

Kaon Physics: Theory View

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→ Technion (from Oct.)

Workshop on the physics of HL-LHC,
and perspectives at HE-LHC

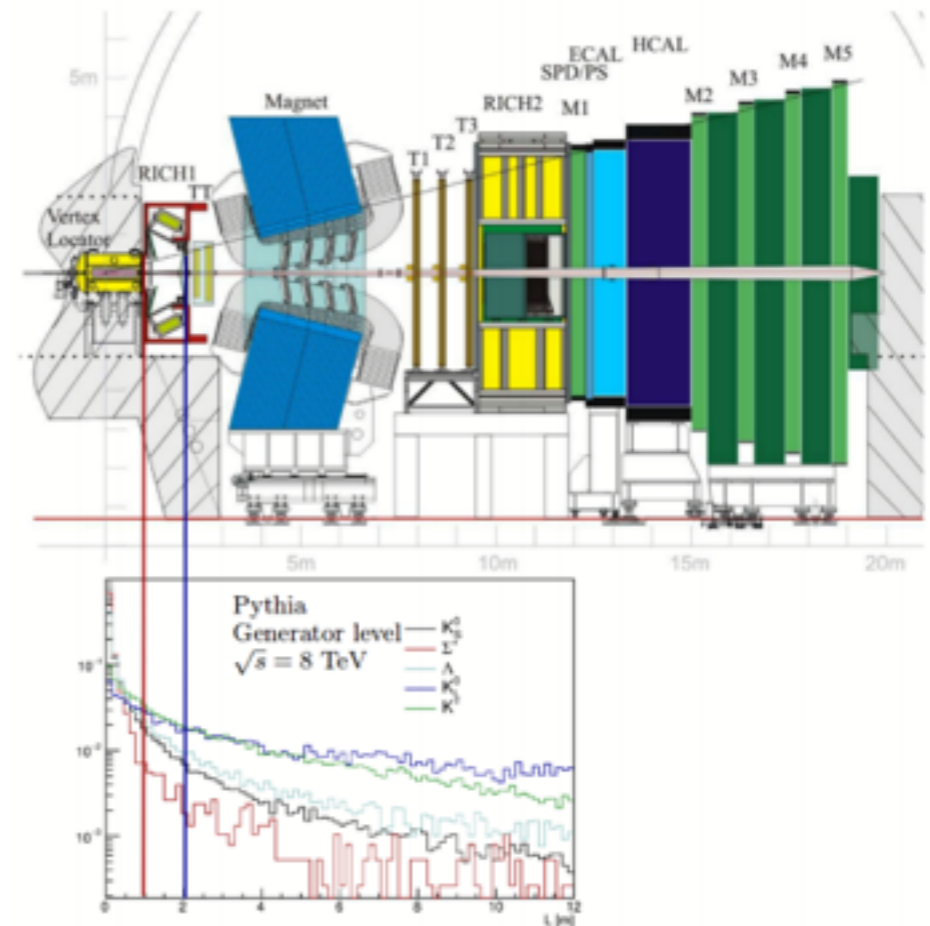


CERN, June 20, 2018



Kaon

in LHCb

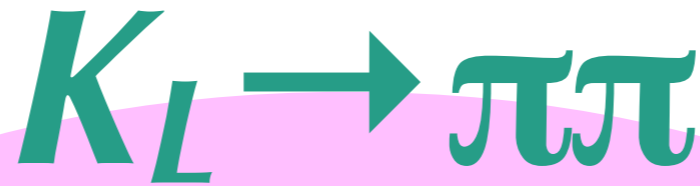


- LHCb experiment has been designed for efficient reconstructions of b and c
- Huge production of strangeness [$O(10^{13})/\text{fb}^{-1} K_S^0$] is suppressed by its trigger efficiency [$\epsilon \sim 1\text{-}2\%$ @LHC Run-I, $\epsilon \sim 18\%$ @LHC Run-II]
- LHCb Upgrade (LS2=Phase I upgrade, LS4=Phase II upgrade) could realize high efficiency for K_S^0 [$\epsilon \sim 90\%$ @LHC Run-III] [[M. R. Pernas, HL/HE LHC meeting, FNAL, 2018](#)]
- In LHC Run-III and HL-LHC, we could probe the *ultra* rare decay $\text{Br} \sim O(10^{-11\sim 12})$

collider search

Lattice
perturbative calculations
meson effective theory (ChPT)

ϵ_K and ϵ'_K discrepancies?

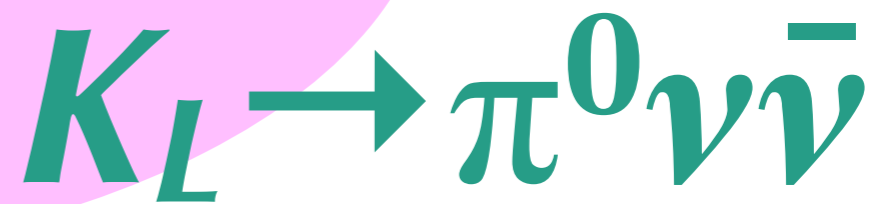


correlations

B

could give stronger constraints

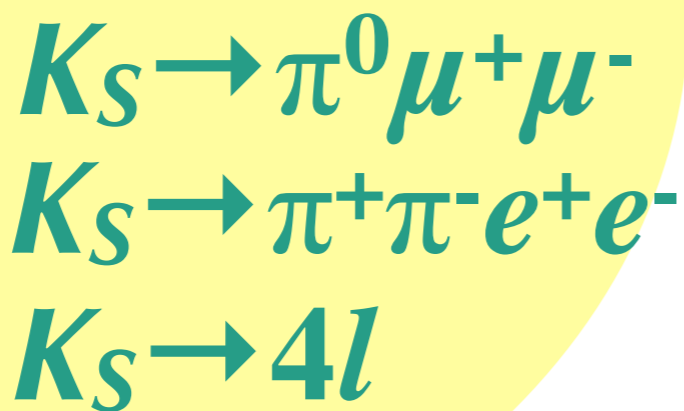
CP-violating
FCNC



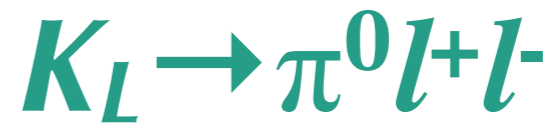
Yellow Report



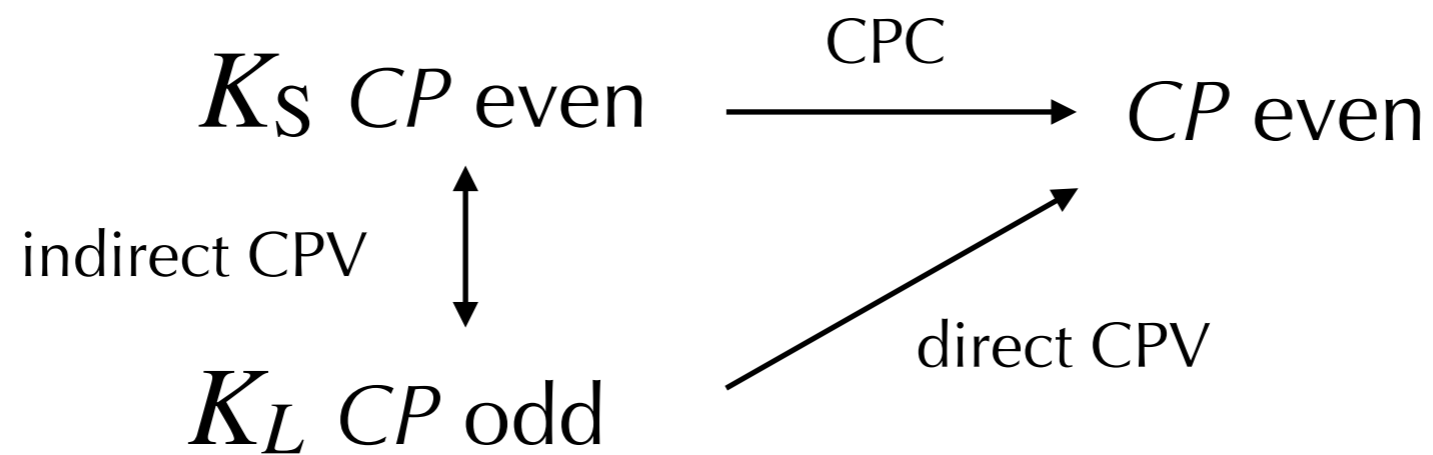
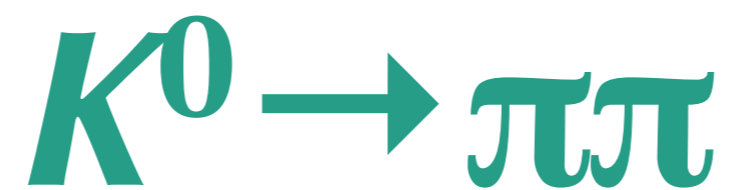
Understanding of ChPT



reduce th. error



less sensitive because of LD contributions



$K^0 \rightarrow \pi\pi$ systems: two CP violations

- Precise measurements for neutral kaon decay into two pions have revealed **two types of CP violations**: **indirect CPV ε_K** & **direct CPV ε'_K** :

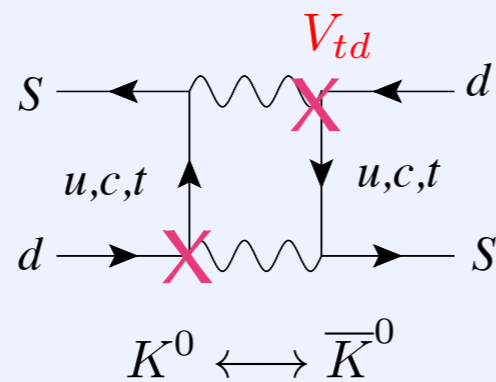
$$\mathcal{A}(K_L \rightarrow \pi^+\pi^-) \propto \varepsilon_K + \varepsilon'_K \quad \text{with } \varepsilon_K = \mathcal{O}(10^{-3}) \neq 0 \quad [\text{Christenson, Cronin, Fitch, Turlay '64 with Nobel prize}]$$

$$\mathcal{A}(K_L \rightarrow \pi^0\pi^0) \propto \varepsilon_K - 2\varepsilon'_K \quad \varepsilon'_K = \mathcal{O}(10^{-6}) \neq 0 \quad [\text{NA48/CERN and KTeV/FNAL '99}]$$



$$\text{Re}\left(\frac{\varepsilon'_K}{\varepsilon_K}\right) = \frac{1}{6} \left[1 - \frac{\mathcal{B}(K_L \rightarrow \pi^0\pi^0) \mathcal{B}(K_S \rightarrow \pi^+\pi^-)}{\mathcal{B}(K_S \rightarrow \pi^0\pi^0) \mathcal{B}(K_L \rightarrow \pi^+\pi^-)} \right] = \mathcal{O}(10^{-3})$$

