

ΔM_s interplay with B-anomalies

10th International Workshop on the CKM
Unitarity Triangle - 18.09.2018

Luca Di Luzio



In collaboration with Matthew Kirk and Alexander Lenz
arXiv:1712.06572 + work in progress

Outline

1. ΔM_s in the SM [theoretical uncertainties]

- Hadronic Matrix Element
- V_{cb} dependence

2. Impact on B-anomalies

- Neutral currents [Z' , LQ]
- Model building directions

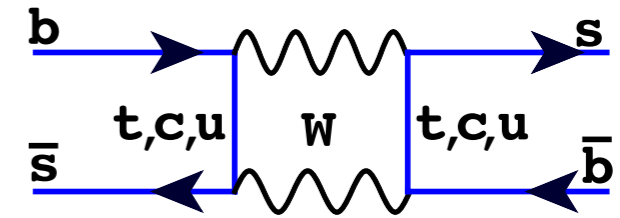
Part-I

ΔM_s in the SM

SM prediction [ingredients]

- $\Delta M_s \equiv M_H^s - M_L^s = 2 |M_{12}^s|$

[For a review see Lenz, Nierste hep-ph/0612167
Artuso, Borissov, Lenz 1511.09466]

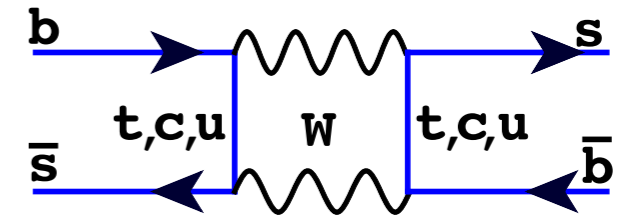


$$M_{12}^s = \frac{G_F^2}{12\pi^2} \lambda_t^2 M_W^2 S_0(x_t) B f_{B_s}^2 M_{B_s} \hat{\eta}_B$$

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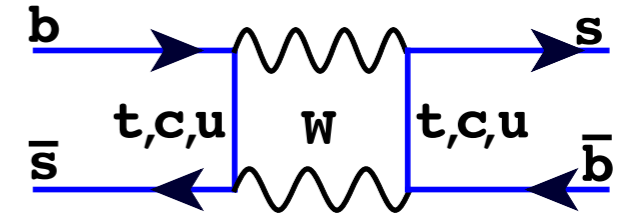
★ Inami-Lim function $S_0(x_t = \bar{m}_t^2(\bar{m}_t)/M_W^2) \approx 2.368$

[Inami, Lim PTR65 (1981)]

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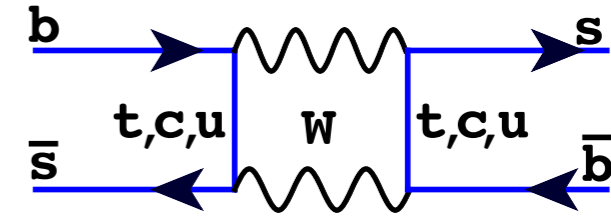
★ Perturbative NLO QCD corrections $\hat{\eta}_B \approx 0.8379$

[Buras, Jamin, Weisz NPB347 (1990)]

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$$M_{12}^s = \frac{G_F^2}{12\pi^2} \lambda_t^2 M_W^2 S_0(x_t) \underbrace{B f_{B_s}^2}_{\text{Hadronic matrix element}} M_{B_s} \hat{\eta}_B$$

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★ **Hadronic matrix element** (Lattice / HQET Sum Rules)

[See talks by
Andreas Kronfeld, Aida El-Khadra,
Thomas Mannel, Thomas Rauh]

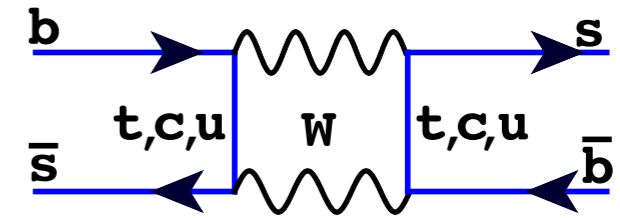
$$\langle B_s^0 | Q | \bar{B}_s^0 \rangle = \frac{8}{3} M_{B_s}^2 f_{B_s}^2 B(\mu) \quad Q = [\bar{s} \gamma_\mu (1 - \gamma_5) b] [\bar{s} \gamma^\mu (1 - \gamma_5) b]$$

$$\hat{\eta}_B B \equiv \eta_B \hat{B} \quad (\text{Bhat renormalization scale and scheme independent})$$

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★ Hadronic matrix element (Lattice / HQET Sum Rules)

★ CKM elements

$$\lambda_t \equiv V_{ts}^* V_{tb} \quad \leftarrow \quad V_{us} \quad V_{cb} \quad |V_{ub}/V_{cb}| \quad \gamma_{\text{CKM}}$$

in terms of 4 inputs, assuming CKM unitarity
(not necessarily true in presence of NP)

Hadronic matrix element [Lattice]

[November 2017 web-update of Flavour Lattice Averaging Group (FLAG) | 1607.00299]

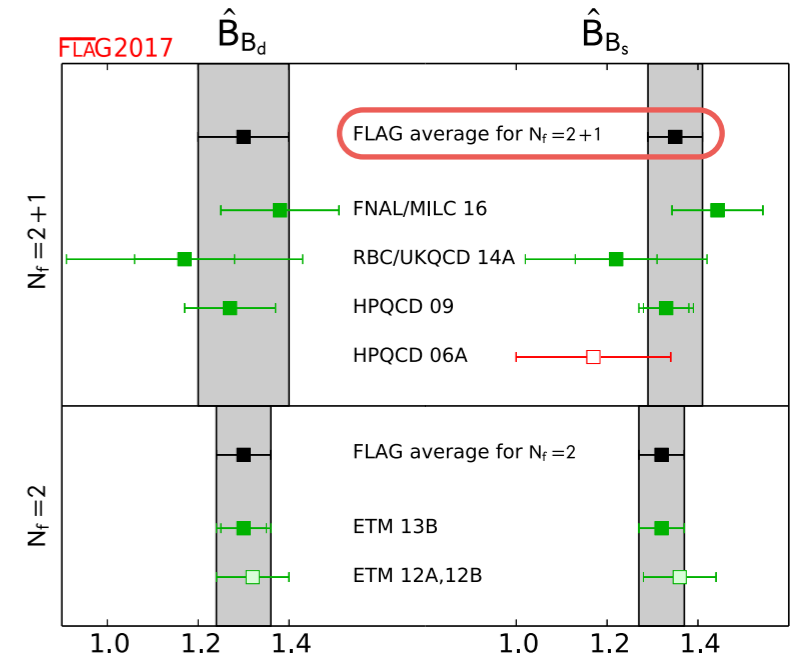
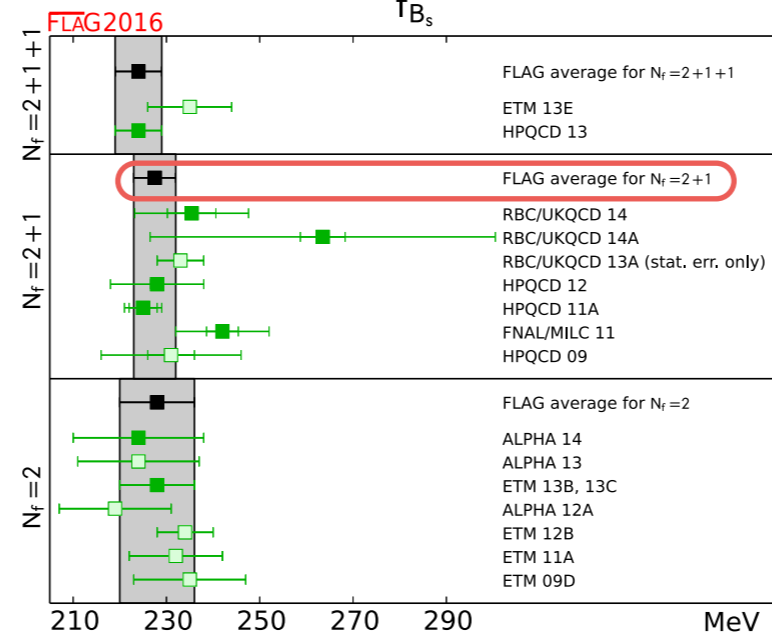
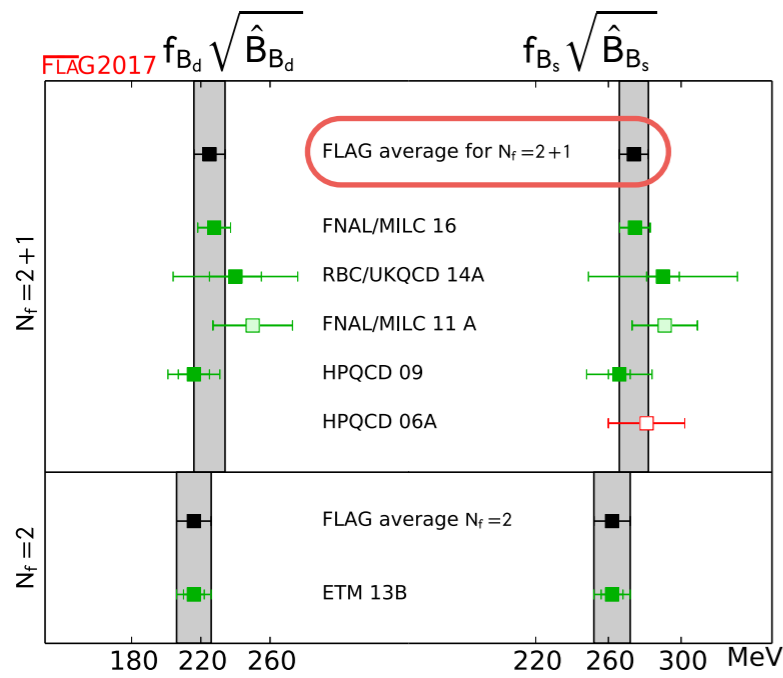
S. Aoki et al., *Review of lattice results concerning low-energy particle physics*, 1607.00299

Collaboration	Ref.	N_f	publication status	continuum extrapolation	chiral extrapolation	finite volume	renormalization/matching	heavy-quark treatment	$f_{B_d} \sqrt{\hat{B}_{B_d}}$	$f_{B_s} \sqrt{\hat{B}_{B_s}}$	\hat{B}_{B_d}	\hat{B}_{B_s}
FNAL/MILC 16	[57]	2+1	A	★	○	★	○	✓	227.7(9.5)	274.6(8.4)	1.38(12)(6) [⊙]	1.443(88)(48) [⊙]
RBC/UKQCD 14A	[15]	2+1	A	○	○	○	○	✓	240(15)(33)	290(09)(40)	1.17(11)(24)	1.22(06)(19)
FNAL/MILC 11A	[56]	2+1	C	★	○	★	○	✓	250(23) [†]	291(18) [†]	–	–
HPQCD 09	[19]	2+1	A	○	○	▽	○	○	216(15) [*]	266(18) [*]	1.27(10) [*]	1.33(6) [*]
HPQCD 06A	[58]	2+1	A	■	■	★	○	✓	–	281(21)	–	1.17(17)
ETM 13B	[9]	2	A	★	○	○	★	✓	216(6)(8)	262(6)(8)	1.30(5)(3)	1.32(5)(2)
ETM 12A, 12B	[24, 59]	2	C	★	○	○	★	✓	–	–	1.32(8) [◇]	1.36(8) [◇]

[⊙] PDG averages of decay constant f_{B^0} and f_{B_s} [2] are used to obtain these values.

