



# Measurement of $\sin^2\beta$ at LHCb

10th International Workshop on the CKM Unitarity Triangle

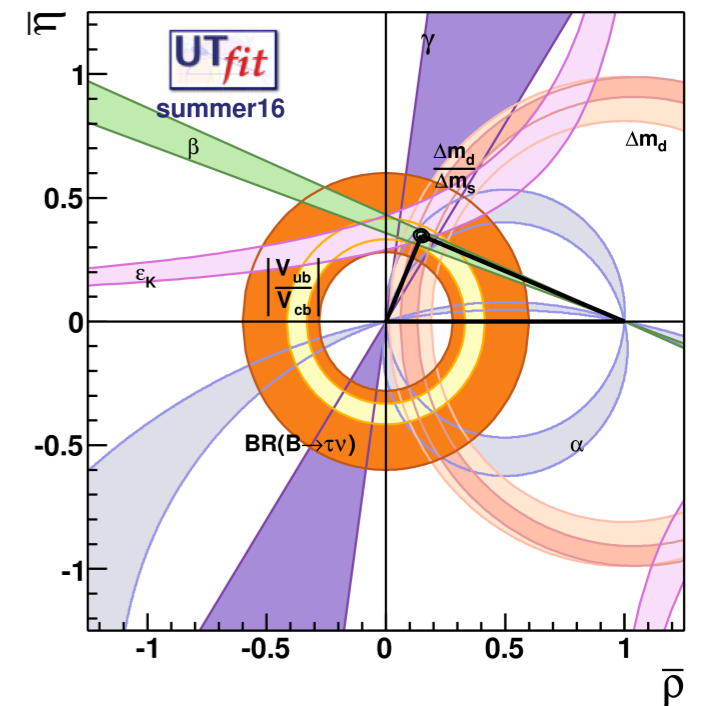
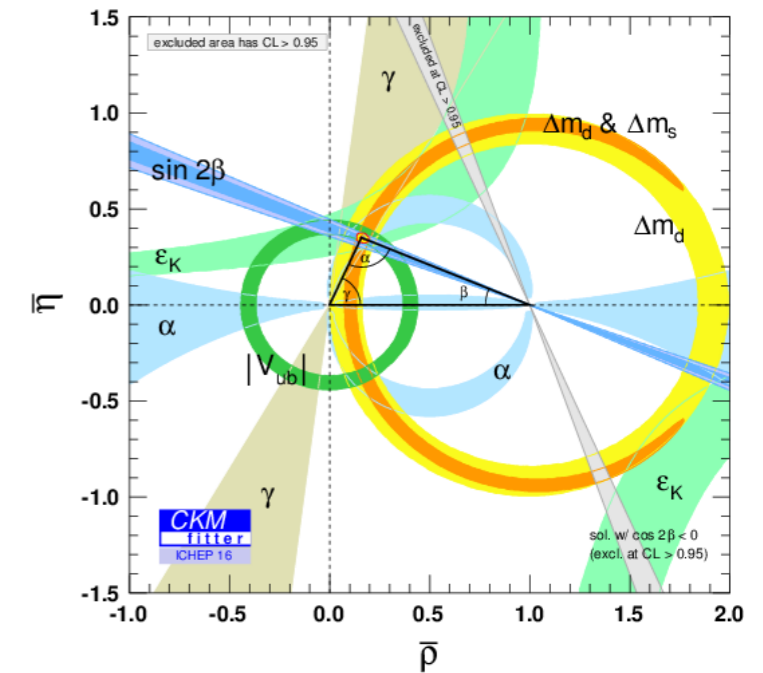
Heidelberg, Germany, 17-21 September 2018

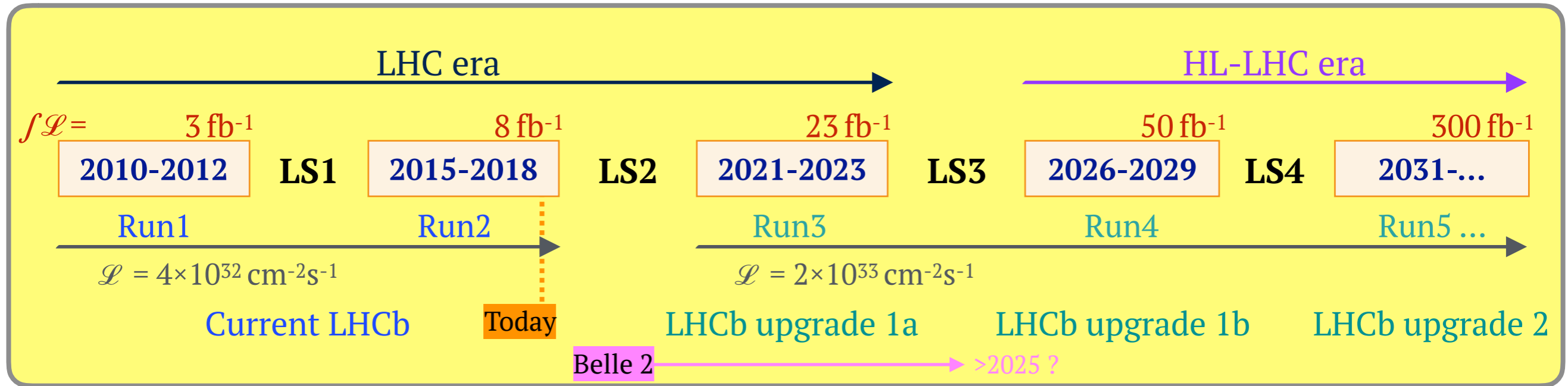
Simon Akar  
on behalf of the **LHCb Collaboration**

Laboratoire de Physique Nucléaire et de Hautes Energies IN2P3 – CNRS,  
Sorbonne Université et Université Denis Diderot



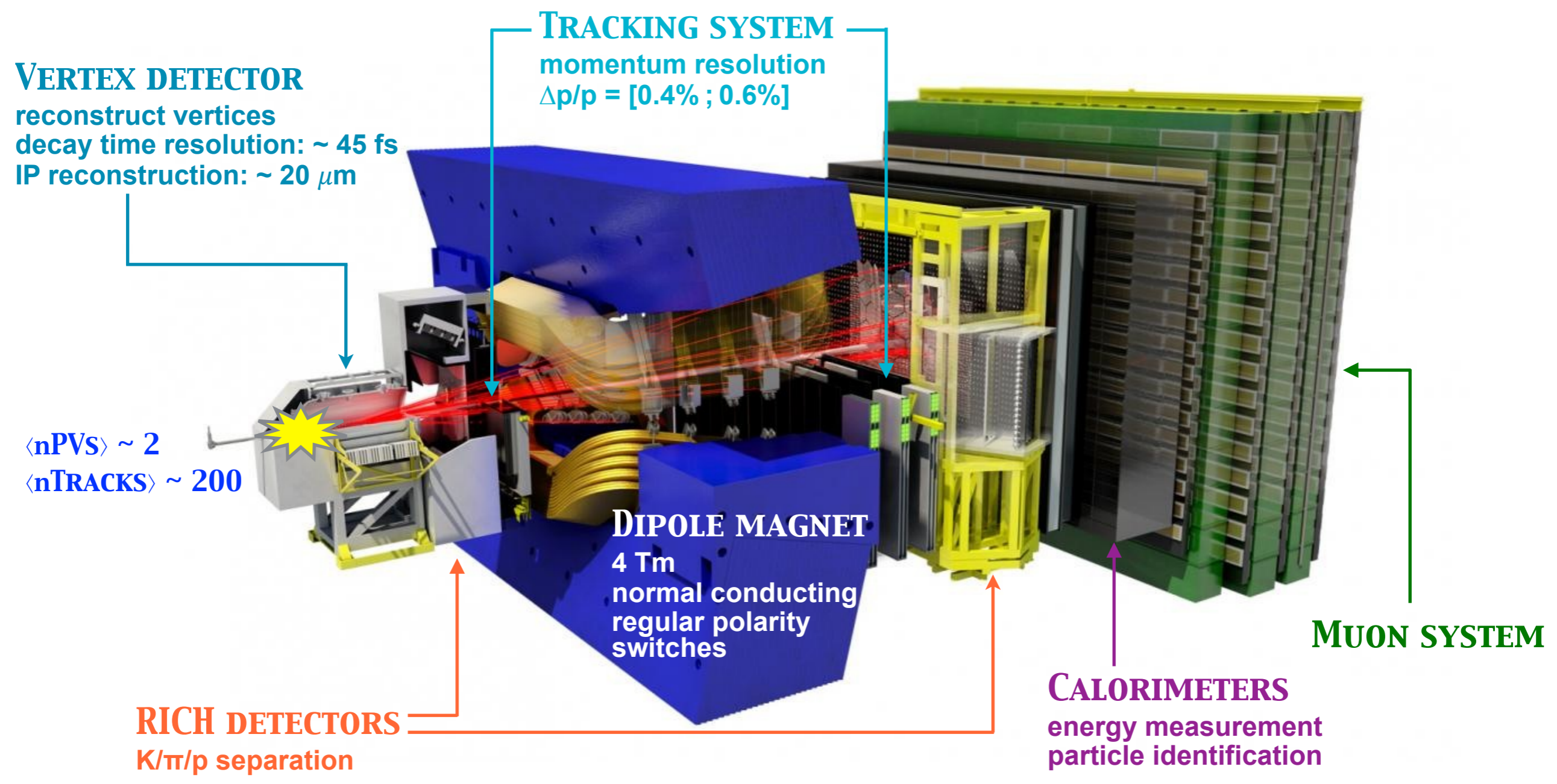
- **CKM mechanism introduces  $CP$  violation and neutral meson mixing phenomena**
  - ▶ The presence of new heavy particles exchanged in virtual loops could introduce additional phases altering the corresponding measurements
  - ▶ Constraining these phases put stringent limits on a large range of NP models
- **$CP$  violation is needed to explain baryon asymmetry in the Universe**
  - ▶ Discovered in 1964 in the kaons, 2004 in the  $B$  and each time awarded with Nobel Prizes
  - ▶ Still missing 10 orders of magnitudes!
- **Experimentally,  $CP$  violation observables accessed through ratios of measured quantities**
  - ▶ Cancellation of many experimental systematics
  - ▶ Flagship measurements for LHCb and Belle II





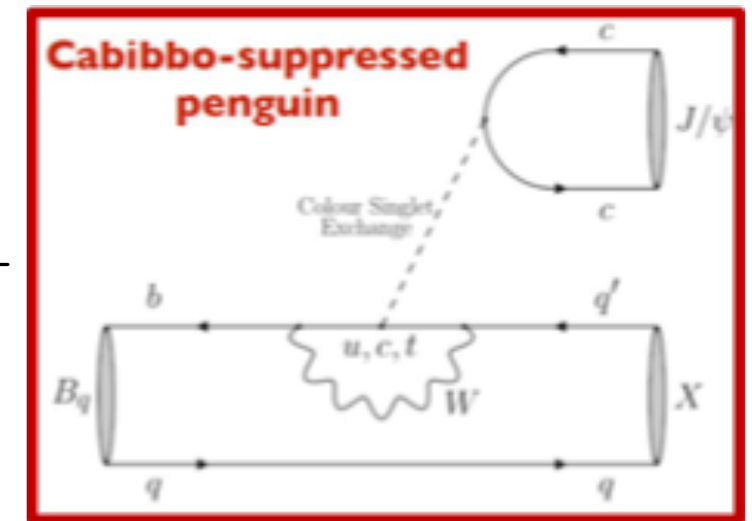
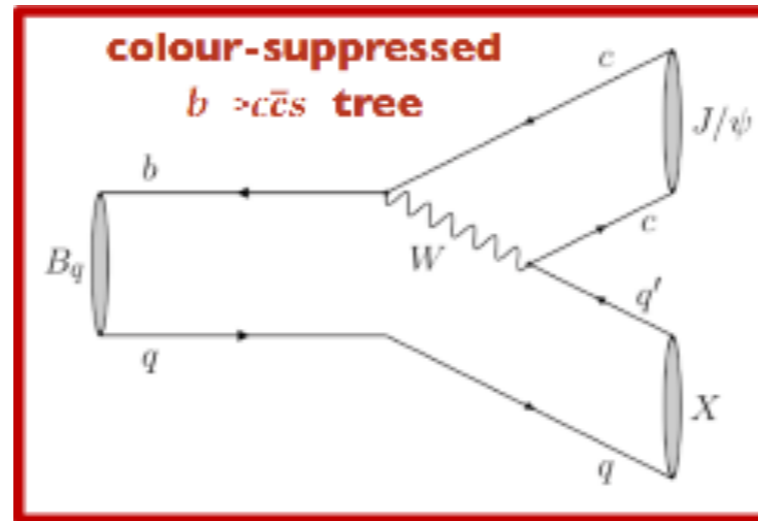
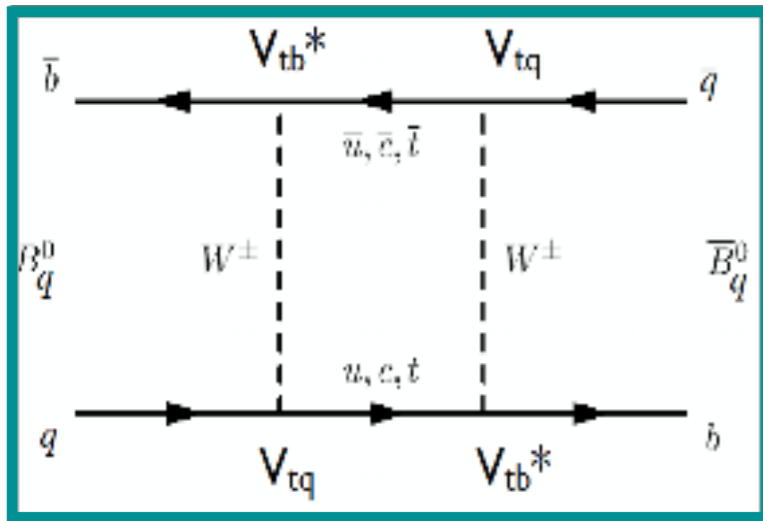
- LHCb is currently the main actor in flavour physics
- Belle 2 is entering the game
- LHCb may be the only large-scale flavour physics experiment operating in the HL-LHC era

