

# Patterns of Flavor and CP Violation in Supersymmetric Theories

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Interplay of Collider and Flavour Physics  
3<sup>rd</sup> general meeting

CERN, December 14 - 16, 2009

based on:



**WA, A.J. Buras and P. Paradisi**

*“Low Energy Probes of CP Violation in a Flavor Blind MSSM”*

Phys. Lett. B **669** (2008) 239



**WA, A.J. Buras, S. Gori, P. Paradisi and D. Straub**

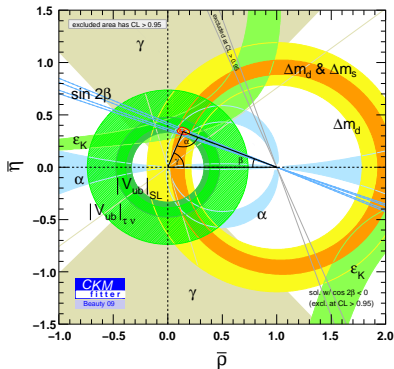
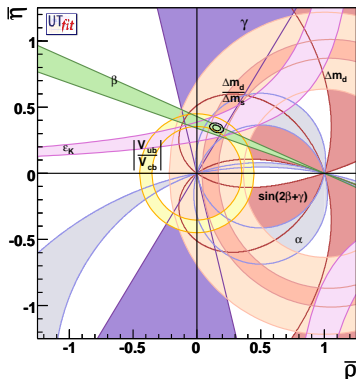
*“Anatomy and Phenomenology of FCNC and CPV effects in SUSY theories”*

arXiv:0909.1333 [hep-ph]

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- 1 Introduction: Flavor Problems
- 2 Phenomenology of CP Violation in a MFV MSSM
- 3 Predictions for  $S_{\psi\phi}$  in SUSY Flavor Models
- 4 Interplay between Flavor and Collider Physics
- 5 Summary

# Flavor Violation in the SM



Impressive consistency of the SM CKM picture  
of flavor and CP violation

(apart from some small tensions...

Lunghi, Soni '08, '09; Buras, Guadagnoli 08', 09'; WA, Buras, Gori, Paradisi, Staub '09; Laiho, Lunghi, Van de Water 09' )

# The NP Flavor Problem

FCNC processes are strongly suppressed in the SM

- ▶ loop suppression
- ▶ GIM mechanism
- ▶ small CKM angles

⇒ highly sensitive probes of NP degrees of freedom

Consider a generic NP contribution to e.g. Kaon mixing

$$\frac{C}{\Lambda_{\text{NP}}^2} (\bar{s}\gamma_{\mu}P_L d)^2$$

Measurements of  $\Delta M_K$  and  $\epsilon_K$  lead to strong constraints on  $C/\Lambda_{\text{NP}}^2$

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$\Delta M_K$	$\epsilon_K$
$C \simeq 1 \Rightarrow \Lambda_{\text{NP}} \gtrsim 10^3 \text{TeV}$	$\text{Im}(C) \simeq 1 \Rightarrow \Lambda_{\text{NP}} \gtrsim 10^4 \text{TeV}$
$\Lambda_{\text{NP}} \simeq 1 \text{TeV} \Rightarrow C \lesssim 10^{-6}$	$\Lambda_{\text{NP}} \simeq 1 \text{TeV} \Rightarrow \text{Im}(C) \lesssim 10^{-8}$

- ▶ a generic flavor structure of NP requires a very high NP scale
- ▶ NP degrees of freedom at the TeV scale have to have a highly non-generic flavor structure

# The SUSY Flavor Problem

Misalignment between quark and squark masses parametrized by **Mass Insertions**  $\delta$

$$M_{\tilde{q}}^2 = \tilde{m}^2 (\mathbb{1} + \delta_q)$$

$$\delta_q = \begin{pmatrix} \delta_q^{LL} & \delta_q^{LR} \\ \delta_q^{RL} & \delta_q^{RR} \end{pmatrix}$$

Complex Mass Insertions lead to **flavor and CP violating gluino-quark-squark interactions** that will generate the dominant contributions to FCNCs

