ohm
E <sub>max</sub> /E <sub>0</sub>	1.599	2
B <sub>max</sub> /E <sub>0</sub>	3.53 mT/(MV/m)	4.26 mT/(MV/m)

*B. Aune, et al, The Superconducting TESLA cavity, Phys.Rev.ST Accel.Beams (2000)*

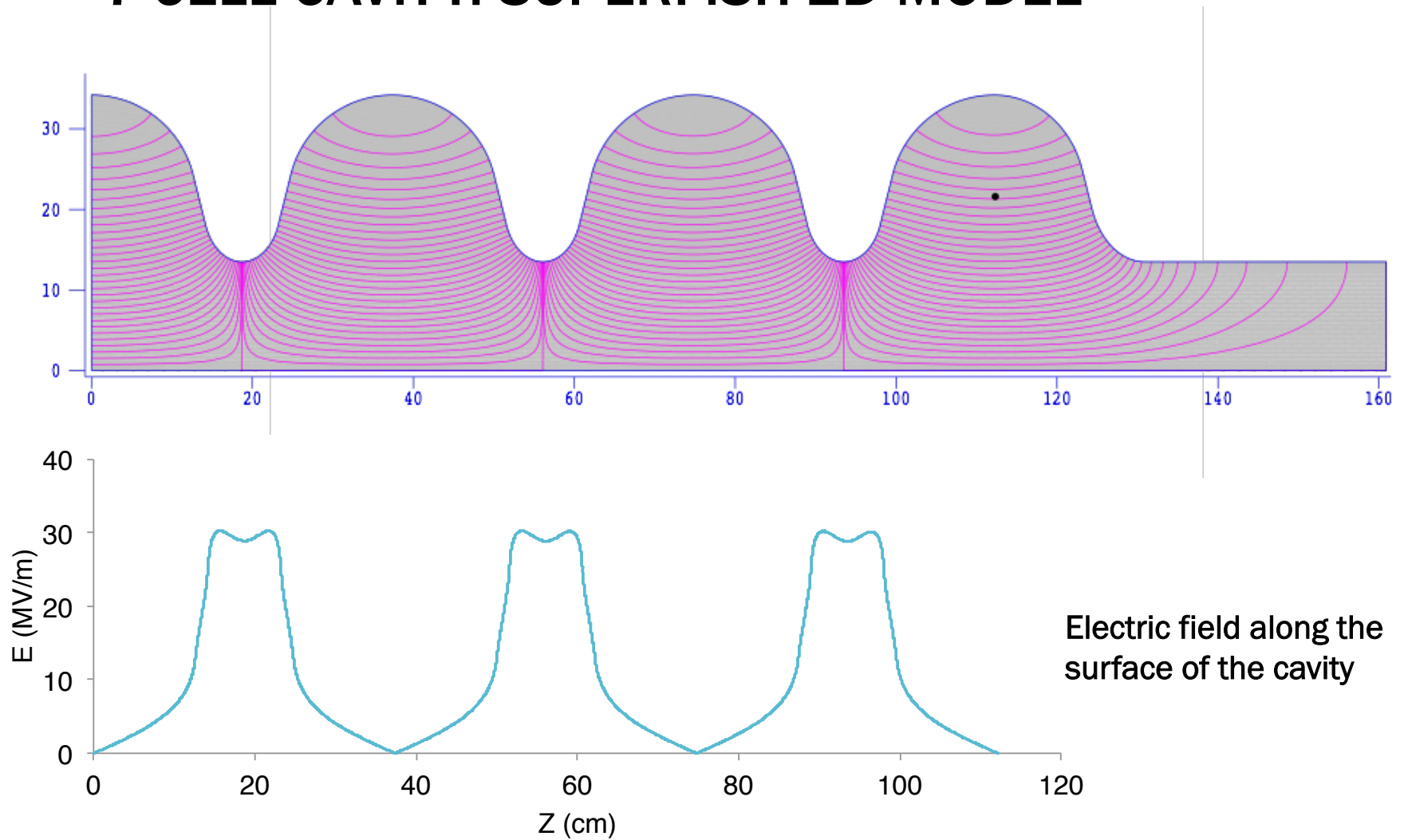
# ACCELERATING GRADIENTS

Number of cells required to achieve 34.2 MV/turn with different accelerating gradients

