

# Experimental particle. physics

**esipap**...  
European School of Instrumentation  
in Particle & Astroparticle Physics

**2.** a few things about  
particle accelerators

# why?

a small hint...

$$E = mc^2$$

Aren't natural radioactive processes enough?  
What about cosmic rays?

# Why accelerating and colliding particles?

Aren't natural radioactive processes enough? What about cosmic rays?

High energy

$$E = mc^2$$

- Probe smaller scale
- Produce heavier particles

Large number of collisions

$$N = \mathcal{L} \cdot \sigma$$

- Detect rare processes
- Precision measurements

# Luminosity

Number of events  
in unit of time

$$N = \mathcal{L} \cdot \sigma$$

$[\text{t}^{-1}]$

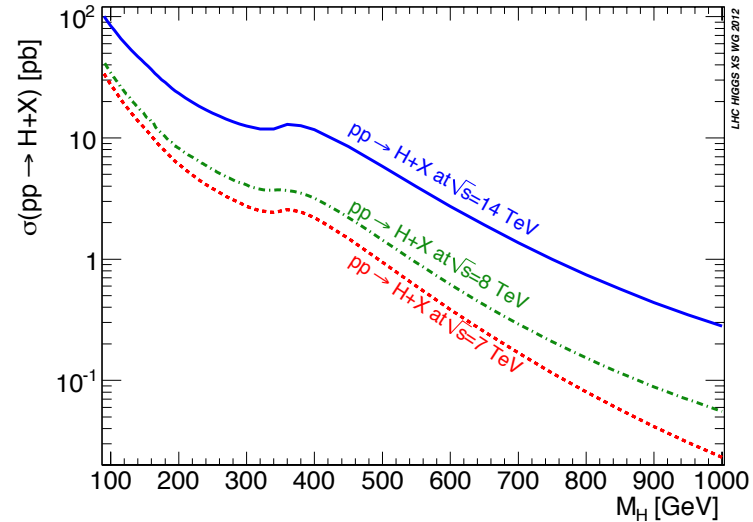
?

$[\text{L}^{-2} \text{t}^{-1}]$

$10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

$[\text{L}^2]$

$\sigma(\text{pp} \rightarrow \text{H}+\text{X}) \sim 20 \text{ pb}$



In a collider ring...

$$\mathcal{L} = \frac{1}{4\pi} \frac{fkN_1N_2}{\sigma_x\sigma_y}$$

Current

Beam sizes (RMS)

# What particle to accelerate and collide?

- **Stable (charged) particle**

- ✓ Electron/positron
  - ✓ Proton/antiproton
- } *what particle should we use?*

- **Secondary beams of charged or neutral particles**

- ✓ (Anti)neutrinos
- ✓ Muons
- ✓ Photons
- ✓ Charged pions
- ✓ Kaons
- ✓ ...

# Particle accelerations for dummies

(non-relativistic)  
Lorentz Force

$$\vec{F}_L = q \left( \vec{E} + \vec{v} \times \vec{B} \right)$$

time variation of  
kinetic energy

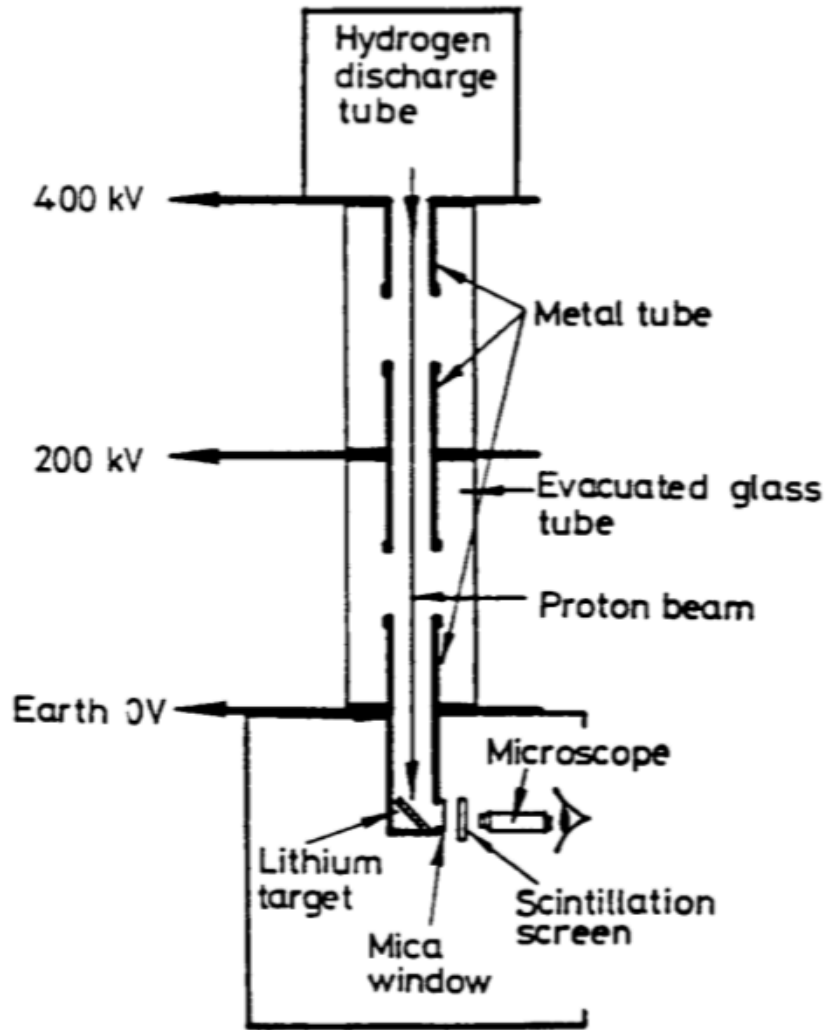
$$\frac{dE_{\text{kin}}}{dt} = \vec{F}_L \cdot \vec{v} = q\vec{v} \cdot \vec{E}$$

- Only longitudinal component of electrical field matters
- Time-varying electrical field to change energy
- (Static) magnetic field cannot change particle momentum...
- ... but can be used to bend its trajectory!

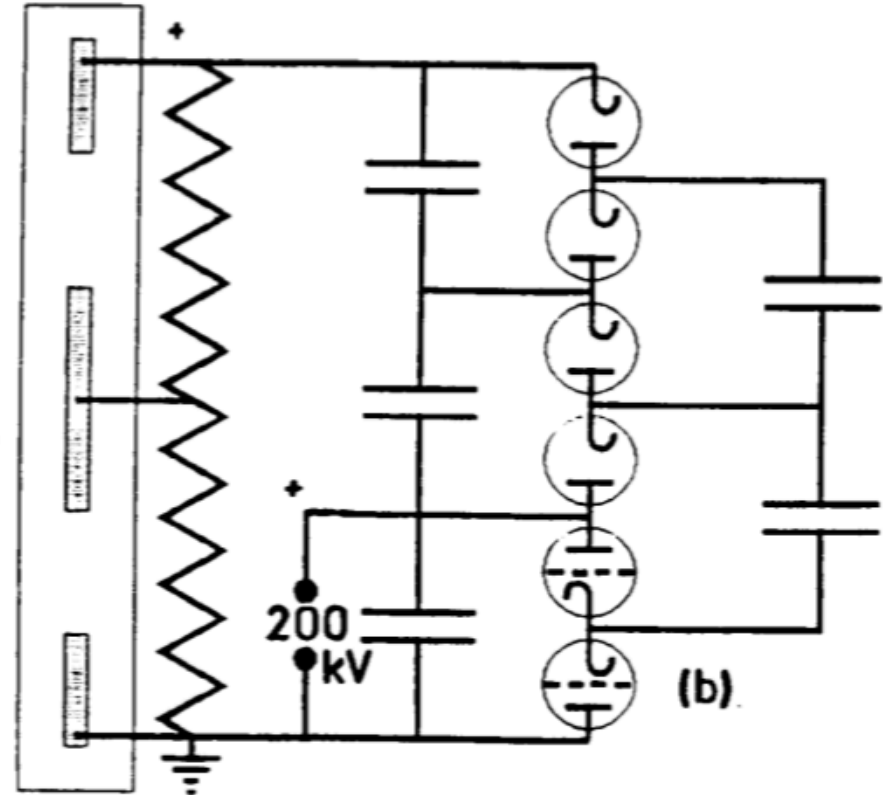
# A brief history of particle accelerators – part I

1895	Lenard. Electron scattering on gases (Nobel Prize).	< 100 keV electrons. Wimshurst-type machines.
1913	Franck and Hertz excited electron shells by electron bombardment.	
1906	Rutherford bombards mica sheet with natural alphas and develops the theory of atomic scattering.	Natural alpha particles of several MeV
1911	Rutherford publishes theory of atomic structure.	
1919	Rutherford induces a nuclear reaction with natural alphas.	
	... Rutherford believes he needs a source of many MeV to continue research on the nucleus. This is far beyond the electrostatic machines then existing, but ...	
1928	<b>Gamov predicts tunnelling and</b> perhaps 500 keV would suffice ...	
1928	Cockcroft & Walton start designing an 800 kV generator encouraged by Rutherford.	
1932	Generator reaches 700 kV and Cockcroft & Walton split lithium atom with only 400 keV protons. They received the Nobel Prize in 1951.	

# Cockcroft and Walton's apparatus



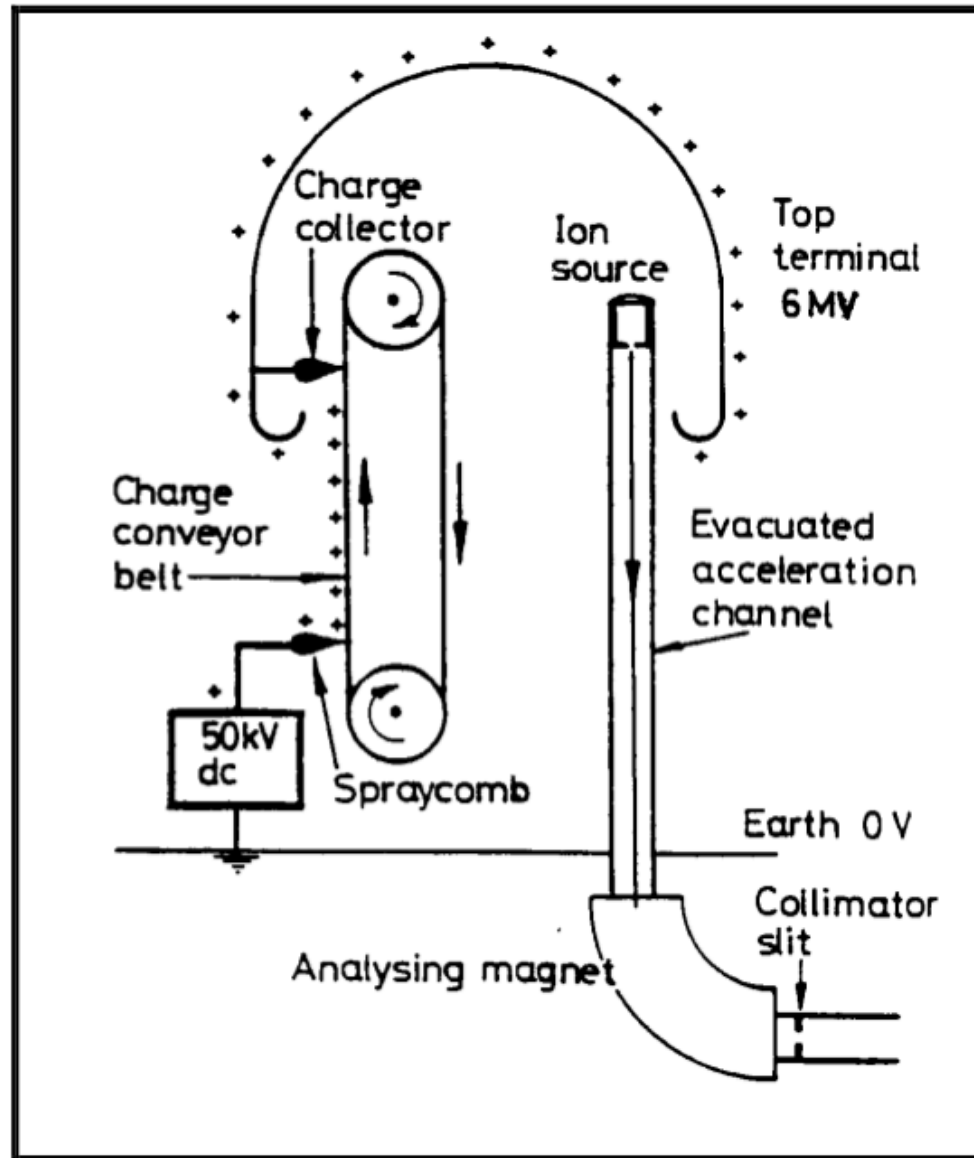
(a) Accelerating column



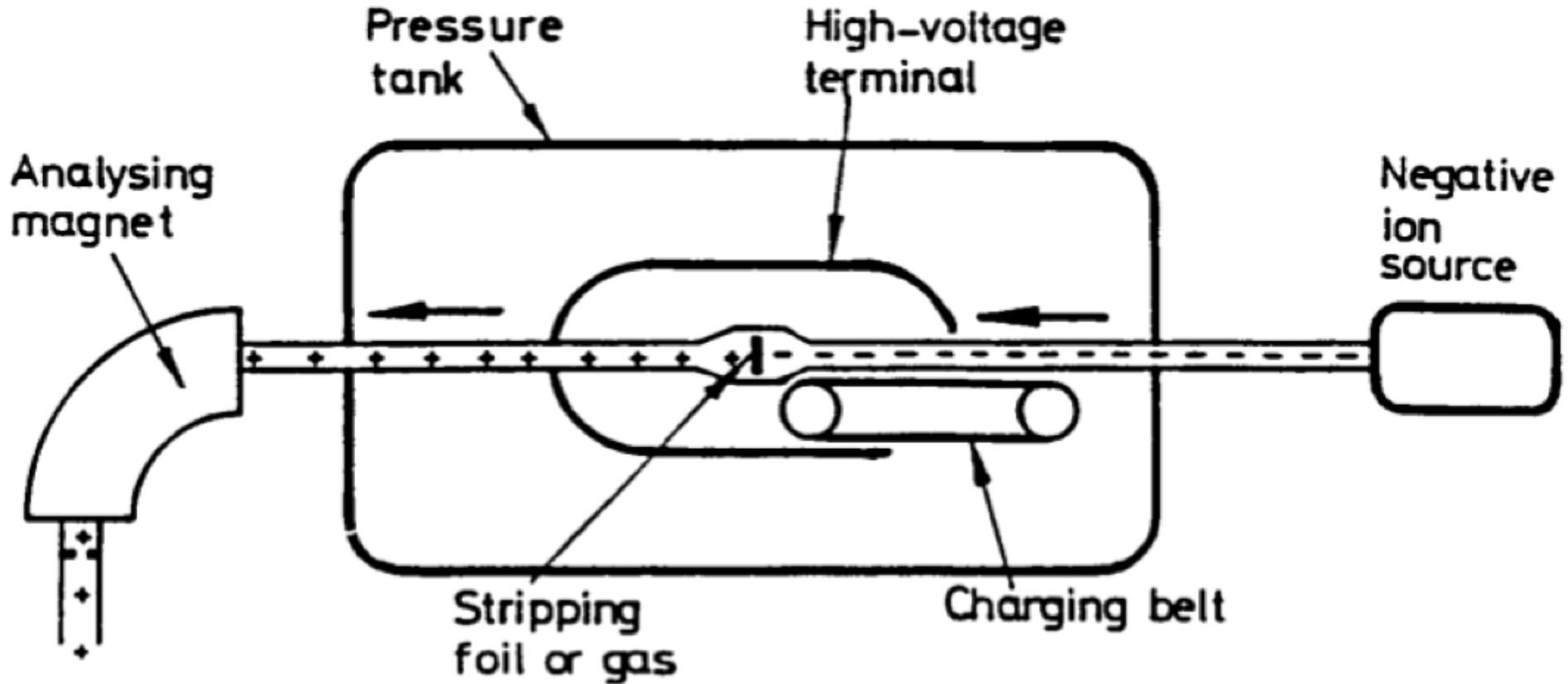
(b) DC generator



# Van de Graaff electrostatic generator



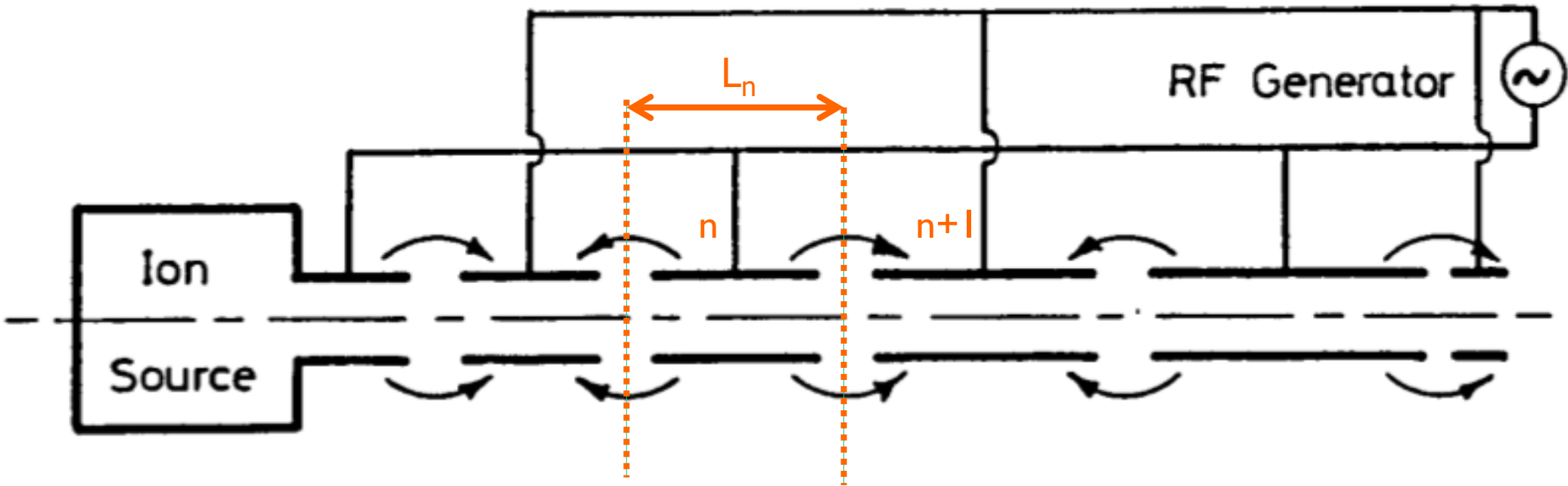
# Two-stage Tandem accelerator



# A brief history of particle accelerators – part 2

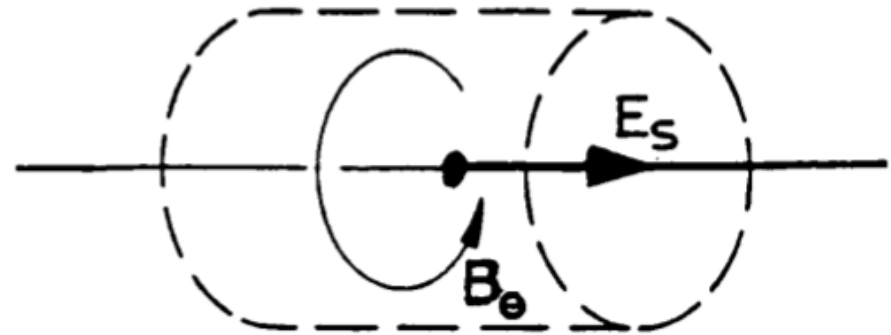
- |      |   |
|------|---|
| 1924 | Ising proposes time-varying fields across drift tubes. This is "resonant acceleration", which can achieve energies above that given by the highest voltage in the system. |
| 1928 | Wideröe demonstrates Ising's principle with a 1 MHz, 25 kV oscillator to make 50 keV potassium ions.  |
| 1929 | Lawrence, inspired by Wideröe and Ising, conceives the cyclotron.   |
| 1931 | Livingston demonstrates the cyclotron by accelerating hydrogen ions to 80 keV.  |
| 1932 | Lawrence's cyclotron produces 1.25 MeV protons and he also splits the atom just a few weeks after Cockcroft and Walton (Lawrence received the Nobel Prize in 1939).       |

# RF linear accelerator (LINAC)



$$L_n = k \frac{v_n}{c} \frac{\lambda}{2}$$

Where:  $k=1, L < \lambda$



# LINAC length

Total LINAC length

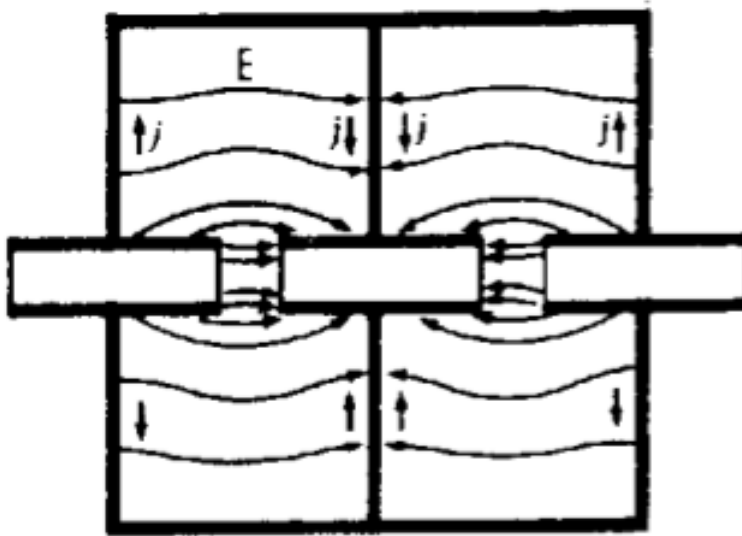
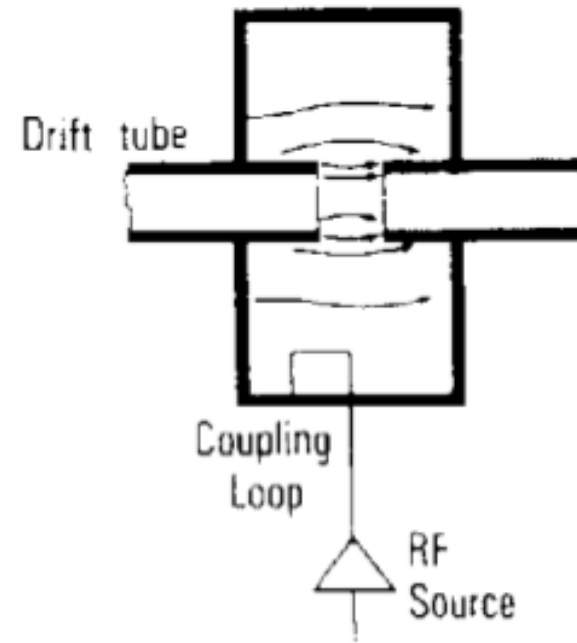
$$L = \frac{k}{\Delta E} \sqrt{\frac{E^3}{Amc^2}} \frac{\lambda}{2}$$

energy gain per gap      ion atomic number      final particle energy

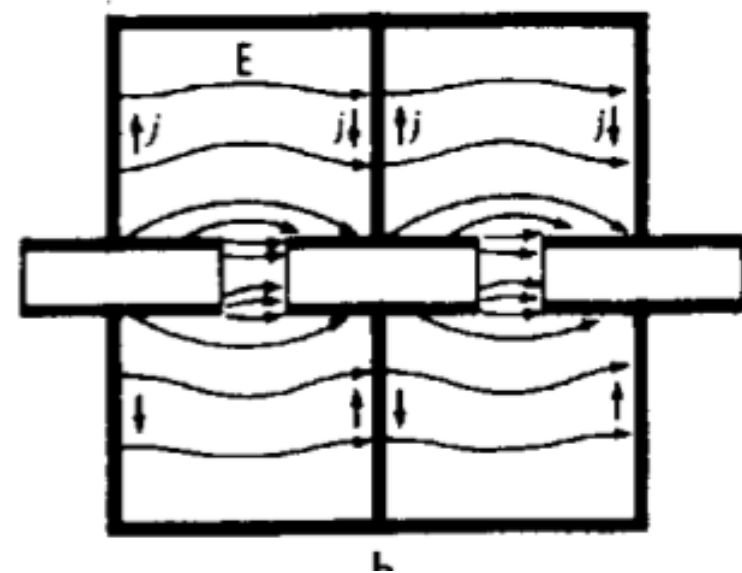
- Example: proton ( $A=1$ ) with  $E = 1 \text{ MeV}$  ( $\beta = 4.6 \cdot 10^{-2}$ ) if  $\nu_{\text{RF}} = 7 \text{ MHz}$  will travel about  $1 \text{ m}$  in half a RF cycle
- Total LINAC length increases dramatically with increasing speed
- A possible solution would be to increase  $\nu_{\text{RF}}$
- ... but at very high  $\nu_{\text{RF}}$  open tube structure radiates too much energy!

