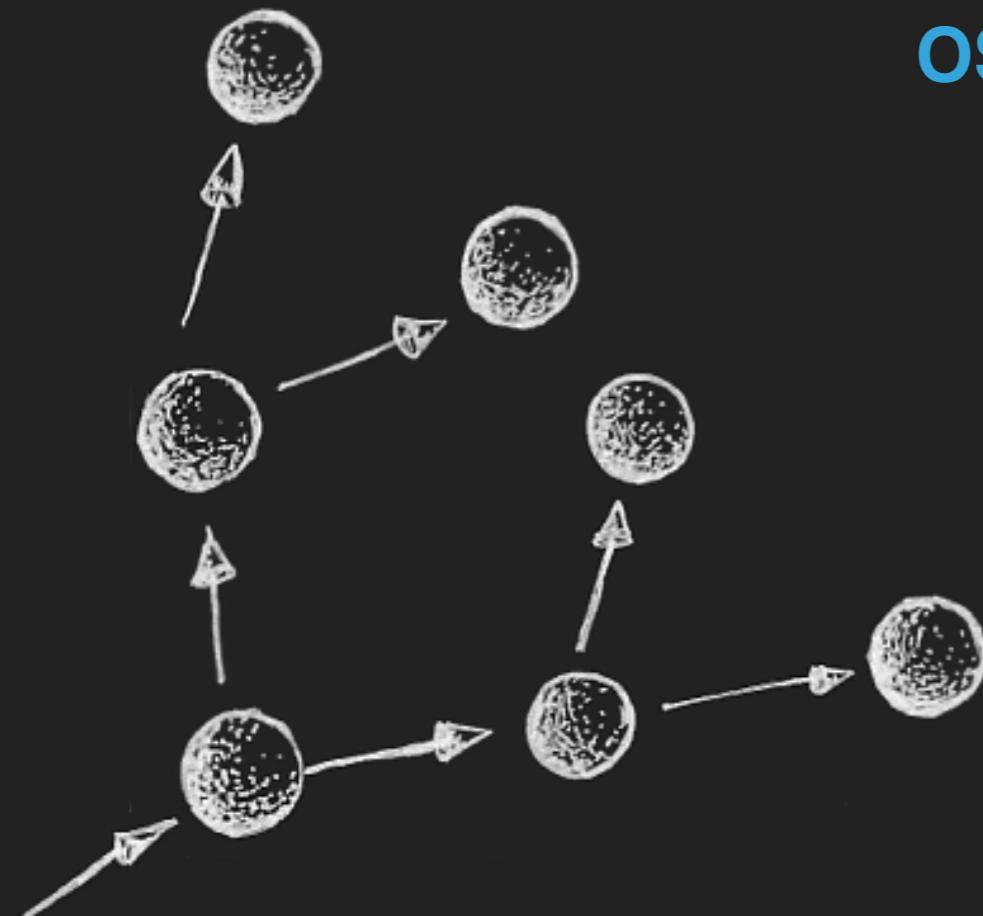




INCLUSIVE PROMPT PHOTON PRODUCTION FROM THE CGC

OSCAR GARCIA-MONTERO

In collaboration with
Sanjin Benic
Kenji Fukushima
Raju Venugopalan

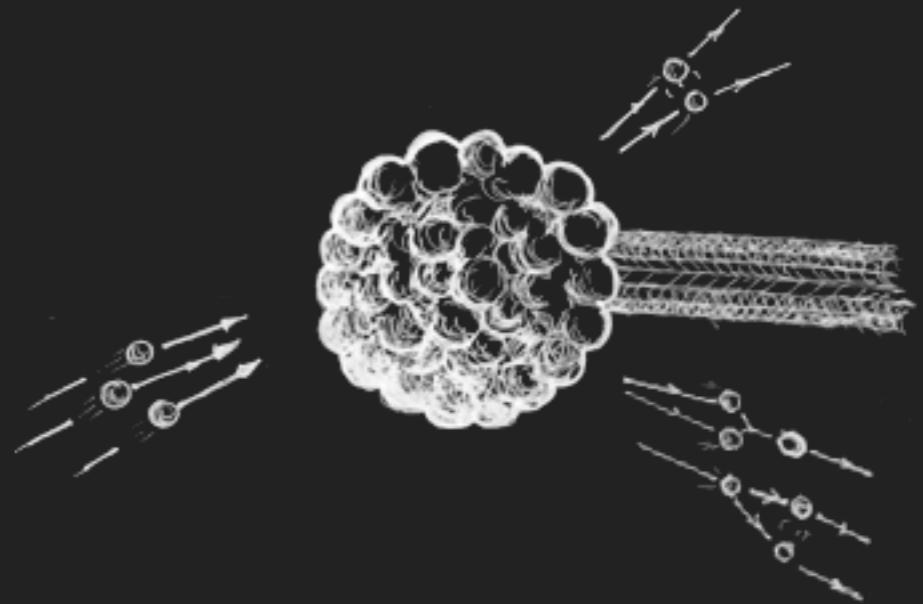


CONTENTS

- ➡ Motivation
- ➡ Framework: CGC
- ➡ Power counting
- ➡ Some results
- ➡ Summary and Outlook

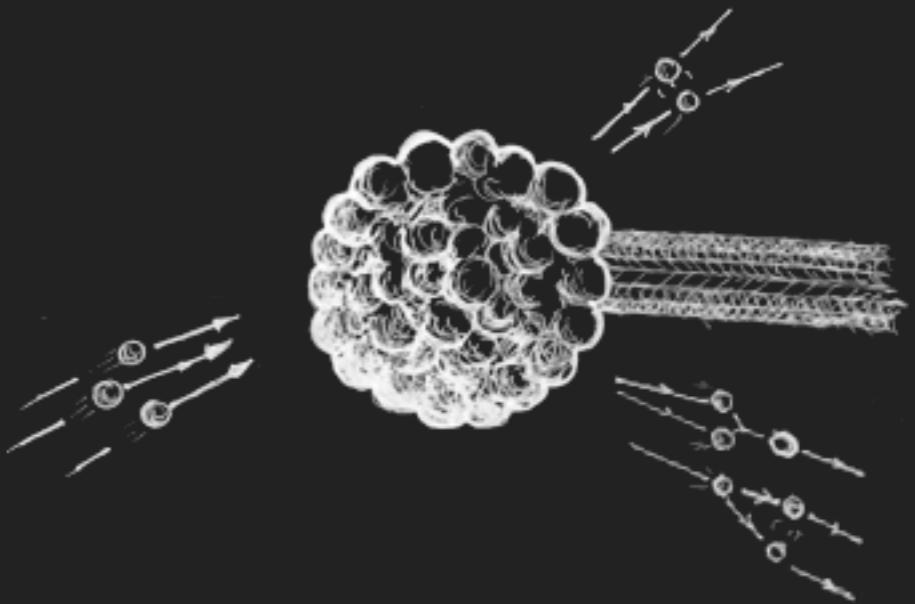
GLOBAL GOAL

Understand nuclear matter under
extreme conditions



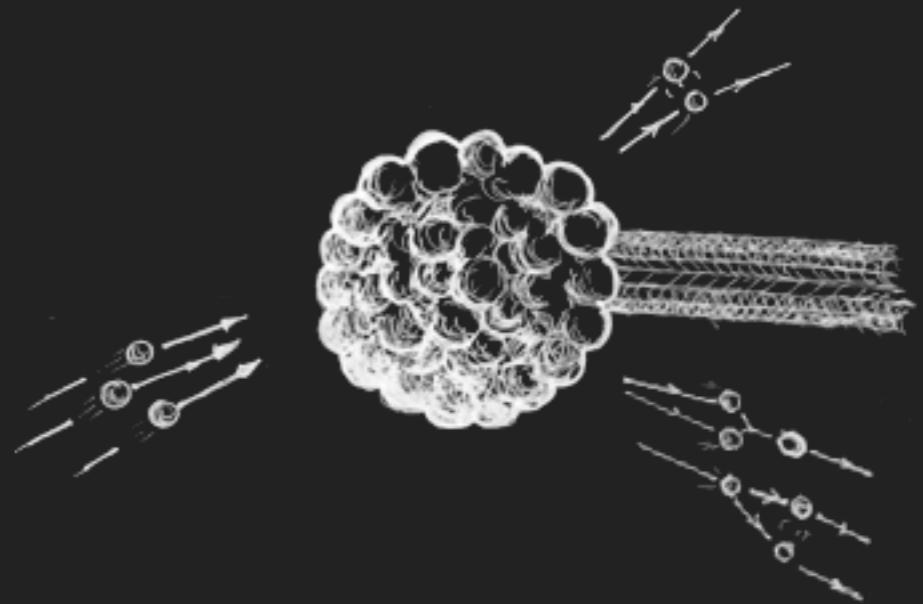
LOCAL GOAL

Use photons as probes for saturation
in highly energetic p+A collisions



LOCAL GOAL

Use photons as probes for saturation
in highly energetic p+A collisions

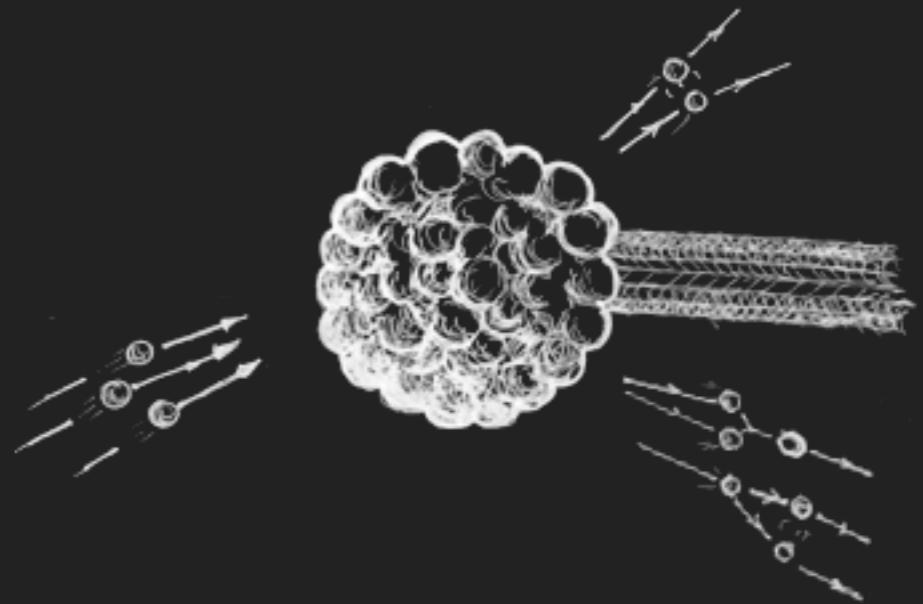


WHY PHOTONS?

No strong interaction

LOCAL GOAL

Use photons as probes for saturation
in highly energetic p+A collisions



WHY PHOTONS?

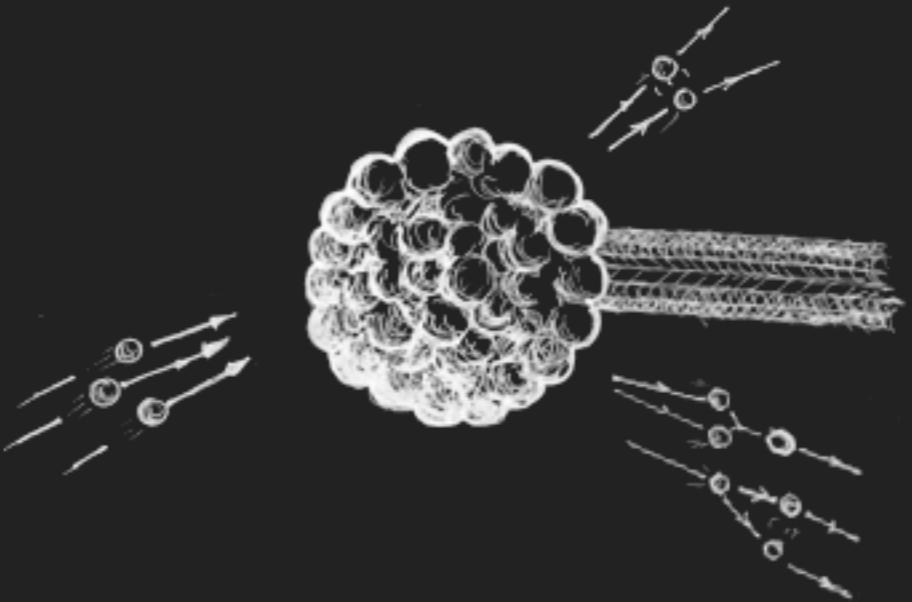
No strong interaction



Clean probes.

LOCAL GOAL

Use photons as probes for saturation
in highly energetic p+A collisions



WHY PHOTONS?

No strong interaction

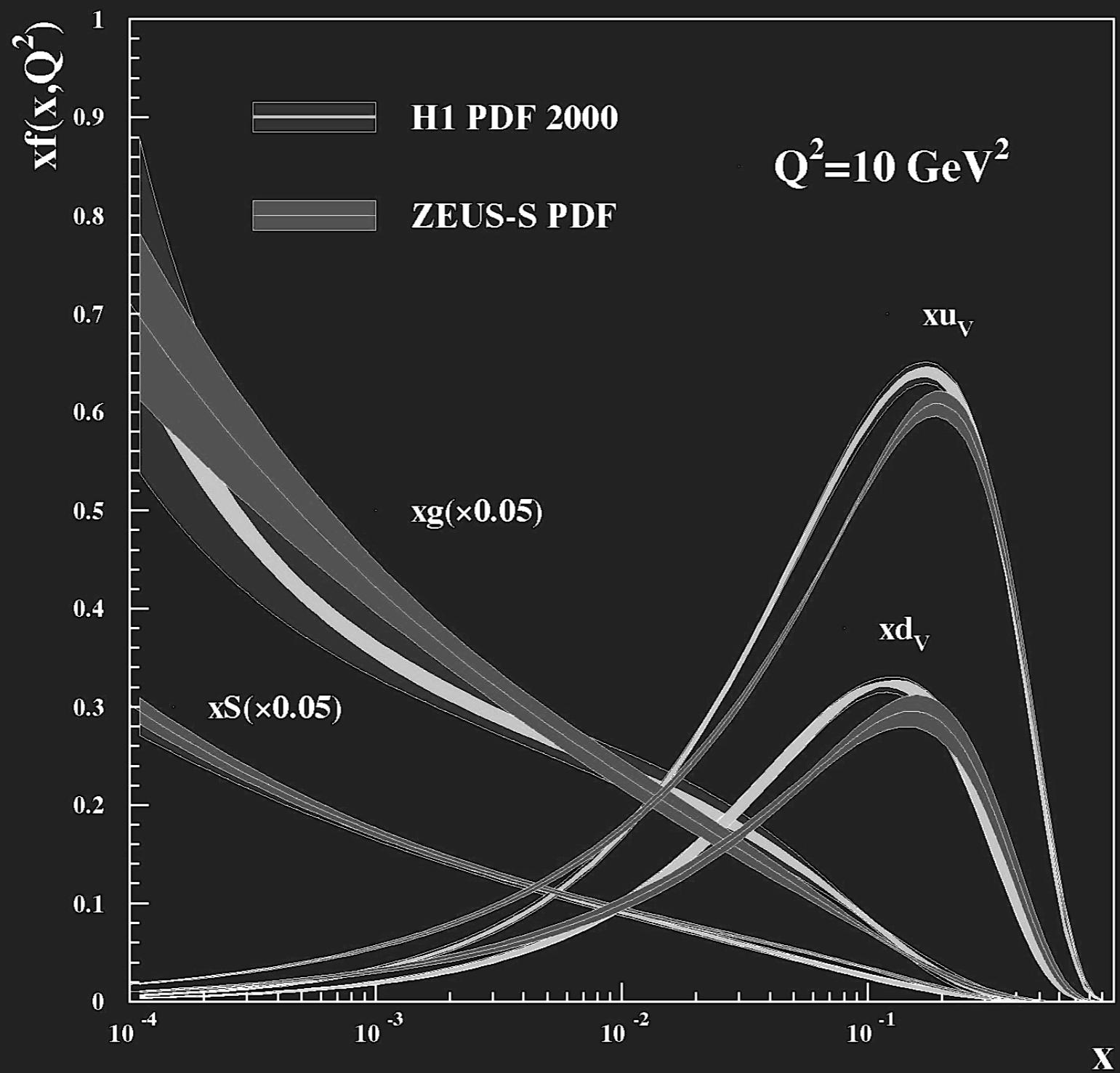


Clean probes.

WHY P+A?

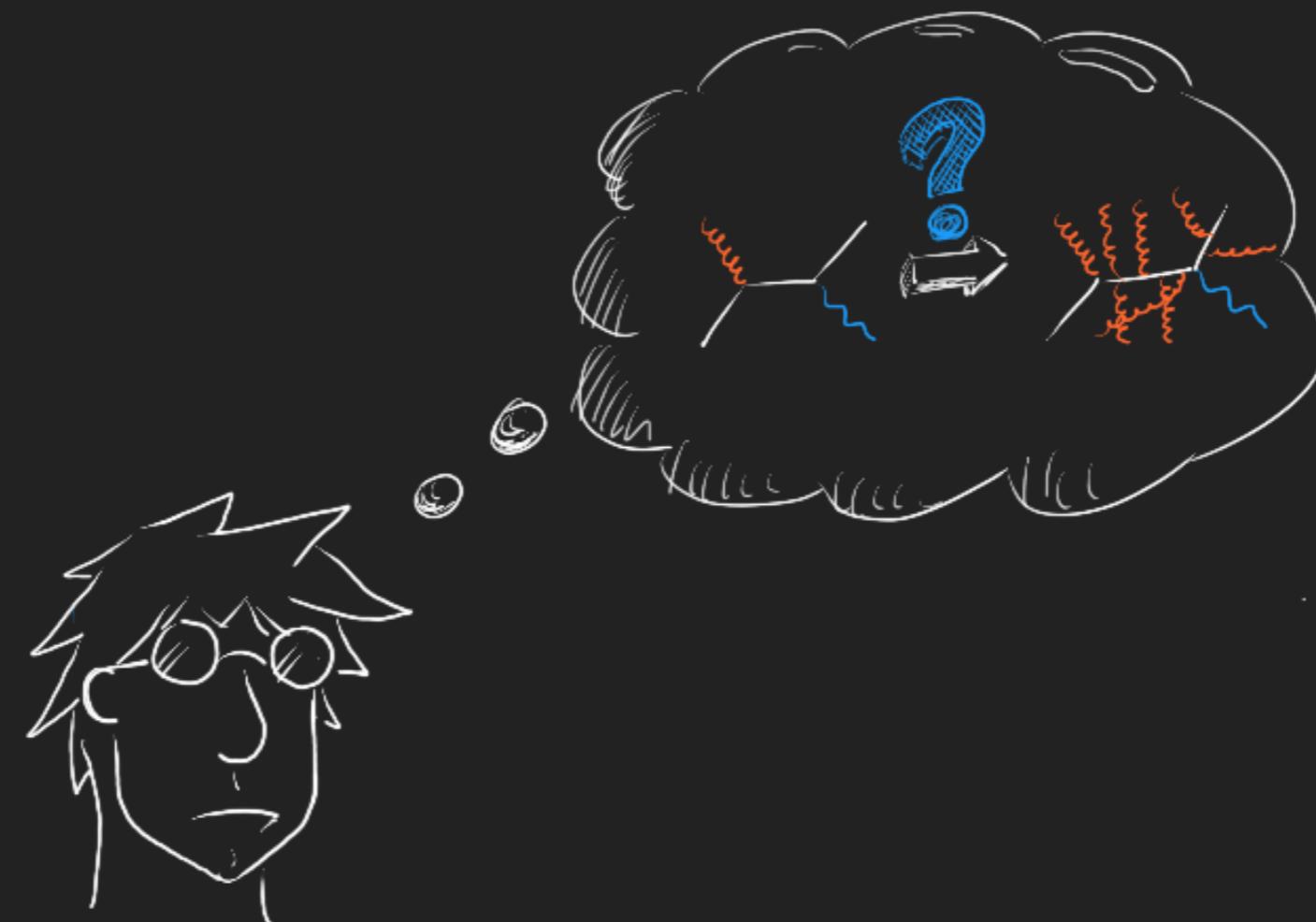
Use known probes to probe the "unknown"

