

Experimental review of flavour anomalies in b -hadron decays

T. Blake for the LHCb collaboration

CKM 2018, Heidelberg

Flavour anomalies

1. $b \rightarrow s\ell^+\ell^-$ processes

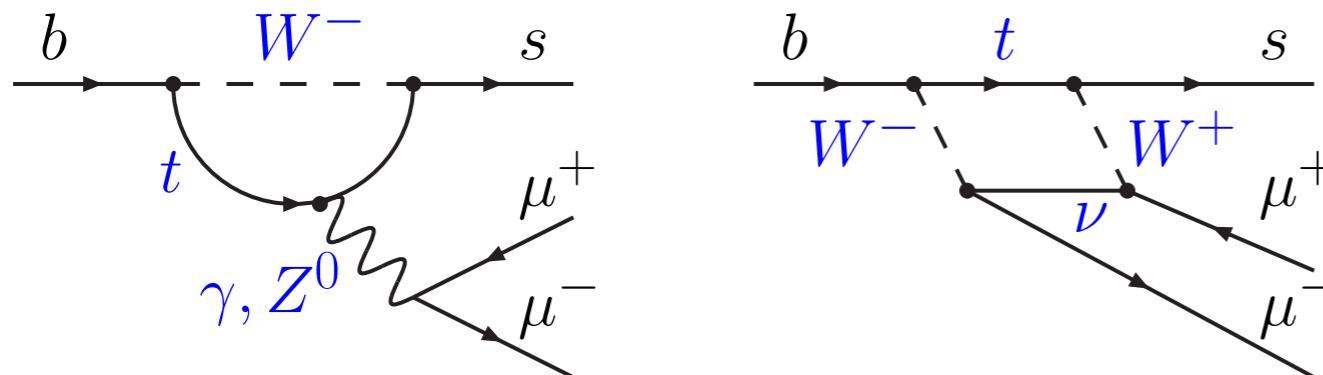
- Rate and angular distribution of exclusive $b \rightarrow s\mu^+\mu^-$ decays.
- Relative rates of $b \rightarrow se^+e^-$ and $b \rightarrow s\mu^+\mu^-$ decays ($R_{K^{(*)}}$)

2. $b \rightarrow c\tau^-\bar{\nu}_\tau$ decays

- Rate of $b \rightarrow c\tau^-\bar{\nu}_\tau$ decays versus decays with e/μ ($R(D^{(*)})$).

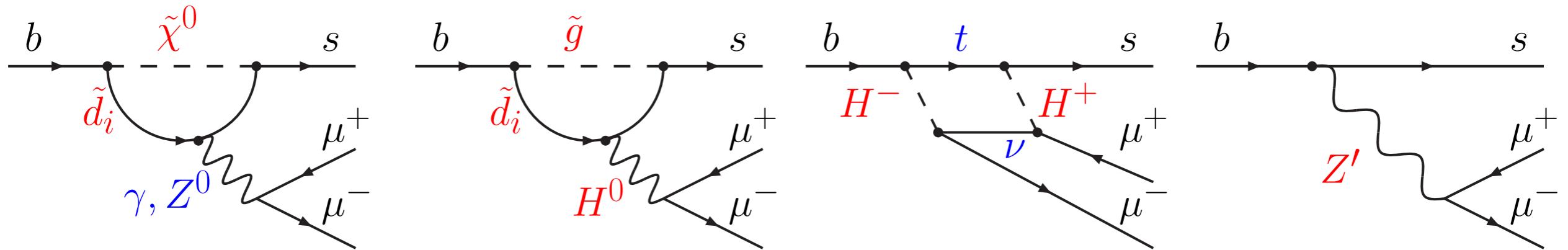
Electroweak penguin decays

- Flavour changing neutral current transitions that only occur at loop order (and beyond) in the SM.



SM diagrams involve the charged current interaction.

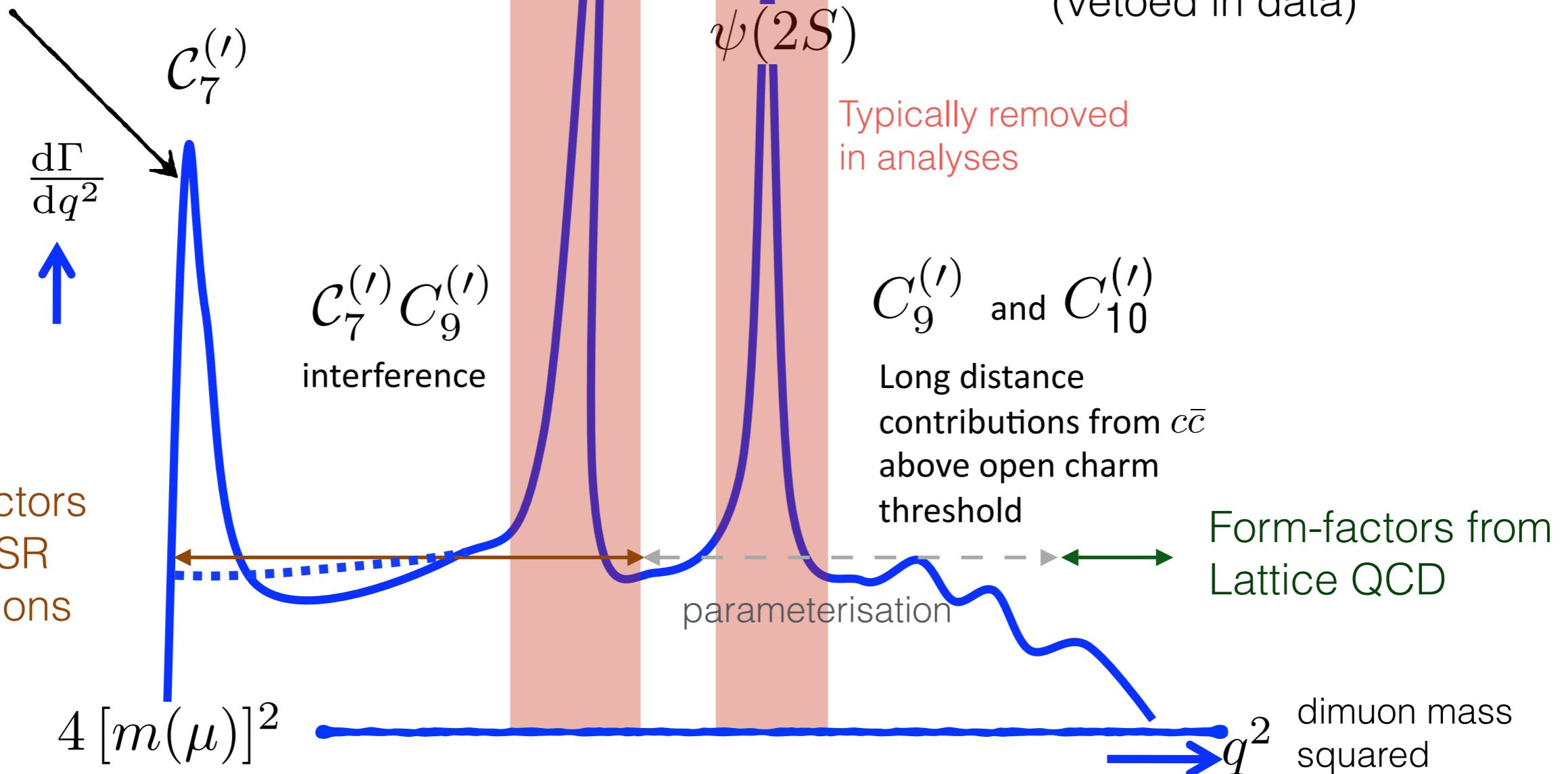
- New particles can also contribute:



enhancing/suppressing decay rates, introducing new sources of CP violation and/or modifying the angular distribution of the final-state particles.

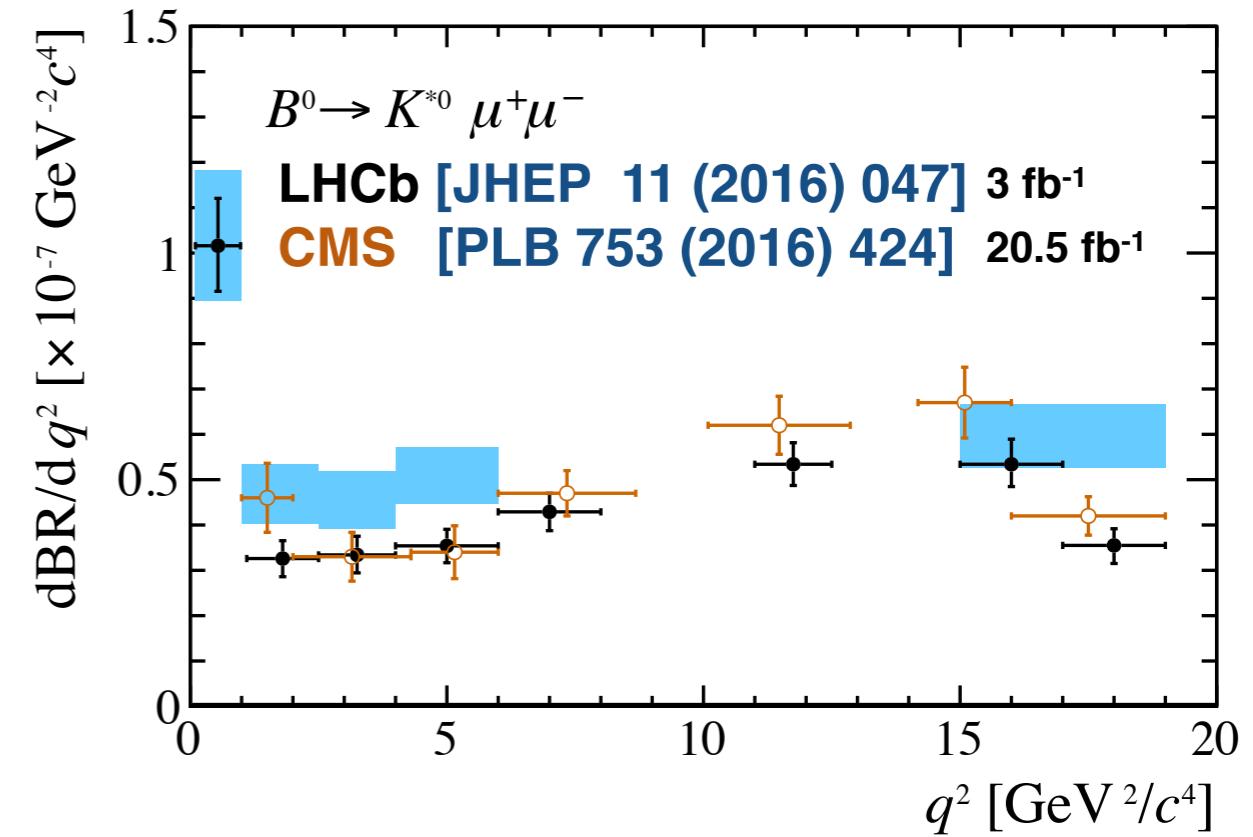
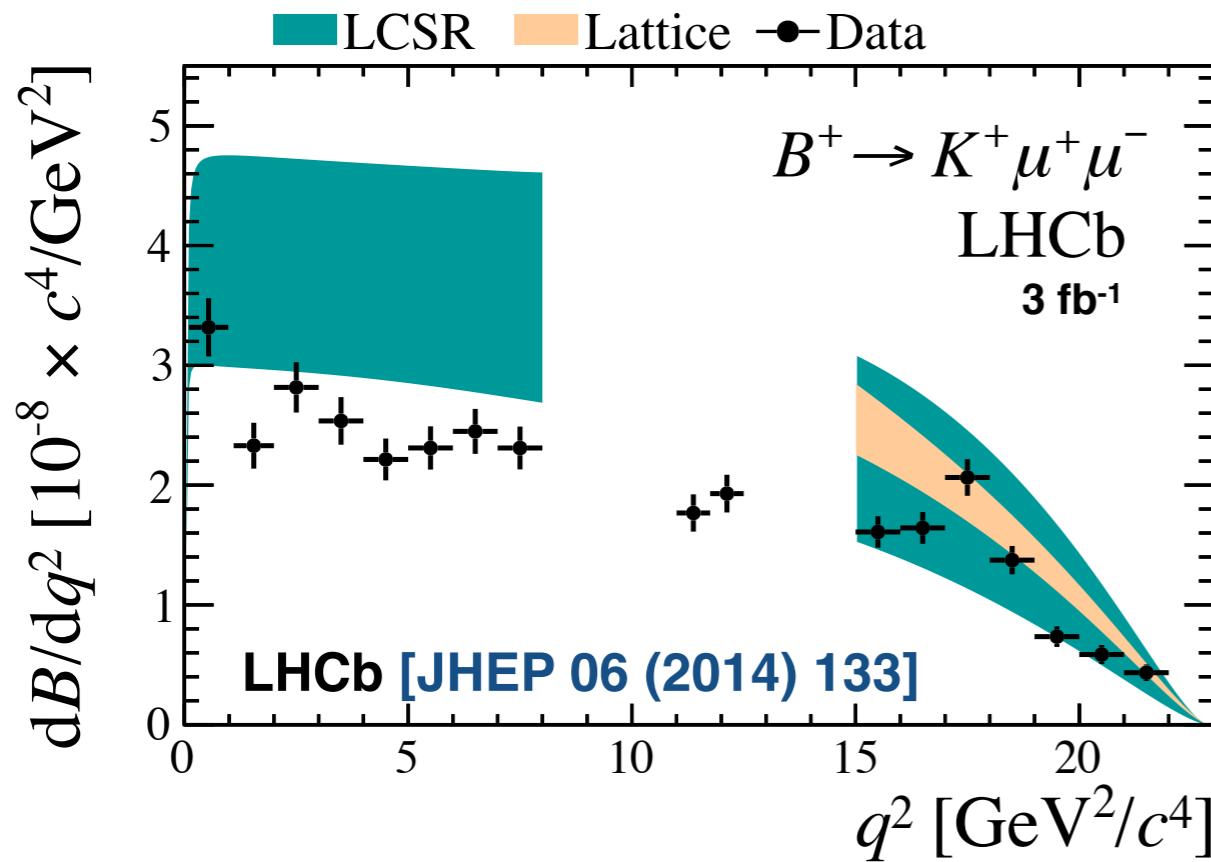
Expected $d\Gamma/dq^2$ spectrum

Photon pole enhancement
(no pole for
 $B \rightarrow P\ell\ell$ decays)



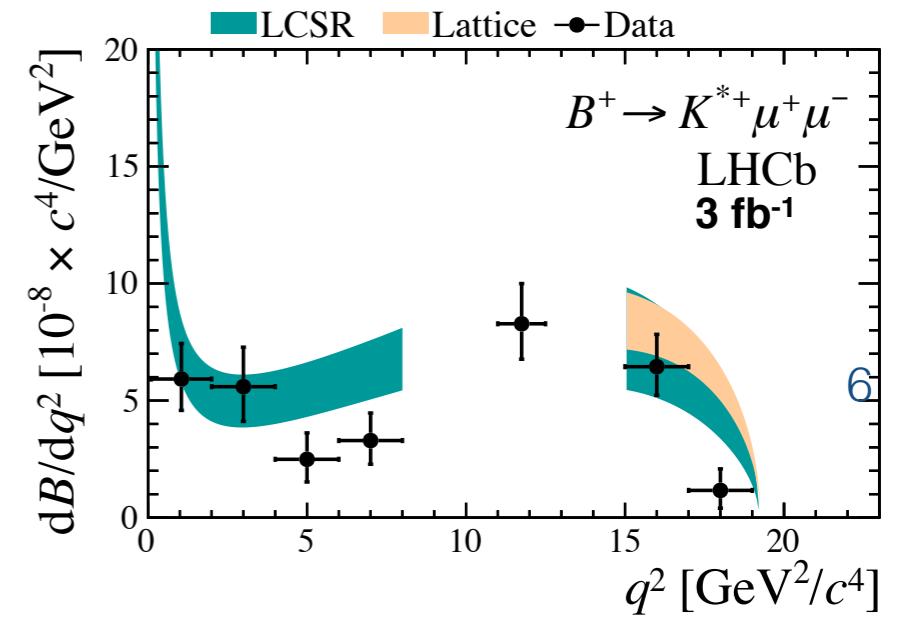
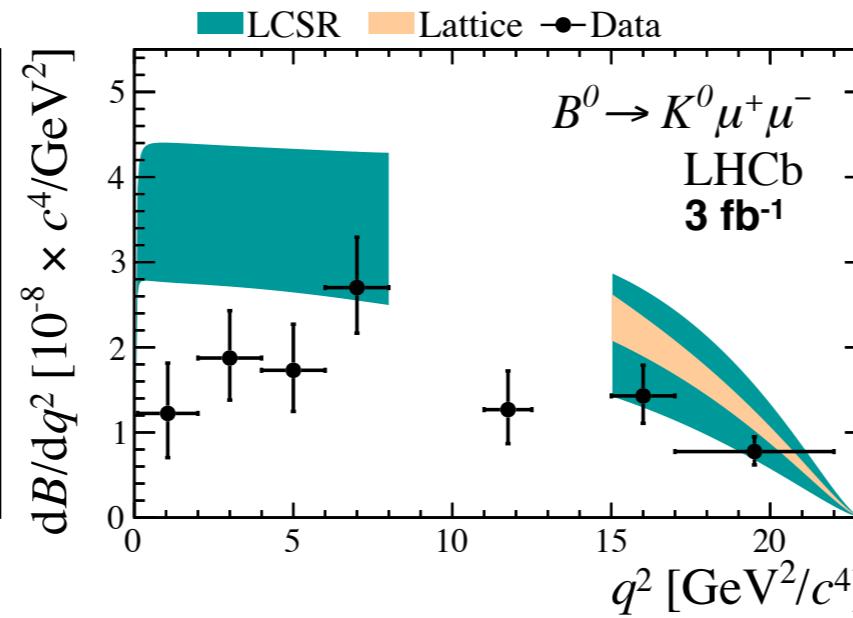
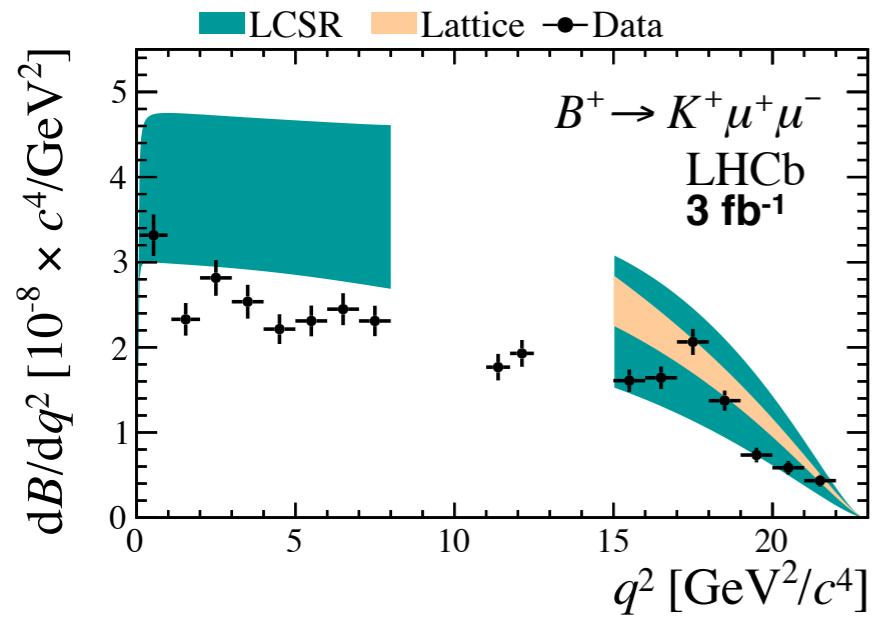
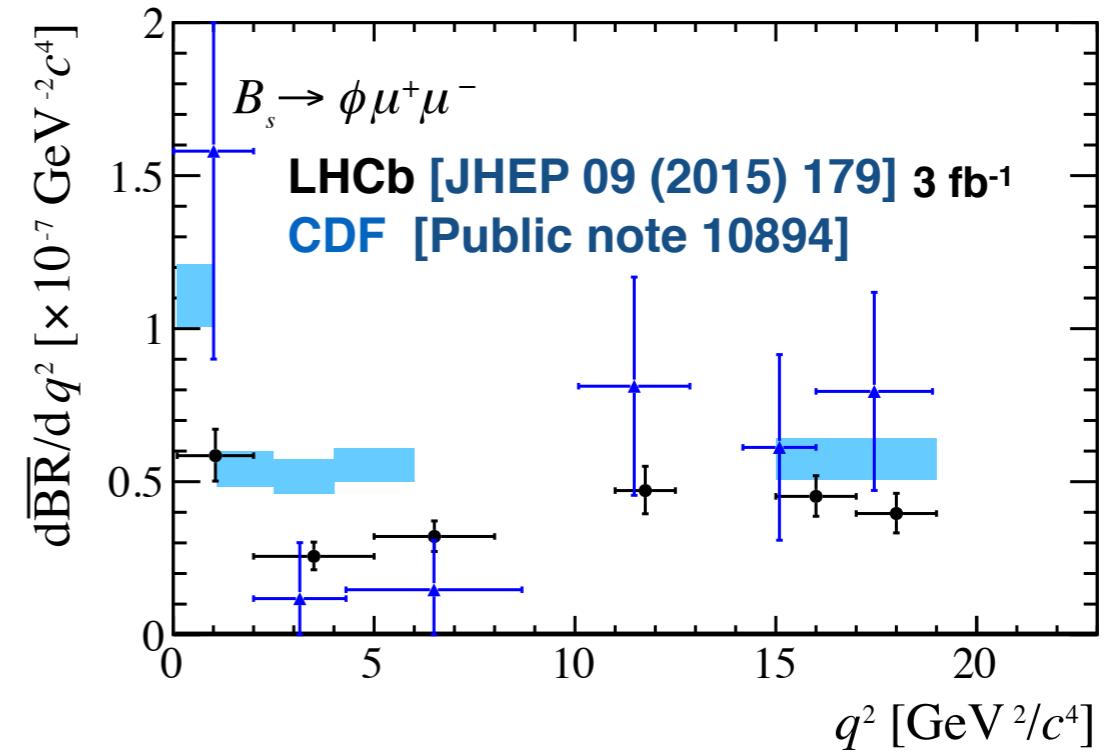
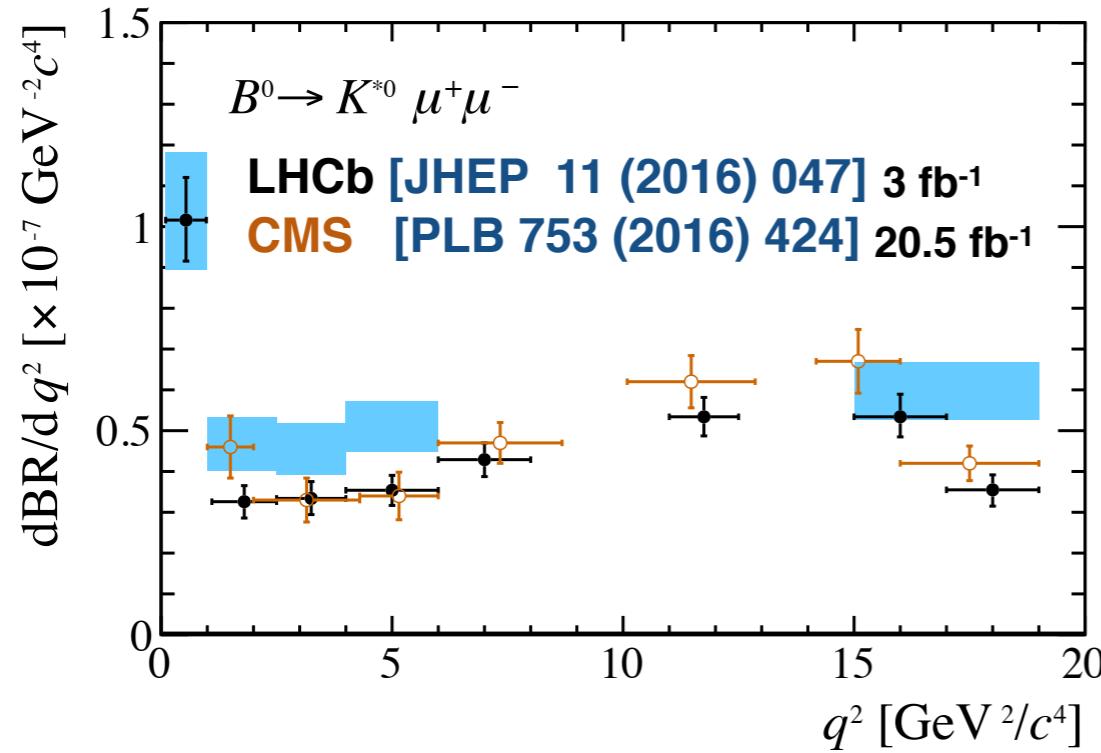
Branching fraction measurements