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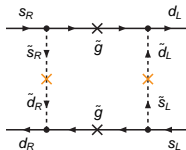
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e.g. Kaon mixing in presence of  $\delta_d^{LL}$  and  $\delta_d^{RR}$



$$\propto \frac{\alpha_s}{\tilde{m}^2} (\delta_d^{LL})_{21} (\delta_d^{RR})_{21} (\bar{s}P_L d) (\bar{s}P_R d)$$

- ▶ operator matrix element is **chirally enhanced** by  $M_K^2/m_s^2$
- ▶ Wilson coefficient is **color and RGE enhanced**

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- ▶ **severe constraints** on the SUSY scale and the Mass Insertions

$$(\delta_d^{LL})_{21} \simeq (\delta_d^{RR})_{21} \simeq 1$$

$$\Rightarrow \tilde{m} \gtrsim 10^3 (10^4) \text{ TeV}$$

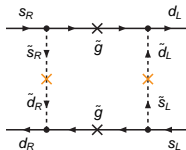
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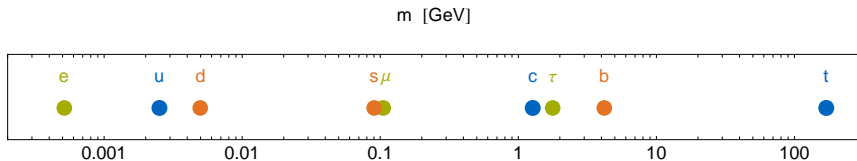


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# The SM Flavor Problem



$$V_{\text{CKM}} = \begin{pmatrix} \blacksquare & \blacksquare & \lightgray \\ \blacksquare & \blacksquare & \lightgray \\ \lightgray & \lightgray & \blacksquare \end{pmatrix} \approx \begin{pmatrix} 1 & \lambda & \lambda^3 \\ \lambda & 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix}$$

Also the SM flavor parameters are **highly non generic**.  
Both the fermion masses and mixing angles show a  
**hierarchical structure**.

## Minimal Flavor Violation

D'Ambrosio, Giudice, Isidori, Strumia '02

- ▶ the global  $U(3)^5$  flavor symmetry of the gauge sector is only broken by the SM Yukawa couplings
- ▶ CKM matrix is the only source of flavor violation
- ▶ FCNCs naturally suppressed
- ▶ visible effects possible in helicity suppressed processes as  $b \rightarrow s\gamma$ ,  $B_s \rightarrow \mu^+\mu^-$ ,  $B \rightarrow \tau\nu$
- ▶ additional sources of CP violation are in principle allowed!

**But:** only a solution to the NP/SUSY flavor problem, no explanation of the Yukawa hierarchies...

# Possible ways to address these problems

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## Alignment

Nir, Seiberg '93

- ▶ quark and squark masses are approximately aligned  
 $\rightarrow \delta_{ij} \ll 1, i \neq j$
- ▶ naturally realized in abelian flavor models

## Degeneracy

- ▶ squark masses are approximately universal  
 $\rightarrow \delta_{ij} \ll 1$
- ▶ can e.g. be realized in frameworks with low scale gauge mediation or in non-abelian flavor models

**Ambitious approach of SUSY flavor models:**  
simultaneous explanation of the Yukawa hierarchies and a non-generic squark flavor structure

# How to test such scenarios?

Look for characteristic NP effects in flavor observables that are not/only poorly measured.

the rare decay  
 $B_s \rightarrow \mu^+ \mu^-$

$$\text{BR}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}} = (3.6 \pm 0.4) \times 10^{-9}$$

$$\text{BR}(B_s \rightarrow \mu^+ \mu^-)_{\text{exp}} < 5.8 \times 10^{-8}$$

the  $B_s$  mixing  
phase

$$S_{\psi\phi}^{\text{SM}} \simeq 0.036$$

$$S_{\psi\phi}^{\text{exp}} = 0.81^{+0.12}_{-0.32}$$

the direct CP  
asymmetry in  
 $b \rightarrow s\gamma$

$$A_{CP}(b \rightarrow s\gamma)_{\text{SM}} = (-0.44^{+0.}_{-0.})\%$$

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+  $D_0 - \bar{D}_0$  mixing,  $B \rightarrow K^* \ell^+ \ell^-$ ,  $B \rightarrow K^* \gamma$ ,  $B \rightarrow K^{(*)} \nu \bar{\nu}$ , ...

