

# Current experimental status of $\Delta\Gamma$ and $\Delta m$

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on behalf of the LHCb collaboration

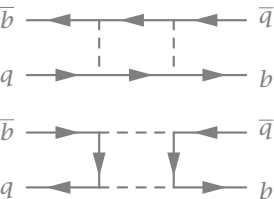
University of Glasgow

September 18th, 2018

- $B_{d/s}^0$  mixing,  $\Delta m_{d/s}$  and  $\Delta\Gamma_{d/s}$
- measuring  $\Delta m_{d/s}$
- measuring  $\Delta\Gamma_{d/s}$
- conclusions



# $B_{d/s}^0$ mixing



■ mixing goes through box diagrams

$$\blacksquare \Delta m_q \sim m_W^2 m_{B_q} \hat{\mathcal{B}}_q f_{B_q}^2 (V_{tq}^* V_{tb})^2 \quad q = d, s$$

$$\blacksquare \Delta \Gamma_q \sim m_b^2 m_{B_q} \hat{\mathcal{B}}_q f_{B_q}^2 \left( (V_{tq}^* V_{tb})^2 + V_{tq}^* V_{tb} V_{cq}^* V_{cb} \mathcal{O}(m_c^2/m_b^2) + (V_{cq}^* V_{cb})^2 \mathcal{O}(m_c^4/m_b^4) \right)$$

■ current WA: [HFLAV 2018]

$$\blacksquare \Delta m_d = (0.5064 \pm 0.0019) \text{ ps}^{-1}$$

$$\blacksquare \Delta \Gamma_d / \Gamma_d = (-0.2 \pm 1.0) \cdot 10^{-2}$$

$$\blacksquare \Delta m_s = (17.757 \pm 0.021) \text{ ps}^{-1}$$

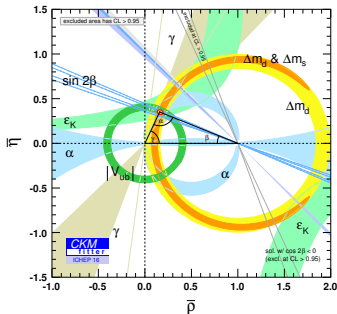
$$\blacksquare \Delta \Gamma_s / \Gamma_s = (0.132 \pm 0.008)$$

■ constrain apex of unitarity triangle:

$$\frac{\Delta m_s}{\Delta m_d} = \frac{m_{B_s}}{m_{B_d}} \xi^2 \left| \frac{V_{ts}}{V_{td}} \right|^2$$

■ get  $\xi^2 = \frac{\hat{\mathcal{B}}_s f_{B_s}^2}{\hat{\mathcal{B}}_d f_{B_d}^2}$  from lattice QCD

$$\blacksquare |V_{td}/V_{ts}| = 0.2053 \pm 0.0004(\text{exp}) \pm 0.0029(\text{lattice}) \quad [\text{PDG2018}]$$



# measuring $\Delta m_q$



# measuring $\Delta m_{d/s}$

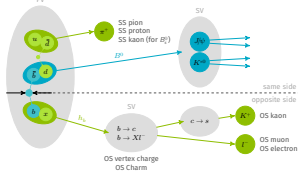
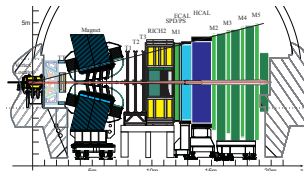
- best precision from time dependent mixing analysis in flavour specific decays

- $A_{mix}^{th} = \frac{\Gamma_{B_q^0 \rightarrow \bar{f}}(t) - \Gamma_{B_q^0 \rightarrow f}(t)}{\Gamma_{B_q^0 \rightarrow \bar{f}}(t) + \Gamma_{B_q^0 \rightarrow f}(t)} \sim \cos(\Delta m_q t)$

- experimental factors affecting significance:

- signal yield:  $\sqrt{N/2} f_{sig}$

- large  $b\bar{b}$  x-section, large data sample (so far,  $\sim 5.5 \text{ fb}^{-1}$  in run 2)
    - efficient trigger, reconstruction, excellent momentum and vertex resolution
    - excellent particle identification



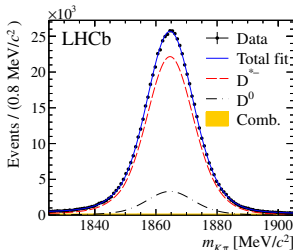
- diluted through time resolution:  $e^{-(\Delta m_q \sigma_t)^2/2}$  ( $\sigma_t \sim 45 - 55 \text{ fs}$ )

- diluted through flavour tagging:  $\sqrt{\epsilon_{tag}(1-2\omega)^2} \sim (3 \dots 6)\%$

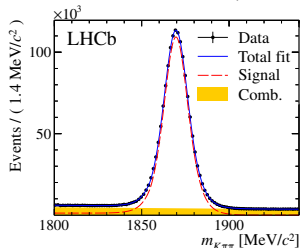
- opposite side:  $e, \mu, K, \text{Vertex, charm}$
    - same side:  $\pi, p, K$

# measuring $\Delta m_d$ at LHCb

- from semileptonic  $B \rightarrow D^{(*)-} \mu^+ \nu_\mu X$  decays
- large BR  $\sim 2 - 5\%$
- reconstruct  $D^{*-} \rightarrow \overline{D^0}(K^+ \pi^-) \pi^-$  and  $D^- \rightarrow K^+ \pi^- \pi^-$
- $D^{(*)-} \mu^+$  form common vertex, missing  $\nu_\mu$ 
  - cannot apply mass/kinematic cuts on  $B_d$ , only on  $D^0, D^{*-}, D^-$
- veto mis-ID  $J/\psi, \Lambda_c$
- BGs:  $D^0$  from  $B, B^+ \rightarrow D^{(*)-} \mu^+ \pi^+ \nu_\mu$ , combinatorial



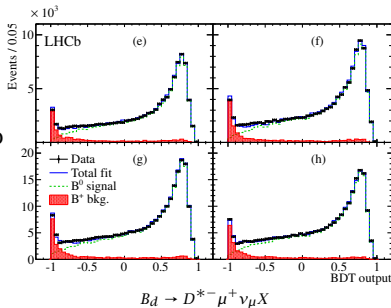
$\sim 0.8$  M  $B_d \rightarrow D^{*-} \mu^+ \nu_\mu X$



$\sim 1.4$  M  $B_d \rightarrow D^- \mu^+ \nu_\mu X$

# measuring $\Delta m_d$ at LHCb

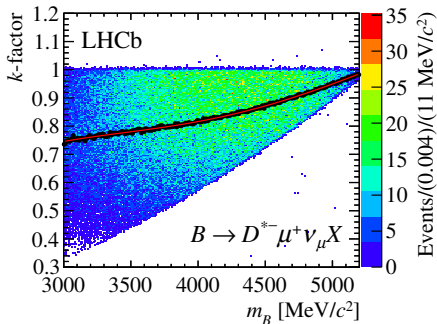
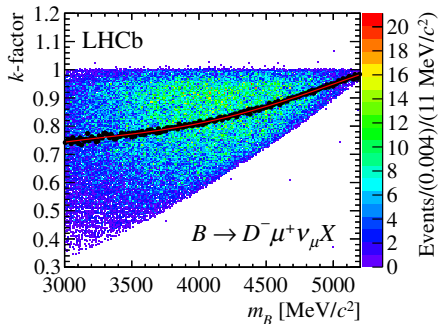
- physics BG:  $B^+ \rightarrow D^{(*)-} \mu^+ \pi^+ \nu_\mu$ 
  - expected at  $\sim 10\%$  level, but BR is only known with a precision of 10%
  - fraction of BG correlated with fitted value for  $\Delta m_d$
  - model correctly, reduce BG for low systematic uncertainty
- train MVA classifier to discriminate this BG from signal
  - train on MC, in 4 separate tagging categories
  - inputs:
    - geometrical and kinematic info on  $D^{(*)-} \mu$  system
    - isolation of tracks in cone around it
- use to suppress this BG by 70%
- use to evaluate remaining fraction ( $3\%(D^{*-} \mu \nu_\mu X)/6\%(D^- \mu \nu_\mu X)$ ) on data



