QCD under Extreme Conditions

(second lecture)

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Second lecture:

- * Effective model building
- \star Z(N), the Polyakov loop, and confinement
- * Chiral symmetry breaking
- * One example on relevance and difficulties in exploring the phase diagram
 - Drawing the phase diagram
 - And, if there is time: Chiral magnetic effect and the strong CP problem

***** Final comments



To go beyond in our study of the phases of QCD, we need to know its symmetries, and how they are broken spontaneously or explicitly. But QCD is very complicated:

- First, it is a non-abelian $SU(N_c)$ gauge theory, with gluons living in the adjoint representation
- Then, there are N_f dynamical quarks (who live in the fund. rep.)
- On top of that, all these quarks have masses which are all different! Very annoying from the point of view of symmetries!

So, in studying the phases of QCD, we do it by parts, and consider many "cousin theories" which are very similar to QCD but simpler (more symmetric). We also study the dependence of physics on parameters which are fixed in nature.



The basic hierarchy is the following:

pure glue SU(N):

- Z(N) symmetry (SSB)
- order parameter: Polyakov loop L
- deconfining trans.: N=2 (2nd order), N=3 (weakly 1st order)
 - + massless quarks:
 - chiral symmetry (SSB)
 - \bullet order parameter: chiral condensate σ
 - Z(N) explicitly broken, but rise of L -> deconf.
 - chiral trans.: N=3,2 (N_f=2) 2^{nd} order

+ massive quarks:

Z(N) and chiral explicitly broken Yet vary remarkably and L <--> σ

Ø

$SU(N_c)$, $Z(N_c)$ and the Polyakov loop

For the QCD Lagrangian (massless quarks)

$$\mathcal{L} = \frac{1}{2} tr G_{\mu\nu}^2 + \bar{q} i \gamma^{\mu} D_{\mu} q \qquad D_{\mu} = \partial_{\mu} - ig A_{\mu} \quad , \quad G_{\mu\nu} = \frac{1}{-ig} [D_{\mu}, D_{\nu}]$$

we have invariance under local $SU(N_c)$. In particular, we have invariance under elements of the center $Z(N_c)$

$$\Omega_c = e^{i\frac{2n\pi}{N_c}}\mathbf{1}$$

At finite temperature, one has also to impose the following boundary conditions:

$$A_{\mu}(\vec{x},\beta) = +A_{\mu}(\vec{x},0)$$
 , $q(\vec{x},\beta) = -q(\vec{x},0)$

Any gauge transf. that is periodic in t will do it. However, 't Hooft noticed that the class of possible tranfs. is more general! They are such that



$$\Omega(\vec{x},\beta) = \Omega_c \quad , \quad \Omega(\vec{x},0) = 1$$

$$A^{\Omega}(\vec{x},\beta) = \Omega_c^{\dagger} A_{\mu}(\vec{x},\beta) \Omega_c = +A_{\mu}(\vec{x},0)$$

$$q^{\Omega}(\vec{x},\beta) = \Omega_c^{\dagger}q(\vec{x},\beta) = e^{-i\phi}q(\vec{x},\beta) \neq -q(\vec{x},0)$$

keeping the gauge fields invariant but not the quarks!

For pure glue, this $Z(N_c)$ symmetry is exact, and we can define an order parameter from the trace of the Polyakov loop:

$$\ell(\vec{x}) = \frac{1}{N_c} \operatorname{Tr} L(\vec{x}) = \frac{1}{N_c} \operatorname{Tr} \mathcal{P} \exp\left[ig \int_0^\beta d\tau \ \tau^a A_0^a(\vec{x},\tau)\right]$$

$$L(\vec{x}) \mapsto \Omega_c \ L(\vec{x}) \ \mathbf{1} = e^{i\frac{2n\pi}{N_c}} L(\vec{x})$$

Exercise: show it in detail!

<u>N.B</u>: ℓ is gauge invariant.





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At very high T, g \sim 0, and β -> 0, so that

$$\langle \ell \rangle = e^{i \frac{2n\pi}{N_c}} \ell_0 \,, \ \ell_0 \sim 1$$

and we have a N-fold degenerate vacuum, signaling SSB of global $Z(N_c)$. At T = 0, confinement implies that $\ell_0 = 0$ ['t Hooft (1978)].