- We already have precise measurements of branching fractions from the Run1 data, with at least comparable precision to SM expectations:



- SM predictions have large theoretical uncertainties from hadronic form factors (3 for $B \rightarrow K$ and 7 for $B \rightarrow K^*$ decays). For details see **Bobeth et al [JHEP 01 (2012) 107]**, **Bouchard et al. [PRL111 (2013) 162002]**, **Altmannshofer & Straub [EPJC (2015) 75 382]**.

Branching fraction measurements



Measure smaller branching fractions than predicted by the SM

$B^0 \rightarrow K^{*0} \mu^+ \mu^-$ angular distribution

Complex angular distribution, described by three angles:

$$\frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \left. \frac{d^3(\Gamma + \bar{\Gamma})}{d\vec{\Omega}} \right|_P = \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K + \right.$$

$+ \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_l$

$- F_L \cos^2 \theta_K \cos 2\theta_l + S_3 \sin^2 \theta_K \sin^2 \theta_l \cos 2\phi$

$+ S_4 \sin 2\theta_K \sin 2\theta_l \cos \phi + S_5 \sin 2\theta_K \sin \theta_l \cos \phi$

$+ \frac{4}{3} A_{FB} \sin^2 \theta_K \cos \theta_l + S_7 \sin 2\theta_K \sin \theta_l \sin \phi$

$+ S_8 \sin 2\theta_K \sin 2\theta_l \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_l \sin 2\phi \right]$

fraction of longitudinal
polarisation of the K^*

↗

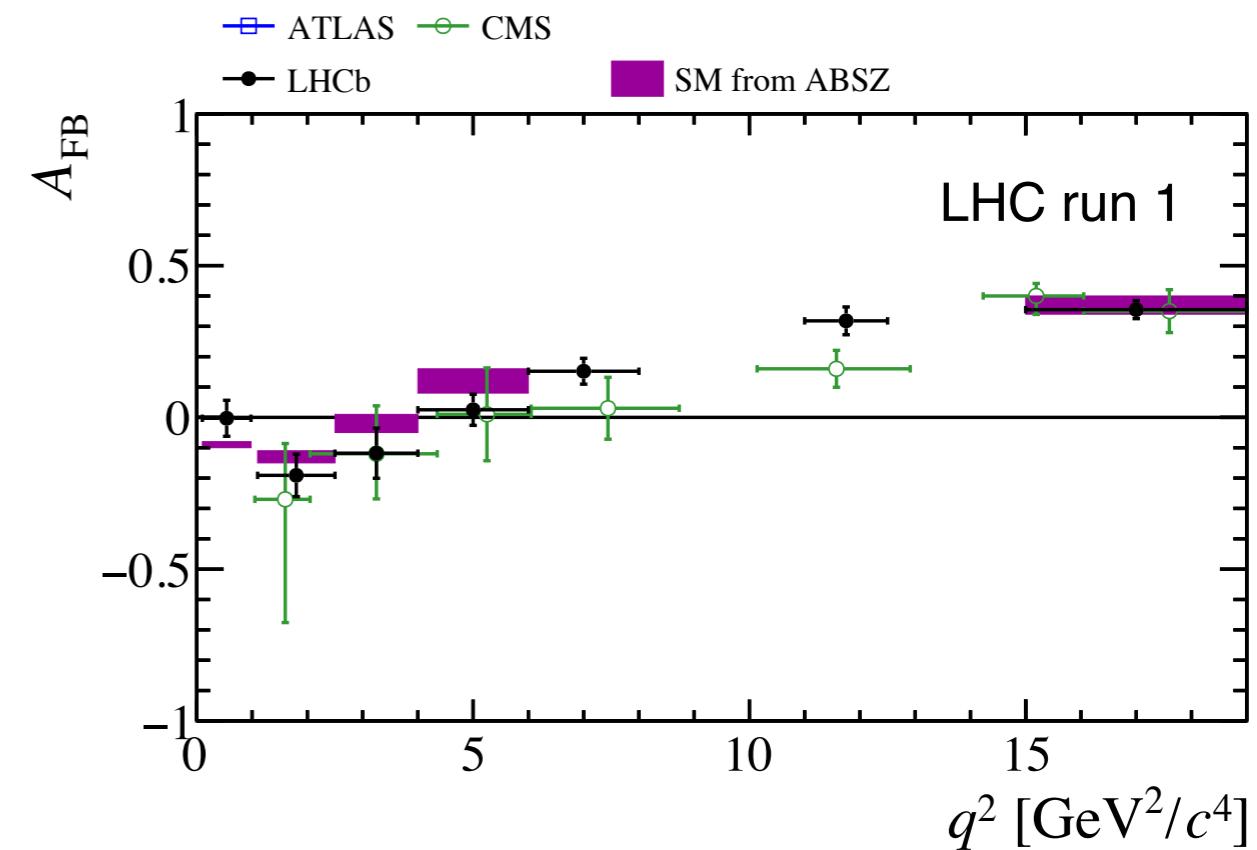
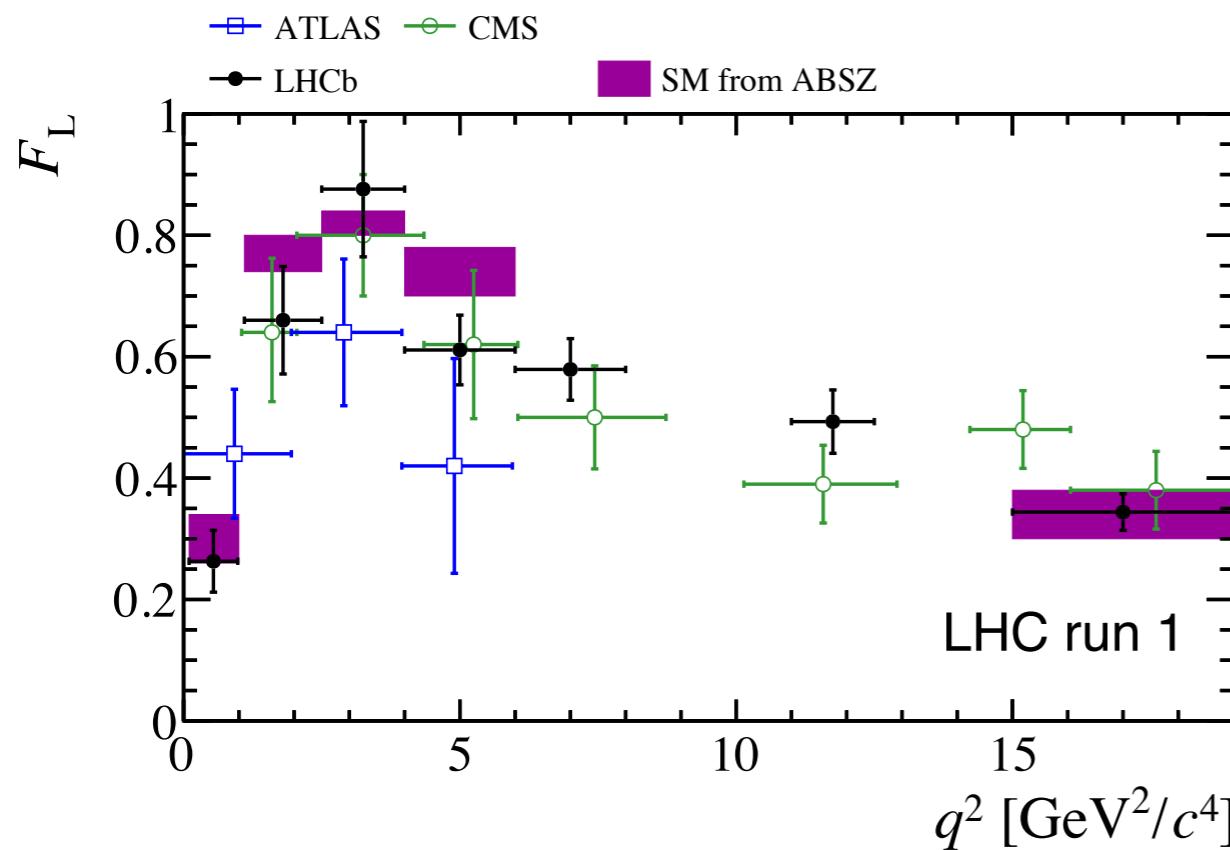
forward-backward
asymmetry of the
dilepton system

→

The observables depend on form-factors for the $B \rightarrow K^*$ transition plus the underlying short distance physics (Wilson coefficients).

Experiments can reduce the complexity by folding the angular distribution, see **LHCb**
[PRL 111 (2013) 191801]

$B^0 \rightarrow K^{*0} \mu^+ \mu^-$ angular observables

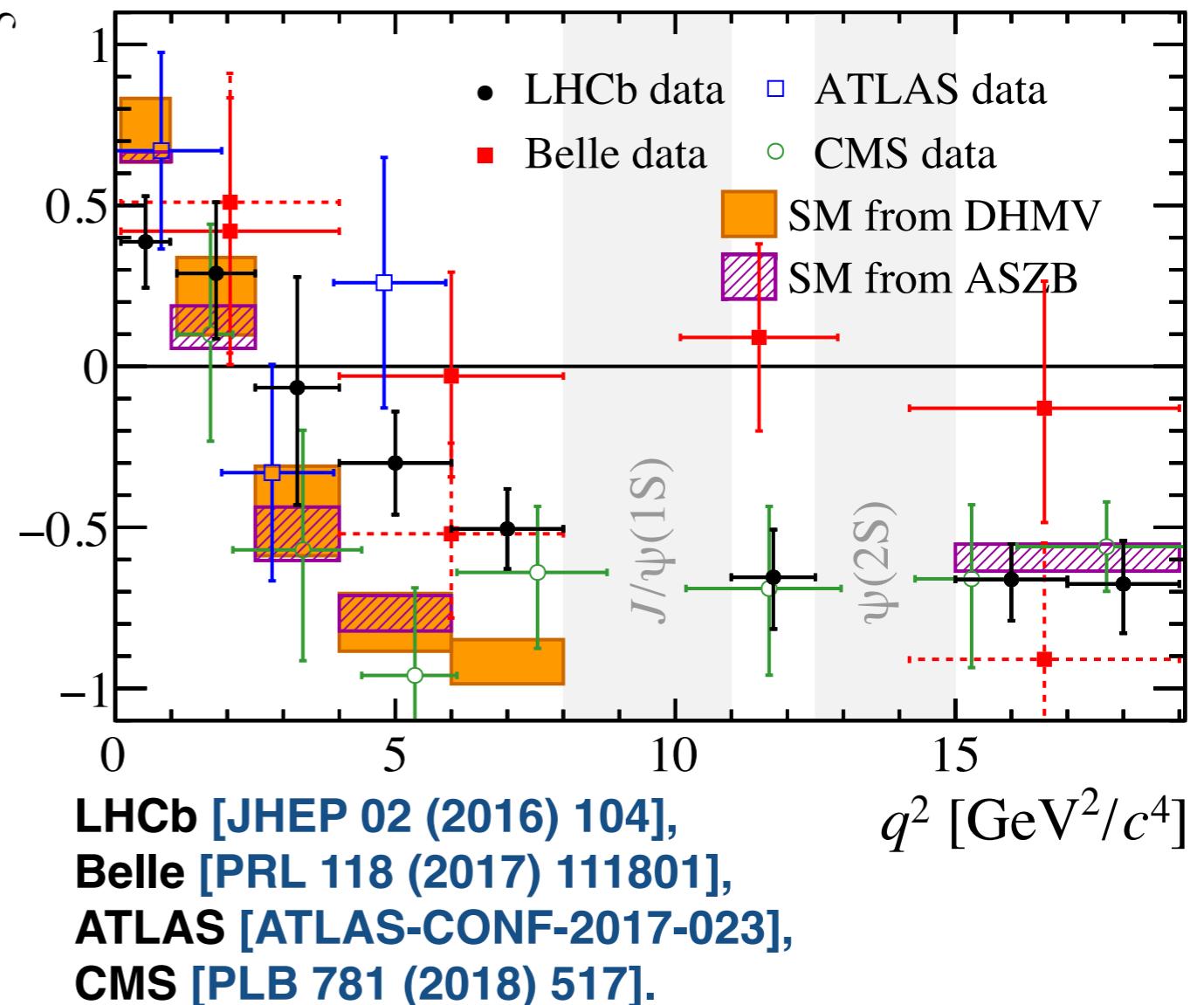


- Overlaying results for F_L and A_{FB} from LHCb [[JHEP 02 \(2016\) 104](#)] , CMS [[PLB 753 \(2016\) 424](#)] and ATLAS [[ATLAS-CONF-2017-023](#)].
- SM predictions based on
Altmannshofer & Straub [[EPJC 75 \(2015\) 382](#)]
LCSR form-factors from Bharucha, Straub & Zwicky, [[JHEP 08 \(2016\) 98](#)]
Lattice form-factors from Horgan, Liu, Meinel & Wingate [[arXiv:1501.00367](#)] } Joint fit performed

Form-factor “free” observables

- In QCD factorisation/SCET there are only two form-factors
 - One is associated with A_0 and the other A_{\parallel} and A_{\perp} .
- Can then construct ratios of observables which are independent of these soft form-factors at leading order, e.g.

