


New directions in B-anomalies model building

Admir Greljo

20 September 2018, CKM

To make progress we need hints...





B-anomalies

2012 -

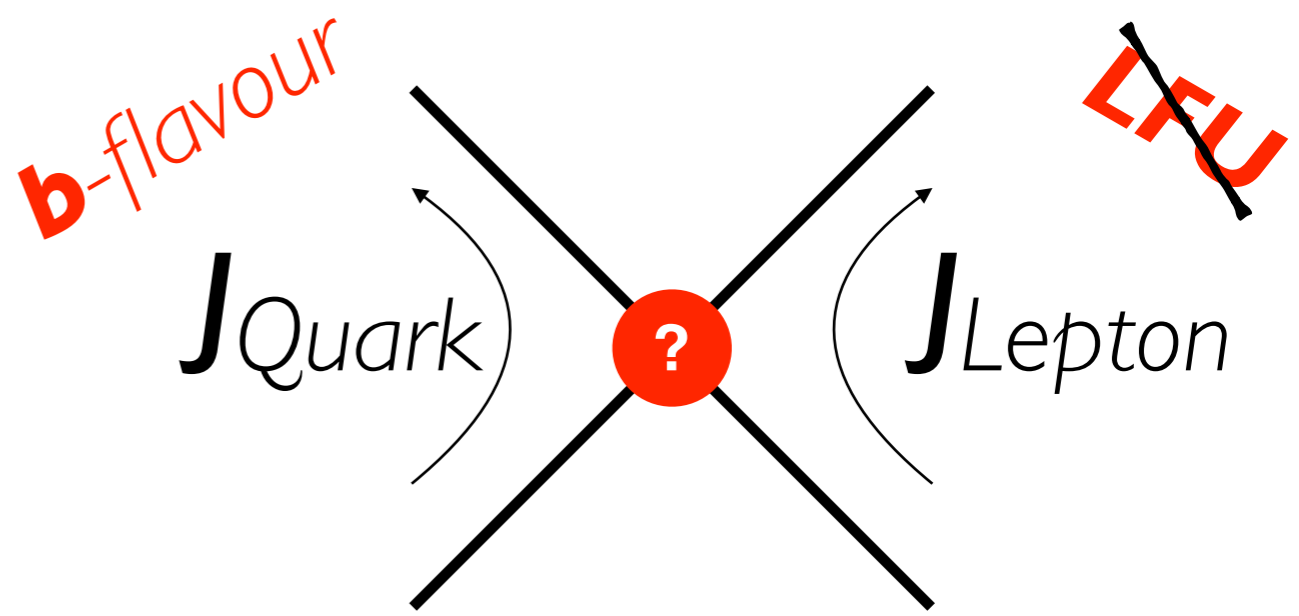
[1205.5442,
1303.0571, 1308.1707,
1406.6482,
1506.08614, 1512.04442,
1612.00529, 1607.07923,
1705.05802, ...]

$$b \rightarrow s\mu\bar{\mu}$$

$$b \rightarrow c\tau\bar{\nu}_\tau$$

Data

- **The largest coherent set of discrepancies between Theory and Experiment today**





?

$$b \rightarrow s\mu\bar{\mu}$$
$$b \rightarrow c\tau\bar{\nu}_\tau$$



$$b \rightarrow s\mu\bar{\mu}$$

V-A operator

$$b \rightarrow c\tau\bar{\nu}_\tau$$

V-A operator



SU(2)_L



Common origin?

$$(\bar{Q}_L^i \gamma_\mu \sigma^a Q_L^j) (\bar{L}_L^\alpha \gamma^\mu \sigma^a L_L^\beta)$$

Hint 1

$$Q_L^i = \begin{pmatrix} V_{ji}^* u_L^j \\ d_L^i \end{pmatrix} \quad L_L^\alpha = \begin{pmatrix} \nu_L^\alpha \\ \ell_L^\alpha \end{pmatrix}$$

?

$$b \rightarrow s\mu\bar{\mu}$$

$$b \rightarrow c\tau\bar{\nu}_\tau$$



$$b \rightarrow s \mu \bar{\mu}$$

V-A operator

$$b \rightarrow c \tau \bar{\nu}_\tau$$

V-A operator



SU(2)_L



Common origin?

$$(\bar{Q}_L^i \gamma_\mu \sigma^a Q_L^j) (\bar{L}_L^\alpha \gamma^\mu \sigma^a L_L^\beta)$$

Hint I

$$Q_L^i = \begin{pmatrix} V_{ji}^* u_L^j \\ d_L^i \end{pmatrix} \quad L_L^\alpha = \begin{pmatrix} \nu_L^\alpha \\ \ell_L^\alpha \end{pmatrix}$$

$$\sim \frac{2}{(3.5 \text{ TeV})^2} (\bar{c}_L \gamma_\mu b_L) (\bar{\tau}_L \gamma^\mu \nu_L)$$

Large NP in
3rd family

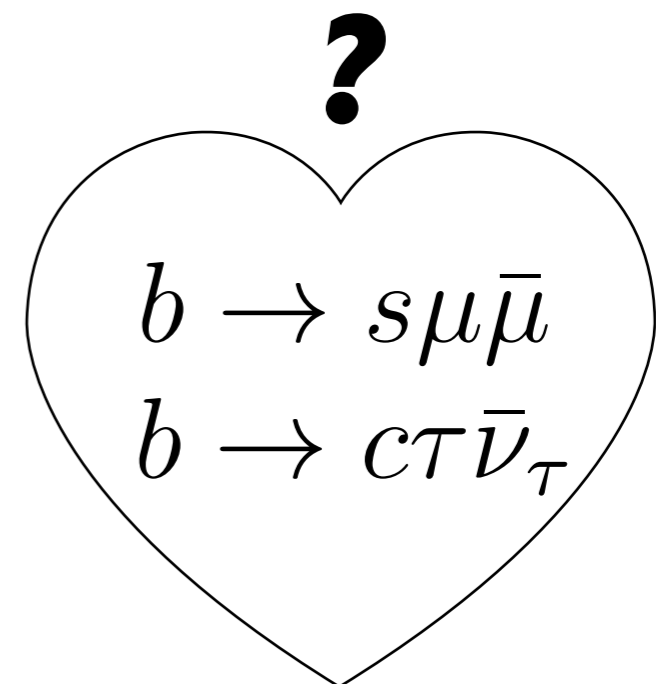
$$\sim \frac{1}{(32 \text{ TeV})^2} (\bar{s}_L \gamma_\mu b_L) (\bar{\mu}_L \gamma^\mu \mu_L)$$

Small NP in
2nd family

Related to

The SM flavour puzzle?

Hint II





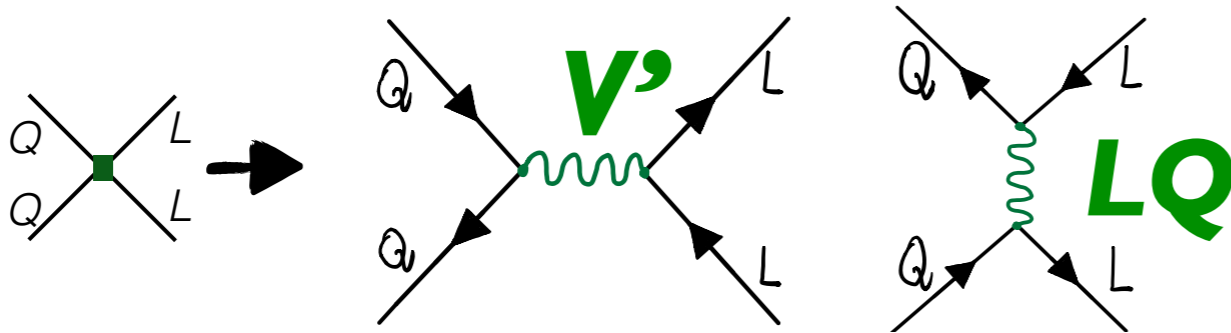
Steps to Models

1 SMEFT + Flavour Symmetries

$$C_T (\bar{Q}_L^i \gamma_\mu \sigma^a Q_L^j) (\bar{L}_L^\alpha \gamma^\mu \sigma^a L_L^\beta) + C_S (\bar{Q}_L^i \gamma_\mu Q_L^j) (\bar{L}_L^\alpha \gamma^\mu L_L^\beta)$$

$$U(2)_q \times U(2)_\ell$$

2 Simplified mediator models



Most notable constraints

- ✗ Other meson decays
- ✗ Neutral meson mixing
- ✗ LFU and LFV in charged leptons
- ✗ Z and W pole precision
- ✗ High- p_T searches

see e.g. [Buttazzo, AG, Isidori, Marzocca]
1706.07808

- ✓ Mature & successful programme
- ✓ A few working solutions identified
- ✓ Complementary low and high- p_T processes identified

Challenges for Model Builders?

$$B_s \leftrightarrow \bar{B}_s$$

$$B \rightarrow K^{(*)} \nu_\tau \bar{\nu}_\tau$$

...

$$pp \rightarrow \tau^+ \tau^-$$

...