Hadronic matrix element [Lattice]

[November 2017 web-update of Flavour Lattice Averaging Group (FLAG) | 607.00299]



$$\left(f_{B_s} \sqrt{\hat{B}_{B_s}} \right)^{\text{FLAG17}} = 274(8) \text{ MeV}$$

$$\left(f_{B_s} \right)^{\text{FLAG16}} \left(\sqrt{\hat{B}_{B_s}} \right)^{\text{FLAG17}} = 265(10) \text{ MeV}^*$$

*Naive combination (does not include updated FNAL/MILC calculation of decay constant)

Hadronic matrix element [Lattice]

- FLAG17 + V_{cb} treatment (see next slide) implies a **1.8 σ discrepancy**

$$\Delta M_s^{\text{SM}} > \Delta M_s^{\text{exp}} = (17.757 \pm 0.021) \text{ ps}^{-1} \quad [\text{HFLAV (CDF + LHCb) 16|2.07233}]$$

Source	$f_{B_s} \sqrt{\hat{B}}$	ΔM_s^{SM}
HPQCD14 [132]	$(247 \pm 12) \text{ MeV}$	$(16.2 \pm 1.7) \text{ ps}^{-1}$
ETMC13 [133]	$(262 \pm 10) \text{ MeV}$	$(18.3 \pm 1.5) \text{ ps}^{-1}$
HPQCD09 [134] = FLAG13 [135]	$(266 \pm 18) \text{ MeV}$	$(18.9 \pm 2.6) \text{ ps}^{-1}$
FLAG17 [70]	$(274 \pm 8) \text{ MeV}$	$(20.01 \pm 1.25) \text{ ps}^{-1}$
Fermilab16 [72]	$(274.6 \pm 8.8) \text{ MeV}$	$(20.1 \pm 1.5) \text{ ps}^{-1}$
HQET-SR [77, 136]	$(278_{-24}^{+28}) \text{ MeV}$	$(20.6_{-3.4}^{+4.4}) \text{ ps}^{-1}$
HPQCD06 [137]	$(281 \pm 20) \text{ MeV}$	$(21.0 \pm 3.0) \text{ ps}^{-1}$
RBC/UKQCD14 [138]	$(290 \pm 20) \text{ MeV}$	$(22.4 \pm 3.4) \text{ ps}^{-1}$
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[LDL, Kirk, Lenz 17|2.06572]

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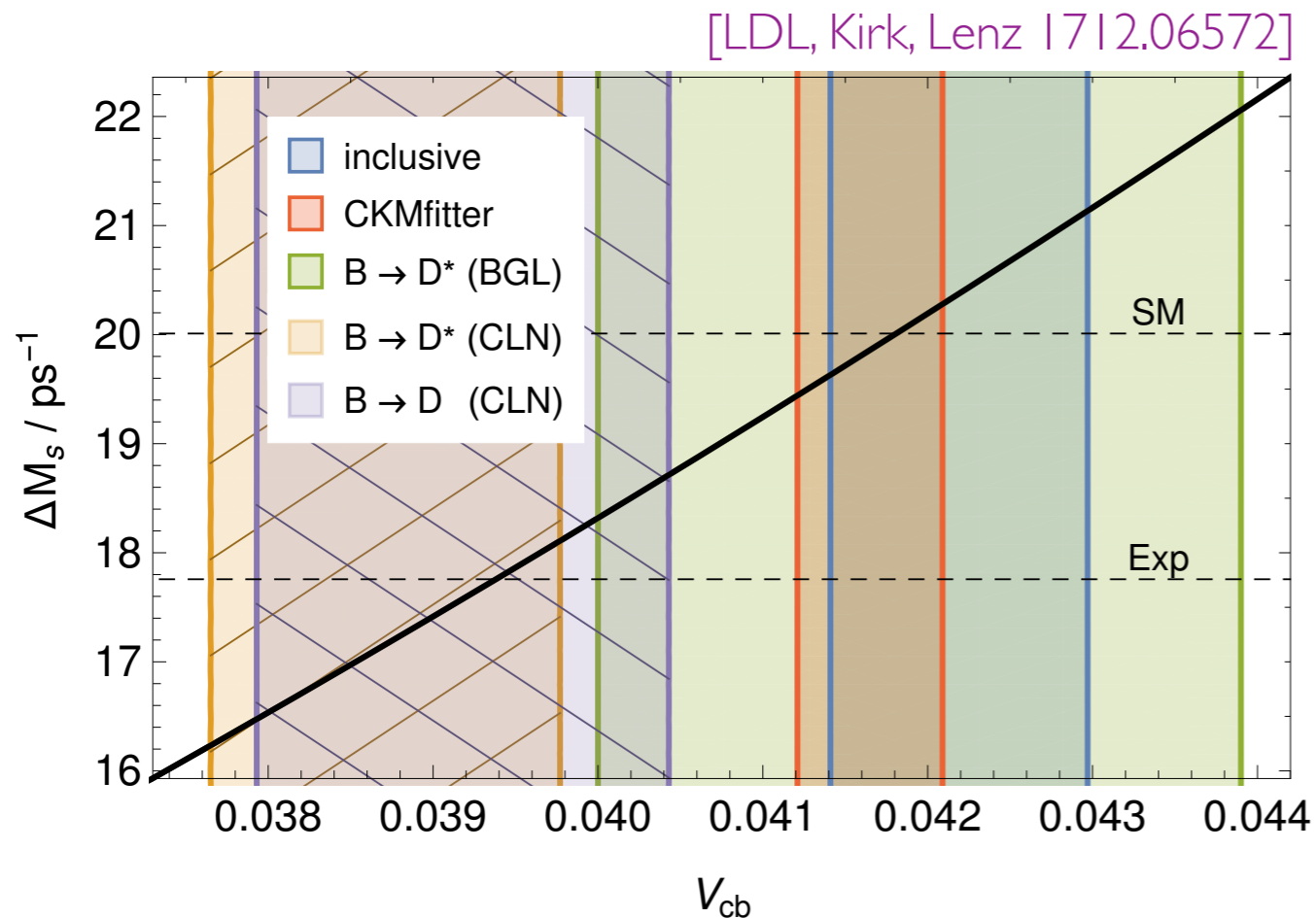
[LDL, Kirk, Lenz 17|2.06572]

★ Lattice updates crucial to settle the issue !

V_{cb} dependence

- V_{cb} is the second most important ingredient for SM prediction

→ we use CKMfitter value* (consistent with inclusive determination)



$$\Delta M_s^{\text{SM}, 2017} = (20.01 \pm 1.25) \text{ ps}^{-1}$$

$$[\Delta M_s^{\text{SM}, 2017 (\text{tree})} = (19.9 \pm 1.5) \text{ ps}^{-1}]$$

*Includes loop-mediated observables (potentially affected by NP)

Part-II

Impact on B-anomalies

ΔM_s vs. new physics (NP)

- As an example let's assume:

1. NP in purely V-A $\Delta B = 2$ operator (same matrix element as in the SM)

2. no NP pollution in the extraction of CKM elements

$$\Delta M_s^{\text{Exp}} = 2 |M_{12}^{\text{SM}} + M_{12}^{\text{NP}}| = \Delta M_s^{\text{SM}} \left| 1 + \frac{M_{12}^{\text{NP}}}{M_{12}^{\text{SM}}} \right|$$

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$$\frac{\Delta M_s^{\text{Exp}}}{\Delta M_s^{\text{SM}}} = \left| 1 + \frac{\kappa}{\Lambda_{\text{NP}}^2} \right| \quad \text{if } \kappa > 0 \quad \rightarrow \quad \frac{\Lambda_{\text{NP}}^{2017}}{\Lambda_{\text{NP}}^{2015}} = \sqrt{\frac{\frac{\Delta M_s^{\text{Exp}}}{(\Delta M_s^{\text{SM}} - 2\delta\Delta M_s^{\text{SM}})^{2015}} - 1}{\frac{\Delta M_s^{\text{Exp}}}{(\Delta M_s^{\text{SM}} - 2\delta\Delta M_s^{\text{SM}})^{2017}} - 1}} \simeq 5 \quad (2 \sigma \text{ bound})$$

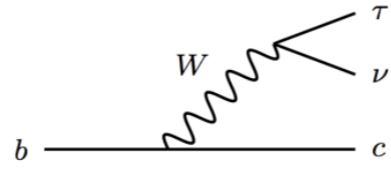
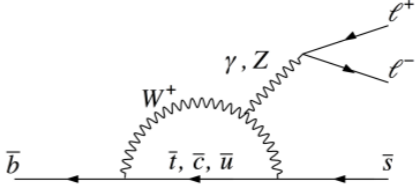
$$\Delta M_s^{\text{SM}, 2015} = (18.3 \pm 2.7) \text{ ps}^{-1} \quad [\text{Artuso, Borissov, Lenz } 1511.09466]$$

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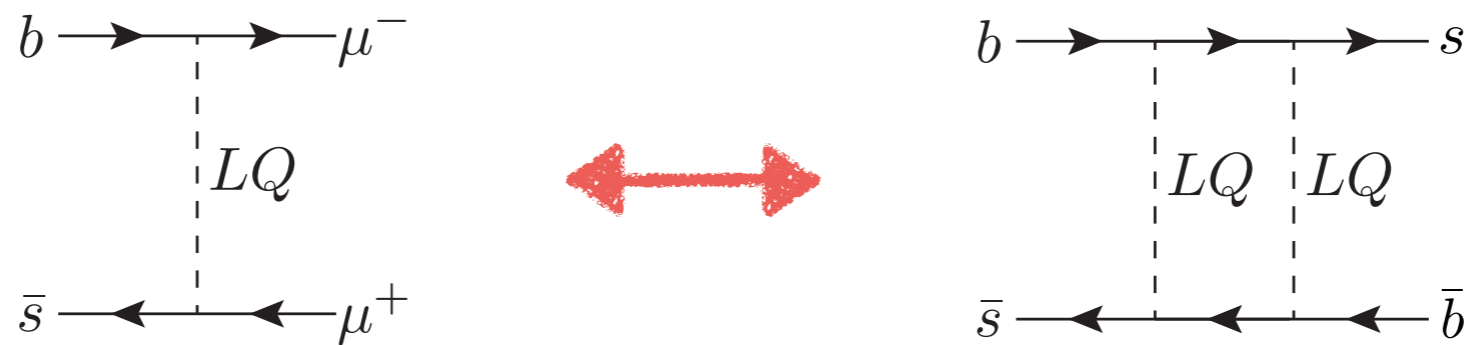
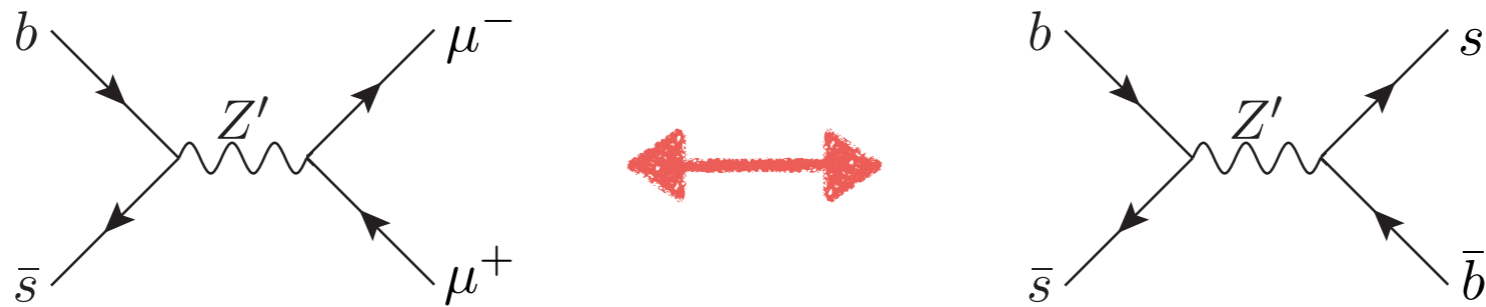
“B-anomalies”

- A seemingly coherent pattern of SM deviations building up since ~ 2012

	$b \rightarrow c\tau\nu$ 	$b \rightarrow s\mu\mu$ 
Lepton Universality	$R(D), R(D^*),$ $R(J/\psi)$	$R(K), R(K^*)$
Angular Distributions		$B \rightarrow K^* \mu\mu (P'_5)$
Differential BR ($d\Gamma/dq^2$)		$B \rightarrow K^{(*)} \mu\mu$ $B_s \rightarrow \phi \mu\mu$ $\Lambda_b \rightarrow \Lambda \mu\mu$

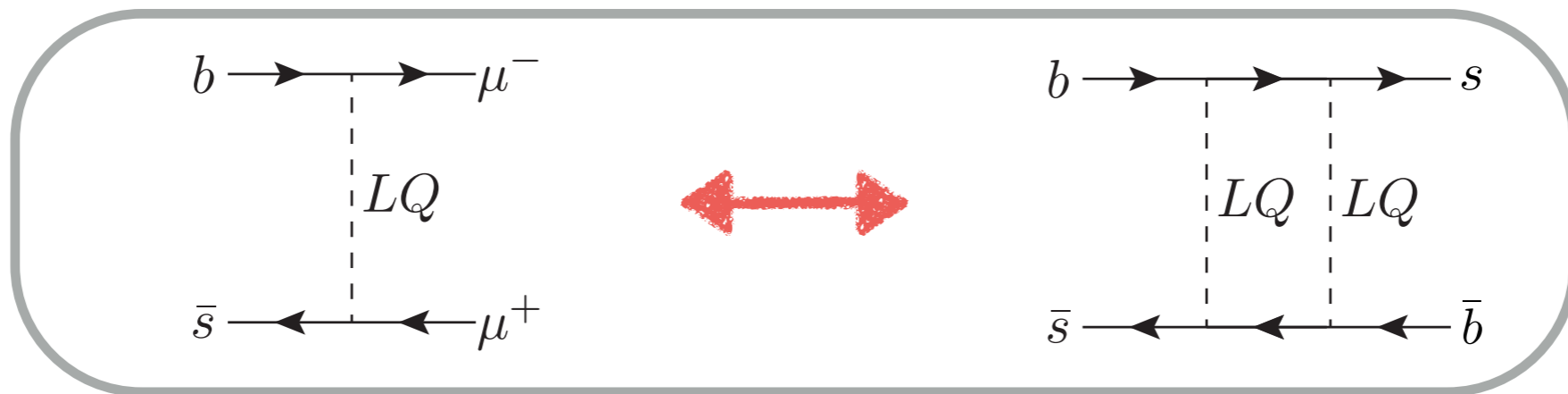
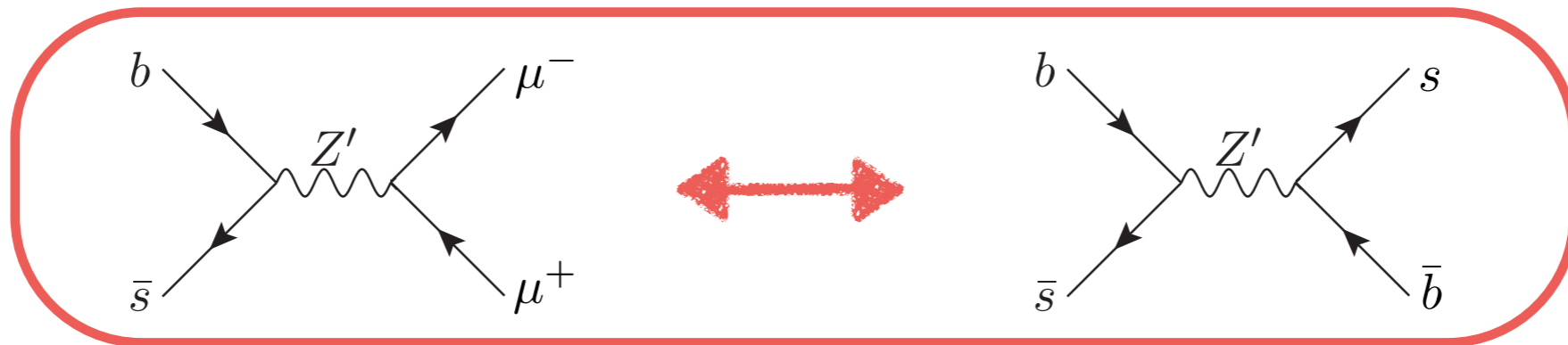
Neutral currents