$$P'_5 = S_5 / \sqrt{F_L(1 - F_L)}$$

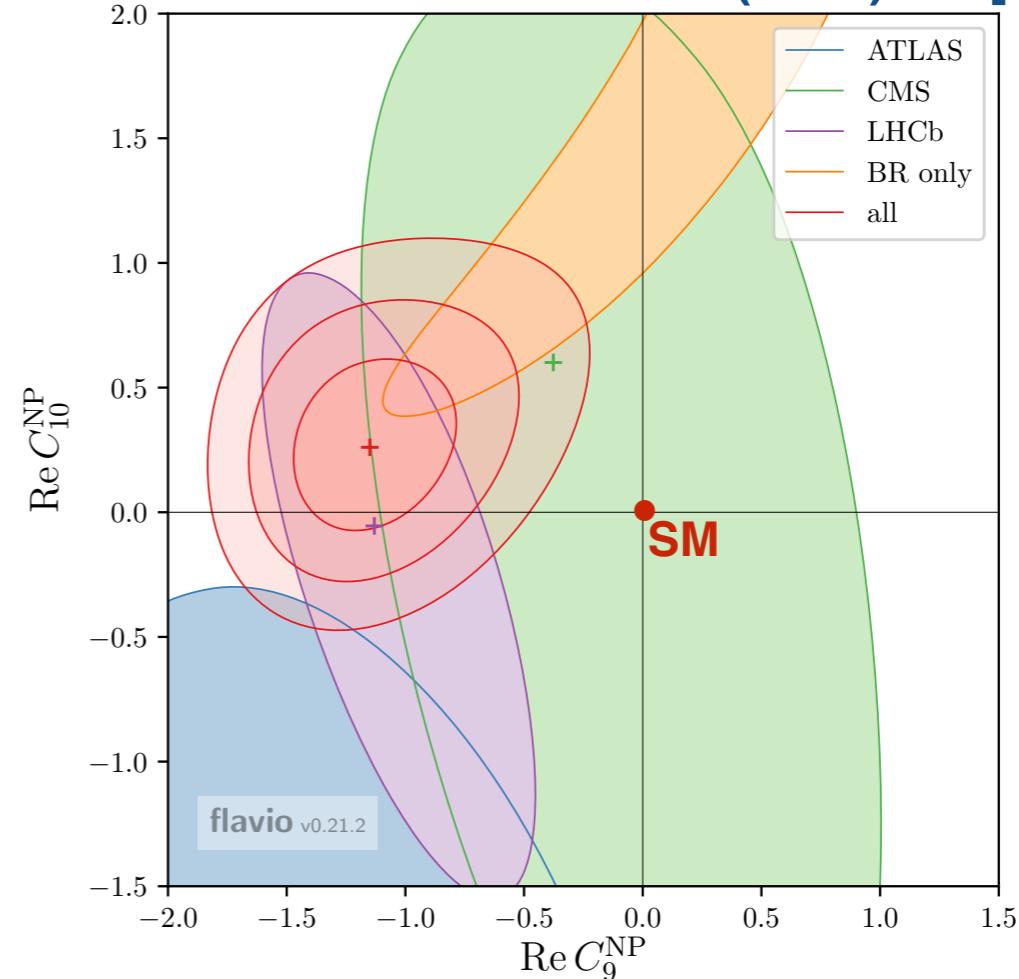
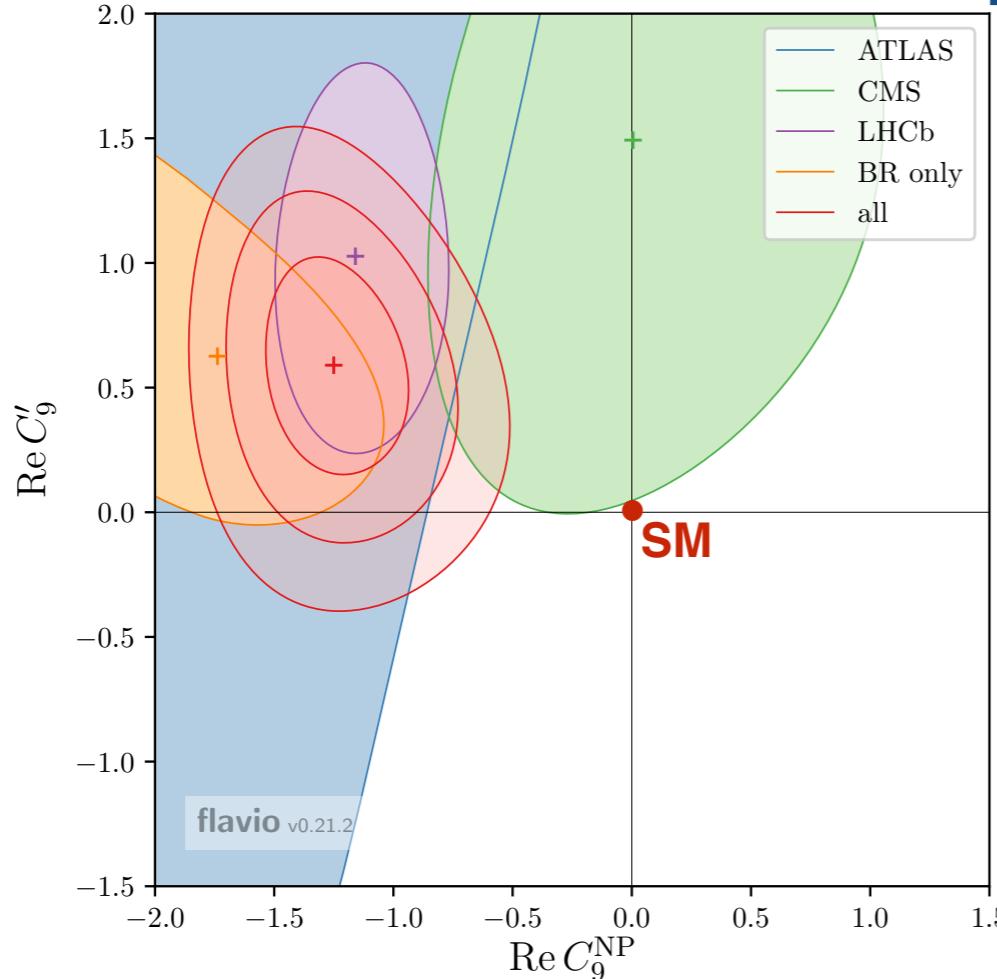


- P'_5 is one of a set of so-called form-factor free observables that can be measured [Descotes-Genon et al. \[JHEP 04 \(2012\) 104\]](#).

Global fits

- Several attempts to interpret our results through global fits to $b \rightarrow s$ data.

[W. Altmannshofer et al. EPJC 77 (2017) 377]



Data are consistent between experiments/measurements and favour a modified vector coupling ($C_9^{\text{NP}} \neq 0$) at $4\text{-}5\sigma$.

see talk by Danny van Dyk (and talk by David Straub)

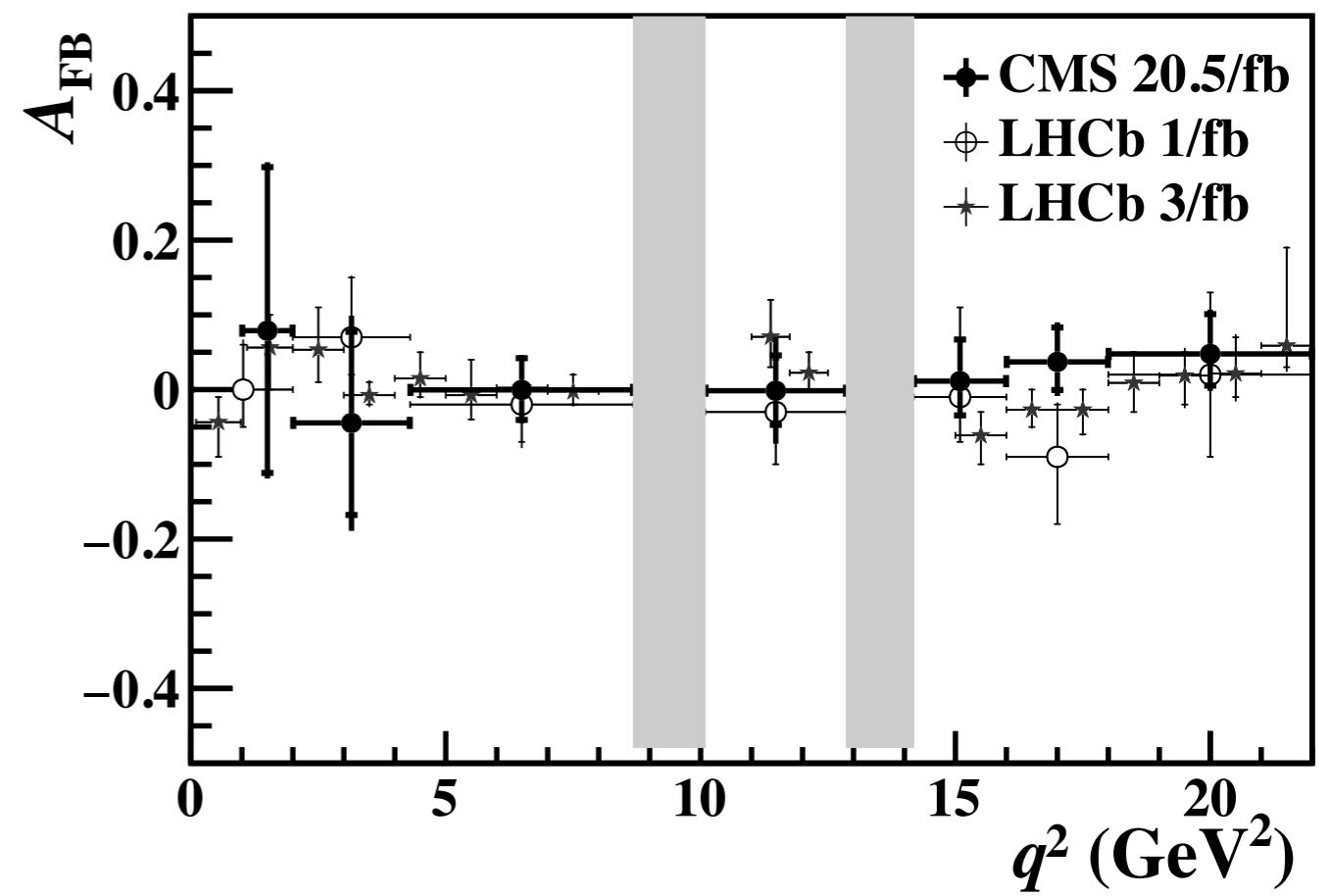
$B^+ \rightarrow K^+ \mu^+ \mu^-$ decay

- Decay described by single angle θ_l and q^2 :

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_l} = \frac{3}{4} (1 - F_H) (1 - \cos^2 \theta_l) + \frac{F_H}{2} + A_{FB} \cos \theta_l$$

- In the SM operator basis $A_{FB} = 0$ and $F_H \approx 0$.
- Only non-zero if there are new scalar/pseudoscalar or tensor contributions.
- Data consistent with a SM-like picture.
- We also know from $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)$ that scalar & pseudoscalar contributions are very small.

CMS [arXiv:1806.00636],
LHCb [JHEP 05 (2014) 082]



$\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ decay

- First observed by the CDF collaboration in [\[PRL 107 \(2011\) 201802\]](#)
- Decay has unique phenomenology:
 - Diquark pair as a spectator rather than single quark;
 - Λ_b can be produced polarised in $p p$ collisions;
 - and the Λ baryon decays via the weak interaction.
- Based on [\[JHEP 06 \(2015\) 115\]](#), expect signal predominantly at low hadronic-recoil ($15 < q^2 < 20$ GeV $^2/c^4$).

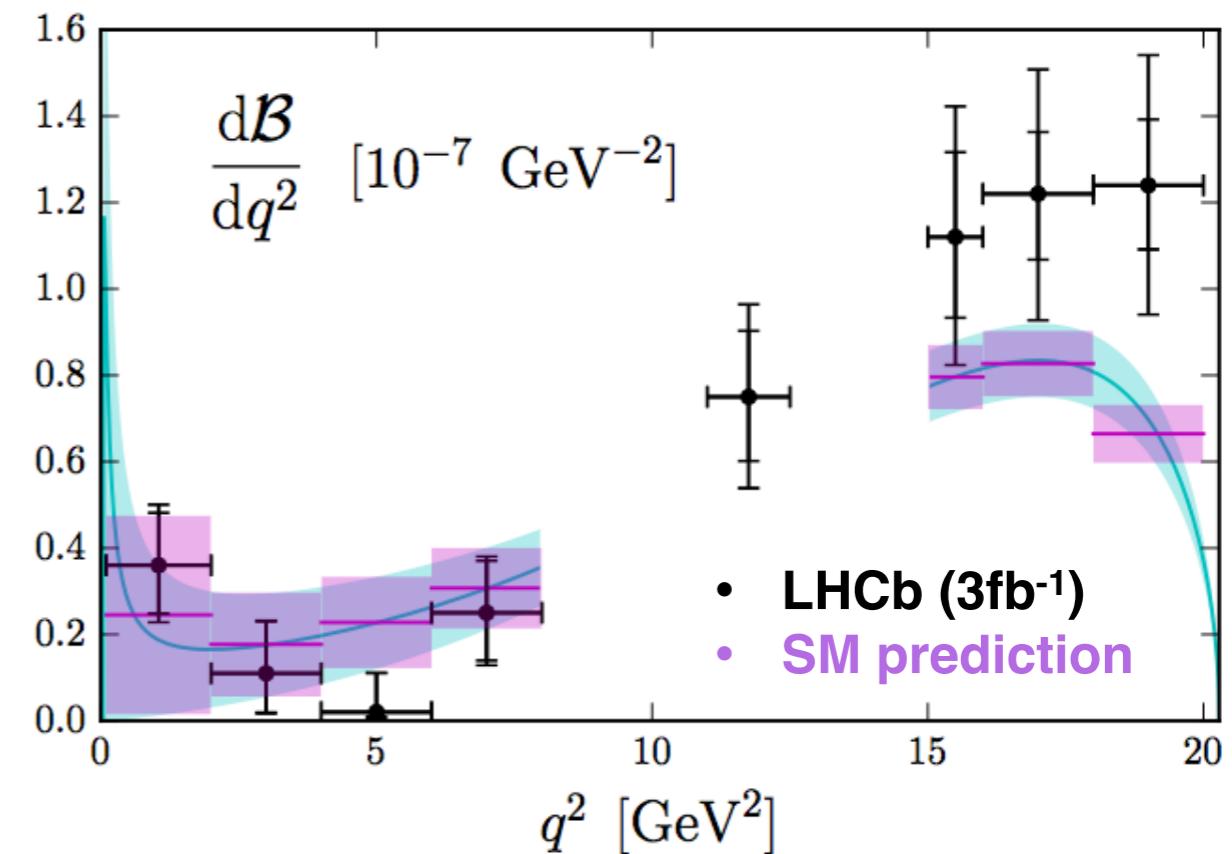


Figure and SM prediction from:
[Detmold et al. \[PRD 93 \(2016\) 074501\]](#)

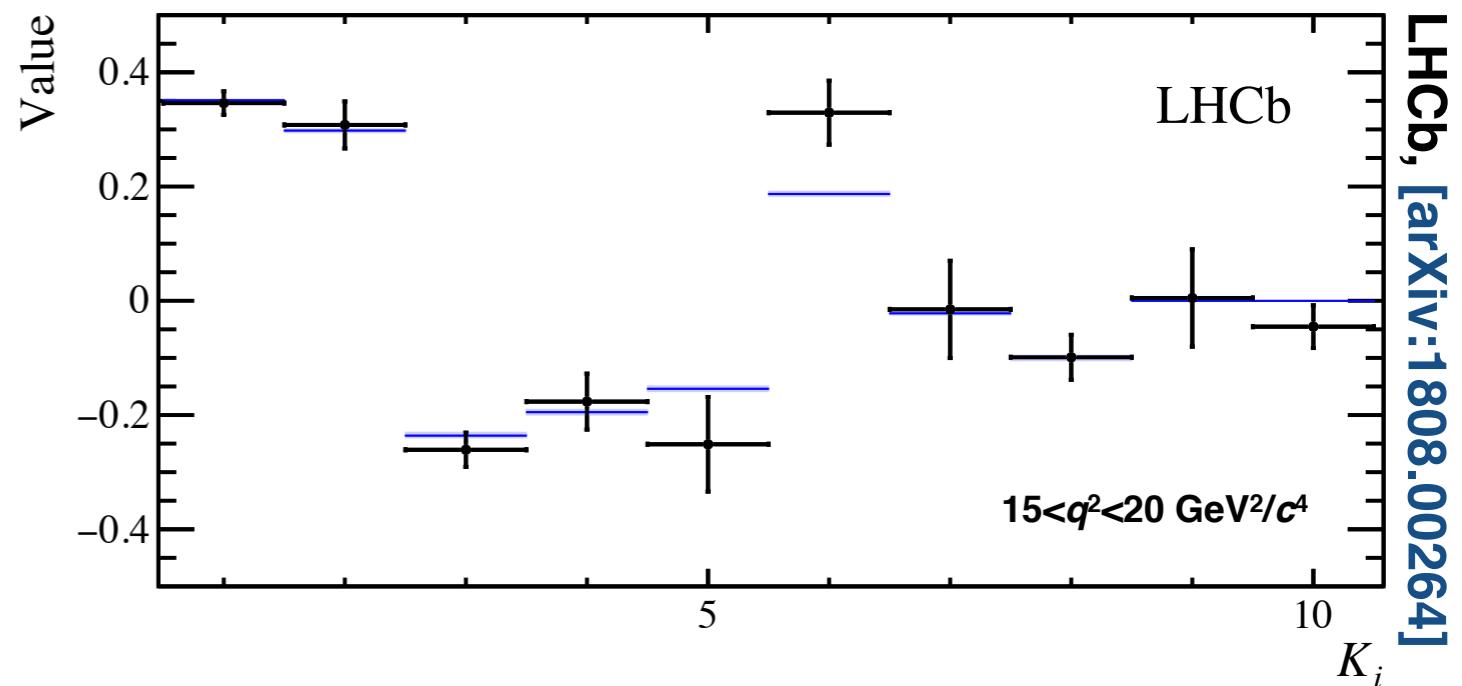
Data from:
LHCb [\[JHEP 06 \(2015\) 115\]](#)

$\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ angular distribution

- First measurement of the full set of angular observables for $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$.
- Decay is described by 5 angles and a normal-vector:

$$\frac{d^5\Gamma}{d\vec{\Omega}} = \frac{3}{32\pi^2} \sum_i^{34} K_i(q^2) f_i(\vec{\Omega})$$

- $K_{11} — K_{34}$ are consistent with having a small production polarisation (i.e. consistent with zero).



Data are consistent with SM predictions from

Boër et al. [JHEP 01 (2015) 155]

Detmold et al. [PRD 93 (2016) 074501]

Lepton universality tests

- In the SM, ratios

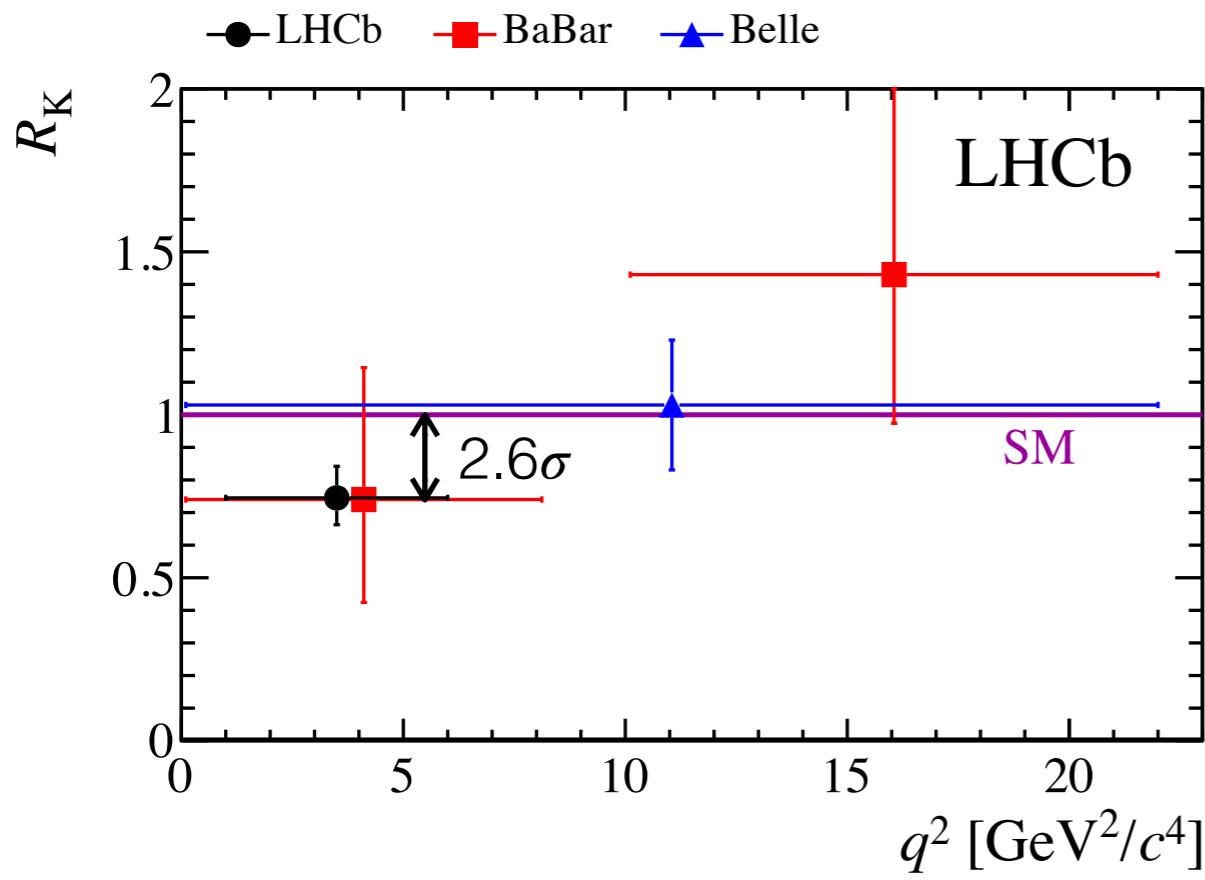
$$R_K = \frac{\int d\Gamma[B^+ \rightarrow K^+ \mu^+ \mu^-]/dq^2 \cdot dq^2}{\int d\Gamma[B^+ \rightarrow K^+ e^+ e^-]/dq^2 \cdot dq^2}$$

only differ from unity by phase space — the dominant SM processes couple equally to the different lepton flavours.