# RF cavities

- The problem can be solved by closing the structure as a **cavity**...
- Cavities can be joined
- Choosing  $k=2$  currents on walls cancel, and walls can be eliminated

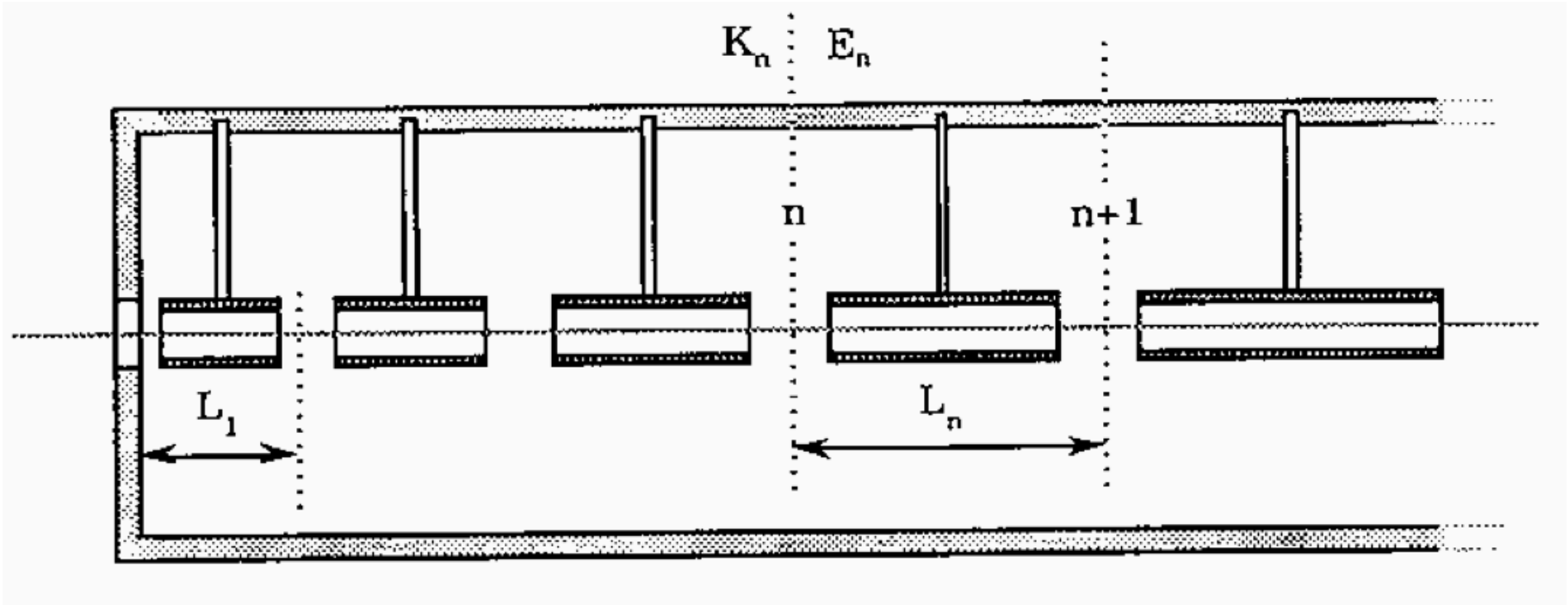


$k=1$



$k=2$

# Alvarez structure



$$k = 2, v_{RF} \sim 100 \text{ MHz}, \lambda < L$$

protons  $\beta \sim 1$  for  $E \sim 10 \text{ GeV}$

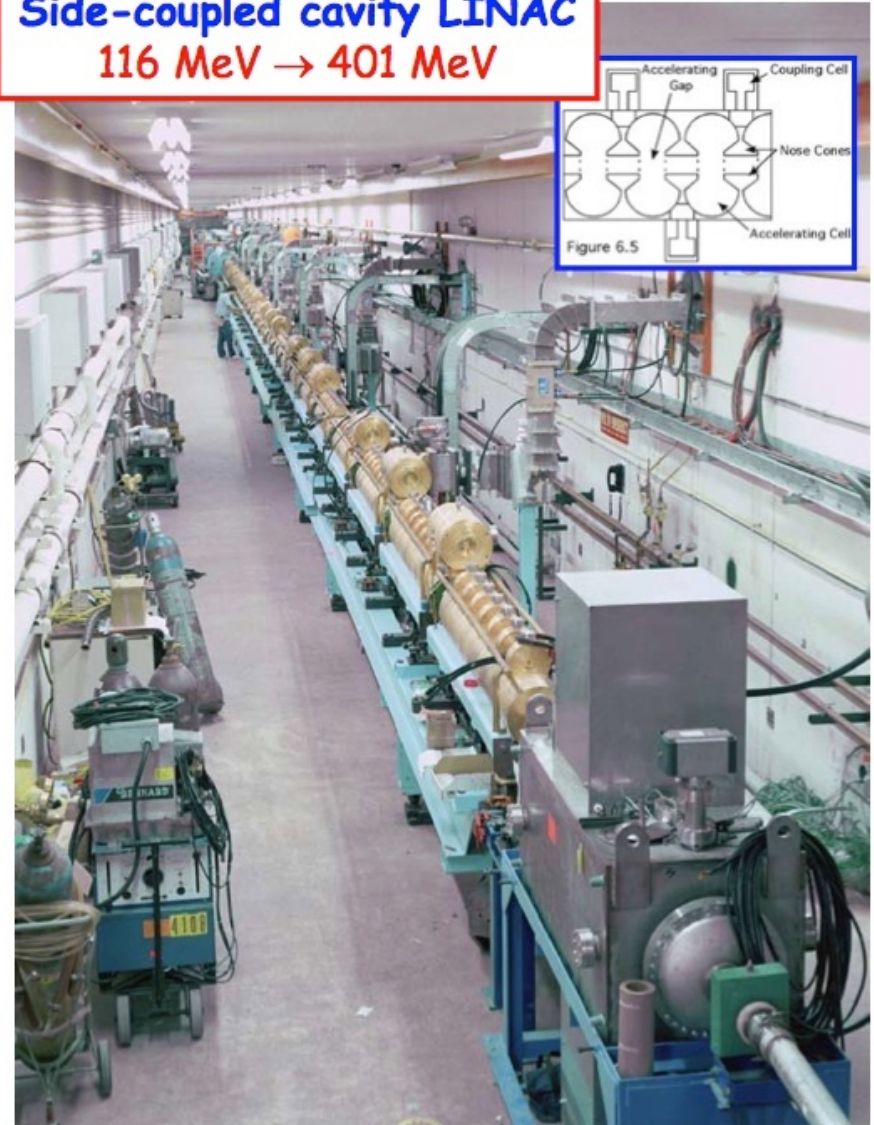
electrons  $\beta \sim 1$  for  $E \sim 10 \text{ MeV}$

already at those energies  $v \sim c \rightarrow$  drift tube length can stay constant!

# Example: Fermilab LINAC

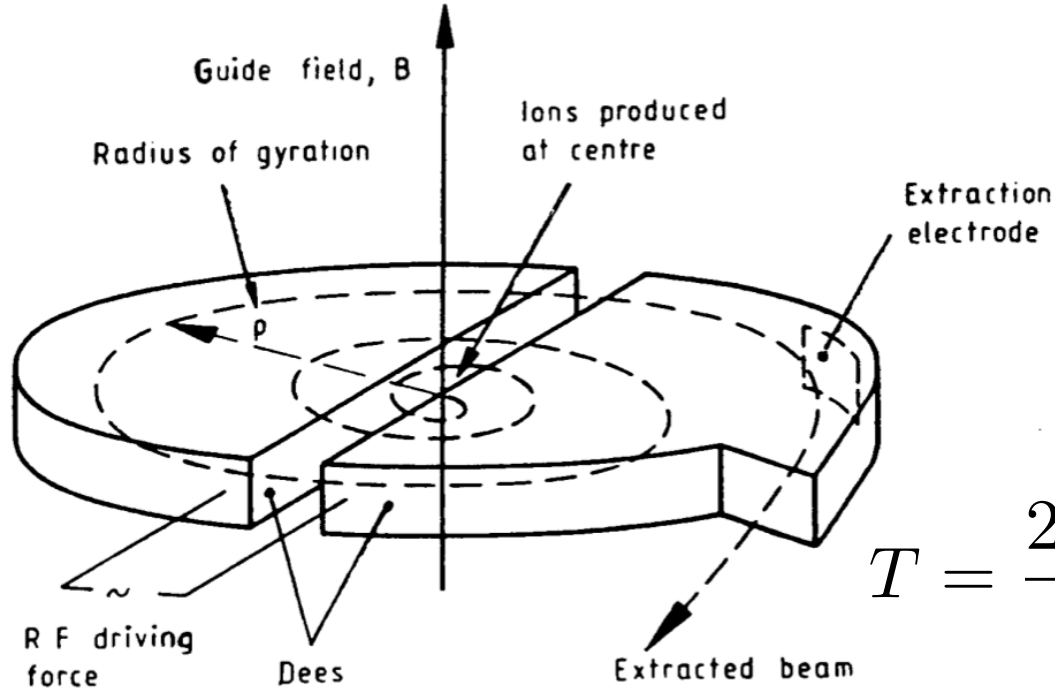


**Side-coupled cavity LINAC**  
116 MeV → 401 MeV





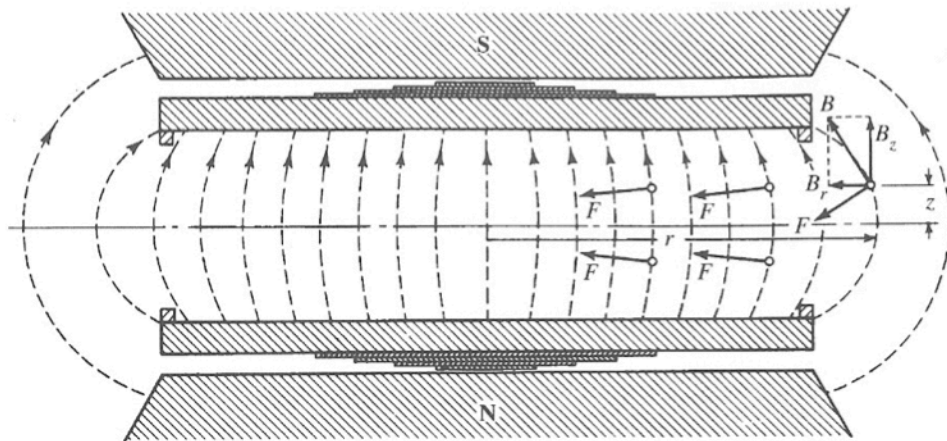
# (Syncro) Cyclotron



$$p = m\gamma\beta$$

$$p = eBR$$

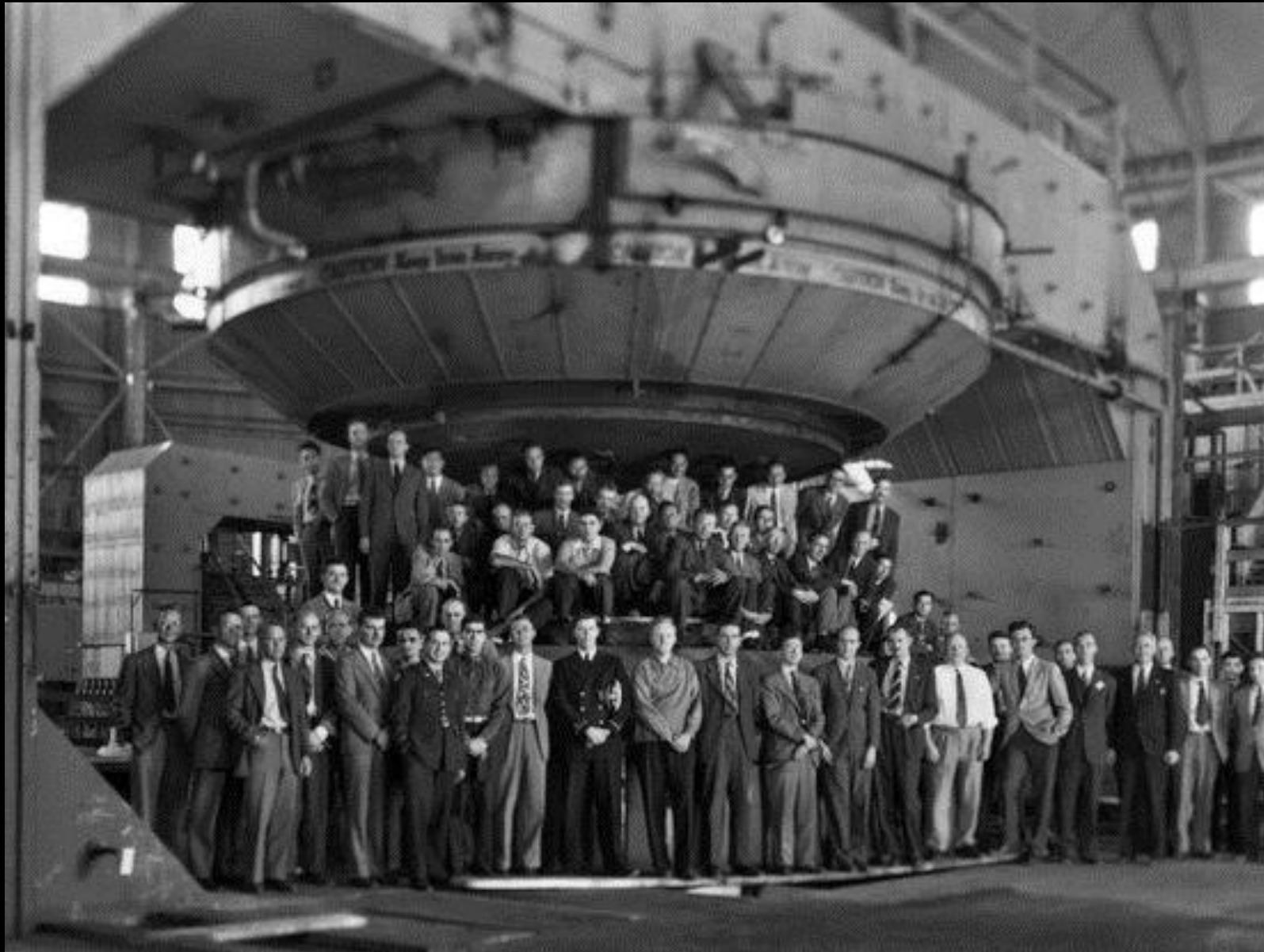
$$T = \frac{2\pi R}{v} = \frac{2\pi R}{\beta c} = \frac{\pi p}{eB\beta c} = \gamma \frac{\pi m}{eB}$$



for relativistic particle **cyclotron frequency** should be adjusted to speed/energy (**synchro-cyclotron**)

weak focusing

# Berkeley syncro-cyclotron ( $p$ , $E = 340$ MeV)



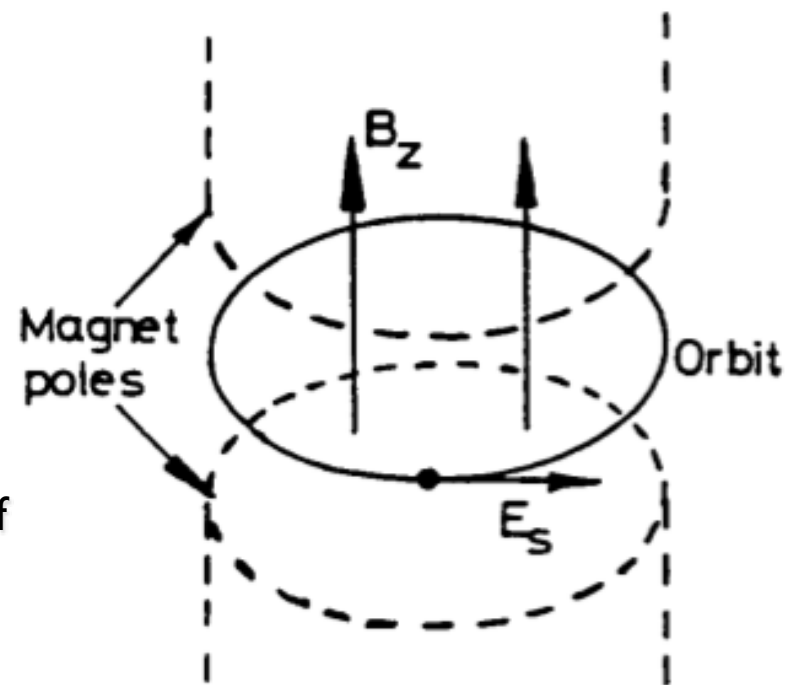
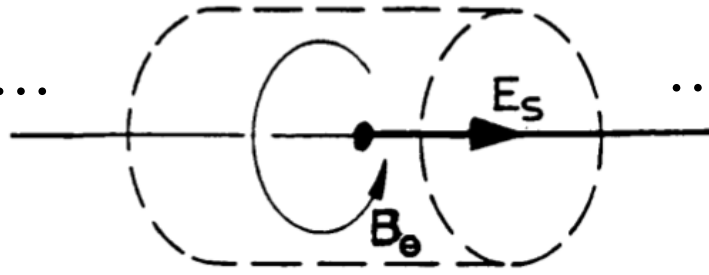
# A brief history of particle accelerators – part 3

*(or as varying magnetic fields could also be used to accelerate particles)*

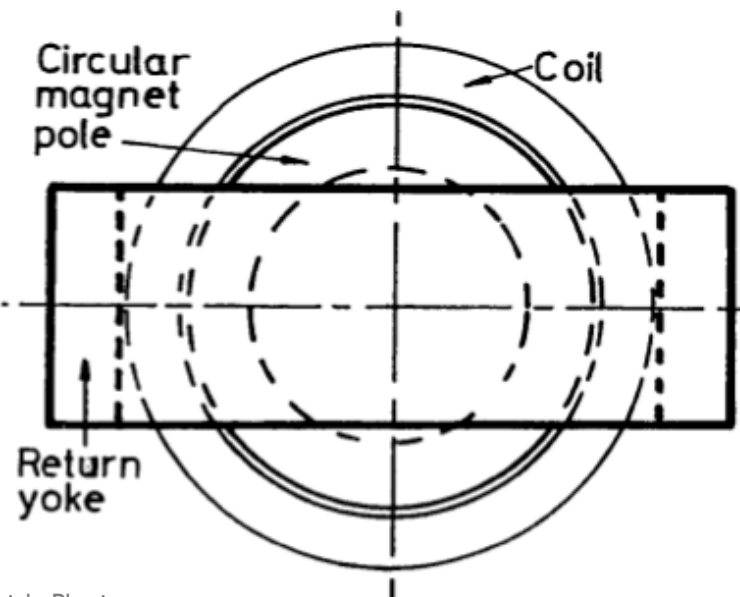
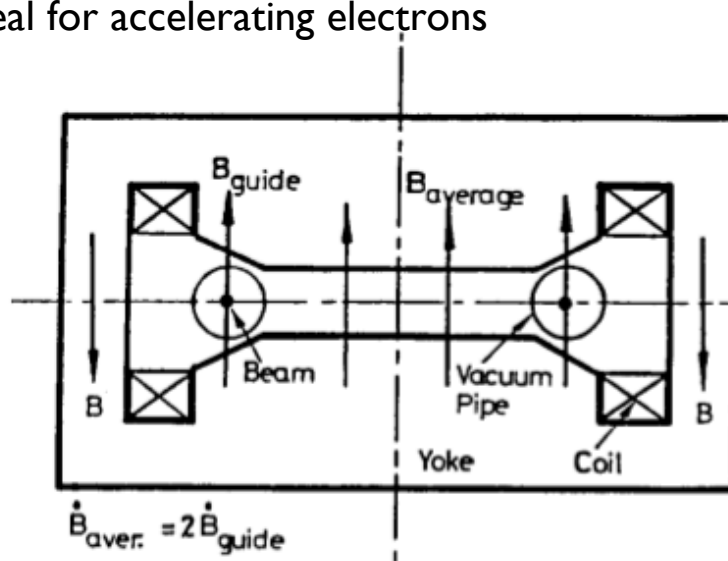
- |      |  |
|------|--|
| 1923 | Wideröe, a young Norwegian student, draws in his laboratory notebook the design of the betatron with the well-known 2-to-1 rule. Two years later he adds the condition for radial stability <b>but does not publish.</b> |
| 1927 | Later in Aachen Wideröe makes a model betatron, but it does not work. Discouraged he changes course and builds the linear accelerator mentioned in Table 2.  |
| 1940 | Kerst re-invents the betatron and builds the first working machine for 2.2 MeV electrons.  |
| 1950 | Kerst builds the world's largest betatron of 300 MeV.  |

# Betatron acceleration

from... ... to ...