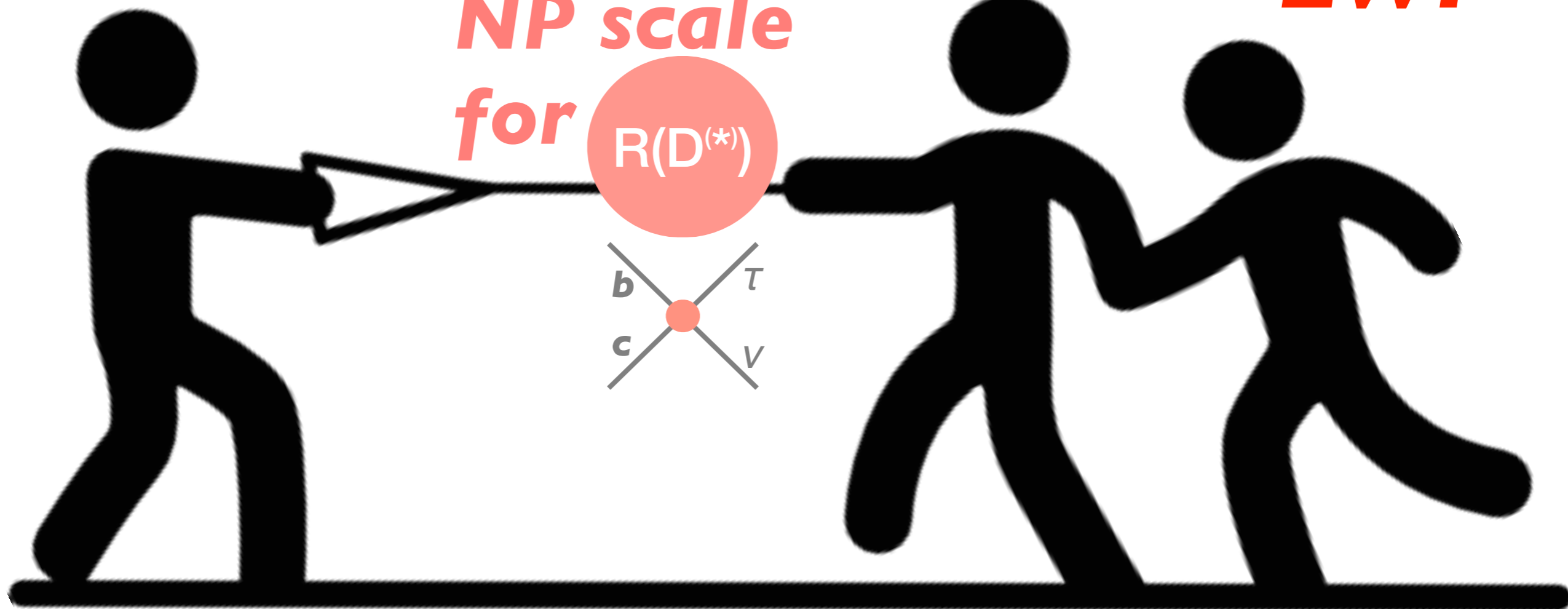
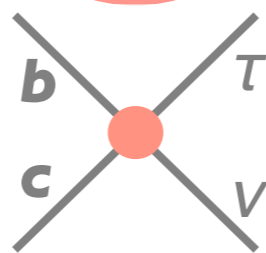
Z decays
 τ decays
 ...

FCNC

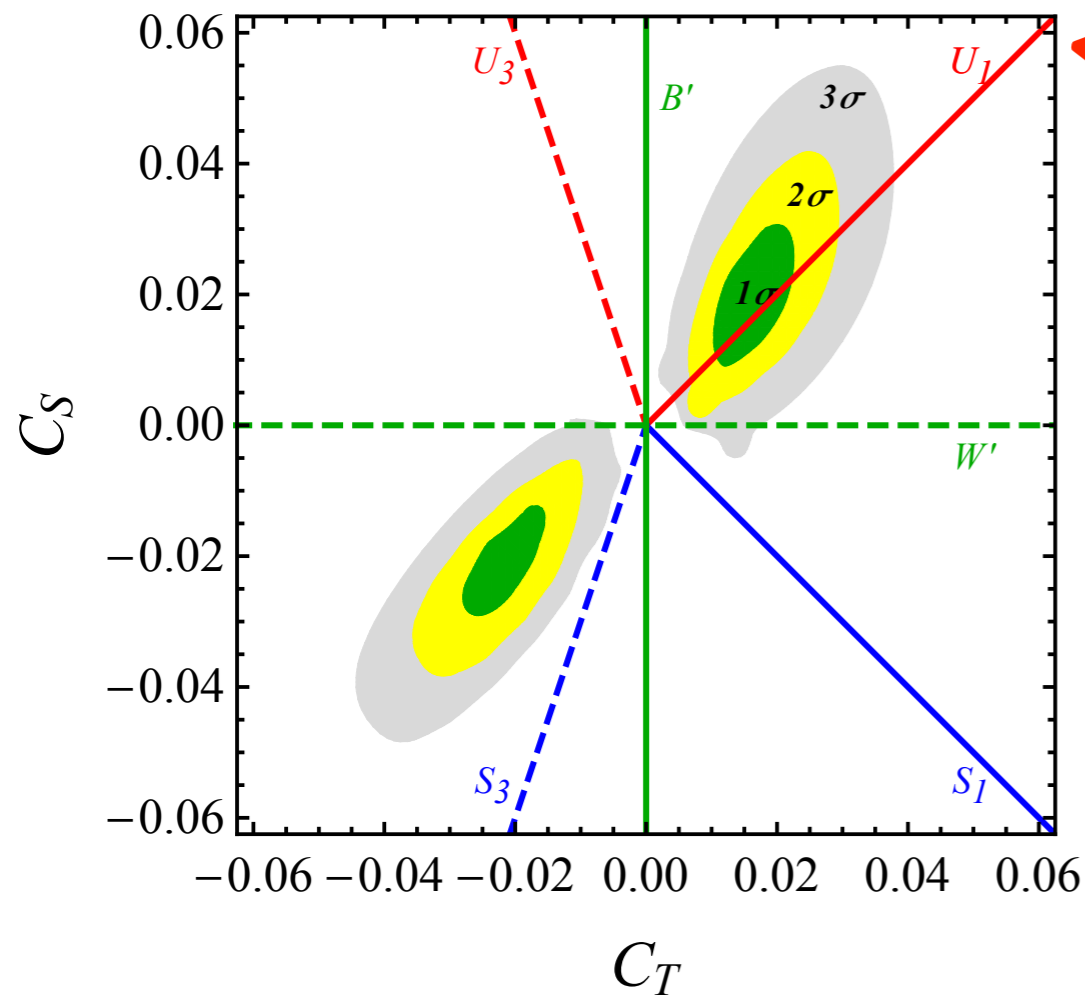
High p_T
LHC

EWP

NP scale
for



Single mediator?



Vector LQ
(3, 1, 2/3)

$$J_U^\mu \equiv \beta_{i\alpha} \bar{Q}_i \gamma^\mu L_\alpha \longrightarrow \mathbf{de} + \mathbf{uv}$$

*Expanding SU(2)

- **Tree-level**

$$b \rightarrow s \mu \bar{\mu}$$

$$b \rightarrow c \tau \bar{\nu}_\tau$$

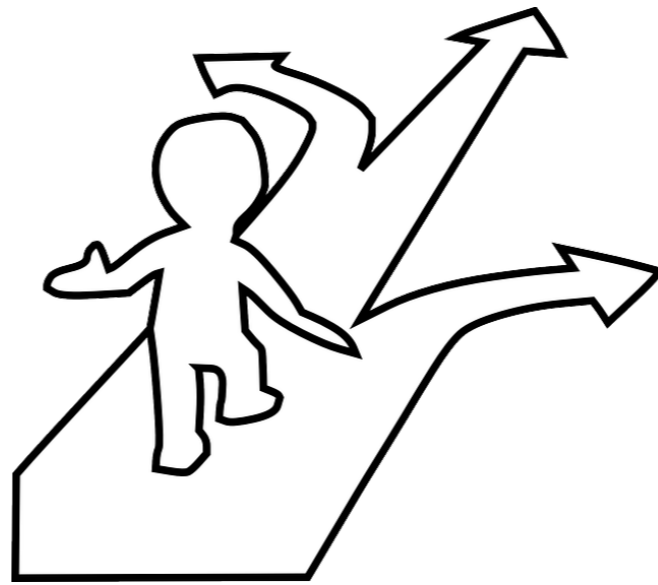
- **Dynamical suppression:**

$$B_s \leftrightarrow \bar{B}_s \quad B \rightarrow K^{(*)} \nu_\tau \bar{\nu}_\tau$$