- Theoretically clean since hadronic uncertainties cancel in the ratio.
- Experimentally challenging due to differences in muon/electron reconstruction (in particular Bremsstrahlung from the electrons).
 - Take double ratios with $B \rightarrow J/\psi K^{(*)}$ decays to cancel possible sources of systematic uncertainty.
 - Correct for migration of events in q^2 due to FSR/Bremsstrahlung using MC (with PHOTOS).

Lepton universality tests

- Interesting hints of non-universal lepton couplings in LHCb's run 1 dataset:

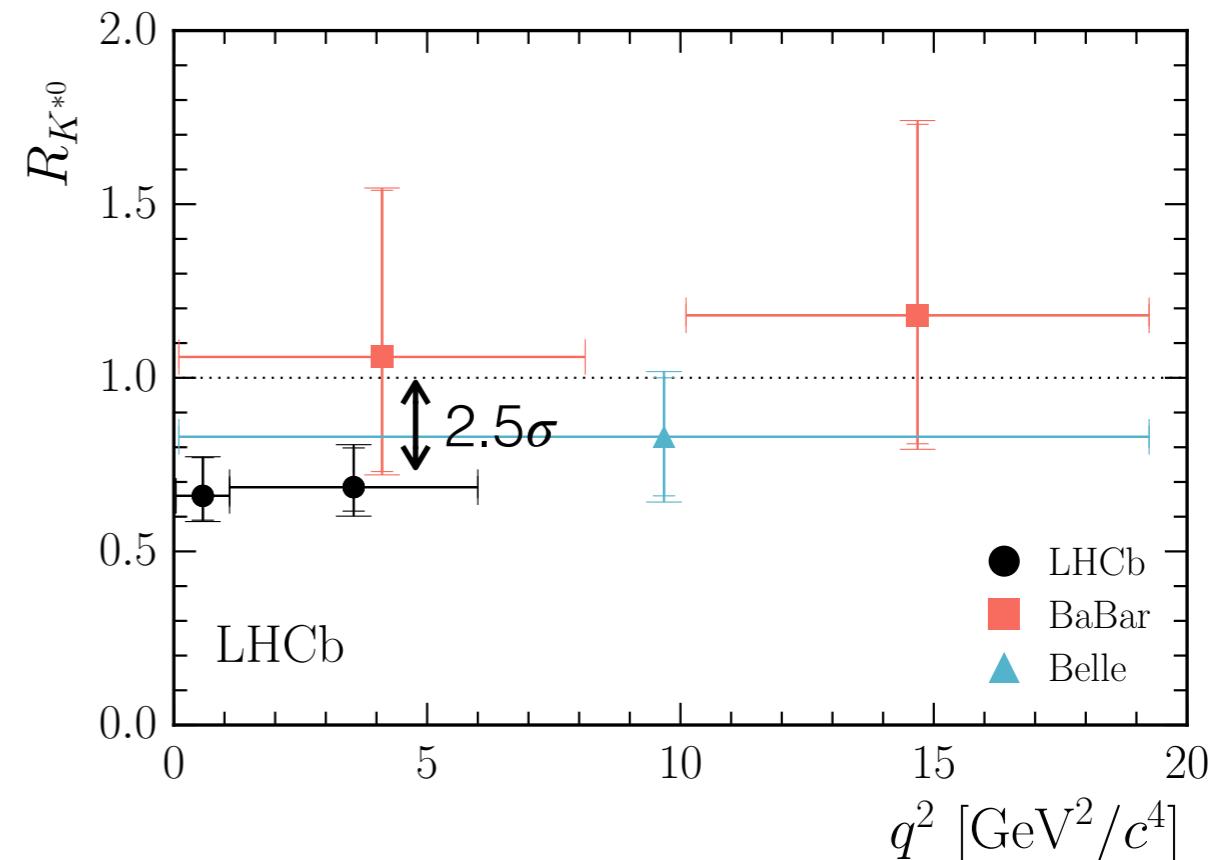


LHCb [PRL113 (2014) 151601]

LHCb [LHCb-PAPER-2017-013]

BaBar [PRD 86 (2012) 032012]

Belle [PRL 103 (2009) 171801]



NB $R_K \approx 0.8$ was a prediction of one class of model explaining the $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ angular observables, see $L_\mu - L_\tau$ models
W. Altmannshofer et al. [PRD 89 (2014) 095033]

Flavour anomalies

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- Rate and angular distribution of exclusive $b \rightarrow s\mu^+\mu^-$ decays.
- Relative rates of $b \rightarrow se^+e^-$ and $b \rightarrow s\mu^+\mu^-$ decays ($R_{K^{(*)}}$)

2. $b \rightarrow c\tau^-\bar{\nu}_\tau$ decays

- Rate of $b \rightarrow c\tau^-\bar{\nu}_\tau$ decays versus decays with e/μ ($R(D^{(*)})$).

$b \rightarrow c\tau\nu$ decays

- Ratios $R(D^{(*)}) = \Gamma[B \rightarrow D^{(*)}\tau\nu]/\Gamma[B \rightarrow D^{(*)}\ell\nu]$ are also theoretically clean in the SM:

- Coupling to leptons is universal.
- Hadronic uncertainties and $|V_{cb}|$ cancel in the ratio.

and can be enhanced in extensions of the SM (e.g. with charged Higgs).

- Complicated experimentally by missing energy in the final-state from multiple missing neutrinos.

Feynman diagram showing the decay of a b quark (shaded blob) into a c quark (shaded blob) and a D^* meson. The b quark line enters from the left, and the c quark line exits to the right. A W^+ boson (curly line) exchanges mass with the b quark, and a neutrino (ν) and muon (μ^+) are produced. The D^* meson line exits to the right.

Two Feynman diagrams for $b \rightarrow c$ transitions. The left diagram shows a b quark (shaded blob) decaying into a c quark (shaded blob) and a D^* meson. A charged Higgs boson (H^+) (dashed line) exchanges mass with the b quark, and a neutrino (ν) and muon (μ^+) are produced. The right diagram shows a b quark (shaded blob) decaying into a c quark (shaded blob) and a D^* meson. A left-handed quark (LQ) (dashed line) exchanges mass with the b quark, and a neutrino (ν) and muon (μ^+) are produced.

3D diagram illustrating a particle interaction vertex (PV). A central grey oval represents the vertex. Several outgoing particles are shown as colored arrows: a blue arrow labeled B (dashed line), a green arrow labeled D (solid line) with pions (π), a red arrow labeled τ (dashed line) with neutrinos (ν), and a black arrow labeled μ (dotted line). A red diagonal line represents a missing neutrino (ν). The background shows a grid of grey lines representing other particles or energy flow.

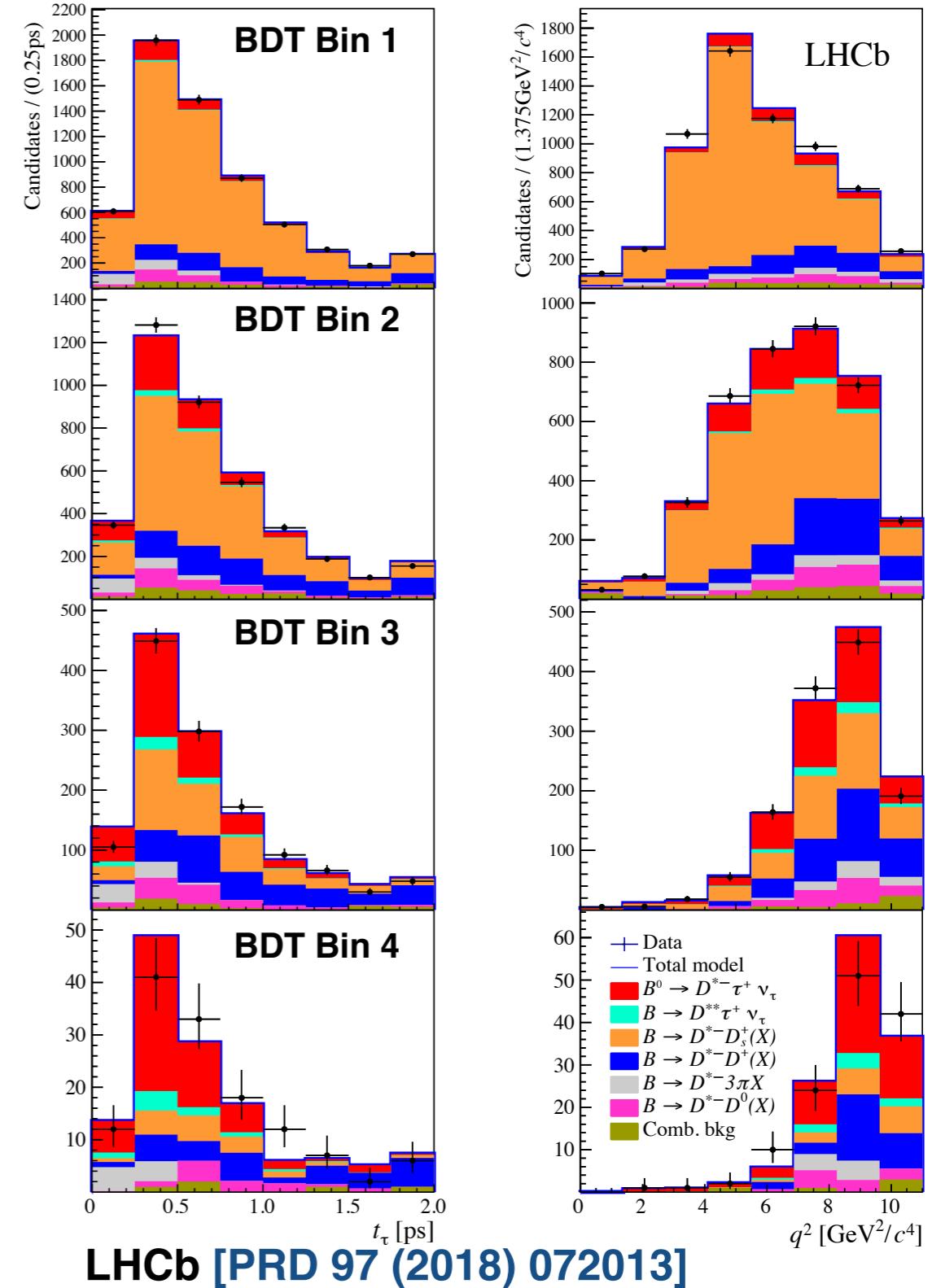
T. Blake

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$R(D^*)$ with $\tau \rightarrow 3\pi(\pi^0)\nu$

- Experimental challenge is to separate signal from backgrounds.
 - Use missing mass, lepton energy, q^2 and multivariate discriminants.
 - Can use boost approximation to determine kinematic quantities $((\beta_z \gamma)_{\text{vis}} \approx (\beta_z \gamma)_B)$.
- B -factory experiments can exploit leptonic/hadronic tag of the other B in the event and centre-of-mass constraints.

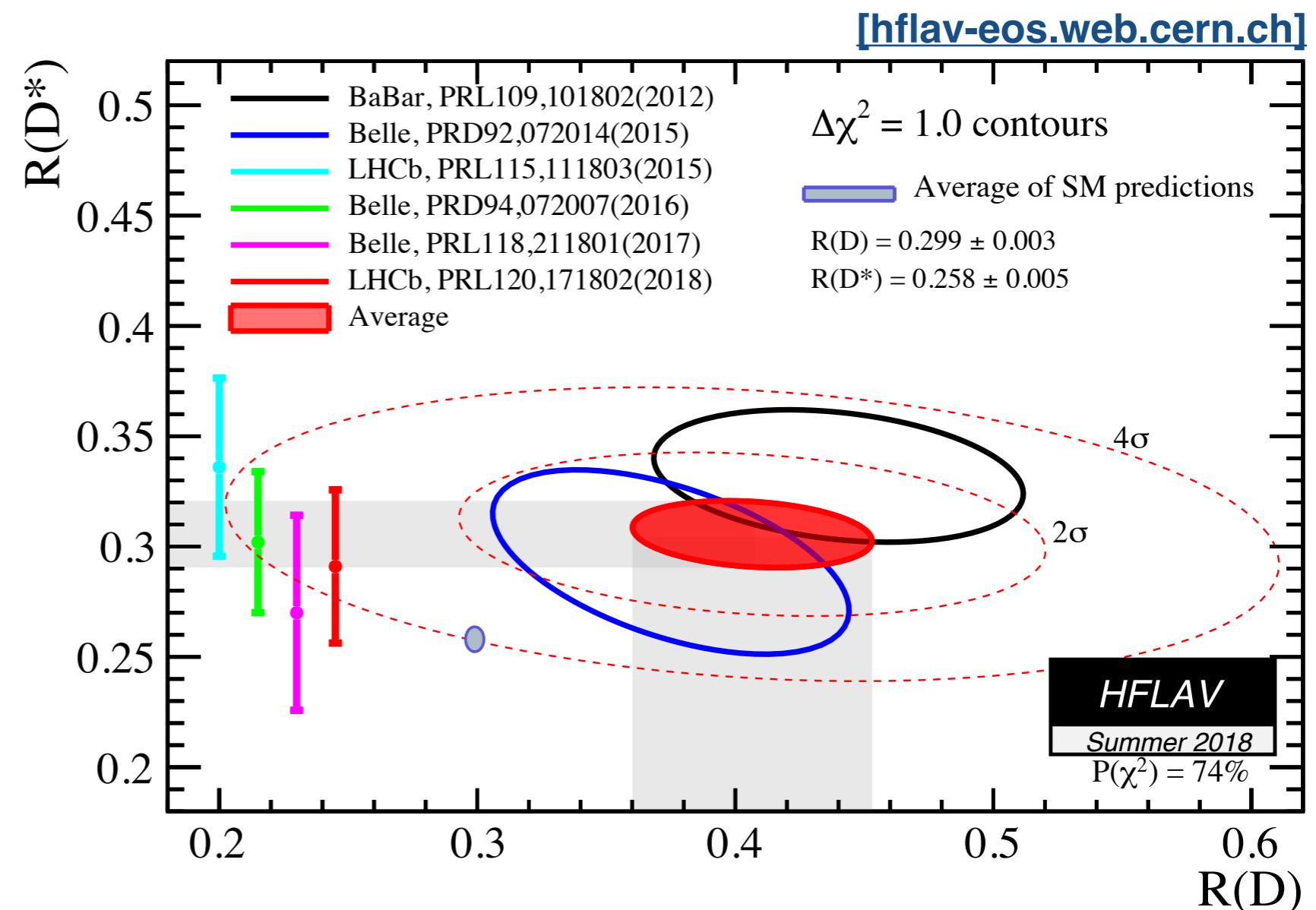
Modelling of D^{} and hadronic backgrounds is important**



LHCb [PRD 97 (2018) 072013]

$R(D)$ versus $R(D^*)$

Combination of $R(D)$ and $R(D^*)$ is 3.8σ from the corresponding SM prediction.



- SM predictions:
 - $R(D)$ from **FLAG working group [EPJC 77 (2017) 112]**.
 - $R(D^*)$ from **S. Fajfer et al. [PRD 85 (2012) 094025]**.

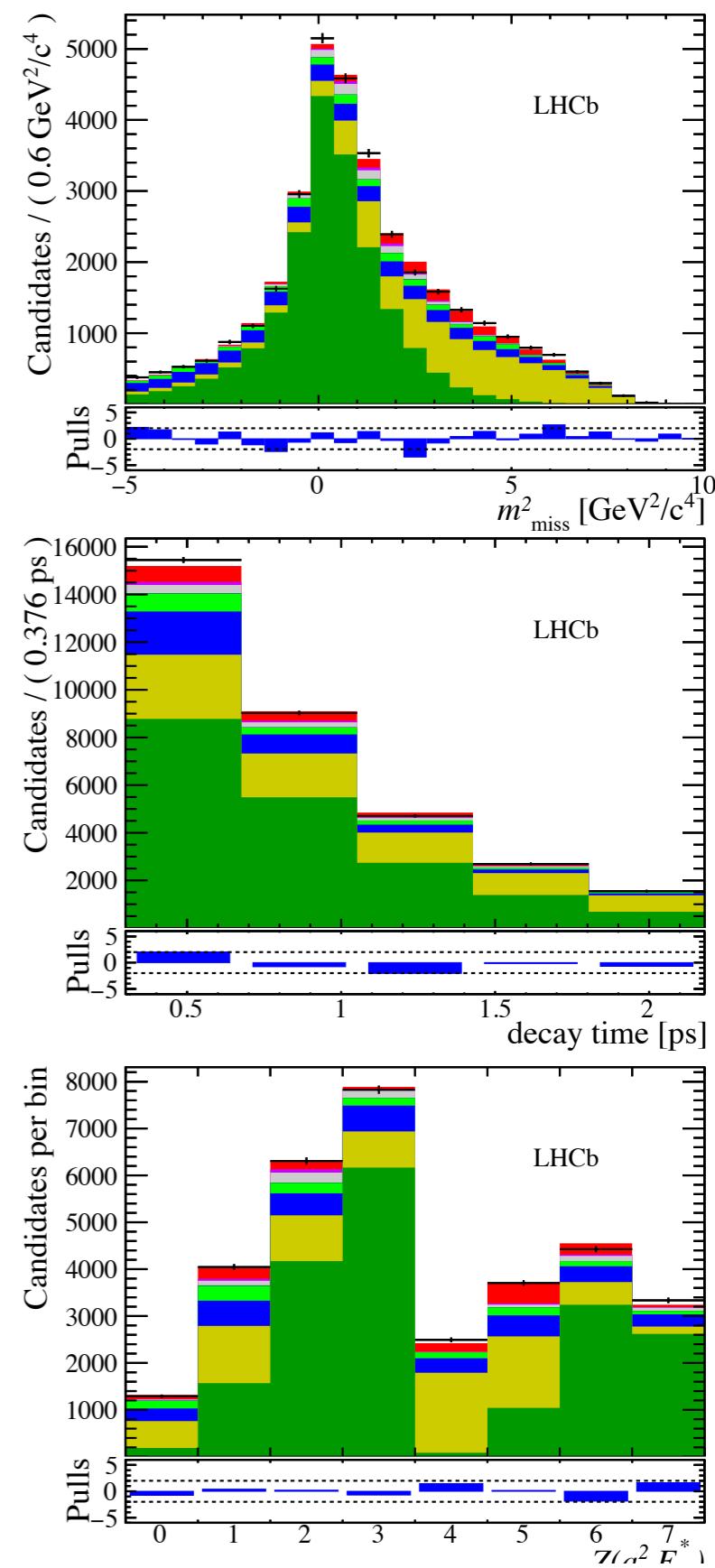
$R(J/\psi)$

- LHCb has also measured a similar ratio using B_c decays:

$$R(J/\psi) = \frac{\Gamma[B_c^+ \rightarrow J/\psi \tau^+ \nu_\tau]}{\Gamma[B_c^+ \rightarrow J/\psi \mu^+ \nu_\mu]} = 0.71 \pm 0.17 \text{ (stat)} \pm 0.18 \text{ (syst)}$$

[LHCb, PRL120 (2018) 121801]

- Perform a template fit to the B_c decay time, to m_{miss}^2 and a category label $Z(q^2, E_\mu^*)$.
- SM predictions based on the quark-model/QCD sum rules are in the range 0.25–0.28.
- Systematic uncertainty driven by knowledge of the $B_c^+ \rightarrow J/\psi$ form-factors and the size of the simulated samples used to derive the templates.