- Forward General-Purpose Detector at the LHC
- ~30 % of heavy quark production cross-section with just 4% of solid angle



# Time-dependent CP violation

► CPV in interference between mixing and decay:



$$B_{H,L} = p B_{(s)}^{\pm} \pm q B_{(s)}^{-}$$

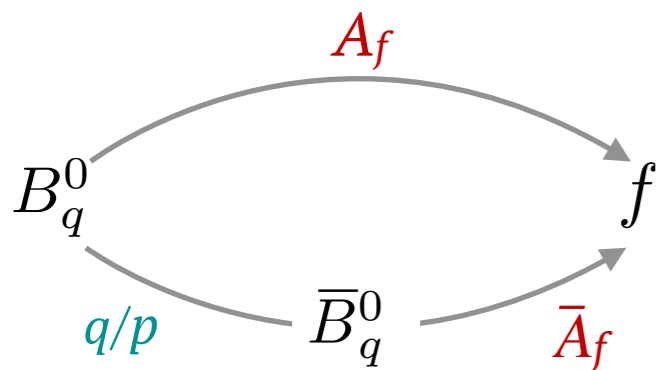
+ smaller weak exchange (E) and penguin annihilation (PA) diagrams

## Measurable CPV if

$$\arg(\lambda_f) = \arg\left(\frac{q}{p} \frac{\bar{A}_f}{A_f}\right) \neq 0$$

$$\arg(\lambda_{J/\psi K_S^0}) = 2\beta + \Delta\beta^{\text{peng}} + \Delta\beta^{\text{NP}}$$

$$\beta = \arg\left(\frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*}\right)$$



$$2\beta^{\text{eff}} = (47.48^{+2.26}_{-1.96})^\circ$$

[CKMFitter]

SM prediction from global fit

► **Measurement ingredients:**

$$A_{CP}(t) = \frac{\Gamma(\bar{B}_q^0(t) \rightarrow f) - \Gamma(B_q^0(t) \rightarrow f)}{\Gamma(\bar{B}_q^0(t) \rightarrow f) + \Gamma(B_q^0(t) \rightarrow f)} = \frac{\mathcal{S}_f \sin(\Delta m t) - \mathcal{C}_f \cos(\Delta m t)}{\cosh\left(\frac{\Delta\Gamma t}{2}\right) + \mathcal{A}_{\Delta\Gamma} \sinh\left(\frac{\Delta\Gamma t}{2}\right)}$$

► **Mixing parameters:**

$$\Delta m = m_H - m_L$$

$$\Delta\Gamma = \Gamma_L - \Gamma_H$$

► **CP observables:**

$$\mathcal{S}_f = \frac{2\Im(\lambda_f)}{1 + |\lambda_f|^2}, \quad \mathcal{C}_f = \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2}, \quad \mathcal{A}_{\Delta\Gamma} = -\frac{2\Re(\lambda_f)}{1 + |\lambda_f|^2}$$

$$\lambda_f = \eta_f \frac{q}{p} \frac{A(\bar{B}_q^0(t) \rightarrow f)}{A(B_q^0(t) \rightarrow f)} = \eta_f |\lambda_f| e^{i\phi_q}$$

$$\mathcal{S}_f = -\eta_f \frac{2|\lambda_f| \sin(\phi_q)}{1 + |\lambda_f|^2}, \quad \mathcal{A}_{\Delta\Gamma} = \eta_f \frac{2|\lambda_f| \cos(\phi_q)}{1 + |\lambda_f|^2}$$

# Time-dependent CP violation

► **Measurement ingredients:**

For  $B^0 \rightarrow J/\psi K_S^0$

$$A_{CP}(t) = \frac{\Gamma(\bar{B}_q^0(t) \rightarrow f) - \Gamma(B_q^0(t) \rightarrow f)}{\Gamma(\bar{B}_q^0(t) \rightarrow f) + \Gamma(B_q^0(t) \rightarrow f)} = \frac{\mathcal{S}_f \sin(\Delta m t) - \mathcal{C}_f \cos(\Delta m t)}{\cosh\left(\frac{\Delta\Gamma t}{2}\right) + \mathcal{A}_{\Delta\Gamma} \sinh\left(\frac{\Delta\Gamma t}{2}\right)}$$

► **Mixing parameters:**

$$\Delta m = m_H - m_L = 0.5065 \pm 0.0019 \text{ ps}^{-1} \quad [\text{HFLAV}]$$

$$\Delta\Gamma = \Gamma_L - \Gamma_H \propto (-0.002 \pm 0.010) \times \Gamma_d$$

► **CP observables:**

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$$A_{\text{meas}}(t) = \mathcal{A}_{CP}(t) \times D_{\text{res}} \times D_{\text{tag}} \pm \mathcal{A}_{\text{det/prod}}$$



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▶ **Decay time resolution: ~45 fs**

$$D_{\text{res}} = e^{-\frac{\Delta m^2 \sigma_t^2}{2}}$$

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$$D_{\text{res}} = e^{-\frac{\Delta m^2 \sigma_t^2}{2}}$$

► **Tagging dilution:**

$$D_{\text{tag}} = (1 - 2\omega)$$

- Initial B flavor efficiency:  $\epsilon_{\text{tag}}$

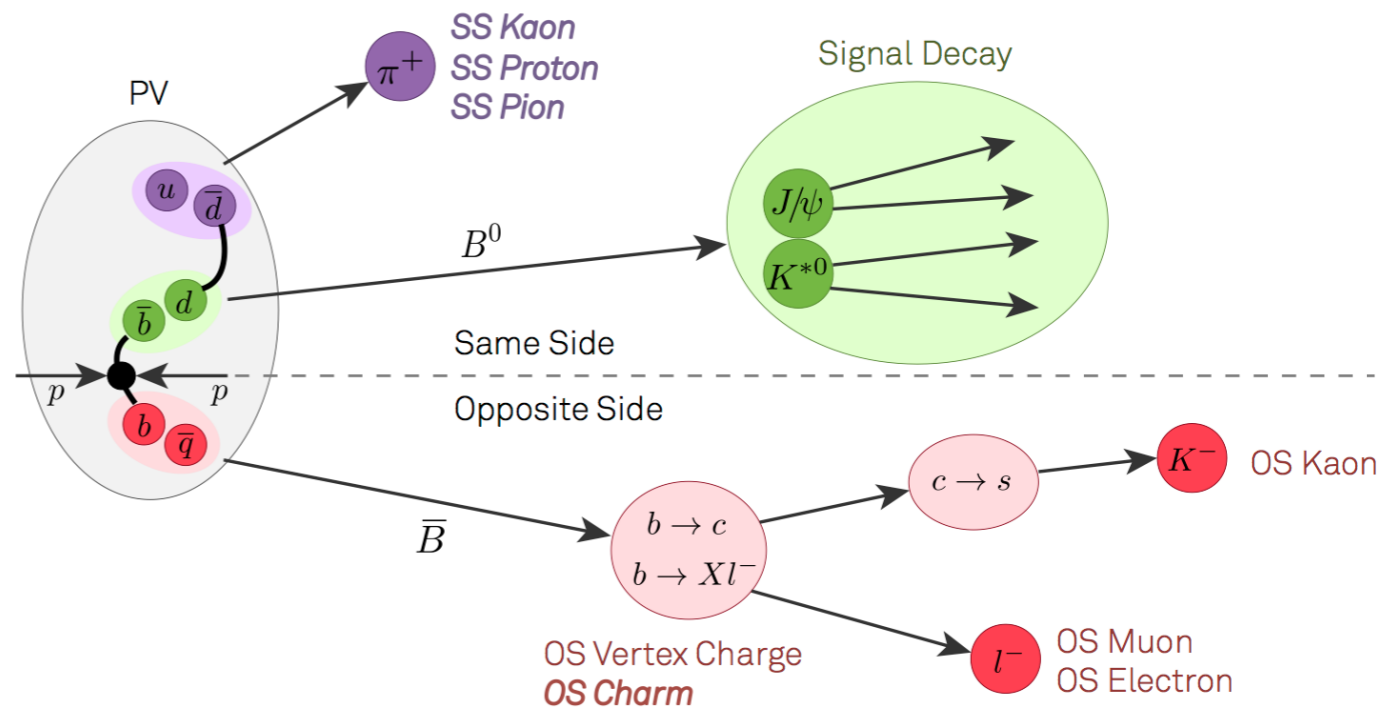
- Wrong tag rate:  $\omega$

- Effective tagging power:

$$\epsilon_{\text{eff}} = \epsilon_{\text{tag}}(1 - 2\omega)^2$$

$$\sigma^{\text{stat}}(CPV) \propto \frac{1}{\sqrt{\epsilon_{\text{eff}} N}}$$

**Same side (SS):** exploit the charge of the **fragmentation particles**



**Opposite side (OS):** exploit the charge of the particles produced from the **other b-hadron**

► Measurement ingredients:

$$A_{\text{meas}}(t) = A_{CP}(t) \times D_{\text{res}} \times D_{\text{tag}} \pm A_{\text{det/prod}}$$