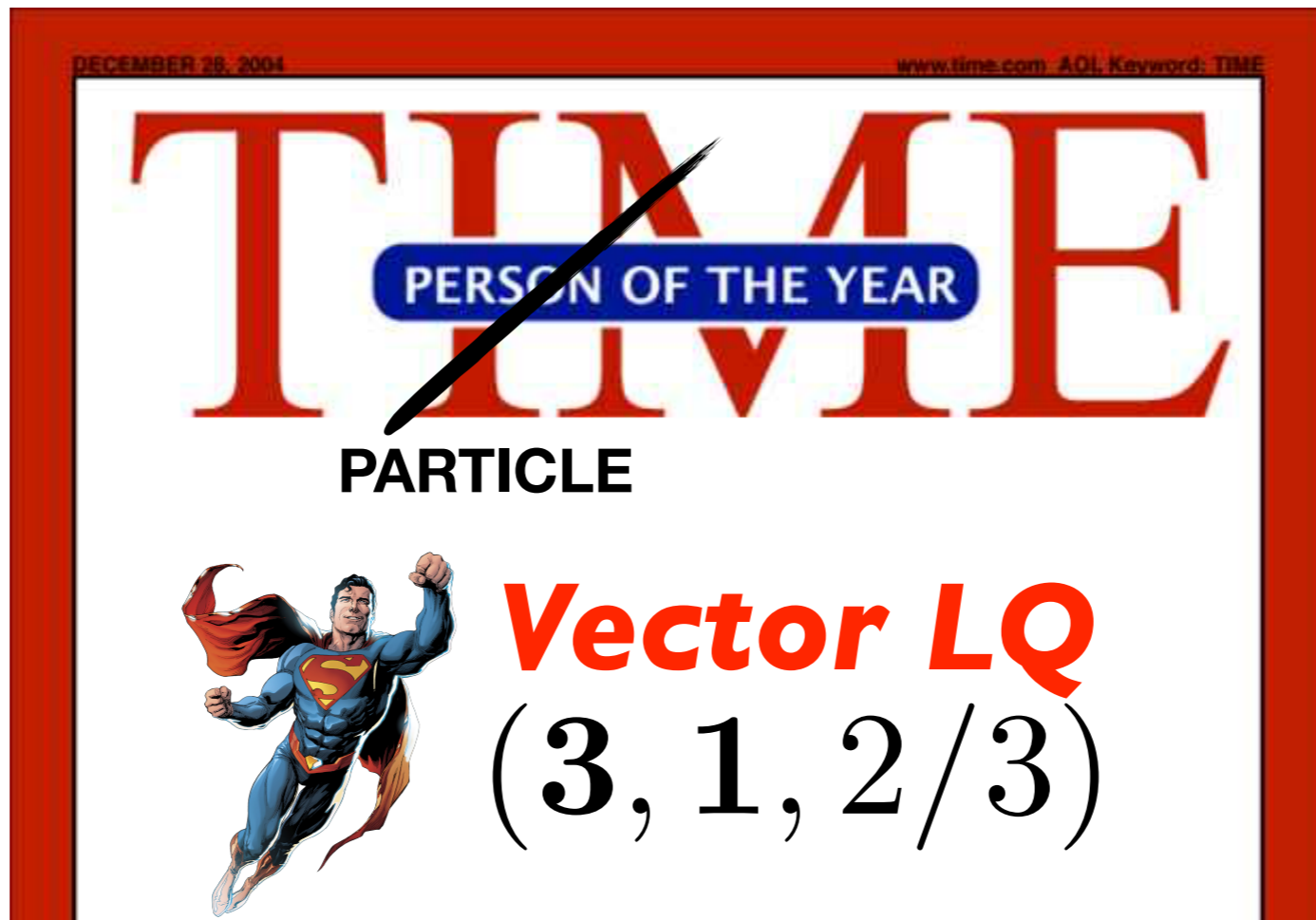
$$Z \rightarrow \tau^+ \tau^-$$

[1706.07808,
1708.08450,
1709.00692,
1712.01368,
1712.06844,
1801.07256,
1802.04274,
1805.09328,
1805.03209,
1806.07403,
1807.02068,
1807.10745,
1808.00942,
1808.05511,
1808.07492,
1808.08179,
...]

Only a selection



Direction I



A cake by
[Buttazzo], 2017



'74 Pati-Salam

- ***Pati-Salam quark-lepton unification***
$$4 = 3q + 1_\ell$$
- ***Resolves another open problem of the SM — charge quantisation***
- ***Low-scale Pati-Salam***
 - ✓ ***No proton decay***
 - ✗ ***Flavour $\gtrsim 1000$ TeV*** [1801.02895]

A cake by
[Buttazzo], 2017



'74 Pati-Salam

- ***Pati-Salam quark-lepton unification***
$$4 = 3q + 1_\ell$$
- ***Resolves another open problem of the SM — **charge quantisation*****
- ***Low-scale Pati-Salam***
 - ✓ ***No proton decay***
 - ✗ ***Flavour $\gtrsim 1000$ TeV*** [1801.02895]

Consistent model
with Pati-Salam
LQ at the TeV
scale?

A cake by
[Buttazzo], 2017



'74 Pati-Salam

- **Pati-Salam quark-lepton unification**
 $4 = 3q + 1_\ell$
- **Resolves another open problem of the SM — *charge quantisation***
- **Low-scale Pati-Salam**
 - ✓ **No proton decay**
 - ✗ **Flavour $\gtrsim 1000$ TeV** [1801.02895]

Establishing links (The big picture)

[Talk by Isidori]



Consistent model with Pati-Salam LQ at the TeV scale?

- **Hierarchy**
- **Charge quantization**
- **Flavour problem**
- **Neutrino masses**
- **B-anomalies**

[This talk]

- Massive vector craves a UV completion
- Simplified mediator model approach is incomplete!
- I want a model to be
 - Complete** (but simple),
 - Renormalizable**,
 - Calculable** (perturbatively)
- **'Proper'** low-energy model to check the stability of the B-anomalies solution

Consistent model
with Pati-Salam
LQ at the TeV
scale?

'4321' model

Extended gauge symmetry

$$G \equiv SU(4) \times SU(3)' \times SU(2)_L \times U(1)'$$

Field content

Field	$SU(4)$	$SU(3)'$	$SU(2)_L$	$U(1)'$
q_L^i	1	3	2	1/6
u_R^i	1	3	1	2/3
d_R^i	1	3	1	-1/3
ℓ_L^i	1	1	2	-1/2
e_R^i	1	1	1	-1
Ψ_L^i	4	1	2	0
Ψ_R^i	4	1	2	0
H	1	1	2	1/2
Ω_1	$\bar{4}$	1	1	-1/2
Ω_3	$\bar{4}$	3	1	1/6
Ω_{15}	15	1	1	0

Fermions

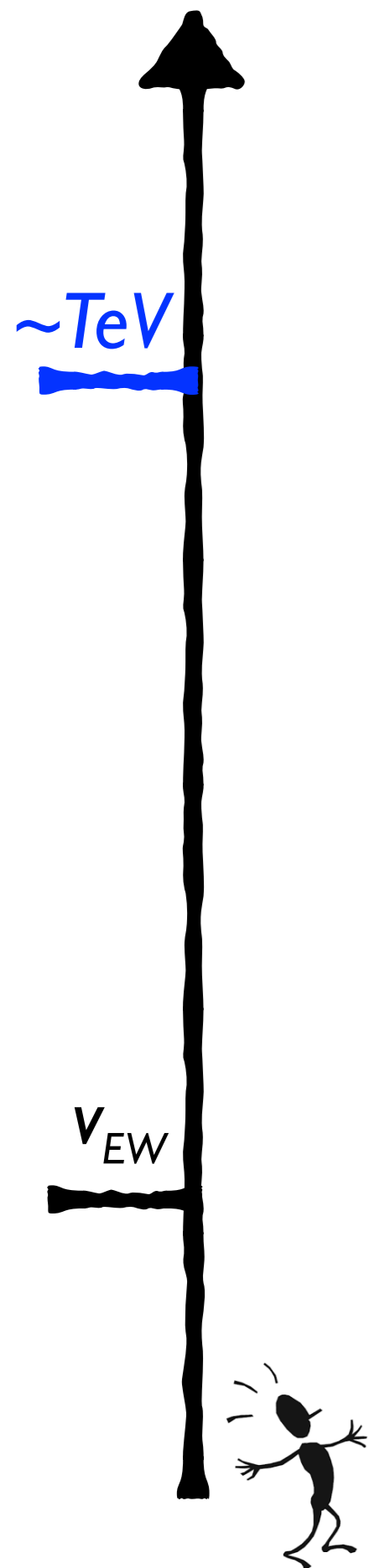
Scalars

$i=1,2,3$

4321 Model for B-anomalies
[Di Luzio, AG, Nardecchia]
1708.08450

Phenomenology
[Di Luzio, Fuentes-Martin,
AG, Nardecchia, Renner]
1808.00942

Model structure from
[Georgi, Nakai], 1606.05865
[Diaz, Schmaltz, Zhong], 1706.05033



'4321' model

Extended gauge symmetry

$$G \equiv SU(4) \times SU(3)' \times SU(2)_L \times U(1)'$$



$$\text{SSB: } \langle \Omega_3 \rangle > \langle \Omega_1 \rangle \gg \langle \Omega_{15} \rangle \gg \langle H \rangle$$

$$G_{\text{SM}} \equiv SU(3)_c \times SU(2)_L \times U(1)_Y$$

Embedding:

$$SU(3)_4 \times U(1)_4 \subset SU(4)$$

and

$$SU(3)_c = (SU(3)_4 \times SU(3)')_{\text{diag}}$$

$$U(1)_Y = (U(1)_4 \times U(1)')_{\text{diag}}$$

Scalars:

$$\Omega_1 = (\bar{4}, 1, 1, -1/2)$$

$$\Omega_3 = (\bar{4}, 3, 1, 1/6)$$

$$\langle \Omega_3 \rangle = \begin{pmatrix} \frac{v_3}{\sqrt{2}} & 0 & 0 \\ 0 & \frac{v_3}{\sqrt{2}} & 0 \\ 0 & 0 & \frac{v_3}{\sqrt{2}} \\ 0 & 0 & 0 \end{pmatrix}, \quad \langle \Omega_1 \rangle = \begin{pmatrix} 0 \\ 0 \\ 0 \\ \frac{v_1}{\sqrt{2}} \end{pmatrix}$$