+	Data	$B_c^+ \rightarrow J/\psi \mu^+ \nu_\mu$
Yellow	Mis-ID bkg.	$J/\psi + \mu$ comb. bkg.
Green	J/ψ comb. bkg.	$B_c^+ \rightarrow J/\psi H_c^+$
Grey	$B_c^+ \rightarrow \chi_c(1P) l^+ \nu_l$	$B_c^+ \rightarrow \psi(2S) l^+ \nu_l$
Red	$B_c^+ \rightarrow J/\psi \tau^+ \nu_\tau$	

$B \rightarrow D^* \tau V$ angular distribution

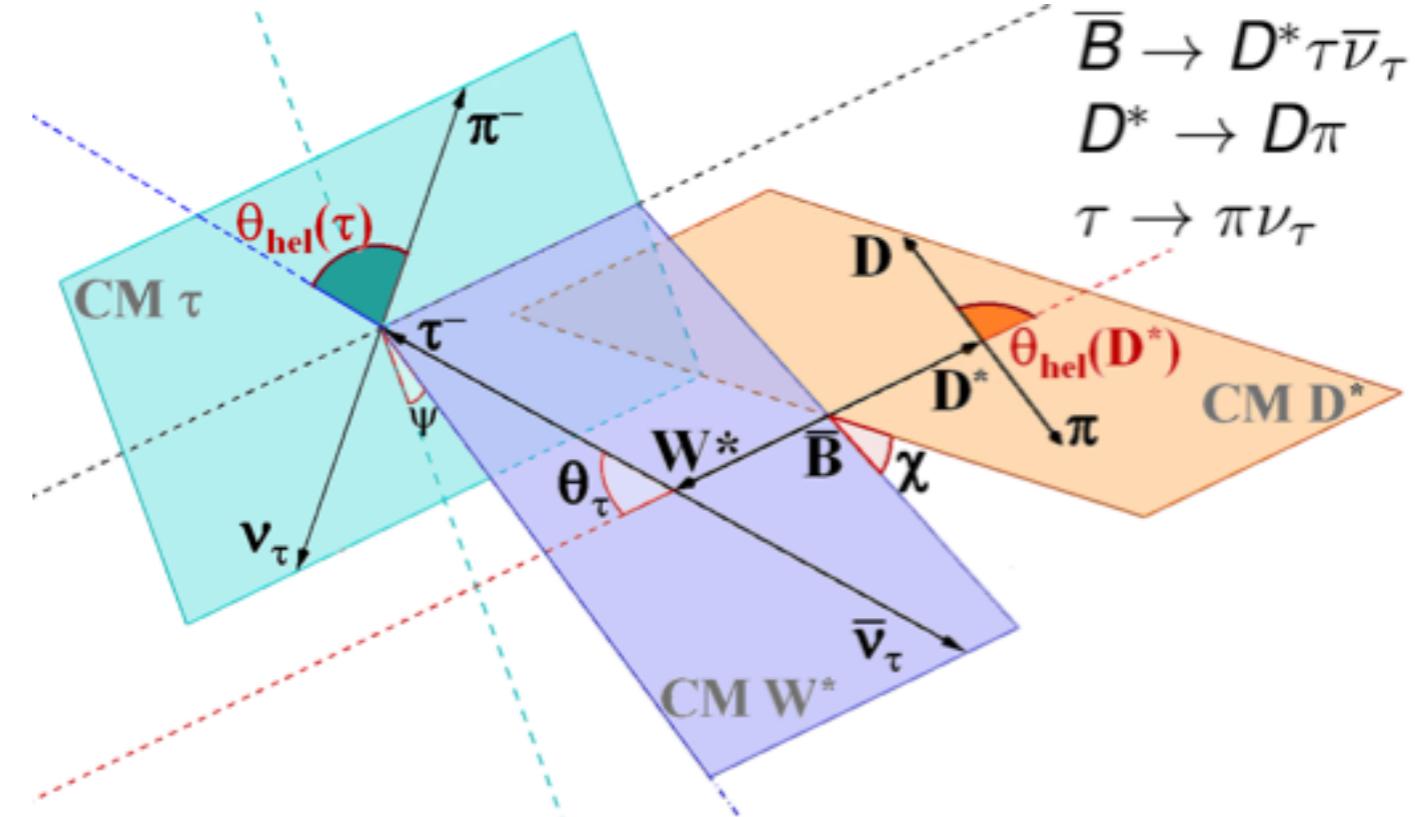
- Can also look at the angular distribution of the final-state particles.

eg Can measure $\theta_{\text{hel}}(\tau)$ and $\theta_{\text{hel}}(D^*)$ using hadronic τ decays.

- Angular projections:

$$\frac{d\Gamma}{d \cos \theta_{\text{hel}}(\tau)} = \frac{1}{2} (1 + \alpha P_\tau \cos \theta_{\text{hel}}(\tau))$$

$$\frac{d\Gamma}{d \cos \theta_{\text{hel}}(D^*)} = \frac{3}{4} (2F_L \cos^2 \theta_{\text{hel}}(D^*) + (1 - F_L) \sin^2 \theta_{\text{hel}}(D^*))$$



From talk by Karol Adamczyk

$B \rightarrow D^* \tau V$ angular distribution

- From the forward-backward asymmetry of 1-prong decays Belle measures:

$$P_\tau(D^*) = -0.38 \pm 0.51 \text{ (stat)}^{+0.21}_{-0.16} \text{ (syst)}$$

with [\[PRL118 \(2017\) 211801\]](#).

- Preliminary measurement of F_L also shown for the first time at CKM 2018:

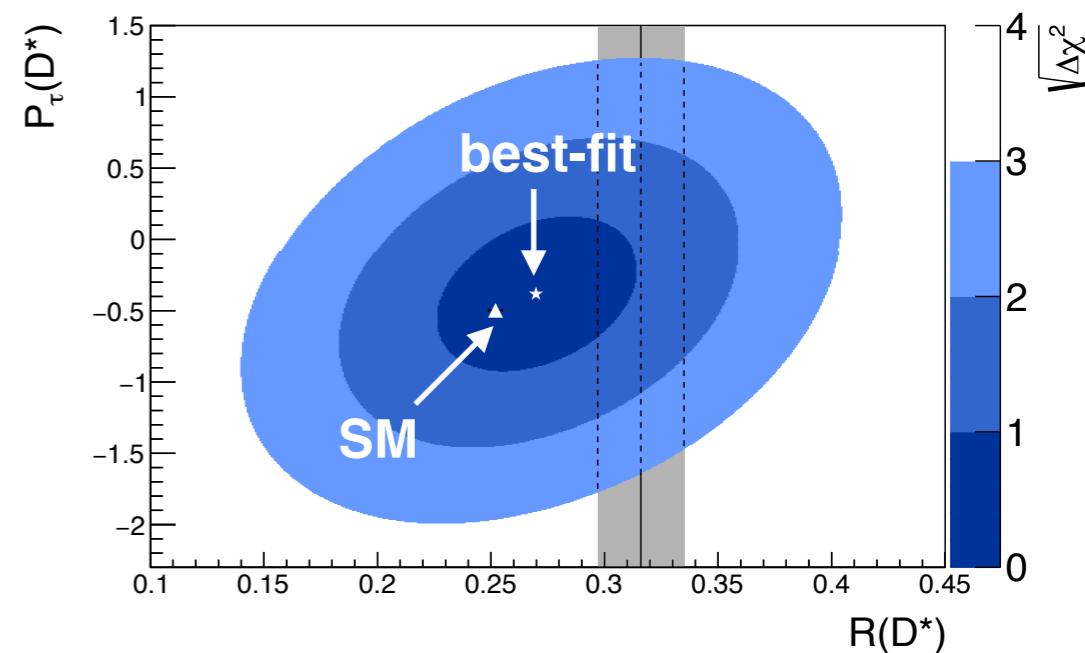
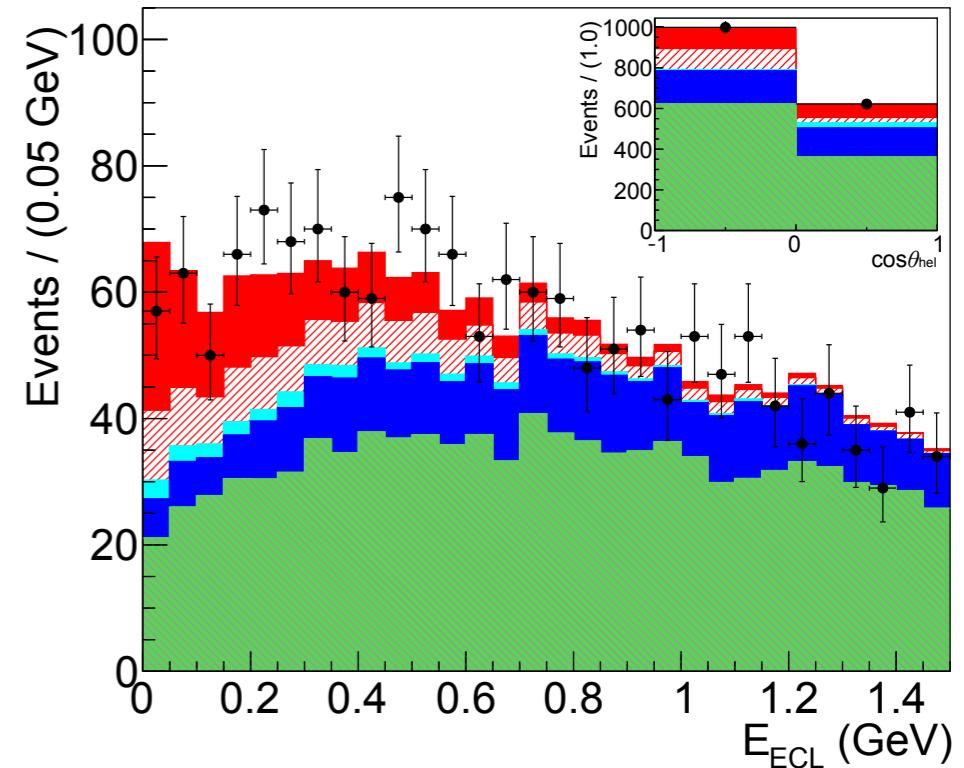
$$F_L = 0.60 \pm 0.08 \text{ (stat)} \pm 0.035 \text{ (syst)}$$

[\[see talk by K. Adamczyk\]](#).

- Measured value of F_L consistent with SM predictions within 2σ e.g.

[Alok et al. \[PRD 95 \(2017\) 115038\]](#).

Belle [PRL 118 (2017) 211801]

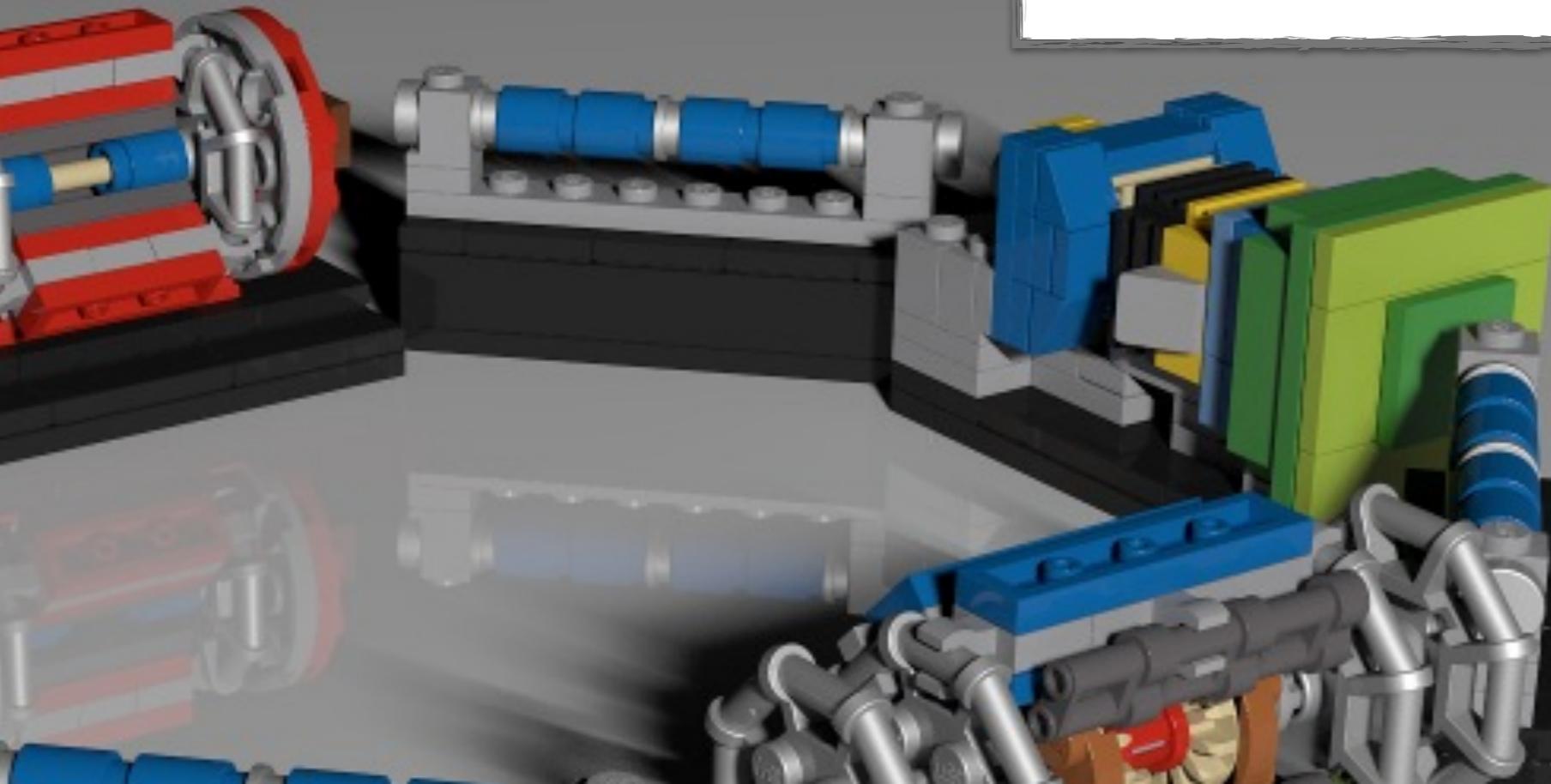
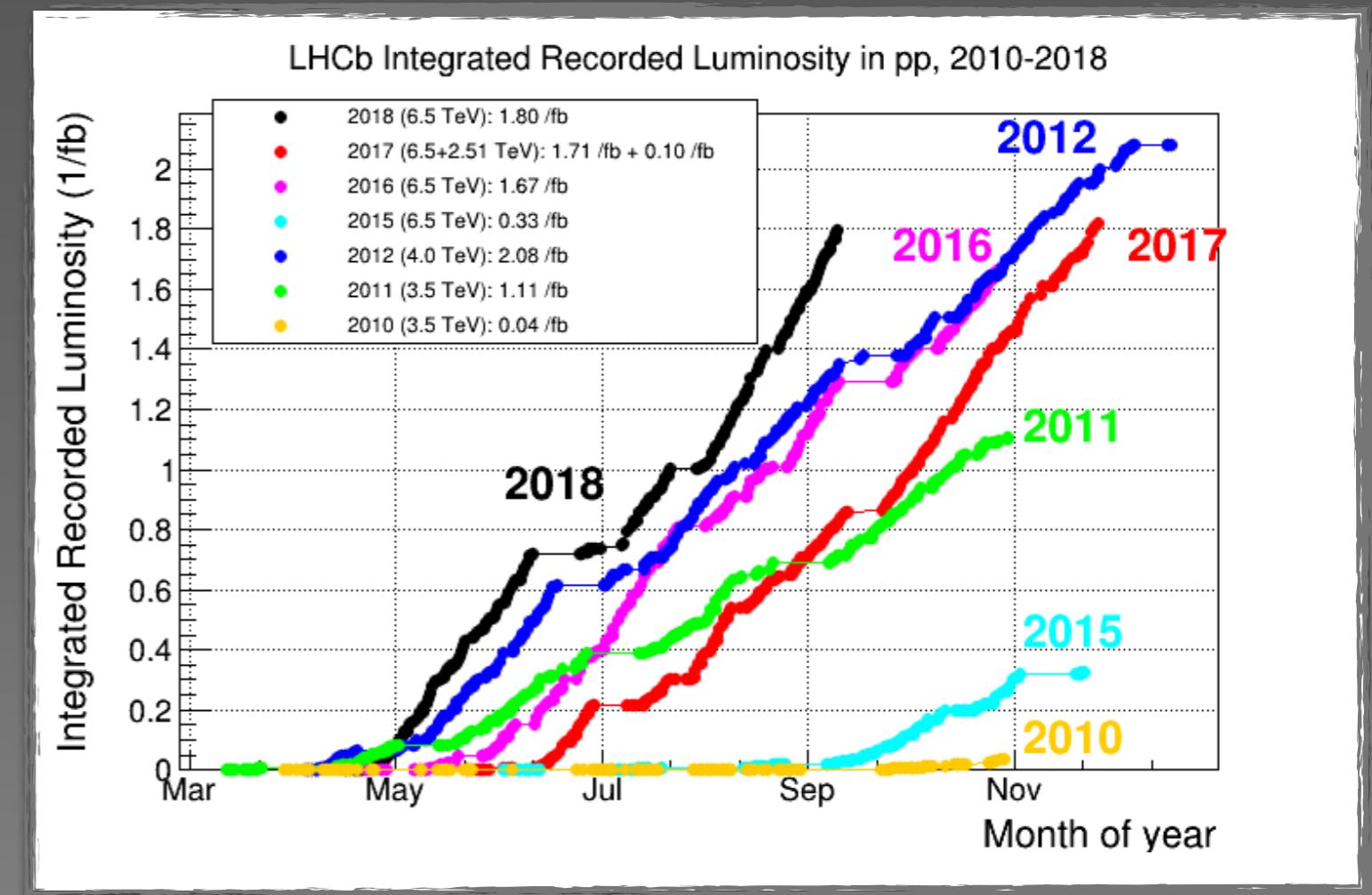


Summary

- Anomalies in $b \rightarrow s\ell^+\ell^-$ processes:
 - Branching fractions of $b \rightarrow s\mu^+\mu^-$ processes systematically below SM predictions (inclusive branching fraction is consistent).
 - R_K and R_{K^*} different from unity.
 - P'_5 anomaly in the angular distribution of $B^0 \rightarrow K^{*0}\mu^+\mu^-$.
 - Anomalies in $b \rightarrow c\ell^-\bar{\nu}_\ell$ processes:
 - $R(D)$ and $R(D^*)$ larger than SM predictions.
 - Long-standing tension between inclusive and exclusive determinations of $|V_{ub}|$ and $|V_{cb}|$.
- 

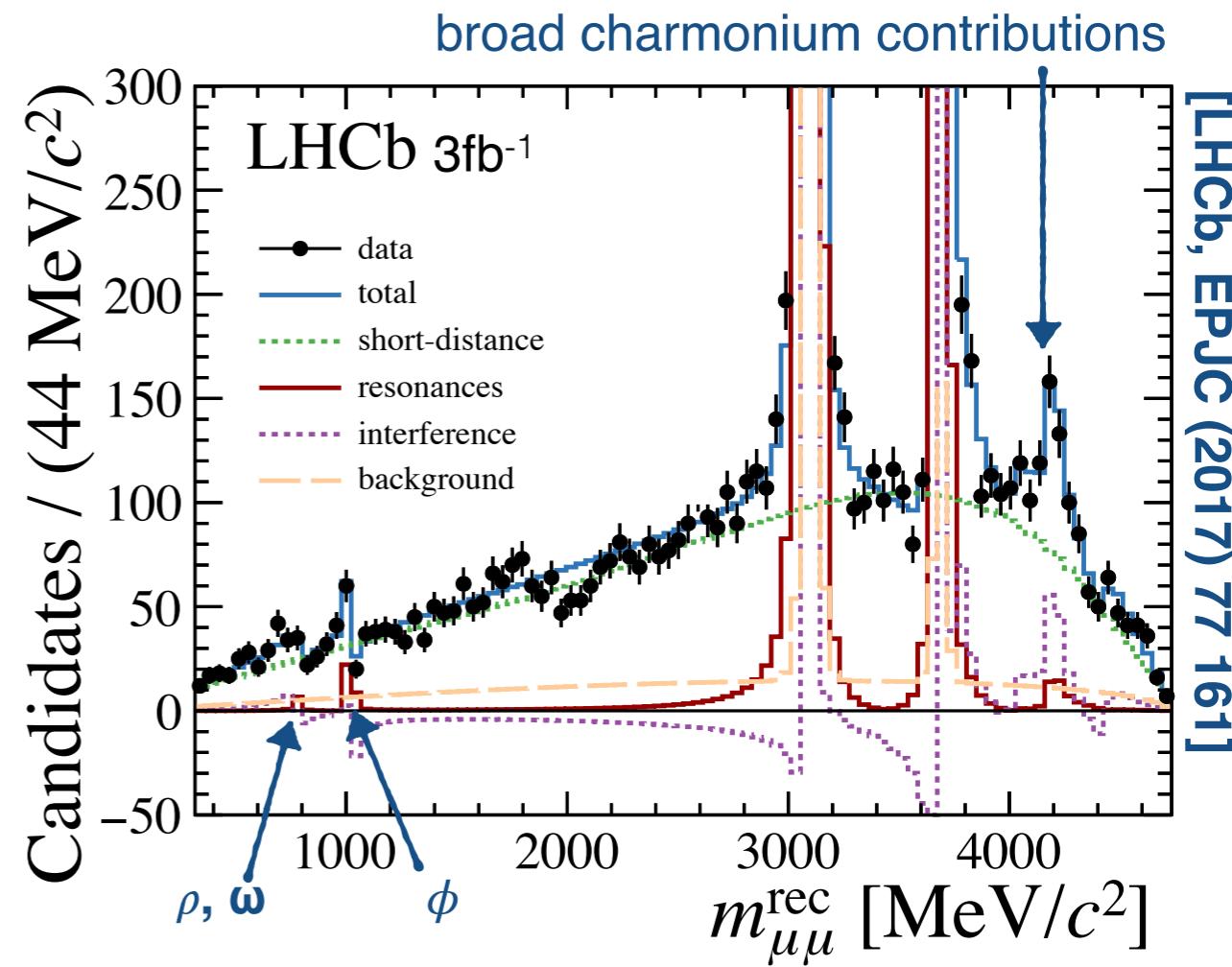
Summary

- Huge progress expected in the next five years with new data from the LHC experiments (including parked datasets) and from Belle II.