PARTON DISTRIBUTION FUNCTIONS

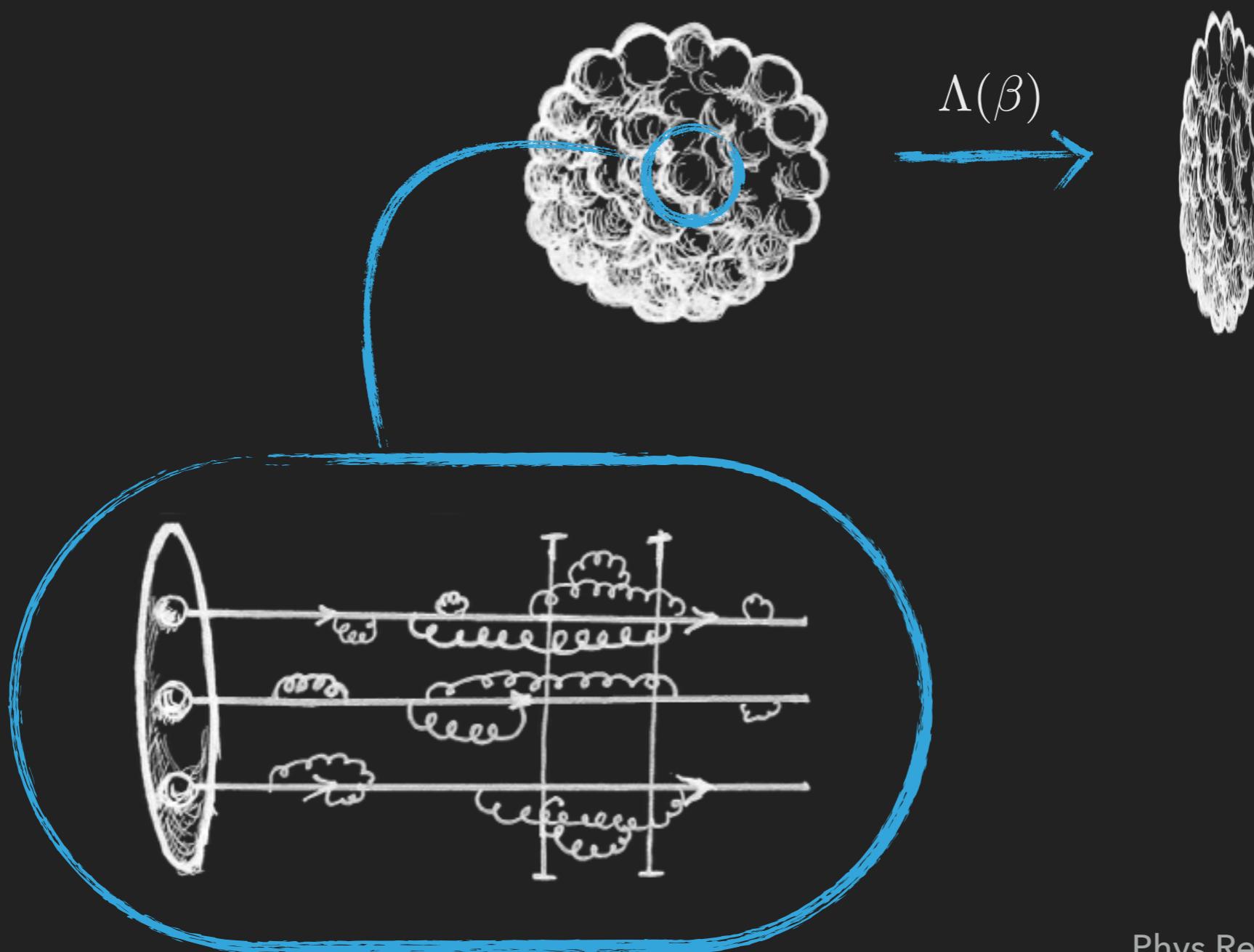


HOW TO CATCH A GLUON SOUP?

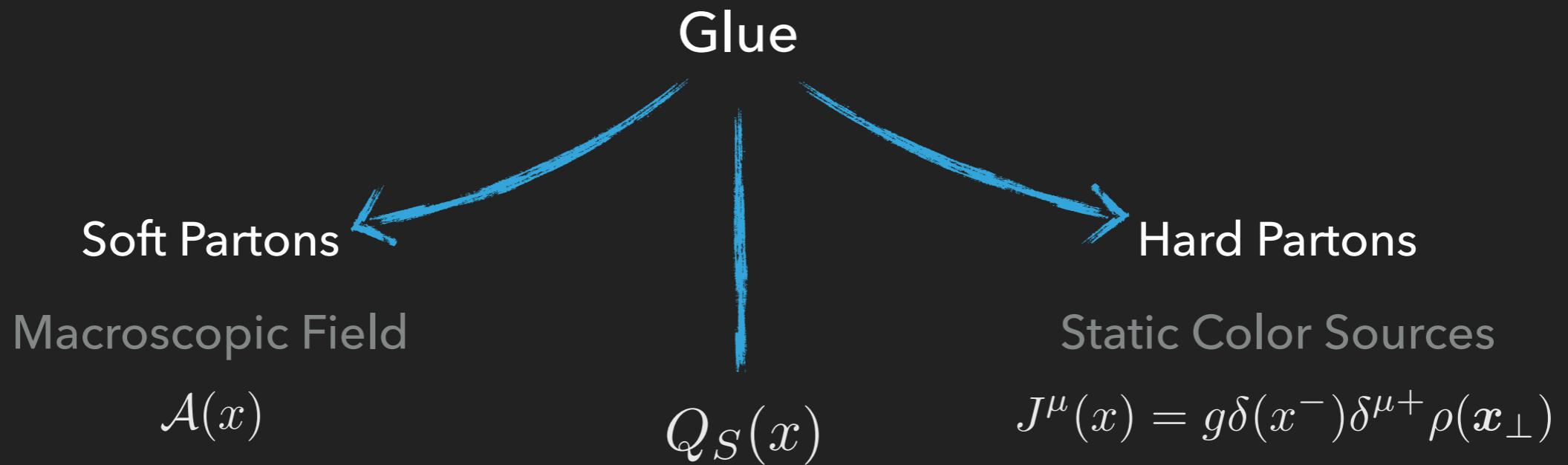
HOW TO CATCH A GLUON SOUP?



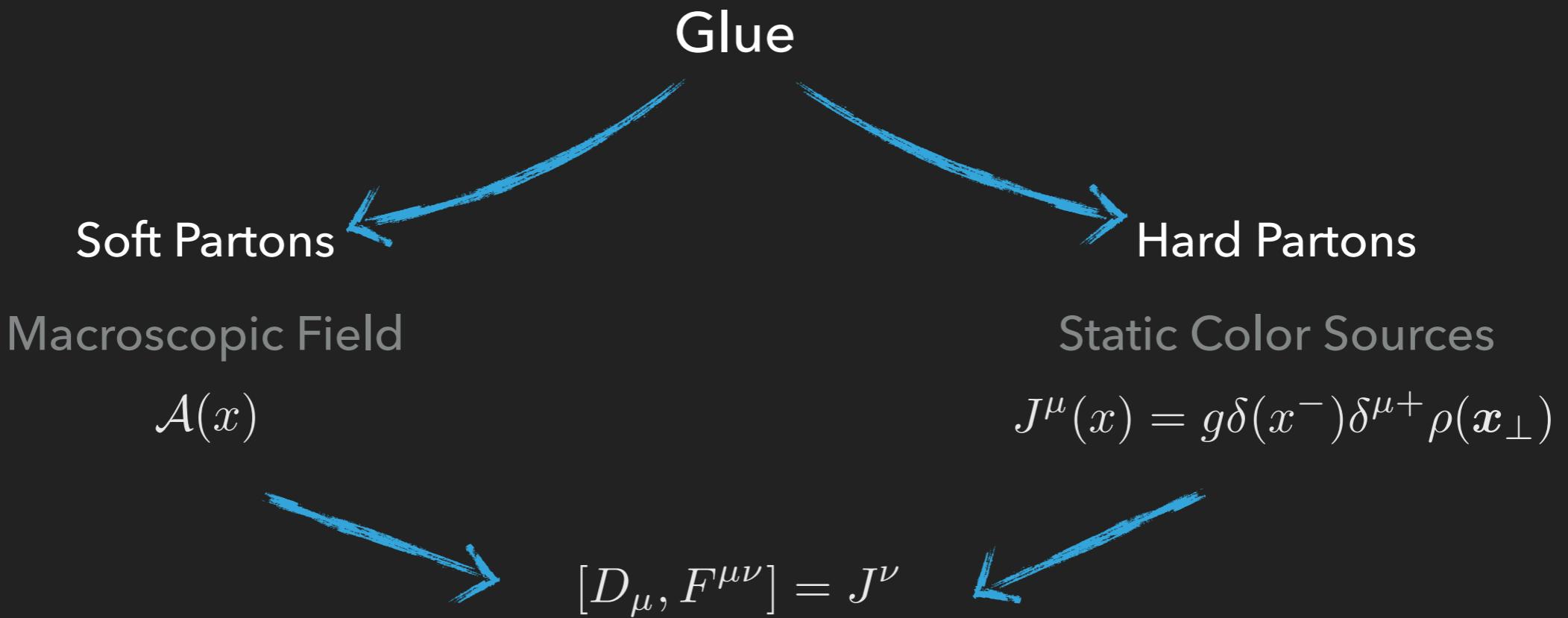
COLOR GLASS CONDENSATE



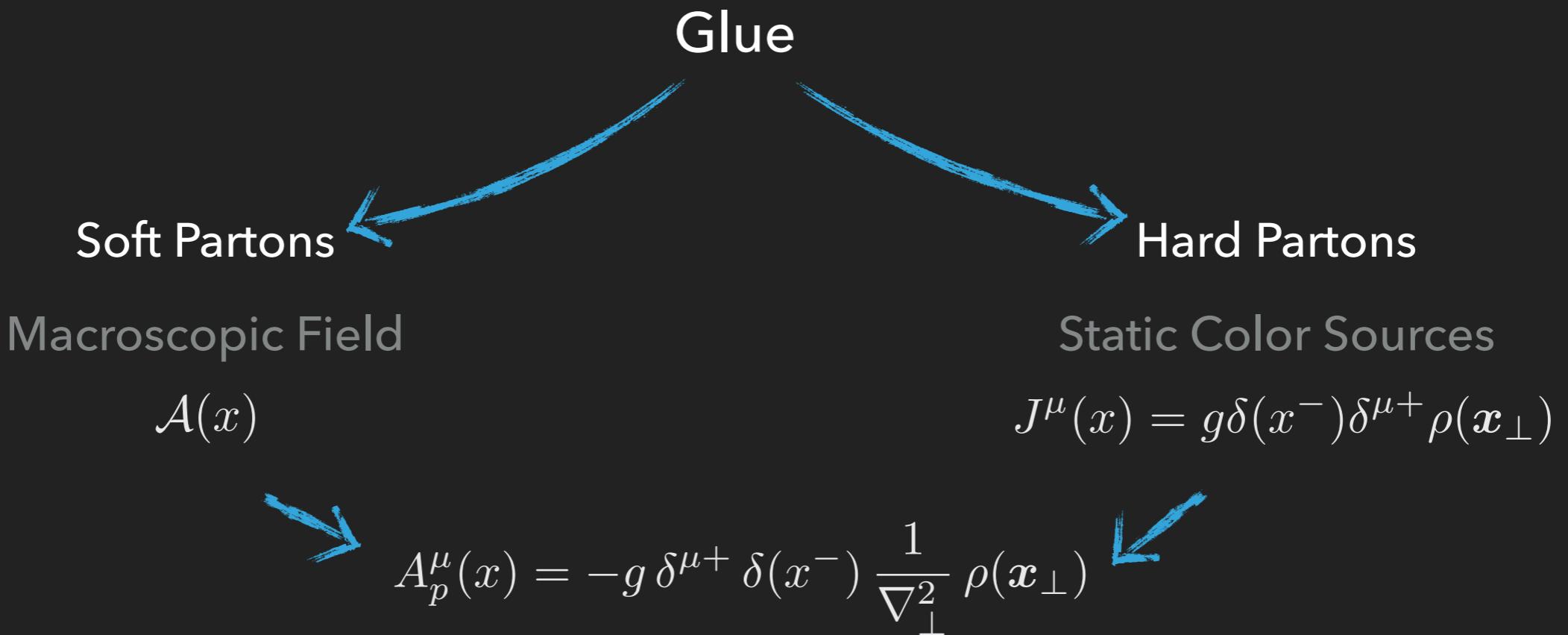
COLOR GLASS CONDENSATE



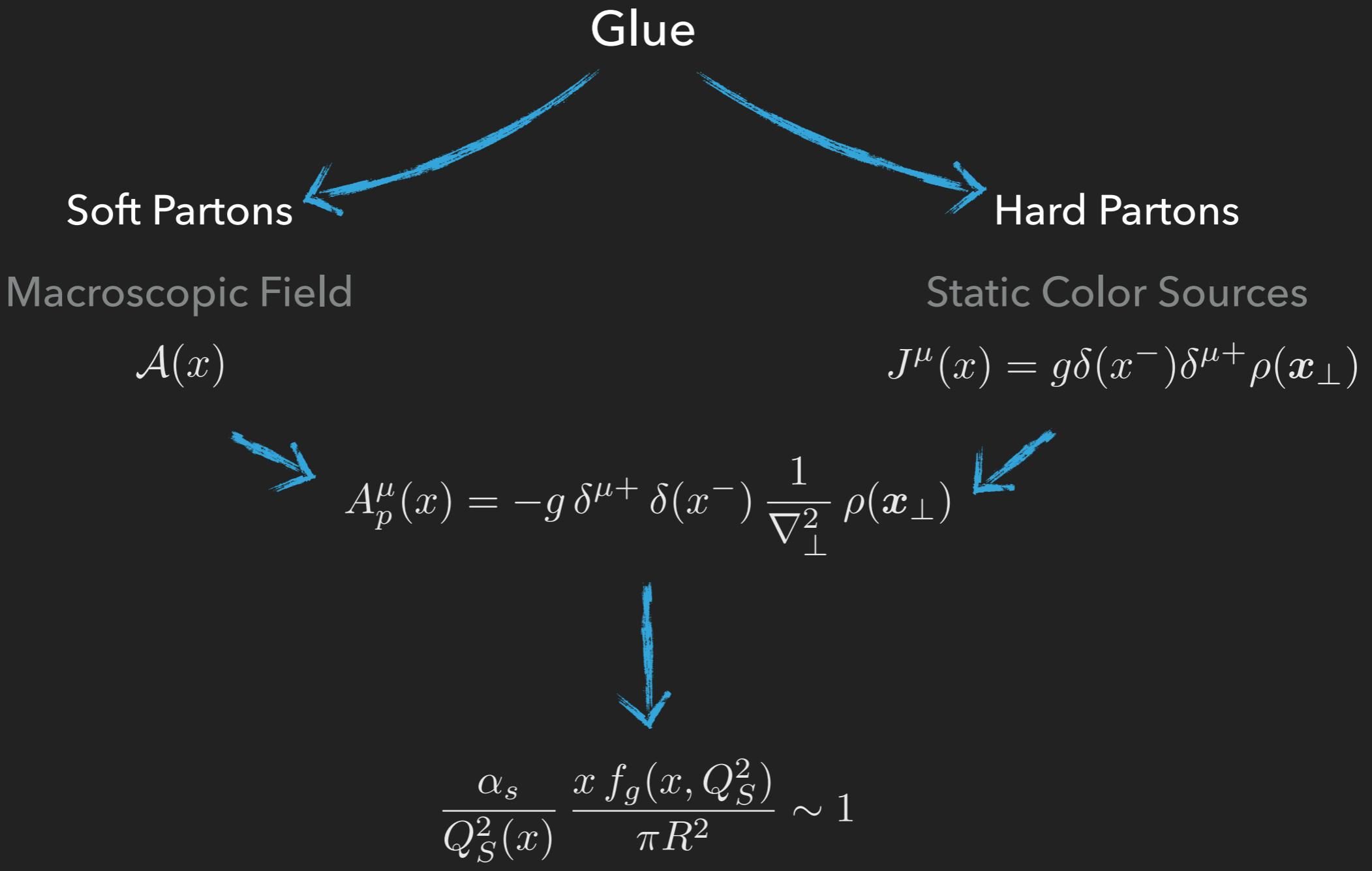
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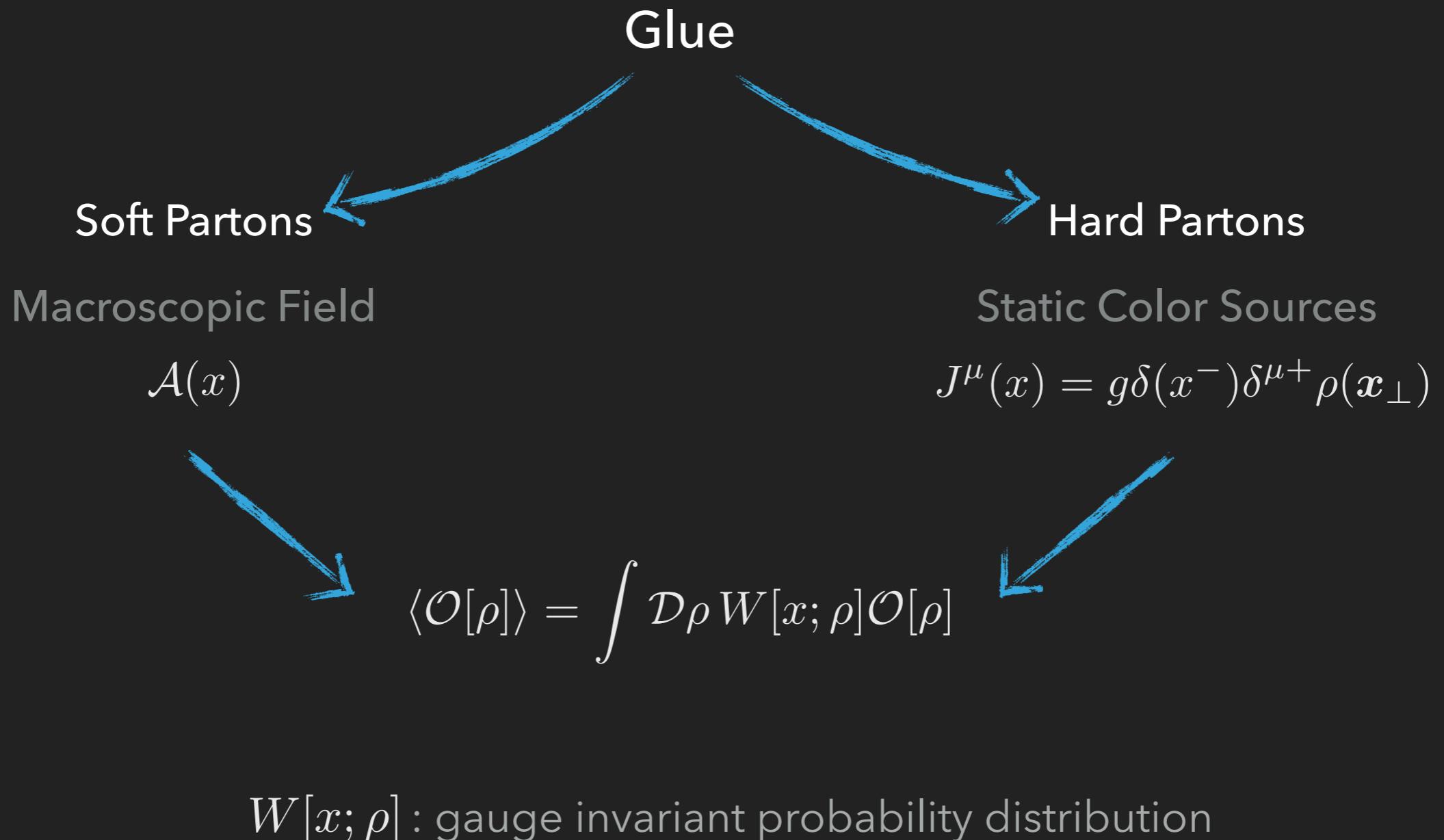
COLOR GLASS CONDENSATE