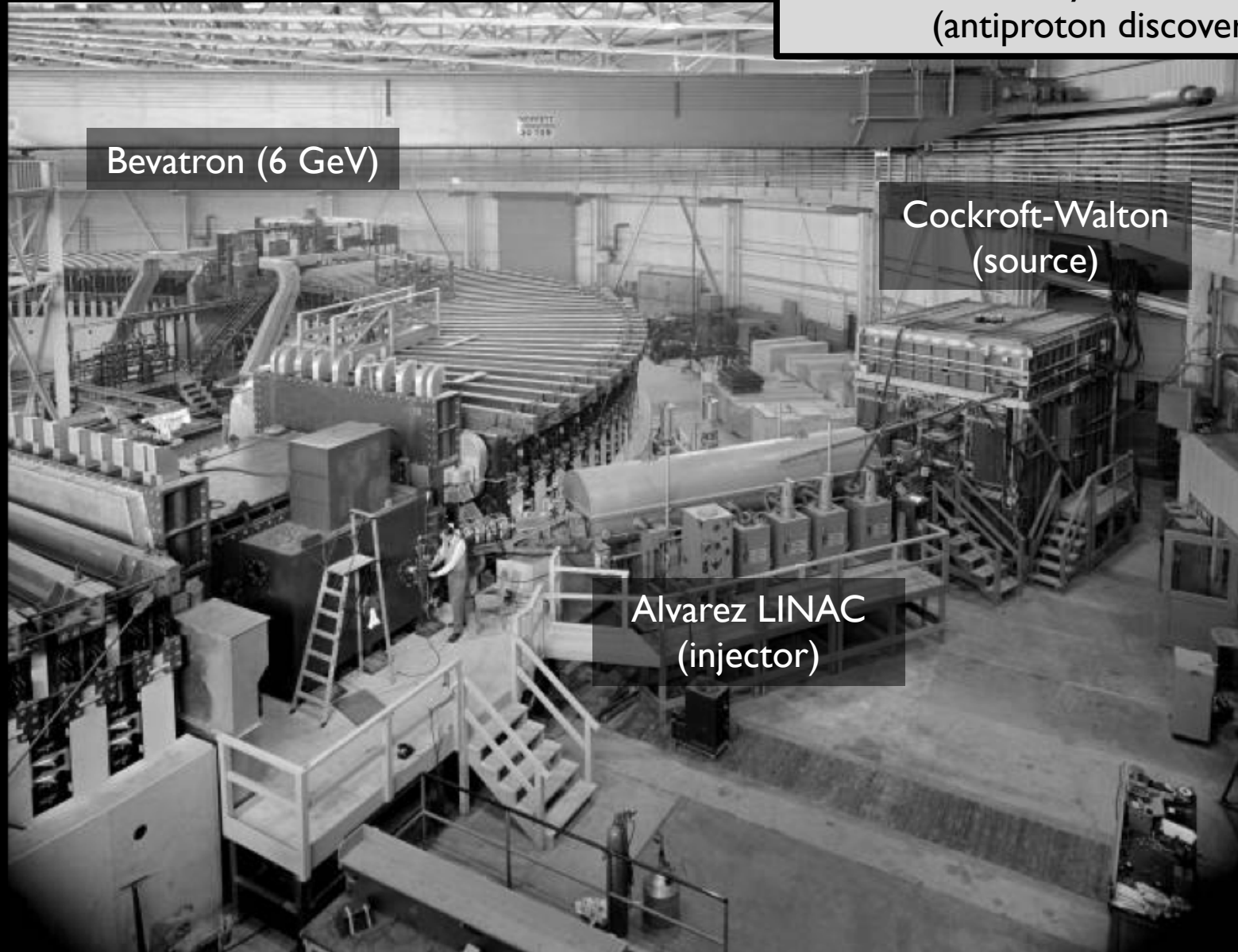


- Trick is to arrange magnetic field increase in vicinity of beam to correspond to increase of particle energy
  - ✓ beam stays on the same orbit (“2-to-1 rule”)
- Betatrons insensitive to relativistic effects
  - ✓ ideal for accelerating electrons



# Accelerators work together!

Lawrence Berkeley National Laboratory  
(antiproton discovery)



Bevatron (6 GeV)

Cockroft-Walton  
(source)

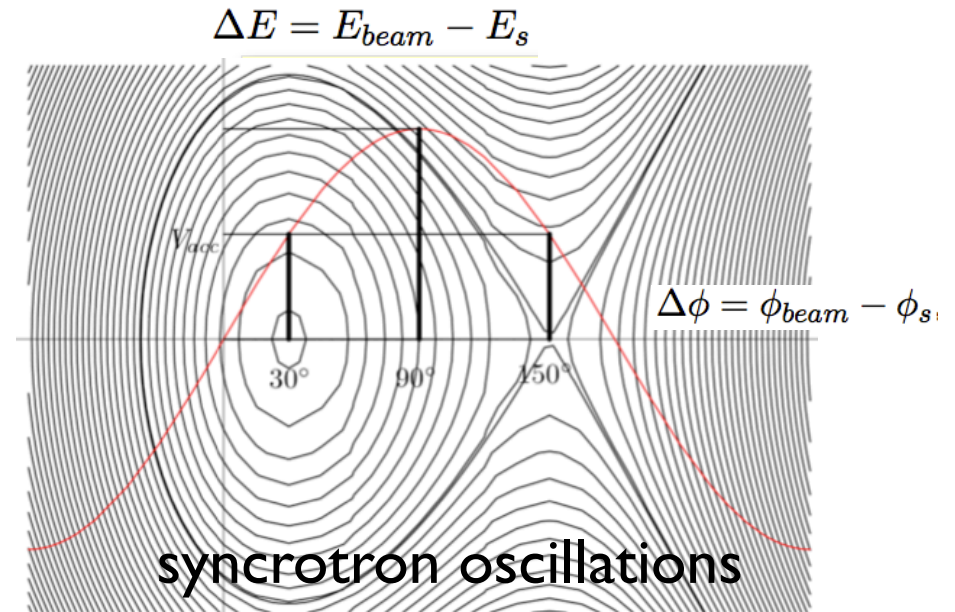
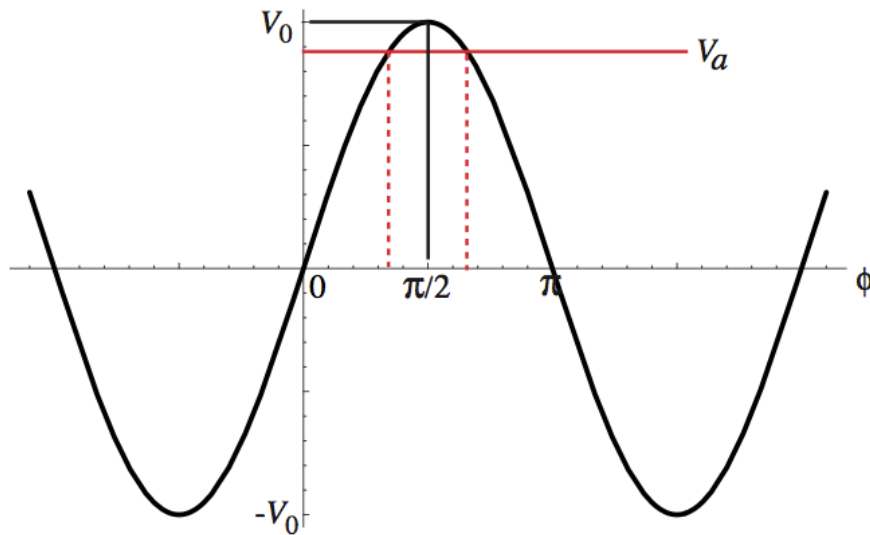
Alvarez LINAC  
(injector)

# The road toward synchrotrons

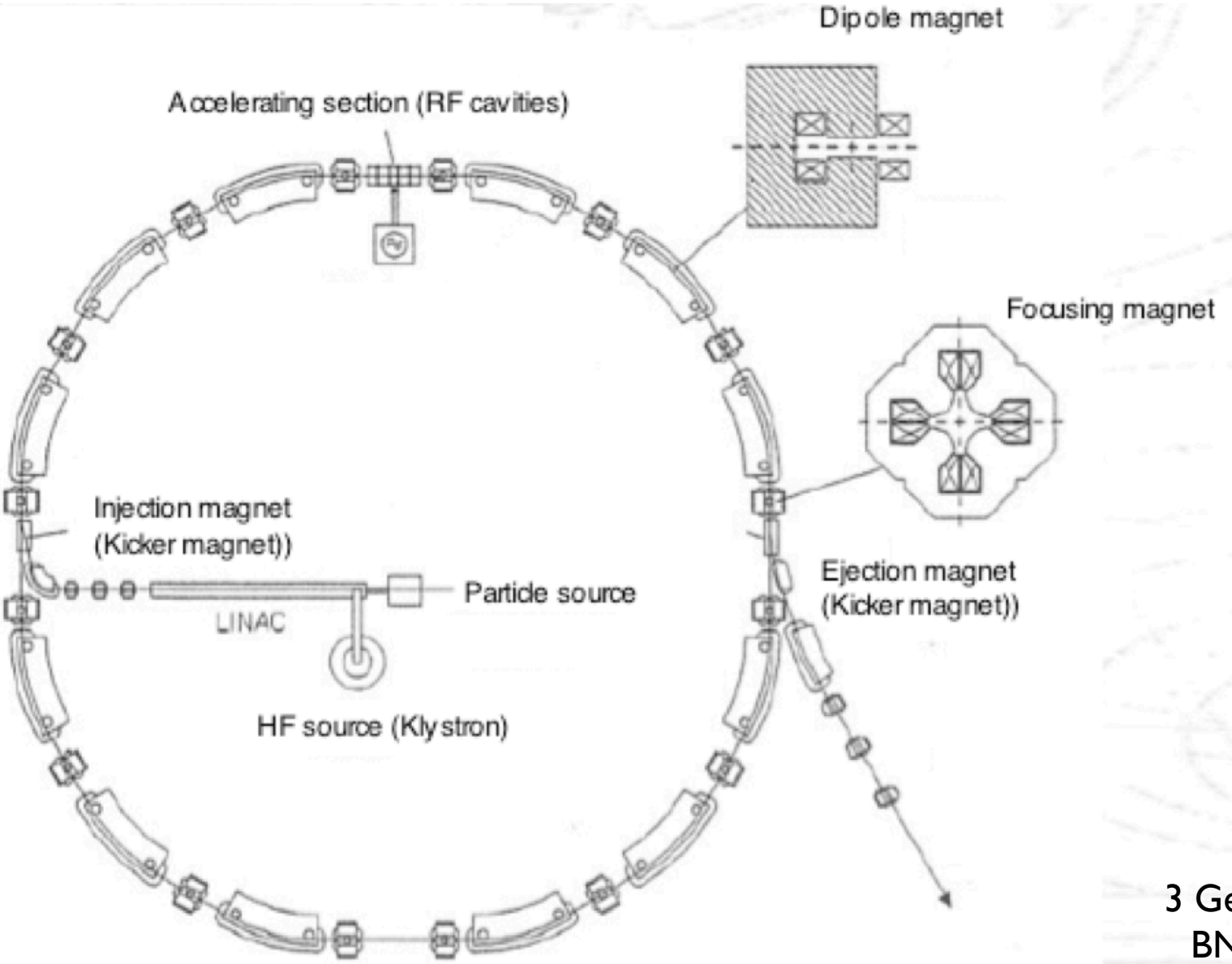
- Problems in RF acceleration in the 1940s...
  - ✓ Linacs
    - poor RF sources; electron tube technology was yet in its infancy
  - ✓ Cyclotrons
    - relativistic effects → asynchronous RF
  - ✓ Betatrons
    - intensity of trapped beam depends critically on the injected beam's positions and angles
    - analysis of particle transverse oscillations led to theory of **betatron oscillations**
- Advancements during WW2
  - ✓ High power microwave tubes for the radars were put to practical use
    - magnetrons and klystrons
  - ✓ Discovery of the **phase stability principle** in RF acceleration
    - Vladimir Veksler (1944) and Edwin M. McMillan (1945)
    - cyclotron → synchrocyclotron → synchrotron

# Phase stability

- Particles of different energies have differences in velocity and in orbit length
  - ✓ particles may be asynchronous wrt RF frequency
- RF field have however a restoring force at a certain phase, around which asynchronous particles be captured in **bunches**
- The phenomenon enables a stable, continuous acceleration of the whole particles in a bunch to high energies: circular accelerators based on this principle are called “synchrotron”
  - ✓ Principle is also applicable to linacs, particularly in low energy range, to bunch continuous beams emitted from a source and to lead bunches to downstream accelerator sections



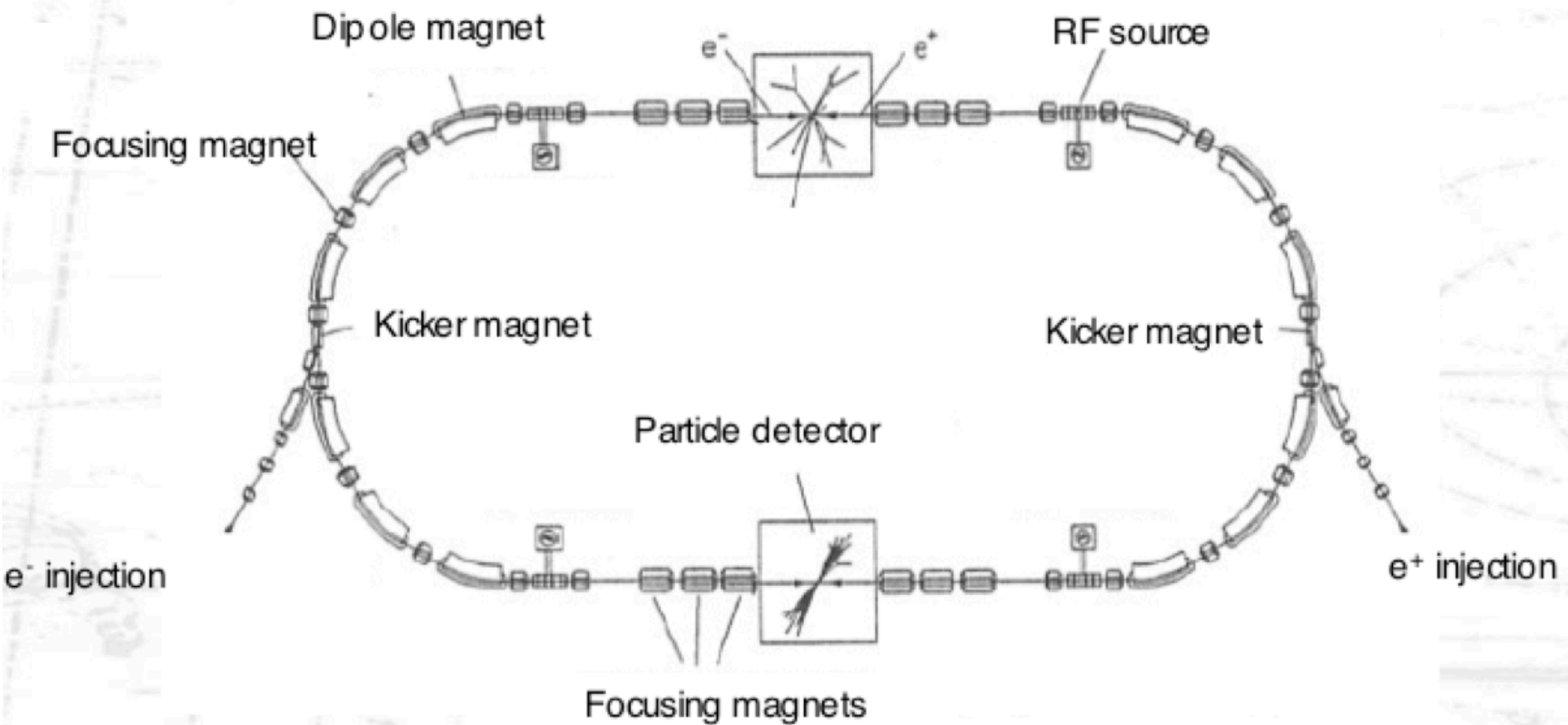
# Synchrotron



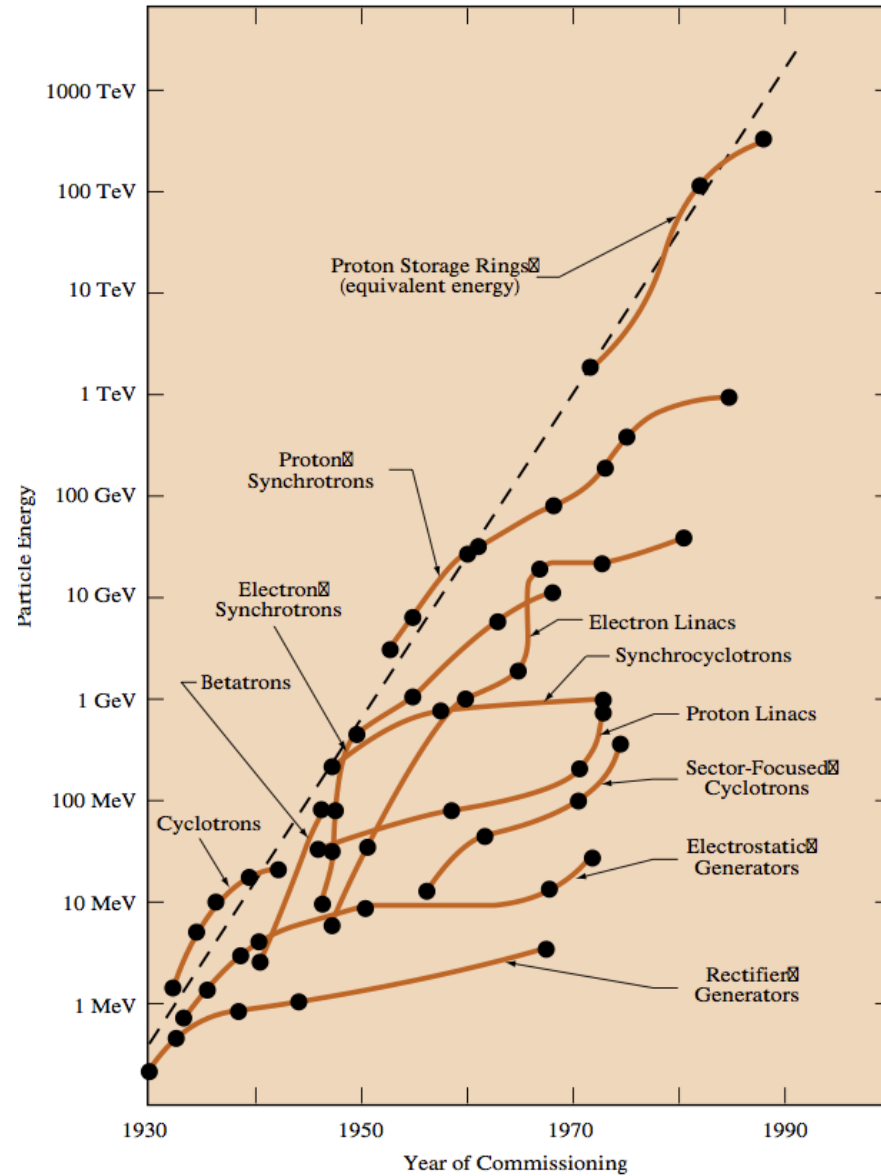
3 GeV protons  
BNL ~ 1950



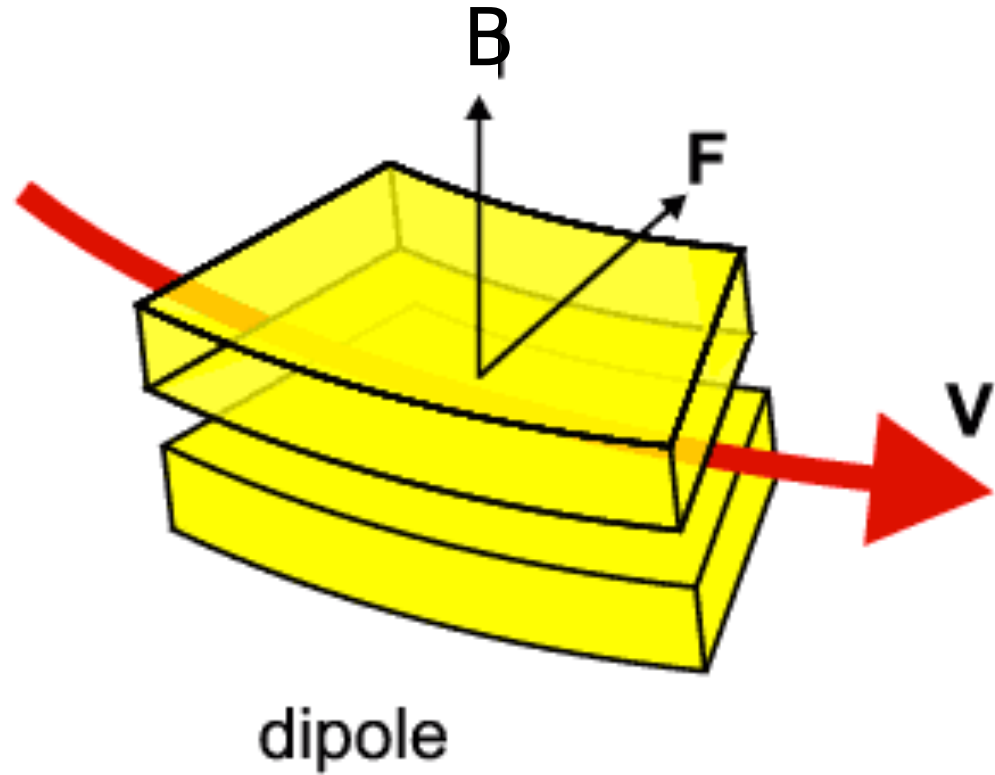
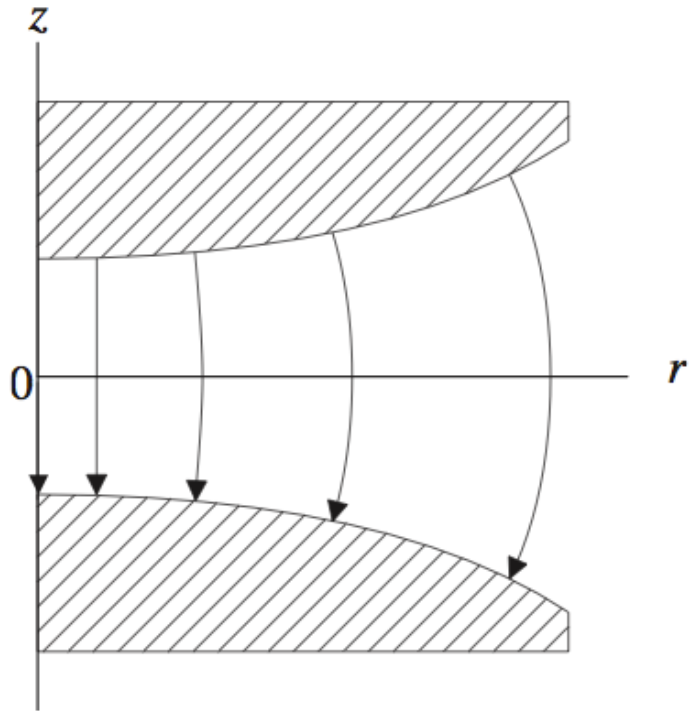
# Storage rings