[Eur. Phys. J. C(2016) 76:412]

# measuring $\Delta m_d$ at LHCb

- further complication:  $\nu_\mu$  escapes,  $X$  not reconstructed
  - need to correct measured decay time:  $t = \frac{M_{B_d} L}{p_{D^{(*)}\mu} c / k(m_B)}$
  - with:  $k(m_B) = \langle p_{D^{(*)}\mu} / p_{B_d}^{true} \rangle$
- decay time is smeared, only average correction known





# measuring $\Delta m_d$ at LHCb

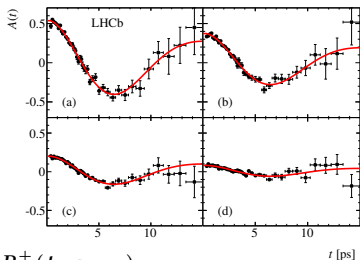
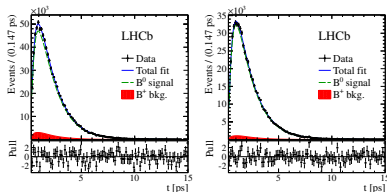
- $q_{mix} = \pm 1$ : mixed/unmixed from  $\mu$  charge and flavour tagging decision
  - 4 categories in mistag  $\omega$  to gain sensitivity
  - tagging power  $\epsilon(1 - 2\omega)^2 \sim 2.3 - 2.6\%$

- fit  $m_{D^-}$  and  $m_{D^0}/\delta_m = m_{D^*} - m_{D^0}$  distributions
- use to extract sWeights for signal +  $B^+$  (subtracts combinatorial +  $D^0$  from  $B$ ):

$$P(t, q_{mix}) = (1 - f_{B^+})S(t, q_{mix}) + f_{B^+}B^+(t, q_{mix})$$

$$S(t, q_{mix}) = a(t) \left( e^{-t/\tau} (1 + q_{mix}(1 - 2\omega) \cos(\Delta m_d t)) \right) \otimes R(t) \otimes F(k)$$

- from data: acceptance  $a(t)$ ,  $f_{B^+}$ ,  $\omega$
- from simulation: resolution  $R(t)$ , correction  $F(k)$



[Eur. Phys. J. C(2016) 76:412]

 $B_d \rightarrow D^- \mu^+ \nu_\mu X$

measuring  $\Delta m_d$  at LHCb

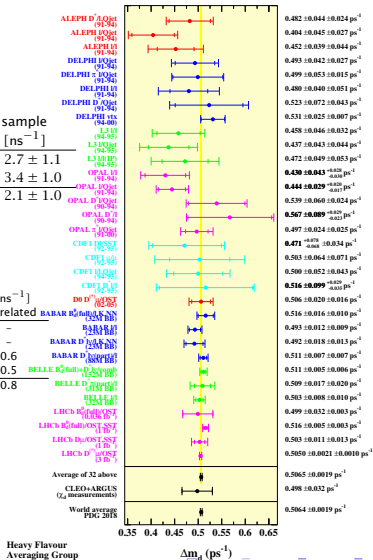
- result: [Eur. Phys. J. C(2016) 76:412]