Then, l_0 can be used as an <u>order parameter</u> for the deconfining transition:

$$\ell_0 = 0$$
 , $T < T_c$; $\ell_0 > 0$, $T > T_c$

Usually the Polyakov loop is related to the free energy of an infinitely heavy test quark via [McLerran & Svetitsky (1981)]

$$\langle \ell \rangle = e^{-F_{test}/T}$$
 (confinement

(confinement: no free quark)

Exercise: do you see any possible problem in the equation above? (Cf. 1st eqn in this slide!) If so, could we, instead, relate $\langle \ell \rangle$ to the propagator for a test quark?



3

 W_2^2

Form of the effective potential for the Polyakov loop







Adding massless quarks (chiral symmetry)

In the limit of massless quarks, QCD is invariant under global chiral rotations $U(N_f)_L \times U(N_f)_R$ of the quark fields.

One can rewrite this symmetry in terms of vector (V = R + L) and axial (A = R - L) rotations

$U(N_f)_L \times U(N_f)_R \sim U(N_f)_V \times U(N_f)_A$

As U(N) \sim SU(N) x U(1), one finds

 $U(N_f)_L \times U(N_f)_R \sim SU(N_f)_L \times SU(N_f)_R \times U(1)_V \times U(1)_A$

where we see the $U(1)_V$ from quark number conservation and the $U(1)_A$ broken by instantons.

Exercise: can we restore $U(1)_A$ in a hot and dense medium? Think of possible consequences and observables.

Quarks (even massless) break explicitly Z(3)!









In QCD, the remaining $SU(N_f)_L \times SU(N_f)_R$ is explicitly broken by a <u>nonzero</u> mass term. Take, for simplicity, $N_f=2$:

$$\mathcal{L} = -\frac{1}{4} F^{a}_{\mu\nu} F^{a\mu\nu} + \bar{\psi}^{f}_{L} \gamma^{\mu} D_{\mu} \psi_{L} + \bar{\psi}^{f}_{R} \gamma^{\mu} D_{\mu} \psi^{f}_{R} - m_{u} \left(\bar{u}_{L} u_{R} + \bar{u}_{R} u_{L} \right) - m_{d} \left(\bar{d}_{L} d_{R} + \bar{d}_{R} d_{L} \right)$$

so that, for non-vanishing $m_u = m_d$, the only symmetry that remains is the vector isospin SU(2)_V. In the light quark sector of QCD, chiral symmetry is just approximate.

Then, for massless QCD, one should find parity doublets in the vacuum, which is not confirmed in the hadronic spectrum. Thus, chiral symmetry must be broken in the vacuum by the presence of a quark chiral condensate, so that

$$SU(N_f)_L \times SU(N_f)_R \to SU(N_f)_V$$

and the broken generators allow for the existence of pions, kaons, ...

Ø

Hence, for massless QCD, we can define an order parameter for the SSB of chiral symmetry in the vacuum – the chiral condensate:

$$\langle 0|\bar{\psi}\psi|0\rangle = \langle 0|\bar{\psi}_L\psi_R|0\rangle + \langle 0|\bar{\psi}_R\psi_L|0\rangle$$

so that this vacuum expectation value couples together the L & R sectors, unless in the case it vanishes.

For very high temperatures or densities (low α_s), one expects to restore chiral symmetry, melting the condensate that is a function of T and m and plays the role of an order parameter for the chiral transition in QCD.