# Livingstone chart

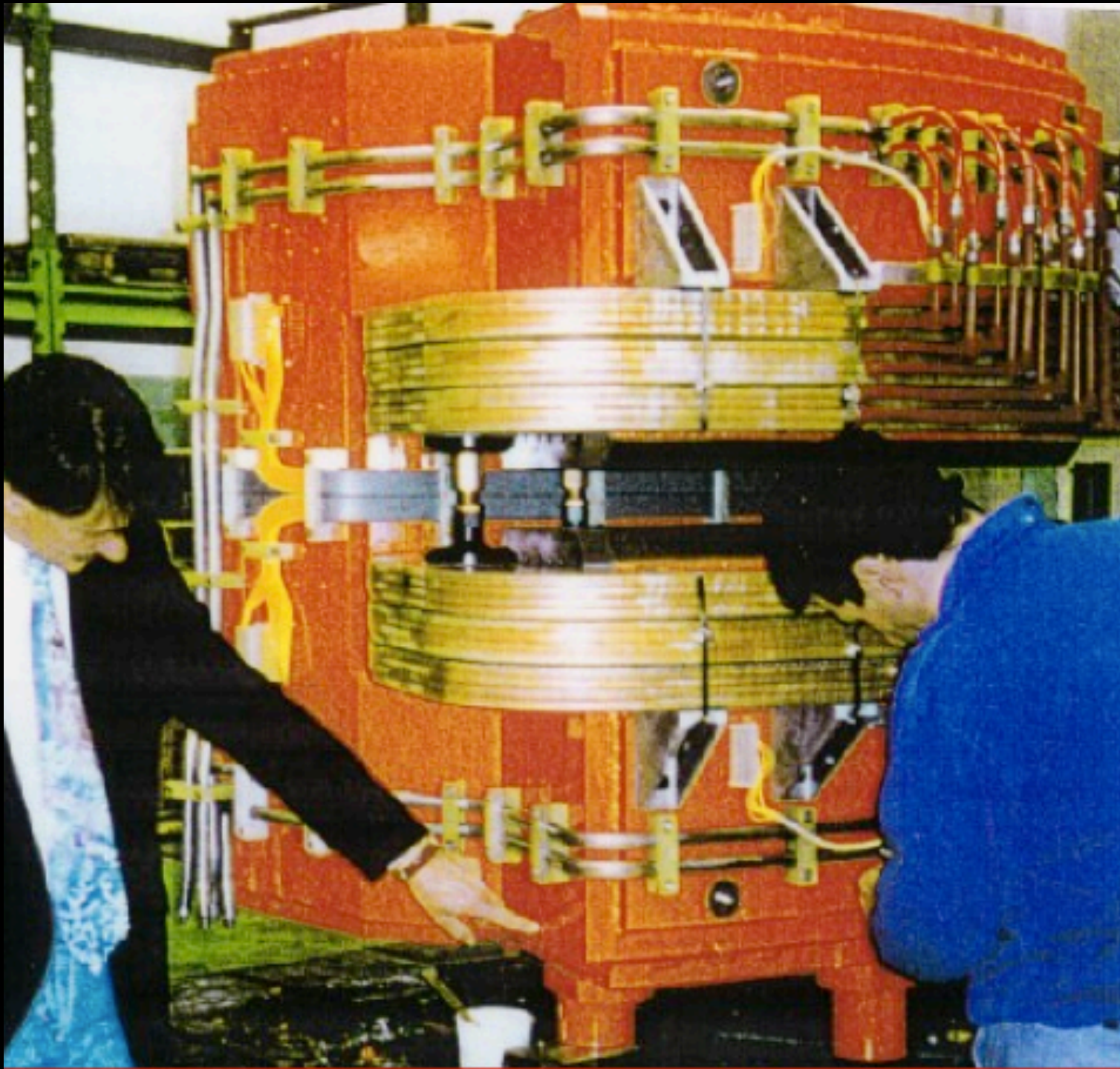


# Bending: dipoles



$$\begin{aligned} B_x &= 0 \\ B_y &= B \\ B_z &= 0 \end{aligned}$$

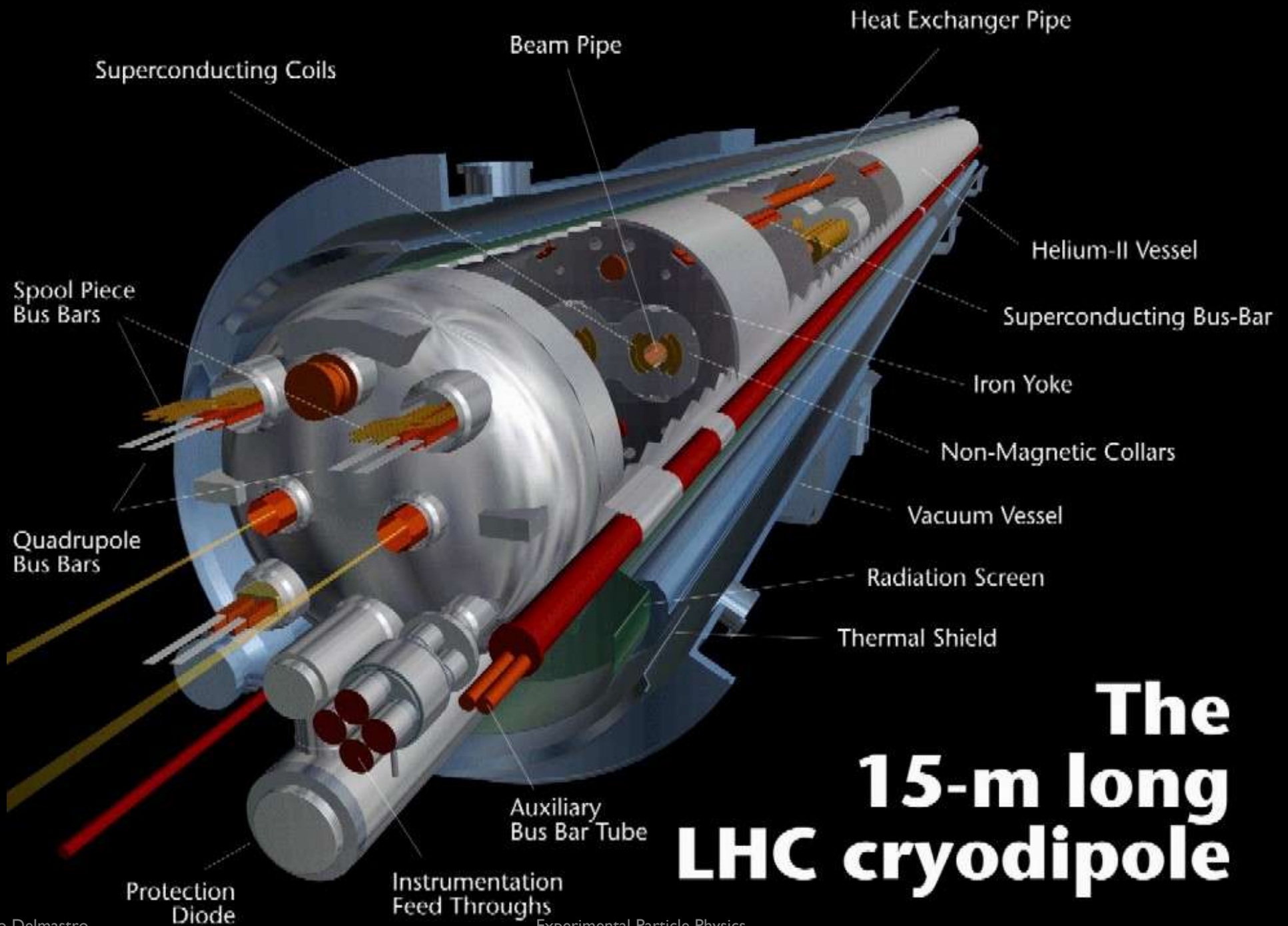
$$\frac{1}{R} [\text{m}^{-1}] = 0.3 \frac{B[\text{T}]}{E[\text{GeV}]}$$





11.56

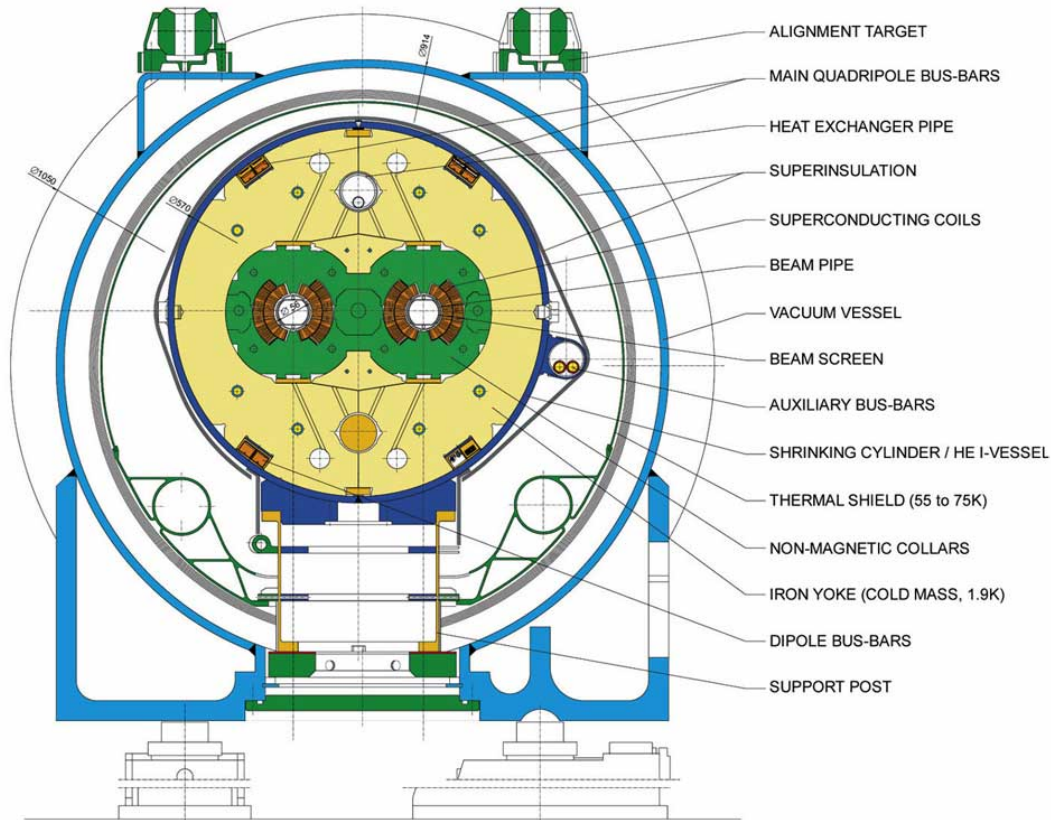
21R8  
BG



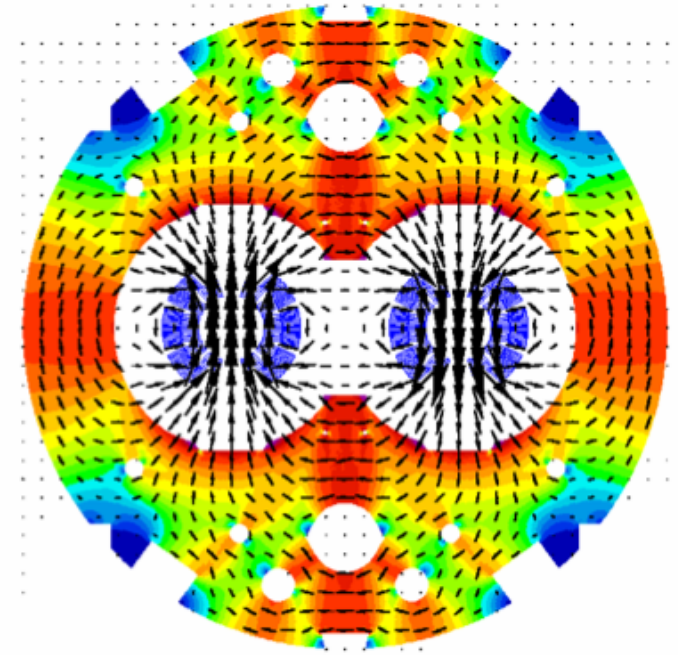
# LHC dipoles

## LHC DIPOLE : STANDARD CROSS-SECTION

CERN AC/DI/MM - HE 107 - 30 04 1999



$|B_{tot}|$  (T)