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# Minimal Flavor Violation

# A Flavor Blind MSSM with CP Violating Phases

In a flavor blind MSSM (FBMSSM) there are no additional flavor structures apart from the CKM matrix. In particular, we assume

- ▶ universal squark masses
- ▶ hierarchical and flavor diagonal trilinear couplings
- ▶ flavor conserving but CP violating phases (in particular in the A-terms)



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Within this setup large NP effects arise dominantly through the **magnetic and chromomagnetic dipole operators**

$$\mathcal{O}_7 = \frac{e}{16\pi^2} m_b \bar{s}_L \sigma^{\mu\nu} F_{\mu\nu} b_R ,$$

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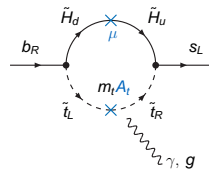
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The corresponding Wilson coefficients receive the dominant contributions from **Higgsino-stop loops\*** and are therefore mainly sensitive to **one complex parameter combination**

$$C_{7,8} \propto \mu A_t$$

\* see Hofer, Nierste, Scherer '09 for additional 2loop gluino contributions



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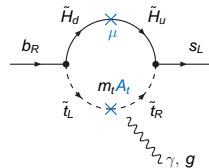
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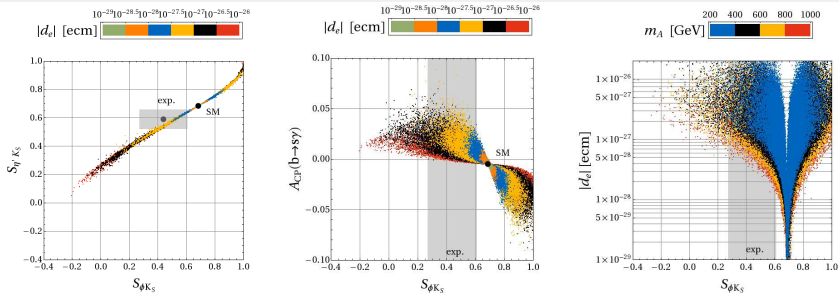
→ Interesting correlated effects in CP violating observables

For analyses of similar frameworks see:

Baek, Ko '99; Bartl, Gajdosik, Lunghi, Masiero, Porod, Stremnitzer, Vives '01; Ellis, Lee, Pilaftsis '07; Mercolli, Smith '09; Paradisi, Straub '09

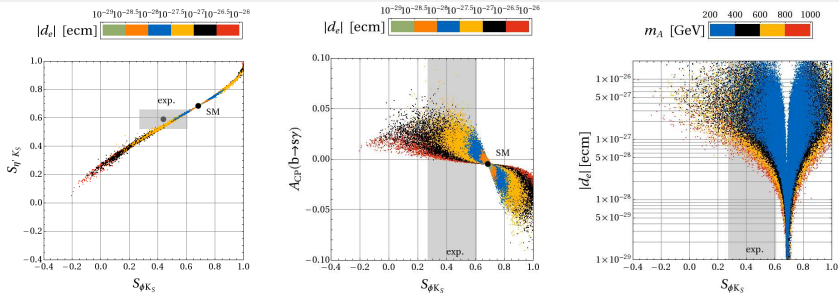
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# Phenomenology of CP Violation in a FBMSSM



- ▶ CP violating  $\Delta F = 0$  and  $\Delta F = 1$  dipole amplitudes can be strongly modified
- ▶  $S_{\phi K_S}$  and  $S_{\eta' K_S}$  can simultaneously be brought in **agreement with the data**
- ▶ sizeable and correlated effects in  $A_{CP}^{b \to s \gamma} \simeq 0\% - 5\%$
- ▶ **lower bounds** on the electron and neutron EDMs at the level of  $d_{e,n} \gtrsim 10^{-28}$  ecm
- ▶ large and correlated effects in the CP asymmetries in  $B \rightarrow K^* \mu^+ \mu^-$  (WA, Ball, Bharucha, Buras, Straub, Wick)