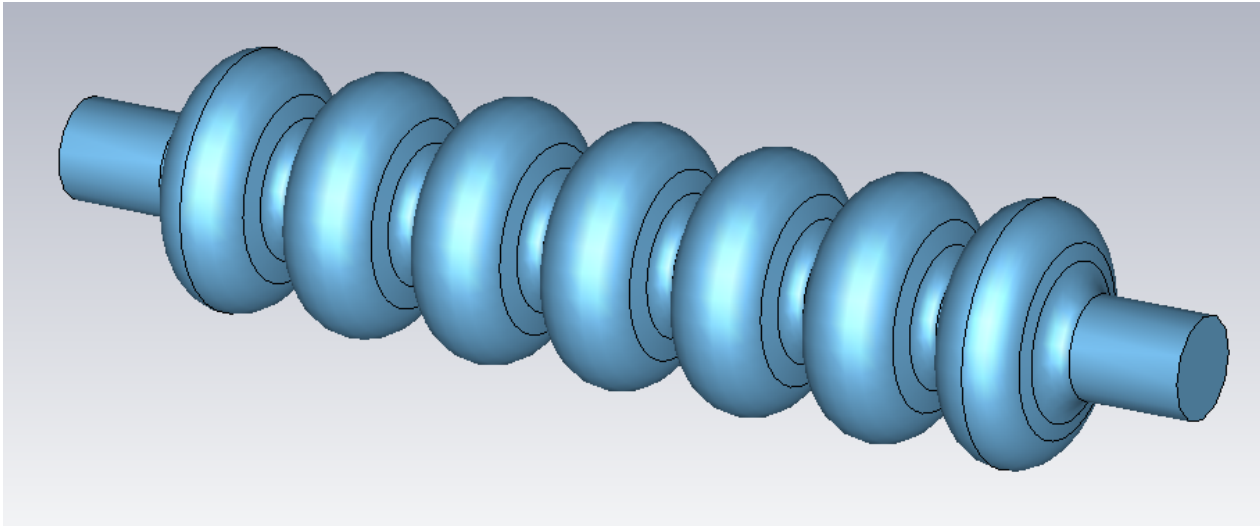
ACCELERATING VOLTAGE GRADIENTS	5 MV/m	10 MV/m	20MV/m	31.5MV/m
Voltage per cell (MV)	1.87	3.74	7.48	11.8
Transit Time Factor	0.778398	0.778398	0.778398	0.778398
Effective Voltage (MV)	1.37	2.74	5.47	8.62
No. cells	25	13	7	5

We have chosen **20 MV/m** for our model, as it minimises RF space - which in the FCC-ee (~500 cavities) is vital - and is on the frontier of the superconducting RF cavity technology, soon to be achievable at the 400.8MHz accelerating frequency

# 7-CELL CAVITY: SUPERFISH 2D MODEL

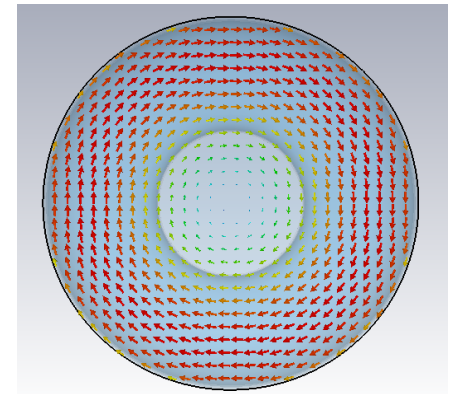
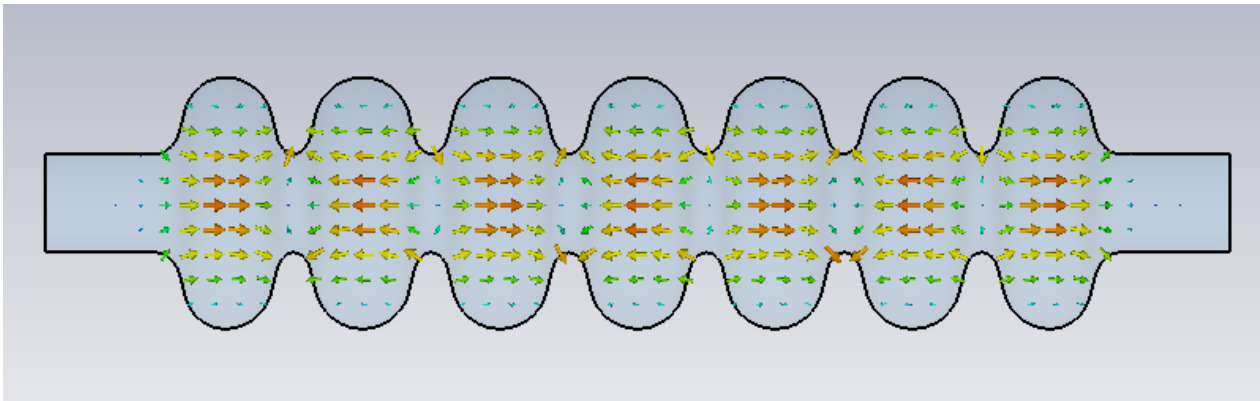


