



# **Study of $K_S^0$ pair and $\eta_c(1S)$ , $\eta_c(2S)$ and non-resonant $\eta'\pi\pi$ production in two-photon collisions at Belle**

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On behalf of the Belle collaboration  
IHEP & UCAS, Beijing

ICHEP 2018

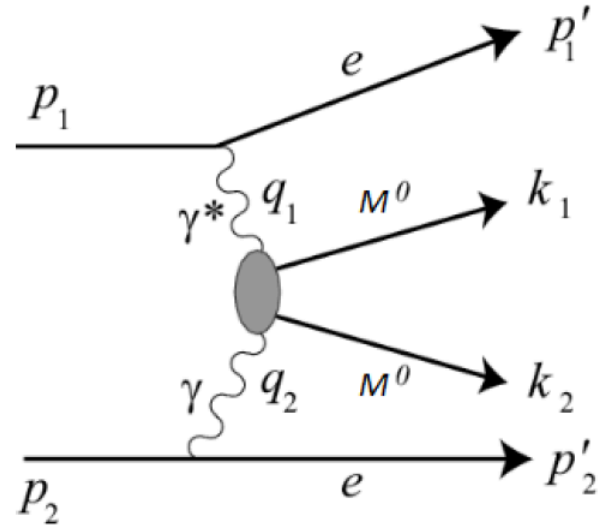
4-11 July 2018, Seoul

# Motivation of single-tag two-photon process

Reaction:

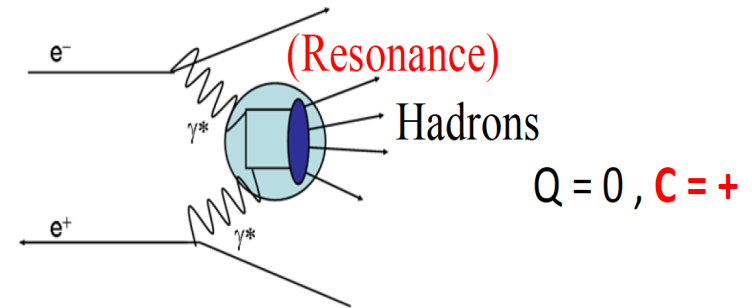
$e^+e^- \rightarrow e^\pm(\text{undetected } e^\mp) \text{ hadrons}$

- ▶ Study strong interaction in low energy region, where pQCD can't be applied;
- ▶ Measure  $Q^2$  dependence of Transition Form Factor (TFF);
- ▶ Provide input for a data-driven estimate of the hadronic light-by-light contribution significant for the problem of muon  $g-2$ .



# Motivation of no-tag two-photon process

- ▶ Lowest heavy-quarkonium  $\eta_c(1S)$ , plus J/psi,  $\eta_b(1S)$  and  $\Upsilon(1S)$ , as benchmarks for the fine tuning of input parameters in QCD calculation.
- ▶ Attempt to measure  $\Gamma_{\gamma\gamma}$  for  $\eta_c(2S)$  and to address the discrepancy between data and QCD predictions.

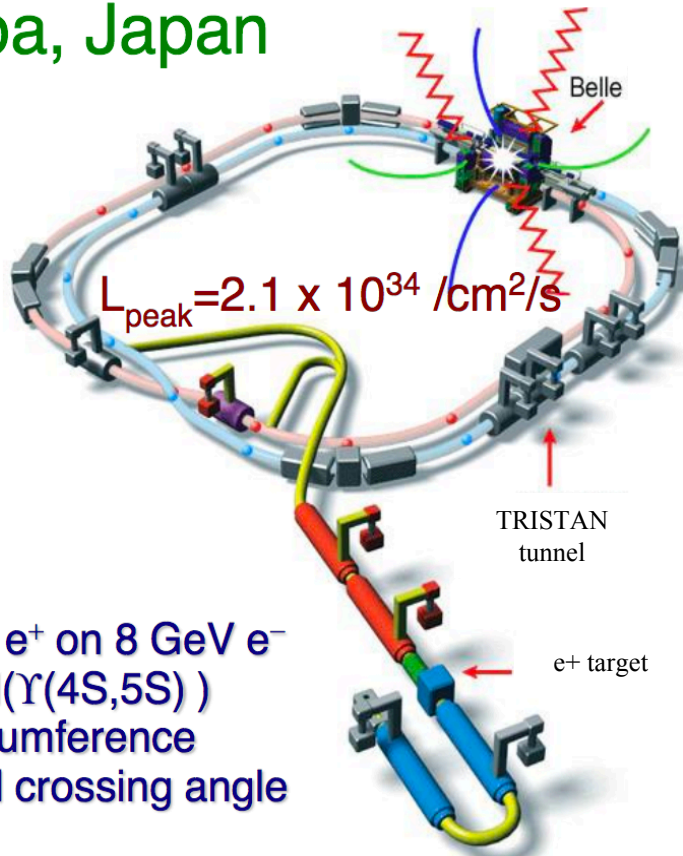


- ▶ Improved precision in both data and QCD predictions at higher  $W$  mass would provide more sensitive comparisons.
- ▶ **pseudo-scalar meson** pairs were measured by Belle [1]  
Charged-meson pairs:  $\pi^+\pi^-$ ,  $K^+K^-$ . Neutral-meson pairs:  $K_S^0K_S^0$ ,  $\pi^0\pi^0$ ,  $\eta\pi^0$ ,  $\eta\eta$ .
- ▶ **pseudo-scalar tensor** pair  $\eta'f_2(1270)$  and three-body final state  $\eta'\pi\pi$  would provide new information to validate QCD models.

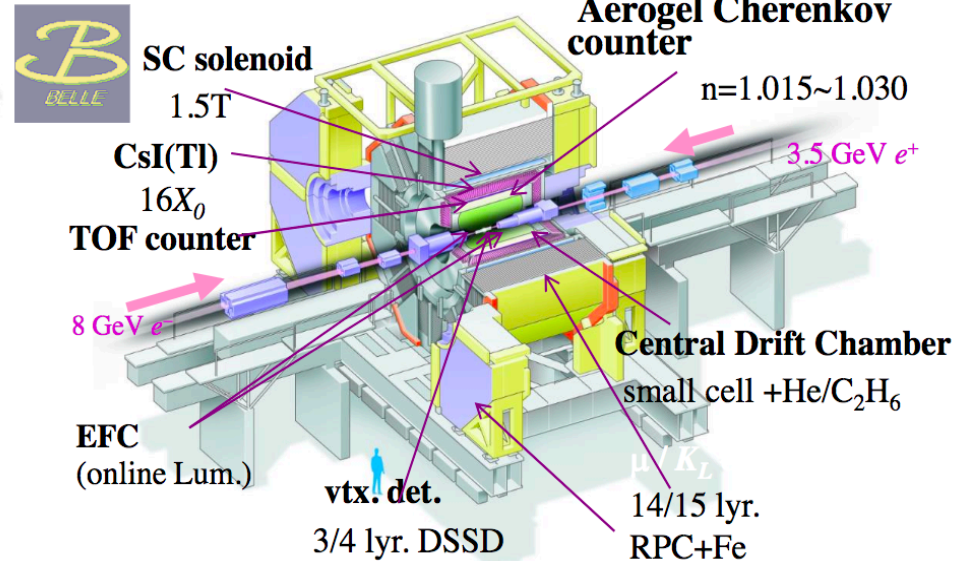
[1] Belle, Euro.Phys.Jour.C (2014) 74:3026

# KEKB and Belle Detector

Tsukuba, Japan



3.5 GeV  $e^+$  on 8 GeV  $e^-$   
 $W_{\text{CM}} = M(\Upsilon(4S, 5S))$   
 3km circumference  
 ~11mrad crossing angle