- Generic robust connection between neutral current anomalies and ΔM_s



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[See backup slides]

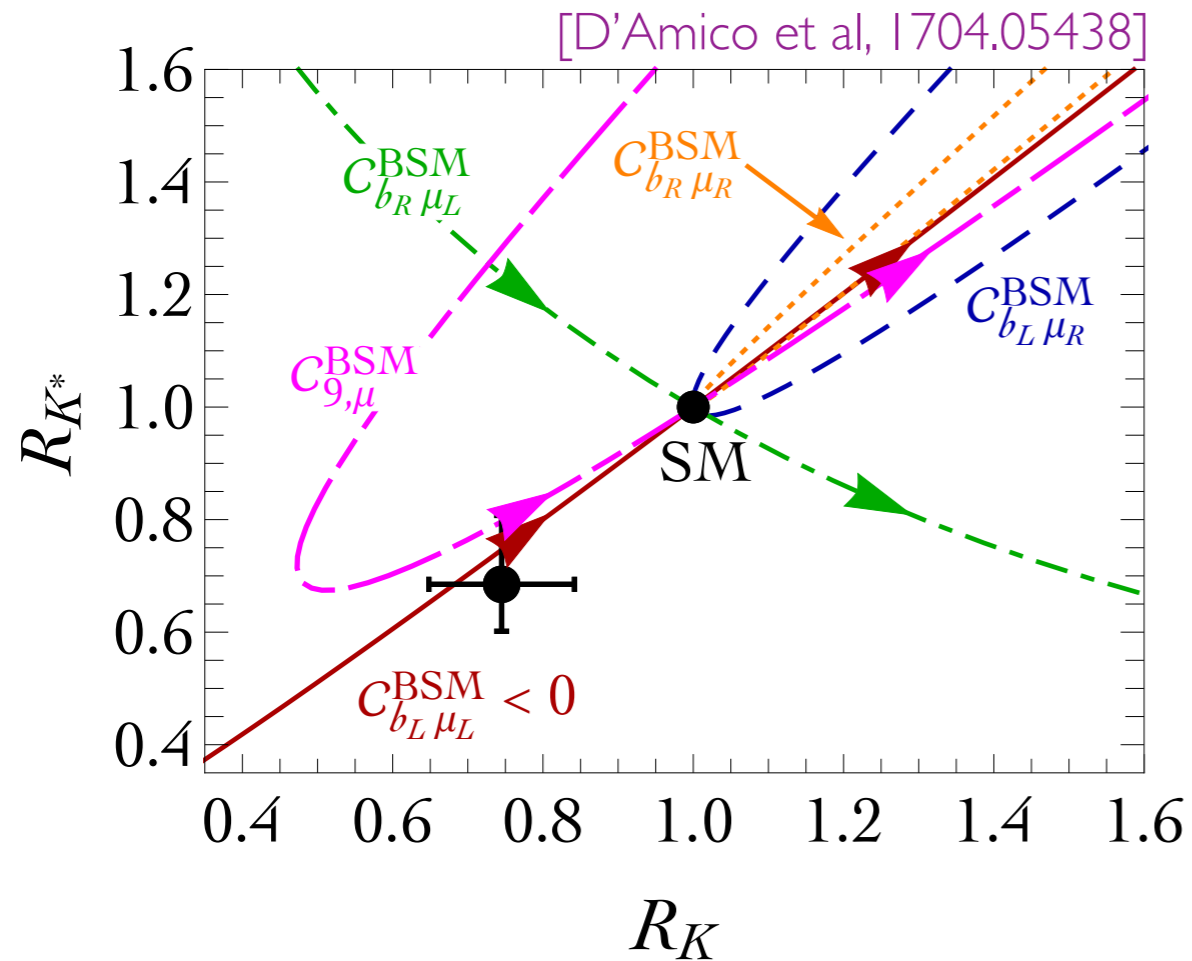
Neutral currents - Z'

- Simplified Z' model with purely LH couplings

[For an anomaly-free UV completion see e.g. Alonso, Cox, Han, Yanagida 1705.03858]

$$\mathcal{L}_{Z'} = \frac{1}{2} M_{Z'}^2 (Z'_\mu)^2 + \left(\lambda_{ij}^Q \bar{d}_L^i \gamma^\mu d_L^j + \lambda_{\alpha\beta}^L \bar{\ell}_L^\alpha \gamma^\mu \ell_L^\beta \right) Z'_\mu$$

$$C_{b_L \mu_L}^{\text{BSM}} = - \frac{\pi}{\sqrt{2} G_F M_{Z'}^2 \alpha} \left(\frac{\lambda_{bs}^Q \lambda_{\mu\mu}^L}{V_{tb} V_{ts}^*} \right)$$



$$\mathcal{L}_{b \rightarrow s \mu \mu}^{\text{NP}} \supset \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{\alpha}{4\pi} C_{b_L \mu_L}^{\text{BSM}} [\bar{s}_L \gamma_\mu b_L] [\bar{\mu}_L \gamma^\mu \mu_L]$$

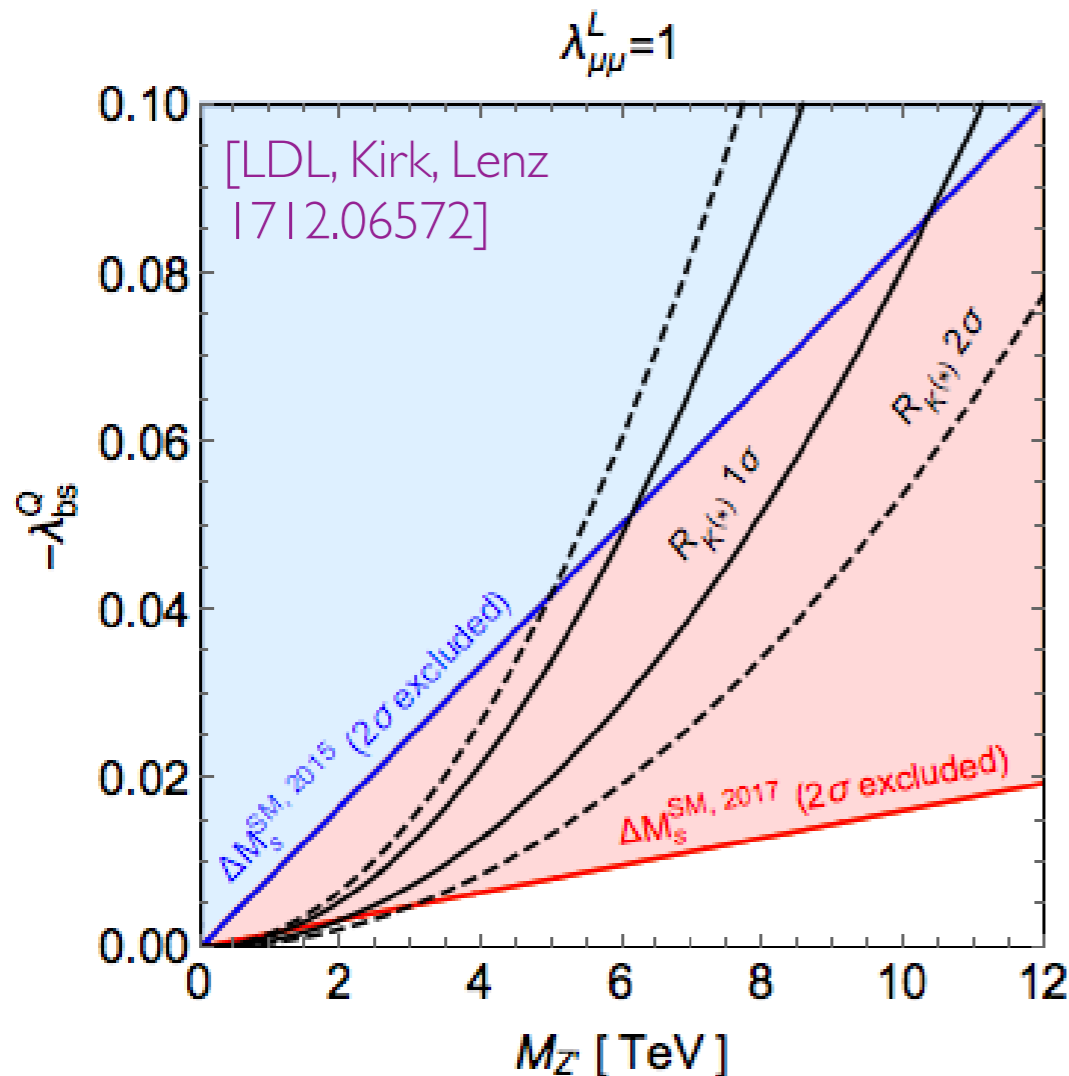
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$$\mathcal{L}_{\Delta B=2}^{\text{NP}} \supset -\frac{4G_F}{\sqrt{2}} (V_{tb} V_{ts}^*)^2 C_{bs}^{LL} [\bar{s}_L \gamma_\mu b_L]^2$$

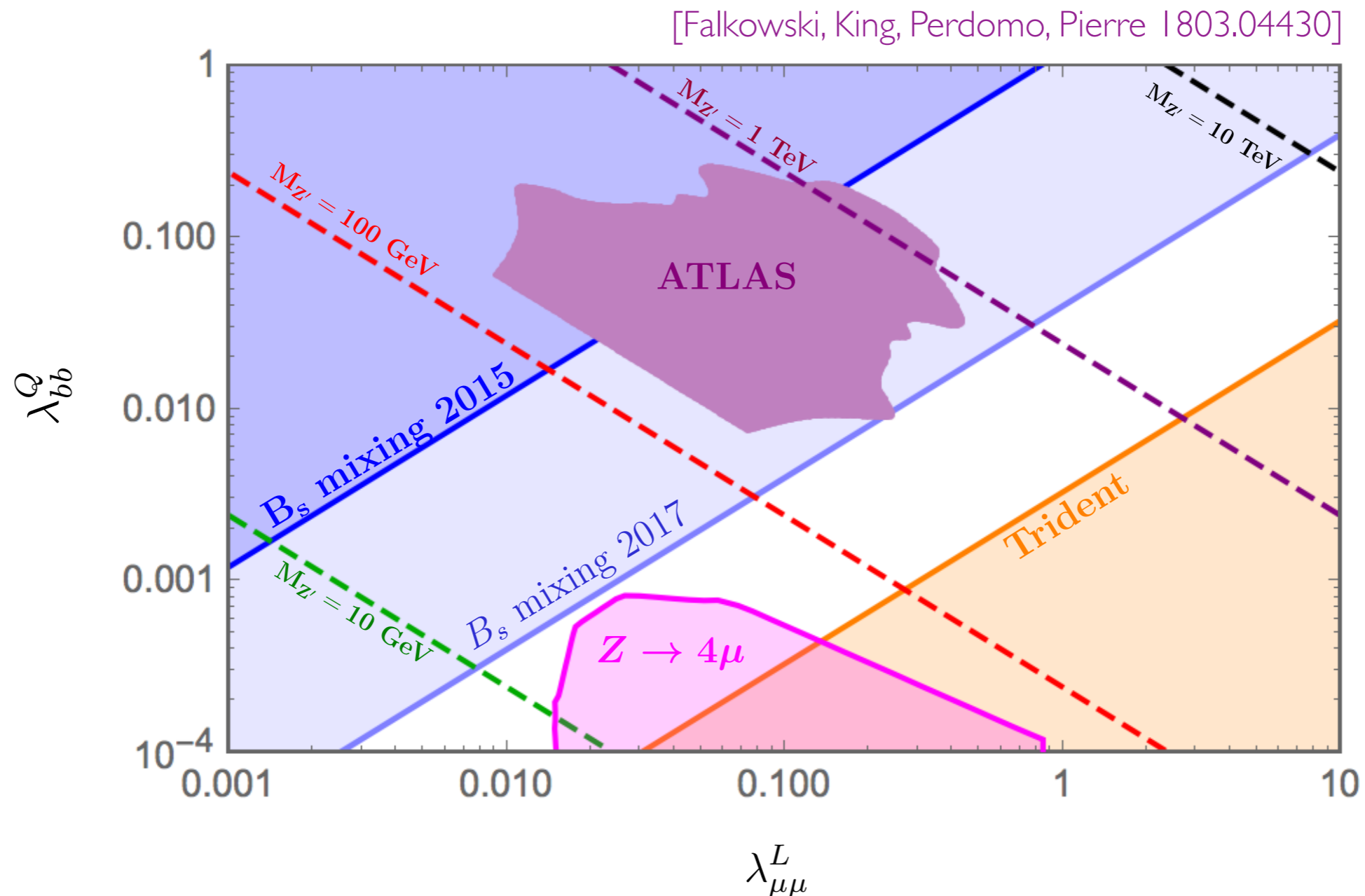
$$C_{bs}^{LL} = \frac{1}{4\sqrt{2} G_F M_{Z'}^2} \left(\frac{\lambda_{bs}^Q}{V_{tb} V_{ts}^*} \right)^2 > 0$$