► **Decay time resolution: ~45 fs**

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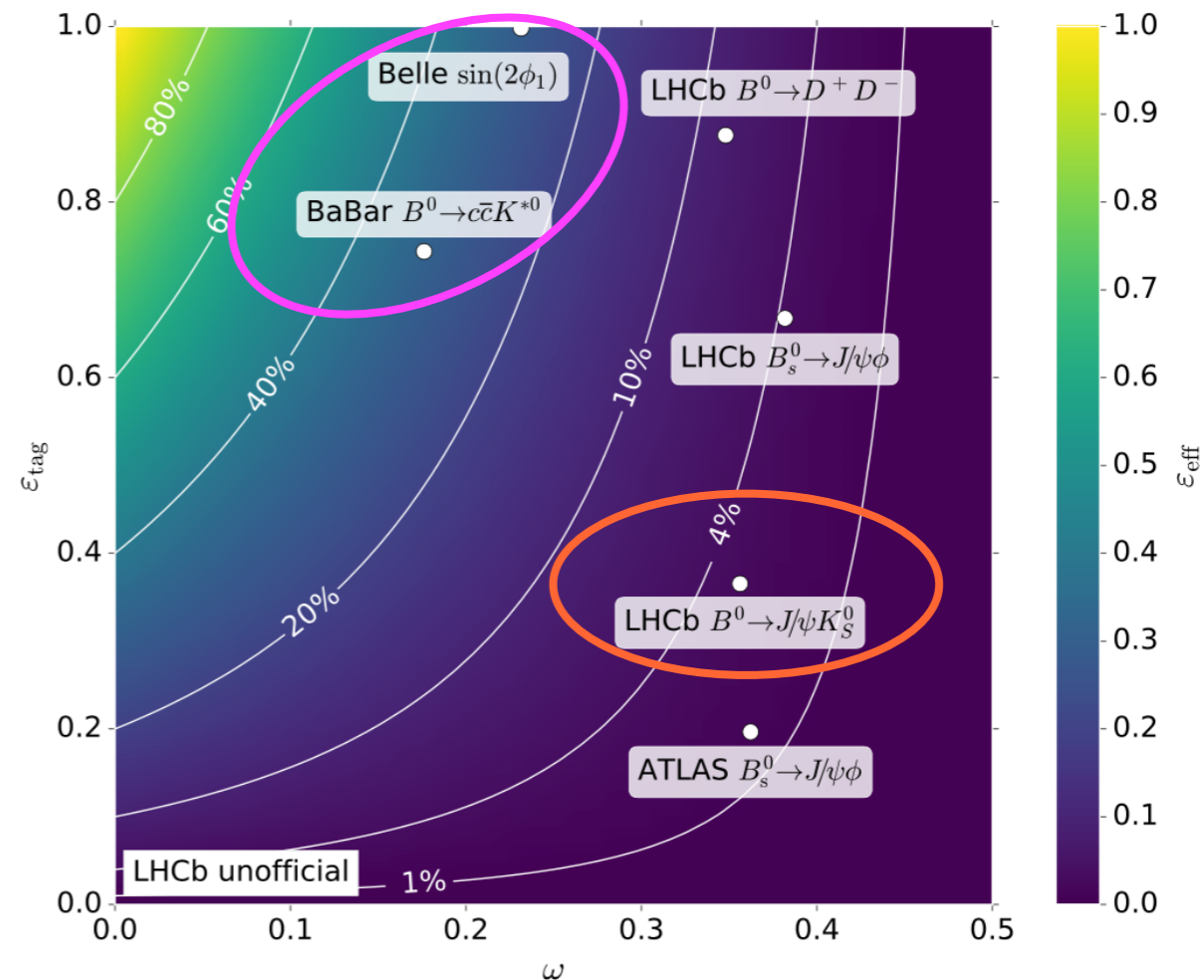
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[CERN-THESIS-2016-152]

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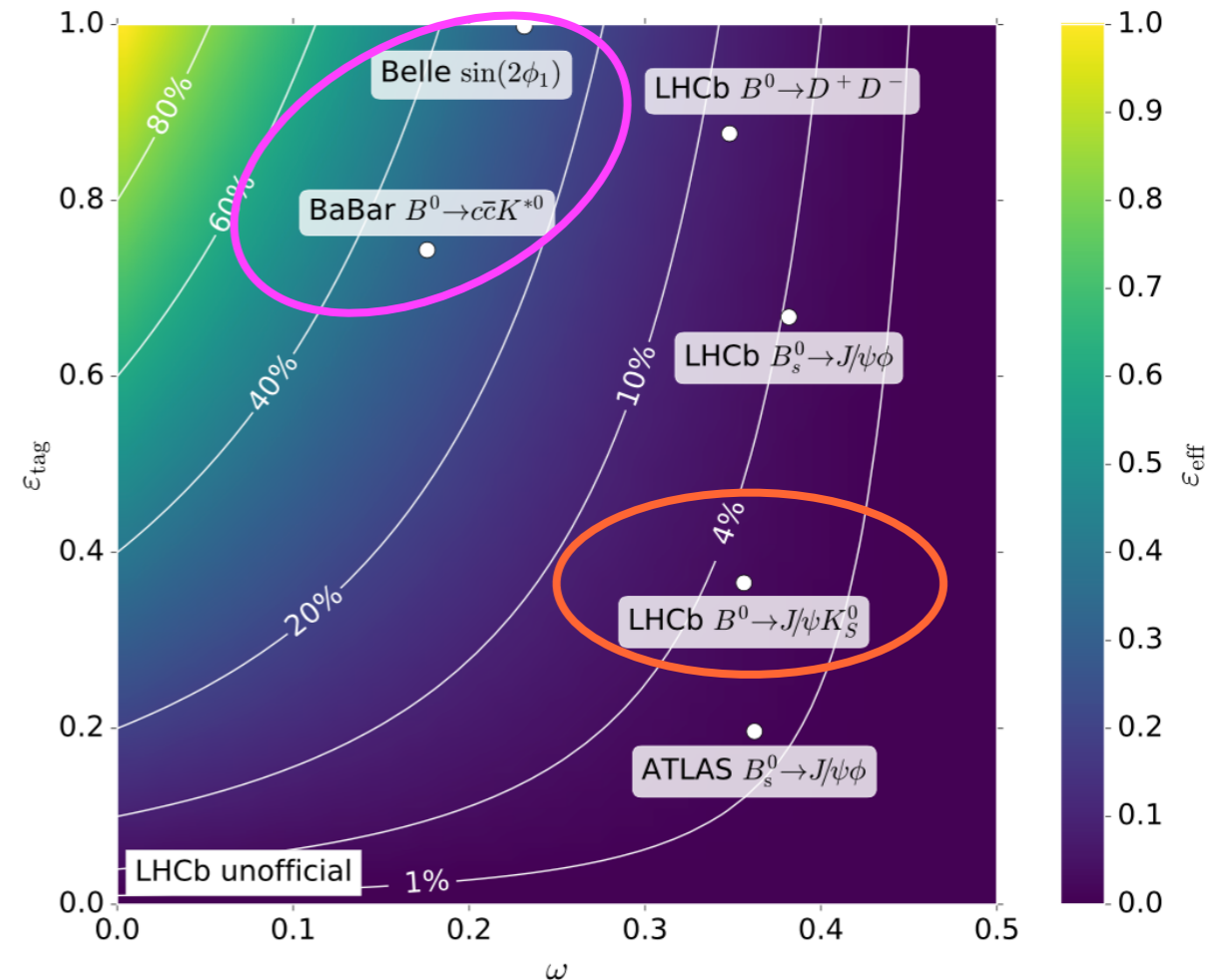
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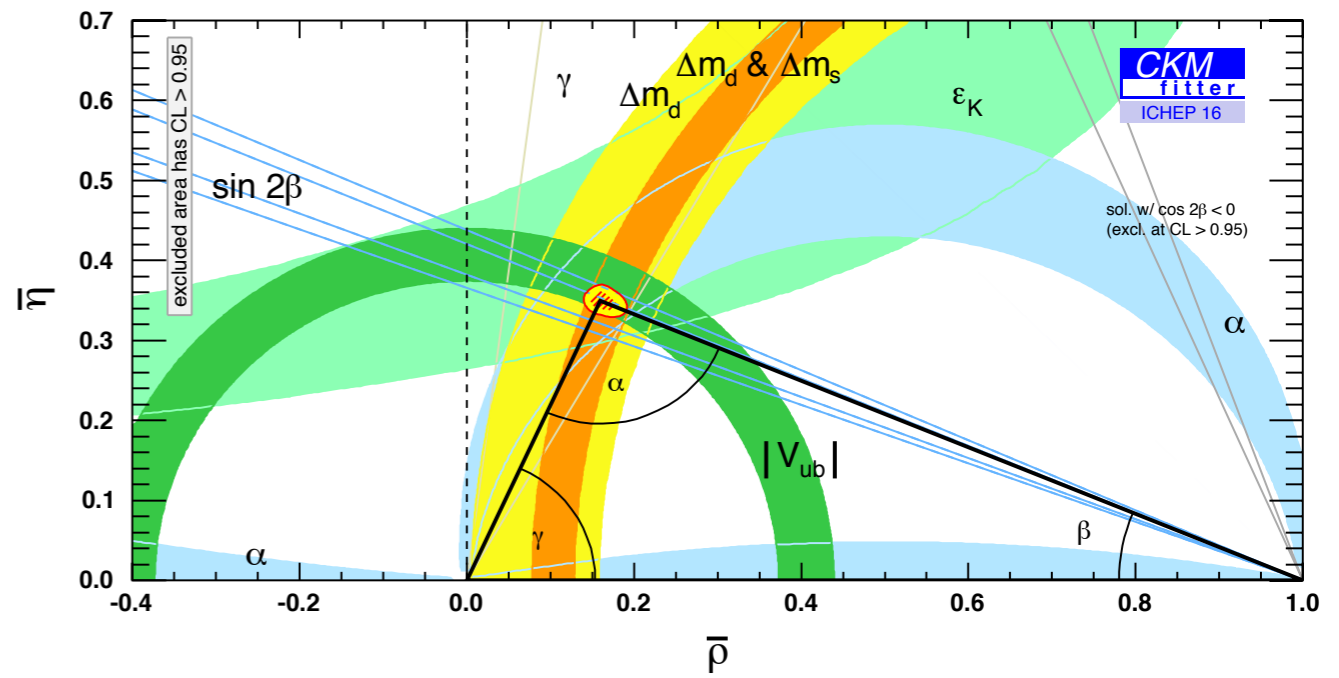
$$\sigma^{\text{stat}}(CPV) \propto \frac{1}{\sqrt{\epsilon_{\text{eff}} N}}$$

- Also need to account for detection/production asymmetries, acceptance effects on time and angular variables ( $P \rightarrow VV$ ), ...



[CERN-THESIS-2016-152]

- ▶  $\beta$  is the most precisely measured angle of the Unitarity triangle
- ▶ CPV measurement in time-dependent decay rates of  $b \rightarrow c\bar{c}s$  transitions



$$A_{CP}(t) \stackrel{\Delta\Gamma \approx 0}{\approx} S_{c\bar{c}s} \sin(\Delta m_d t) - C_{c\bar{c}s} \cos(\Delta m_d t)$$

$S_{c\bar{c}s} \approx \sin(2\beta)$  if no direct CPV and neglecting higher order contributions

$C_{c\bar{c}s} \approx 0$  if no direct CPV (good enough approx. given current precision)

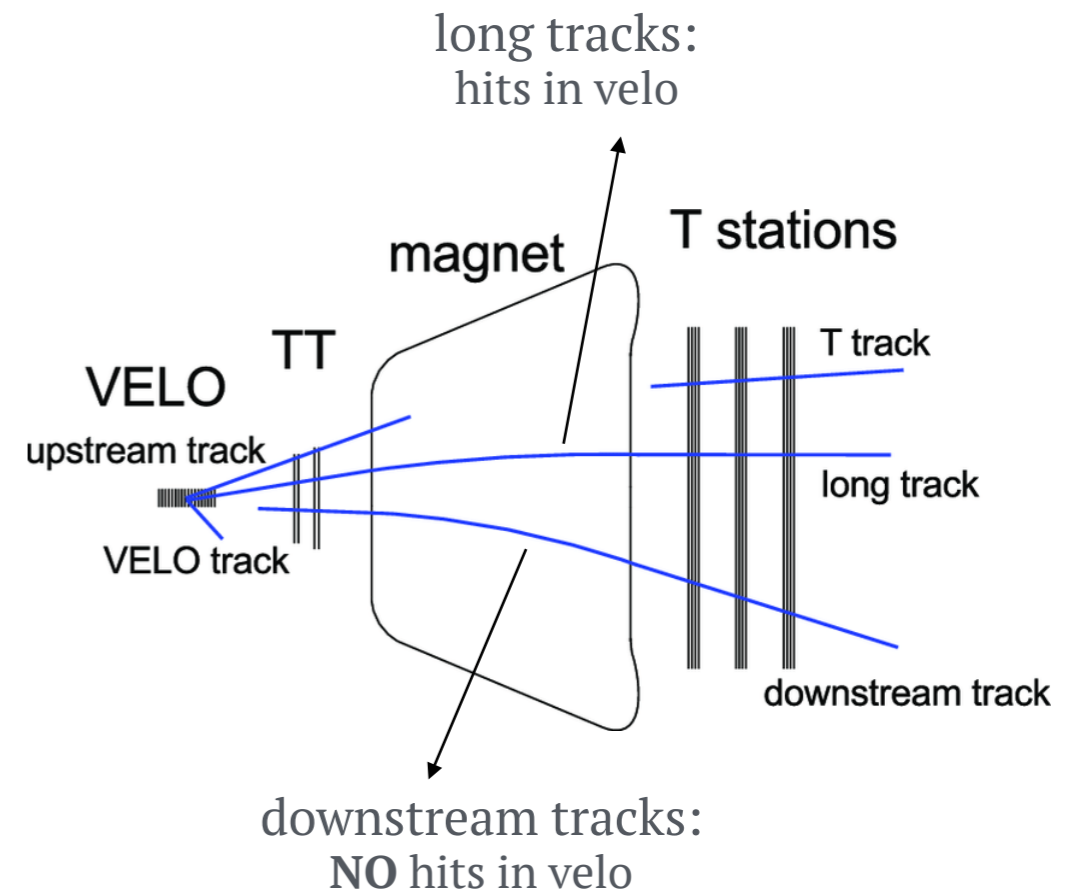
$$\sin(2\beta_{c\bar{c}s}^{SM}) = 0.740^{+0.020}_{-0.025} \quad [CKMFitter]$$