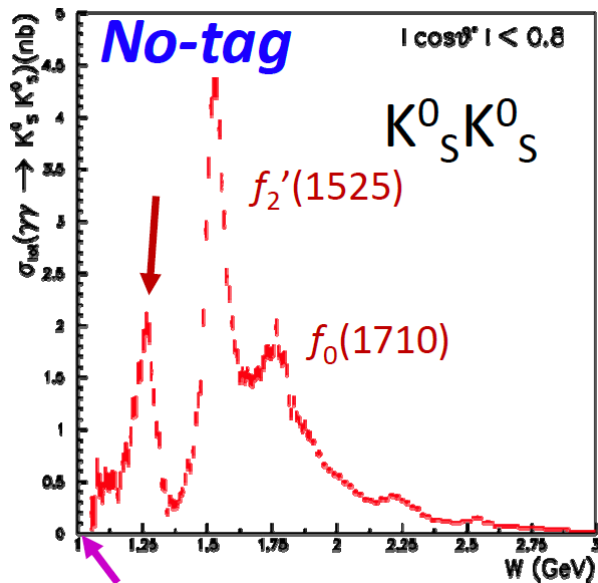


$$\gamma^* \gamma \rightarrow K_S^0 K_S^0$$

**Dataset: 759 fb<sup>-1</sup>**

**PRD 97, 052003 (2018)**

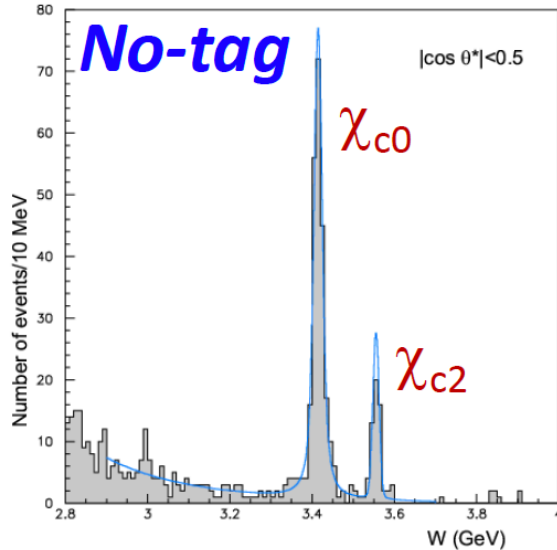
# No-tag results for $K_S^0 K_S^0$ process



PTEP 2013, 123C01 (2013)

Maximum at the  $f_2'(1525)$  peak  
 $\downarrow$   $f_2(1270)/a_2(1320)$  destructive interference  
 Two-photon coupling of  $f_0(1710)$

$\nwarrow$  No data near the  $K_S^0 K_S^0$  mass threshold



$\chi_{c_j}$  Yield

Two-photon decay width  $\times$   $B(K_S^0 K_S^0)$

Interference	$N_{\chi_{c0}}$	$N_{\chi_{c2}}$	$-2 \ln \mathcal{L}/\text{ndf}$
not included	$248.3^{+17.9}_{-17.2}$	$53.0^{+8.1}_{-7.4}$	57.34/73
included	$266 \pm 53$	$53^{+14}_{-12}$	57.22/71

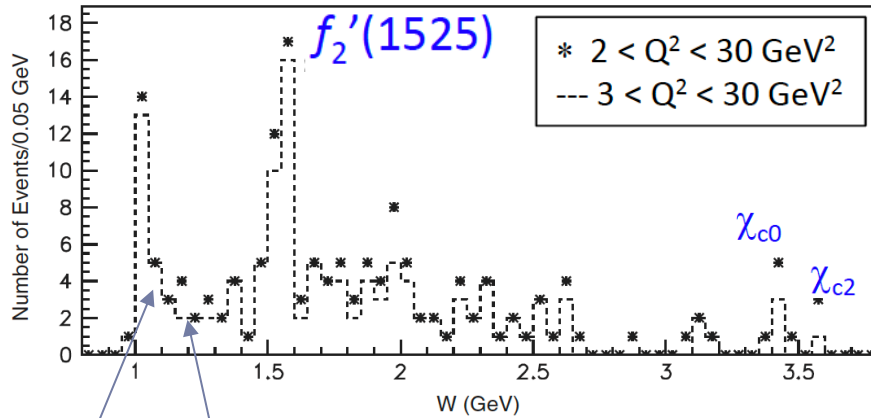
Interference	$\Gamma_{\gamma\gamma} \mathcal{B}(\chi_{c0})$ (eV)	$\Gamma_{\gamma\gamma} \mathcal{B}(\chi_{c2})$ (eV)
not included	$8.09 \pm 0.58 \pm 0.83$	$0.268^{+0.041}_{-0.037} \pm 0.028$
included	$8.7 \pm 1.7 \pm 0.9$	$0.27^{+0.07}_{-0.06} \pm 0.03$
Belle 2007	$7.00 \pm 0.65 \pm 0.71$	$0.31 \pm 0.05 \pm 0.03$
PDG 2012	$7.3 \pm 0.5$	$0.297 \pm 0.026$

2018/7/7

$$\gamma^* \gamma \rightarrow K_S^0 K_S^0$$

## W dependence and $\gamma^* \gamma$ cross section at $Q^2$ bins

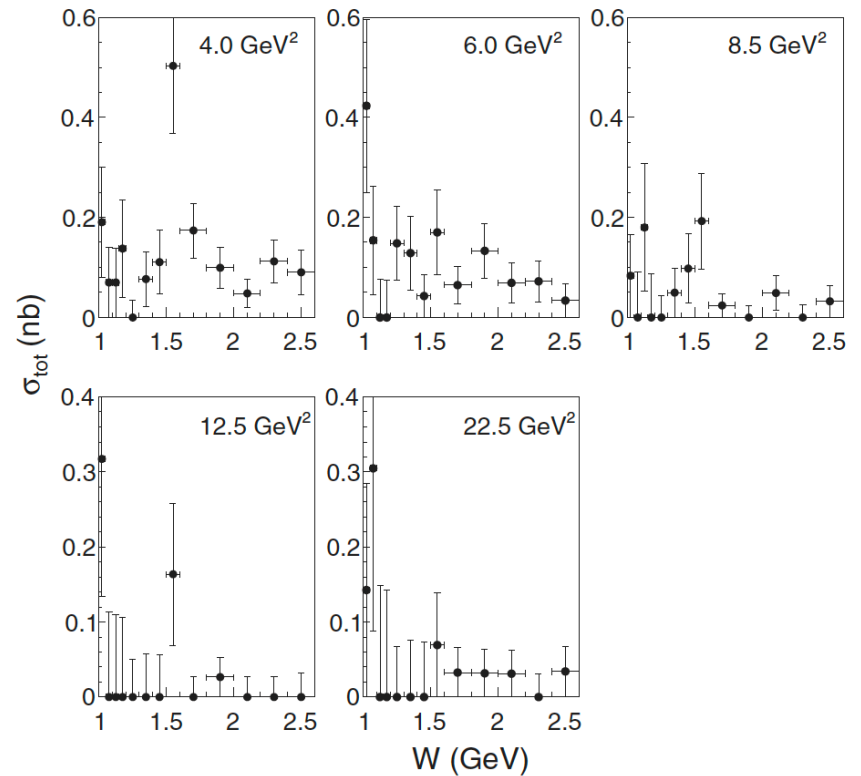
W distributions includes background



No  $f_2(1270)/a_2(1320)$  is seen

Threshold enhancement,  
may be associated with  $f_0(980)/a_0(980)$ .

$$\sigma_{\text{tot}}(\gamma^* \gamma \rightarrow K_S^0 K_S^0) = \frac{1}{2} \frac{d^2 L_{\gamma^* \gamma}}{dW dQ^2} \frac{Y(W, Q^2)}{(1 + \delta) \varepsilon(W, Q^2) \Delta W \Delta Q^2 \int \mathcal{L} dt B^2}$$