↓

(assuming real couplings)

Global view on Z' par. space

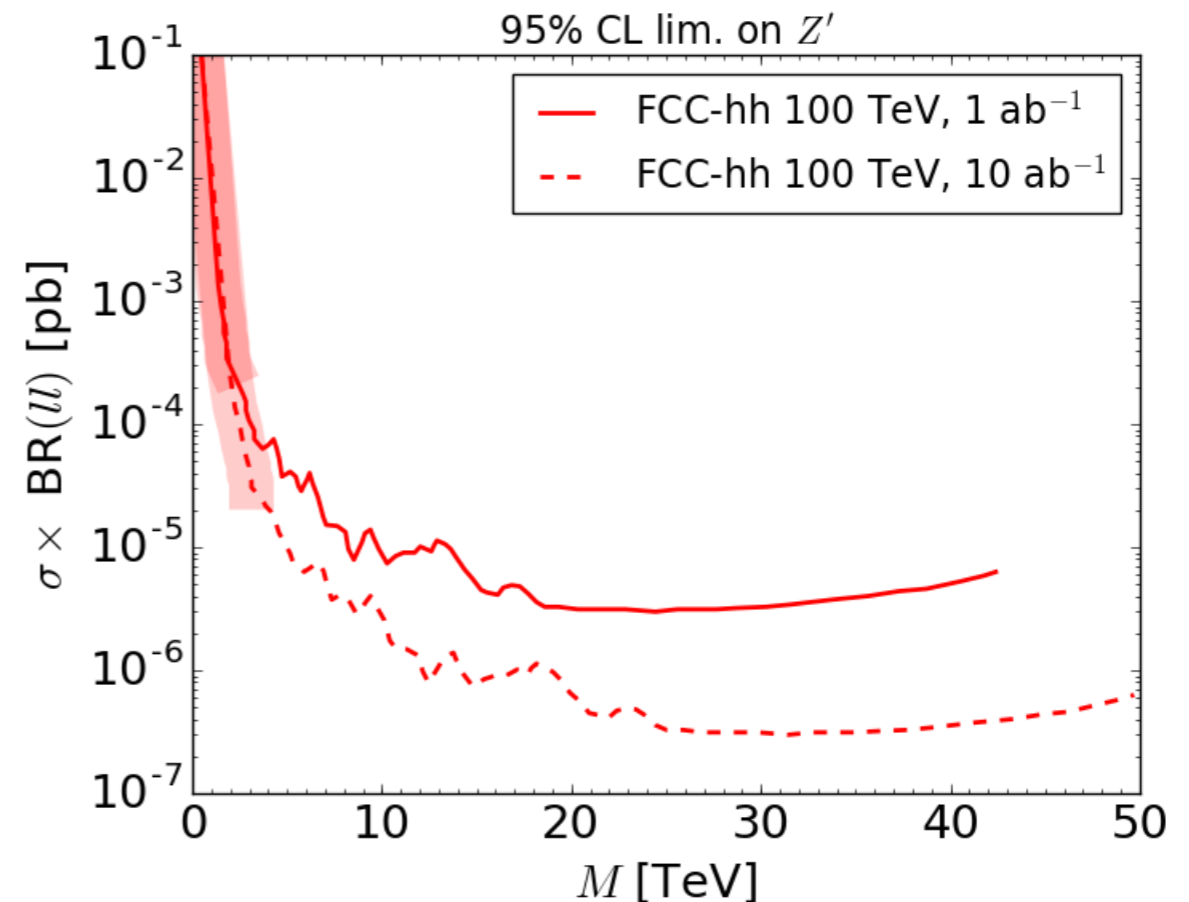
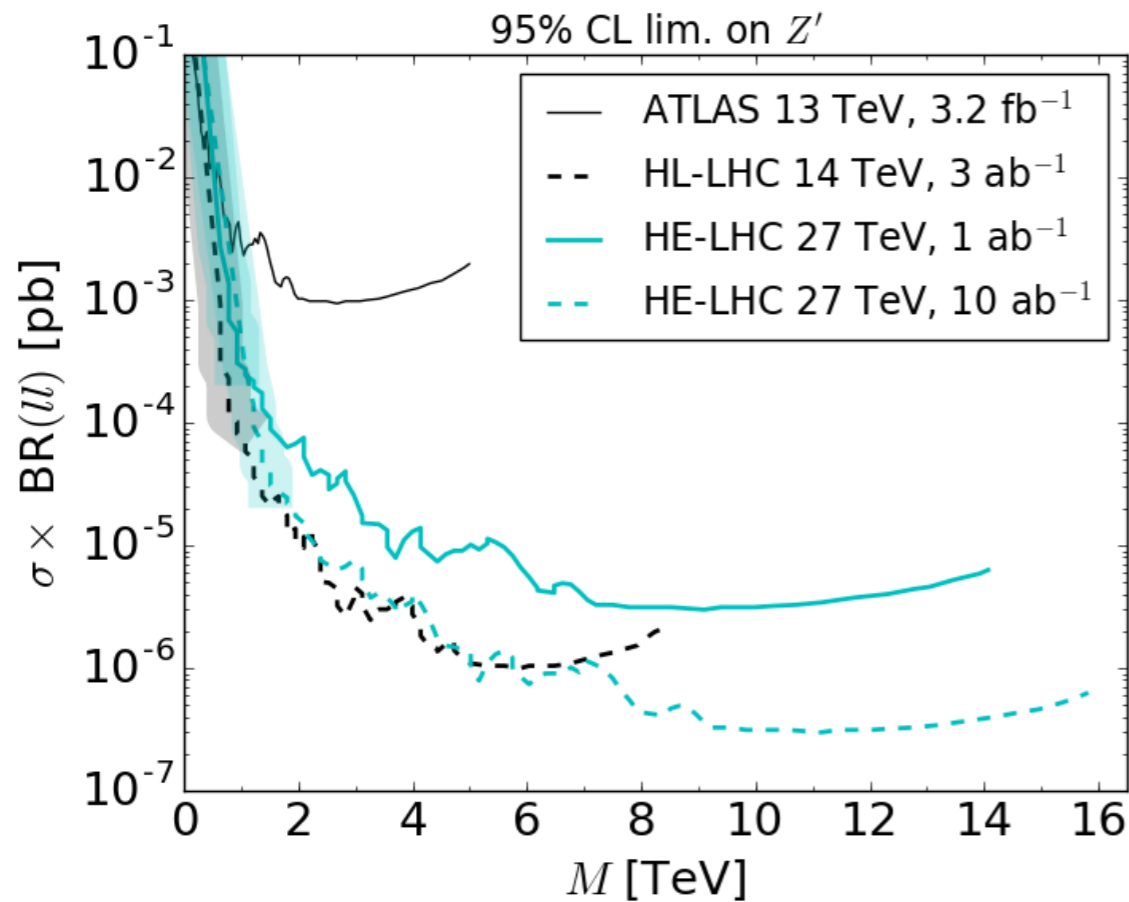
- Simplified Z' model with purely LH couplings (assuming $\lambda_{bs}^Q = \lambda_{bb}^Q V_{ts}$)



Z' at future colliders

- Pessimistic scenario: only bs and $mumu$ couplings fixed by anomaly $\frac{g_L^{bs} g_L^{\mu\mu}}{M_{Z'}^2} = \frac{1}{(31 \text{ TeV})^2}$

- Projected sensitivities of di-muons resonance searches [Allanach, Gripaio, You, 1710.06363]



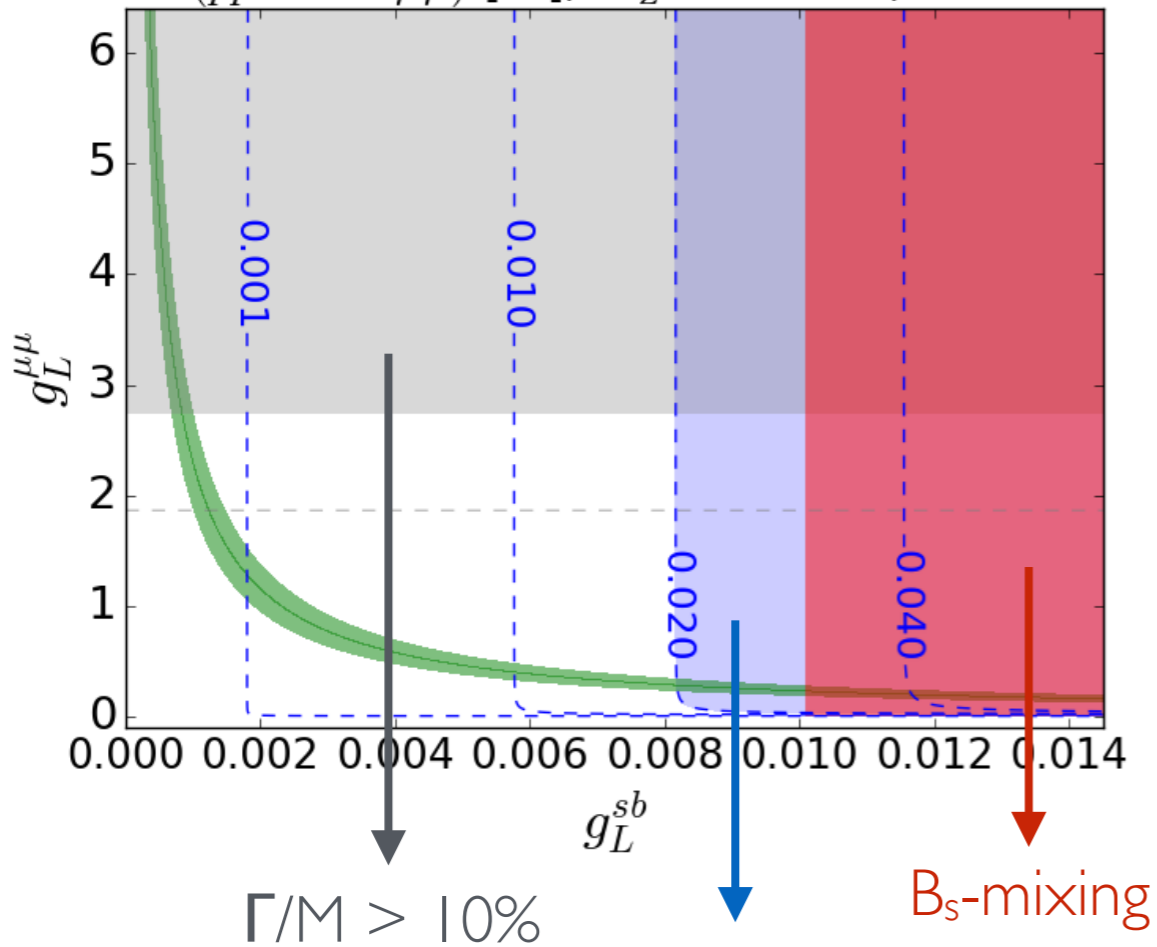
[See also talk by Allanach]