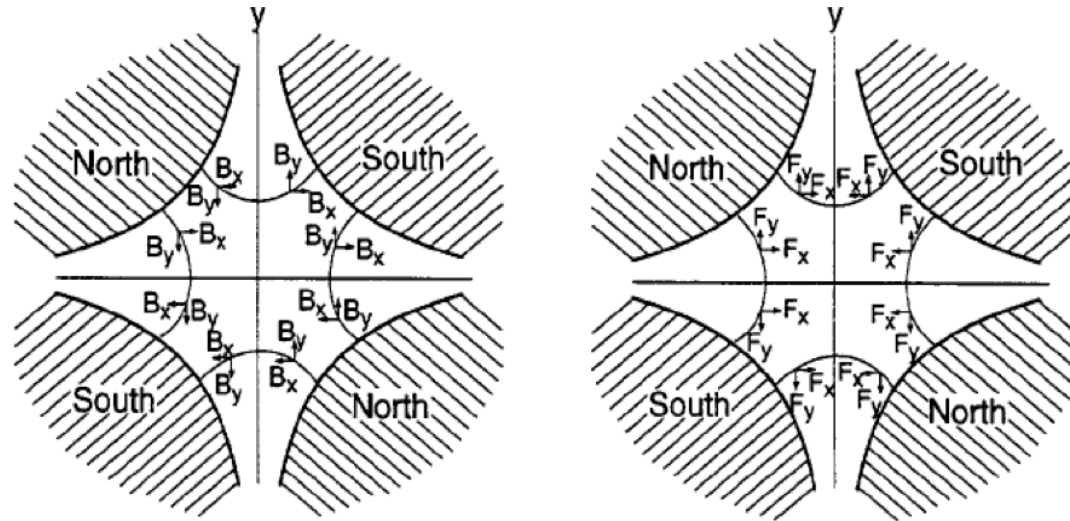
# Focusing (defocusing): quadrupoles

$$B_x = -g \times x$$

$$B_y = -g \times y$$

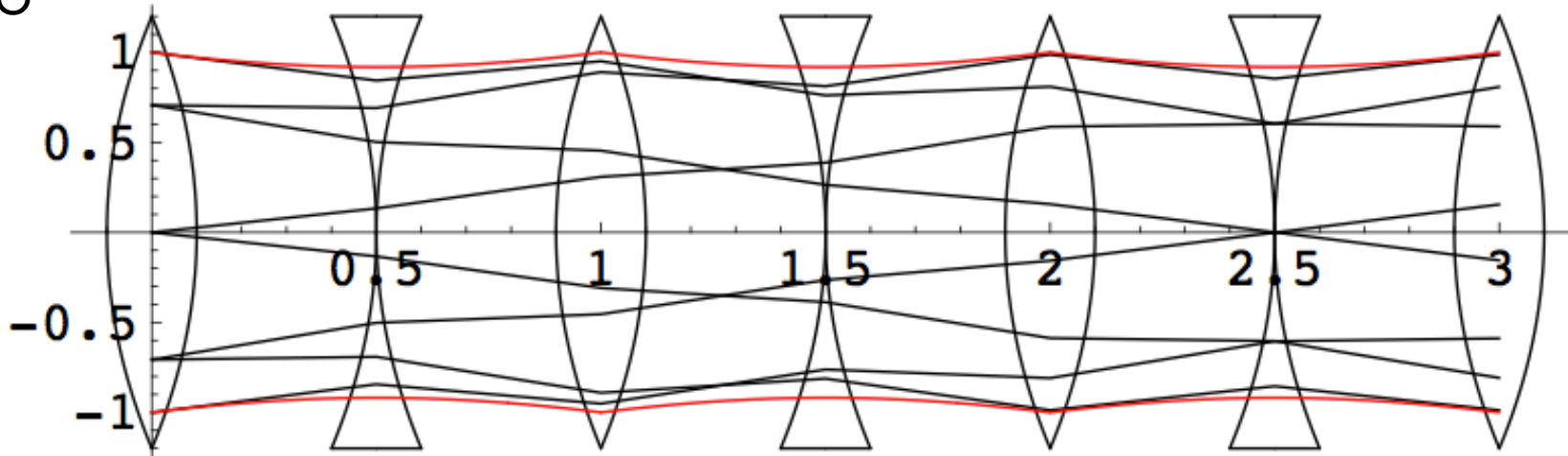
$$B_z = 0$$

$g[\text{T/n}] = \text{field gradient}$

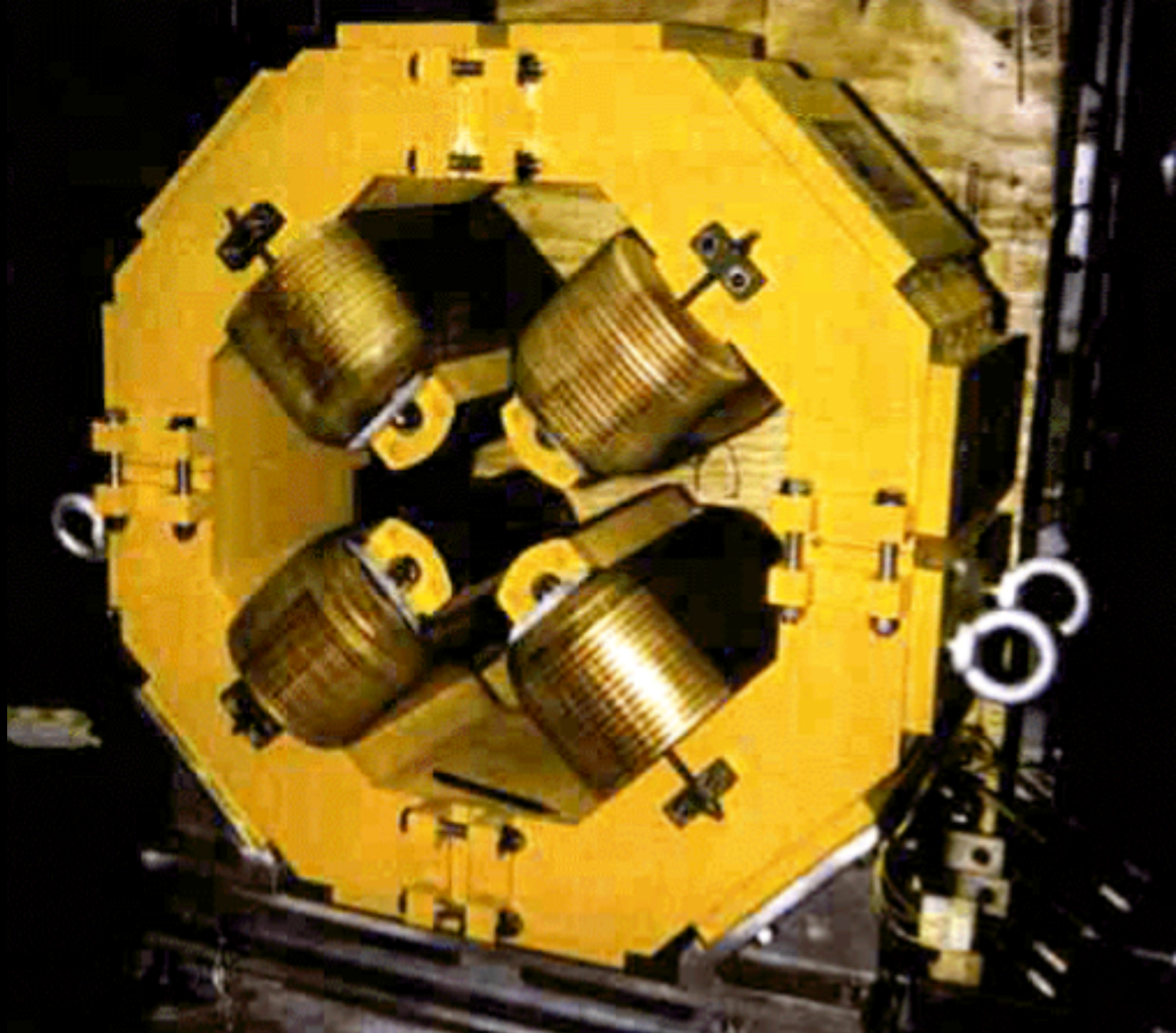


Focusing in one direction, defocusing in the other

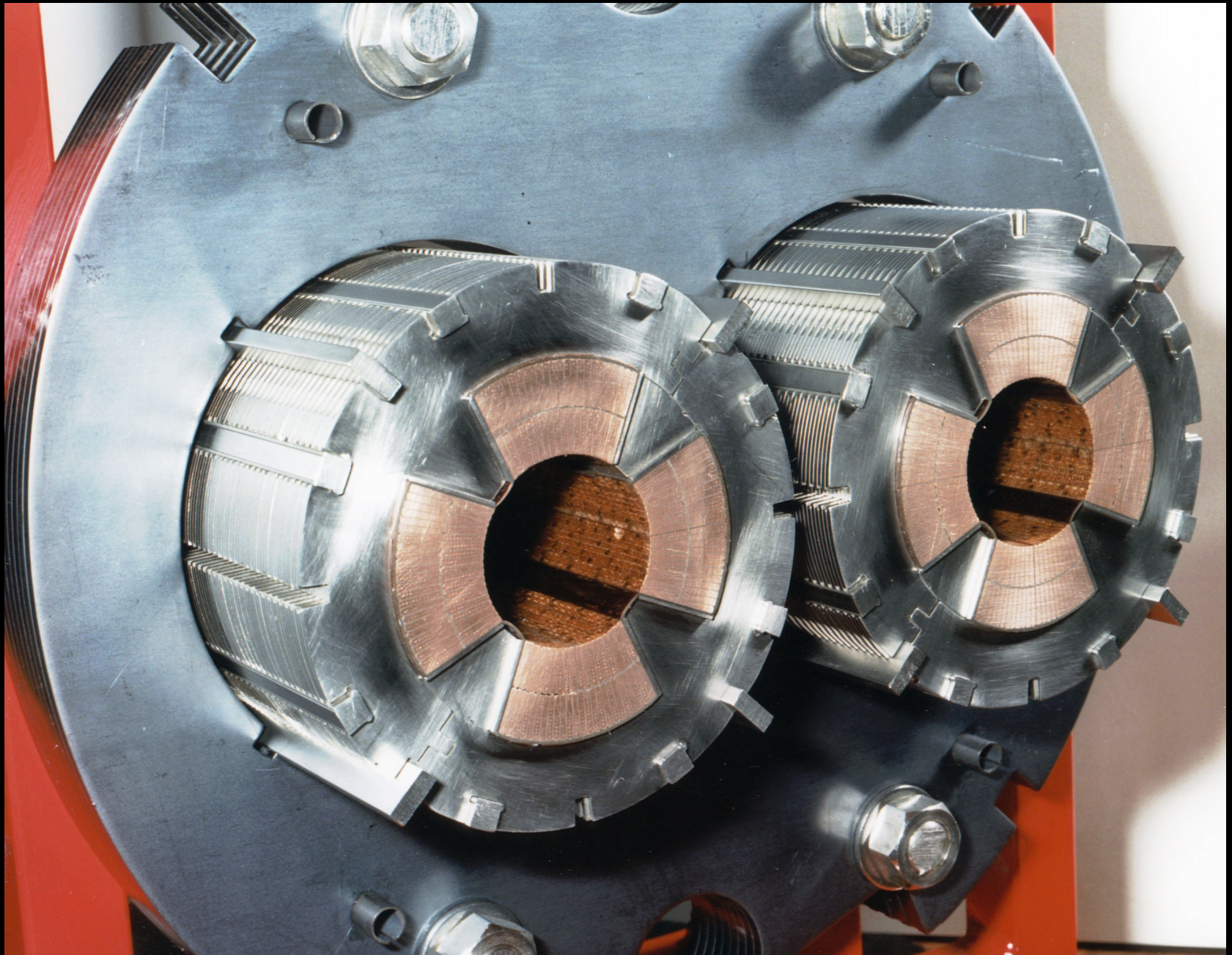
FO-DO  
array



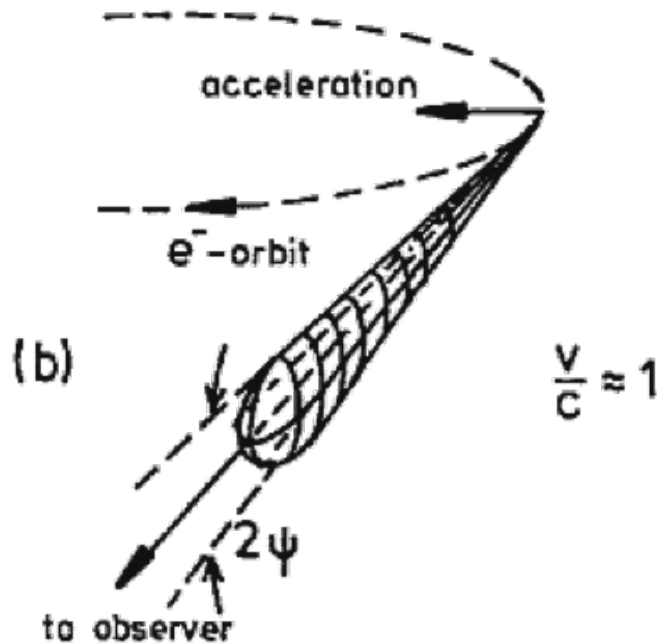
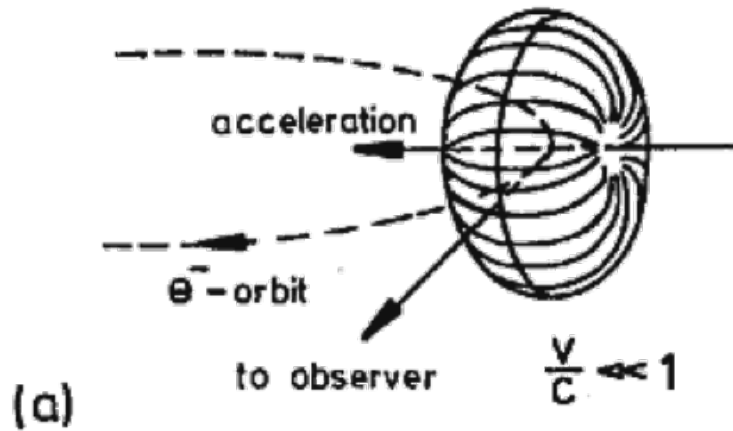








# Synchrotron radiation



energy lost per revolution

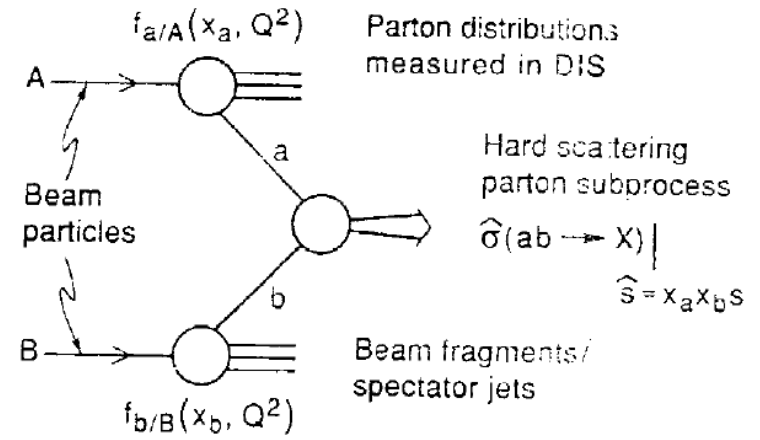
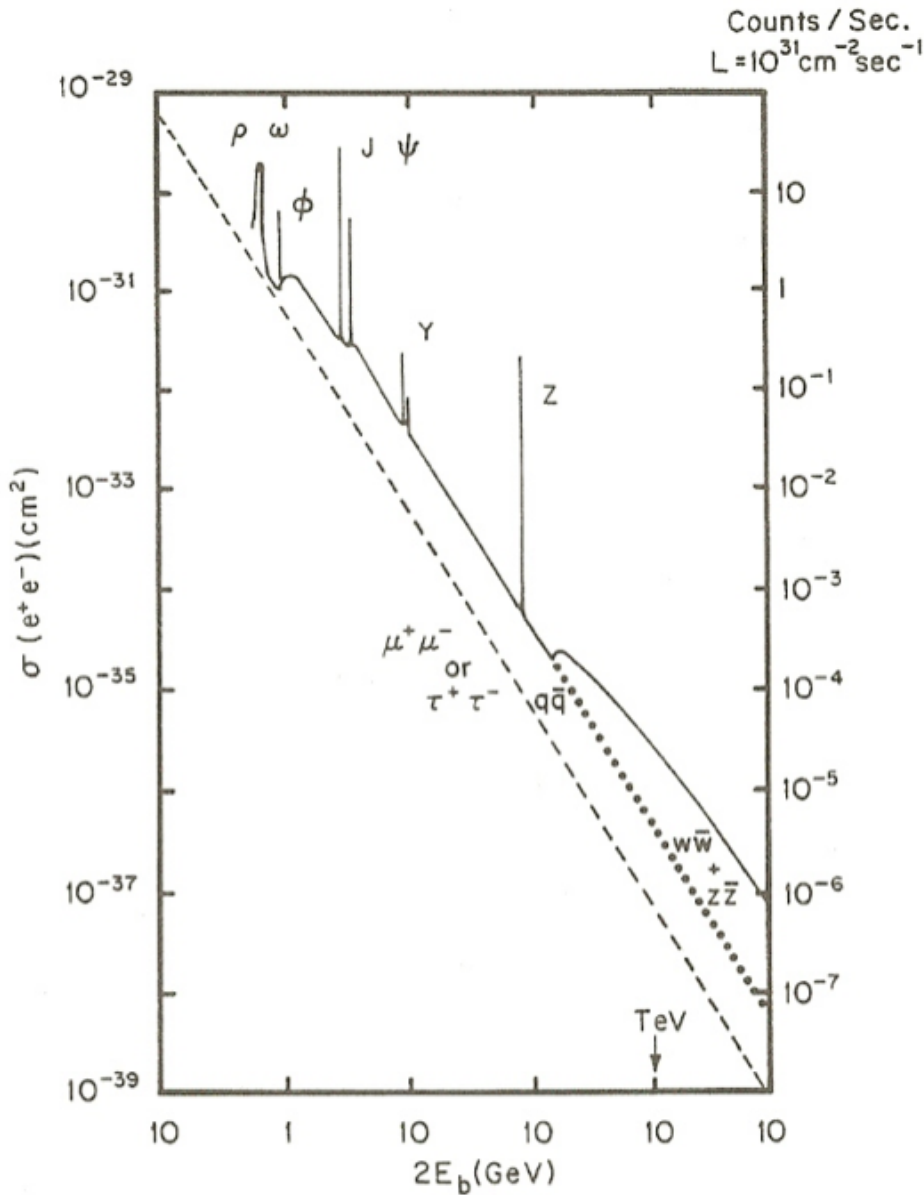
$$\Delta E = \frac{4\pi}{3} \frac{1}{4\pi\epsilon_0} \left( \frac{e^2 \beta^3 \gamma^4}{R} \right)$$

electrons vs. protons

$$\frac{\Delta E_e}{\Delta E_p} \simeq \left( \frac{m_p}{m_e} \right)^4$$

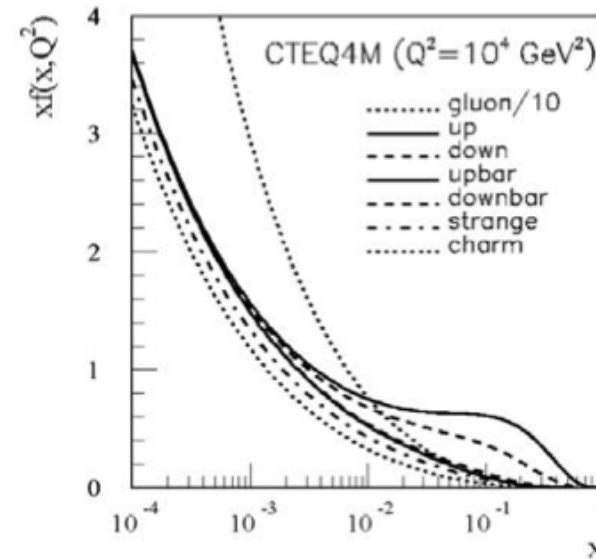
It's easier to accelerate protons to higher energies, but protons are fundamentals...

# $e^+e^-$ vs. hadron collider

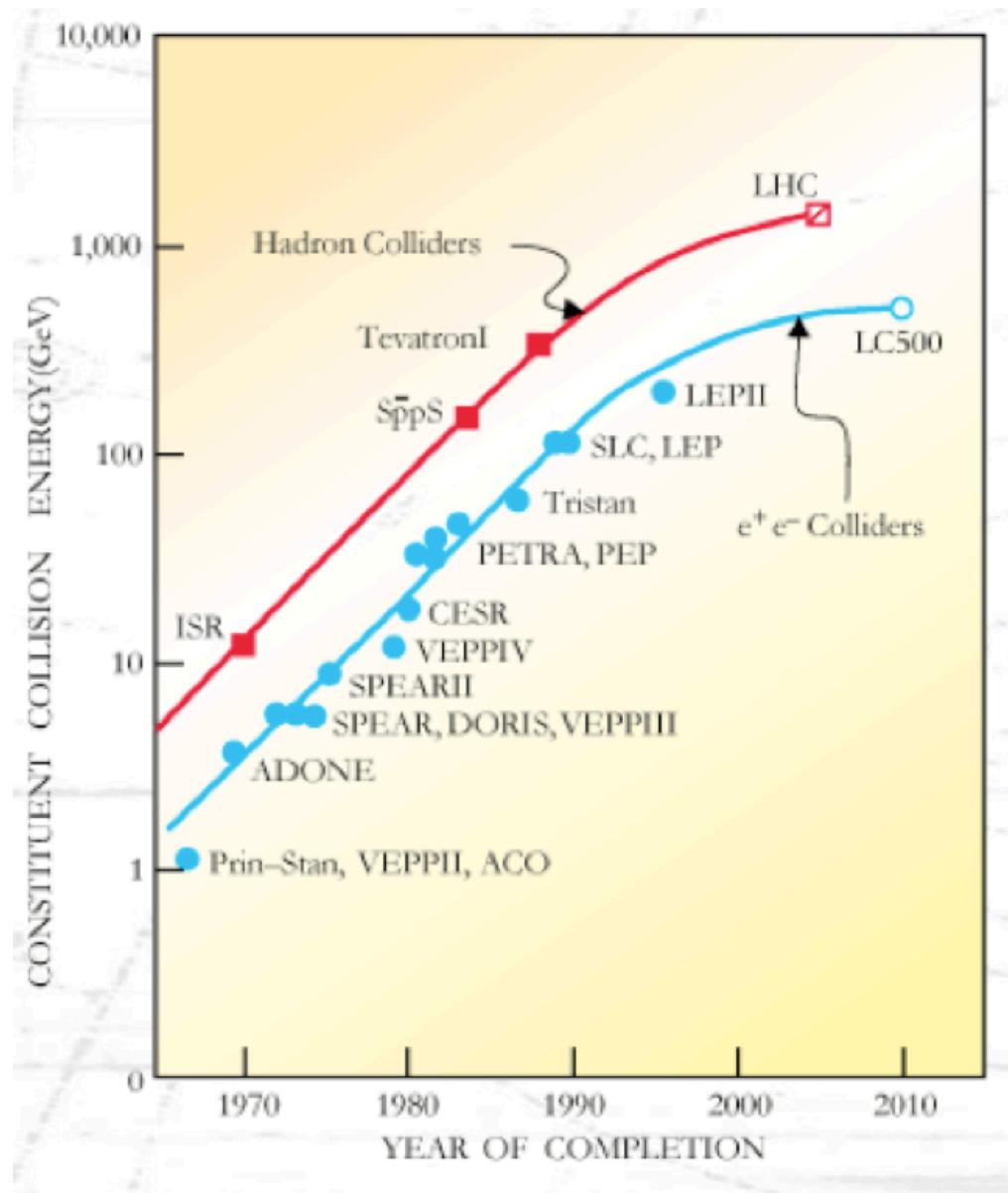


$$\sqrt{\hat{s}} = \sqrt{x_a x_b s}$$

$$\sigma = \sum_{a,b} \int dx_a dx_b f_a(x, Q^2) f_b(x, Q^2) \hat{\sigma}_{ab}(x_a, x_b)$$



# $e^+e^-$ vs. hadron collider



↕ 5-10

# Accelerators around the world (past and present)

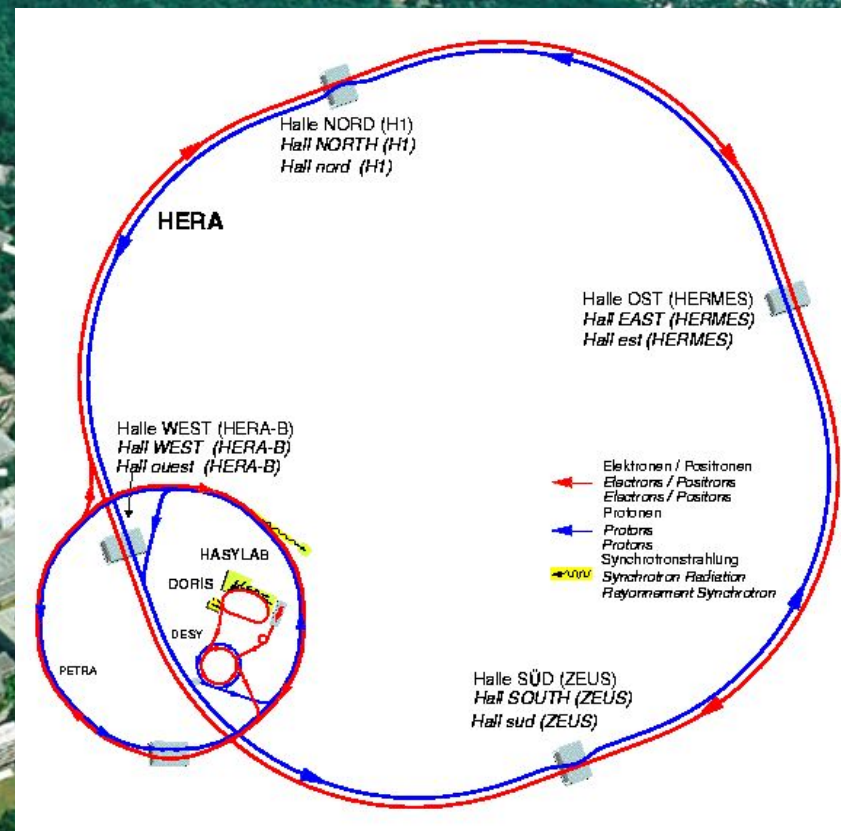
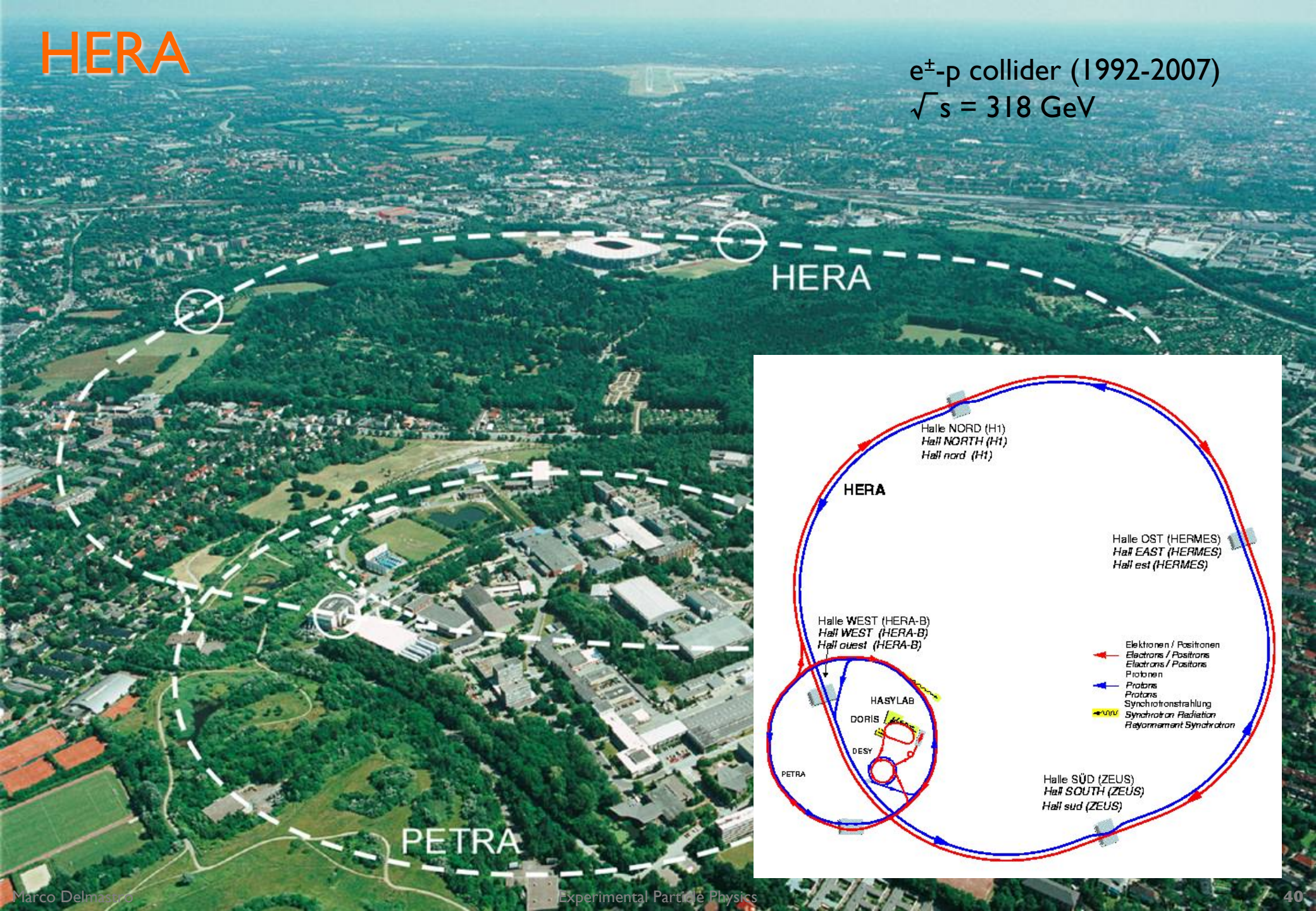
Political Map of the World