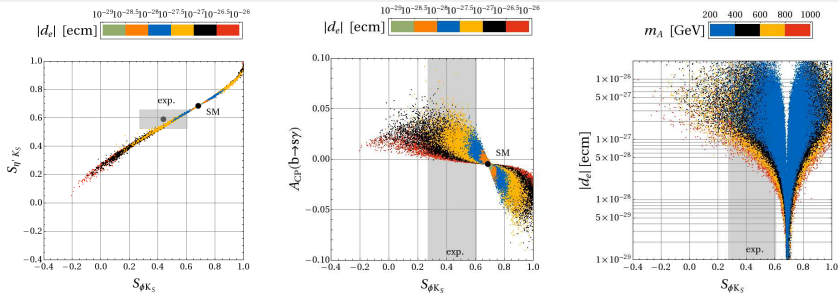
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- ▶ the leading NP contributions to  $\Delta F = 2$  amplitudes are **not sensitive** to the new phases of the FBMSSM
- ▶ CP violation in meson mixing is **SM like**
- ▶ i.e. small effects in  $S_{\psi\phi}$ ,  $S_{\psi K_S}$  and  $\epsilon_K$
- ▶ in particular:  $0.03 < S_{\psi\phi} < 0.05$

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A combined study of all these observables and their correlations constitutes a **very powerful test** of the FBMSSM

# Beyond MFV

# Representative Flavor Structures

only CKM like  $\delta_d^{LL}$   
mass insertions

comparable  $\delta_d^{LL}$  and  $\delta_d^{RR}$   
mass insertions that are  
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large  $\delta_d^{RR}$  mass  
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- ▶ many phenomenological features are similar to MFV frameworks (in particular typically small effects in  $\Delta F = 2$  amplitudes)
- ▶ distinction from MFV through the violation of “golden MFV relations” like

$$\frac{\text{BR}(B_s \rightarrow \mu^+ \mu^-)}{\text{BR}(B_d \rightarrow \mu^+ \mu^-)} = \frac{\hat{B}_d \tau_{B_s} \Delta M_s}{\hat{B}_s \tau_{B_d} \Delta M_d}$$

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- ▶  $(\delta_d^{RR})_{32}$  is only poorly constrained by data
- ▶ What are the phenomenological implications of a large  $(\delta_d^{RR})_{32}$  ?

# Implications of a large $(\delta_d^{RR})_{32}$ on $B_s$ mixing

## 1 Gluino boxes

$$\propto \frac{\alpha_s^2}{\tilde{m}^2} (\delta_d^{LL})_{32} (\delta_d^{RR})_{32} (\bar{b}P_{LS})(\bar{b}P_{RS})$$

$$\propto \frac{\alpha_s^2}{\tilde{m}^2} (\delta_d^{RR})_{32}^2 (\bar{b}\gamma_\mu P_{RS})^2$$

- ▶ color and RGE enhancement if  $(\delta_d^{LL})_{32}$  and  $(\delta_d^{RR})_{32}$  present simultaneously
- ▶ **decoupling** with  $1/\tilde{m}^2$

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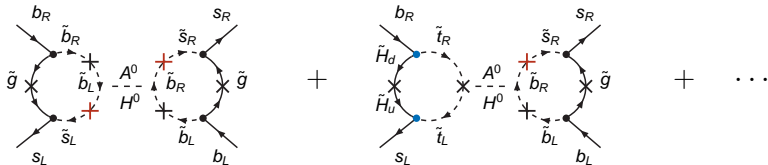
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## 2 Double Higgs Penguins



$$\propto \frac{\alpha_2}{4\pi} \frac{\alpha_s^2}{M_A^2} \frac{m_b^2}{M_W^2} \tan^4 \beta \frac{\mu^2 M_{\tilde{g}}^2}{\tilde{m}^4} (\delta_d^{LL})_{32} (\delta_d^{RR})_{32}$$

$$\propto \frac{\alpha_s}{4\pi} \frac{\alpha_2^2}{M_A^2} \frac{m_b^2}{M_W^2} \tan^4 \beta \frac{\mu^2 A_t M_{\tilde{g}}}{\tilde{m}^4} V_{tb} V_{ts}^* (\delta_d^{RR})_{32}$$

► proportionality to  $m_b^2$

► **no decoupling** with the SUSY scale! (but with  $1/M_A^2$ )

There are many flavor models  
that predict sizable  $\delta_d^{RR}$

► Abelian:

Nir, Seiberg '93; Nir, Raz '02;  
Agashe, Carone '03; ...