$$\sin(2\beta_{c\bar{c}s}^{SM}) = 0.724 \pm 0.028 \quad [UTFit]$$

$$\sin(2\beta_{c\bar{c}s}) = 0.691 \pm 0.017 \quad [HFLAV]$$

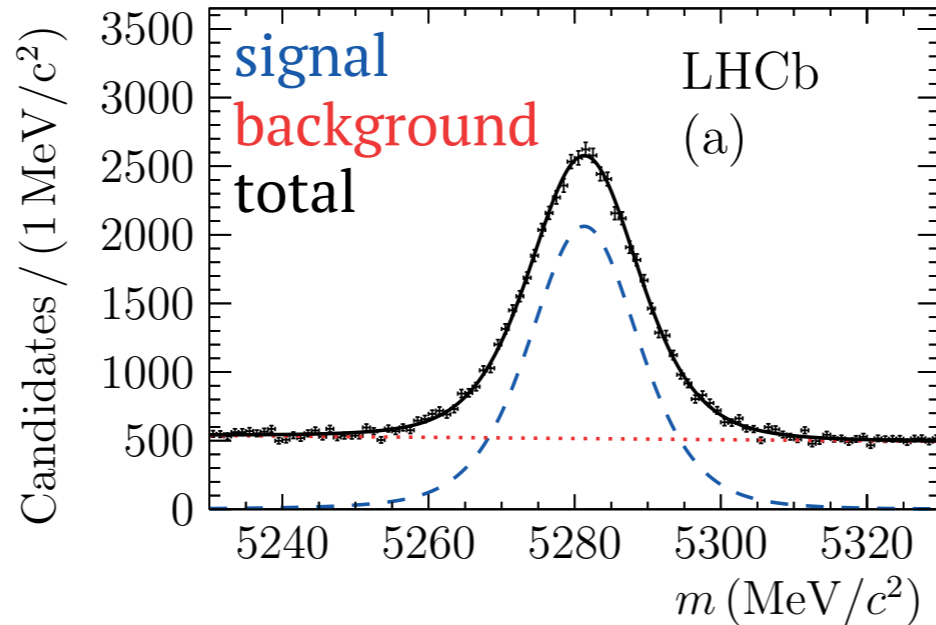
- **New physics contributions, if present, will be small!**
- **Controlling contributions from penguin topologies becomes mandatory**

- ▶  $B^0 \rightarrow J/\psi [\mu^+\mu^-] K_S^0$ : (golden mode)
  - ▶ Using 2011+2012 (3 fb<sup>-1</sup>) data
  - ▶ Cut-based selection
  - ▶ **DD & LL** reconstructed  $K_S^0 \rightarrow \pi^+\pi^-$ 
    - $\langle \sigma(t)_{DD} \rangle > \langle \sigma(t)_{LL} \rangle$
  - ▶ **OS and SS $\pi$  taggers:  $\epsilon_{\text{eff}} \sim 3\%$**
  - ▶ **~42000 tagged candidates**
  
- ▶ **Simultaneous fit in 24 categories:**
  - (2011,2012) x (SS $\pi$ ,OS,OS&SS $\pi$ ) x (DD,LL) x (AU,EB)
  - signal & background components
  - *CP* parameters S and C free
  - $\Delta m$  constraint to  $0.5100 \pm 0.0030$  ps



►  $B^0 \rightarrow J/\psi [\mu^+\mu^-] K_S^0$ : (golden mode)

► **Fit results:**



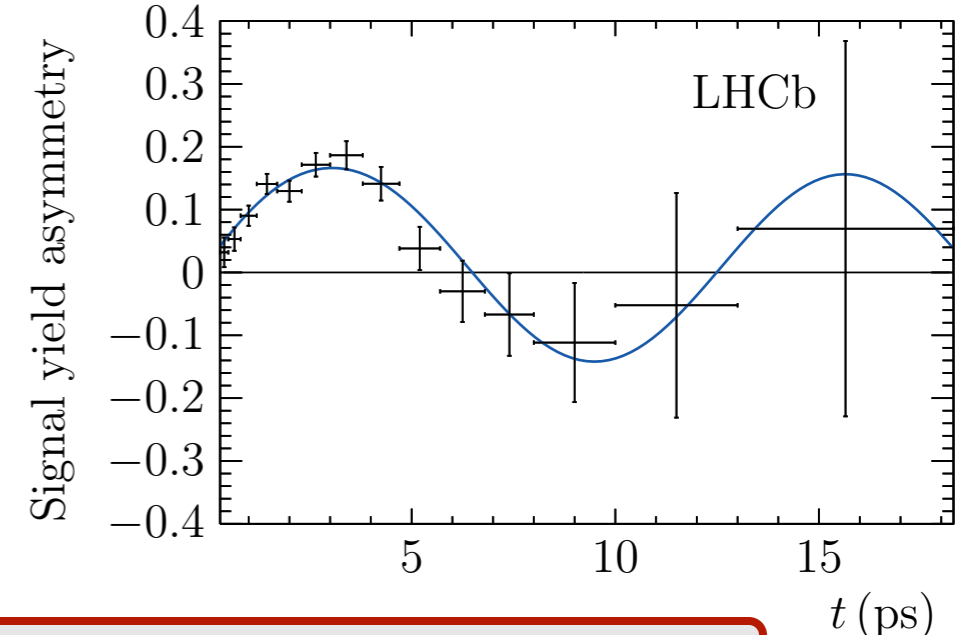
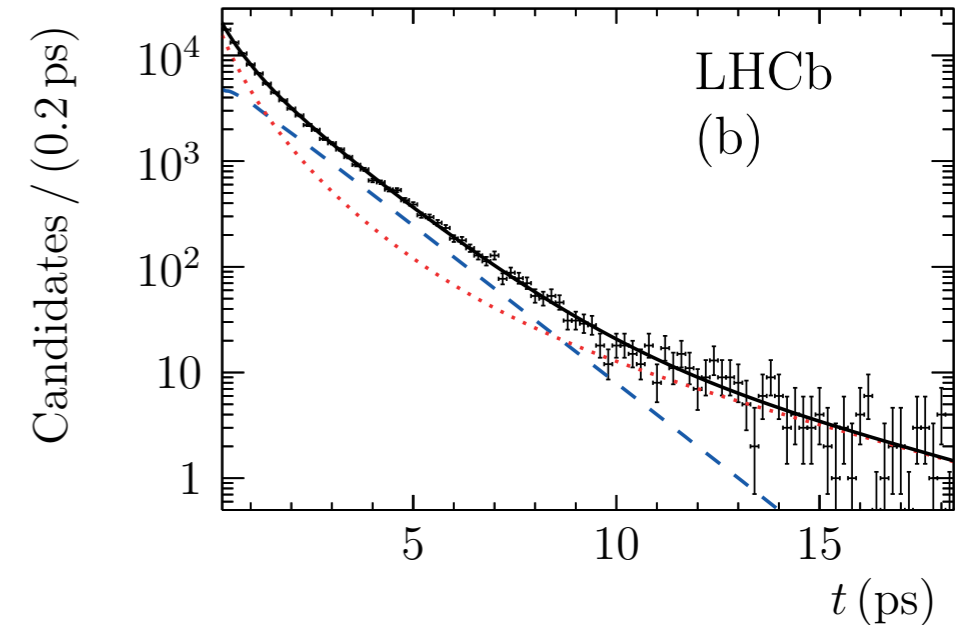
$$S = 0.731 \pm 0.035(\text{stat}) \pm 0.020(\text{syst})$$

$$C = -0.038 \pm 0.032(\text{stat}) \pm 0.005(\text{syst})$$

$$\rho(S, C) = 0.483$$

► **Main systematics:**

- **S**: Background Tagging Asymmetry  
→ expect to scale with more data
- **C**:  $\Delta m$



**Close to precision of  $B$ -Factories and statistically limited**

▶  $B^0 \rightarrow J/\psi [e^+e^-] K_S^0$  &  $B^0 \rightarrow \psi(2S) [\mu^+\mu^-] K_S^0$ :

▶ Using 2011+2012 (3 fb<sup>-1</sup>) data

▶ BDT in selection

▶ DD & LL reconstructed  $K_S^0$

▶ OS and SS $\pi$ BDT + SS $p$  taggers:

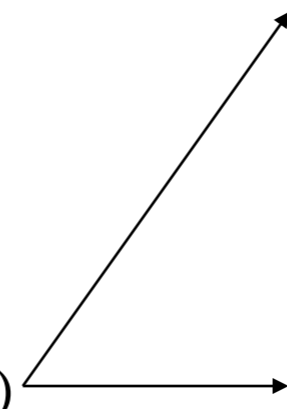
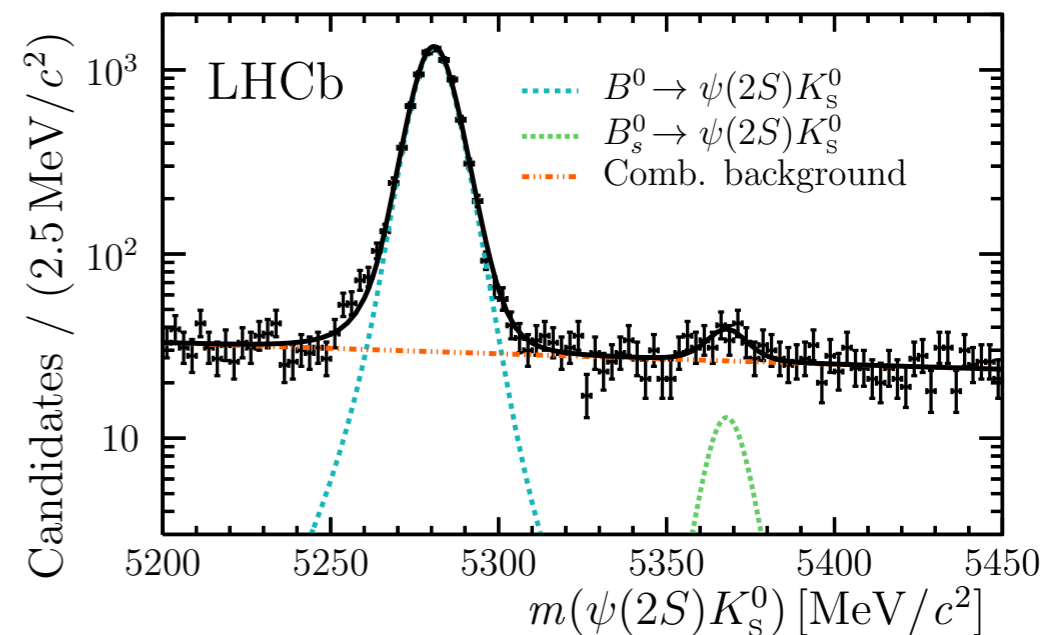
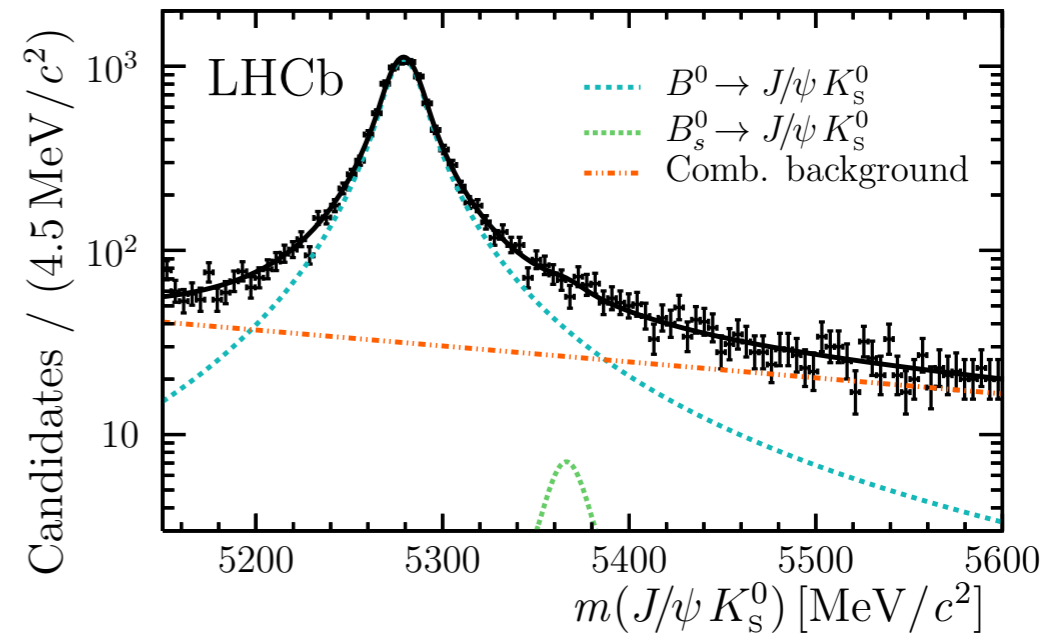
-  $\epsilon_{\text{eff}} \sim 6\%$  ( $B^0 \rightarrow J/\psi [e^+e^-] K_S^0$ )