802373 (R00350) 4-95

# HERA

$e^{\pm}$ -p collider (1992-2007)  
 $\sqrt{s} = 318 \text{ GeV}$

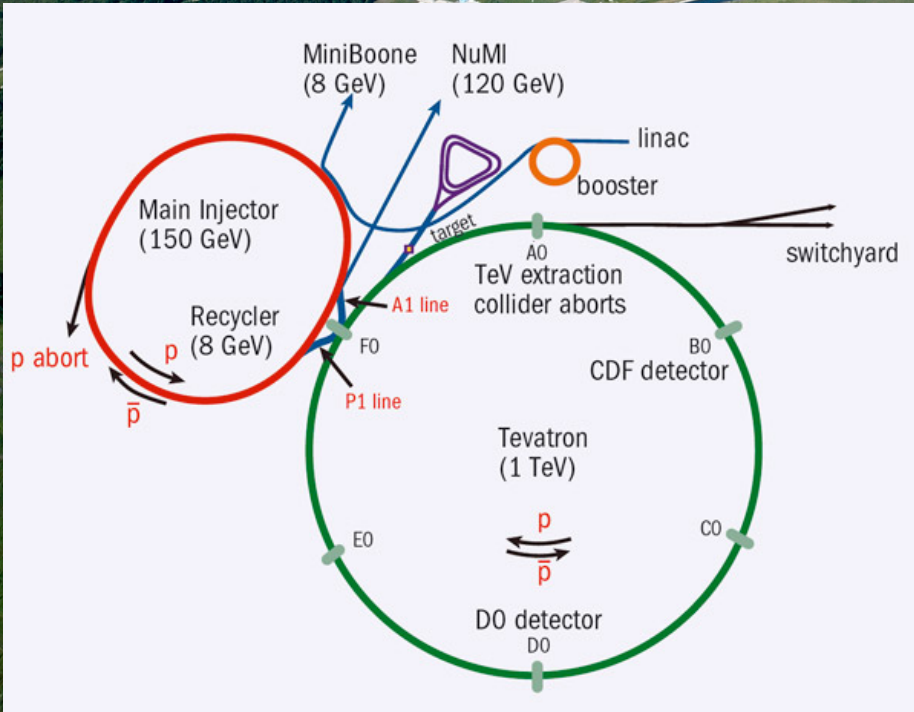




# Tevatron

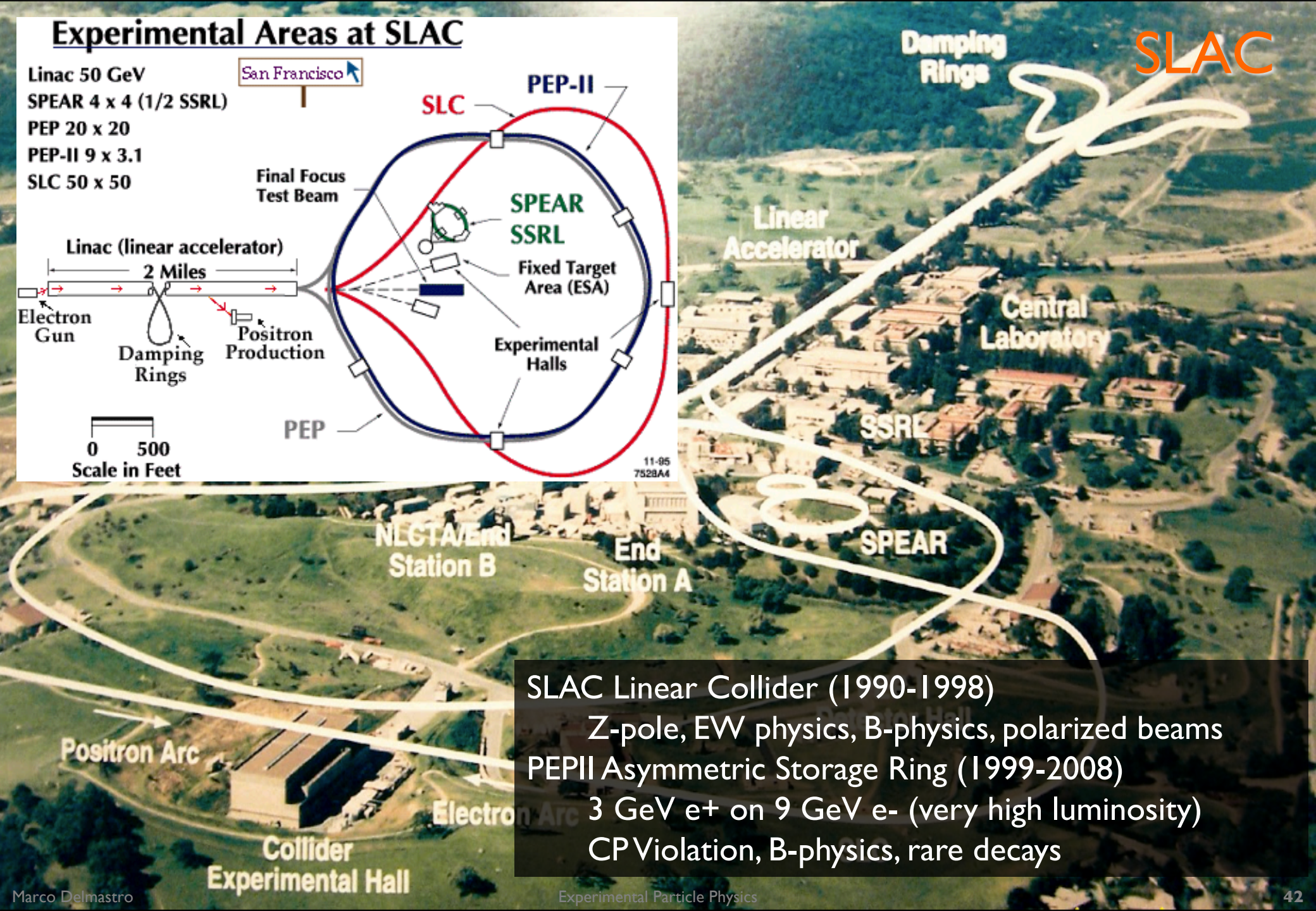
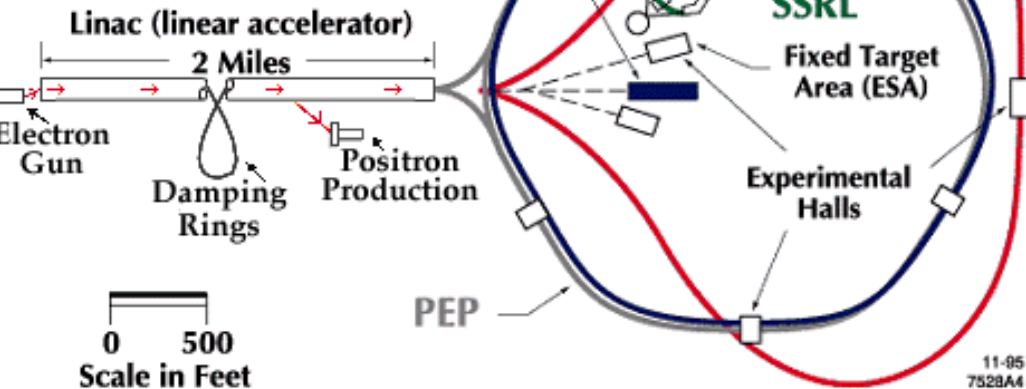
$p\bar{p}$  collider (1983-2011)  
 $\sqrt{s} = 1.96 \text{ TeV}$

CDF-D0  
top quark discovery  
Higgs search  
new physics



# Experimental Areas at SLAC

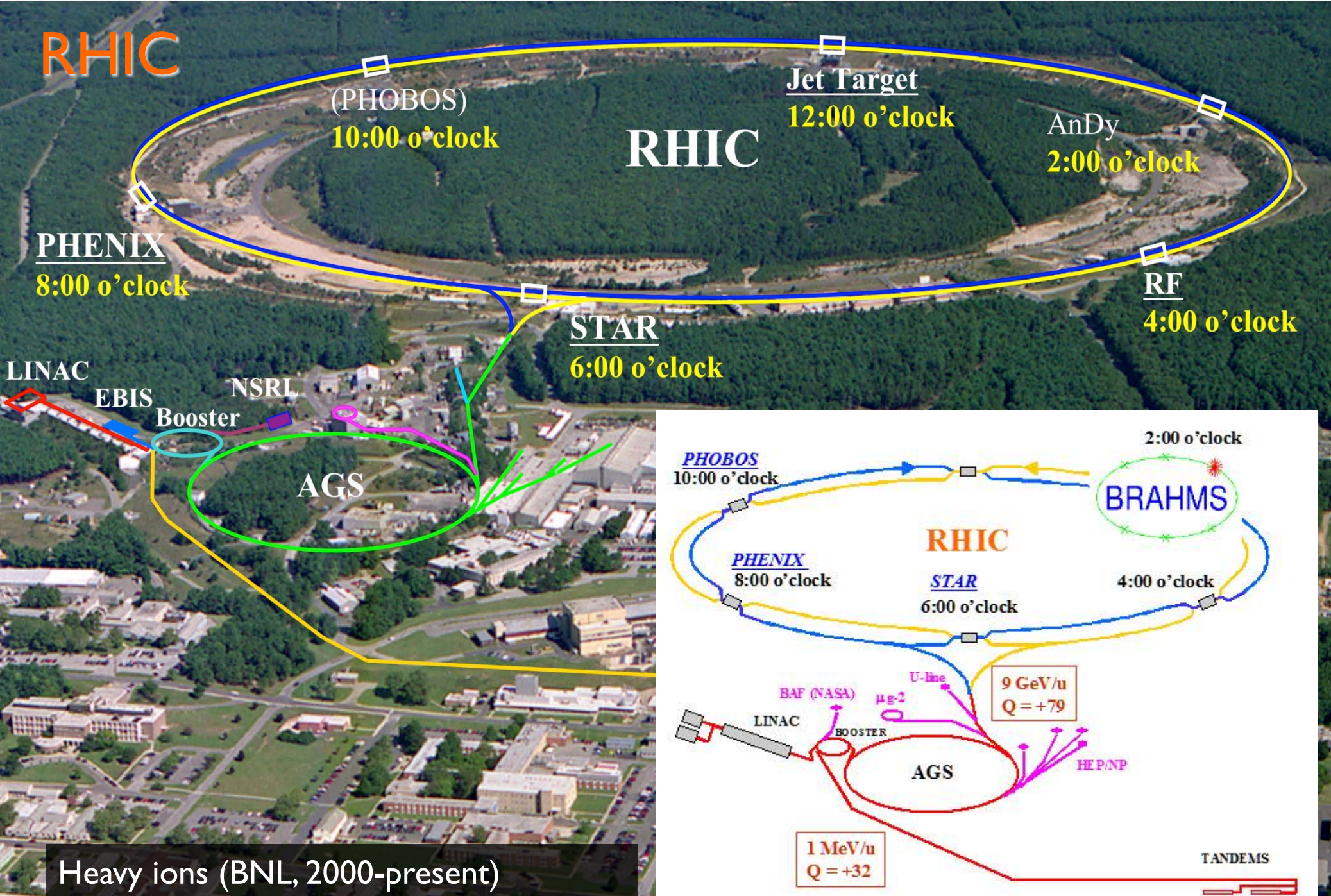
Linac 50 GeV  
 SPEAR 4 x 4 (1/2 SSRL)  
 PEP 20 x 20  
 PEP-II 9 x 3.1  
 SLC 50 x 50



SLAC

SLAC Linear Collider (1990-1998)  
 Z-pole, EW physics, B-physics, polarized beams  
 PEP-II Asymmetric Storage Ring (1999-2008)  
 3 GeV  $e^+$  on 9 GeV  $e^-$  (very high luminosity)  
 CP Violation, B-physics, rare decays

# RHIC



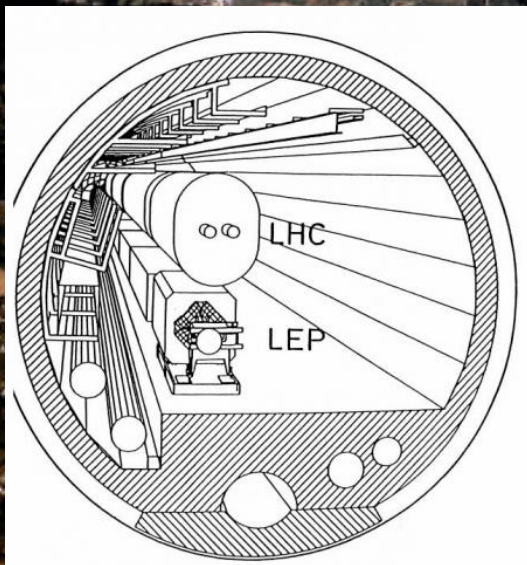
Heavy ions (BNL, 2000-present)

# LEP

$e^+e^-$  collider (1998-2000)

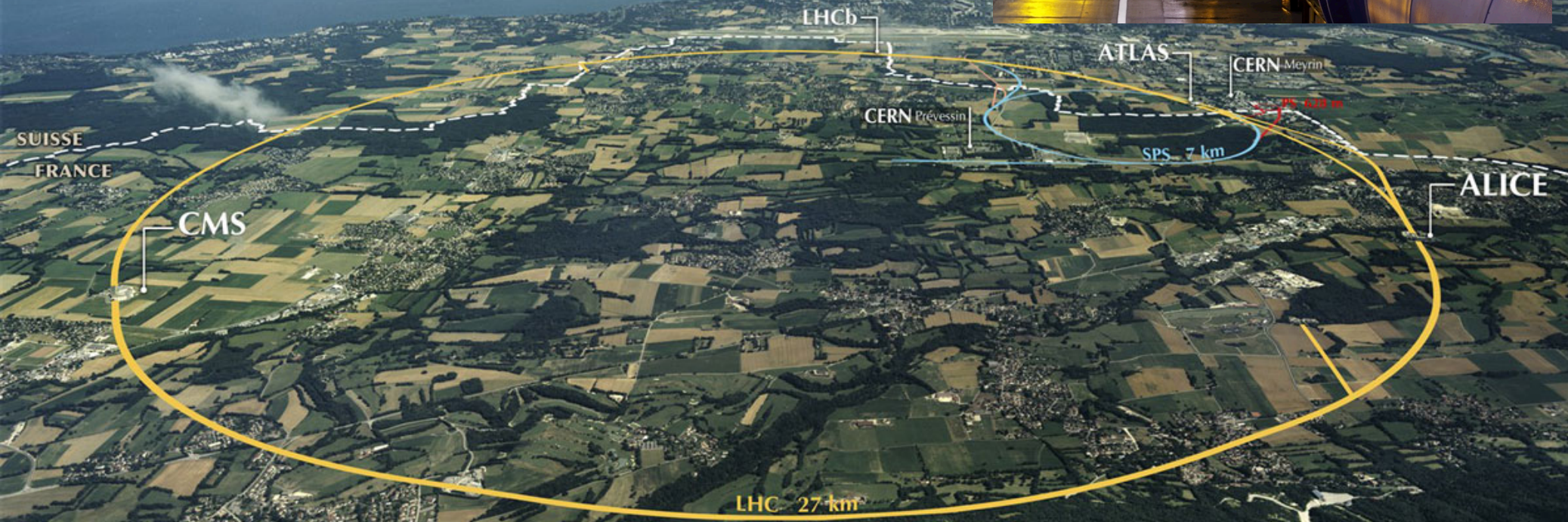
$\sqrt{s} = 91 \text{ GeV}$  (LEP)

$\sqrt{s} \sim 200 \text{ GeV}$  (LEP2)

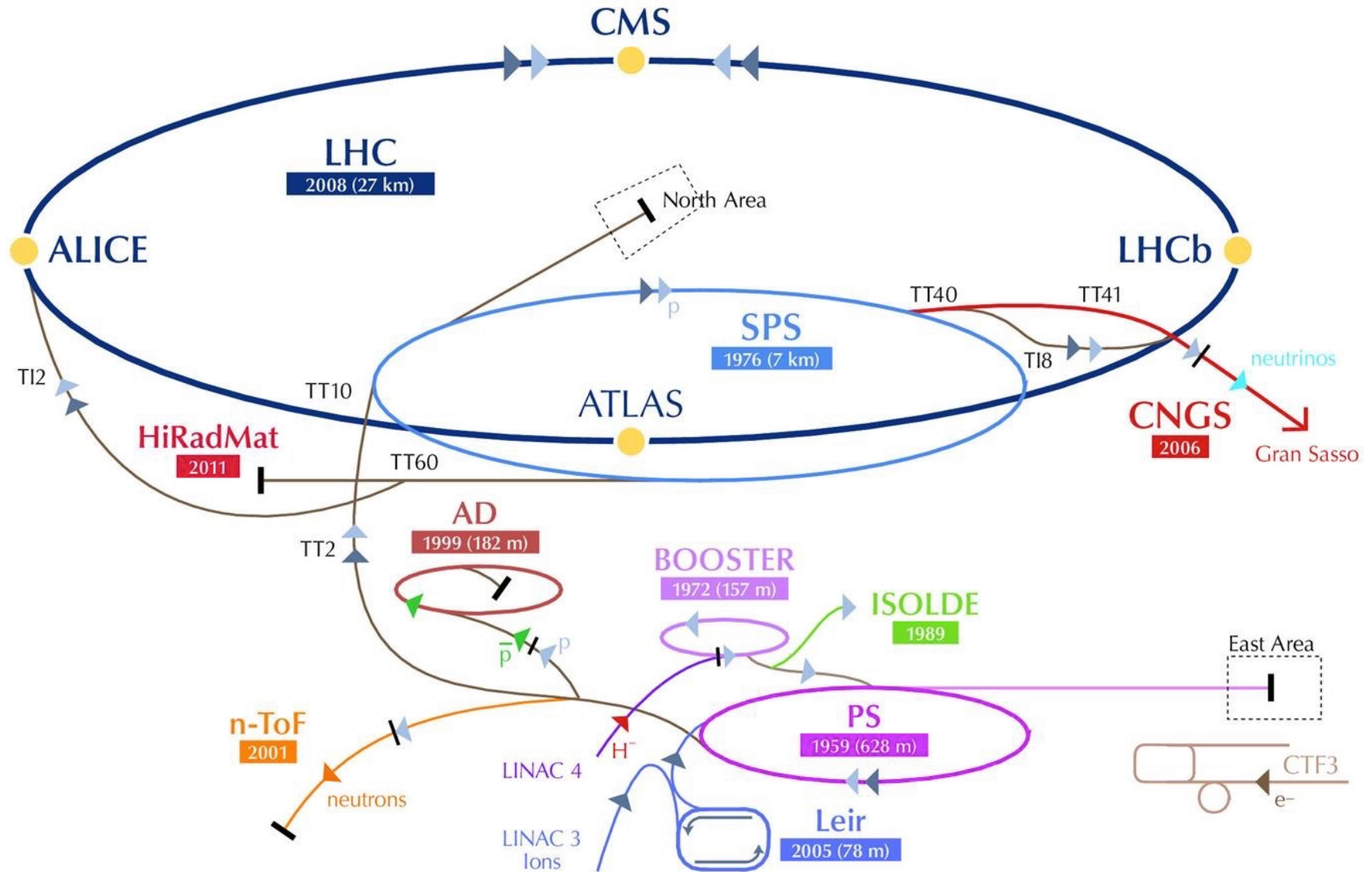


# LHC

pp collider (2008-present)  
 $\sqrt{s} = 7\text{-}13\text{ (}14\text{) GeV}$

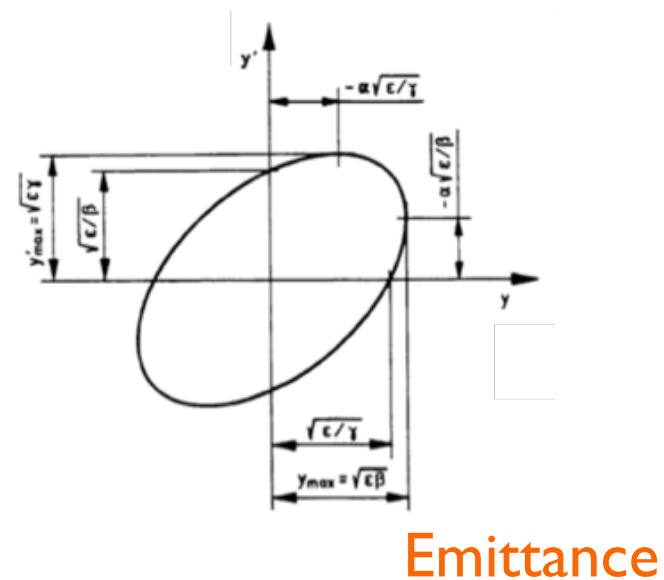
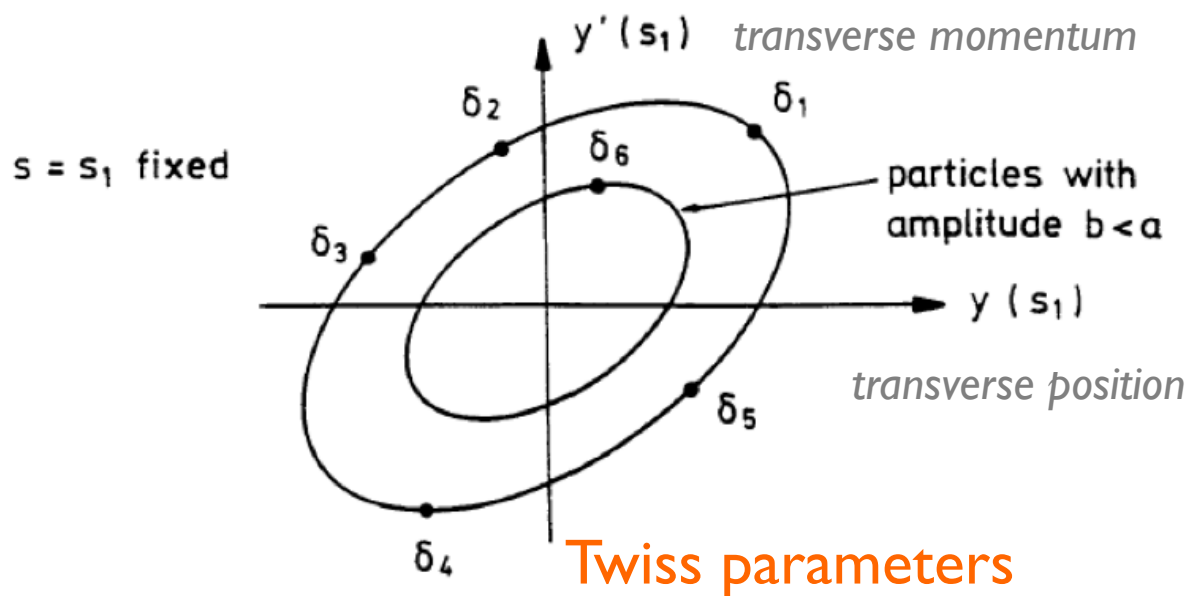