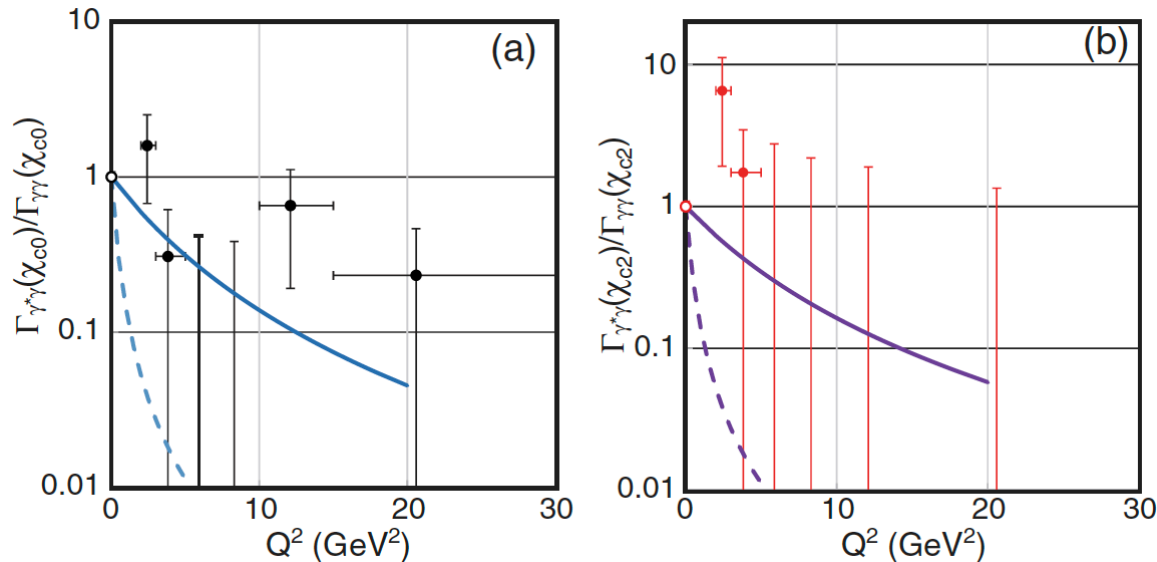


$$\gamma^* \gamma \rightarrow K_S^0 K_S^0$$

## Partial decay width of $\chi_{cJ}$ mesons

Assume that in total 7 events (3 events) peaking near the  $\chi_{c0}$  ( $\chi_{c2}$ ) mass are purely from the charmonium (backgrounds are estimated  $<1$  event in total)

$Q^2$  dependence  $\Gamma_{\gamma^* \gamma} / \Gamma_{\gamma \gamma}$



The first measurement of  $\chi_{cJ}$  production in high- $Q^2$  single-tag two-photon collisions.

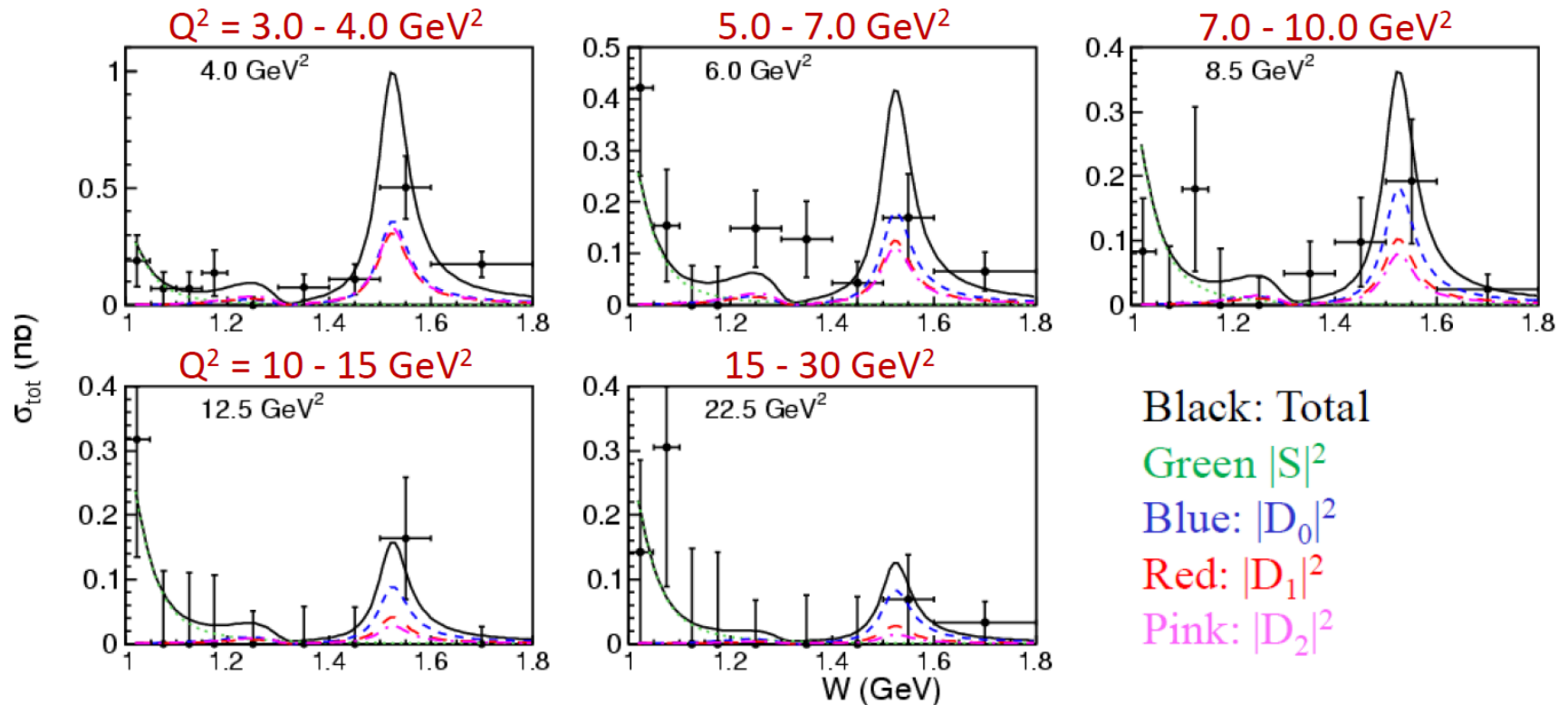
Solid curve: SBG [1] with the charmonium-mass scale (much favored).  
Dashed curve: With the  $\rho$ -mass scale (VDM like)

[1] Schuler, Berends, and van Gulik, Nucl. Phys. B523, 423 (1998).



$$\gamma^* \gamma \rightarrow K_S^0 K_S^0$$

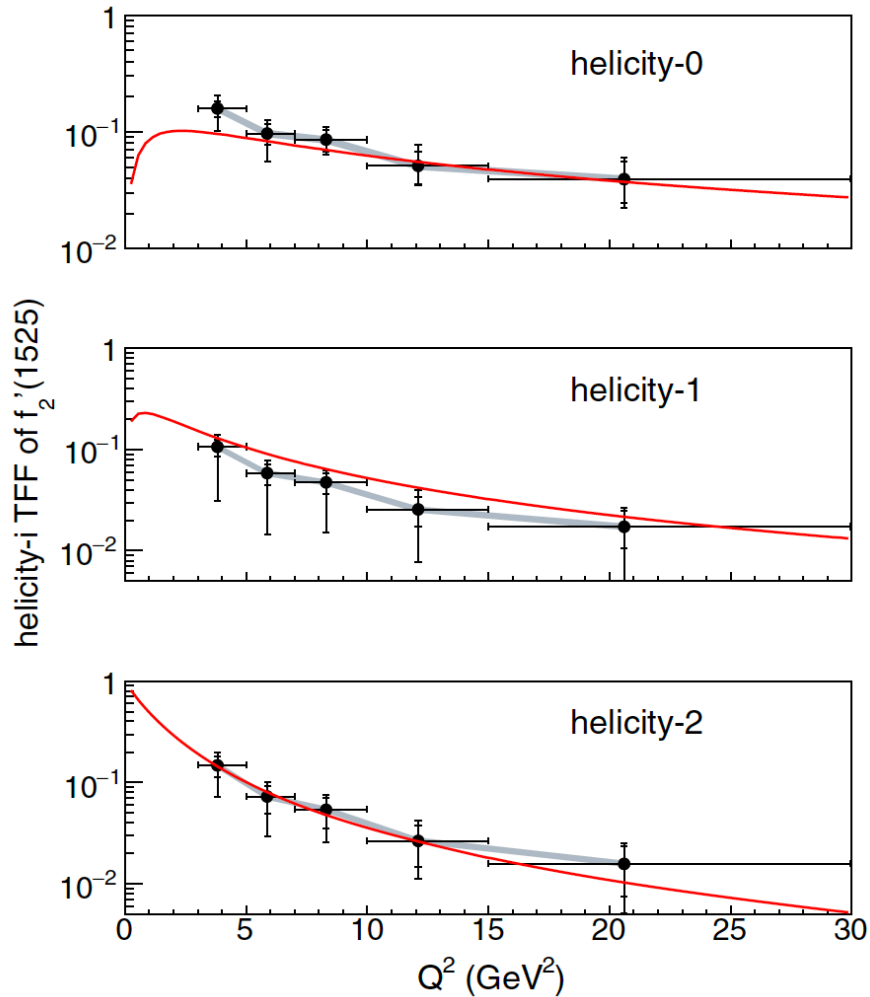
## PWA results in W dependence at $Q^2$ bins



- Non-zero  $D_0$  and  $D_1$  components in the  $f_2'(1525)$ .
- No  $f_2(1270)/a_2(1320)$  is seen.
- An enhancement near the threshold (0.995 GeV).

$$\gamma^* \gamma \rightarrow K_S^0 K_S^0$$

## $f_2'(1525)$ TFF results



The obtained helicity-0, -1, and -2 TFF of the  $f_2'(1525)$  meson as a function of  $Q^2$ .