-  $\epsilon_{\text{eff}} \sim 3.4\%$  ( $B^0 \rightarrow \psi(2S) [\mu^+\mu^-] K_S^0$ )

▶ ~10600 + 8000 tagged candidates

▶ Fit strategy:

- first fit invariant mass (obtain sWeights)
- simultaneously fit decay time of both samples (next slide)
- $CP$  parameters S and C + acceptance parameters free





►  $B^0 \rightarrow J/\psi [e^+e^-] K_S^0$  &  $B^0 \rightarrow \psi(2S) [\mu^+\mu^-] K_S^0$ :

► Decay-time fit results

$$S_{J/\psi K_S^0} = 0.83 \pm 0.08(\text{stat}) \pm 0.01(\text{syst})$$

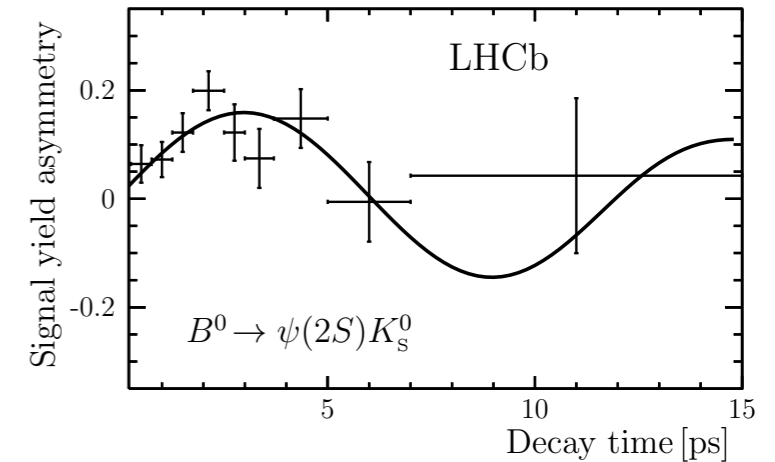
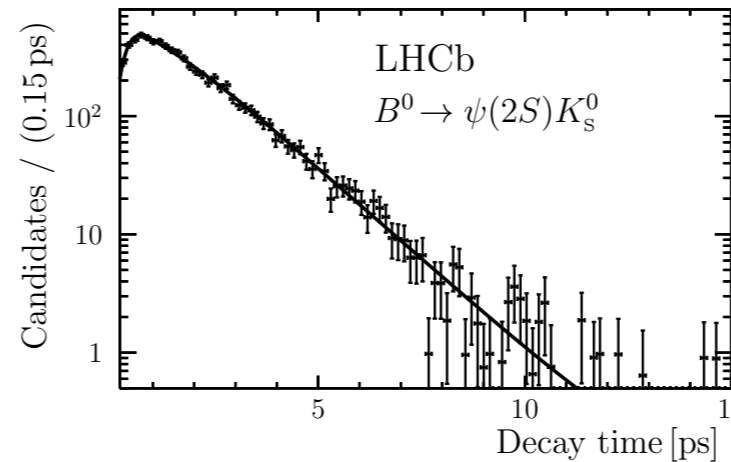
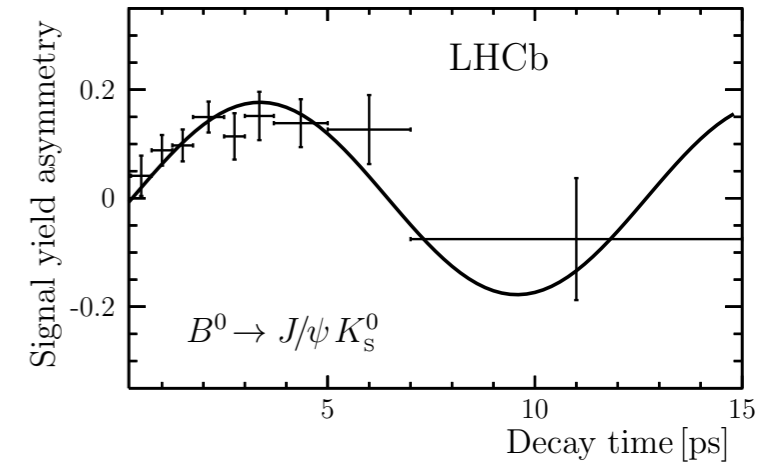
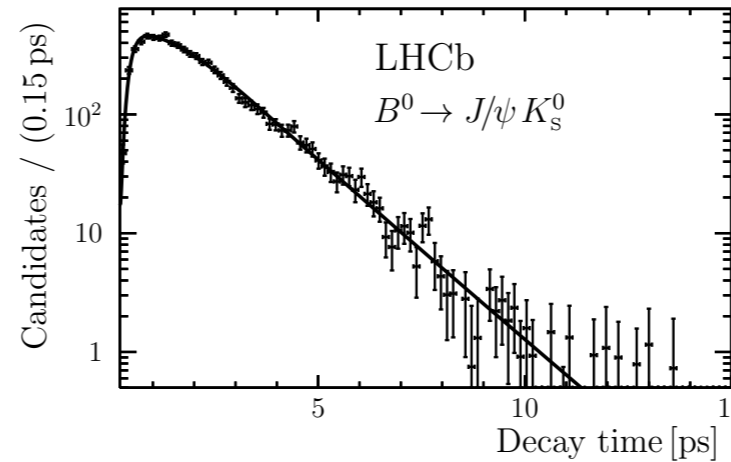
$$C_{J/\psi K_S^0} = 0.12 \pm 0.07(\text{stat}) \pm 0.02(\text{syst})$$

$$\rho(S, C)_{J/\psi K_S^0} = 0.46$$

$$S_{\psi(2S) K_S^0} = 0.84 \pm 0.10(\text{stat}) \pm 0.01(\text{syst})$$

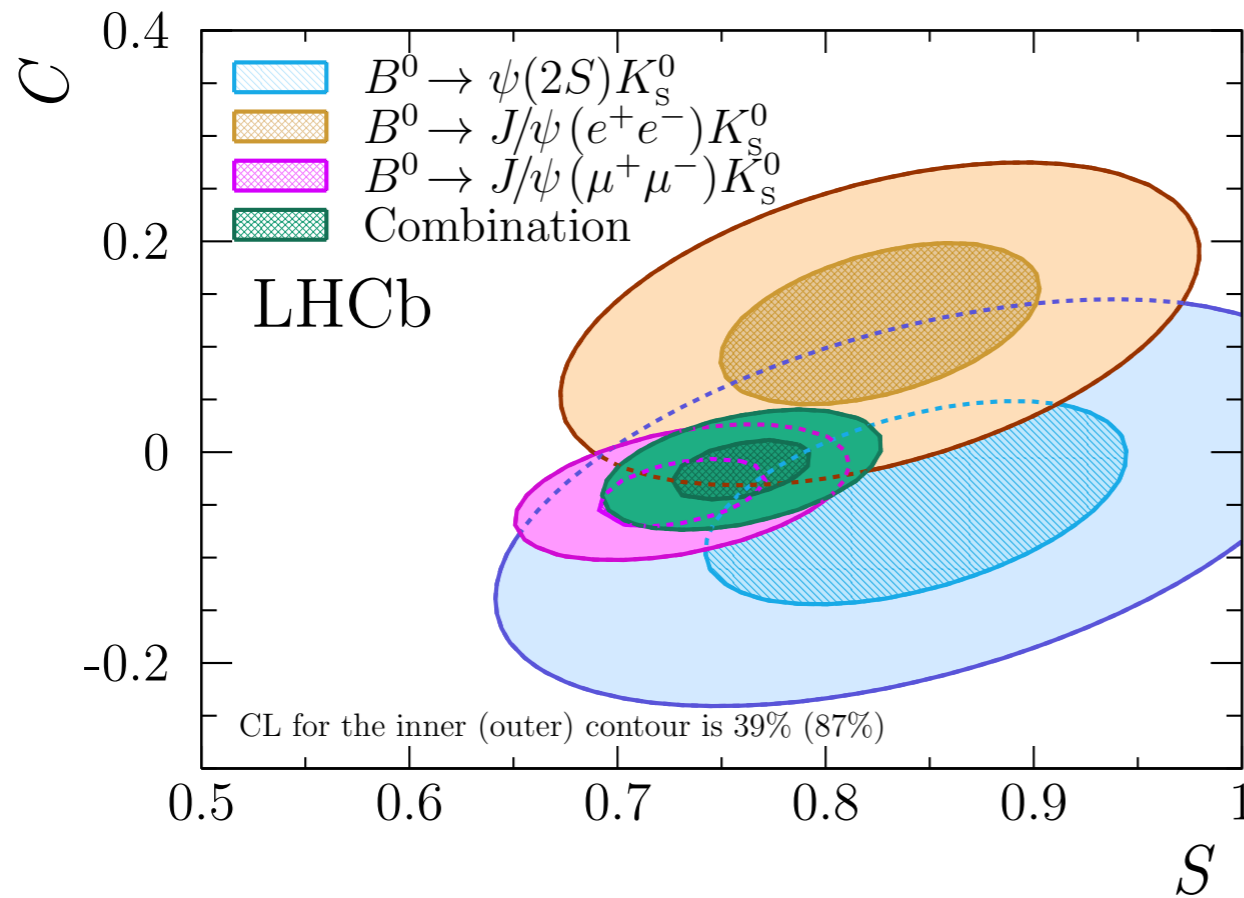
$$C_{\psi(2S) K_S^0} = -0.05 \pm 0.10(\text{stat}) \pm 0.01(\text{syst})$$

$$\rho(S, C)_{\psi(2S) K_S^0} = 0.48$$



▶  $B^0 \rightarrow J/\psi [e^+e^-] K_S^0$  &  $B^0 \rightarrow \psi(2S) [\mu^+\mu^-] K_S^0$ :

▶ **Combination + golden mode ( $B^0 \rightarrow J/\psi [\mu^+\mu^-] K_S^0$ ) results**