# CERN accelerator complex



# Beam emittance

- Beam size and distribution of particle momenta evolve during motion in collider ring
- Each particle position in *phase space* sits in ellipse of **constant area**
  - ✓ From beam motion equation and Liouville theorem...



$$\gamma y^2 + 2\alpha yy' + \beta y'^2 = \text{const} = \epsilon$$

# Beam dimensions

position along beam directions

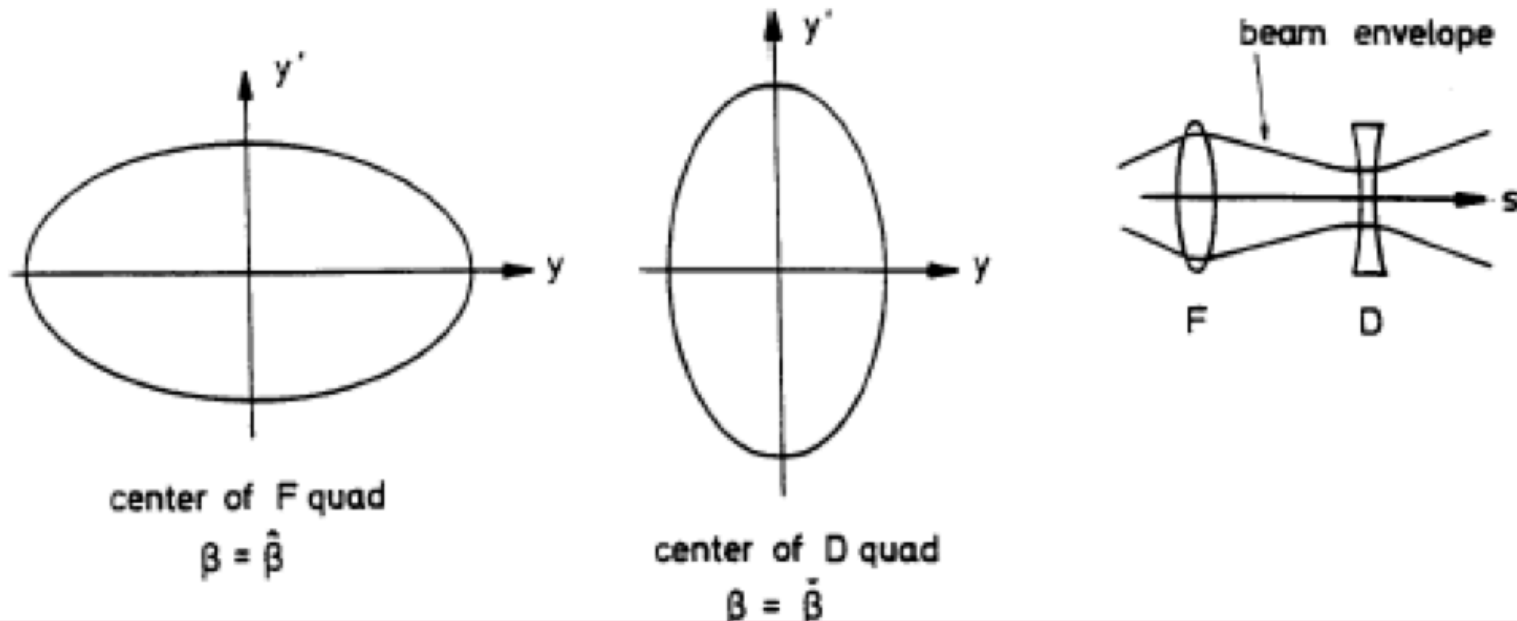
Gaussian width (RMS)  
in transverse direction

$$\sigma(z) = \sqrt{\underbrace{\epsilon}_{\text{emittance}} \underbrace{\beta(z)}_{\text{Twiss parameter (amplitude function)}}}$$

emittance Twiss parameter (amplitude function)

“Beta star” at interaction  
point, often adjusted to be  
minimum

$$\beta^* = \beta(z_0)$$





# Improvements to luminosity?

increase number  
of bunches?

increase number particle  
per bunch?

$$\mathcal{L} = \frac{1}{4\pi} \frac{f k N_1 N_2}{\sqrt{\epsilon_x \beta_x^* \epsilon_y \beta_y^*}}$$

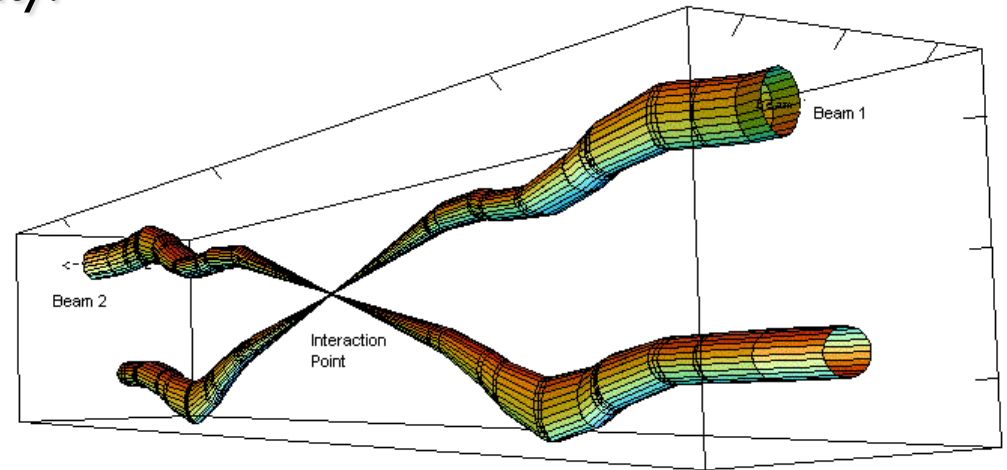
decrease emittance!

decrease beta star!

# Crossing angle

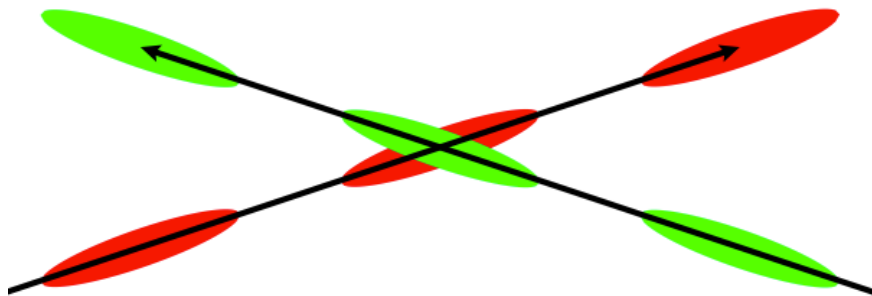
- To avoid parasitic encounters, beams with close bunches often cross at an angle
  - ✓ LHC beams cross at an angle of 300 microradian (bunch spacing 25 ns)
- Crossing angle has an impact on luminosity!

$$\frac{L}{L_0} = \frac{1}{\sqrt{1 + \left(\frac{\sigma_z}{\sigma_x} \tan \frac{\theta_c}{2}\right)^2}}$$

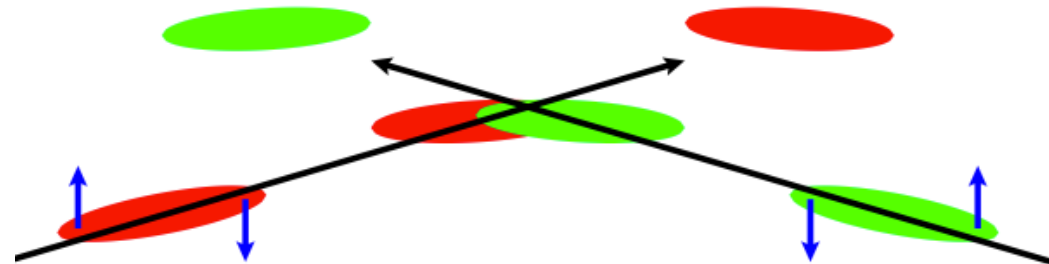


Relative beam sizes around IP1 (Atlas) in collision

with crossing angle

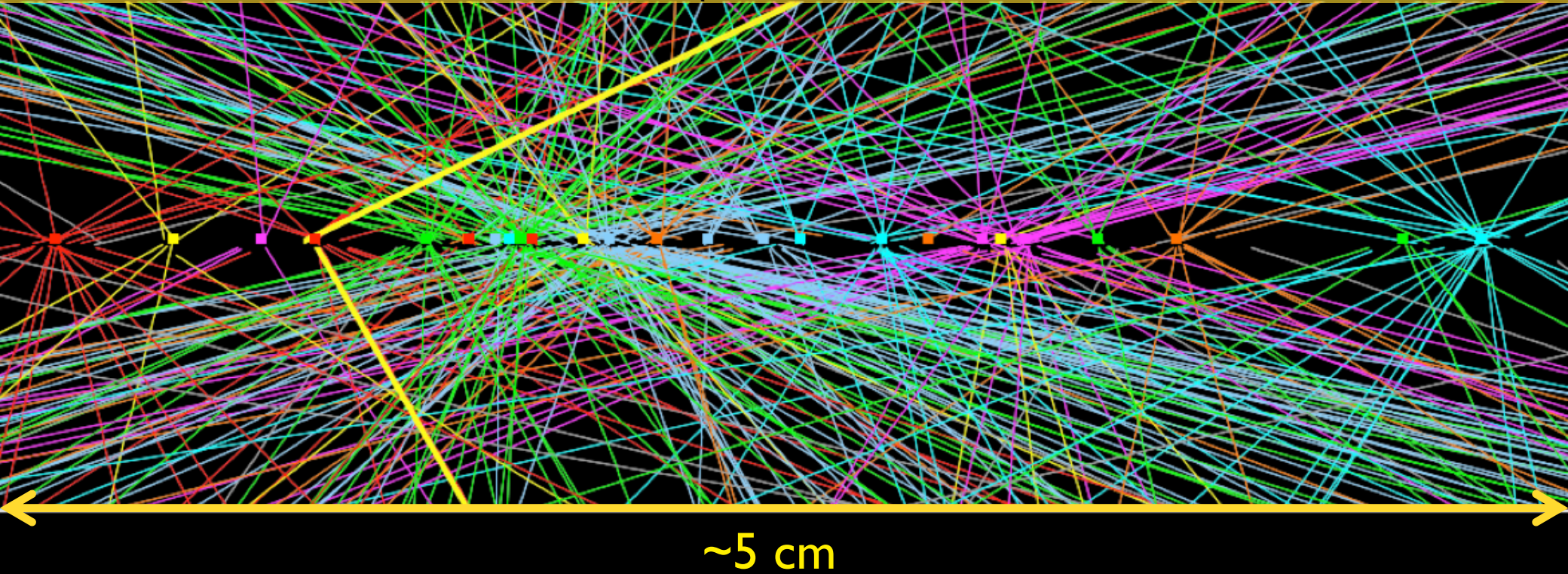


“crab” crossing



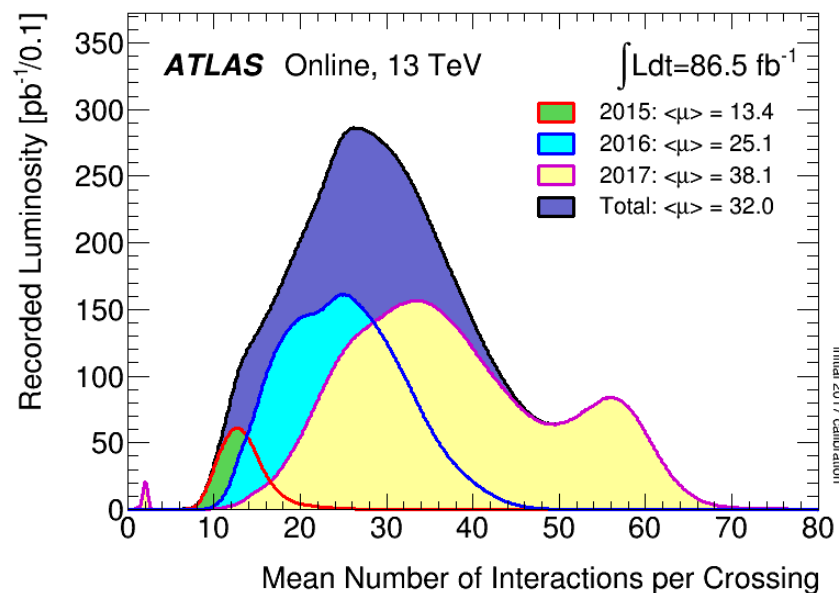
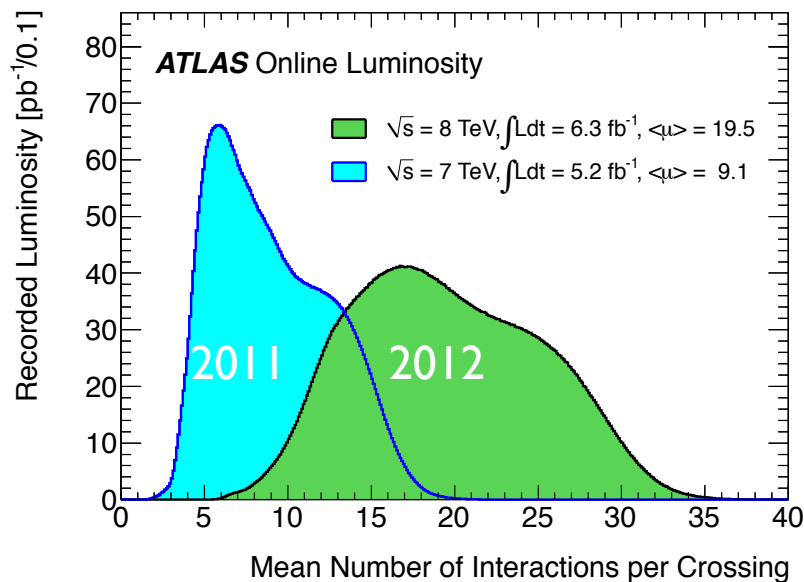
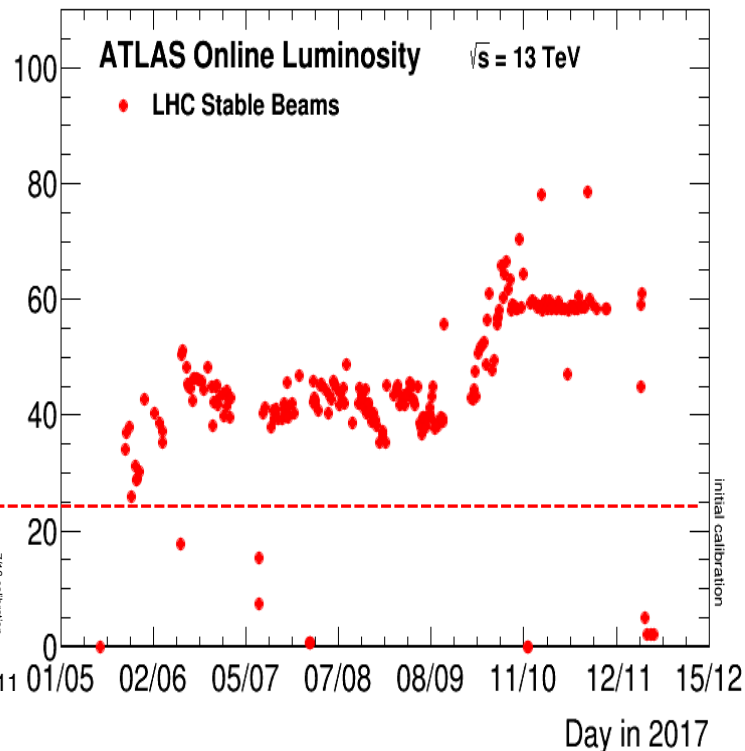
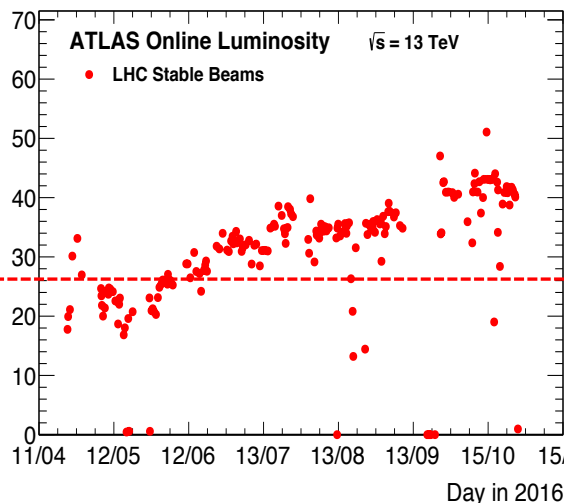
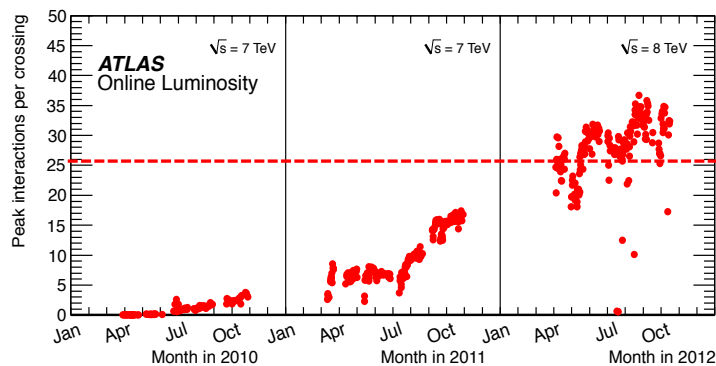
# $Z \rightarrow \mu\mu$ event with 25 reconstructed vertices