Mode	2011 sample $\Delta m_d$ [ns <sup>-1</sup> ]	2012 sample $\Delta m_d$ [ns <sup>-1</sup> ]	Total sample $\Delta m_d$ [ns <sup>-1</sup> ]
$B_d \rightarrow D^- \mu^+ \nu_\mu X$	$506.2 \pm 5.1$	$505.2 \pm 3.1$	$505.5 \pm 2.7 \pm 1.1$
$B_d \rightarrow D^{*-} \mu^+ \nu_\mu X$	$497.5 \pm 6.1$	$508.3 \pm 4.0$	$504.4 \pm 3.4 \pm 1.0$
combination			$505.0 \pm 2.1 \pm 1.0$

- systematic uncertainties:

Source of uncertainty	$B_d \rightarrow D^- \mu^+ \nu_\mu X$ [ns <sup>-1</sup> ]		$B_d \rightarrow D^{*-} \mu^+ \nu_\mu X$ [ns <sup>-1</sup> ]	
	Uncorrelated	Correlated	Uncorrelated	Correlated
$B^+$ background	0.4	0.1	0.4	-
Other backgrounds	-	0.5	-	-
$k$ -factor distribution	0.4	0.5	0.3	0.6
Other fit-related	0.5	0.4	0.3	0.5
Total	0.8	0.8	0.6	0.8

- most precise measurement, dominates WA



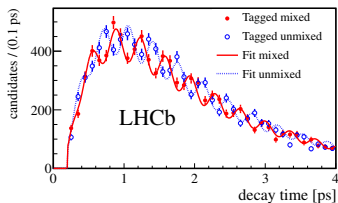
# measuring $\Delta m_s$ at LHCb

- decay rates for  $B_H$  and  $B_L$  to final state  $f$  can be different, so

$$\Gamma_{B_q \rightarrow f}(t) = e^{-\Gamma_q t} \left( \cosh(\Delta\Gamma_q t/2) + A_{\Delta\Gamma}^f \sinh(\Delta\Gamma t/2) + A_{CP}^{dir,f} \cos(\Delta m_q t) + A_{CP}^{mix,f} \sin(\Delta m_q t) \right)$$

$$\Gamma_{B_q \rightarrow f}(t) = e^{-\Gamma_q t} \left( \cosh(\Delta\Gamma_q t/2) + A_{\Delta\Gamma}^f \sinh(\Delta\Gamma t/2) - A_{CP}^{dir,f} \cos(\Delta m_q t) - A_{CP}^{mix,f} \sin(\Delta m_q t) \right)$$

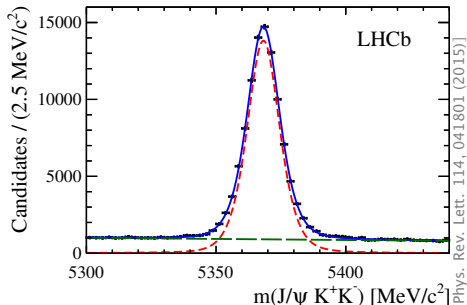
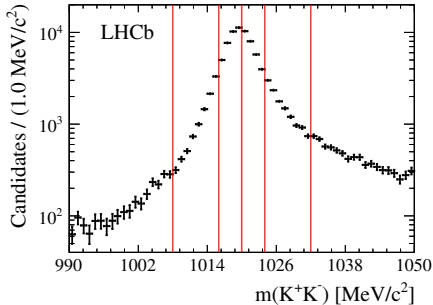
- time-dependent analyses of  $B_q^0$  decays give access to
  - $\Delta m_q$
  - sometimes also  $\Delta\Gamma_q$  (we'll see in a bit...)
- often a flavour-specific channel like  $B_s \rightarrow D_s \pi$  will give the best results
- will look into  $B_s \rightarrow J/\psi K^+ K^-$ , since it's newer...