Gauge couplings:

$$g_s = \frac{g_4 g_3}{\sqrt{g_4^2 + g_3^2}}$$

$$g_Y = \frac{g_4 g_1}{\sqrt{g_4^2 + \frac{2}{3} g_1^2}}$$

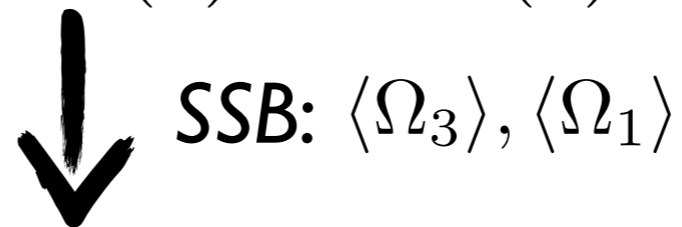
*One free coupling constant



'4321' model

Extended gauge symmetry

$$G \equiv SU(4) \times SU(3)' \times SU(2)_L \times U(1)'$$



$$G_{\text{SM}} \equiv SU(3)_c \times SU(2)_L \times U(1)_Y$$

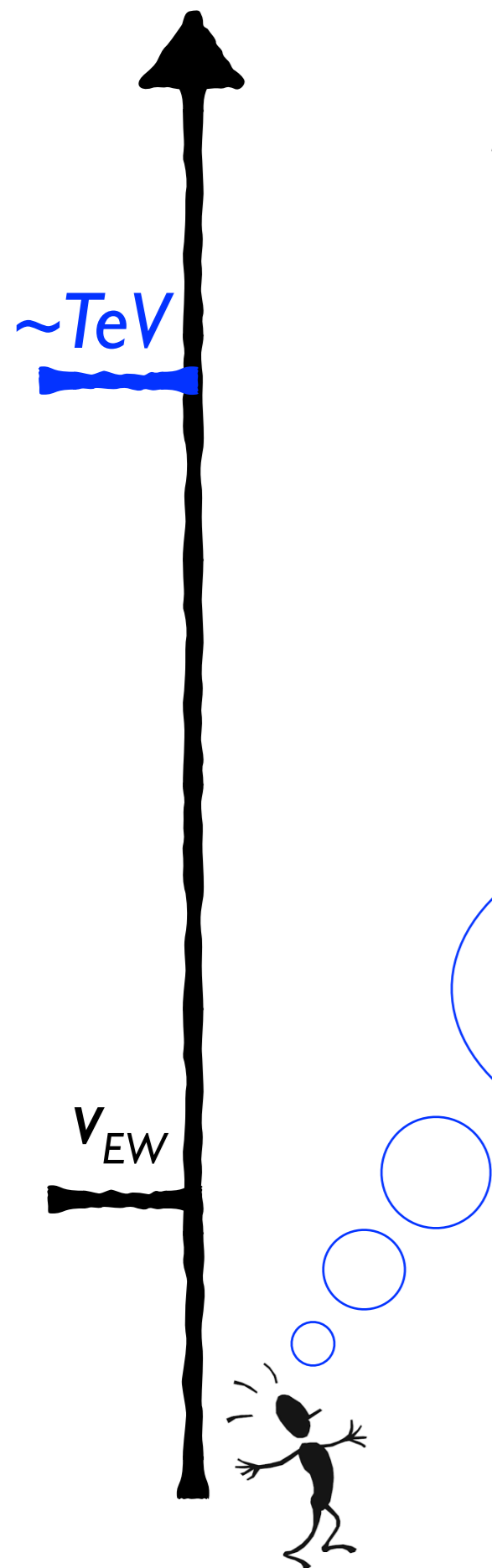
15 broken generators

$(3, 1, 2/3)$
Leptoquark
*Complex

$(8, 1, 0)$
G'

$(1, 1, 0)$
Z'

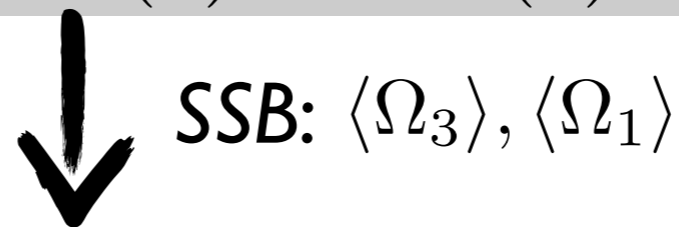
Close in mass to the LQ!



'4321' model

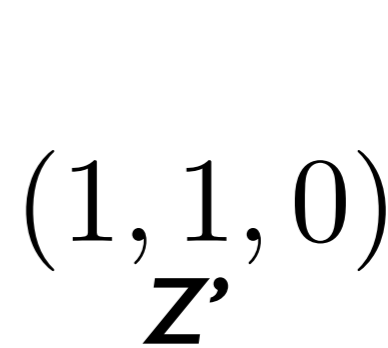
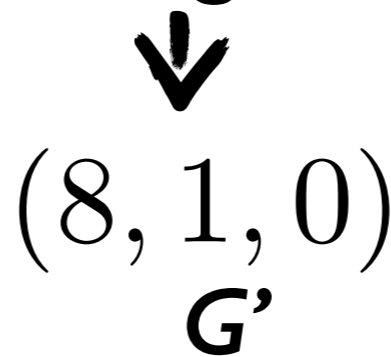
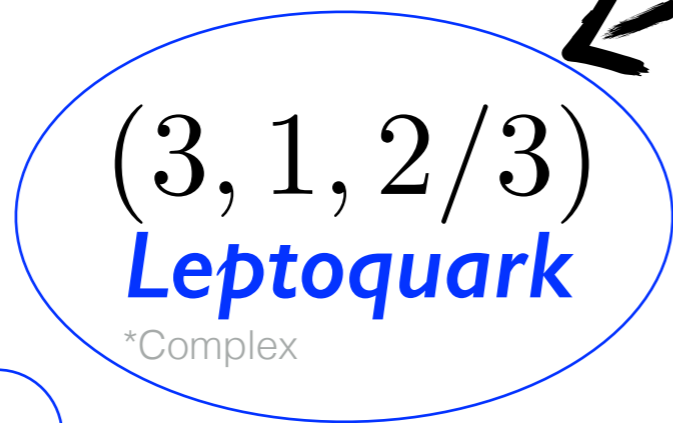
Extended gauge symmetry

$$G \equiv SU(4) \times SU(3)' \times SU(2)_L \times U(1)'$$

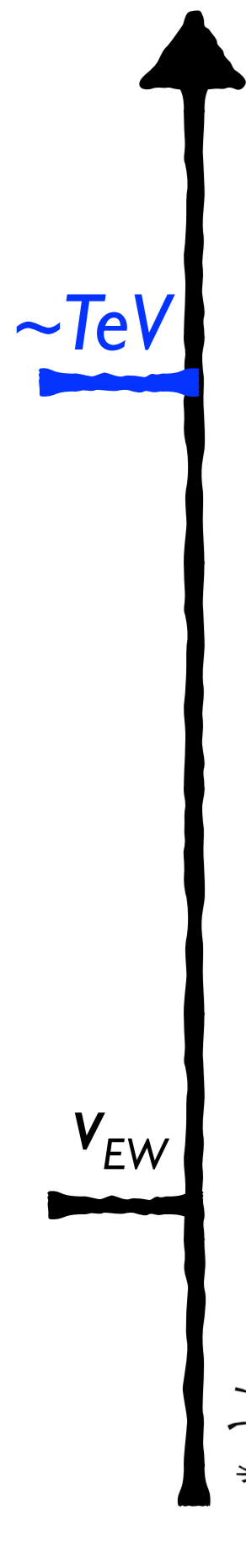


$$G_{\text{SM}} \equiv SU(3)_c \times SU(2)_L \times U(1)_Y$$

15 broken generators



- SM fermions in **321**, not coupled to LQ
 $(q'_L, \ell'_L, u'_R, d'_R, e'_R)$



'4321' model

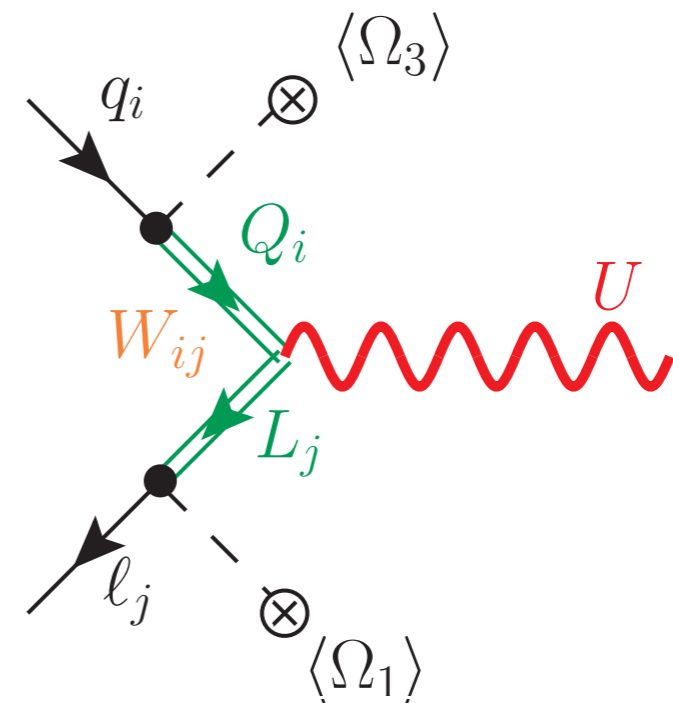
A vector-like fermion rep. $(4, 1, 2, 0)$

$$\Psi_{L,R} = (Q'_{L,R}, L'_{L,R})^T$$

$$-\bar{q}'_L \lambda_q \Omega_3^T \Psi_R - \bar{\ell}'_L \lambda_\ell \Omega_1^T \Psi_R$$