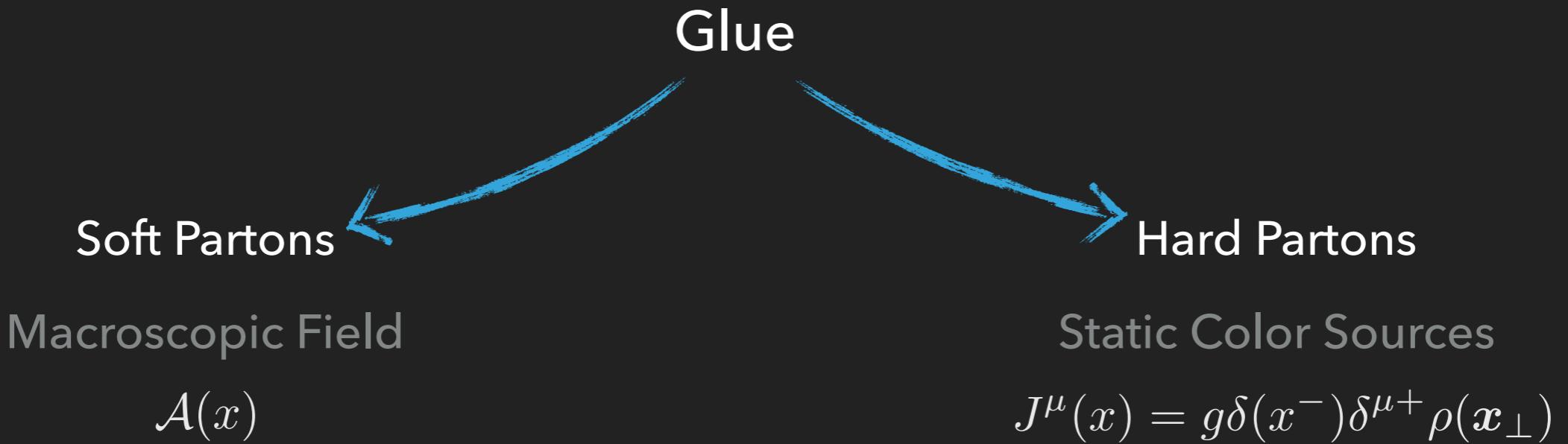
COLOR GLASS CONDENSATE



COLOR GLASS CONDENSATE



COLOR GLASS CONDENSATE



SPECIAL CASE

McLerran-Venugopalan Model

$$\langle \rho^a(\mathbf{x}_\perp) \rho^b(\mathbf{y}_\perp) \rangle = g^2 \delta^{ab} \mu^2 \delta^{(2)}(\mathbf{x}_\perp - \mathbf{y}_\perp)$$

GLUON PROPAGATOR



Is the gluon field (proton)
modified by the nuclear CGC?



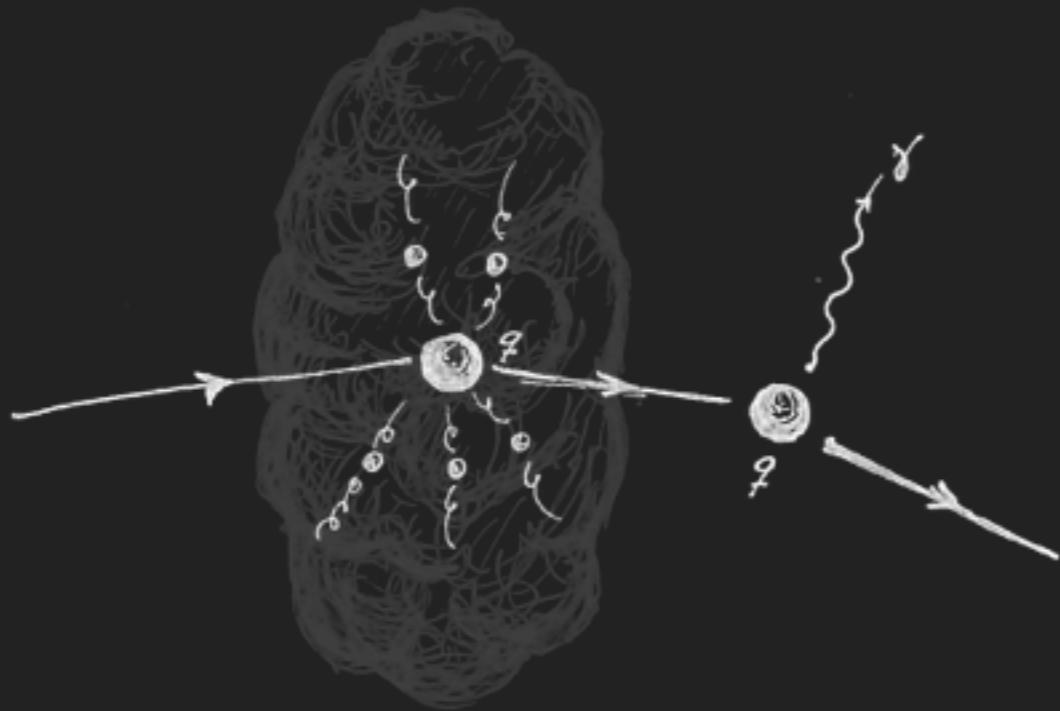
Multiple Scatterings

$${}^A \times \text{wavy lines} = \rho_p \times \text{wavy lines} + {}^{A_p} \times \text{wavy lines} \odot \text{wavy lines}$$



$$A^\mu(q) = A^\mu(q) + \frac{i g}{q^2 + i q^+ \epsilon} \int_{\mathbf{k}_\perp} \int_{\mathbf{x}_\perp} e^{i(\mathbf{q}_\perp - \mathbf{k}_\perp) \cdot \mathbf{x}} C^\mu(q, \mathbf{k}_\perp)) U(\mathbf{x}_\perp) \frac{\rho_p(\mathbf{k}_\perp)}{k_\perp^2}$$

QUARK PROPAGATOR



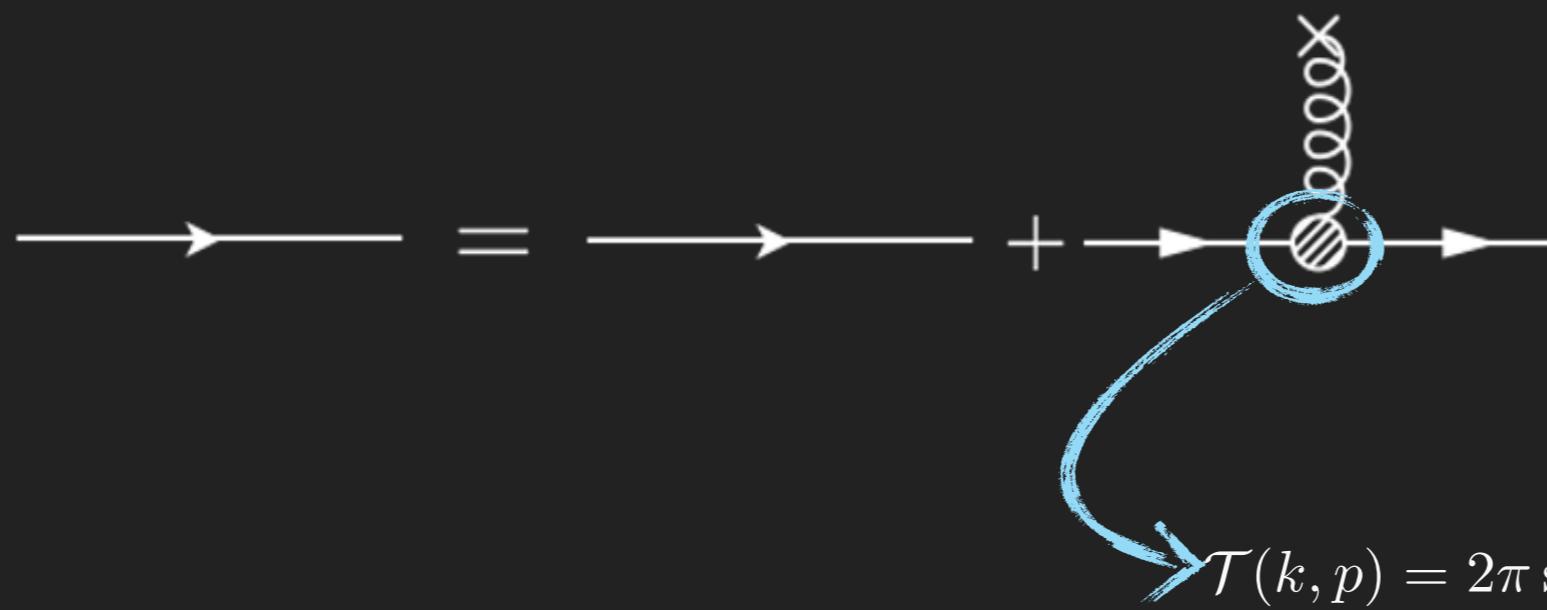
How do quarks behave
through the CGC?



Multiple Scatterings

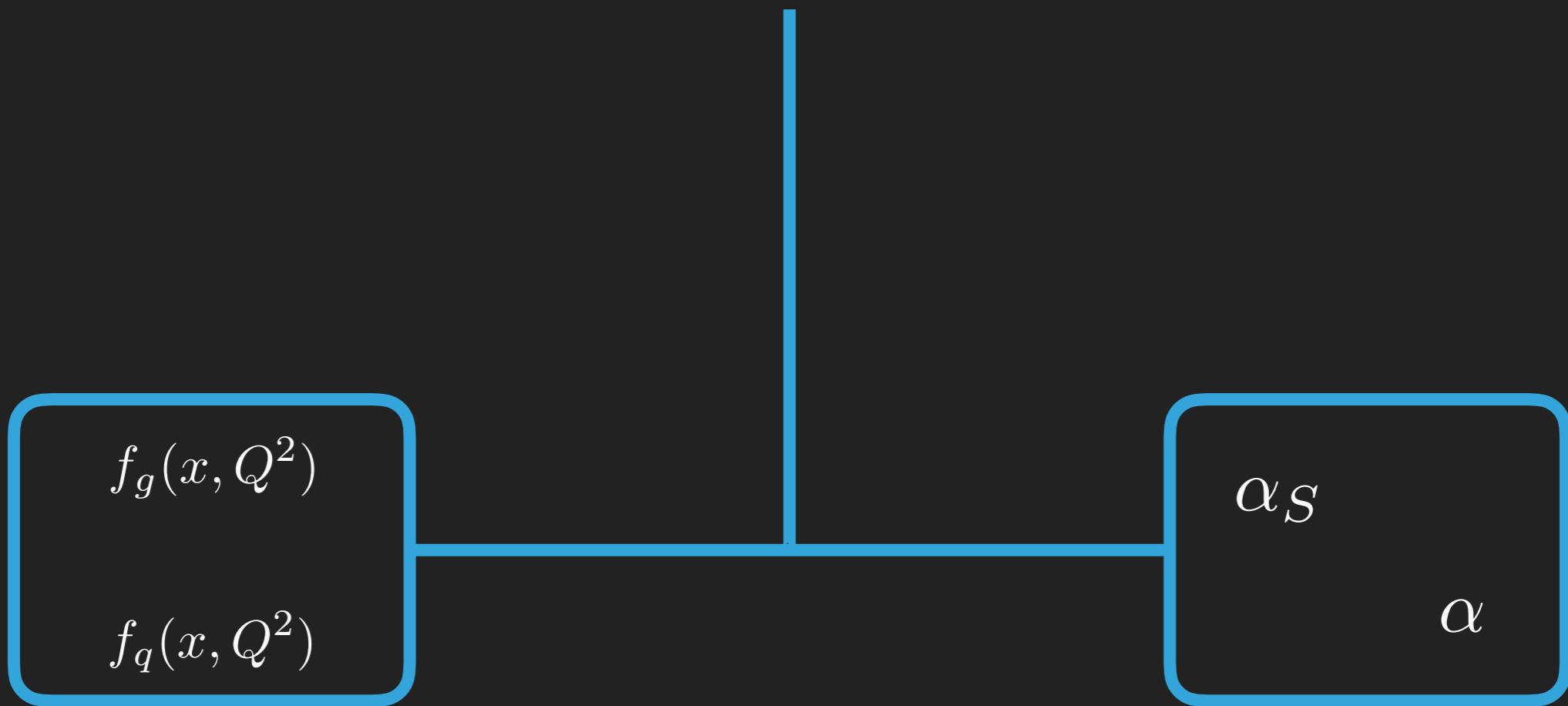


Dressed propagator

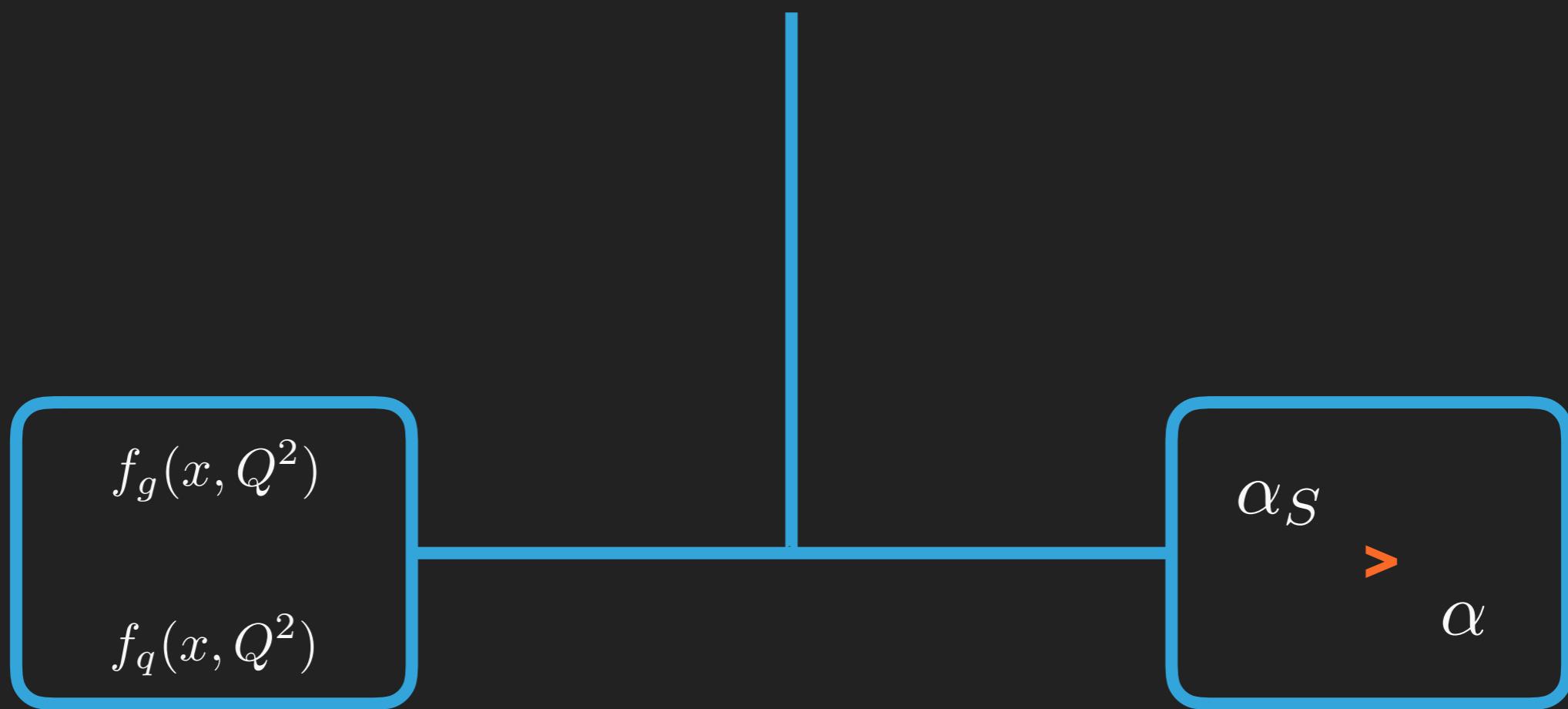


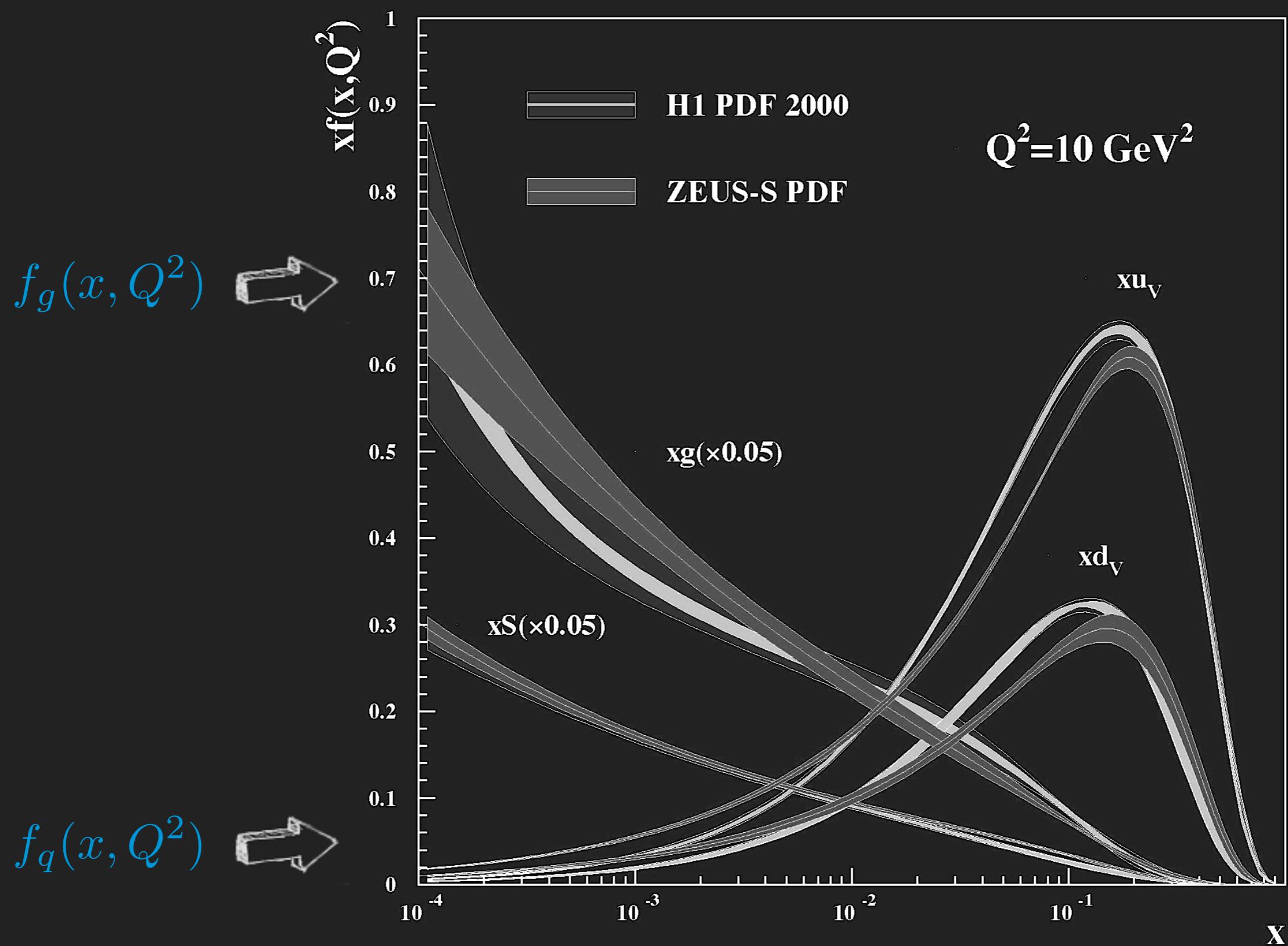
$$\mathcal{T}(k, p) = 2\pi \operatorname{sgn}(p^+) \gamma^+ \int_{\mathbf{x}_\perp} e^{i\mathbf{x}_\perp \cdot \mathbf{k}_\perp} [\tilde{U}(\mathbf{x}_\perp) - 1]$$