Shorter error bars: statistical  
Longer error bars: statistical and systematic  
Shaded areas: overall systematic on  $\Gamma_{\gamma\gamma}$ .

— Schuler, Berends, van Glick (SBG)  
Nucl. Phys. B 523, 423, (1998).

helicity-0 and -2 agree well with SBG.  
helicity-1 -- slightly smaller, but not inconsistent.



$$\gamma\gamma \rightarrow \eta' \pi^+ \pi^-$$

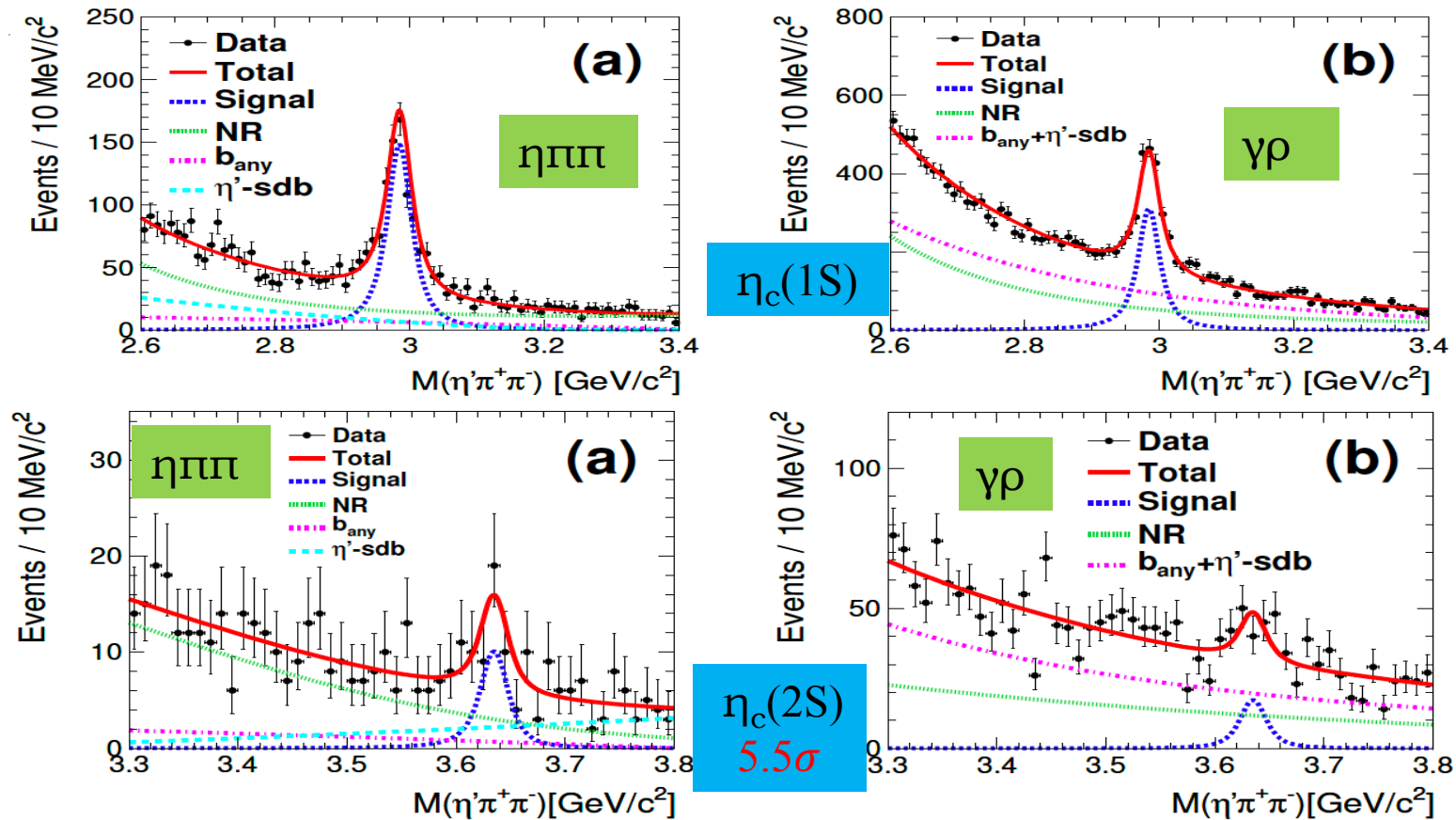
**Dataset: 941 fb<sup>-1</sup>**

**arXiv: 1805.03044**

**Submitted to PRD**

$$\gamma\gamma \rightarrow \eta' \pi^+ \pi^-$$

## Simultaneous Fit for $\eta_c(1S)$ and $\eta_c(2S)$



	$\eta_c(1S)$		$\eta_c(2S)$	
	$\gamma\rho$	$\eta\pi^+\pi^-$	$\gamma\rho$	$\eta\pi^+\pi^-$
$n_s$	$1728^{+69}_{-68}$	$945^{+38}_{-37}$	$65^{+14}_{-13}$	$41^{+9}_{-8}$
$M$ (MeV/c <sup>2</sup> )	$2984.6 \pm 0.7 \pm 2.2$		$3635.1 \pm 3.7 \pm 2.9$	
$\Gamma$ (MeV)	$30.8^{+2.3}_{-2.2} \pm 2.5$		11.3[fixed]	
$\Gamma_{\gamma\gamma}\mathcal{B}$ (eV)	$65.4 \pm 2.6 \pm 6.9$		$5.6^{+1.2}_{-1.1} \pm 1.1$	

$$\gamma\gamma \rightarrow \eta' \pi^+ \pi^-$$

## Discussion on $\Gamma_{\gamma\gamma}$ of $\eta_c(2S)$

◆ Defining the ratio  $R = \frac{\Gamma_{\gamma\gamma}(\eta_c(2S))B(\eta_c(2S))}{\Gamma_{\gamma\gamma}(\eta_c(1S))B(\eta_c(1S))}$ , which is directly measured,

	This work	BaBar( $K\bar{K}\pi$ )[1]	CLEO[2]
R	$(8.6 \pm 2.6) \cdot 10^{-2}$	$(10.6 \pm 2.0) \cdot 10^{-2}$	$(18 \pm 5 \pm 2) \cdot 10^{-2}$

Consistent

so, we have  $R_B = \frac{B(\eta_c(2S) \rightarrow \eta' \pi \pi)}{B(\eta_c(1S) \rightarrow \eta' \pi \pi)} \cong \frac{B(\eta_c(2S) \rightarrow K\bar{K}\pi)}{B(\eta_c(1S) \rightarrow K\bar{K}\pi)}$  within error.

◆ Assuming  $R_B \cong 1$  [3] and

using the world average value  $\Gamma_{\gamma\gamma}(\eta_c(1S)) = 5.1 \pm 0.4$  keV,  
 we obtain  $\Gamma_{\gamma\gamma}(\eta_c(2S)) = 0.44 \pm 0.13$  keV for  $\eta' \pi \pi$  (this) and  
 $0.54 \pm 0.11$  keV for BaBar( $K\bar{K}\pi$ ) [1].