Form of the effective potential for the chiral condensate

 $T >> T_c$:

 $T \ll T_c$:







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From pure gauge deconfinement to the chiral limit: Playing with quark masses in the "QCD transition(s)"



Some results from the lattice [Borsányi et al (2012), from 3 papers]



pure gauge and pQCD



QCD with physical quark masses



QCD with physical quark masses



QCD with physical quark masses





 Two relevant phase transitions in QCD associated with SSB mechanisms for <u>different</u> symmetries of the action

- Approximate $Z(N_c)$ symmetry and deconfinement [exact for pure gauge $SU(N_c)$]. Order parameter: (trace of the) Polyakov loop
- Approximate chiral symmetry and chiral transition [exact for massless quarks]. Order parameter: chiral condensate.
- Some good estimates within a very simple framework: the bag model. Very crude, disagrees with lattice QCD on the nature of the transition, but still used in several calculations (EoS for compact stars, hydro evolution of the QGP, etc.)
- Going beyond: effective models (based on symmetries of S_{QCD})



Effective models: general idea

Keep relevant symmetries

• Try to include in the effective action all terms allowed by the chosen symmetries

- Mimic QCD at low energy using a simpler field theory
- Analytic results: estimates, qualitative behavior, etc.
- Examples: linear σ model, NJL model, Polyakov loop model, ...

• Just part of the story – combined with lattice QCD and/or data from experiments may provide good insight

NB: chiral perturbation theory - "the" effective model

Examples:

Linear σ model:

$$\mathcal{L} = \bar{q} \left[i \gamma^{\mu} \partial_{\mu} - g \left(\sigma + i \gamma_5 \vec{\tau} \cdot \vec{\pi} \right) \right] q + \frac{1}{2} \left(\partial_{\mu} \sigma \partial^{\mu} \sigma + \partial_{\mu} \vec{\pi} \cdot \partial^{\mu} \vec{\pi} \right) - U(\sigma, \vec{\pi})$$

$$U(\sigma, \vec{\pi}) = \frac{\lambda^2}{4} \left(\sigma^2 + \vec{\pi}^2 - v^2 \right)^2 - H\sigma$$

NJL model:

$$\mathcal{L} = \bar{q} \left(i \gamma^{\mu} \partial_{\mu} - m_0 \right) q + \frac{G}{2} \left[(\bar{q}q)^2 + (\bar{q}i\gamma_5 \vec{\tau}q)^2 \right]$$

Polyakov loop model:

$$\mathcal{V}(\ell) = \left(-\frac{b_2}{2} |\ell|^2 - \frac{b_3}{6} (\ell^3 + (\ell^*)^3) + \frac{1}{4} (|\ell|^2)^2\right) b_4 T^4$$



Example: LSM & the chiral transition

- Symmetry: for massless QCD, the action is invariant under $SU(N_f)_L \ x \ SU(N_f)_R$
- "Fast" degrees of freedom: quarks "Slow" degrees of freedom: mesons
- Typical energy scale: hundreds of MeV
- For $SU(N_f=2)$, for simplicity, we have pions and the sigma
- Framework: coarse-grained Landau-Ginzburg effective potential
- $SU(2) \times SU(2)$ spontaneously broken in the vacuum
- Can also accommodate explicit breaking by massive quarks



Building the effective lagrangian

[with scalars allowed by χ symmetry]

• Kinetic terms:

$$\frac{1}{2}\partial_{\mu}\sigma\partial^{\mu}\sigma + \frac{1}{2}\partial_{\mu}\vec{\pi}\cdot\partial^{\mu}\vec{\pi}$$

• Fermion-meson interaction:

$$g(i\bar{q}\gamma_5\vec{\tau}q)\cdot\vec{\pi}$$



$$g(\bar{q}q)\sigma$$

• Chiral self-interaction:

$$V = V(\pi^{2} + \sigma^{2}) = \frac{\lambda}{4} ((\pi^{2} + \sigma^{2}) - f_{\pi}^{2})^{2}$$

• Explicit chiral symmetry breaking term:

$$\delta \mathcal{L}_{SB} = h\sigma$$



Exercise: prove that the terms above are the ones allowed by <u>chiral</u> symmetry, except for the last which breaks it explicitly.