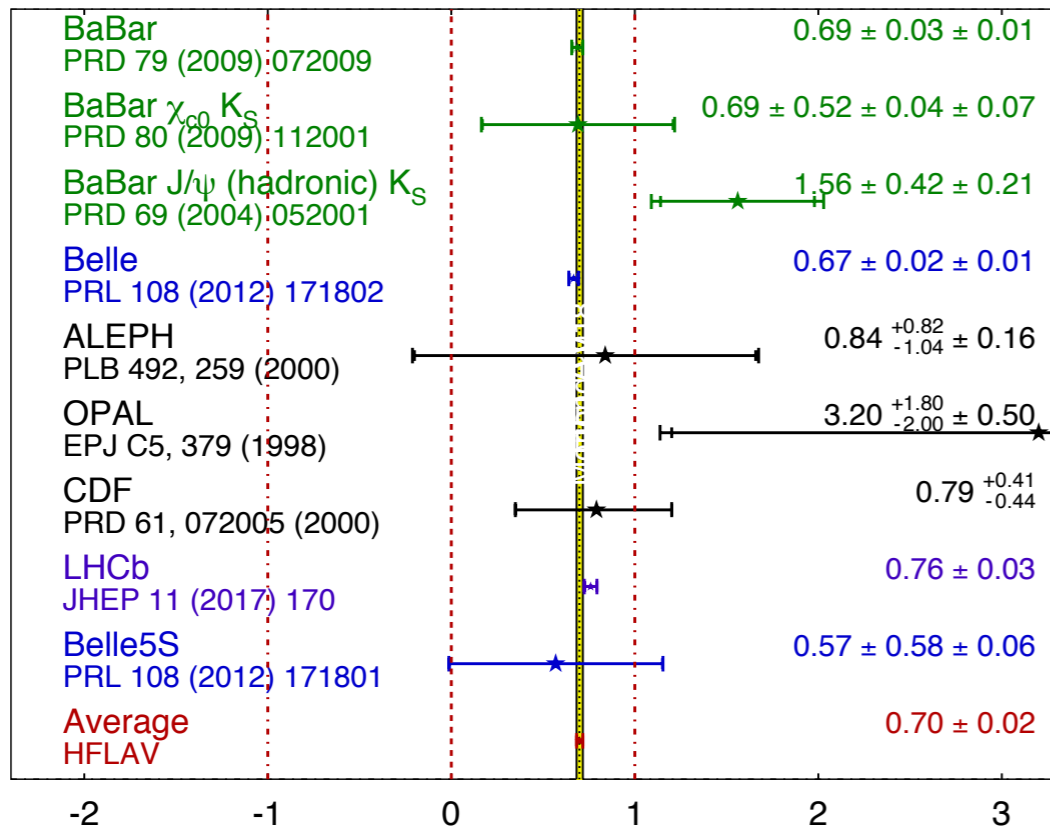


$$S_{[c\bar{c}]K_S^0} = 0.760 \pm 0.034$$

$$C_{[c\bar{c}]K_S^0} = -0.017 \pm 0.029$$

$J/\psi [e^+e^-]$  &  $\psi(2S) [\mu^+\mu^-]$  modes provide **additional ~15%** on the overall LHCb precision

$\sin(2\beta) \equiv \sin(2\phi_1)$  **HFLAV**  
Moriond 2018  
PRELIMINARY

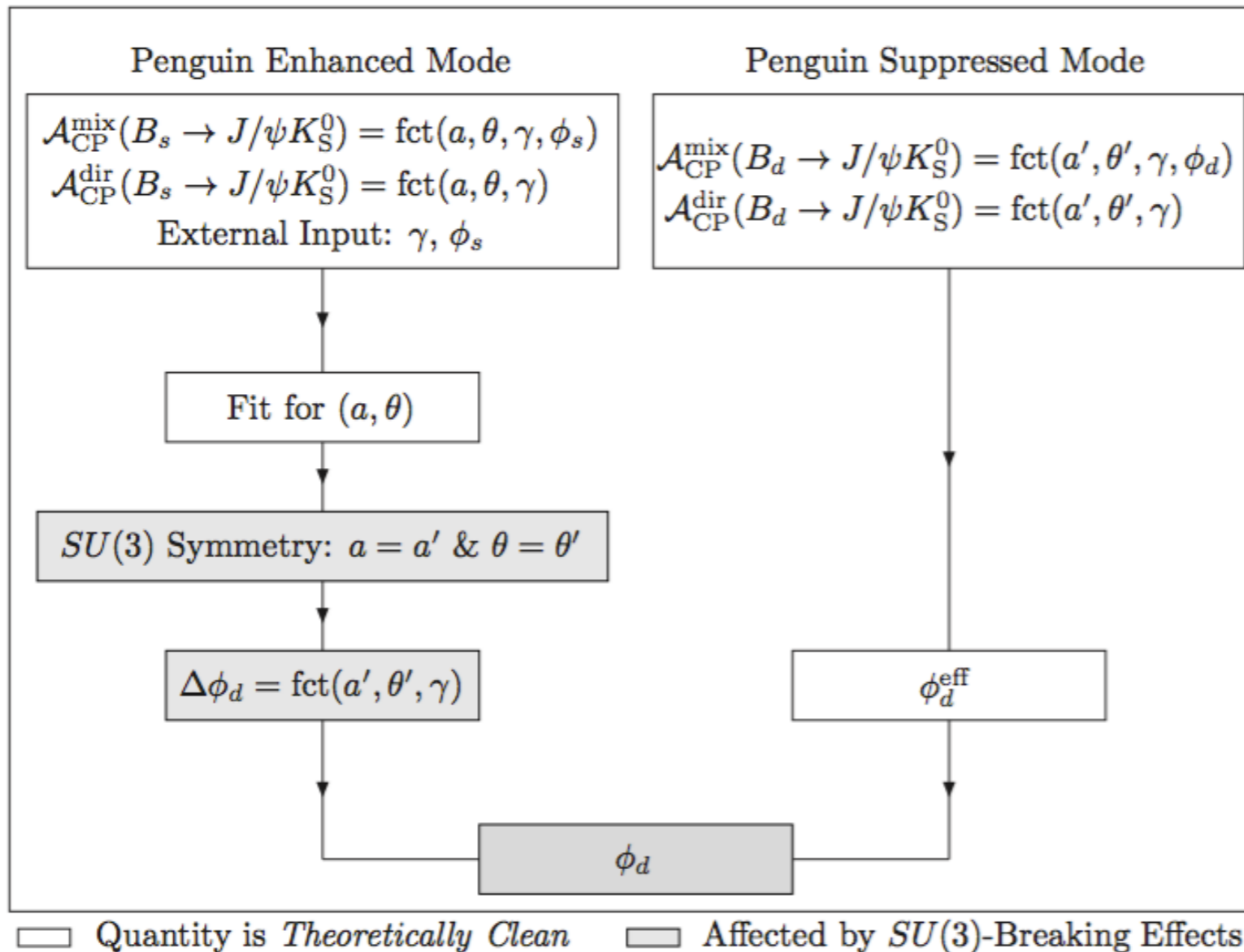


$\sigma_{\text{stat}}(\mathcal{S}(J/\psi K_S^0))$	now	50 $\text{ab}^{-1}$	
Belle/II	0.029	0.005	
	now	50 $\text{fb}^{-1}$	300 $\text{fb}^{-1}$
LHCb	0.035	0.006	0.003

- ▶ **LHCb achieves similar precision wrt  $B$ -Factories**
- ▶ **Belle 2 and LHCb Upgrades target significantly improved sensitivities with mostly uncorrelated systematics**  
→ **mandatory to control penguin pollution!**

► **Strategy:**

- use U-spin and SU(3) related modes, where penguin not suppressed  
[S. Faller, R. Fleischer, M. Jung, T. Mannel, PRD79:014030,2009]
- the decay mode  $B_s^0 \rightarrow J/\psi K_S^0$  can be used to control  $\Delta\phi_d \propto \Delta\beta^{\text{peng}}$ :



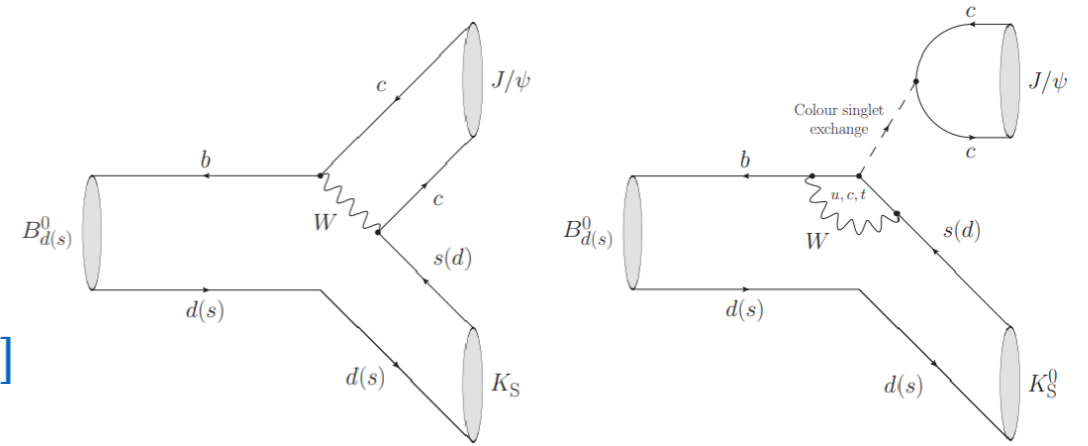
►  $B_s^0 \rightarrow J/\psi K_S^0$ :

- same topology as  $B^0 \rightarrow J/\psi K_S^0$
- LHCb performed first **flavor-tagged time-dependent** analysis: [LHCb, *JHEP* 06 (2015) 131]

$$\mathcal{A}_{\Delta\Gamma}(B_s^0 \rightarrow J/\psi K_S^0) = +0.49_{-0.65}^{+0.77}(\text{stat}) \pm 0.06(\text{syst})$$

$$\mathcal{C}(B_s^0 \rightarrow J/\psi K_S^0) = -0.28 \pm 0.41(\text{stat}) \pm 0.08(\text{syst})$$

$$\mathcal{S}(B_s^0 \rightarrow J/\psi K_S^0) = -0.08 \pm 0.40(\text{stat}) \pm 0.08(\text{syst})$$

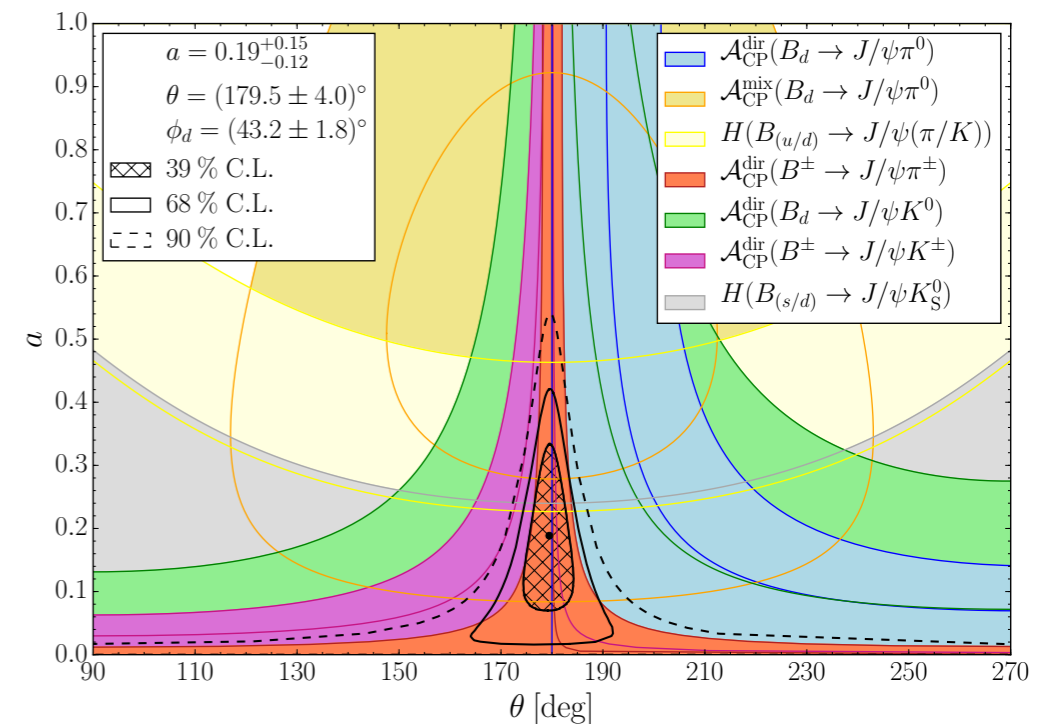


⇒ Successful proof of concept waiting for more statistics

- Using information from  $B^0 \rightarrow J/\psi \pi^0$  [Belle, *PRL* 93, 261801] together with inputs from  $B^+ \rightarrow J/\psi K^+$  and  $B^+ \rightarrow J/\psi \pi^+$  [LHCb *JHEP* 03 (2017) 036] [LHCb, *PRD* 95 (2017) 052005] translates into penguin shift on  $\beta$ :