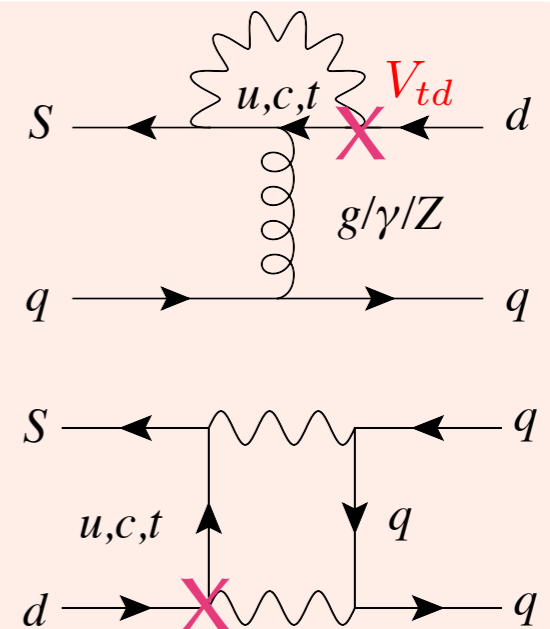
$\Delta S=2$
Indirect CP violation
[Kaon mixing]



W box

$$\varepsilon_K \propto \text{Im}[(\text{CKM})^2]$$

$\Delta S=1$
Direct CP violation
penguin and W-box



$$\varepsilon'_K \propto \text{Im}[\text{CKM}]$$

ϵ_K discrepancy

- SM prediction of the indirect CP violation ϵ_K is sensitive to $|V_{cb}|$

$$\epsilon_K = \epsilon_K(\text{SD}) + \epsilon_K(\text{LD}) \quad \leftarrow \quad \epsilon_K(\text{LD}) = -3.6(2.0)\% \times \epsilon_K(\text{SD})_{\text{SM}} \quad [\text{Buras, Guadagnoli, Isidori '10}]$$

$$\epsilon_K(\text{SD}) \propto \text{Im}\lambda_t [-\text{Re}\lambda_t \eta_{tt} S_0(x_t) + (\text{Re}\lambda_t - \text{Re}\lambda_c) \eta_{ct} S_0(x_c, x_t) + \text{Re}\lambda_c \eta_{cc} S_0(x_c)]$$

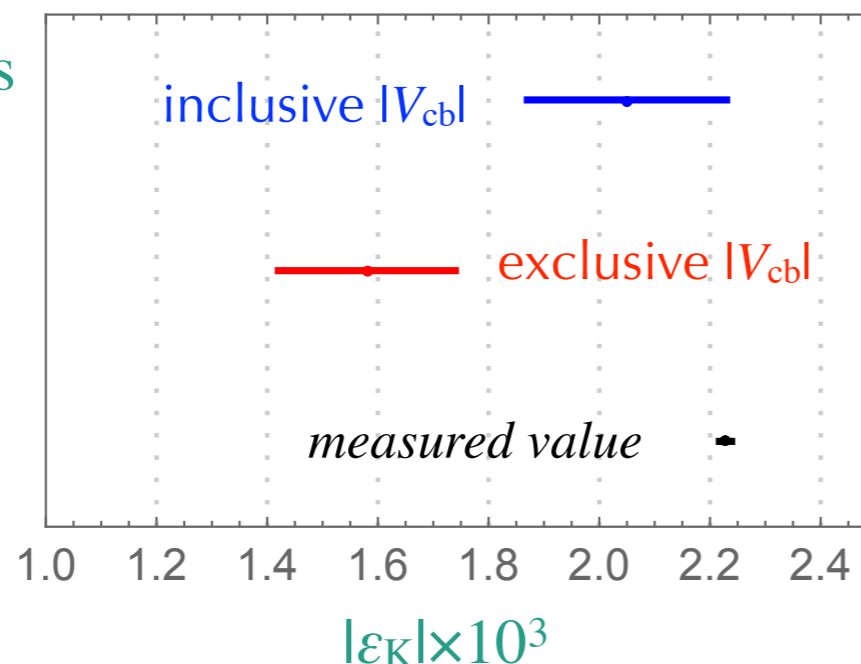
Wolfenstein parametrization \rightarrow $\simeq \bar{\eta} \lambda^2 |V_{cb}|^2 [|V_{cb}|^2 (1 - \bar{\rho}) \eta_{tt} S_0(x_t) + \eta_{ct} S_0(x_c, x_t) - \eta_{cc} S_0(x_c)]$

Leading contribution is proportional to $|V_{cb}|^4$

$|\epsilon_K|$ predictions

($\pm 1\sigma$ error bar)

errors are dominated by $|V_{cb}|, \bar{\eta}, \eta_{ct}, \eta_{cc}$



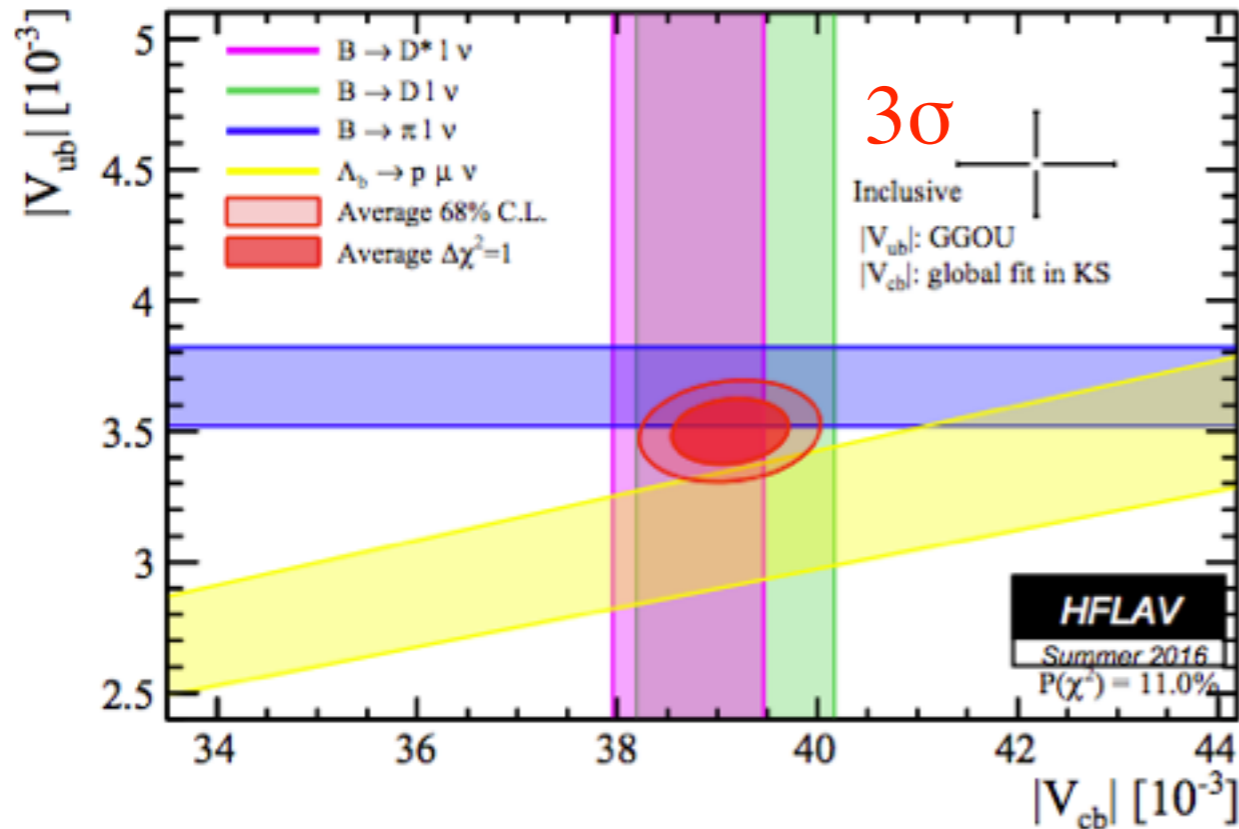
Theoretical prediction of ϵ_K with **inclusive $|V_{cb}|$** is consistent with the measured value, while there is **4.0σ tension** in **exclusive $|V_{cb}|$ case**

[LANL-SWME, 1710.06614]

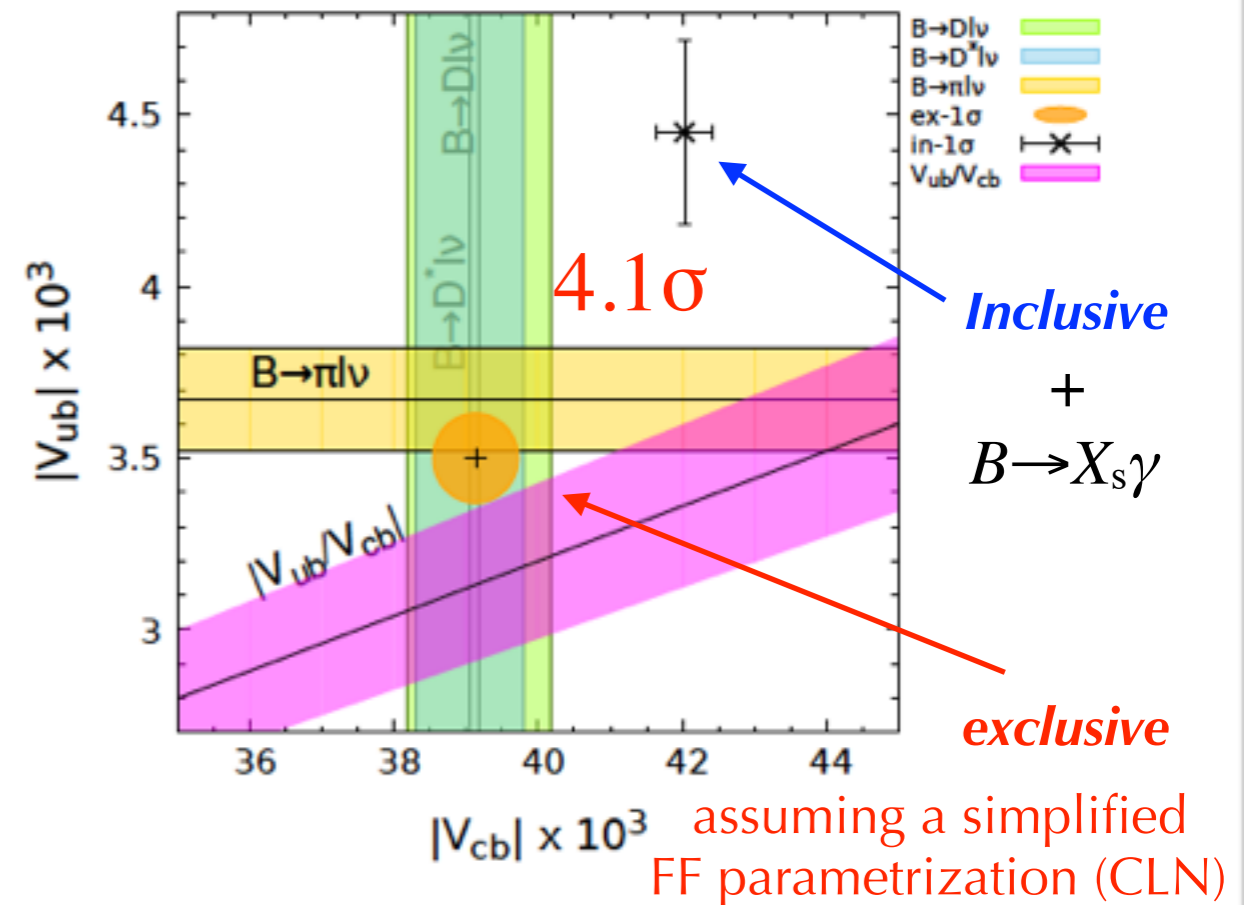
Wolfenstein parameters are determined by the angle-only fit

