

CPV in charm decays into neutral kaons

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Direct CP violation

- Direct CP asymmetry established in kaon and bottom decays
- Not yet in charm decays, so its search is a top mission in particle physics
- Usually arises from interference between tree and penguin amplitudes
- Most precise measurement from LHCb

$$\begin{aligned}\Delta A_{CP} &\equiv A_{CP}(D^0 \rightarrow K^+ K^-) - A_{CP}(D^0 \rightarrow \pi^+ \pi^-) \\ &= (-1.0 \pm 0.8 \pm 0.3) \times 10^{-3},\end{aligned}$$

Tree-tree interference

- $D^0 \rightarrow K^+K^-$, $\pi^+\pi^-$ are singly Cabibbo suppressed modes

$$T_{SCS} \propto V_{cd(s)}^* V_{ud(s)}$$

$$P \propto V_{ci}^* V_{ui} \exp(i\delta)$$

order λ (Wolfenstein parameter)

strong phase

- Direct CP asymmetry can also be induced by interference between Cabibbo favored and doubly Cabibbo suppressed tree amplitudes

$$T_{CF} \propto V_{cs}^* V_{ud}$$

$$T_{DCS} \propto V_{cd}^* V_{us} \exp(i\delta)$$

order unity

order λ^2

Weak phase of DCS/CF

- Standard parametrization of CKM matrix

$$\begin{aligned}
 & \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13} e^{-i\delta_{13}} \\ 0 & 1 & 0 \\ -s_{13} e^{i\delta_{13}} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix} \\
 & = \begin{bmatrix} c_{12} c_{13} & s_{12} c_{13} & s_{13} e^{-i\delta_{13}} \\ -s_{12} c_{23} - c_{12} s_{23} s_{13} e^{i\delta_{13}} & c_{12} c_{23} - s_{12} s_{23} s_{13} e^{i\delta_{13}} & s_{23} c_{13} \\ s_{12} s_{23} - c_{12} c_{23} s_{13} e^{i\delta_{13}} & -c_{12} s_{23} - s_{12} c_{23} s_{13} e^{i\delta_{13}} & c_{23} c_{13} \end{bmatrix}.
 \end{aligned}$$

$$\phi \equiv \text{Arg} [-V_{cd}^* V_{us} / V_{cs}^* V_{ud}]$$

$$= (-6.2 \pm 0.4) \times 10^{-4}$$

Belle data

- Belle measurement with 3.2 sigma from zero

$$A_{CP}(D^+ \rightarrow \pi^+ K_S^0) = (-3.63 \pm 0.94 \pm 0.67) \times 10^{-3}$$

- Note that K_S is reconstructed via decay into two charged pions
- K_L also decays into two pions
- Data mainly due to kaon mixing of order 10^{-3}
- Postulated in literature: **deducting kaon mixing, data reveal direct CP asymmetry in charm decays**