# 7-CELL CAVITY 3D MODEL: CST STUDIO



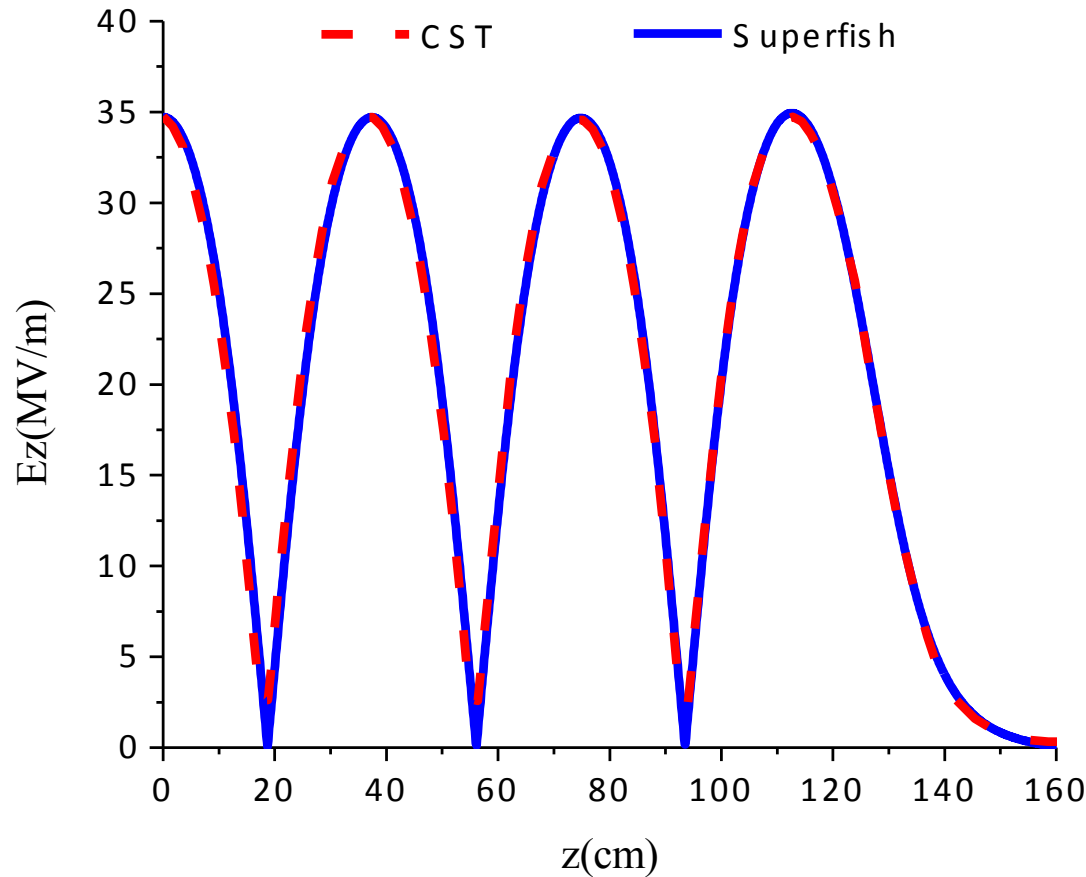
ACCELERATING MODE  
FREQUENCY

400.7886 MHz



# 2D & 3D ACCELERATING FIELD

Comparing the accelerating electric field strength of the SUPERFISH and CST STUDIO models on the axis of the cavity



Good agreement!