Both  $\Gamma_{\gamma\gamma}(\eta_c(2S))$  values by Belle and BaBar are lower than  
 $0.92 \pm 0.28$  keV from CLEO [2]

Discrepancy between data and QCD values

◆ QCD predictions for two-photon decay width of  $\eta_c(2S)$  are ranged from 1.4 to 5.7.

◆ It is essential to have precise measurement of either  $B(\eta_c(2S) \rightarrow K_s K \pi)$  or  $B(B \rightarrow K \eta_c(2S))$

[1] del Amo Sanchez, P. et al. (BaBar Collaboration) Phys.Rev. D84 (2011) 012004.

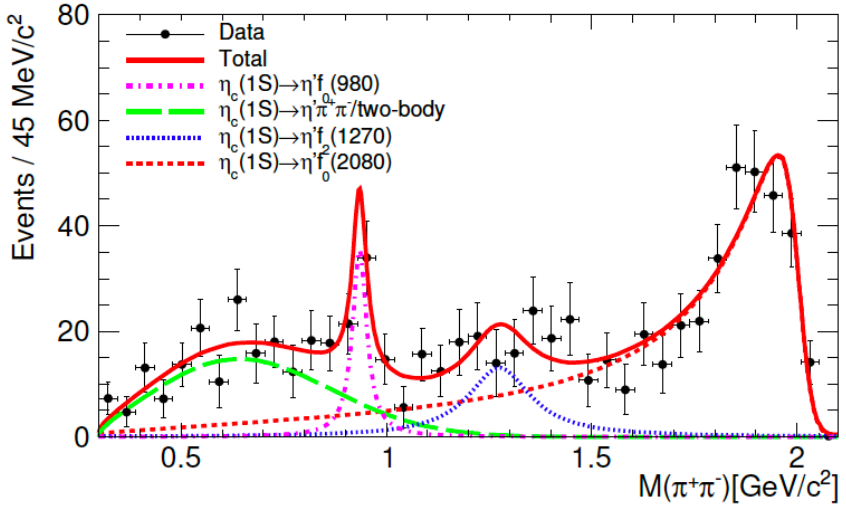
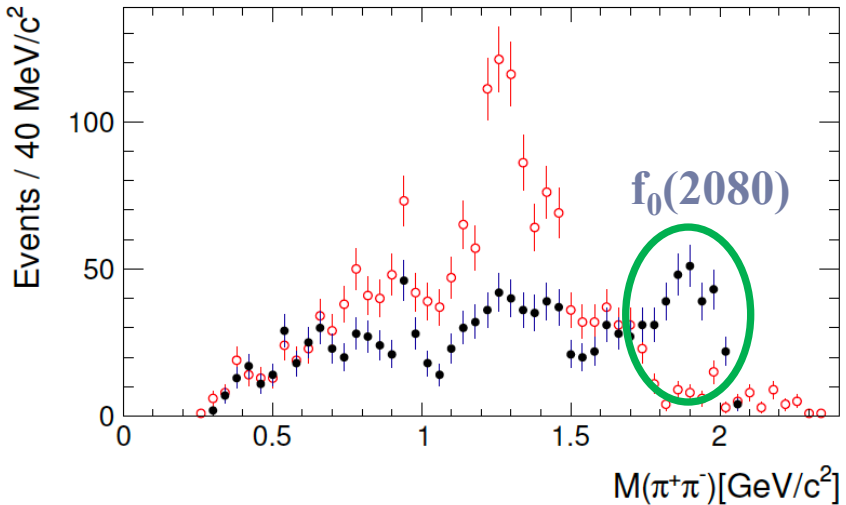
[2] D. M. Asner et al. CLEO Collaboration, Phys. Rev.Lett. 92 (2004) 142001.

[3] T. Barnes, T. E. Browder, and S. F. Tuan, Phys. Lett. B 385, 391 (1996).

[4] J.P. Lansberg, T.N. Pham, AIP Conf. Proc. 1038 (2008) 259.

$$\gamma\gamma \rightarrow \eta' \pi^+ \pi^-$$

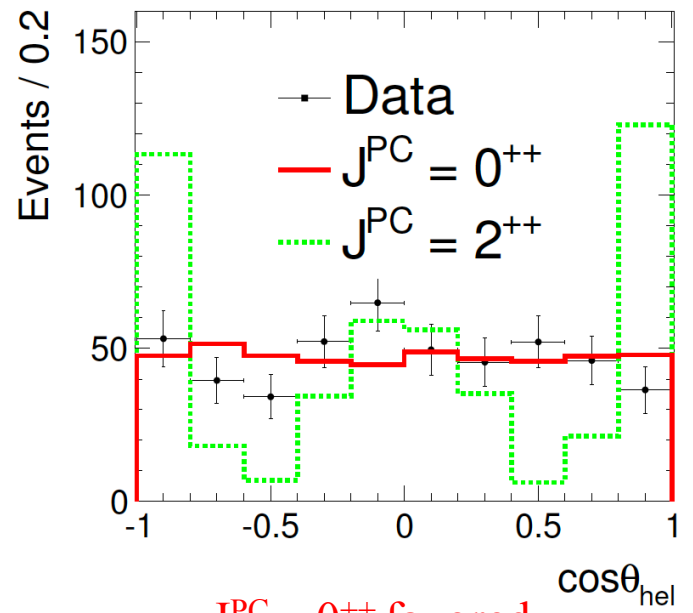
## Study of $\eta_c(1S) \rightarrow \eta' f_0(2080) \rightarrow \pi^+ \pi^-$ decay with $f_0(2080) \rightarrow \pi^+ \pi^-$



$$M = 2083_{-66}^{+63} \pm 32 \text{ MeV}, \quad \Gamma = 178_{-178}^{+60} \pm 55 \text{ MeV}$$

**Black dots** and **red circles** for events selected in  $\eta_c(1S)$  **signal** and **sideband** regions.

No enhanced structure is seen in the Dalitz distributions for the  $\eta_c(1S) \rightarrow a_2^\pm \pi^\mp$  with  $a_2^\pm \rightarrow \eta' \pi^\pm$

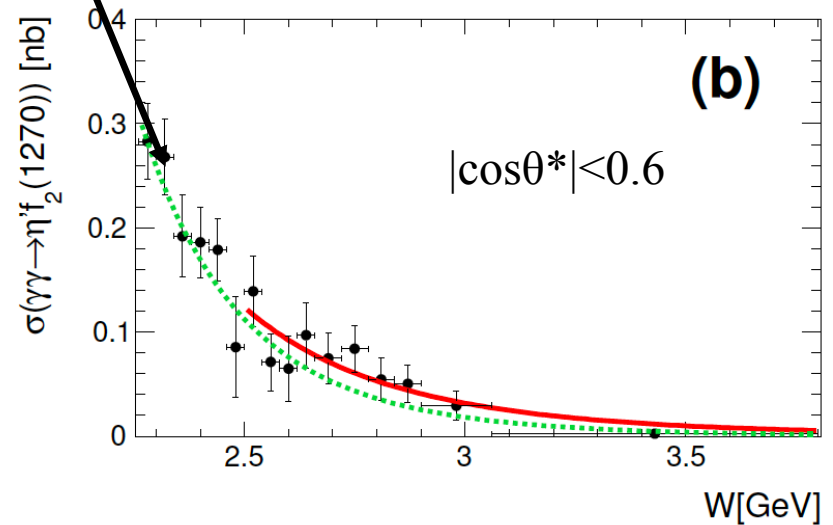
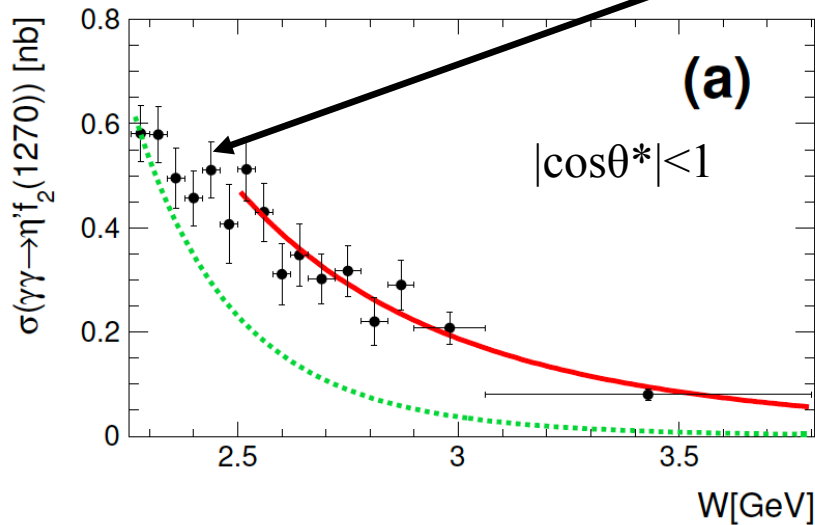