Lipkin, Xing 1999

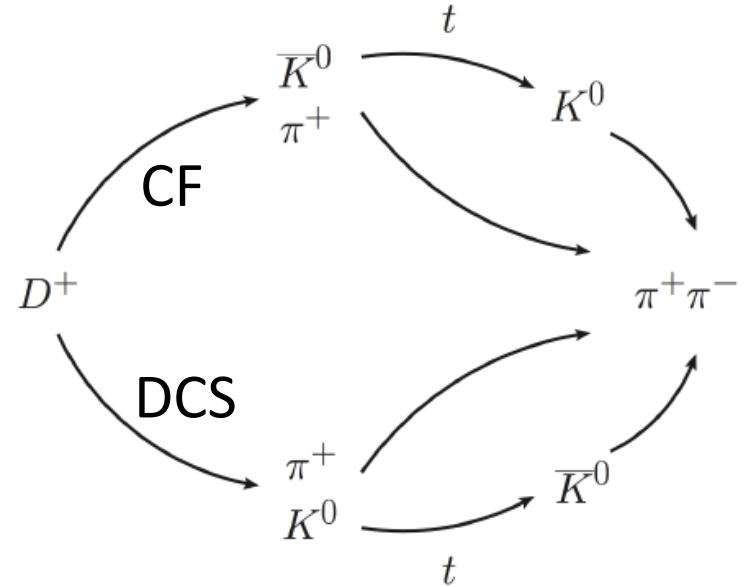
D'Ambrosio, Gao 2001

Bianco, Fabbri, Benson, Bigi 2003

Grossman, Nir 2012

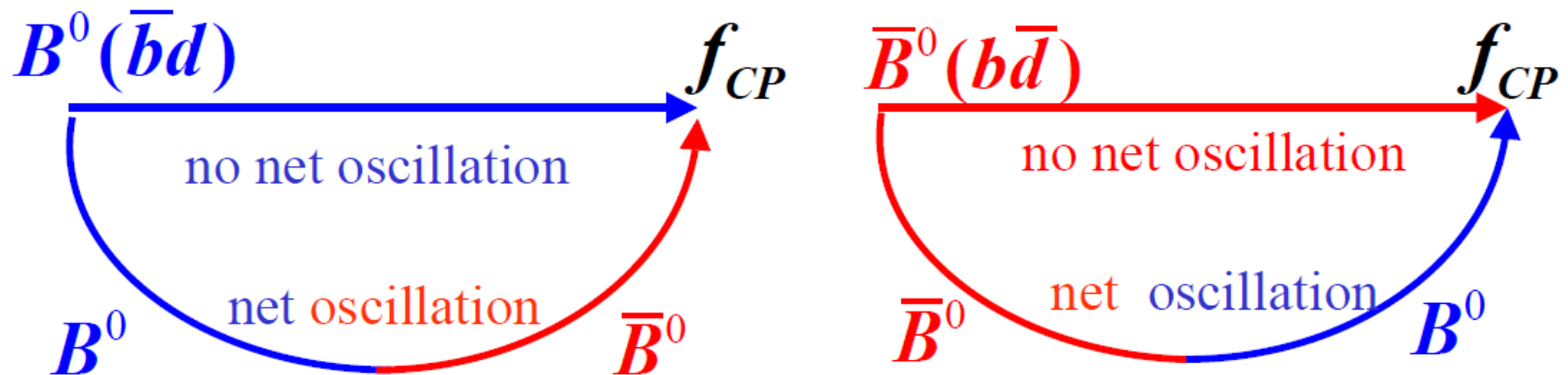
Our observation

- This is not correct
- Kaon mixing induces a new CP observable
- More complicated than ordinary mixing-induced CP asymmetry in, say, $B^0(t) \rightarrow \pi^+\pi^-$: both oscillation and decay occur in mother particle
- The new observable arises from **interference between mother decay and daughter mixing**



“Strong phase” from oscillation

- Ordinary mixing-induced CP violation



- $\exp(i \Delta m t)$ plays the role of “strong phase”
- Feature of CP violation from oscillation:
as $t \rightarrow 0$, it vanishes

Time-dependent CP violation

- The rest is detail
- Consider

$$A_{CP}(t) \equiv \frac{\Gamma_{\pi\pi}(t) - \bar{\Gamma}_{\pi\pi}(t)}{\Gamma_{\pi\pi}(t) + \bar{\Gamma}_{\pi\pi}(t)}$$

$$\Gamma_{\pi\pi}(t) \equiv \Gamma(D \rightarrow fK(t) (\rightarrow \pi^+ \pi^-))$$

$$\bar{\Gamma}_{\pi\pi}(t) \equiv \Gamma(\bar{D} \rightarrow \bar{f}K(t) (\rightarrow \pi^+ \pi^-))$$

↑
 $K^0(t)$ or $\bar{K}^0(t)$

Relevant variables

- Kaon mixing $|K_{S,L}^0\rangle = p|K^0\rangle \mp q|\bar{K}^0\rangle$

indirect CP
violation 

$$q/p = (1 - \epsilon)/(1 + \epsilon)$$

$$|\epsilon| = (2.228 \pm 0.011) \times 10^{-3} \quad \phi_\epsilon = 43.52 \pm 0.05^\circ$$

- averaged width $\Gamma = (\Gamma_S + \Gamma_L)/2$
- Width difference $\Delta\Gamma \equiv \Gamma_S - \Gamma_L$
- Mass difference $\Delta m \equiv m_L - m_S$
- Ratio of DCS/CF

$$\mathcal{A}(D \rightarrow fK^0)/\mathcal{A}(D \rightarrow f\bar{K}^0) = r_f e^{i(\phi + \delta_f)}$$

$$r_f \propto |V_{cd}^* V_{us}/V_{cs}^* V_{ud}| \sim \mathcal{O}(10^{-2})$$

3 CP observables

- Neglect direct CP asymmetry in $K \rightarrow \pi\pi$

$$A_{CP}(t) \simeq \left[A_{CP}^{\bar{K}^0}(t) + A_{CP}^{\text{dir}}(t) + A_{CP}^{\text{int}}(t) \right] / D(t)$$