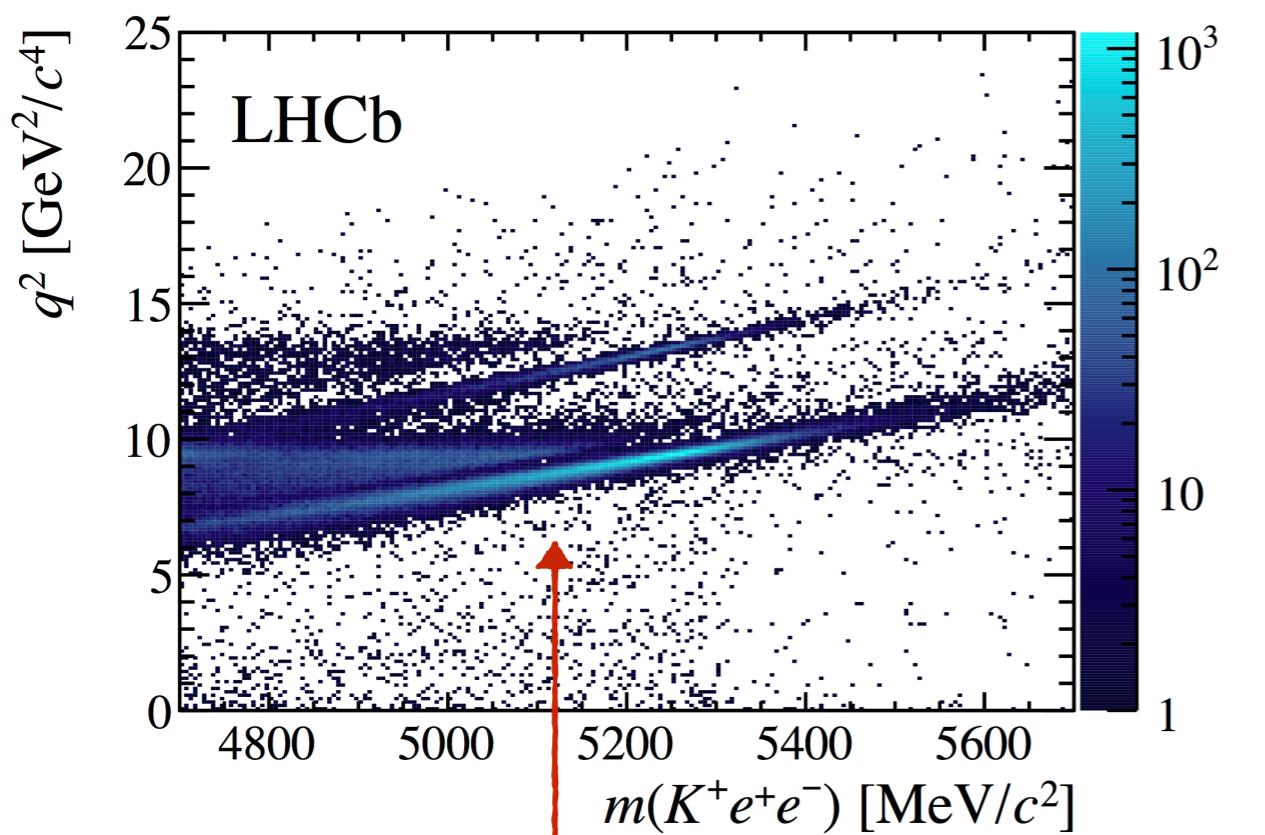
Resonant contributions

- With the large LHC datasets can also explore the shape of the $d\Gamma/dq^2$ spectrum in detail.
- See evidence for broad charmonium states and light quark contributions.
- Can determine relative magnitude/phases of the different contributions.
- Data could be used to exclude models proposing new GeV-scale particles as an explanation for R_K/R_{K^*} . **[F. Sala & D. Straub, arXiv:1704.06188]**

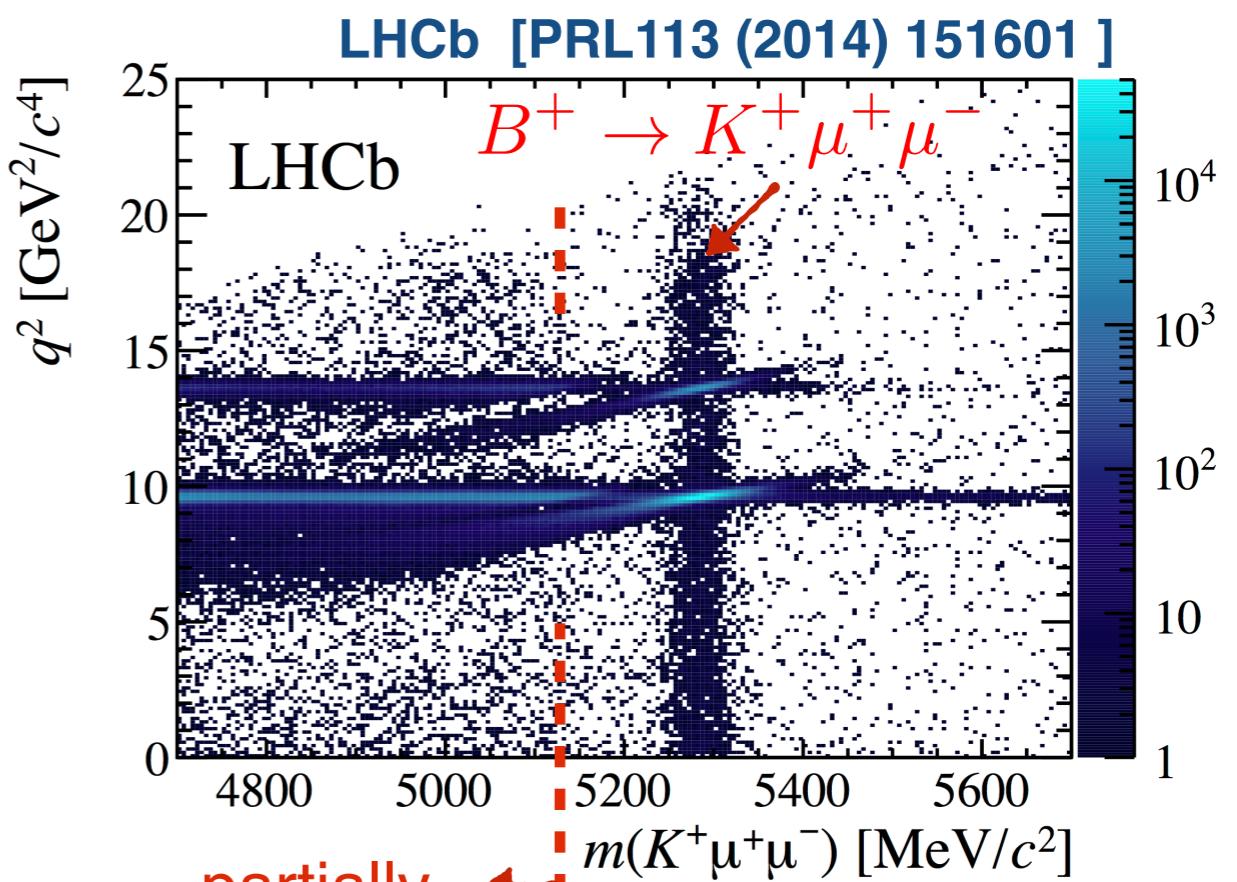


$B^+ \rightarrow K^+ \ell^+ \ell^-$ candidates

- Even after Bremsstrahlung recovery there are significant differences between dielectron and dimuon final states:



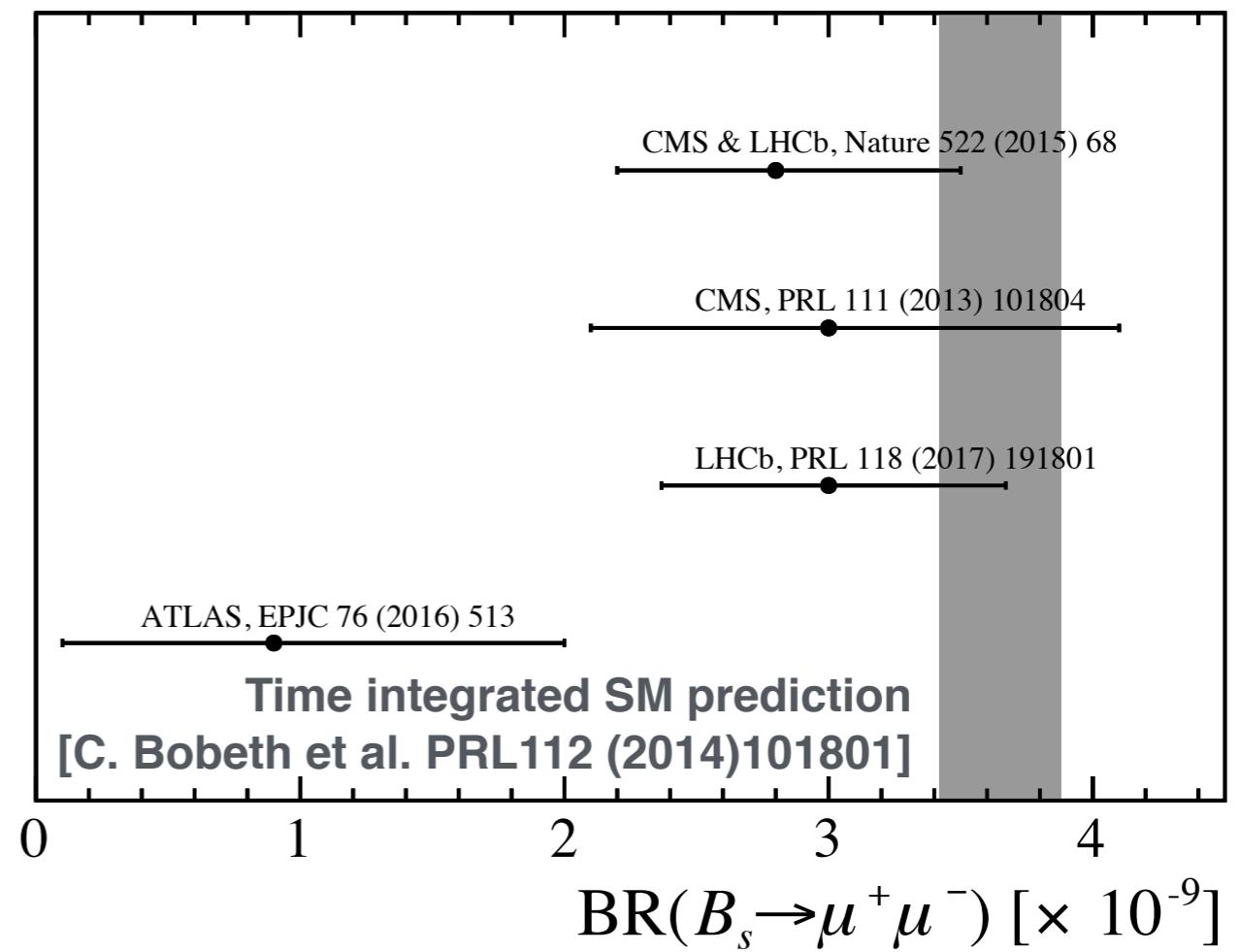
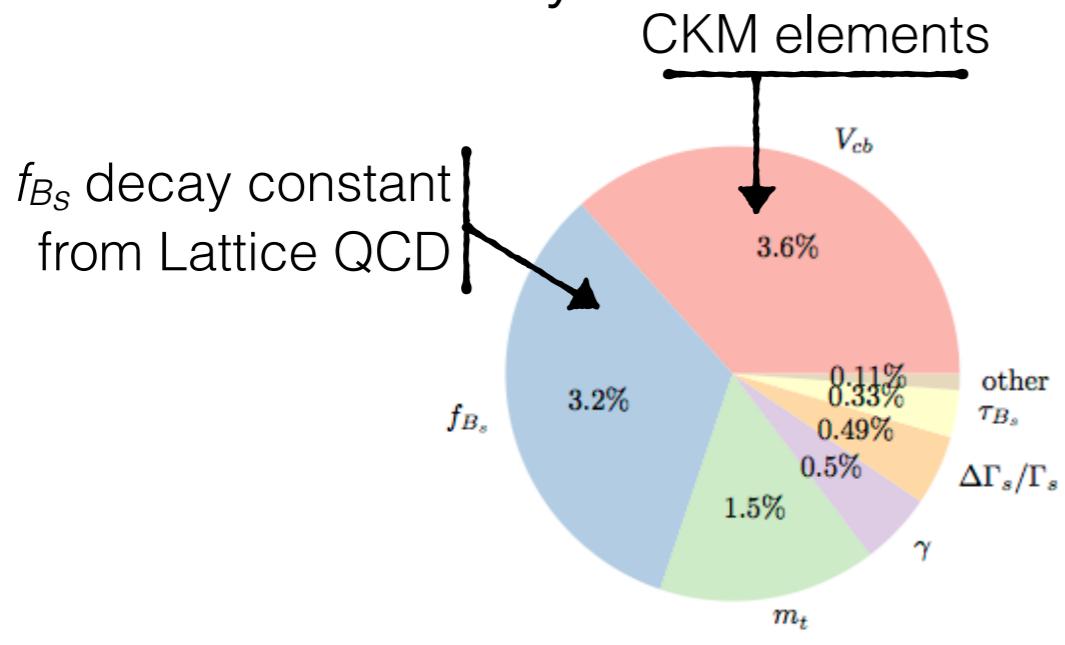
Large radiative tail and migration of events
(even after Brem. recovery).



partially
reconstructed
decays

$B_s \rightarrow \mu^+ \mu^-$

- Recent LHCb analysis using run 1 and 2 data ($3\text{fb}^{-1} + 1.4\text{fb}^{-1}$) provided the first single experiment observation of $B_s \rightarrow \mu^+ \mu^-$ at more than 7σ .
[LHCb, PRL 118 (2017) 191801]
- Measurements are all consistent with the SM expectation.
 - Can exclude large scalar contributions.
- Branching fraction predicted precisely in the SM with a $\sim 6\%$ uncertainty.

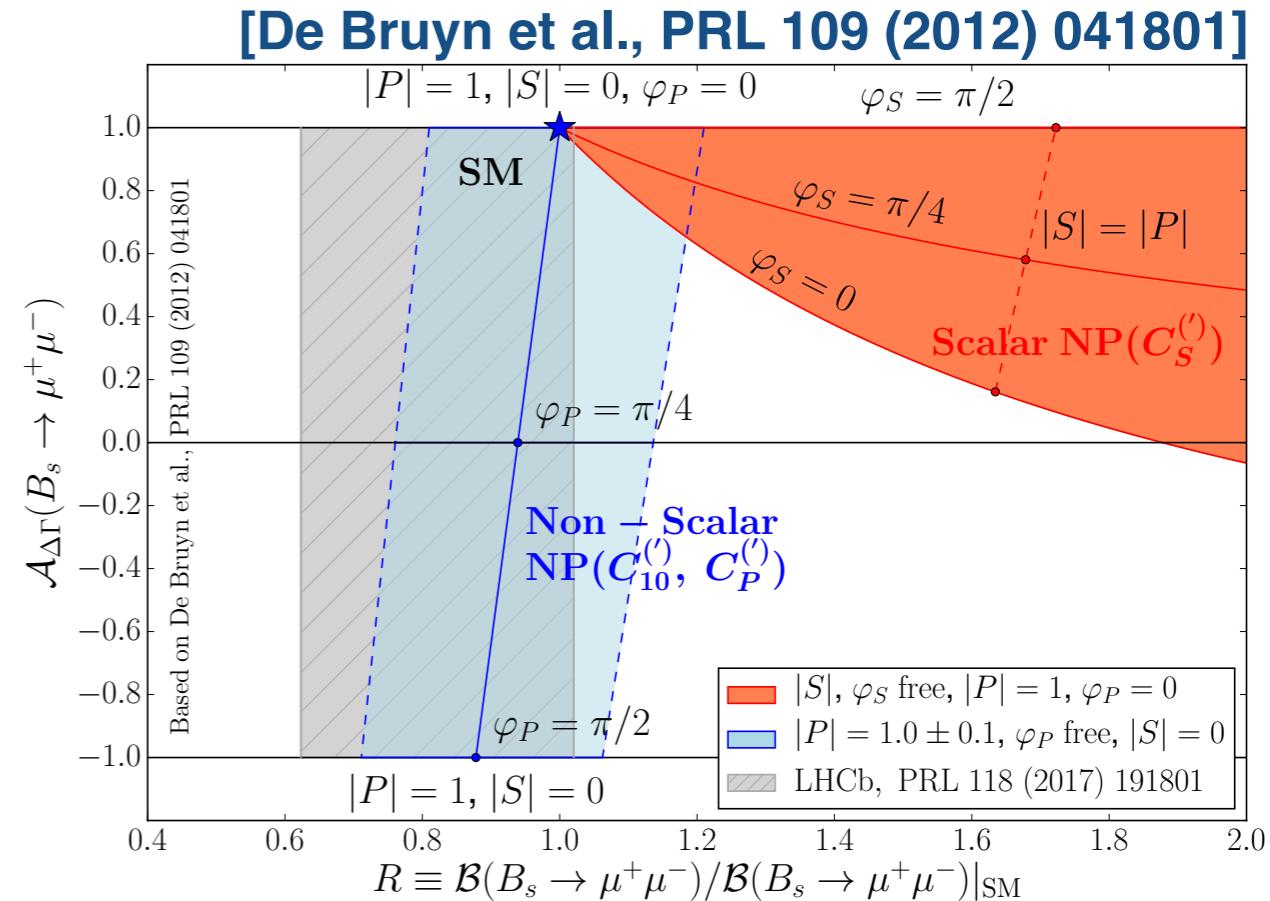


Effective lifetime

- The untagged time dependent decay rate is

$$\Gamma[B_s(t) \rightarrow \mu^+ \mu^-] + \Gamma[\bar{B}_s(t) \rightarrow \mu^+ \mu^-] \propto e^{-t/\tau_{B_s}} \left\{ \cosh\left(\frac{\Delta\Gamma_s}{2}t\right) + A_{\Delta\Gamma} \sinh\left(\frac{\Delta\Gamma_s}{2}t\right) \right\}$$

- $A_{\Delta\Gamma}$ provides additional separation between scalar and pesudoscalar contributions.
- In the SM $A_{\Delta\Gamma} = 1$ such that the system evolves with the lifetime of the heavy B_s mass eigenstate.