$J^{PC} = 0^{++}$  favored

$$\gamma\gamma \rightarrow \eta' \pi^+ \pi^-$$

## Result of $\sigma(\gamma\gamma \rightarrow \eta' f_2(1270))$

Solid points are the measured cross section in data



- **Green dashed** is the leading term QCD predictions for neutral meson pairs  $\sim 1/W^{10}$  [1]
- No prediction for  $\gamma\gamma \rightarrow \eta' f_2(1270)$ .
- Assuming  $\sigma \sim 1/w^n$ .
- The **red solid line** is the fitted value of  $n = 5.1 \pm 1.0$  for  $|\cos\theta^*| < 1$  and  $n = 7.5 \pm 2.0$  for  $|\cos\theta^*| < 0.6$ .

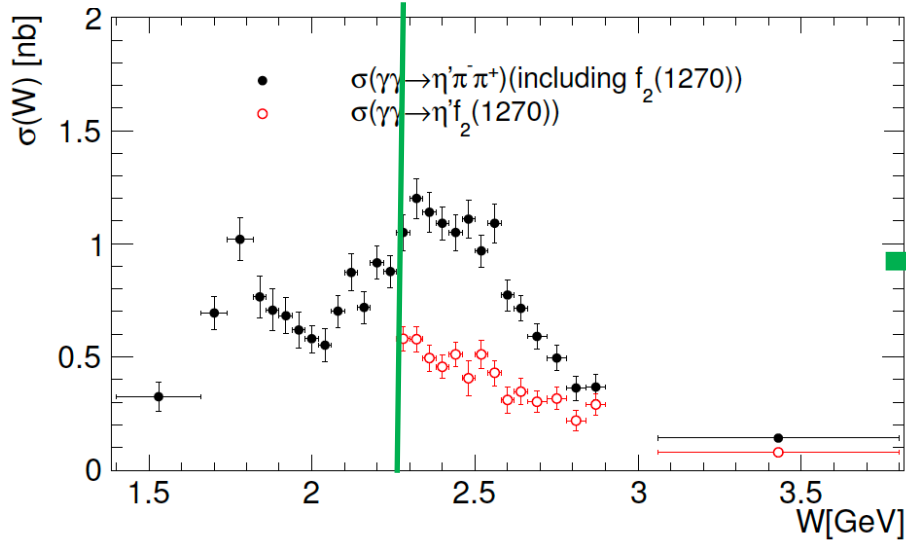
[1] Ed. A.J. Bevan, B. Golob, Th. Mannel, S. Prell, and B.D. Yabsley, Euro.Phys.Jour.C (2014) 74:3026.



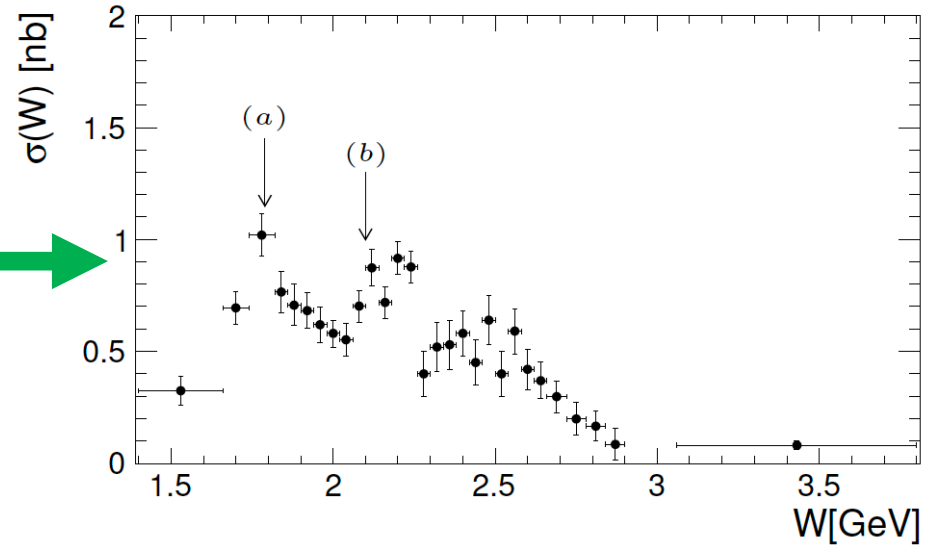
$$\gamma\gamma \rightarrow \eta' \pi^+ \pi^-$$

## Result of $\sigma(\gamma\gamma \rightarrow \eta' \pi\pi)$

$\eta' f_2(1270)$  threshold



$\sigma(\gamma\gamma \rightarrow \eta' \pi\pi)$  after subtraction  $\eta' f_2(1270)$  contribution in  $W > 2.26 \text{ GeV}$  region.



(a). Structure near  $1.8 \text{ GeV}/c^2$  is contributed from  $X(1835)$  or  $\eta(1760)$  [1].

(b) Enhancement at  $2.1 \text{ GeV}/c^2$  is possible contribution from  $\gamma\gamma \rightarrow I(2100) \rightarrow \eta' f_0(980)$ .

[1] C.C. Zhang et al. Belle Collaboratin, Phys. Rev D86, 052002 (2012).



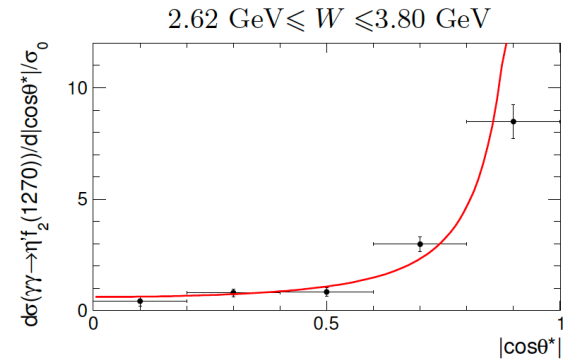
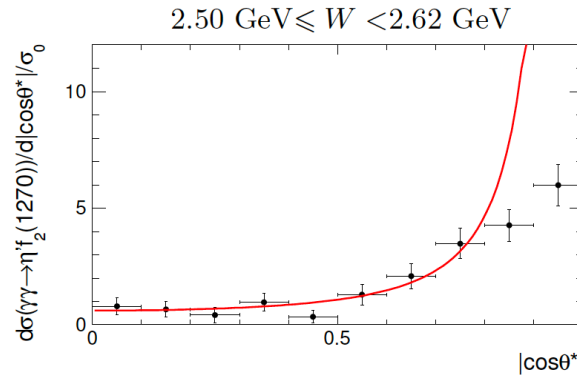
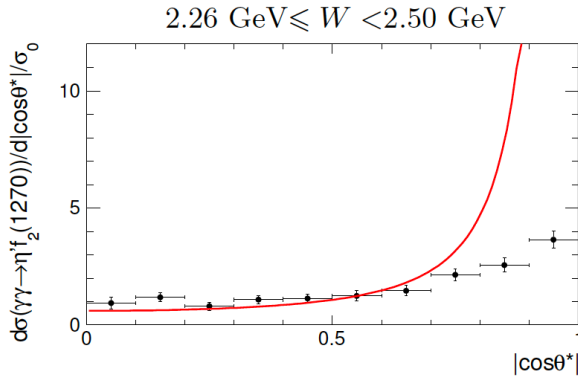
$$\gamma\gamma \rightarrow \eta' \pi^+ \pi^-$$

## Cross Section in $|\cos\theta^*|$

- Black dots with error bar are the  $|\cos\theta^*|$  dependent cross sections in data