► Non Abelian:

Barbieri, Hall, Romanino '97;  
Carone, Hall, Moroi '97; ...  
Ross, Velasco-Sevilla, Vives '04;  
Antusch, King, Malinsky '07 ...

# Concrete Examples

Example: Agashe, Carone '03 (AC)

- ▶ Abelian flavor model based on a  $U(1)$  horizontal symmetry
- ▶ “remarkable level of alignment”

$$(\delta_d^{LL}) \sim \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & \lambda^2 \\ 0 & \lambda^2 & 1 \end{pmatrix}$$

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Expected phenomenology:

- ▶ Small effects in  $b \rightarrow d$  and  $s \rightarrow d$  transitions
- ▶ Large effects in  $D_0$ - $\bar{D}_0$  mixing (general feature of abelian models)
- ▶ Large effects in  $B_s$ - $\bar{B}_s$  mixing (in particular in  $S_{\psi\phi}$  for complex  $\delta s$ )

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Example: Ross, Velasco-Sevilla, Vives '04 (RVV)

- ▶ Non abelian flavor model based on a  $SU(3)$  flavor symmetry
- ▶ 1<sup>st</sup> and 2<sup>nd</sup> generation of squarks approximately degenerate

$$(\delta_d^{LL}) \sim \begin{pmatrix} \lambda^4 & \lambda^5 & \lambda^3 \\ \lambda^5 & \lambda^4 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix}$$

$$(\delta_d^{RR}) \sim \begin{pmatrix} \lambda^3 & \lambda^4 & \lambda^3 \\ \lambda^4 & \lambda^3 & \lambda \\ \lambda^3 & \lambda & 1 \end{pmatrix}$$

Expected phenomenology:

- ▶ Small effects in  $b \rightarrow d$  and  $s \rightarrow d$  transitions
- ▶ Large effects in  $D_0$ - $\bar{D}_0$  mixing (general feature of abelian models)
- ▶ Large effects in  $B_s$ - $\bar{B}_s$  mixing (in particular in  $S_{\psi\phi}$  for complex  $\delta_s$ )



# Concrete Examples

Example: Agashe, Carone '03 (AC)

- ▶ Abelian flavor model based on a  $U(1)$  horizontal symmetry
- ▶ “remarkable level of alignment”

$$(\delta_d^{LL}) \sim \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & \lambda^2 \\ 0 & \lambda^2 & 1 \end{pmatrix}$$

$$(\delta_d^{RR}) \sim \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & \lambda \\ 0 & \lambda & 1 \end{pmatrix}$$

Expected phenomenology:

- ▶ Small effects in  $b \rightarrow d$  and  $s \rightarrow d$  transitions
- ▶ Large effects in  $D_0$ - $\bar{D}_0$  mixing (general feature of abelian models)
- ▶ Large effects in  $B_s$ - $\bar{B}_s$  mixing (in particular in  $S_{\psi\phi}$  for complex  $\delta_s$ )

Example: Ross, Velasco-Sevilla, Vives '04 (RVV)

- ▶ Non abelian flavor model based on a  $SU(3)$  flavor symmetry
- ▶ 1<sup>st</sup> and 2<sup>nd</sup> generation of squarks approximately degenerate

$$(\delta_d^{LL}) \sim \begin{pmatrix} \lambda^4 & \lambda^5 & \lambda^3 \\ \lambda^5 & \lambda^4 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix}$$

$$(\delta_d^{RR}) \sim \begin{pmatrix} \lambda^3 & \lambda^4 & \lambda^3 \\ \lambda^4 & \lambda^3 & \lambda \\ \lambda^3 & \lambda & 1 \end{pmatrix}$$

Expected phenomenology:

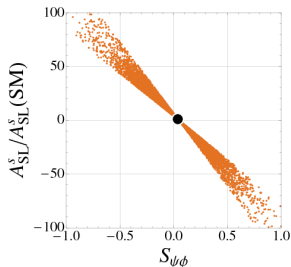
- ▶ Moderate effects in  $b \rightarrow d$  and  $s \rightarrow d$  transitions (large effects in  $\epsilon_K$ )
- ▶ Small effects in  $D_0$ - $\bar{D}_0$  mixing
- ▶ Sizeable effects in  $B_s$ - $\bar{B}_s$  mixing (in particular in  $S_{\psi\phi}$  for complex  $\delta_s$ )