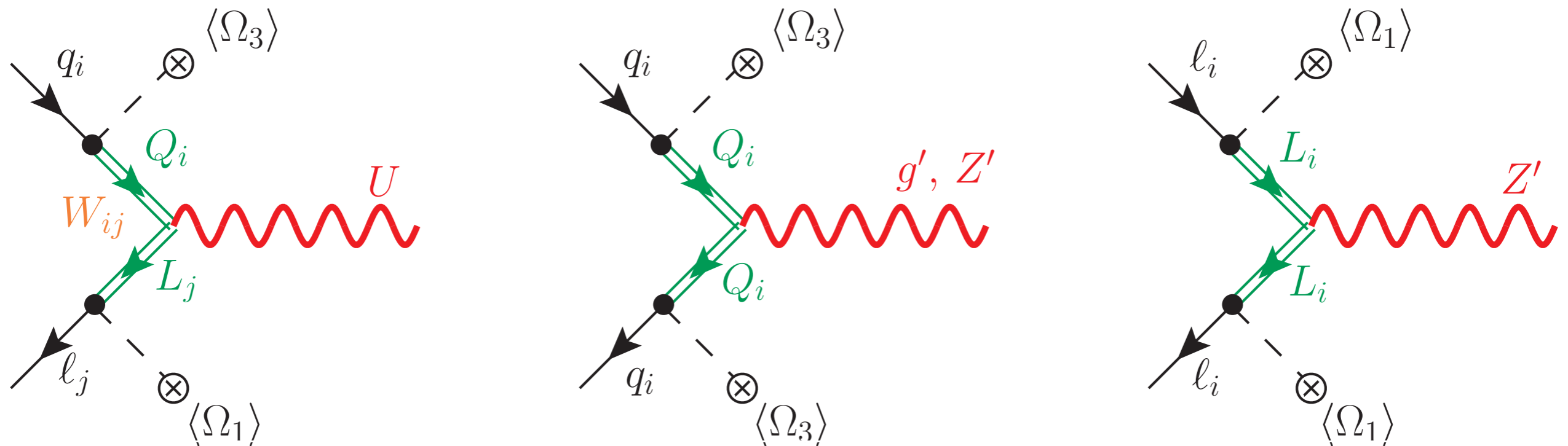
- $\langle \Omega_3 \rangle$ mixes the would-be SM state q'_L with $Q'_L \subset \Psi_L$
- $\langle \Omega_1 \rangle$ mixes the would-be SM state ℓ'_L with $L'_L \subset \Psi_L$.

SM fermion **doublets** mix with the vector-like partners



Left-handed dominance!

- *How to get large flavour violation to be mediated only by the LQ?*



Cabibbo mechanism for LQ

Cabibbo mechanism for LQ

Without loss of generality

$$\mathcal{L}_{\text{SM-like}} = -\bar{q}'_L V^\dagger \hat{Y}_u d_R \tilde{H} - \bar{q}'_L \hat{Y}_d d_R H - \bar{\ell}'_L \hat{Y}_e e_R H + \text{h.c.},$$

$$\mathcal{L}_{\text{mix}} = -\bar{q}'_L \lambda_q \Psi_R \Omega_3 - \bar{\ell}'_L \lambda_\ell \Psi_R \Omega_1 - \bar{\Psi}_L (\hat{M} + \lambda_{15} \Omega_{15}) \Psi_R + \text{h.c.}$$

Assumptions

1 $\lambda_q = \hat{\lambda}_q \equiv \text{diag}(\lambda_{12}^q, \lambda_{12}^q, \lambda_3^q),$

2 $\lambda_\ell = \hat{\lambda}_\ell W^\dagger \equiv \text{diag}(\lambda_1^\ell, \lambda_2^\ell, \lambda_3^\ell) \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{LQ} & -\sin \theta_{LQ} \\ 0 & \sin \theta_{LQ} & \cos \theta_{LQ} \end{pmatrix}$

3 $\lambda_{15} \propto \hat{M} \propto \mathbb{1},$

*a hat means diagonal

1

- **No tree-level Z' , g' FCNC for down quarks**
- **Strong suppression of tree-level FCNC for up quarks**

$$\mathcal{G}_Q \equiv U(2)_{q'+\Psi} \times U(1)_{q'_3+\Psi_3}$$

$$\lambda_\ell \rightarrow 0$$

'4321' model

2

3

- **Redefine**

$$\Psi_L = (Q'_L, L'_L)^T = (Q_L, W L_L)^T$$

*same for the right-handed

- **No tree-level Z' FCNC for leptons**

$$\lambda_q \rightarrow 0 \quad \mathcal{G}_L = U(1)_{\ell'_1+\tilde{\Psi}_1} \times U(1)_{\ell'_2+\tilde{\Psi}_2} \times U(1)_{\ell'_3+\tilde{\Psi}_3}$$

- **Only LQ interaction feels W matrix!**

$$i\bar{\Psi}_L \gamma^\mu D_\mu \Psi_L \supset \frac{g_4}{\sqrt{2}} U_\mu \bar{Q}_L \gamma^\mu \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{LQ} & \sin \theta_{LQ} \\ 0 & -\sin \theta_{LQ} & \cos \theta_{LQ} \end{pmatrix} L_L.$$

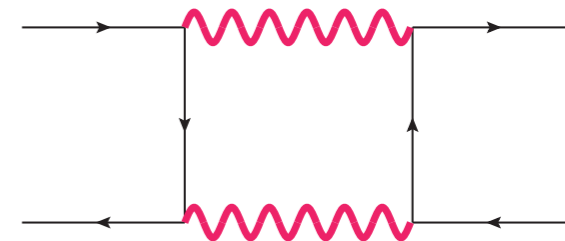
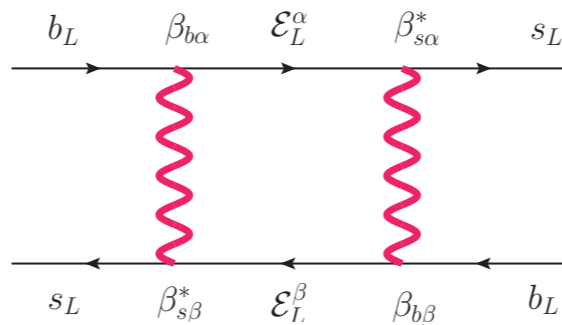
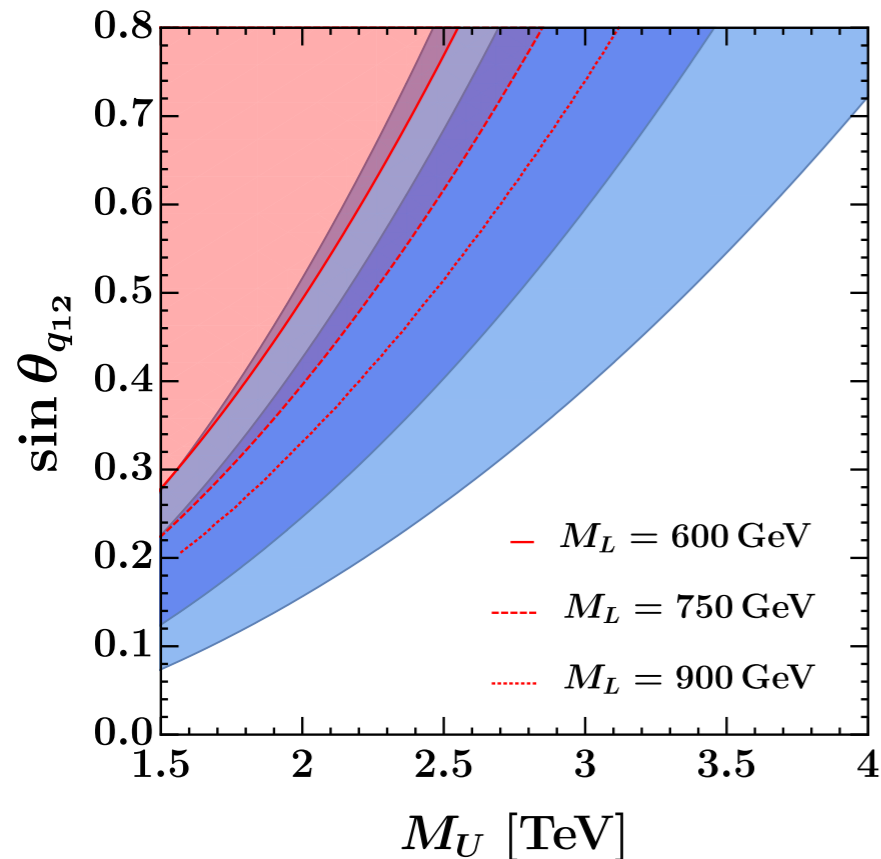
**Calculable,
so calculate!**