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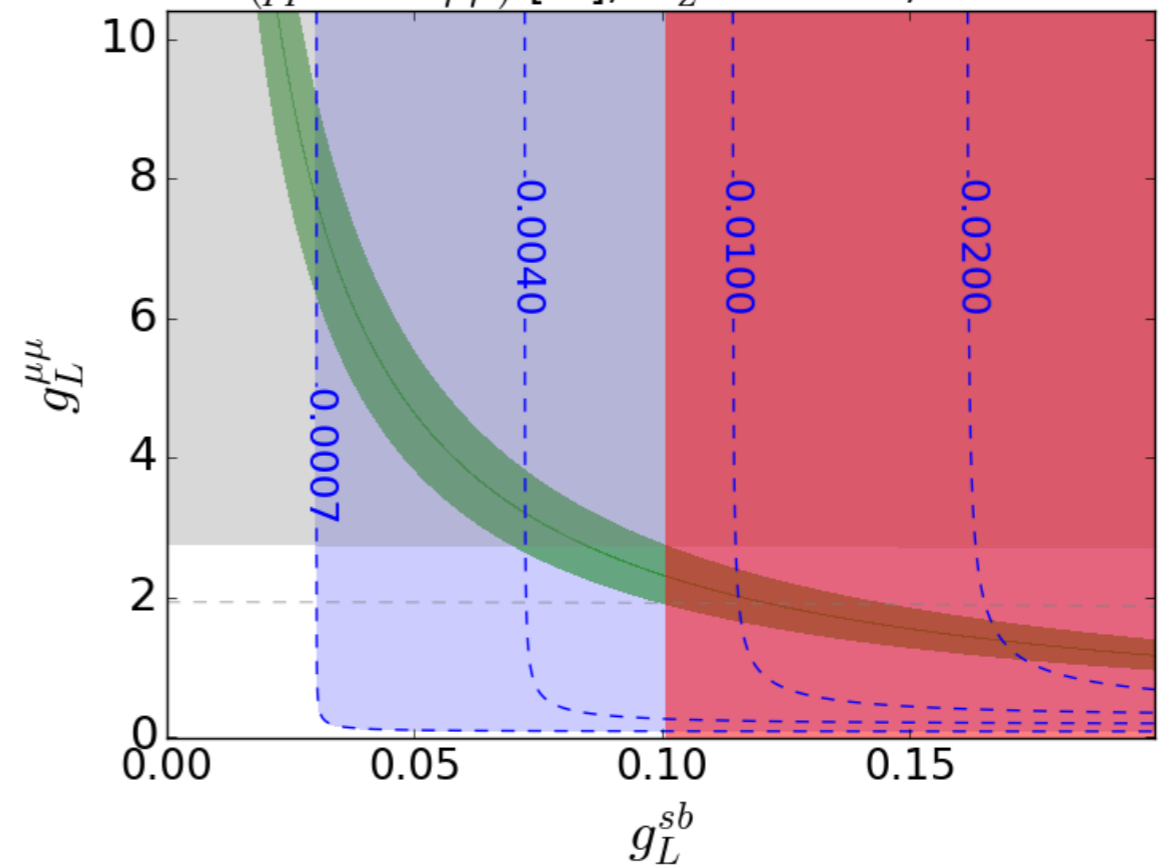
Naive $\sigma(pp \rightarrow Z' \rightarrow \mu\bar{\mu})$ [fb], $M_{Z'} = 1.5 \text{ TeV}$, $\sqrt{s} = 14 \text{ TeV}$



$\Gamma/M > 10\%$

95% CL limit
@ future hadron collider

Naive $\sigma(pp \rightarrow Z' \rightarrow \mu\bar{\mu})$ [fb], $M_{Z'} = 15 \text{ TeV}$, $\sqrt{s} = 100 \text{ TeV}$



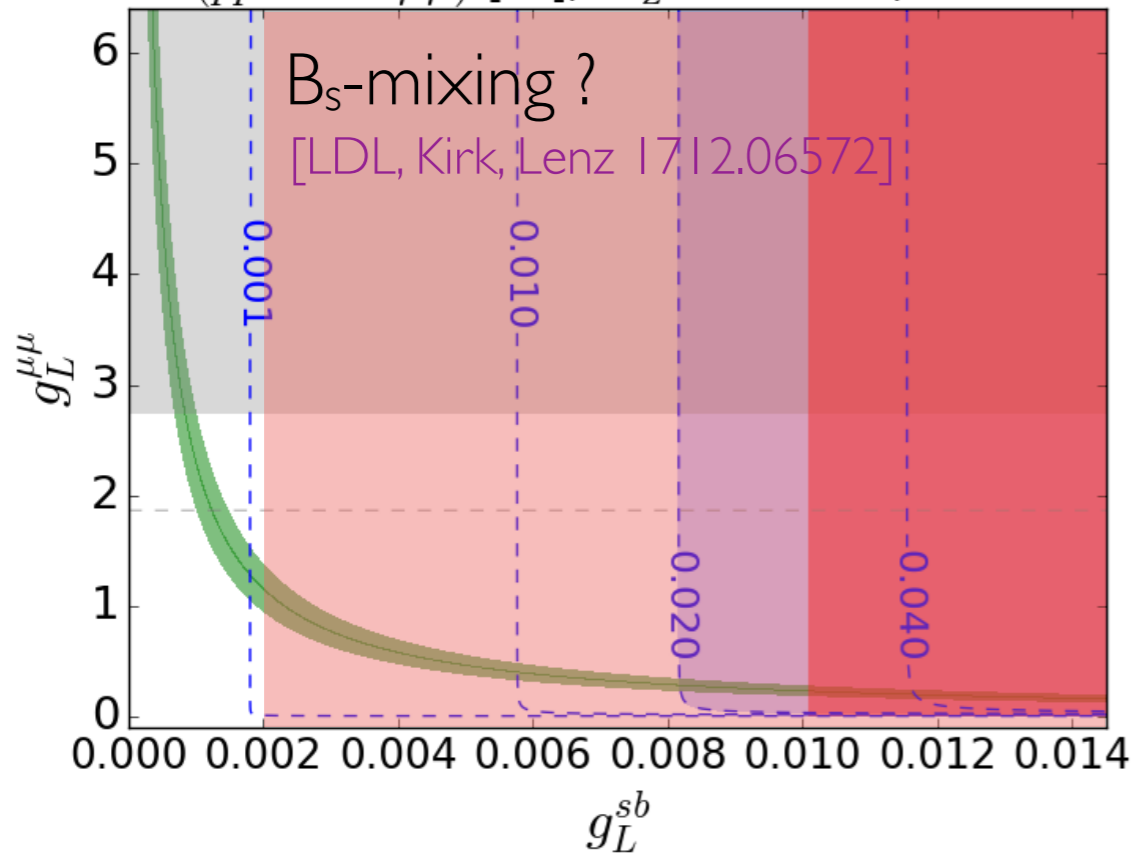
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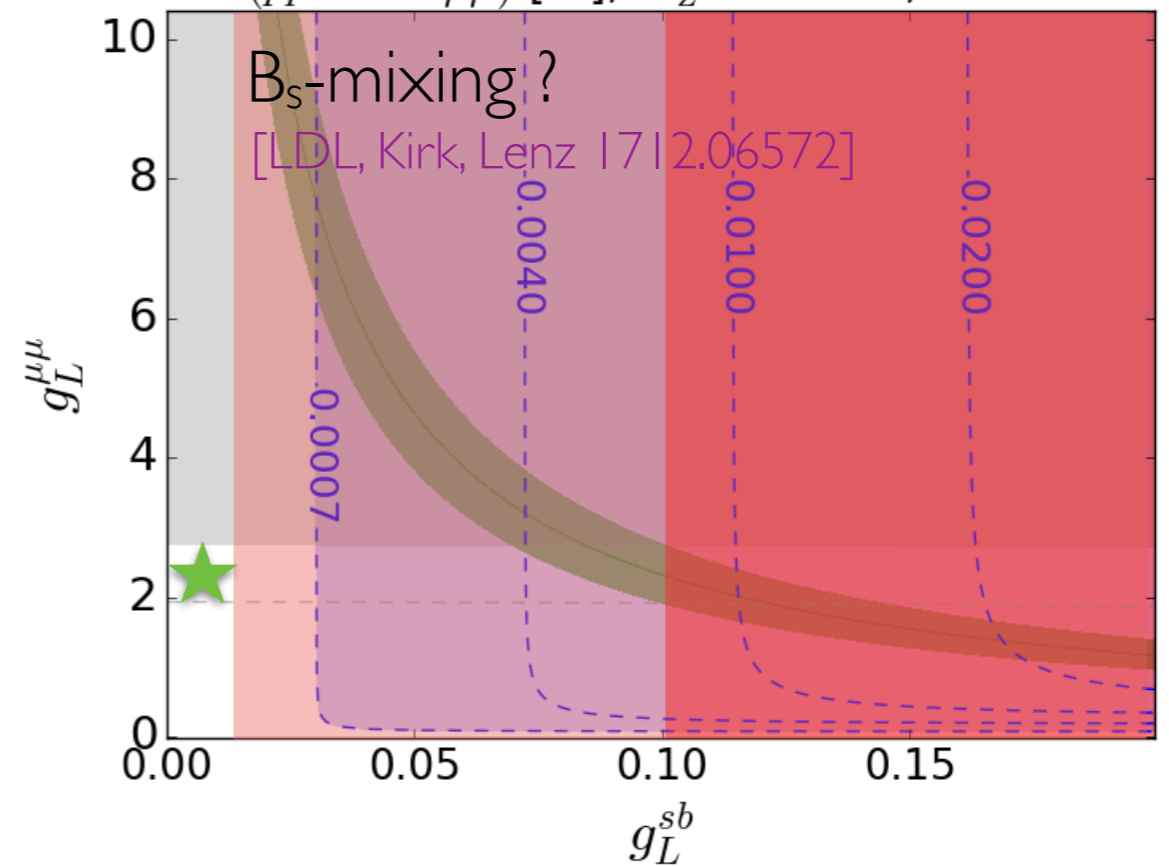
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Naive $\sigma(pp \rightarrow Z' \rightarrow \mu\bar{\mu})$ [fb], $M_{Z'}=1.5 \text{ TeV}$, $\sqrt{s} = 14 \text{ TeV}$



Naive $\sigma(pp \rightarrow Z' \rightarrow \mu\bar{\mu})$ [fb], $M_{Z'}=15 \text{ TeV}$, $\sqrt{s} = 100 \text{ TeV}$



➔ ΔM_s bound stronger than future colliders ?

[See also talk by Allanach]

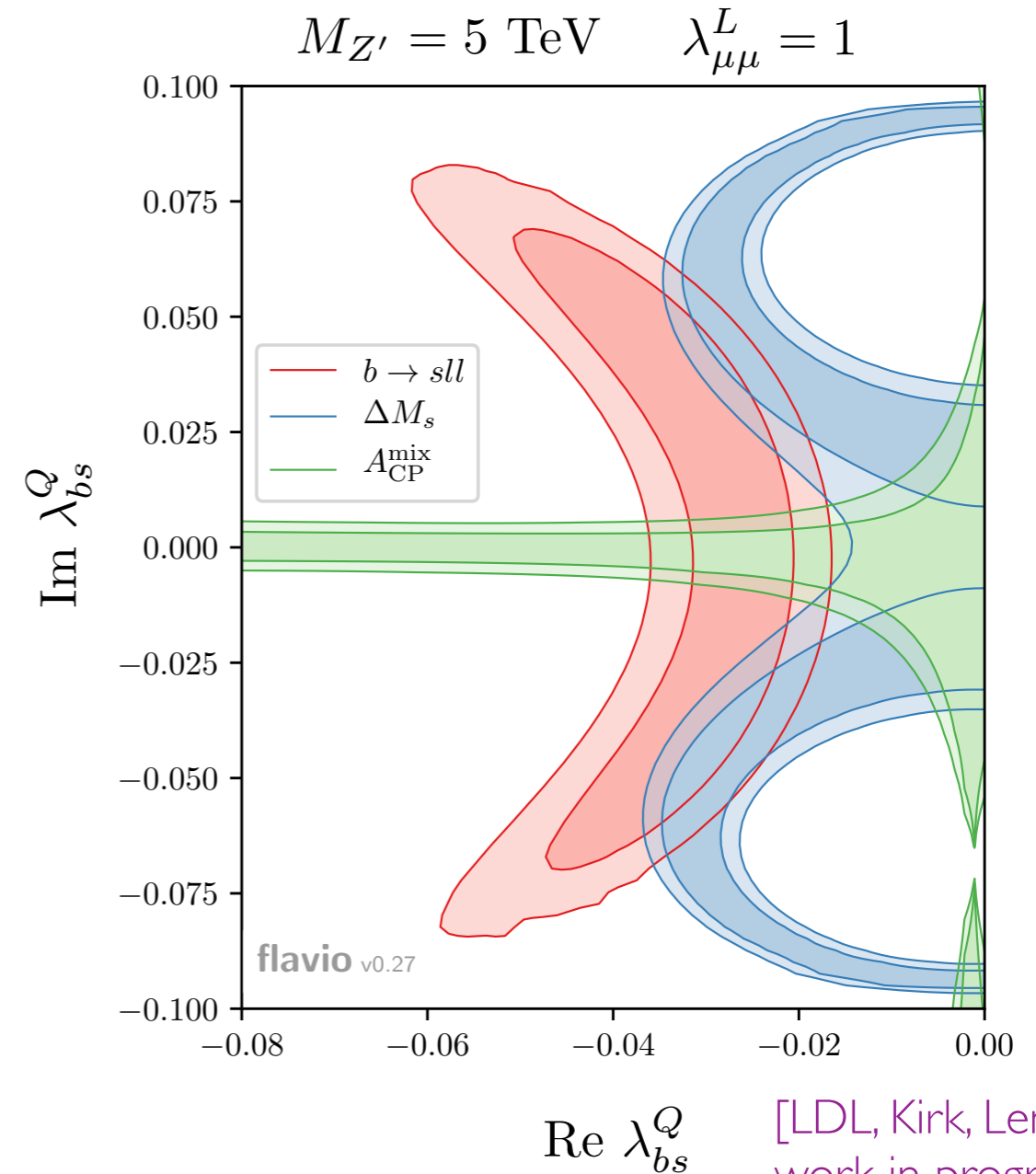
How to fit the ΔM_s “discrepancy”