POWER COUNTING

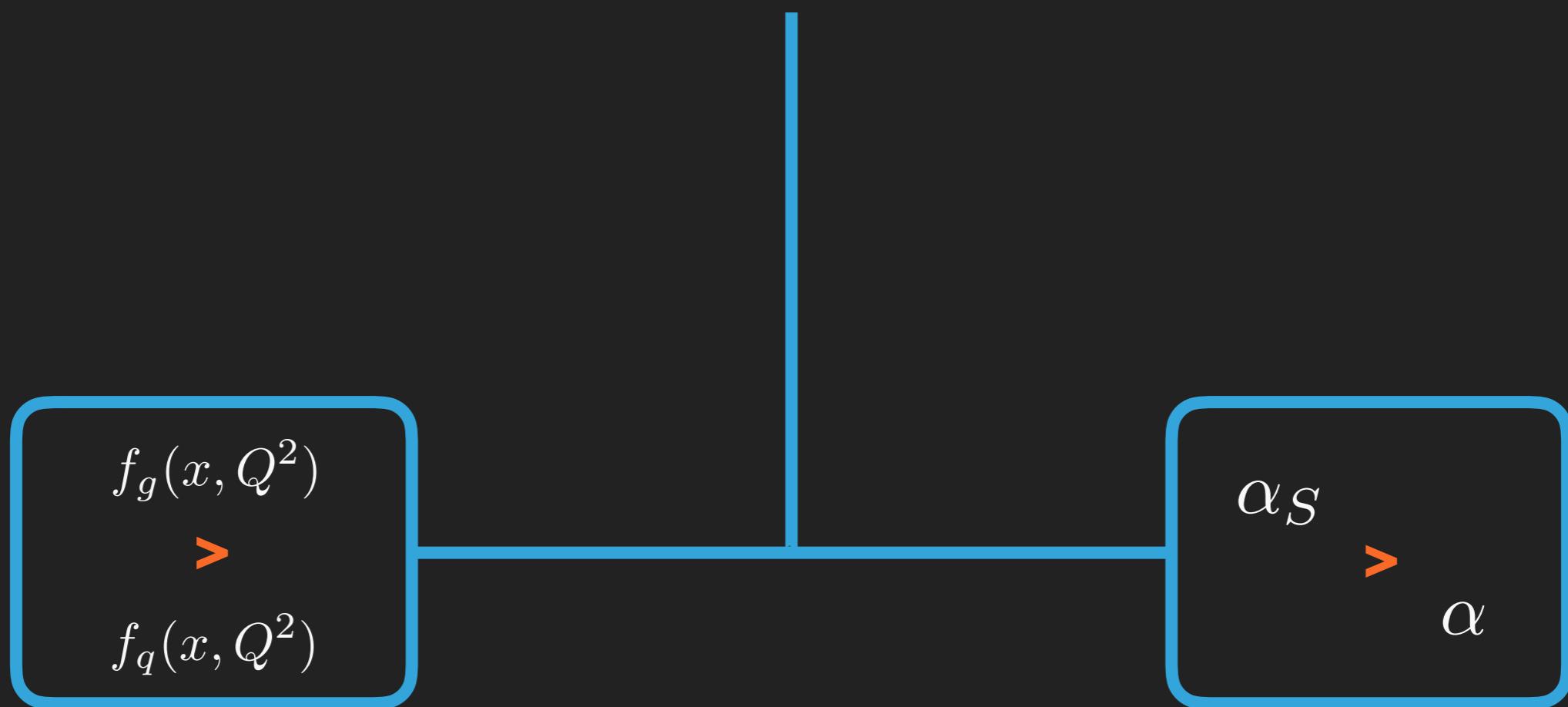


POWER COUNTING

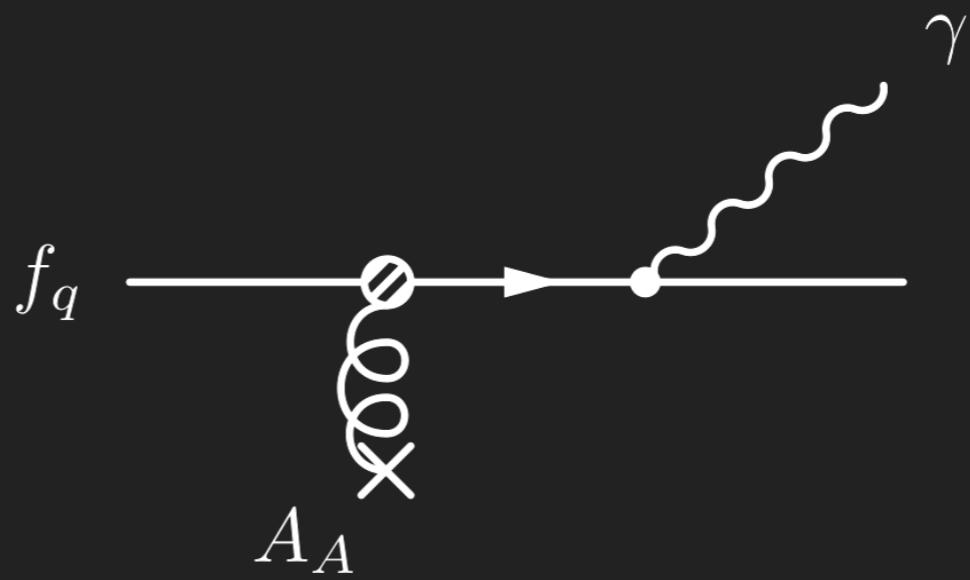
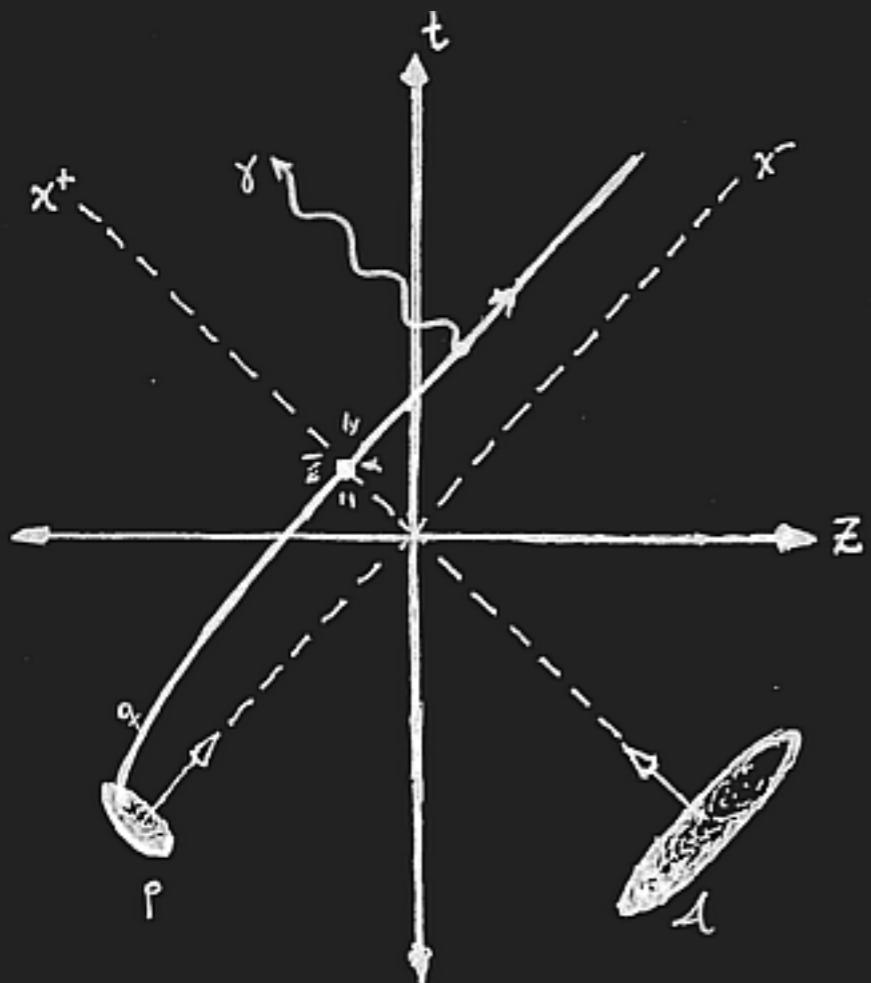




POWER COUNTING



$\text{LO } [\mathcal{O}(\alpha)]$



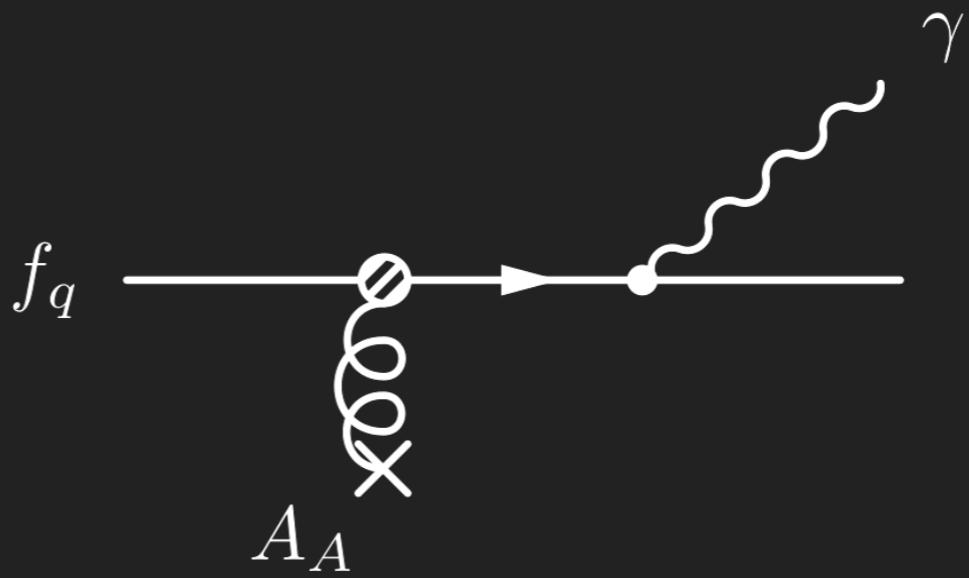
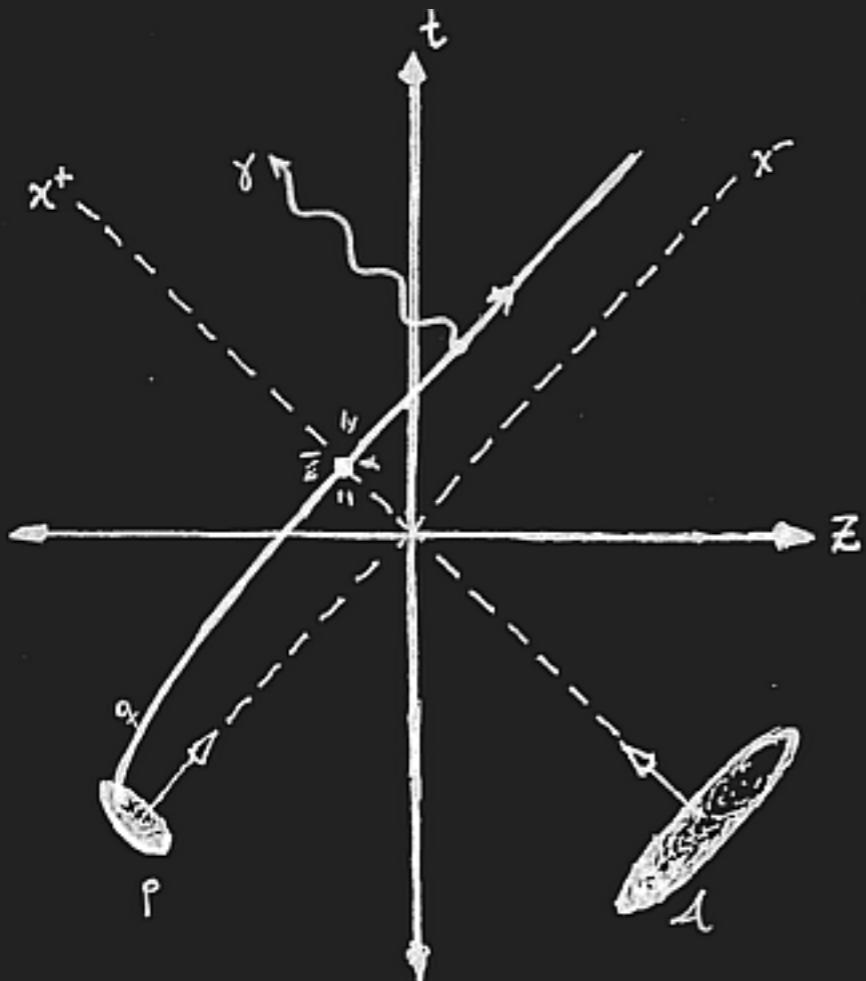
$$x \sim 10^{-2}$$



$$f_g(x, Q^2) \gg f_q(x, Q^2)$$

- Kopeliovich, Tarasov, Schaefer, Phys. Rev. C 59 (1999) 1609
Gelis, Jalilian-Marian, Phys. Rev. D 66 (2002) 014021
Baier, Mueller, Schi, Nucl. Phys. A 741 (2004) 358

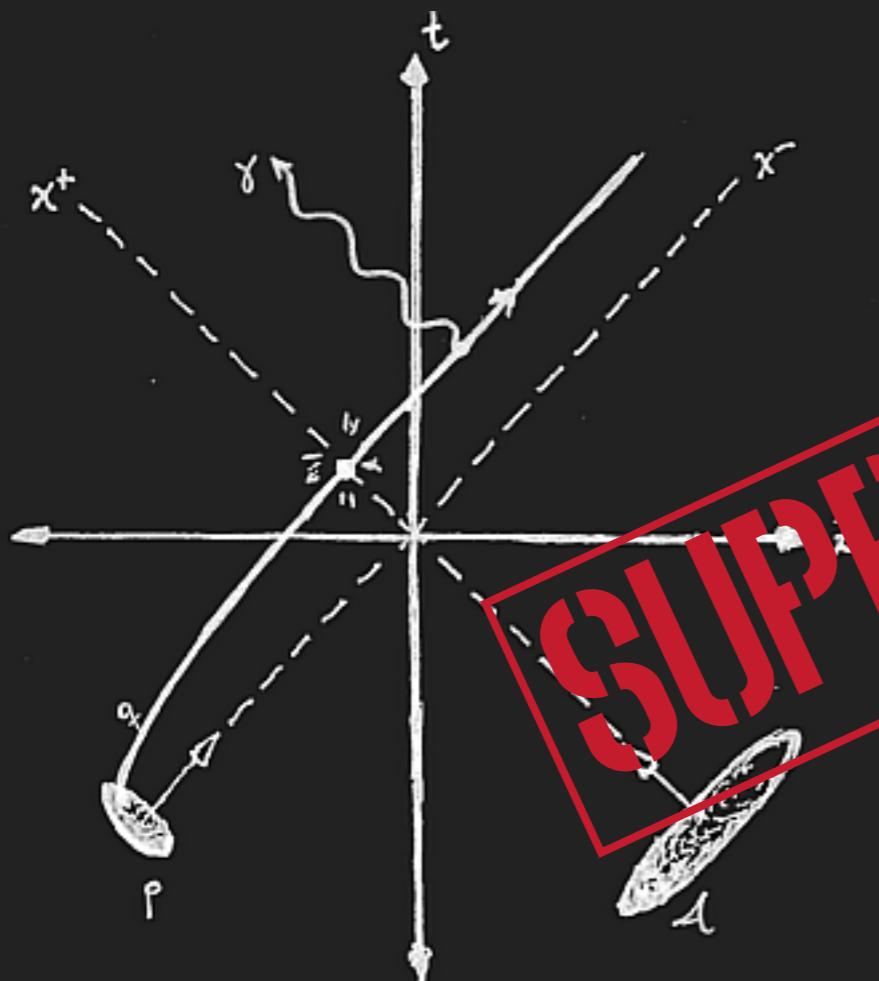
LO [$\mathcal{O}(\alpha)$]



$$\frac{d\sigma}{d^2 \mathbf{k}_{\gamma\perp} d\eta_\gamma} = \frac{\alpha \alpha_S^2 q_f^2}{(2\pi)^8 C_F} \int_{\eta_q} \int_{\mathbf{q}_\perp} \int_{x_p} (2\pi) \delta(l^+ - q^+ - k_\gamma^+) \\ \times f_{q,p}(x_p, Q^2) \mathcal{N}_A(x_A, \mathbf{q}_\perp + \mathbf{k}_{\gamma\perp}) \theta_{LO}(q, k_\gamma)$$

- Kopeliovich, Tarasov, Schaefer, Phys. Rev. C 59 (1999) 1609
 Gelis, Jalilian-Marian, Phys. Rev. D 66 (2002) 014021
 Baier, Mueller, Schi, Nucl. Phys. A 741 (2004) 358

LO [$\mathcal{O}(\alpha)$]



SUPPRESSED!