ϵ_K discrepancy $\sim |V_{cb}|$ discrepancy

[HFLAV average, 1612.07233]



[LANL-SWME, 1710.06614]



Recent progress on exclusive $|V_{cb}|$ in $B \rightarrow D^*$ transition

$B \rightarrow D^* \ell \bar{\nu}$
 [Belle, 1702.01521]

Model independent form factors parametrization [Boyd-Grinstein-Lebed (BGL) '97]

$|V_{cb}|_{\text{BGL}}^{\text{excl.}} = (40.6_{-1.3}^{+1.2}) \times 10^{-3}$ [Bigi, Gambino, Schacht '17]

error will be reduced by future lattice result

+ Similar recent progress [Grinstein, Kobach '17, Bernlochner, Ligeti, Papucci, Robinson '17]

Direct CP violation in $K^0 \rightarrow \pi\pi$

- Further strong suppression of ϵ'_K comes from **the smallness of the $\Delta I=3/2$ amplitude (i.e. $\Delta I=1/2$ rule)** and **an accidental cancellation** between the SM penguins

$$\mathcal{A}(K^0 \rightarrow (\pi\pi)_I) \equiv \mathcal{A}_I e^{i\delta_I}$$

I : two-pion isospin=0,2

pion = isospin triplet

$$\mathcal{A}(\bar{K}^0 \rightarrow (\pi\pi)_I) \equiv \bar{\mathcal{A}}_I e^{i\delta_I} = \mathcal{A}_I^* e^{i\delta_I}$$

δ_I : strong phase

$$\frac{\epsilon'_K}{\epsilon_K} = \frac{1}{\sqrt{2}|\epsilon_K|\text{Re}A_0} \frac{\text{Re}A_2}{\text{Re}A_0} \left(-\text{Im}A_0 + \frac{\text{Re}A_0}{\text{Re}A_2} \text{Im}A_2 \right)$$

sensitive

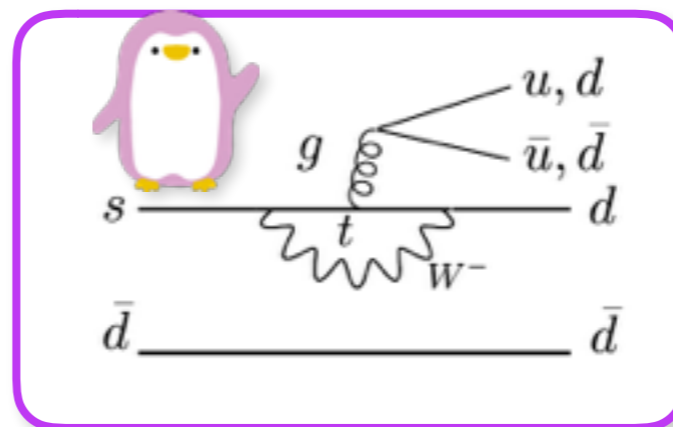
$\Delta I=1/2$ rule: factor = 0.04

Accidental cancellation

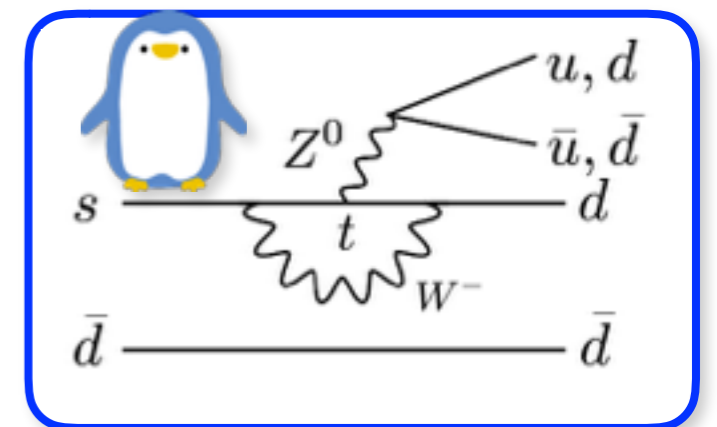
$$\mathcal{O}(\alpha_s) \sim \frac{1}{\omega} \mathcal{O}(\alpha)$$

$$\text{where } \frac{1}{\omega} \equiv \frac{\text{Re}A_0}{\text{Re}A_2} = 22.46 \text{ (exp.)}$$

$\sim \text{Im} [\text{QCD penguin}]$



$\sim \text{Im} [\text{EW penguin}]$



Progress on RG evolution

- Analytic solution of $f=3$ QCD-NLO RG evolution has a unphysical singularity [Ciuchini,Franco,Martinelli,Reina '93, '94, Buras,Jamin,Lautenbacher '93]

$$\hat{J}_s - \left[\hat{J}_s, \frac{\hat{\gamma}_s^{(0)T}}{2\beta_0} \right] = \frac{\beta_1}{\beta_0} \frac{\hat{\gamma}_s^{(0)T}}{2\beta_0} - \frac{\hat{\gamma}_s^{(1)T}}{2\beta_0}, \quad \longleftrightarrow \quad \left(\hat{V}^{-1} \hat{J}_s \hat{V} \right)_{ij} = \frac{\dots}{2\beta_0 \mp \left((\hat{\gamma}_{s,D}^{(0)T})_{jj} - (\hat{\gamma}_{s,D}^{(0)T})_{ii} \right)}.$$

10x10 matrix \hat{J}_s is a solution of the $f=3$ QCD-NLO RG evolution

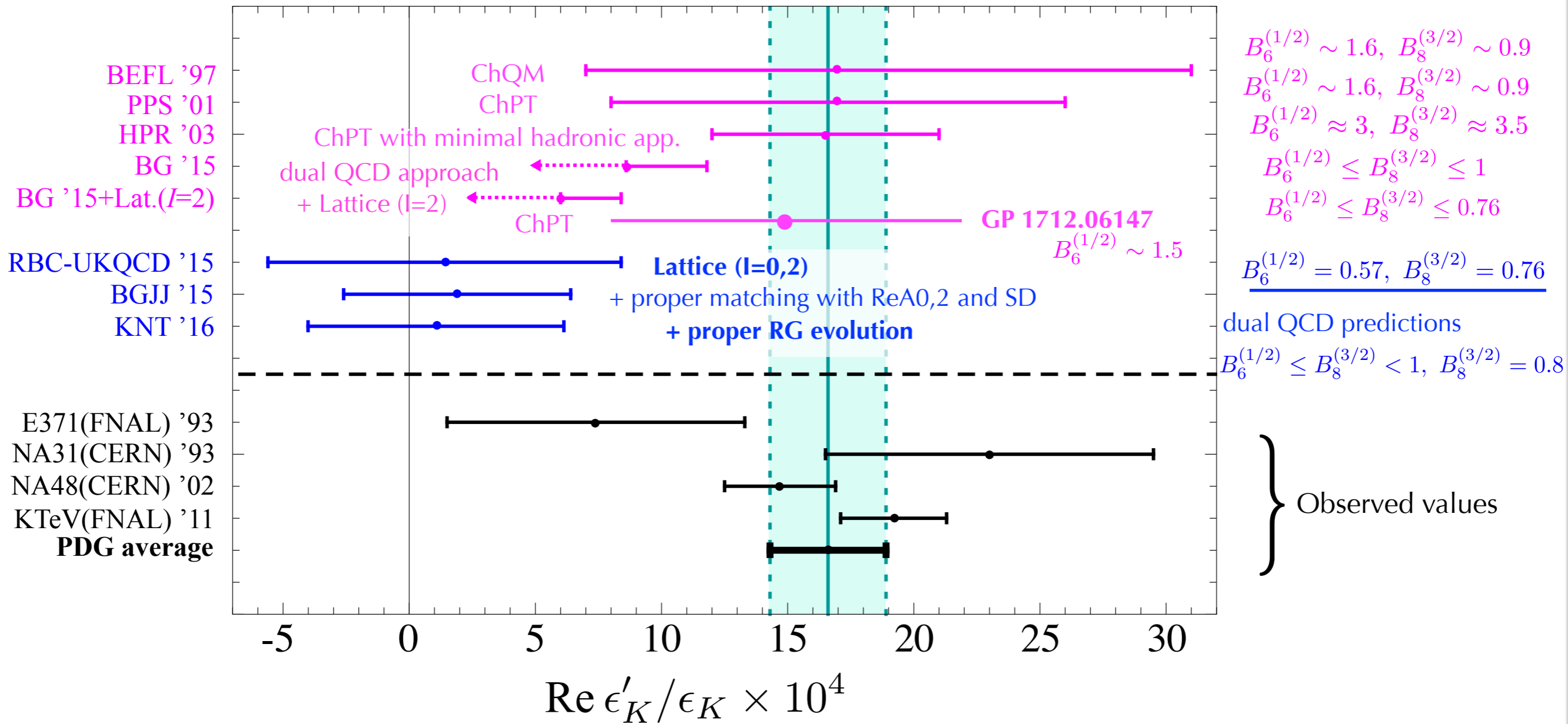
$2\beta_0 = 18$, $\hat{\gamma}_{s,D}^{(0)T} \supset +2, -16$ leads to singularity, which requires a regulator in ADM $\hat{\gamma}_s^{(0)}$

- Similar singularities exist in QED-NLO and QCD-QED-NLO RG evolutions
- Singularity-free analytic solutions are obtained using more generalized ansatz for the NLO evolution matrices [TK, Nierste, Tremper, JHEP '16]
 - $\ln \alpha_s(\mu_2)/\alpha_s(\mu_1)$ terms are added compared to the previous solution
 - Contribution of order α^2/α_s^2 is also included for the first time and we find it is numerically irrelevant in the SM \rightarrow good perturbation

Current situation of ϵ'_K/ϵ_K

$$\propto \text{Im}A_0 - \left(\frac{\text{Re}A_0}{\text{Re}A_2}\right) \text{Im}A_2$$

$$\propto B_6^{(1/2)} \qquad \propto B_8^{(3/2)}$$



$\Delta I = 1/2$ rule $\left(\frac{\text{Re}A_0}{\text{Re}A_2}\right)$	Exp.	ChPT	dual QCD	Lattice
	22.45 ± 0.05	~ 14	16.0 ± 1.5	31.0 ± 11.1

$\varepsilon'_K/\varepsilon_K$ discrepancy

- Lattice result with recent progress on the short-distance physics predicts $\varepsilon'_K/\varepsilon_K = O(10^{-4})$ which is below the experimental average **at 2.8-2.9 σ level**
NNLO QCD in progress [Cerdà-Sevilla, Gorbahn, Jäger, Kokulu]
- A large- N_c analysis (dual QCD method) including final-state interaction (FSI) is consistent with lattice results [Buras, Gerard, '15, '17]
- ChPT including FSI predicts $\varepsilon'_K/\varepsilon_K = O(10^{-3})$ with large error which is consistent with measured values [Gisbert, Pich 1712.06147]
- Main difference comes from $B_6^{(1/2)} = 0.6$ (lattice) vs 1.5 (ChPT)
- The lattice simulation includes FSI as the Lellouch-Lüscher finite-volume correction and explained $\Delta I=1/2$ rule for the first time. But, the strong phase of $I=0$ is smaller than a phenomenological expectation **at 2.7 σ level**
[Colangelo, Passemar, Stoffer '15]
- For $I=2$ decay, lattice/dual QCD/ChPT give well consistent results