1) Complex couplings

$$C_{b_L\mu_L}^{\text{BSM}} = -\frac{\pi}{\sqrt{2}G_F M_{Z'}^2 \alpha} \left(\frac{\lambda_{bs}^Q \lambda_{\mu\mu}^L}{V_{tb} V_{ts}^*} \right)$$

$$R_{K^{(*)}} \approx 1 + 2 \operatorname{Re} \left(\frac{C_{b_L\mu_L}^{\text{BSM}}}{C_{b_L\mu_L}^{\text{SM}}} \right)$$

Not strong dependence from Im part
(as long as we are in the linear regime)



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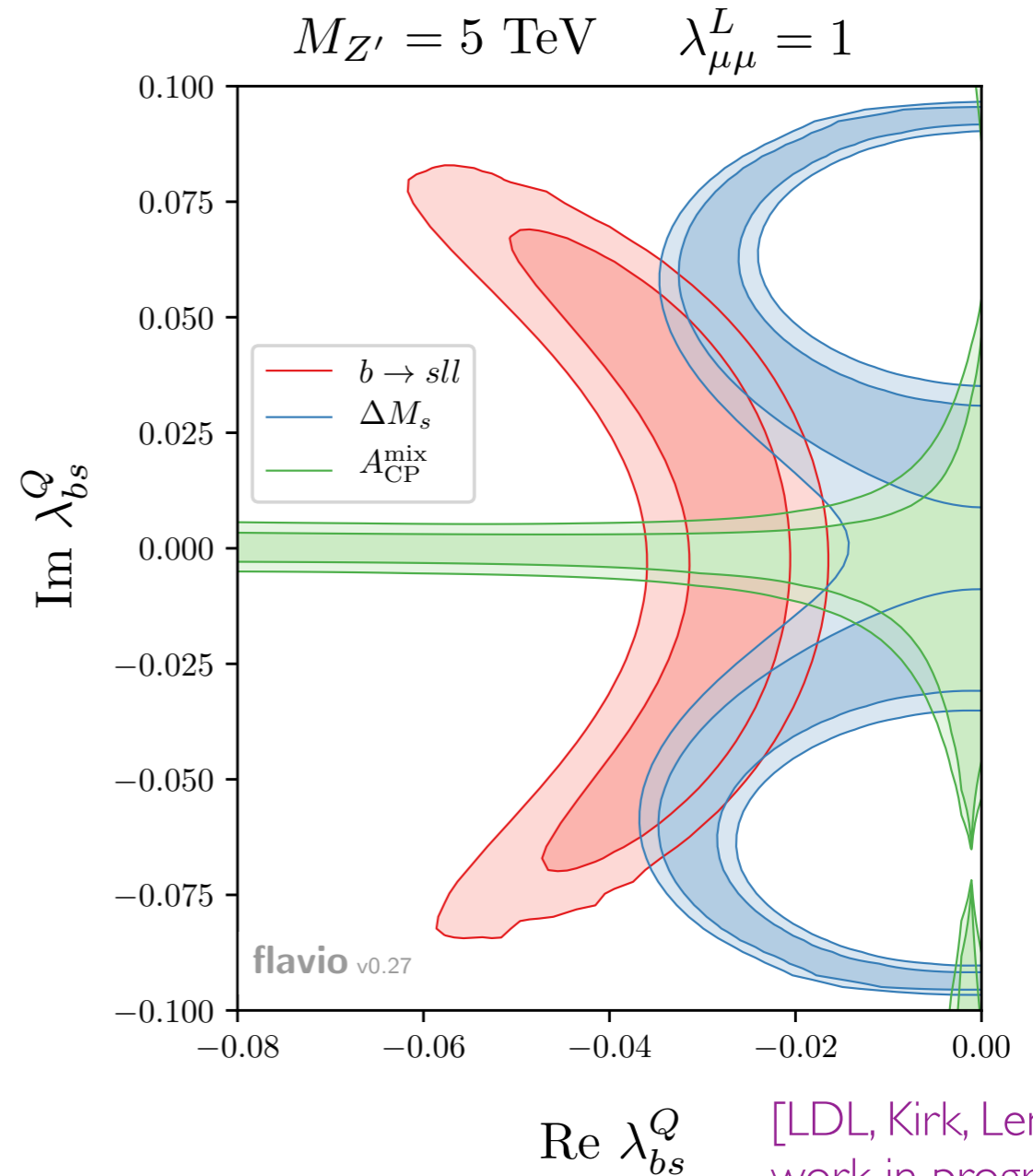
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$$\frac{M_{12}^{\text{SM+NP}}}{M_{12}^{\text{SM}}} \equiv |\Delta| e^{i\phi_\Delta}$$

$$\frac{\Delta M_s^{\text{Exp}}}{\Delta M_s^{\text{SM}}} = |\Delta| = \left| 1 + \frac{C_{bs}^{LL}}{R_{\text{SM}}^{\text{loop}}} \right|$$

Blue and Red regions have a 1σ overlap



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$$C_{b_L\mu_L}^{\text{BSM}} = -\frac{\pi}{\sqrt{2}G_F M_{Z'}^2 \alpha} \left(\frac{\lambda_{bs}^Q \lambda_{\mu\mu}^L}{V_{tb} V_{ts}^*} \right)$$

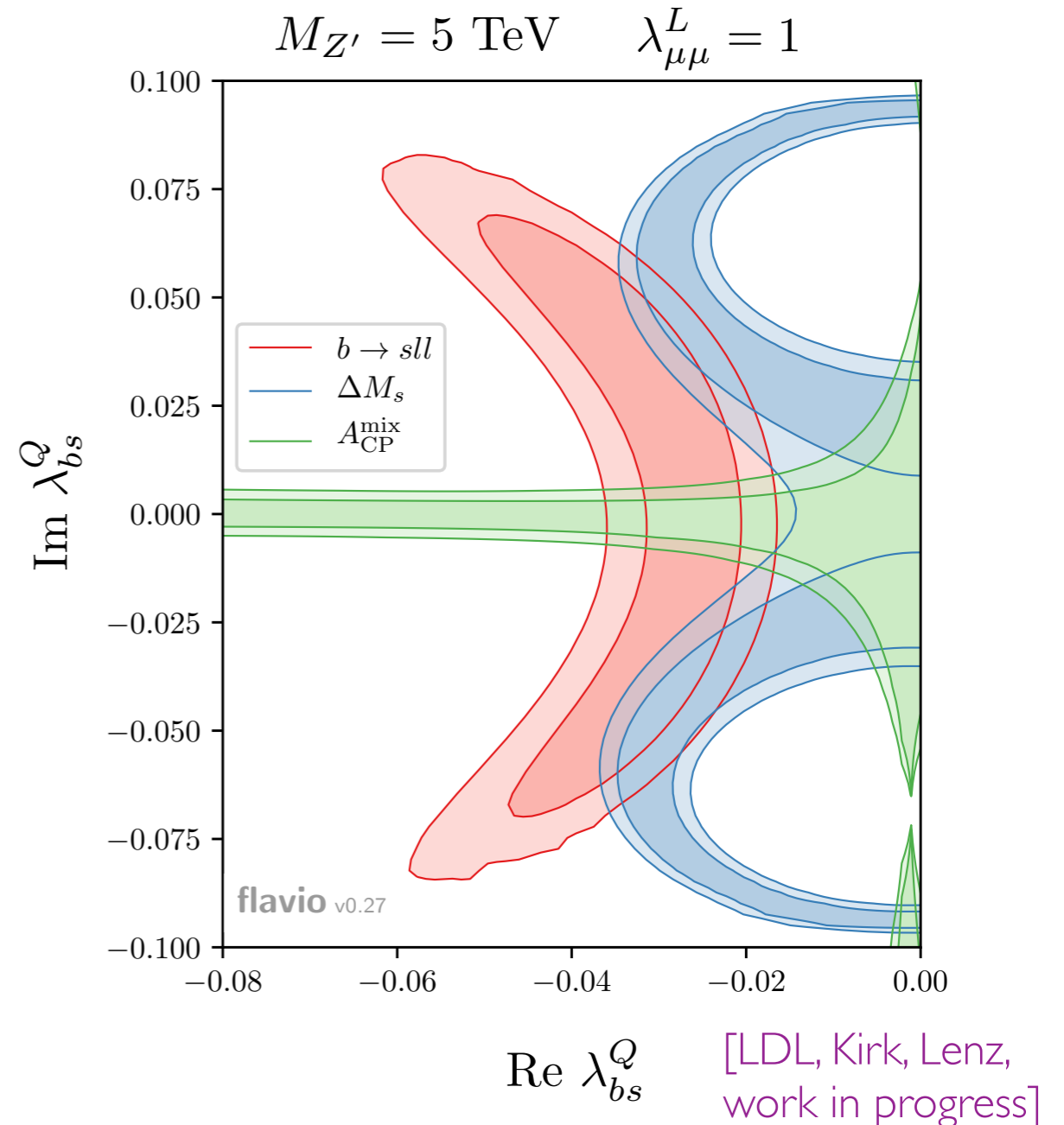
$$\frac{M_{12}^{\text{SM+NP}}}{M_{12}^{\text{SM}}} \equiv |\Delta| e^{i\phi_\Delta}$$

$$\phi_\Delta = \text{Arg} \left(1 + \frac{C_{bs}^{LL}}{R_{\text{SM}}^{\text{loop}}} \right)$$

$$A_{\text{CP}}^{\text{mix}}(B_s \rightarrow J/\psi\phi) = \sin(\phi_\Delta - 2\beta_s)$$

$$A_{\text{CP}}^{\text{mix}} = -0.021 \pm 0.031 \quad [\text{HFLAV 16|2.07233}]$$

$$\beta_s = 0.01852 \pm 0.00032 \quad [\text{CKMFitter}]$$



CP violation in mixing limits imaginary part

How to fit the ΔM_s “discrepancy”

1) Complex couplings

$$C_{b_L\mu_L}^{\text{BSM}} = -\frac{\pi}{\sqrt{2}G_F M_{Z',\alpha}^2} \left(\frac{\lambda_{bs}^Q \lambda_{\mu\mu}^L}{V_{tb} V_{ts}^*} \right)$$

Need new phases close to maximal

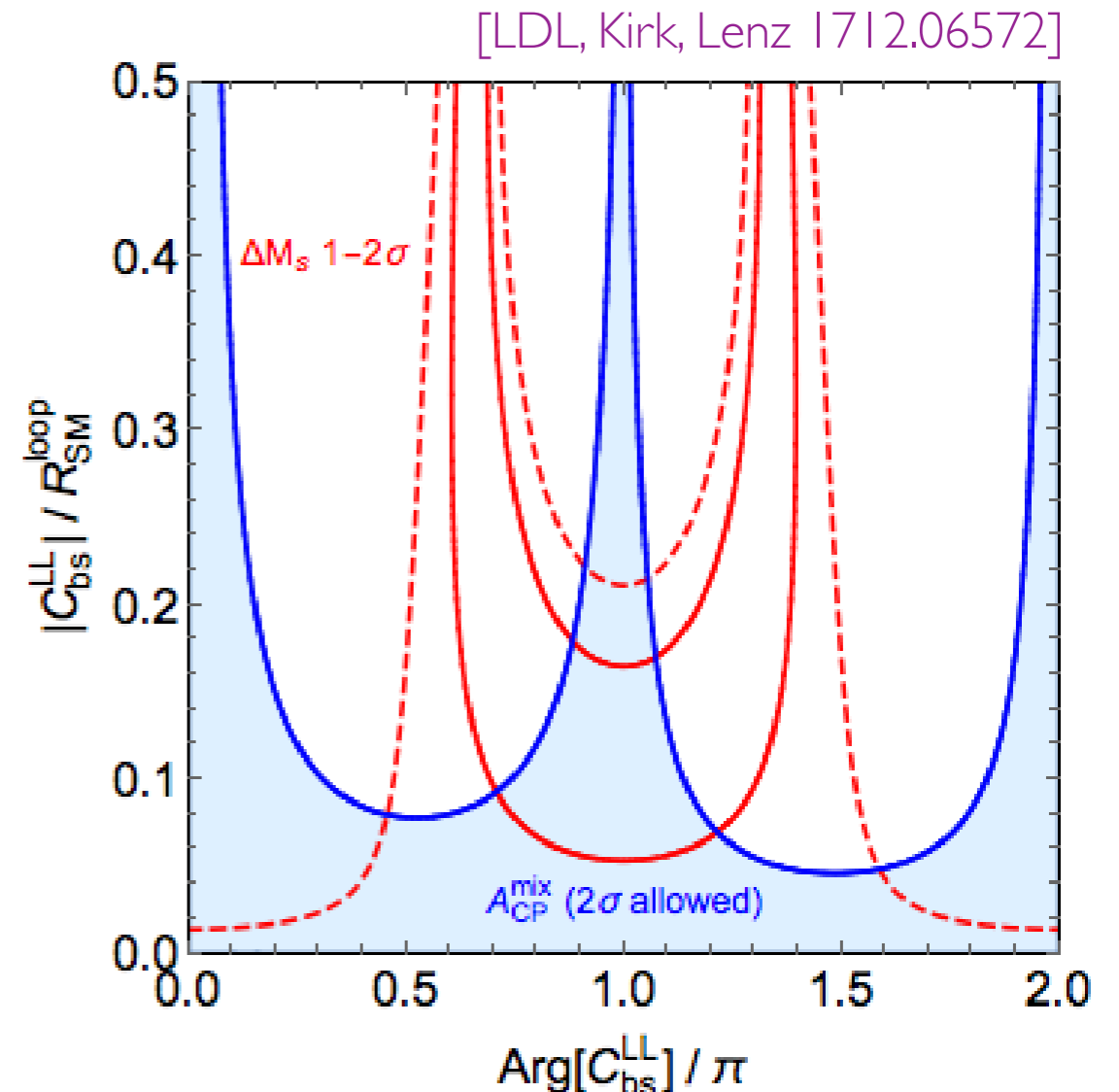
$$\text{Arg}(\lambda_{bs}^Q) \sim \pi/2$$

not directly connected to $R(K^{(*)})$

Interesting option:

in UV complete models of vector leptoquark ($R(K^{(*)}) + R(D^{(*)})$) extra Z'/G' states can naturally (compatibly with a $U(2)$ spurion analysis) accommodate that