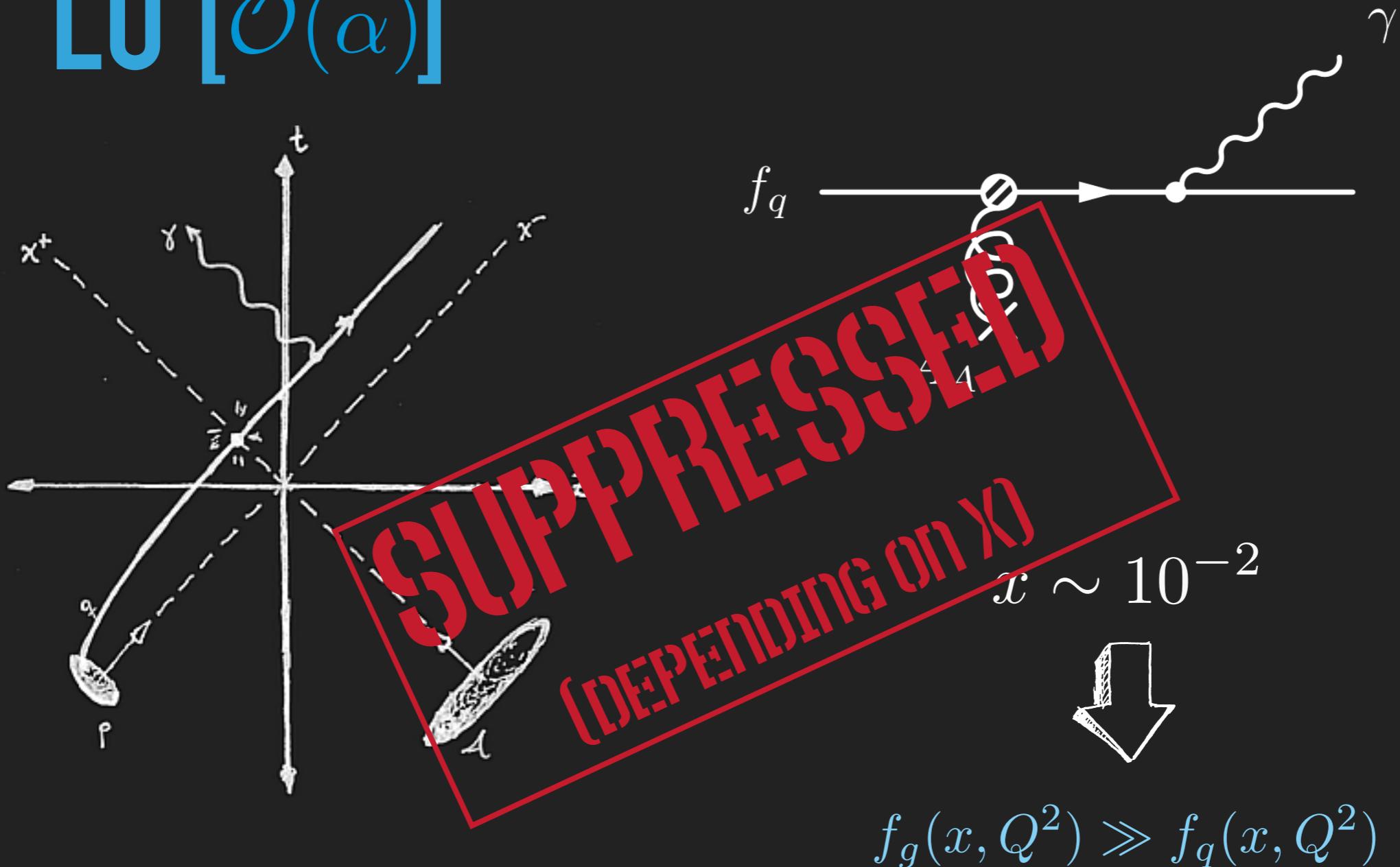
$$x \sim 10^{-2}$$



$$f_g(x, Q^2) \gg f_q(x, Q^2)$$

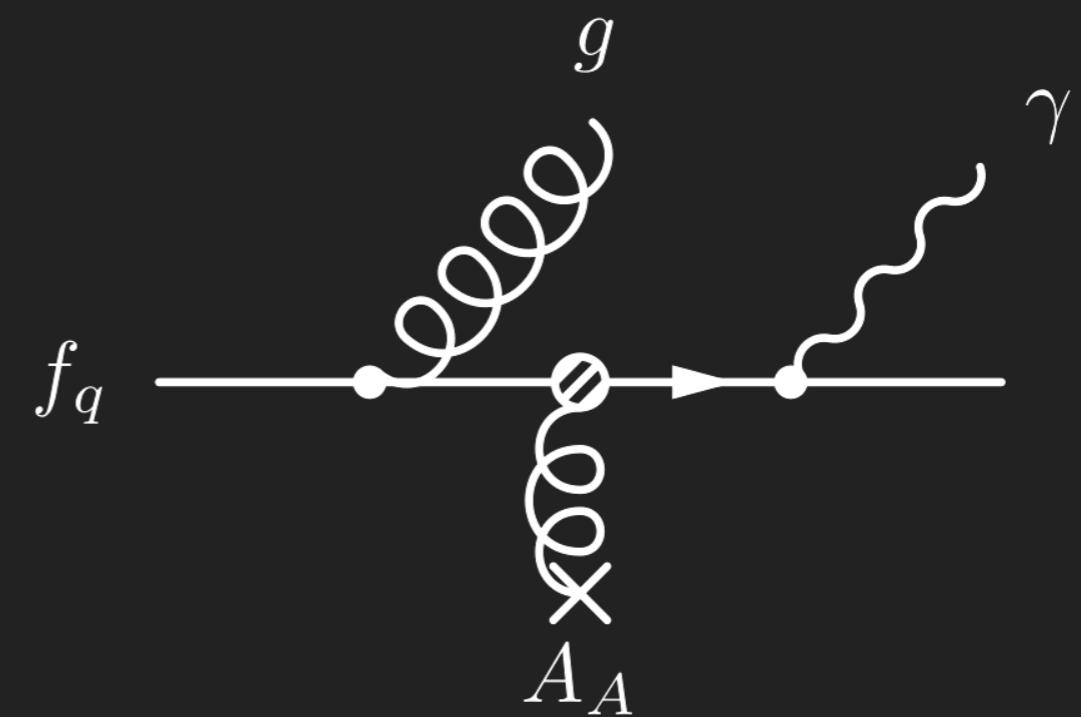
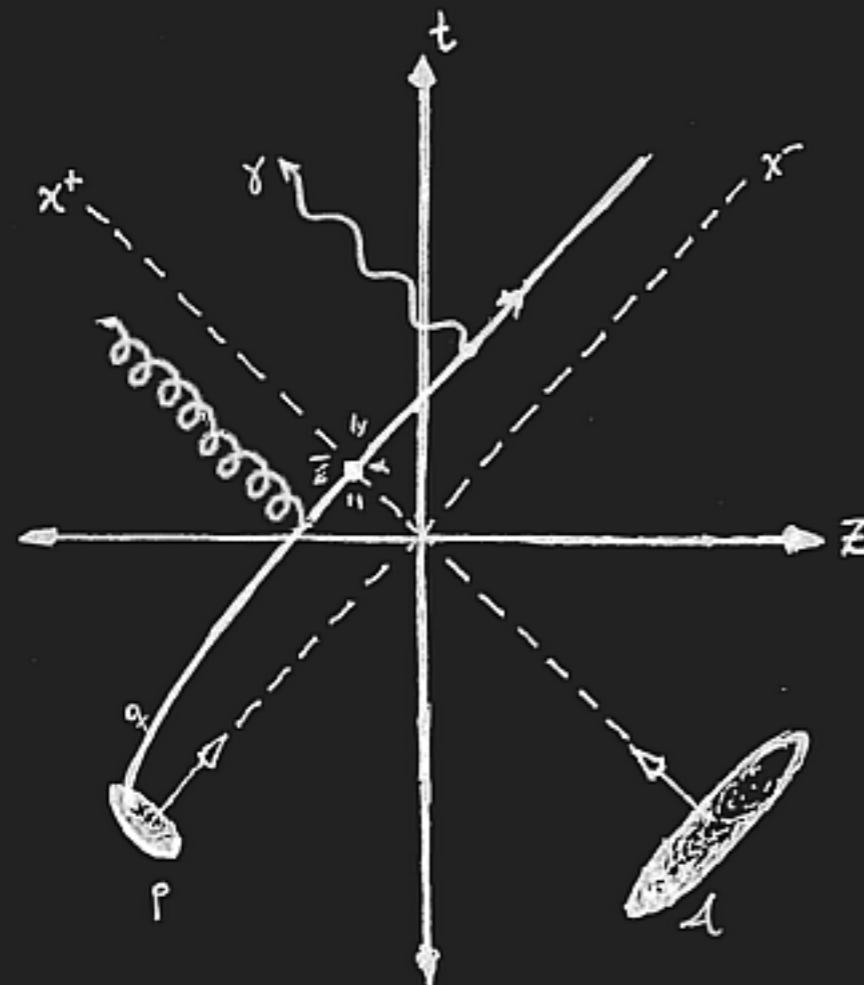
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LO [$\mathcal{O}(\alpha)$]



Kopeliovich, Tarasov, Schaefer, Phys. Rev. C 59 (1999) 1609
Gelis, Jalilian-Marian, Phys. Rev. D 66 (2002) 014021
Baier, Mueller, Schi, Nucl. Phys. A 741 (2004) 358

NLO: GLUON BREMSSTRAHLUNG



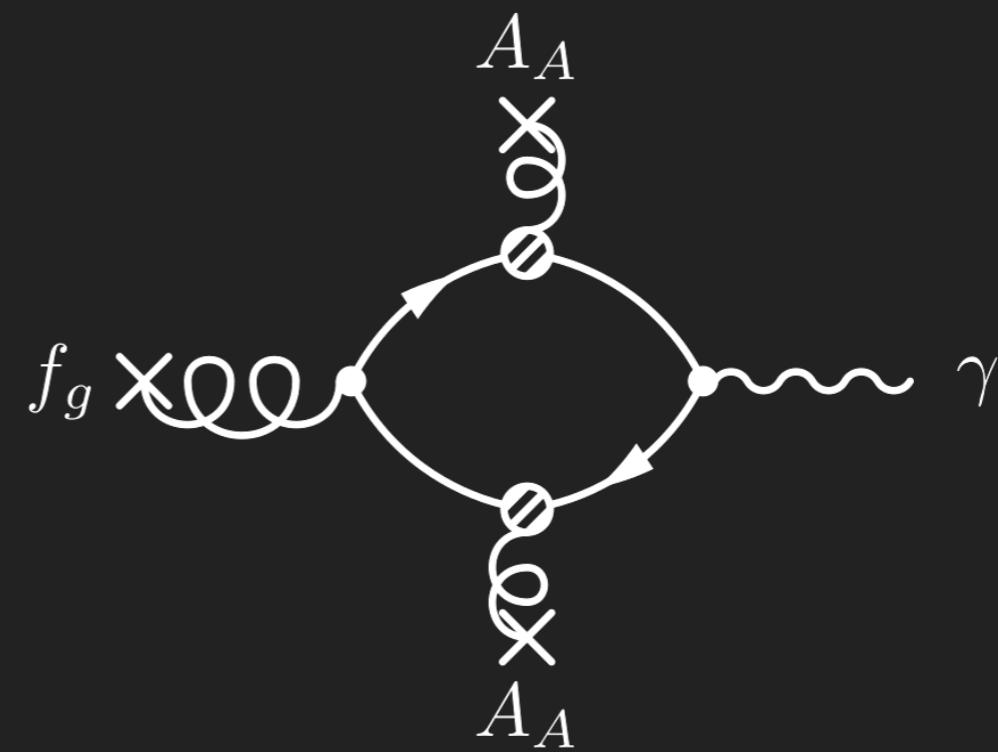
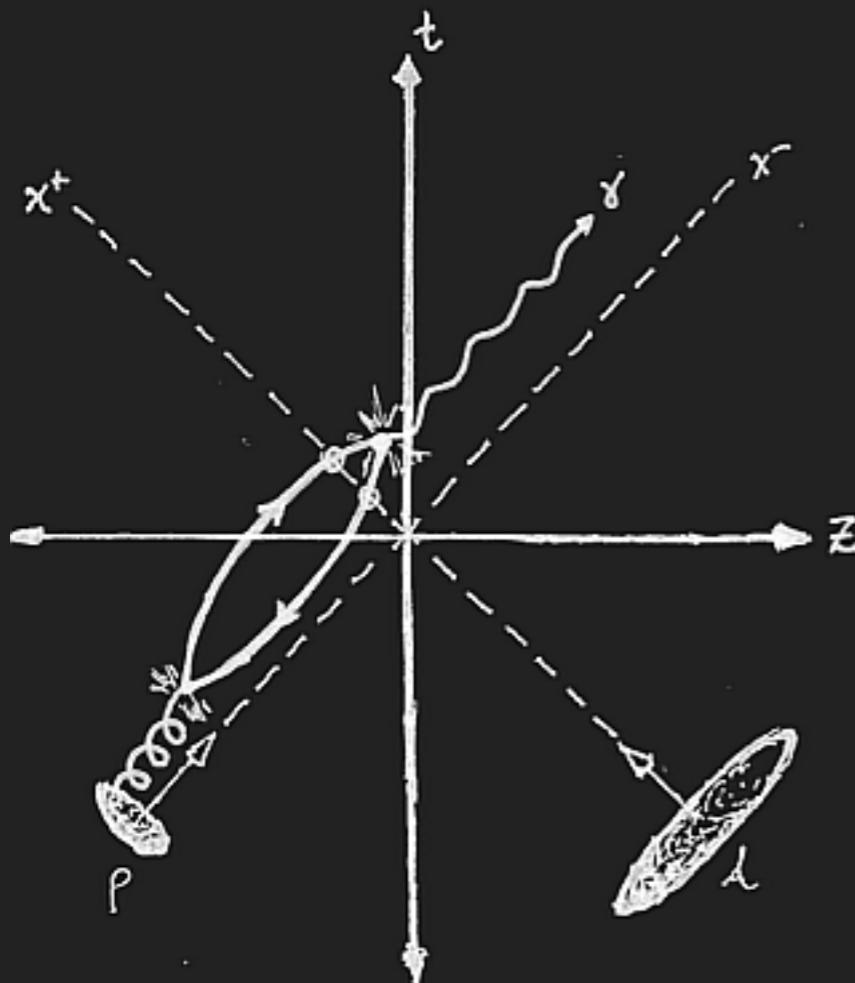
$$x \sim 10^{-2}$$

$$f_g(x, Q^2) \gg f_q(x, Q^2)$$



Can be reabsorbed as renormalisation of $f_q(x, Q^2)$

NLO: ANNIHILATION



Enhanced by $f_g(x, Q^2)$

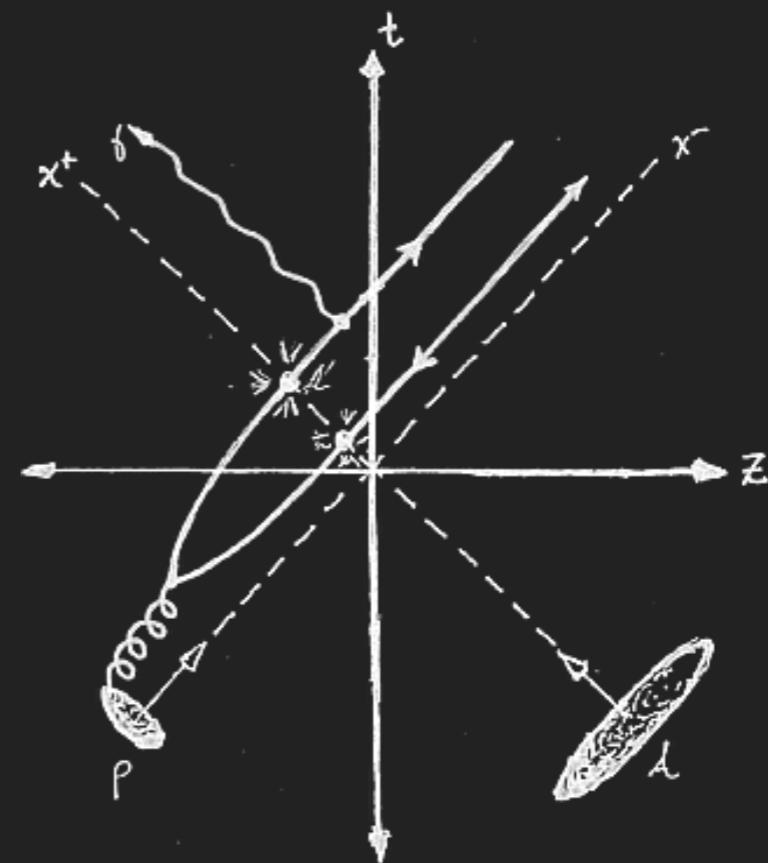
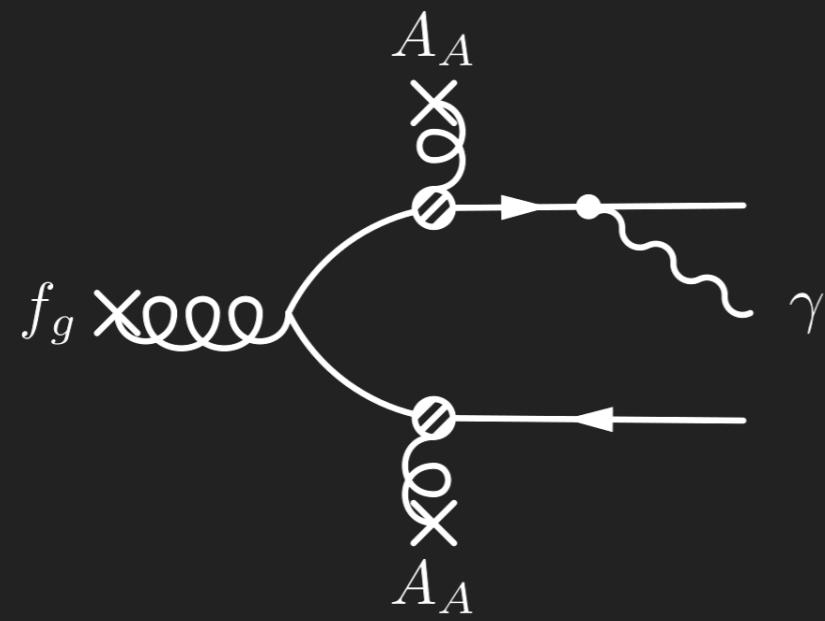
- ➡ Kinematically constrained
- ➡ Dominated by $k_\perp^2 = Q_{S,A}^2$

NLO: ANNIHILATION

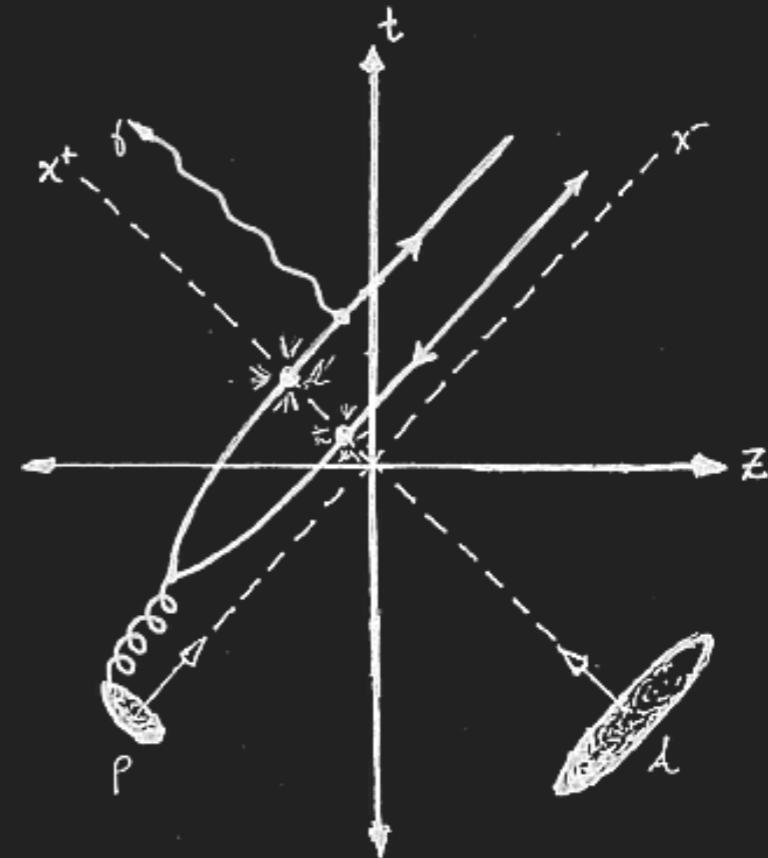
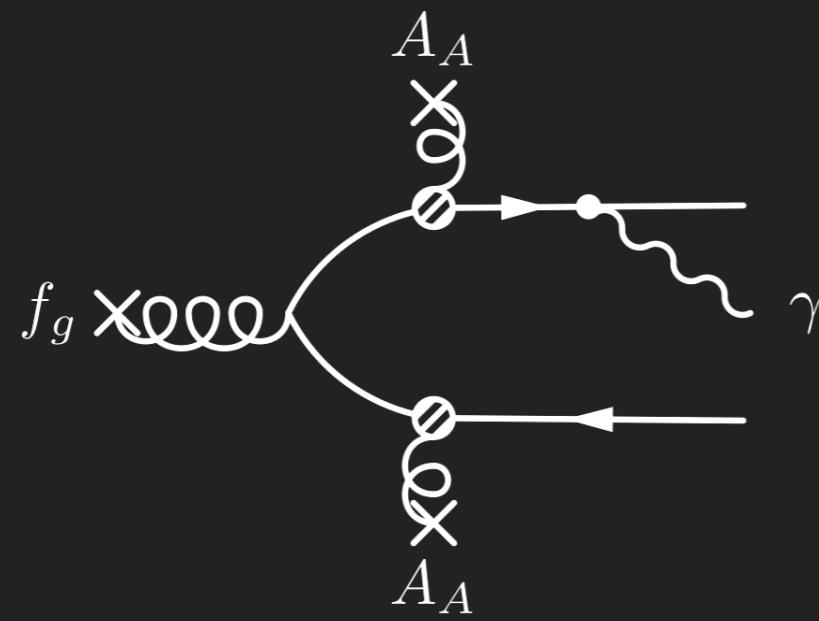