# Numerical Results for $S_{\psi\phi}$

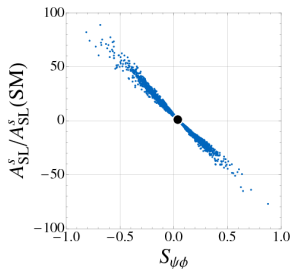
- ▶ Both models can have large effects in  $S_{\psi\phi}$
- ▶ Strong (model independent) correlation with the semileptonic asymmetry  $A_{SL}^s$

(Ligeti, Papucci, Prerez '06)

(\*) plots for the flavor models based on MSUGRA like spectrum  
 $5 < \tan \beta < 55$ ,  $m_0 < 2\text{TeV}$ ,  $m_{12} < 1\text{TeV}$ ,  
 $-3m_0 < A_0 = 3m_0$ ,  $\mu > 0$   
with flavor structures implemented at the GUT scale



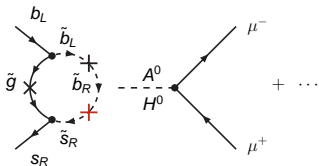
AC



RVV

# Correlation with $B_s \rightarrow \mu^+ \mu^-$

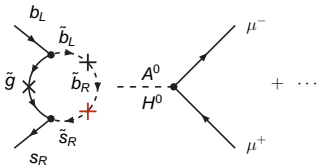
- ▶ for large double penguin contributions to  $B_s$  mixing, a correlation with  $B_s \rightarrow \mu^+ \mu^-$  is expected



$$\propto \frac{\alpha_s \alpha_2}{M_A^2} \frac{m_b m_\mu}{M_W^2} \tan^3 \beta \frac{\mu M_{\tilde{g}}}{\tilde{m}^2} (\delta_d^{RR})_{32} + \dots$$

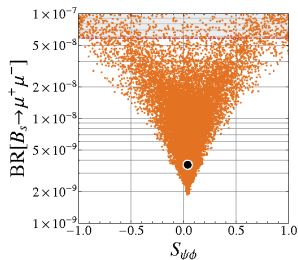
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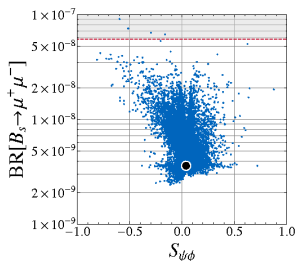


$$\propto \frac{\alpha_s \alpha_2}{M_A^2} \frac{m_b m_\mu}{M_W^2} \tan^3 \beta \frac{\mu M_{\tilde{g}}}{\tilde{m}^2} (\delta_d^{RR})_{32} + \dots$$

- ▶ double penguins are dominant in the AC model  $\Rightarrow$  lower bound on  $\text{BR}(B_s \rightarrow \mu^+ \mu^-)$  at the level of  $10^{-8}$
- ▶ in RVV model also boxes play a role  $\Rightarrow$  no correlation



AC

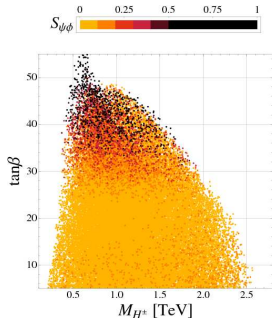
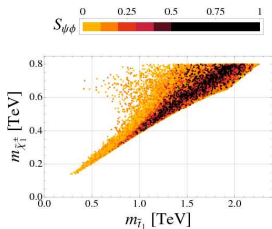


RVV

# Flavor vs. Collider

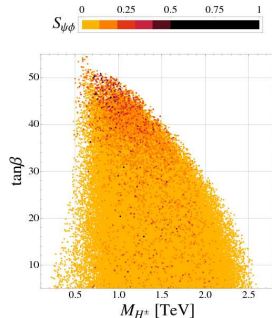
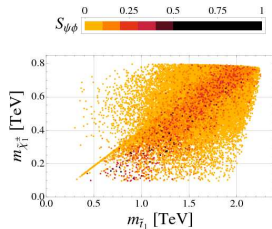
# Flavor Model Implications for Direct Searches