$B_s \rightarrow \mu^+ \mu^-$ effective lifetime

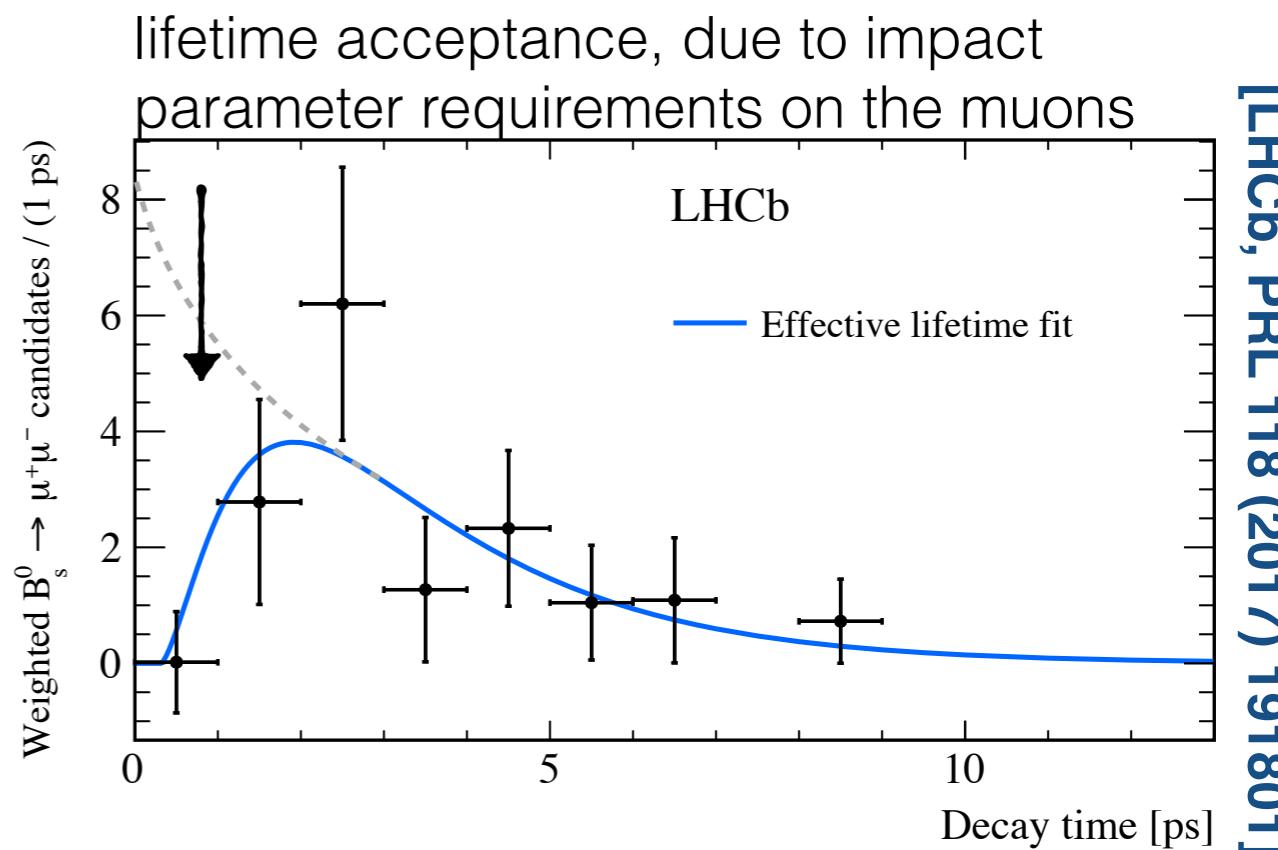
- The $A_{\Delta\Gamma}$ parameter modifies the effective lifetime of the decay:

$$\tau_{\text{eff}} = \frac{\tau_{B_s}}{1 - y_s^2} \left(\frac{1 + 2A_{\Delta\Gamma} y_s + y_s^2}{1 + A_{\Delta\Gamma} y_s} \right) \quad \text{where} \quad y_s = \tau_{B_s} \frac{\Delta\Gamma}{2}$$

- LHCb have performed a first measurement of τ_{eff} , giving

$$\tau[B_s^0 \rightarrow \mu^+ \mu^-] = 2.04 \pm 0.44 \pm 0.05 \text{ ps}$$

NB Not yet sensitive to $A_{\Delta\Gamma}$ (the stat. uncertainty is larger than the change in the lifetime from $\Delta\Gamma_s$). This will become more interesting during runs 3 and 4.

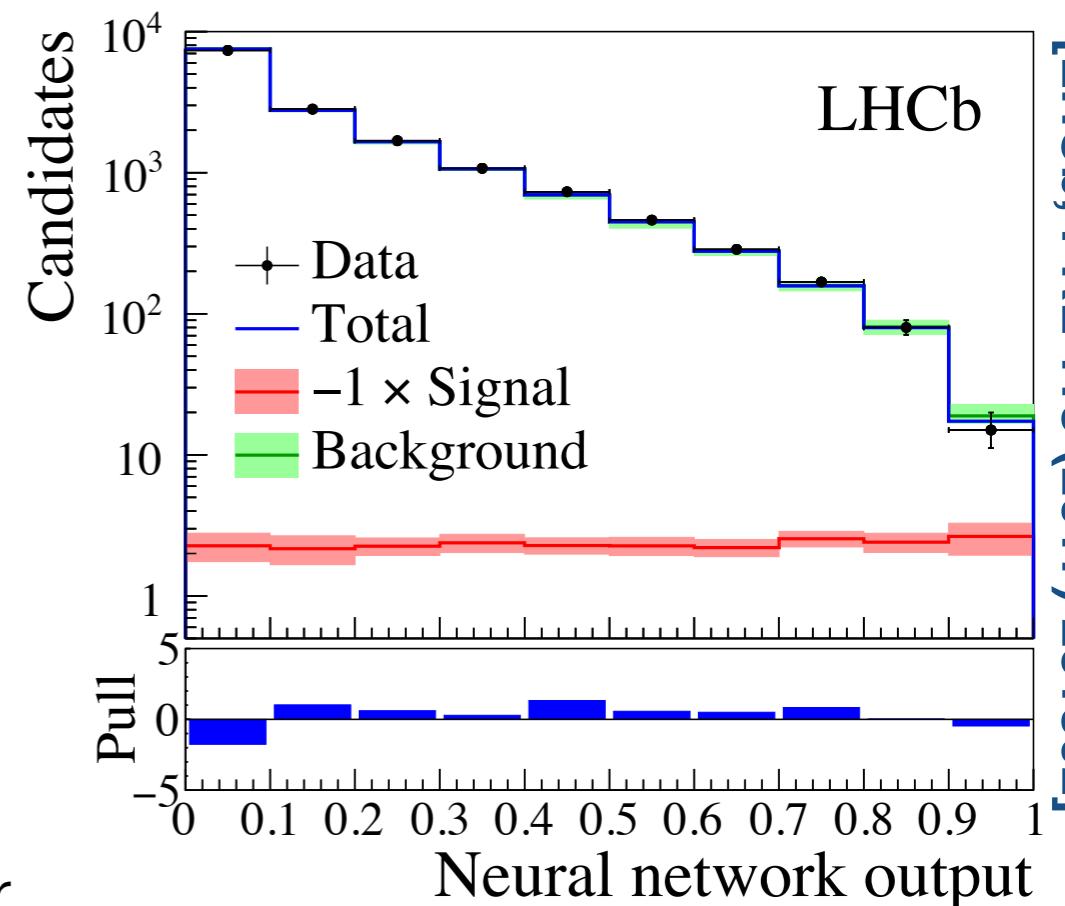


$B_{(s,d)} \rightarrow \tau^+ \tau^-$

- LHCb performs a search for $B_{(s,d)} \rightarrow \tau^+ \tau^-$ decays using $\tau^- \rightarrow \pi^- \pi^+ \pi^- \nu_\tau$.
 - Exploit the $\tau^- \rightarrow a_1(1260)^- \nu_\tau$ and $a_1(1260)^- \rightarrow \rho(770)^0 \pi^-$ decays to select signal/control regions of dipion mass.
- Fit Neural network response to discriminate signal from background.
 - Ditaum mass is not a good discriminator due to missing neutrino energy.
- LHCb sets limits on:

$$\mathcal{B}(B_s^0 \rightarrow \tau^+ \tau^-) < 6.8 \times 10^{-3} \text{ (95\% CL)}$$

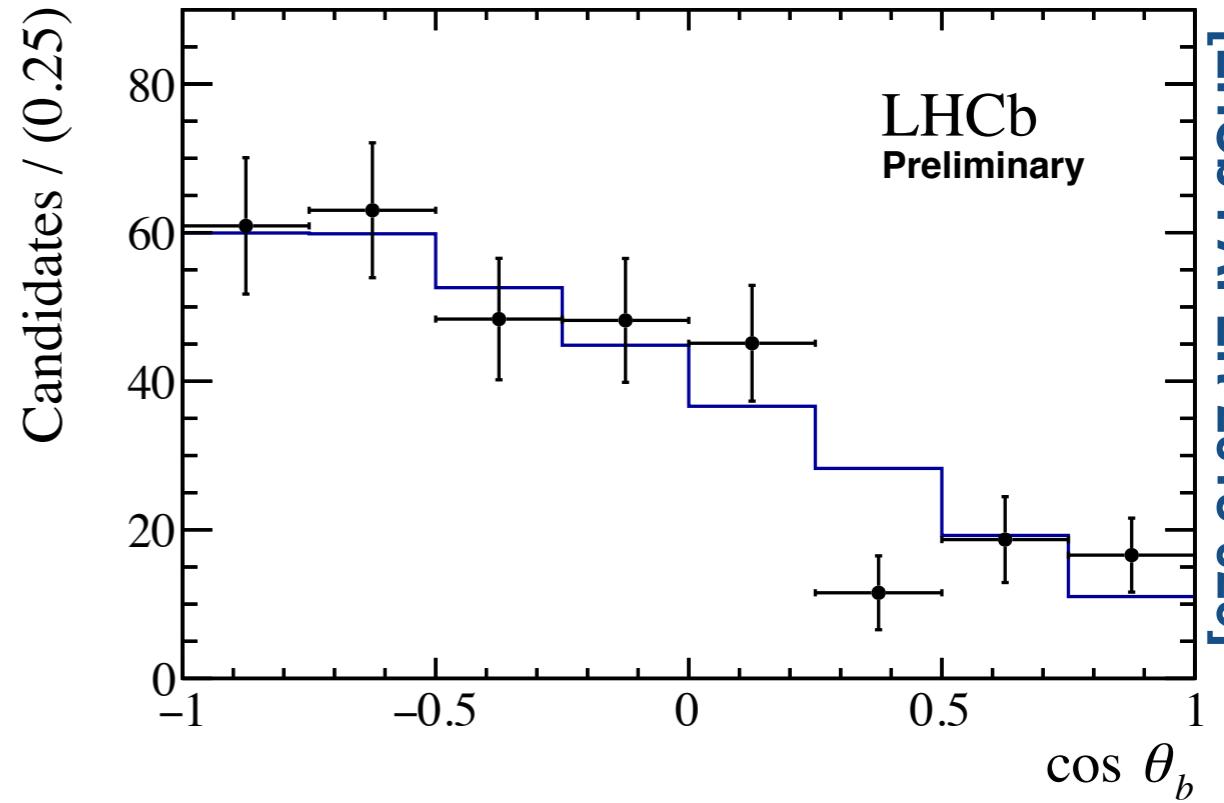
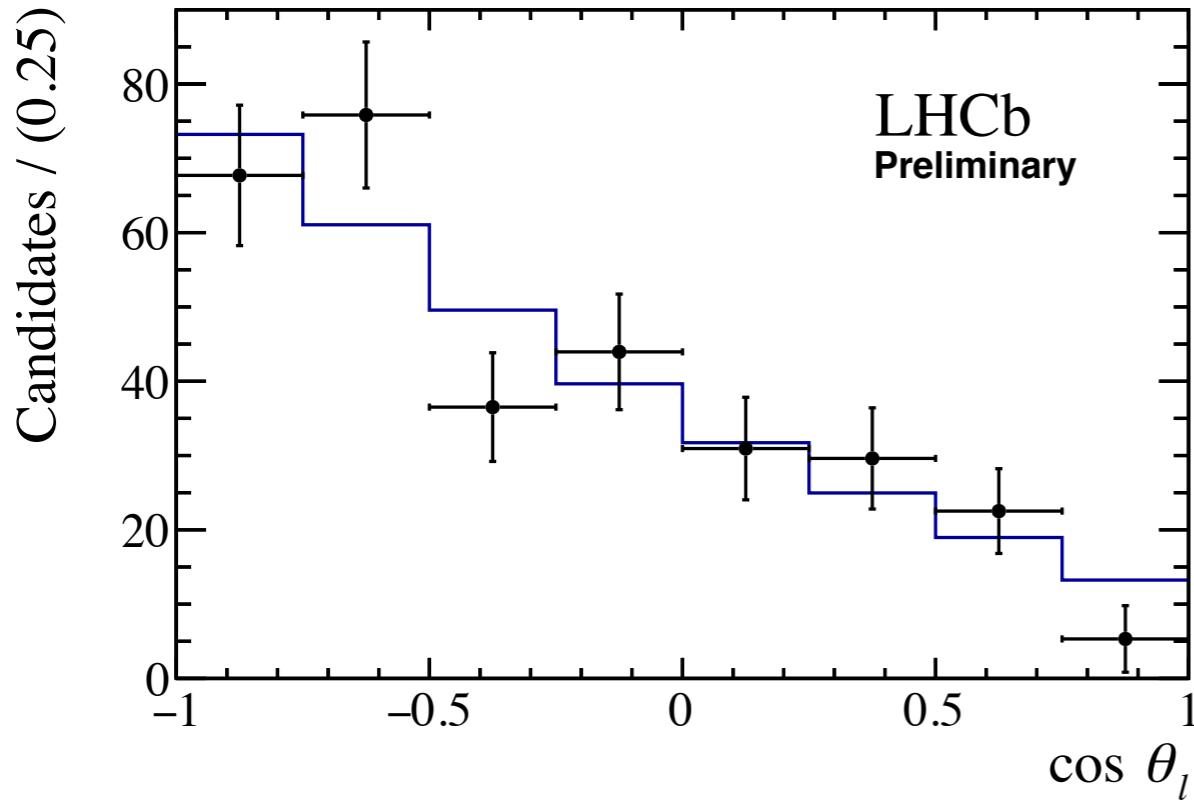
$$\mathcal{B}(B^0 \rightarrow \tau^+ \tau^-) < 2.1 \times 10^{-3} \text{ (95\% CL)}$$



[LHCb, PRL 118 (2017) 251802]

**First limit on $B_s \rightarrow \tau^+ \tau^-$ and
worlds best limit on $B^0 \rightarrow \tau^+ \tau^-$**

$\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ angular distribution



[LHCb-PAPER-2018-029]

- Large asymmetries on both the lepton- and hadron-side:

$A_{\text{FB}}^{\ell} = -0.39 \pm 0.04 \text{ (stat)} \pm 0.01 \text{ (syst)}$	Preliminary	}	Consistent with SM predictions [PRD 93 (2016) 074501] ($A_{\text{FB}}^{\ell h}$ is $\sim 2\sigma$ from its prediction)
$A_{\text{FB}}^h = -0.30 \pm 0.05 \text{ (stat)} \pm 0.02 \text{ (syst)}$	Preliminary		
$A_{\text{FB}}^{\ell h} = +0.25 \pm 0.04 \text{ (stat)} \pm 0.01 \text{ (syst)}$	Preliminary		
- Hadron-side asymmetry due to the weak decay of the Λ baryon.

Effective theory

- Can write a Hamiltonian for an effective theory of $b \rightarrow s$ processes:

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{\alpha_e}{4\pi} \sum_i C_i(\mu) \mathcal{O}_i(\mu),$$

$$\Delta \mathcal{H}_{\text{eff}} = \frac{\kappa_{\text{NP}}}{\Lambda_{\text{NP}}^2} \mathcal{O}_{\text{NP}}$$

κ_{NP} can have all/some/none of the suppression of the SM, e.g. MFV inherits SM CKM suppression.

Wilson coefficient
(integrating out scales above μ)

Local 4 fermion operators with different Lorentz structures

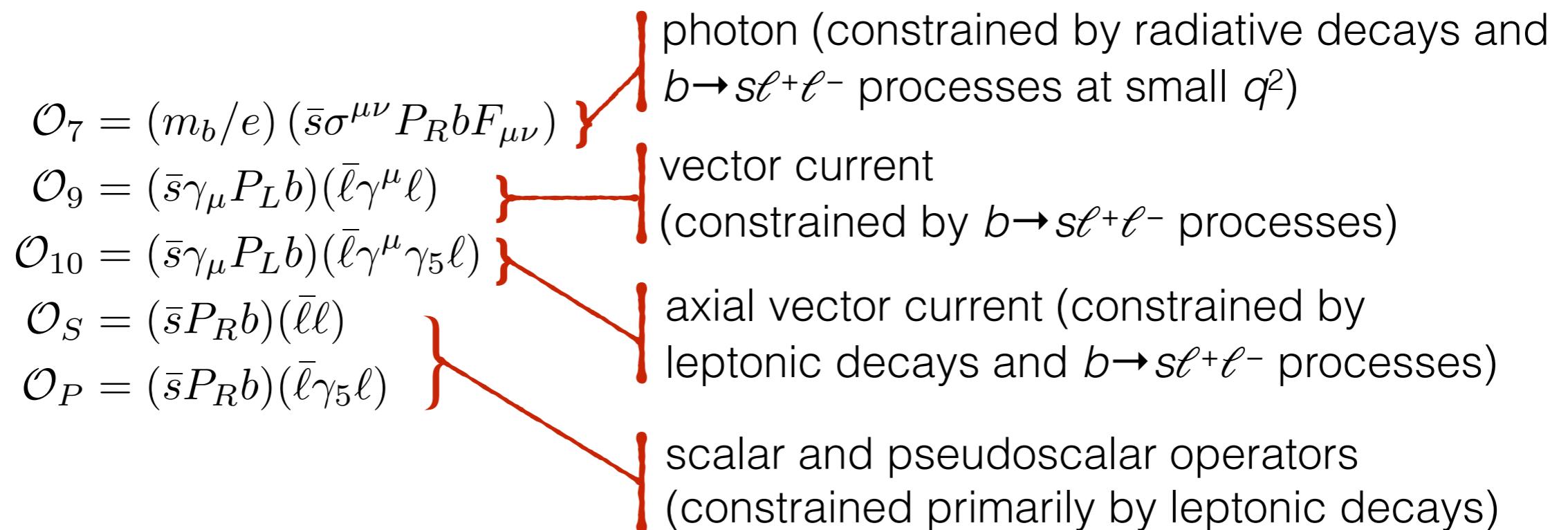
c.f. Fermi theory of weak interaction where at low energies:

$$\lim_{q^2 \rightarrow 0} \left(\frac{g^2}{m_W^2 - q^2} \right) = \frac{g^2}{m_W^2}$$

i.e. the full theory can be replaced by a 4-fermion operator and a coupling constant, G_F .

Operators

- Different processes are sensitive to different 4-fermion operators.
 - Can exploit this to over-constrain the system.