- ➡ Kinematically constrained
- ➡ Dominated by $k_\perp^2 = Q_{S,A}^2$

NLO: Q \bar{Q} PAIR + PHOTON

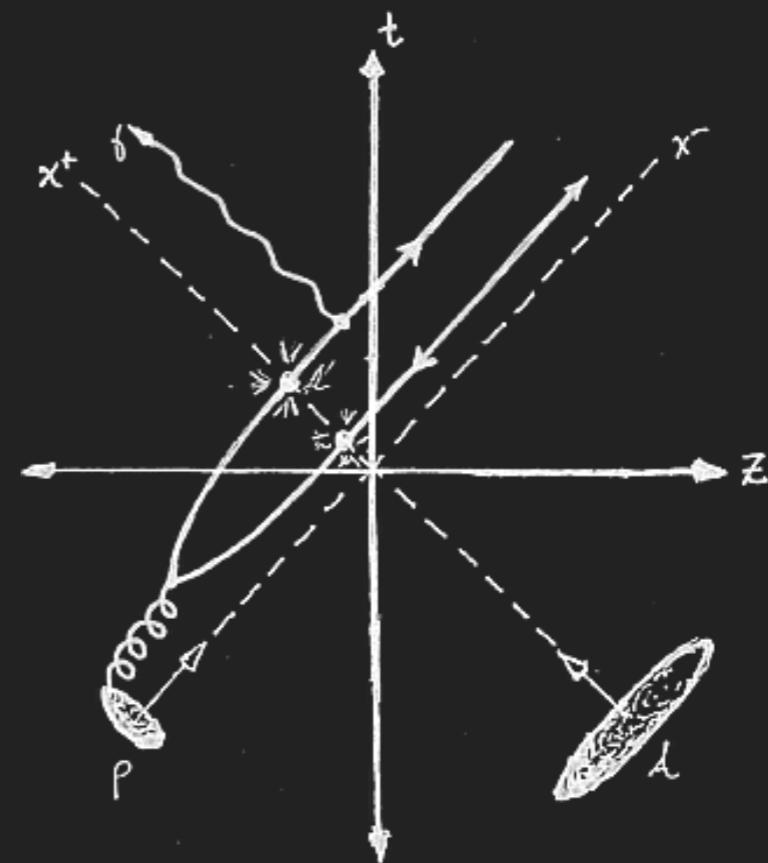
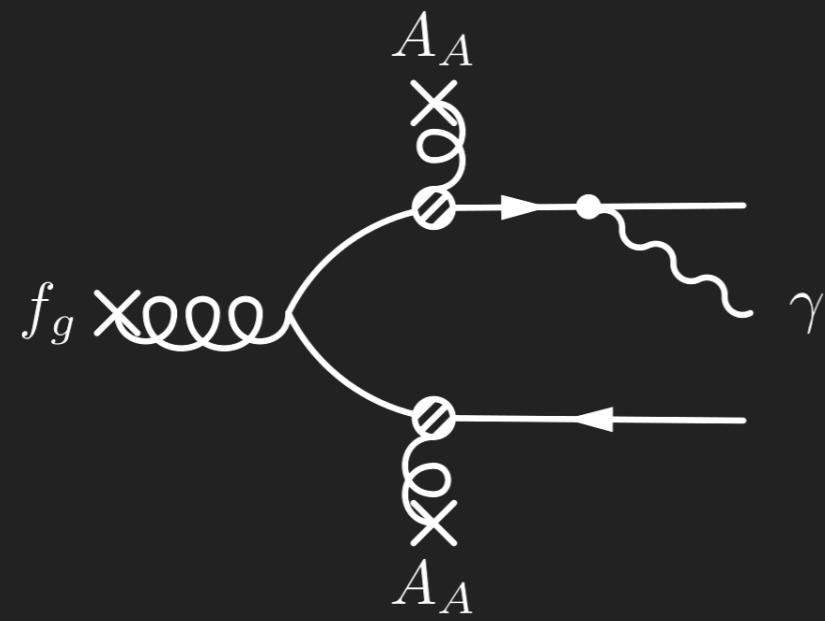


NLO: Q \bar{Q} PAIR + PHOTON



$$\begin{aligned} \frac{d\sigma}{d^2\mathbf{k}_{\gamma\perp} d\eta_\gamma} = & \frac{\alpha\alpha_S^2 q_f^2}{(2\pi)^8 C_F} \int_{\eta_q, \eta_p} \int_{\mathbf{q}_\perp, \mathbf{p}_\perp, \mathbf{k}_\perp, \mathbf{k}_{1\perp}, \mathbf{k}_{2\perp}} \delta^{(2)}(\mathbf{P}_\perp - \mathbf{k}_{1\perp} - \mathbf{k}_{2\perp}) \frac{\varphi_p(\mathbf{k}_{1\perp})}{k_{1\perp}^2} \\ & \times \left\{ \tau_{g,g}(\mathbf{k}_{1\perp}) \frac{\phi_A^{g,g}(\mathbf{k}_{2\perp})}{\mathbf{k}_{2\perp}} \right. \\ & + 2\tau_{g,qq}(\mathbf{k}_{1\perp}, \mathbf{k}_\perp) \frac{\phi_A^{qq,g}(\mathbf{k}_\perp, \mathbf{k}_{2\perp})}{\mathbf{k}_{2\perp}} \\ & \left. + 2\tau_{g,qq}(\mathbf{k}_{1\perp}, \mathbf{k}_\perp, \mathbf{k}_\perp) \frac{\phi_A^{qq,g}(\mathbf{k}_\perp, \mathbf{k}_{2\perp})}{\mathbf{k}_{2\perp}} \right\} \end{aligned}$$

NLO: Q \bar{Q} PAIR + PHOTON

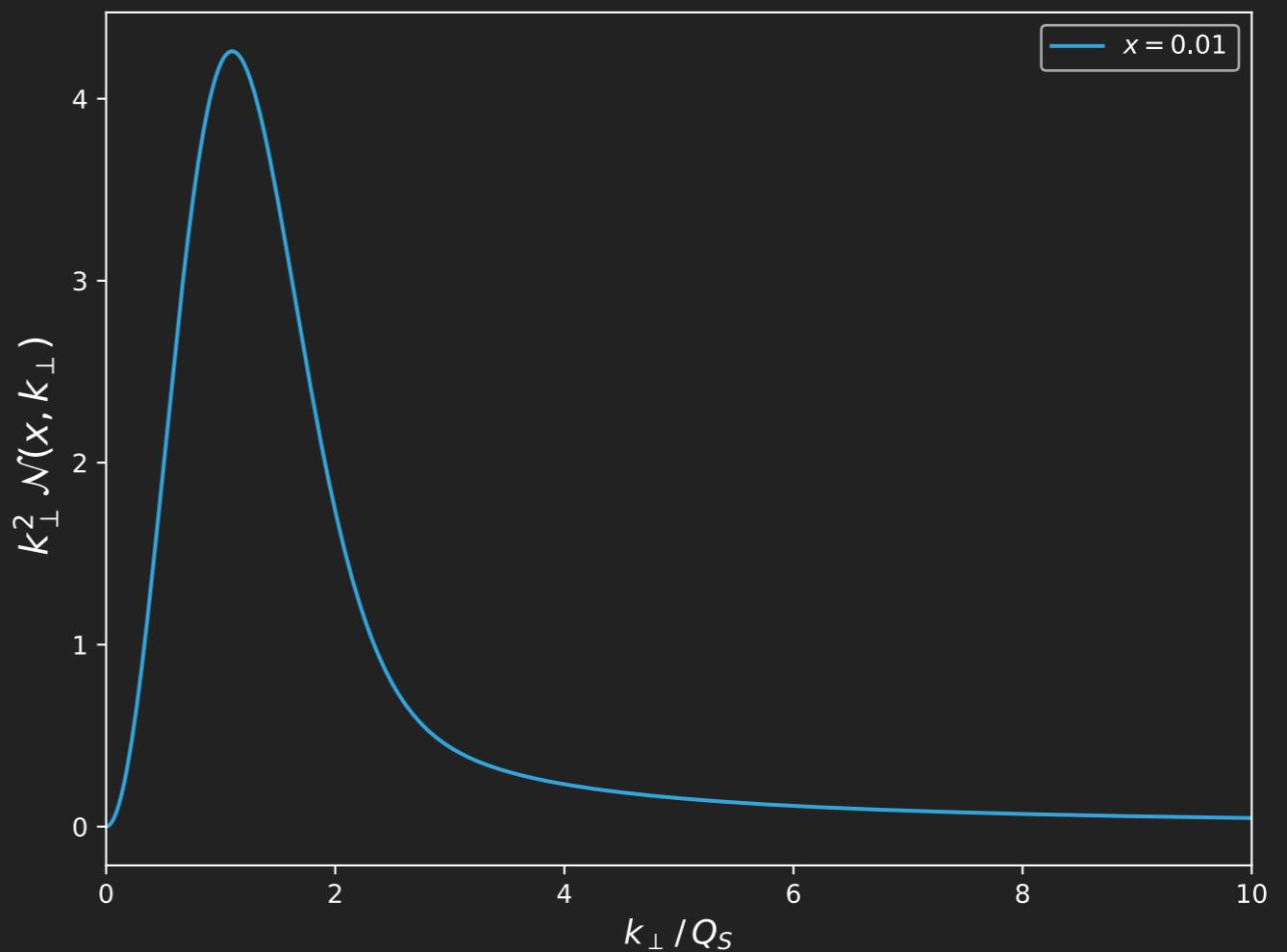


$$\begin{aligned} \frac{d\sigma}{d^2 k_{\gamma \perp} d\eta_\gamma} = & \frac{\alpha \alpha_S^2 q_f^2}{(2\pi)^8 C_F} \int_{\eta_q, \eta_p} \int_{\mathbf{q}_\perp, \mathbf{p}_\perp, \mathbf{k}_\perp, \mathbf{k}_{1\perp}, \mathbf{k}_{2\perp}} \delta^{(2)}(\mathbf{P}_\perp - \mathbf{k}_{1\perp} - \mathbf{k}_{2\perp}) \frac{\varphi_p(\mathbf{k}_{1\perp})}{k_{1\perp}^2} \\ & \times \theta(\mathbf{k}_{1\perp}, \mathbf{k}_\perp, \mathbf{k}'_\perp) \mathcal{N}(x_0, \mathbf{k}_{2\perp}) \mathcal{N}(x_0, \mathbf{k}_\perp - \mathbf{k}_{2\perp}) \end{aligned}$$

DIPOLE

@ MV-model

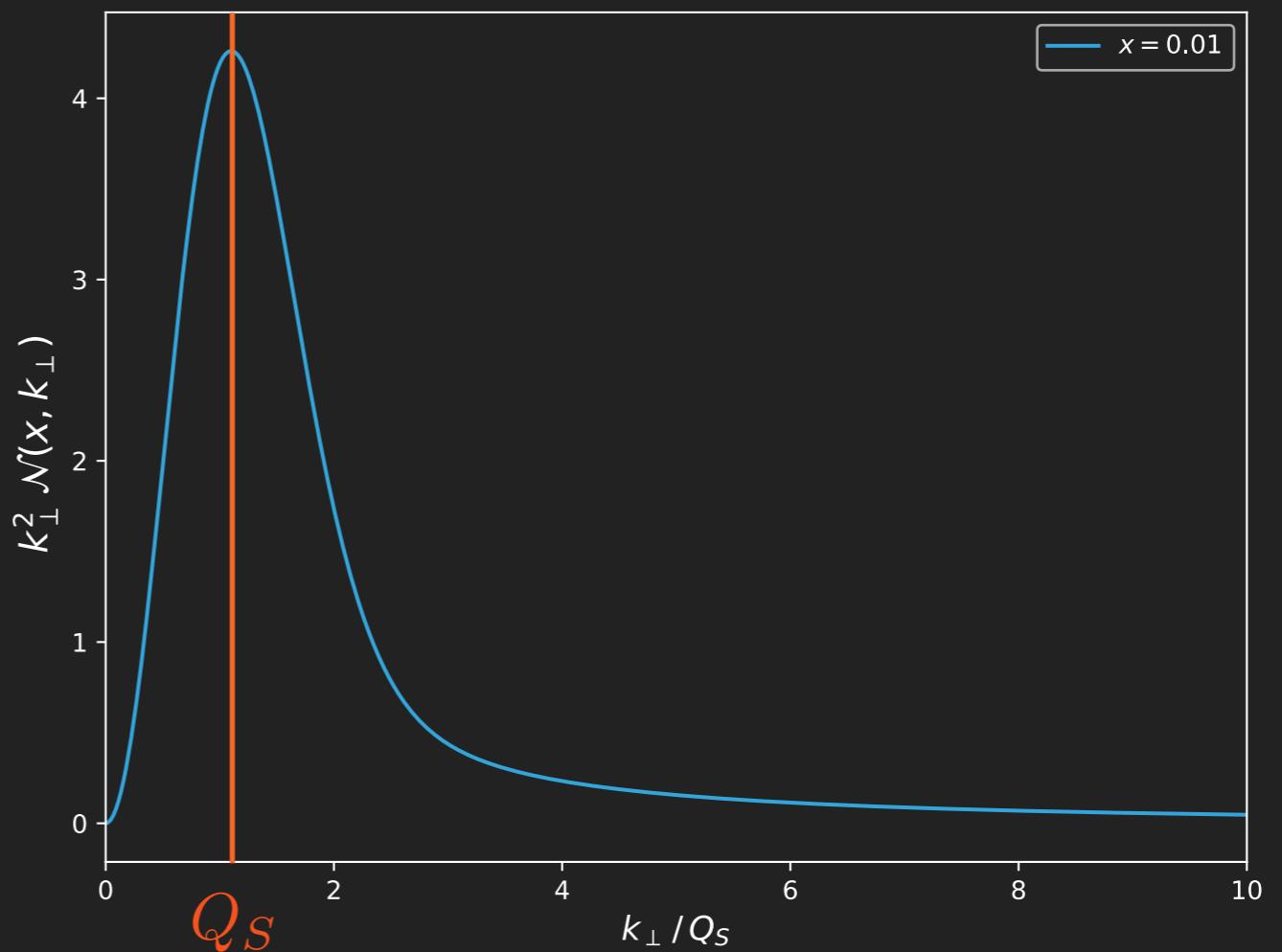
$$N(x_0, k) = \frac{1}{N_C} \langle U(k) U^\dagger(0) \rangle$$



DIPOLE

@ MV-model

$$N(x_0, k) = \frac{1}{N_C} \langle U(k) U^\dagger(0) \rangle$$



EVOLUTION

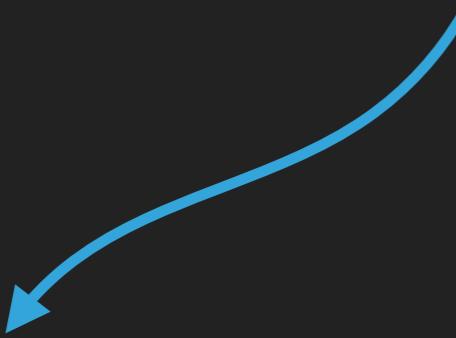


rcBK on the dipole

EVOLUTION



rcBK on the dipole

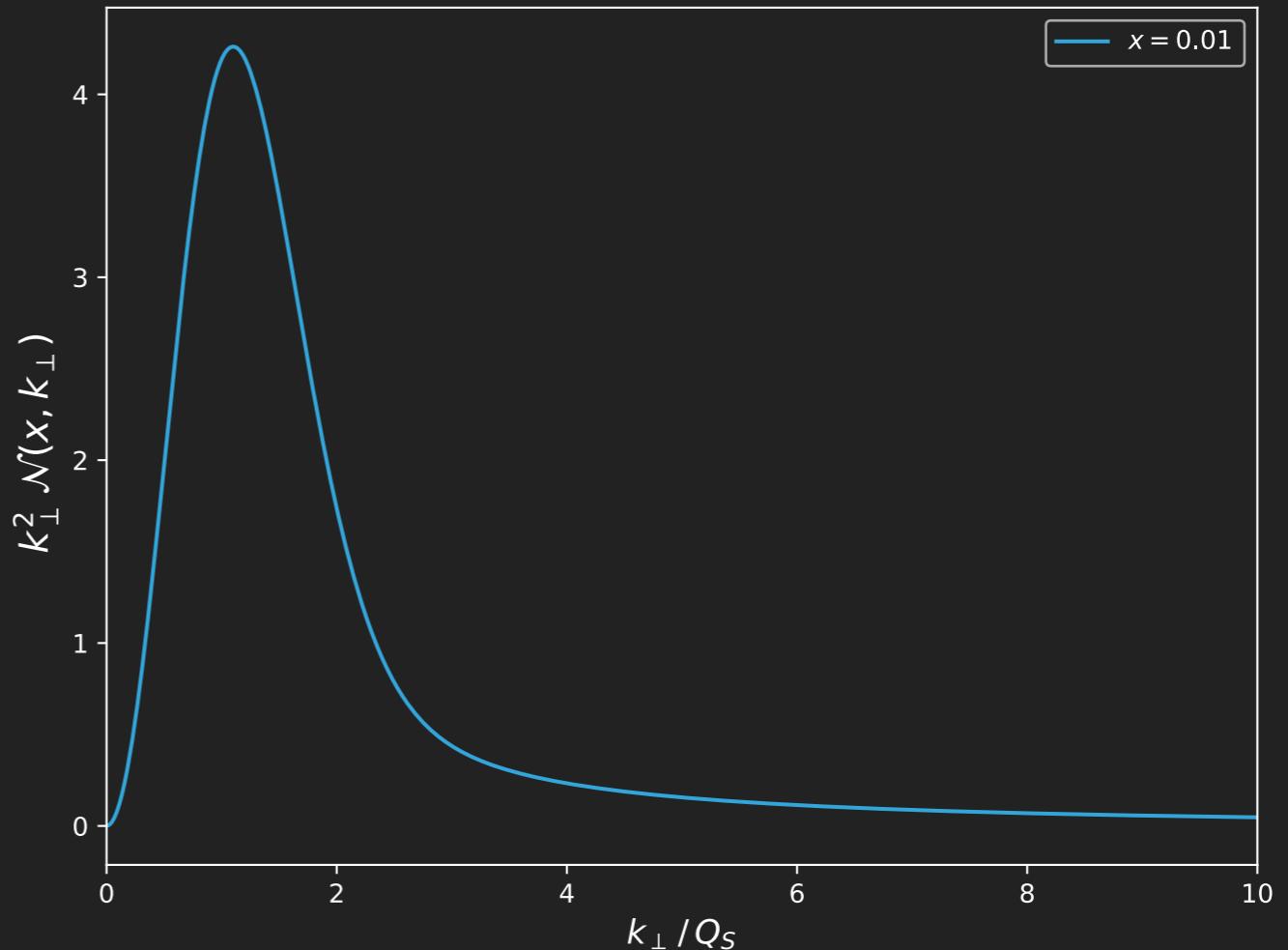


$$\frac{\partial \mathcal{N}(\mathbf{r}, x)}{\partial \log(x_0/x)} = \int d\mathbf{r}_1 K^{\text{run}}(\mathbf{r}, \mathbf{r}_1, \mathbf{r}_2) [\mathcal{N}(\mathbf{r}_1, x) + \mathcal{N}(\mathbf{r}_2, x) - \mathcal{N}(\mathbf{r}, x) - \mathcal{N}(\mathbf{r}_1, x)\mathcal{N}(\mathbf{r}_2, x)]$$