April 15<sup>th</sup>, 2012

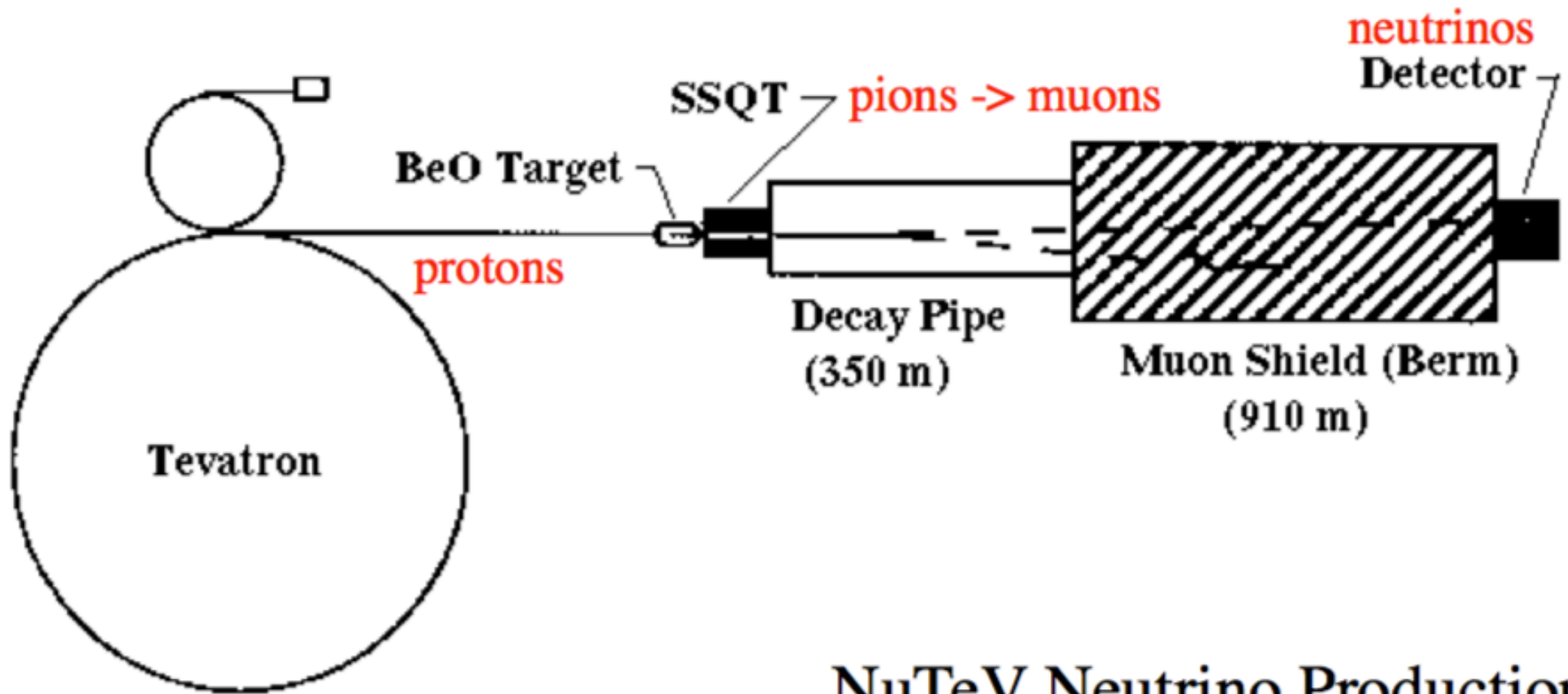


# Pileup!

ATLAS design value  
 $L = 10^{34} \text{ cm}^{-1}\text{s}^{-1} @ 25 \text{ ns}$

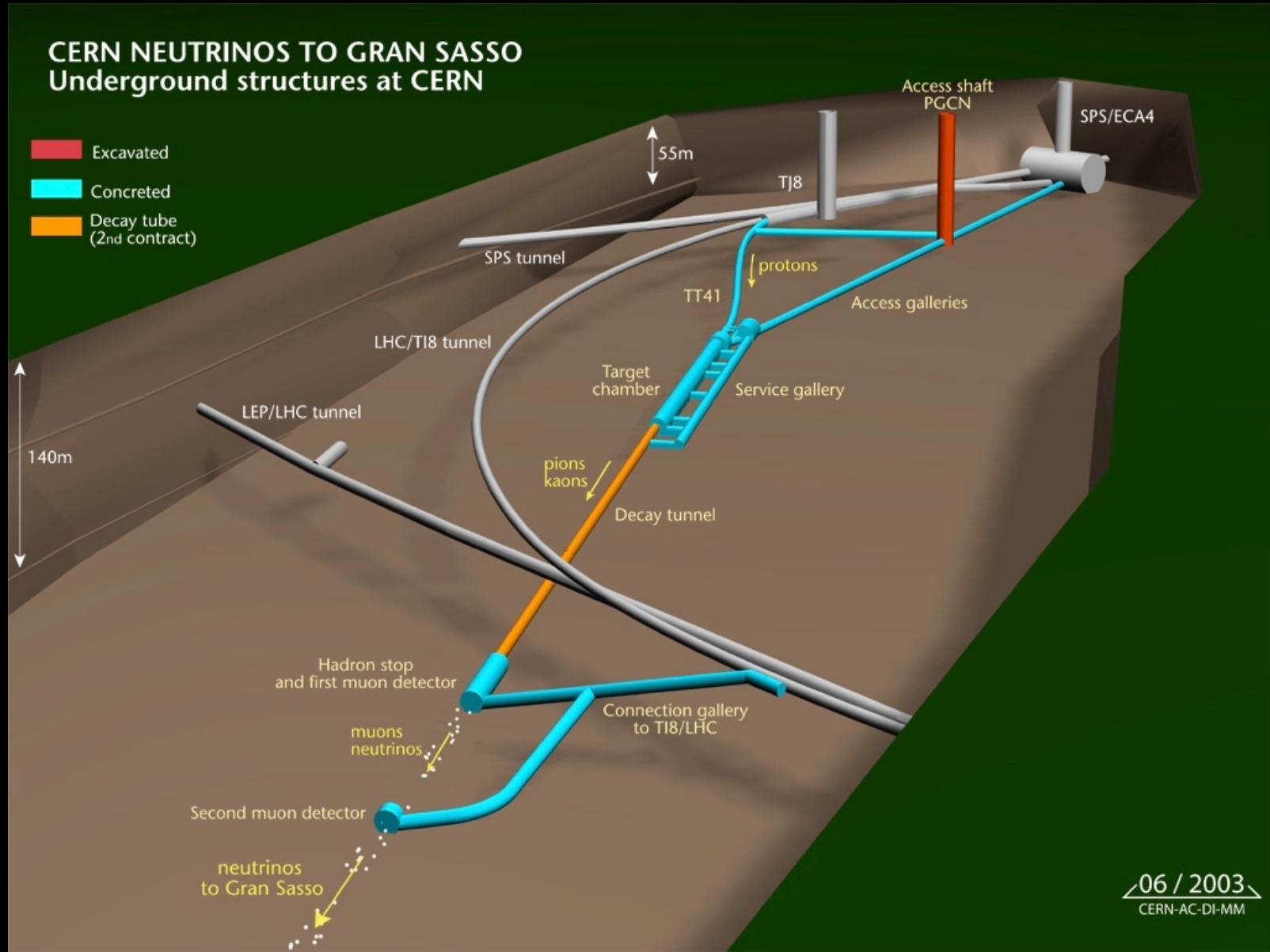


# Production of secondary beams

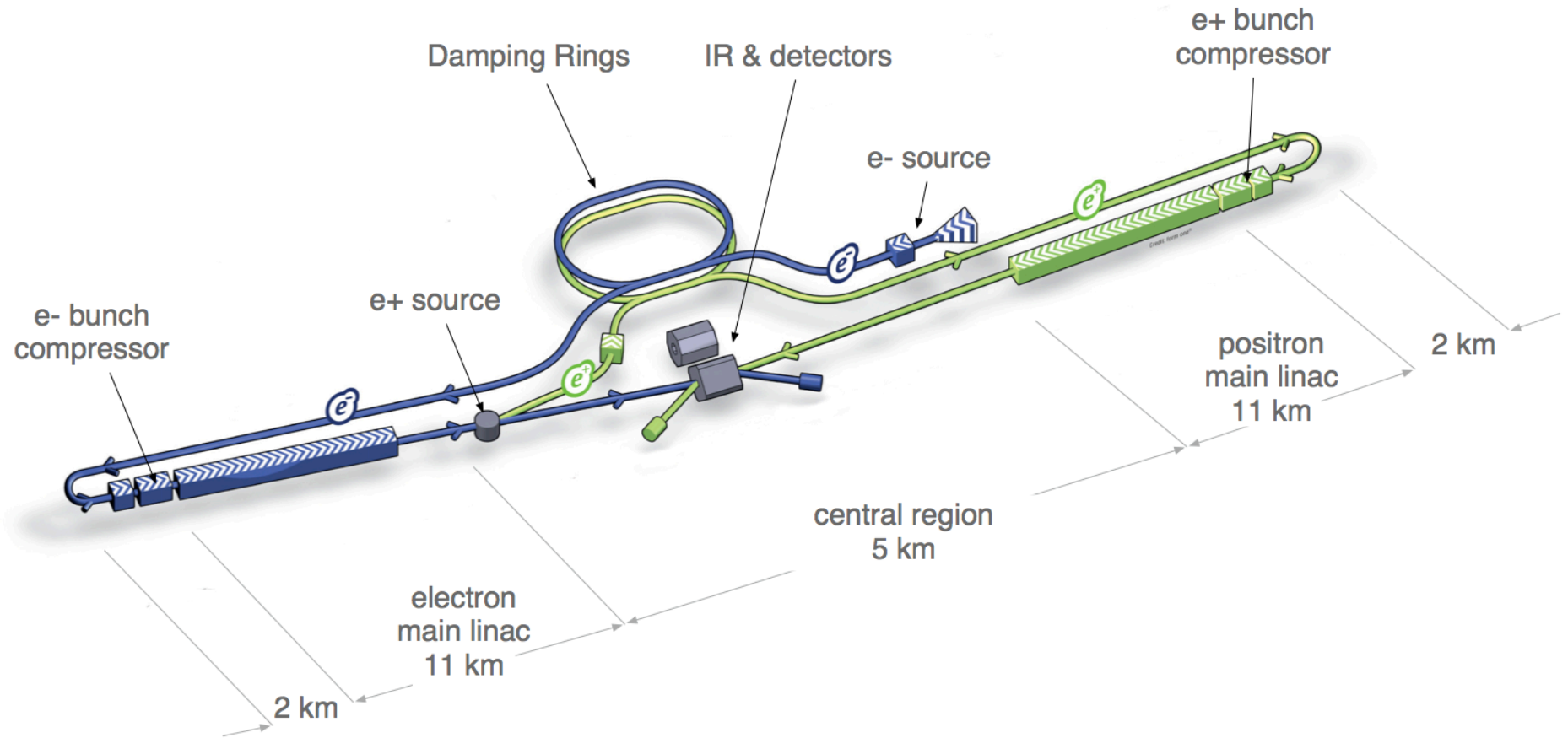


**NuTeV Neutrino Production**

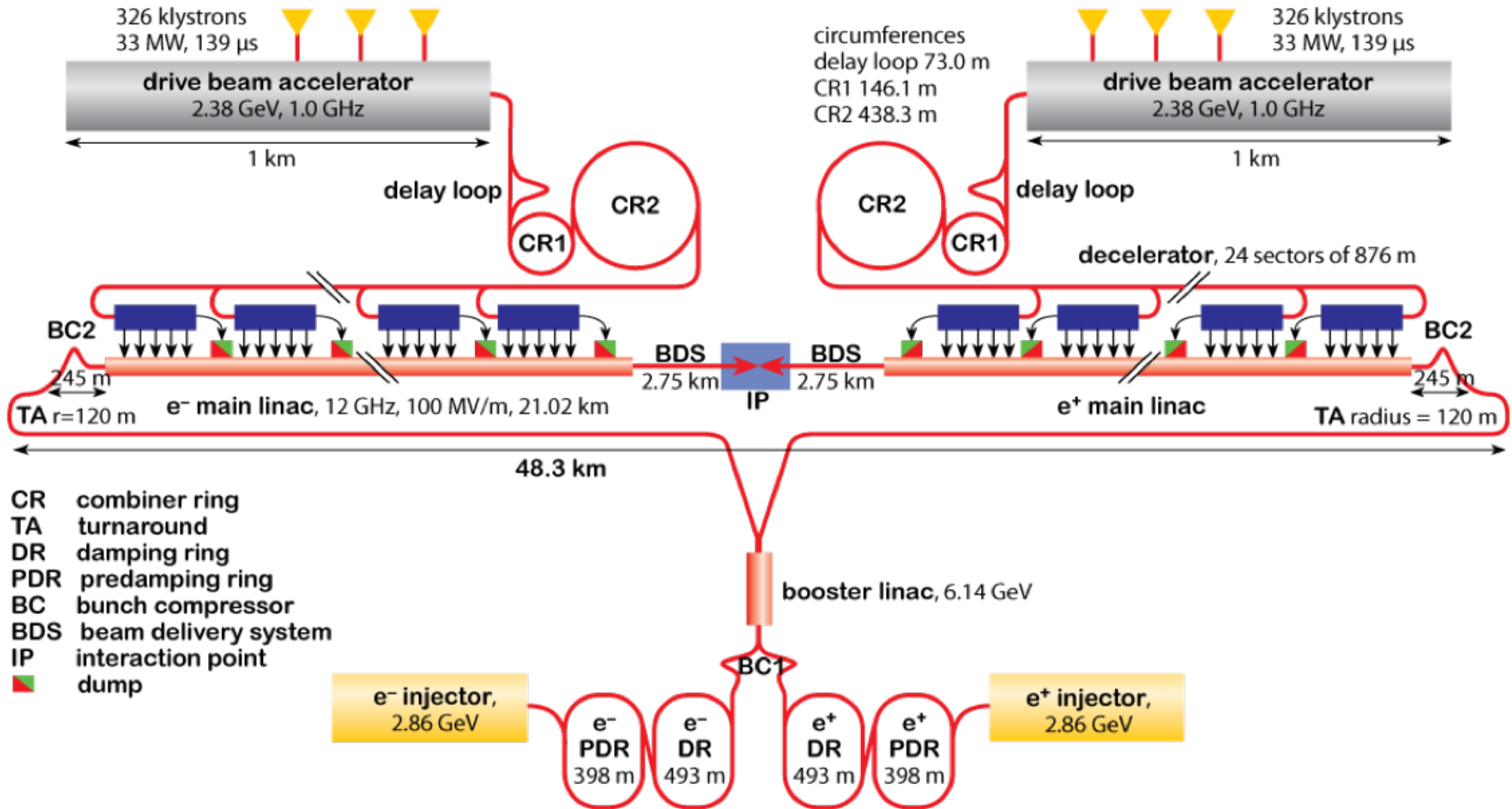
# Production of secondary beams



# Future colliders? ILC

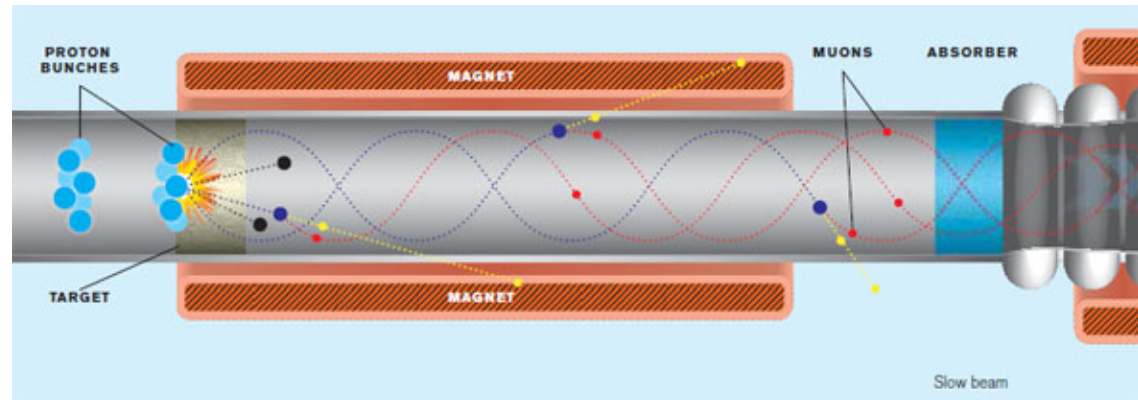
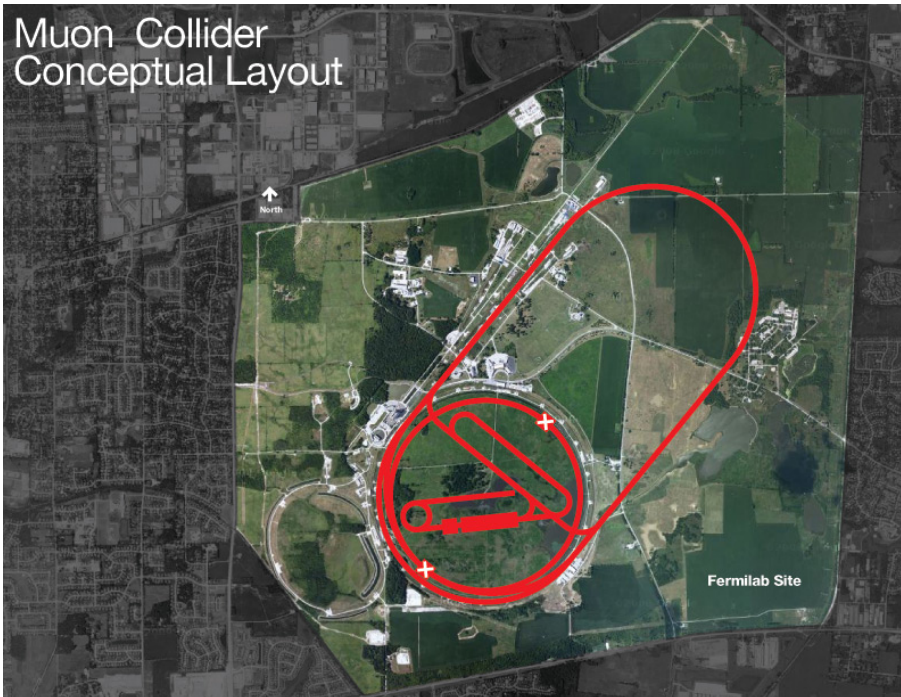
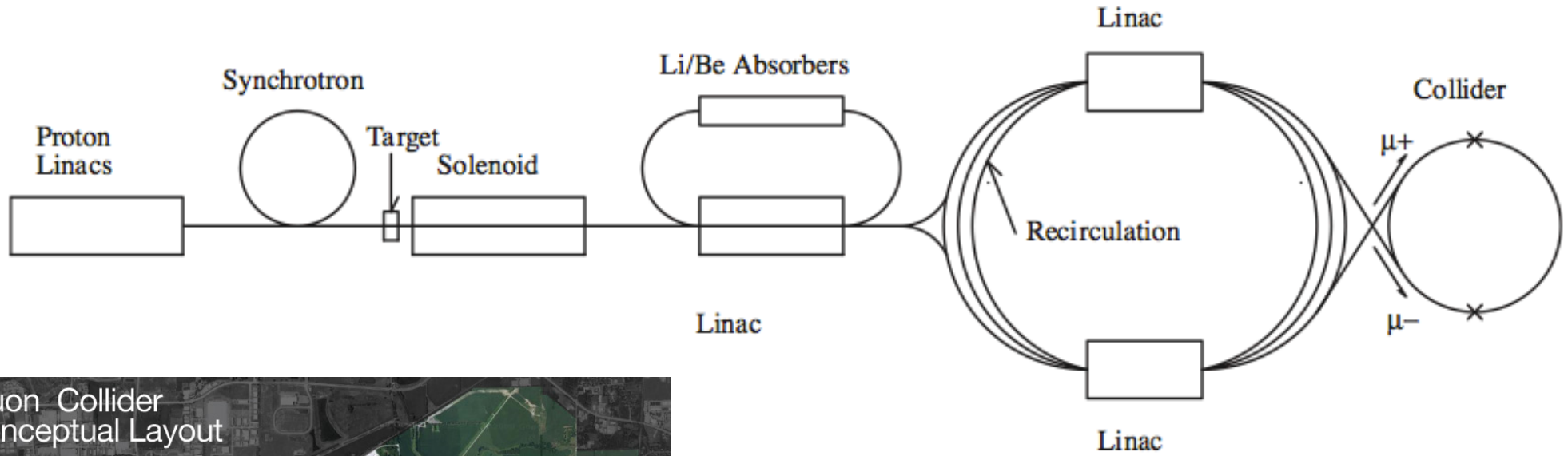


# Future colliders? CLIC





# Future colliders? Muon collider





Muon collider  
d=2km



ILC  
l=30km

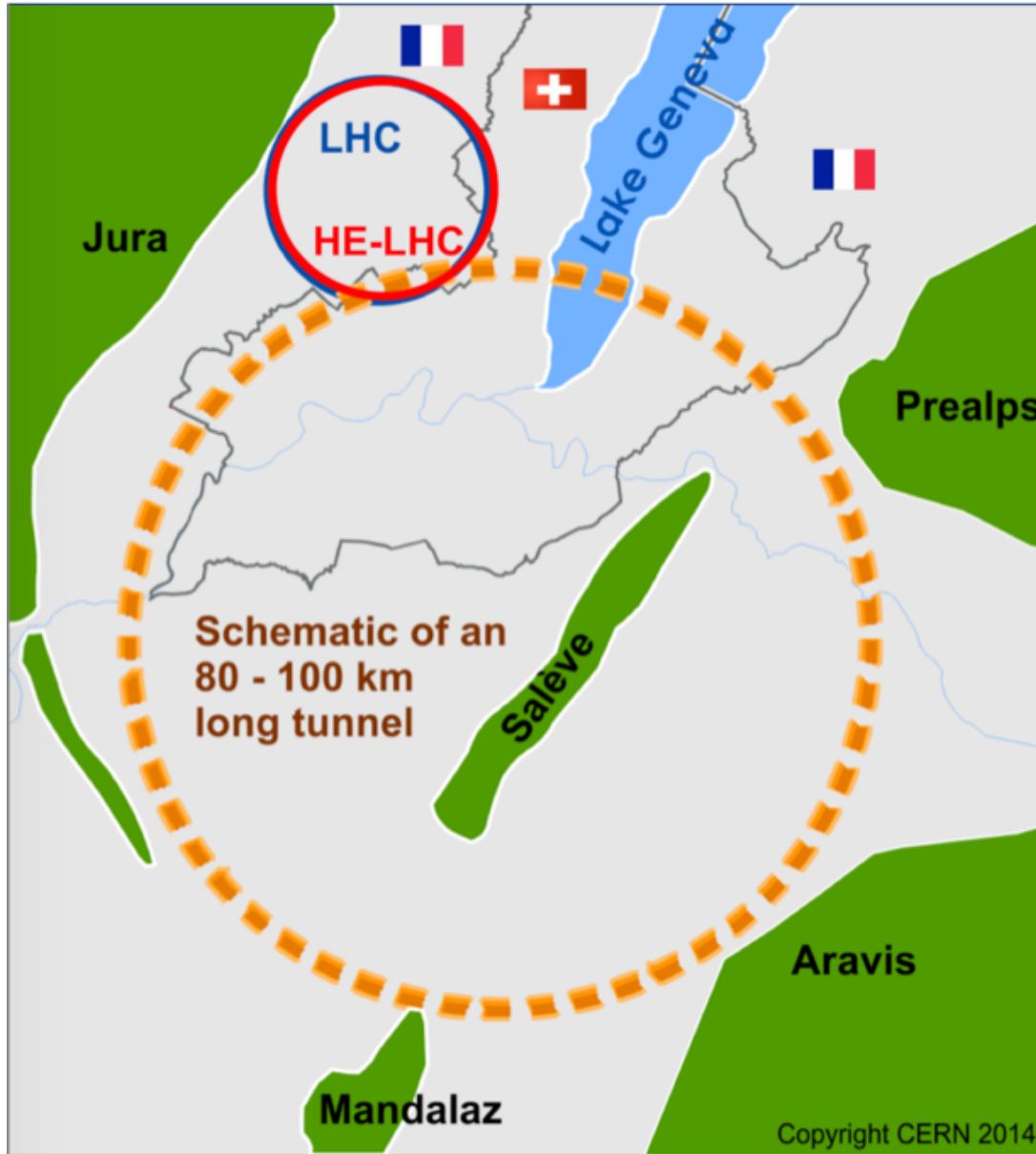


CLIC  
l=50km



LHC  
d=8.4km

# Future Circular Collider (FCC)



International FCC collaboration (CERN as host lab) to study:

- $pp$ -collider (*FCC-hh*)  
→ main emphasis, defining infrastructure requirements

**$\sim 16 T \Rightarrow 100 \text{ TeV } pp \text{ in } 100 \text{ km}$**

- $\sim 100 \text{ km}$  tunnel infrastructure in Geneva area, site specific
- $e^+e^-$  collider (*FCC-ee*), as potential first step
- HE-LHC with *FCC-hh* technology
- $p-e$  (*FCC-he*) option, IP integration,  $e^-$  from ERL

# Future Circular Collider (FCC)

## FCC-ee:

- Exploration of 10 to 100 TeV energy scale via couplings with precision measurements
- ~20-50 fold improved precision on many EW quantities (equiv. to factor 5-7 in mass) ( $m_Z$ ,  $m_W$ ,  $m_{\text{top}}$ ,  $\sin^2 \theta_w^{\text{eff}}$ ,  $R_b$ ,  $\alpha_{\text{QED}}(m_Z)$ ,  $\alpha_s(m_Z)$ , Higgs and top quark couplings)
- Machine design for highest possible luminosities at Z, WW, ZH and  $t\bar{t}$  working points

## FCC-hh:

- Highest center of mass energy for direct production up to 20 - 30 TeV
- Huge production rates for single and multiple production of SM bosons (H,W,Z) and quarks
- Machine design for 100 TeV c.m. energy & integrated luminosity  $\sim 20\text{ab}^{-1}$  within 25 years

## HE-LHC:

- Doubling LHC collision energy with FCC-hh 16 T magnet technology
- c.m. energy = 27 TeV  $\sim 14\text{ TeV} \times 16\text{ T}/8.33\text{ T}$ , target luminosity  $\geq 4 \times \text{HL-LHC}$
- Machine design within constraints from LHC CE and based on HL-LHC and FCC technologies