- Known kaon mixing $D(t) = e^{-\Gamma st} (1 - 2r_f \cos \delta_f \cos \phi)$

$$A_{CP}^{\bar{K}^0}(t) = 2e^{-\Gamma st} \underline{\mathcal{R}e(\epsilon)} - 2e^{-\Gamma t} \left[\mathcal{R}e(\epsilon) \cos(\Delta mt) + \mathcal{I}m(\epsilon) \sin(\Delta mt) \right]$$

- Direct CP asymmetry

$$A_{CP}^{\text{dir}}(t) = e^{-\Gamma st} \underline{2r_f} \sin \delta_f \underline{\sin \phi}$$

- New observable

$$A_{CP}^{\text{int}}(t) = -\underline{4r_f} \cos \phi \sin \delta_f \left[e^{-\Gamma st} \underline{\mathcal{I}m(\epsilon)} - e^{-\Gamma t} \left(\mathcal{I}m(\epsilon) \cos(\Delta mt) - \mathcal{R}e(\epsilon) \sin(\Delta mt) \right) \right]$$

Global fits

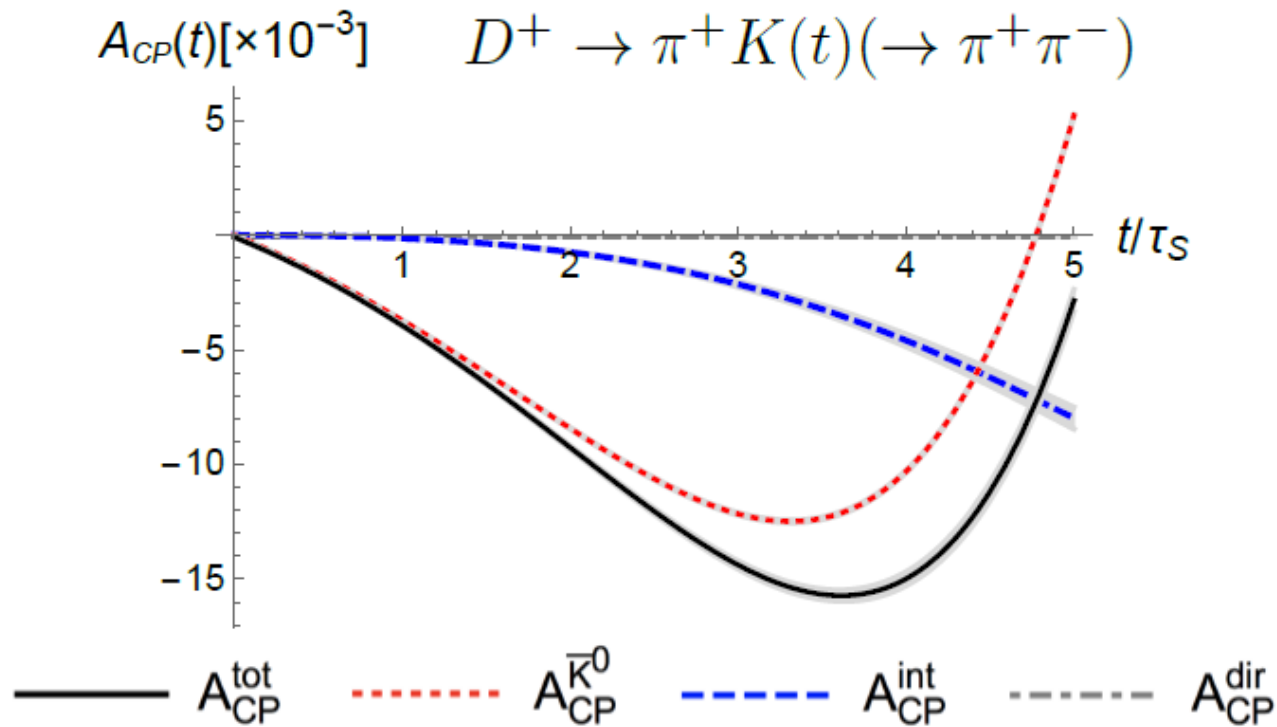
- Adopt factorization-assisted topological-amplitude approach
- DCS/CF parameters for $D^+ \rightarrow \pi^+ K_S^0$ and $D_s^+ \rightarrow K^+ K_S^0$ maximize new CP observable
 $r_{\pi^+} = -0.073 \pm 0.004,$ $\delta_{\pi^+} = -1.39 \pm 0.05,$
 $r_{K^+} = -0.055 \pm 0.002,$ $\delta_{K^+} = +1.45 \pm 0.05$
- Direct CP asymmetry at t=0