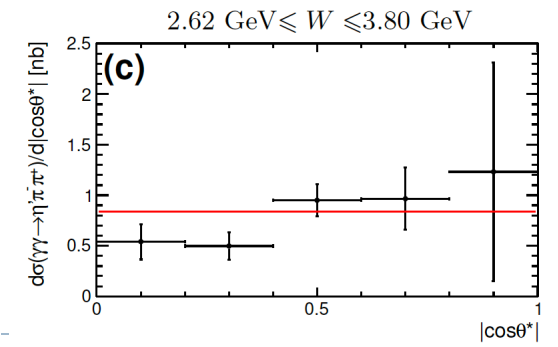
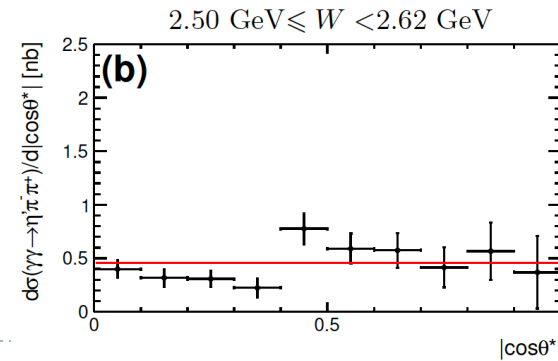
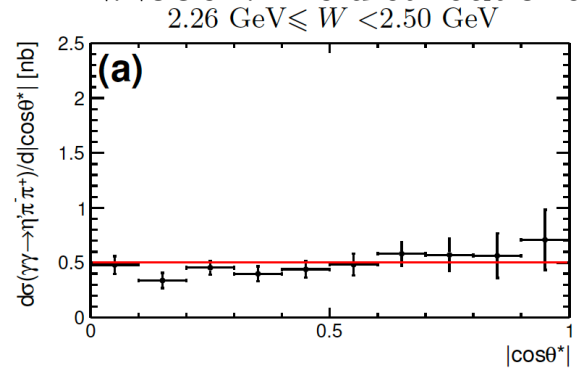
$$\gamma\gamma \rightarrow \eta' f_2(1270)$$

Red lines, normalized to the data, follows a  $1/\sin^4\theta$  behavior.



$$\gamma\gamma \rightarrow \eta' \pi\pi$$

Measured cross section **after subtracting** the  $\gamma\gamma \rightarrow \eta' f_2(1270)$  contribution in W region above 2.26 GeV. The distributions in data comparable with a uniform distribution (red lines).



# Summary

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## Single-tag two-photon results

- Cross section for  $\gamma^*\gamma \rightarrow K_S^0 K_S^0$  has been measured for  $2M(K_S^0) < W < 2.6 \text{ GeV}$ ,  $3 \text{ GeV}^2 < Q^2 < 30 \text{ GeV}^2$
- $Q^2$  dependence of  $\Gamma_{\gamma^*\gamma}$  of  $\chi_{c0}$  and  $\chi_{c2}$  has been measured.
- $Q^2$  dependence of  $f_2'(1525)$  TFF has been measured.

## No-tag two-photon results

- First observation of  $\eta_c(2S) \rightarrow \eta' \pi \pi$  with a significance  $5.5\sigma$  including systematic error.
- First observation of  $\eta_c(1S) \rightarrow \eta' f_0(2080)$  decay with  $f_0(2080) \rightarrow \pi^+ \pi^-$  with a significance  $20\sigma$
- Measurements of pseudo-scalar tensor pair  $\eta' f_2(1270)$  production, as well as that of  $\eta' \pi \pi$ , are made for the first time.

Thanks for your attention!



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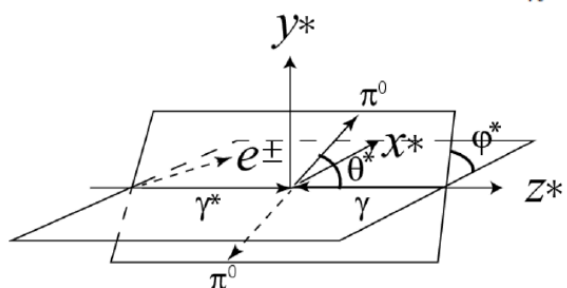
# Backup

## Partial Wave Analysis for TFF of $f'_2(1525)$

Applied for  $W < 1.8$  GeV. We take into account partial waves up to  $J=2$ .  $J=1$  does not couple with  $K_S^0 K_S^0$  ( $\rightarrow J^P = 0^+$  and  $2^+$ )

PRD 97, 052003 (2018)

$$\frac{d\sigma(\gamma^* \gamma \rightarrow K_S^0 K_S^0)}{d\Omega} = \sum_{n=0}^2 t_n \cos(n\varphi^*),$$



$\gamma^* \gamma$  c.m. frame  
 $z^*$  axis  $\parallel \gamma^*$   
 $x^* z^*$  plane includes tag-e

Resonance amplitude for  $f'_2$ , etc.

$$A_R^J(W) = F_R(Q^2) \sqrt{1 + \frac{Q^2}{m_R^2}} \sqrt{\frac{8\pi(2J+1)m_R}{W}} \\ \times \frac{\sqrt{\Gamma_{\text{tot}}(W)\Gamma_{\gamma\gamma}(W)\mathcal{B}(K_S^0 K_S^0)}}{m_R^2 - W^2 - im_R\Gamma_{\text{tot}}(W)}$$

$$t_0 = |SY_0^0 + D_0Y_2^0|^2 + |D_2Y_2^2|^2 + 2\epsilon_0|D_1Y_2^1|^2, \\ t_1 = 2\epsilon_1 \Re [(D_2^*|Y_2^2| - S^*Y_0^0 - D_0^*Y_2^0)D_1|Y_2^1|], \\ t_2 = -2\epsilon_0 \Re [D_2^*|Y_2^2|(SY_0^0 + D_0Y_2^0)].$$

TFF of  $f'_2$  for helicity  $i = \lambda$

$$\sqrt{r_{ifp}} F_{f2p} \quad (i = 0, 1, 2) \\ r_{0fp} + r_{1fp} + r_{2fp} = 1$$

$S, D_0$ , etc. --- Partial-wave amplitudes

$\epsilon_0, \epsilon_1$  --- Spin-dependent flux factor ratios for the virtual photon

$Y_j^m$  --- Spherical harmonics

# Formalism of PWA and parametrizations

**Problems:** Low statistics

Only 3 out of  $S$ ,  $D_0$ ,  $D_1$  and  $D_2$  are independent

Non-unique solution (multiple solutions for resonances)

→ Parametrization of the amplitudes with modelled  $W$  and  $Q^2$  dependences

$$\begin{aligned}
 S &= A_{BW} e^{i\phi_{BW}} + B_S e^{i\phi_{BS}}, \\
 D_i &= \sqrt{r_{ifa}(Q^2)} (A_{f_2(1270)} - A_{a_2(1320)}) e^{i\phi_{faD_i}} \\
 &\quad + \sqrt{r_{ifp}(Q^2)} A_{f_2'(1525)} e^{i\phi_{fpD_i}} \\
 &\quad + B_{D_i} e^{i\phi_{BD_i}},
 \end{aligned}$$

$$\begin{aligned}
 A_{BW}(W) &= \sqrt{\frac{8\pi m_S}{W}} \frac{f_S}{m_S^2 - W^2 - im_S g_S} \\
 &\quad \times \frac{1}{(Q^2/m_0^2 + 1)^{p_S}},
 \end{aligned}$$

Nominal fit

$B_S = 0$

$$B_S = \frac{\beta a_S (W_0/W)^{b_S}}{(Q^2/m_0^2 + 1)^{c_S}},$$

$$B_{D_0} = \frac{\beta^5 a_{D_0} (W_0/W)^{b_{D_0}}}{(Q^2/m_0^2 + 1)^{c_{D_0}}},$$

$$B_{D_1} = \frac{\beta^5 Q^2 a_{D_1} (W_0/W)^{b_{D_1}}}{(Q^2/m_0^2 + 1)^{c_{D_1}}},$$

$$B_{D_2} = \frac{\beta^5 a_{D_2} (W_0/W)^{b_{D_2}}}{(Q^2/m_0^2 + 1)^{c_{D_2}}},$$