Lattice simulation with improved methods and higher statistics is on-going [1711.05648]

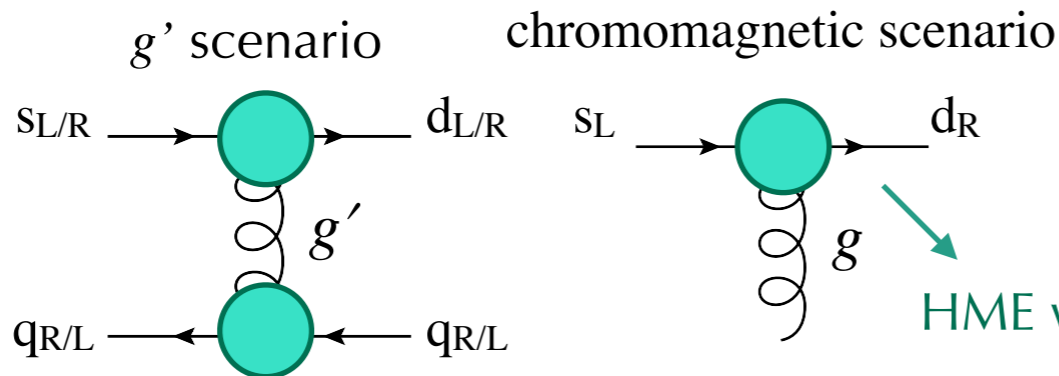
ϵ'_K/ϵ_K in the BSM

- Several types of BSM can explain ϵ'_K/ϵ_K discrepancy

$$\frac{\epsilon'_K}{\epsilon_K} = \frac{1}{\sqrt{2}|\epsilon_K|\text{Re}A_0} \frac{\text{Re}A_2}{\text{Re}A_0} \left(-\text{Im}A_0 + \frac{\text{Re}A_0}{\text{Re}A_2} \text{Im}A_2 \right)$$

$$\frac{\text{Re}A_0}{\text{Re}A_2} = 22.46 \text{ (exp.)}$$

$\text{Im}A_0$



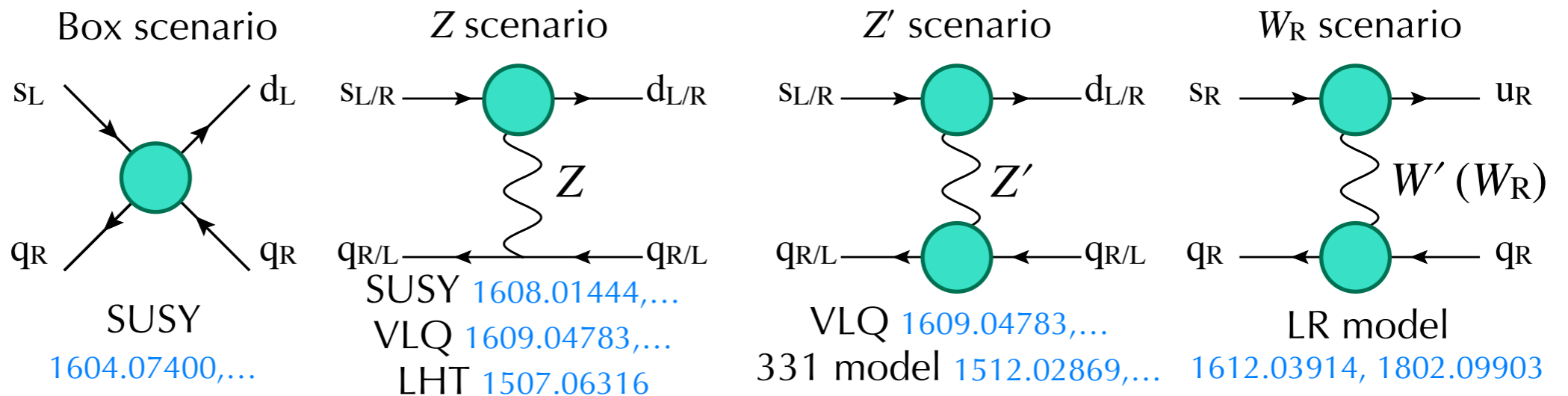
: BSM vertex (must include CPV phase)

HME would be suppressed [1712.09824, 1803.08052]

RS model 1404.3824
 chiral-flavorful vector 1806.02312

SUSY 1711.11030,...
 Type-III 2HDM 1805.07522

$\text{Im}A_2$



SUSY 1604.07400,...

SUSY 1608.01444,...
 VLQ 1609.04783,...
 LHT 1507.06316

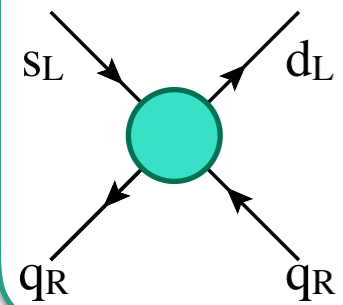
VLQ 1609.04783,...
 331 model 1512.02869,...

LR model 1612.03914, 1802.09903

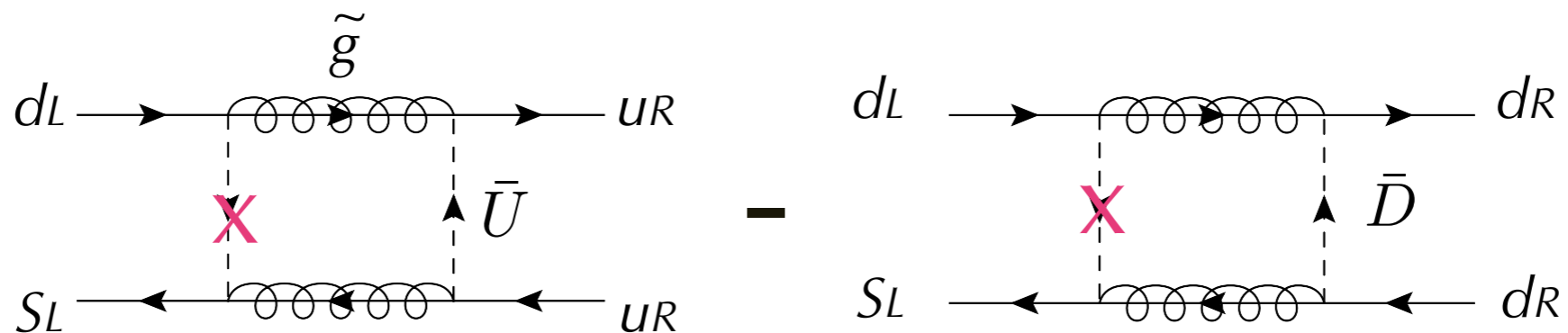
Gluino-box contribution

[Kagan, Neubert, PRL '99, Grossman, Kagan, Neubert, JHEP '99, TK, Nierste, Tremper, PRL '16]

Box scenario



- In the supersymmetric models, the gluino box can significantly contribute to $\varepsilon'_{\text{K}}/\varepsilon_{\text{K}}$
- In spite of QCD correction, gluino box **can** break isospin symmetry through mass difference between right-handed up and down squarks, which contributes **ImA2**



$m_{\bar{U}} \neq m_{\bar{D}}$ $\xrightarrow{\text{RGE}}$ EW penguin operator Q_8 is generated at the low energy scale

with HMEs

\longrightarrow contribute to **ImA2** \longrightarrow

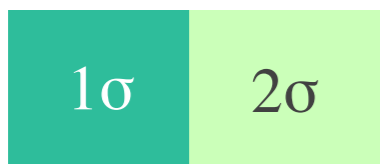
$\varepsilon'_{\text{K}}/\varepsilon_{\text{K}}$ can be solved

SUSY contributions to $\varepsilon'_K/\varepsilon_K$

[TK, Nierste, Tremper, PRL '16]
[Crivellin, D'Ambrosio, TK, Nierste '17]

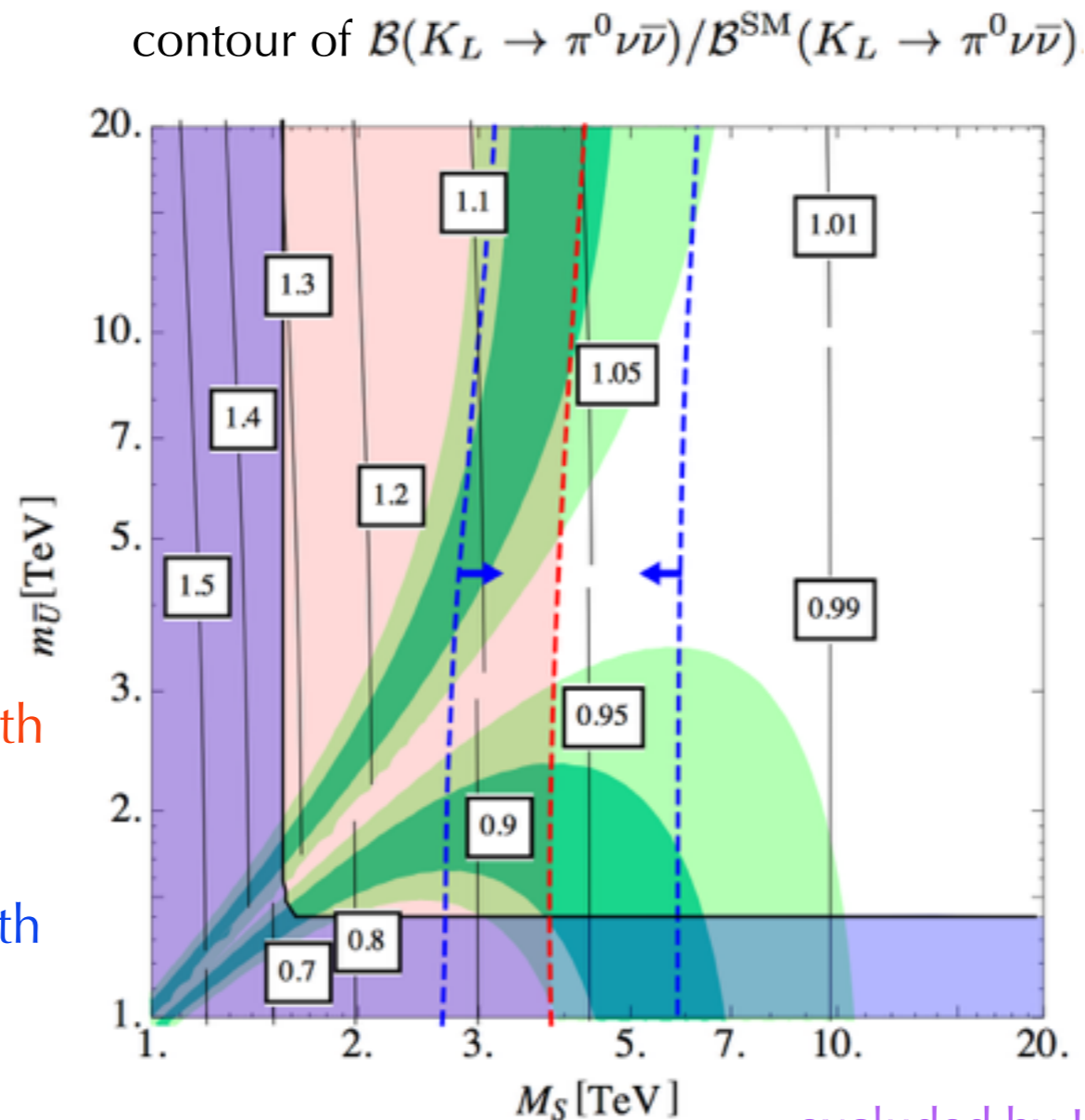
- We take universal SUSY mass (M_S) without gaugino masses (M_3) and right-handed up-type squark mass ($m_{\bar{U}}$)