Contents	
1 Introduction	1
2 The 4321 model	4
3 Cabibbo mechanism for leptoquarks	6
4 Low-energy phenomenology	11
4.1 Constraints on fermion mixing	13
4.2 Semileptonic processes	13
4.2.1 Charged currents	14
4.2.2 Neutral currents	15
4.2.3 Lepton Flavour Violating transitions	17
4.3 Hadronic processes	18
4.3.1 $B_s - \bar{B}_s$ mixing	19
4.3.2 $D - \bar{D}$ mixing	21
4.4 Leptonic processes	23
4.5 Perturbativity	24
5 High-p_T signatures	25
5.1 Resonances spectrum	25
5.2 Decay channels	27
5.2.1 Vector decays	27
5.2.2 Fermion decays	28
5.3 Collider constraints	31
5.3.1 Coloron searches in $t\bar{t}$ and $b\bar{b}$ final states	31
5.3.2 Z' search in $\tau^+\tau^-$ final state	34
5.3.3 Leptoquark signatures	34
5.3.4 Vector-like lepton production	36
5.3.5 Vector-like quark production	37
5.3.6 Multi-leptons plus multi-jets	37
6 Conclusions	39
A Anatomy of the 4321 model	41
A.1 Scalar potential	41
A.2 Scalar spectrum	42
A.3 Radial modes	43
A.4 Gauge boson spectrum	44
A.5 Gauge boson spectrum beyond minimal scalar sector	46
A.6 Fermion diagonalization to the mass basis	46
A.7 Vector-fermion interactions in the mass basis	48
A.8 Tri-linear gauge boson vertices	50
A.9 Renormalisation group equations	52
A.10 $SU(4)$ generators	53

'4321' model

'4321' model

$B_s - \bar{B}_s$



GIM suppression! $C_{bs}^{LL} \sim \Delta R_{D^{(*)}}^2 M_L^2$



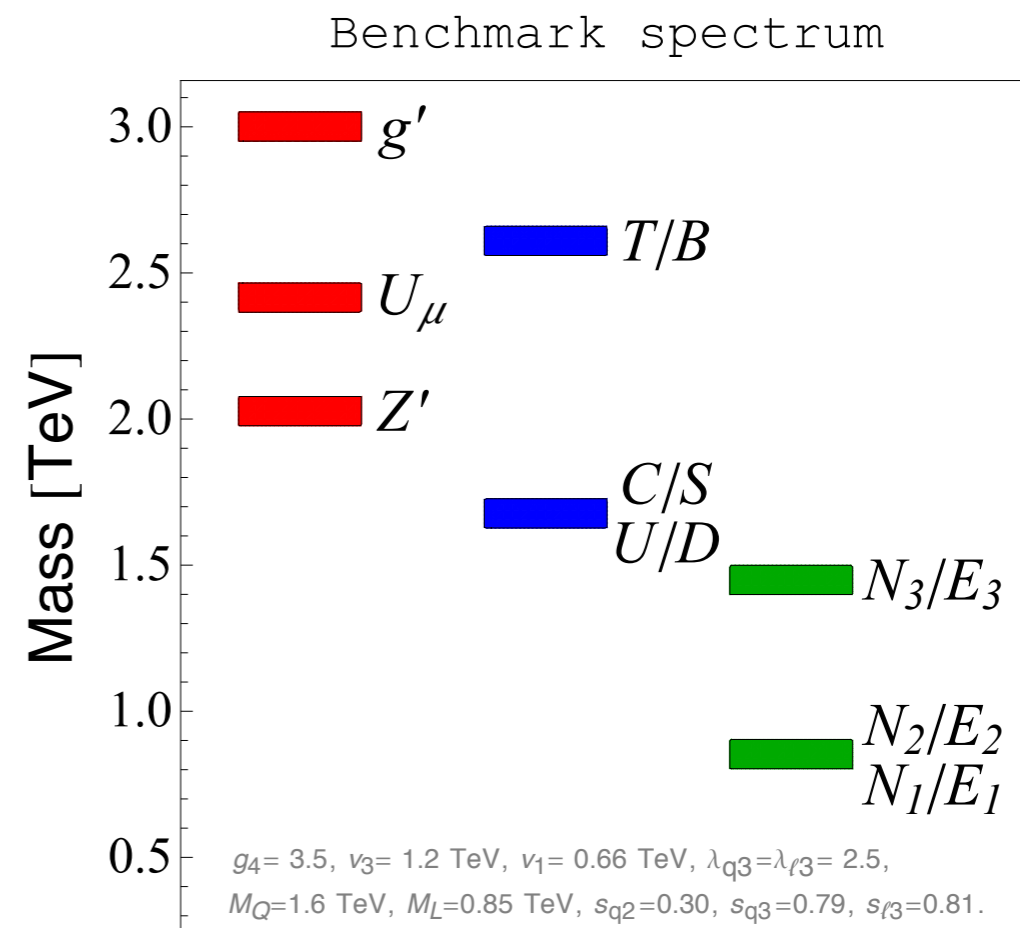
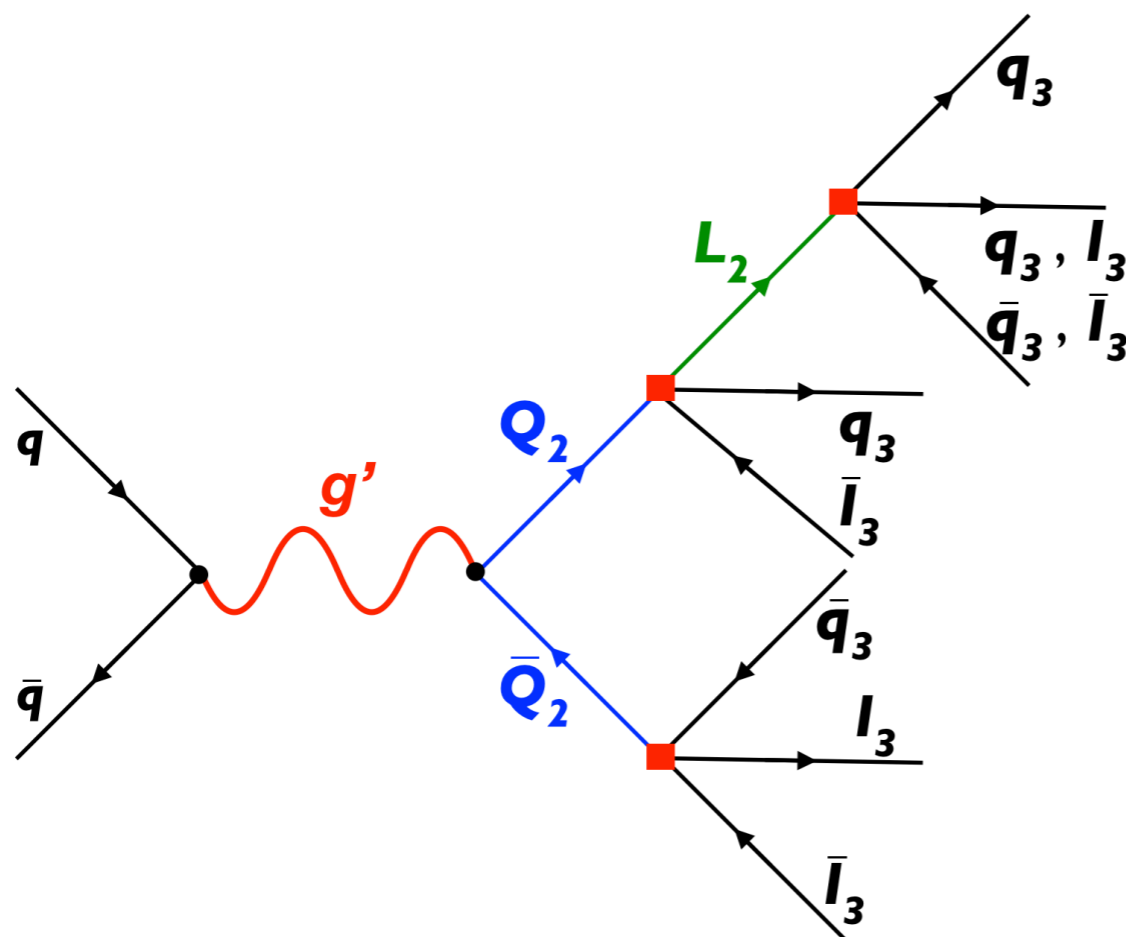
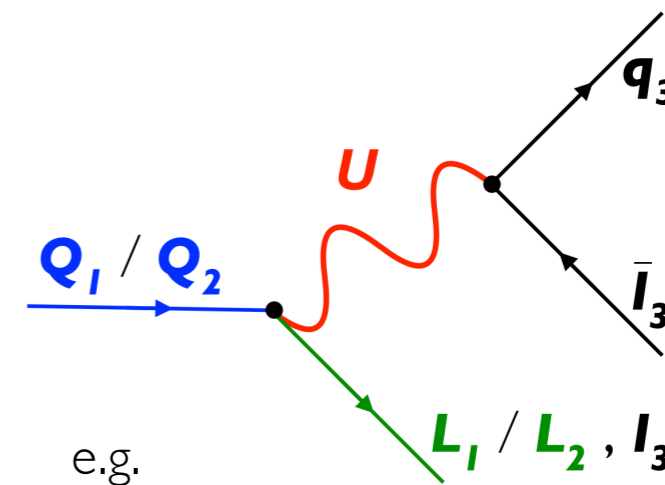
$$C_{bs}^{LL} = -\frac{g_4^2}{64\pi^2} C_U \frac{1}{(V_{tb}V_{ts}^*)^2 R_{SM}^{\text{loop}}} \sum_{\alpha,\beta} \lambda_\alpha^B \lambda_\beta^B F(x_\alpha, x_\beta)$$