Parameters should be fixed such that:

• SU(2)_L x SU(2)_R is spontaneously broken in the vacuum, with $\langle \sigma \rangle = f_{\pi}$, $\langle \pi \rangle = 0$

 h should be related to the nonzero pion mass (plays a role analogous to an external magnetic field for a spin system)

• $f_{\pi} = 93$ MeV is the pion decay constant, determined experimentally. It comes about when one computes the weak decay of the pion, which is proportional to the amplitude

$$\langle 0|J^{\mu a}_{axial}(x)|\pi^b(q)\rangle = -if_{\pi}q^{\mu}\delta^{ab}e^{-iq\cdot x}$$

a,b: isospin



• The small but nonzero pion mass breaks "softly" the axial current:

$$\langle 0|\partial_{\mu}J^{\mu a}_{axial}(x)|\pi^{b}(q)\rangle = -f_{\pi}q^{2}\delta^{ab}e^{-iq\cdot x} = f_{\pi}m_{\pi}^{2}\delta^{ab}e^{-iq\cdot x}$$

• PCAC: "partial conservation of the axial current"

• Including a term \sim h σ brings the following consequences:

- The true vacuum (in the σ direction) is shifted [we can redefine f_{π} such that it coincides with the experimental value]



– The σ mass is modified

$$m_{\sigma}^2 = \left(\frac{\partial^2 V}{\partial \sigma^2}\right)_{\sigma_0} = 2\lambda f_{\pi}^2 + \frac{h}{f_{\pi}}$$

- Pions acquire a nonzero mass

$$m_{\pi}^2 = \left(\frac{\partial^2 V}{\partial \pi^2}\right)_{\sigma_0} = \frac{h}{f_{\pi}} > 0$$

which fixes h to be:

$$h = f_{\pi} m_{\pi}^2$$

Then, all parameters can be chosen to reproduce the vacuum features of mesons.

- The connection with the quark mass is given by the Gell-Mann--Oakes--Renner (GOR) relation:

"by construction", since one wants this term to mimic the QCD explicit breaking of chiral symmetry

 $\langle 0|h\sigma|0\rangle = \langle 0|(-m\bar{\psi}\psi)|0\rangle$

Connection not only between m_{π} and m_{q} , but also between the σ field condensate and the chiral condensate

 $m_{\pi}^{2} f_{\pi}^{2} = -\frac{m_{u} + m_{d}}{2} \left< 0 |\bar{u}u + \bar{d}d| 0 \right>$

- In a medium, one can use $\langle \sigma \rangle$ (T) in the effective model to describe the melting of the chiral condensate at high T.



Phase diagram and effective potential



[Scavenius et al. (2001)]

One example on relevance and difficulties in exploring the phase diagram:





and if there is time...





"Drawing" the phase diagram



One of the main (very tough!) goal of high-energy heavy ion collisions





Mapping (part of) the QCD phase diagram



Experimentalists do make miracles to extract clean info!

- finding good observables
- dealing with several sources of background
- each step towards the phase diagram is very hard
- need to talk to theorists! Dangerous, they know...





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LEP: e<sup>+</sup> + e<sup>-</sup> -> q qbar (≈200 GeV)
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Using all we can!



[Stephanov (2010)]

Many phase diagrams... A few examples:



In the critical region — large fluctuations expected!

$$\xi_{\infty} \sim t^{-\nu} \quad ; \quad t \equiv \frac{T - T_{\text{CEP}}}{T_{\text{CEP}}} \qquad \langle \sigma^n \rangle \sim \xi^{p_n} f_n(\xi/L)$$



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* Experimentalists can measure multiplicities that fluctuate event-by-event

 \star These fluctuations increase in magnitude near the critical point as a power of the correlation length (contribution of the order parameter)

$$\langle \sigma^n \rangle \sim \xi^{p_n} f_n(\xi/L)$$

 $\langle (\delta N)^3 \rangle \sim \xi^{4.5}, \qquad \langle (\delta N)^4 \rangle - 3 \langle (\delta N)^2 \rangle^2 \sim \xi^7$ [Stephanov (2009)]

★ Higher cumulants grow faster with ξ , BUT are harder to compute and much harder to measure (large background/signal!)

* Combinations of moments may help...

[Athanasiou, Rajagopal & Stephanov (2010)]

★ But there are spurious effects in real life, as experimentalists know better...

So, there is the background to be surpassed, there is critical slowing down, and...

• In heavy ion collisions the system size will depend on centrality:



• Measurements will generally probe *pseudocritical*, smoothened, shifted thermodynamic quantities. Ex. – cumulants:



- Most (≈all) signatures based on non-monotonic behavior of observables [e.g.: Stephanov (2009)].
- partially hidden by background. shifts and smoothening.