$\varepsilon'_K/\varepsilon_K$ discrepancy can be solved at



excluded by ε_K with inclusive $|V_{cb}|$

preferred by ε_K with exclusive $|V_{cb}|$



$$M_3 = 1.5 M_S$$

for suppressed ε_K

$$m_{Q,ij}^2 = \Delta_{Q,ij} M_S^2$$

$$\Delta_{Q,12} = 0.1 \exp(-i\pi/4)$$

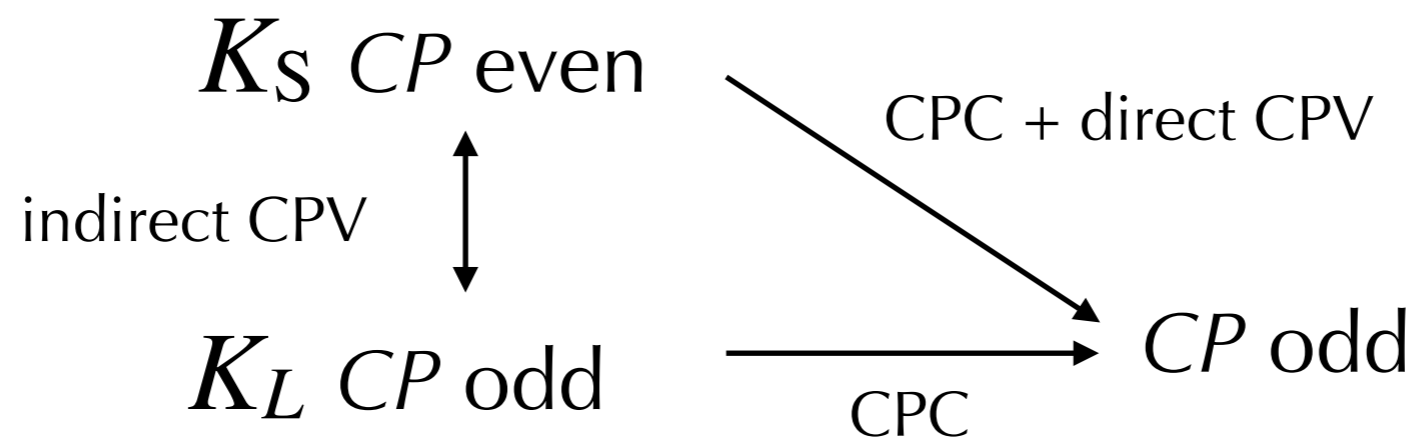
maximum CPV phase for ε_K

when $i\pi/4 \rightarrow i\pi/2$

amplifies $\varepsilon'_K/\varepsilon_K$

suppresses ε_K

excluded by LHC



$K^0 \rightarrow \mu^+ \mu^-$ systems

- SM predictions: [Ecker, Pich '91, Isidori, Unterdorfer '04, TK, D'Ambrosio '17]

$$\mathcal{B}(K_L \rightarrow \mu^+ \mu^-)_{\text{SM}} = \begin{cases} (6.85 \pm 0.80 \pm 0.06) \times 10^{-9} (+) \\ (8.11 \pm 1.49 \pm 0.13) \times 10^{-9} (-) \end{cases}$$

LD other

An unknown sign ambiguity

$$\pm = \text{sgn} \left[\frac{\mathcal{A}(K_L \rightarrow \gamma\gamma)}{\mathcal{A}(K_L \rightarrow (\pi^0)^* \rightarrow \gamma\gamma)} \right]$$

changes the relative sign between LD and SD

$$\begin{aligned} \mathcal{B}(K_S \rightarrow \mu^+ \mu^-)_{\text{SM}} &= [4.99(\text{LD}) + 0.19(\text{SD})] \times 10^{-12} \\ &= (5.18 \pm 1.50 \pm 0.02) \times 10^{-12} \end{aligned}$$

LD other

- $K_S \rightarrow \mu\mu$ is dominated by P-wave CP-conserving LD contribution, while S-wave CP-violating SD is subleading

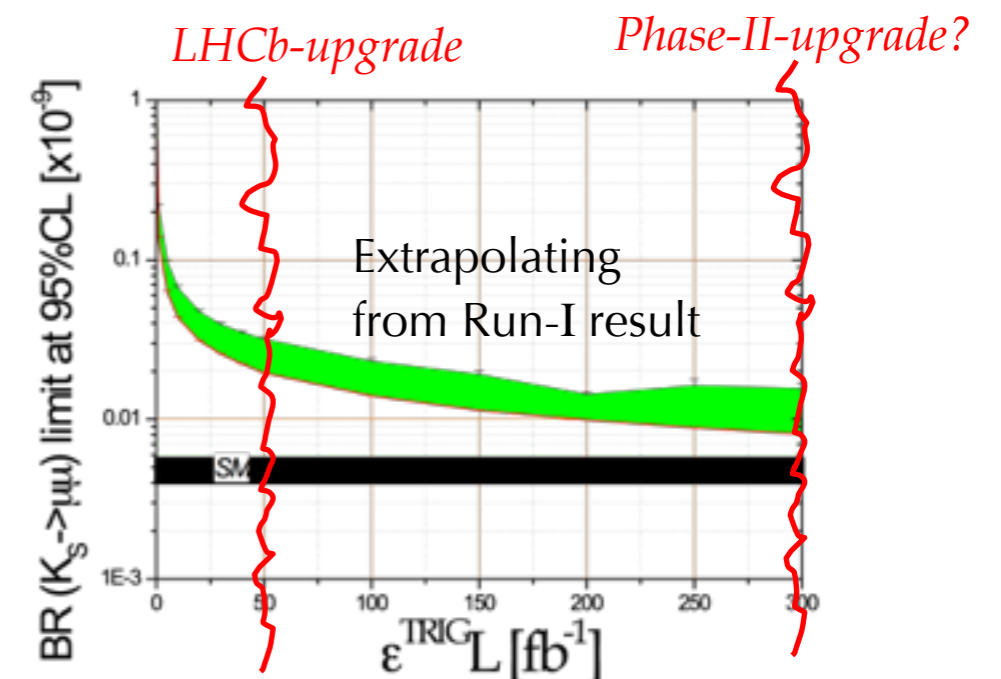
- Current bounds:

$$\mathcal{B}(K_L \rightarrow \mu^+ \mu^-)_{\text{exp}} = (6.84 \pm 0.11) \times 10^{-9} \quad [\text{BNL E871 '00}]$$

$$\mathcal{B}(K_S \rightarrow \mu^+ \mu^-)_{\text{exp}} < 0.8 \times 10^{-9} \quad [\text{LHCb, Run-I 1706.00758}]$$

- LHCb Upgrade is aiming to reach the SM sensitivity of $K_S \rightarrow \mu\mu$

[D. M. Santos, HQL2018]



Interference between K_S and K_L

- Decay intensity of neutral kaon beam into f states

$$\begin{aligned}
 I(K \rightarrow f)(t) &= \frac{1+D}{2} \left| \langle f | -\mathcal{H}_{\text{eff}}^{|\Delta S|=1} | K^0(t) \rangle \right|^2 + \frac{1-D}{2} \left| \langle f | -\mathcal{H}_{\text{eff}}^{|\Delta S|=1} | \bar{K}^0(t) \rangle \right|^2 \\
 &= \frac{1}{2} \left[\left\{ (1 - 2D \text{Re}[\bar{\epsilon}]) |\mathcal{A}(K_1)|^2 + 2 \text{Re}[\bar{\epsilon} \mathcal{A}(K_1)^* \mathcal{A}(K_2)] \right\} e^{-\Gamma_S t} \right. \\
 &\quad \left. + \left\{ (1 - 2D \text{Re}[\bar{\epsilon}]) |\mathcal{A}(K_2)|^2 + 2 \text{Re}[\bar{\epsilon} \mathcal{A}(K_1) \mathcal{A}(K_2)^*] \right\} e^{-\Gamma_L t} \right. \\
 &\quad \left. + \left\{ 2D \text{Re} \left[e^{-i\Delta M_K t} (\mathcal{A}(K_1)^* \mathcal{A}(K_2) + \bar{\epsilon} |\mathcal{A}(K_1)|^2 + \bar{\epsilon}^* |\mathcal{A}(K_2)|^2) \right] \right. \right. \\
 &\quad \left. \left. - 4 \text{Re}[\bar{\epsilon}] \text{Re} \left[e^{-i\Delta M_K t} \mathcal{A}(K_1)^* \mathcal{A}(K_2) \right] \right\} e^{-\frac{\Gamma_S + \Gamma_L}{2} t} \right] \\
 &\quad + \mathcal{O}(\bar{\epsilon}^2),
 \end{aligned}$$

$\leftarrow |\mathcal{A}(K_S \rightarrow f)|^2$
 $\leftarrow |\mathcal{A}(K_L \rightarrow f)|^2$
 $\leftarrow \text{Interference}$
 $\leftarrow \mathcal{A}(K_S \rightarrow f)^* \mathcal{A}(K_L \rightarrow f)$

$D = \frac{K^0 - \bar{K}^0}{K^0 + \bar{K}^0}$

\leftarrow time dependence \leftarrow $\tau \sim 2\tau_S$

- $f = \mu^+ \mu^-$ case [TK, D'Ambrosio, PRL '17]

$$\sum_{\text{spin}} \mathcal{A}(K_1 \rightarrow \mu^+ \mu^-)^* \mathcal{A}(K_2 \rightarrow \mu^+ \mu^-)$$

$$\mathcal{H}_{\text{eff}}^{|\Delta S|=1} = \frac{G_F \alpha}{\sqrt{2}} \lambda_t y'_{7A} (\bar{s} \gamma_\mu \gamma_5 d) (\bar{\mu} \gamma^\mu \gamma_5 \mu) + \text{H.c.}$$

$$= \frac{16i G_F^4 M_W^4 F_K^2 M_K^2 m_\mu^2 \sin^2 \theta_W}{\pi^3} \text{Im}[\lambda_t] y'_{7A} \{ A_{L\gamma\gamma}^\mu - 2\pi \sin^2 \theta_W (\text{Re}[\lambda_t] y'_{7A} + \text{Re}[\lambda_c] y_c) \}$$