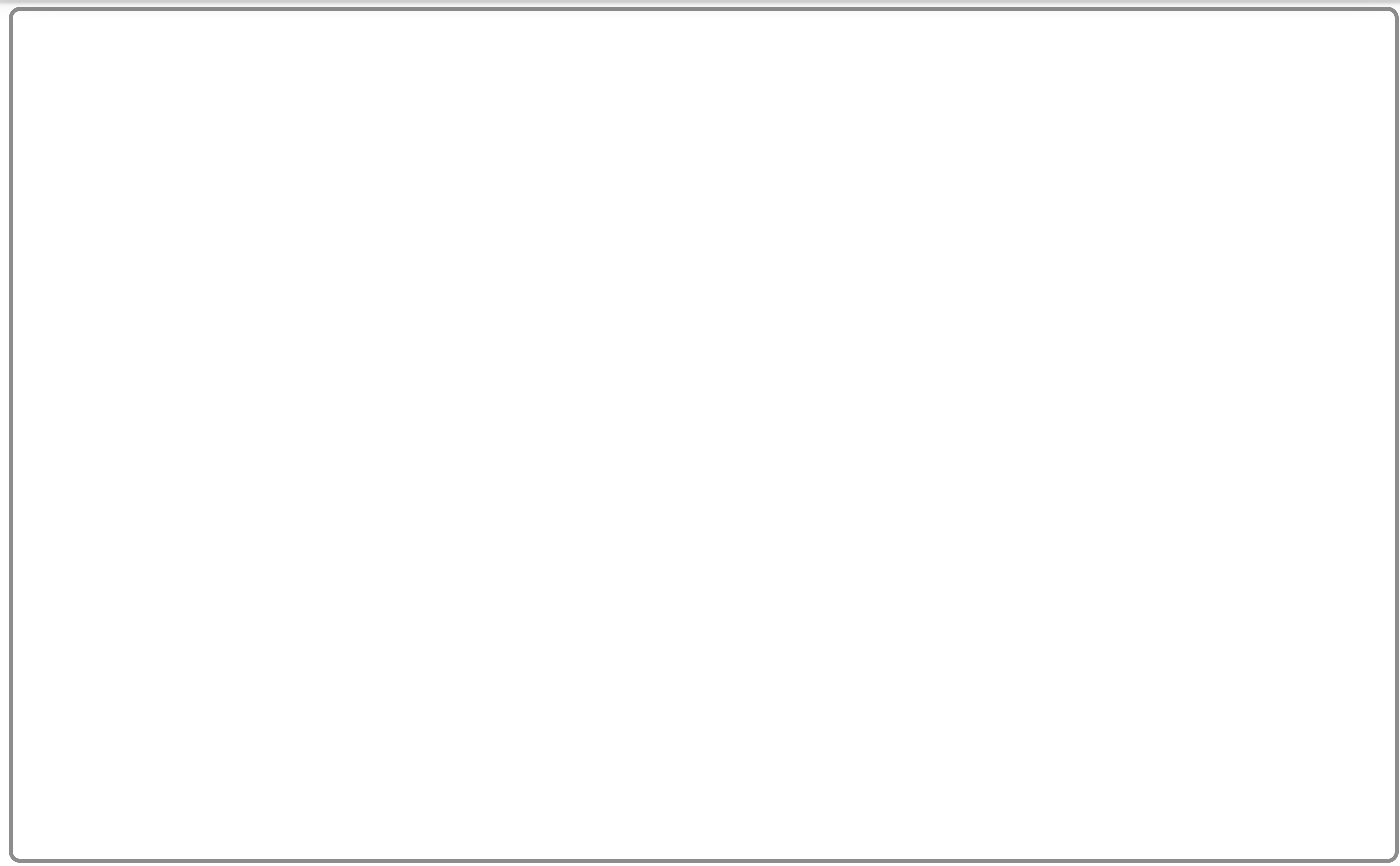
$$\Delta\beta^{\text{peng}} = (-1.10_{-0.85}^{+0.70})^\circ$$

same order of uncertainties on  $2\beta$   
 ⇒ needs to be improved with more data!



[De Bruyn, Fleischer, *JHEP* 1503 (2015) 145]

- $\beta$  is and will remain the most precisely measured angle of the unitarity triangle
- Controlling higher order corrections becomes mandatory:
  - penguin pollution to be determined with increased precision in U-spin and SU(3)-related modes both by LHCb and Belle II
- For the future:
  - Measurements statistically dominated
    - look forward to Run-2 updates (and LHCb-upgrade)



►  $B^0 \rightarrow J/\psi [e^+e^-] K_S^0$  &  $B^0 \rightarrow \psi(2S) [\mu^+\mu^-] K_S^0$ :

► Systematics

Source	$B^0 \rightarrow J/\psi K_S^0$		$B^0 \rightarrow \psi(2S) K_S^0$	
	$\sigma_S$	$\sigma_C$	$\sigma_S$	$\sigma_C$
$\Delta\Gamma$	0.003	0.007	0.007	0.003
$\Delta m$	0.004	0.004	0.004	0.004
Production asymmetry	0.004	0.009	0.007	0.005
Tagging calibration	0.002	0.005	0.005	0.002
Decay-time bias	0.006	0.006	0.006	0.004
$\sigma_t$ scaling	0.003	0.005	0.002	0.002
Decay-time efficiency	0.006	0.004	0.006	0.004
Total	0.011	0.016	0.014	0.010

$$S_{J/\psi K_S^0} = 0.83 \pm 0.08(\text{stat}) \pm 0.01(\text{syst})$$

$$C_{J/\psi K_S^0} = 0.12 \pm 0.07(\text{stat}) \pm 0.02(\text{syst})$$

$$\rho(S, C)_{J/\psi K_S^0} = 0.46$$

$$S_{\psi(2S) K_S^0} = 0.84 \pm 0.10(\text{stat}) \pm 0.01(\text{syst})$$

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$$\rho(S, C)_{\psi(2S) K_S^0} = 0.48$$



- ▶ **Tagging Efficiency**: fraction of tagged events

$$\epsilon_{\text{tag}} = \frac{N_{\text{wrong}} + N_{\text{correct}}}{N_{\text{wrong}} + N_{\text{correct}} + N_{\text{untagged}}}$$

- Correlated with the transverse momentum of the signal  $B$

- ▶ **Mistag fraction**: fraction of events with wrong tag decision

$$\omega = \frac{N_{\text{wrong}}}{N_{\text{wrong}} + N_{\text{correct}}}$$

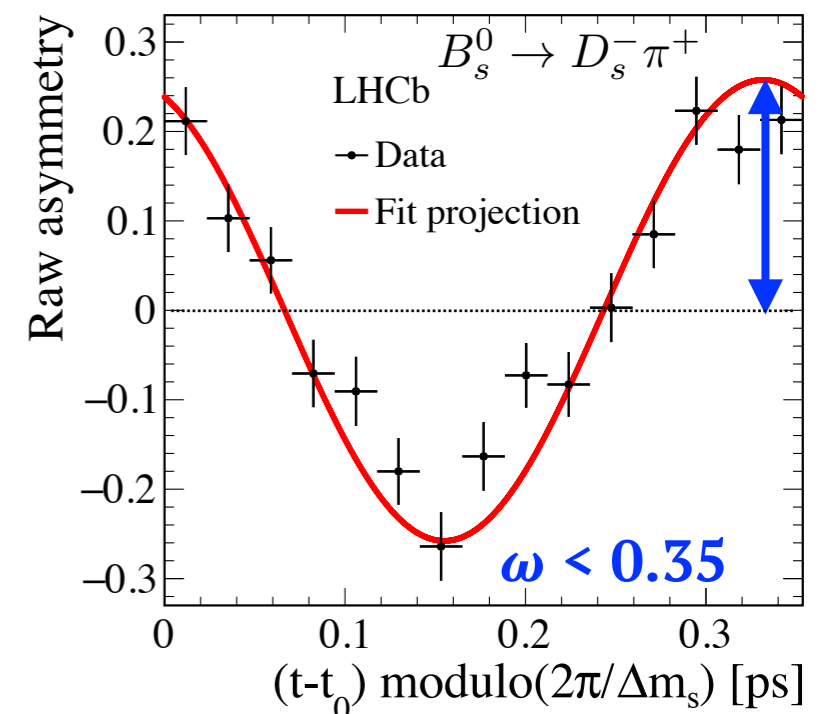
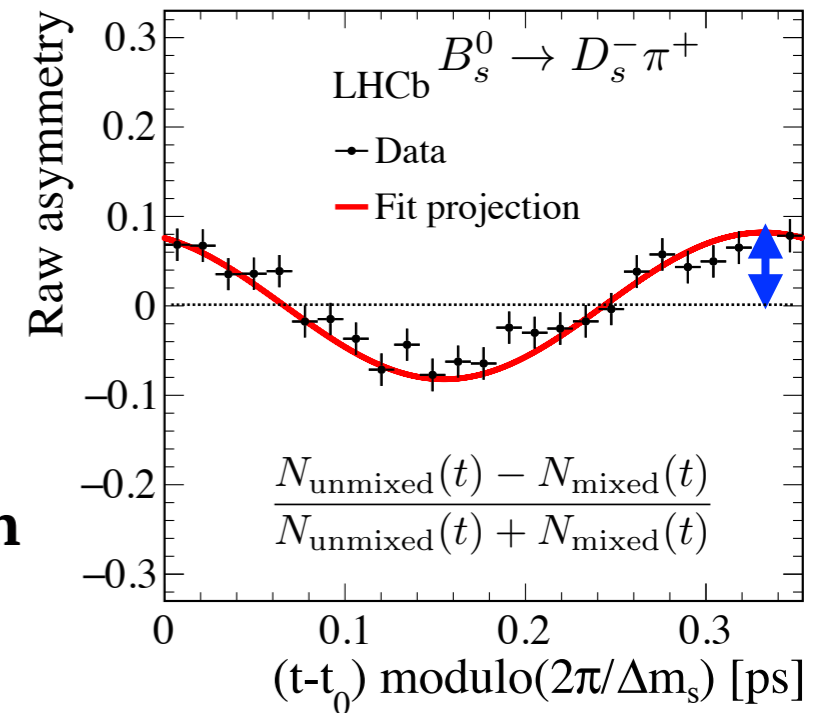
- **Dilution**:  $D = (1 - 2\omega)$  of asymmetries and decay rates.
- Predicted mistag,  $\eta$ , computed by taggers needs calibration  $\omega(\eta)$  to provide unbiased estimate of  $\omega$

- ▶ **Tagging power**: statistical degradation of  $CP$  asym.

$$\epsilon_{\text{eff}} = \epsilon_{\text{tag}} D^2 = \epsilon_{\text{tag}} \langle (1 - 2\omega)^2 \rangle$$

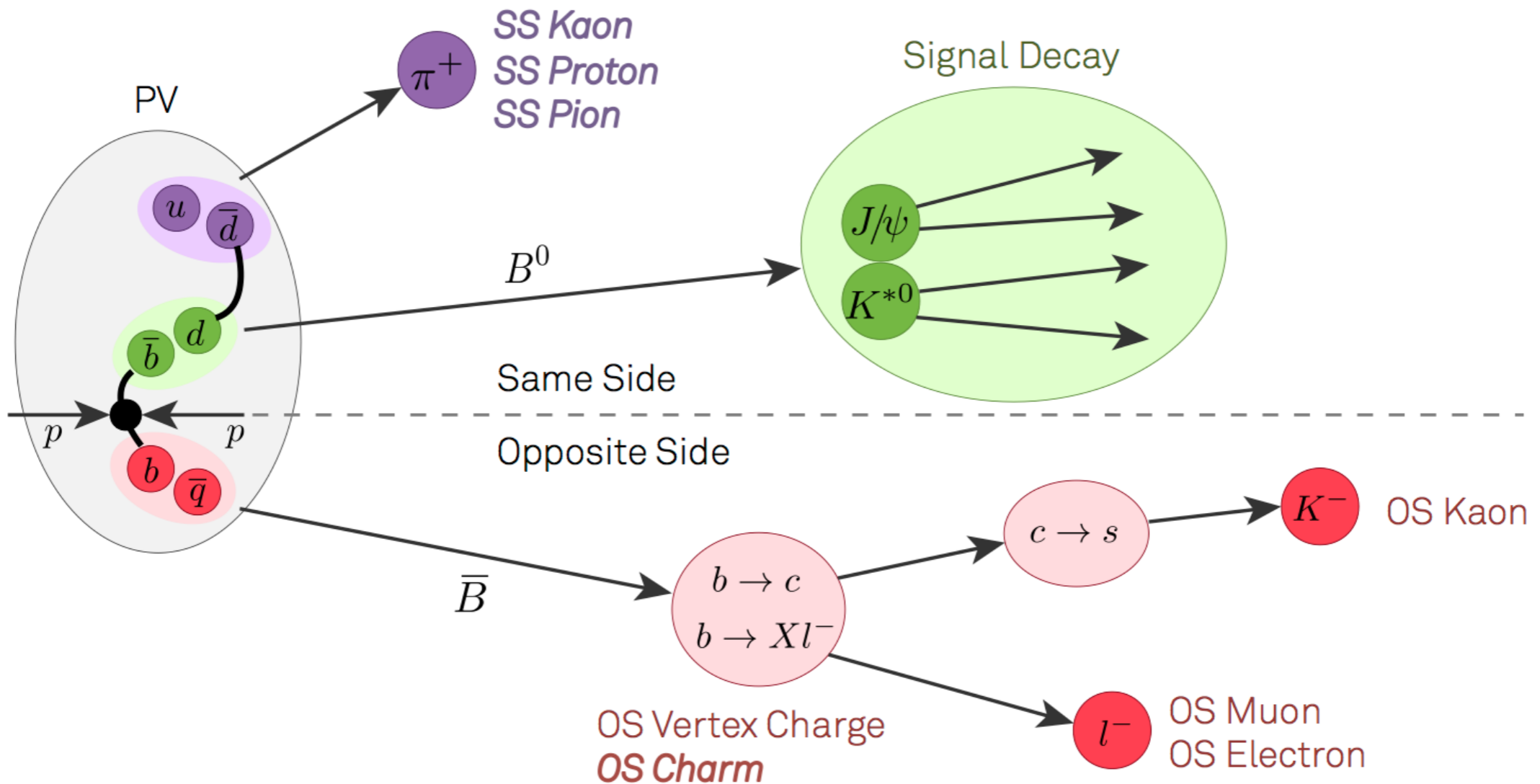
$$\sigma^{\text{stat}}(CP \text{ asym}) \propto \frac{1}{\sqrt{\epsilon_{\text{eff}} N}}$$