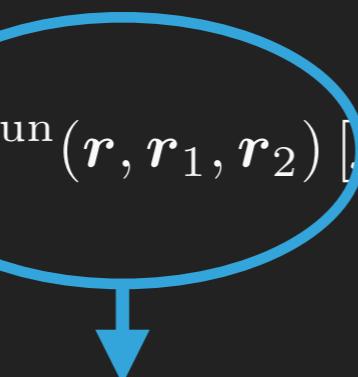
EVOLUTION



rcBK on the dipole



$$\frac{\partial \mathcal{N}(\mathbf{r}, x)}{\partial \log(x_0/x)} = \int d\mathbf{r}_1 K^{\text{run}}(\mathbf{r}, \mathbf{r}_1, \mathbf{r}_2) [\mathcal{N}(\mathbf{r}_1, x) + \mathcal{N}(\mathbf{r}_2, x) - \mathcal{N}(\mathbf{r}, x) - \mathcal{N}(\mathbf{r}_1, x)\mathcal{N}(\mathbf{r}_2, x)]$$

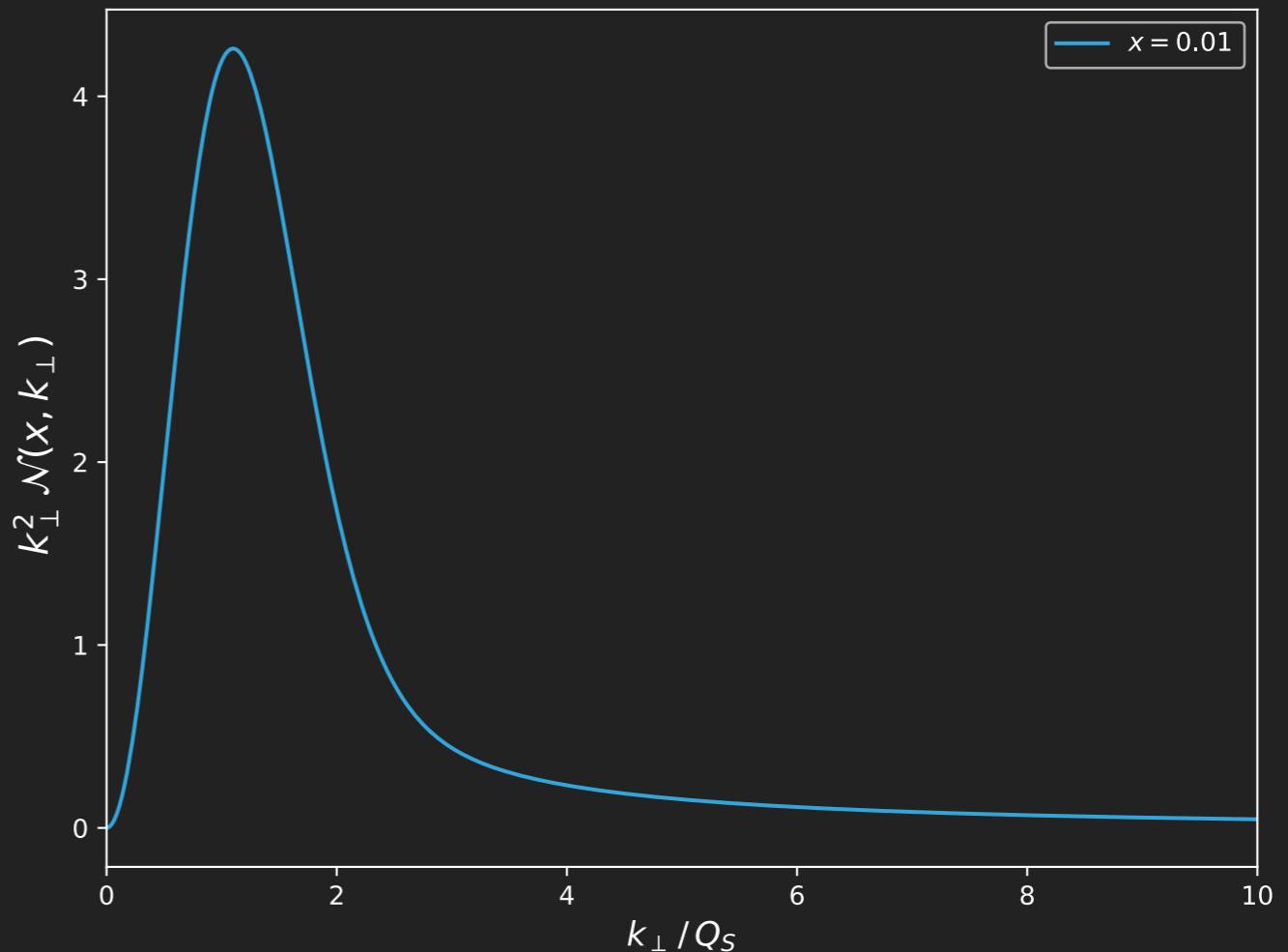


Kernel

EVOLUTION



rcBK on the dipole



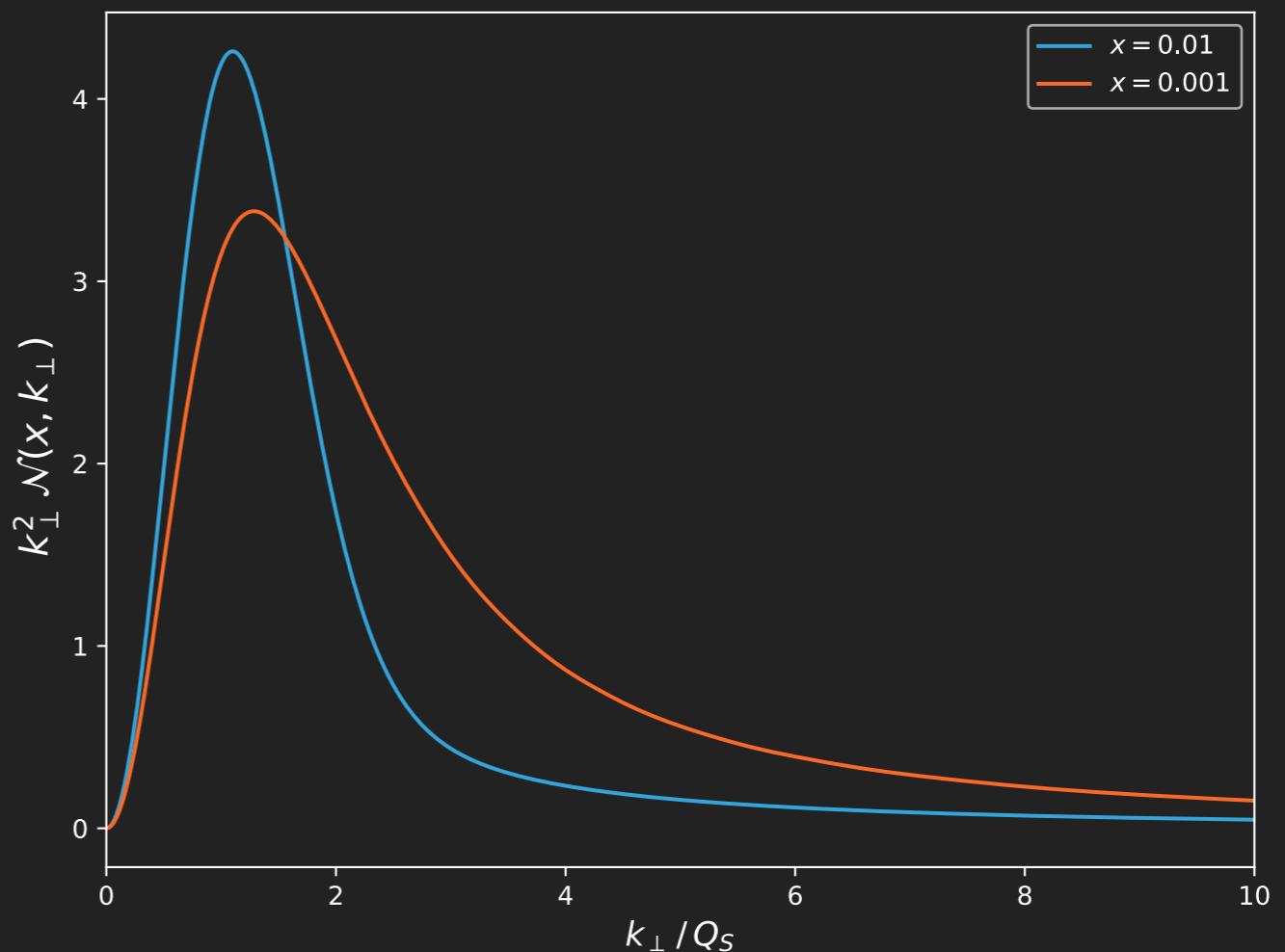
$$\frac{\partial \mathcal{N}(\mathbf{r}, x)}{\partial \log(x_0/x)} = \int d\mathbf{r}_1 K^{\text{run}}(\mathbf{r}, \mathbf{r}_1, \mathbf{r}_2) [\mathcal{N}(\mathbf{r}_1, x) + \mathcal{N}(\mathbf{r}_2, x) - \mathcal{N}(\mathbf{r}, x) - \mathcal{N}(\mathbf{r}_1, x)\mathcal{N}(\mathbf{r}_2, x)]$$

The equation is split into two parts by blue ovals. The left part, under the Kernel label, contains the terms $\mathcal{N}(\mathbf{r}_1, x) + \mathcal{N}(\mathbf{r}_2, x)$. The right part, under the Non-linear terms label, contains the terms $-\mathcal{N}(\mathbf{r}, x) - \mathcal{N}(\mathbf{r}_1, x)\mathcal{N}(\mathbf{r}_2, x)$.

EVOLUTION



rcBK on the dipole



$$\frac{\partial \mathcal{N}(\mathbf{r}, x)}{\partial \log(x_0/x)} = \int d\mathbf{r}_1 K^{\text{run}}(\mathbf{r}, \mathbf{r}_1, \mathbf{r}_2) [\mathcal{N}(\mathbf{r}_1, x) + \mathcal{N}(\mathbf{r}_2, x) - \mathcal{N}(\mathbf{r}, x) - \mathcal{N}(\mathbf{r}_1, x)\mathcal{N}(\mathbf{r}_2, x)]$$

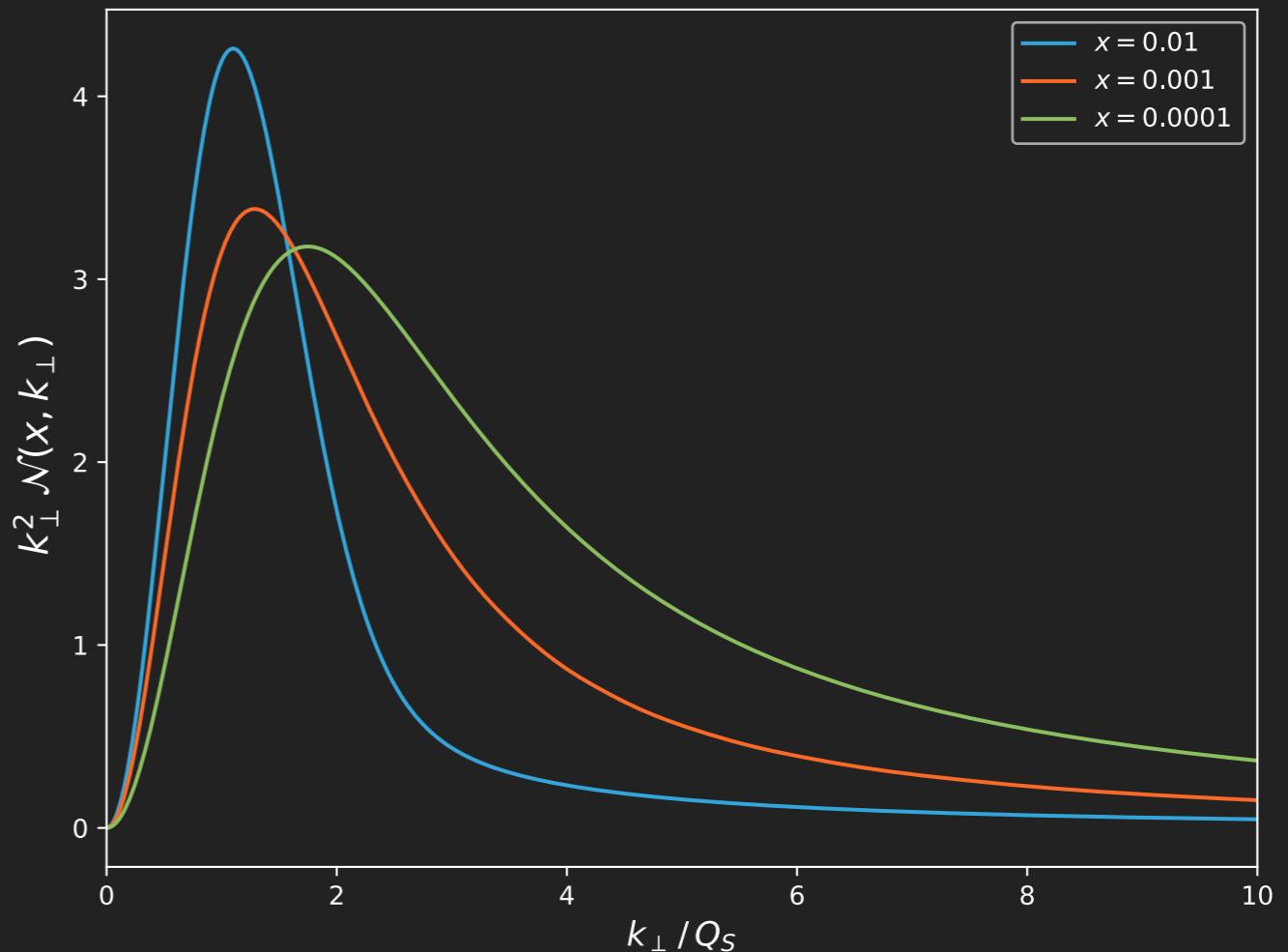
Kernel

Non-linear terms

EVOLUTION



rcBK on the dipole



$$\frac{\partial \mathcal{N}(\mathbf{r}, x)}{\partial \log(x_0/x)} = \int d\mathbf{r}_1 K^{\text{run}}(\mathbf{r}, \mathbf{r}_1, \mathbf{r}_2) [\mathcal{N}(\mathbf{r}_1, x) + \mathcal{N}(\mathbf{r}_2, x) - \mathcal{N}(\mathbf{r}, x) - \mathcal{N}(\mathbf{r}_1, x)\mathcal{N}(\mathbf{r}_2, x)]$$

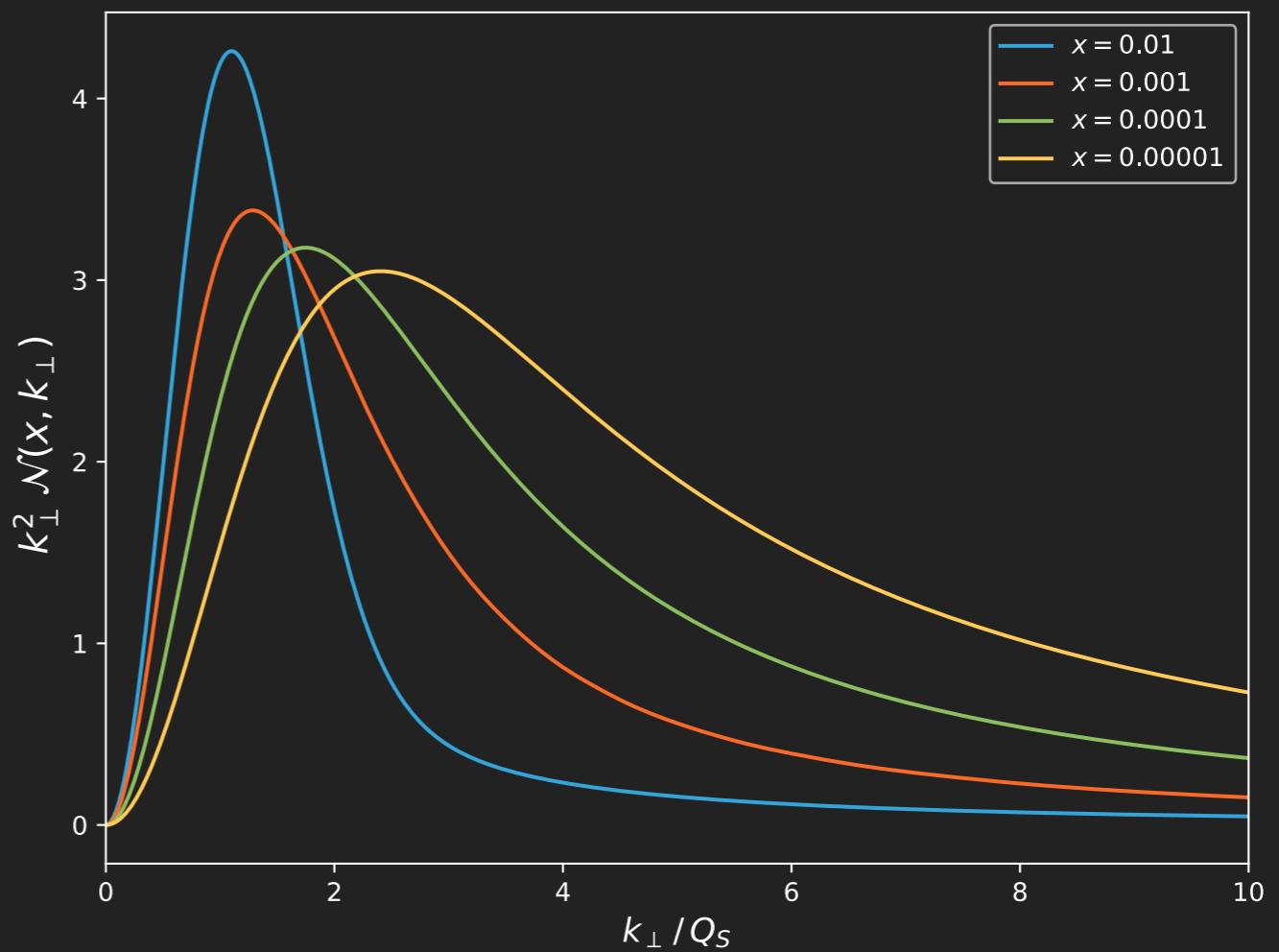
The equation is split into two parts by blue ovals:

- The left part, $\int d\mathbf{r}_1 K^{\text{run}}(\mathbf{r}, \mathbf{r}_1, \mathbf{r}_2) [\mathcal{N}(\mathbf{r}_1, x) + \mathcal{N}(\mathbf{r}_2, x) - \mathcal{N}(\mathbf{r}, x)]$, is labeled "Kernel".
- The right part, $- \mathcal{N}(\mathbf{r}_1, x)\mathcal{N}(\mathbf{r}_2, x)$, is labeled "Non-linear terms".