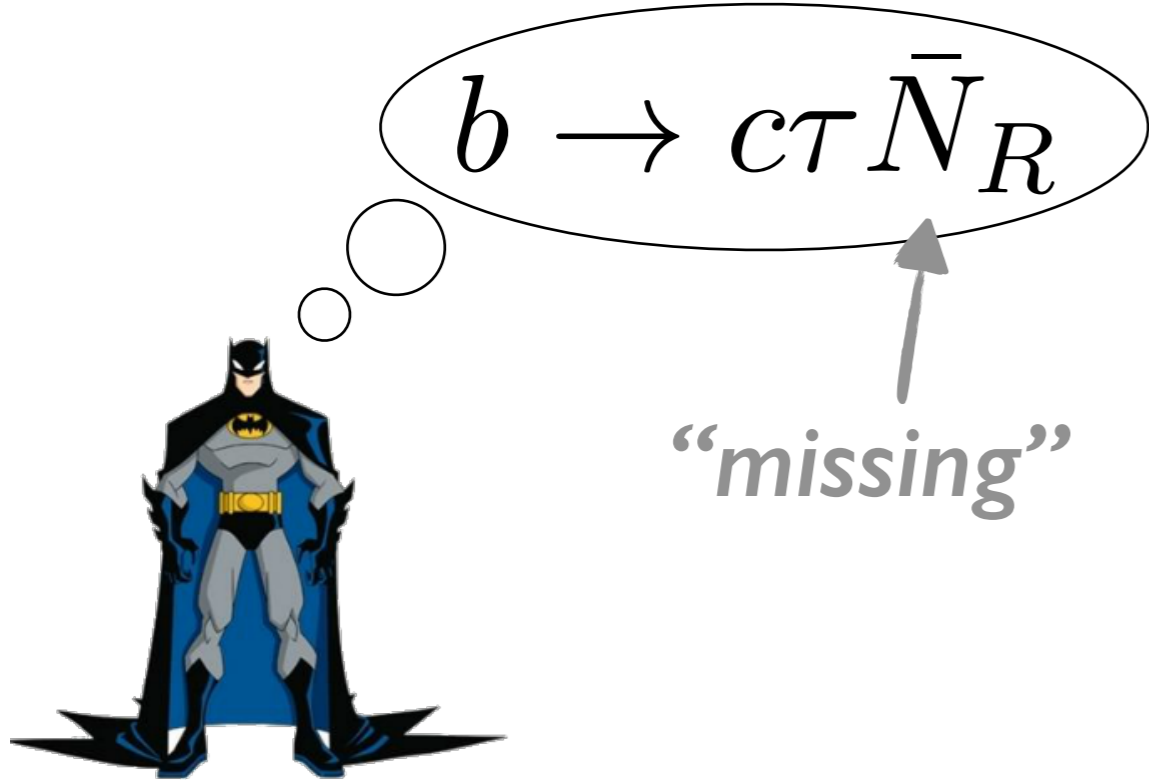
$$\begin{aligned}
 F(x_\alpha, x_\beta) = & \frac{1}{(1-x_\alpha)(1-x_\beta)} \left(\frac{7x_\alpha x_\beta}{4} - 1 \right) \\
 & + \frac{x_\alpha^2 \log x_\alpha}{(x_\beta - x_\alpha)(1-x_\alpha)^2} \left(1 - 2x_\beta + \frac{x_\alpha x_\beta}{4} \right) \\
 & + \frac{x_\beta^2 \log x_\beta}{(x_\alpha - x_\beta)(1-x_\beta)^2} \left(1 - 2x_\alpha + \frac{x_\alpha x_\beta}{4} \right)
 \end{aligned}$$

The lightest new states are vector-like leptons!

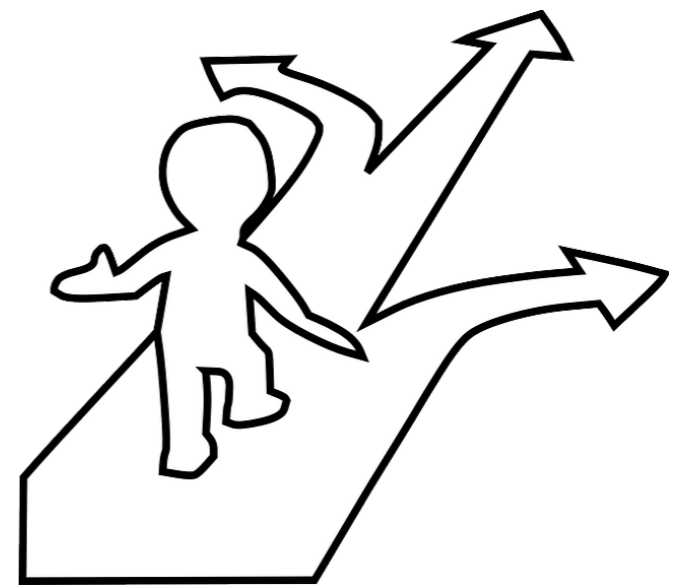
'4321' model

- Peculiar high- p_T signatures
- Dominant decays of new fermions are $l > 3$
- Exotic multi-lepton & multi-jet signatures





Old idea, see e.g. [Bečirević, Fajfer, Košnik, Sumensari] 1608.08501



Direction II

‘SU(2)_L was a blessing, but also a curse’

- Idea: **Decorrelate R(D^(*)) from FCNC limits**

Recent activity

[1804.04642,
1804.04135,
1807.04753,
1807.10745,
1809.01107,
...]

$$W' = (1, 1, +1)$$

+ light

$$N_R = (1, 1, 0)$$



[Asadi, Buckley, Shih]

1804.04135



[AG, Robinson, Shakya, Zupan]

1804.04642

‘3221’ model

[backup]

$$\begin{aligned}
 b &\rightarrow s\mu\bar{\mu} \\
 b &\rightarrow c\tau\bar{\nu}_\tau
 \end{aligned}$$

$$\begin{aligned}
 U_1^\mu &\sim (\mathbf{3}, \mathbf{1}, 2/3) \\
 &\quad \text{ + \text{light} \quad \text{} \\
 N_R &= (\mathbf{1}, \mathbf{1}, 0)
 \end{aligned}$$

Simplified mediator model

[Marzocca et al], 1807.10745

$$b \rightarrow s\mu\bar{\mu}$$

$$b \rightarrow c\tau\bar{\nu}_\tau$$

$$U_1^\mu \sim (\mathbf{3}, \mathbf{1}, 2/3)$$

+ light

$$N_R = (\mathbf{1}, \mathbf{1}, 0)$$

Simplified mediator model

[Marzocca et al], 1807.10745

'4321'

Completion of the Vector LQ + RHN solution from 1807.10745

- Field content

Vector-like fermions

Field	SU(4)	SU(3)'	SU(2) _L	U(1)'
$\Psi_{L,R}$	4	1	2	0
$\Psi_{R,L}^u$	4	1	1	1/2
$\Psi_{R,L}^d$	4	1	1	-1/2

1 family

Decomposition under the SM:

$$\Psi_{L,R} = \begin{pmatrix} Q'_{L,R} \\ L'_{L,R} \end{pmatrix} \quad \Psi_{L,R}^u = \begin{pmatrix} U'_{L,R} \\ N'_{L,R} \end{pmatrix}$$

$$\Psi_{L,R}^{ud} = \begin{pmatrix} D'_{L,R} \\ E'_{L,R} \end{pmatrix} \quad \text{*Full 'Pati-Salam' family}$$

$i=1,2,3$ SM-like fermions

Field	SU(4)	SU(3)'	SU(2) _L	U(1)'
q_L^i	1	3	2	1/6
u_R^i	1	3	1	2/3
d_R^i	1	3	1	-1/3
ℓ_L^i	1	1	2	-1/2
e_R^i	1	1	1	-1

Light-sterile neutrinos

- 4321 > 321 breaking from 1708.08450
- Yukawa

$$\mathcal{L}_Y \supset -\bar{q}'_L Y_d H d'_R - \bar{q}'_L Y_u \tilde{H} u'_R - \bar{\ell}'_L Y_e H e'_R \quad (9)$$

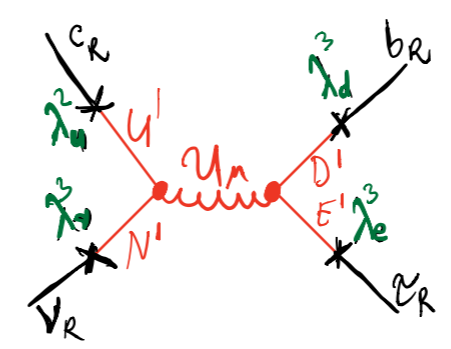
$$- \bar{q}'_L \lambda_q \Omega_3^T \Psi_R - \bar{\ell}'_L \lambda_\ell \Omega_1^T \Psi_R - \bar{\Psi}_L M \Psi_R + \text{h.c.},$$

$$- \bar{\Psi}_L^u \lambda_u \Omega_3^* \Psi_R^u - \bar{\Psi}_L^u \lambda_\nu \Omega_1^* \Psi_R^u - \bar{\Psi}_L^u M^u \Psi_R^u$$

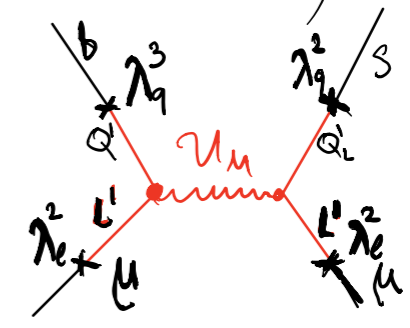
$$- \bar{\Psi}_L^d \lambda_d \Omega_3^* \Psi_R^d - \bar{\Psi}_L^d \lambda_e \Omega_1^* \Psi_R^d - \bar{\Psi}_L^d M^d \Psi_R^d + \text{h.c.}$$