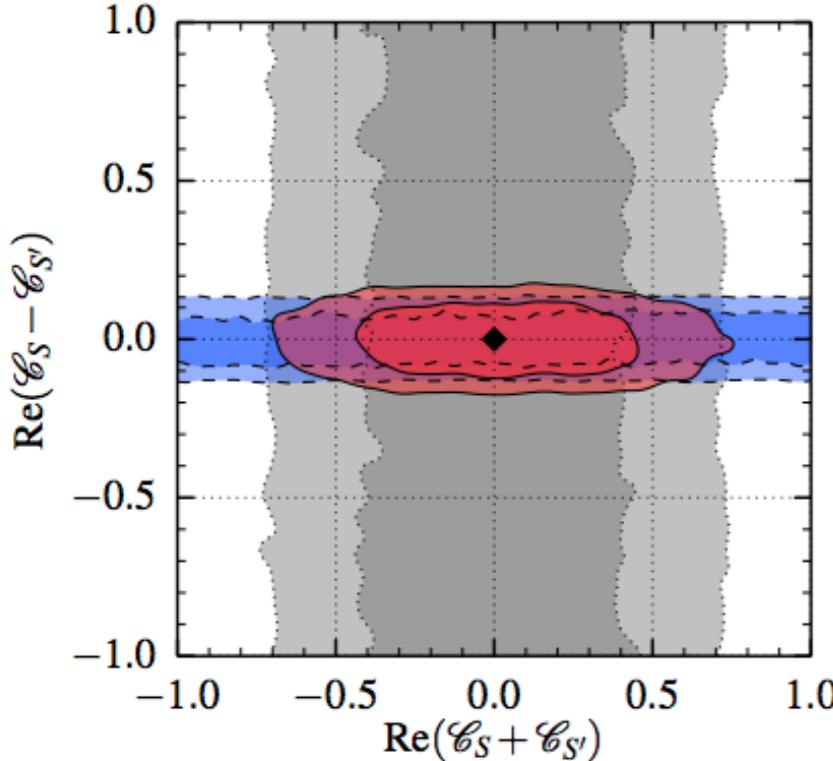
- e.g.
- $B_s^0 \rightarrow \mu^+ \mu^-$ constrains $C_{10} - C'_{10}$, $C_S - C'_S$, $C_P - C'_P$
 - $B^+ \rightarrow K^+ \mu^+ \mu^-$ constrains $C_9 + C'_9$, $C_{10} + C'_{10}$
 - $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ constrains $C_7 \pm C'_7$, $C_9 \pm C'_9$, $C_{10} \pm C'_{10}$

The primes denote right-handed counterparts of the operators whose contribution is small in the SM.

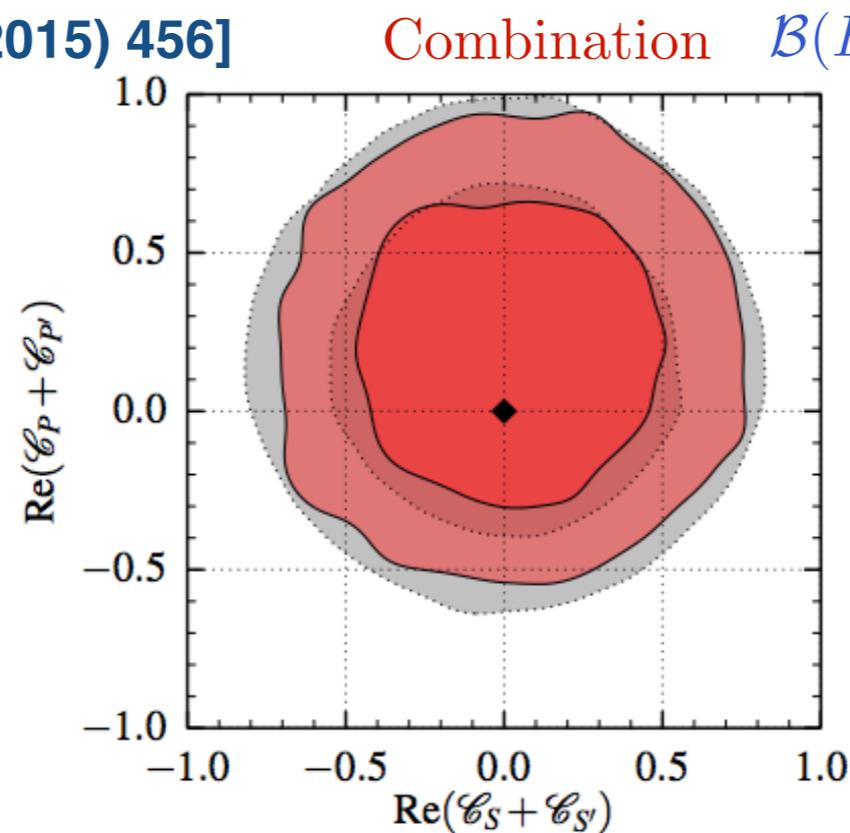
$B^+ \rightarrow K^+ \ell^+ \ell^-$

- Angular distribution of $B^+ \rightarrow K^+ \ell^+ \ell^-$ is a null test of SM, but can be sensitive to new scalar/pseudoscalar/tensor contributions, e.g.

[F. Beaujean et al. EPJC 75 (2015) 456]

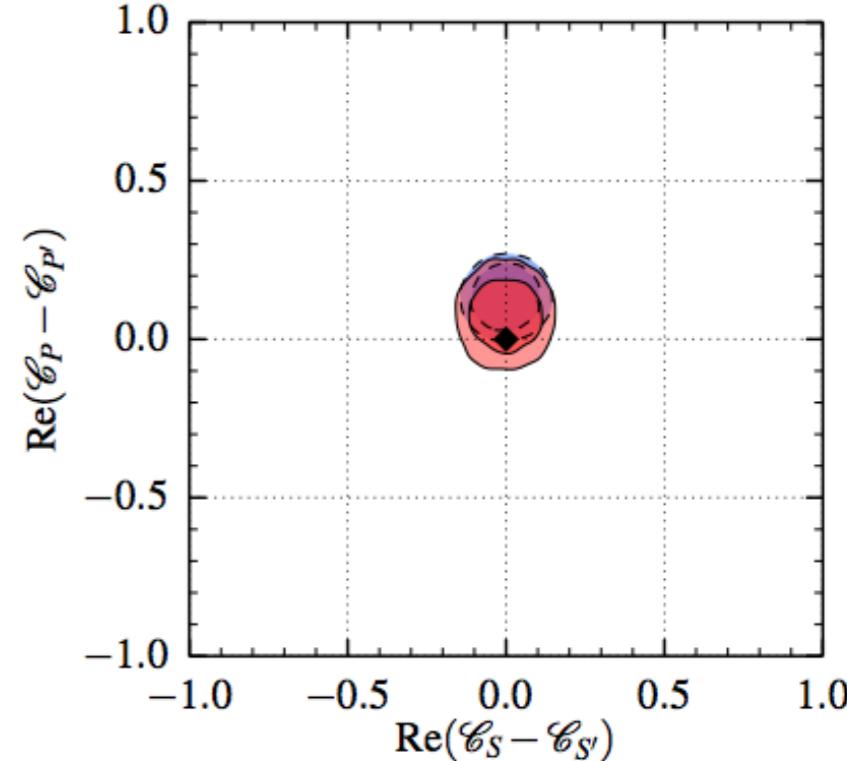


Combination



$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)$

$F_H[B^+ \rightarrow K^+ \mu^+ \mu^-]$

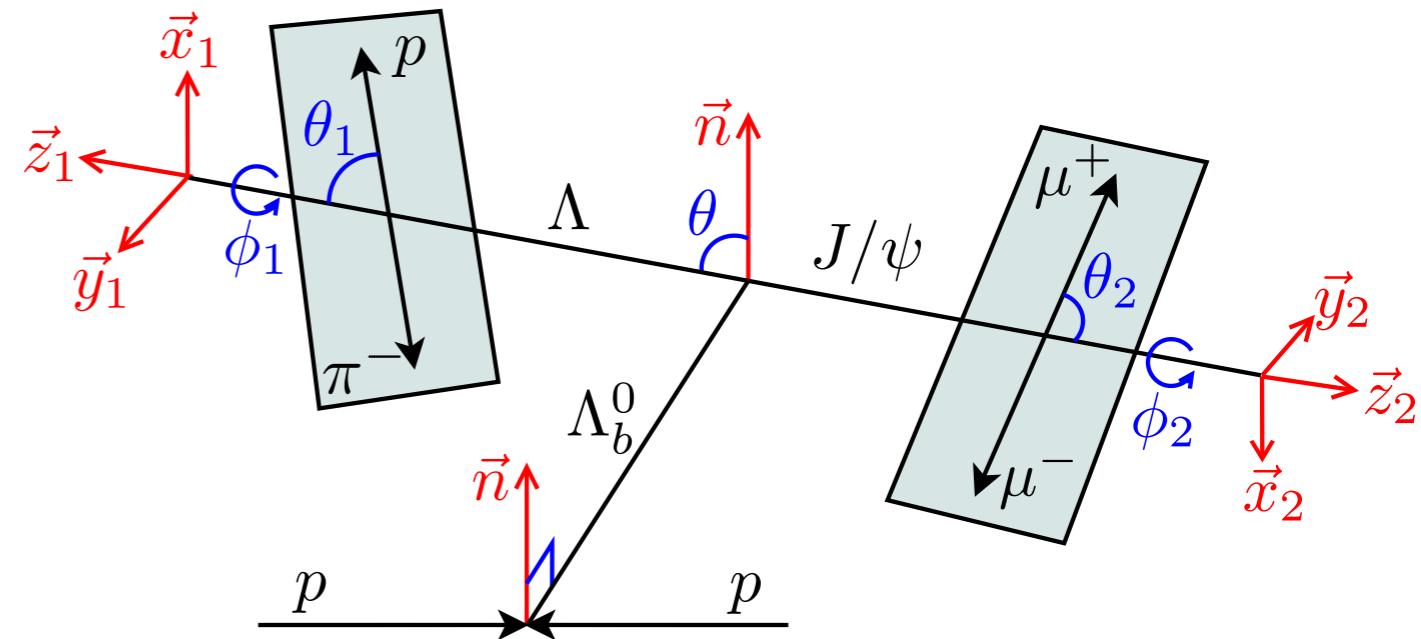


$\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ angular distribution

- If the Λ_b is produced polarised the decay is described by 5 angles and normal-vector, \hat{n} .
- Large number of observables:

$$\frac{d^5\Gamma}{d\vec{\Omega}} = \frac{3}{32\pi^2} \sum_i^{34} K_i(q^2) f_i(\vec{\Omega})$$

where $K_{11} - K_{34}$ are zero if the Λ_b is unpolarised. [Blake et al. JHEP 11 (2017) 138]

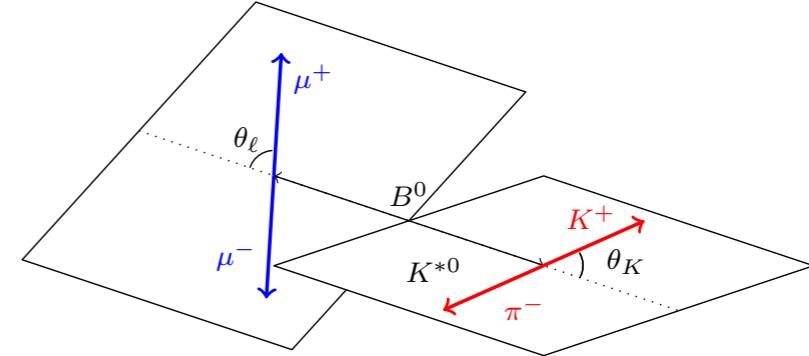


- Determine observables using the *method of moments* and a set of orthogonal weighing functions.
- Correct for angular efficiency using per-candidate weights determined on simulated phasespace events.
- Analysis cross-checked using $B^0 \rightarrow J/\psi K_S$ and $\Lambda_b \rightarrow J/\psi \Lambda$ decays selected in same way as the signal.

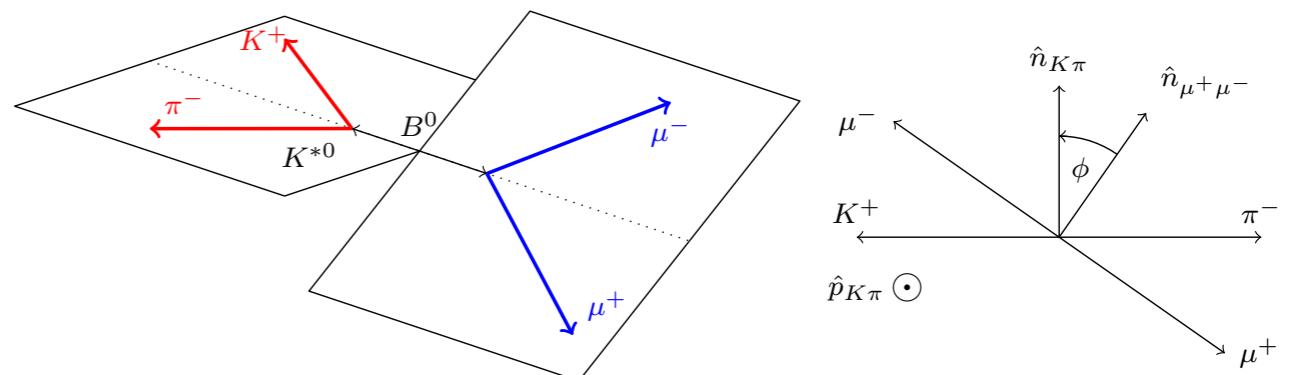
Angular observables

- Angular distribution provides many observables that are sensitive to BSM effects.
- Constraints are orthogonal to branching fraction measurements, both in their impact in global fits and in terms of experimental uncertainties.

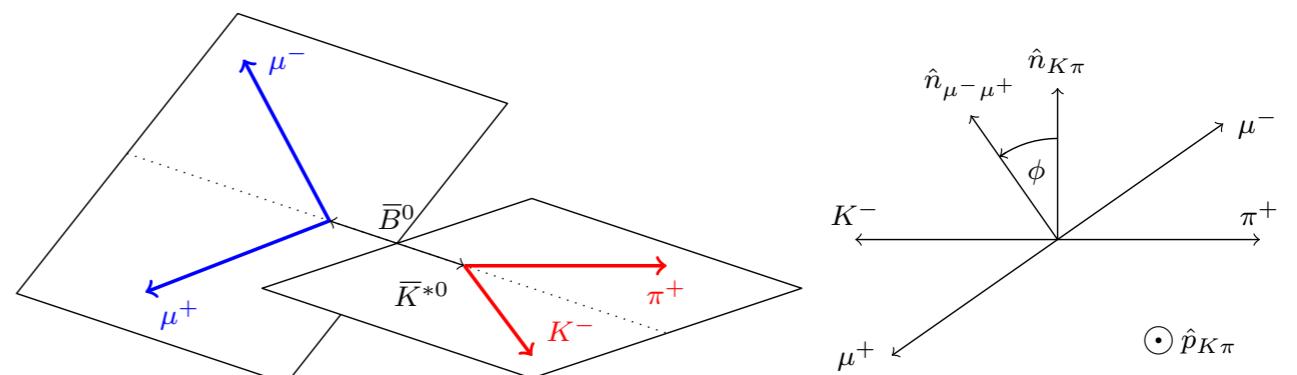
eg $B \rightarrow K^{*0} \mu^+ \mu^-$ decay described by three angles and q^2 .



(a) θ_K and θ_ℓ definitions for the B^0 decay



(b) ϕ definition for the B^0 decay

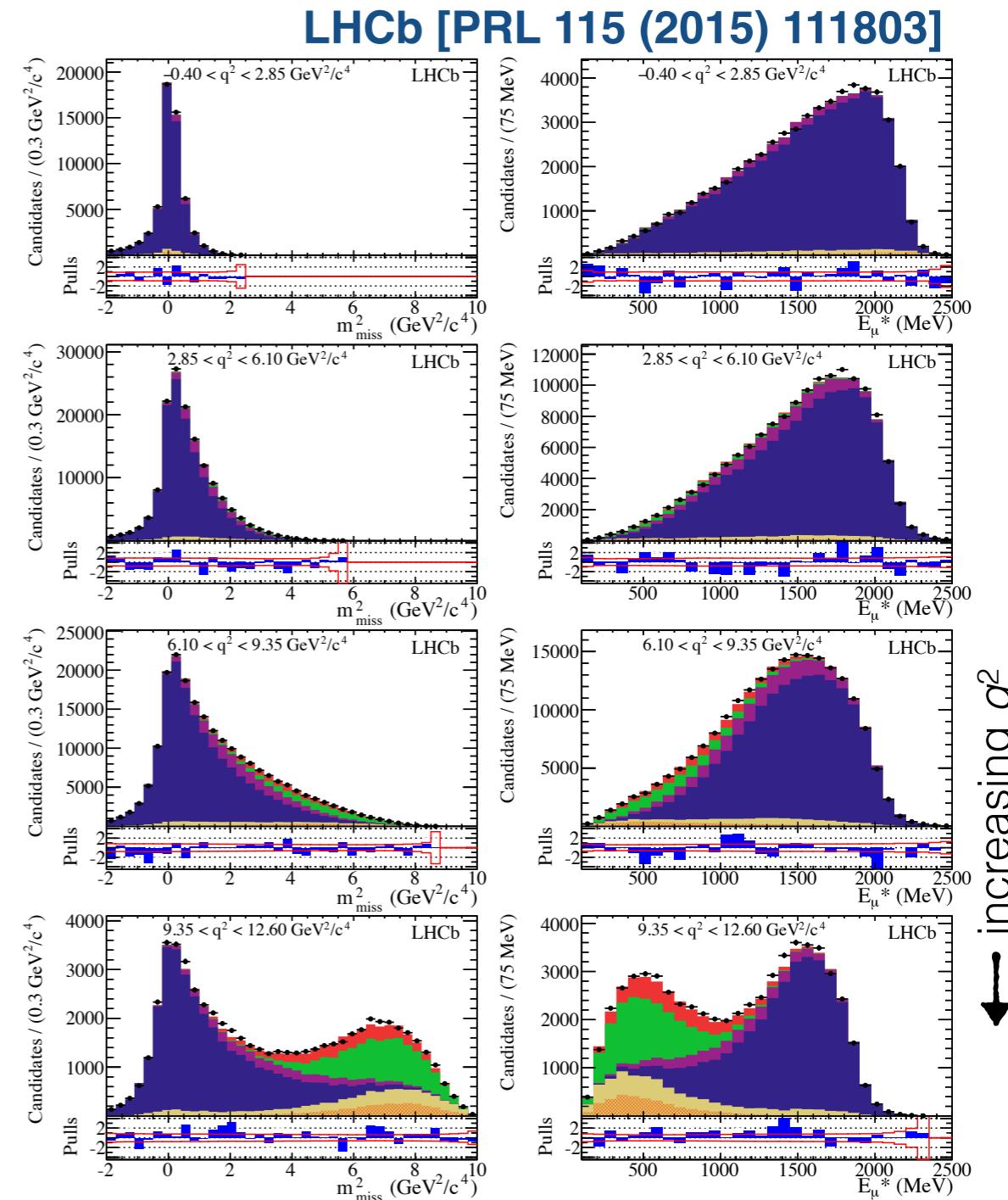


(c) ϕ definition for the \bar{B}^0 decay

$R(D^*)$ with $\tau \rightarrow \mu V$

- Experimental challenge is to separate signal from backgrounds.
 - Use missing mass, lepton energy, q^2 and multivariate discriminants.
 - Can use boost approximation to determine kinematic quantities $((\beta_z \gamma)_{\text{vis}} \approx (\beta_z \gamma)_B)$.
- B -factory experiments can exploit leptonic/hadronic tag of the other B in the event and centre-of-mass constraints.

Modelling of D^{} and hadronic background is important**



$B \rightarrow D^* \tau v$, $B \rightarrow D^* H_c (\rightarrow \mu v X)$, X , $B \rightarrow D^{**} \mu v$,
 $B \rightarrow D^* \mu v$, **combinatorial**, **misidentified**

V_{ub} and V_{cb}

[hflav.web.cern.ch]

- Long-standing tension between inclusive and exclusive determinations of V_{ub} and V_{cb} .