# CONCLUSIONS

- Calculated accelerating voltage required - **34.2 MV/turn**.
- Optimised the cavity geometry to achieve this at 400.8MHz by altering elliptical cavity **iris** and **dome** shape to **minimise peak electric and magnetic fields**, and **maximise quality factor, Q**.
- 2D and 3D models in Superfish and CST Studio.
- Good agreement between models.
- Also shown cavity model is quite flexible and can be adjusted in geometry and number of cells to accommodate different voltage requirements and accelerating gradients etc.



# CONCLUSION

Hannah Harrison

- Ideas proposed
- Physics Implications

# IDEAS PROPOSED

- **Lattice design** → reduction of aperture from 40mm to 30mm without reduction in beam energy
- **Instabilities** → loss of luminosity and huge increase in instabilities for aperture reduction from 40mm to 30mm
- **Magnet design** → high costs of installing Nb<sub>3</sub>Sn dipoles, two solutions proposed - both at lower energy of 80TeV
- **RF cavities** → flexible to changes to design, don't impose constraints on the machine

# IMPORTANCE OF...

- **High Energies**

- Higher masses

- As a rule of thumb →

*“At fixed luminosity, discovery reach scales like  $2/3$   $E_{beam}$ ” (Presentation – Mangano (2014) CERN)*