- Interference comes from $K_S \rightarrow \mu\mu$ S-wave SD times $K_L \rightarrow \mu\mu$ S-wave CPC LD; $K_S \rightarrow \mu\mu$ P-wave LD is dropped

- Proportional to direct CPV

- Insensitive to indirect CPV $\bar{\epsilon}$

$$\begin{aligned}
 y'_{7A} &= -0.654(34), & A_{L\gamma\gamma}^\mu &= \pm 2.01(1) \cdot 10^{-4} \cdot [0.71(101) - i5.21] \\
 \text{top loop} & & \gamma\gamma \text{ loop} & \text{sign ambiguity}
 \end{aligned}$$

Direct CP asymmetry in $K_S \rightarrow \mu\mu$

[TK, D'Ambrosio, PRL '17] [Chobanova, D'Ambrosio, TK, Martinez, Santos, Fernandez, Yamamoto '18]
 [Endo, Goto, TK, Mishima, Ueda, Yamamoto, '18]

- Interference contribution is comparable size to CPC of $K_S \rightarrow \mu\mu$ thanks to the large absorptive part of long-distance contributions to $K_L \rightarrow \mu\mu$
- The unknown sign of $\mathcal{A}(K_L \rightarrow \gamma\gamma)$ can be probed
- Nonzero dilution factor (D) can be achieved by an accompanying charged kaon tagging and a charged pion tagging

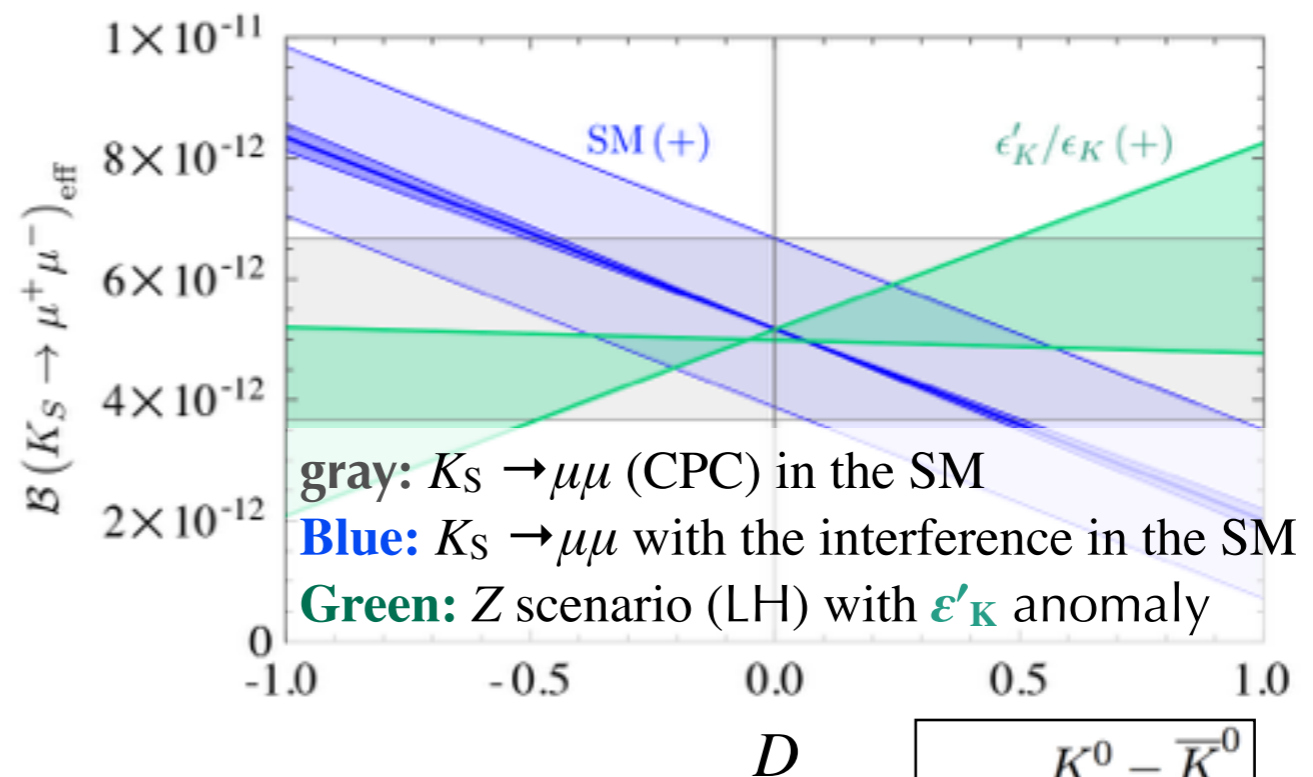
$$pp \rightarrow K^0 K^- X$$

$$pp \rightarrow K^{*+} X \rightarrow K^0 \pi^+ X$$

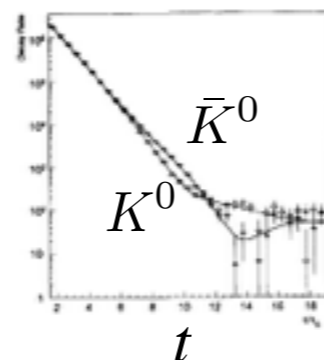
with $K^0 \rightarrow \{K_S, K_L\} \rightarrow \mu^+ \mu^-$

cf. CPLEAR experiment
 (1990-99@CERN)

$$p\bar{p} \rightarrow \begin{cases} K^0 K^- \pi^+ \\ \bar{K}^0 K^+ \pi^- \end{cases}$$



$$D = \frac{K^0 - \bar{K}^0}{K^0 + \bar{K}^0}$$



$\{K_S, K_L\} \rightarrow \pi^+ \pi^-$

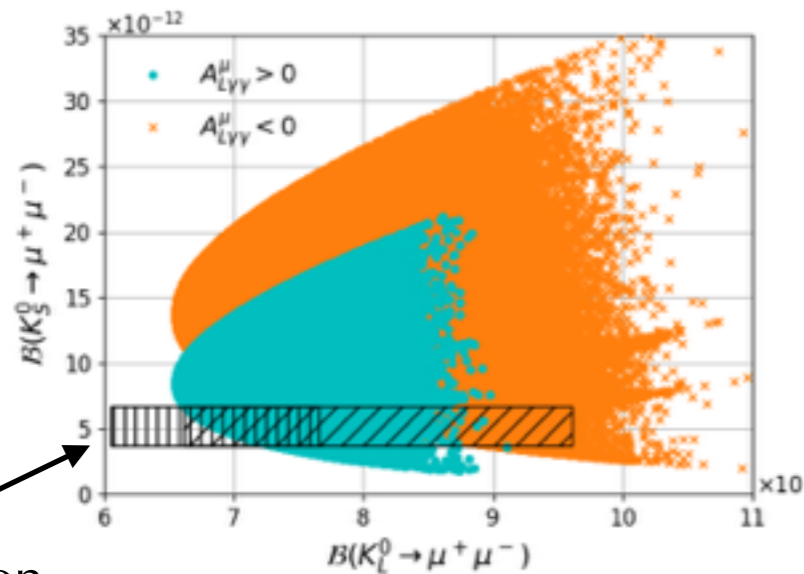
measured the interference between K_S and K_L
 [CPLEAR collaboration '95]

SUSY contributions to $K^0 \rightarrow \mu^+ \mu^-$

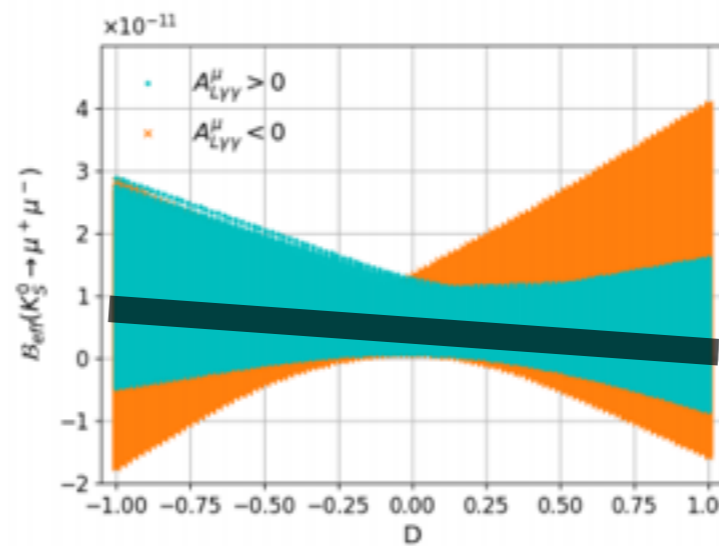
One of the MSSM scenario from Chobanova, D'Ambrosio, TK, Martinez, Santos, Fernandez, Yamamoto '18

mass difference between right-handed squarks, large $\tan\beta$, light $M_A \sim \text{TeV}$

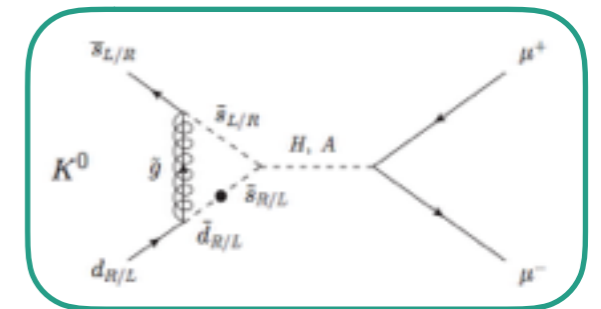
No interference plot
($D=0$)



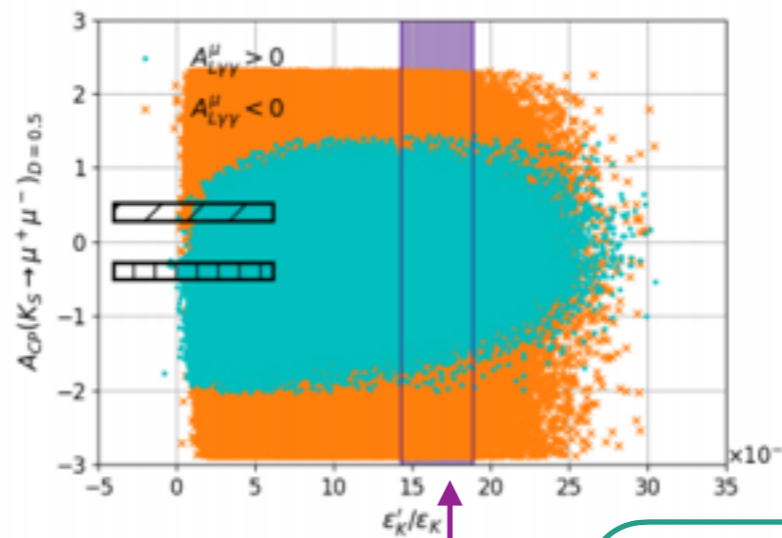
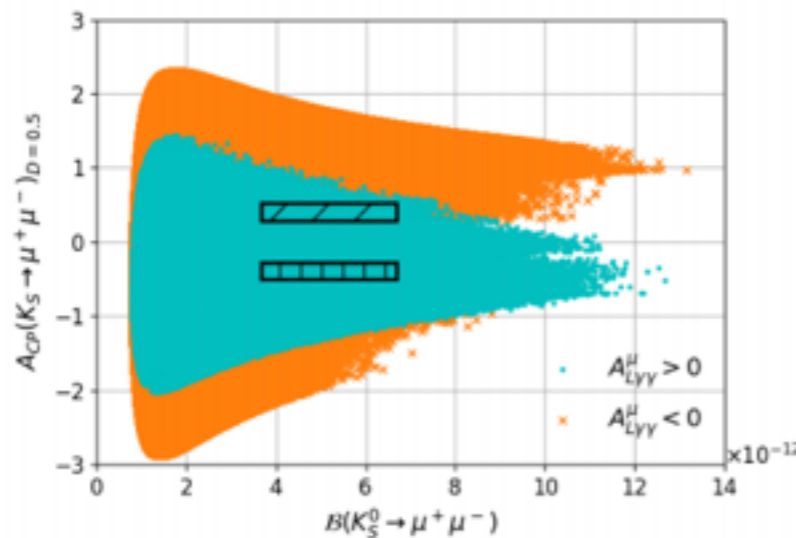
SM prediction