$$A_{CP}^{\text{dir}}(D^+ \rightarrow \pi^+ K_S^0) = (-8.6 \pm 0.4) \times 10^{-5}$$

$$A_{CP}^{\text{dir}}(D_s^+ \rightarrow K^+ K_S^0) = (6.6 \pm 0.3) \times 10^{-5}.$$

Numerical results

- Direct CP asymmetry always negligible
- New observable becomes comparable to kaon mixing as $t \sim$ few times of K short lifetime



Experimental verification

- To verify the new CP violation effect, measure

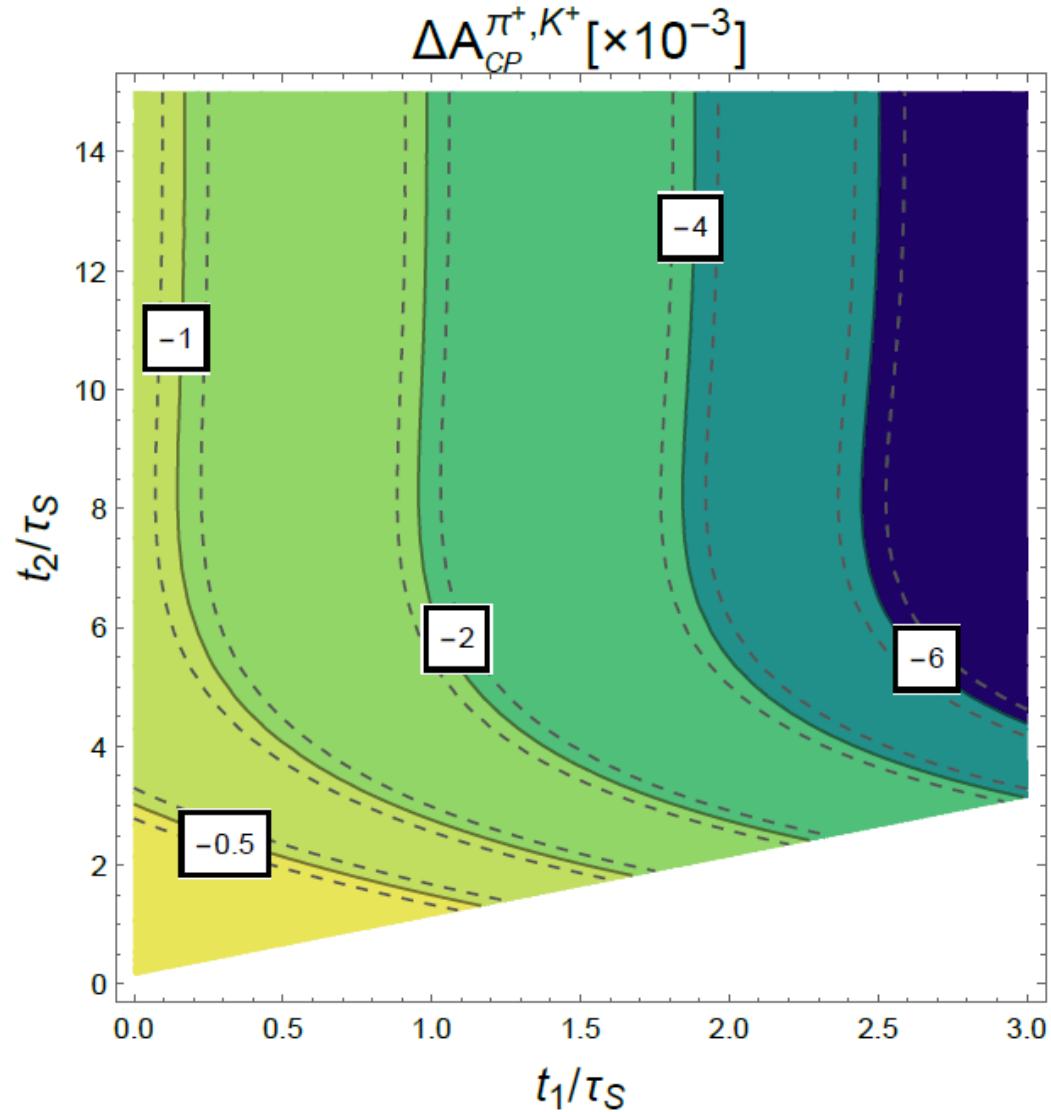
$$\begin{aligned}\Delta A_{CP}^{\pi^+, K^+} &\equiv A_{CP}^{D^+ \rightarrow \pi^+ K_S^0}(t_1, t_2) - A_{CP}^{D_s^+ \rightarrow K^+ K_S^0}(t_1, t_2) \\ &\simeq A_{CP}^{\text{int}, D^+ \rightarrow \pi^+ K_S^0}(t_1, t_2) - A_{CP}^{\text{int}, D_s^+ \rightarrow K^+ K_S^0}(t_1, t_2)\end{aligned}$$