EVOLUTION



rcBK on the dipole



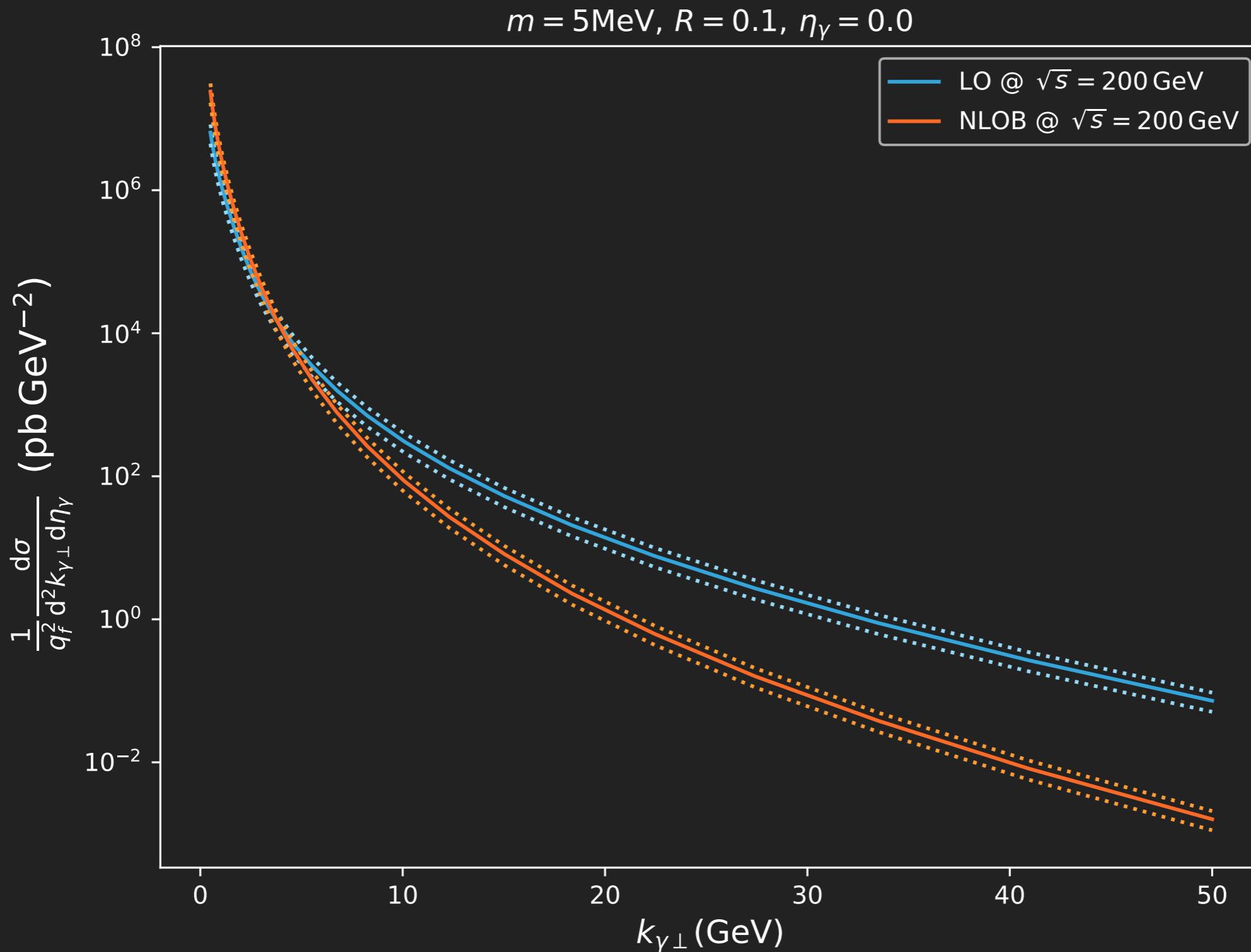
$$\frac{\partial \mathcal{N}(\mathbf{r}, x)}{\partial \log(x_0/x)} = \int d\mathbf{r}_1 K^{\text{run}}(\mathbf{r}, \mathbf{r}_1, \mathbf{r}_2) [\mathcal{N}(\mathbf{r}_1, x) + \mathcal{N}(\mathbf{r}_2, x) - \mathcal{N}(\mathbf{r}, x) - \mathcal{N}(\mathbf{r}_1, x)\mathcal{N}(\mathbf{r}_2, x)]$$

The equation is split into two parts by blue ovals:

- Kernel:** $\int d\mathbf{r}_1 K^{\text{run}}(\mathbf{r}, \mathbf{r}_1, \mathbf{r}_2) [\mathcal{N}(\mathbf{r}_1, x) + \mathcal{N}(\mathbf{r}_2, x) - \mathcal{N}(\mathbf{r}, x) - \mathcal{N}(\mathbf{r}_1, x)\mathcal{N}(\mathbf{r}_2, x)]$
- Non-linear terms:** $\int d\mathbf{r}_1 K^{\text{run}}(\mathbf{r}, \mathbf{r}_1, \mathbf{r}_2) [\mathcal{N}(\mathbf{r}_1, x) + \mathcal{N}(\mathbf{r}_2, x) - \mathcal{N}(\mathbf{r}, x) - \mathcal{N}(\mathbf{r}_1, x)\mathcal{N}(\mathbf{r}_2, x)]$

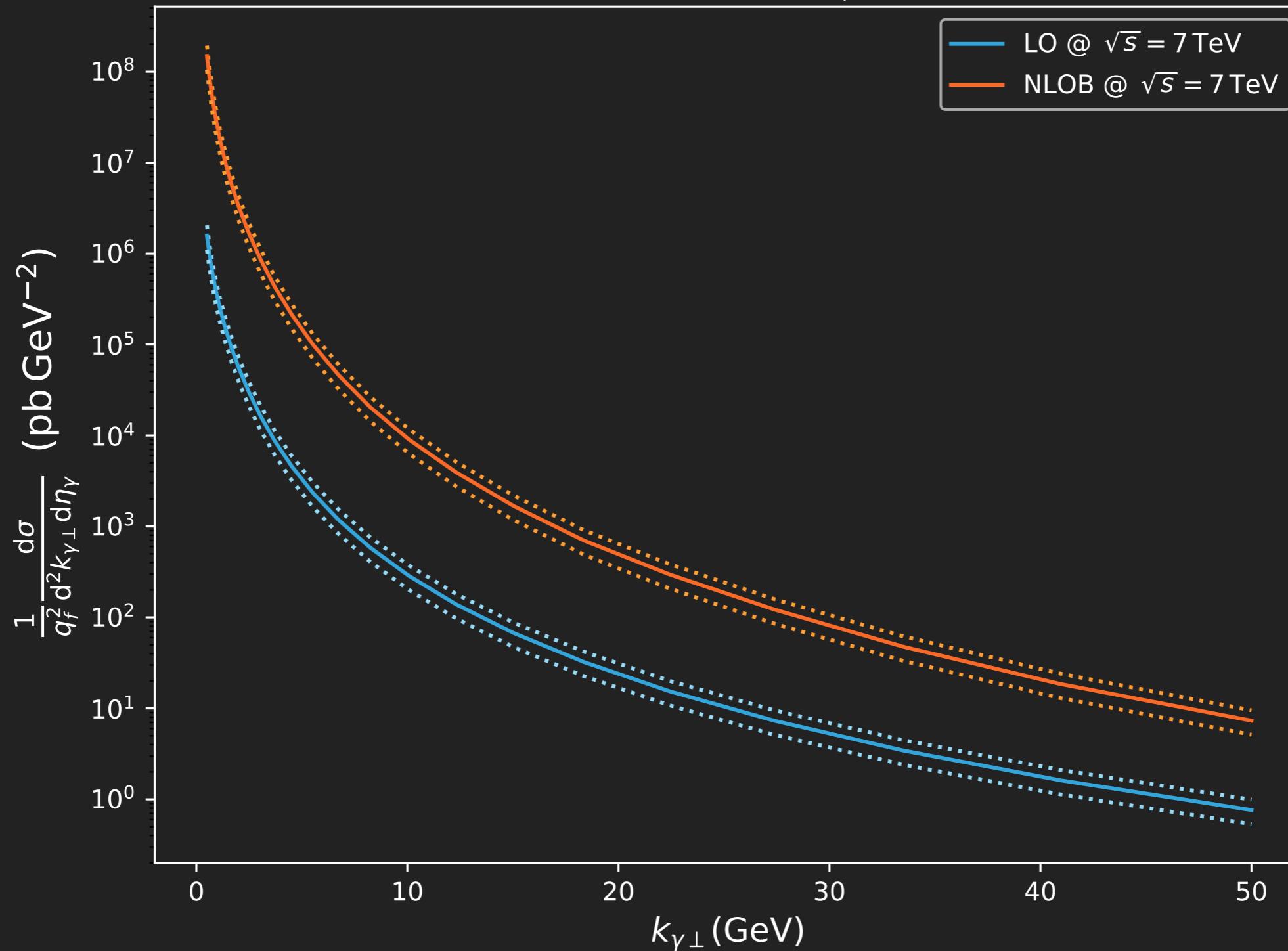
RESULTS

CROSS SECTION



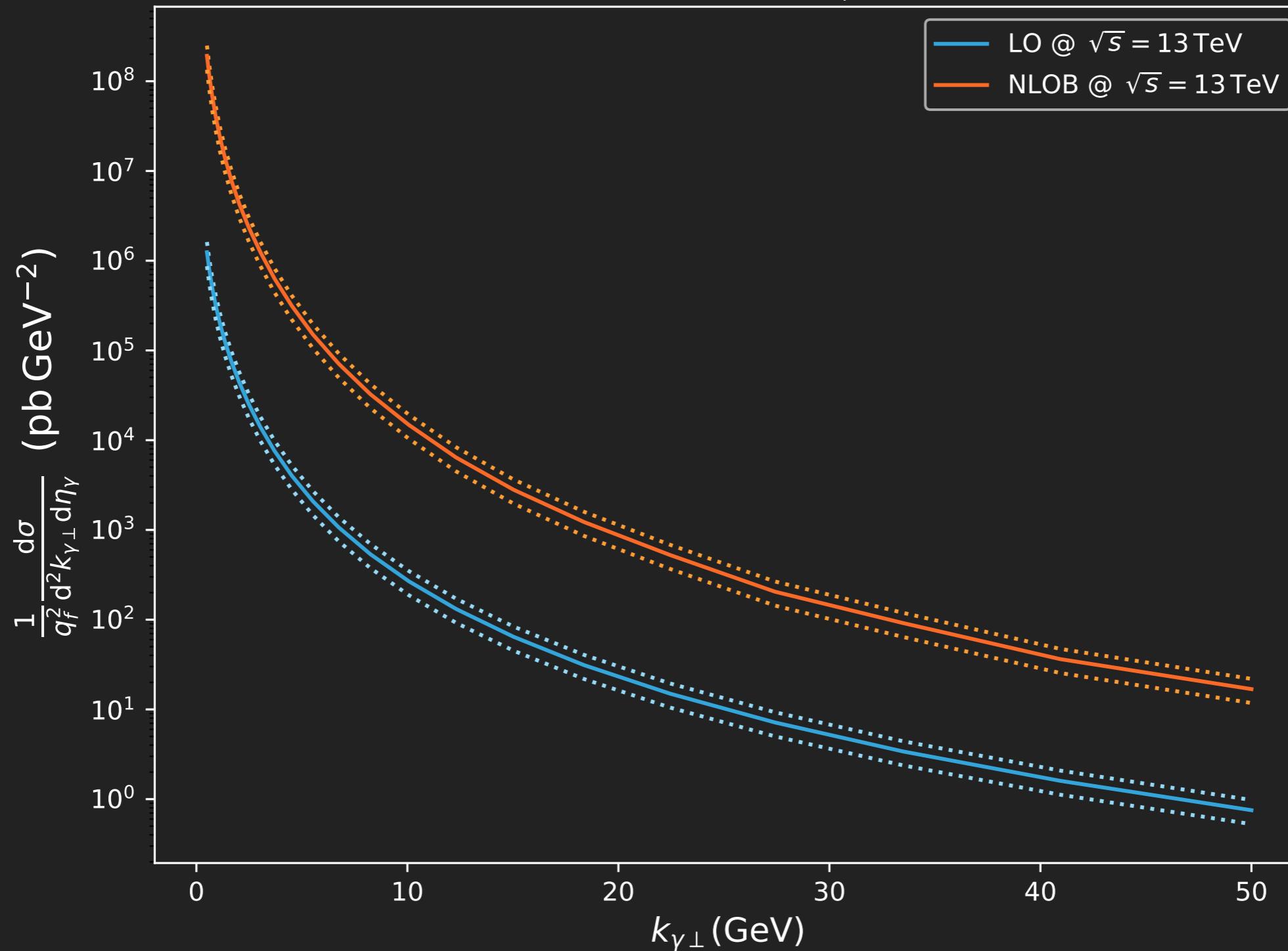
CROSS SECTION

$m = 5\text{MeV}$, $R = 0.1$, $\eta_\gamma = 0.0$

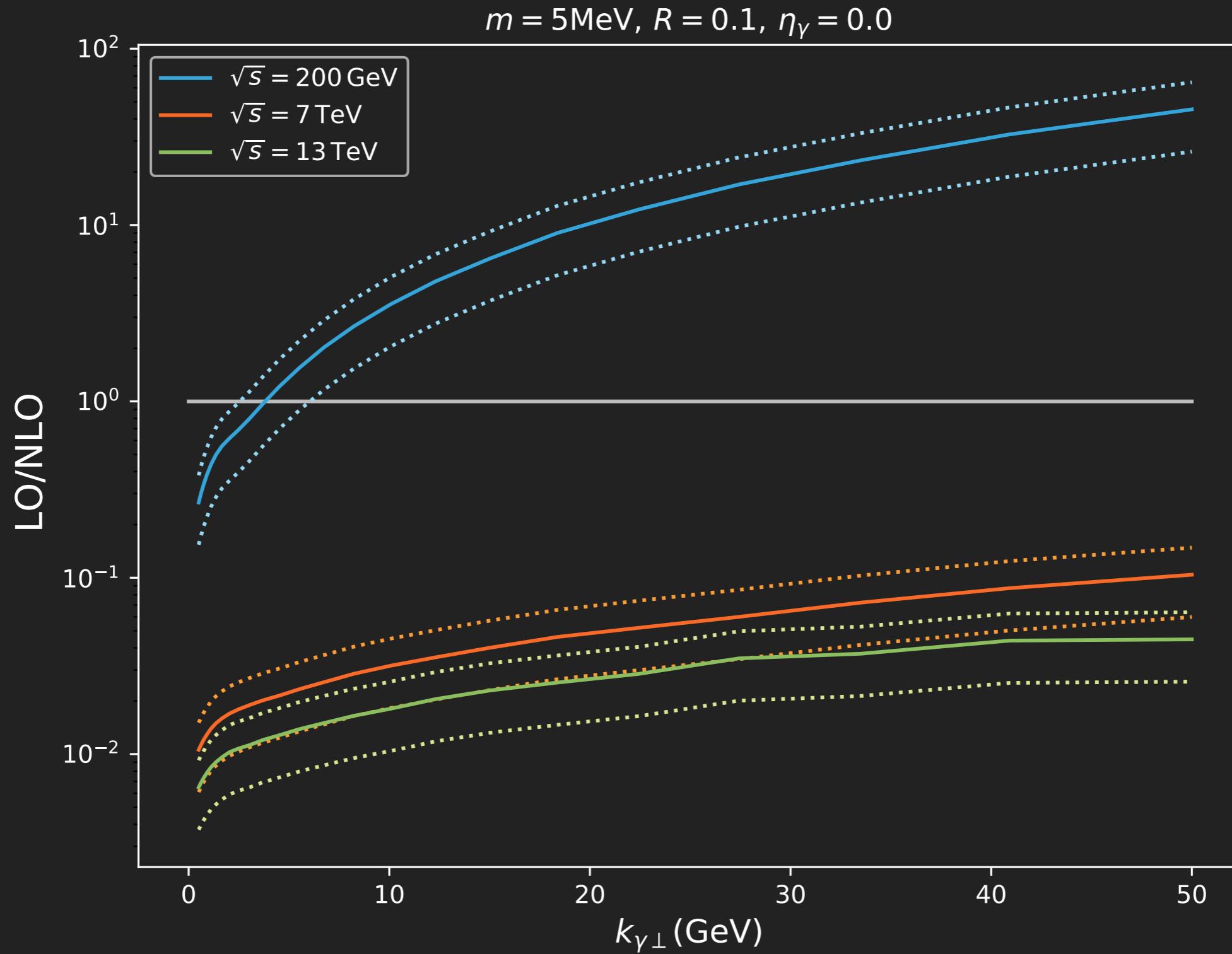


CROSS SECTION

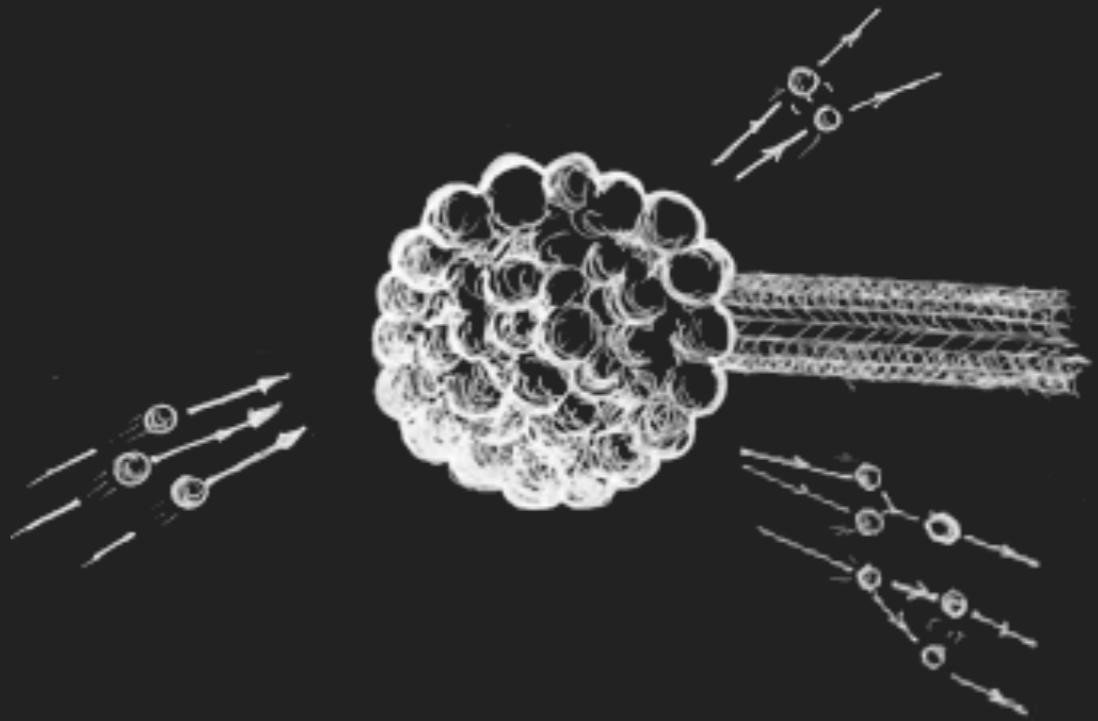
$m = 5\text{MeV}$, $R = 0.1$, $\eta_\gamma = 0.0$



RATIOS



SUMMARY



- ➊ Saturation modifies the emission process thanks to multi-particle scatterings
- ➋ Complete analytical result at NLO, $\mathcal{O}(\alpha \alpha_s)$
- ➌ CGC formalism yields correct limits to the pQCD results

OUTLOOK



Comparison to current pp and pA experimental data, as well as prediction for new runs.



Photon-hadron correlations are sensitive to saturation.



More exciting studies:

- NNLO?
- Higher particle correlations?
- Saturation and Anomalies?



THANK YOU