SM prediction [$\text{sgn}(A_{L\gamma\gamma}^\mu) > 0$]



$D=0.5$

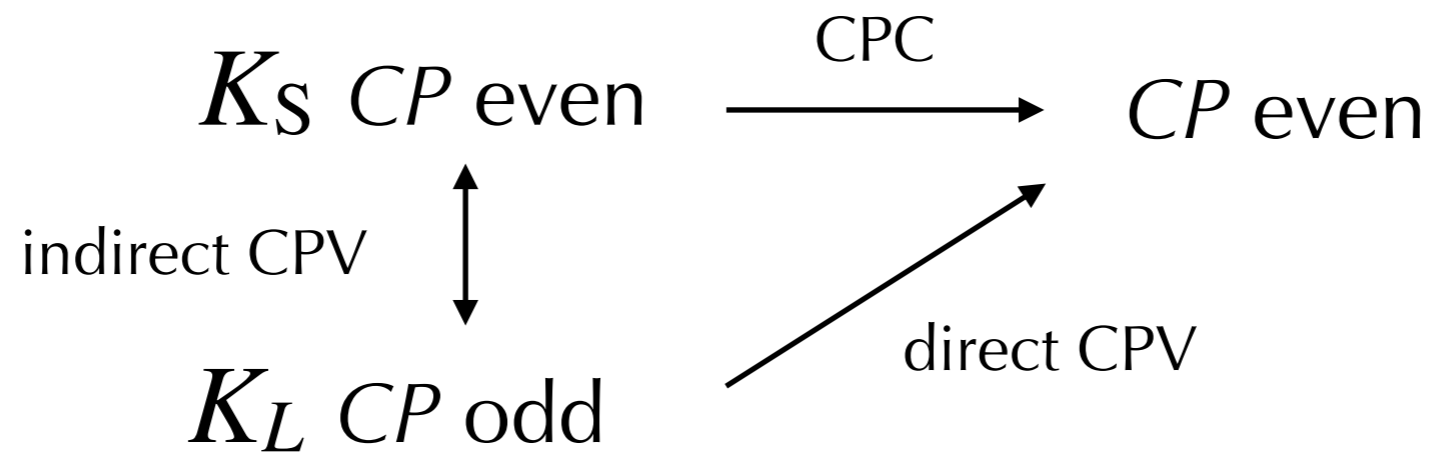


measured ϵ'_K/ϵ_K

Large deviations from SM predictions are possible in the MSSM

$$\mathcal{B}(K_S \rightarrow \mu^+ \mu^-)|_{\text{MSSM}} \sim \mathcal{O}(1) \times 10^{-11}$$

$$K \rightarrow \pi \nu \bar{\nu}$$



$K_L \rightarrow \pi^0 \nu \bar{\nu}$ and $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

- Both channels are theoretical clean and very sensitive to short-distance contributions, especially $K_L \rightarrow \pi^0 \nu \bar{\nu}$ is pure direct CPV decay

- SM predictions: [Buras, Buttazzo, Girschbach-Noe, Kneijens '15]

$$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})_{\text{SM}} = (8.4 \pm 1.0) \times 10^{-11}, \quad (9.11 \pm 0.72) \times 10^{-11}$$

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})_{\text{SM}} = (3.4 \pm 0.6) \times 10^{-11}, \quad (3.00 \pm 0.31) \times 10^{-11}$$

CKM from tree

CKM from tree+loop

- Current bounds:

$$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})_{\text{exp}} = 17.3_{-10.5}^{+11.5} \times 10^{-11} \quad [\text{E949, BNL '08}]$$

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})_{\text{exp}} \leq 2.6 \times 10^{-8} \quad [\text{E391a, J-PARC '10}]$$

- On-going experiments:



@CERN

$$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = 2.8_{-2.3}^{+4.4} \times 10^{-10} \quad (68\% \text{ CL}) \quad [\text{NA62, 2016data, HQL2018}]$$

- ~20 SM events are expected before LS2



@J-PARC

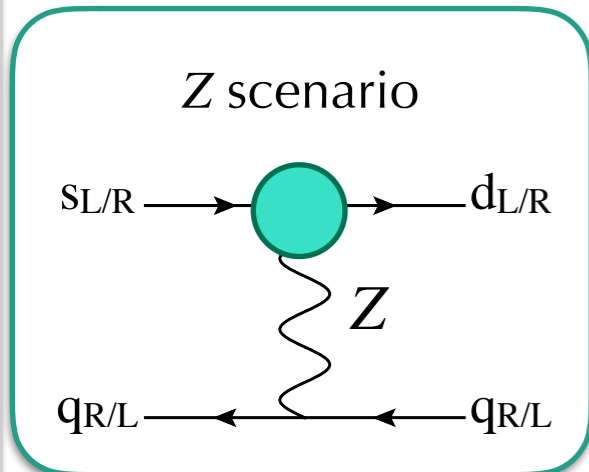
$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \lesssim \mathcal{O}(10^{-9}) \quad [\text{First result will be presented in this summer}]$$

- detector upgrade in this summer-autumn

- KOTO-step2 will aim at ~100 SM events

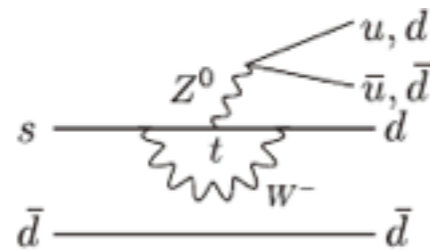
Modified Z-coupling scenario

[Buras, De Fazio, Girrbach, '13, '14] [Buras, Buttazzo, Kneijens, '15][Buras, '16]
 [Endo, TK, Mishima, Yamamoto, '16] [Bobeth, Buras, Celis, Jung, '17]

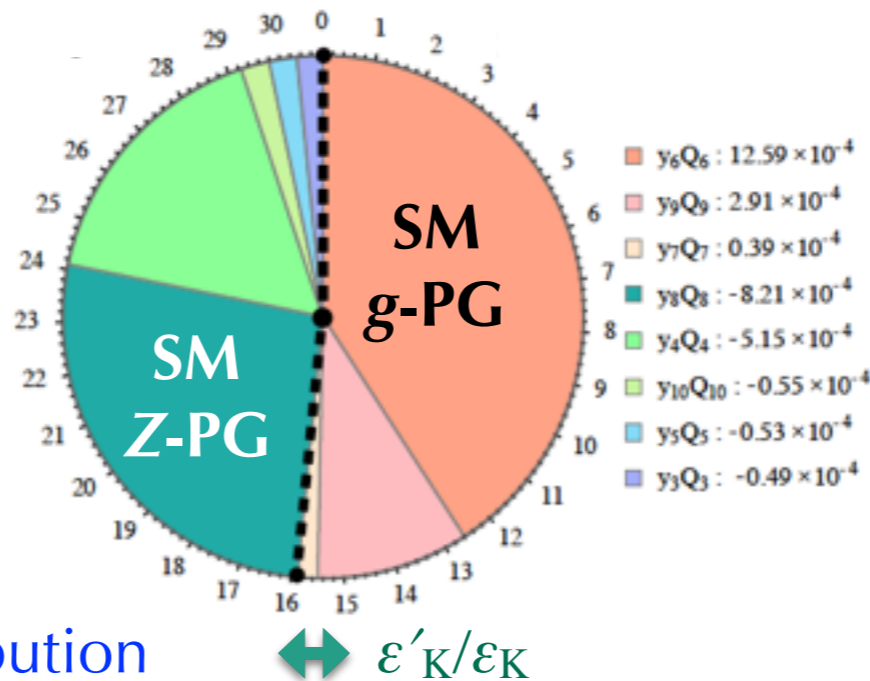


- When NP contribution to FCNC (sdZ) coupling is the same magnitude as the SM, ϵ'_K/ϵ_K discrepancy be explained

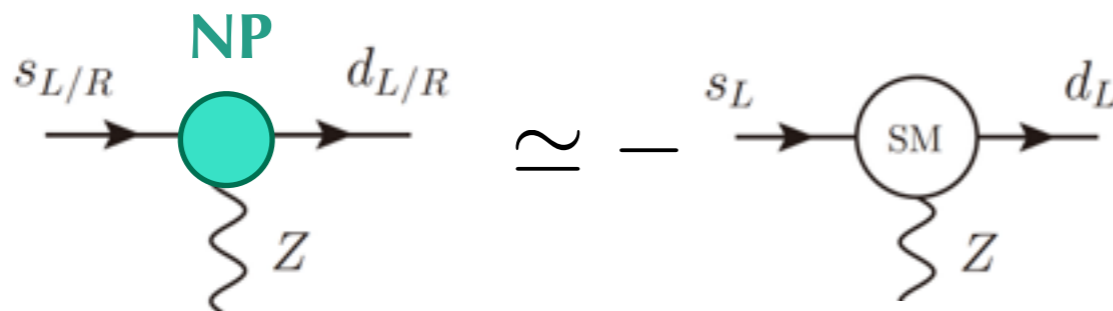
Negative contribution



SM Z-penguin gives the biggest negative contribution



Positive contribution



ϵ'_K/ϵ_K can be solved
 O(1) contribution to $\mathcal{B}(K \rightarrow \pi \nu \bar{\nu})$

Note: Although Z' FCNC scenario can also explain ϵ'_K/ϵ_K , a correlation to $\mathcal{B}(K \rightarrow \pi \nu \bar{\nu})$ is **model-dependent**

Modified Z-coupling scenario

- For gauge-invariant predictions, SM + dimension-six effective theory (SMEFT) should be introduced [Endo, TK, Mishima, Yamamoto, '16] [Bobeth, Buras, Celis, Jung, '17]

[Endo, Goto, TK, Mishima, Ueda, Yamamoto, '18]