where time-integrated CP asymmetry

$$A_{CP}(t_1, t_2) = \frac{\int_{t_1}^{t_2} \left[A_{CP}^{\bar{K}^0}(t) + A_{CP}^{\text{dir}}(t) + A_{CP}^{\text{int}}(t) \right] dt}{\int_{t_1}^{t_2} D(t) dt}$$

- Kaon mixing cancels in the difference, and direct CP asymmetry is negligible

Theoretical prediction



Conclusion

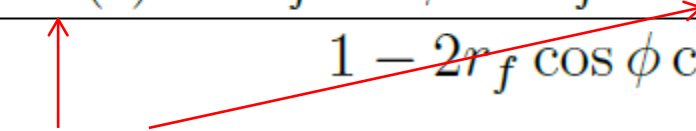
- New effect, from interference between mother decay and daughter mixing, can be measured at Belle II and LHCb upgrade with precision of $\mathcal{O}(10^{-4})$
- If verified, need to be subtracted in order to extract direct CP asymmetry in charm decays
- Then direct CP asymmetry from DCS and CF interference, **both being tree and better controlled by branching-ratio data**, can be used to test new physics

Direct CPA in Belle data

- Recall Belle data

$$A_{CP}(D^+ \rightarrow \pi^+ K_S^0) = (-3.63 \pm 0.94 \pm 0.67) \times 10^{-3}$$

- Consider the integrated CP asymmetry in the limit

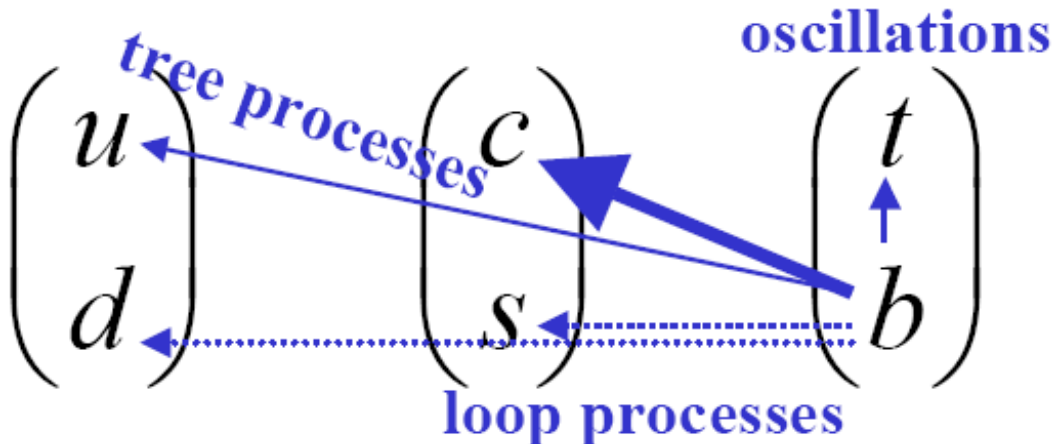
$$A_{CP}(t_1 \ll \tau_S \ll t_2 \ll \tau_L) \simeq \frac{-2\mathcal{R}e(\epsilon) + 2r_f \sin \phi \sin \delta_f - 4\mathcal{I}m(\epsilon)r_f \cos \phi \sin \delta_f}{1 - 2r_f \cos \phi \cos \delta_f}$$


inputs

- Extract direct CP asymmetry from Belle data
 $(-0.06 \pm 1.15) \times 10^{-3}$

Back-up slides

Cabbibo-Kobayashi-Maskawa Matrix



$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

(Wolfenstein parametrization)