More details in the discussion sessions!!

A few remarks are in order:

- One of the ultimate goals of the heavy ion programs is mapping the phase diagram of strong interactions. Or, at least, finding clear fingerprints of its major features.
- It is amusing to see that a Google search (images) for something like "successful phase diagram mapping physics" produces lots of QCD phase diagrams, even though we only have cartoons...
- We can generously interpret this as our community being very active and/ or optimistic.
- On the other hand, several phase diagrams have been obtained in different realms of physics, experimentally and theoretically.

• However, we are still light-years away from something like:

FIG. 4. (Color online) Electronic phase diagram of 1T-TaSe_{2-x}Te_x as a function of temperature and Te content.

case of 1 T-TaTe₂. However, according to the experimentally obtained phase diagram of Fig. 4, one should notice

[Liu et al (2014)]

[Marcano et al (2013)]

• The problem for us is that we have a very small, short-lived, noisy, fastevolving system that is (very) indirectly probed in the experiments.

The phase diagram for QCD can be schematically divided, assuming it behaves roughly as a simplified cartoon of this sort (as suggested by several model descriptions):

Also assuming the experiment spans a large enough region, so that a CEP and a 1st-order line can be, in principle, probed.

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CEP region (near criticality):

- $(\xi)^{power}$ -dominated signatures
- background/noise -> spurious fluctuations
- finite size, finite lifetime, critical slowing down
- fast dynamics

1st-order transition region:

- finite size, finite lifetime
- bubble nucleation & spinodal decomposition
- two-peak structure
- structure formation (patterns)
- nonzero (conserved) baryon number
- fast dynamics

So

- 2 distinct regions, even if there is no clear boundary in practice
- 2 sets of problems, features, needed techniques, etc
- related sometimes, but different

Remark - direct comparison to lattice QCD can be dangerous:

- sign problem in this region (no benchmark EoS): we do not have the "correct" EoS!
- the actual systems are finite and come in different sizes (lattice results are extrapolated to the thermodynamic limit)
- the QGP formed is very noisy, fluctuates a lot, and is indirectly measured within a given acceptance
- dynamics is crucial (totally absent on the lattice)

Nevertheless: several statistical mechanics techniques successfully used in lattice simulations can be useful in analyzing the data! So, good luck! :-)

and if there is time...

Strong CP problem (a real fundamental problem!!)

The vacuum of QCD is topologically nontrivial!

Strong CP problem & HIC

 Topologically nontrivial configurations of the gauge fields allow for a CPviolating term in the Lagrangian of QCD

$$\mathcal{L}_{\theta} = -\frac{\theta}{32\pi^2} g^2 F^{\mu\nu a} \tilde{F}^a_{\mu\nu}$$

However, experiments indicate $\theta < 10^{-10}$.

- Spontaneous breaking of P and CP are forbidden in the true vacuum of QCD for θ =0 [Vafa & Witten (1984)]. However, this does not hold at finite temperature [Bronoff & Korthals Altes; Azcoiti & Galante; Cohen,...] and metastable states are allowed -> chance to probe the topological structure of QCD !
- <u>Metastable</u> P- and CP-odd <u>domains</u> could be produced in heavy ion collisions [Kharzeev, Pisarski & Tytgat (1998)]
- Signature? Mechanism based on the separation of charge -> the chiral magnetic effect [Kharzeev (2006); Kharzeev & Zhitnitsky (2007); Kharzeev, McLerran & Warringa (2008); Fukushima, Kharzeev & Warringa (2008)] under very strong magnetic fields in non-central collisions; sensitive experimental observable [Voloshin (2000,2004)]

[Leinweber]

From Kharzeev, QM 2009:

The existence of P and CP odd domains expected close to the deconfinement phase transition