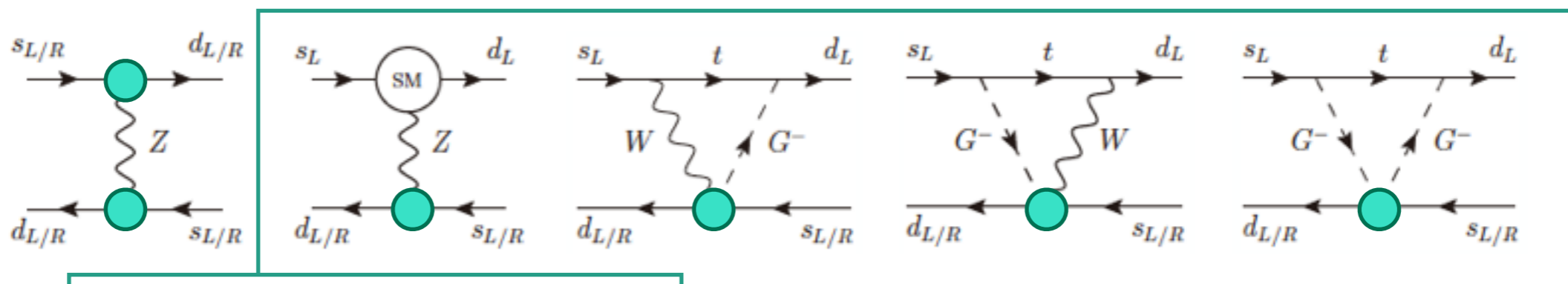
$$\begin{aligned} \mathcal{L} &= \mathcal{L}_{\text{SM}} + \frac{c_L}{\Lambda^2} i(H^\dagger \overleftrightarrow{D}_\mu H)(\bar{Q}_L \gamma^\mu Q'_L) + \frac{c_R}{\Lambda^2} i(H^\dagger \overleftrightarrow{D}_\mu H)(\bar{d}_R \gamma^\mu d'_R), \\ &= \mathcal{L}_{\text{SM}} - \frac{\sqrt{2}vM_Z}{\Lambda^2} (c_L \bar{s} \gamma^\mu Z_\mu P_L d + c_R \bar{s} \gamma^\mu Z_\mu P_R d) + \dots \end{aligned}$$

→ After EWSB, in addition to FCNC terms, some NG boson vertices emerge

- Constraint comes from $\Delta S=2$ process: ϵ_K

$$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{s}_R \gamma^\mu d_R) \quad @\text{high scale} \quad \xrightarrow{\text{top-Yukawa RG}} \quad (\bar{s}_L \gamma_\mu d_L)(\bar{s}_R \gamma^\mu d_R) \quad @\text{low scale}$$

$\Delta S = 1$ ← constraint $\Delta S = 2$



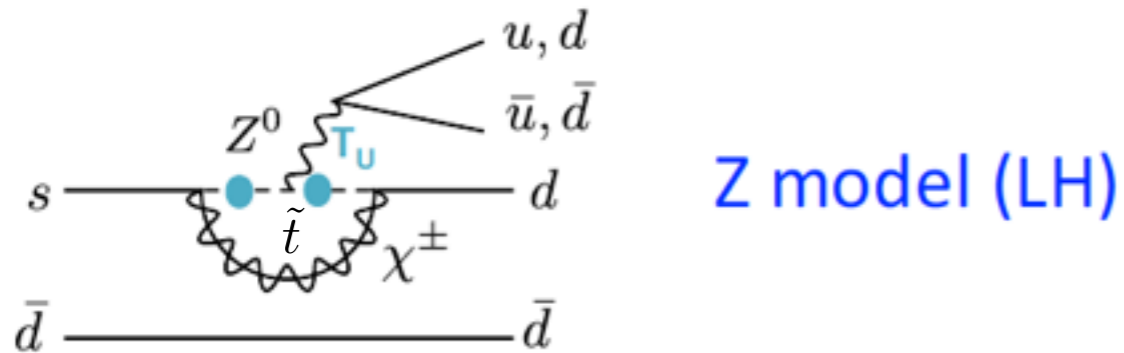
Interference (NP and SM) terms

They can be significant in a certain case

$B(K_L \rightarrow \pi^0 \nu \bar{\nu})$ in Z scenario (MSSM)

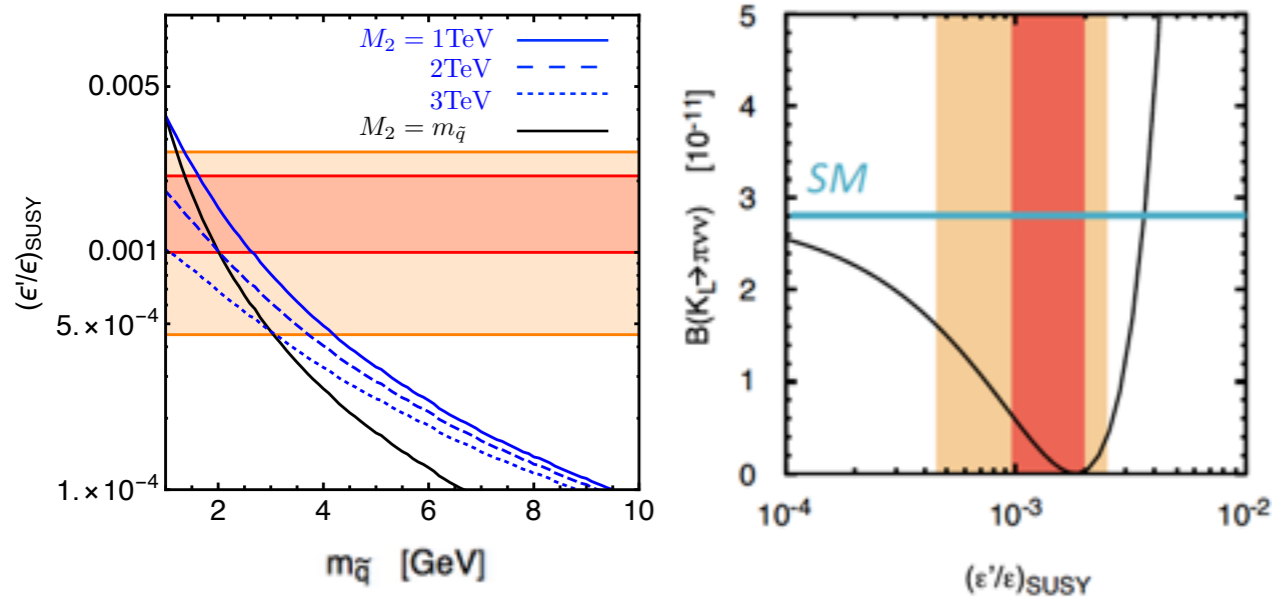
chargino Z-penguin in the MSSM

[Endo, Mishima, Ueda, Yamamoto, '16]



Upper bounds under the constraints:

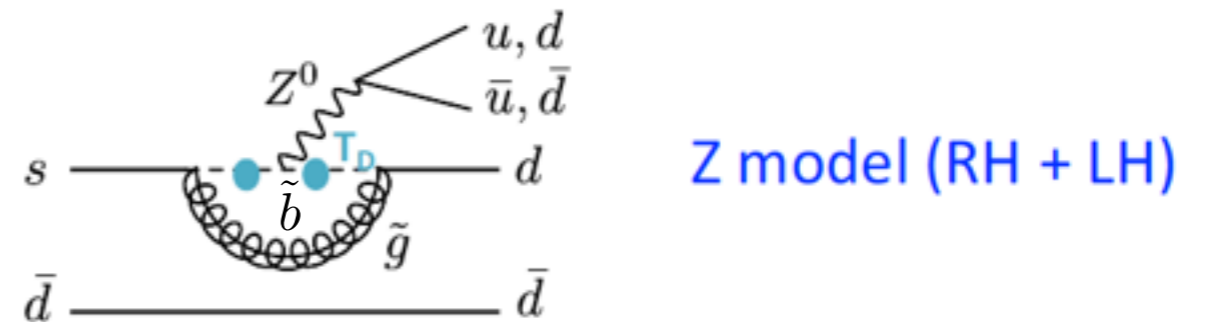
Vacuum, ϵ_K , ΔM_K , $K_L \rightarrow \mu\mu$



gluino Z-penguin in the MSSM

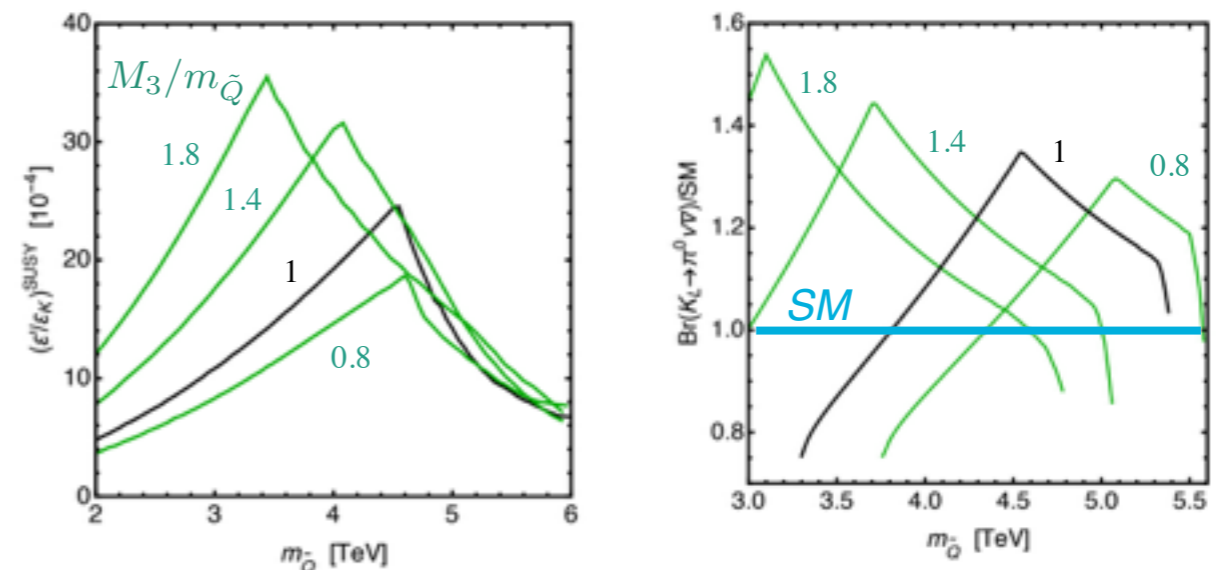
[Tanimoto, Yamamoto, '16]

[Endo, Goto, TK, Mishima, Ueda, Yamamoto, '18]



Upper bounds under the constraints:

Vacuum, ϵ_K , ΔM_K , $K_L \rightarrow \mu\mu$, $b \rightarrow s(d)\gamma$



with $B(K^+ \rightarrow \pi^+ \nu \bar{\nu})/SM \lesssim 1.5$

Conclusions

- **Kaon physics can probe CP -violating FCNC from various ways**
- First lattice result indicates $\varepsilon'_K/\varepsilon_K$ discrepancy in $K^0 \rightarrow \pi\pi$ (**2.8-2.9 σ**)
- $\mathcal{B}(K_S \rightarrow \mu^+ \mu^-)|_{\text{MSSM}} \sim \mathcal{O}(1) \times 10^{-11}$ can be probed by **LHCb Upgrade**
- **LHCb Upgrade** could open a short distance window by **the interference effect** in $K^0 \rightarrow \mu^+ \mu^-$
- **10% precisions** in $K_L \rightarrow \pi^0 \nu \nu$ and $K^+ \rightarrow \pi^+ \nu \nu$ are crucial