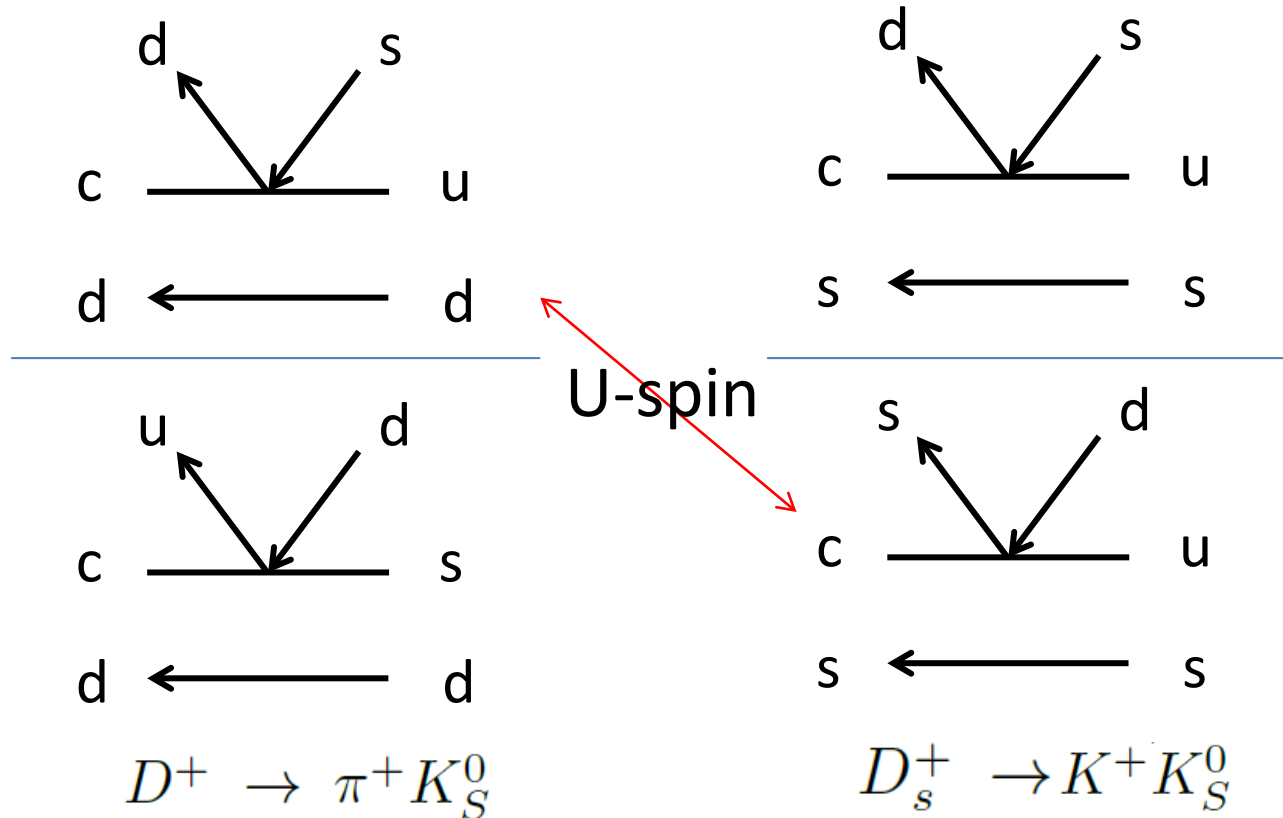


$$; \begin{pmatrix} 0.97 & 0.23 & 0.004 \\ -0.23 & 0.97 & 0.04 \\ 0.004 & -0.04 & 1 \end{pmatrix}$$

Weak phase, $\cancel{\phi}$
(magnitudes only)

U-spin symmetry

- Ratio of DCS/CF



- Reason why strong phase opposite in sign