- Anomalies

$$\mathcal{R}(\mathbb{D}^{(*)})$$



$$\mathcal{R}(K^{(*)})$$





[LHCb please
stop this
madness]

Backup slides

'3221' model

Extended gauge symmetry

$$\mathcal{G} \equiv SU(3)_c \times SU(2)_L \times SU(2)_V \times U(1)'$$

SSB: $\langle H_V \rangle$ ↓

$$G_{\text{SM}} \equiv SU(3)_c \times SU(2)_L \times U(1)_Y$$

3 broken generators

$(1, 1, +1)$

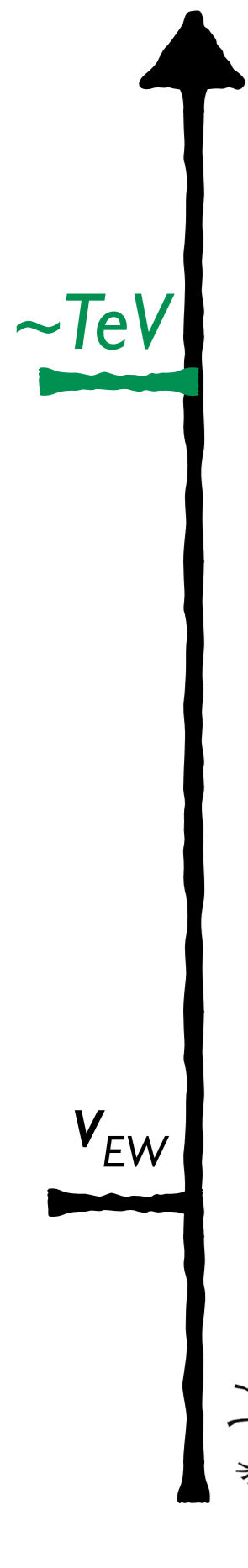
W'

$(1, 1, 0)$

Z'

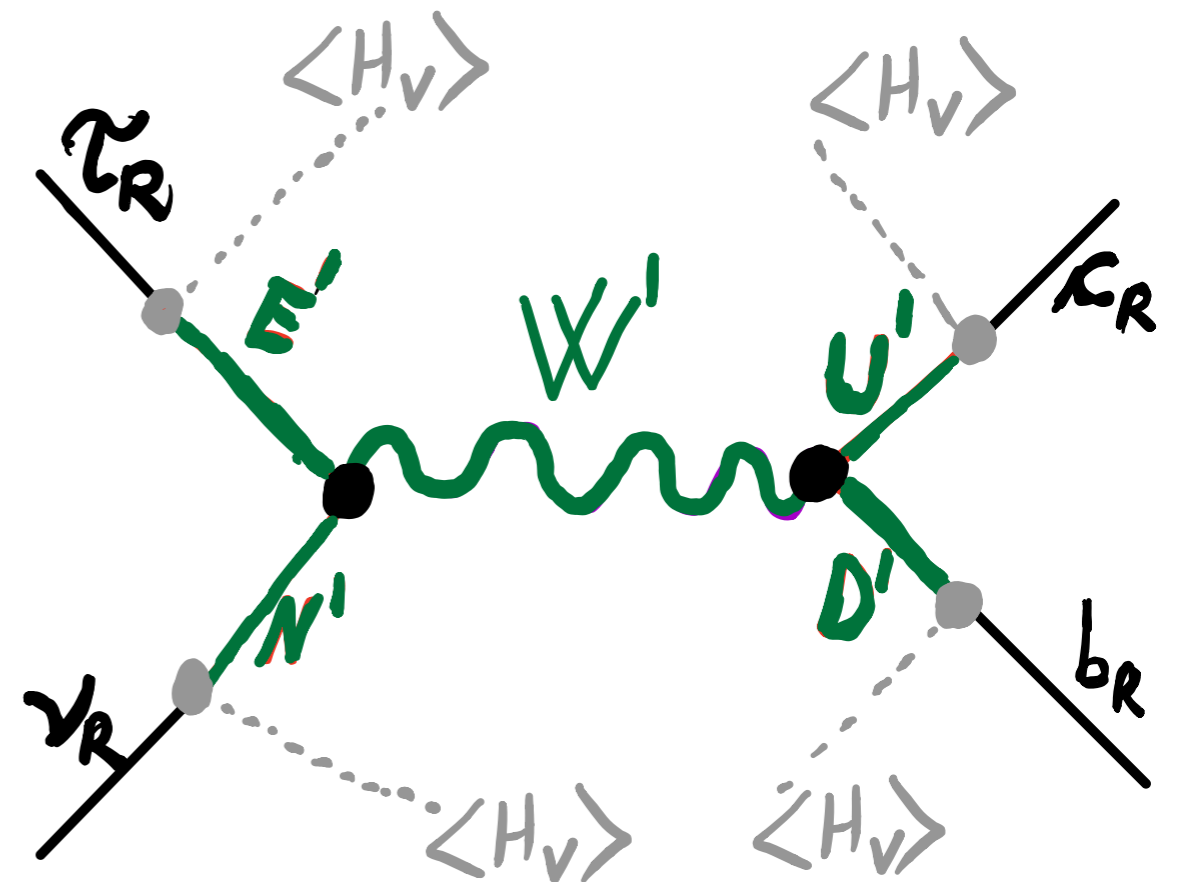
$R(D^{(*)})$

$$\mathcal{L}_{\text{VR}} = \frac{C_{ij,k}}{\Lambda_{\text{eff}}^2} (\bar{u}_R^i \gamma^\mu d_R^j) (\bar{e}_R^k \gamma_\mu N_R)$$



'3221' model**Matter content**

Field	$SU(3)_c$	$SU(2)_L$	$SU(2)_V$	$U(1)'$
SM-like chiral fermions				
q_L^i	3	2	1	1/6
ℓ_L^i	1	2	1	-1/2
u_R^i	3	1	1	2/3
d_R^i	3	1	1	-1/3
e_R^i	1	1	1	-1
ν_R^i	1	1	1	0
Extra vector-like fermions				
$Q'_{L,R}$	3	1	2	1/6
$L'_{L,R}$	1	1	2	-1/2
Scalars				
H	1	2	1	1/2
H_V	1	1	2	1/2

**FL-23 case:**

$$\lambda_d^i \sim (0, 0, 1) \quad \lambda_u^i \sim (0, 1, 0)$$

$$\begin{aligned} \mathcal{L} \supset \mathcal{L}_{\text{Yuk}}^{\text{SM}} &- \lambda_d^i \bar{Q}'_L H_V d_R^i - \lambda_u^i \bar{Q}'_L \tilde{H}_V u_R^i \\ &- \lambda_e^i \bar{L}'_L H_V e_R^i - \lambda_\nu^i \bar{L}'_L \tilde{H}_V \nu_R^i \\ &- M_Q \bar{Q}'_L Q'_R - M_L \bar{L}'_L L'_R + \text{h.c.} \end{aligned}$$

:) FV Z' couplings uncorrelated!

'4321' model

[Di Luzio, AG, Nardecchia],
Phys.Rev. D96 (2017)
115011

Extended gauge symmetry

$$G \equiv SU(4) \times SU(3)' \times SU(2)_L \times U(1)'$$

$\alpha = 1, \dots, 15$ $a = 1, \dots, 8$ $i = 1, 2, 3$
 H_μ^α $G_\mu'^a$ W_μ^i B'_μ



SSB: $\langle \Omega_3 \rangle, \langle \Omega_1 \rangle$
 $\Omega_3 = (\bar{4}, 3, 1, 1/6)$
 $\Omega_1 = (\bar{4}, 1, 1, -1/2)$

$$G_{\text{SM}} \equiv SU(3)_c \times SU(2)_L \times U(1)_Y$$

Embedding:

$$SU(3)_c = (SU(3)_4 \times SU(3)')_{\text{diag}}$$

$$U(1)_Y = (U(1)_4 \times U(1)')_{\text{diag}}$$

where

$$SU(3)_4 \times U(1)_4 \subset SU(4)$$

$$g_s = \frac{g_4 g_3}{\sqrt{g_4^2 + g_3^2}} \quad g_Y = \frac{g_4 g_1}{\sqrt{g_4^2 + \frac{2}{3}g_1^2}}$$

Massive gauge boson spectrum:

G/G_{SM}

Leptoquark

$$(3, 1, 2/3) \quad M_U = \frac{1}{2} g_4 \sqrt{v_1^2 + v_3^2}$$

$$U_\mu^{1,2,3} = \frac{1}{\sqrt{2}} (H_\mu^{9,11,13} - i H_\mu^{10,12,14})$$

Color octet: $(8, 1, 0)$

Z': $(1, 1, 0)$

$$g_\mu'^a = \frac{g_4 H_\mu^a - g_3 G_\mu'^a}{\sqrt{g_4^2 + g_3^2}}$$

$$Z'_\mu = \frac{g_4 H_\mu^{15} - \sqrt{\frac{2}{3}} g_1 B'_\mu}{\sqrt{g_4^2 + \frac{2}{3}g_1^2}}$$

$$M_{g'} = \frac{1}{\sqrt{2}} \sqrt{g_4^2 + g_3^2} v_3$$

$$M_{Z'} = \frac{1}{2} \sqrt{\frac{3}{2}} \sqrt{g_4^2 + \frac{2}{3}g_1^2} \sqrt{v_1^2 + \frac{1}{3}v_3^2}$$

Orthogonal field: **Gluon**

Orthogonal field: **Hypercharge**

[Georgi, Nakai],
1606.05865
[Diaz, Schmaltz,
Zhong],
1706.05033