$\Delta m_s$  from  $B_s^0 \rightarrow D_s \pi$

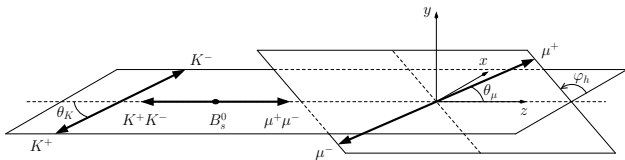
# measuring $\Delta m_s$ at LHCb

- do a time-dependent analysis of  $B_s \rightarrow J/\psi K^+ K^-$ :
  - usually people do this to learn about mixing phase  $\phi_s$
  - complicated angular analysis
- corresponding to a data set of  $3 \text{ fb}^{-1}$
- $> 95\text{k}$   $B_s \rightarrow J/\psi K^+ K^-$  candidates, very clean
- main BG: combinatorial,  $K/\pi$  mis-ID, subtracted using sWeights
- flavour tagging: opposite side + same side Kaon,  $\epsilon(1 - 2\omega)^2 = (3.73 \pm 0.15)\%$



# measuring $\Delta m_s$ at LHCb

- final state  $J/\psi K^+ K^-$  is mixture of CP eigenstates
  - depends on relative angular momentum of  $J/\psi$  and  $K^+ K^-$ -system
  - to learn about  $\phi_s$ , need to disentangle CP-even and CP-odd component (for details, see talks by [Maria](#), [Varvara](#), [Pavel](#))
- analyse decay rate as function of helicity angles  $\cos(\theta_K), \cos(\theta_\mu), \phi_h$

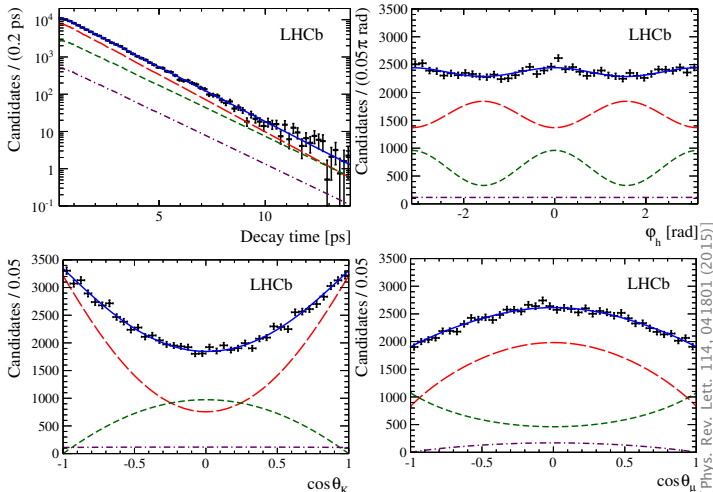


[Phys. Rev. D 87, 112010 (2013)]

- forward geometry of LHCb cuts into these angles
- model 3D angle-dependent efficiency using simulation
- helps to disentangle  $B_{S,H}$  and  $B_{S,L}$

# measuring $\Delta m_s$ at LHCb

- simultaneous fit in decay time and angular analysis
- long- and short-lived component separated thanks to different angular dependence!



measuring  $\Delta m_s$  at LHCb

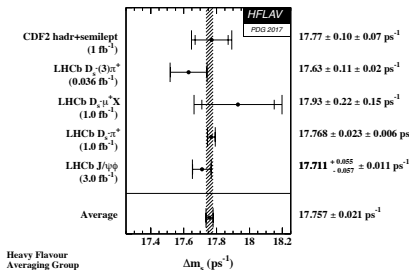
Parameter	Value
$\Gamma_s$ [ $\text{ps}^{-1}$ ]	$0.6603 \pm 0.0027 \pm 0.0015$
$\Delta\Gamma_s$ [ $\text{ps}^{-1}$ ]	$0.0805 \pm 0.0091 \pm 0.0032$
$ A_\perp ^2$	$0.2504 \pm 0.0049 \pm 0.0036$
$ A_0 ^2$	$0.5241 \pm 0.0034 \pm 0.0067$
$\delta$ [rad]	$3.26^{+0.10}_{-0.17} \pm 0.06$
$\delta_\perp$ [rad]	$3.08^{+0.14}_{-0.15} \pm 0.06$
$\phi_s$ [rad]	$-0.058 \pm 0.049 \pm 0.006$
$ \lambda $	$0.964 \pm 0.019 \pm 0.007$
$\Delta m_s$ [ $\text{ps}^{-1}$ ]	$17.711^{+0.055}_{-0.057} \pm 0.011$