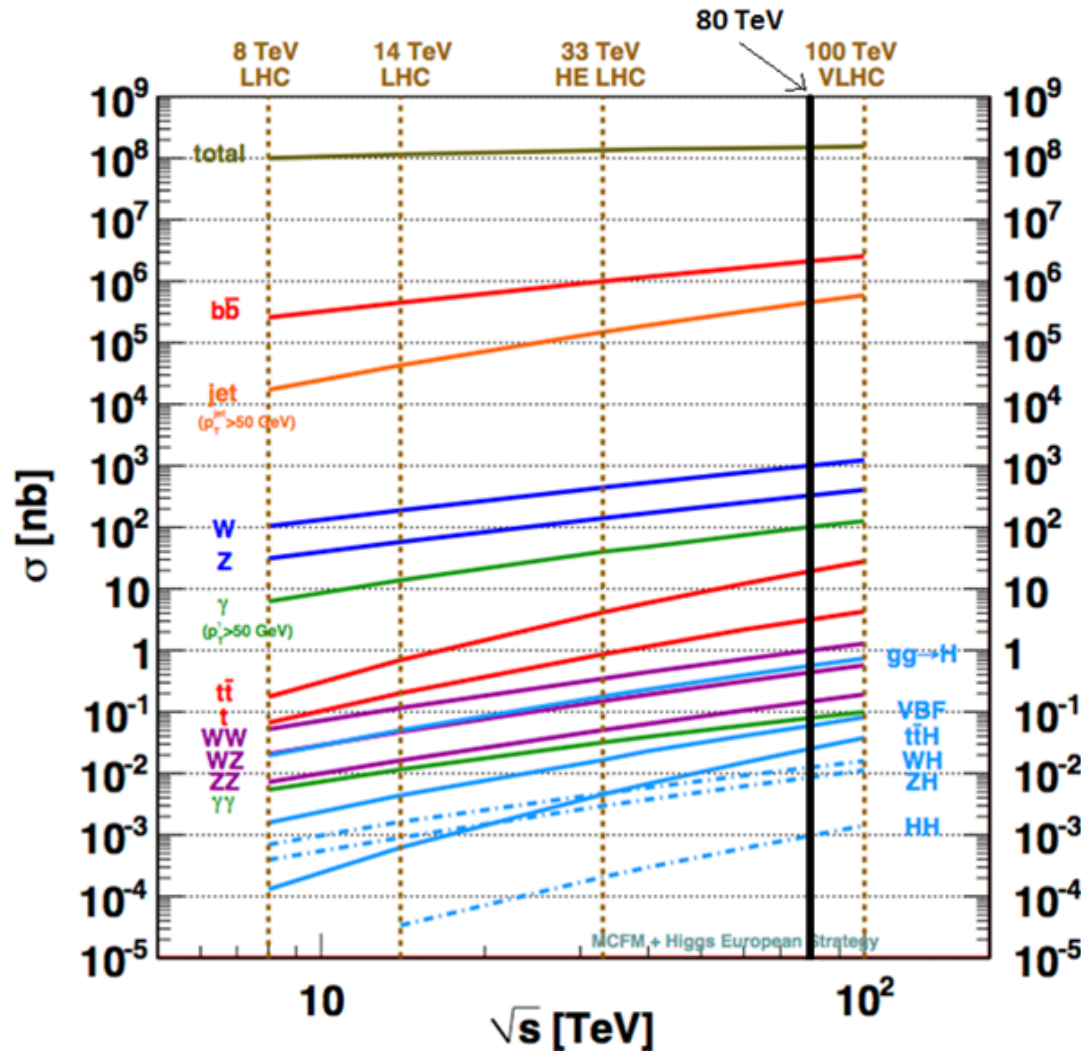
- **High Luminosities**

- Smaller Couplings (for smaller masses)

- *Luminosity particularly important as it is unknown if any particles of higher mass will be discovered.*

- The suggested changes to the Aperture would result in a large drop in luminosity → a possible deal breaker from a physics perspective

# CONSEQUENCES OF LOWERING THE ENERGY



Cross section predictions at proton-proton colliders as a function of centre-of-mass operating energy  $\sqrt{s}$

From: Report of the Snowmass 2013 energy frontier QCD working group

Campbell et al.

# CONSEQUENCES OF LOWERING THE ENERGY

Process	$\sigma(14 \text{ TeV})$	R(33)	R(40)	R(60)	R(80)	R(100)
$gg \rightarrow H$	50.4 pb	3.5	4.6	7.8	11	15
$qq \rightarrow qqH$	4.40 pb	3.8	5.2	9.3	14	19
$q\bar{q} \rightarrow WH$	1.63 pb	2.9	3.6	5.7	7.7	10
$q\bar{q} \rightarrow ZH$	0.90 pb	3.3	4.2	6.8	10	13
$pp \rightarrow HH$	33.8 fb	6.1	8.8	18	29	42
$pp \rightarrow ttH$	0.62 pb	7.3	11	24	41	61

Evolution of the cross sections for different Higgs production processes in  $pp$  collisions with centre-of-mass energy. The cross sections at  $\sqrt{S} = 14\text{TeV}$  are given in the 2<sup>nd</sup> column and the ratios  $R(E) = \frac{\sigma(E \text{ TeV})}{\sigma(E=14\text{TeV})}$  in the following columns. All rates assume  $M_H = 125 \text{ GeV}$  and SM couplings.

From: Future hadron Colliders – From physics perspectives to technology R&D. Barletta et al. (2014)

# FINAL CONCLUSIONS

- **Analysis of various aspects of the FCC-hh design**
  - Lattice Design
  - Instabilities
  - Magnet Design
  - RF cavities
- **Considered possible alterations to the original design proposal**
  - Aperture Reduction
  - Change of superconducting material
  - Proposal of phased construction to limit initial costs
- **Highlighted various issues and limiting factors facing the project**
  - High cost of constructing dipoles with Nb<sub>3</sub>Sn
  - Damaging effects of luminosities at smaller apertures
  - Reduction in physics applications → especially from reduced luminosity

# FUTURE WORK

- **Lattice Design**
  - Include Mini-Beta Insertions
  - Controlling Chromaticity
  - Add Kickers and BPMs
- **Instabilities**
  - Increase complexity of the models for the instabilities analysed
  - Look at more instabilities → for example electron cloud instabilities
- **Magnet Design**
  - Further optimisation of designs to reduce materials and improve quality
  - Feasibility study of staged magnet design
  - Design for quadrupoles (and sextupoles and octupoles!)
- **RF Cavities**
  - Check other modes do not interfere with accelerating mode
  - Look at other factors → such as the electric field input, polishing of the surface
  - In-depth study of magnetic field on cavity surface
  - The possibility of using multiple frequencies

THANK YOU

SPECIAL THANKS TO:

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*Neil Marks*



# LATTICE FURTHER INFORMATION

Christopher Arran

# EFFECT OF DIPOLE NUMBER

- Lattice  $\Rightarrow$  Bending radius:  $N \downarrow D \Downarrow D = 2\pi\rho$
- $\Rightarrow$  Magnetic rigidity ( $p \gg m$ ):  $B\rho = p/e \approx E \downarrow eV / c$
- $\Rightarrow$  Beam energy:  $E \downarrow eV = N \downarrow D \Downarrow D Bc / 2\pi$

# EFFECT OF APERTURE SIZE

Smaller aperture, diameter  $D$

- Smaller maximum beta  $D \geq 14\sigma \propto \sqrt{\beta}$
- Shorter FODO cells  $L \propto \beta$
- Stronger quadrupoles  $k \propto Q = f^{-1} \propto \beta^{-1}$
- But quadrupole strength:  $k \propto dB/dx / dy \propto D^{-1}$

More length in quadrupoles and spacing

⇒ Less dipole per unit length of cell

# EFFECT OF APERTURE SIZE

Less dipole per unit length of arc:

- Longer arcs required
- Shorter straights

Reduces number of dipoles  $N \downarrow D$

Reduces beam energy  $E \propto N \downarrow D$

# EFFECT OF DIPOLE STRENGTH

Reduces magnetic rigidity

Reduces possible beam energy

BUT:

- Increases quadrupole strength  $k \propto (B\rho)^{\uparrow-1}$
- Reduces quadrupole length  $l \downarrow Q \propto k^{\uparrow-1}$
- Slightly reduces cell length
- Slightly increases dipole fill factor

# 14.7 T RESULTS:

Aperture	40mm	30mm	20mm
Maximum Beta	354.6 m	199.4 m	88.7 m
Beam energy	50 TeV	48.2 TeV	34.4 TeV
Dipoles per cell	12	6	2
Quadrupole field gradient	450 Tm <sup>-1</sup>	600 Tm <sup>-1</sup>	900 Tm <sup>-1</sup>
Quadrupole strength	0.002698 m <sup>-2</sup>	0.003732 m <sup>-2</sup>	0.007844m <sup>-2</sup>
Quadrupole length	5.17 m	4.62 m	5.55 m
Cell length	208.14 m	114.04 m	53.3 m
No. Dipoles	5016	4836	3532
Dipole Fill factor	71%	69%	50%
No. Quadrupoles	948	1708	3628
No. Arc Cells	442	828	1788
Average Arc Length	7654 m	7869 m	7942 m
Short Straight Length	416 m	114 m	53 m
Long Straight Length	1203 m	1109 m	1042 m

# 10.5 T RESULTS:

Aperture	40mm	30mm	20mm
Maximum Beta	354.6 m	199.4 m	88.7 m
Beam energy	37.3 TeV	35.4 TeV	26.5 TeV
Dipoles per cell	12	6	2
Quadrupole field gradient	450 Tm <sup>-1</sup>	600 Tm <sup>-1</sup>	900 Tm <sup>-1</sup>
Quadrupole strength	0.003617 m <sup>-2</sup>	0.005081 m <sup>-2</sup>	0.01018 m <sup>-2</sup>
Quadrupole length	2.65 m	3.27 m	3.83 m
Cell length	203.1 m	111.34 m	50.46 m
No. Dipoles	5256	4980	3740
Dipole Fill factor	75%	71%	53%
No. Quadrupoles	972	1756	3820
No. Arc Cells	462	854	1896
Average Arc Length	7819 m	7905 m	7973 m
Short Straight Length	203 m	111 m	50 m
Long Straight Length	1136 m	1006 m	1006 m

# 16 T RESULTS:

Aperture	40mm	30mm
Maximum Beta	354.6 m	199.4 m
Beam energy	<b>50 TeV</b>	<b>50 TeV</b>
Dipoles per cell	12	6
Quadrupole field gradient	450 Tm <sup>-1</sup>	600 Tm <sup>-1</sup>
Quadrupole strength	0.002698 m <sup>-2</sup>	0.003598 m <sup>-2</sup>
Quadrupole length	5.17 m	4.82 m
Cell length	208.14 m	114.44 m
No. Dipoles	4632	4620
Dipole Fill factor	66%	66%
No. Quadrupoles	948	1684
No. Arc Cells	410	768
Average Arc Length	7078 m	7553 m
Short Straight Length	1040 m	229 m
Long Straight Length	1584 m	1368 m