AC

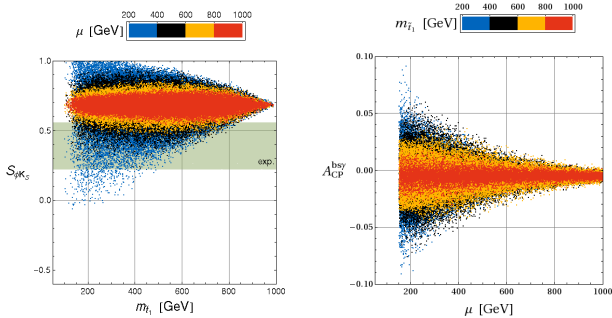


- ▶ Sizeable effects in  $S_{\psi\phi}$  are possible in a large region of parameter space
- ▶ Even **sparticles beyond the LHC reach** can lead to **visible departures of  $S_{\psi\phi}$  from its SM prediction** (non decoupling of double Higgs penguins)

RVV



# FBMSSM Implications for Direct Searches



- ▶  $S_{\phi K_S} \simeq 0.4$  implies  $\mu \lesssim 600\text{GeV}$  and  $m_{\tilde{t}_1} \lesssim 700\text{GeV}$
- ▶ similarly, large non standard effects in  $A_{CP}^{bsy} \gtrsim 2\%$  imply  $\mu \lesssim 600\text{GeV}$  and  $m_{\tilde{t}_1} \lesssim 800\text{GeV}$
- ▶ squarks lie well **within the reach of LHC**

# Summary

- ▶ in a MFV MSSM, CP violating  $\Delta F = 0$  and  $\Delta F = 1$  dipole amplitudes can be strongly modified
- ▶ one finds highly correlated effects in the EDMs,  $A_{CP}^{bs\gamma}$ , CP asymmetries in  $B \rightarrow K^* \ell^+ \ell^-$ ,  $S_{\phi K_S}$  and  $S_{\eta' K_S}$
- ▶ such effects imply SUSY particles in the reach of LHC
- ▶  $\Delta F = 2$  amplitudes remain however SM like (in particular: small effects in  $S_{\psi\phi}$ )



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  - ▶ such effects imply SUSY particles in the reach of LHC
  - ▶  $\Delta F = 2$  amplitudes remain however SM like (in particular: small effects in  $S_{\psi\phi}$ )
- 
- ▶ sizeable  $\delta_d^{RR}$  mass insertions lead to flavor changing right handed currents that imply a qualitatively very different phenomenology
  - ▶  $\Delta F = 2$  amplitudes can receive large NP effects
  - ▶ in the large  $\tan\beta$  regime, double Higgs penguin contributions to  $B_s$  mixing lead to a correlation between  $S_{\psi\phi}$  and  $B_s \rightarrow \mu^+ \mu^-$ , implying a lower bound on  $\text{BR}(B_s \rightarrow \mu^+ \mu^-)$  at the level of  $10^{-8}$  for  $S_{\psi\phi} \simeq 0.8$
  - ▶ these effects do not decouple with the SUSY scale
  - ▶ testable SUSY signatures in flavor observables even for sparticles that are beyond the LHC reach

# “Flavor DNA”

	GMSSM	AC	RVV	$\delta_{LL}$ only	FBMSSM
$D^0 - \bar{D}^0$ mixing	★★★★	★★★★	★	★	★
$\epsilon_K$	★★★★	★	★★★★	★	★
$S_{\psi\phi}$	★★★★	★★★★	★★★★	★	★
$S_{\phi K_S}, S_{\eta' K_S}$	★★★★	★★★★	★★	★★★★	★★★★
$A_{CP}^{bs\gamma}$	★★★★	★	★	★★★★	★★★★
$\langle A_{7,8} \rangle (B \rightarrow K^* \mu^+ \mu^-)$	★★★★	★	★	★★★★	★★★★
$\langle A_9 \rangle (B \rightarrow K^* \mu^+ \mu^-)$	★★★★	★	★	★	★
$B_s \rightarrow \mu^+ \mu^-$	★★★★	★★★★	★★★★	★★★★	★★★★
$B \rightarrow K^{(*)} \nu \bar{\nu}$	★★	★	★	★	★
$K \rightarrow \pi \nu \bar{\nu}$	★★★★	★	★	★	★
$d_e$	★★★★	★★★★	★★★★	★	★★★★

★★★★: large effects, ★★: moderate effects, ★: small effects