[Bordone, Cornella, Fuentes-Martin, Isidori 1805.09328]



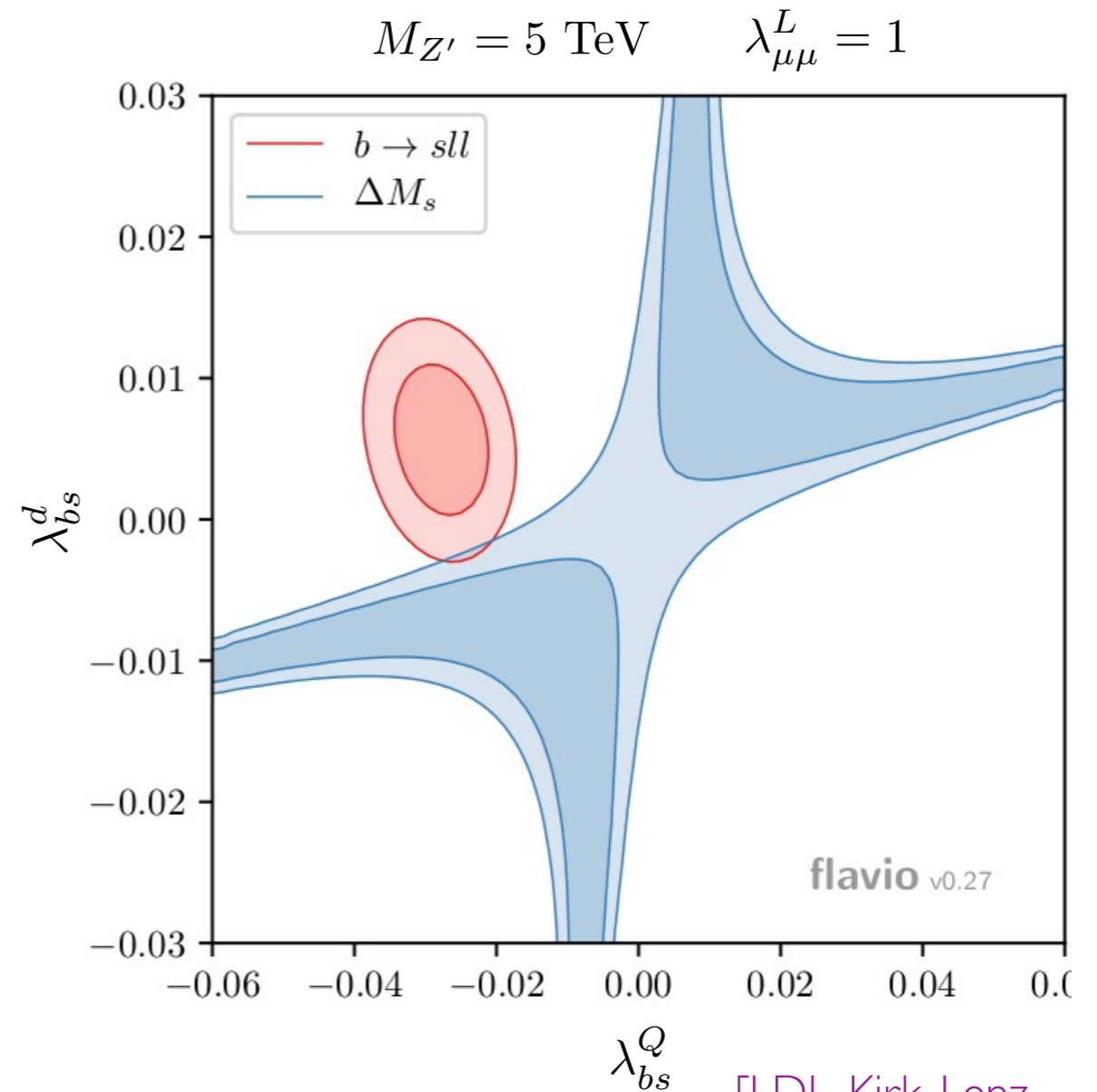
How to fit the ΔM_s “discrepancy”

1) Complex couplings

2) RH currents contamination

$$\mathcal{L}_{Z'} \supset \frac{1}{2} M_{Z'}^2 (Z'_\mu)^2 + \left(\lambda_{ij}^Q \bar{d}_L^i \gamma^\mu d_L^j + \lambda_{ij}^d \bar{d}_R^i \gamma^\mu d_R^j \right) Z'_\mu$$

$$\mathcal{L}_{Z'}^{\text{eff}} \supset -\frac{1}{2M_{Z'}^2} \left[(\lambda_{23}^Q)^2 (\bar{s}_L \gamma_\mu b_L)^2 + (\lambda_{23}^d)^2 (\bar{s}_R \gamma_\mu b_R)^2 + 2\lambda_{23}^Q \lambda_{23}^d (\bar{s}_L \gamma_\mu b_L)(\bar{s}_R \gamma_\mu b_R) + \text{h.c.} \right]$$



[LDL, Kirk, Lenz,
work in progress]

How to fit the ΔM_s “discrepancy”

1) Complex couplings

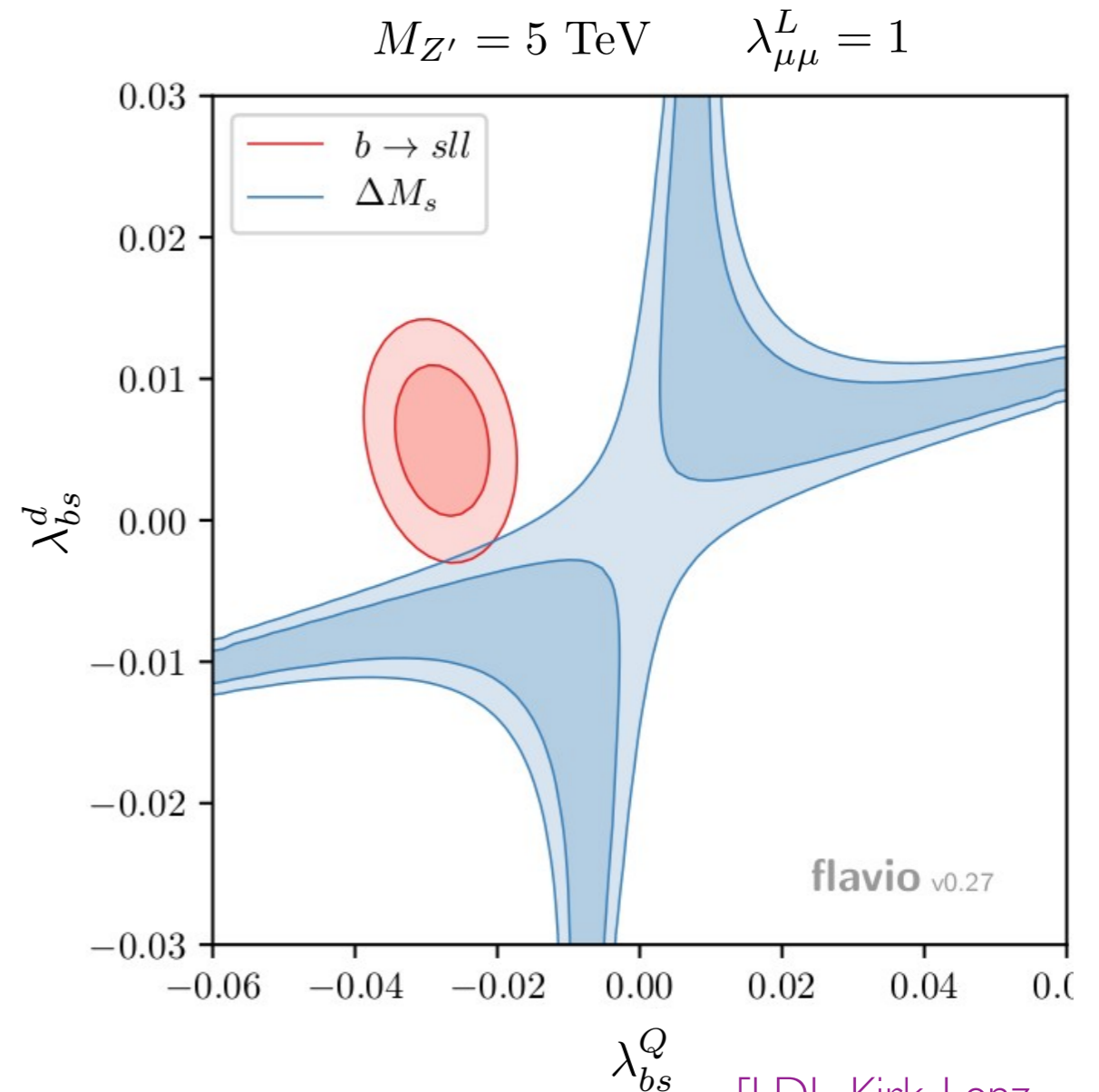
2) RH currents contamination

$$\mathcal{L}_{Z'} \supset \frac{1}{2} M_{Z'}^2 (Z'_\mu)^2 + \left(\lambda_{ij}^Q \bar{d}_L^i \gamma^\mu d_L^j + \lambda_{ij}^d \bar{d}_R^i \gamma^\mu d_R^j \right) Z'_\mu$$

$$\mathcal{L}_{Z'}^{\text{eff}} \supset -\frac{1}{2M_{Z'}^2} \left[(\lambda_{23}^Q)^2 (\bar{s}_L \gamma_\mu b_L)^2 + (\lambda_{23}^d)^2 (\bar{s}_R \gamma_\mu b_R)^2 \right. \\ \left. + 2\lambda_{23}^Q \lambda_{23}^d (\bar{s}_L \gamma_\mu b_L)(\bar{s}_R \gamma_\mu b_R) + \text{h.c.} \right]$$


LR operator can have any sign
and gets RG enhanced

However RH quark currents worsen
the fit of neutral current anomalies



[LDL, Kirk, Lenz,
work in progress]

Conclusions

1. ΔM_s is a powerful test of the SM
2. If new physics in $b \rightarrow s \ell \ell$ natural to expect a deviation in ΔM_s
 -  Looking forward for Lattice / HQET-SR updates !