[Phys. Rev. Lett. 114, 041801 (2015)]

- hugely complex fix, but gives access to

- $\Delta m_s$
- $\Gamma_s, \Delta\Gamma_s$
- mixing phase  $\phi_s$
- amplitudes and phases of different angular components

- LHCb measurements in  $B_s^0 \rightarrow D_s \pi$  and  $B_s^0 \rightarrow J/\psi K^+ K^-$  dominate the WA



[Eur. Phys. J. C 77 (2017) 895]

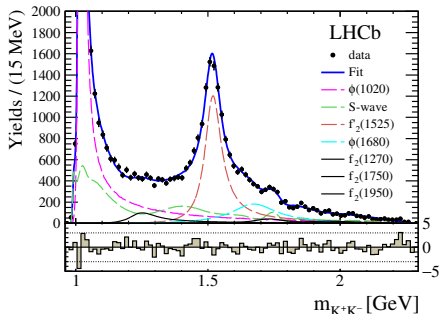


# measuring $\Delta\Gamma_q$



# measuring $\Delta\Gamma_s$ at LHCb

- have already seen  $B_s \rightarrow J/\psi K^+ K^-$  with  $K^+ K^-$  in the  $\phi(1020)$  region [Phys. Rev. Lett. 114, 041801 (2015)]
- similar example: use higher  $K^+ K^-$  invariant masses: [JHEP 08 (2017) 037]
  - also uses  $3 \text{ fb}^{-1}$
  - similar to analysis with  $K^+ K^-$  in the  $\phi$  region
  - more than 33k candidates with  $m_{KK} > 1.05 \text{ GeV}$



- can combine both:

$$\phi_s = -25 \pm 45 \pm 8 \text{ mrad} \quad \Gamma_s = 0.6588 \pm 0.0022 \pm 0.0015 \text{ ps}^{-1}$$

$$|\lambda| = 0.978 \pm 0.013 \pm 0.003 \quad \Delta\Gamma_s = 0.0813 \pm 0.0073 \pm 0.0036 \text{ ps}^{-1}$$

$$\phi_s = 119 \pm 107 \pm 34 \text{ mrad},$$

$$|\lambda| = 0.994 \pm 0.018 \pm 0.006,$$

$$\Gamma_s = 0.650 \pm 0.006 \pm 0.004 \text{ ps}^{-1},$$

$$\Delta\Gamma_s = 0.066 \pm 0.018 \pm 0.010 \text{ ps}^{-1}$$



# measuring $\Delta\Gamma_q$

- have already seen how to get  $\Delta\Gamma_q$  from time-dependent mixing analyses

- other method: **effective lifetime** depends on  $y_q = 2\Delta\Gamma_q/\Gamma_q$ :

$$\tau_{B_q \rightarrow f}^{eff} = \frac{1}{\Gamma_q} \frac{1}{1-y_q^2} \frac{1+2A_{\Delta\Gamma}^f y_q + y_q^2}{1+A_{\Delta\Gamma}^f y_q}$$

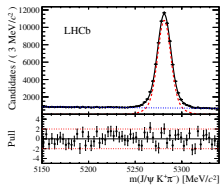
- can use different decay channels (different  $A_{\Delta\Gamma}^f$ ) (e.g. [JHEP04(2014)114])

- $B^0 \rightarrow J/\psi K^{*0}$  ( $A_{\Delta\Gamma}^f = 0$ )
- $B^0 \rightarrow J/\psi K_S^0$  ( $A_{\Delta\Gamma}^f = \cos(2\beta)$ )