[Journal of Instrumentation 11 (2016) P05010]



# Flavour tagging algorithms

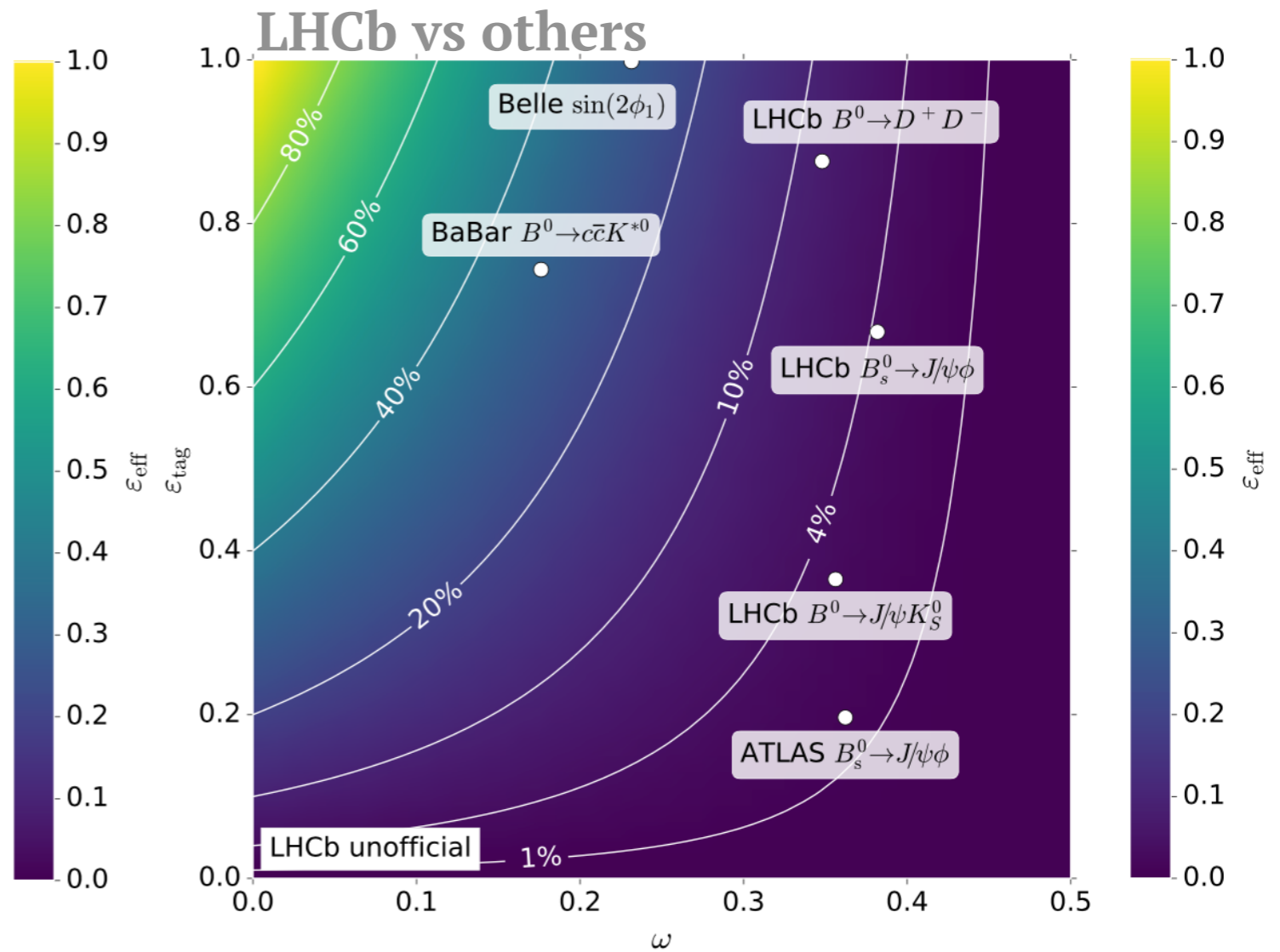
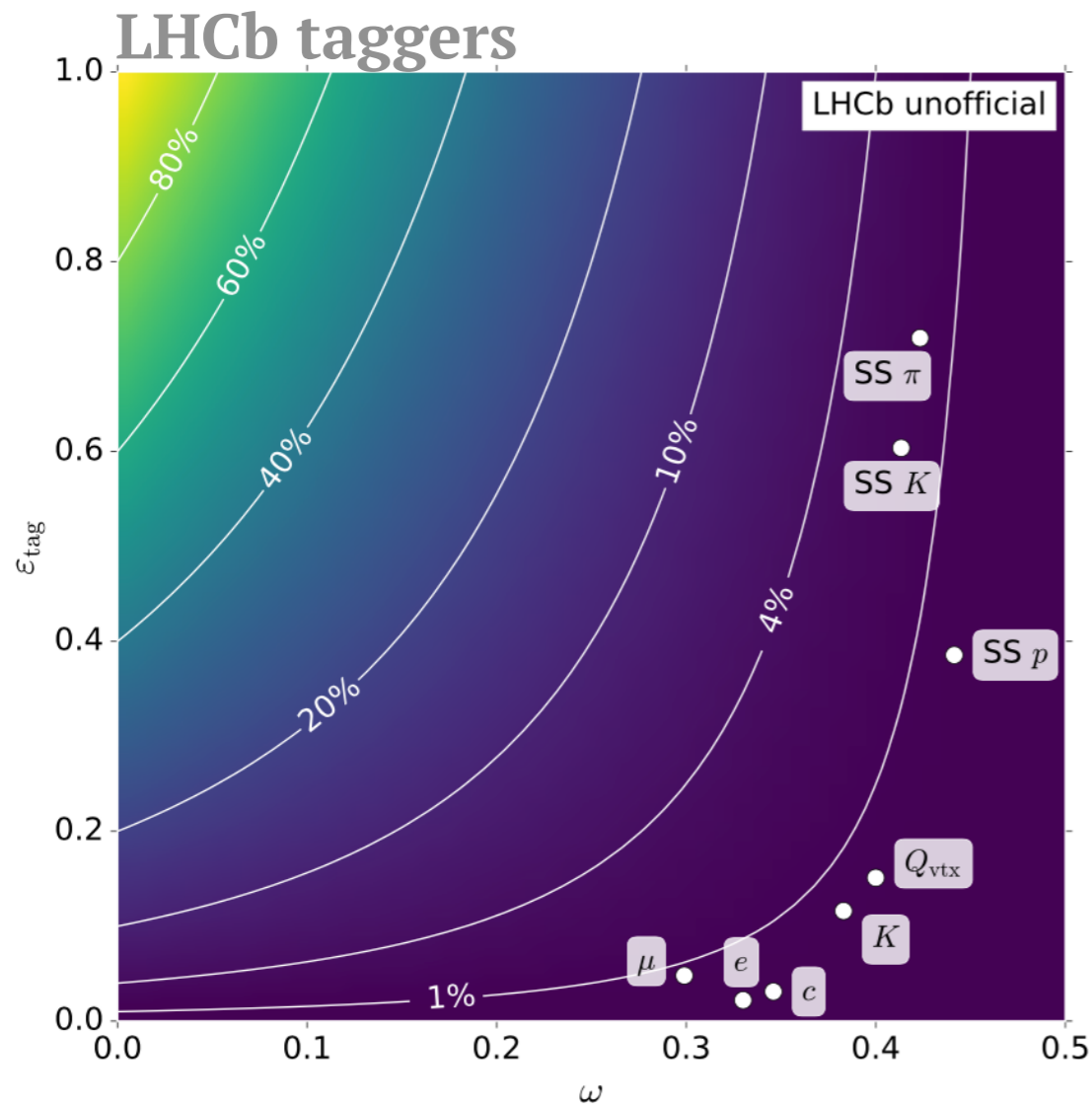
**Same side (SS):** exploit the charge of the **fragmentation particle** (pion, kaon, proton) produced next to the signal  $b$ -hadron in the hadronisation process to infer its initial flavour ( $t=0$ )



**Opposite side (OS):** exploit the charge of the particle (lepton, kaon, charm decays) or of the **reconstructed secondary vertex produced from the other  $b$ -hadron** in the event to infer signal  $b$ -hadron initial flavour ( $t=0$ )

# Typical performances

[CERN-THESIS-2016-152]

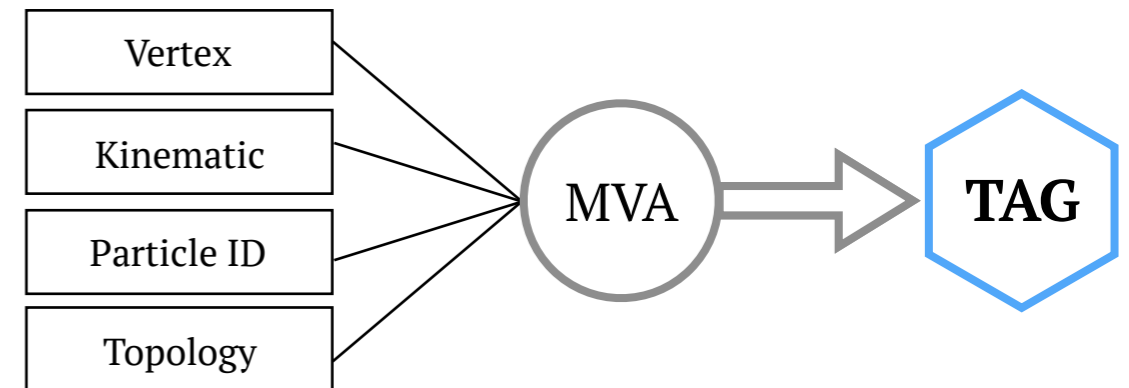


- ▶ **OS taggers: good mistag but low decision rate**
- ▶ **SS taggers: modest mistag but high decision rate**
- ▶ **Tagging performances are channel dependent**

$$\sigma^{\text{stat}}(CP \text{ asym}) \propto \frac{1}{\sqrt{\epsilon_{\text{eff}} N}}$$

## • Tagging tracks identification

- ▶  $pp$  collisions harsh environment
- ▶ few tracks among  $O(10^2)$
- ▶ FT algorithms based on MVA classifiers designed to isolate specific physical process (SS tracks, OS tracks divided by categories)



## • Taggers calibration

$$\omega = p_0 + p_1 (\eta - \langle \eta \rangle)$$

measured ev-by-ev mistag  $\rightarrow$   $\omega$      
 estimated ev-by-ev mistag  $\rightarrow$   $\eta$      
 estimated mean mistag  $\rightarrow$   $\langle \eta \rangle$

- ▶ Calibration performed on control channels:

- Charged modes:  $B^+ \rightarrow J/\psi K^+$ ,  $B^+ \rightarrow D^0 \pi^+$   
No oscillation, large samples
- Neutral  $B^0$  modes:  $B^0 \rightarrow J/\psi K^*$ ,  $B^0 \rightarrow D^- \pi^+$   
large samples
- Neutral  $B_s^0$  modes:  $B_s^0 \rightarrow D_s^- \pi^+$   
only control decay for data SSK, statistically limited