DK, R. Pisarski, M. Tytgat,

Phys.Rev.Lett.81:512-515,1998

Thursday, April 2, 2009

 $P(Q_l)$

Diffusion of Chern-Simons number in QCD: real time lattice simulations

/327

Ncs=Jd4x g2 FF

DK, A.Krasnitz and R.Venugopalan, Phys.Lett.B545:298-306,2002

P.Arnold and G.Moore, Phys.Rev.D73:025006,2006

Time (tm)

200

300

100

High temperature and low density

high magnetic fields in <u>non-central</u> RHIC collisions

[Kharzeev, McLerran & Warringa (2008)]

 $eB \sim 10^4 - 10^5 MeV^2 \sim 10^{19} G$

[Voloshin, QM2009]

For comparison:

- "Magnetars": B $\sim 10^{14}$ - 10^{15} G at the surface, higher in the core [Duncan & Thompson (1992/1993)]
- Early universe (relevant for nucleosynthesis): B~ 10²⁴ G for the EWPT epoch [Grasso & Rubinstein (2001)]

Plus: mechanism based on separation of charge for the detection of the Chiral Magnetic Effect and P-odd effects [Voloshin (2000,2004), Kharzeev (2006); Kharzeev & Zhitnitsky (2007); Kharzeev, McLerran & Warringa (2008); Fukushima, Kharzeev & Warringa (2008)]

 $Q_w = \pm 1$

CP violation in heavy ion collisions

(no quarks)

• Rate of instanton transitions at zero temperature (tunneling) ['+ Hooft (1976)]:

$$\frac{dN_t^{\pm}}{d^3x dt d\rho} = 0.0015 \left(\frac{2\pi}{\alpha_s}\right)^6 e^{-2\pi/\alpha_s} \frac{1}{\rho^5}$$

• High T tends to decrease this rate [Pisarski & Yaffe (1980], but allows for sphaleron transitions (rate increases with T). For Yang-Mills [Moore et al. (1998); Bodeker et al. (2000)]:

$$\frac{dN_t^{\pm}}{d^3xdt} \sim 25.4 \ \alpha_w^5 T^4$$

• Estimate for QCD via N_c scaling [Kharzeev et al (2008)]:

$$\frac{dN_t^{\pm}}{d^3xdt} \sim 192.8 \ \alpha_s^5 T^4$$

• Due to the anomaly the Ward identities are modified, and the charges Q_L and Q_R obey the following relations (for $N_1=N_1$ at $t \rightarrow -\infty$):

$$(N_L - N_R)_{t \to \infty} = 2N_f Q_w$$
 $N_L - N_R = \int d^4 x \ (Q_L - Q_R) = -\int d^4 x \ Q_5$

so that fermions interacting with non-trivial gauge fields ($Q_w \neq 0$) have their chirality changed!

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Chiral magnetic effect

In <u>non-central</u> heavy ion collisions a <u>strong</u> magnetic field is generated in the orbital angular momentum direction (perpendicular to the reaction plane) <u>and</u> there can be regions with $Q_w \neq 0$ (inducing *sphaleron* transitions):

[Kharzeev, McLerran & Warringa (2008)]

- The strong B field restricts quarks (all in the lowest Landau level, aligned with B) to move along its direction
- Q_w =-1, e.g., converts L -> R: inversion of the direction of momentum
- Net current and charge difference created along the B direction

[Kharzeev, QM2009]

Magnetic QCD

Several theoretical/phenomenological questions arise:

How does the QCD phase diagram look like including a nonzero uniform B ? (another interesting "control parameter" ?)

Where are the possible metastable CP-odd states and how "stable" they are? What are their lifetimes ?

Are there modifications in the nature of the phase transitions ?

Are the relevant time scales for phase conversion affected ?

Are there other new phenomena (besides the chiral magnetic effect)?

What is affected in the plasma formed in heavy ion collisions ?

Which are the good observables to look at ? Can we investigate it experimentally ? Can we simulate it on the lattice ?

Besides...

Strong interactions under intense magnetic fields can be found, in principle, in a variety of systems:

High density and low temperature

"Magnetars": B $\sim 10^{14}$ – 10^{15} G at the surface, much higher in the core [Duncan & Thompson (1992/1993)]

Stable stacks of π^0 domain walls or axial scalars (η , η') domain walls in nuclear matter: B ~ 10¹⁷-10¹⁹ G [Son & Stephanov (2008)

High magnetic fields in heavy-ion collisions have been computed...