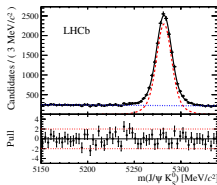
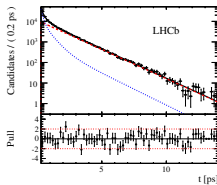
- can use measurements of  $\Delta\Gamma_q$  for many things on the theory side
  - e.g. to derive bounds on quark-hadron duality, to mention a recent example [arXiv:1603.07770v2]

# measuring $\Delta\Gamma_d$ at LHCb

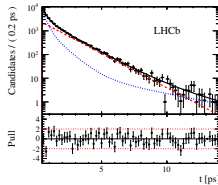
- idea is to measure effective lifetimes of e.g.
  - $B^0 \rightarrow J/\psi K^{*0}$
  - $B^0 \rightarrow J/\psi K_S^0$
- trigger on  $\mu$ ,  $3 \text{ fb}^{-1}$  data sample
- minimise decay time biasing selection criteria
- fully reconstruct decay, model efficiencies with MC and control channels
- fit time and invariant mass



$\sim 71k B^0 \rightarrow J/\psi K^{*0}$



$\sim 17k B^0 \rightarrow J/\psi K_S^0$

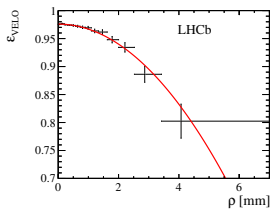


[JHEP04(2014)114]

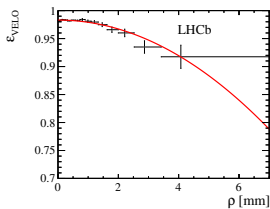


# measuring $\Delta\Gamma_d$ at LHCb

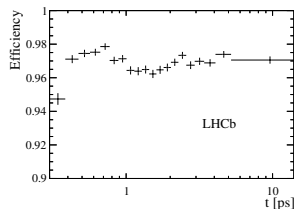
- of course, (effective) lifetime measurements require precise control of efficiency as function of decay time (and flight distance)
- two main contributions:
  - VELO reconstruction efficiency as one moves away from beamline radially ( $\rho$ )
  - combined trigger and selection efficiency as a function of time



online reco



offline reco



combined trigger + selection eff.

[JHEP04(2014)114]



# measuring $\Delta\Gamma_d$ at LHCb

## ■ results: [JHEP04(2014)114]

$$\tau_{B^0 \rightarrow J/\psi K^*} = 1.524 \pm 0.006 \pm 0.004 \text{ ps}$$

$$\tau_{B^0 \rightarrow J/\psi K_S^0} = 1.499 \pm 0.013 \pm 0.005 \text{ ps}$$

## ■ use $\tau_{B_q \rightarrow f}^{eff} = \frac{1}{\Gamma_q} \frac{1}{1-\gamma_q^2} \frac{1+2A_{\Delta\Gamma}^f \gamma_q + \gamma_q^2}{1+A_{\Delta\Gamma}^f \gamma_q}$