$\beta = \sqrt{1 - 4m_{K_S^0}^2/W^2}$  is the  $K_S^0$  velocity

$$r_{0fp} : r_{1fp} : r_{2fp} = k_0 Q^2 : k_1 \sqrt{Q^2} : 1$$

-Destructive interference between  $f_2(1270)$  and  $a_2(1320)$   
 $-r_i(Q^2)$  and TFF for  $f_2(1270)$  and  $a_2(1320)$  are the same;  
 use the values obtained in single-tag  $\pi^0\pi^0$

Determine each component and the relative phase by a fit

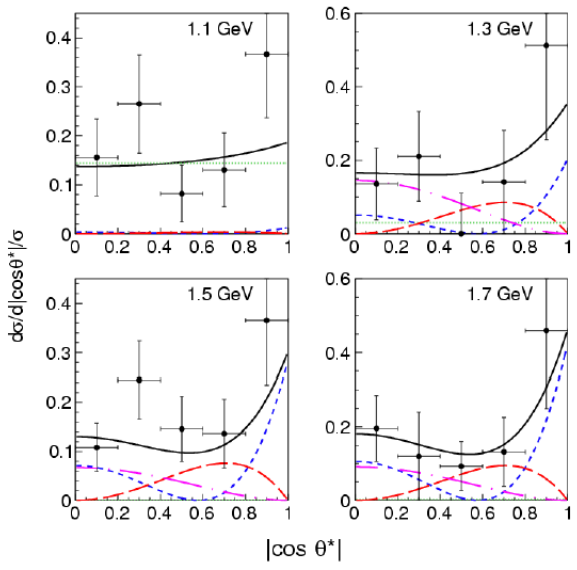
# Angular dependence and the PWA fit

Due to a lack of statistics, we use **Q<sup>2</sup>-integrated angular differential cross section** derived with the following convention (MC generated isotropically)

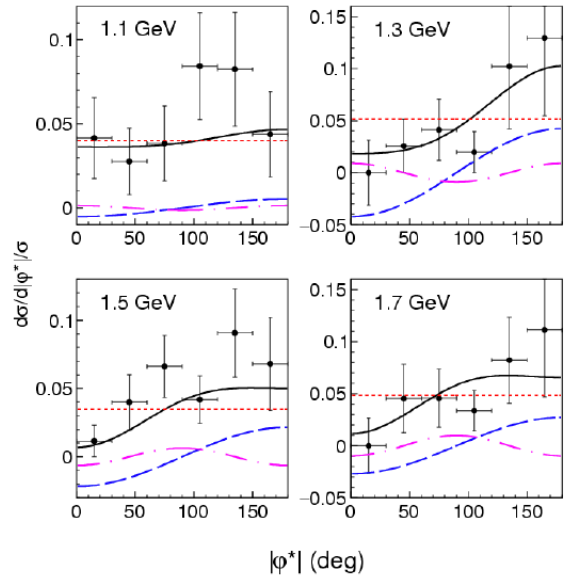
$$\frac{d^2\sigma/d|\cos\theta^*|d|\varphi^*|}{N_{\text{EXP}}(|\cos\theta^*|, |\varphi^*|)/N_{\text{MC}}(|\cos\theta^*|, |\varphi^*|)} \propto$$

Q<sup>2</sup>: integrated over the full range between 3 and 30 GeV<sup>2</sup>  
 W: 4 bins

**|cos θ\*| dependence (|φ\*| integrated)**



**|φ\*| dependence (|cos θ\*| integrated)**



We regard this as the angular dependence at  $\langle Q^2 \rangle = 6.5 \text{ GeV}^2$

Fit:  
 Black: total  
 Red:  $t_0$   
 Blue:  $t_1 \cos\varphi^*$   
 Magenta:  $t_2 \cos 2\varphi^*$

The fit is applied to the two-dimensional angular-dependence data.  
 Forward enhancement is from the helicity-0 component.

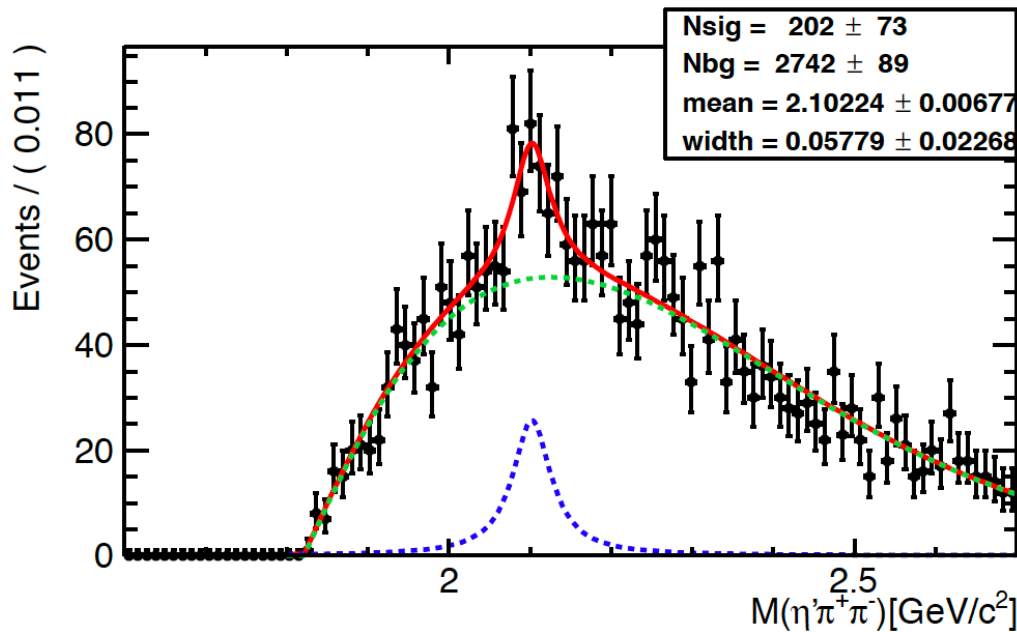
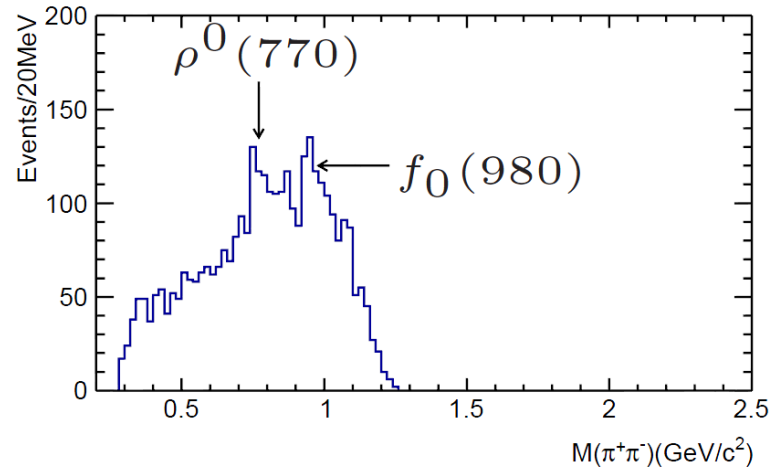
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From PDG 2017

	Branching fraction
$\eta_c(1S) \rightarrow K\bar{K}\pi$	$(7.3 \pm 0.5)\%$
$\eta_c(2S) \rightarrow K\bar{K}\pi$	$(1.9 \pm 1.2)\%$
$B \rightarrow K(\eta_c(1S) \rightarrow K_S K\pi)$	$(2.7 \pm 0.6) \times 10^{-5}$
$B \rightarrow K(\eta_c(2S) \rightarrow K_S K\pi)$	$(3.4^{+2.3}_{-1.6}) \times 10^{-6}$

Possible intermediate from  $\gamma\gamma \rightarrow I(2100) \rightarrow \eta' f_0(980)$

$$2.0 < W < 2.2 \text{ GeV}/c^2$$



- In  $f_0(980)$  signal region  $0.86 < M(\pi\pi) < 1.10 \text{ GeV}/c^2$ .
- $I(2100)$  with statistic significance  $3.5\sigma$ .