• Fields very flat in the central region (system may be deconfined/chiral)

 semi-analytic estimates & UrQMD agree well

[Skokov, Illariunov & Toneev (2009)]

- HIJING computation
- RHIC vs LHC energies

- Huge fields for ultraperipheral collisions due to event-by-event fluctuations
- Possible vacuum SUC via ρ meson condensation [Chernodub (2010)]
- Possible building of spincharge correlation for quarks

[Deng & Huang (2012)]

Comparison of magnetic fields

The Earths magnetic field	0.6 Gauss	
A common, hand-held magnet	100 Gauss	
The strongest steady magnetic fields achieved so far in the laboratory	4.5 x 10⁵ Gauss	
The strongest man-made fields ever achieved, if only briefly	10 ⁷ Gauss	
Typical surface, polar magnetic fields of radio pulsars	10 ¹³ Gauss	
Surface field of Magnetars	10 ¹⁵ Gauss	
http://solomon.as.utexas.edu/~duncan/magnetar.htm		
Hanvy ion colligions, the strongest ma		

Heavy ion collisions: the strongest magnetic field ever achieved in the laboratory Off central Gold-Gold Collisions at 100 GeV per nucleon $eB(\tau=0.2 \text{ fm}) = 10^3 \sim 10^4 \text{ MeV}^2 \sim 10^{17} \text{ Gauss}$

<u>Strong motivation:</u> in-medium strong interactions under extreme magnetic fields are:

of experimental relevance
HICs, early universe, magnetars

rich in new phenomenology
Chiral magnetic effect, new QCD phase diagram, vacuum SUC

amenable to lattice simulations: new open channel for comparison!

 \diamond model constraining, tests for pQCD and nonpert. methods, ...

Incorporating a magnetic background in loop integrals

Let us assume the system is in the presence of a strong magnetic field background that is constant and homogeneous:

choice of gauge $A^{\mu}=(A^0,\vec{A})=(0,-By,0,0)$

• charged mesons (new dispersion relation):

 $\vec{B} = B\hat{z}$

$$p_{0n}^2 = p_z^2 + m^2 + (2n+1)|q|B$$

• quarks (new dispersion relation):

$$\begin{bmatrix} i\gamma^{\mu}\partial_{\mu} - m)\psi = 0\\ \partial_{\mu} \to \partial_{\mu} + iqA_{\mu} \end{bmatrix} \longrightarrow \begin{bmatrix} u''(y) + 2m \left[\left(\frac{p_0^2 - p_z^2 - m^2 + qB\sigma}{2m} \right) - \frac{q^2B^2}{2m} \left(y + \frac{p_x}{qB} \right)^2 \right] u(y) = 0 \\ \end{bmatrix}$$

$$p_0^2 = p^2 + m^2 + (2n + 1 - \sigma)|q|B \qquad \sigma = \pm 1$$

$$p_{0n}^2 = p_z^2 + m^2 + (2n+1-\sigma)|q|B$$

• integration measure:

T > 0:

$$\frac{d^4k}{(2\pi)^4} \mapsto \frac{|q|B}{2\pi} \sum_{n=0}^{\infty} \int \frac{dk_0}{2\pi} \frac{dk_z}{2\pi}$$

$$T\sum_{\ell} \int \frac{d^3k}{(2\pi)^3} \mapsto \frac{|q|BT}{2\pi} \sum_{\ell} \sum_{n=0}^{\infty} \int \frac{dk_z}{2\pi}$$

l: Matsubara index n: Landau level index

From the lattice:

[Bali et al (2012)]

A result that is not obtained in the majority of models!

The field is wide open yet ...

More details in the discussion sessions!!

Instead of conclusions... just a final comment

To make progress in understanding (or at least in collecting facts about) (de)confinement and chiral symmetry, we need it all:

- Experiments and observations
- Lattice simulations
- Theory developments
- Effective models

And also combinations whenever possible.

It is crucial to have theorists and experimentalists working and discussing together!

A last piece of advice: don't trust theorists that much...