Backup slides

Input parameters

Parameter	Value	Reference
M_W	80.385(15) GeV	PDG 2017
G_F	$1.1663787(6)10^{-5}$ GeV ⁻²	PDG 2017
\hbar	$6.582119514(40)10^{-25}$ GeV s	PDG 2017
M_{B_s}	5.36689(19) GeV	PDG 2017
m_t	173.1(0.6) GeV	PDG 2017
$\bar{m}_t(\bar{m}_t)$	165.65(57) GeV	own evaluation
$\bar{m}_b(\bar{m}_b)$	4.203(25) GeV	NRSR
$\alpha_s(M_Z)$	0.1181(11)	PDG 2017
$\alpha_s(\bar{m}_b)$	0.2246(21)	own evaluation
$\Lambda^{(5)}$	0.2259(68) GeV	own evaluation
V_{us}	$0.22508^{+0.00030}_{-0.00028}$	CKMfitter
V_{cb}	$0.04181^{+0.00028}_{-0.00060}$	CKMfitter
$ V_{ub}/V_{cb} $	0.0889(14)	CKMfitter
γ_{CKM}	$1.141^{+0.017}_{-0.020}$	CKMfitter
$f_{B_s} \sqrt{\hat{B}}$	274(8) MeV	FLAG

[LDL, Kirk, Lenz 1712.06572]

Error budget

ΔM_s^{SM}	This work	ABL 2015 [65]	LN 2011 [66]	LN 2006 [119]
Central Value	20.01 ps ⁻¹	18.3 ps ⁻¹	17.3 ps ⁻¹	19.3 ps ⁻¹
$\delta(f_{B_s} \sqrt{B})$	5.8%	13.9%	13.5%	34.1%
$\delta(V_{cb})$	2.1%	4.9%	3.4%	4.9%
$\delta(m_t)$	0.7%	0.7%	1.1%	1.8%
$\delta(\alpha_s)$	0.1%	0.1%	0.4%	2.0%
$\delta(\gamma_{\text{CKM}})$	0.1%	0.1%	0.3%	1.0%
$\delta(V_{ub}/V_{cb})$	< 0.1%	0.1%	0.2%	0.5%
$\delta(\overline{m}_b)$	< 0.1%	< 0.1%	0.1%	— — —
$\sum \delta$	6.2%	14.8%	14.0%	34.6%

[LDL, Kirk, Lenz 1712.06572]

Scalar LQ

[LDL, Kirk, Lenz 1712.06572]

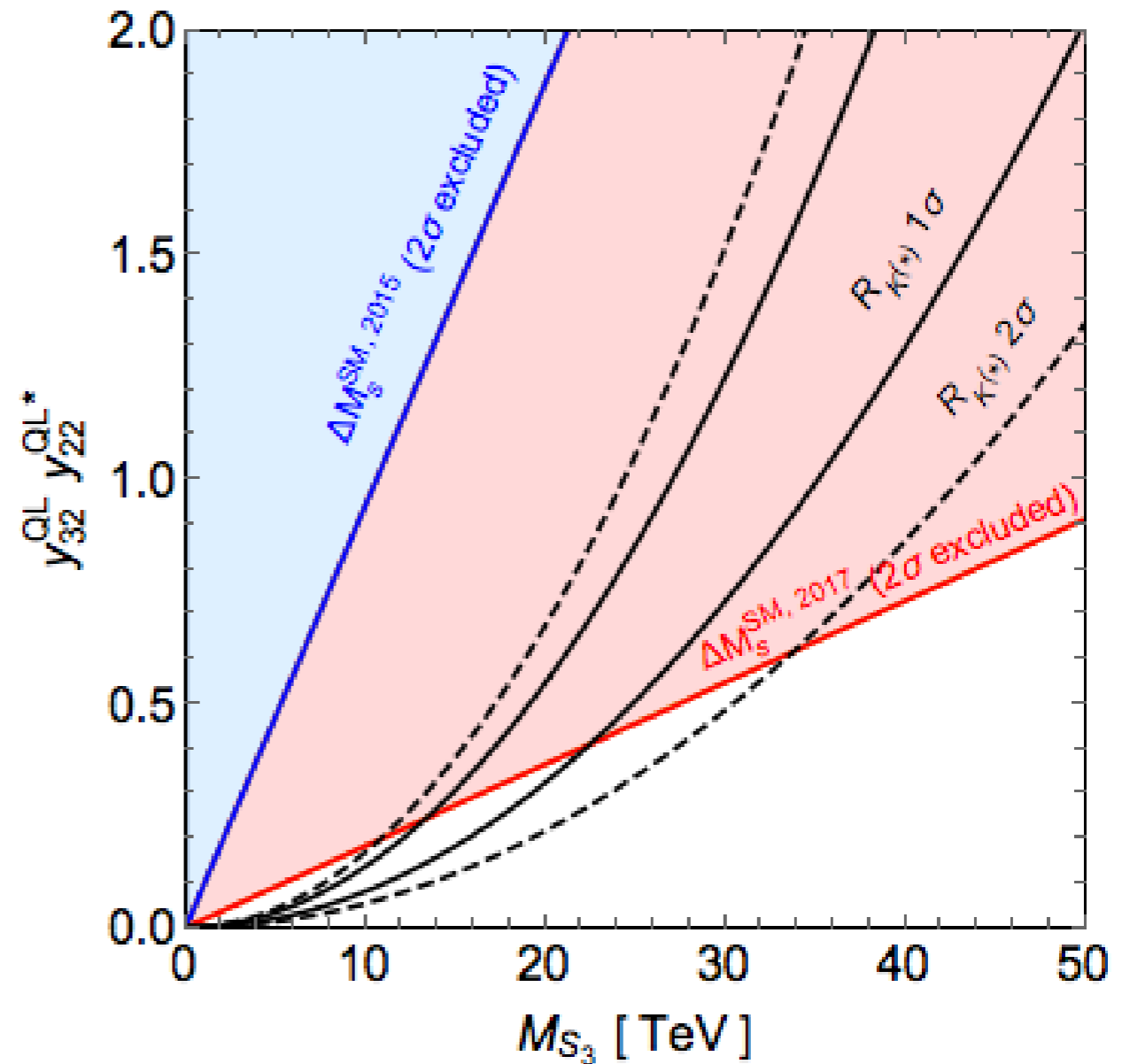
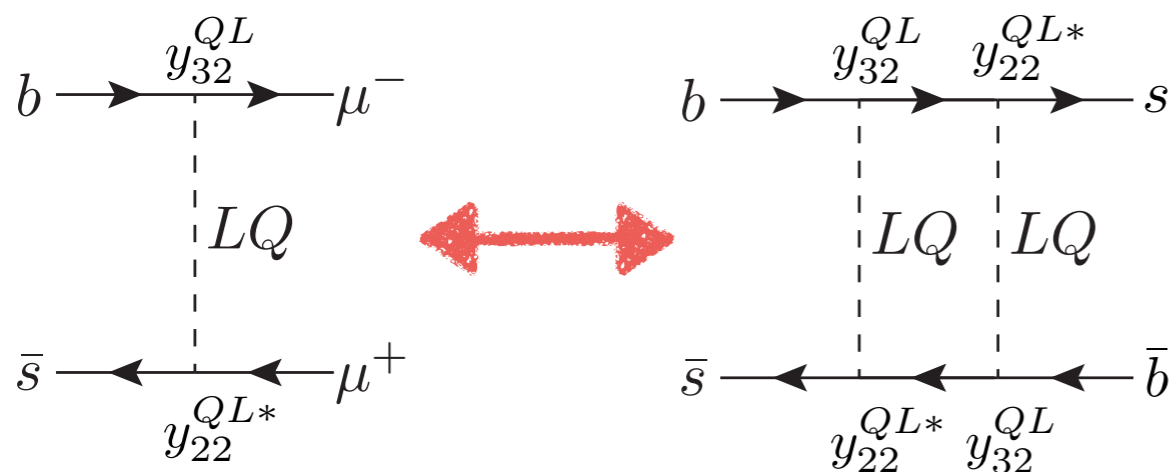
- $S_3 \sim (\bar{3}, 3, 1/3)$

$$\mathcal{L}_{S_3} = -M_{S_3}^2 |S_3^a|^2 + y_{i\alpha}^{QL} \bar{Q}^{c i} (\epsilon \sigma^a) L^\alpha S_3^a$$

$$\delta C_9^\mu = -\delta C_{10}^\mu = \frac{\pi}{\sqrt{2} G_F M_{S_3}^2 \alpha} \left(\frac{y_{32}^{QL} y_{22}^{QL*}}{V_{tb} V_{ts}^*} \right)$$

$$C_{bs}^{LL} = \frac{1}{4\sqrt{2} G_F M_{S_3}^2} \frac{5}{64\pi^2} \left(\frac{y_{3\alpha}^{QL} y_{2\alpha}^{QL*}}{V_{tb} V_{ts}^*} \right)^2$$

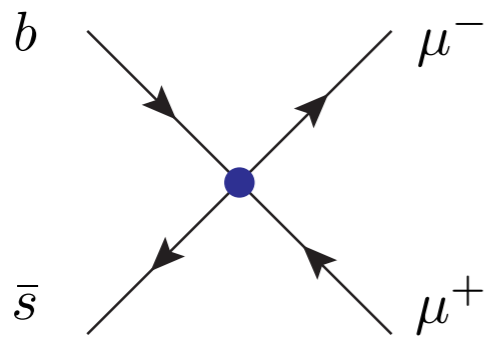
Connection is “more direct” (compared to Z’), but bounds are weaker



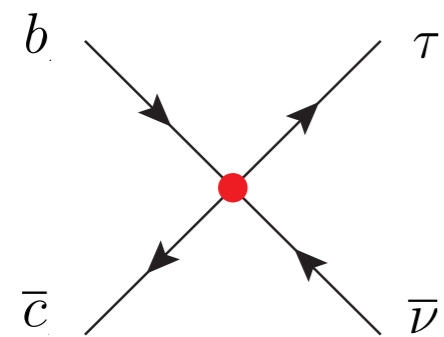
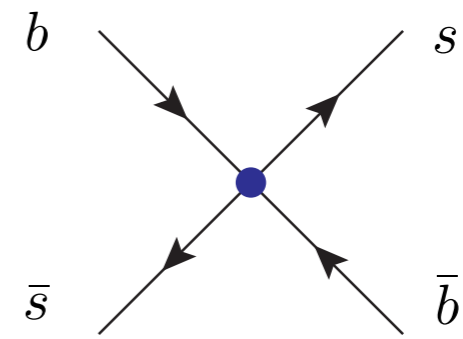
$M_{S_3} \gtrsim 900 \text{ GeV}$ [CMS 1703.03995]

Charged currents

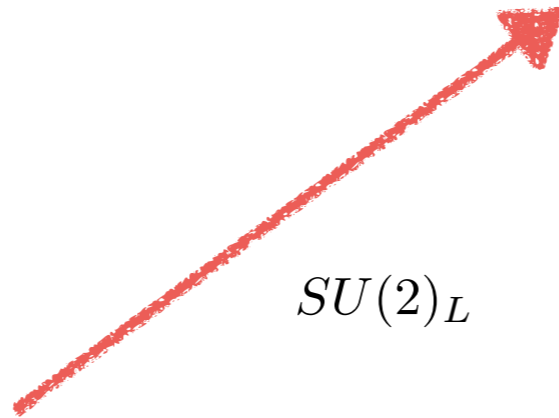
- Connection between $R(D^{(*)})$ and ΔM_s in presence of an $SU(2)_L$ triplet op.



$$\Lambda_{R_K} = 31 \text{ TeV}$$



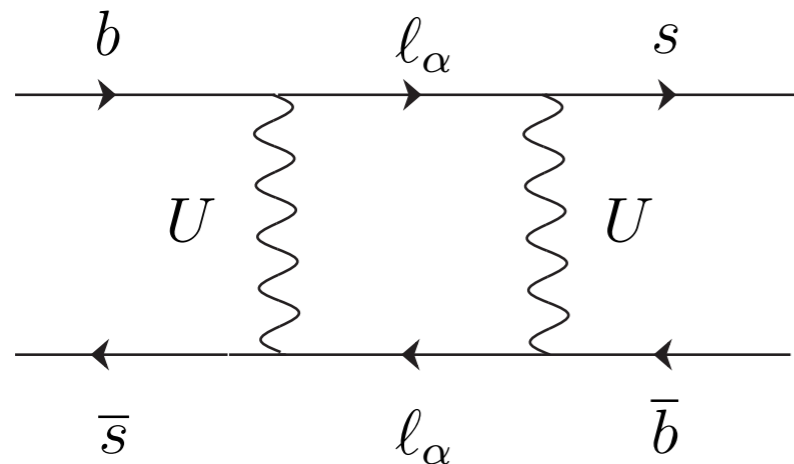
$$\Lambda_{R_D} = 3.4 \text{ TeV}$$



Vector LQ [UV complete]

- FCNC @ 1-loop under control

[LDL, Fuentes-Martin, Greljo, Nardecchia, Renner 1808.00942]



$$\mathcal{H}_{\text{eff}}^{\text{NP}} = -\frac{g_4^4}{128\pi^2 m_U^2} (\bar{b}_L \gamma^\mu s_L) (\bar{b}_L \gamma_\mu s_L) \sum_{\alpha, \beta} \lambda_\alpha \lambda_\beta F(x_\alpha, x_\beta)$$

$$\lambda_\alpha = (\mathcal{V}^\dagger)_{\alpha b}^* \mathcal{V}_{\alpha s}^\dagger \quad x_\alpha = m_\alpha^2 / M_U^2$$

$\sum_\alpha \lambda_\alpha = 0$ ensures cancellation of quadratic divergencies + GIM-like suppression

$F(x_\alpha, x_\beta) \simeq \cancel{1} + x_\alpha + x_\beta + \dots \rightarrow$ light lepton partners welcomed!

$$C_{bs}^{LL} \sim \Delta R_{D^{(*)}}^2 M_U^2 \rightarrow C_{bs}^{LL} \sim \Delta R_{D^{(*)}}^2 M_L^2$$



in absence of GIM protection

Vector LQ [UV complete]

- FCNC @ 1-loop under control

[LDL, Fuentes-Martin, Greljo, Nardecchia, Renner 1808.00942]