### ■ $A_{\Delta\Gamma}^f = 0$ for flavour specific decays

### ■ $A_{\Delta\Gamma}^f = \cos(2\beta)$ for $B^0 \rightarrow J/\psi K_S^0$

## ■ combine from these results:

$$\Gamma_d = 0.656 \pm 0.003 \pm 0.002 \text{ ps}^{-1}$$

$$\Delta\Gamma_d = -0.029 \pm 0.016 \pm 0.007 \text{ ps}^{-1}$$

$$\frac{\Delta\Gamma_d}{\Gamma_d} = -0.044 \pm 0.025 \pm 0.011$$

Source	$\tau_{B^+}/\tau_{B^0}$	$\tau_{B_s^0}/\tau_{B^0}$	$\tau_{\Lambda_b}/\tau_{B^0}$	$\tau_{B^+}/\tau_{B^-}$	$\tau_{\Lambda_b}/\tau_{\Lambda_b^-}$	$\tau_{B^0}/\tau_{\bar{B}^0}$	$\Delta\Gamma_d/\Gamma_d$
Statistical uncertainty	5.0	8.5	18.0	4.0	35.0	8.0	25.0
VELO reconstruction	1.6	1.7	1.1	-	-	-	4.1
Simulation sample size	2.0	2.2	2.8	2.1	5.3	3.0	6.3
Mass-time correlation	1.6	1.2	2.3	-	-	-	4.7
Trigger and selection eff.	1.1	1.8	1.5	-	-	-	4.0
Background modelling	0.3	0.1	1.5	0.2	3.0	1.4	3.8
Mass modelling	0.2	0.4	0.2	0.1	0.2	0.2	0.8
Peaking background	-	0.3	0.7	-	-	-	0.5
Effective lifetime bias	-	1.0	-	-	-	-	-
$B^0$ production asym.	-	-	-	-	-	8.5	1.9
Total systematic	3.2	3.7	4.4	2.1	6.1	9.1	10.7

## ■ ATLAS has a decay-length dependent analysis with $\sim 139\text{k } B^0 \rightarrow J/\psi K_S^0$ and $\sim 685\text{k } B^0 \rightarrow J/\psi K^{*0}$ , yielding $\Delta\Gamma_d/\Gamma_d = -0.001 \pm 0.011 \pm 0.009$

[JHEP06 (2016) 081]

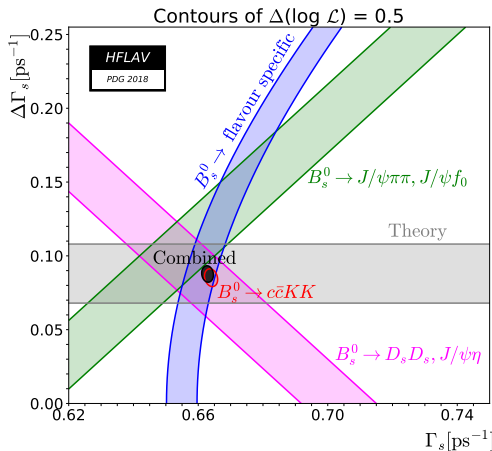
# conclusion

- LHCb measurements of  $\Delta m_d$ ,  $\Delta m_s$  still dominate WA
  - experimental status similar to that of last CKM
  - help constrain CKM matrix → **important test of SM**
  - more and more of run 2 data is analysed
  - new results are being produced
  - **stay tuned for more!**
- also some progress on  $\Delta\Gamma_s$  in the last year or so
  - **also stay tuned for more!**
- theory limits current precision of  $|V_{ts}|$  and  $|V_{td}|$ 
  - looking forward for the lattice to become even better

# backup



# $\Gamma_s$ versus $\Delta\Gamma_s$



[Eur. Phys. J. C77 (2017) 895]

- $B_s^0 \rightarrow D\mu X$  [Phys. Rev. Lett. 119, 101801 (2017)]
- $B_s^0 \rightarrow D_s\pi$  [Phys. Rev. Lett. 113, 172001 (2014)]
- $B_s^0 \rightarrow J/\psi f_0$  [Phys. Rev. Lett. 109, 152002 (2012)]
- $B_s^0 \rightarrow J/\psi\phi$  [Phys. Rev. Lett. 114, 041801 (2015)]
- $B_s^0 \rightarrow J/\psi KK$  [JHEP 08 (2017) 037]
- $B_s^0 \rightarrow \psi(2S)\phi$  [PLB 762 (2016) 253]
- $B_s^0 \rightarrow J/\psi\eta$  [Physics Letters B 762C (2016) pp. 484-492]
- $B_s^0 \rightarrow D_s D_s$  [Phys. Rev. Lett. 112, 111802 (2014)]

- many lifetime measurements in  $B_s^0$  sector by LHCb, pinning down  $\Gamma_s$  and  $\Delta\Gamma_s$
- excellent laboratory to test quantitative understanding of  $\Delta\Gamma_s$  from first principles